

**LHC**  
**SUPERSYMMETRY**  
**and**  
**NEW PARTICLES**

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*LHC days in Split*

*Split, 7 october 2010*

**LHC is operating**

**a great machine** (*with great physicists*)

**What can we expect or hope to discover at LHC ?**

What are the **constituents of matter** ?

What is the **origin of mass** ?

How do **weak and electromagnetic interactions differentiate** ?

Do **new states of matter** exist ?

What is the nature of **Dark Matter** ?

Are there **new forces** beyond the ones we know ?

Are there **hidden dimensions** of space-time ?

etc.

*are some of the most fundamental questions*

*about the basic laws of our Universe*

**LHC should bring us answers to some of these questions ...**

*starting point:*

## STANDARD MODEL

**strong, electromagnetic and weak interactions** of **quarks and leptons**

$$SU(3) \times SU(2) \times U(1)$$

**spin-1** gauge bosons: **gluons,  $W^+$ ,  $W^-$ ,  $Z$ , photon**

**spin- $\frac{1}{2}$**  fermions: **quarks, leptons**

+ **1** (still unobserved) spin-0 **Brout-Englert-Higgs-... boson**

*associated with* **spontaneous electroweak symmetry breaking**

– remarkably successful

– *but leaves many questions unanswered:* (a long list ...)

- What about fundamental Higgs-... fields ?

( do they actually exist ? )

*We heard talks about Higgs physics*

*We are confident that*

**LHC should elucidate the mechanism  
by which weak and electromagnetic interactions differentiate,  
and quarks and leptons acquire masses**

presumably (?) through the expected discovery of one (or several) **Higgs boson(s)**

**or possibly through some other mechanism.**

*Even if Higgs bosons are discovered we still have questions ...:*

- **why a potential**

$$V(\varphi) = \lambda |\varphi|^4 - \mu^2 |\varphi|^2 \quad ?$$

*what determines the Higgs boson mass ? (  $m_H = \mu \sqrt{2} = v \sqrt{2\lambda} \dots$  )*

what fixes

$\mu$  ?

what fixes coupling constant

$\lambda$  ?

*is B-E-Higgs ... sector as in SM, **or more complicated** ... ?*

- do **new particles** exist ? maybe also **new forces** ?

*after LEP, we think we know all (sequential) quarks and leptons*

growing evidence for **non-baryonic DARK MATTER**

**What is dark matter made of ??**

## Other interrogations :

- **role of gravity** (related to **spacetime** through general relativity)

can it be more closely **connected with particle physics** ?

a consistent theory of **quantum gravity** ?

question of cosmological constant  $\Lambda$  ...

- **can interactions be unified?** approach of **grand-unification** :

$SU(3) \times SU(2) \times U(1) \subset$  e.g.  $SU(5)$ , ...

$$\left\{ \begin{array}{l} \text{gluons} \longleftrightarrow W^\pm, Z, \gamma \quad (+ \text{ other gauge bosons e.g. } X^{\pm 4/3}, Y^{\pm 1/3}, \dots) \\ \text{quarks} \longleftrightarrow \text{leptons} \end{array} \right.$$

**with its own questions:** *Higgs potential and symmetry breaking, origin of hierarchy of mass scales, many coupling constants, relations between  $q$  and  $l$  masses ...*

- can one **relate particles of different spins** ? approach of **supersymmetry**  $\rightarrow$

...



*a “new” tool,*

## **SUPERSYMMETRY**

**BOSONS**  $\longleftrightarrow$  **FERMIONS**

*(integer spins)*

*(half-integer spins)*

*what can we do with it ?*

**can it be of any help in the real world  
of fundamental particles and interactions ?**



*This would be very attractive !*

*but unfortunately*

*things don't work out that way !! ...*

## SUSY ALGEBRA :

$$\begin{cases} \{ Q, \bar{Q} \} = -2 \gamma_\mu P^\mu \\ [ Q, P^\mu ] = 0 \end{cases}$$

*Gol'fand-Likhtman, Volkov-Akulov, Wess-Zumino, 1970-73*

$P^\mu \rightarrow$  space-time translations

## Fundamental connection of supersymmetry with SPACE-TIME

$\rightarrow$  relation with general relativity, *gravitation*  $\rightarrow$  supergravity

spacetime  $x^\mu = \begin{pmatrix} ct \\ \vec{x} \end{pmatrix}$  extended to **superspace**  $(x^\mu, \theta)$

$\theta = \begin{pmatrix} \theta_1 \\ \theta_2 \\ \theta_3 \\ \theta_4 \end{pmatrix} =$  spin- $\frac{1}{2}$  Majorana **anticommuting coordinate**

$$\theta_1 \theta_2 = -\theta_2 \theta_1, \quad (\theta_1)^2 = 0 \dots$$

**SUPERFIELDS**  $\Phi(x, \theta)$  describe both **BOSONS** and **FERMIONS**

*Extension of space-time to include*  
**new fermionic coordinates (or bosonic ones)**



**SUPERSPACE**  
 $(x^\mu, \theta) \dots$

**EXTRA DIMENSIONS**  
 $(x^\mu, x^5, x^6) \dots$

*furthermore:*

*extended supersymmetric theories are naturally formulated  
using extra (compact) space dimensions*

**( $N = 2$  SUSY obtained from 5 or 6 dimensions,  $N = 4$  SUSY from 10 dimensions)**

*we shall concentrate on simple ( $N = 1$ ) supersymmetry*

*well, but ...*

*Can SUSY apply to fundamental laws of Nature ?*

*( what would this imply ... ? )*

*Nature is “obviously” not supersymmetric !*

*it seems*

**1 Bosons and fermions should have EQUAL MASSES :**

*this is not the case*

*→ break (spontaneously (?)) susy ??*

**But: spontaneous susy breaking did not seem possible !**

*( SUSY vacuum has  $E = 0$ , always stable ... )*

**still it turns out possible, but very constrained**

*( → easier to use soft susy-breaking terms:*

*price to pay : many arbitrary parameters,*

*in the absence of a better understanding of the susy-breaking mechanism ... )*

2 Spontaneous SUSY breaking → **spin- $\frac{1}{2}$  Goldstone fermion**

*it cannot be a neutrino, why has not it been observed ?*

*we think we know the answer:*

**it is eliminated in favor of**

→

**massive spin- $\frac{3}{2}$  GRAVITINO**

**which should normally have extremely small interactions with matter**

**and not be directly observable ...**



**(but there is a caveat, with the possibility of an observable gravitino ...)**

*the gravitino, if very light, may still behave very much as a  $\text{spin-}\frac{1}{2}$  goldstino ... !!*

*(with effective coupling  $\propto \kappa \sqrt{\frac{2}{3}} \frac{k^\mu}{m_{3/2}}$ ) which could be **observable** ... ! depending on  $m_{3/2}$*

*e.g. through decays of SUSY particles, like*

**neutralino  $\rightarrow$  gravitino + photon**

**gravitino “lightest susy particle”, stable ...**

*limits on such processes, since PETRA experiments in the 80's ...*

**One possible SUSY signature, that should be searched for at LHC ...**

*interactions of the gravitino much weaker than weak interactions*

*decouples much before neutrinos, during evolution of Universe*

**a possible DM candidate**

*main question, if susy is to be applicable to the real world :*

- **Which bosons and fermions relate ?**

$$\left\{ \begin{array}{l} \textit{photon} \quad \overset{?}{\longleftrightarrow} \quad \textit{neutrino} \\ W^{\pm} \quad \overset{?}{\longleftrightarrow} \quad e^{\pm} \\ \textit{gluons} \quad \overset{?}{\longleftrightarrow} \quad \textit{quarks} \\ \dots \end{array} \right.$$

*does not work ...*

**and also:**

- **How to deal with Majorana fermions ?**

*SUSY theories involve (self-conjugate) Majorana fermions*

*Nature only knows Dirac fermions !*

- **How to construct Dirac fermions ?**

*carrying conserved quantum numbers ( $B$  and  $L$ )*

## How to give fermions

conserved quantum numbers ( $B, L$ ) ?

$B$  and  $L$  carried by fermions only (*quarks and leptons*), not bosons !

*this cannot be, in a supersymmetric theory ... !!*

*problems, problems, problems ... !*

*Now, solutions:*

1) accept **Majorana fermions** → **new class of particles:**

photon not associated with  $\nu_e$ ,  $\nu_\mu$  or  $\nu_\tau$

but with new “*photonic neutrino*” called **PHOTINO**

and gluons with **GLUINOS** ...

Majorana fermions of SUSY → **NEUTRALINOS, GLUINOS ...**

2) introduce **new BOSONS** carrying baryon and lepton numbers

**SQUARKS, SLEPTONS**

⇒ all particles get associated with new superpartners

<i>photon</i>	↔	spin- $\frac{1}{2}$	<i>photino</i>
<i>gluons</i>	↔	spin- $\frac{1}{2}$	<i>gluinos</i>
<i>leptons</i>	↔	spin-0	<i>sleptons</i>
<i>quarks</i>	↔	spin-0	<i>squarks</i>
		...	

→

“doubling the number of degrees of freedom” in susy theories

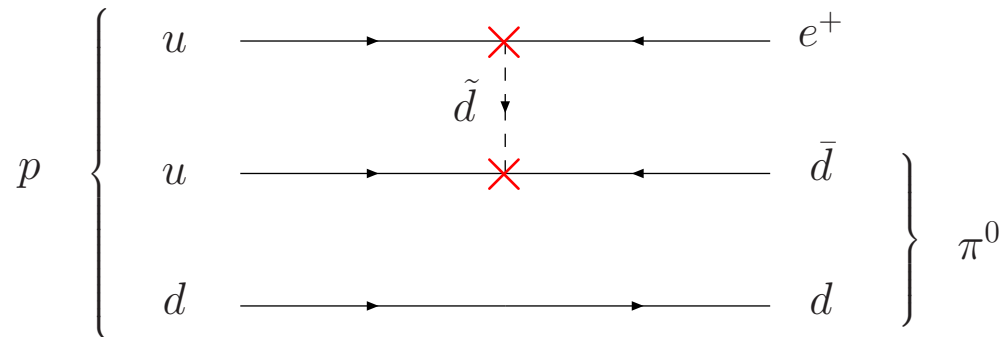
<b>Known bosons</b>	↔	<b>New fermions</b>
<b>Known fermions</b>	↔	<b>New bosons</b>

*(this was long mocked as a sign of irrelevance of supersymmetry !)*

still a problem: get interactions from  $W^\pm$ ,  $Z$ , photon and gluon exchanges

**avoid unwanted spin-0 exchanges ?**

(  $\tilde{q}, \tilde{l}$  carrying  $B$  and  $L$  )



proton decay that might be induced by  $\tilde{d}$  squark exchange

this exchange is forbidden by  **$R$ -parity**

## ***R*-PARITY**

*initial continuous  $U(1)_R$  symmetry acts chirally on SUSY generator*

*but it would require the **gluinos** and **photino** to be **massless** ...*

**$U(1)_R$  broken (by gravitino and gluino mass terms ...) to  $R_p$**

$$R_p = \begin{cases} +1 & : \text{ordinary particles} \\ -1 & : \text{superpartners} \end{cases}$$

***R-parity*** then identified as  $(-1)^{2S} (-1)^{3B+L}$

→ *pair production of SUSY particles*

→ *lightest SUSY particle stable*

→ **stable dark matter candidate**

*also:*

**gluinos and other gaugino masses may be naturally  $\approx$  gravitino mass  $m_{3/2}$**

**$R$ -parity  $\Rightarrow$  LSP stable**

candidate for non-baryonic **dark matter** of Universe

usually a **neutralino**

combination of superpartners of neutral gauge and Higgs bosons,

$$\{W_3, W'; h_1^\circ, h_2^\circ; \dots\} \xleftrightarrow{SUSY} \underbrace{\{\tilde{W}_3, \tilde{W}'; \tilde{h}_1^\circ, \tilde{h}_2^\circ; \dots\}}_{\text{neutralinos}}.$$

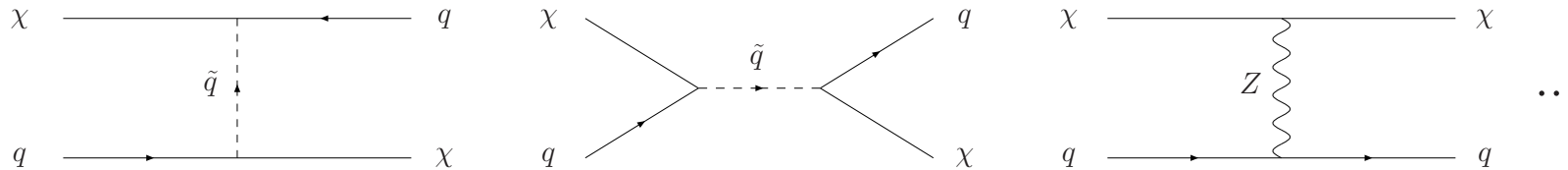
relation of **dark matter** with **gauge** ( $\gamma, Z, \dots$ ) and **Higgs bosons**



*Relic density of dark matter particles*

*evaluated from annihilation cross-sections at freeze-out time*

with  $\sigma_{ann} \approx$  **weak cross sections** from **squark, slepton, Z or Higgs** exchanges



*interactions of dark matter with quarks*

*(annihilation processes of dm particles are similar)*

**neutralino = natural WIMP candidate**

*precise relic density of neutralinos depends on the details of mass spectrum*

**No SUSY relation between known particles and forces ...**

*but ...*

**DARK MATTER candidate naturally obtained  
from lightest Majorana fermion (**neutralino**)  
in SUSY extension of Standard Model**

→

**DARK MATTER related with  
mediators of ELECTROWEAK INTERACTIONS**

**DARK MATTER ↔ FORCES**

## Producing DARK MATTER at particle colliders

**pair-production of neutralinos** (*or other DM candidates*)

stable from *R*-parity (*or similar conservation law*)

Missing energy -momentum signature of SUSY ...

(1977)

*neutralinos interact  $\sim$  weakly with matter through  $\tilde{q}$  etc. exchanges*

*lightest neutralino became natural DM candidate*

$$e^+ e^- \rightarrow \dots \rightarrow \mathbf{2 \text{ neutralinos}} + \dots$$

$$p \ p \rightarrow \textit{pair-production of } \tilde{q} \textit{ or } \tilde{g} \rightarrow \mathbf{2 \text{ neutralinos}} + \dots$$

or e.g., for unstable neutralinos (N)LSP decaying e.g. into (photon + gravitino):

$$\left\{ \begin{array}{l} e^+ e^- \rightarrow 2 \text{ neutralinos} + \dots \rightarrow \gamma \gamma + 2 \text{ gravitinos} + \dots \\ p p \rightarrow 2 \text{ neutralinos} + \dots \rightarrow \gamma \gamma + 2 \text{ gravitinos} + \dots \end{array} \right.$$

**Accelerators can look for the Dark Matter of the Universe ...**

( ... , *PETRA*, *PEP*, *LEP*) *FNAL*, **LHC**, *ILC*, ...

About Higgs-. bosons ...

we need a pair of doublet Higgs superfields,

3 reasons:  $\left\{ \begin{array}{l} \text{avoid massless chiral chargino} \\ H_1 \text{ gives masses to } d \text{ and } e, H_2 \text{ to } u \\ \text{cancel anomalies} \end{array} \right.$

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}, \quad (\text{left-handed})$$

$$\text{mixing angle } \beta, \quad \tan \beta = \frac{v_2}{v_1}.$$

Charged Higgs bosons  $H^\pm$

+ 3 neutral ones  $H, h, A$  + maybe others ...

Ingredients of **Supersymmetric Standard Model** (*minimal or not ...*)

1)  $SU(3) \times SU(2) \times U(1)$  gauge superfields

[ $\times$  extra- $U(1)$ ]

2) chiral quark and lepton superfields

3) **two** doublet Higgs superfields  $H_1$  and  $H_2$

4) trilinear superpotential for  $q$  and  $l$  masses

• Superpotential even function of quark and lepton superfields !

$$h_e H_1 \cdot \bar{E} L + h_d H_1 \cdot \bar{D} Q - h_u H_2 \cdot \bar{U} Q \quad [ + \mu H_1 H_2 ]$$

$R$ -invariance  $\rightarrow$   $R$ -parity

*Minimal content of*  
**Supersymmetric Standard Model**

Spin 1	Spin 1/2	Spin 0
gluons $g$ photon $\gamma$	gluinos $\tilde{g}$ photino $\tilde{\gamma}$	
<hr style="width: 100%;"/> $W^\pm$ $Z$	<hr style="width: 100%;"/> winos $\tilde{W}_{1,2}^\pm$ zinos $\tilde{Z}_{1,2}$  higgsino $\tilde{h}^0$	<hr style="width: 100%;"/> $H^\pm$ $H$ $h, A$
	leptons $l$ quarks $q$	$\left. \begin{array}{l} H^\pm \\ H \\ h, A \end{array} \right\} \text{Higgs bosons}$  sleptons $\tilde{l}$ squarks $\tilde{q}$

2 neutral gauginos + 2 higgsinos mix  $\rightarrow$  **4 neutralinos**

“MSSM”

**Nice features of Higgs interactions** *in supersymmetric theories*

*(and not so nice ones ... )*



*SUSY quartic Higgs interactions*

appear as **electroweak gauge interactions**, with

$$V_{\text{quartic}} = \frac{g^2 + g'^2}{8} (h_1^\dagger h_1 - h_2^\dagger h_2)^2 + \frac{g^2}{2} |h_1^\dagger h_2|^2$$

= **quartic Higgs potential of the MSSM**

**Quartic couplings fixed by electroweak gauge couplings !**

→

$$m \text{ (lightest Higgs)} \leq m_Z + \underbrace{\text{rad. corr.}}_{\text{should be large !!}} \text{ in MSSM}$$

*(potentially problematic, as it requires radiative correction effects to be large)*

*(requires **squark masses**  $\approx$  TeV scale, recreates (“little”) hierarchy problem ...)*

→ **“Beyond MSSM”**

introduce **EXTRA SINGLET  $S$**  (1975)

*$\mu$  parameter of MSSM promoted to dynamical variable  $\mu(x, \theta) = \lambda S(x, \theta)$*

*(cf. electron mass  $m_e \rightarrow \lambda_e \varphi(x)$  in SM)*

$$\mu H_1 H_2 \rightarrow \lambda H_1 H_2 S$$

$\lambda \langle S \rangle$  can recreate effective  $\mu \dots$

→  $\mu H_1 H_2 + \lambda H_1 H_2 S + f(S)$  superpotential

**N/nMSSM**

with  $f(S) = \frac{\kappa}{3} S^3 + \frac{\mu_S}{2} S^2 + \sigma S$

tends to be required to make all Higgs bosons sufficiently heavy  
*without relying too much on large radiative corrections*

### Potential of N/nMSSM:

$$V = \frac{g^2 + g'^2}{8} (h_1^\dagger h_1 - h_2^\dagger h_2)^2 + \frac{g^2}{2} |h_1^\dagger h_2|^2$$
$$+ \left| \lambda h_1 h_2 + \frac{\partial f(s)}{\partial s} \right|^2 + \lambda^2 |s|^2 (h_1^\dagger h_1 + h_2^\dagger h_2) + \dots$$

$\lambda$  allows to get

**all Higgs bosons sufficiently heavy**

→ **additional singlino**

## EXTRA- $U(1)$

*supersymmetric extensions of the SM*

**gauge extra- $U(1)$  symmetry ...**  $\rightarrow$  (“USSM”)

$\rightarrow$  **additional gaugino**

*where is such an extra  $U(1)$  coming from ?*

*various possibilities, among which  $U(1)$ 's from groups like  
 $SU(3) \times SU(2)_L \times SU(2)_R \times U(1)$  or  $O(10)$  or  $E(6)$  GUT groups*

in SUSY extensions of the standard model

$$h_1 = \begin{pmatrix} h_1^{\circ} \\ h_1^{-} \end{pmatrix}, \quad h_2 = \begin{pmatrix} h_2^{+} \\ h_2^{\circ} \end{pmatrix}$$

possibility of rotating independently the two doublets

$$h_1 \rightarrow e^{i\alpha} h_1, \quad h_2 \rightarrow e^{i\alpha} h_2$$

→ extra-  $U(1)$

*acts axially on quarks and leptons ( + possible vector coupling)*

**(global)** or **local** → new gauge boson  $Z'$  or  $U$

**broken explicitly** by (small) superpotential terms and/or (small) soft susy-breaking terms

or **spontaneously** through the *2 Higgs doublets* and possibly a large *singlet v.e.v.*

# LIGHT DARK MATTER

with C. Boehm

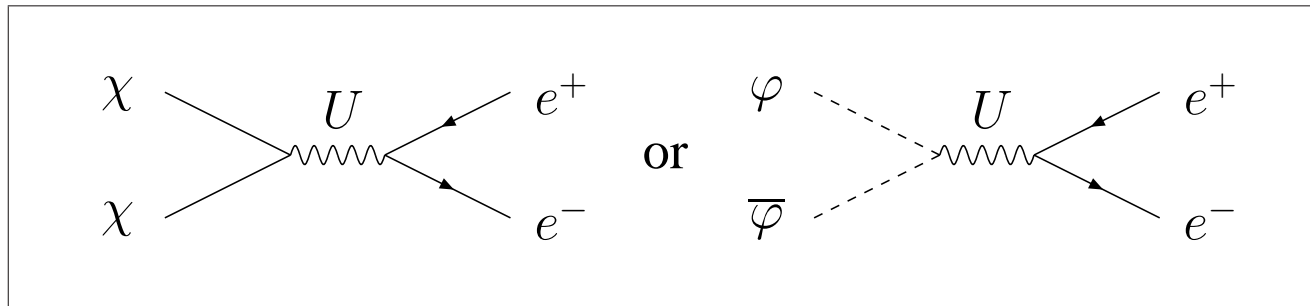
( a few words )

Too *light dark matter particles* (say in MeV to GeV range) normally forbidden  
as they could not annihilate sufficiently  $\rightarrow$  relic abundance too large ...

unless *a new interaction* exists

as induced by a new light spin-1 **U boson**

sufficiently strong at lower energies,



DM annihilations into  $e^+e^-$ , for spin- $\frac{1}{2}$  or spin-0 particles

*extra-U(1) symmetry ...*

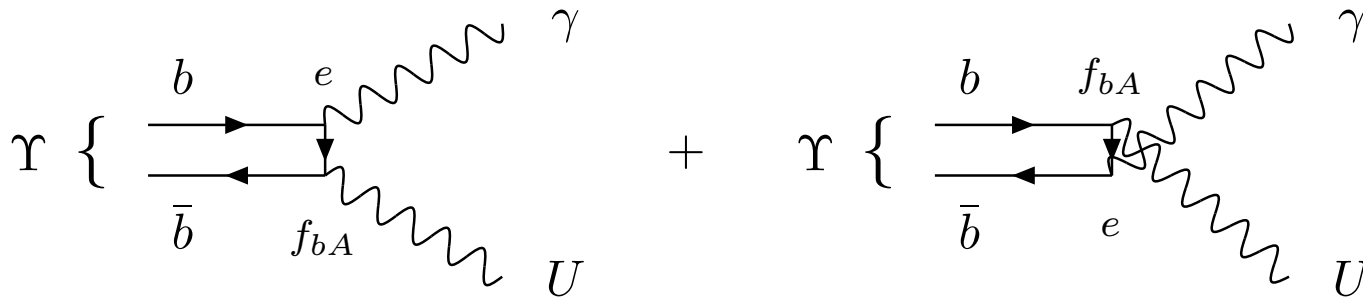
how a light **U** could be detected ?

# SEARCHING FOR A LIGHT $U$

*in particle physics experiments*

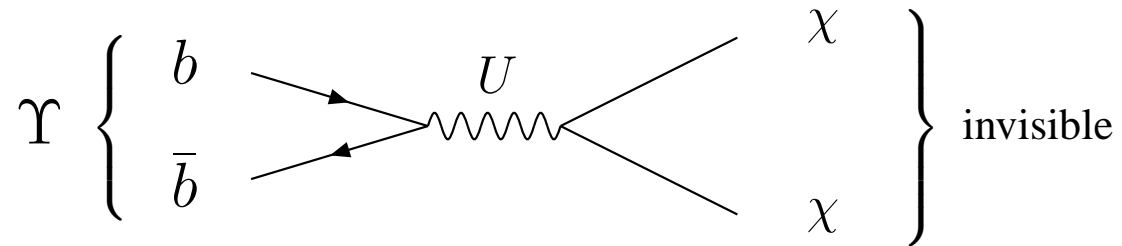
for example in  $\psi$  and  $\Upsilon$  DECAYS:

$$\Upsilon \rightarrow \gamma U$$



## Dark Matter at accelerators

*waiting for LHC results, we already have information from other experiments*



***Invisible  $\Upsilon$  decay into light dark matter particles***

$$\Upsilon \rightarrow \underbrace{\chi\chi}_{\text{inv}} < 3 \cdot 10^{-4} \text{ (Babar)} \Rightarrow$$

$$|e_\chi f_{bV}| < 5 \cdot 10^{-3}$$



## Searches for EXTRA SPACE DIMENSIONS

expect **series of heavy copies of ordinary particles**

(“KK excitations”)

expect new stable particles (presumably neutral, but might also be charged ...)

$$\text{masses} \approx \frac{\hbar}{L c} \quad L = \text{compactification scale}$$

*CHAMPs* → *superheavy stable isotopes of hydrogen ... ?*

**new Dark Matter candidates**

(e.g. lightest excitation of photon or weak-hypercharge gauge boson,  
or associated scalars ...)

**what is the compactification scale (s) ?**

$\sim m_{\text{GUT}} ? \quad \sim m_{\text{Planck}} ? \quad \sim \text{TeV} ?$

**also, stay attentive to unconventional scenarios**

**possibility of**

**UNEXPECTED DISCOVERIES ...**

## CONCLUSIONS

with **LHC** we expect to elucidate the mechanism responsible for  
**EW symmetry breaking + mass generation**  
*presumably (?) through the discovery of **spin-0 (Higgs-..) bosons***

we hope to elucidate the nature of Dark Matter through pair-production of  
**new particles, decaying into stable DM particles**  
*more specifically*

we hope to discover **SUPERSYMMETRY** through pair-production of  
**Superpartners = SUSY particles**

the lightest, usually a **neutralino** (or ...)  
stable from ***R*-parity** and  $\sim$  “**weakly-interacting**”  
being a natural Dark Matter candidate

*(provided SUSY particles are not too heavy,  $\lesssim$  TeV scale, as usually expected)*

*expected Higgs sector:*

**2 doublets + possible singlet**  
with  $\lambda H_1 H_2 S$  trilinear coupling

**singlet welcome** (*possibly required*) to make Higgs bosons sufficiently heavy

*MSSM* already very tightly (*too tightly* ?) constrained ....  $\rightarrow$  *N/nMSSM*, *USSM*, ...

**if superpartners too heavy, SUSY might also show up indirectly**  
through its characteristic Higgs sector

search for new gauge bosons  $Z'$ ,  $W_R$ , ...

and possible signs of **extra dimensions** ...

(*especially if responsible for susy-breaking*  
*through boundary conditions involving  $R$ -parity*)

(+ *possibility of light weakly (or very weakly) coupled particles*)

***NEW PARTICLES, NEW FORCES, NEW (super) SPACETIME DIMENSIONS ...***