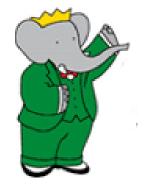
Precise Measurement of the $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$ Cross Section with BaBar and the Muon g-2

Michel Davier (LAL – Orsay, BaBar Collaboration)

- the muon magnetic anomaly
- e^+e^- and (revisited) τ spectral functions
- the BaBar ISR (Initial State Radiation) analysis
- test of the method: $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$
- results on $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$
- combination of all ee data
- discussion and perpectives





Lepton Magnetic Anomaly: from Dirac to QED

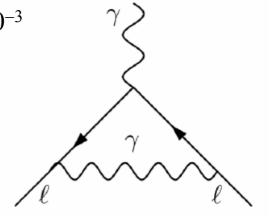
$$\vec{\mu} = g \frac{e}{2m} \vec{s}, \qquad \qquad a = (g-2)/2$$

Dirac (1928) $g_e=2 a_e=0$

anomaly discovered: Kusch-Foley (1948) $a_e = (1.19 \pm 0.05) \ 10^{-3}$

and explained by O(α) QED contribution: Schwinger (1948) $a_e = \alpha/2\pi = 1.16 \ 10^{-3}$

first triumph of QED



 \Rightarrow a_e sensitive to quantum fluctuations of fields

More Quantum Fluctuations

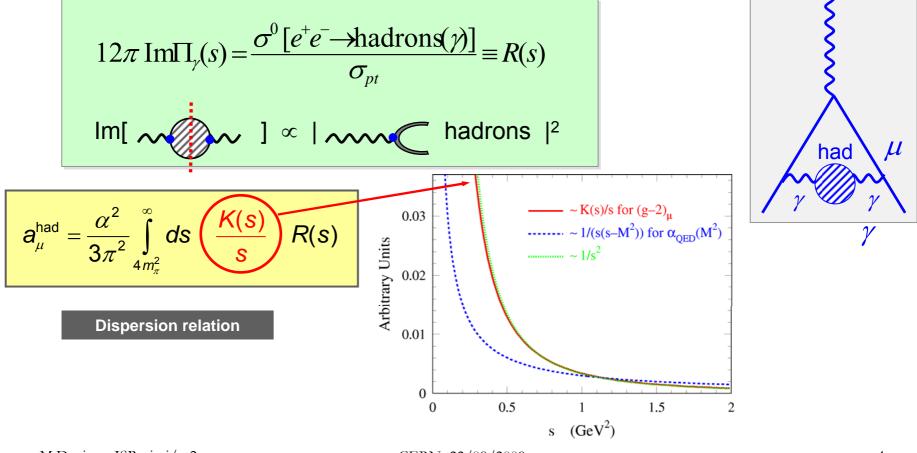
$$a = a^{\text{QED}} + a^{\text{had}} + a^{\text{weak}} + ? \text{ a new physics } ?$$
typical contributions:
QED up to O(\alpha^4), \alpha^5 in progress (Kinoshita et al.)
Hadrons
vacuum polarization
Hadrons
vacuum polarization
ight-by-light (models)
$$\pi^0, \eta, \eta' \qquad \eta_1 \qquad \eta_2 \qquad \eta_1 \qquad \eta_2 \qquad \eta_1 \qquad \eta_2 \qquad \eta_2 \qquad \eta_2 \qquad \eta_1 \qquad \eta_2 \qquad \eta_2$$

Hadronic Vacuum Polarization and Muon $(g-2)_{\mu}$

Dominant uncertainty from lowest-order HVP piece

Cannot be calculated from QCD (low mass scale), but one can use experimental data on e+e→hadrons cross section

Born: $\sigma^{(0)}(s) = \sigma(s)(\alpha / \alpha(s))^2$

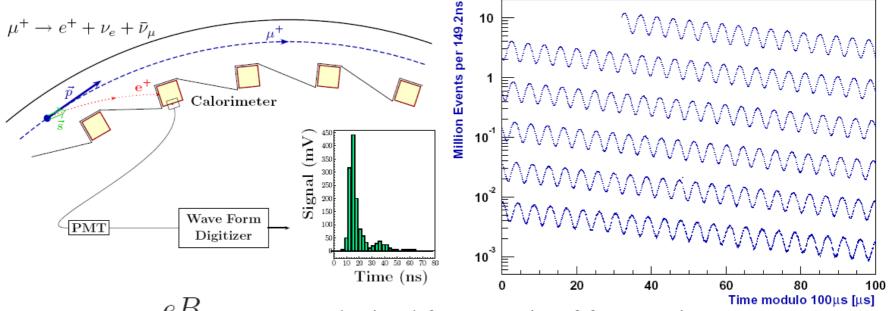


M.Davier ISR pi pi/g-2

CERN 22/09/2009

The E-821 Direct a_{μ} Measurement at BNL

Storage ring technique pionneered at CERN (Farley-Picasso...)



$$\omega_a = a_\mu \, \frac{eB}{m_\mu}$$

 $\omega_{\text{precession}} - \omega_{\text{rotation}}$

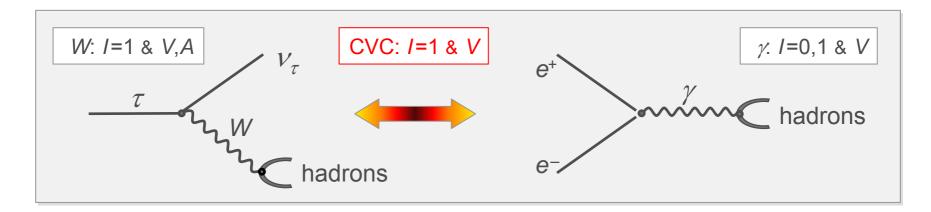
 a_{μ} obtained from a ratio of frequencies result updated with new value for μ_{μ}/μ_{p} (+0.9 10⁻¹⁰) (see next review in RPP2009 (Hoecker-Marciano)

$$a_{\mu}^{exp} = (11\ 659\ 208.9 \pm 5.4 \pm 3.3)\ 10^{-10} (\pm 6.3) \ (0.54\ ppm)$$

M.Davier ISR pi pi/g-2

CERN 22/09/2009

The Role of τ Data through CVC – SU(2)



Hadronic physics factorizes (spectral Functions)

$$\sigma^{(l=1)} \left[e^+ e^- \to \pi^+ \pi^- \right] = \frac{4\pi\alpha^2}{s} \upsilon \left[\tau^- \to \pi^- \pi^0 \upsilon_\tau \right]$$
$$\upsilon \left[\tau^- \to \pi^- \pi^0 \upsilon_\tau \right] \propto \frac{\mathsf{BR} \left[\tau^- \to \pi^- \pi^0 \upsilon_\tau \right]}{\mathsf{BR} \left[\tau^- \to e^- \overline{\upsilon_e} \upsilon_\tau \right]} \frac{1}{N_{\pi\pi^0}} \frac{dN_{\pi\pi^0}}{ds} \frac{m_\tau^2}{\left(1 - s/m_\tau^2 \right)^2 \left(1 + s/m_\tau^2 \right)}$$
$$\mathsf{branching fractions} \quad \mathsf{mass spectrum} \quad \mathsf{kinematic factor (PS)}$$

SU(2) Breaking

Corrections for SU(2) breaking applied to τ data for dominant $\pi^-\pi^+$ contrib.:

- Electroweak radiative corrections:
 - dominant contribution from short distance correction $S_{\rm EW}$
 - subleading corrections (small)
 - long distance radiative correction $G_{\text{EM}}(s)$
- Charged/neutral mass splitting:
 - $m_{\pi^-} \neq m_{\pi^0}$ leads to phase space (cross sec.) and width (FF) corrections
 - $\rho \omega$ mixing (EM $\omega \rightarrow \pi^- \pi^+$ decay) corrected using FF model
 - $m_{\rho-} \neq m_{\rho0}$ *** and $\Gamma_{\rho-} \neq \Gamma_{\rho0}$ ***
- Electromagnetic decays: $\rho \rightarrow \pi \pi \gamma^{***}$, $\rho \rightarrow \pi \gamma$, $\rho \rightarrow \eta \gamma$, $\rho \rightarrow l^+l^-$
- Quark mass difference $m_u \neq m_d$ (negligible)

| Marciano-Sirlin' | 88 |
|------------------|----|
| | |
| | |

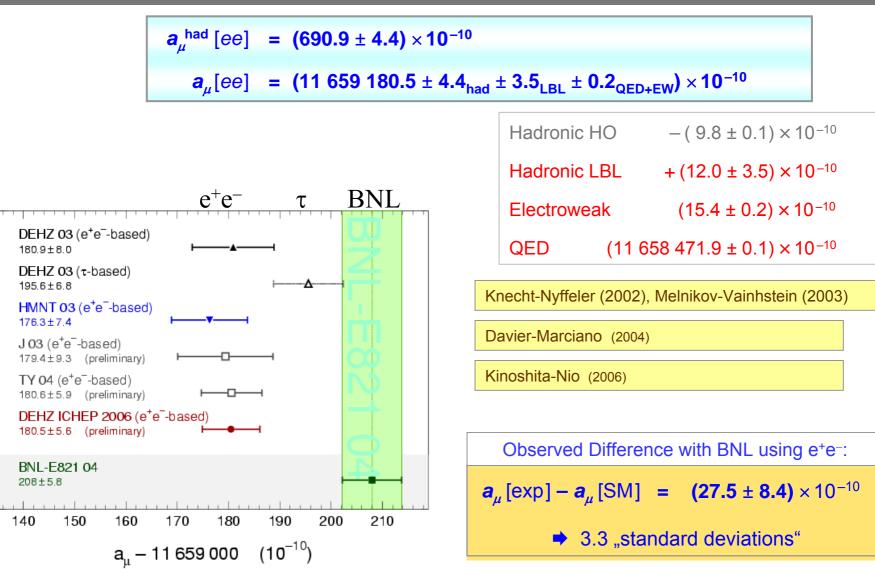
Braaten-Li' 90

Cirigliano-Ecker-Neufeld' 02 Lopez Castro et al.' 06

Alemany-Davier-Höcker' 97, Czyż-Kühn' 01

Flores-Baez-Lopez Castro' 08 Davier et al.'09

Situation at ICHEP'06 / 08

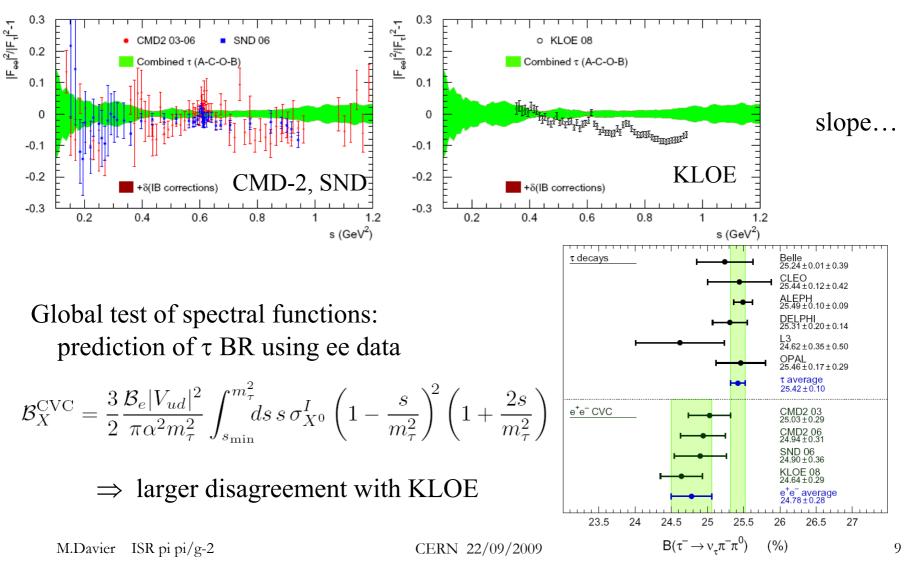


Estimate using τ data consistent with E-821

Revisited Analysis using τ Data: Belle + new IB

arXiv:0906-5443 MD et al.

Relative comparison of τ and ee spectral functions (τ green band)



Goals of the BaBar Analysis

- Measure $\sigma[e^+e^- \rightarrow \pi^+\pi^-(\gamma)]$ with high accuracy for vacuum polarization calculations, using the ISR method $e^+e^- \rightarrow \pi^+\pi^-\gamma(\gamma)$
- $\pi\pi$ channel contributes 73% of a_{μ}^{had}
- Dominant uncertainty also from $\pi\pi$
- Also important to increase precision on $\alpha(M_Z^2)$ (EW tests, ILC)
- Present systematic precision of e⁺e⁻ experiments CMD-2 0.8% SND 1.5% in agreement KLOE (ISR from 1.02 GeV) 2005 1.3% some deviation in shape 2008 0.9% better agreement
- Big advantage of ISR: all mass spectrum covered at once, from threshold to 3 GeV, with same detector and analysis
- Measure simultaneously $\pi^+ \pi^- \gamma(\gamma)$ and $\mu^+ \mu^- \gamma(\gamma)$
- * Compare to spectral functions from previous e^+e^- data and τ decays

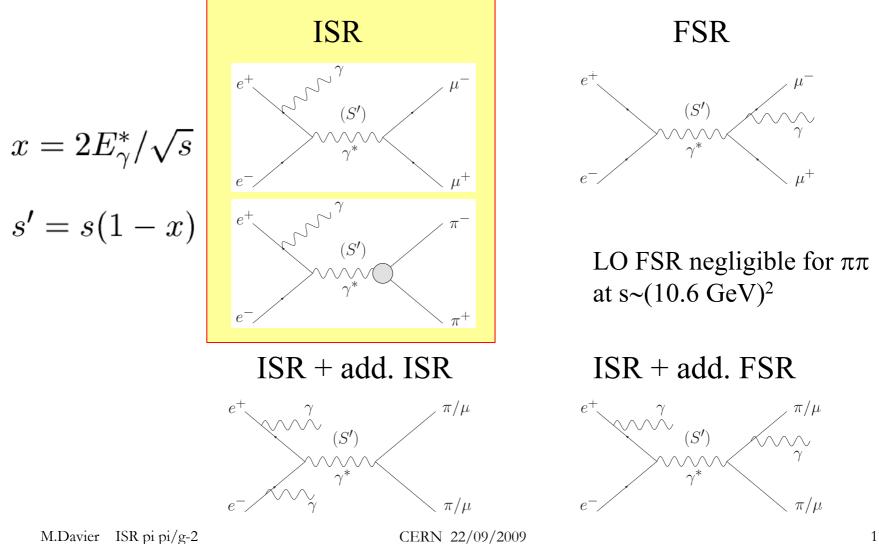
 \Rightarrow aim for a measurement with <1% accuracy (syst. errors at per mil level)

great interest to clarify the situation as magnitude of possible discrepancy with SM is of the order of SUSY contributions with masses of a few 100 GeV

M.Davier ISR pi pi/g-2

The Relevant Processes

 $e^+e^- \rightarrow \mu^+\mu^-\gamma(\gamma)$ and $\pi^+\pi^-\gamma(\gamma)$ measured simultaneously



CERN 22/09/2009

The Measurement

- ISR photon at large angle in EMC
- 1 (for efficiency) or 2 (for physics) tracks of good quality
- identification of the charged particles
- separate $\pi\pi/KK/\mu\mu$ event samples
- kinematic fit (not using ISR photon energy) including 1 additional photon
- obtain all efficiencies (trigger, filter, tracking, ID, fit) from same data
- measure ratio of $\pi\pi\gamma(\gamma)$ to $\mu\mu\gamma(\gamma)$ cross sections to cancel

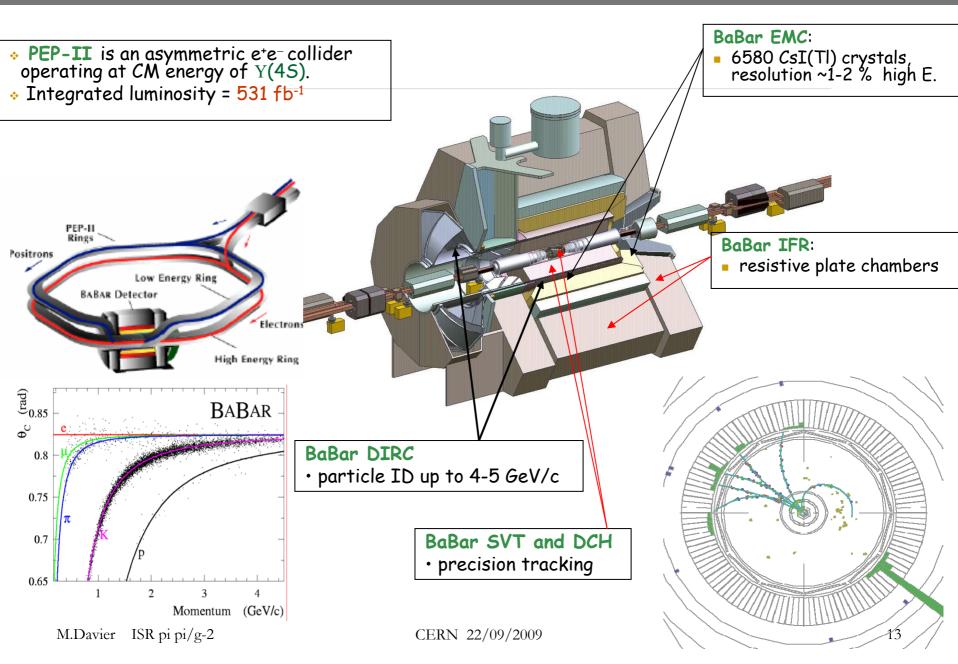
ee luminosity additional ISR vacuum polarization ISR photon efficiency

• otherwise ~2% syst error

- correct for $|FSR|^2$ contribution in $\mu\mu\gamma(\gamma)$ (QED, <1% below 1 GeV)
- additional FSR photons measured

$$R_{\exp}(s') = \frac{\sigma_{[\pi\pi\gamma(\gamma)]}(s')}{\sigma_{[\mu\mu\gamma(\gamma)]}(s')} = \frac{\sigma^{0}_{[\pi\pi(\gamma)]}(s')}{(1+\delta^{\mu\mu}_{\text{FSR}})\sigma^{0}_{[\mu\mu(\gamma)]}(s')} = \frac{R(s')}{(1+\delta^{\mu\mu}_{\text{FSR}})(1+\delta^{\mu\mu}_{add,FSR})}$$

BaBar / PEP II



Analysis Steps

232 fb⁻¹ (Y(4S) on-peak & off peak)

- Geometrical acceptance (using Monte Carlo simulation)
- All efficiencies measured on data (data/MC corrections)
- Triggers (L1 hardware, L3 software), background-filter efficiencies
- Tracking efficiency
- Particle ID matrix (ID and mis-ID efficiencies): $\mu \pi K$
- Kinematic fitting

reduce non 2-body backgrounds

 χ^2 cut efficiency

additional radiation (ISR and FSR)

secondary interactions

- Unfolding of mass spectra
- Consistency checks for $\mu\mu$ (QED test, ISR luminosity) and $\pi\pi$
- Unblinding $R \Rightarrow$ partial preliminary results (Tau08, Sept. 2008)
- Additional studies and checks
- Final results on $\pi\pi$ cross section and calculation of dispersion integral

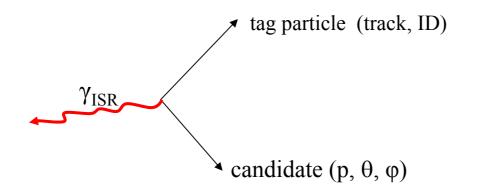
MC Generators

- Acceptance and efficiencies determined initially from simulation, with data/MC corrections applied
- Large simulated samples, typically 10 × data, using AfkQed generator
- AfkQed: lowest-order (LO) QED with additional radiation: ISR with structure function method, γ assumed collinear to the beams and with limited energy FSR using PHOTOS
- Phokhara 4.0: (almost) exact second-order QED matrix element, limited to NLO
- Studies comparing Phokhara and AfkQed at 4-vector level with fast simulation
- QED test with $\mu \mu \gamma (\gamma)$ cross section requires reliable NLO generator
- $\pi \pi (\gamma)$ cross section obtained through $\pi \pi \gamma / \mu \mu \gamma$ ratio, rather insensitive to detailed description of radiation in MC

M.Davier ISR pi pi/g-2

CERN 22/09/2009

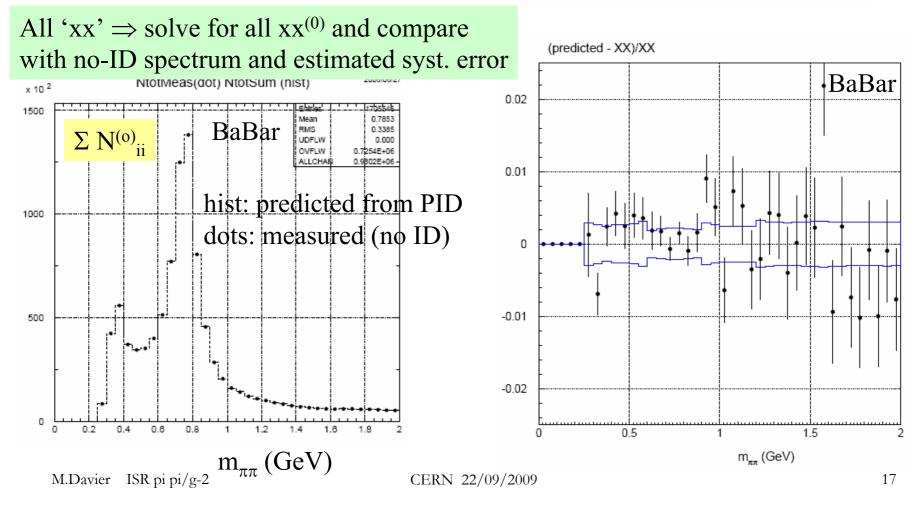
Particle-related Efficiency Measurements



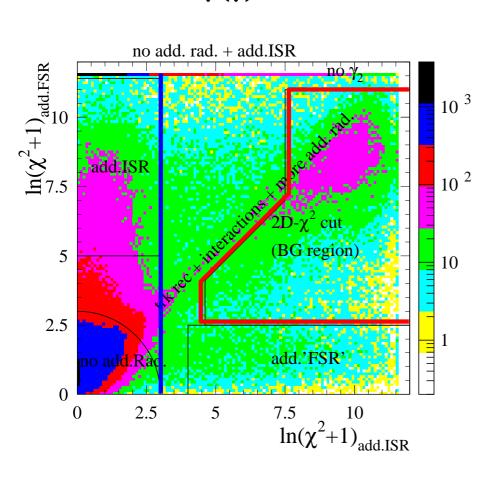
- benefit from pair production for tracking and particle ID
- kinematically constrained events
- efficiency automatically averaged over running periods
- measurement in the same environment as for physics, in fact same events!
- applied to particle ID with $\pi/K/\mu$ samples, tracking, study of secondary interactions...
- assumes that efficiencies of the 2 particles are uncorrelated
- in practice not true ⇒ study of 2-particle overlap in the detector (trigger,tracking, EMC, IFR) required a large effort to reach per mil accuracies

PID separation and Global Test

$$N_{'\pi\pi'} = N_{\mu\mu}^{(0)} \varepsilon_{\mu\mu\to'\pi\pi'} + N_{\pi\pi}^{(0)} \varepsilon_{\pi\pi\to'\pi\pi'} + N_{KK}^{(0)} \varepsilon_{KK\to'\pi\pi'} + N_{ee/'\pi\pi'}^{(0)}$$
$$N_{'\mu\mu'} = N_{\mu\mu}^{(0)} \varepsilon_{\mu\mu\to'\mu\mu'} + N_{\pi\pi}^{(0)} \varepsilon_{\pi\pi\to'\mu\mu'} + N_{KK}^{(0)} \varepsilon_{KK\to'\mu\mu'}$$
$$N_{'KK'} = N_{\mu\mu}^{(0)} \varepsilon_{\mu\mu\to'KK'} + N_{\pi\pi}^{(0)} \varepsilon_{\pi\pi\to'KK'} + N_{KK}^{(0)} \varepsilon_{KK\to'KK'}$$



Kinematic Fitting



 $\pi\pi\gamma(\gamma)$

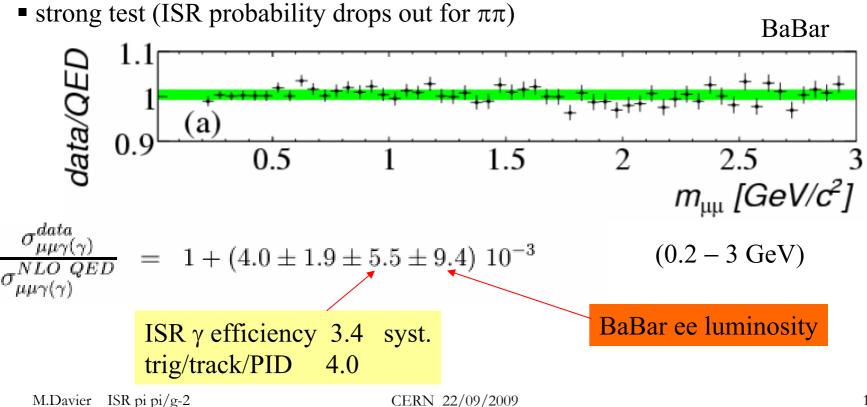
 Two kinematic fits to X X γ_{ISR} γ_{add} (ISR photon defined as highest energy)

Add. ISR fit: γ_{add} assumed along beams Add. 'FSR' if γ_{add} detected

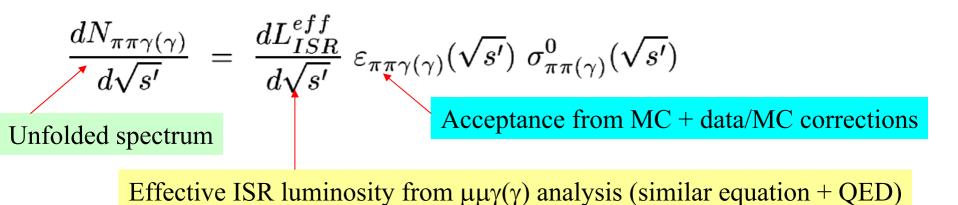
- First analysis to measure cross section with additional photons (NLO)
- Loose χ² cut (outside BG region in plot) for μμ and ππ in central ρ region
- Tight χ² cut (ln(χ²+1)<3) for ππ in ρ tail region
- q \bar{q} and multi-hadronic ISR background from MC samples + normalization from data using signals from $\pi^0 \rightarrow \gamma_{ISR} \gamma$ (q \bar{q}), and ω and ϕ ($\pi\pi\pi^0\gamma$)

QED Test with µµγ sample

- \blacksquare absolute comparison of $\mu\mu$ mass spectra in data and in simulation
- simulation corrected for data/MC efficiencies
- AfkQed corrected for incomplete NLO using Phokhara



Obtaining the $\pi\pi(\gamma)$ cross section



 $\pi\pi$ mass spectrum unfolded (Malaescu arXiv:0907-3791) for detector response

Additional ISR almost cancels in the procedure $(\pi\pi\gamma(\gamma) / \mu\mu\gamma(\gamma) \operatorname{ratio})$ Correction (2.5 ±1.0) 10⁻³ $\Rightarrow \pi\pi$ cross section does not rely on accurate description of NLO in the MC generator

ISR luminosity from μμγγ in 50-MeV energy intervals (small compared to variation of efficiency corrections)

Systematic uncertainties

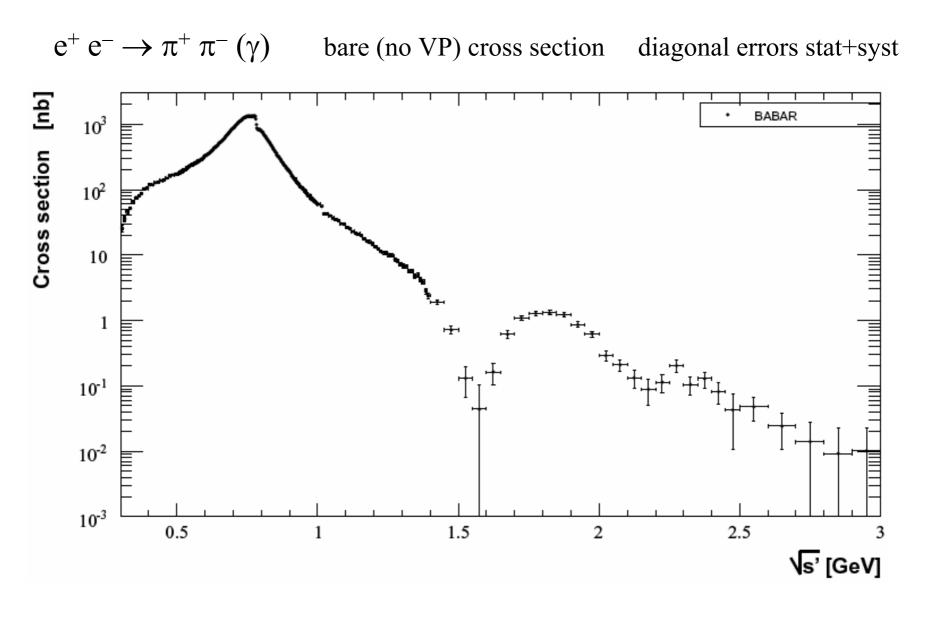
 $\sqrt{s'}$ intervals (GeV)

errors in 10⁻³

| sources | 0.3-0.4 | 0.4-0.5 | 0.5-0.6 | 0.6-0.9 | 0.9-1.2 | 1.2 - 1.4 | 1.4-2.0 | 2.0-3.0 |
|--------------------------|---------|---------|---------|---------|---------|-----------|---------|---------|
| trigger/ filter | 5.3 | 2.7 | 1.9 | 1.0 | 0.5 | 0.4 | 0.3 | 0.3 |
| tracking | 3.8 | 2.1 | 2.1 | 1.1 | 1.7 | 3.1 | 3.1 | 3.1 |
| $\pi\text{-ID}$ | 10.1 | 2.5 | 6.2 | 2.4 | 4.2 | 10.1 | 10.1 | 10.1 |
| background | 3.5 | 4.3 | 5.2 | 1.0 | 3.0 | 7.0 | 12.0 | 50.0 |
| acceptance | 1.6 | 1.6 | 1.0 | 1.0 | 1.6 | 1.6 | 1.6 | 1.6 |
| kinematic fit (χ^2) | 0.9 | 0.9 | 0.3 | 0.3 | 0.9 | 0.9 | 0.9 | 0.9 |
| correl $\mu\mu$ ID loss | 3.0 | 2.0 | 3.0 | 1.3 | 2.0 | 3.0 | 10.0 | 10.0 |
| $\pi\pi/\mu\mu$ cancel. | 2.7 | 1.4 | 1.6 | 1.1 | 1.3 | 2.7 | 5.1 | 5.1 |
| unfolding | 1.0 | 2.7 | 2.7 | 1.0 | 1.3 | 1.0 | 1.0 | 1.0 |
| ISR luminosity | 3.4 | 3.4 | 3.4 | 3.4 | 3.4 | 3.4 | 3.4 | 3.4 |
| sum (cross section) | 13.8 | 8.1 | 10.2 | 5.0 | 6.5 | 13.9 | 19.8 | 52.4 |

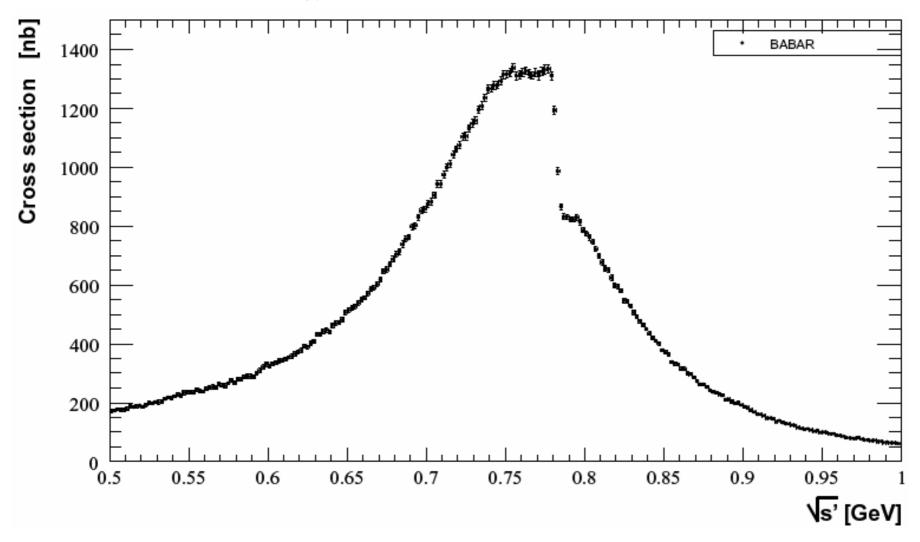
Dominated by particle ID (π -ID, correlated $\mu\mu \rightarrow \pi\pi$, μ -ID in ISR luminosity)

BaBar results (arXiv:0908.3589)

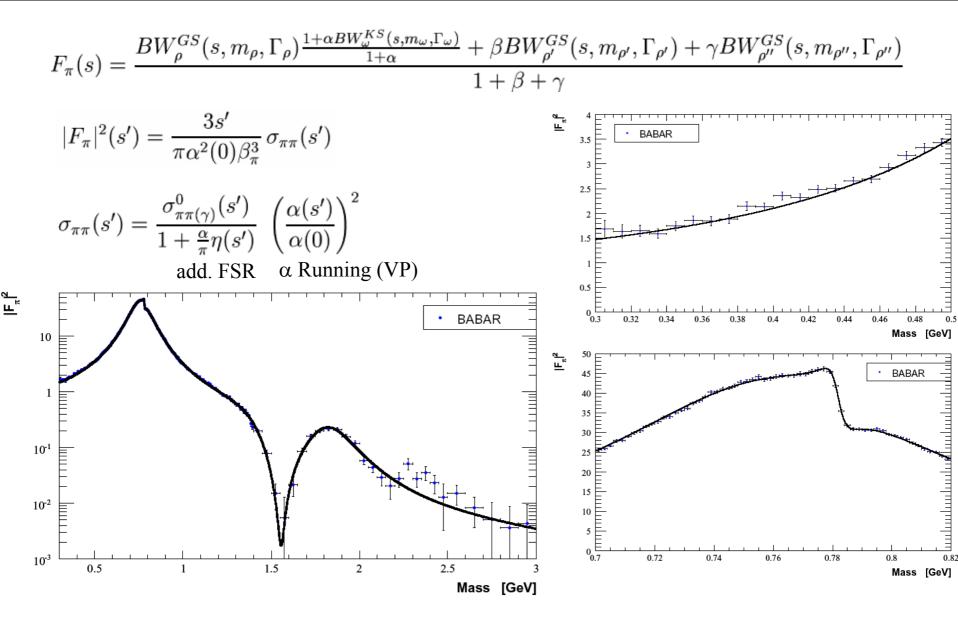


BaBar results in p region

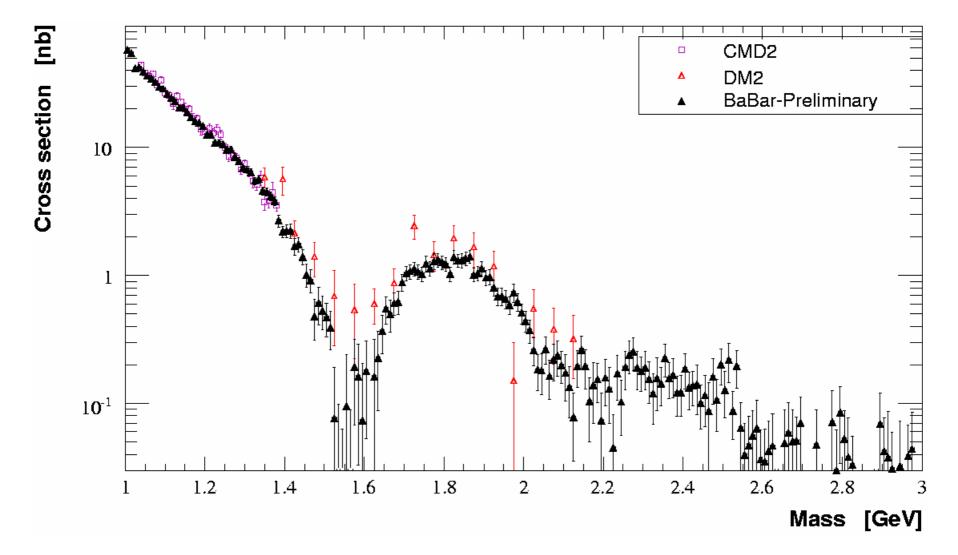
2-MeV energy intervals



VDM fit of the pion form factor

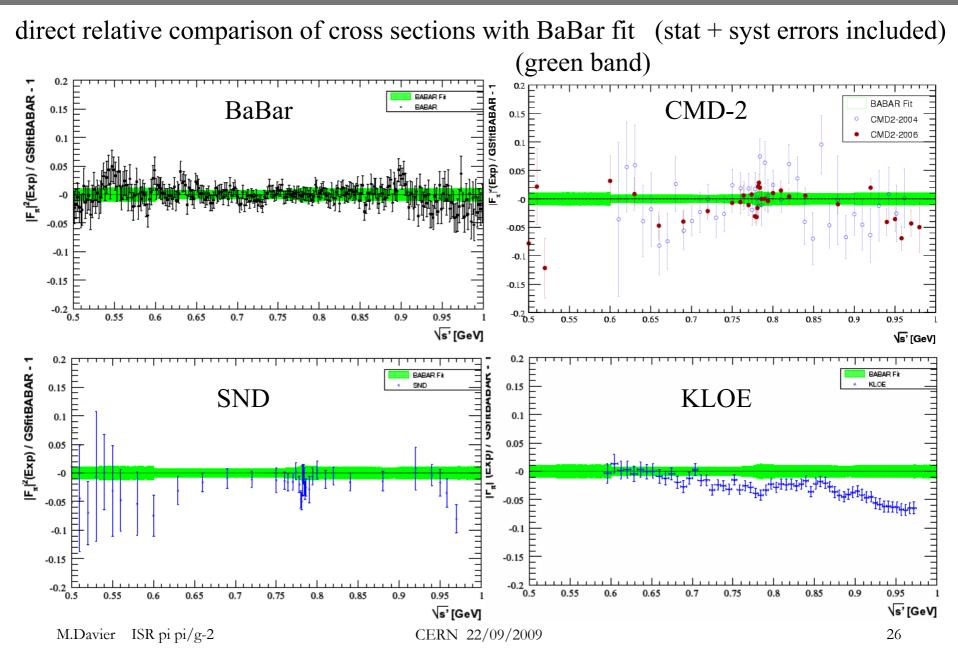


BaBar vs. other experiments at larger mass

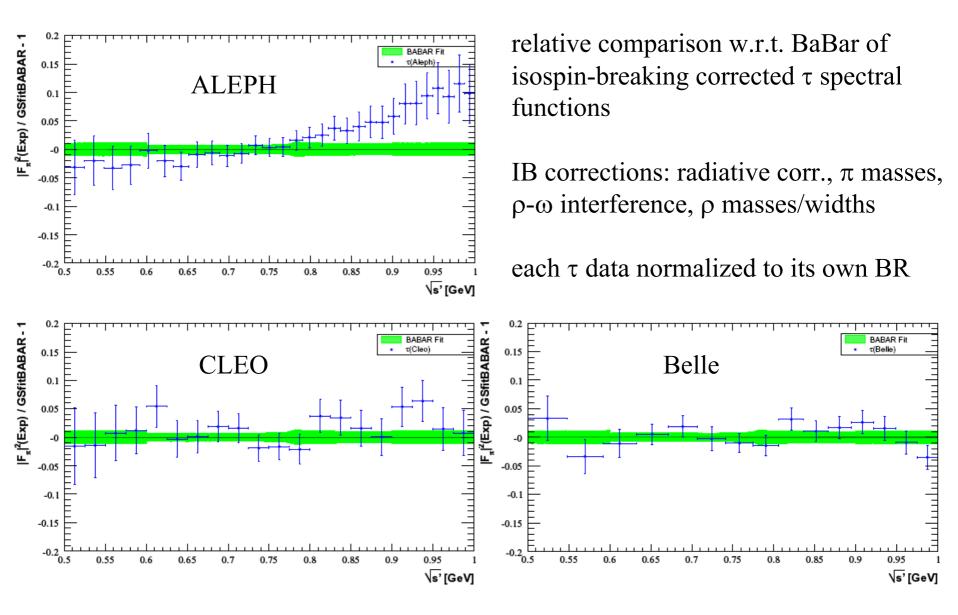


M.Davier ISR pi pi/g-2

BaBar vs.other ee data (0.5-1.0 GeV)



BaBar vs. IB-corrected τ data (0.5-1.0 GeV)



Computing $a_{\mu}^{\pi\pi}$

$$a_{\mu}^{\pi\pi(\gamma),LO} = \frac{1}{4\pi^3} \int_{4m_{\pi}^2}^{\infty} ds \, K(s) \, \sigma_{\pi\pi(\gamma)}^0(s) \; ,$$

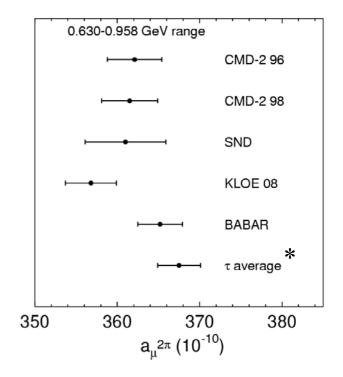
where K(s) is the QED kernel,

$$K(s) = x^{2} \left(1 - \frac{x^{2}}{2}\right) + (1 + x)^{2} \left(1 + \frac{1}{x^{2}}\right) \left[\ln(1 + x) - x + \frac{x^{2}}{2}\right] + x^{2} \frac{1 + x}{1 - x} \ln x ,$$

with
$$x = (1 - \beta_{\mu})/(1 + \beta_{\mu})$$
 and $\beta_{\mu} = (1 - 4m_{\mu}^2/s)^{1/2}$.

| $m_{\pi\pi}$ range (GeV) | $a^{\pi\pi(\gamma),LO}_{\mu}$ BABAR | |
|--------------------------|-------------------------------------|---------------------|
| 0.28 - 0.30 | $0.55 \pm 0.01 \pm 0.01$ | $(\times 10^{-10})$ |
| 0.30 - 0.50 | $57.62 \pm 0.63 \pm 0.55$ | |
| 0.50 - 1.00 | $445.94 \pm 2.10 \pm 2.51$ | , |
| 1.00 - 1.80 | $9.97 \pm 0.10 \pm 0.09$ | |
| 0.28 - 1.80 | $514.09 \pm 2.22 \pm 3.11$ | |

$$\begin{array}{ll} 0.28 - 1.8 \ (GeV) \\ \hline BABAR & 514.1 \pm 3.8 \\ previous \ e^+e^- \ combined & 503.5 \pm 3.5 \ * \\ \tau \ combined & 515.2 \pm 3.5 \ * \end{array}$$



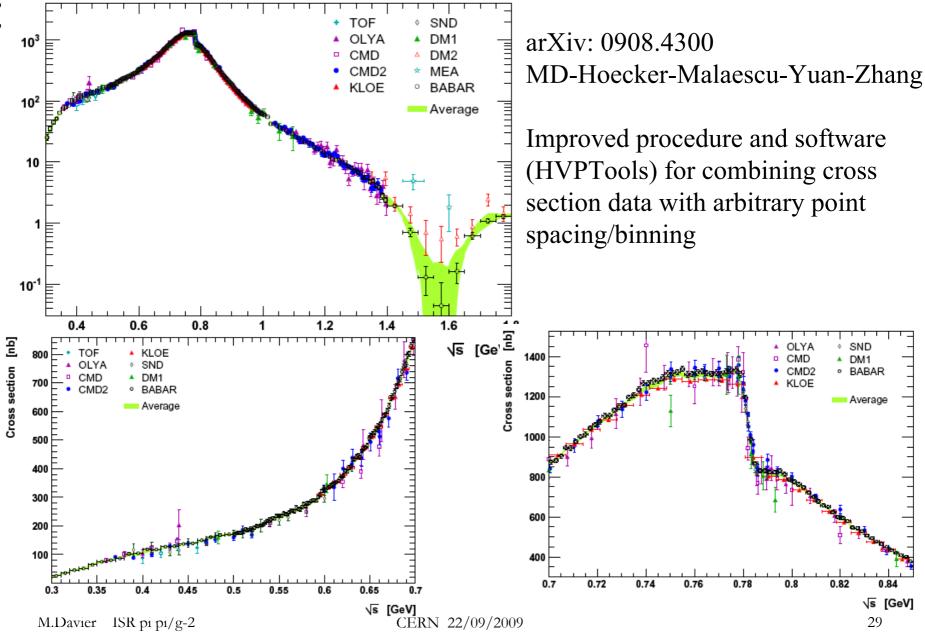
* arXiv:0906-5443 MD et al. 28

M.Davier ISR pi pi/g-2

CERN 22/09/2009

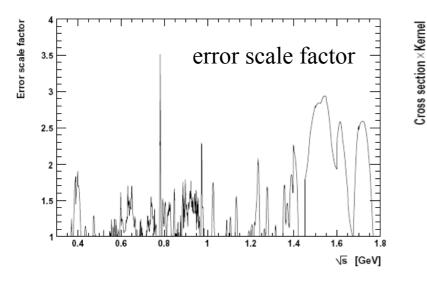
Including BaBar in the e⁺e⁻ Combination

Cross section [nb]



Obtaining the average cross section

- local weighted average performed
- full covariance matrices
- local χ^2 used for error rescaling
- average dominated by BaBar and KLOE, BaBar covering full range



relative weights Relative weight in average 0.8 BABAR LOE SND 0.6 CMD2 (2004) CMD2 (2006) Other exp 0.4 0.2 0.4 0.6 0.8 1.2 1.6 1.4 1.8 0.16 0.14 integrand (dispersion integral) 0.12 è error 0.1 0.08 0.06 0.04 0.5 0.02 0 0.6 0.8 1.2 0.4 1.4 1.6 √s [GeV]

Cross section error ×Kerne

Other hadronic contributions

from MD-Eidelman-Hoecker-Zhang (2006)

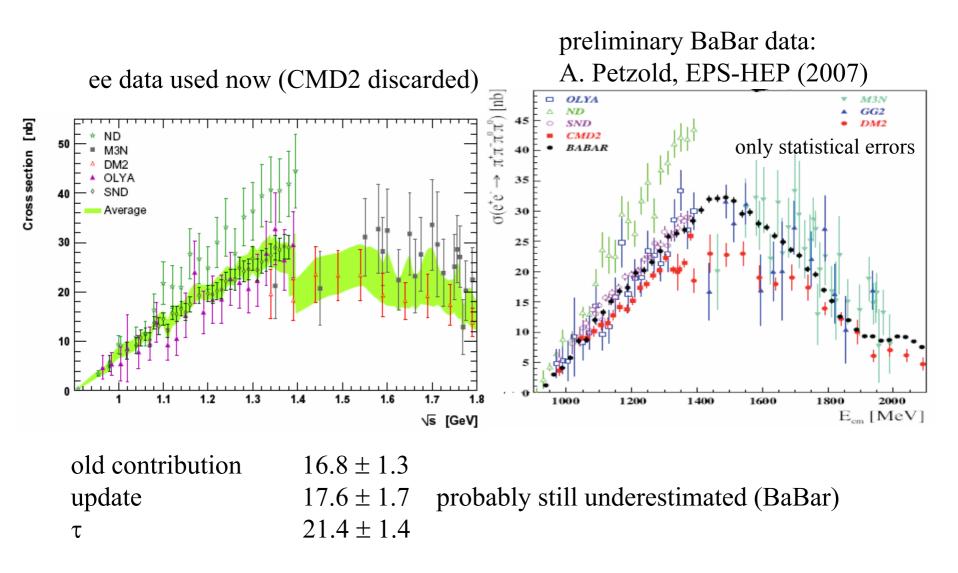
| Modes | Energy [GeV] | e+e- | au |
|-------------------------|-------------------------------|---------------------------------------|-----------------------------------|
| $\pi^+\pi^-2\pi^0$ | 2 <i>m</i> _π – 1.8 | 16.8 ± 1.3 ± 0.2 _{rad} | 21.4 ± 1.3 ± 0.6 _{SU(2)} |
| $2\pi^+2\pi^-$ (+BaBar) | 2 <i>m</i> _π – 1.8 | 13.1 ± 0.4 ± 0.0 _{rad} | 12.3 ± 1.0 ± 0.4 _{SU(2)} |
| <i>w</i> (782) | 0.3 – 0.81 | 38.0 ± 1.0 ± 0.3 _{rad} | - |
| <i>ф</i> (1020) | 1.0 – 1.055 | 35.7 ± 0.8 ± 0.2 _{rad} | - |
| Other excl. (+BaBar) | $2m_{\pi} - 1.8$ | 24.3 ± 1.3 ± 0.2 _{rad} | - |
| <i>JΙψ</i> , ψ(2S) | 3.08 – 3.11 | 7.4 ± 0.4 ± 0.0 _{rad} | - |
| R [QCD] | 1.8 – 3.7 | 33.9 ± 0.5 _{theo} | - |
| R [data] | 3.7 – 5.0 | 7.2 ± 0.3 ± 0.0 _{rad} | - |
| R [QCD] | 5.0 − ∞ | 9.9 ± 0.2 _{theo} | - |

 \Rightarrow another large long-standing discrepancy in the $\pi^+ \pi^- 2\pi^0$ channel !

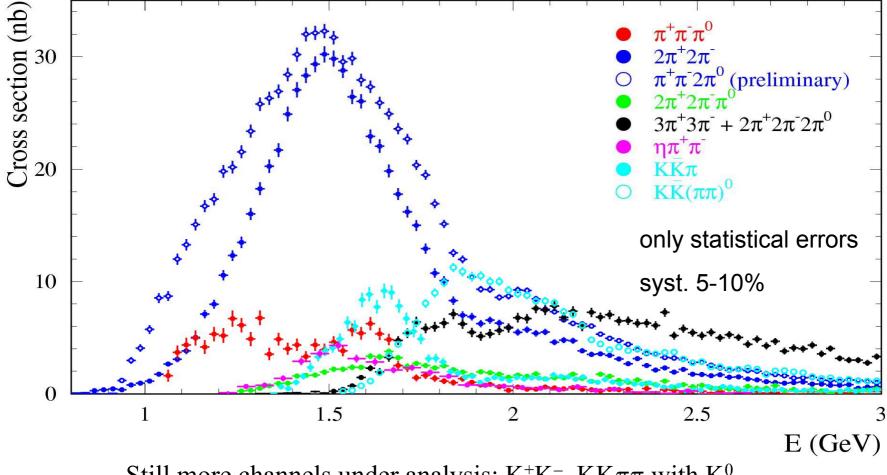
M.Davier ISR pi pi/g-2

CERN 22/09/2009

The Problematic $2\pi 2\pi^0$ Contribution



BaBar Multi-hadronic Results



Where are we?

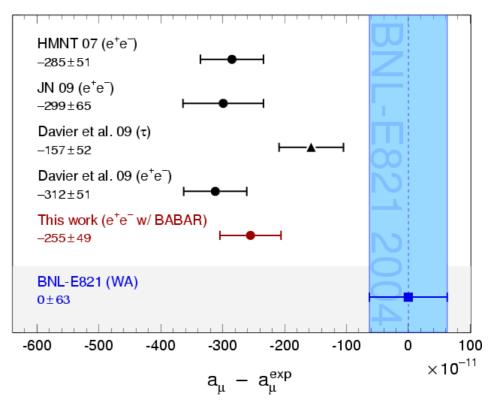
• including BaBar 2π results in the e+e- combination + estimate of hadronic LBL contribution (Prades-de Rafael-Vainhstein, 2009) yields

 $a_{\mu}^{SM}[e+e-] = (11\ 659\ 183.4\ \pm4.1\ \pm2.6\ \pm0.2)\ 10^{-10}$

• E-821 updated result

11 659 208.9 ±6.3

- deviation (ee) 25.5 ± 8.0 (3.2 σ)
- updated τ analysis
 +Belle +revisited IB corrections
- deviation (τ) 15.7 ± 8.2 (1.9 σ)



Discussion

- BaBar 2π data complete and the most accurate, but expected precision improvement on the average not reached because of discrepancy with KLOE
- however, previous τ /ee disagreement strongly reduced

 $2.9\sigma(2006) \rightarrow 2.4\sigma (\tau \text{ update}) \rightarrow 1.5\sigma (\text{including BaBar})$

• a range of values for the deviation from the SM can be obtained, depending on the 2π data used:

| BaBar | 2.4σ |
|---------------|------|
| all ee | 3.2σ |
| all ee –BaBar | 3.7σ |
| all ee -KLOE | 2.9σ |
| τ | 1.9σ |

- all approaches yield a deviation, but SM test limited by systematic effects not accounted for in the experimental analyses (ee) and/or the corrections to τ data
- at the moment some evidence for a deviation $(2-4\sigma)$, but not sufficient to establish a contribution from new physics

Perspectives

- first priority is a clarification of the BaBar/KLOE discrepancy:
 - origin of the 'slope' (was very pronounced with the 2004 KLOE results, reduced now with the 2008 results)
 - normalization difference on ρ peak (most direct effect on a_{μ})
 - Novosibirsk results in-between, closer to BaBar
 - slope also seen in KLOE/ τ comparison; BaBar agrees with τ
- further checks of the KLOE results are possible: as method is based on MC simulation for ISR and additional ISR/ISR probabilities \Rightarrow long-awaited test with $\mu\mu\gamma$ analysis
- contribution from multi-hadronic channels will continue to be updated with more results forthcoming from BaBar, particularly $2\pi 2\pi^0$
- more ee data expected from VEPP-2000 in Novosibirsk
- experimental error of E-821 direct a_{μ} measurement is a limitation, already now
 - \Rightarrow new proposal submitted to Fermilab to improve accuracy by a factor 4
 - \Rightarrow project at JPARC

Conclusions

- BaBar analysis of $\pi\pi$ and $\mu\mu$ ISR processes completed
- Precision goal has been achieved: 0.5% in ρ region (0.6-0.9 GeV)
- \bullet Absolute $\mu\mu$ cross section agrees with NLO QED within 1.1%
- $ee \rightarrow \pi\pi(\gamma)$ cross section very insensitive to MC generator
- full range of interest covered from 0.3 to 3 GeV
- Structures observed in pion form factor at large masses
- Comparison with data from earlier experiments fair agreement with CMD-2 and SND, poor with KLOE agreement with τ data
- Contribution to a_{μ} from BaBar is (514.1 ±2.2±3.1)×10⁻¹⁰ in 0.28-1.8 GeV
- BaBar result has comparable accuracy (0.7%) to combined previous results
- Deviation between BNL measurement and theory prediction reduced using BaBar $\pi\pi$ data

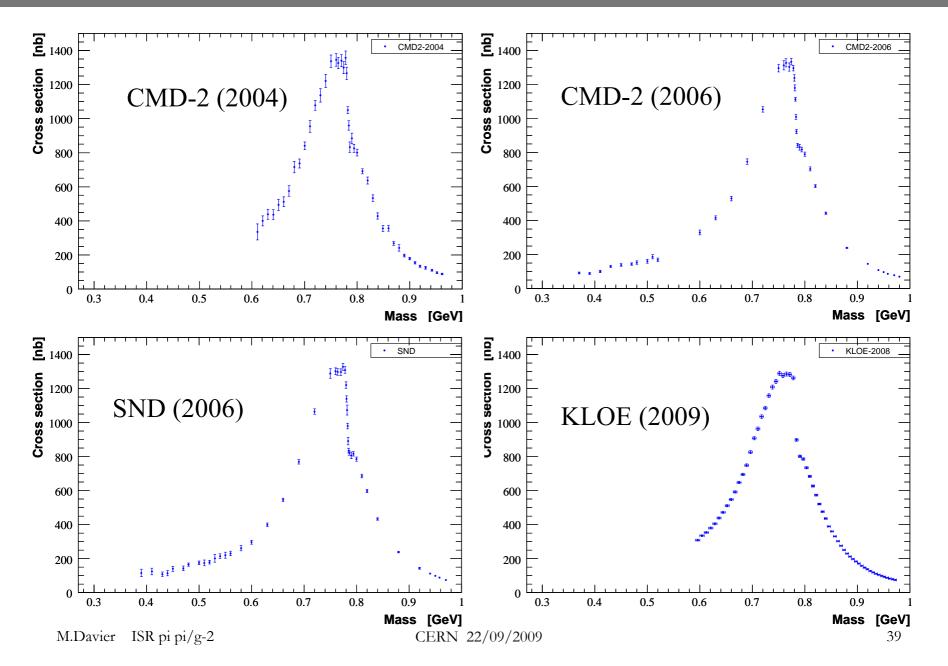
 a_{μ} [exp] – a_{μ} [SM] =(19.8 ± 8.4)×10⁻¹⁰ 25.5 ± 8.0

 2π from BaBar only

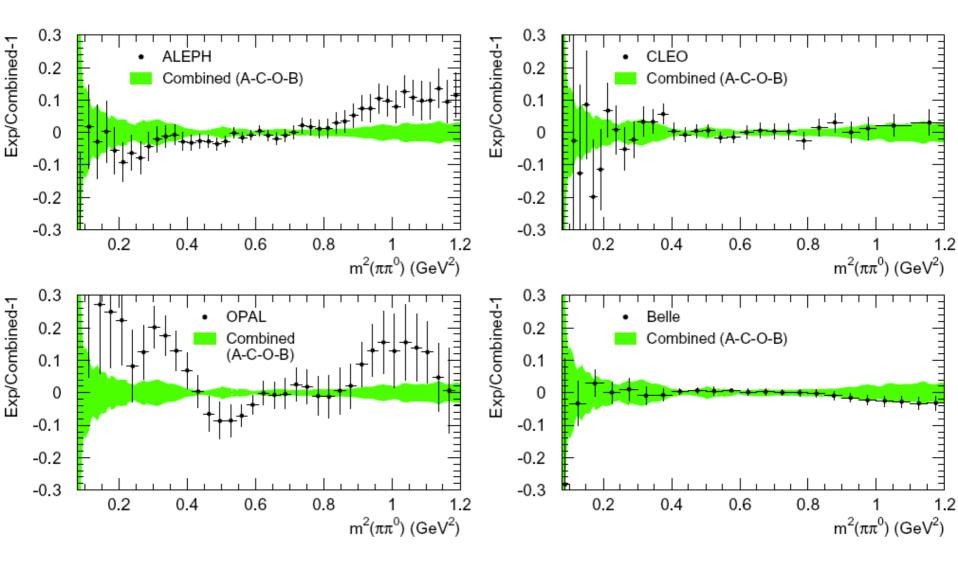
combined ee including BaBar

Backup Slides

Data on $e^+e^- \rightarrow hadrons$



Revisited Analysis using τ Data: including Belle



Revisited Analysis τ Data: new IB corrections

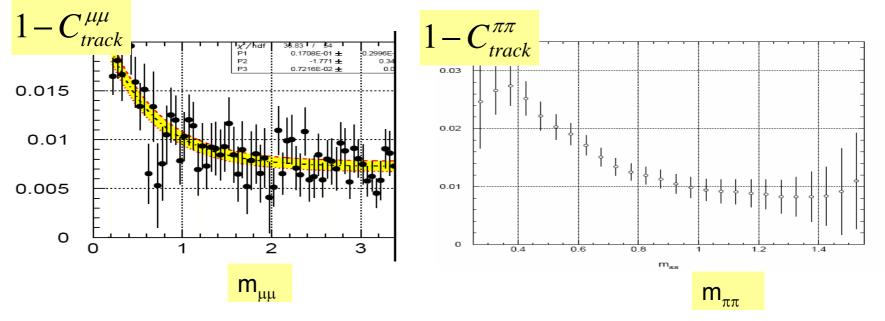
| Source | $\Delta a_{\mu}^{\rm had, LO}[\pi \pi, \tau] \ (10^{-10})$ | |
|---|--|------------------------|
| | GS model | KS model |
| $S_{\rm EW}$ | -12.21 ± 0.15 | |
| $G_{\rm EM}$ | -1.92 ± 0.90 | |
| FSR | $+4.67 \pm 0.47$ | |
| $\rho – \omega$ interference | $+2.80\pm0.19$ | $+2.80\pm0.15$ |
| $m_{\pi^{\pm}} - m_{\pi^{0}}$ effect on σ | -7.88 | |
| $m_{\pi^{\pm}} - m_{\pi^{0}}$ effect on Γ_{ρ} | +4.09 | +4.02 |
| $m_{\rho\pm} - m_{\rho_{\text{bare}}^0}$ | $0.20_{-0.19}^{+0.27}$ | $0.11^{+0.19}_{-0.11}$ |
| $\pi\pi\gamma$, electrom. decays | -5.91 ± 0.59 | -6.39 ± 0.64 |
| Total | -16.07 ± 1.22 | -16.70 ± 1.23 |
| | -16.07 ± 1.85 | |

Data/MC Tracking Correction to $\pi\pi\gamma$, $\mu\mu\gamma$ cross sections

- single track efficiency
- correlated loss probability f₀
- probability to produce more than 2 tracks f₃

$$C_{track}^{\mu\mu} = \left(\frac{\varepsilon_{track}^{data}}{\varepsilon_{track}^{MC}}\right)^2 \frac{(1 - f_0 - f_3)^{data}}{(1 - f_0 - f_3)^{MC}}$$

and similarly for $\pi\pi$



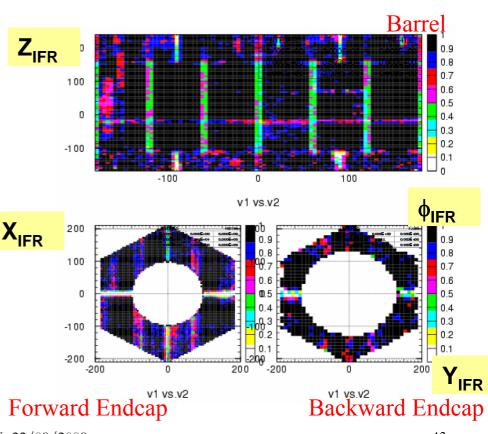
M.Davier ISR pi pi/g-2

Particle Identification

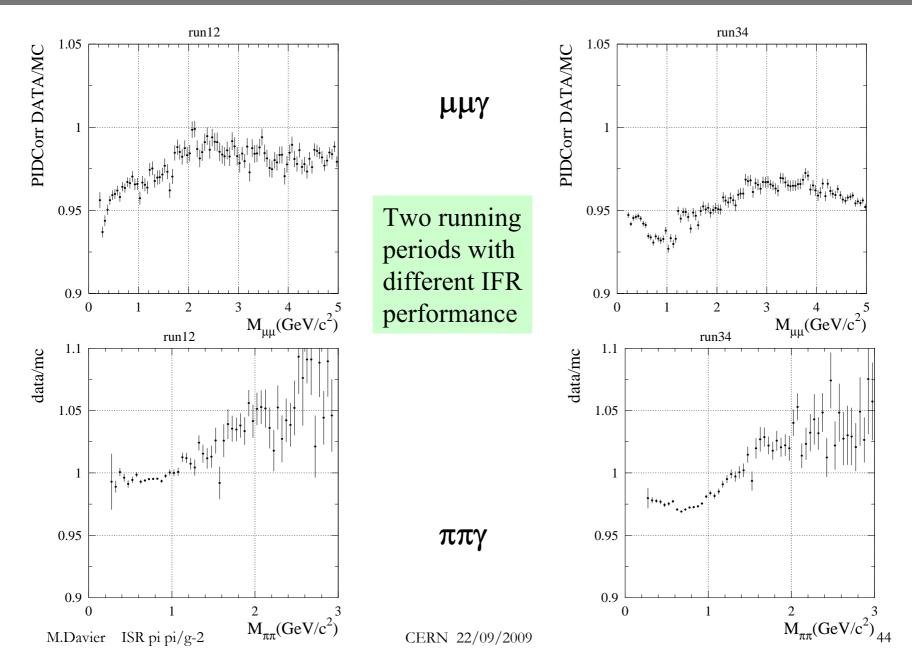
- Particle identification required to separate XXγ final processes
- Define 5 ID classes using cuts and PID selectors (complete and orthogonal set)
- Electrons rejected at track definition level (E_{cal}, dE/dx)
 - All ID efficiencies measured

 $\epsilon_{x \to I}$

• a tighter π ID (π_h) is used for tagging in efficiency measurements and to further reject background in low cross section regions. * isolated muons Mµµ > 2.5 GeV
→ efficiency maps (p,v₁,v₂) impurity (1.1±0.1) 10⁻³
* correlated efficiencies/close tracks
→ maps (dv₁,dv₂)

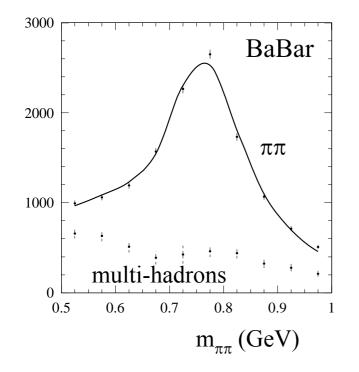


Data/MC PID corrections to $\mu\mu$ and $\pi\pi$ cross sections



Backgrounds

- background larger with loose χ^2 cut used in 0.5-1.0 GeV mass range
- $q \overline{q}$ and multi-hadronic ISR background from MC samples + normalization from data using signals from $\pi^0 \rightarrow \gamma_{ISR} \gamma$ (qq), and ω and ϕ ($\pi \pi \pi^0 \gamma$)
- global test in background-rich region near cut boundary



Fitted BG/predicted = 0.968 ± 0.037

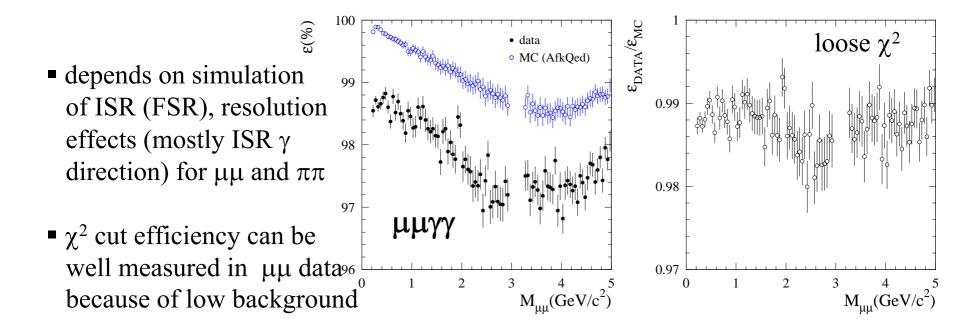
BG fractions in 10⁻² at $m_{\pi\pi}$ values

| process | $0.525~{\rm GeV}$ | $0.775~{ m GeV}$ | $0.975~{\rm GeV}$ |
|-------------------------|-------------------|------------------|-------------------|
| $\mu\mu$ | 3.48 ± 0.36 | 0.37 ± 0.23 | 2.71 ± 0.31 |
| KK | 0.08 ± 0.01 | 0.01 ± 0.01 | 0.08 ± 0.01 |
| $\gamma 2\pi \pi^0$ | 8.04 ± 0.41 | 0.39 ± 0.05 | 0.88 ± 0.19 |
| $q\overline{q}$ | 1.11 ± 0.17 | 0.26 ± 0.03 | 1.81 ± 0.19 |
| $\gamma 2\pi 2\pi^0$ | 1.29 ± 0.16 | 0.06 ± 0.01 | 0.46 ± 0.09 |
| $\gamma 4\pi$ | 0.20 ± 0.04 | 0.09 ± 0.01 | 0.24 ± 0.06 |
| $\gamma p \overline{p}$ | 0.22 ± 0.02 | 0.04 ± 0.01 | 0.52 ± 0.06 |
| $\gamma \eta 2\pi$ | 0.02 ± 0.01 | 0.03 ± 0.01 | 0.09 ± 0.01 |
| $\gamma K_S K_L$ | 0.18 ± 0.03 | 0.01 ± 0.01 | 0.10 ± 0.02 |
| $\gamma 4\pi 2\pi^0$ | < 0.01 | < 0.01 | < 0.01 |
| $\tau \tau$ | 0.17 ± 0.03 | 0.04 ± 0.01 | 0.31 ± 0.05 |
| γee | 0.63 ± 0.63 | 0.03 ± 0.03 | 0.27 ± 0.27 |
| total | 15.38 ± 0.87 | 1.31 ± 0.24 | 7.37 ± 0.51 |

M.Davier ISR pi pi/g-2

CERN 22/09/2009

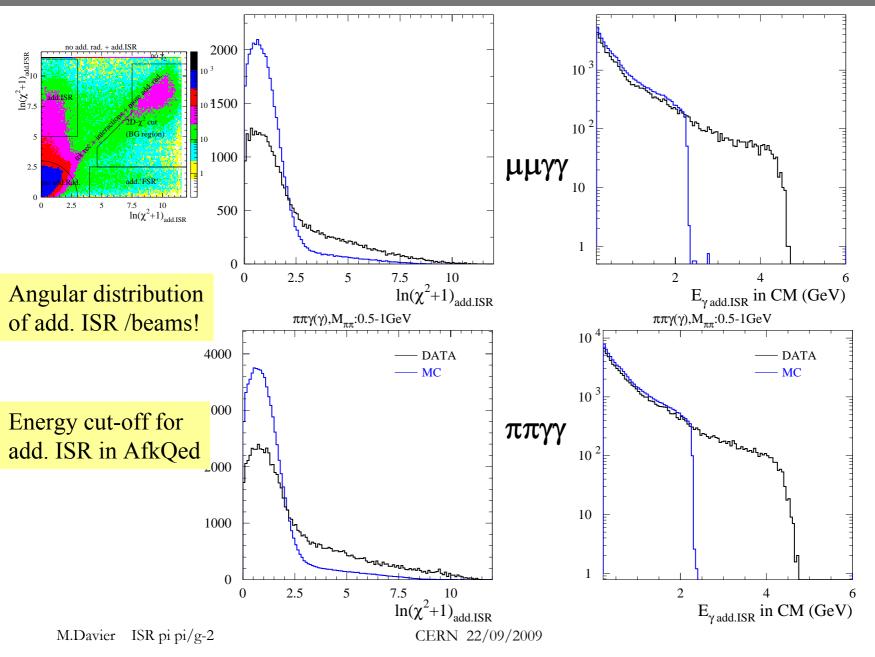
χ^2 cut Efficiency Correction



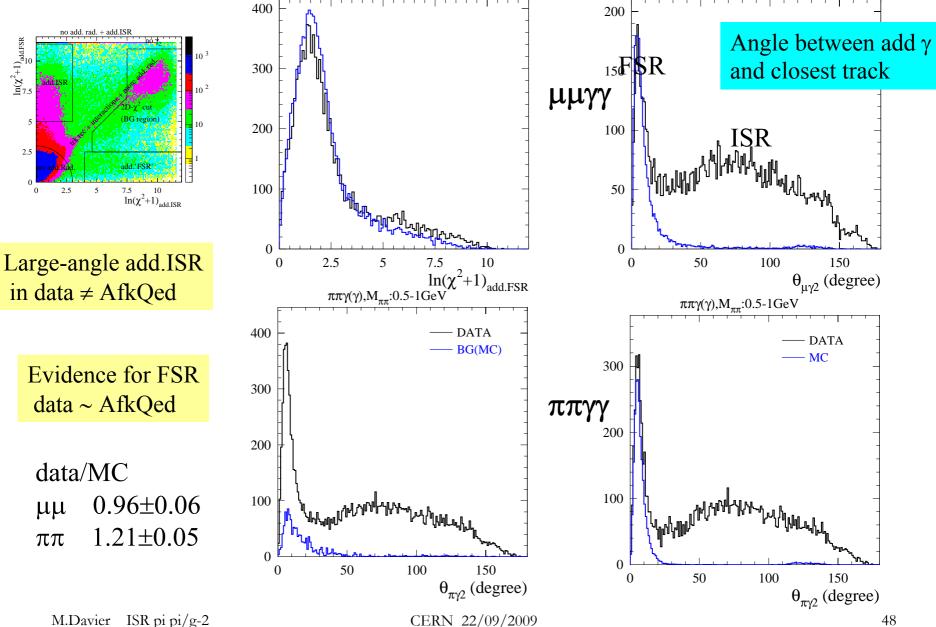
- main correction from lack of angular distribution for additional ISR in AfkQed
- common correction: 1% for loose χ^2 , 7% for tight χ^2
- additional loss for ππ because of interactions studied with sample of interacting events much better study now, 2 independent methods

secondary interactions data/MC 1.51 ± 0.03 syst error $0.3 - 0.9 \times 10^{-3}$

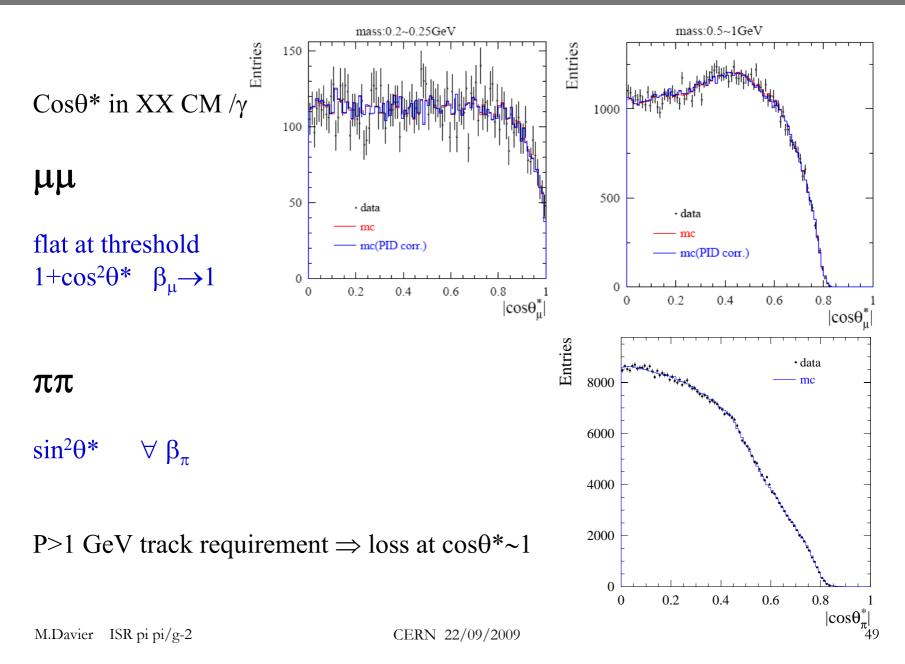
Additional ISR



Additional FSR

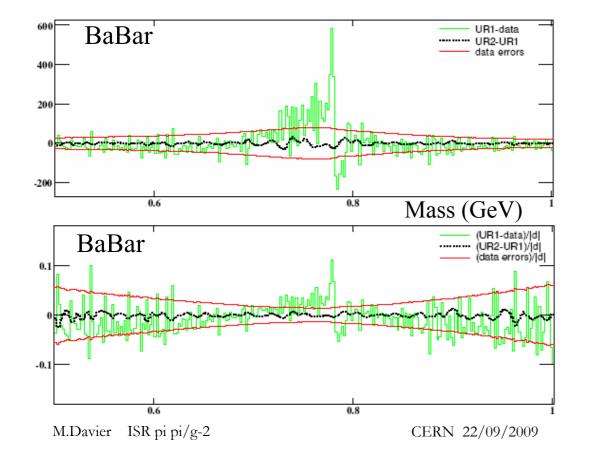


Checking Known Distributions



Unfolding $\pi\pi$ Mass Spectrum

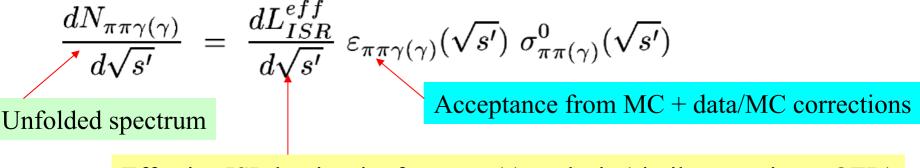
- measured mass spectrum distorted by resolution effects and FSR ($m_{\pi\pi}$ vs. $\sqrt{s'}$)
- iterative unfolding method (B. Malaescu arXiv:0907-3791)
- mass-transfer matrix from simulation with corrections from data
- 2 MeV bins in 0.5-1.0 GeV mass range, 10 MeV bins outside
- most salient effect in ρ - ω interference region (little effect on $a_{\mu}^{\pi\pi}$)



Absolute difference unfolded(1) – raw data unfolded(2) – unfolded(1) Statistical errors (band)

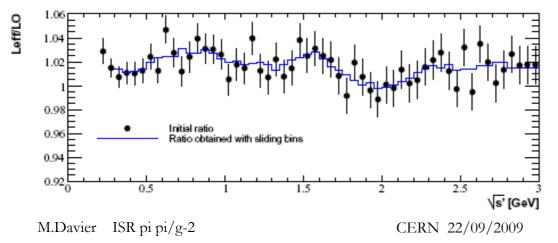
Relative difference

Obtaining the $\pi\pi(\gamma)$ cross section



Effective ISR luminosity from $\mu\mu\gamma(\gamma)$ analysis (similar equation + QED)

Additional ISR almost cancels in the procedure $(\pi\pi\gamma(\gamma) / \mu\mu\gamma(\gamma) \operatorname{ratio})$ Correction (2.5 ±1.0) 10⁻³ $\Rightarrow \pi\pi$ cross section does not rely on accurate description of NLO in the MC generator



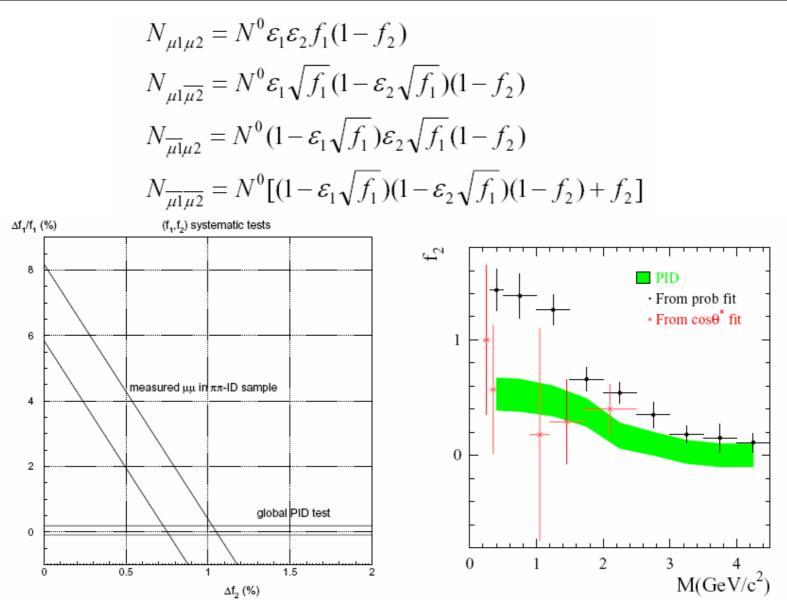
ratio μμ ISR lumi / LO formula should behave smoothly (HVP effects on resonances cancel)

Use measured lumi in 50-MeV bins averaged in sliding 250-MeV bins for smoothing

Changes since preliminary results at Tau08

- preliminary results Sept. 2008: only 0.5-3 GeV (excess/expect. near threshold)
- problem explored (Oct. 2008- Feb. 2009): trigger/BGFilter, ee background
- $\mu\mu \rightarrow \pi\pi'$ re-investigated \Rightarrow direct measurement achieved using ID probabilities before: model for correlated loss, no precise direct check \Rightarrow significant changes $\mu\mu$ efficiency for ISR lumi $\uparrow +0.9\%$ $\mu\mu$ contamination in $\pi\pi'$ sample \downarrow $\Rightarrow \pi\pi$ cross section $\downarrow -1.8\%$ 0.525 GeV -1.0% 0.775 GeV -1.4% 0.975 GeV
- other changes: MC unfolding mass matrix corrected for data/MC differences
 (small) ISR lumi now used in 50-MeV sliding bins, instead of global fit
 cancellation of add ISR in ππ/μμ ratio studied/corrected
- extensive review

f₂ Story



M.Davier ISR pi pi/g-2

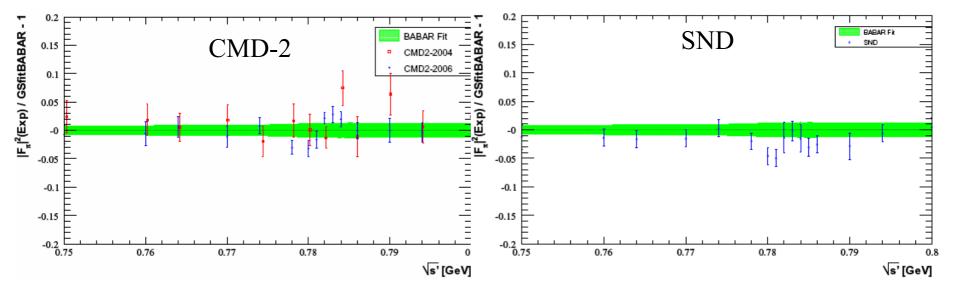
CERN 22/09/2009

BaBar vs.other ee data (ρ – ω interference region)

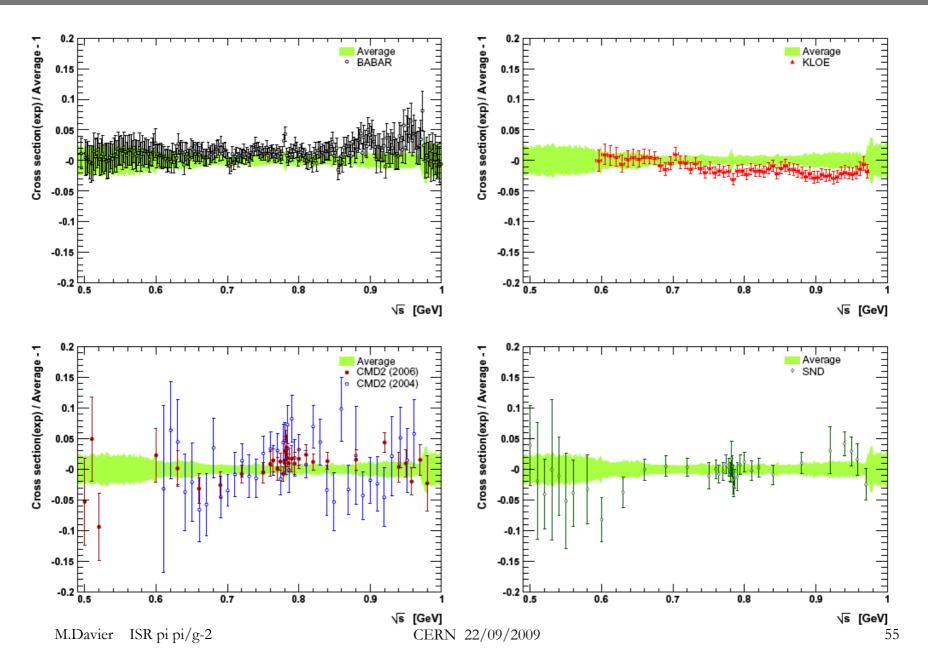
- \bullet mass calibration of BaBar checked with ISR-produced J/ $\psi \rightarrow \mu \mu$
- expect $-(0.16 \pm 0.16)$ MeV at ρ peak
- $\hfill \omega$ mass determined through VDM mass fit

 $m_{\omega}^{\text{fit}} - m_{\omega}^{\text{PDG}}$ = -(0.12 ± 0.29) MeV

- Novosibirsk data precisely calibrated using resonant depolarization
- comparison BaBar/CMD-2/SND in ρ-ω interference region shows no evidence for a mass shift



Consistency of Experiments with Average



Backup Slides

| Energy range (GeV) | Experiment | $a_{\mu}^{\text{had,LO}}[\pi\pi] \ (10^{-10})$ |
|---------------------|-------------------------|---|
| $2m_{\pi\pm} - 0.3$ | Combined e^+e^- (fit) | 0.55 ± 0.01 |
| 0.30 - 0.63 | Combined e^+e^- | $132.6 \pm 0.8 \pm 1.0 \ (1.3_{\rm tot})$ |
| 0.63 - 0.958 | CMD2 03 | $361.8 \pm 2.4 \pm 2.1 \ (3.2_{tot})$ |
| | CMD2 06 | $360.2 \pm 1.8 \pm 2.8 \ (3.3_{\rm tot})$ |
| | SND 06 | $360.7 \pm 1.4 \pm 4.7 \ (4.9_{tot})$ |
| | KLOE 08 | $356.8 \pm 0.4 \pm 3.1 \ (3.1_{\rm tot})$ |
| | BABAR 09 | $365.2 \pm 1.9 \pm 1.9 (2.7_{tot})$ |
| | Combined e^+e^- | $360.8 \pm 0.9 \pm 1.8 \ (2.0_{\rm tot})$ |
| 0.958 - 1.8 | Combined e^+e^- | $14.4 \pm 0.1 \pm 0.1 \ (0.2_{\rm tot})$ |
| Total | Combined e^+e^- | $508.4 \pm 1.3 \pm 2.6 \ (2.9_{tot})$ |
| Total | Combined τ [1] | $515.2 \pm 2.0_{\text{exp}} \pm 2.2_{\mathcal{B}} \pm 1.6_{\text{IB}} (3.4_{\text{tot}})$ |

Backup Slides

