

# MINIMAL SUSY BREAKING IN GUTS

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(JSI, LJUBLJANA, SLOVENIA)

LHC DAYS  
IN SPLIT 06

WORK DONE WITH  
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①

SUPERSYMMETRY (SUSY)

MOTIVATED BY (TALK SENJANOVIĆ!)

— GAUGE COUPLING UNIFICATION

— HIERARCHY PROBLEM

— DYNAMICAL ELECTROWEAK  
SYMMETRY BREAKING

SUSY PART OF MSSM (W) KNOWN  
SUPER POTENTIAL

~~SUSY~~ PART OF MSSM UNKNOWN

PHENOMENOLOGICAL CONSTRAINTS:

DIRECT SEARCHES  $\Rightarrow \tilde{m} \gtrsim 100 \text{ GeV}$

FCNC  $\Rightarrow$  FLAVOUR STRUCTURE OF  
SPERMIONS SIMILAR TO  
FERMIONS ( $V_{CKM}$ )

# SUPERSYMMETRY:



$$e \longrightarrow E = \tilde{e} + \theta e + \theta\theta F$$

Labels for the equation above:

- $e$ : FERMION  $S = 1/2$
- $E$ : SUPERFIELD
- $\tilde{e}$ : BOSON  $S = 0$
- $\theta e$ : FERMION  $S = 1/2$
- $\theta\theta F$ : AUXILIARY FIELD

$\theta$  ... GRASSMAN VARIABLE

$$F \neq 0 \iff \text{SUSY}$$

① CAN WE BREAK SUSY  
IN MSSM?

$$F_{H, \bar{H}} \neq 0 \quad (\text{THE ONLY POSSIBILITY})$$

$$\int d^2\theta y_e H \cdot \cancel{L} e^c \rightarrow y_e F_H \tilde{e} \tilde{e}^c$$

$$V = \sum_i \left| \frac{\partial W}{\partial \varphi_i} \right|^2 = y_e^2 |H|^2 (|\tilde{e}|^2 + |\tilde{e}^c|^2) + \dots$$

$$\begin{pmatrix} \tilde{e}^* & \tilde{e}^c \end{pmatrix} \begin{pmatrix} y_e^2 v^2 & y_e^2 F \\ y_e^2 F & y_e^2 v^2 \end{pmatrix} \begin{pmatrix} \tilde{e} \\ \tilde{e}^{c*} \end{pmatrix}$$

$$m_{1,2}^2 = y_e^2 (v^2 \pm F)$$

$\Downarrow$

$$m_1^2 + m_2^2 = 2 m_e^2$$

IMPOSSIBLE!

SUCH ~~OPERATOR~~  
MASS SUM RULE

ALWAYS IN SUSY  
AT TREE ORDER.

WAYS OUT:

a) USE OF LOCAL SUSY (SUGRA)

b) SUSY BREAKING BY LOOPS

IN BOTH CASES

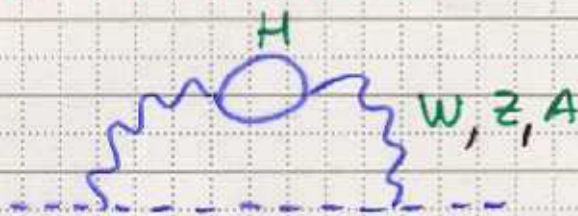
NONRENORMALIZABLE OPERATORS  
(BUT IN b) CALCULABLE)

② CAN ONE ADD JUST ONE EXTRA FIELD WITH  $F \neq 0$  ?

NO!

$\int d^2\theta H\bar{H} (\mu + X) \Rightarrow m_{\tilde{H}} = \mu$  (HIGGSING)  
 $m_{H_1}^2 = \mu^2 - F$  (SM HIG)  
 $m_{H_2}^2 = \mu^2 + F$

OTHER FERMIONS:



$m_{\tilde{f}}^2 \sim \left(\frac{\alpha}{4\pi}\right)^2 \left(\frac{F}{M}\right)^2 \ll F$

$F \sim \mu^2$  LARGE ( $m_{H_1}^2 \sim m_W^2$ )

GAUGINO:



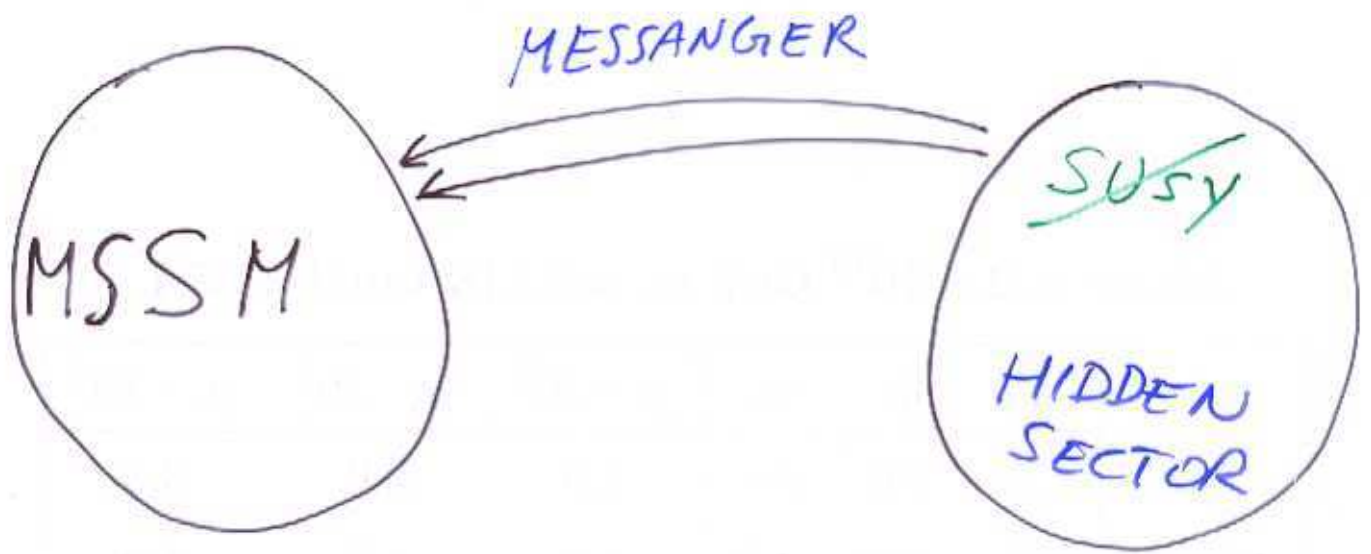
SIMILAR

BUT  $y_t \sim 1$ :



$\Rightarrow m_{\tilde{t}_c}^2 \approx -y_t^2 F$

LARGE AND NEGATIVE



(3) FEW SHORT COMMENTS ON KNOWN MODELS OF SUSY:

(A) GRAVITY MEDIATION

MESSANGER  $\Rightarrow$  GRAVITY

— GRAVITY ALREADY THERE

— JUST A PARAMETRIZATION,  
SOFT TERMS DEPEND ON ~~THE~~  
ASSUMPTIONS ON KÄHLER

CMSSM:

EVERYTHING CALCULABLE  
IN TERMS OF FEW PARAMETERS

$(m_0, m_{1/2}, A, B, \dots)$ ,

BUT THEORETICALLY NOT MOTIVATED!

WHY SHOULD KÄHLER BE CANONICAL?





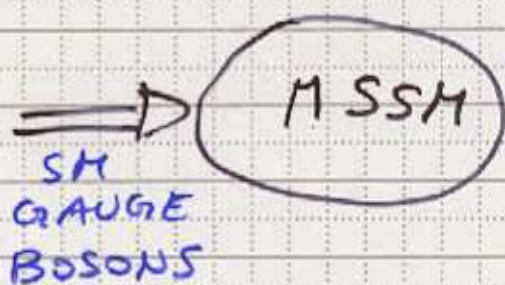
# (C) GAUGE MEDIATION

ALREADY SEEN AN UNSUCCESSFUL EXAMPLE WITH  $-F_X \neq 0$

$-X$  COUPLED TO  $H \bar{H}$

$$F_X \neq 0$$

EXTRA  $q, \bar{q}, e, \bar{e}$   
GETS MSSM MASSES



$$W = \lambda_q X \bar{q} q + \lambda_e X \bar{e} e + W_{\text{MSSM}}$$

APPARENTLY FLAVOUR CONSERVING  
(GAUGE INTERACTIONS FLAVOUR BLIND)

BUT TO SAVE GAUGE COUPLING UNIFICATION

$$5 \sim (q, e) \quad \bar{5} \sim (\bar{q}, \bar{e})$$

"d" "L"

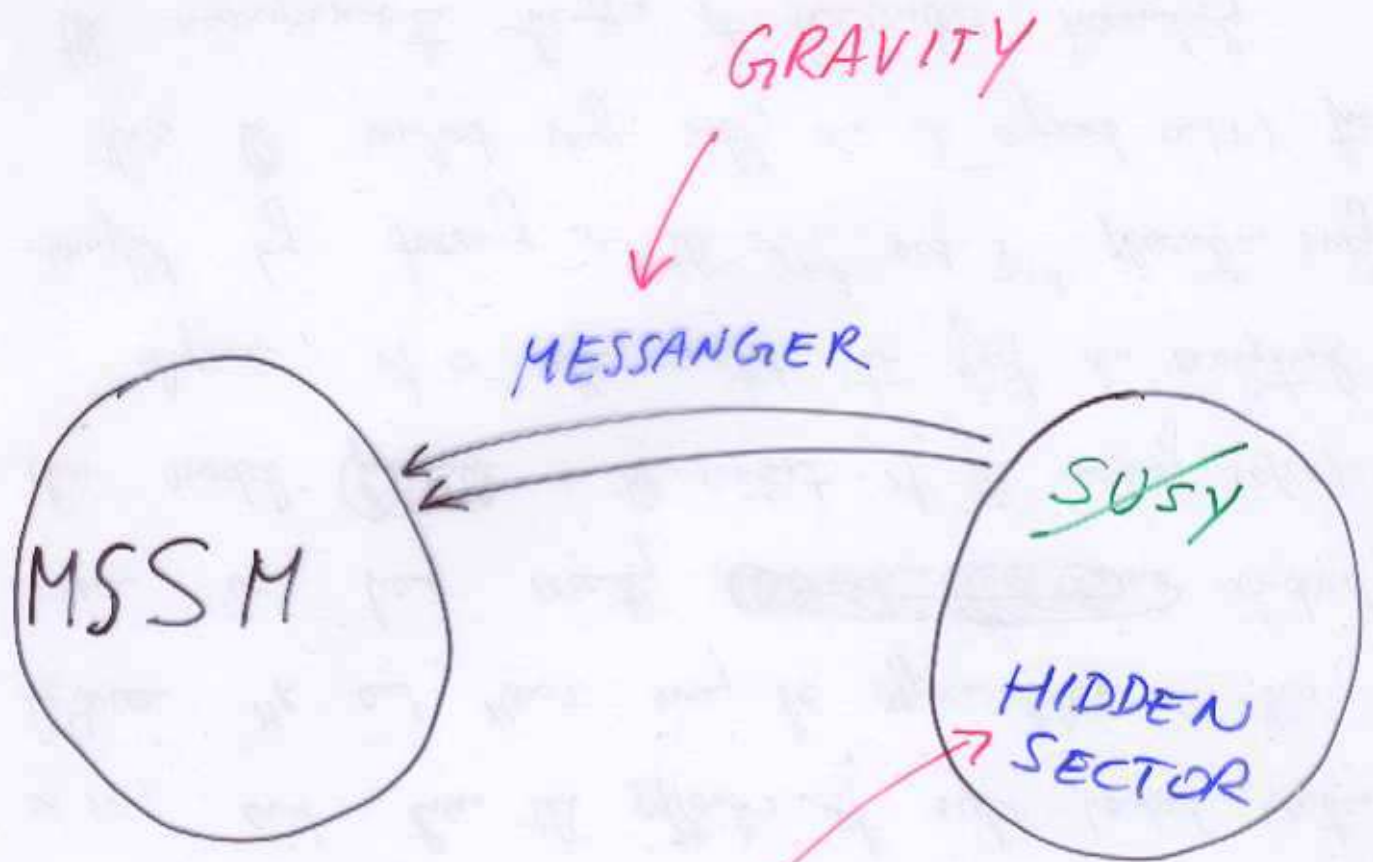
$\Rightarrow \tilde{Y} H e^c$  POSSIBLE  
(EXTRA FLAVOUR MIXING!)

$$\Rightarrow \tilde{Y} \ll 1$$

NOT ~~MUCH~~ BETTER THAN SUGRA!

④ SUSY NATURALLY TIED  
WITH GUTS  
(GAUGE COUPLING UNIFICATION)

CAN WE GET ANY  
INSIGHT IF WE CONNECT  
THE FIELD  $X$  THAT  
BREAKS SUSY ( $F_x \neq 0$ )  
WITH A GUT MULTIPLY?



CAN IT BE THE HIGGS  
SECTOR IN A GUT?

(FOR EX.  $24_H$  IN  $SU(5)$ )

## RULES OF THE GAME :

① NO EXTRA INTERACTIONS  
EXCEPT GUT

(NO ROOM FOR DYNAMICAL  
SYMMETRY BREAKING  
OR FAYET-ILIPOULOS)

AND GRAVITY

(= MESSENGER)

② NO SINGLET

(NO ROOM FOR O'RAIFEARTAIGH)

$$\Sigma = \sigma \begin{pmatrix} 2 & & & & \\ & 2 & & & \\ & & 2 & & \\ & & & \emptyset & \\ \emptyset & & & -3 & \\ & & & & -3 \end{pmatrix} + \begin{pmatrix} \Sigma_8 & & & & \\ & \dots & & & \\ & & \dots & & \\ & & & \dots & \\ & & & & \Sigma_3 \end{pmatrix}$$

SIMILAR TO X BEFORE

$$F_\sigma \neq 0$$

$$\langle \sigma \rangle = M_{\text{GUT}}$$

$\Sigma_8 \dots$  COLOR OCTET

USUALLY

$\Sigma_3 \dots$  WEAK TRIPLET

$$M_{3,8} \sim M_{\text{GUT}}$$

## ⑤ RESULTS

(A) CAN BE DONE, BUT  
FINE-TUNING NEEDED  
IN MINIMAL MODELS

$$\sigma(1) - \sigma(1) \approx \sigma(10^{-13})$$

DUE TO

GAUGE COUPLING UNIFICATION  
CONSTRAINTS

## (B) INTERMEDIATE MASS SCALES

$$M_{3,8} \sim \frac{M_{\text{GUT}}^2}{M_{\text{pe}}} ; \quad \frac{\mu_3}{\mu_8} = 4$$

GOOD NEWS!

$$M_{\text{GUT}} = M_{\text{GUT}}^0 \left( \frac{M_{\text{GUT}}^0}{(\mu_3 \mu_8)^{1/2}} \right)^{1/2}$$

$$\mu_T = \mu_T^0 \left( \frac{\mu_3}{\mu_8} \right)^{5/2}$$

$\mu_T$  HEAVIER  $\Rightarrow$  PROTON DECAY ( $d=5$ )  
SUPPRESSED

$$\tau_p \approx 10^3 \tau_p^0$$



# CONCLUSIONS

- ① EXERCISE SUCCESSFUL :  
BREAKING OF SUSY AND GUT  
BY THE SAME FIELD POSSIBLE
- ② GUT + GRAVITY, NO SINGLET  
(GOOD NEWS)
- ③ A LOT OF FINE-TUNING  
(PRICE TO PAY)
- ④ NOT MUCH INFORMATION ON ~~SOFT~~  
SOFT TERMS (AS IN POLONYI  
IT DEPENDS ON KÄHLER)
- ⑤ A LOT OF INFORMATION  
ON THE HIGGS SECTOR

MOST IMPORTANT :

D=5 PROTON DECAY NATURALLY  
PUSHED TO  $\tau_p \rightarrow 10^{34}$  yrs