

# ADD gravitons & black holes at the LHC

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METU, CMS



SUSY07, Karlsruhe,  
25/07 – 01/08/2007  
Exotics WG



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# ADD gravitons - introduction

- Arkani-Hamed, Dimopoulos, Dvali model introduces  $n$  compactified LEDs with radius  $R$  to solve the Hierarchy problem where gravitation unifies with the other forces at a lowered,  $\sim$ TeV order scale

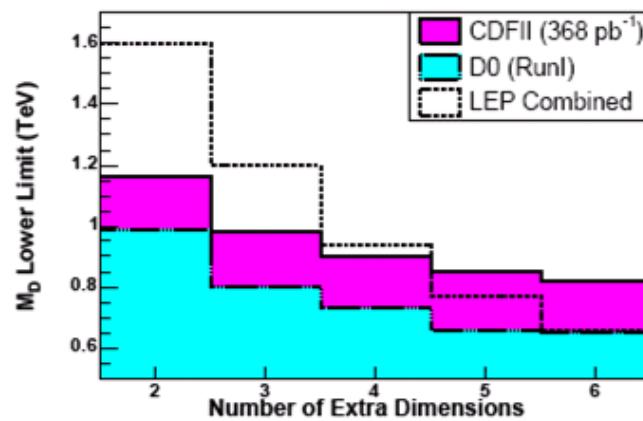
$$M_4^2 = M_{4+n}^{2+n} R^n$$

- Only gravitons probe the bulk space while others are confined to the 3-brane. Hence, a KK tower of graviton modes: 0-mode is massless; higher modes are massive spin-2 particles that can couple to SM matter. Following consequences are possible:

- Direct graviton emission

$$q\bar{q}/gg \rightarrow g/\gamma G_{KK}^{ADD}, \quad gq \rightarrow qG_{KK}^{ADD}$$

LEP &  
Tevatron  
constraints  
on  $M_{(4+n)}$   
from jet+G  
channel



- Virtual graviton exchange:

$$q\bar{q} \rightarrow \gamma/Z^0/G_{KK}^{ADD} \rightarrow ll/\gamma\gamma/jj$$

Find the deviation from SM caused by virtual graviton exchange

%95CL lower limits on  $M_{(4+n)}$  for LED with 200pb<sup>-1</sup> D0 Run II diEM sample and the combined limit for Run I and II

	GRW		HLZ					Hewett
	$n=2$	$n=3$	$n=4$	$n=5$	$n=6$	$n=7$	$\lambda=+1$	
Run II	1.36	1.56	1.61	1.36	1.23	1.14	1.08	1.22
Run I+II, combined	1.43	1.67	1.70	1.43	1.29	1.20	1.14	1.28

# ADD graviton emission in $\gamma + \text{MET}$ channel: I



$q\bar{q}/gg \rightarrow \gamma G_{KK}^{ADD}$

J.Weng, G.Quast, C.Saout, A.de Roeck, M.Spiropulu, CMS-NOTE  
2006/129

## Signatures:

A single high- $p_T$  photon in the central  $\eta$  region.

High missing  $p_T$  back-to-back with the photon in the azimuthal plane

Not strongly dependent on ADD model parameters.

**Trigger: Single photon (L1+HLT),  $E > 80\text{GeV}$ , %100**

## Event selection:

$E_{T\text{miss}} > 400\text{ GeV}$

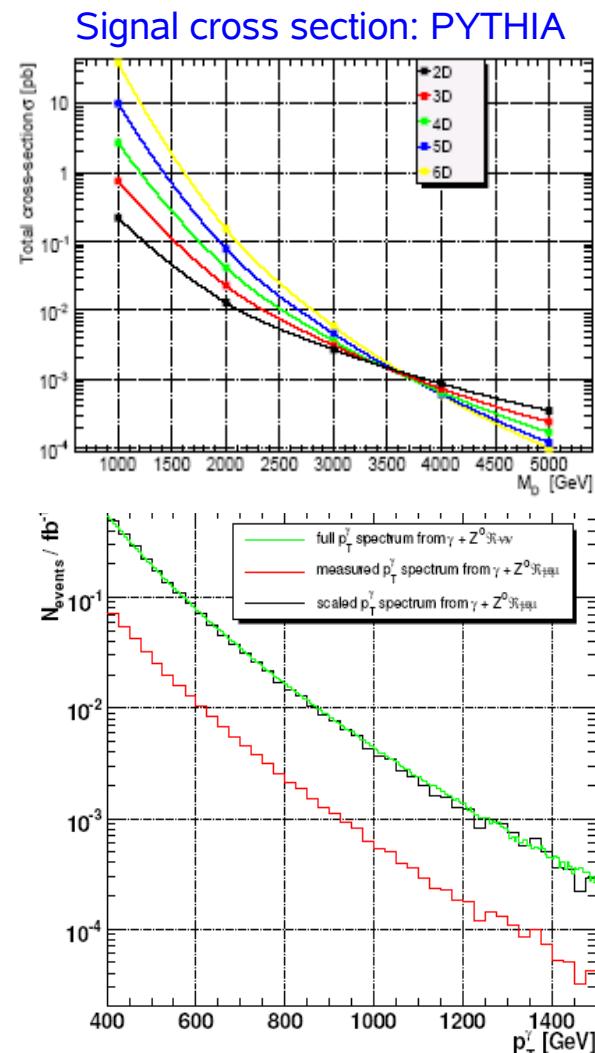
$p_T > 400\text{ GeV}$

$\Delta\Phi(E_{T\text{miss}}, \gamma) > 2.5$

$|\eta| < 2.4$

Track veto  $> 40\text{ GeV}$

$\gamma$  likelihood  $> 0.2$

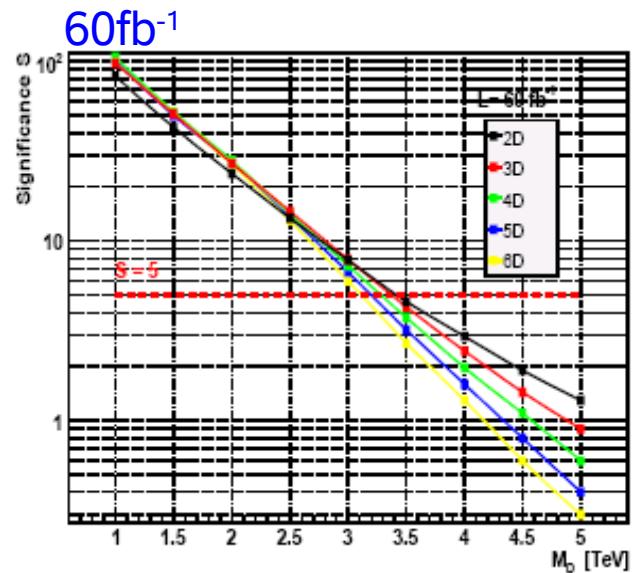
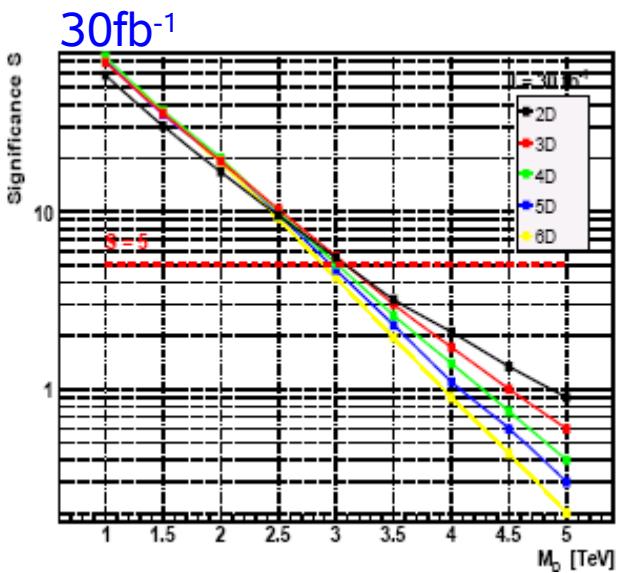
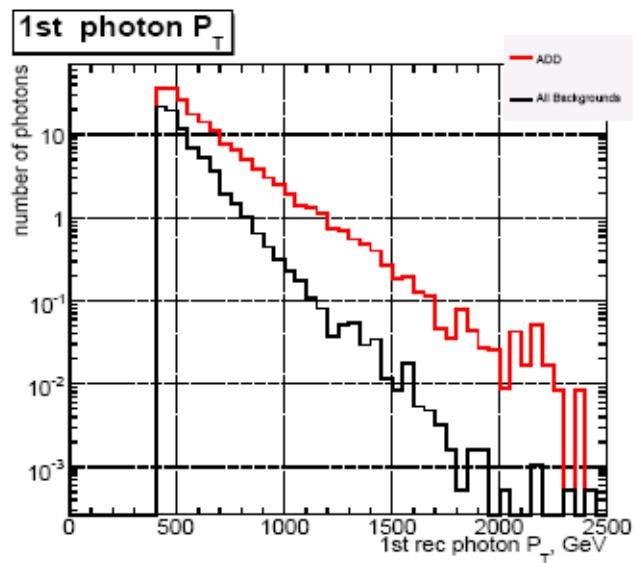
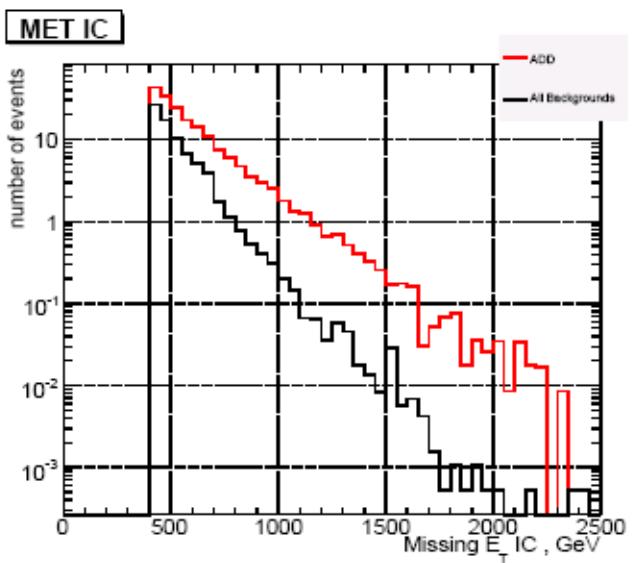


Background	$\sigma$ for $p_T > 400\text{ GeV}$
$Z^0 \gamma \rightarrow \nu\bar{\nu} + \gamma$	2.16 fb
$W^\pm \rightarrow e\nu$	18.2 fb
$W^\pm \rightarrow \mu\nu$	18.2 fb
$W^\pm \rightarrow \tau\nu$	18.2 fb
$W^\pm \gamma \rightarrow e\nu + \gamma$	0.83 fb
$\gamma + \text{Jets}$	2.50 pb
QCD	2.15 nb
di- $\gamma$ born	5.20 fb
di- $\gamma$ box	0.14 fb
$Z^0 + \text{jets}$	0.69 pb

Estimation of  $\gamma + Z(\rightarrow \nu\nu)$  background from  $\gamma + Z(\rightarrow \mu\mu)$  processes.

# ADD graviton emission in $\gamma + \text{MET}$ channel: II

$M_{4+n} = 2.5\text{TeV}$ ,  
 $n = 2$   
**PYTHIA+CMKIN  
+FAMOS**



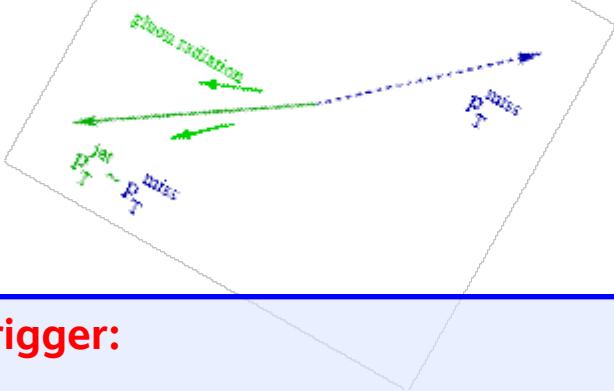


# ADD graviton emission in jet+MET channel: I



$$qg \rightarrow qG_{KK}^{ADD}, \quad gg/q\bar{q} \rightarrow gG_{KK}^{ADD}$$

**Signature:** Monojet back-to-back in azimuth with missing  $p_T$ . Additional jets come from ISR/FSR



## Trigger:

**Single jet + MET**

jet:  $|\eta| < 3.2$ ,  $p_T > 50$  GeV

$p_{T\text{miss}} > 50$  GeV (low L)

$p_T s \rightarrow 100$  GeV for high L

## Event selection:

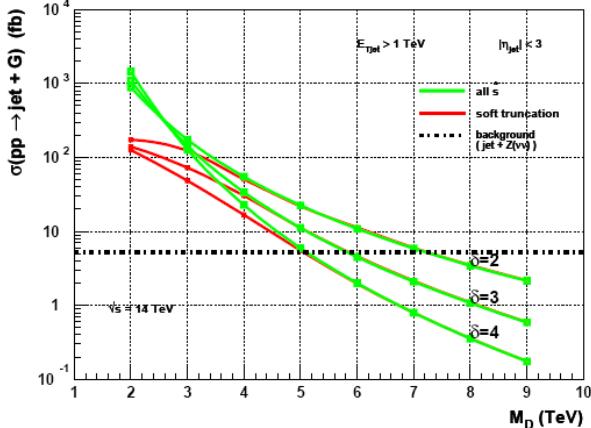
Lepton veto:

Electrons:  $p_T > 5$  GeV,  $|\eta| < 2.5$

Muons:  $p_T > 6$  GeV,  $|\eta| < 2.5$

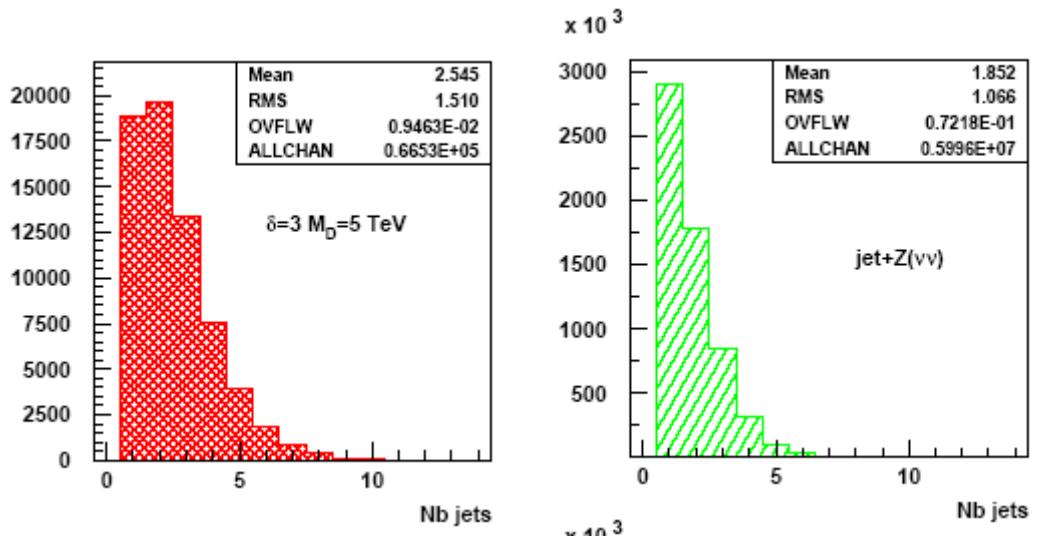
L.Vacavant, I.Hinchliffe, ATLAS-PHYS-2000-016

S&B cross sections for jets  
with  $E_\tau > 1$  TeV -:ISAJET



## Backgrounds:

- Jet + Z( $\rightarrow vv$ )
- jet + W( $\rightarrow \tau\nu$ )
- jet + W( $\rightarrow \mu\nu$ )
- jet + W( $\rightarrow e\nu$ )



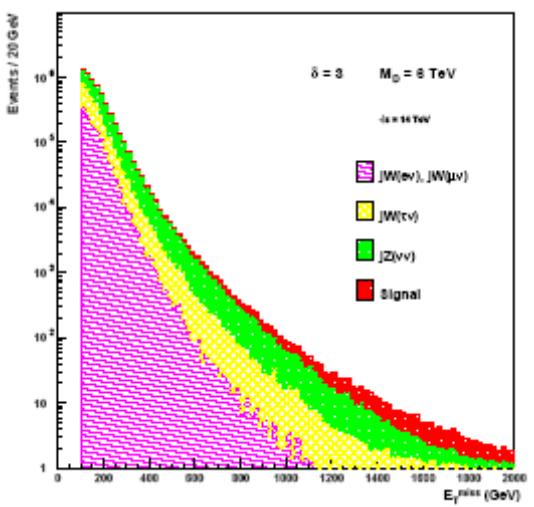
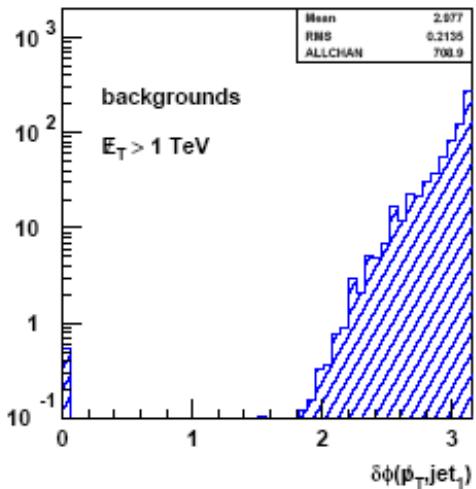
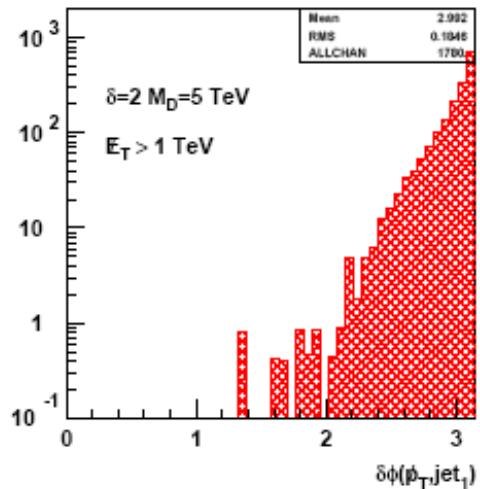
# of jets: ISAJET + ATLFAST



# ADD graviton emission in jet+MET channel: II



ISAJET + ATLFAST



$\delta$	$M_D$	Low luminosity, $30 fb^{-1}$			High luminosity, $100 fb^{-1}$		
		$S$	$S/\sqrt{B}$	$S/\sqrt{7B}$	$S$	$S/\sqrt{B}$	$S/\sqrt{7B}$
2	4	1036.4	81.6	30.8	3542.2	150.2	56.8
	5	417.0	32.9	12.4	1426.9	60.4	22.8
	6	205.9	16.3	6.2	700.6	29.6	11.2
	7	111.3	8.8	3.3	379.4	16.1	6.1
	8	65.3	5.2	2.0	222.5	9.4	3.5
3	4	641.8	50.6	19.1	2168.4	92.0	34.8
	5	211.5	16.6	6.3	706.0	30.0	11.3
	6	85.1	6.8	2.6	287.5	12.1	4.6
	7	39.3	3.1	1.2	134.0	5.7	2.2
4	4	436.2	34.3	13.0	1473.4	62.5	23.6
	5	113.0	8.8	3.3	383.4	16.3	6.2
	6	37.8	2.9	1.1	128.5	5.4	2.0

Remaining signal events after the selection cuts +  $E_{T\text{miss}} > 1$  TeV, and statistical significance

B estimation via normalization is 7 times smaller than expected due to calibration effects, hence  $S/(7B)^{1/2}$  is also used as a worst case scenario.

# ADD graviton contribution in dimuon channel: I



$$q\bar{q} \rightarrow \gamma/Z^0/G_{KK}^{ADD} \rightarrow \mu\mu$$

I.Belotelov, I.Golotvin, A.Lanyov, E.Rogalev, M.Savina, S.Shmatov,  
D.Bourikov, CMS-NOTE 2006/076

## Signatures:

**Two high- $p_T$  muons.**

## Trigger:

**Single muon & dimuon (L1+HLT)**  
 $p_T > 7\text{ GeV}(\mu\mu), 19\text{ GeV}(\text{single } \mu)$

**Efficiency > %98**

## Event selection:

$M(\mu\mu)_{\text{inv}} > M_{\text{min}}$

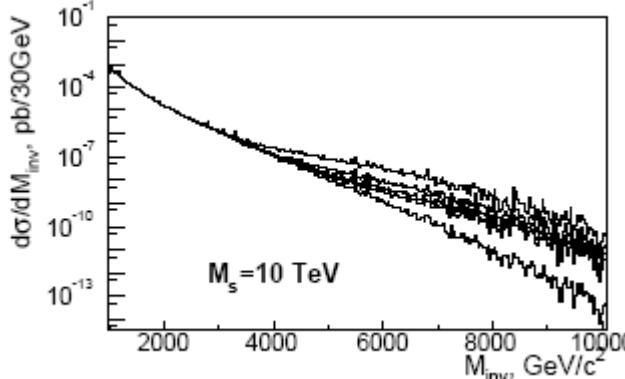
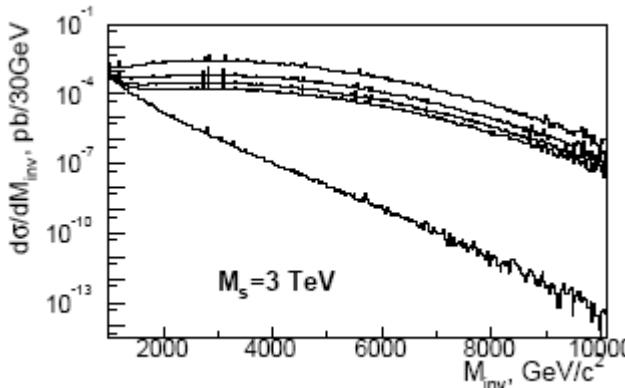
**Different  $M_{\text{min}}$  for different  $M_{4+n}$ :**

$M_{\text{min}} = 1\text{ TeV}$  for  $M_{4+n} = 3\text{ TeV}$

$M_{\text{min}} = 1.5\text{ TeV}$  for  $M_{4+n} = 5\text{ TeV}$

## LO DY cross section

$M_S, \text{TeV}/c^2$	3.0	4.0	5.0	7.0
$n = 3$	$1.5 \times 10^3$	160	32.1	8.1
$n = 6$	103	11.4	10.1	6.4



## Backgrounds:

**For  $M(\mu\mu)_{\text{inv}} > 1\text{ TeV}$**

**ZZ/WZ/WW:**

$\sigma = 2.59 \times 10^{-4} \text{ fb}^{-1}$

**tt:**

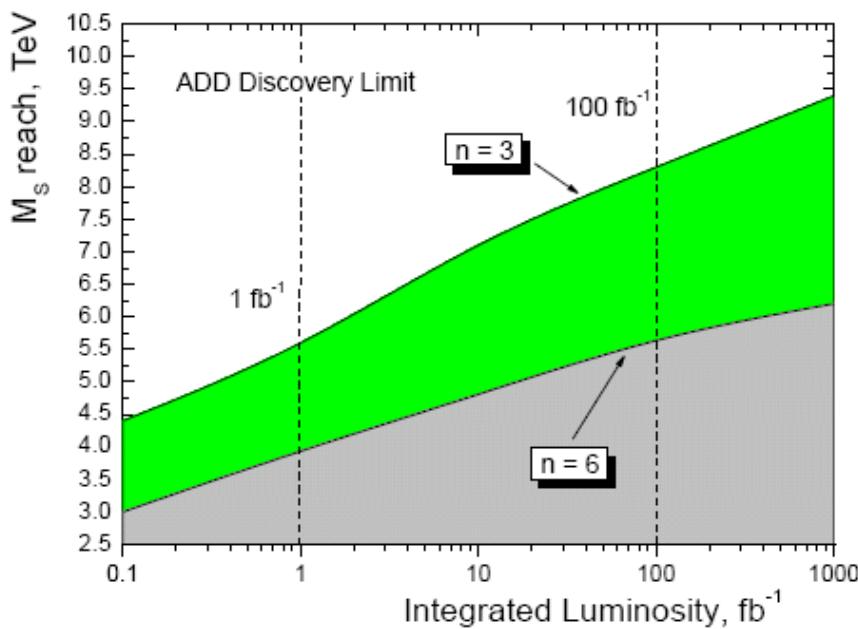
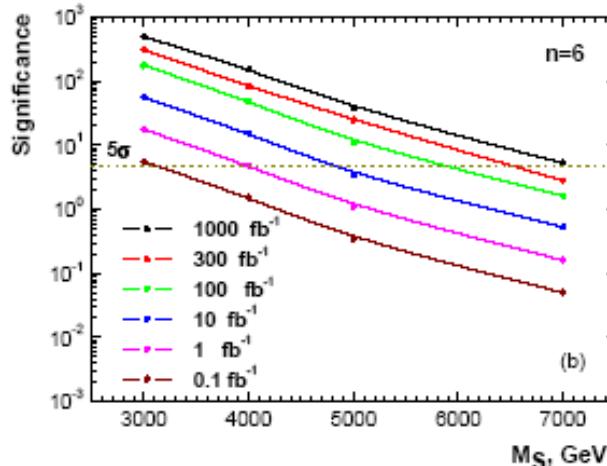
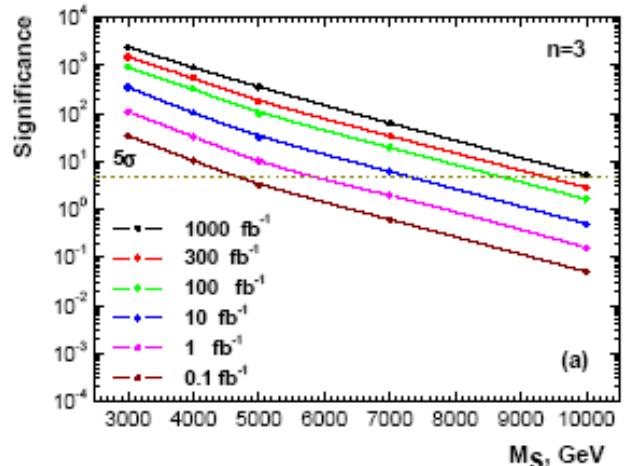
$\sigma = 2.88 \times 10^{-4} \text{ fb}^{-1}$

Landsberg code +  
STAGEN + PHOTIA +  
ORCA + OSCAR

Bottom to top:  
SM,  $n = 6, 5, 4, 3$

# ADD graviton contribution in dimuon channel: II

## Significance:



5 $\sigma$  limit on  $M_{4+n}$  for the number of extra dimensions  $n = 3, 4, 5, 6$



# ADD graviton contribution in $\gamma\gamma/l l$ channels: I

V.Kabachenko, A. Miagkov, A. Zenin ATLAS-PHYS-2001-012

$$q\bar{q}/gg \rightarrow \gamma/Z^0/G_{KK}^{ADD} \rightarrow \gamma\gamma/l l$$

**Signature:** Two photons or leptons

**Trigger:**

- 

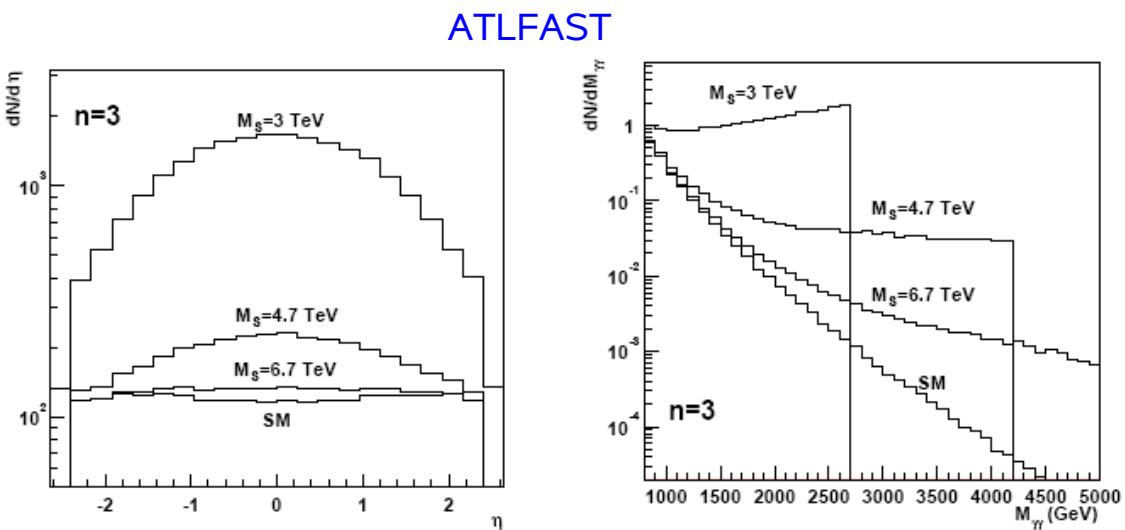
**Event selection:**

$$M(\gamma\gamma/l l)_{inv} < 0.9 M_{4+n}$$

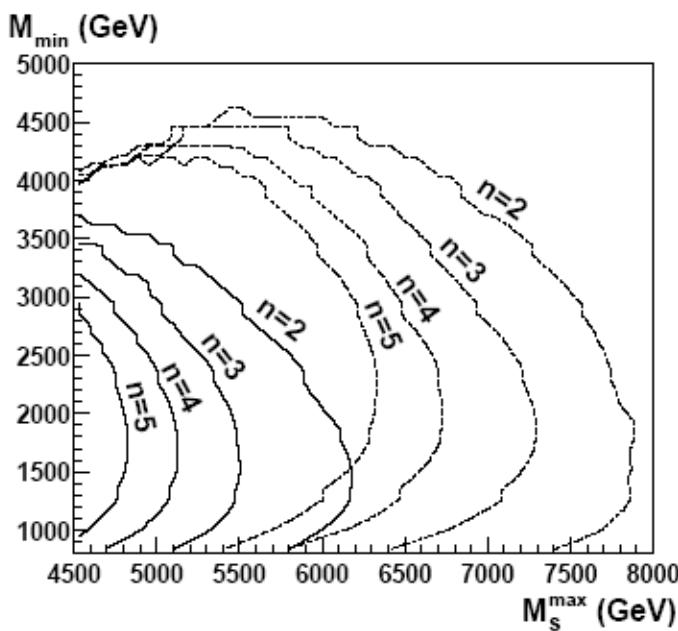
$$M(\gamma\gamma/l l)_{inv} > M_{min} > 0.8 \text{ TeV}$$

$$p_T(\gamma/l) > 50 \text{ GeV}$$

$$|\eta| < 2.5$$



Diphoton production, maximal reach at  $5\sigma$  level in the scale  $M_{4+n}$  as a function of the lower cut  $M_{min}$ . Solid lines:  $10\text{fb}^{-1}$ , dashed lines  $100\text{fb}^{-1}$ .



# Higher-dimensional black holes - introduction

Schwarzschild radius

4+n d

$$r_{4+n} = \frac{1}{\sqrt{\pi} M_{4+n}} \left( \frac{M_{BH}}{M_{4+n}} \left( \frac{8\Gamma((n+3)/2)}{n+2} \right) \right)^{\frac{1}{n+1}}$$

4d

$$r_4 = \frac{1}{M_4} \left( \frac{M_{BH}}{M_4} \right) = \frac{1}{M_{4+n}} \left( \frac{M_{BH}}{M_{4+n}} \right) \frac{1}{(M_{4+n}R)^n}$$

$$r_4 < r_{4+n} < R$$

## FORMATION

4d

$$T_4 = \frac{dE}{dS}$$

$$T_4 = \frac{dE}{dS}$$

$$\tau_4 \sim \frac{1}{M_4} \left( \frac{M_{BH}}{M_4} \right)^3$$

Hawking temperature

$$T_4 > T_{4+n}$$

Lifetime

$$\tau_4 < \tau_{4+n}$$

4+n d

$$T_{4+n} = \frac{dM}{dA}$$

$$T_{4+n} \sim M_{4+n} \left( \frac{M_{4+n}}{M_{BH}} \right)^{\frac{1}{n+1}}$$

$$\tau_{4+n} \sim \frac{1}{M_{4+n}} \left( \frac{M_{BH}}{M_{4+n}} \right)^{\frac{n+3}{n+1}}$$

## BH production – cross sections

For  $M_{BH} \gg M_{4+n}$ , parton level BH formation cross section is given by semi-classical arguments through a geometrical approach:

$$\sigma(s = M_{BH}^2) = F_n \pi r_{4+n}^2 = \frac{F_n}{M_{4+n}^2} \left( \frac{M_{BH}}{M_{4+n}} \frac{8\Gamma((n+3)/2)}{n+2} \right)^{\frac{2}{n+1}}$$

where  $F_n$  is the formation factor. However, the definition of  $F_n$  is yet uncertain.  
 **$\sigma_{BH}$  dominates in high energies.**

For  $M_{BH} \sim M_{4+n}$  quantum gravity effects come into play.

Differential production cross section in pp collisions is calculated using parton luminosity approach:

$$\frac{d\sigma(pp \rightarrow BH + X)}{dM_{BH}} = \frac{dL}{dM_{BH}} \sigma(ab \rightarrow BH)|_{\hat{s}=M_{BH}^2}$$

$$\frac{dL}{dM_{BH}} = \frac{2M_{BH}}{s} \sum_{a,b} \int_{M_{BH}^2/s}^1 \frac{dx_a}{x_a} f_a(x_a) f_b\left(\frac{M_{BH}^2}{sx_a}\right)$$

where  $f_i(x_i)$  are the PDFs.

# Hawking radiation and multiplicity

f:flux, N: multiplicity,  $x = E/T_H$

$$\frac{df}{dx} \sim \frac{x^3}{e^x + c}$$

$$\frac{dN}{dE} \sim \frac{1}{E} \frac{df}{dE} \sim \frac{x^2}{e^x + c}$$

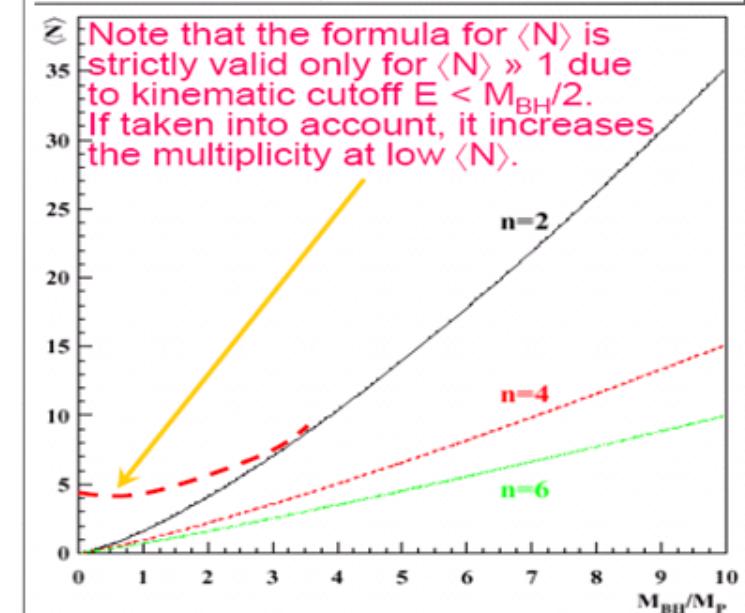
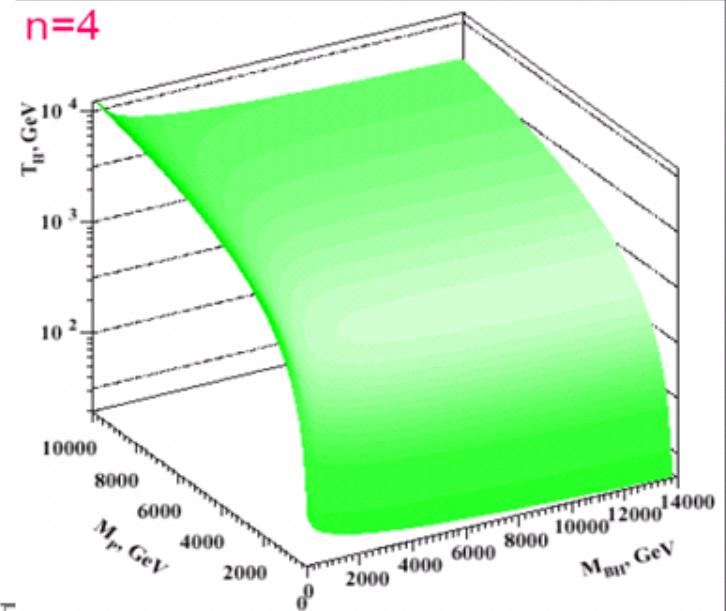
$$\left\langle \frac{1}{E} \right\rangle = \frac{1}{T_H} \frac{\int_0^\infty dx \frac{x^2}{e^x + c}}{\int_0^\infty dx \frac{1}{x} \frac{x^2}{e^x + c}} = \frac{a}{T_H}$$

Use  $a = 0.5$  for Boltzman statistics.

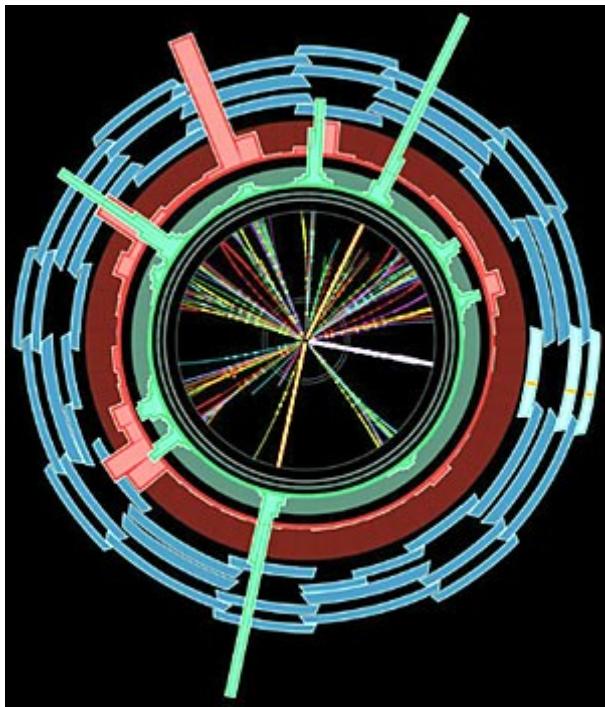
$$\langle N \rangle = \left\langle \frac{M_{BH}}{E} \right\rangle = \frac{M_{BH}}{2T_H}$$

BHs decay democratically to all SM particles

Landsberg, Dimopoulos,  
PRL 87, 161602 (2001)



# Reconstructing BHs at the LHC



ATLAS

BH event generators:

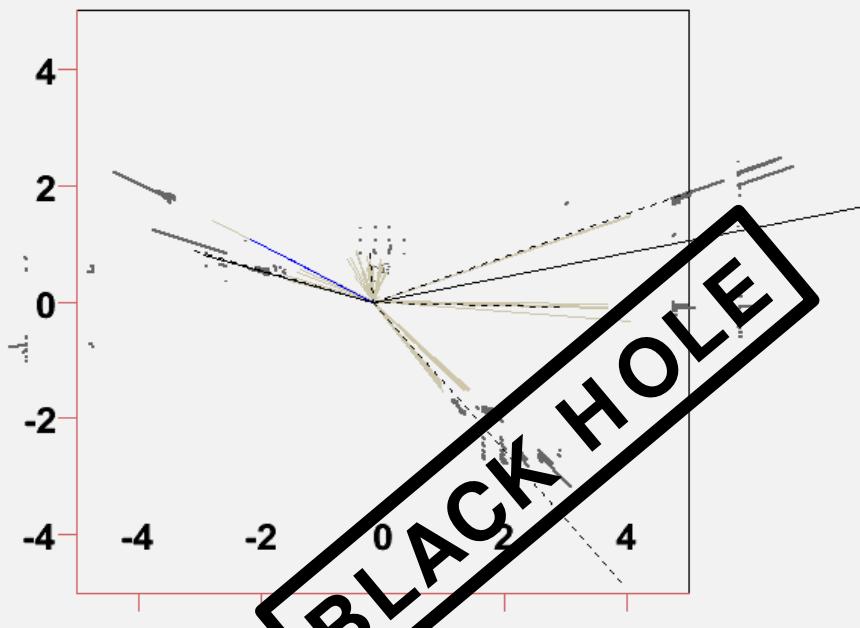
- TRUNOIR (Landsberg, Dimopoulos)
- Unnamed MC by Japan group
- Charybdis (Harris, Richardson, Webber )
- Catfish (Cavaglia, Cremaldi, Godang, Summers)

**Event 017:-1:2982.6%**

H. Gamsizkan, CMS, Charybdis  
 $M_{4+n} = 2, n = 3$

Legend

- Jet
- Top quark
- Electron
- Muon
- Tau
- Photon
- W/Z/Higgs
- Neutrino



# BH signatures

H.Gamsizkan, A.de Roeck, S.Sekmen, M.T.Zeyrek, CMS-AN 2006/088

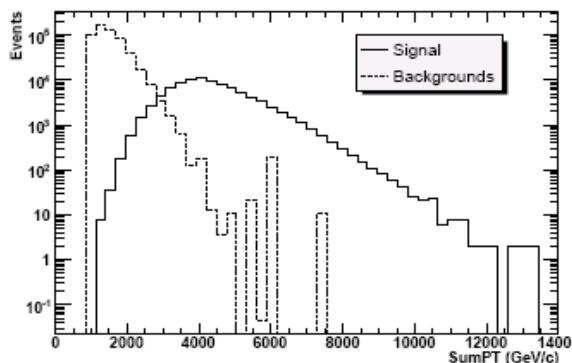
**Signature:** Due to thermal decay, BHs have high sphericity, high  $\Sigma p_T$  and high multiplicity compared to SM events – and due to democratic decay, jets/leptons ratio  $\sim 5 : 1$

**Trigger:** >4 jets, softest having  $E_T > 120$  GeV (efficiency > %93). BHs can be tagged efficiently by requiring a prompt photon or lepton.

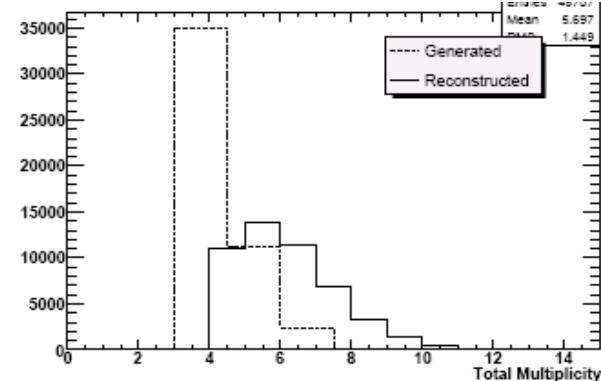
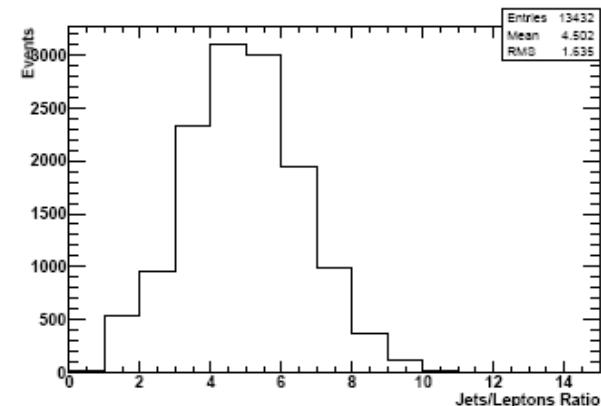
**Event selection:**  
 $M_{BH}(\text{reco}) > 2$  TeV  
Multiplicity > 4  
 $E(\chi) < M_{BH}/2$   
Sphericity < 0.28

$M_{4+n} = 2$ ,  $n = 3$ ,  $M_{BH} = 4-14$ ,  
 $\sigma = 18.85$  pb  
Charybdis+ORCA+OSCAR

$$\sum p_T = \sum_{i<4} |p_T(\text{jet}_i)| \quad (\text{4 hardest jets})$$

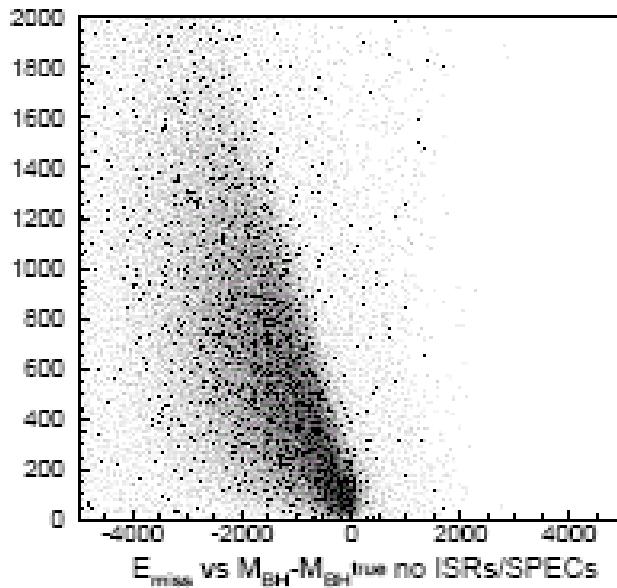
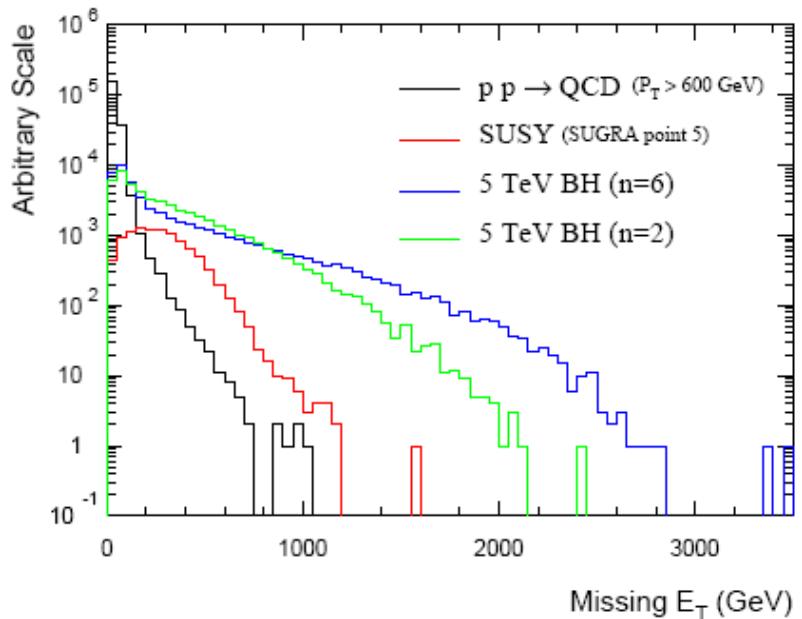


**Backgrounds:** tt+jets,  
W/Z+jets, QCD, WW+jets



# BH signatures: High missing energy

BHs would have high missing  $E_T$  due to high energies of democratically emitted neutrinos.



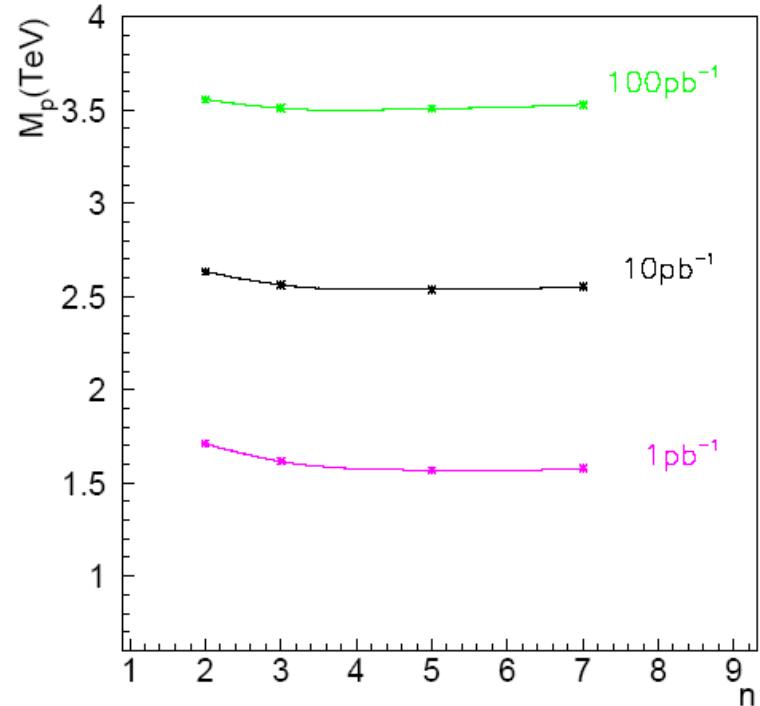
Harris, Palmer, Parker, Richardson,  
Sabetfakhri, Webber, ATLAS, JHEP 0505  
(2005) 053  
Charybdis + ATLFAST

Tanaka, Yamamura, Asai, Kanzaki,  
ATLAS, Eur. Phys. J. C41 (2005) 19-23  
Unnamed MC  
 $M_{4+n} = 1$ ,  $n = 3$ ,  $M_{\text{BH}} = 1-14$

Most analyses use  $E_{\text{miss}} > 100$  GeV cut.

# BH significance

$M_{(4+n)}$	min $M_{BH}$	4+n	Cross section (pb)	Luminosity to reach $5\sigma$ ( $\text{fb}^{-1}$ )
2	4	7	18.85	$3.71 \times 10^{-3}$
2.5	5	7	2.661	1.20
1	1	6	27980	$6.50 \times 10^{-6}$
1	1	8	23510	$8.50 \times 10^{-6}$
1	1	10	24910	$8.50 \times 10^{-6}$
1	2	6	3086	$1.95 \times 10^{-5}$
1	2	8	2282	$2.95 \times 10^{-5}$
1	2	10	2284	$3.15 \times 10^{-5}$
2	2	6	486.1	$1.52 \times 10^{-4}$
2	2	8	432.4	$1.82 \times 10^{-4}$
2	2	10	468.3	$1.74 \times 10^{-4}$
2	3	6	93.06	$5.79 \times 10^{-4}$
2	3	8	75.54	$8.74 \times 10^{-4}$
2	3	10	78.7	$8.88 \times 10^{-4}$
2	4	6	23.3	$2.30 \times 10^{-3}$
2	4	10	17.73	$5.29 \times 10^{-3}$
3	3	6	31.56	$2.47 \times 10^{-3}$
3	3	8	28.55	$2.96 \times 10^{-3}$
3	3	10	31.15	$2.74 \times 10^{-3}$
3	4	6	7.904	$1.45 \times 10^{-2}$
3	4	8	6.638	$2.38 \times 10^{-2}$
3	4	10	7.017	$2.32 \times 10^{-2}$
4	4	6	3.67	1.21
4	4	8	3.328	1.81
4	4	10	3.636	2.10

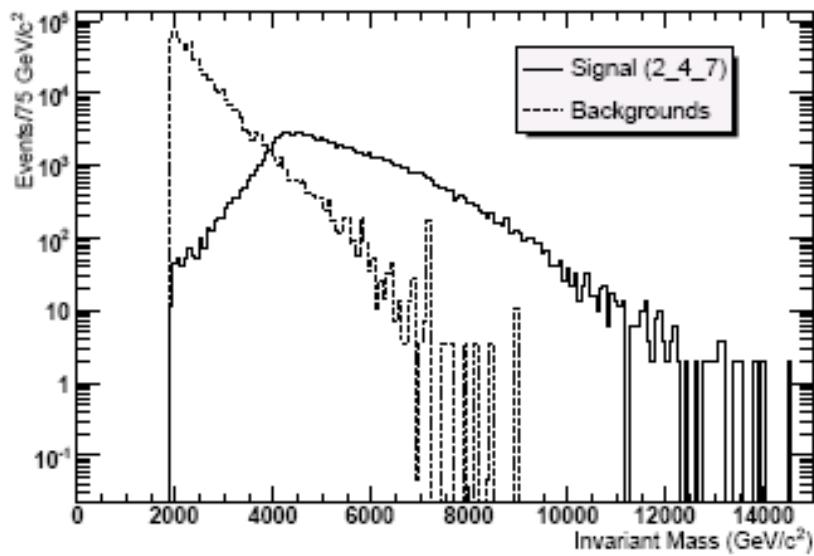


Tanaka, et.al., ATLAS,  
Eur. Phys. J. C41 (2005) 19-23  
Unnamed MC + ATLFAST  
 $M_{BH} = M_{4+n} + 1$  to 14

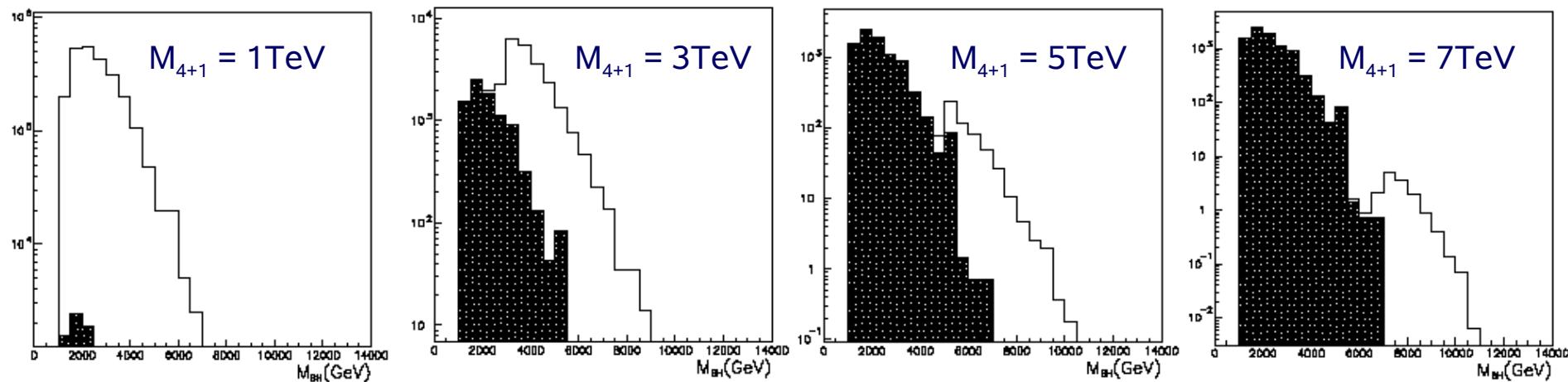
# BH invariant mass

$$M_{BH} = \sqrt{(\sum_i p_i)^2}$$

Gamsızkan et.al., CMS-AN 2006/088  
 Charybdis + ORCA + OSCAR  
 $M_{4+n} = 2, n = 3, M_{BH} = 4-14$



Tanaka et.al., ATLAS,  
 Unnamed MC,  
 $n = 3, M_{BH} = 1-14$ ,  
 solid line: S+B, cross-hatched: B only

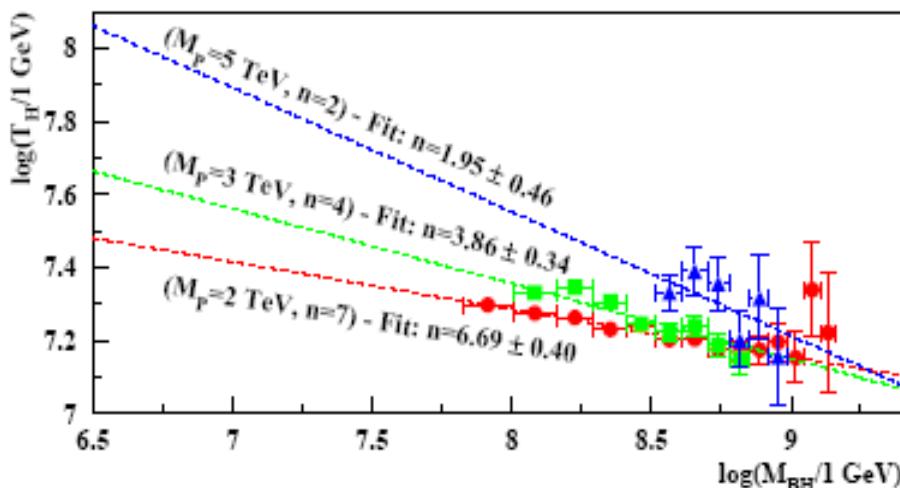


# Learning about spacetime

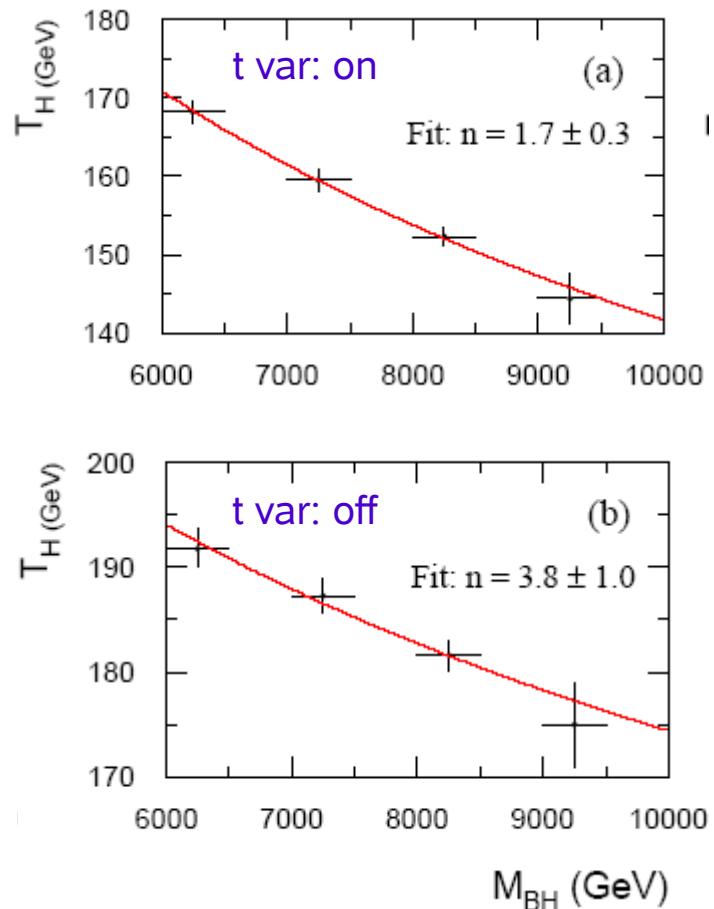
Take the logarithm of both sides of  $T_H$ :

$$\log(T_H) = \frac{-1}{n+1} \log(M_{BH}) + \text{const}$$

Plot  $M_{BH}$  vs.  $T_H$  and fit to a line. Find  $n$  from the slope.



But, including time variation leads to problems!



Landsberg, Dimopoulos, PRL 87, 161602 (2001)

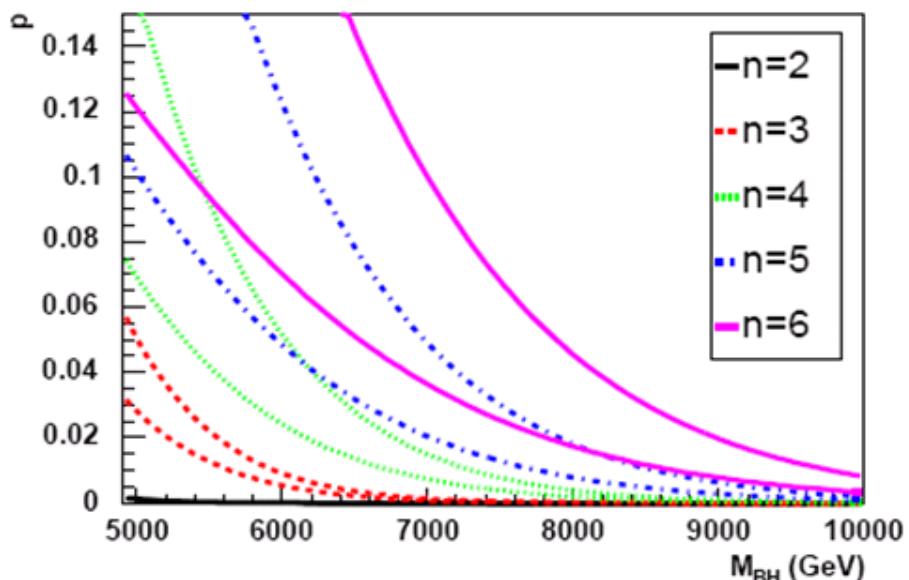
Harris et al tried a method in which they determined the order of particles emitted, reconstructed  $M_{BH}$  and  $T_H$  after each emission.

# Learning about spacetime

Harris et al, ATLAS, Charybdis,  $M_{4+n} = 1$ ,  $n = 2$

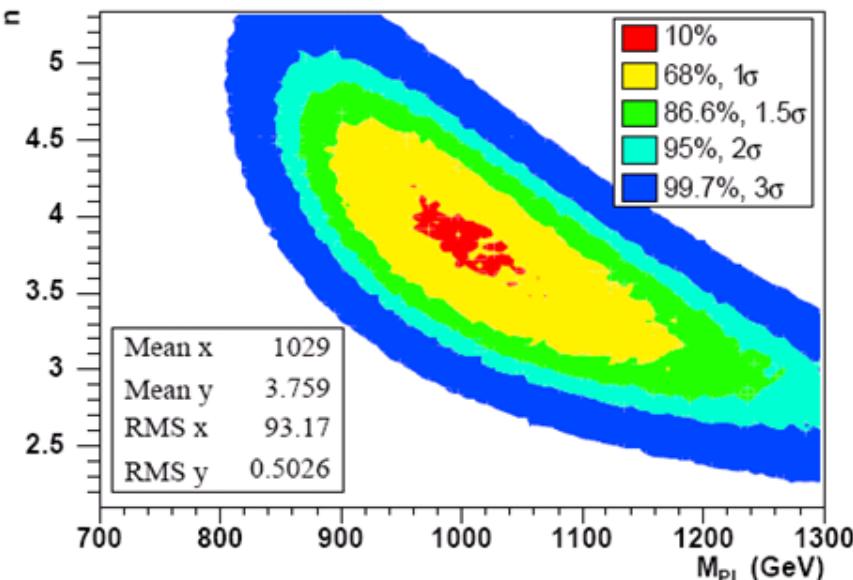
To find n: Plot the fraction p of events which emit particles with energy  $E_{cut} = M_{BH}/2 - d$ . This fraction is strongly dependent on n.

To find  $M_{(4+n)}$ : Make use of cross sections since they strongly depend on  $M_{(4+n)}$  but their n-dependence is negligible.



Theoretical upper and lower limits on p:

$$p_{lower} = k \int_{E_{cut}}^{M_{BH}/2} PdE \quad p_{upper} = k \int_{E_{cut}}^{\infty} PdE$$



The final fit!

Combines "n" determination from p parameter and " $M_{(4+n)}$ " determination from cross sections

## CONCLUSIONS

Both direct ADD graviton production and ADD graviton contribution to DY processes can be observed with sufficient significance for moderate values of  $M_{4+n}$

Copious BH production might be possible at the LHC, and if this is realized, BHs will be identified by their significant signature. By looking at BH decay products, BH mass, Hawking temperature and spacetime properties might be reconstructed.