

# **B-Field Corrections to Gas Monitor RT Functions**

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# Procedure

- Use the functional form of Oliver Kortner's solution to the drift electron's equation of motion in the MDT environment with a B-Field on
- Compute a scalable correction function based on Garfield
- Assign an average B-Field to every Chamber from AMDB and a static B-Field map
- Compute an RT function for every Chamber

# $dT_B$

- **Equation of Motion for Drift Electrons:**

$$\ddot{\mathbf{x}} = -\left(\frac{\dot{\mathbf{x}}}{\tau}\right)^{1+\epsilon} + \frac{q}{m} [\mathbf{E} + \dot{\mathbf{x}} \times \mathbf{B}] ; \quad \tau \equiv \text{mean free time}$$

$\epsilon \approx .0074$ : experimentally determined

- **Solution:**

$$l(r, \mathbf{B}) = l(r, \mathbf{B} = \mathbf{0}) + B^{2-\epsilon} \times \int_{r_{\text{wire}}}^r \frac{v_{B=0}^{1+\epsilon}}{E^{2-\epsilon}} dr$$

- **Corrections:**

$$\begin{aligned} dt(r, B_{\text{obs}} - B_{\text{ref}}) \\ = (B_{\text{obs}}^{2-\epsilon} - B_{\text{ref}}^{2-\epsilon}) \times I(E(r), v(r))_{B=0} \end{aligned}$$

# $B_{eff}$

- First Order Corrections:

$$B_{v_{e^-}}^{perp}$$

- Second Order:  $B_{v_{e^-}}^{\parallel}$

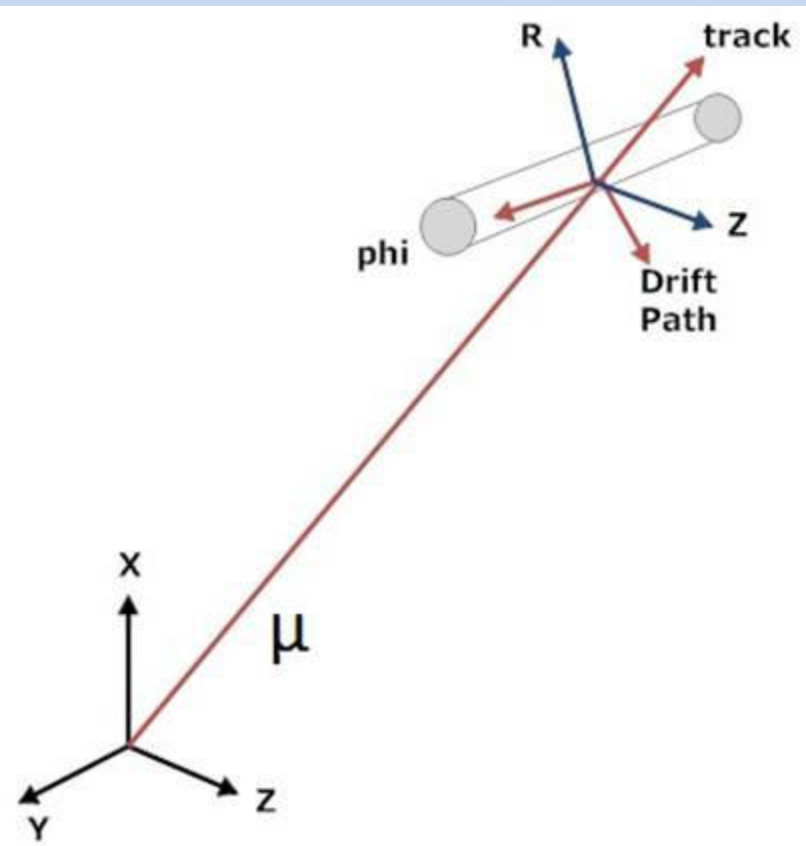
- Coordinates:

- Effective B-Field that requires correction is

$$|B_{v_{e^-}}^{perp}| = \sqrt{B_{\mu_{\parallel}}^2 + B_{wire_{\parallel}}^2}$$

- Work out the transformations

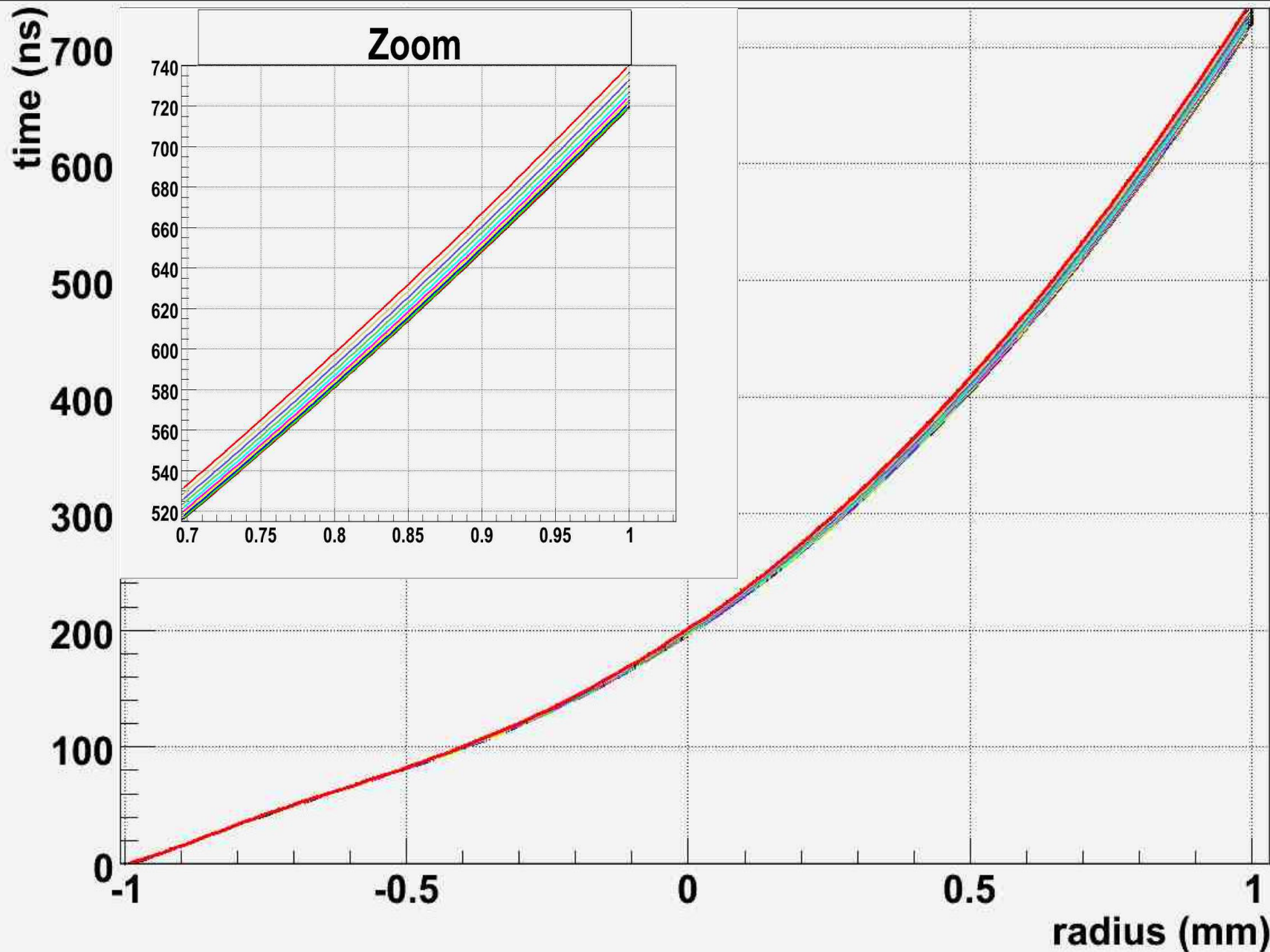
$$|B_{v_{e^-}}^{perp}| = \sqrt{B_{\phi}^2 + B_r^2 \left(\frac{r}{\rho}\right)^2 + 2B_r B_z \left(\frac{r z}{\rho^2}\right) + B_z^2 \left(\frac{z}{\rho}\right)^2}$$



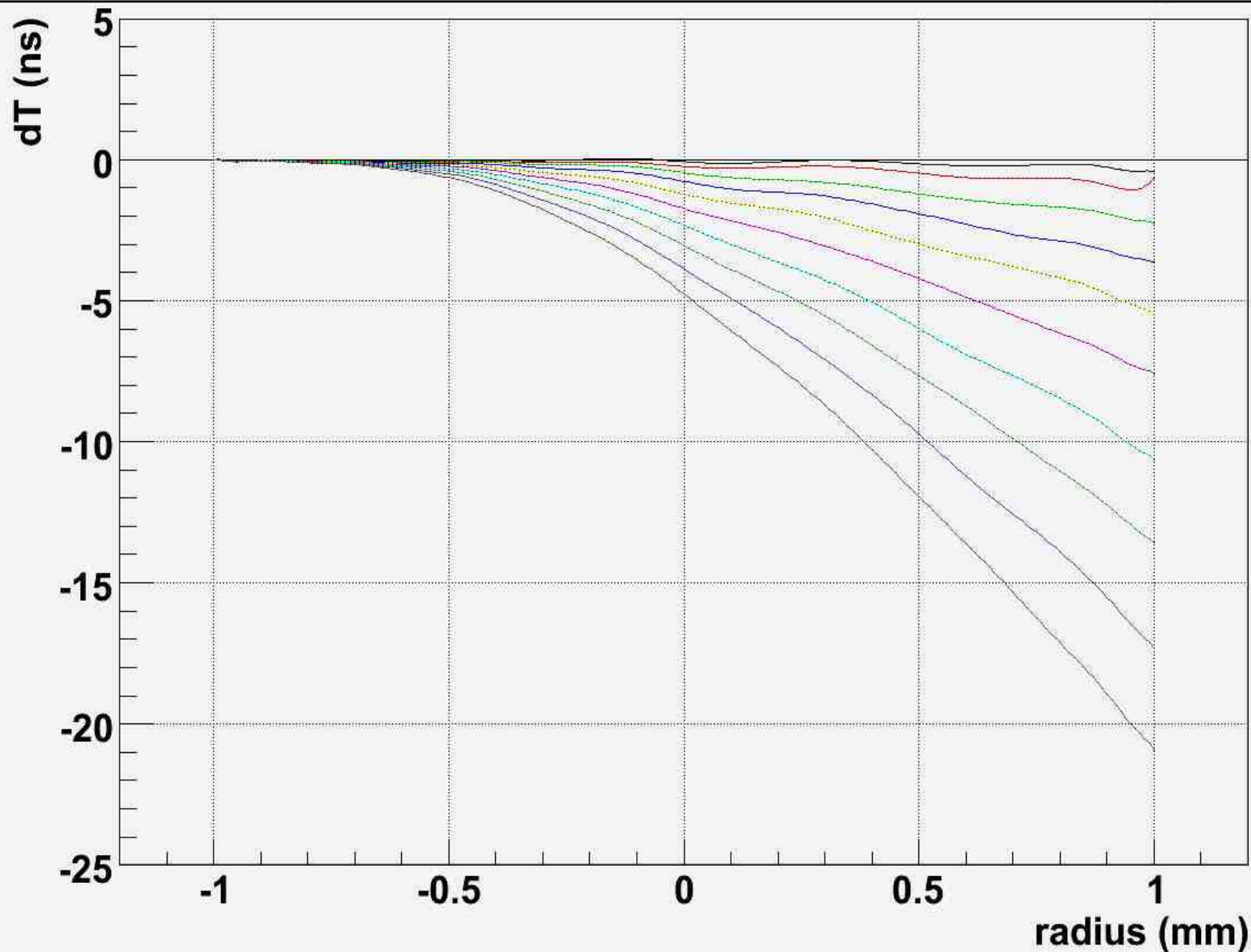
# Garfield Simulation Correction Function

- Garfield
- Output TRs in  $B_{eff}$  steps of .05T from 0T to 1T
- Compute all possible combinations of  $dT(r, B_{obs}^{eff} - B_{ref}^{eff})$  and normalize to reference field.
- Use average and cutting procedure to create a scalable correction function from the normalized  $dTRs$ .

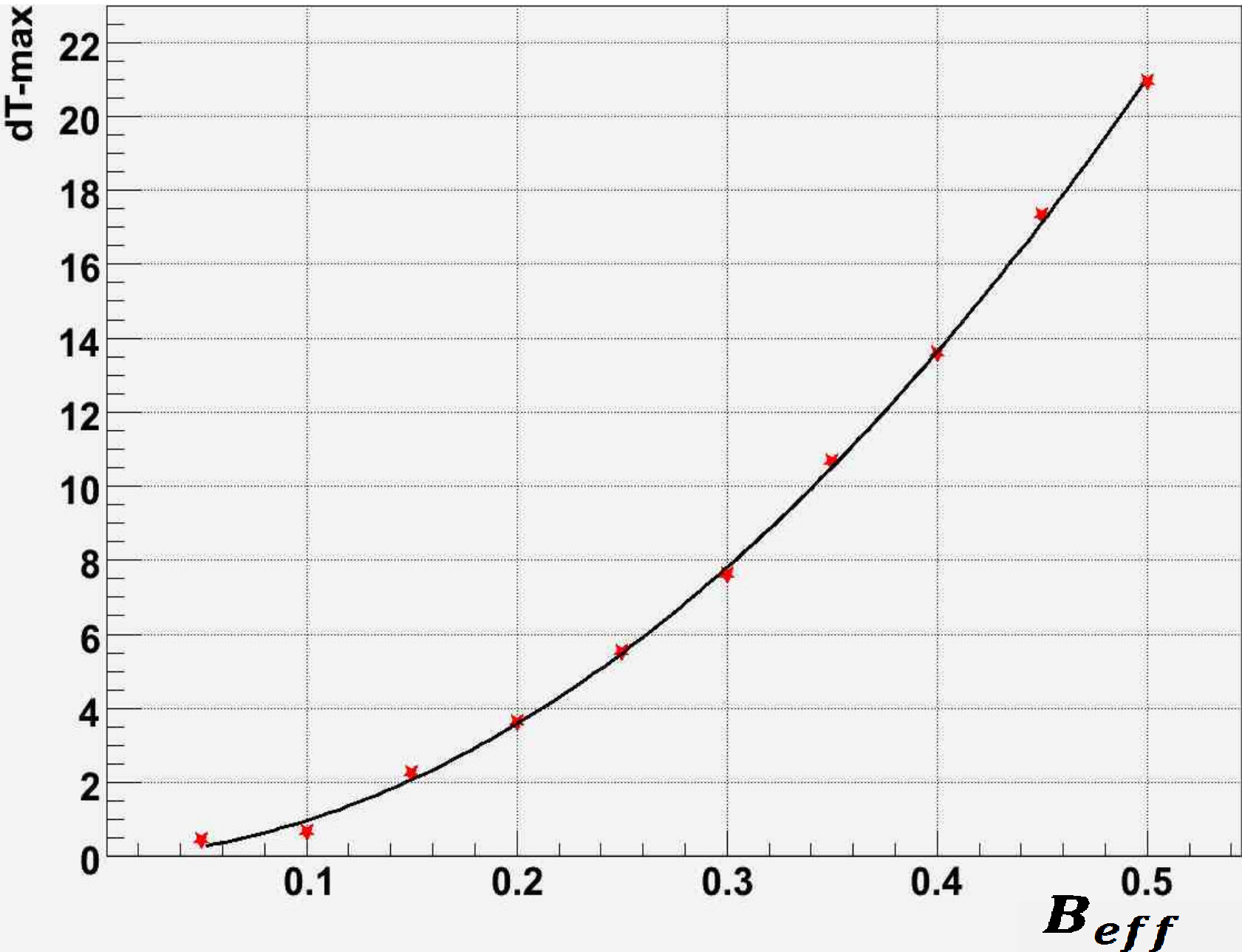
# TR functions with $B=n*.05T$ from Garfield Simulations in Chebyshev Space



# Set of dTR Combinations: .05T steps

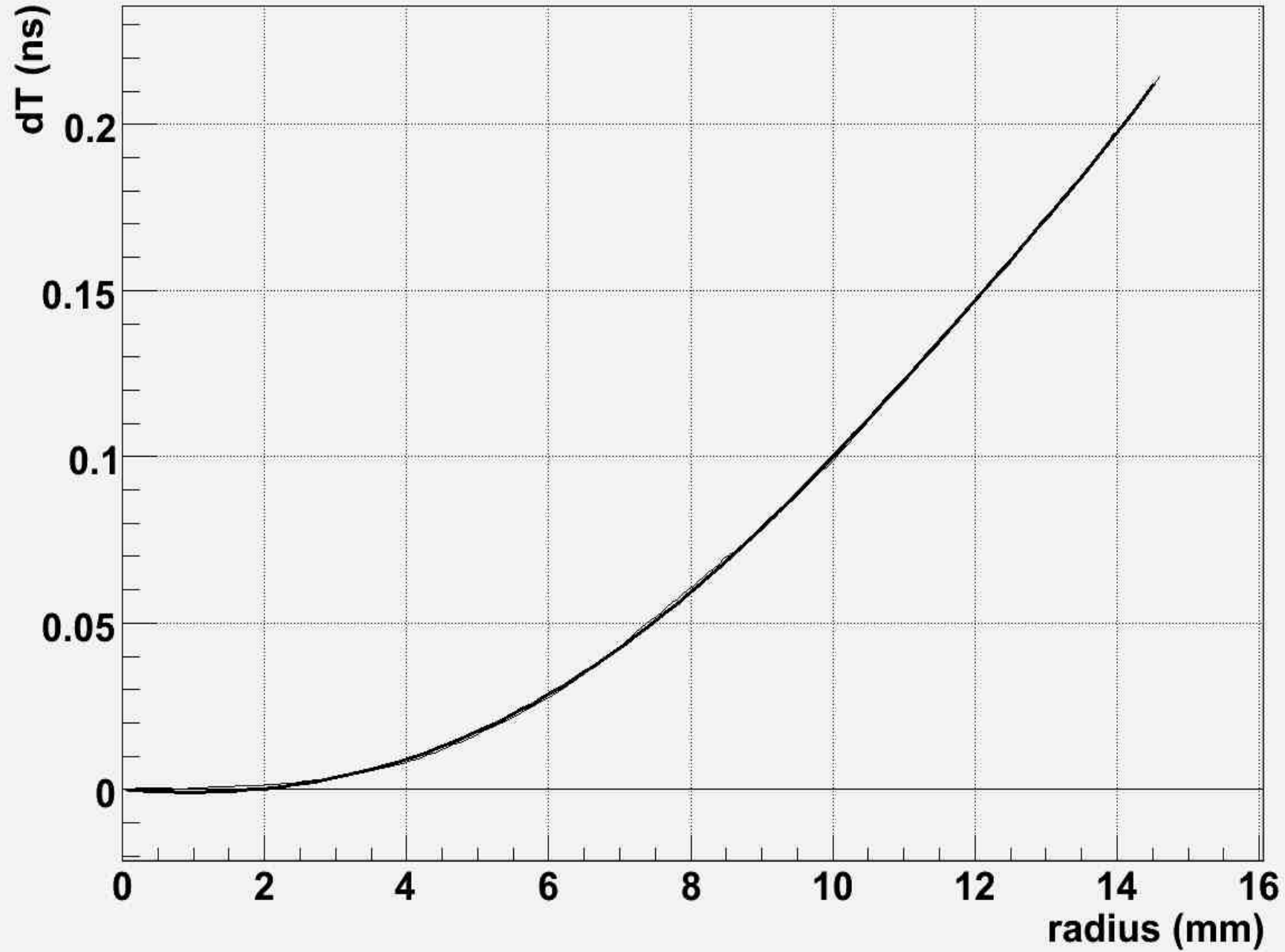


# Non Linear Corrections at the Tube Wall: Nearly Quadratic

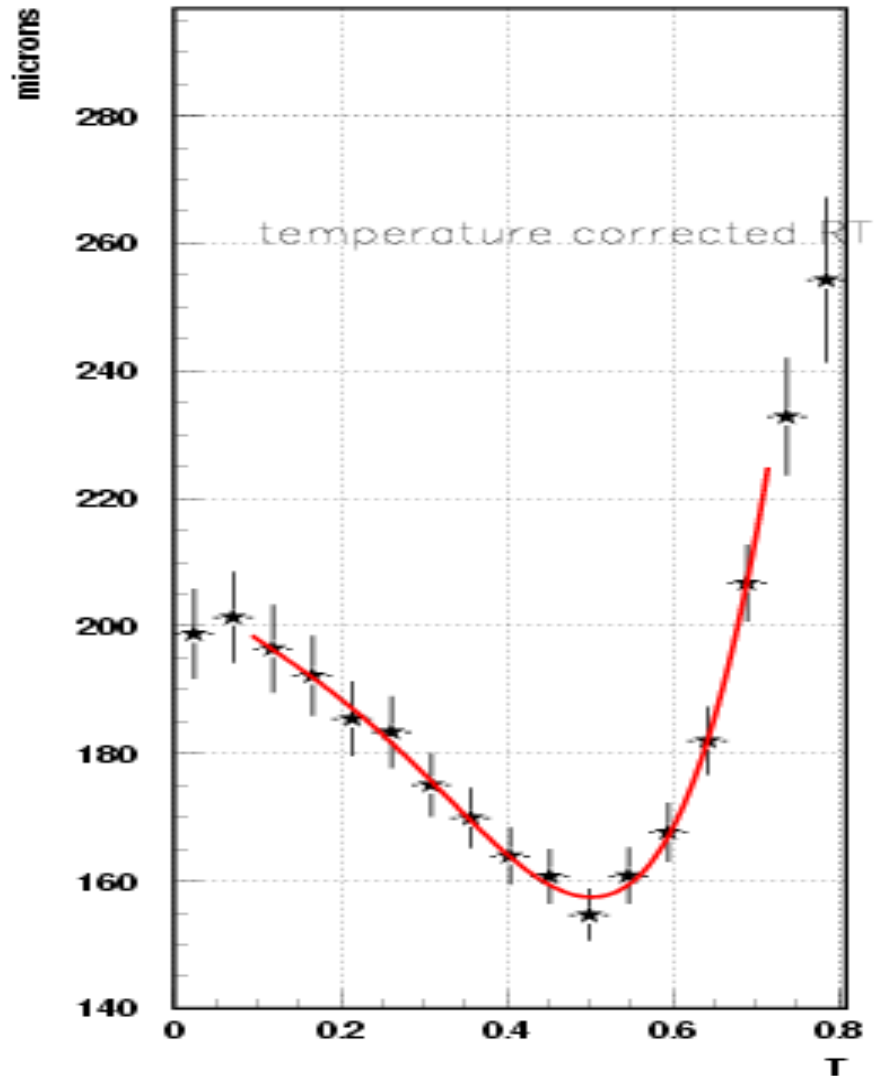
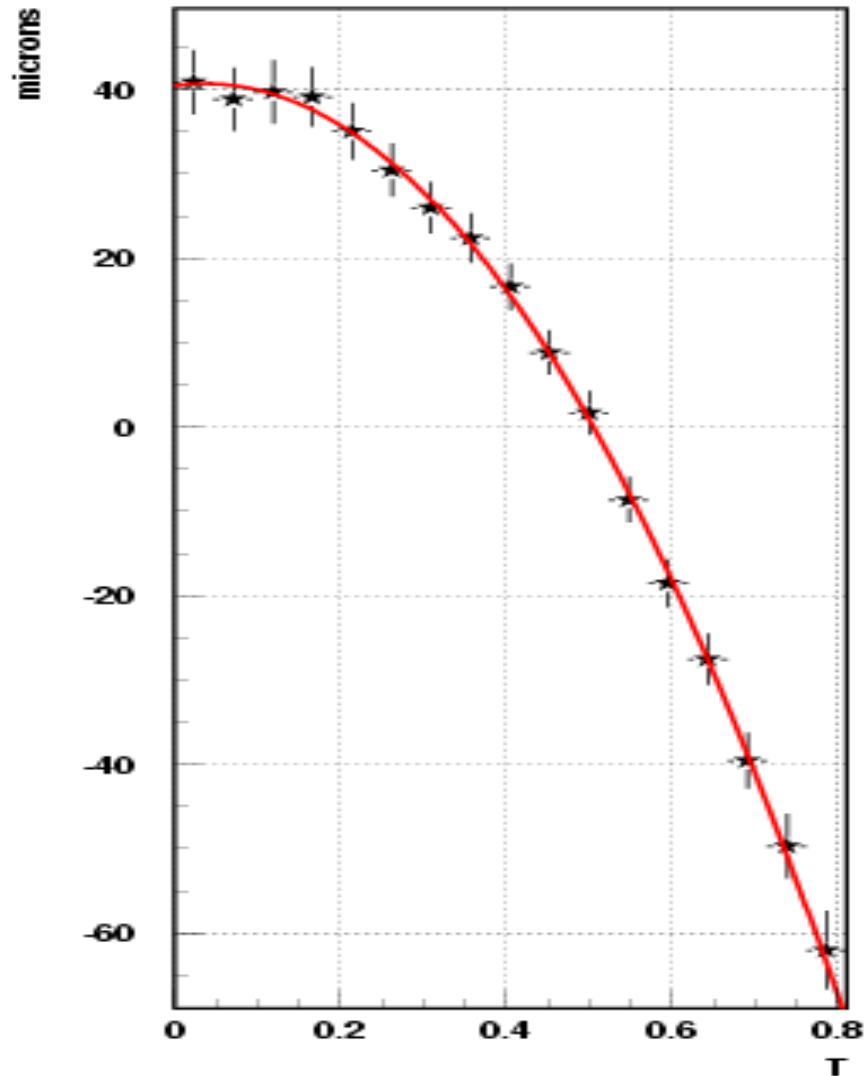




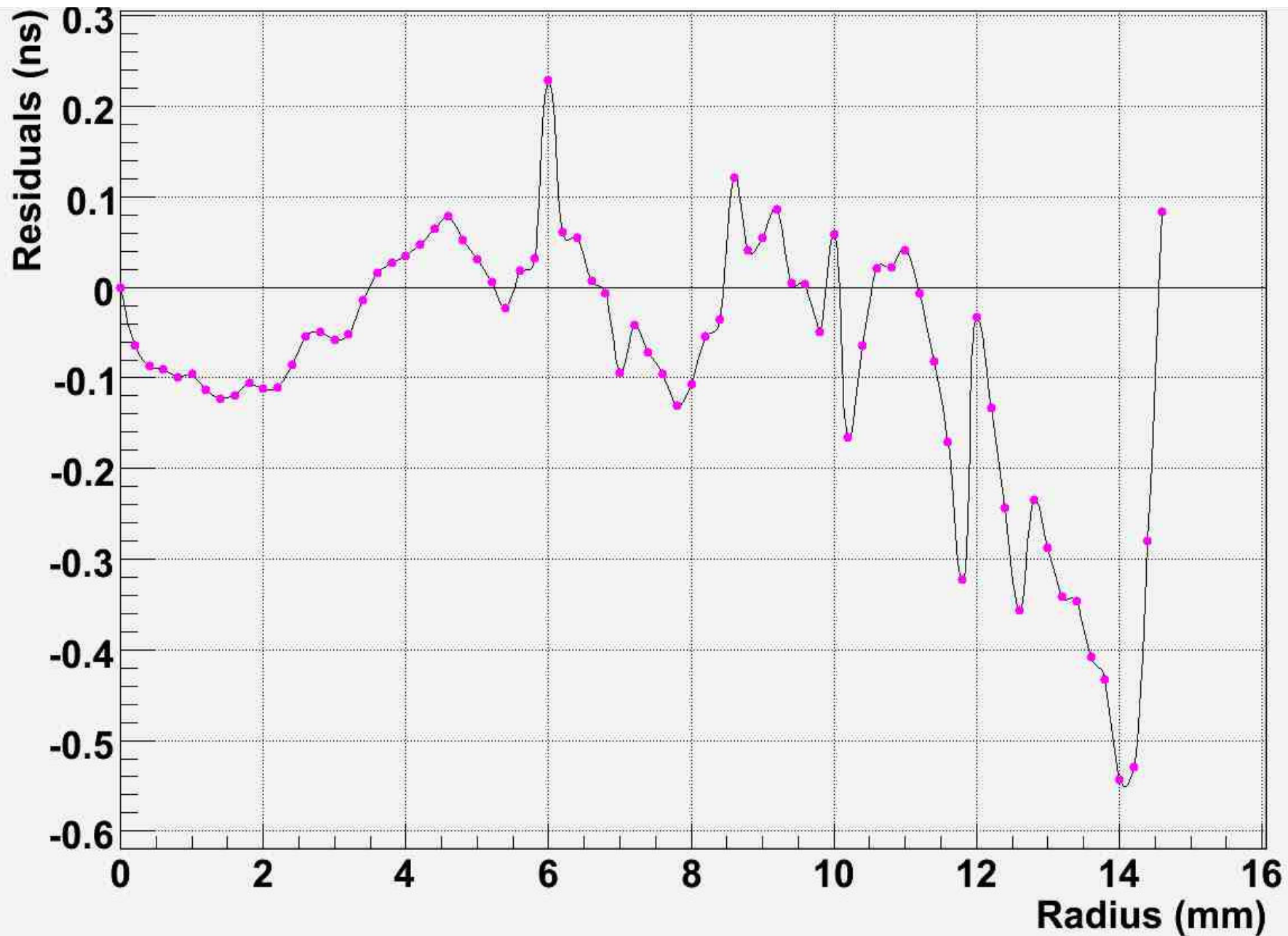
# Correction Function Normalized to $B_{eff} = .05T$



# Real Data Comparison Using Track Reconstruction Program MUTRAK



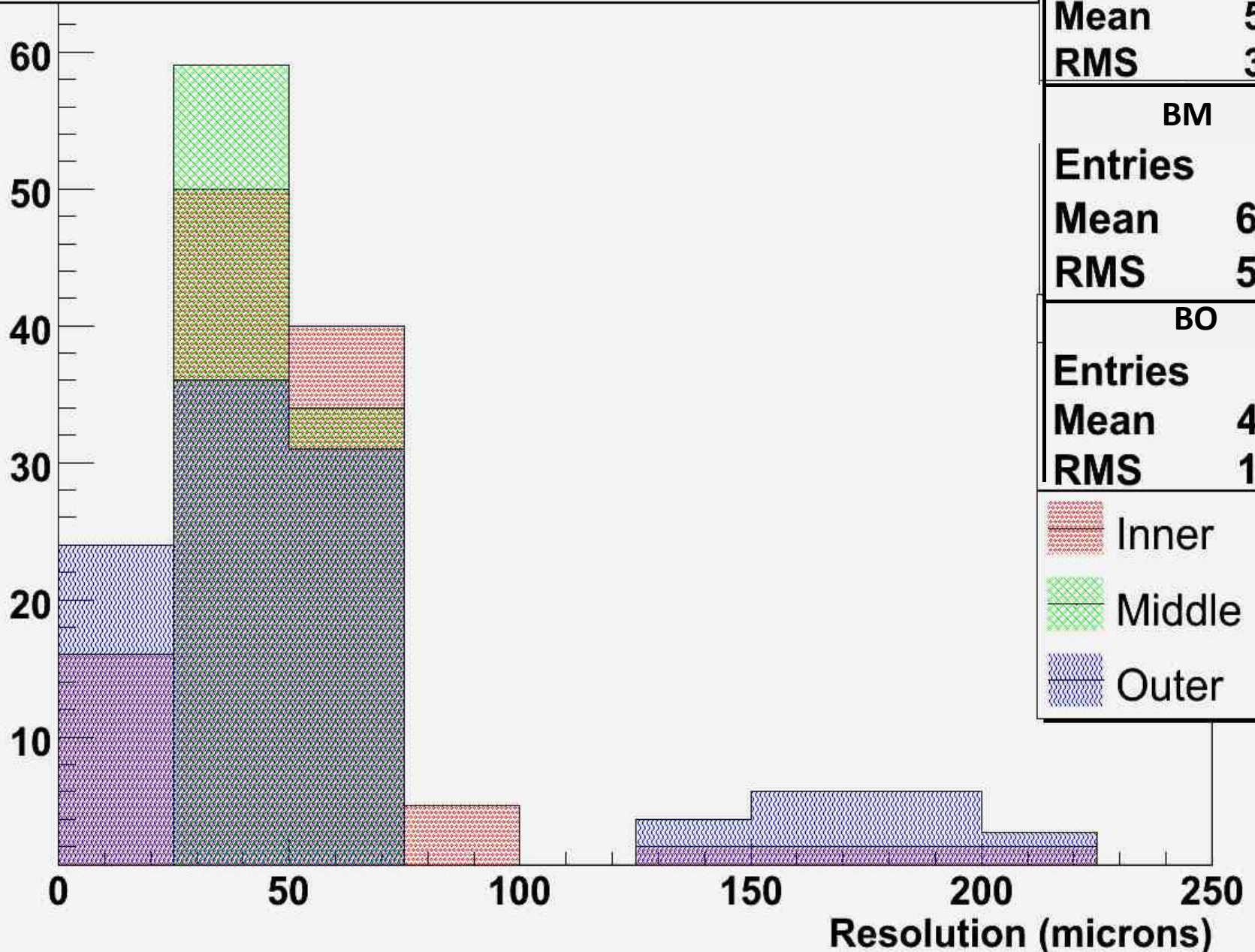
Residuals: RT(B=0) and Correction Function with RT(Bx=.3T,By=.3T,Bz=.3T)



# Can We Use A Single B-Field Corrected RT Per Chamber?

- Assign an average B-Field per Chamber from a line integral along bases with even steps.
- Compute the average drift time correction in an MDT at a particular location from the average B-Field and the actual B-Field.
- Take the difference between these measurements and multiply by the average drift velocity. This will be the local resolution degradation.
- Repeat this process iteratively over the chamber and average the results. This will be the average resolution degradation in a given chamber.
- We want this to be less than  $50\mu\text{m}$ : the overall tube resolution will be  $94\mu\text{m}$ .

# Systematic Resolution Degradation



BI	
Entries	123
Mean	53.85
RMS	37.17

BM	
Entries	110
Mean	62.32
RMS	51.53

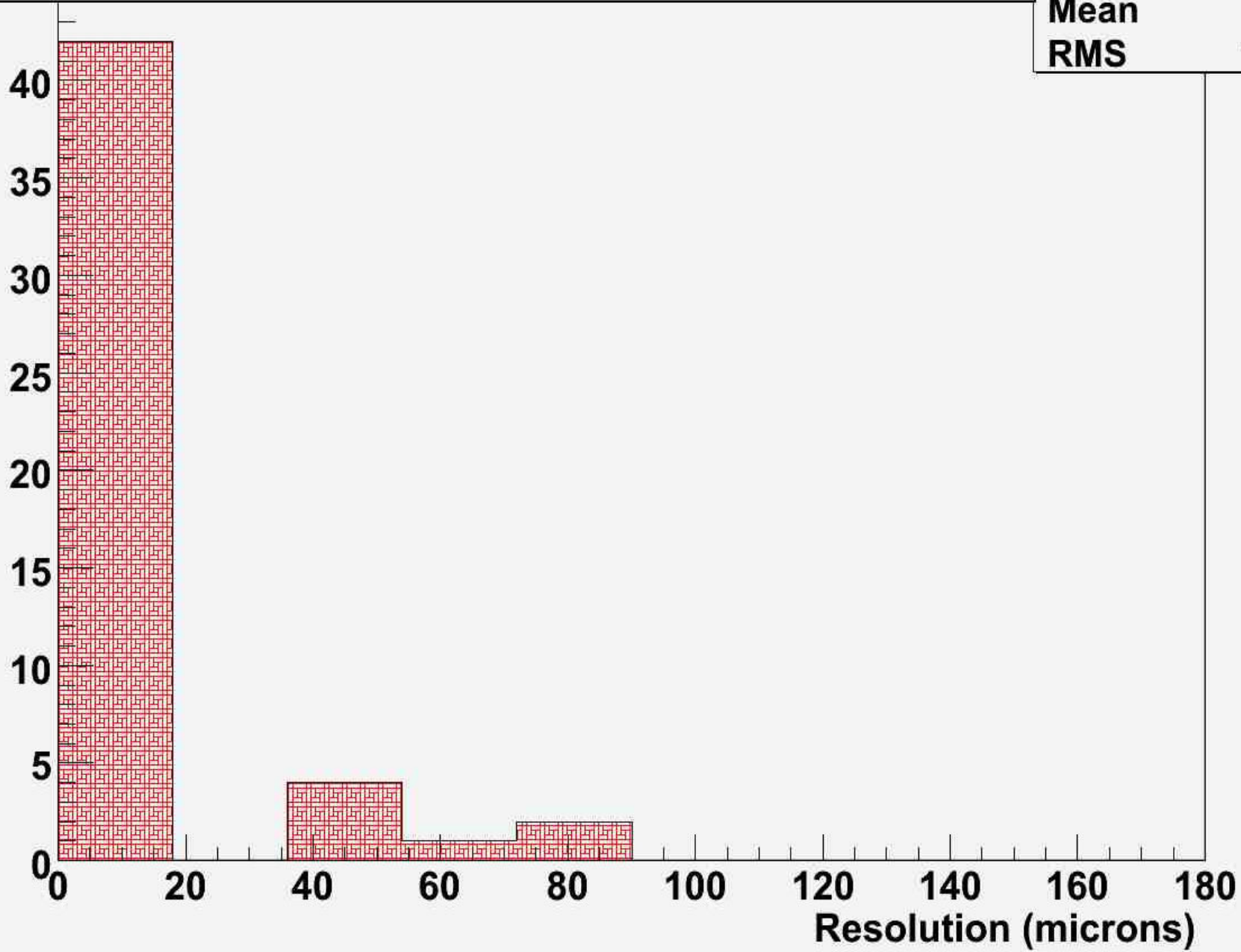
BO	
Entries	93
Mean	45.85
RMS	10.86

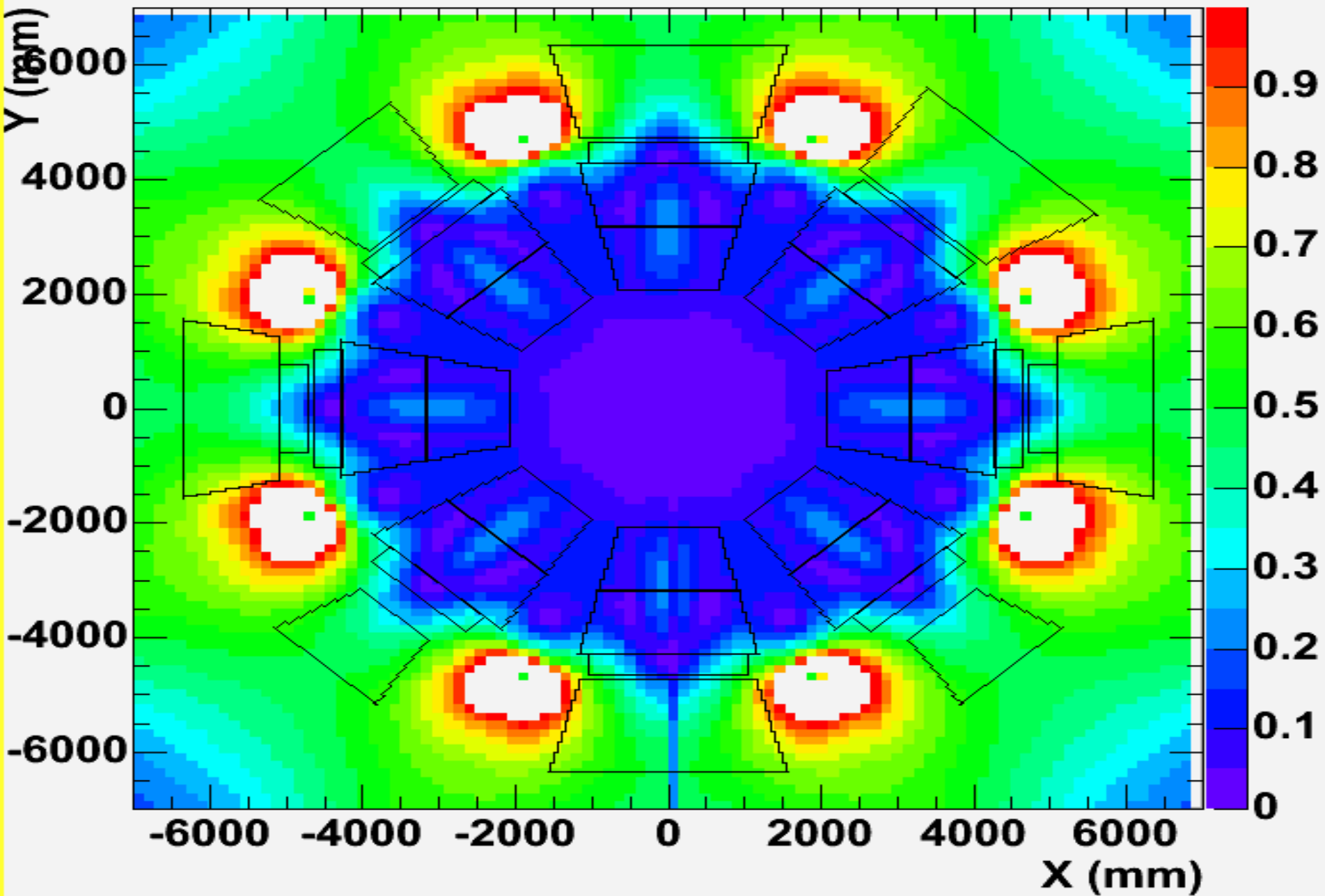
Inner	
Middle	
Outer	

# Systematic Resolution Degradation

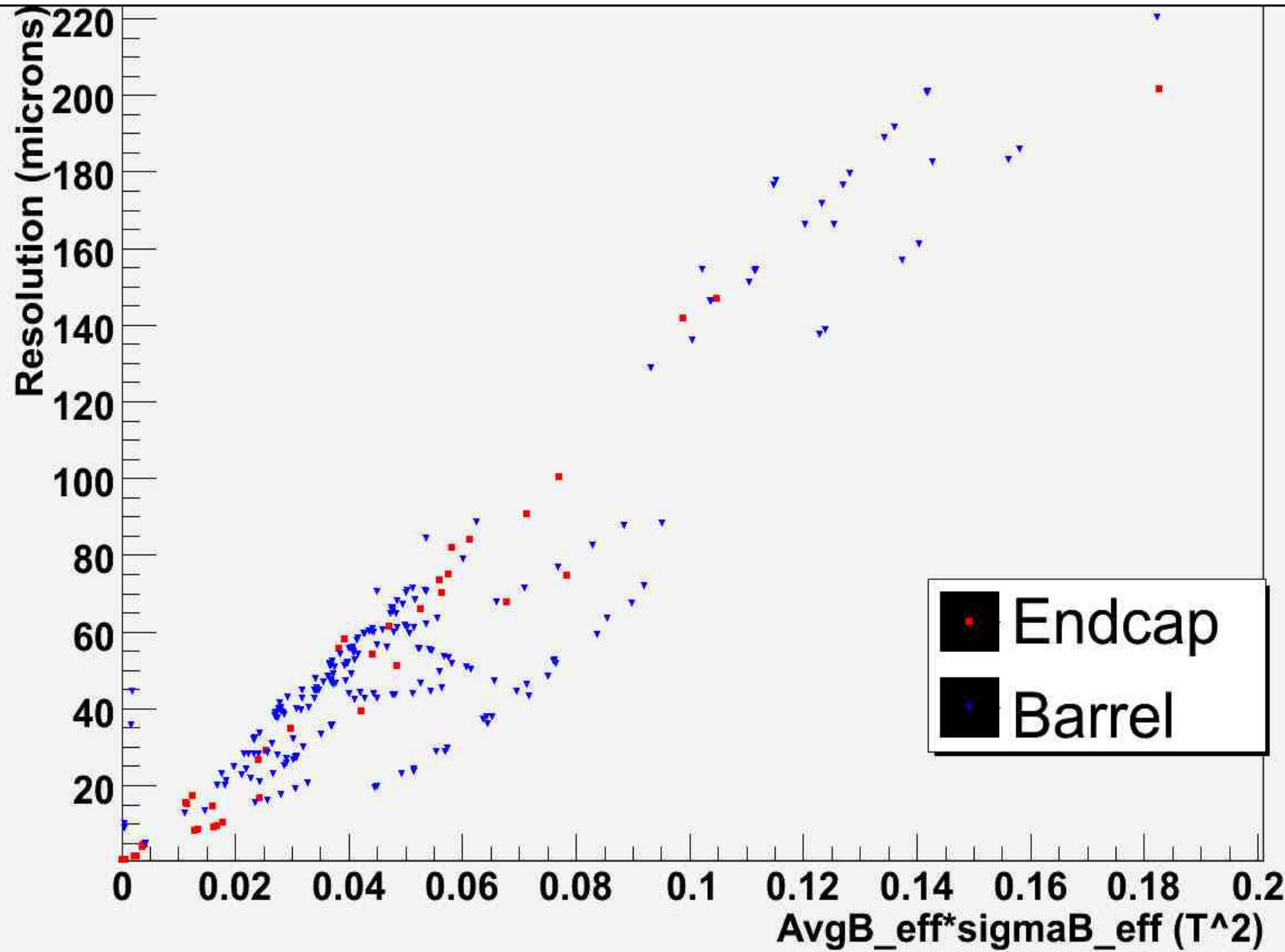
	El
<b>Entries</b>	<b>50</b>
<b>Mean</b>	<b>13.6</b>
<b>RMS</b>	<b>18.94</b>



**EIL B eff. field map**



# Resolution Degradation vs. The Product of $B_{eff}$ and $\sigma_B$





# Conclusion

- The resolution degradation is less than  $50\mu\text{m}$ , in 69% of the chambers.
- 87% in the Endcap: Exceptions are EIL4, EEL1, EEL2, EES1, EES2.
- 90% in EI, 100% in EM, 100% in EO, and 10% in EE.
- 55% in the Barrel: 54% in BI, 63% in BM, and 55% in BO.
- Corrections in the Barrel will have to be made at the hit-level.
- Endcap corrections could be added to the Automated Temperature Correction Procedure