

Introduction

❖ g-2/EDM experiment

➢ Measure the following values with high precision

○ Anomalous magnetic moment of positive muon (g-2) : < 0.1 ppm

○ Electric dipole moment of positive muon (EDM) : 1e-21 e.cm

➢ Requirements for Magnet

➢ Storage region

○ Field strength : 3 T

○ Homogeneity: <±0.1 ppm

○ Size :

Radius: 33.3 cm ± 1.5 cm

Height: ±5 cm

➢ Injection region

○ $B_r \times B_z > 0$

➢ Weak Focus field

○ $B_r = -n \frac{B_{0z}}{R}$ $n: 5 \times 10^{-5} - 2 \times 10^{-4}$

➢ How to shim magnetic field ?

➢ Iron pieces (shims) put on the inner surface of magnet bore

• Shimming scheme

• Measure field distribution in target region

• Calculate shim arrangement to cancel error field

• Put iron shims in pockets of shim trays, and insert trays.

➢ Iron has large magnetization

➔ ~1000 ppm error could be shimmed in general

Ex) MuSEUM Magnet

➢ Present homogeneity : 0.45 ppm_{pp}

shimmed with 0.06 cc iron piece

Fig. 1 : Superconducting solenoid magnet for g-2/EDM

Fig. 2: MRI magnet for MuSEUM

Fig. 3: Photos of shim trays of MuSEUM MRI magnet

Fig. 4: Homogeneity in x-z plane interpolated from measured data on surface of 50 cm DSV.

❖ MuSEUM experiment

➢ Measure the following values with high precision

○ ground state hyperfine structure interval of Muonium : < 3 ppb

○ ratio of muon and proton magnetic moment : < 10 ppb

➢ Requirements for Magnet

➢ Storage region

○ Field strength : 1.7 T

○ Homogeneity: <±0.1 ppm

○ Size :

Spheroidal volume

Length : 30 cm

Radius: 10 cm

➢ Homogeneity :

very important

➢ Simulation study

➢ Attainable homogeneity with different size iron shims

Minimum unit size of iron shim	Attainable homogeneity
0.06 cc	0.39 ppm _{pp}
0.02 cc	0.27 ppm _{pp}
0.012 cc	0.27 ppm _{pp}
0.0006 cc	0.27 ppm _{pp}

➢ due to discrete size of pieces

✓ Limitation of magnet performance

• to get maximum homogeneity, size of iron shim has to be smaller than 0.02 cc

• In principle, much smaller size of iron piece is required to reach ultimate homogeneity, but...

• Difficult to handle and fix on shim trays; ➔ if it's too small, misalignment might be occurred frequently

• Optimum size depends on magnet and magnetic condition; ➔ difficult to expect optimum size beforehand

❖ Ferrofluid material

Liquid having magnetism

✓ easy to get arbitrary volume

✓ much smaller magnetization than Fe

One possible candidate for fine shimming

★ R&D of shimming system with ferrofluid materials

❑ Feasibility study on fine shimming with ferrofluid

❑ Develop and test prototype shimming system

❑ Develop Field mapping system

➢ will report

➢ basic study of ferrofluid

➢ development status of field mapping CW-NMR probe

Basic study on ferrofluid

➢ Measurement setup

Glass Bottle

Polystyrene stand

NMR probe

z moving stage

Magnet

x-y moving stage

Fig. 5: Photos of measurement setup

❖ Suitable material for fine shimming

➢ Moderate magnetic susceptibility compared with iron

➢ Easy controllability of magnetization, that is, volume

➢ Schematic view of setup

Bottle

NMR probe

Field strength : 1.7 T

Polystyrene stand

Table for sample

Table for probe

Rail

x-y stage

Fig. 6: Schematic side view of measurement setup

➢ Scan in x-y plane to search the position where the effect of sample is maximized.

➢ Probe is fixed, and sample is moved in z direction by moving stage

➢ Measure magnetic field with and without samples

➢ Calculate magnetic moment from measured distribution

➢ How to calculate magnetic moment

*Assume point Magnetic moment

Magnetic flux density created by magnetic moment

$$B = -\frac{\mu_0}{4\pi} \nabla \frac{m \cdot r}{r^3} \quad (1)$$
$$B = -10^{-7} \times \nabla \frac{m \cdot r}{r^3} \quad (2) \quad m = (0, 0, m_z)$$
$$B = -10^{-7} \times \frac{m_z}{r^3} (-3xz, -3yz, r^2 - 3z^2) \quad (3)$$
$$B_z = 2 \times 10^{-7} \times \frac{m_z}{z^3} \quad (4) \quad x = y = 0, r = z$$

Fitting function

$$B_z = \frac{P_0}{(z-P_1)^3} + P_2 \quad (5)$$
$$P_0 = 2 \times 10^{-7} \times m_z \quad (6)$$

B_z : Magnetic field

m_z : Magnetic moment

z : Position

P_1 : Error of position

P_2 : Error of magnetic field

※ m_z of Fe: 1.711 Am²

➢ Measurement results

(1) One empty bottle : 5 times

- Check the measurement error

(2) 5 empty bottles : 1 time each

- Check individual differences between bottles

(3) 5 bottles with Ferrofluid of 1 cc

- Check the consistency of ferrofluid volumes

(4) Ferrofluid 1,2,3 cc

- Check the controllability of ferrofluid volume

Fig. 7: Empty bottles and bottles filled with ferrofluid

(1) One empty bottle : 5 times

B_z (mT)

Symbol : Average of 5 meas.

Error bar : Standard dev. of 5 meas.

➢ m_z : $-7.649e-5 \pm 2.314e-6$ (Am²)

➢ P_1 : $-1.309e-2 \pm 3.162e-4$ (m)

➢ P_2 : $-3.264e-9 \pm 7.715e-10$ (T)

Fig. 8: Magnetic field shift due to empty bottle; z represents distance from bottle center.

(2) 5 empty bottles

Bottles	M_z (Am ²)	P_1 (m)	P_2 (T)
#1	-7.598e-5	-1.186e-2	-2.721e-9
#2	-7.549e-5	-1.213e-2	-3.715e-9
#3	-9.369e-5	-1.419e-2	3.467e-9
#4	-6.811e-5	-1.061e-2	-8.768e-9
#5	-9.067e-5	-1.385e-2	8.129e-9
Avg.	-8.079e-5	-1.253e-2	-7.217e-10
St. dev.	1.091e-5	1.483e-3	5.587e-9

• Bottle variation : ~ 13 % of average

• Sufficiently smaller than ferrofluid ➔ can be neglected

✓ Next step : increase number of data to decrease statistical uncertainty

(3) 5 bottles with Ferrofluid of 1 cc

Bottles	M_z (Am ²)	P_1 (m)	P_2 (T)
#1	3.593e-2	-1.136e-2	-2.358e-8
#2	4.039e-2	-2.249e-2	-2.882e-8
#3	4.164e-2	-2.371e-2	-3.666e-8
#4	4.096e-2	-2.211e-2	-3.528e-8
#5	4.100e-2	-2.180e-2	-3.979e-8
Avg.	3.998e-2 (4.100e-2)	-2.029e-2 (-2.253e-2)	-3.283e-8 (-3.514e-8)
St. dev.	2.311e-3 (5.131e-4)	5.044e-3 (8.350e-4)	6.533e-9 (4.616e-9)

• m_z of 1cc ferrofluid : ~1/40 of iron of 1 cc

• Almost agree with specification

• #1 : large difference from others

• #1 : filled by syringe, #2-#5 : filled by spoon

• Density might be different

✓ Next step : check reproducibility considering density control

(4) Ferrofluid 1, 2, 3 cc

m_z [Am²]

$y = 0.0411x + 0.0086$

$R^2 = 0.9996$

Fig. 9: Measured magnetic moment of different volume of ferrofluid

• m_z : almost linear relative to volume

• Magnetization can be controlled by volume

• y-intercept should be zero

• Caused by different density?

R&D of field mapping CW-NMR probe

❖ Need precision field mapping system for fine shimming

➢ NMR magnetometer is only solution for precise measurement

➢ Need quick measurement to neglect time variation of B.

➢ Developing high precision multi channels CW-NMR field mapping system for MuSEUM experiment

• CW-NMR with frequency modulation

• Sweep RF frequency to detect NMR signal

• Need to place electronics board including RF detection circuit close to RF coil for high SNR

• Field mapping probe for MuSEUM

• Spheroidal volume : 30 cm in length, 10 cm in radius

• NMR probes are aligned on half of ellipse arc and they are rotated around the long axis so that the field map could be quickly obtained.

➢ Need a smaller board for multi channel system

➢ Develop smaller probe including the wave detector and pre-amplifier.

Fig. 10: Example layout of multi channels field mapping system for MuSEUM experiment with 24 probes. 12 electronics boards are implemented on this side, and others are implemented on the backside.

Fig. 11: Board for single probe which is commercially available by Japanese company.

Fig. 12: Production prototype board for evaluating the performance of re-designed circuit and magnetization.

➢ Trial board test

➢ Resistors and capacitors were replaced with non-magnetic tips commercially available.

➢ There are no same models of SM tips for several transistors

➢ Test different types of SM alternatives considering magnetization

1ss86 -> 1ss154; 2SK19 -> 2SK208-R; 2sc1907 -> DSC2G03;

Ex) 2sc1907 : two candidates were tested

2sc1907 : Original signal

DSC2G03

MMBTH10-7

Fig. 13: NMR signals with different transistors.

➢ Both candidates show almost the performance as original tip.

➢ MMBTH10-7 has larger magnetization than DSC2G03 ➔ Choose DSC2G03

➢ Production prototype board

➢ SM chips are selected based on trial board

➢ Use 4 layers printed circuit board

➢ Preliminary results

➢ Clear resonance peak by vector network analyzer

➢ Obtain NMR peak signal at 1.7 T

➢ Magnetization of the circuit is about 21 % of commercial one. (-17.1 ppb ➔ -3.76 ppb)

Fig. 14: Transmission response.

Fig. 15: NMR signal using new board.

Summary

✓ Studying shimming system with ferrofluid materials

❖ Basic study of ferrofluid

➢ measure magnetic moment of glass bottles and bottles filled with ferrofluid

➢ m_z was sufficiently smaller than ferrofluid so that it could be neglected in fine shimming

➢ m_z of ferrofluid DS-50 was about 1/40 of iron, that is consistent with specification.

➢ m_z of bottle filled with ferrofluid could be changed at will by controlling the volume of ferrofluid.

❖ Development of high precision multi channel field mapping system

➢ made production prototype of electronics board

➢ TH type components were replaced with SM type components with smaller magnetization

➢ Could obtain NMR peak signal at 1.7 T

✓ Next step

➢ Increase number of data to decrease statistical uncertainty

➢ Check reproducibility considering density control

➢ Check time variation of magnetization

➢ Test different ferrofluid samples to determine optimum one for fine shimming

➢ Design and Build support system for fine shimming with ferrofluid

➢ Test production prototype board and measure its magnetization in detail

• Study the performance when several channels are connected in parallel

➢ Make and test multi channel system

Try shimming operation with MRI magnet for MuSEUM

❖ Acknowledgment : The authors would like to thank Dr. T. Nakajima of Echo-denshi for his help. This work was supported by JSPS KAKENHI Grant Number 18H01239.