



Charmless Branching Fraction Studies of

$$B^0 \rightarrow K_S^0 \pi^+ \pi^- \text{ at } BABAR$$

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The *BABAR* Collaboration



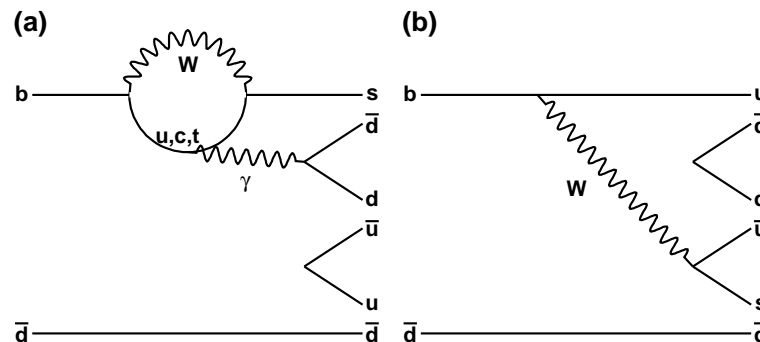
Outline

- Physics Motivation
- Method - Inclusive BF
 - Variables & Cuts
 - Calibration Channel $B^0 \rightarrow D^- \pi^+$, $D^- \rightarrow K_S^0 \pi^-$
 - Model (Signal, Continuum Background, B Background)
 - Fit Tests & Systematics
 - Results & Branching Fraction
- Quasi 2 Body Modes
- Conclusions and Future



Physics Motivation

- The decay mode $B^0 \rightarrow K_S^0 \pi^+ \pi^-$ is mediated by a combination of tree and penguin amplitudes, of comparable magnitudes. Fig (a) represents the penguin diagram, fig (b) represents the tree.
- Measurements of $B^0 \rightarrow K_S^0 \pi^+ \pi^-$ final states, along with other $K\pi\pi$ modes, can help to yield the CKM angle γ . [arXiv:hep-ph/0207257](https://arxiv.org/abs/hep-ph/0207257)
- Inclusive and quasi 2 body BFs needed, as well as time dependent analyses of $\rho^0 K_S^0$ and $f^0 K_S^0$.
- The quasi-two-body intermediate states $K^{*+} \pi^-$, $\rho^0 K_S^0$, $f^0 K_S^0$, $K_X^+(1430) \pi^-$, higher $f_X K_S^0$, and higher $K^{*+} \pi^-$ all interfere with each other in the Dalitz plot, allowing their relative phases to be determined by amplitude analysis, when statistics allow.





Discriminating Variables

- m_{ES} - Energy Substituted Mass of the event:

$$m_{ES} = \sqrt{E_x^2 - p^2}, \text{ where } E_x = \frac{E_{beam}^2 - p_{beam}^2 + 2p_{beam} \cdot p}{E_{beam}}$$

- ΔE - difference between the energy of the reconstructed B and the expected B decay energy.

$$\Delta E = E_x - E_{Bcand}$$

- **Fisher** - the Cornelius (CLEO) Fisher uses 9 cones of different size around the direction of the B candidate (CMS frame). Discriminates between jet-like $q\bar{q}$ events and spherical B events. The coefficients of the cones maximise the separation between the two types of events.
- $\cos(\theta_{thrust})$ - angle between the thrust axis (direction which maximises the sum of the longitudinal momenta of the particles in the event) and the momenta of the B candidate. Again tests event topology.
- K_S^0 lifetime significance = $c\tau/\sigma_{c\tau}$
- $\cos \theta_{K_S^0}$ - angle between the line of flight of the K_S^0 and its momentum vector.
- $\cos \theta_{hel}$ - Angle between the momentum vectors of one of the daughter particles from the resonance and the spectator particle, in the resonance's rest frame.

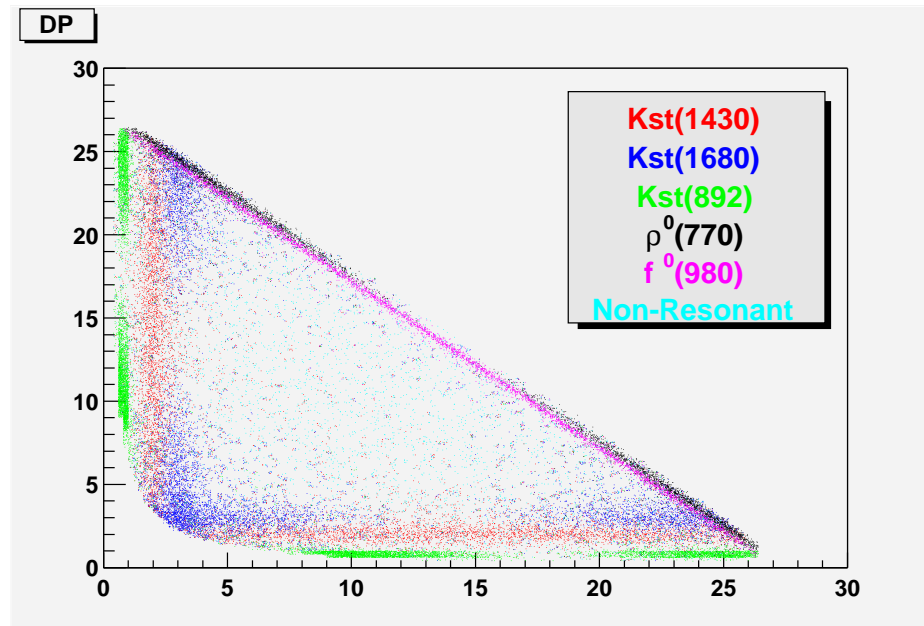


Selection Criteria

- Require each candidate to have 4 tracks, 2 of which make the K_S^0 candidate.
- GoodTracksLoose: Charged Tracks, $0.1 < p_t < 10$ GeV, > 20 DCH Hits, Maximum Distance of Closest Approach (DOCA) in xy = 1.5cm, DOCA in z axis < 10 cm
- $5.22 < m_{ES}(\text{GeV}) < 5.29$
- $q_{\pi_1} * q_{\pi_2} = -1$
- Particle Identification: π_1 and π_2 should fail electron and kaon selectors
- $0.483 < m_{K_S^0}(\text{GeV}) < 0.513$
- $|\cos \theta_{thrust}| < 0.9$
- Lifetime significance: $c\tau_{K_S^0} / \sigma_{c\tau} > 5$ cm
- $\cos \theta_{K_S^0} > 0.999$



Inclusive BF measurement Method



Dalitz plot contains many charmless modes:

$K^{*+} \pi^{-}$, $K^{*+} (1410) \pi^{-}$, $K^{*+} (1680) \pi^{-}$, $K_{0,2}^{*+} (1430) \pi^{-}$, $\rho^0 K_S^0$, $f^0 K_S^0$, higher $f^0 K_S^0$...

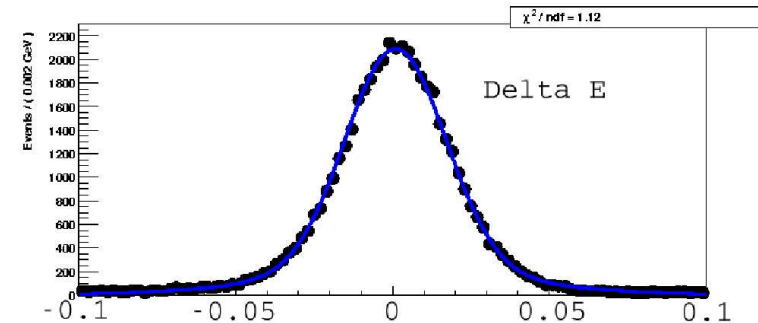
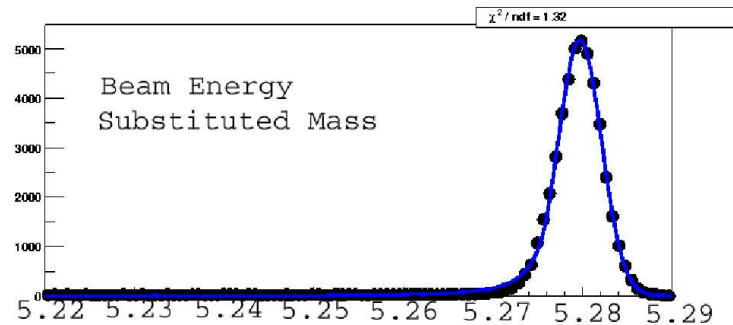
The ultimate aim would be to achieve a full Dalitz Plot analysis - but more data is needed first. (This analysis is on 81 fb^{-1}).

This is an ML analysis, fitting to m_{ES} , ΔE and Fisher.

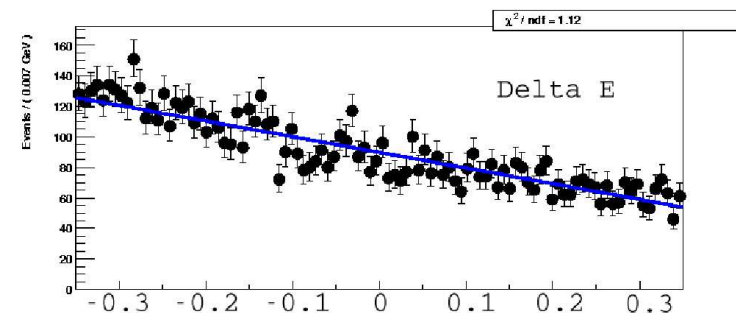
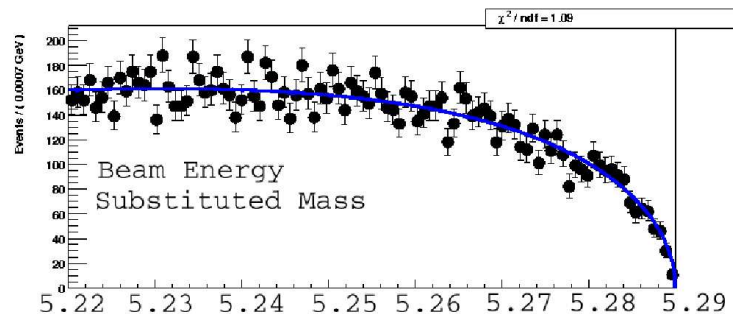


Model for the Inclusive Measurement

- The **signal** is modelled using non-resonant $B^0 \rightarrow K_S^0 \pi^+ \pi^-$ MC.



- The **background** is modelled using a ΔE sideband in on-resonance data (taken at $\sqrt{s} = \Upsilon(4S)$) for m_{ES} and Fisher and off-resonance data for ΔE (taken 40MeV below $\sqrt{s} = \Upsilon(4S)$).





- The major charmed backgrounds

$$B^0 \rightarrow D^- \pi^+ (D^- \rightarrow K_S^0 \pi^-),$$

$$B^0 \rightarrow J/\psi K_S^0 (J/\psi \rightarrow \mu^+ \mu^- \text{ or } \pi^+ \pi^-),$$

$$B^0 \rightarrow \psi(2S) K_S^0 (\psi(2S) \rightarrow \mu^+ \mu^- \text{ or } \pi^+ \pi^-),$$

$$B^0 \rightarrow \chi_{0c} K_S^0 (\chi_{0c} \rightarrow \pi^+ \pi^-)$$

are vetoed in a 5σ band about the mean of their distribution.

- In addition to signal and background PDFs, the model also includes PDFs for these B backgrounds:

- $B^0 \rightarrow D^- \pi^+, D^- \rightarrow K_S^0 \pi^-$

- $B^0 \rightarrow \eta' K_S^0, \eta' \rightarrow \pi^+ \pi^- \gamma$

- $B^0 \rightarrow D^- \rho^+, D^- \rightarrow K_S^0 \pi^-$

- $B^0 \rightarrow D^- \pi^+, D^- \rightarrow K_S^0 K^-$

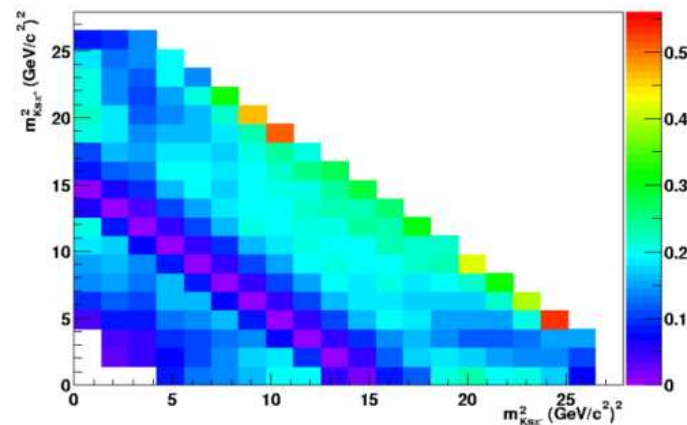
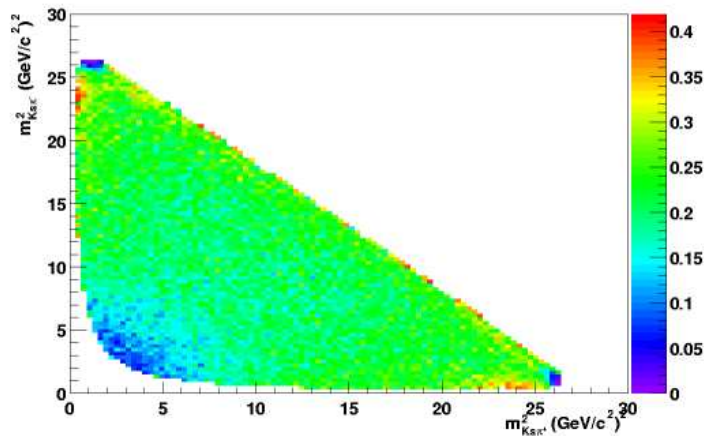
- $B^+ \rightarrow D^{*0} \pi^+, D^{*0} \rightarrow D^0 \gamma, D^0 \rightarrow K_S^0 \pi^0$

- $B^+ \rightarrow D^{*0} \pi^+, D^{*0} \rightarrow D^0 \pi^0, D^0 \rightarrow K_S^0 \pi^0$

- Expect 0 cross-feed from $B^0 \rightarrow K_S^0 K^+ K^-$, < 6 events from $B^0 \rightarrow K_S^0 K^+ \pi^-$ (dependent on UL of BF)



- We tested > 35 B backgrounds for possible contamination
- Efficiency binned within the Dalitz plot. Corrections for tracking, PID and K_S^0 are also applied to calculate the efficiency in each bin.

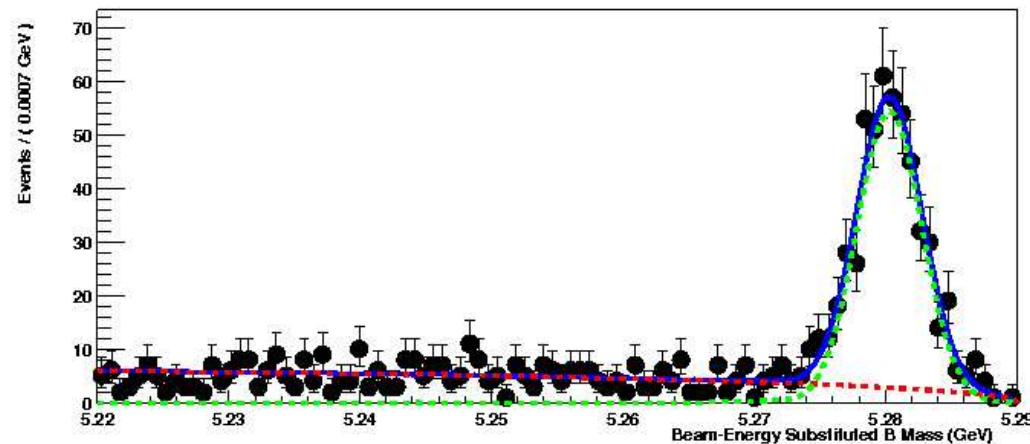


- Thorough fit testing of the model completed.



Calibration Channel - $B^0 \rightarrow D^- \pi^+, D^- \rightarrow K_S^0 \pi^-$

- PDG: $\mathcal{B} = 41.7 \pm 6.2 \times 10^{-6}$
- Use additional mass cut to select the $D\pi$ channel:
$$1.847 < m_{D^\pm} < 1.887$$
- No significant B background expected
- Float all parameters to check for discrepancies with MC
- Signal Yield = 484.7 ± 23.2
- $\mathcal{B} = 43.9 \pm 2.1 \pm 2.2 \times 10^{-6}$





Systematics

Systematic Consideration	BF Uncertainty %
Particle Identification	1.90
Tracking	1.70
K_S^0 efficiency	4.18
Fit Bias	4.11
PDF parameterisation	1.46
B background	0.37
Dalitz plot Efficiency	3.50
B counting	1.1
TOTAL	7.5



Unblinded Yields

$$\text{Signal Yield} = 309.74 \pm 27.132$$

(Background Yield = 21980 \pm 149.54)

which yields a

$$\mathcal{B}(B^0 \rightarrow K_S^0 \pi^+ \pi^-) = 21.9 \pm 1.9(\text{stat}) \times 10^{-6}$$

We choose to quote the BF without $K^0 \rightarrow K_S^0$:

$$\mathcal{B}(B^0 \rightarrow K^0 \pi^+ \pi^-) = 43.8 \pm 3.8(\text{stat}) \pm 3.4(\text{syst}) \times 10^{-6}$$

Belle's BF = $41.7 \pm 7.2 \times 10^{-6}$ (arXiv:hep-ex/0207003)

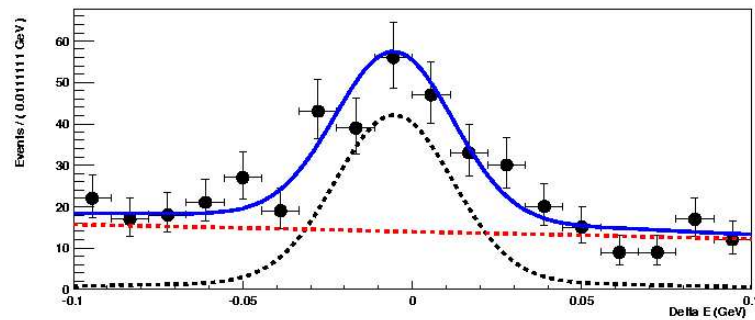
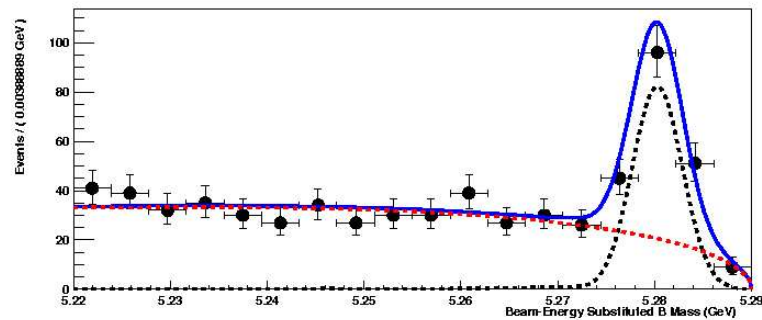
CLEO's BF = $50.0 \pm 12.2 \times 10^{-6}$ (arXiv:hep-ex/0206024)



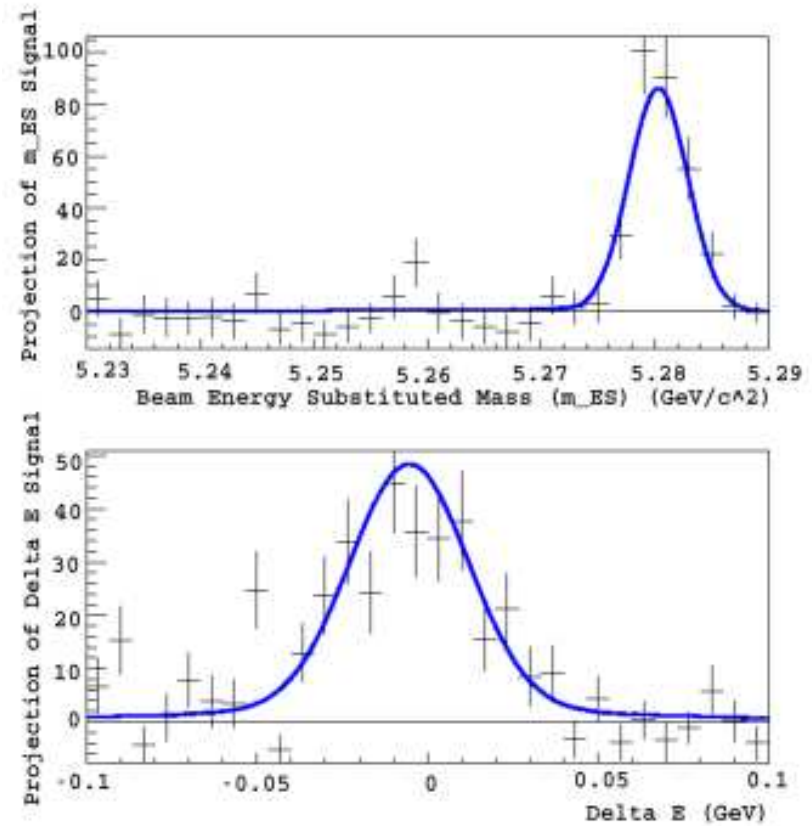
Projection Plots

Top - m_{ES} , Bottom - ΔE

Likelihood plots ($\mathcal{L} > 0.8$)

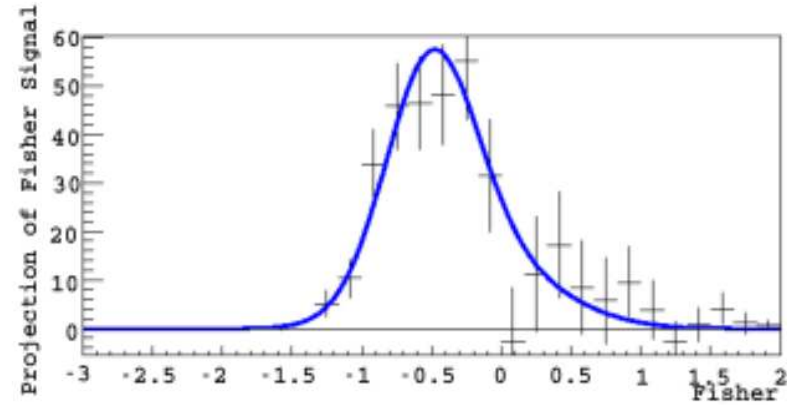
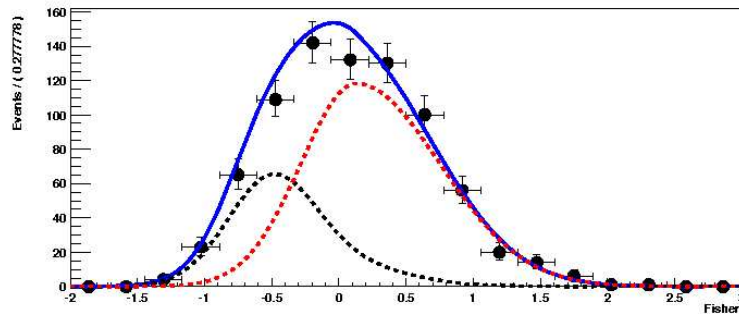


Projection Plots ([arXiv:physics/0402083](https://arxiv.org/abs/physics/0402083))

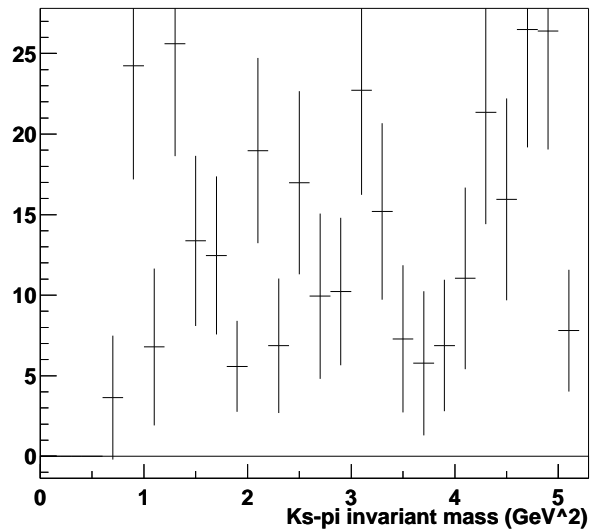




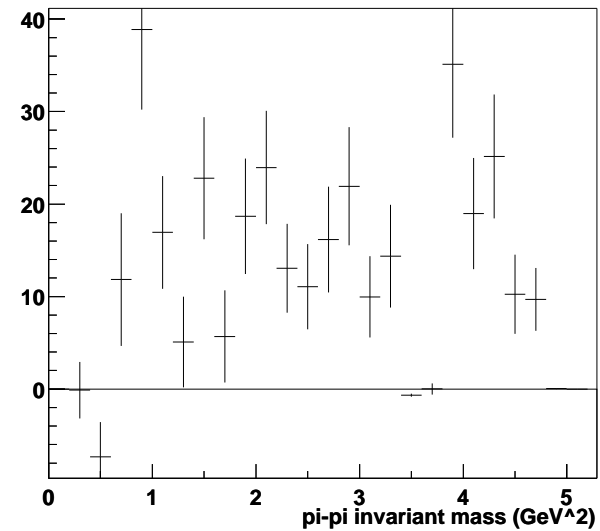
Fisher

 $m_{K_S^0 \pi^+}$ Plot Projection

A RooPlot of "Ks-pi invariant mass"

 $m_{\pi^+ \pi^-}$ Plot Projection

A RooPlot of "pi-pi invariant mass"





Quasi Two Body Modes

Currently looking at $K^{*\pm} \pi^\mp$, $\rho^0 K_S^0$, $f^0 K_S^0$. We use the same selection but for

- A mass cut of 3σ about the resonance:
 - $K^{*\pm}$ - $0.792 < m_{K^{*\pm}} < 0.992$
 - f^0 - $0.875 < m_{f^0} < 1.075$
 - ρ^0 - $0.53 < m_{\rho^0} < 0.91$
- A helicity cut for the $\rho^0 K_S^0$:
 - $0.53 < \cos \theta_{hel} < 0.91$
- Fit testing is done.
- B background studies done.
- Working on final interference systematics.

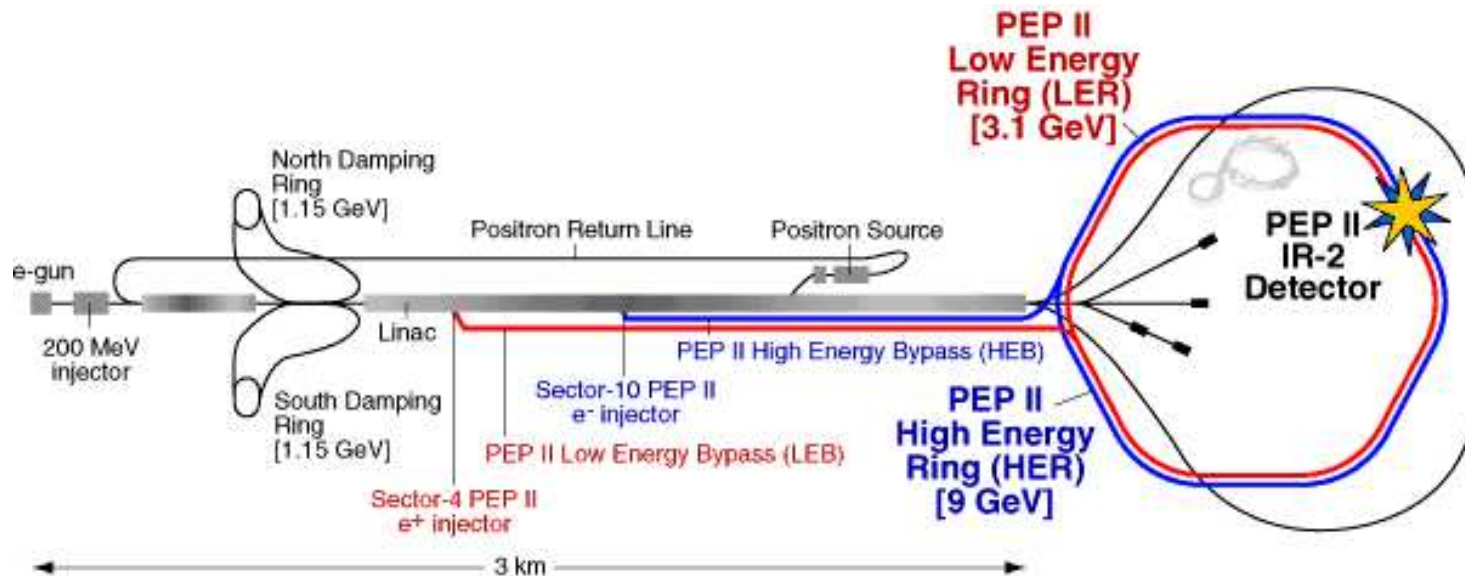


Conclusions & Future

- $\mathcal{B}(B^0 \rightarrow K^0 \pi^+ \pi^-) = 43.8 \pm 3.8(\text{stat}) \pm 3.4(\text{syst}) \times 10^{-6}$ on 81 fb^{-1} of data at *BABAR*
- $\mathcal{B}(B^0 \rightarrow D^\mp \pi^\pm, D^\mp \rightarrow K_S^0 \pi^\mp) = 43.9 \pm 2.1 \pm 2.2 \times 10^{-6}$
- These measurements went to Moriond EW
- Need to finish systematics on quasi two body modes
- Write Paper
- Summer update of all modes on maximum available sample (hopefully around 200 fb^{-1})
- We intend to do a full Dalitz plot analysis, when statistics allow



SLAC and PEP-II

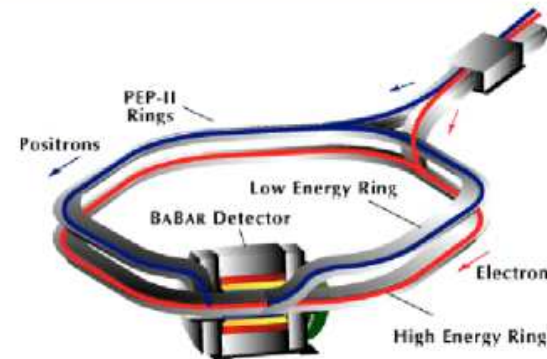
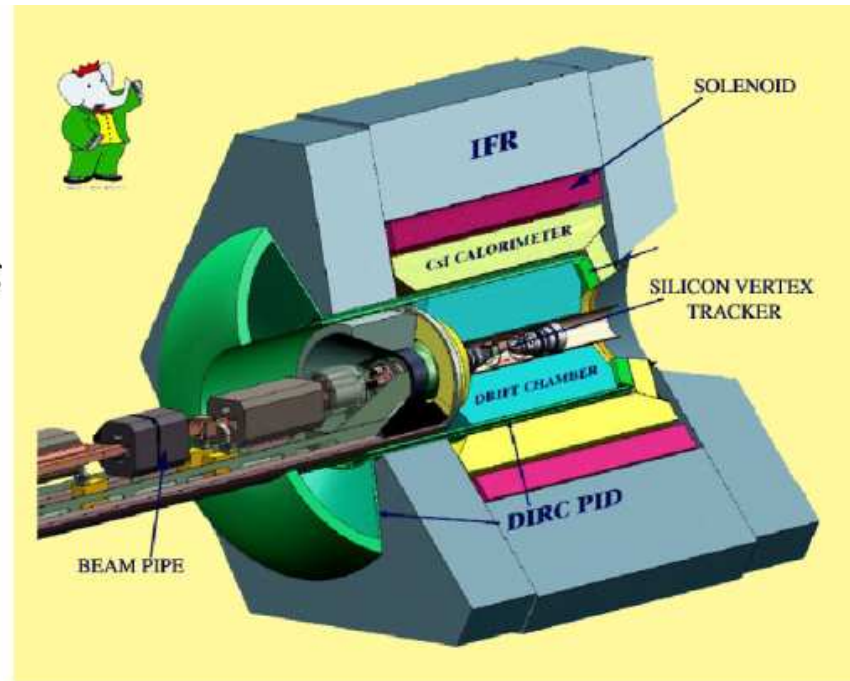


- SLAC runs the PEP-II accelerator
- Delivers asymmetric beams of electrons and positrons
- HER - 9 GeV, LER - 3.1 GeV
- Interaction Region is inside the *BABAR* detector
- Running the *B* Factory since 1999.



the BABAR Experiment

- SVT - tracking + vertexing
- DCH - tracking
- EMC - neutrals, energy measurements
- DIRC - PID
- IFR - muon separation
- Magnet
- Trigger





Maximum Likelihood Method

For each event x_i , the likelihood is defined as:

$$\mathcal{L}_i = \sum_{j=1}^k N_j \mathcal{P}_j(x_i)$$

where N_j is the number of events associated with the j^{th} hypothesis (signal, bg, etc). $\mathcal{P}_j(x_i)$ is the probability of the fit evaluated for that event, i :

$$\mathcal{P}_j(x_i) = \mathcal{S}_j(m_{ESi}) \cdot \mathcal{T}_j(\mathcal{F}_i) \cdot \mathcal{U}_j(\Delta E_i)$$

For N events, this becomes:

$$\mathcal{L} = \frac{\exp(-\sum_j N_j)}{N!} \prod_i^N \mathcal{L}_i$$

where the coefficient takes poissonian fluctuations for the observed number of events into account.



Fit Tests

We conduct several tests of our fitting procedure to see: Can we get back what we put in?

- Toy tests of full model, and with varying amounts of signal.
- Embedded fits - use toy data for continuum background, MC for signal and B bgs. - here we observe a small bias of +4.1%, which is included as a systematic.
- Mock Data Set tests - use a full data set constructed purely from MC, subjected to our selection criteria
- Negative Log Likelihood tests



sPlots - a BRIEF Explanation

In order to calculate the BF, and provide clean signal plots, we use the sPlot method ([arXiv:physics/0402083](https://arxiv.org/abs/physics/0402083))

The description is very involved, although implementation is relatively simple.

For each species in your fit (signal, continuum bg etc.), you can define an sWeight (a “covariance-weighted weight”) for each event

$${}_s\mathcal{P}_n(y_e) = \frac{\sum_{j=1}^{N_s} \mathbf{V}_{nj} f_j(y_e)}{\sum_{k=1}^{N_s} N_k f_k(y_e)}$$

where \mathbf{V} is the covariance matrix of the fit, and f is the value of the species pdf for that event e .

To calculate the branching fraction for the inclusive measurement, and take into account the variation of efficiency over the Dalitz plane, we need to weigh each event by its efficiency.

$$\mathcal{B} = \frac{\sum_{e=1}^N \frac{{}_s\mathcal{P}_n(y_e)}{\epsilon(x_e)}}{N_{B\bar{B}}}$$