



EFNUDAT

European Facilities for Nuclear Data Measurements



"HAS

Final EFNUDAT scientific workshop

PGAA analysis of enriched samples

Tamás Belgya

Institute of Isotopes Hungarian Academy of Sciences, H-1525, POB 77, Budapest,
Hungary

*E-mail: Belgya@IKI.KFKI.HU, <http://www.iki.kfki.hu/nuclear/>

CERN, Geneva, 30 Aug. -02 Sept.
2010

Content

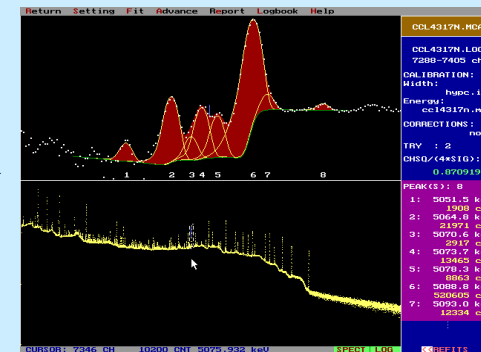
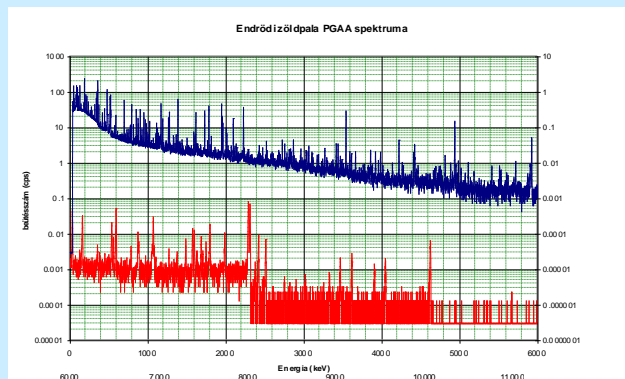
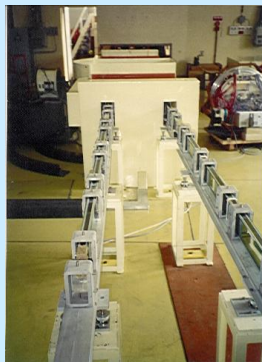
- Motivations:
 - Users required characterization of targets
 - Capture cross sections can be measured for certain isotopes
- The Prompt Gamma Activation Analysis
- New method for isotopic analysis
- Examples
- Conclusion

The Prompt Gamma Activation Analysis

(Features)

- Non-destructive nuclear
- Multi-elemental, multi-isotopic
- Independent of chemical environment
- Minimal sample preparation
- Average composition of the irradiated volume
- Exact for homogeneous samples
- Good for major, minor components and some traces, unique for H, B
- Great variety in elemental sensitivities, detection limits

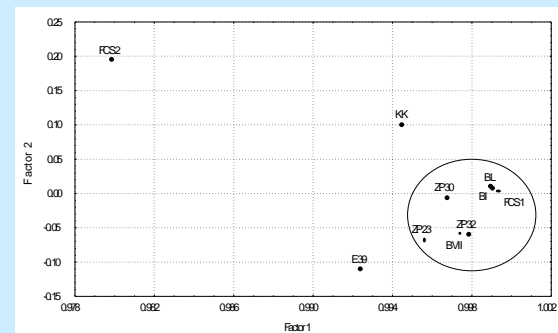
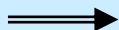
PGAA analysis of natural samples



Spectr C:\HY\PC\IS\PECT RA\ARC\HEO\ZOLDP ALA\FV4103C.MCA
Live Tim 3290.48

Z	EI	M	m	unc%	m(bka)	unc%	mh eθ	n(ox)	m(ox)	unc%	% atom	% el/el	% el/ox	% ox/ox	unc%
1	H	1.0094	0.0229	1.2	0.0018	3.0	0.0272	0.5	0.699	1.2	0.027	0.904	0.484	4.328	1.2
5	B	10.811	6.7E-05	1.1	1E-08	0.0	6.7E-05	1.5	0.0022	1.2	3E-04	8E-04	4E-04	0.001	1.2
11	Na	22.9898	0.3095	2.5	0.0	0.0	0.3095	0.5	0.5099	2.5	3.36	4.859	2.604	3.51	2.5
12	Mg	24.305	0.9332	3.6	0.0	0.0	0.9332	1.1	1.9077	3.6	8.48	11.6	6.216	10.31	3.6
13	Al	26.9815	1.2162	1.6	0.00273	5.0	1.2889	1.5	2.28416	1.6	12.19	15.03	9.951	15.21	1.6
14	Si	28.0855	3.0938	1.5	0.0	0.0	3.0938	2.6	6.1136	1.5	32.45	38.41	20.58	44.03	1.5
16	S	32.066	0.0361	5.8	0.0	0.0	0.0361	3.0	0.0891	5.8	0.403	0.418	0.224	0.559	5.8
17	Cl	35.4527	0.0115	7.0	1.8E-05	20.0	0.0049	0.0	0.0049	7.0	0.02	0.018	0.01	0.01	7.0
19	K	39.0983	0.0432	12.4	0.0	0.0	0.0432	0.5	0.0821	12.4	0.706	0.691	0.322	0.388	12.4
20	Ca	40.078	0.7577	2.0	0.0	0.0	0.7577	1.1	1.0973	2.0	11.35	9.414	5.944	7.958	2.0
21	Sc	44.9559	0.0063	14.5	0.0	0.0	0.0063	1.5	0.0097	14.5	0.011	0.008	0.004	0.006	14.5
22	Ti	47.867	0.1515	1.0	0.0	0.0	0.1515	2.0	2.2877	1.0	2.711	1.883	1.009	1.683	1.0
23	V	50.9418	0.0071	6.8	0.0	0.0	0.0071	2.5	0.0041	6.8	0.09	0.059	0.031	0.056	6.8
24	Cr	51.9961	0.0084	7.9	0.0	0.0	0.0084	1.5	0.01438	7.9	0.191	0.122	0.066	0.096	7.9
25	Mn	54.938	0.0509	2.4	0.0	0.0	0.0509	1.0	0.0948	2.4	0.31	0.188	0.101	0.13	2.4
26	Fe	55.845	1.322	1.2	0.0044	5.0	1.3206	1.5	1.8835	1.2	27.57	16.42	8.786	12.58	1.2
27	Co	58.9332	0.00531	4.0	0.0	0.0	0.00531	1.0	0.0076	4.0	0.117	0.066	0.035	0.045	4.0
62	Sm	150.36	5.4E-05	2.1	0.0	0.0	5.4E-05	1.5	6.3E-05	2.1	0.003	7E-04	4E-04	4E-04	2.1
64	Gd	157.25	7.6E-05	2.0	0.0	0.0	7.6E-05	1.5	8.7E-05	2.0	0.004	9E-04	5E-04	6E-04	2.0
66	Dy	162.5	0.0014	18.3	0.0	0.0	0.0014	1.5	0.0017	18.3	0.009	0.002	1E-03	0.001	18.3

8.04523 15.0151 0.806 100 100 53.58 100
- O calculated 6.99885 46.42 %
mass: wo O 8.04523



DETERMINATION OF CHEMICAL COMPOSITION

$$A_{\gamma} = m \cdot S \cdot t; \quad S = \frac{N_A}{M} \cdot \underbrace{\theta \cdot \sigma_0 \cdot P_{\gamma}}_{\sigma_{\gamma}} \cdot \phi \cdot \varepsilon(E_{\gamma}) \cdot f(E_{\gamma})$$

Fit
from spectrum

From PGAA library

m : Mass of the element

S : Sensitivity

A_{γ} : Peak area

N_A : Avogadro-number

M : Molar weight

θ : Isotopic abundance

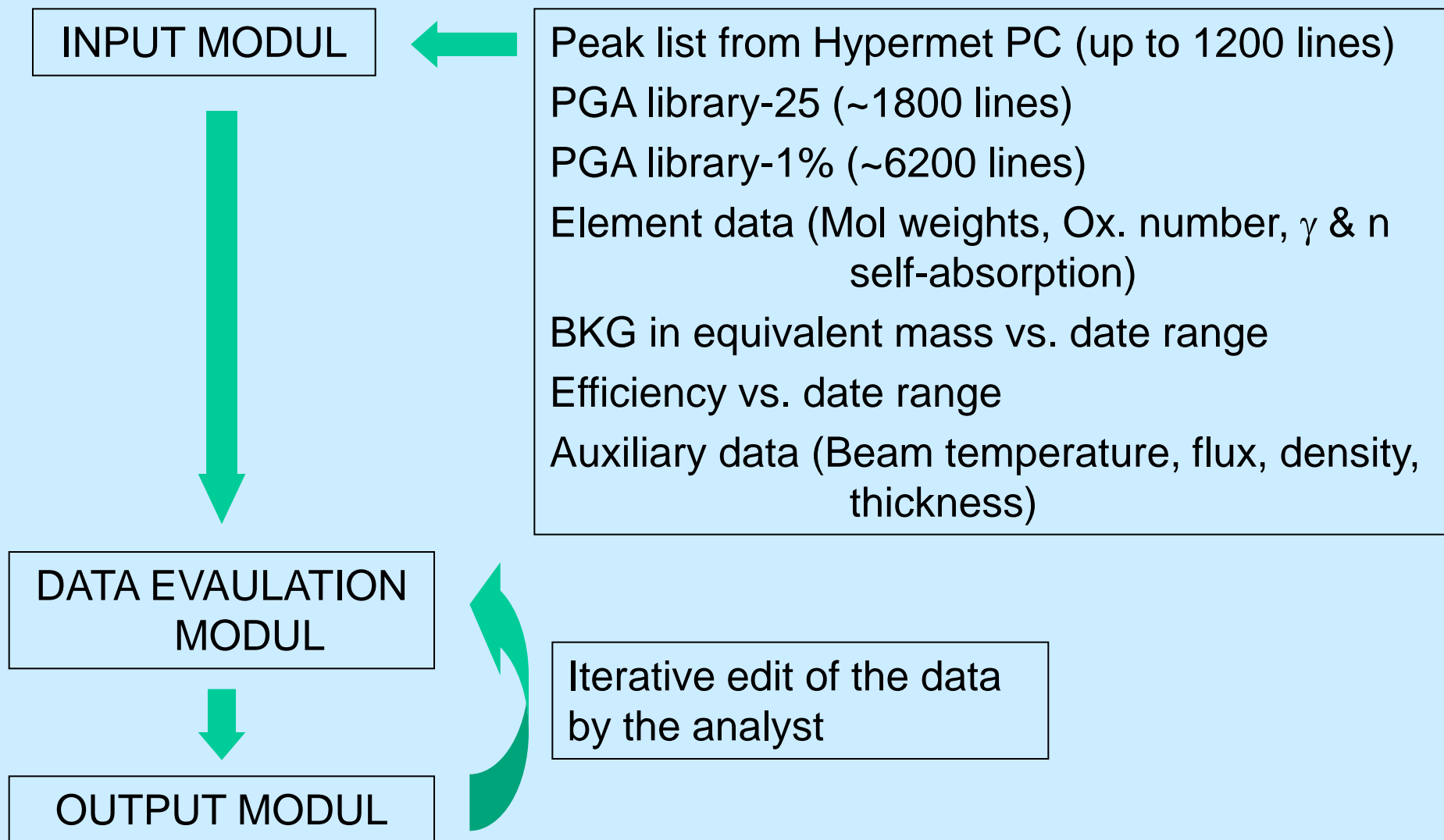
σ_0 : Neutron capture cross-section

P_{γ} : Gamma-yield

ϕ_0 : Neutron flux

$\varepsilon(E_{\gamma})$: Detector efficiency

PGA analysis program in EXCEL



PGAA result

(Bio ash)

Spectrum: N22HAM1.MCA

Peak list: N22HAM1.pkl

Uncertainty calculation: **statistical**

Live time: 39126.63 s

Neutron Flux: 1.50E+8 ±2 %, temp 35 K,

BKG: 13 vac08jan

Conc. format: ppm / %

Z	EI	M	m meas	unc %	m Bkg	unc %	m net	ox. st.	m ox	unc %	c% atom	unc %	c% el/el	unc %	c% el/ox	unc %	c% ox/ox	unc %
1	H	1.008	6.82E-4	0.6	1.15E-5	2.0	6.70E-4	1	5.99E-3	0.6	4.02	1.9	0.187	1.5	0.093	0.9	0.83	1.8
6	C	12.01	0.080	3.8		0.0	0.08	4	0.29	3.8	40	2.5	22	3.2	11.1	3.4	41	2.4
9	F	19	4.89E-2	5.	2.06E-4	20.	4.87E-2	-1	4.87E-2	5.	16	4.	14	4.	6.8	5.	6.8	5.
12	Mg	24.31	1.08E-2	5.		0.0	1.08E-2	2	1.79E-2	5.	2.7	5.	3.0	5.	1.5	5.	2.5	5.
13	Al	26.98	1.06E-2	1.6	1.73E-3	3.0	8.84E-3	3	1.67E-2	2.0	1.98	2.7	2.47	2.4	1.23	2.1	2.32	2.6
14	Si	28.09	0.064	2.1		0.0	0.06	4	0.14	2.1	13.7	2.5	17.8	2.2	8.8	2.1	18.9	2.4
15	p	30.97	7.23E-3	5.		0.0	7.23E-3	5	1.66E-2	5.	1.4	6.	2.0	6.	1.0	5.	2.3	6.
17	Cl	35.45	7.99E-4	39.		0.0	7.99E-4	-1	7.99E-4	39.	0.1	39.	0.2	39.	0.11	39.	0.11	39.
19	K	39.1	3.78E-2	2.4		0.0	3.78E-2	1	4.56E-2	2.4	5.9	2.9	10.6	2.5	5.3	2.4	6.3	2.8
20	Ca	40.08	0.092	2.4		0.0	0.09	2	0.13	2.4	13.9	2.7	26	2.1	12.8	2.2	18.0	2.6
22	Ti	47.87	8.30E-4	2.4		0.0	8.30E-4	4	1.39E-3	2.4	0.105	3.0	0.23	2.7	0.115	2.5	0.193	2.9
24	Cr	52	1.21E-5	49.		0.0	1.21E-5	3	1.77E-5	49.	10 ppm	49.	30 ppm	49.	20 ppm	49.	20 ppm	49.
25	Mn	54.94	2.35E-3	3.8	3.18E-6	10.	2.35E-3	3	3.37E-3	3.8	0.26	4.	0.65	4.0	0.33	3.8	0.47	4.
27	Co	58.93	1.08E-5	15.		0.0	1.08E-5	2	1.38E-5	15.	11 ppm	15.	30 ppm	15.	15 ppm	15.	19 ppm	15.
28	Ni	58.69	3.35E-5	11.		0.0	3.35E-5	2	4.27E-5	11.	35 ppm	11.	90 ppm	11.	50 ppm	11.	60 ppm	11.
34	Se	78.96	2.59E-4	8.		0.0	2.59E-4	4	3.64E-4	8.	200 ppm	9.	0.07	8.	360 ppm	8.	0.051	8.
38	Sr	87.62	9.19E-4	5.		0.0	9.19E-4	2	1.09E-3	5.	0.063	5.	0.26	5.	0.13	5.	0.15	5.
48	Cd	112.4	1.07E-6	1.9		0.0	1.07E-6	2	1.22E-6	1.9	0.58 ppm	2.6	3.0 ppm	2.3	1.49 ppm	2.0	1.70 ppm	2.6
49	In	114.8	3.63E-6	8.		0.0	3.63E-6	3	4.39E-6	8.	1.9 ppm	8.	10 ppm	8.	5.0 ppm	8.	6.1 ppm	8.
50	Sn	118.7	3.13E-3	6.		0.0	3.13E-3	2	3.55E-3	6.	0.16	6.	0.87	6.	0.43	6.	0.49	6.
60	Nd	144.2	1.13E-5	8.		0.0	1.13E-5	3	1.32E-5	8.	4.7 ppm	9.	31 ppm	8.	16 ppm	8.	18 ppm	9.
62	Sm	150.4	6.74E-7	1.6		0.0	6.74E-7	3	7.82E-7	1.6	0.271ppm	2.4	1.88 ppm	2.1	0.94 ppm	1.8	1.09 ppm	2.4
64	Gd	157.3	9.60E-7	19.		0.0	9.60E-7	3	1.11E-6	19.	0.4 ppm	19.	3 ppm	19.	1.3 ppm	19.	1.5 ppm	19.
		0																
		0																
		0																

0.35818 2.6 0.71964 1.3 100.31 100.36 49.78 100.43

Quantification limit for 50 %

- O calculated 0.36146 50 % O/ total

mass without O 0.35818

self-abs.: no (recalc.: Ctrl+Shift+S)

thickness (mm) : 1

density: 2.7

oxide: yes

Enriched samples

- Questions are the isotopic and chemical compositions
- Target forms (measured in the EFNUDAT project)
 - Self supporting targets \Rightarrow Fe, Ni, Zr (metals)
 - Compounds packed in Al discs \Rightarrow $^{96}\text{ZrO}_2$, $^{176,177,178,179}\text{HfO}_2$
- Evaluation software exists for elemental samples
- Evaluation of enriched samples can also be done with this software
 - Solution is the definition of a new „element” of interest with its predetermined composition
 - First we needed to determine the enrichment

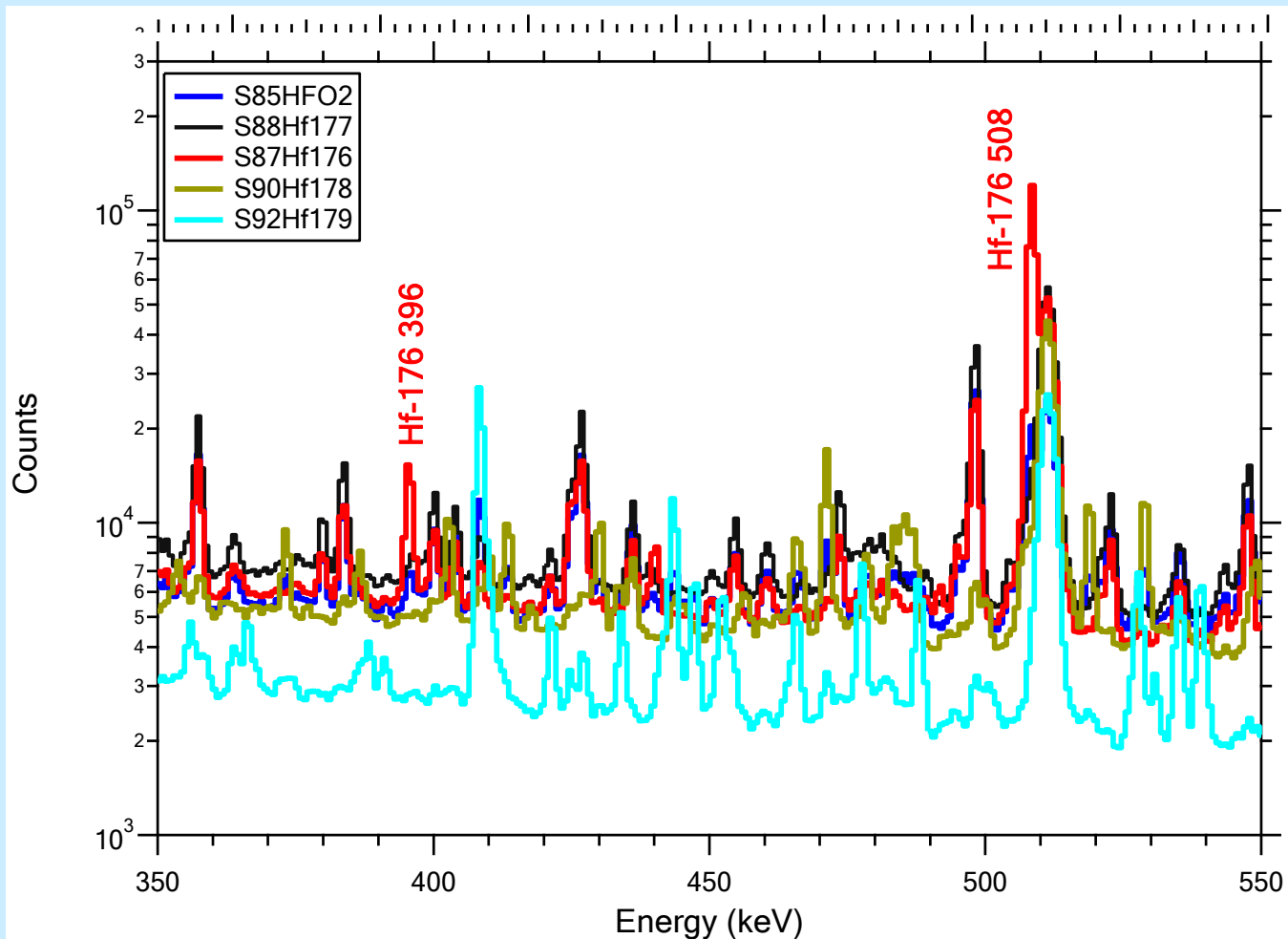
Example

Enrichment of Hf samples

- Samples from Bulgaria were measured to determine enrichment and purity (Hf-176, Hf-177, Hf-178, Hf-179) + Natural Hf
- First step is the gamma-ray identification

Identification of gamma rays

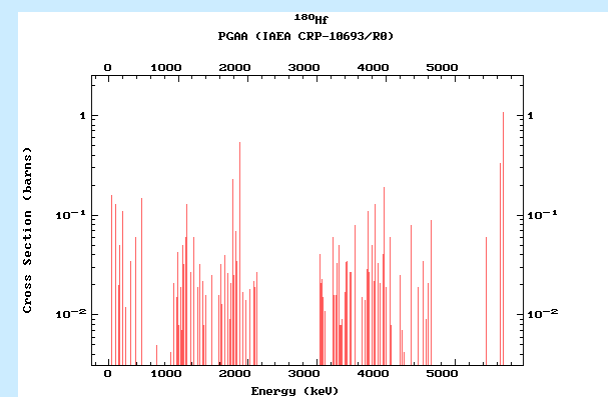
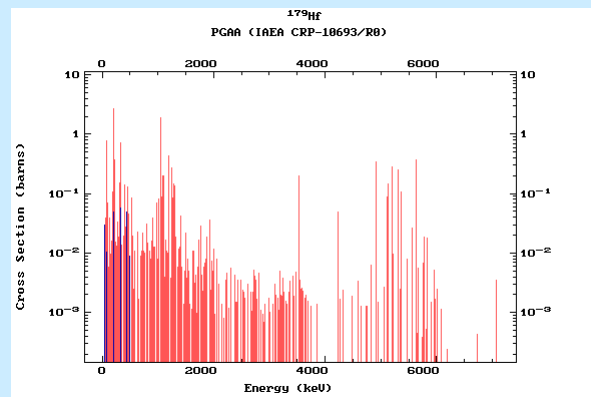
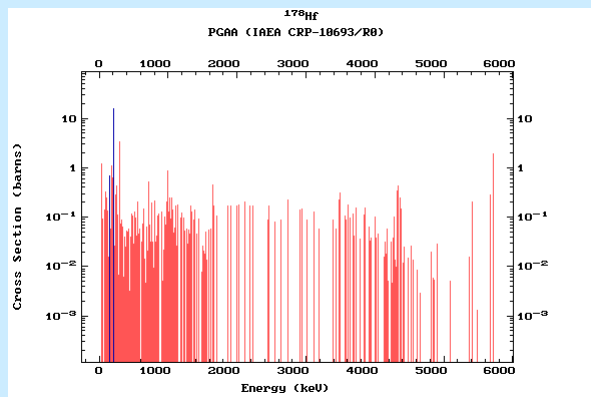
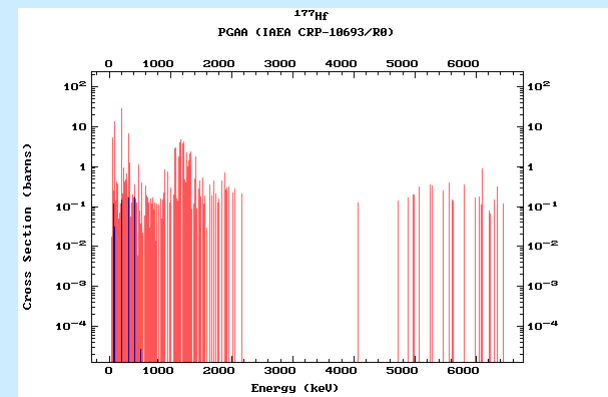
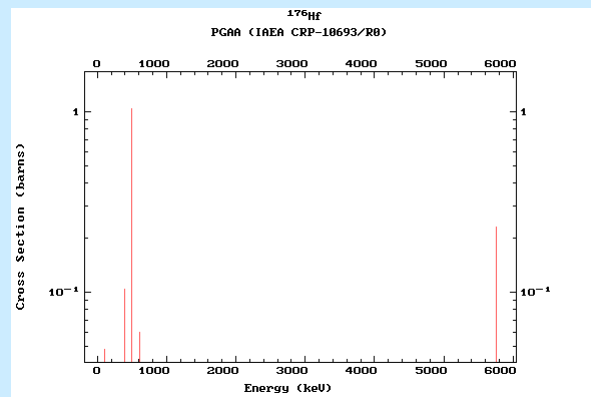
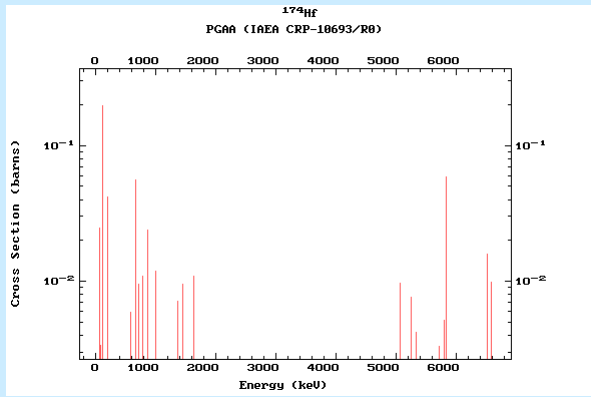
- The gamma-ray identification can be done
 - using the ENSDF (EGAF) or
 - by comparing spectra



Identification by ENSDF and EGAF

(Richard B. Firestone)

Isotope	$\theta(\%)$	$\sigma_V^Z(b)$	g_w	N_V
Hf-174	0.16(1)	549(7)	0.98	23
Hf-176	5.26(7)	24(3)	1	5
Hf-177	18.60(9)	373(10)	1.02	308
Hf-178	27.28(7)	137(7)	1	347
Hf-179	13.629(6)	41(3)	0.99	339
Hf-180	35.08(16)	13.04(7)	0.99	105



Determination of enrichment

(second step)

- Comparator method can be used for determination of isotopic (i) composition of samples (X) in comparison with natural elemental sample (N)

$$\frac{A_{Xi\gamma}}{A_{Ni\gamma}} = \frac{n_X}{n_N} \frac{\theta_{Xi}}{\theta_{Ni}} \frac{P_{Xi\gamma}}{P_{Xi\gamma}} \frac{\sigma_{Xith}}{\sigma_{Xith}} \frac{\phi_X}{\phi_N} \frac{\varepsilon(E_{Xi\gamma})}{\varepsilon(E_{Xi\gamma})} \frac{f_X(E_{Xi\gamma})}{f_N(E_{Xi\gamma})} \frac{t_X}{t_N} ; \text{if } f_X \approx f_N$$

$$\frac{A_{Xi\gamma}}{A_{Ni\gamma}} = \frac{n_X}{n_N} \underbrace{\frac{\phi_X}{\phi_N} \frac{t_X}{t_N}}_C \frac{\theta_{Xi}}{\theta_{Ni}} \Rightarrow \theta_{Xi} = \frac{1}{C} \frac{A_{Xi\gamma}}{A_{Ni\gamma}} \theta_{Ni}$$

- The factor C can be determined from the renormalization of the isotopic compositions θ_{Xi}
- Good isotopic identification of gamma rays is important

Enrichment of Hf samples

(Preliminary results)

Area ratio relative to natural						
Area	Eg	176Hf	177Hf	178Hf	179Hf	Natural
176	395	23523	3871	100	100	3265
177	1419	38789	58606	6006	1940	26720
178	1003	6610	4633	94842	5180	19159
179	1065	5072	100	20457	260424	32362
180	5694	591	100	315	4434	4780
Area ratio						
	Eg	176Hf	177Hf	178Hf	179Hf	Natural abundance
176	395	7.205	1.186	0.031	0.031	5.26
177	1419	1.452	2.193	0.225	0.073	18.6
178	1003	0.345	0.242	4.950	0.270	27.29
179	1065	0.157	0.003	0.632	8.047	13.62
180	5694	0.124	0.021	0.066	0.928	35.08
Unnorm abundance						
	Eg	176Hf	177Hf	178Hf	179Hf	
176	395	37.90	6.24	0.16	0.16	
177	1419	27.00	40.80	4.18	1.35	
178	1003	9.42	6.60	135.09	7.38	
179	1065	2.13	0.04	8.61	109.60	
180	5694	4.34	0.73	2.31	32.54	
		80.785	54.408	150.356	151.034	
Normalized abundance						
	Eg	176Hf	177Hf	178Hf	179Hf	
176	395	46.91	11.46	0.11	0.11	
177	1419	33.42	74.98	2.78	0.89	
178	1003	11.65	12.13	89.85	4.89	
179	1065	2.64	0.08	5.73	72.57	
180	5694	5.37	1.35	1.54	21.55	
		100.000	100.000	100.000	100.000	

Summary of results for other samples

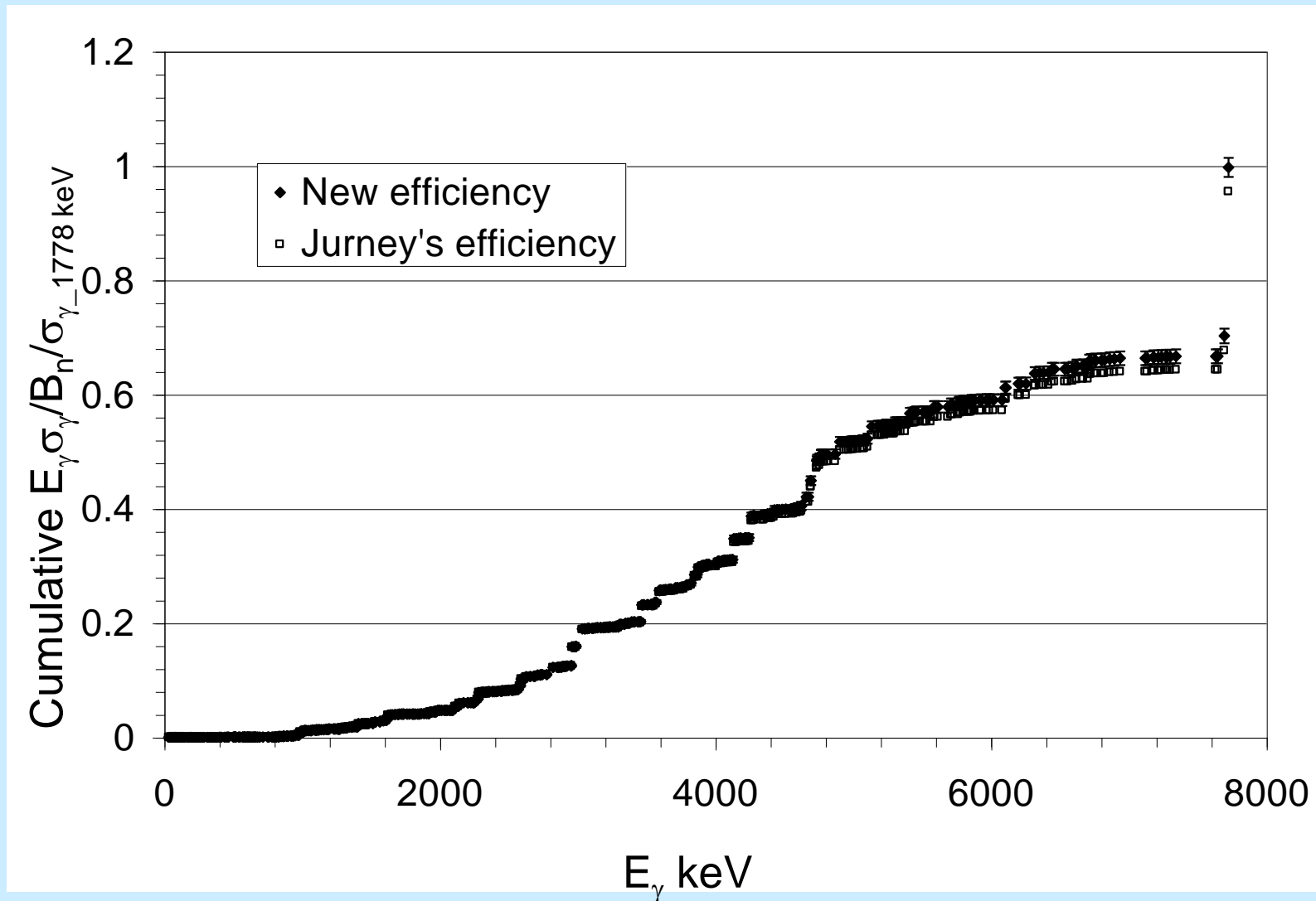
- We have written reports on the results of the analysis that were sent to the proposers
- Results on $^{96}\text{ZrO}_2$ sample and three Zr metal discs from Geel.
 - The enriched sample had Cl, Ti, Hf impurities, Hf is disastrous for observing ^{96}Zr
 - The old Zr disc is the purest (B, Ti, Mn, Fe, Pr, Hf, Au on the ppm level), while the other two had substantial Hf impurity
- Results for enriched $^{58,60,62}\text{Ni}$ and $^{54,56,57}\text{Fe}$ samples
 - The isotopic composition of the samples were found in agreement with its certificate (the main components >99.5%)
 - For elemental impurities we found H, V, Mn, Ni, Cu in the Fe and H, P in the Ni samples on the ppm level, while H on the 1% level

Conclusions

- The PGAA method is capable to determine the isotopic composition of enriched samples
 - It is especially good since it is sensitive to the high cross section materials, which is the same for other low energy neutron experiments
- There are difficulties in case of very high cross section materials because of the complexity of the spectra and the suppression of the low yield components
- At extreme high enrichment it is also difficult to find the small concentration isotopes
- These later two difficulties are related to the relatively small dynamic range, which is about 10^{-4}

Thank you for your attention!

Test of nitrogen new intensities $^{27}\text{Al}(n,\gamma)$ reaction inverted Q-value

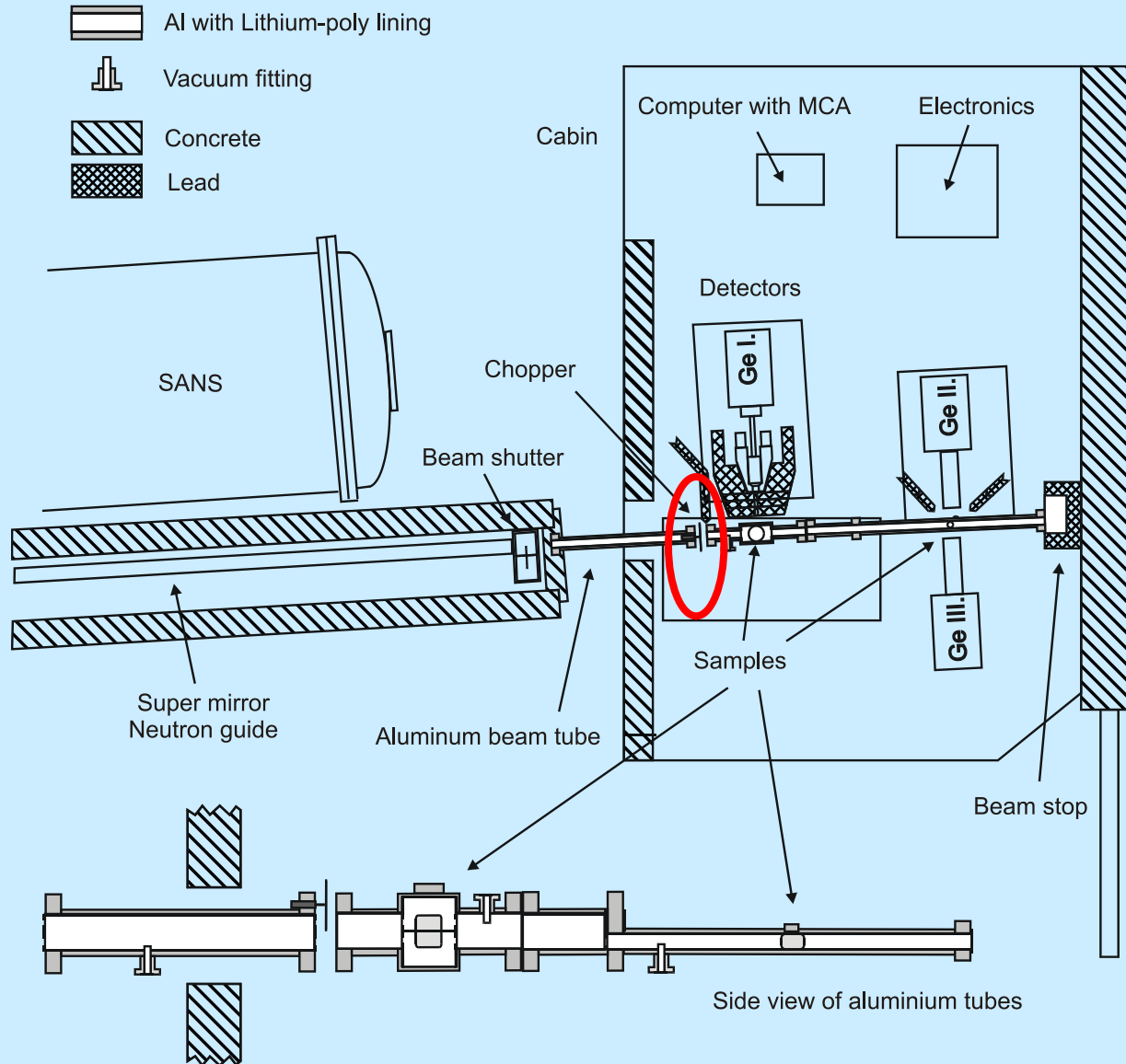


T. Belgia, Phys. Rev. C 74, 024603 (2006).

PGAA-NIPS facilities

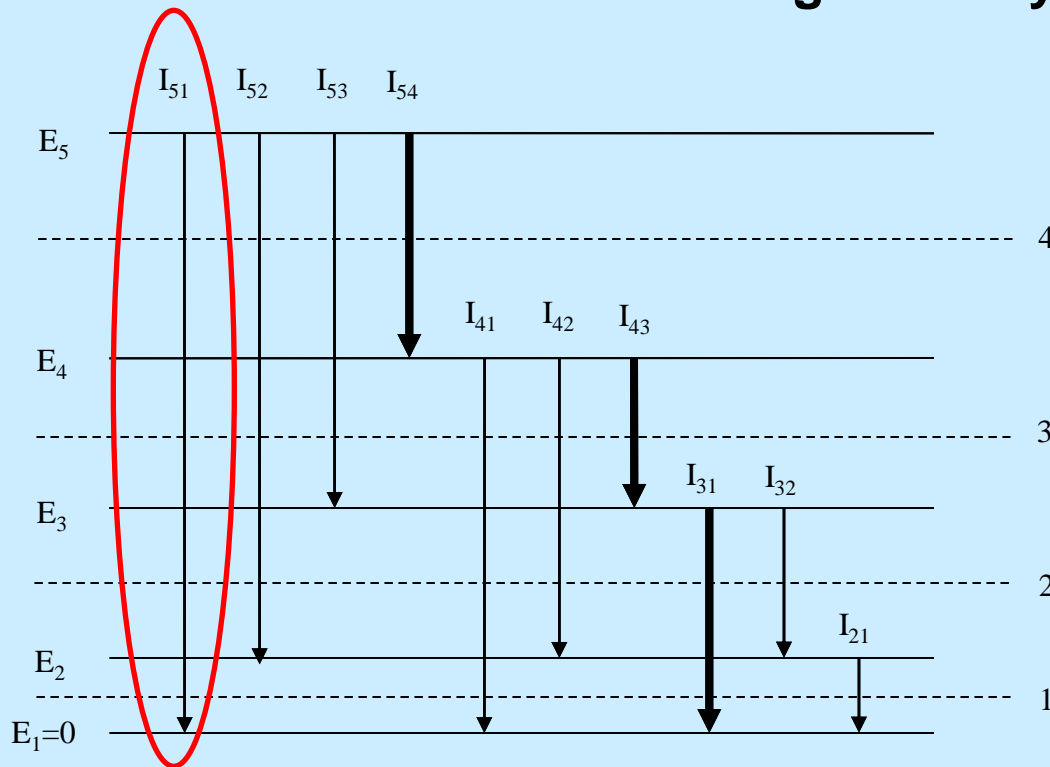


The PGAA-NIPS facility



Determination of nitrogen intensities and detector efficiency function in one step

Crossing Intensity Sum (CIS)



$$I_{i,j} = A_{i,j} \varepsilon^{-1}(E_{i,j})$$

$$T_f = \sum_{\substack{i>f \\ j\leq f}} I_{i,j} = \sum_{\substack{i>f \\ j\leq f}} A_{i,j} \varepsilon^{-1}(E_{i,j}) = C \quad f = 1, 2, \dots, n-1$$

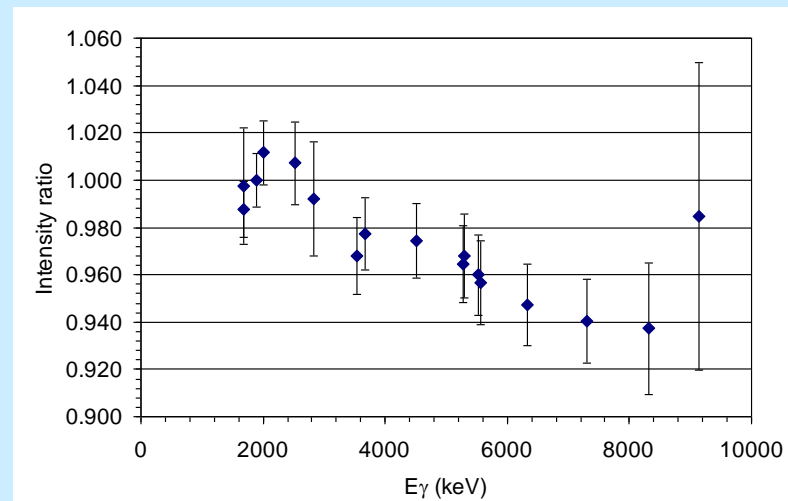
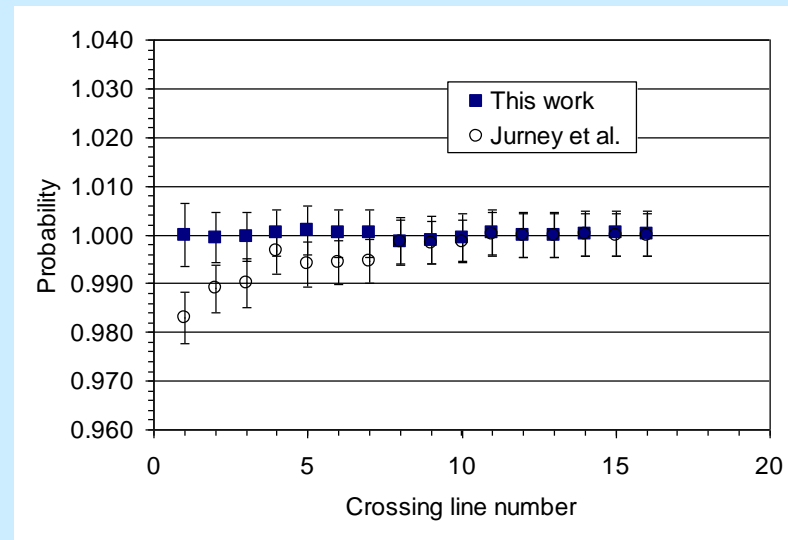
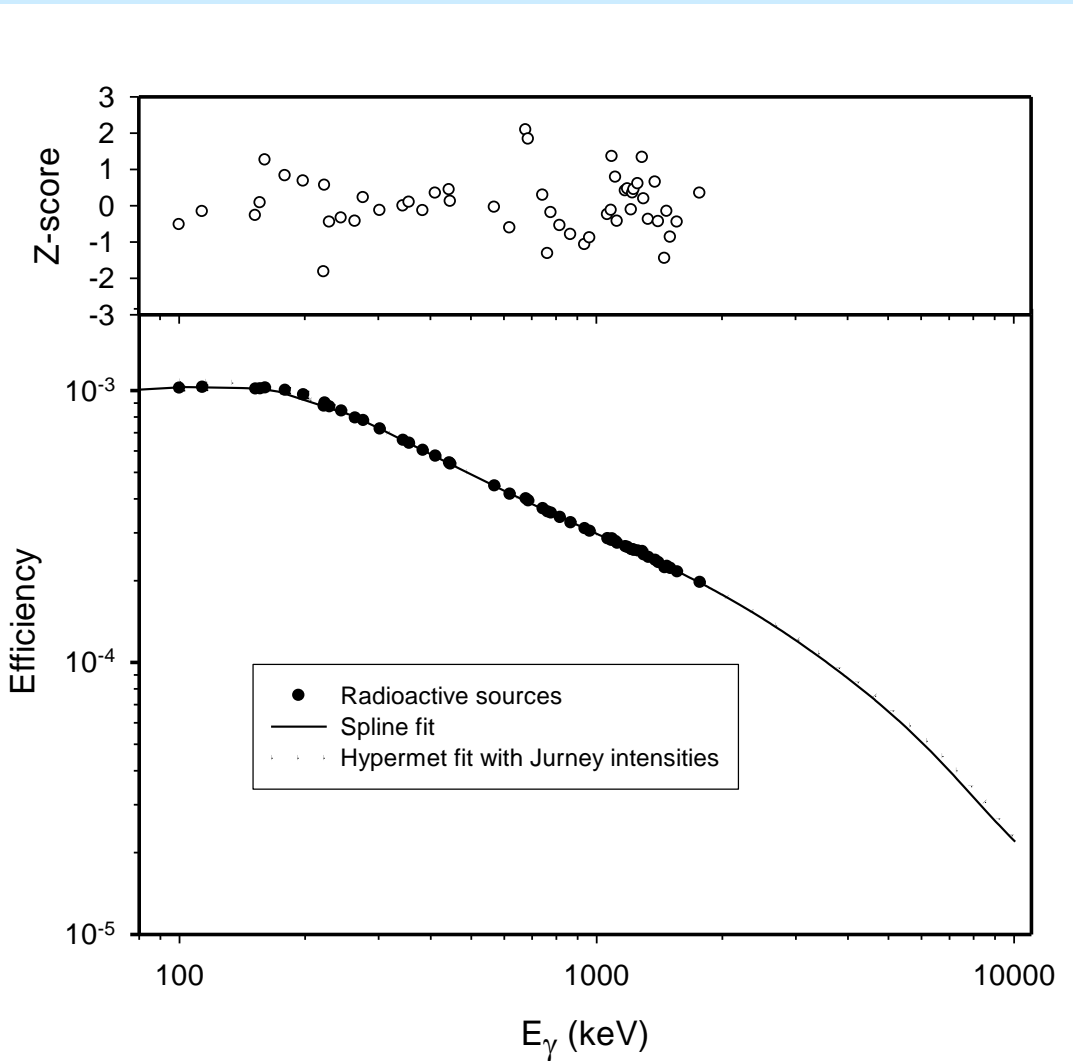
$$Q = \sum_{\substack{1\leq f\leq n-1 \\ 1\leq s\leq n-1}} (T_f - C) w_{f,s} (T_s - C) + \sum_m \frac{(\tilde{\varepsilon}_m^{-1} - \varepsilon^{-1}(E_{i,j}))^2}{\sigma_m^2}$$

- Sums of crossing intensities are constant C
- Least-squares fit for inverse efficiency function ε^{-1} and C
- Input is peak areas and efficiencies at low energy
- CIS for line 1 \equiv intensity sum to the ground state
- CIS for line $n-1 \equiv$ intensity sum for the primary transitions

New : $\sigma_{th} = 80 - 83 \text{ mb}$

Mughabghab : $\sigma_{th} = 79.8(14) \text{ mb}$

Results



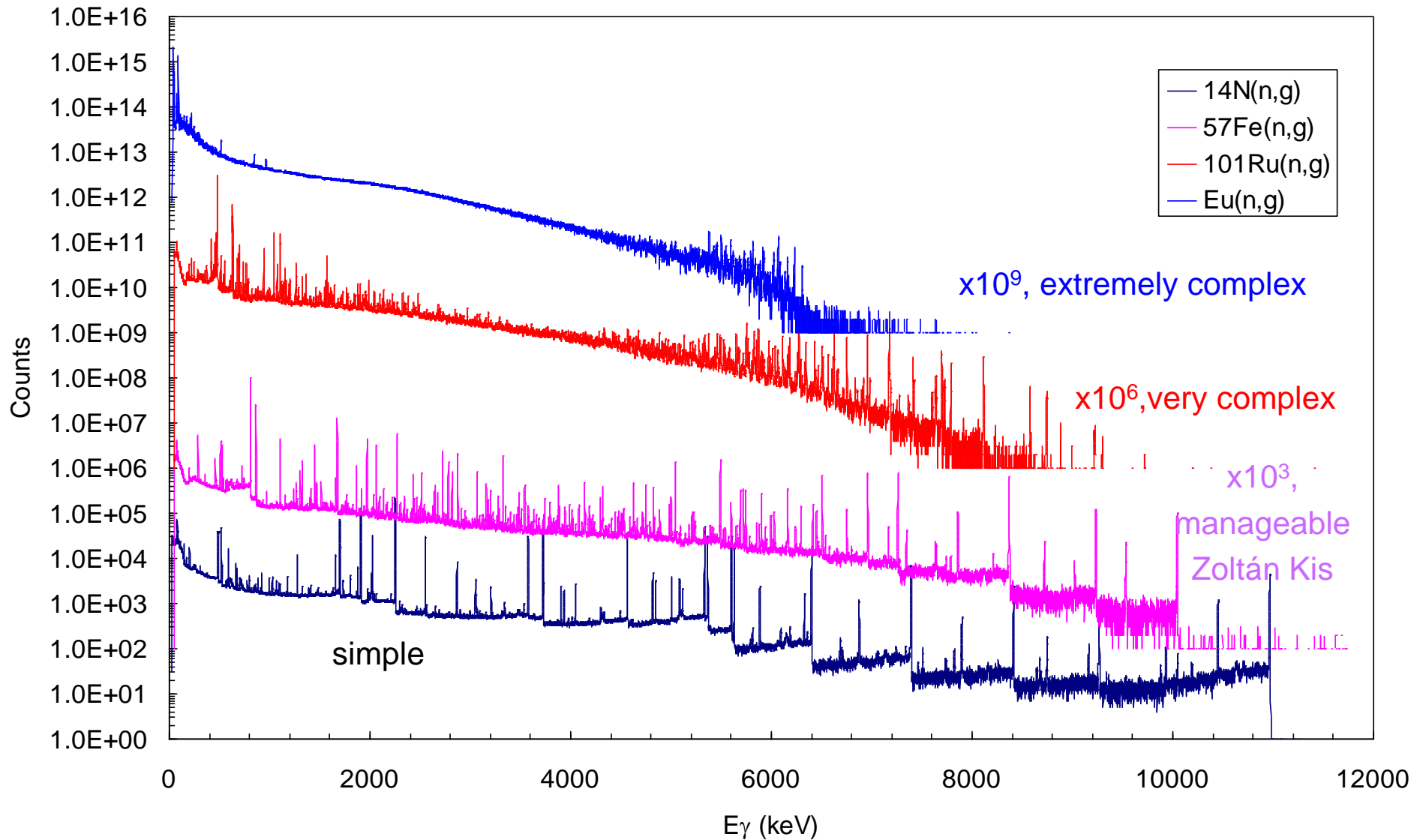
Ratio=Intensity Journey / Intensity this work

Total neutron capture cross section from γ -spectroscopy

Method	Equation	Notes
1	$\sigma_{th} = \frac{\sigma_{\gamma}}{\theta P_{\gamma}}$	P_{γ} must be known, for example from beta decay if the captured nucleus is unstable.
2	$\sigma_{th} = \sum_{f=1}^{n-1} \sigma_{\gamma C \rightarrow f} (1 + \alpha_f)(1 + PCC_f)$	The sum of all primary transitions from the capture state can be used for nuclei with relatively simple decay scheme.
3	$\sigma_{th} = \sum_{i=2}^n \sigma_{\gamma i \rightarrow g.s.} (1 + \alpha_i)(1 + PCC_i)$	The sum of all ground state transitions can be used for nuclei with relatively simple decay scheme. Conversion coefficients α must be known.
4	Average of CISs: $Q = \min \left(\sum_{\substack{1 \leq f \leq n-1 \\ 1 \leq s \leq n-1}} (T_f - \sigma_{th}) w_{f,s} (T_s - \sigma_{th}) \right)$	Well balanced and relatively simple decay scheme. Conversion coefficients α must be known.
5	$\sigma_{th} = \sum_i E_i \sigma_{\gamma i} (1 + \alpha_i)(1 + PCC_i) / B_n$	The energy weighted sum can be used for any nuclei with resolved gamma-transitions. E_i is the energy of the transition, B_n is the binding energy and PCC is the pair conversion.

For which nuclei we can use that

(Simple and complex spectra)



Consequences

- Method 1 based on decay γ -rays or X-rays can be used for any complexity
 - Precision depends on the P_γ value
- Method 2-5 is applicable for nuclei with manageable decay scheme (~ 500 γ -rays)
 - Limitation can be the unobserved conversion electron intensities
- Method 5 is applicable for spectra with resolvable γ -lines (~ 700 - 800 γ -rays)
 - Limitation can be the unobserved conversion electron intensities
 - Similar to the weighting function method used with C_6D_6 detectors
- Above that quasi continuum of γ -rays appears in the spectra
 - A possible approach is stripping or deconvolution of spectra on the few percent level accuracy
 - C_6D_6 detector or total absorption detector (needs highly enriched sample, unobserved conversion electron can also be a problem)

Question of completeness from the experimental point of view

- The Q-value test (equivalent to method 5) was applied in the past to estimate completeness

$$B_n = \sum_{i \in \text{observed } \gamma} \frac{E_i \sigma_{\gamma i}}{\sigma_{th}}; \quad \sigma_{th} = \sum_{i \in \text{observed } \gamma} \frac{E_i \sigma_{\gamma i}}{B_n}$$

- This is still the best way to find out the degree of completeness, however we propose to use the inverse Q-value instead and compare it directly to other independent Xsection values
- There are experimental methods that do not depend on observing all of the γ -rays, they provide the independent Xsections (they usually have other problems)
 - Pile oscillator, activation, transmission and calorimeter

An example

$^{101}\text{Ru}(n,\gamma)$ reaction (proposed by ILL)

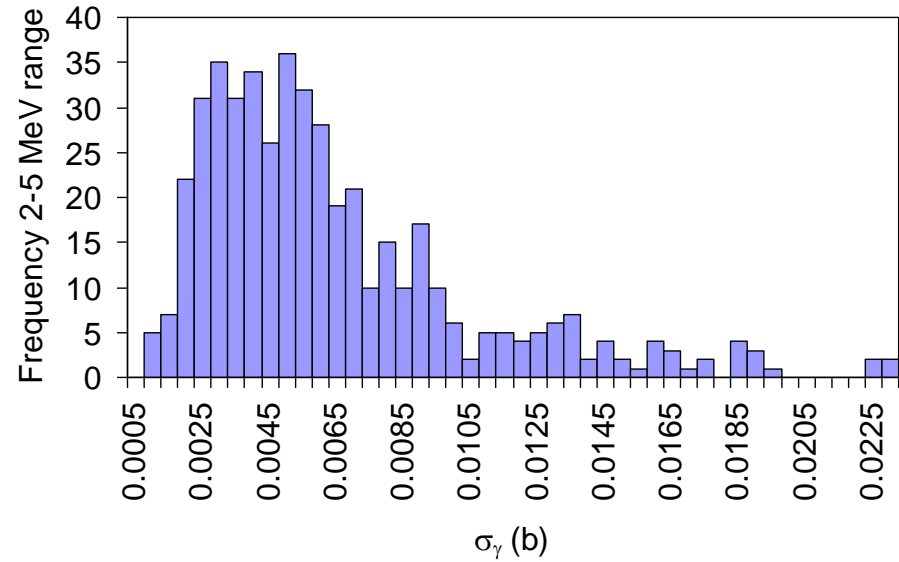
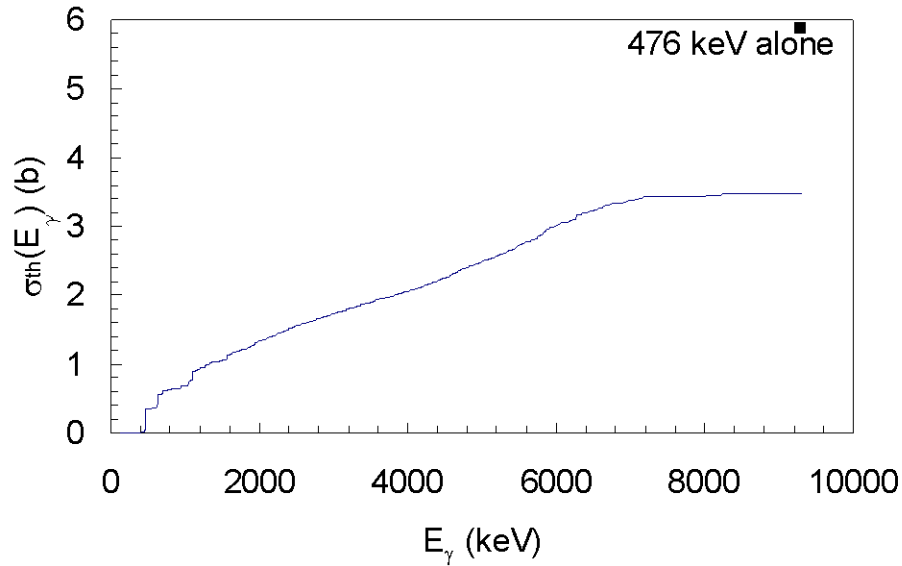
Earlier data:

- No γ -rays in the ENSDF database
- EXFOR

σ_{th} (b)	Facility	Method	Author	year
3.4(9)	Reactor Internal McMaster	PGAA	Islam	1991
3.1(9)	Reactor Oakridge	Activation ??	Halperin	1964
5.5(1.4)	Reactor Oakridge	Mass spectrometry	Halperin	1965

The only independent or different method is the mass spectrometry

$^{101}\text{Ru}(n,\gamma)$ reaction studied at our PGAA facility



Unobserved continuum is at least 40%

^{101}Ru g.s. spin $5/2^+$ \rightarrow capture state spins 2^+ and 3^+

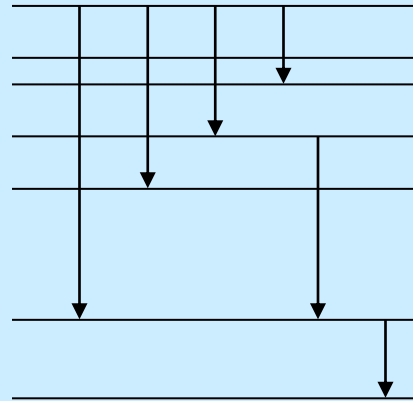
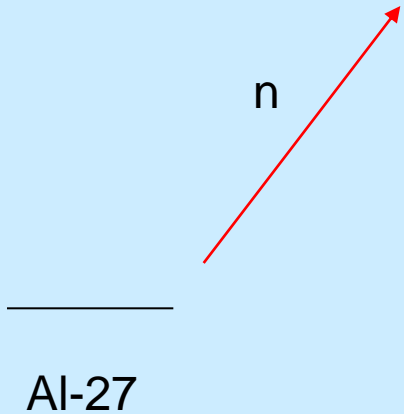
^{102}Ru : final state cumulative level number for spins 2,3,4,5 at 9.3 MeV $\sim 1.5 \times 10^5$

Minimum observed σ_γ in the 2-5 MeV range is 0.001 b

Estimate: maximum missing intensity = $1.5 \times 10^5 \times 0.001 / 4 = 37.5$ b ! \rightarrow

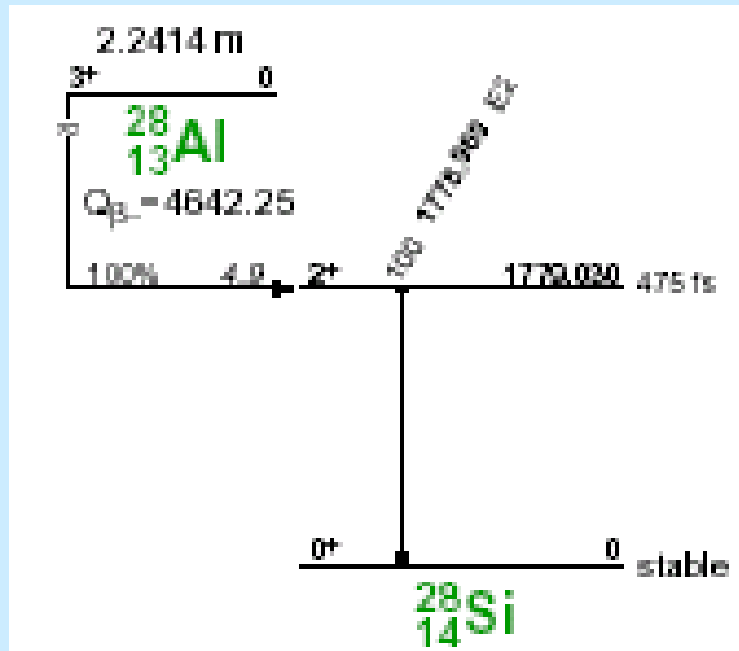
useless limit \rightarrow We need to use better model (e.g. DICEBOX Frantisek Becvar)

Test with $^{27}\text{Al}(n,\gamma)$



Method 4

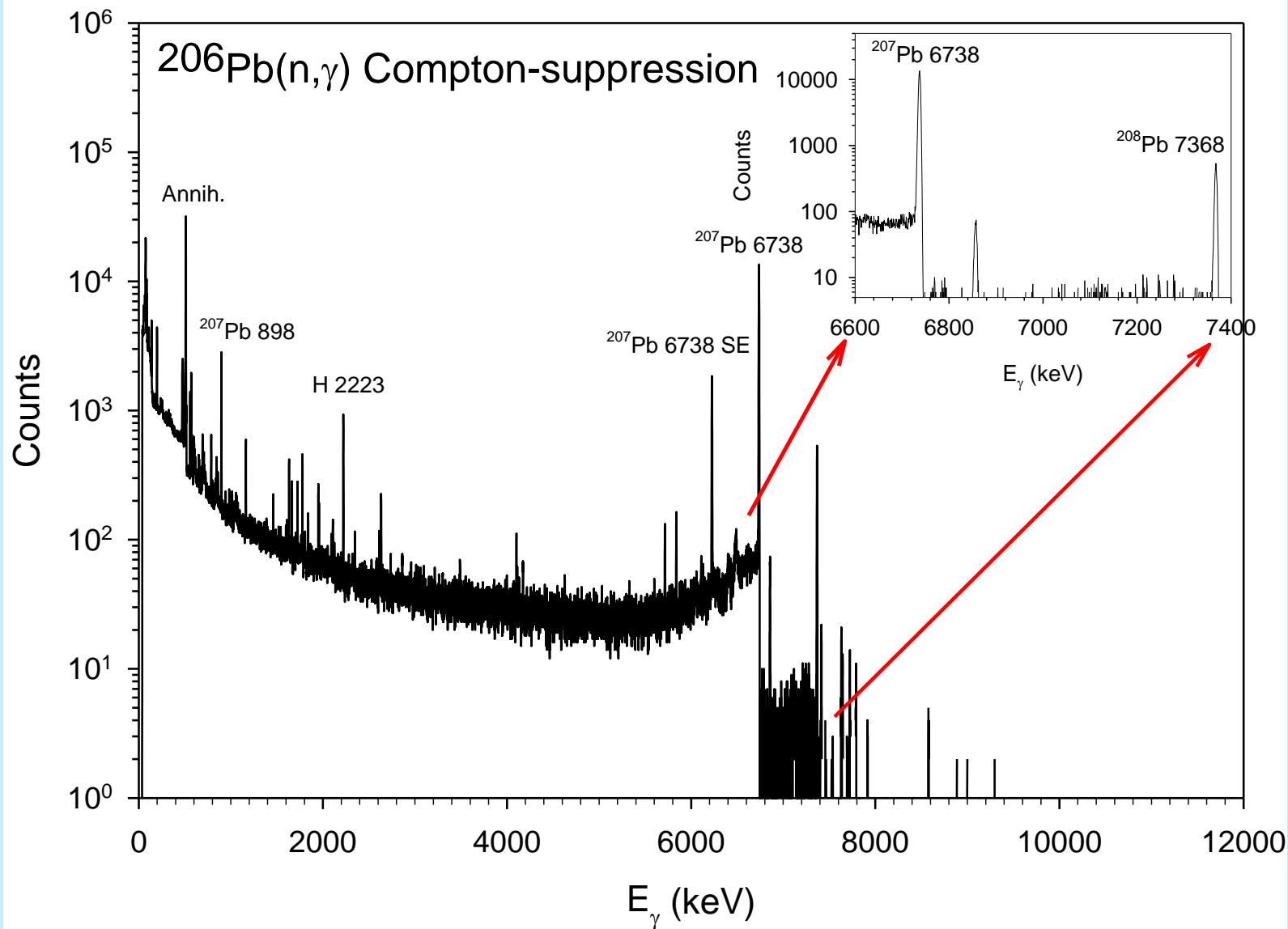
$$\sigma_{\text{th}} = \sum E_i \sigma_{\gamma i} c_i / B_n$$



Method 1

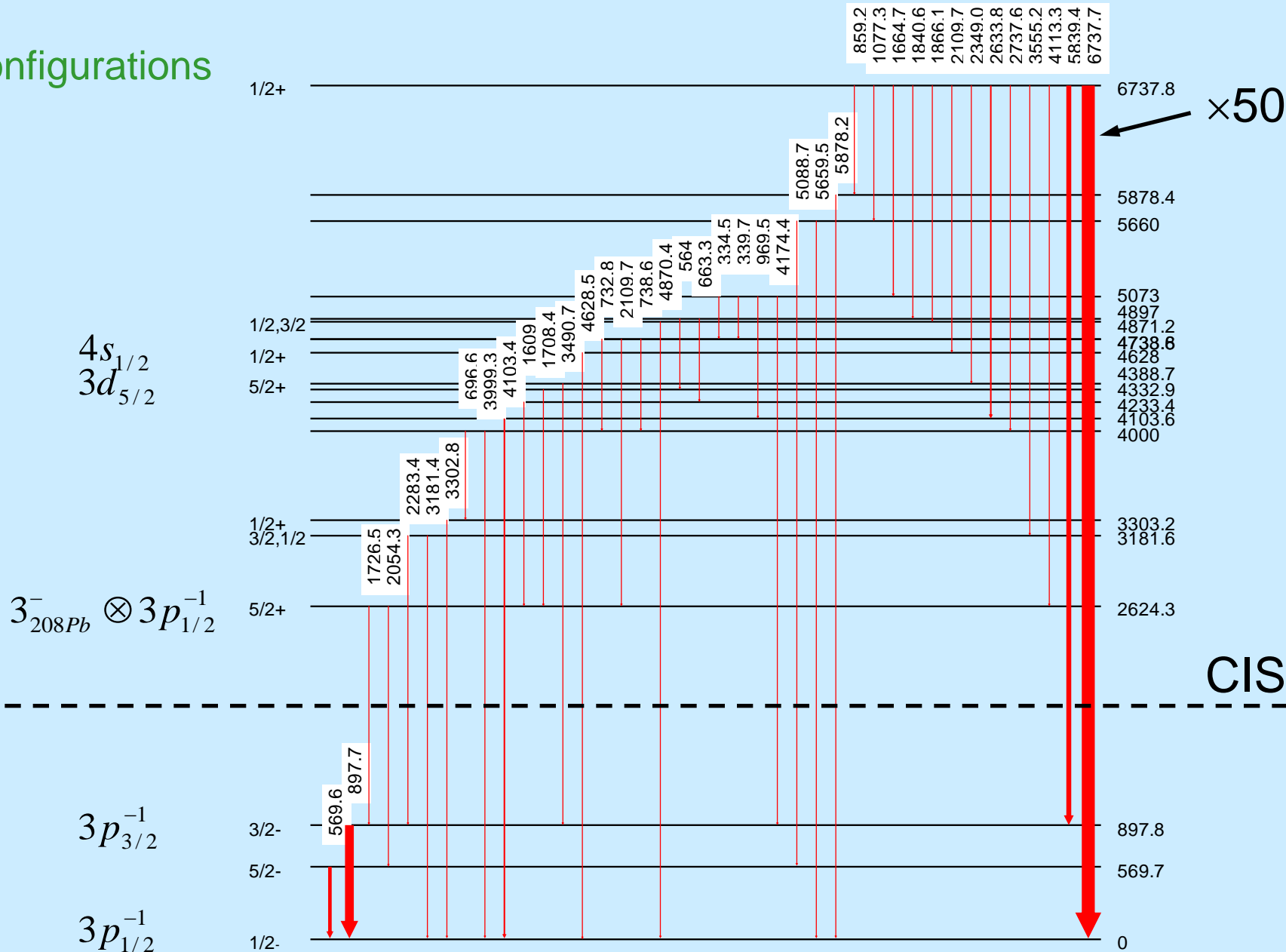
$$\sigma_{\text{th}} = \sigma_{\gamma 1779}$$

$^{206}\text{Pb}(n,\gamma)$ spectrum

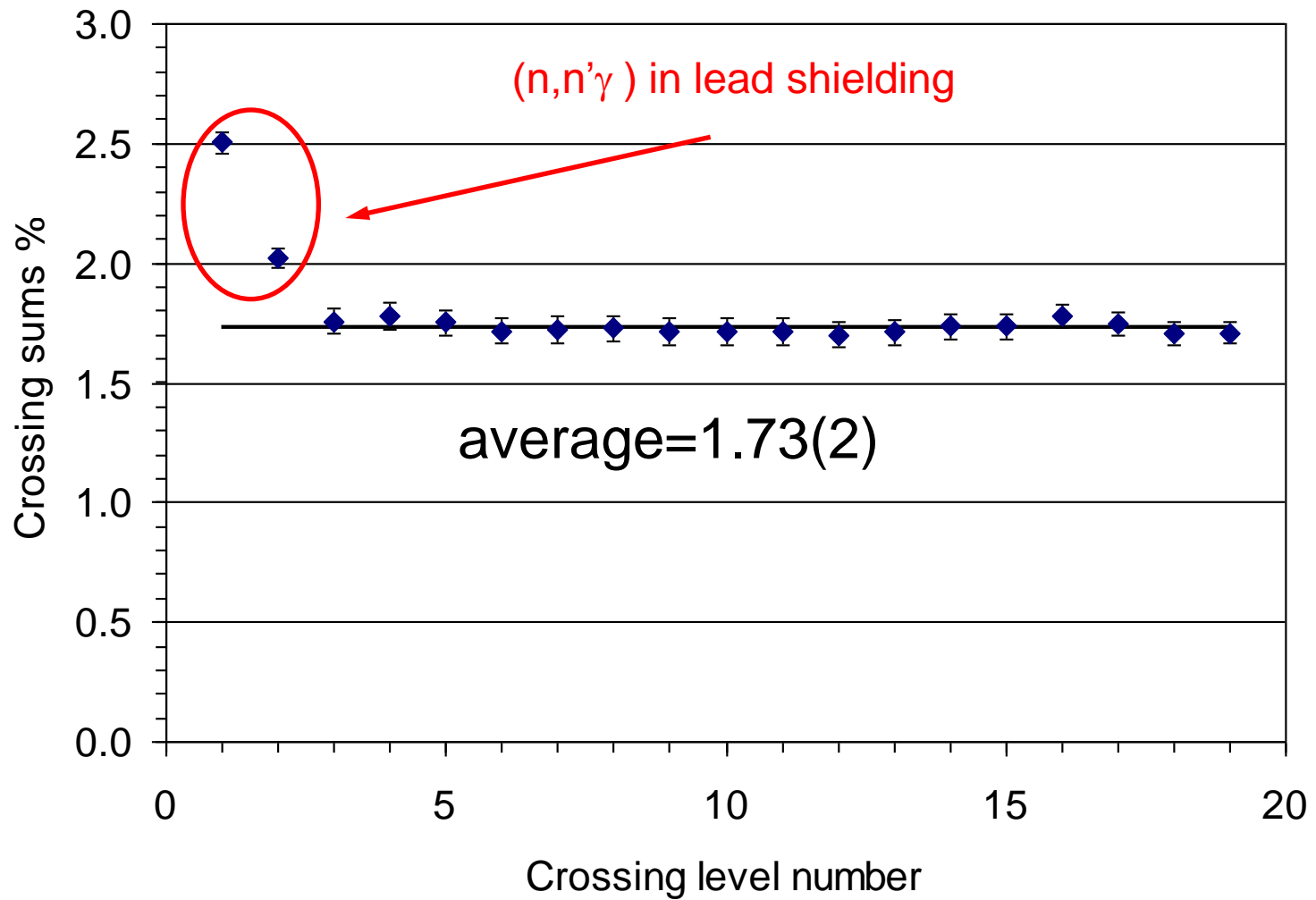


New neutron capture decay scheme of ^{207}Pb

Configurations



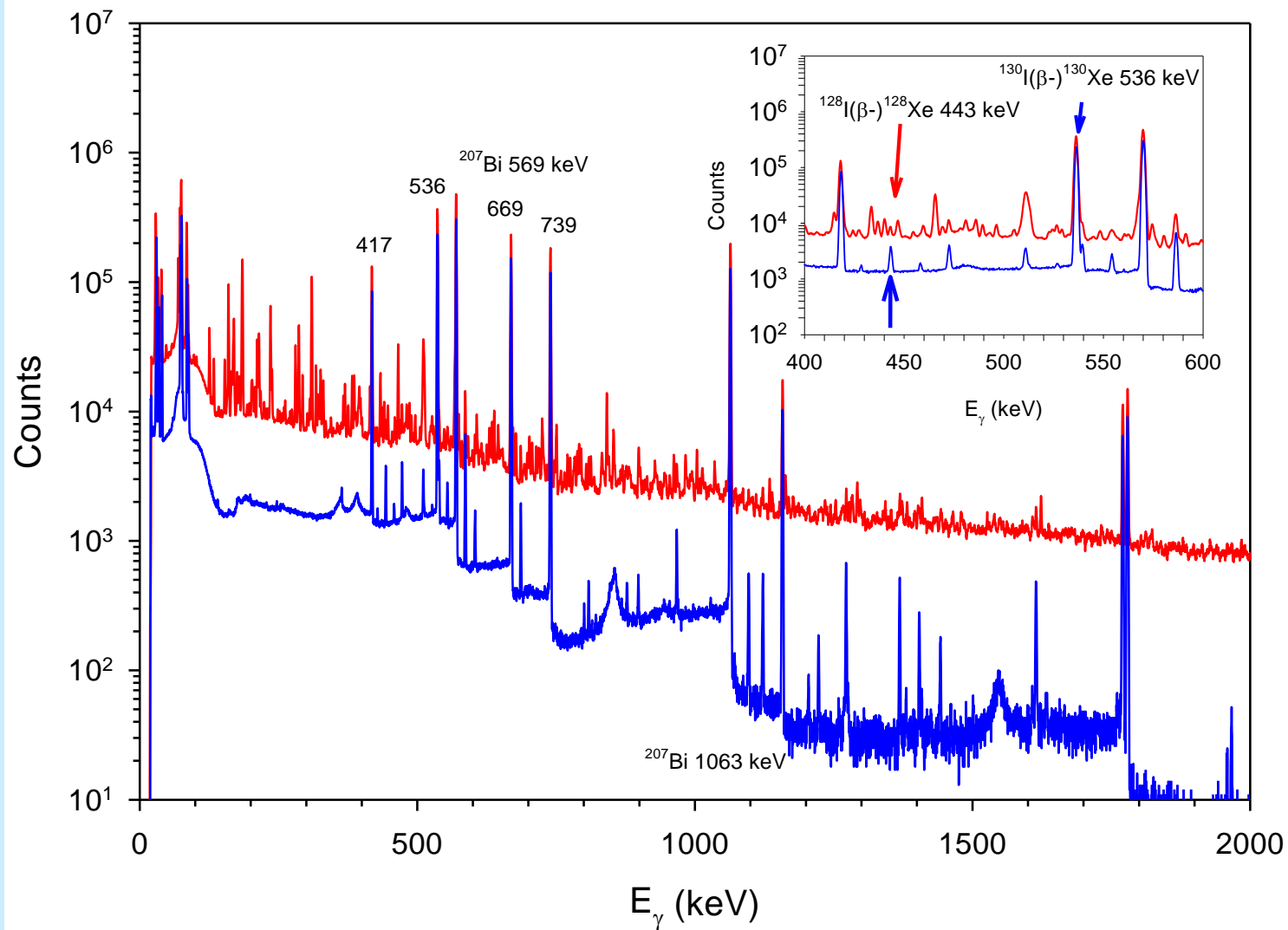
Crossing Intensity Sums for the decay scheme of ^{207}Pb



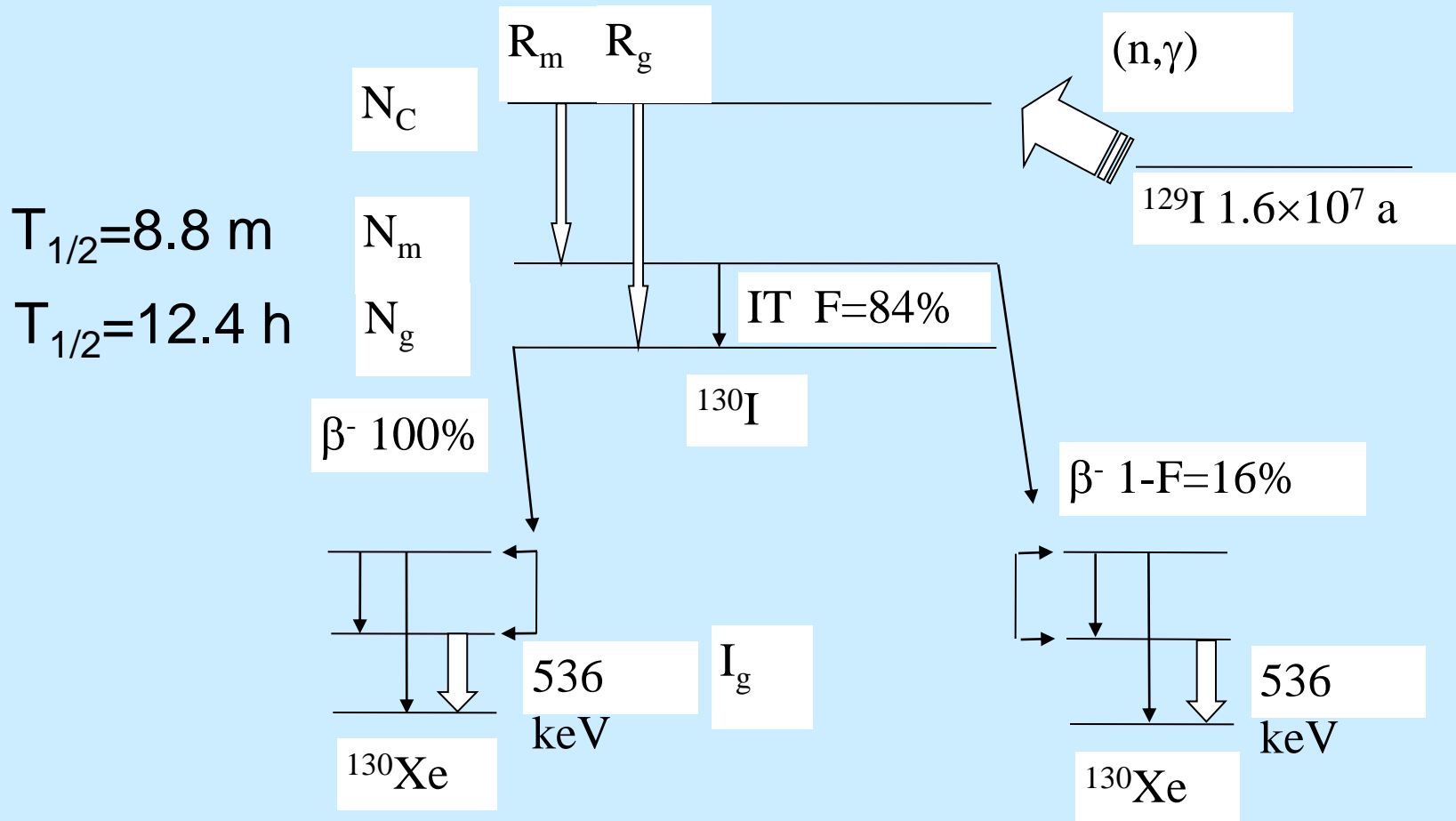
Results for $^{204,206,207}\text{Pb}$ Xsec

Isotope	This work (mb)	Mugabgab (mb)	Comment
^{204}Pb	482(20)	661(70)	preliminary
^{206}Pb	28.7(7)	26.6(12)	Increase is due to the N source
^{207}Pb	649(14)	625(30)	increase is due to the N source

$^{127,129}\text{I}$ chopped beam (n, γ) spectra



Simplified decay scheme of ^{130}I from literature

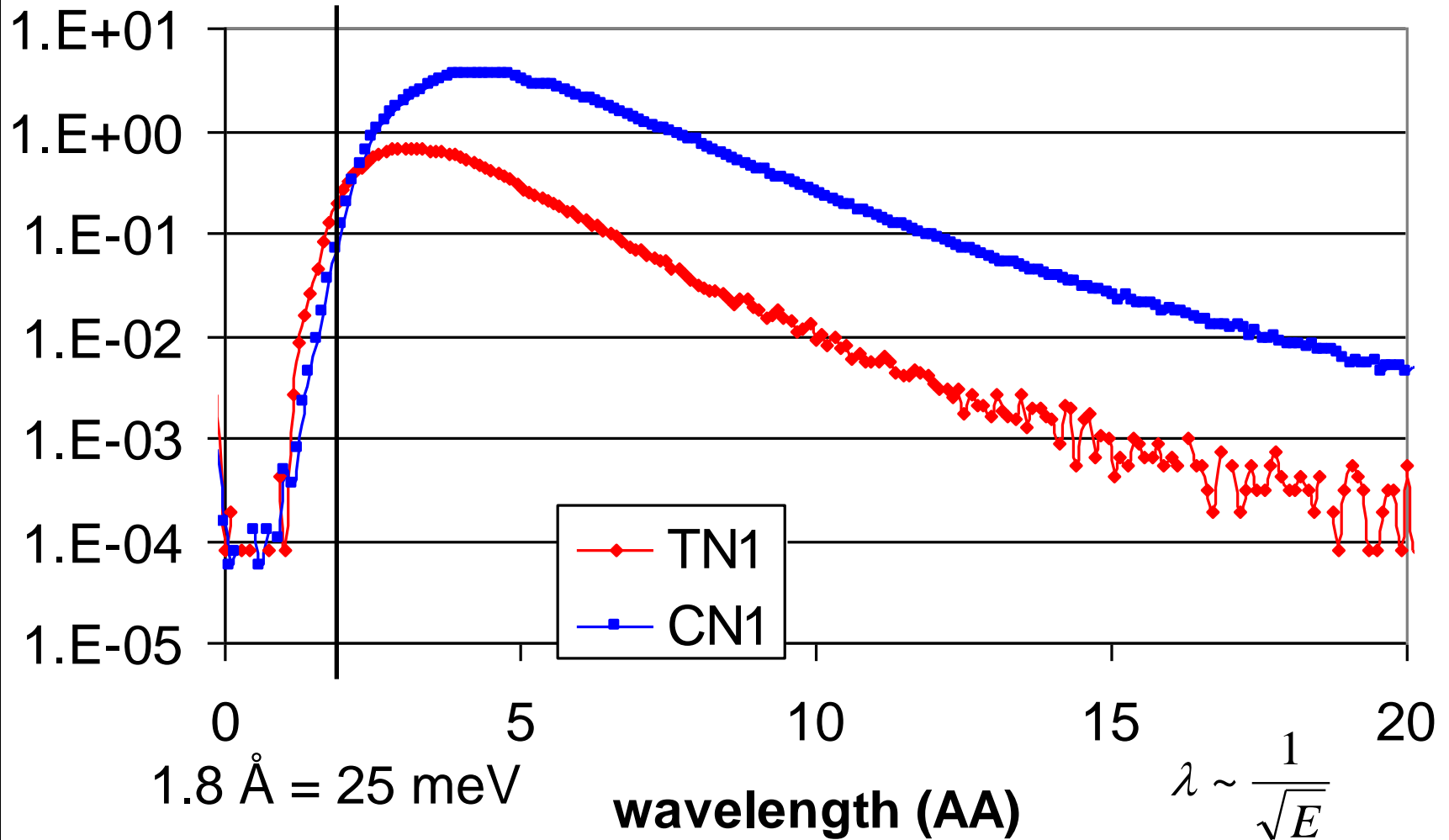


Results for ^{129}I Xsec

Year	Author	Method	σ_{th} (b)
1956	Purkayastha <i>et al.</i>	Activation reactor	35
1958	Roy <i>et al.</i>	Activation reactor	26.7(20)
1963	Pattenden <i>et al.</i>	TOF	28(2)
1969	Block <i>et al.</i>	TOF	31(4)
1983	Friedmann <i>et al.</i>	Activation reactor	33.9(19)
1996	Nakamura <i>et al.</i>	Activation reactor	30.3(12)
2007	Belgya <i>et al.</i>	Chopped cycl. act.	30.6(11)

Neutron energy is mostly below the first resonance

Wavelength spectra of thermal and cold beams



Total neutron capture cross section

another way

- Total energy detector concept, $\varepsilon = E_\gamma$ or inverse Q value;

$$\sigma_{th} = \sum_i E_i \sigma_{\gamma i} (1 + \alpha_i) (1 + PCC_i) / B_n$$

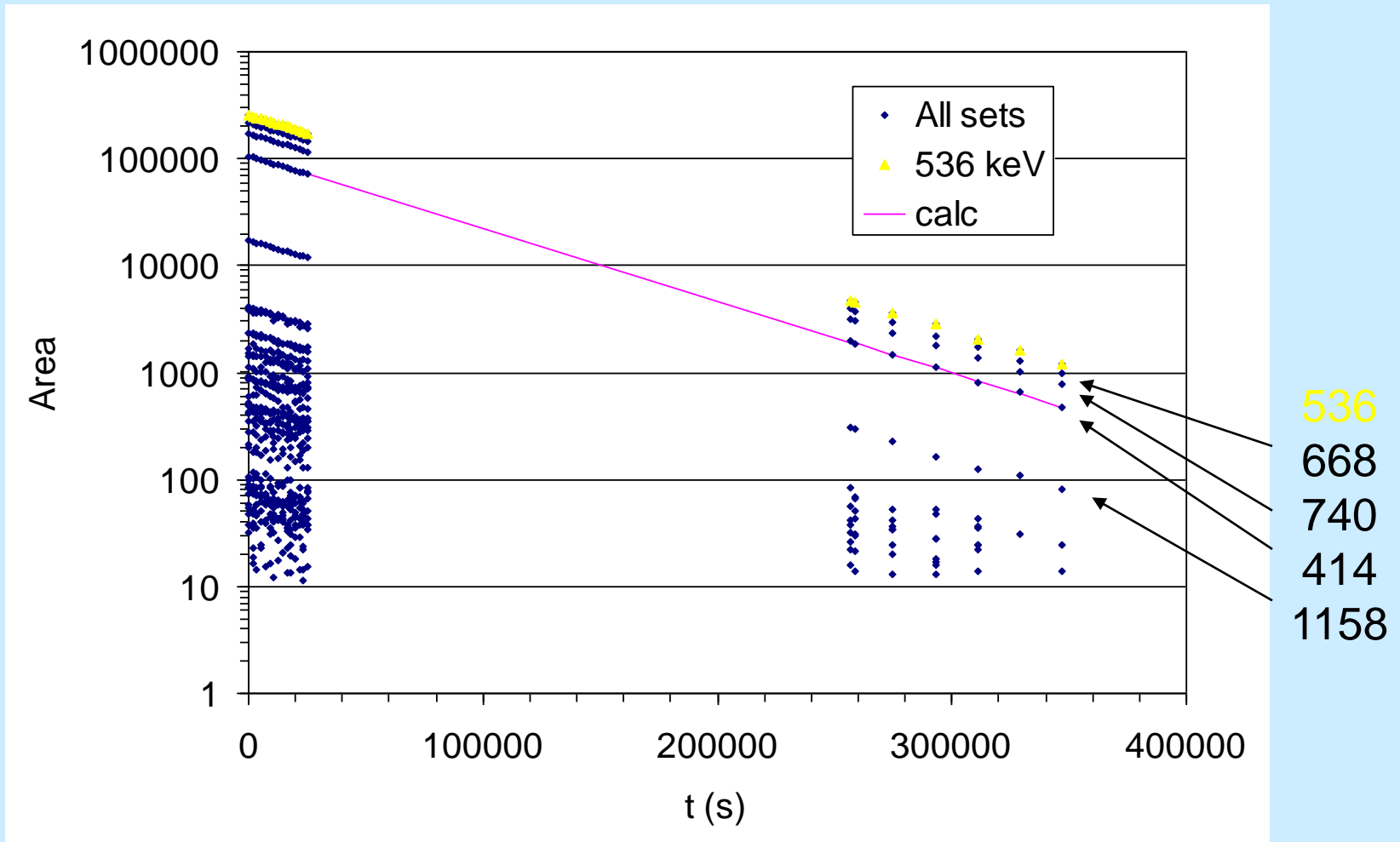
- i = all transitions, (no decay scheme is needed)
- Good identification is necessary, eg. ^{209}Bi , ^{206}Pb , ^{27}Al , etc.

Total neutron capture cross section

another way

- From decay gamma rays: $\sigma_{th} = \frac{\sigma_{\gamma}}{\theta P_{\gamma}}$
 - Continuous beam activation (traditional)
 - Chopped beam activation (new)
 - Absolute decay probability P_{γ} is needed, $^{238,235}\text{U}$, ^{232}Th , ^{129}I , ^{99}Tc , ^{27}Al , Te isotopes etc.,

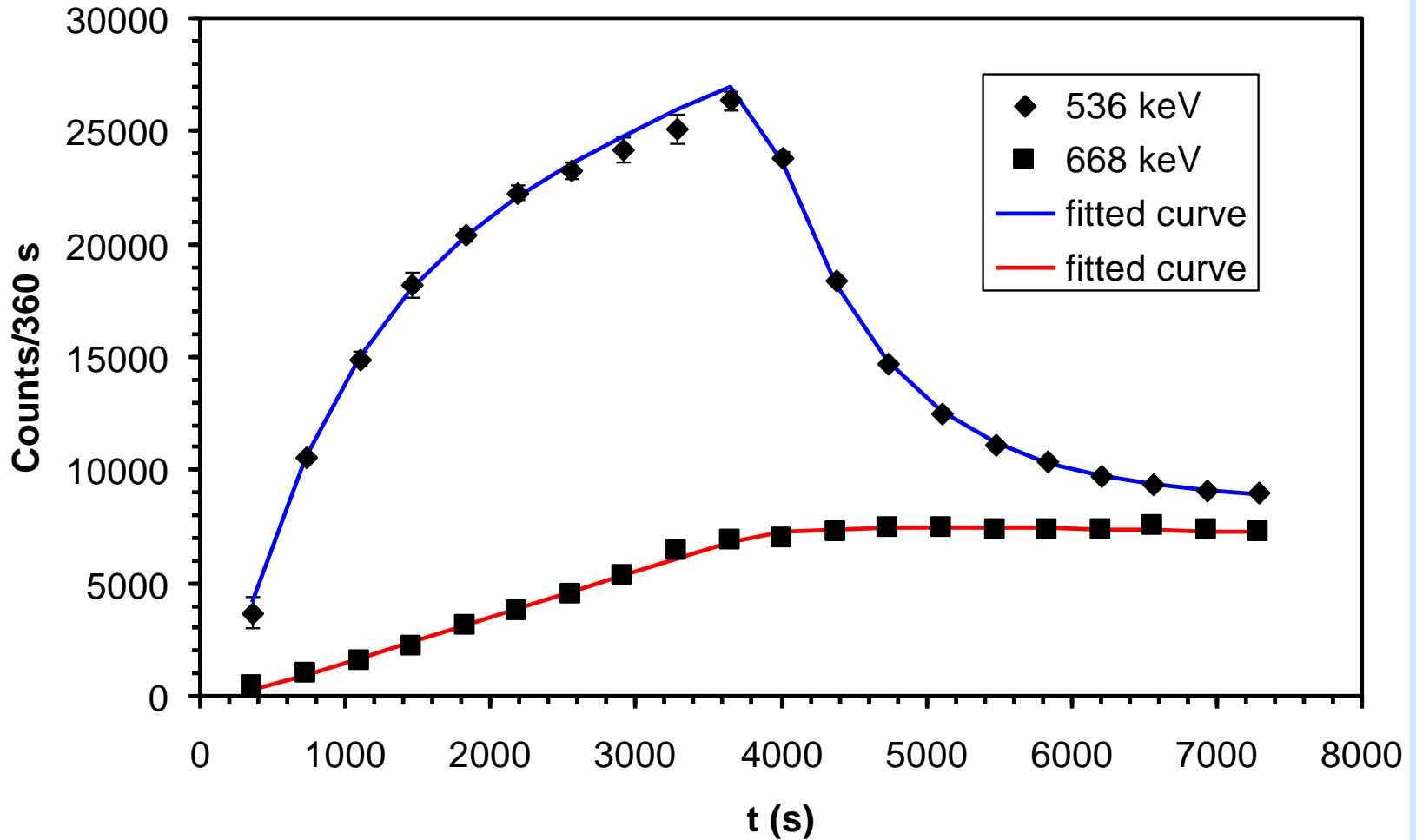
Long decay of ^{130}I ground state



E (keV)	T1/2 (h)	Uncertainty	mean	deviation	ENSDF	ucertainty
417	12.375	0.031	12.390	0.035	12.36	0.01
536	12.439	0.019				
668	12.360	0.022				
740	12.387	0.020				
1158	12.253	0.039				

Peak area of 536 and 668 keV $^{130}\text{I}(\beta^-)^{130}\text{Xe}$ decay gamma rays during activation and decay

$F=71\%$, $R_m=36\%$, $\lambda_m=1.279\text{E-}3$, $\chi^2=1.25$ **proposed new**



New fit results and uncertainties

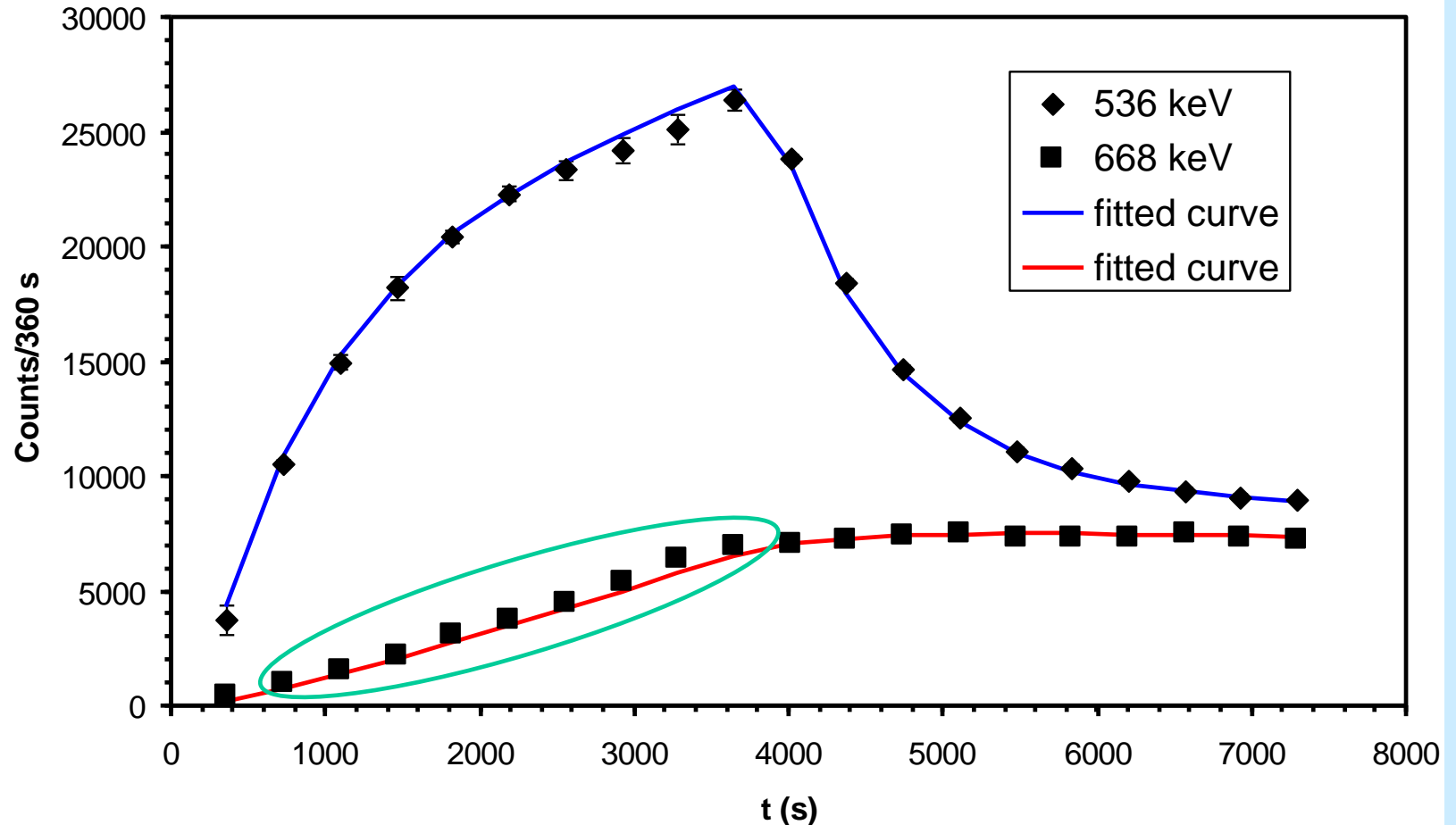
	Present work	Unc.	Rel. U.	Literature
d	516.9	8.0	1.55	-
R_m	0.355	0.008	2.14	0.60(9) a)
λ_m	1.279E-3	1.6E-05	1.27	1.316E-3(3E-6) b)
λ_g	1.558E-05	2.3E-07	1.49	fixed
F	0.709	0.009	1.26	0.83(3) a)
b_g	0.997	0.016	1.58	fixed
b_m	0.987	0.034	3.39	fixed
deadt_corr	0.0218	0.0013	6.10	-
b668g	0.832	0.012	1.39	-

a) P.K. Hopke, A.G.Jones, W.B. Walters, A. Prindle, R.A. Meyer, PRC 2 (1973) 745

b) S. Nakamura, H. Harada, T. Katoh, Z. Ogata, J. Nucl. Sci. Techn. 33 (1996) 283

Peak area of 536 and 668 keV $^{130}\text{I}(\beta^-)^{130}\text{Xe}$ decay gamma rays during activation and decay

$F=83\%$ (fixed), $R_m=0.6$, $\lambda_m=1.344\text{E-}3$ $\chi^2=4.5$ Literature



Uncertainty budget

ISO Guide to the expression of Uncertainty in Measurement (GUM)

$$\sigma_{\gamma x} = \sigma_{\gamma c} \frac{n_c A_{\gamma x} / \varepsilon(E_{\gamma x}) / f(E_{\gamma x})}{n_x A_{\gamma c} / \varepsilon(E_{\gamma c}) / f(E_{\gamma c})}$$

- Advantages of the relative internal calibration method
 - Absolute flux, inhomogeneity of sample and flux, multiple scattering (build up effect), dead time, energy distribution of flux, sample weight cancel out
- Uncertainty components for partial gamma ray cross sections
 - Uncertainty (1σ , δA) of the area A is obtained from peak fitting with Hypermet PC
 - Uncertainty efficiency ratio can be obtained from the correlation matrix of the efficiency fit. Relative uncertainty of the efficiency is about 0,5-1% in the 0.1-10 MeV range.
 - Gamma and neutron self absorption is calculated with numerical integration over simple shape of samples. For thin samples they are close to 1 and the estimated uncertainty is 5% of the difference from 1

A nice summary: Zs. Révay, Nucl. Instr. & Methods **A 564** (4-6), 688-697 (2006)

Uncertainty calculation example

Continuous beam

$$\sigma_{\gamma x} (1 \pm \delta\sigma_{\gamma x}) = \sigma_{\gamma c} \frac{A_{\gamma x} n_c \varepsilon(E_{\gamma c}) f(E_{\gamma c})}{A_{\gamma c} n_x \varepsilon(E_{\gamma x}) f(E_{\gamma x})}$$

$$\left(1 \pm \sqrt{(\delta A_{\gamma x})^2 + (\delta A_{\gamma c})^2 + (\delta \varepsilon(E_{\gamma x}))^2 + (\delta \varepsilon(E_{\gamma c}))^2 - 2\delta \text{cov}(\varepsilon(E_{\gamma x}), \varepsilon(E_{\gamma c})) + (\delta \sigma_c)^2 + \left(\delta \frac{\varepsilon(E_{\gamma x})}{\varepsilon(E_{\gamma c})} \right)^2} \right)$$

- Without correlation we get overestimate of the uncertainty
- For sum of partial cross sections the uncertainty calculus must be used, if we use simple re-normalization than the correlation is neglected
- For calculus of decay partial gamma-ray cross sections and uncertainties related to chopper methodology please see

Szentmiklósi, L., Z. Révay and T. Belgya (2006). *Measurement of partial gamma-ray production cross-sections and k_0 factors for radionuclides with chopped-beam PGAA*, Nucl. Instr. and Methods A **564**: 655-661.

Selected recent publications

Handbook of PGAA with neutron beams (Eds. G.L. Molnár, Kluwer Academic Publisher), 2004

$^{99}\text{Tc}(n,\gamma)$:

G.L. Molnár et al., Radiochim. Acta **90** (2002) 479-482, T. Belgia et al., Proc. of the enlargement workshop on Neutron Measurements and Evaluations for Applications (Eds. A.J.M. Plompen), 5-8 Nov. 2003, Budapest, Hungary, EUR Report 21100 EN, Luxembourg, ISBN 92-894-6041-5, 2004, 2004, pp. 159-163.

$^{127,129}\text{I}(n,\gamma)$:

Belgia, T., G. L. Molnár, Z. Révay and J. Weil (2005). *Determination of thermal neutron capture cross sections using cold neutron beams*, 10th International Conference on Nuclear Data for Science and Technology, September 26 - October 1, 2004, Santa Fe, New Mexico, AIP 769, pp. 744-747

$^{238}\text{U}(n,\gamma)$:

G.L. Molnár, Zs. Révay and T. Belgia, Nucl. Instr. Methods B 213, 389 (2004)

$^{209}\text{Bi}(n,\gamma)$

Borella, A., A. Moens, P. Schillebeeckx, R. Van Bijlen, G. L. Molnár, et al. (2005). *Determination of the $^{209}\text{Bi}(n,g)$ capture cross section at a cold neutron beam*, Journal of Radioanalytical and Nuclear Chemistry **265**(2): 267-271.

Te isotopes:

I. Tomandl et al., Phys. Rev. C **68** (2003) 067602

Pb in progress

^{15}N , ^{208}Pb , ^{27}Al :

Belgia, T. (2006). *Improved accuracy of gamma-ray intensities from basic principles for the calibration reaction $^{14}\text{N}(n,g)^{15}\text{N}$* , Physical Review C **74**: 024603; Belgia, T. (2007). *New gamma-ray intensities for the $^{14}\text{N}(n,g)^{15}\text{N}$ high energy standard and its influence on PGAA and on nuclear quantities*, Journal of Radioanalytical and Nuclear Chemistry: accepted

Pd:

Firestone, R. B., M. Kritcka, D. P. McNabb, B. W. Sleaford, U. Agvaanluvsan, et al. (2005). *Thermal neutron capture cross section of the palladium isotopes*, 12nd international Conference on Capture Gamma-Ray Spectroscopy and Related Topics, September 4-9, 2005 University of Notre Dame, Indiana, USA, API, pp.

Absolute FEP efficiency

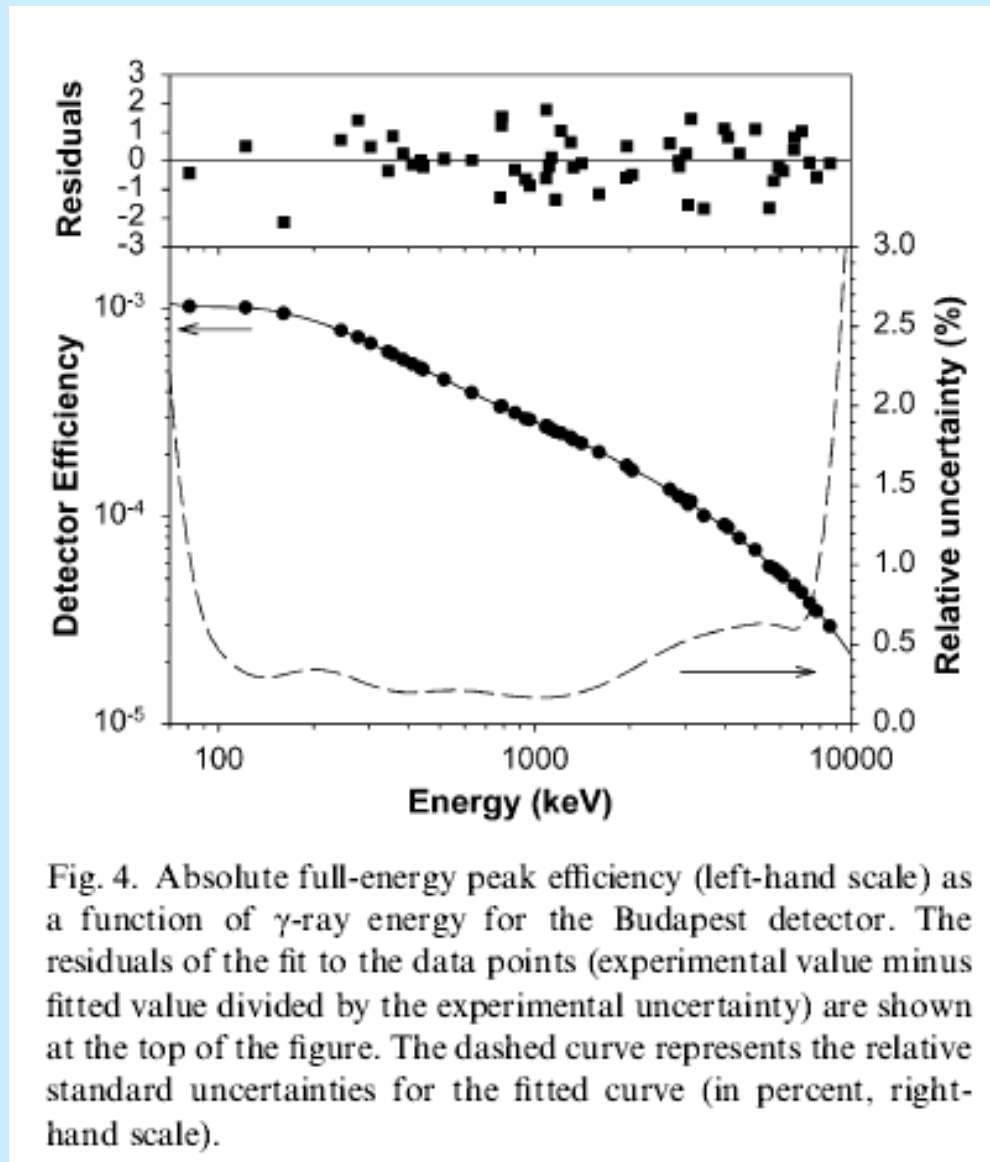
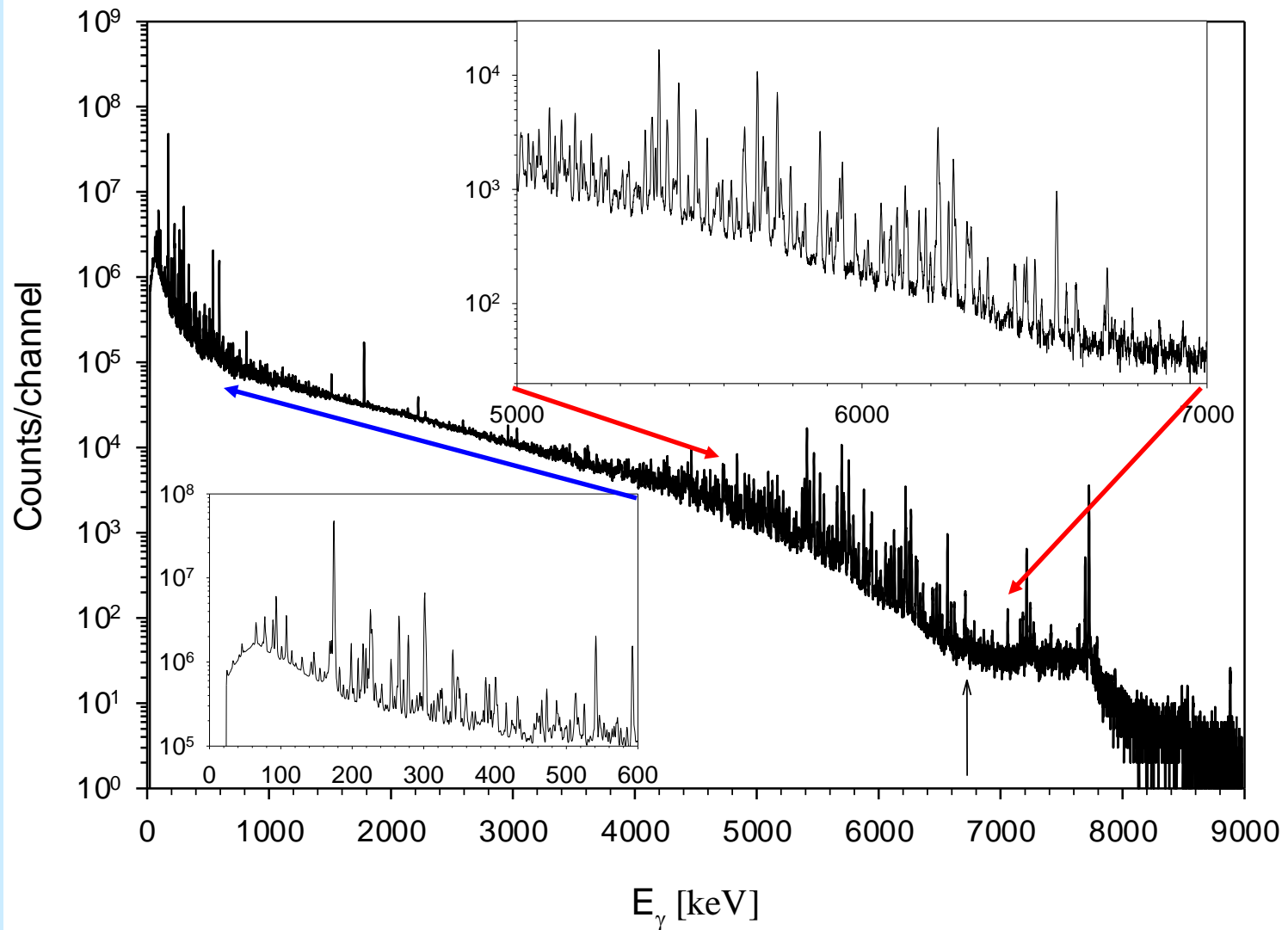


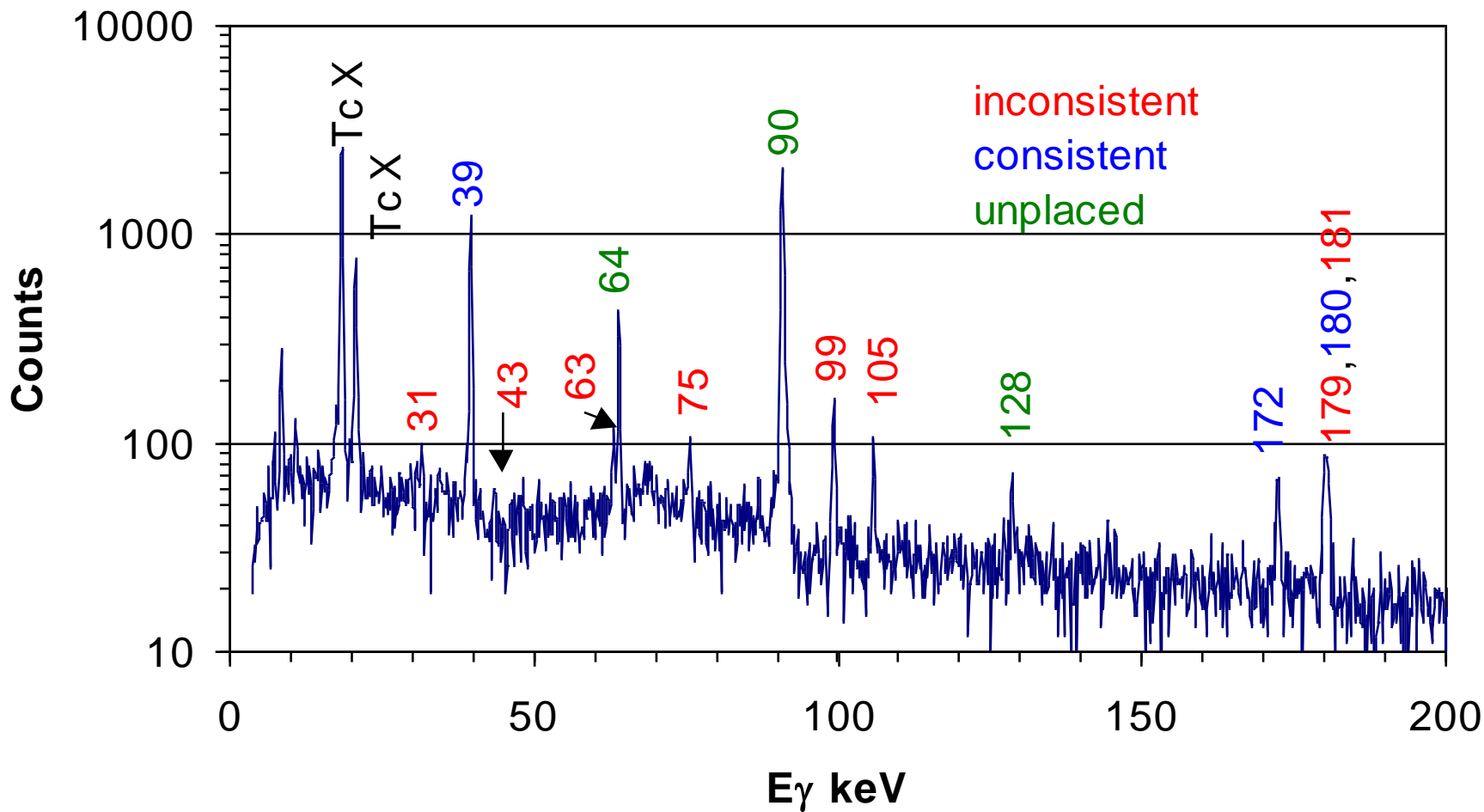
Fig. 4. Absolute full-energy peak efficiency (left-hand scale) as a function of γ -ray energy for the Budapest detector. The residuals of the fit to the data points (experimental value minus fitted value divided by the experimental uncertainty) are shown at the top of the figure. The dashed curve represents the relative standard uncertainties for the fitted curve (in percent, right-hand scale).

^{99}Tc 0.5 g sample (n, γ) spectrum



^{99}Tc (n, γ γ) prompt-coincidence spectrum

Gate on 299 keV



Partial γ -ray production cross sections of capture and decay lines for a ^{99}Tc target

E_γ (keV)	Origin	P_γ (γ /100 captures or decays)	σ_γ^a (b)	Sensitivity (cps/mg)
172.1	$^{99}\text{Tc}(n,\gamma)$	67 ± 6	16.61 ± 0.15	3.0
223.4	$^{99}\text{Tc}(n,\gamma)$	6.1 ± 0.6	1.472 ± 0.013	0.24
263.5	$^{99}\text{Tc}(n,\gamma)$	5.9 ± 0.5	1.425 ± 0.012	0.21
539.5	$^{100}\text{Tc} \beta^-$	<u>6.6 ± 0.5^b</u>	1.604 ± 0.014	0.14
590.7	$^{100}\text{Tc} \beta^-$	5.3 ± 0.5	1.296 ± 0.011	0.10
89.5	$^{99}\text{Tc} \beta^-$	$(6.5\pm 1.5)\times 10^{-4}^c$		4.3×10^{-3}

Inferred total thermal-neutron capture cross section of ^{99}Tc

Method	Basis	σ (b)	Comment
$^{100}\text{Tc}(\beta^-)^{100}\text{Ru}$	539 γ	24.7 ± 2.3	with P_γ Furutaka et al.
	591 γ	23.9 ± 1.8	
	<i>Average</i>	24.3 ± 2.2	<i>unweighted average</i>
$^{99}\text{Tc}(n,\gamma)^{100}\text{Tc}$	$\Sigma \sigma_\gamma$ g.s.	21.21 ± 0.17	lower limit

Literature: EXFOR database

H. Pomerance 1975	19 ± 2 b	pile oscillator
R.B. Tattersall 1960	16 ± 7 b	pile oscillator
N.J. Pattenden 1958	25 ± 2 b	transmission
M. Lucas 1977	20 ± 2 b	mass spectrometer
V.V. Ovechkin 1973	24 ± 4 b	activation
H. Harada 1995	22.9 ± 2.6 b	activation
Mughabgab 2003	20 ± 1	evaluation INDC(NDS)-440

Parameters of the NIPS station

- Neutron beam cross section: $2.5 \times 2.5 \text{ cm}^2$
- Thermal-equivalent flux at target: $\approx 3 \times 10^7 \cdot \text{cm}^{-2} \text{s}^{-1}$
- Vacuum in target chamber (optional): $\approx 1 \text{ mbar}$
- Form of target at room temperature: Solid, powder, liquid, gas in pressure container
- Largest target dimensions: $1.5 \times 1.5 \times 3.5 \text{ cm}^3$
- γ -ray detector No.1 n-type coax. HPGe
- Relative efficiency: 13% at 1332 keV
- FWHM: 1.8 keV at 1332 keV
- γ -ray detector No 2. n-type coax. HPGe
- Relative efficiency: 30% at 1332 keV
- FWHM: 1.9 keV at 1332 keV
- γ -ray detector No 3. Planar HPGe
- FWHM: 0.6 keV at 122 keV

Parameters of the PGAA station

- beam cross section: $\leq 2 \times 2 \text{ cm}^2$
- Thermal-equivalent flux at target: $\approx 5 \times 10^7 \text{ cm}^{-2}\text{s}^{-1}$
- Vacuum in target chamber (optional): $\approx 1 \text{ mbar}$
- Form of target at room temperature: Solid, powder, liquid, gas in pressure container
- Largest target dimensions: $4 \times 4 \times 10 \text{ cm}^3$
- γ -ray detector: n-type coax. HPGe, with BGO shield
- Distance from target to detector: 23.5 cm
- Relative efficiency: 25% at 1332 keV
- FWHM: 1.8 keV at 1332 keV
- Compton suppression enhancement: ≈ 5 (1332 keV) to ≈ 40 (7000 keV)

What's **NIPS**?

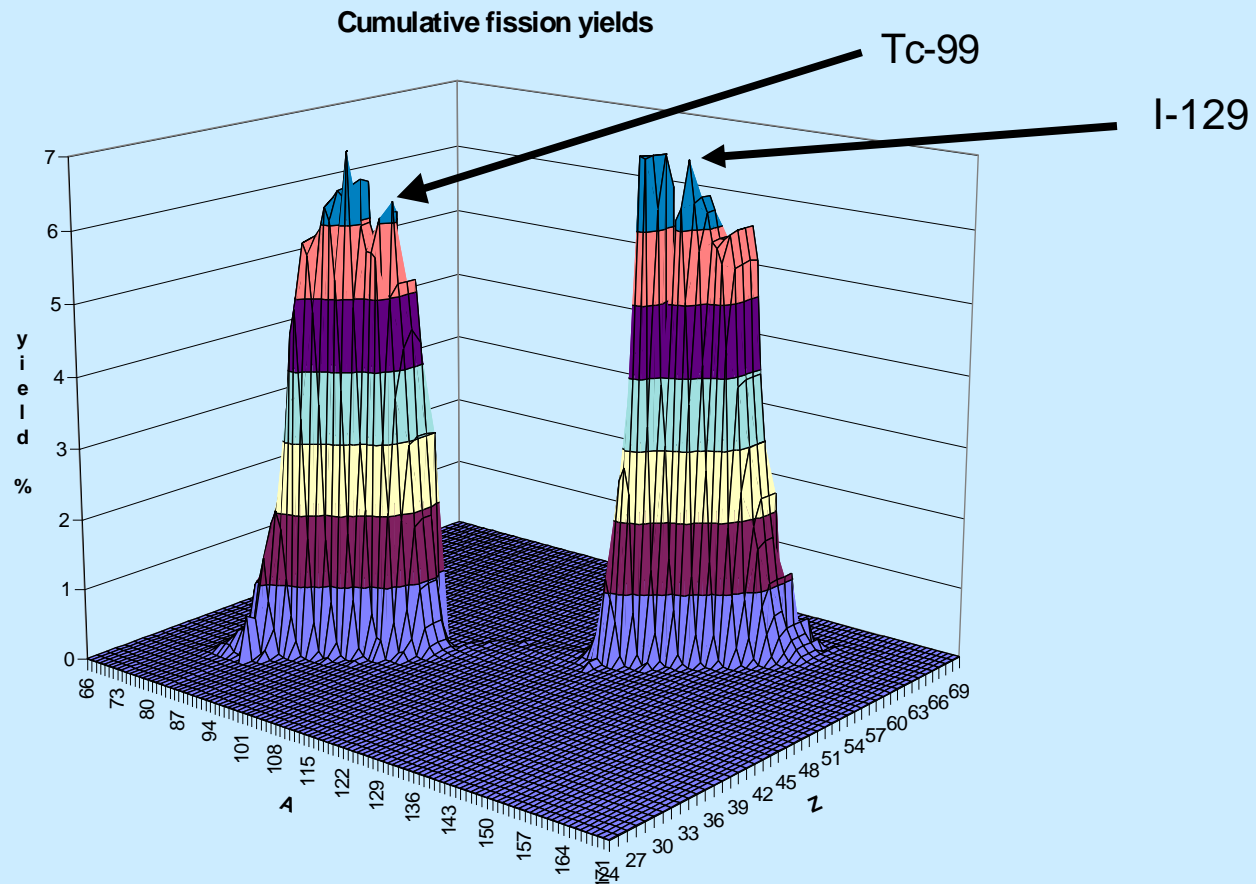
- **N**eutron **I**nduced **P**rompt gamma-ray **S**pectroscopy
- Intent: To build a multipurpose experimental station
 - Close detector geometry (2.5 cm)
 - Place for more detectors (≥ 3)
 - Good shielding (^6Li -poly)
 - Multiparameter data acquisition

Publications

- P.P. Ember, T. Belgya, G.L. Molnár, *Improvement of capabilities of PGAA by coincidence techniques*, Appl. Radiat. Isot. 56 (2002) 535
- P.P. Ember, T. Belgya, J.L. Weil, G.L. Molnár, *Coincidence measurement setup for PGAA and nuclear structure studies*, Appl. Radiat. Isot. (2002) In print
- T. Belgya, Zs. Révay, L. Szentmiklósi, M. Lakatos, J.L. Weil, *The application of a digital spectrometer in PGAA*, IRRMA-V (2002)
- T. Belgya, G.L. Molnár, *Accurate relative gamma-ray intensities from neutron capture on natural chromium*, IRRMA-V (2002)
- G.L. Molnár, T. Belgya, Zs. Révay, S.M. Qaim, *Partial and total neutron capture cross section for non-destructive assay and transmutation monitoring of ^{99}Tc* , Radiochemia Acta, submitted

The ^{99}Tc

- One of the most important LLFF
- ^{99}Tc half-life: 210 000 years
- cumulative fission yield in reactor: 6.1%
- The (n,γ) reaction can efficiently destroy the Tc waste



^{99}Tc transmutation

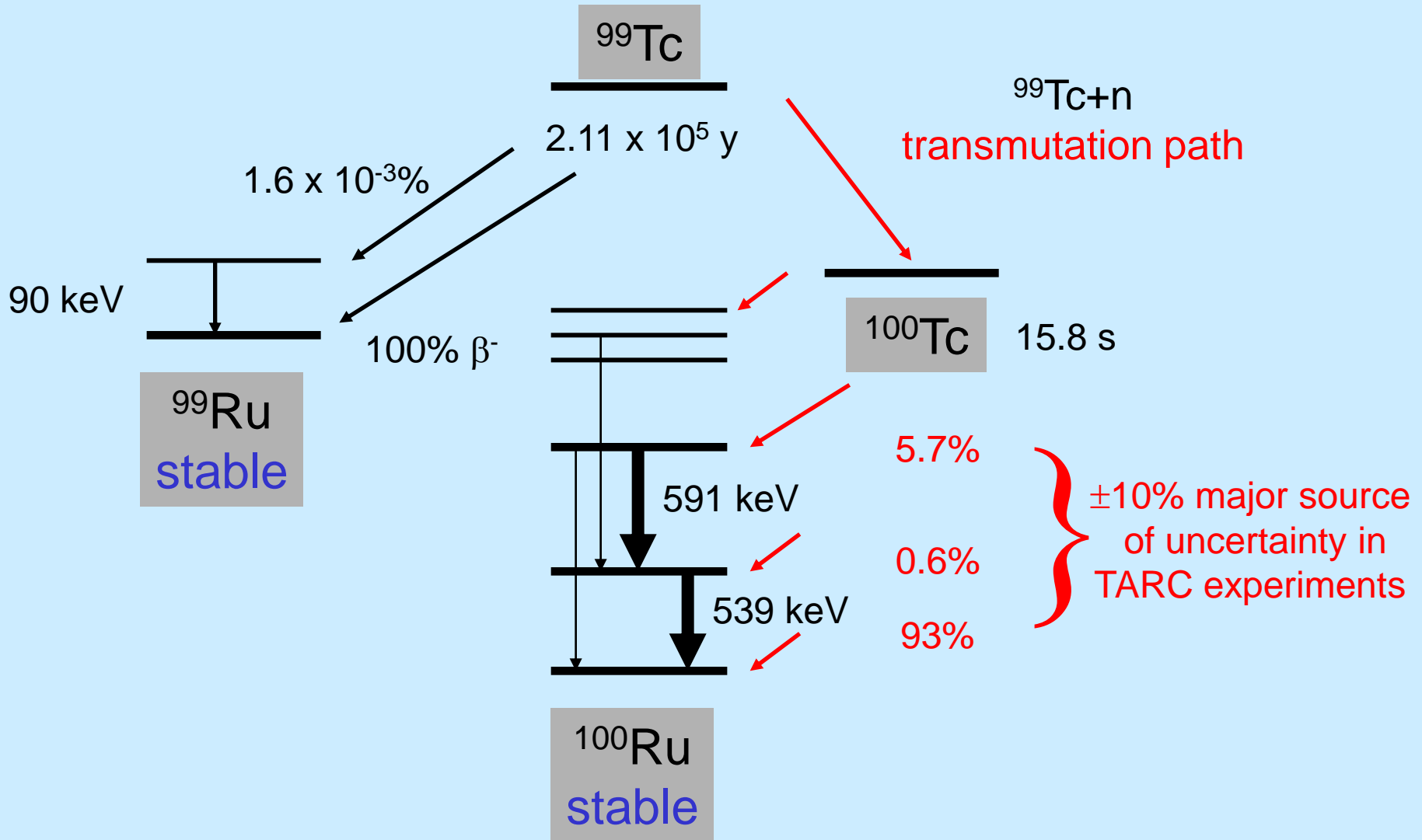
- TARC experiments at CERN to measure transmutation rates
- A. Abanades et al., Nucl. Instr. and Methods A 478 (2002) 577–730

CERN
COURIER



Carlo Rubbia's TARC (Transmutation by Adiabatic Resonance Crossing) experiment at CERN. Accelerator-driven transmutation has emerged as a potentially complementary technology for radioactive waste handling by transmuting the longest-lived radioactive isotopes into short-lived or stable ones.

Scheme of transmuted ^{99}Tc



^{99}Tc measurements at our PGAA & NIPS facilities

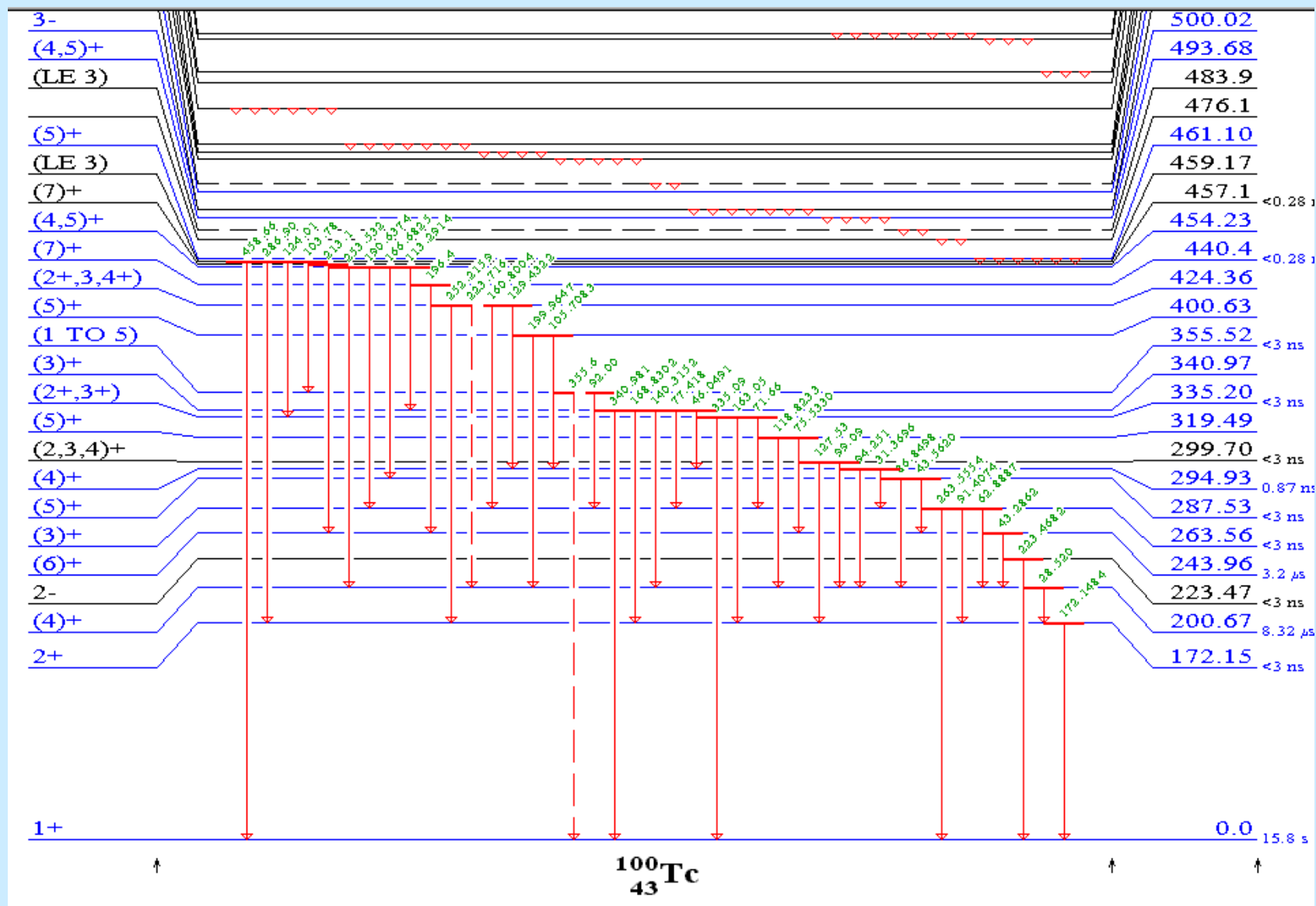
- ✓ NH_4TcO_4 PGAA (partial cross section)
- ✓ $^{99}\text{Tc}(n,\gamma)$ PGAA (rel. γ intensities)
- ✓ $^{99}\text{Tc}(n,\gamma)$ Chopped beam PGAA
(^{100}Tc β^- decay rel. γ intensities)

Evaluation is in progress:

- $^{99}\text{Tc}(n,\gamma\gamma)$ Coincidence (decay scheme)
- $^{99}\text{Tc}(d,p)^{100}\text{Tc}$ High resolution proton spectrum
(level scheme)

measured at , TU Munich

^{100}Tc levels observed in (d,p) spectrum

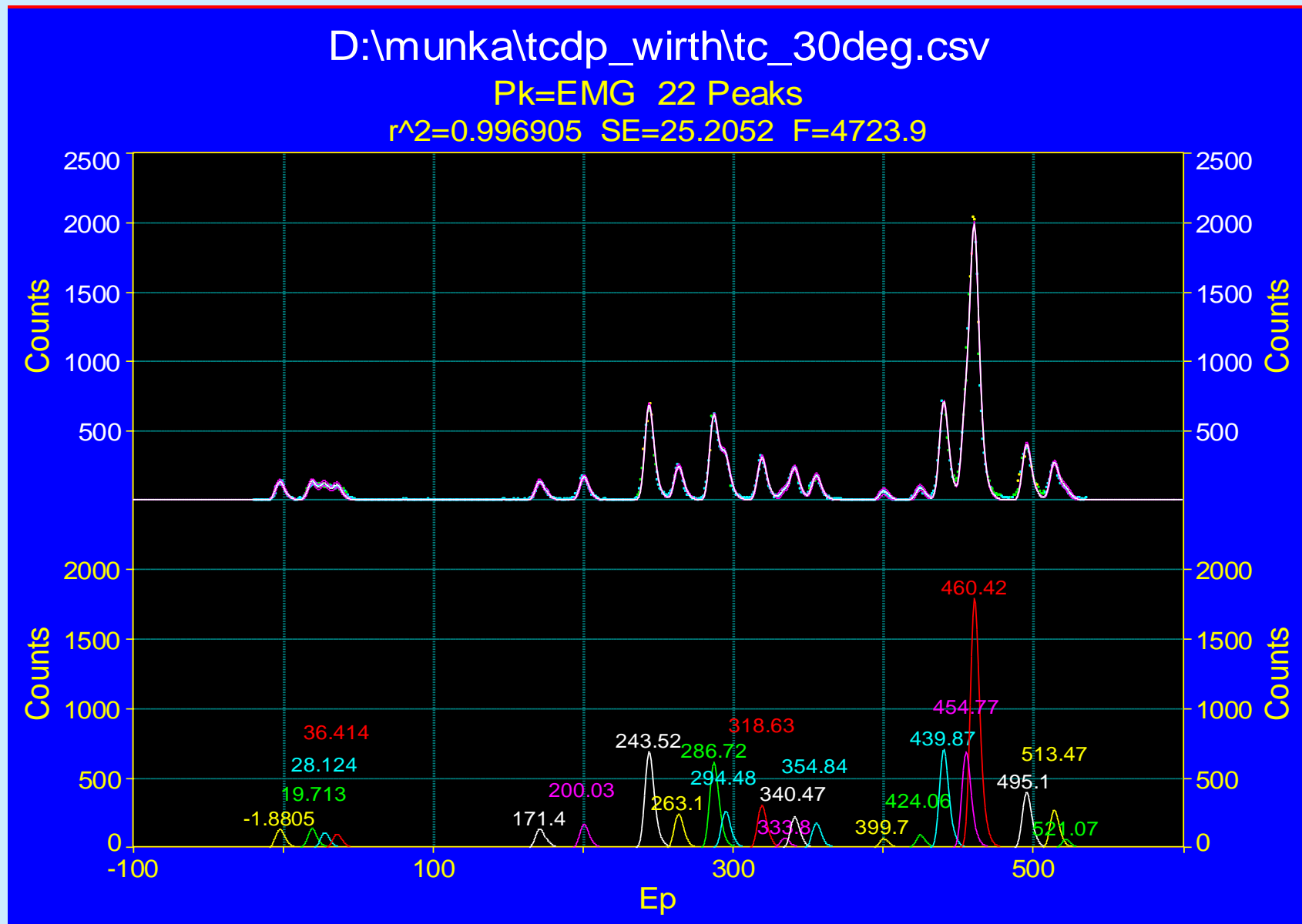


Quantities we can measure and their role in nuclear waste transmutation

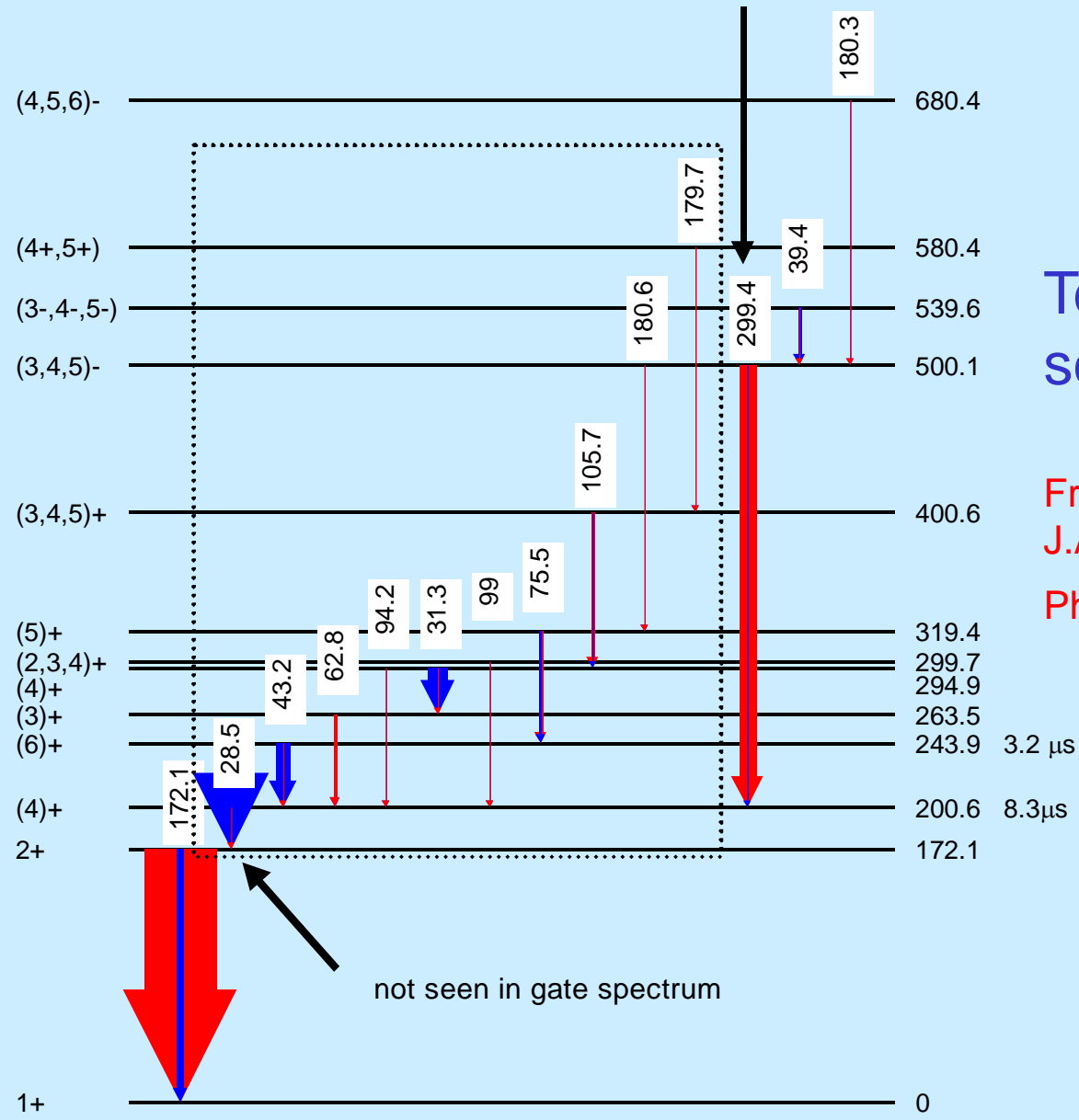
- Partial gamma-ray cross sections
 - on-line transmutation yield measurement
 - non-destructive assay of waste by PGAA
- Decay gamma-ray partial cross sections
 - on- and off-line transmutation yield measurement
- Thermal neutron capture cross sections
 - transmutation yield calculations
 - normalization point for differential cross section experiments (e.g. GELINA, Geel, Belgium, n-TOF, CERN)

Our goal is to measure these quantities with high precision

^{99}Tc (d,p) spectrum (München tandem)



gate on 299 keV



Tc(n,γ) partial Level-scheme

From ENSDF &
J.A. Pinston et al. Nucl.
Phys. **A321** (1979) 25

¹⁰⁰Tc

Why to measure nuclear waste, structural material capture cross sections?

- Waste is generated by power production
- Safe disposal → transmutation by ADS
- Problematic wastes are the Long-Lived Fission Fragments or LLFFs (^{99}Tc , ^{129}I , ...) and minor actinides
- Structural materials are parts of ADS (Bi, Pb, ...)
- For optimization of transmutation yields, control of transmutation and detection of various isotopes in waste:



Accurate γ -ray yields and thermal neutron cross sections are needed

Objectives

(n,γ) reactions

PGAA

Cross sections

Nuclear Physics

Research

- Archaeology (IAEA)
- Geology
- Catalyst
- Material sciences
- In-beam Mössbauer
- Safeguard

Methodology

- PGAA library (IAEA, LBL)
- Chopped beam PGAA
- Standards (IAEA)

Research

- Xsections for ADS
- LLFF
 - ^{99}Tc , ^{129}I (IRMM)
- Fuel
 - $^{238,235}\text{U}$, ^{232}Th
- Structural mat.
 - ^{209}Bi , $^{204,206,207}\text{Pb}$ (IRMM)

Methodology

- Internal comparator
- Chopped beam

Research

- Decay schemes
 - $^{204,206,207}\text{Pb}$ (IRMM)
 - ^{99}Tc
- Strength functions
 - ^{57}Fe (Oslo, Frank L.)
 - Mo, Yb, Gd
- Modeling Decay s.
 - ^{99}Tc

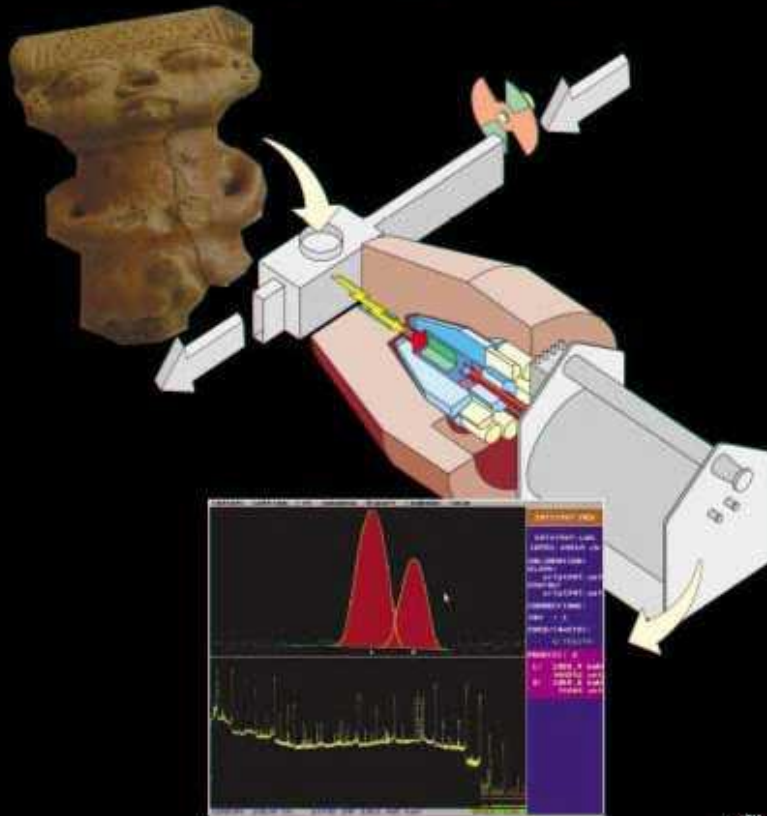
Methodology

- (n,γ), (n,γγ)
- Monte Carlo

HANDBOOK OF PROMPT GAMMA ACTIVATION ANALYSIS

WITH NEUTRON BEAMS

Edited by Gábor L. Molnár



Editor: G. L. Molnár†

- 1. Principles of the PGAA method**
(Zs. Révay, T. Belgya)
- 2. Beams and Facilities**
(R.M. Lindstrom, Zs. Révay)
- 3. Samples and Standards**
(R.M. Lindstrom, Ch. Yonezawa)
- 4. Gamma-Ray Spectrometry**
(T. Belgya, Zs. Révay)
- 5. Quantitative Analysis**
(Ch. Yonezawa)
- 6. Applications of PGAA with Neutron Beams**
(D.L. Anderson, Zs. Kasztovszky)
- 7. Appendices Reference Data**
(R.B. Firestone, G.L. Molnár, Zs. Révay)

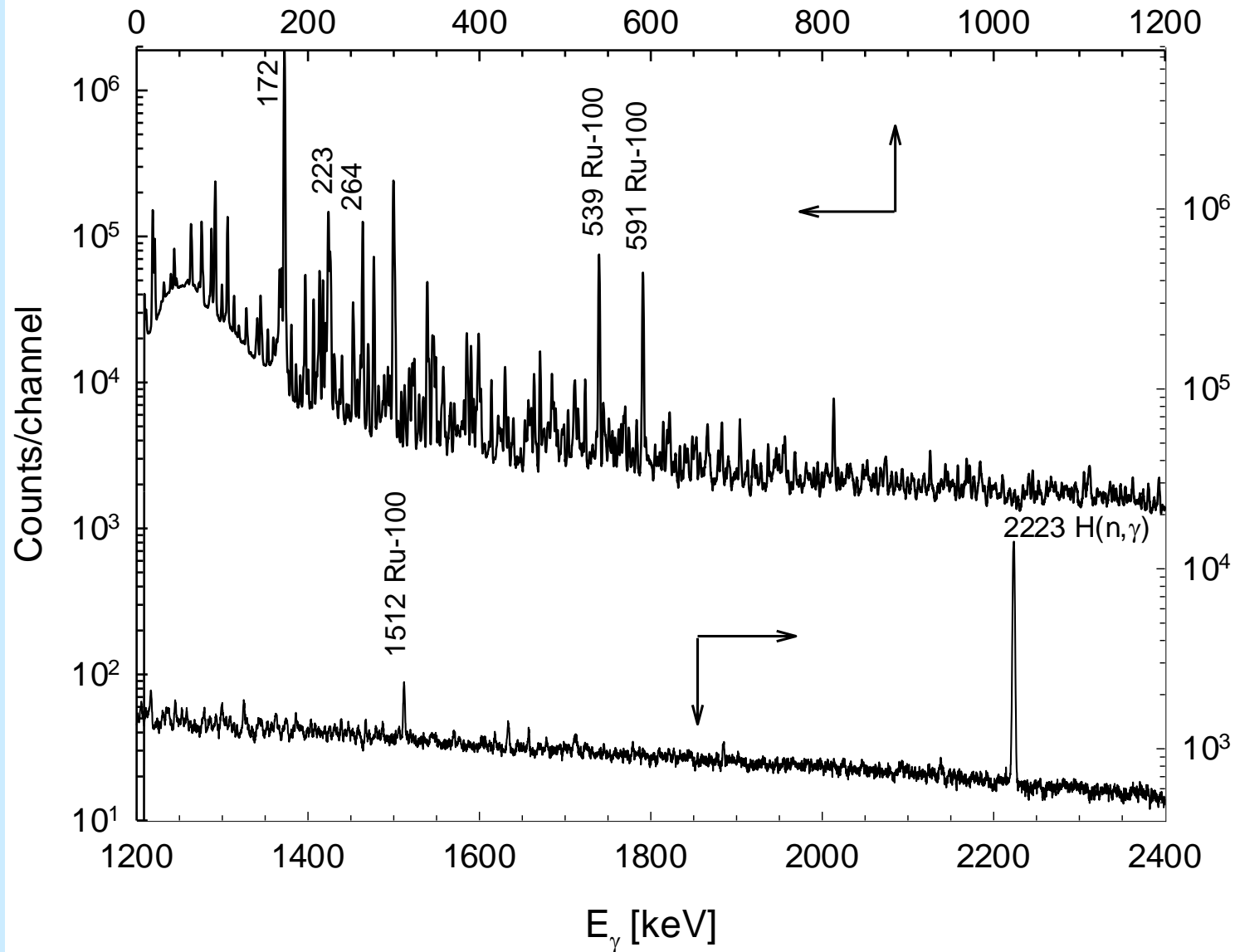
+ CD supplement

General precision 1-5% for

σ_γ



NH_4TcO_4 (n, γ) spectrum, H comparator



Precision of internal σ_γ calibration for enriched samples

$$\sigma_{\gamma X} = \sigma_{\gamma C} \frac{n_C}{n_X} \frac{A_{\gamma X}}{A_{\gamma C}} \frac{\varepsilon(E_{\gamma C})}{\varepsilon(E_{\gamma X})} \frac{f(E_{\gamma C})}{f(E_{\gamma X})}$$

①
②
③
④
⑤

Factor number	Type of error
1. Derived from primary (H) or secondary (Cl, N...) standards (table or dedicated experiment)	Systematic (~ 1%)
2. Exactly 1	0
3. Uncertainty can be decreased by time or by count rate	Statistical
4. Uncertainty can be decreased to systematic level (Most important term which can be minimized by improving standards)	Statistical + systematic, 0 at pivot ($\equiv E_{\gamma C}$) point, (~ 1%)
5. Can be measured or calculated using attenuation models (thin sample minimizes the uncertainty)	Statistical + systematic or systematic (~ 1%)