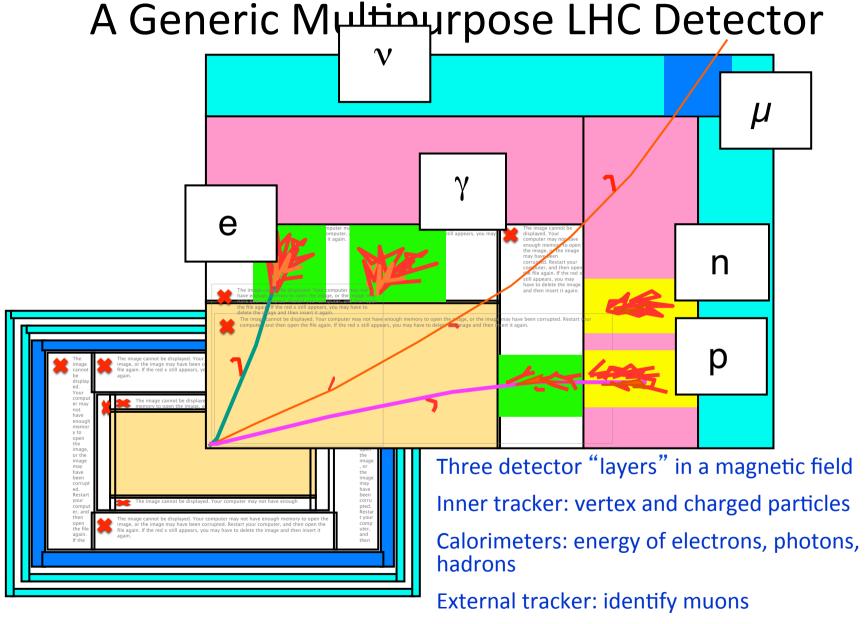
# Floating Point in Experimental HEP Data Processing (aka Reconstruction)

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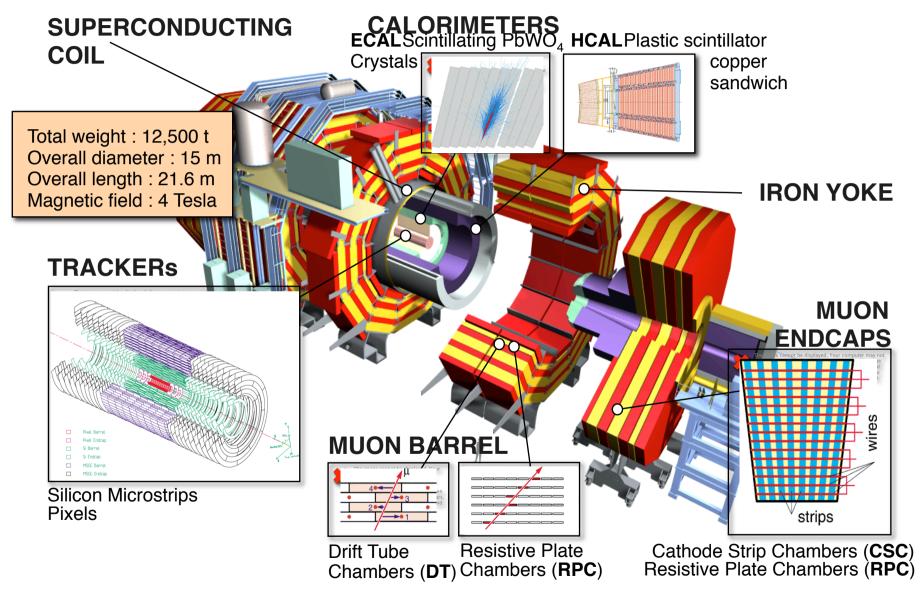
CERN

PH/SFT & CMS





# An experiment: CMS



#### Data and Algorithms

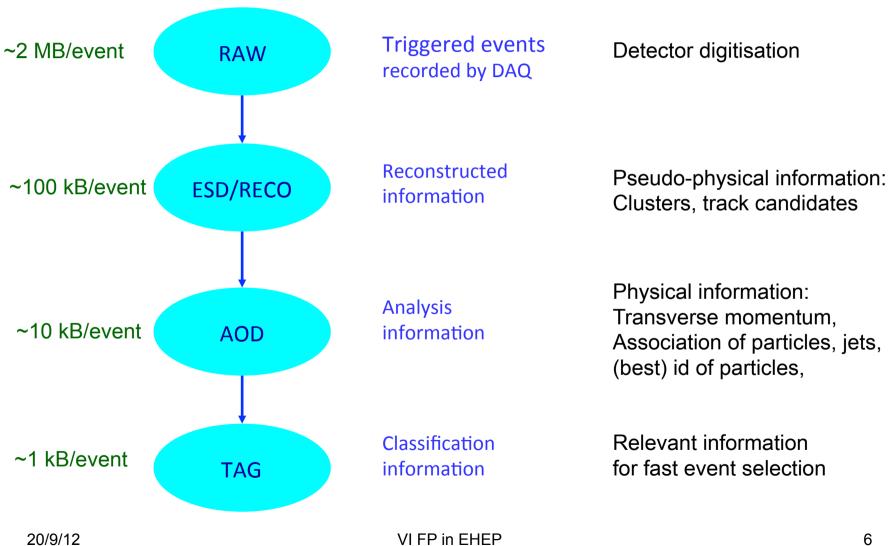
- HEP main data are organized in Events (particle collisions)
- Simulation, Reconstruction and Analysis programs process "one Event at the time"
  - Events are fairly independent of each other
  - Trivial parallel processing
- Event processing programs are composed of a number of Algorithms selecting and transforming "raw" Event data into "processed" (reconstructed) Event data and statistics
  - Algorithms are mainly developed by "Physicists"
  - Algorithms may require additional "detector conditions" data (e.g. calibrations, geometry, environmental parameters, etc.)
  - Statistical data (histograms, distributions, etc.) are typically the final data processing results

# High Energy Analysis Model

Real Data MC Data Comparison Reconstruction "goes **MonteCarlo GenParticles Particles** back in time" from Simulation follows digital signals to the the evolution of original particles **MCParticles** physics processes ProtoParticles produced in the from collision to collision digital signals **Tracks MCHits Clusters MCDeposits Digits MCDigits** (Raw data) Processing'

Analysis compares (at statistical level) reconstructed events from real data with those from simulation

#### **Data Hierarchy** "RAW, ESD, AOD, TAG"



# Analogies with Industry

- Signal/image processing
  - DAC (including calibrations)
  - Pattern recognition, "clustering"
- Topological problems
  - Closest neighbor, minimum path, space partitioning
- Gaming (our main source of inspiration!)
  - "walk-through" complex 3D geometries
  - Detection of "collisions"
- Navigation/Avionics (Kalman filtering)
  - Tracking in a force field in presence of "noise"
  - Trajectory identification and prediction

#### Accuracy, Precision

- Measurement themselves require a modest precision (16,24 bits)
- Geometry/Materials often known at per-cent level
- Dynamic range, when converted in natural units, often requires a high precision FP representation
  - Enengy range >10<sup>9</sup>
  - Position: micron over 20m
- Many conversions back and forth various coordinate/measurement systems
- Error manipulation (including correlations)
  - Squared quantities: each transformation requires two matrix multiplications

## FP operations in reconstruction

- Signal calibration
  - Ideal for vectorization
    - (if was not that calib requires lookup!)
    - Calib-params may depend on "reconstructed quantities"
- "Geometry" transformation
  - Trigonometry (also log/exp!)
  - Small matrices (max 5x5, 6x6)
- Many logs, exp coming from parameterizations

#### Vectorization?

- Current code design and implementation often hinder vectorization
  - High granularity "naïve" object model
  - Fragmentation in several libraries (plugin model)
    - Ito will not help
  - "Linear thinking" conditional code
- Only a massive redesign of data-structures and algorithms will make vectorization effective
  - Not alone: see
    - http://research.scee.net/files/presentations/gcapaustralia09/ Pitfalls of Object Oriented Programming GCAP 09.pdf
    - http://www.slideshare.net/DICEStudio/introduction-to-dataoriented-design

# Typical Profile (today)

CPI (cycle per instruction): 0.9636

load instructions %: 30.577%

store instructions %: 13.737%

load and store instructions %: 44.314%

resource stalls % (of cycles): 30.631%

branch instructions % (approx): 17.065%

% of branch instr. mispredicted: 2.247%

% of L3 loads missed: 2.087%

computational x87 instr. %: 0.038%

% of SIMD in all uops: 19.22%

% of comp. SIMD in all uops: 10.17%

breakdown: %of all uops % of all SIMD

PACKED DOUBLE: 0.663% 3.449%

PACKED SINGLE: 0.613% 3.190%

SCALAR DOUBLE: 13.485% **70.159**%

SCALAR\_SINGLE: 4.038% 21.010%

VECTOR INTEGER: 0.421% 2.192%

#### More details (see next page):

Function where time is spent most

- No hot-spot: top 30 each between 2.5% and 0.5% of total
- Trig/trans functions
- div/sqrt latency

BR_INST_EXEC.IND	RECT_NON_CALL \$	UOPS_RETIRED.	STALL_CYCLES \$	ARITH.CYCLE	ES_DIV_BUSY \$	Function -+	
9.5e+07	5.30 %	8.1e+09	41.41 %	2e+09	10.07 %	ieee754_exp	
3.5e+08	13.71 %	8.1e+09	45.49 %	0	0.00 %	arena_malloc_small	
6.7e+06	0.23 %	7.5e+09	47.55 %	3.8e+09	24.31 %	ieee754_atan2	
6.6e+07	46.92 %	9.9e+09	63.11 %	4.2e+09	26.82 %	<pre>void TkGluedMeasurementDet::doubleMatch&lt; .</pre>	
1.9e+08	15.15 %	4.9e+09	33.67 %	0	0.00 %	arena_dalloc_bin	
1.4e+08	7.66 %	9.6e+09	68.94 %	5.9e+09	42.28 %	ThirdHitPredictionFromCircle::phi(double	
3.4e+07	1.05 %	6e+09	43.11 %	3.6e+09	25.47 %	atanf	
3.9e+08	17.85 %	7.8e+09	58.89 %	0	0.00 %	free	
4.4e+07	2.68 %	8.5e+09	65.22 %	2.4e+09	18.60 %	ieee754_acos	
2.5e+07	2.56 %	4.3e+09	34.11 %	1.1e+08	0.90 %	ROOT::Math::SMatrix <double, (unsigned="" in<="" th=""></double,>	
1.1e+07	11.71 %	4.4e+09	41.21 %	0	0.00 %	cms::TrackListMerger::produce(edm::Event	
8.5e+07	204.00 %	8.6e+09	81.25 %	4.2e+09	39.96 %	magfieldparam::TkBfield::Bcyl(double, do	
6.2e+06	0.59 %	4.6e+09	46.46 %	5.6e+08	5.70 %	ieee754_log	
1.7e+06	0.99 %	4.9e+09	53.99 %	5.6e+07	0.61 %	<unknown(s)></unknown(s)>	
1.8e+08	7.49 %	5.1e+09	59.85 %	2.8e+07	0.33 %	strcmp	
2.6e+08	20.20 %	5.5e+09	67.64 %	2.6e+09	32.26 %	PixelTripletLargeTipGenerator::hitTriple	
0	0.00 %	4.3e+09	57.80 %	1.1e+08	1.51 %	do_lookup_x	
9.3e+07	11.99 %	4.9e+09	66.54 %	3.9e+09	53.23 %	DAClusterizerInZ::update(double, std::ve	
3.4e+07	11.88 %	3.5e+09	48.00 %	3.1e+08	4.22 %	sincos	
1.3e+08	24.73 %	2.5e+09	41.40 %	4.2e+08	6.82 %	PixelTripletHLTGenerator::hitTriplets(Tr	
4.8e+07	19.87 %	4.7e+09	77.57 %	4.5e+08	7.34 %	tan	
0	0.00 %	2.5e+09	45.01 %	0	0.00 %	<unknown(s)></unknown(s)>	
7.3e+07	8.77 %	2.1e+09	37.74 %	5.9e+08	10.71 %	ieee754_atan2f	
9.8e+06	5.74 %	3.9e+09	71.26 %	2e+09	37.42 %	AnalyticalCurvilinearJacobian::computeFu	
8.4e+06	9.26 %	3.4e+09	64.46 %	1.5e+09	28.77 %	JacobianCurvilinearToLocal::JacobianCurv	
7.3e+06	9.85 %	1.7e+09	32.66 %	0	0.00 %	SiStripRecHit2D::sharesInput(TrackingRec	
6.7e+07	24.80 %	3.1e+09	62.12 %	1.2e+09	23.72 %	StripCPEfromTrackAngle::localParameters(	
2.4e+07	17.47 %	2.9e+09	62.58 %	7e+08	15.34 %	std::pair <bool, double=""> Chi2MeasurementE</bool,>	
1.6e+08	13.06 %	1.7e+09	36.84 %	0	0.00 %	arena_malloc	
0	0.09 %	5.3e+08	12.62 %	0	0.00 %	PixelHitMatcher::compatibleSeeds(std::ve	
6.6e+07	23.53 %	2.9e+09	69.80 %	2e+09	47.86 %	ThirdHitPredictionFromCircle::angle(doub	
2.8e+05	5.50 %	1.8e+09	43.09 %	1.7e+09	41.04 %	RectangularPlaneBounds::inside(Point3DBa	
2.8e+05	0.04 %	1.1e+09	28.79 %	0	0.00 %	inflate_fast	
0	0.00 %	2.3e+09	59.12 %	0	0.00 %	fesetenv	

Cost of operations (in cpu cycles)

ор	instruction	sse s	sse d	avx s	avx d
+,-	ADD,SUB	3	3	3	3
== <>	COMISS CMP	2,3	2,3	2,3	2,3
f=d d=f	CVT	3	3	4	4
,&,^	AND,OR	1	1	1	1
*	MUL	5	5	5	5
/,sqrt	DIV, SQRT	10-14	10-22	21-29	21-45
1.f/ , 1.f/sqrt	RCP, RSQRT	5		7	
=	MOV	1,3,	1,3,	1,4,	1,4,

# Cost of functions (in cpu cycles i7sb)

	Gnu libm	Cephes scalar	Cephes autovect	Cephes handvect	Approx (16bits)	Intel svml	Amd libm
	s d	s d	s d	S		s d	s d
sin,cos large x	55 100 > <b>500</b>	30 50	11 30	20		12 30	25 45
sincos	70	40	15	22			50
atan2	50 100	30	13			17 52	67 87
ехр	<b>650</b> 65	42 55	10 23	27		12 26	16 36
log	50 105	37 42	11 28	24	12	12 30	27 59

SET\_RESTORE\_ROUND\_NOEXF (FE\_TONEAREST);

# Where/how can we improve?

- Cost of a sin/cos/exp close to div/sqrt and to the overhead of an indirect function call
  - Inline math functions
    - Help autovectorization too
- Trig-funs spend not negligible time in range reduction
  - Our angles are ALL in [-pi,pi] range
    - Special version for reduced range?
    - Move to "fractional-pi" instead of radiant

# Where/how can we improve?

- Double precision often required to keep under control coordinate system transformations (in particular for the error matrices)
  - Develop more robust algorithms
  - avoid back&forth
  - Choose (dynamically?) units (metrics) to avoid too large dynamic-ranges
- Arguments of log/exp often in a limited range
  - Use specialized implementation
- rsqrt/rcp (+ "tunable" Newton-Raphson)
  - C-implementation in double precision faster than sse!

# Example: multiple scattering

```
double ms(double radLen, double m2, double p2) {
  constexpr double amscon = 1.8496e-4; // (13.6MeV)**2
  double e2 = p2 + m2;
  double beta2 = p2/e2;
  double fact = 1.f + 0.038f*log(radLen); fact *=fact;
  double a = fact/(beta2*p2);
  return amscon*radLen*a;
}
```

Already an approximation

Material density, thickness, track angle Known at percent?

float msf(float radLen, float m2, float p2) {
 constexpr float amscon = 1.8496e-4; // (13.6iMeV)\*\*2
 float e2 = p2 + m2;

```
float fact = 1.f + 0.038f*dirtylogf<2>(radLen); fact /= p2; fact *=fact;
```

float a = e2\*fact; return amscon\*radLen\*a;

return amscon raulen a

VI FP in EHEP

2<sup>nd</sup> order polynomial by FdD

# Verify accuracy of approximation

```
float ref = ms(rl,m2,p2);
float rp = ms(rl*1.001, m2, p2); // 0.1% positive
float rm = ms(rl*0.999, m2, p2); // 0.1% negative
float apx = msf(rl, m2, p2); // fast approximation
                                                        diff is in "bits"
// look if approximation inside uncertainty-interval
int dd = std::min(abs(diff(rm,ref)),abs(diff(rp,ref)));
dd -= abs(diff(apx,ref)); # negative if apx-ref is larger than the uncer-interval
dm = std::min(dm,dd);
da = std::max(da,abs(diff(apx,ref))); // maximum "error" by approx
di = std::max(di,abs(diff(rp,ref)));
di = std::max(di,abs(diff(rm,ref))); // maximum uncertantly
// ditto for minimum
```

- 0.1% accuracy corresponds to a difference of 13-14 bits
- Maximum error of the approximation is ~12 bits
- "dm" always positive

## One More example

- In CMS the Vavilov distribution is used to compute the probability of a cluster in a Silicon Detector to come from a m.i.p.
  - It is then encoded in an 8-bit quality word
- Precision tuned-down while verifying that the final result (the 8-bits!) do not change
- Speed up of a factor 3...

# Summary

- FP accounts for ~20% of HEP reconstruction
  - Mostly double (for no good reason?)
  - Not easy to vectorize as it stands
  - Large use of std math-function
- glibm: excellent full-precision reference
  - An overkill for any practical application
- Opportunities for improvements
  - Move to Data-oriented-Design
  - Reduce branches and indirect-calls
  - Use fast (less precise, limited-range) math-fun
  - Use metrics that will allow the use of floats
  - Systematically verify required accuracy