# Determining the Nuclear Gluon Distribution in UPCs 

R. Vogt<br>Nuclear Science Division, LBNL, Berkeley, CA, USA Physics Department, University of California, Davis, CA, USA

- Heavy Quark Photoproduction-Direct and Resolved
- Dijet Photoproduction-Direct


## Photoproduction Comes For Free in Heavy Ion Collisions

- Strong electromagnetic fields surround accelerated nuclei
- Photon from field of one nucleus interacts with gluon from periphery of opposite nucleus
- Photons almost real, virtuality $q^{2}<\left(\hbar c / R_{A}\right)^{2}$, small
- These photons can interact themselves (direct) or fluctuate into states with multiple $q \bar{q}$ pairs and gluons (resolved)
- Grazing collisions with rapidity gap could be clean signal for photoproduction measurements


## Kinematics

Photon beam is not monotonic but a continuum up to

$$
E_{\text {beam }}=\gamma_{L} m_{p}
$$

Relate photon 4-momentum to $x_{1}$ as in hadroproduction,

$$
k=x_{1} \gamma_{L} m_{p}
$$

$x_{1}$ and $x_{2}$ depend on the $p_{T}$ and $y$ of the produced quarks

$$
x_{2}=\left(m_{T} / \sqrt{S}\right)\left(e^{y_{1}}+e^{y_{2}}\right) \quad x_{1}=\left(m_{T} / \sqrt{S}\right)\left(e^{-y_{1}}+e^{-y_{2}}\right)
$$

Photon flux suppressed for $k_{\max }=\gamma_{L} \hbar c / R_{A}$ in the center of mass frame, and $E_{\text {cut }}=\left(2 \gamma_{L}^{2}-1\right) \hbar c / R_{A}$ in lab frame
Maximum possible $\gamma-N$ center-of-mass energy, $\sqrt{S_{\gamma N}}$, less than $\sqrt{S}$ in corresponding $N N$ collisions

$$
\sqrt{S_{\gamma N}}=2 \sqrt{k_{\max } E_{\text {beam }}}=m_{p}^{2}+2 m_{p} E_{\text {cut }}
$$

## Some Numbers

| $A$ | $E_{\text {beam }}(\mathrm{GeV})$ | $\gamma_{L}$ | $k_{\max }(\mathrm{GeV})$ | $E_{\text {cut }}(\mathrm{TeV})$ | $\sqrt{S_{\gamma N}}(\mathrm{GeV})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| O | 125 | 133 | 8.7 | 2.31 | 66 |
| RHIC |  |  |  |  |  |
| Si | 125 | 133 | 7.2 | 1.92 | 60 |
| I | 104 | 111 | 3.6 | 0.81 | 39 |
| Au | 100 | 106 | 3.0 | 0.66 | 35 |
| O | 3500 | 3730 | AA LHC |  |  |
| Ar | 3150 | 3360 | 185.3 | 1820 | 1850 |
| Pb | 2750 | 2930 | 87 | 1080 | 1430 |
| O | 4950 | 5270 | $p A$ LHC |  |  |
| Ar | 4700 | 5000 | 275.4 | 3630 | 950 |
| Pb | 4400 | 4690 | 139.2 | 2410 | 2130 |
|  |  |  |  | 1220 | 1500 |

Table 1: Beam energies, $E_{\text {beam }}$, Lorentz factors, $\gamma_{L}$, photon cutoff energy in the lab frame, $k_{\text {max }}$, and in the nuclear rest frame, $E_{\text {cut }}$, as well as the equivalent $N N$ center-of-mass energy for $E_{\text {cut }}, \sqrt{S_{\gamma N}}$, for $A A$ collisions at RHIC and $A A$ and $p A$ collisions at the LHC.

## Photon Flux

Weizsäcker-Williams flux function of distance from the nucleus, $r$,

$$
\frac{d^{3} N_{\gamma}}{d k d^{2} r}=\frac{Z^{2} \alpha w^{2}}{\pi^{2} k r^{2}}\left[K_{1}^{2}(w)+\frac{1}{\gamma_{L}^{2}} K_{0}^{2}(w)\right]
$$

$w=k r / \gamma_{L}, K_{0}(w)$ and $K_{1}(w)$ are modified Bessel functions
Total flux is integral over transverse area of the target assuming nuclei do not interact, $r>2 R_{A}$ for $A A$ and $r>r_{p}+R_{A}$ for $p A$,

$$
\frac{d N_{\gamma}}{d k}=\frac{2 Z^{2} \alpha}{\pi k}\left[w_{R}^{i A} K_{0}\left(w_{R}^{i A}\right) K_{1}\left(w_{R}^{i A}\right)-\frac{\left(w_{R}^{i A}\right)^{2}}{2}\left(K_{1}^{2}\left(w_{R}^{i A}\right)-K_{0}^{2}\left(w_{R}^{i A}\right)\right)\right]
$$

$w_{R}^{A A}=2 k R_{A} / \gamma_{L}, w_{R}^{p A}=2 k\left(r_{p}+R_{A}\right) / \gamma_{L}$
We numerically evaluate the flux taking into account the nuclear shapes for $A A$ collisions but use the analytical result for $p A$ $A A$ evaluations agree best when $k R_{A} / \gamma_{L} \hbar c \ll 1$ or $M / \sqrt{S_{\gamma N}}$ is small At LHC, analytical and numerical results agree within $8 \%$

## Direct $Q \bar{Q}$ Photoproduction

Hadronic reaction: $\gamma(k)+N\left(P_{2}\right) \rightarrow Q\left(p_{1}\right)+\bar{Q}\left(p_{2}\right)+X$
LO partonic reaction: $\gamma(k)+g\left(x_{2} P_{2}\right) \rightarrow Q\left(p_{1}\right)+\bar{Q}\left(p_{2}\right)$
Partonic cross section

$$
s^{2} \frac{d^{2} \sigma_{\gamma g}}{d t_{1} d u_{1}}=\pi \alpha_{s}\left(Q^{2}\right) \alpha e_{Q}^{2}\left(\frac{t_{1}}{u_{1}}+\frac{u_{1}}{t_{1}}+\frac{4 m^{2} s}{t_{1} u_{1}}\left[1-\frac{m^{2} s}{t_{1} u_{1}}\right]\right) \delta\left(s+t_{1}+u_{1}\right)
$$

Partonic invariants: $s=\left(k+x_{2} P_{2}\right)^{2}=4 k x_{2} m_{p} \gamma_{L}, t_{1}=\left(x_{2} P_{2}-p_{1}\right)^{2}-m^{2}$, $u_{1}=\left(k-p_{1}\right)^{2}-m^{2}$
Couplings: $\alpha=e^{2} / \hbar c, \alpha_{s}\left(Q^{2}\right) \approx 0.11, e_{c}=e_{t}=2 / 3, e_{b}=-1 / 3$
Hadronic cross section, convolution over gluon density, photon flux

$$
S^{2} \frac{d^{2} \sigma_{\gamma A \rightarrow Q \bar{Q} X}}{d T_{1} d U_{1} d^{2} b}=2 \int d z \int_{k_{\min }}^{\infty} d k \frac{d^{3} N_{\gamma}}{d k d^{2} b} \int_{0}^{1} \frac{d x_{2}}{x_{2}} F_{g}^{A}\left(x_{2}, Q^{2}, \vec{b}, z\right) s^{2} \frac{d^{2} \sigma_{\gamma g}}{d t_{1} d u_{1}}
$$

Minimum photon momentum for pair of mass $M$ is $k_{\min }=M^{2} /\left(4 \gamma_{L} m_{p}\right)$ Hadronic invariants: $S=\left(k+P_{2}\right)^{2}, T_{1}=\left(P_{2}-p_{1}\right)^{2}-m^{2}, U_{1}=\left(k-p_{1}\right)^{2}-m^{2}$ Factor of two because both nuclei can be targets

## Resolved Photoproduction

LO partonic reaction:

$$
\begin{aligned}
g(x k)+g\left(x_{2} P_{2}\right) & \rightarrow Q\left(p_{1}\right)+\bar{Q}\left(p_{2}\right) \\
q(x k)+\bar{q}\left(x_{2} P_{2}\right) & \rightarrow Q\left(p_{1}\right)+\bar{Q}\left(p_{2}\right)
\end{aligned}
$$

Partonic cross sections

$$
\begin{aligned}
& \hat{s}^{2} \frac{d^{2} \sigma_{q \bar{q}}}{d \hat{t}_{1} d \hat{u}_{1}}=\pi \alpha_{s}^{2}\left(Q^{2}\right) \frac{4}{9}\left(\frac{\hat{t}_{1}^{2}+\hat{u}_{1}^{2}}{\hat{s}^{2}}+\frac{2 m_{Q}^{2}}{\hat{s}}\right) \delta\left(\hat{s}+\hat{t}_{1}+\hat{u}_{1}\right) \\
& \hat{s}^{2} \frac{d^{2} \sigma_{g g}}{d \hat{t}_{1} d \hat{u}_{1}}=\frac{\pi \alpha_{s}^{2}\left(Q^{2}\right)}{16}\left(\frac{t_{1}}{u_{1}}+\frac{u_{1}}{t_{1}}+\frac{4 m_{Q}^{2} s}{t_{1} u_{1}}\left[1-\frac{m_{Q}^{2} s}{t_{1} u_{1}}\right]\right)\left[3\left(1-\frac{2 \hat{t}_{1} \hat{u}_{1}}{\hat{s}^{2}}\right)-\frac{1}{3}\right] \delta\left(\hat{s}+\hat{t}_{1}+\hat{u}_{1}\right)
\end{aligned}
$$

Partonic invariants: $\hat{s}=\left(x k+x_{2} P_{2}\right)^{2}, \hat{t}_{1}=\left(x_{2} P_{2}-p_{1}\right)^{2}-m^{2}$, $\hat{u}_{1}=\left(x k-p_{1}\right)^{2}-m^{2}$
Resolved cross sections are factor $\alpha_{s}\left(Q^{2}\right) /\left(\alpha e_{Q}^{2}\right)$ larger
Now convolute over parton distributions in the photon too

$$
\begin{aligned}
S^{2} \frac{d^{2} \sigma_{\gamma A \rightarrow Q \bar{Q} X}^{\mathrm{res}}}{d T_{1} d U_{1} d^{2} b}= & 2 \int d z \int_{k_{\min }}^{\infty} d k \frac{d^{3} N_{\gamma}}{d k d b^{2}} \int_{\frac{k_{\min }}{k}} \frac{d x}{x} \int_{x_{2_{\min }}}^{1} \frac{d x_{2}}{x_{2}}\left[F_{g}^{\gamma}\left(x, Q^{2}\right) F_{g}^{A}\left(x_{2}, Q^{2}, \vec{b}, z\right) \hat{s}^{2} \frac{d^{2} \sigma_{g g}}{d \hat{t}_{1} d \hat{u}_{1}}\right. \\
& \left.+\sum_{q=u, d, s} F_{q}^{\gamma}\left(x, Q^{2}\right)\left\{F_{q}^{A}\left(x_{2}, Q^{2}, \vec{b}, z\right)+F_{\bar{q}}^{A}\left(x_{2}, Q^{2}, \vec{b}, z\right)\right\} \hat{s}^{2} \frac{d^{2} \sigma_{q \bar{q}}}{d \hat{t}_{1} d \hat{u}_{1}}\right]
\end{aligned}
$$

## Parton Distribution Functions in the Photon



Figure 1: We show the GRV-G LO (left) and LAC1 (right) quark (a) and gluon (b) distributions of the photon. In (a) the up (solid), down (dashed) and strange (dot-dashed) distributions are evaluated at $2 m_{c}$ (lower curves), $m_{b}$ (middle curves) and $m_{t}$ (upper curves). In (b) the gluon distributions are shown at $2 m_{c}$ (solid), $m_{b}$ (dashed) and $m_{t}$ (dot-dashed).

## Shadowing Parameterizations

## Compare EKS98 and FGS

Recent parameterization by Frankfurt et al also shown, uses EKS98 for valence shadowing, stronger gluon shadowing at low $x$, cuts off modification above $x=0.25$ for sea, 0.03 for gluon


Figure 2: The EKS98 and FGS shadowing parameterizations are compared at the scale $\mu=2 m_{c}=2.4 \mathrm{GeV}$. The solid curves are the EKS98 parameterization, the dashed, FGS.

## Heavy Quark Production Diagrams


a)

c)

b)

d)

Figure 3: Feynman diagrams for heavy quark photoproduction for (a) direct and (b)-(e) resolved photons.

## $Q \bar{Q}$ Photoproduction at RHIC



Figure 4: Charm (left) and bottom (right) photoproduction in peripheral $\mathrm{Au}+\mathrm{Au}$ collisions at RHIC for $b>2 R_{A}$. The single quark $p_{T}$ (a) and rapidity (b) distributions are shown along with the $c \bar{c}$ pair invariant mass (c). The direct (dashed), resolved (dot-dashed), and the sum of the two (solid) are shown. The direct contribution is divided by two to distinguish it from the total while the resolved charm contribution is multiplied by ten (the bottom resolved contribution is unchanged). There are two curves for each contribution: no shadowing and EKS98. At this energy, the curves are almost indistinguishable but the curves with shadowing are somewhat higher, especially at negative rapidities. In the rapidity distributions, the photon is coming from the left. With J. Nystrand and S. Klein.

## Direct $Q \bar{Q}$ Photoproduction at the LHC



Figure 5: Direct $Q \bar{Q}$ photoproduction in peripheral $A A$ collisions. The left-hand side is for charm while the right-hand side is for bottom. The single $Q p_{T}$ (upper) and rapidity (middle) distributions are shown along with the $Q \bar{Q}$ pair invariant mass distributions (lower). The $\mathrm{O}+\mathrm{O}$ (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid) results are given. There are three curves for each contribution: no shadowing, EKS98 and FGS. At $y_{1}>0$, the highest curve is without shadowing, the middle curve with EKS98 and the lower curve with FGS. The photon is coming from the left. With J. Nystrand and S. Klein.

## Shadowing Effects on $Q \bar{Q}$ Photoproduction



Figure 6: Shadowing in direct $Q \bar{Q}$ photoproduction in peripheral $A A$ collisions. The left-hand side shows the results for charm while the right-hand side gives the results for bottom. The single $Q p_{T}$ (upper) and rapidity (middle) ratios are shown along with the $Q \bar{Q}$ pair invariant mass ratios (lower). The results for the EKS98 ( $\mathrm{O}+\mathrm{O}$ (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid)) and FGS ( $\mathrm{O}+\mathrm{O}$ (dotted), $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dot-dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (dash-dash-dash-dotted)) shadowing parameterizations are given. The photon is coming from the left.

## Average $x$ Values for $Q \bar{Q}$ Photoproduction



Figure 7: The average value of the nucleon parton momentum fraction $x$ as a function of quark rapidity (left-hand side) and transverse momentum (right-hand side). The results are given for charm (upper), bottom (middle) and top (lower). The direct values are given for $\mathrm{O}+\mathrm{O}$ (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid) while the resolved values are given for $\mathrm{O}+\mathrm{O}$ (dotted), $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dotdashed) and $\mathrm{Pb}+\mathrm{Pb}$ (dash-dash-dash-dotted). (Resolved production is calculated with the GRV-G photon parton distributions.) The photon is coming from the left.

## Direct $Q \bar{Q}$ Photoproduction Cross Sections

| $\sigma^{\text {dir }}(\mathrm{mb})$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $A A$ | no shad | EKS98 | FGS |  |  |  |
| $c \bar{c}$ |  |  |  |  |  |  |
| $\mathrm{O}+\mathrm{O}$ | 1.66 | 1.50 | 1.35 |  |  |  |
| $\mathrm{Ar}+\mathrm{Ar}$ | 16.3 | 14.3 | 12.3 |  |  |  |
| $\mathrm{~Pb}+\mathrm{Pb}$ | 1246 | 1051 |  |  |  | 850 |
|  | $b \bar{b}$ |  |  |  |  |  |
| $\mathrm{O}+\mathrm{O}$ | 0.0081 | 0.0078 |  |  |  |  |
| $\mathrm{Ar}+\mathrm{Ar}$ | 0.073 | 0.070 | 0.0075 |  |  |  |
| $\mathrm{~Pb}+\mathrm{Pb}$ | 4.89 | 4.71 | 0.066 |  |  |  |
|  | $t \bar{t}$ |  |  |  |  |  |
| $\mathrm{O}+\mathrm{O}$ | $9.13 \times 10^{-9}$ | $9.27 \times 10^{-9}$ | $9.31 \times 10^{-9}$ |  |  |  |
| $\mathrm{Ar}+\mathrm{Ar}$ | $2.86 \times 10^{-8}$ | $2.88 \times 10^{-8}$ | $2.87 \times 10^{-8}$ |  |  |  |
| $\mathrm{~Pb}+\mathrm{Pb}$ | $3.29 \times 10^{-7}$ | $3.21 \times 10^{-7}$ | $3.22 \times 10^{-7}$ |  |  |  |

Table 2: Direct $Q \bar{Q}$ photoproduction cross sections integrated over $b>2 R_{A}$ in peripheral $A A$ collisions. With J. Nystrand and S. Klein.

## Resolved $Q Q$ Photoproduction



Figure 8: Resolved $Q \bar{Q}$ photoproduction in peripheral $A A$ collisions. The left-hand side shows the results for charm while the righthand side gives the results for bottom. The single $Q p_{T}$ (upper) and rapidity (middle) distributions are shown along with the $Q \bar{Q}$ pair invariant mass distributions (lower). The results for the GRV-G ( $\mathrm{O}+\mathrm{O}$ (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid)) and LAC1 $(\mathrm{O}+\mathrm{O}$ (dotted), $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dot-dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (dash-dash-dash-dotted)) photon parton densities are given. There are two curves for each contribution: no shadowing and EKS98. At $y_{1}>0$, the highest curve is without shadowing. The photon is coming from the left. With J. Nystrand and S. Klein.

## Shadowing in Resolved $Q \bar{Q}$ Photoproduction



Figure 9: Shadowing in resolved $Q \bar{Q}$ photoproduction in peripheral $A A$ collisions. The left-hand side shows the results for charm while the right-hand side gives the results for bottom. The EKS98 shadowing parameterization is used in both cases. The single $Q p_{T}$ (upper) and rapidity (middle) ratios are shown along with the $Q \bar{Q}$ pair invariant mass ratios (lower). The results for the GRV-G (O+O (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid)) and LAC1 ( $\mathrm{O}+\mathrm{O}$ (dotted), $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dot-dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (dash-dash-dash-dotted)) photon parton distributions are given. The photon is coming from the left.

## Relative Direct to Resolved $Q \bar{Q}$ Photoproduction



Figure 10: Resolved to direct $Q \bar{Q}$ photoproduction ratio in peripheral $A A$ collisions. The left-hand side shows the results for charm while the right-hand side gives the results for bottom. The EKS98 shadowing parameterization is used in both cases. The single $Q p_{T}$ (upper) and rapidity (middle) ratios are shown along with the $Q \bar{Q}$ pair invariant mass ratios (lower). The results for the GRV-G (O +O (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid)) and LAC1 ( $\mathrm{O}+\mathrm{O}$ (dotted), $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dot-dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (dash-dash-dash-dotted)) photon parton distributions are given. The photon is coming from the left.

## Resolved $Q \bar{Q}$ Photoproduction Cross Sections

|  | GRV |  |  | LAC1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $A A$ | no shad | EKS98 | FGS | no shad | EKS98 |
| $c \bar{c}$ |  |  |  |  |  |
| $\mathrm{O}+\mathrm{O}$ | 0.351 | 0.346 | 0.331 | 2.04 | 2.02 |
| $\mathrm{Ar}+\mathrm{Ar}$ | 3.00 | 2.93 | 2.77 | 16.6 | 16.6 |
| $\mathrm{Pb}+\mathrm{Pb}$ | 190.0 | 186.7 | 174.3 | 987 | 1007 |
| $b \bar{b}$ |  |  |  |  |  |
| $\mathrm{O}+\mathrm{O}$ | 0.0029 | 0.0029 | 0.0029 | 0.0105 | 0.0106 |
| $\mathrm{Ar}+\mathrm{Ar}$ | 0.0222 | 0.0226 | 0.0024 | 0.073 | 0.075 |
| $\mathrm{Pb}+\mathrm{Pb}$ | 1.21 | 1.26 | 1.25 | 3.41 | 3.66 |
| $t \bar{t}$ |  |  |  |  |  |
| $\mathrm{O}+\mathrm{O}$ | $2.81 \times 10^{-10}$ | $2.76 \times 10^{-10}$ | - | $2.92 \times 10^{-10}$ | $2.88 \times 10^{-10}$ |
| $\mathrm{Ar}+\mathrm{Ar}$ | $1.08 \times 10^{-9}$ | $1.04 \times 10^{-9}$ | - | $1.09 \times 10^{-9}$ | $1.05 \times 10^{-9}$ |
| $\mathrm{Pb}+\mathrm{Pb}$ | $1.60 \times 10^{-8}$ | $1.48 \times 10^{-8}$ | - | $1.62 \times 10^{-8}$ | $1.49 \times 10^{-8}$ |

Table 3: Resolved $Q \bar{Q}$ photoproduction cross sections integrated over $b>2 R_{A}$ in peripheral $A A$ collisions. With J. Nystrand and S. Klein.

## Composition of Resolved Contribution

Resolved contribution can be significant, depending on parameterization of photon PDFs
Large $q$ and $\bar{q}$ densities in the photon at large $x$ means that $q \bar{q}$ annihilation is an important component of resolved production, bigger for GRV than LAC1
GRV: $c \bar{c}$ is $4 \% q \bar{q}, b \bar{b}$ is $10 \%$
LAC1: $c \bar{c}$ is $1-2 \% q \bar{q}, b \bar{b}$ is $4-7 \%$

## $x_{2}$ and $p_{T}$ Reach of Direct $\mathrm{Pb}+\mathrm{Pb} b \bar{b}$ Photoproduction



Figure 11: The rate for direct inclusive $b \bar{b}$ photoproduction for a one month $\mathrm{LHC} \mathrm{Pb}+\mathrm{Pb}$ run at $0.42 \times 10^{27} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$. Rates are in counts per bin of $\pm 0.25 x_{2}$ and $\pm 0.75 \mathrm{GeV}$ in $p_{T}$. With M. Strikman and S. White.

## Heavy Quark Photoproduction in $p A$

Calculations done in the equal speed frame
This doesn't make any difference at RHIC because the proton energy is tunable, $\sqrt{S}$ is the same in $p A$ and $A A$
At LHC we assume that the proton beam is used at its maximum energy, 7 TeV so $p A$ energy is higher
Using $p A$ photoproduction to measure the nuclear gluon distribution tricky because differences in flux between $p A$ and $A A$ must be taken into account
In photon flux, $w_{R}^{A A}>w_{R}^{p A}$, so that $c \bar{c}$ in $A A$ is $22-37 \%$ smaller at the same energy, $b \bar{b}$ is $37-65 \%$ smaller (both calculated using analytical formula for the flux)
Difference between $p A$ and $A A$ least for small $A$ where $R_{A}-r_{p}$ is small Difference largest for $b \bar{b}$ because close to threshold

## Direct and Resolved $Q \bar{Q} p A$ Photoproduction Cross Sections

| $p A$ | $\sigma^{\text {dir }}(\mu \mathrm{b})$ | $\sigma^{\mathrm{res}}(\mathrm{GRV})(\mu \mathrm{b})$ | $\sigma^{\mathrm{res}}(\mathrm{LAC} 1)(\mu \mathrm{b})$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| $p \mathrm{O}$ | 75.5 | 19.7 | 120.6 |
| $p \mathrm{Ar}$ | 335 | 81.1 | 486.3 |
| $p \mathrm{~Pb}$ | 5492 | 1160 | 6371 |
|  |  | $b \bar{b}$ |  |
| $p \mathrm{O}$ | 0.419 | 0.190 | 0.773 |
| $p \mathrm{Ar}$ | 1.775 | 0.739 | 2.886 |
| $p \mathrm{~Pb}$ | 26.83 | 9602 | 34.68 |
|  |  | $t \bar{t}$ |  |
| $p \mathrm{O}$ | $1.54 \times 10^{-6}$ | $4.00 \times 10^{-8}$ | $4.00 \times 10^{-8}$ |
| $p \mathrm{Ar}$ | $4.40 \times 10^{-6}$ | $1.23 \times 10^{-7}$ | $1.24 \times 10^{-7}$ |
| $p \mathrm{~Pb}$ | $3.00 \times 10^{-5}$ | $9.74 \times 10^{-7}$ | $9.86 \times 10^{-7}$ |

Table 4: Direct and resolved $c \bar{c}$ and $b \bar{b}$ photoproduction cross sections integrated over $b>r_{p}+R_{A}$ in $p A$ collisions at the LHC.

## $x_{2}$ and $p_{T}$ Reach of Direct $p \mathbf{P b} b \bar{b}$ Photoproduction



Figure 12: The expected inclusive $b \bar{b}$ photoproduction rate in a one month LHC $p \mathrm{~Pb}$ run at $7.4 \times 10^{29} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$. Rates are in counts per bin of $\pm 0.25 x_{2}$ and $\pm 0.75 \mathrm{GeV}$ in $p_{T}$. With M. Strikman and S. White.

## Dijet Production Diagrams


(a)

(d)

(g)

(b)

(e)

(h)

Figure 13: Feynman diagrams for dijet photoproduction from direct, (a) and (b), and resolved photons, (c)-(h). Only a sample of the resolved diagrams are shown. Crossed diagrams are not shown.

## Photon + Jet Production Diagrams




(c)

Figure 14: Feynman diagrams for $\gamma+$ jet photoproduction from direct, (a), and resolved photons, (b) and (c). Crossed diagrams are not shown.

## Jet Photoproduction at LHC

Direct jet photoproduction an easy extension of this calculation, same photon-gluon fusion diagrams, $m_{Q} \rightarrow 0$ plus also QCD Compton diagram
Include fragmentation through KKP determination from $e^{+} e^{-}$data at LEP
Fragmentation functions assume factorization and universality, same as initial state parton distribution
Resolved jet photoproduction includes all $2 \rightarrow 2$ processes, gives larger contribution than direct photoproduction at low $p_{T}$

## Direct Dijet Photoproduction

Hadronic reaction: $\gamma(k)+N\left(P_{2}\right) \rightarrow \operatorname{jet}\left(p_{1}\right)+\operatorname{jet}\left(p_{2}\right)+X$
LO partonic reactions: $\gamma(k)+g\left(x_{2} P_{2}\right) \rightarrow q\left(p_{1}\right)+\bar{q}\left(p_{2}\right)$

$$
\gamma(k)+q\left(x_{2} P_{2}\right) \rightarrow g\left(p_{1}\right)+q\left(p_{2}\right)
$$

Partonic cross section

$$
\begin{aligned}
& s^{2} \frac{d^{2} \sigma_{\gamma g \rightarrow q \bar{q}}}{d t d u}=\pi \alpha_{s}\left(\mu^{2}\right) \alpha e_{Q}^{2}\left[\frac{t^{2}+u^{2}}{t u}\right] \delta(s+t+u), \\
& s^{2} \frac{d^{2} \sigma_{\gamma q \rightarrow g q}}{d t d u}=-\frac{8}{3} \pi \alpha_{s}\left(\mu^{2}\right) \alpha e_{Q}^{2}\left[\frac{s^{2}+t^{2}}{s t}\right] \delta(s+t+u)
\end{aligned}
$$

Partonic invariants: $s=\left(k+x_{2} P_{2}\right)^{2}=4 k x_{2} m_{p} \gamma_{L}, t=\left(x_{2} P_{2}-p_{1}\right)^{2}$, $u=\left(k-p_{1}\right)^{2}$
Hadronic cross section, convolution over parton density, photon flux $S_{N N}^{2} \frac{d^{2} \sigma_{\gamma A \rightarrow \text { jet }+ \text { jet }+X}^{\text {dir }}}{d T d U d^{2} b}=2 \int d z \int_{k_{\text {min }}}^{\infty} d k \frac{d^{3} N_{\gamma}}{d k d^{2} b} \int_{x_{2} \min }^{1} \frac{d x_{2}}{x_{2}}\left[\sum_{i, j, l=q, \bar{q}, g} F_{i}^{A}\left(x_{2}, \mu^{2}, \vec{b}, z\right) s^{2} \frac{d^{2} \sigma_{\gamma i \rightarrow j l}}{d t d u}(1)\right.$

Hadronic invariants: $S=\left(k+P_{2}\right)^{2}, T=\left(P_{2}-p_{1}\right)^{2}, U=\left(k-p_{1}\right)^{2}$, Now $T=$ $-\sqrt{S_{N N}} p_{T} e^{-y_{1}}$ and $x_{1}=\left(p_{T} / \sqrt{S_{N N}}\right)\left(e^{y_{1}}+e^{y_{2}}\right)$ and $x_{2}=\left(p_{T} / \sqrt{S_{N N}}\right)\left(e^{-y_{1}}+e^{-y_{2}}\right)$ since no mass scale

## Direct Dijet Photoproduction



Figure 15: Direct jet photoproduction in peripheral collisions. (a) The $p_{T}$ distributions for $\left|y_{1}\right| \leq 1$ are shown for $A A$ collisions. The solid curves is the total for Pb ions while the produced quarks (dashed), antiquarks (dotted) and gluons (dot-dashed) are shown separately. The total production for Ar (dot-dot-dot-dashed) and O (dot-dash-dash-dashed) ions are also shown. (b) The fraction of gluon-initiated jets as a function of $p_{T}$ for $\mathrm{Pb}+\mathrm{Pb}$ (solid), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{O}+\mathrm{O}$ (dot-dashed) interactions. (c) The EKS98 shadowing ratios for produced partons. The solid curve is the total for Pb ions while the ratios for produced quarks (dashed), antiquarks (dotted) and gluons (dot-dashed) are shown separately. The total ratios for Ar (dot-dot-dot-dashed) and O (dot-dash-dash-dashed) ions are also shown. (d) The same as (c) for FGS.

## Final-state Hadrons From Dijet Photoproduction

Same reactions as before, now jets hadronized

$$
\begin{aligned}
\frac{d \sigma_{\gamma A \rightarrow h X}^{\mathrm{dir}}}{d p_{T} d^{2} b}= & 4 p_{T} \int d z \int_{\theta_{\min }}^{\theta_{\max }} \frac{d \theta_{\mathrm{cm}}}{\sin \theta_{\mathrm{cm}}} \int d k \frac{d^{3} N_{\gamma}}{d k d^{2} b} \int \frac{d x_{2}}{x_{2}} \\
& \times\left[\sum_{i, l=q, \bar{q}, g} F_{i}^{A}\left(x_{2}, \mu^{2}, \vec{b}, z\right) \frac{d \sigma_{\gamma i \rightarrow l X^{\prime}}}{d t} \frac{D_{h / l}\left(z_{c}, \mu^{2}\right)}{z_{c}}\right]
\end{aligned}
$$

$X$ on left-hand side includes all final-state hadrons in addition to $h$, $X^{\prime}$ on right-hand side is unobserved final-state parton
The subprocess cross sections, $d \sigma / d t$, are related to $s^{2} d \sigma / d t d u$ through $\delta(s+t+u)$ and division by $s^{2}$
Integral over rapidity replaced by an integral over center-of-mass scattering angle, $\theta_{\min } \leq \theta_{\mathrm{cm}} \leq \theta_{\max }$, corresponding to a given rapidity cut: $\theta_{\min }=0$ and $\theta_{\max }=\pi$ covers all rapidity; $\theta_{\min }=\pi / 4$ and $\theta_{\max }=3 \pi / 4$ is about $\left|y_{1}\right| \leq 1$
KKP fragmentation functions with $\mu^{2}=p_{T}^{2}$
Resolved rates not shown, higher at low $p_{T}$ but become comparable and then lower than direct as $p_{T}$ increases

## Final-State Hadron Production



Figure 16: Direct photoproduction of leading hadrons in peripheral collisions. (a) The $p_{T}$ distributions for $\left|y_{1}\right| \leq 1$ are shown for $A A$ collisions. The solid curve is the total for $\mathrm{Pb}+\mathrm{Pb}$ while the produced pions (dashed), kaons (dot-dashed) and protons (dotted) are shown separately. The total production for $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dot-dashed) and $\mathrm{O}+\mathrm{O}$ (dot-dash-dash-dashed) are also shown. (b) The fraction of gluon-initiated hadrons as a function of $p_{T}$. The curves are the same as in (a). (c) The EKS98 shadowing ratios for produced pions. The solid curve is the total for $\mathrm{Pb}+\mathrm{Pb}$ while the ratios for pions produced by quarks (dashed), antiquarks (dotted) and gluons (dot-dashed) are shown separately. The total ratios for $\mathrm{Ar}+\mathrm{Ar}$ (dot-dot-dot-dashed) and $\mathrm{O}+\mathrm{O}$ (dot-dash-dash-dashed) are also shown. (d) The same as (c) for FGS.

## Average $x$ Values for Dijet Photoproduction



Figure 17: The average value of the nucleon parton momentum fraction $x$ as a function of transverse momentum. Results are given for (a) direct and (b) resolved gluon jet production and for (c) direct and (d) resolved pion production by gluons. The results are given for $\mathrm{O}+\mathrm{O}$ (dot-dashed), $\mathrm{Ar}+\mathrm{Ar}$ (dashed) and $\mathrm{Pb}+\mathrm{Pb}$ (solid) interactions.

Dijet Rates in $x$ and $p_{T}$


Figure 18: The expected inclusive dijet photoproduction rate for a one month LHC $\mathrm{Pb}+\mathrm{Pb}$ run at $0.42 \times 10^{27} \mathrm{~cm}^{-2} \mathrm{~s}^{-1}$. Rates are in counts per bin of $\pm 0.25 x_{2}$ and $\pm 1 \mathrm{GeV}$ in $p_{T}$.

## Summary

- We have calculated charm, bottom and top photoproduction in heavy ion collisions
- Resolved contribution is very sensitive to the photon parton density
- Rates are high with good reach in $x$ for $b \bar{b}$ production
- We have also considered photoproduction of jets
- Dijet rates also high but best range of $x$ achieved with not too high $p_{T}$ jets
- Both processes can probe nuclear qluon distributions at low $x$ and perturbative scales in relatively clean environment

