

Hadron structure and spectroscopy with COMPASS using π and μ beams the unusual way

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based on works with

IV Anikin, M. Diehl, L. Szymanowski, J.P. Lansberg, OV Teryaev, S Wallon

a simplistic outsider view

⇒ Success of π beams : spectroscopy

→ beautiful $\pi_1(1600)$ discovery

⇒ Success of μ beams : hadronic structure

→ $\Delta G(x)$ historical measurements , TMDs

near future : GPDs through DVCS and other exclusive channels

MY PROPOSAL :

⇒ use π beams to explore the structure of proton in exclusive processes (= one limit of the Drell Yan program)

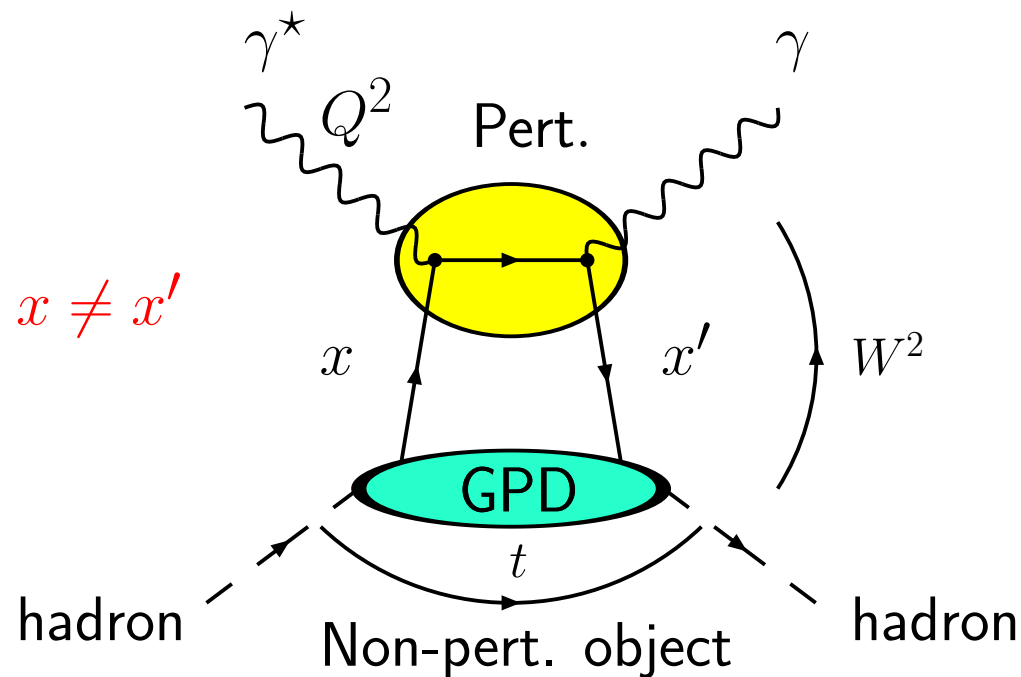
⇒ use μ beams to analyze the hybrid meson $\pi_1(1600)$
(= one limit of the DEMP program)

Plan of the talk

- ⇒ use π beams to explore the structure of proton in **exclusive** processes (= **two limits of Drell Yan**)
 - **Forward exclusive** $\pi N \rightarrow \mu^+ \mu^- N'$ Accessing GPDs $\tilde{E}$ and $\tilde{H}$
 - **Backward exclusive** $\pi N \rightarrow \mu^+ \mu^- N'$ Accessing $\pi \rightarrow N$ TDAs
 - **discover the exclusive K factor**
- ⇒ use μ beams to analyze the 1^{-+} **hybrid** meson $\pi_1(1600)$
 - **scrutenize the hybrid DA**, namely its $\bar{q}q$ Fock state (*sic*)
- ⇒ use quasi real γ beams for Drell Yan pairs on transv. pol. target
 - **scrutenize the γ chiral odd DA and $h_1(x)$**

Success of factorized description of DVCS/TCS

$\gamma^* N \rightarrow \gamma^* N'$ in terms of **Generalized Parton Distributions**

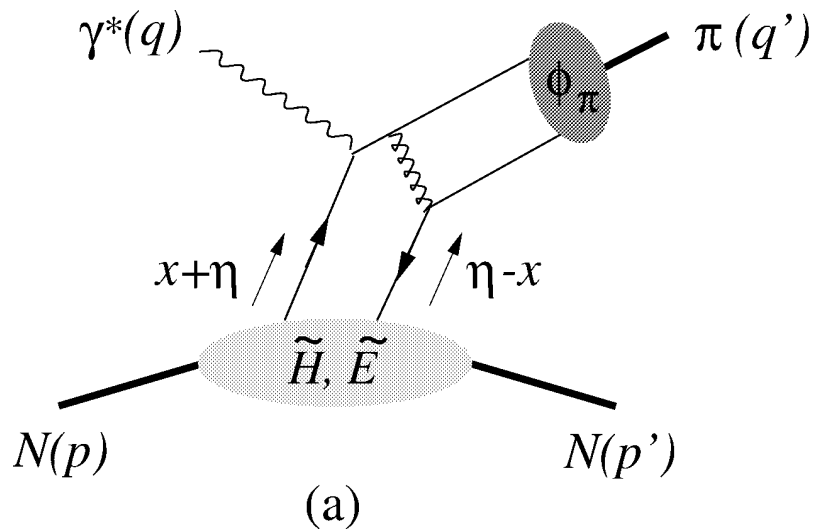


$\gamma^* N \rightarrow \gamma N'$ and $\gamma N \rightarrow \gamma^* N'$ in terms of **the same** GPDs, the same LO coeff. function and **different** NLO contributions

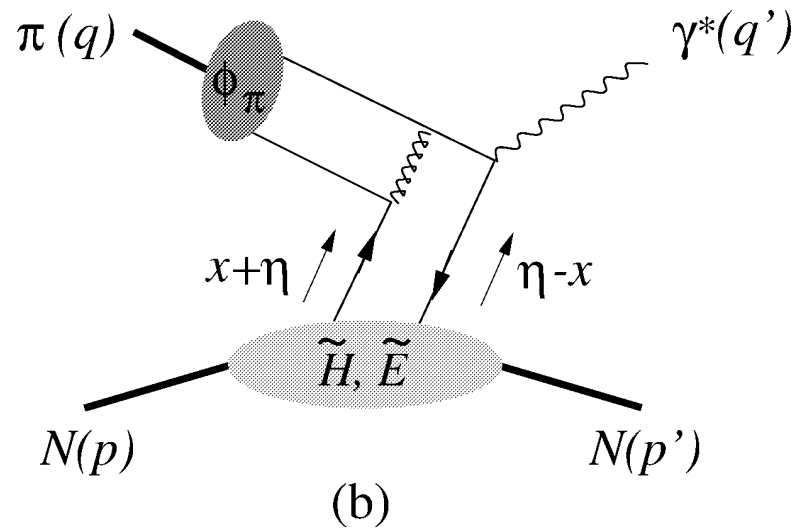
$$\gamma^* N \rightarrow \pi N' \text{ and } \pi N \rightarrow \gamma^* N'$$

E. Berger, M. Diehl, BP, Phys Lett. B523

Pion beams reveal $\tilde{H}, \tilde{E}$ Generalized Parton distributions



spacelike



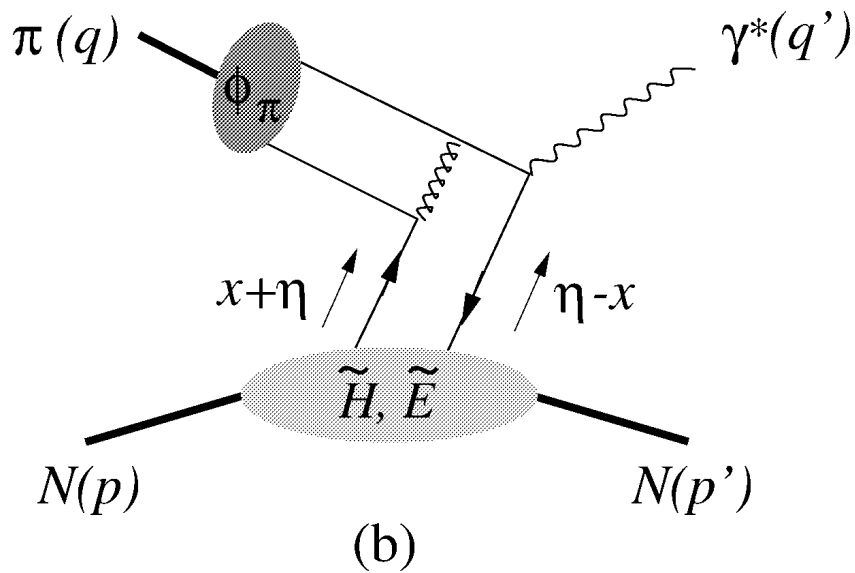
timelike

(= Exclusive Limit of Drell Yan process)

COMPASS with μ beams $\iff$ COMPASS with π beams

Exclusive lepton pair production in πN scattering

$$\pi^- p \rightarrow \gamma^* n \rightarrow \mu^+ \mu^- n$$



Bjorken variable $\tau = \frac{Q'^2}{s-M^2}$

skewness $\eta = \frac{(p-p')^+}{(p+p')^+} = \frac{\tau}{2-\tau}$

$$\frac{d\sigma}{dQ'^2 dt d(\cos \theta) d\varphi} = \frac{\alpha_{\text{em}}}{256 \pi^3} \frac{\tau^2}{Q'^6} \sum_{\lambda', \lambda} |M^{0\lambda', \lambda}|^2 \sin^2 \theta$$

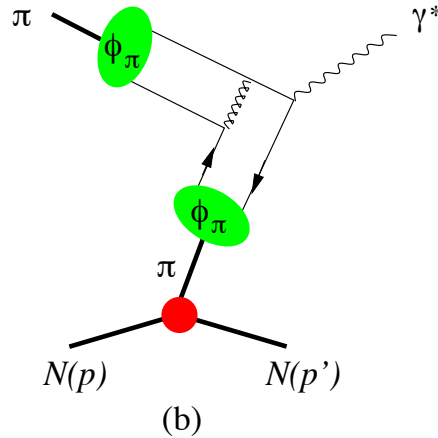
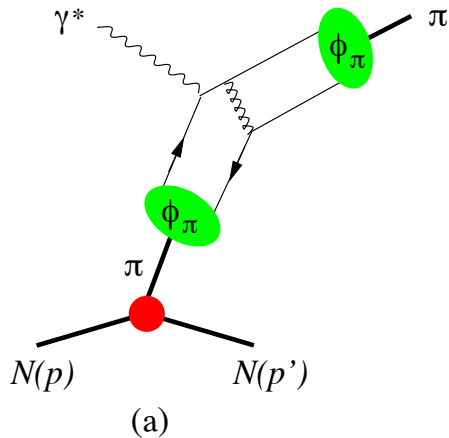
$$M^{0\lambda', \lambda}(\pi^- p \rightarrow \gamma^* n) = -ie \frac{4\pi}{3} \frac{f_\pi}{Q'} \frac{1}{(p+p')^+} \bar{u}(p', \lambda') \left[\gamma^+ \gamma_5 \tilde{\mathcal{H}}^{du}(\eta, t) + \gamma_5 \frac{(p'-p)^+}{2M} \tilde{\mathcal{E}}^{du}(\eta, t) \right] u(p, \lambda)$$

$$\tilde{\mathcal{H}}^{du}(\eta, t) = \frac{8\alpha_S}{3} \int_{-1}^1 dz \frac{\phi_\pi(z)}{1-z^2} \int_{-1}^1 dx \left[\frac{e_d}{-\eta-x-i\epsilon} - \frac{e_u}{-\eta+x-i\epsilon} \right] [\tilde{H}^d(x, \eta, t) - \tilde{H}^u(x, \eta, t)]$$

$\tilde{H}$ and $\tilde{E}$ GPDs

$\Rightarrow \tilde{H}(x, \xi = 0, t = 0) = \Delta q(x)$

$\Rightarrow \tilde{E}$ unknown : Pion pole dominance often assumed

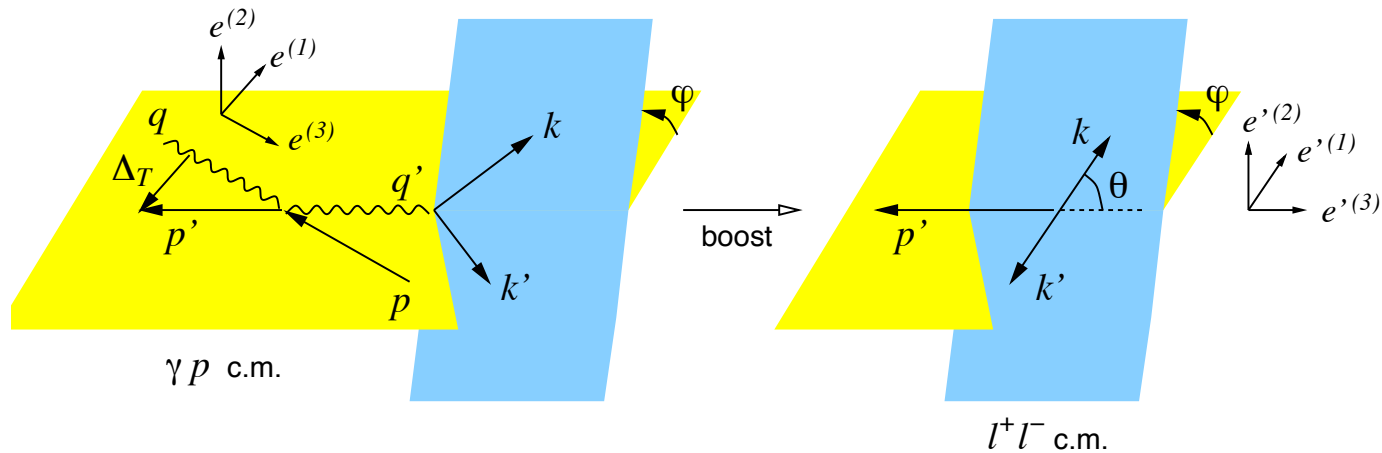


to be tested

$\Rightarrow t$ -dependence $\rightarrow$ **proton femtography**

Lepton angular distribution

Dominant Amplitude : **longitudinal** γ^*



$$\frac{d\sigma}{dQ'^2 dt d(\cos \theta) d\varphi} = \frac{\alpha_{\text{em}}}{256 \pi^3} \frac{\tau^2}{Q'^6} \sum_{\lambda', \lambda} |M^{0\lambda', \lambda}|^2 \sin^2 \theta$$

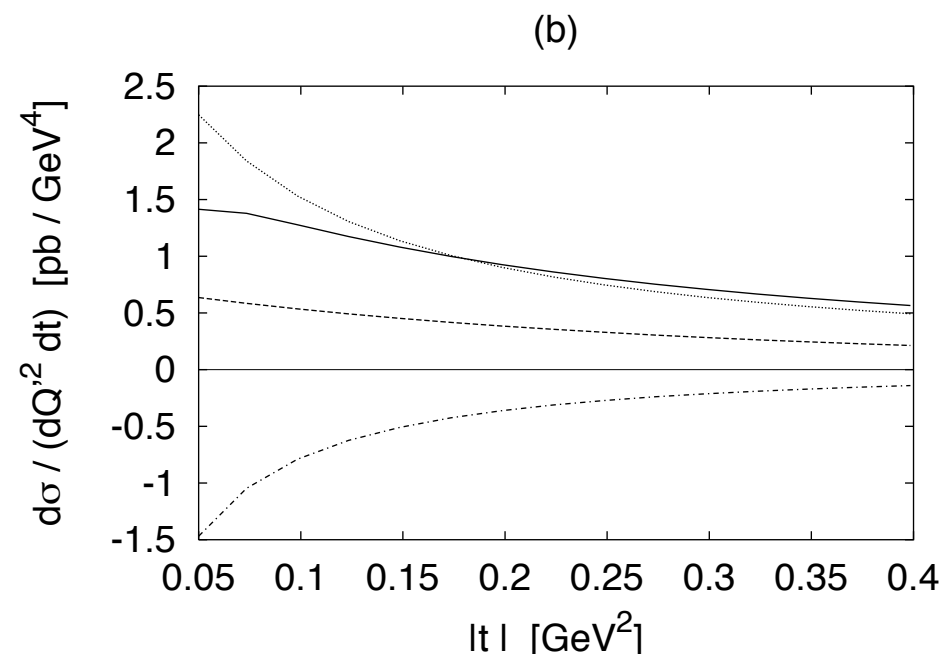
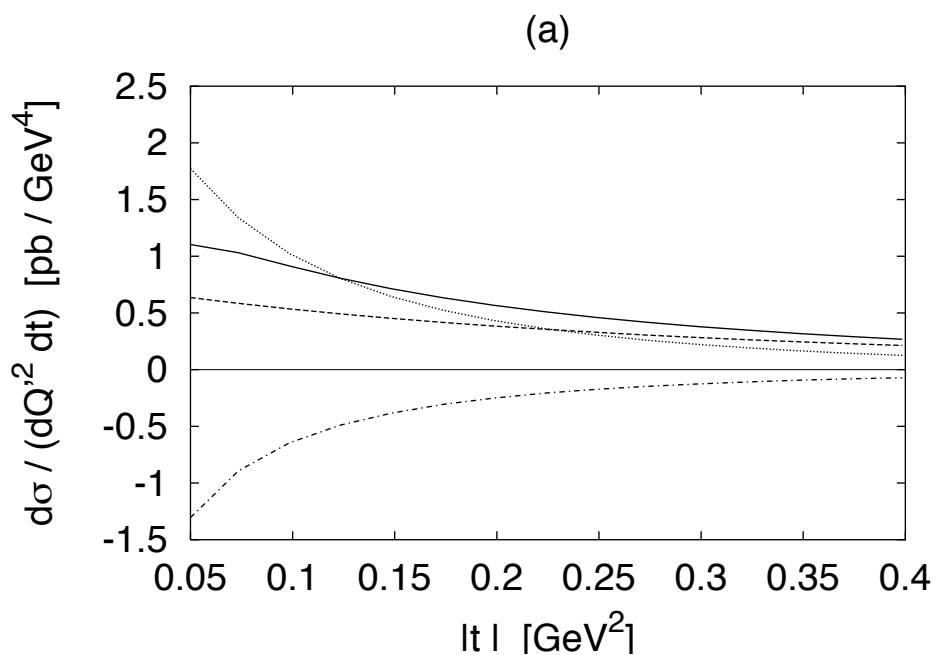
Crucial Test of the validity of the twist expansion

if σ_T not small, extract **GPDs** from σ_L only !

LO Estimates

E. Berger, M. Diehl, BP, Phys Lett. B523

$$Q'^2 = 5 \text{ GeV}^2 \quad \tau = 0.2$$



(dashed) = $|\tilde{\mathcal{H}}|^2$; (dash-dotted) = $\text{Re}(\tilde{\mathcal{H}}^* \tilde{\mathcal{E}})$; (dotted) = $|\tilde{\mathcal{E}}|^2$.

Target Transverse Spin asymmetry

At the twist 2 level : $\frac{d^\uparrow\sigma - d^\downarrow\sigma}{d^\uparrow\sigma + d^\downarrow\sigma} = A_{\text{UT}}^{\sin(\phi - \phi_S)} \sin(\phi - \phi_S) + \text{other harmonics}$

$$A_{UT} = \frac{-2 \sqrt{\frac{t-t_{\min}}{t_{\min}}} \eta^2 \operatorname{Im}(\tilde{\mathcal{H}} \tilde{\mathcal{E}}^*)}{(1-\eta^2)|\tilde{\mathcal{H}}|^2 - \frac{t}{4M^2} |\eta \tilde{\mathcal{E}}|^2 - 2\eta^2 \operatorname{Re}(\tilde{\mathcal{H}} \tilde{\mathcal{E}}^*)}$$

⇒ New information on GPDs.

e.g. if $\tilde{E}$ is well modeled by pion pole, $\tilde{\mathcal{E}}$ is real $\rightarrow A_{UT} \sim \tilde{H}(x, \xi = x, t)$

NLO analysis not done

At **LO**, space - and timelike amplitudes are **related**

$$M^{0\lambda',\lambda}(\pi^- p \rightarrow \gamma^* n) = \left[M^{\lambda',0\lambda}(\gamma^* p \rightarrow \pi^+ n) \right]^*$$

At **higher** orders, significant **differences** expected

→ critical check of the **universality** of GPDs and of **factorization**.

Status of spacelike $\gamma^*(Q)p \rightarrow \pi N$

Data from HERMES :

$\sigma_T + \epsilon\sigma_L$ σ_T VS σ_L ?

(also data from JLab)

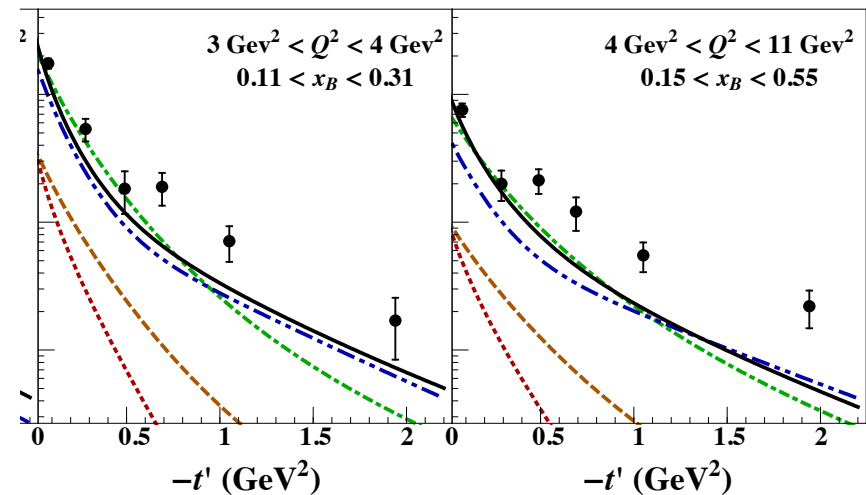
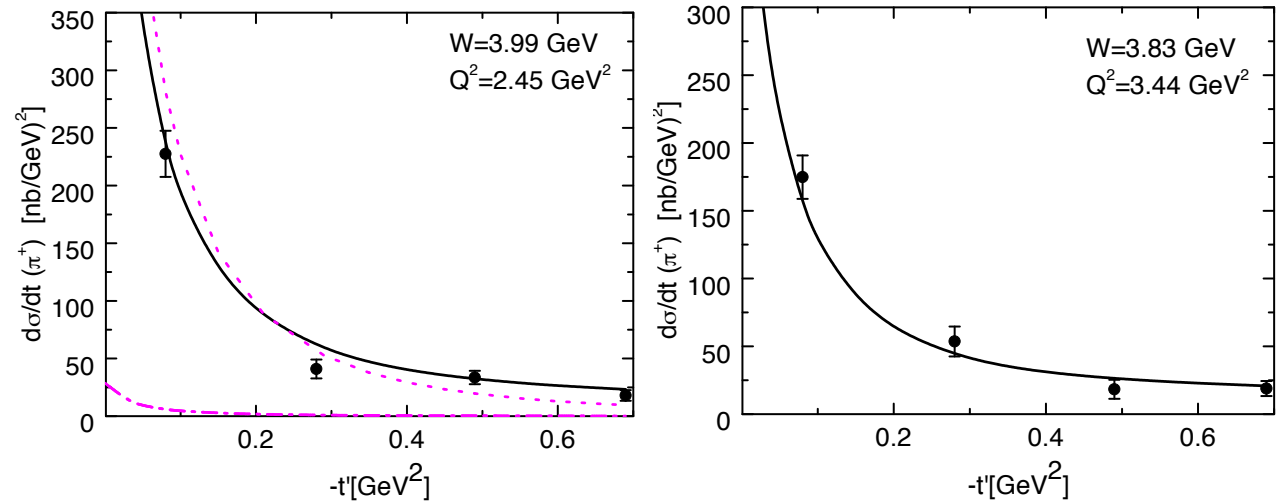
2 contradictory phenom. analysis

π -exchange with exp FF ;

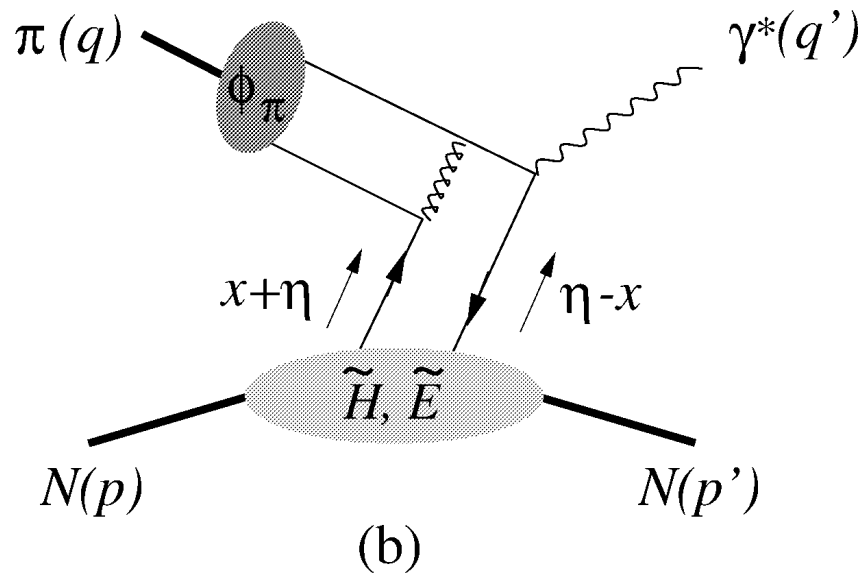
S. Goloskokov and P.Kroll, EPJ, C65

QCD with $\alpha_S = .8$

C. Bechler, D. Muller, ArXiv 0906.2571



Compass Opportunity



Sufficient rates ($O(1 - 10/\text{hour})$)

Transverse spin asymmetry

$$1 < q'^2 < 10 \text{ GeV}^2, \quad \text{small } t = (q - q')^2, \quad \text{fixed } \xi = \frac{p_N^+ - p_{N'}^+}{p_{N'}^+ + p_N^+}$$

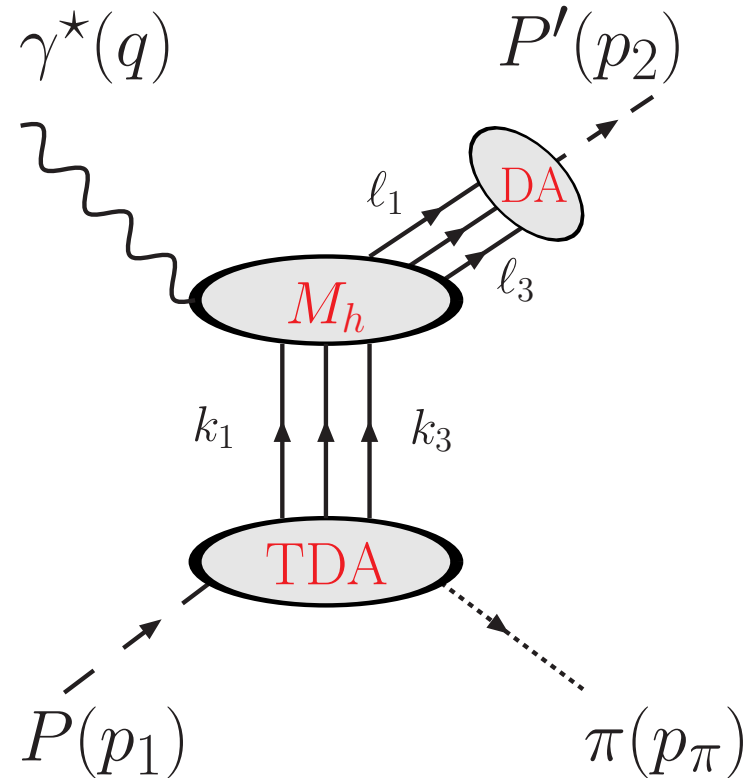
Measure lepton pair momentum ; deduce missing mass² = $\bar{M}^2$.

Select small $\bar{M}^2 \approx M_p^2$. ((or detect final proton with recoil detector?))

Small ξ : lepton pair forward.

How to factorize backward leptonproduction $\gamma^* N \rightarrow N' \pi$

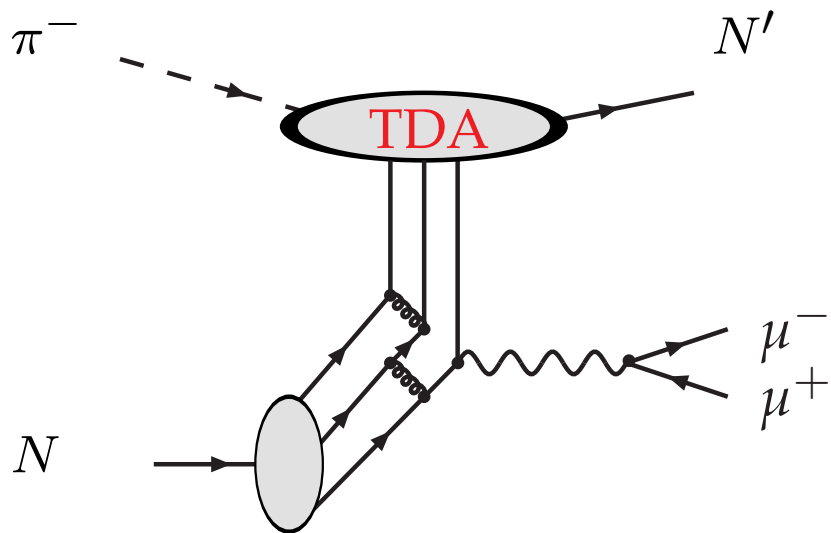
BP, L Szymanowski, PRD71 and PLB622



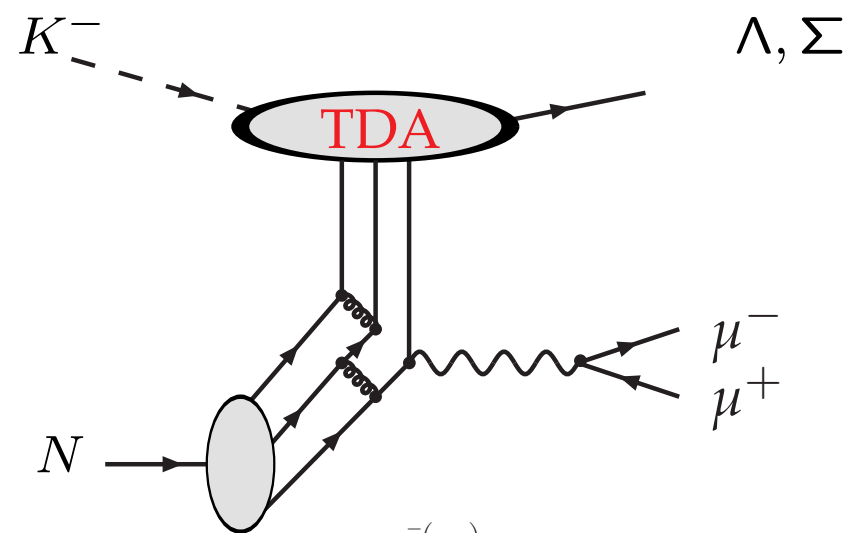
at large q^2 , small $u = (p_1 - p_\pi)^2$, fixed $\xi = \frac{p_{N'}^+ - p_\pi^+}{p_{N'}^+ + p_\pi^+}$

→ factorize timelike versions of backward $\gamma^* N \rightarrow N' \pi$

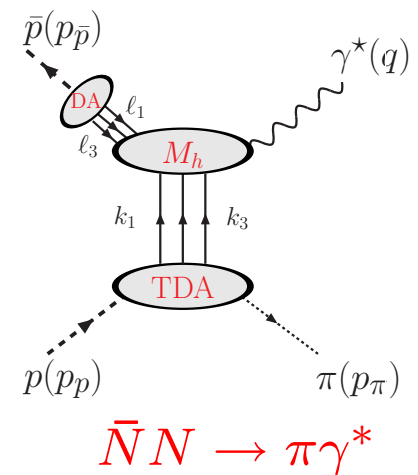
$$\pi N \rightarrow N' \gamma^*(Q')$$



$$K^- N \rightarrow \Lambda \gamma^*(Q') \rightarrow \Lambda \mu^- \mu^+$$



at large Q'^2 , small $u = (p_{N'} - p_\pi)^2$, fixed ξ



$$\bar{N} N \rightarrow \pi \gamma^*$$

Interpretation of the $(\pi \rightarrow N)_{or}(N \rightarrow \pi)$ TDAs

Develop proton wave function as (schematically) $|qqq\rangle + |qqq\pi\rangle + \dots$

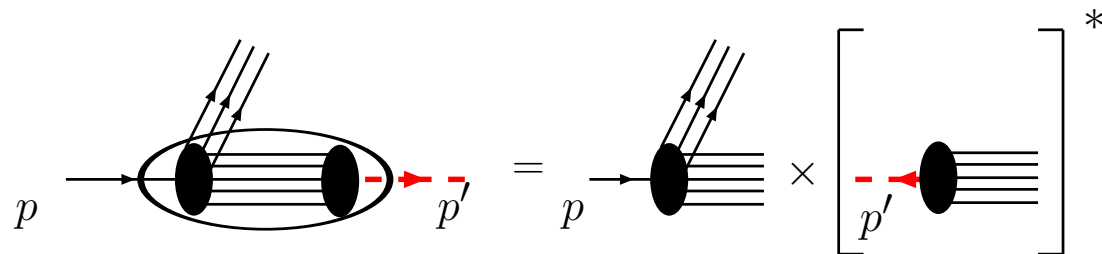
$|qqq\rangle$ is described by proton DA : $\langle 0 | \epsilon^{ijk} u_{\alpha}^i(z_1 n) u_{\beta}^j(z_2 n) d_{\gamma}^k(z_3 n) | p(p, s) \rangle \Big|_{z^+=0, z_T=0}$

Define matrix elements sensitive to $|qqq \pi\rangle$ part : the **TDAs**

$$\langle \pi(p') | \epsilon^{ijk} u_{\alpha}^i(z_1 n) u_{\beta}^j(z_2 n) d_{\gamma}^k(z_3 n) | p(p, s) \rangle \Big|_{z^+=0, z_T=0}$$

light cone matrix elements of operators obeying usual RG evolution equations

⇒ The $\pi \rightarrow N$ TDAs provides information on the next to minimal Fock state in the baryon



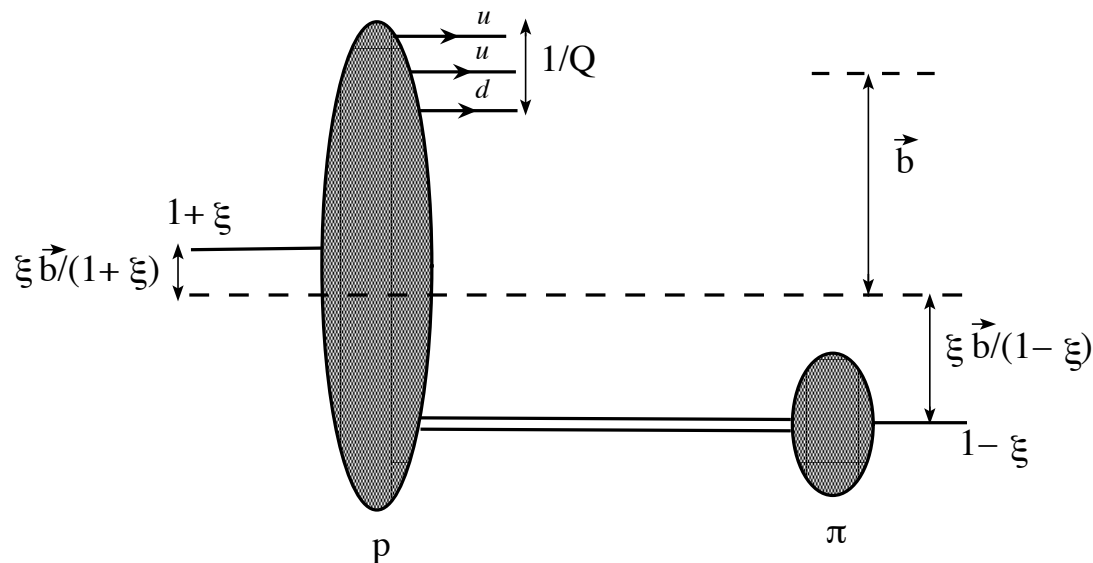
Proton = $|u d d \pi^+ \rangle$ with small transverse separation for the quark triplet

Impact parameter interpretation

- As for GPDs **Fourier transform** $\Delta_T \rightarrow b_T$

$$F(x_i, \xi, u = \Delta^2) \rightarrow \tilde{F}(x_i, \xi, b_T)$$

→ **Transverse** picture of **pion cloud** in the proton



if factorization works

Define Transition Distribution Amplitudes

- Dirac decomposition at leading twist :

$$4 \langle \pi^0(p') | \epsilon^{ijk} u_\alpha^i(z_1) u_\beta^j(z_2) d_\gamma^k(z_3) | p(p, s) \rangle \Big|_{z^+=0, z_T=0} =$$

$$\frac{-f_N}{2f_\pi} \left[V_1^0(\hat{P}C)_{\alpha\beta}(B)_\gamma + A_1^0(\hat{P}\gamma^5 C)_{\alpha\beta}(\gamma^5 B)_\gamma - 3T_1^0(P^\nu i\sigma_{\mu\nu} C)_{\alpha\beta}(\gamma^\mu B)_\gamma \right] +$$

$$V_2^0(\hat{P}C)_{\alpha\beta}(\hat{\Delta}_T B)_\gamma + A_2^0(\hat{P}\gamma^5 C)_{\alpha\beta}(\hat{\Delta}_T \gamma^5 B)_\gamma + T_2^0(\Delta_T^\mu P^\nu \sigma_{\mu\nu} C)_{\alpha\beta}(B)_\gamma$$

$$+ T_3^0(P^\nu \sigma_{\mu\nu} C)_{\alpha\beta}(\sigma^{\mu\rho} \Delta_T^\rho B)_\gamma + \frac{T_4^0}{M}(\Delta_T^\mu P^\nu \sigma_{\mu\nu} C)_{\alpha\beta}(\hat{\Delta}_T B)_\gamma$$

$B =$ nucleon spinor

$V_i(z_i), A_i(z_i), T_i(z_i)$ are the TDAs

V_1 and T_1 dominant . If isospin = 1/2, $T_1 = f(V_1)$

- Fourier transform each TDA, $\rightarrow$ momentum fractions representation

$$F(z_i) = \int_{-1+\xi}^{1+\xi} d^3x \delta(\sum x_i - 2\xi) e^{-iPn \sum x_i z_i} F(x_1, x_2, x_3, \xi, t, Q^2)$$

$$F = V_i, A_i, T_i$$

⇒ Write the **Amplitude** ($\pi N(p_2) \rightarrow N'(p_1) \mu^+ \mu^-$)

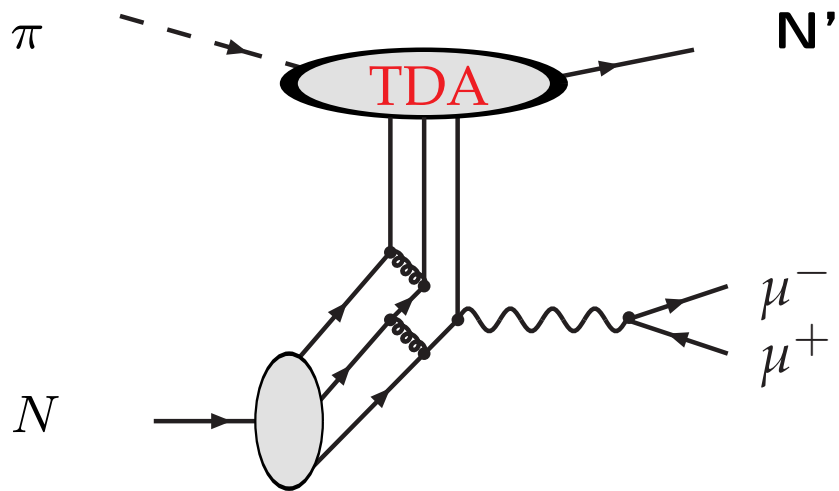
$$\mathcal{M}_{s_1 s_2}^\lambda = -i \frac{(4\pi\alpha_s)^2 \sqrt{4\pi\alpha_{\text{em}}} f_N^2}{54 f_\pi Q^4} \left[\underbrace{\bar{u}(p_2, s_2) \not{\epsilon}(\lambda) \gamma^5 u(p_1, s_1)}_{\mathcal{S}_{s_1 s_2}^\lambda} \underbrace{\int_{-1+\xi}^{1+\xi} d^3x \int_0^1 d^3y \left(2 \sum_{\alpha=1}^7 T_\alpha + \sum_{\alpha=8}^{14} T_\alpha \right)}_I \right. \\ \left. - \underbrace{\epsilon(\lambda)_\mu \Delta_{T,\nu} \bar{u}(p_2, s_2) (\sigma^{\mu\nu} + g^{\mu\nu}) \gamma^5 u(p_1, s_1)}_{\mathcal{S}'_{s_1 s_2}^\lambda} \underbrace{\int_{-1+\xi}^{1+\xi} d^3x \int_0^1 d^3y \left(2 \sum_{\alpha=1}^7 T'_\alpha + \sum_{\alpha=8}^{14} T'_\alpha \right)}_{I'} \right],$$

= baryon helicity conserving + baryon helicity violating amplitudes

⇒ The **Hard Amplitude** is calculated from 21 Feynman diagrams

Interference of $\mathcal{S}$ and $\mathcal{S}' \rightarrow$ Transverse spin asymmetry

Compass Opportunity



also with Kaon beam

($N' \rightarrow \Lambda$)

$$1 < Q^2 < 10 \text{ GeV}^2, \quad \text{small } u = (p_\pi - p_{N'})^2, \quad \text{fixed } \xi = \frac{p_\pi^+ - p_{N'}^+}{p_{N'}^+ + p_\pi^+}$$

Measure lepton pair momentum ; deduce missing mass² = $\bar{M}^2$.

Select small $\bar{M}^2 \approx M_p^2$.

Small $u = (p_{\text{target}} - q)^2$: lepton pair almost at rest in lab frame

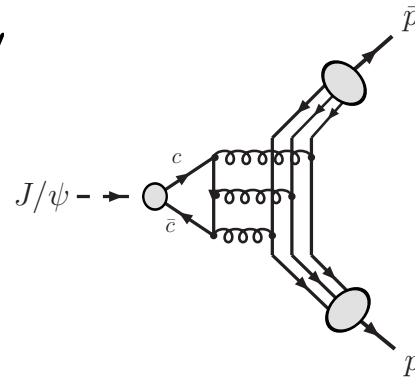
Transverse Target spin asymmetry

Recall $\mathcal{M} = \mathcal{S}T_i + \mathcal{S}'T'_i$; $\mathcal{S}(\mathcal{S}')$ is Nucleon helicity conserving (violating)

- ⇒ Comes from Interference of $\mathcal{S}$ and $\mathcal{S}'$
- ⇒ Leading twist (i.e. not $1/Q^2$) **in eN and $\bar{N}N$ reactions**
- ⇒ zero **in πN reaction**
- ⇒ Proportionnal to **$\mathcal{I}m$** ($T_i T_j'^*$)
 - ⇒ absent in a hadronic (nucleon exchange) description
 - ⇒ i.e. specific to a partonic (TDA) description
- **transversally polarized Λ in $KN \rightarrow \Lambda \mu^+ \mu^-$**

Extending Drell Yan to charmonium case : $\pi N \rightarrow N'\psi$

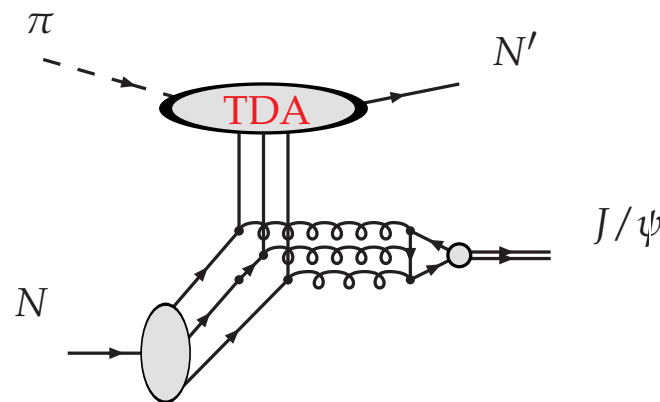
⇒ Recall $\psi \rightarrow \bar{p}p$ decay



the amplitude of which is described with the help of proton (and $\bar{p}$) DAs

⇒ Replace antiproton DA by $\pi \rightarrow N$ TDA

$$\xi \approx \frac{M_\psi^2}{2s_{\pi N}}$$



ψ is isoscalar $\rightarrow$ Isospin $\frac{1}{2}$ part of $\pi \rightarrow N$ TDA selected by hard amplitude

Tests of the applicability of the TDA framework

The process amplitude Factorizes at large enough Q^2 :

$$\mathcal{M}(Q^2, \xi, t) = \int dx dy \phi(y_i) T_H(x_i, y_i, Q^2) F(x_i, \xi, t)$$

You know that you reach the right domain if you check :

- **scaling law** for the amplitude : $\mathcal{M}(Q^2, \xi) \sim \frac{\alpha_s(Q^2)^2}{Q^4}$, (up to log corrections)
 - Dominance of **transversely** polarized virtual photon $\sigma_T \gg \sigma_L$
- ⇒ **crucial test** : **Universality** of TDAs → this description applies as well to **spacelike and timelike** reactions

→ **Backward DEMP** $\gamma^* P \rightarrow P' \pi$ and **Backward** $\pi N \rightarrow N' \gamma^*$

Data exist (JLab) for Q^2 up to a few GeV^2 → More to come !

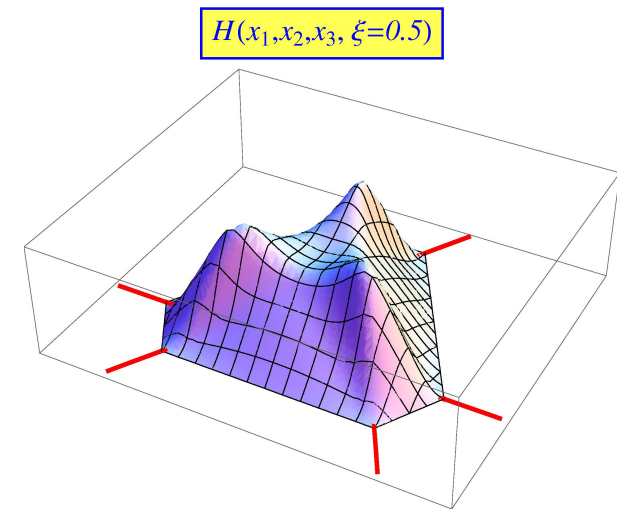
Conclusions

⇒ Exclusive limit of Drell Yan reactions with π (K and $\bar{p}$?) beams will yield crucial information on **GPDs and TDAs**!

GPD and TDA physics explore confinement dynamics in hadrons

⇒ Recent theoretical progress

- Quadruple distribution representation
- Isospin relations
- N and Δ exchange models

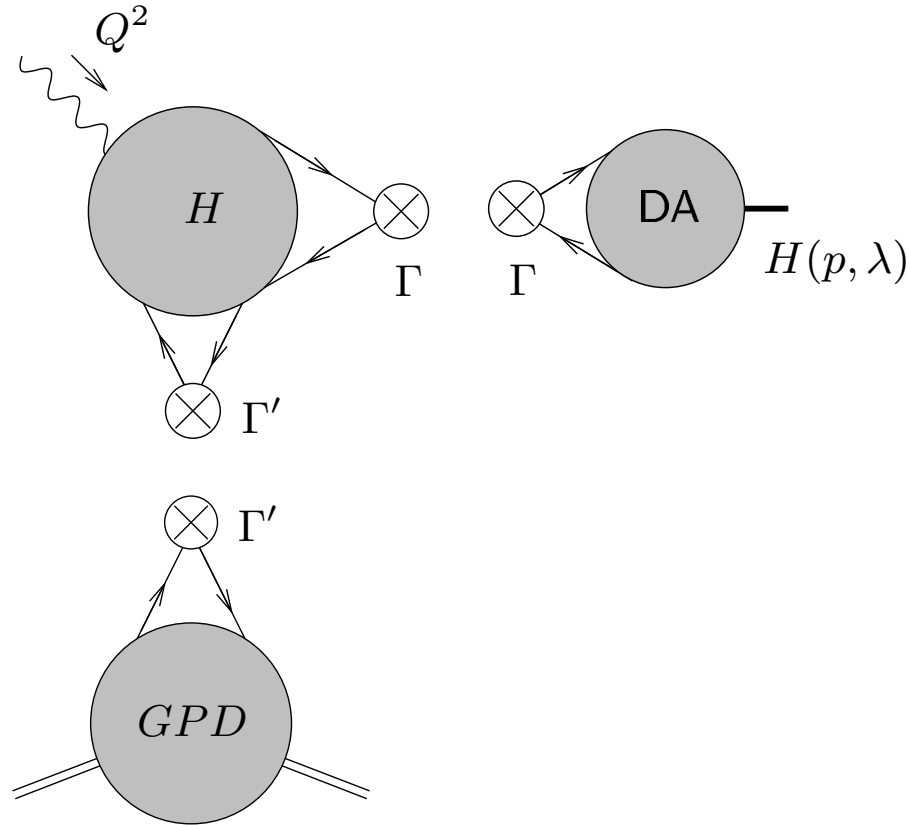


- ⇒ Experimental breakthrough **expected** from **COMPASS** :
- **first** measurements of $\tilde{H}(x, \xi, t)$, $\tilde{E}(x, \xi, t)$ at **small** ξ in spacelike **and** timelike cases
 - **first** measurements of TDA in a timelike regime

HARD μ oPRODUCTION OF EXOTIC HYBRID

IV Anikin, BP, L.Szymanowski, OV Teryaev, S Wallon, Phys. Rev D70 and D71

Factorization framework



⇒ **AIM** : measure **DA** of the hybrid already discovered

(we discussed $\pi_1(1400) \rightarrow \pi\eta$ specific case ; also applicable to $\pi_1(1600)$)

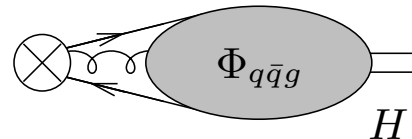
The crucial non perturbative parts

$$\begin{array}{l}
 \begin{array}{c} \text{Diagram 1: A circle labeled 'DA' with a horizontal line to its right. A vertex labeled Γ is connected to the left side of the circle by two lines. The label $H(p, \lambda)$ is placed below the circle.} \end{array} & = \langle H(p, \lambda) | \mathcal{O}(\Psi, \bar{\Psi} A) | 0 \rangle & \text{matrix element of a non-local light-cone operator} \\
 \begin{array}{c} \text{Diagram 2: A circle labeled 'GPD' with two lines entering from the bottom. A vertex labeled Γ' is connected to the top of the circle by two lines.} \end{array} & = \langle N(p') | \mathcal{O}'(\Psi, \bar{\Psi} A) | N(p) \rangle & \text{matrix element of a non-local light-cone operator}
 \end{array}$$

The TWIST 2 DA of the EXOTIC HYBRID

Distribution amplitude of exotic hybrid mesons at twist 2

- One may think that to produce $|q\bar{q}g\rangle$, the fields Ψ , $\bar{\Psi}$, A should appear explicitly in the non-local operator $\mathcal{O}(\Psi, \bar{\Psi}, A)$



- If one tries to produce $H = 1^{-+}$ from a **local operator**, the dominant operator should be $\bar{\Psi}\gamma^\mu G_{\mu\nu}\Psi$ of **twist** = dimension - spin = 5 - 1 = 4
- It means that there should be a $1/Q^2$ suppression in the production amplitude of H with respect to usual ρ -production (which is twist 2)
- But one of the main progress is the understanding of hard exclusive processes in terms of **non-local light-cone operators**, like the **twist 2 operator**

$$\bar{\psi}(-z/2)\gamma_\mu[-z/2; z/2]\psi(z/2)$$

where $[-z/2; z/2]$ is a **Wilson line** which thus hides gluonic degrees of freedom: **the needed gluon is there, at twist 2**. This does not require to introduce explicitly A !

Feasibility - step 1

Counting rates for H versus ρ electroproduction: order of magnitude

- Ratio:

$$\frac{d\sigma^H(Q^2, x_B, t)}{d\sigma^\rho(Q^2, x_B, t)} = \left| \frac{f_H}{f_\rho} \frac{(e_u \mathcal{H}_{uu}^- - e_d \mathcal{H}_{dd}^-) \mathcal{V}^{(H,-)}}{(e_u \mathcal{H}_{uu}^+ - e_d \mathcal{H}_{dd}^+) \mathcal{V}^{(\rho,+)}} \right|^2$$

- Rough estimate:

- neglect $\bar{q}$ i.e. $x \in [0, 1]$

$\Rightarrow \text{Im}\mathcal{A}_H$ and $\text{Im}\mathcal{A}_\rho$ are equal up to the factor $\mathcal{V}^M$

- Neglect the effect of $\text{Re}\mathcal{A}$

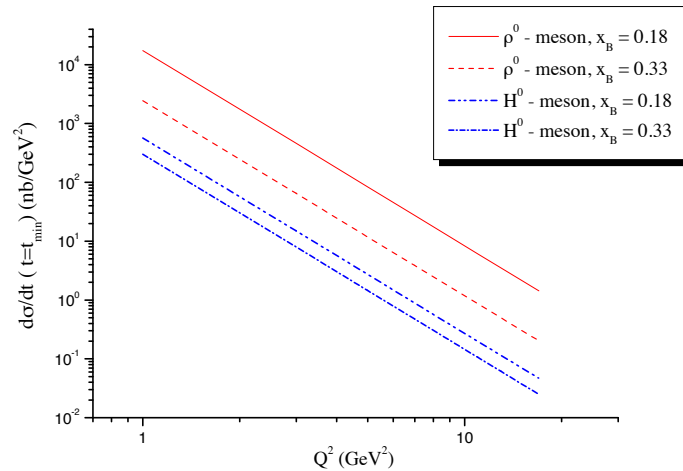
$$\frac{d\sigma^H(Q^2, x_B, t)}{d\sigma^\rho(Q^2, x_B, t)} \approx \left(\frac{5f_H}{3f_\rho} \right)^2 \approx 0.15$$

Feasibility - step 2

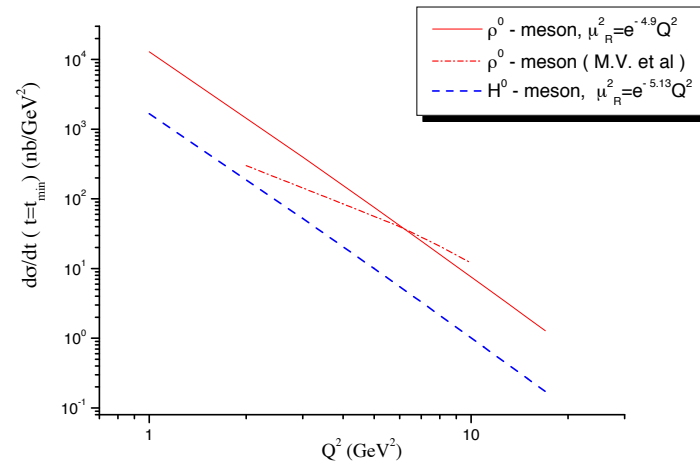
Counting rates for H versus ρ electroproduction: more precise study

- use standard description of GPDs based on Double Distributions
- $\mu_R^2 = Q^2$ versus BLM scale from NLO (at the level of cross-section)

$$\begin{array}{llll} \xi = 0.2 & \mu_R^2 = e^{-4.9} Q^2 & \rho & \xi = 0.1 & \mu_R^2 = e^{-4.68} Q^2 & \rho \\ \text{(or } x_B \approx 0.33) & \mu_R^2 = e^{-5.13} Q^2 & H & \text{(or } x_B \approx 0.18) & \mu_R^2 = e^{-5.0} Q^2 & H \end{array}$$



$$\mu_R^2 = \mu_F^2 = Q^2$$



$$\mu_R^2 = \mu_F^2 = \mu_{BLM}^2 \quad x_B \approx 0.33$$

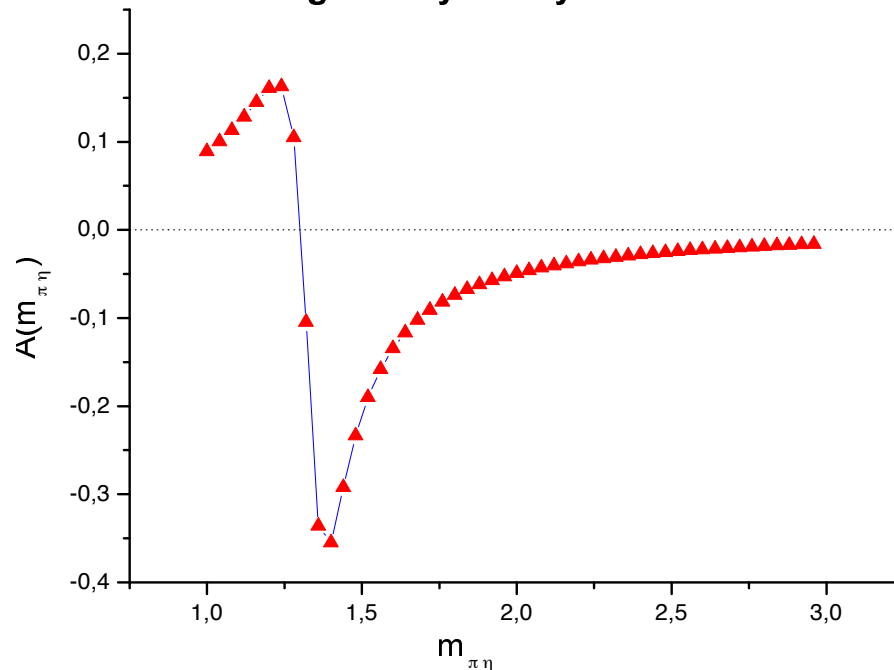
An asymmetry to mimic phase shift analysis

Angular asymmetry to unravel the hybrid meson

- π_1 has rather small amplitude with respect to the a_2 background
- Asymmetry sensitive to their interference:

$$A(Q^2, y_l, \hat{t}, m_{\pi\eta}) = \frac{\int \cos \theta_{cm} d\sigma^{\pi^0\eta}(Q^2, y_l, \hat{t}, m_{\pi\eta}, \cos \theta_{cm})}{\int d\sigma^{\pi^0\eta}(Q^2, y_l, \hat{t}, m_{\pi\eta}, \cos \theta_{cm})}$$

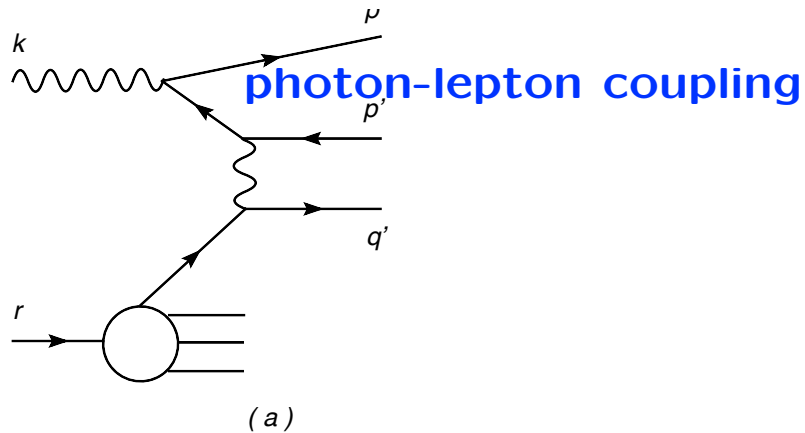
Angular Asymmetry



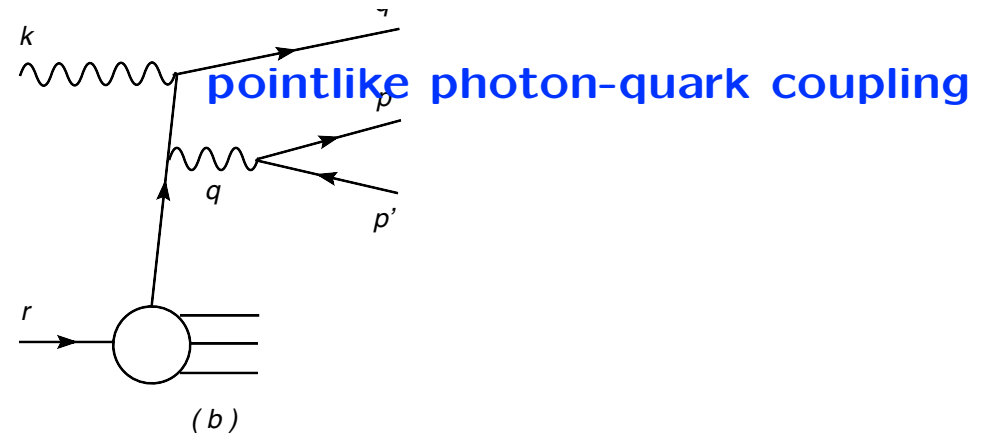
$$= \frac{\frac{8}{15} \text{Re} \left[B_{11}(m_{\pi\eta}^2) B_{12}^*(m_{\pi\eta}^2) \right]}{\frac{2}{3} \left| B_{11}(m_{\pi\eta}^2) \right|^2 + \frac{2}{5} \left| B_{12}(m_{\pi\eta}^2) \right|^2}$$

PHOTOPRODUCTION OF DRELL YAN PAIRS

$$\gamma N \rightarrow l^+ l^- X$$



Bethe - Heitler process



Drell Yan process

- ⇒ Quasi real photon beam
- ⇒ Transversely polarized target
- ⇒ A difficult but rewarding experiment

MOTIVATION

Transverse spin structure of nucleon is very badly known !

Even at the usual (integrated) parton distribution level :
interesting but indirect knowledge of $\Delta_T q(x) = h_1^q(x)$

Basic reason transversity distribution is **CHIRAL ODD**

An observable quantity contains an **even** number of chiral-odd objects

⇒ Drell Yan double polarized cross section $h_1^q(x_1)h_1^{\bar{q}}(x_2) \rightarrow$ **PAX**

⇒ Use another chiral-odd object : fragmentation, TMD ...

BASIC IDEA

Leading Twist Photon Distribution Amplitude and
Transversely polarized Vector Meson Distribution Amplitude
are **CHIRAL ODD**

Recall Distribution Amplitude = hadron light cone wave function

$$\int dx^- e^{-iz(P \cdot x)} \langle 0 | \bar{q}_\alpha(0) q_\beta(x) | H(P) \rangle \Big|_{x^+=0, x_T=0}$$

($\rightarrow$ Fourier Transform $\int dk^- d\vec{k}_T$)

The photon Distribution Amplitude

Non-triviality of the QCD vacuum $\longrightarrow \langle \bar{q}q \rangle \neq 0$

Magnetic susceptibility

$$\chi \neq 0$$

Photon couples to quarks through *em* coupling **and** through a **twist 2** photon distribution amplitude (**DA**) $\phi_\gamma(u)$

$$\langle 0 | \bar{q}(0) \sigma_{\alpha\beta} q(x) | \gamma^{(\lambda)}(k) \rangle = i e_q \chi \langle \bar{q}q \rangle \left(\epsilon_\alpha^{(\lambda)} k_\beta - \epsilon_\beta^{(\lambda)} k_\alpha \right) \int_0^1 dz e^{-iz(kx)} \phi_\gamma(z),$$

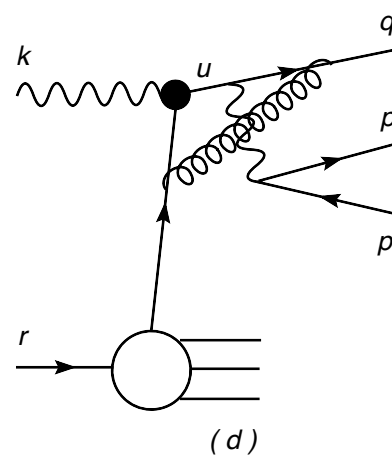
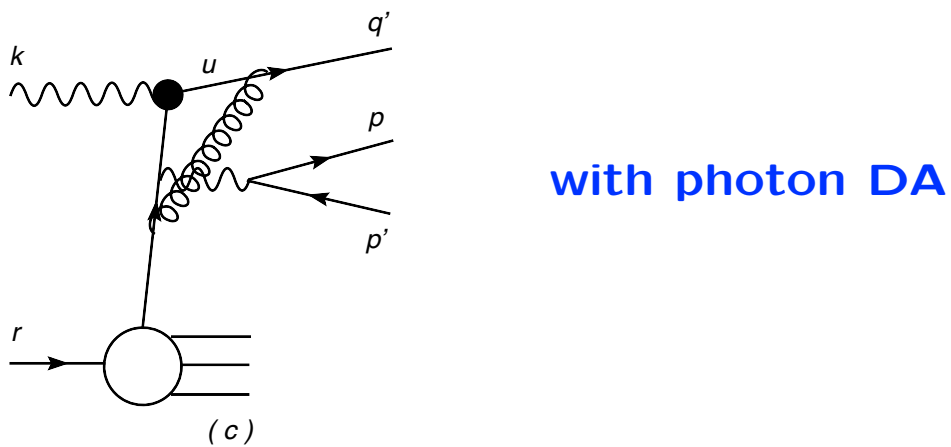
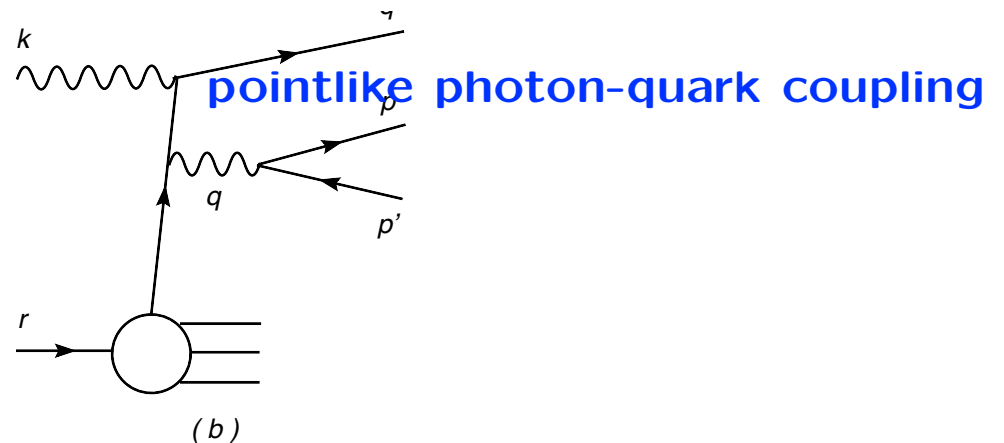
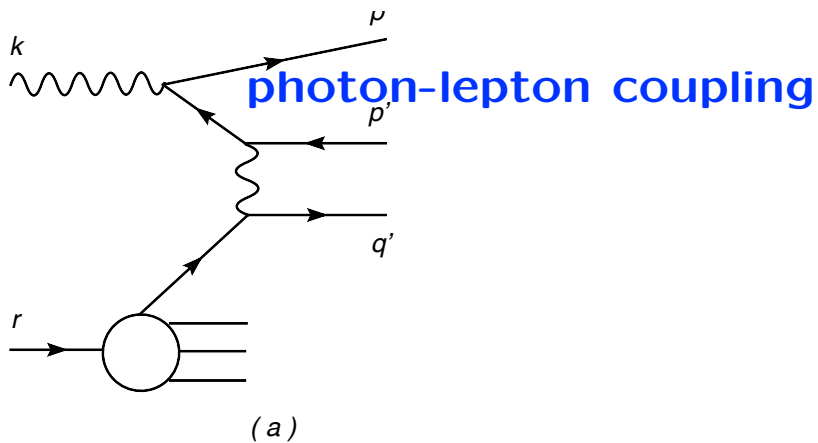
$$\Rightarrow \text{normalization : } \int dz \phi_\gamma(z) = 1,$$

$\Rightarrow z =$ momentum light-cone fraction carried by the quark.

Here the photon is real ; not much change if slightly virtual.

How to access the transversity PDF

Consider $\gamma N \rightarrow l^+ l^- X$



Kinematics

$$\gamma(k)q(xr) \rightarrow l(p)l(p')q(q')$$

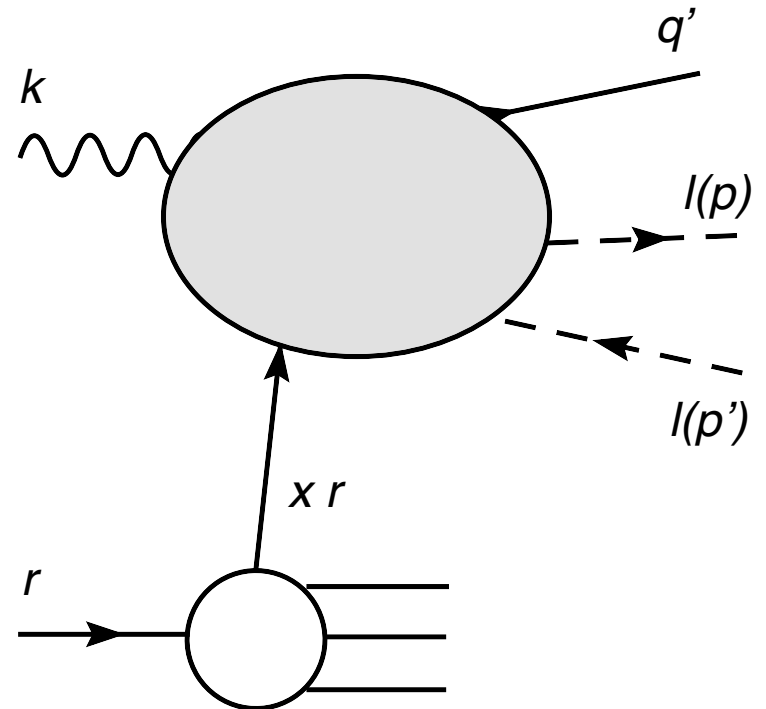
$$p + p' = q = \alpha k + \frac{Q^2 + Q_T^2}{\alpha s} r + Q_\perp$$

$$q' = \bar{\alpha} k + \frac{Q_T^2}{\bar{\alpha} s} r - Q_\perp$$

$$p = \gamma \alpha k + \frac{(\gamma Q_T + l_T)^2}{\gamma \alpha s} r + \gamma Q_\perp + l_\perp$$

$$p' = \bar{\gamma} \alpha k + \frac{(\bar{\gamma} Q_T - l_T)^2}{\bar{\gamma} \alpha s} r + \bar{\gamma} Q_\perp - l_\perp$$

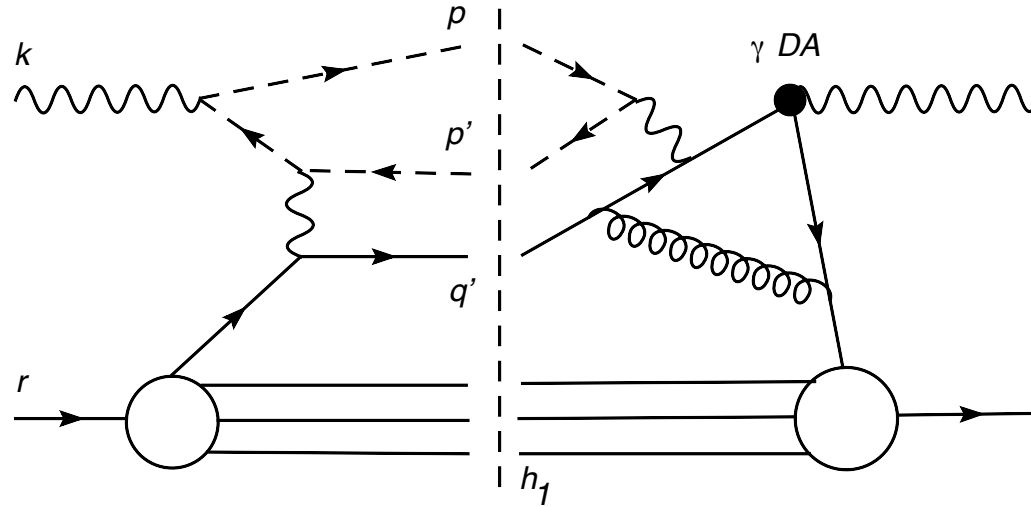
$$x = \frac{\bar{\alpha} Q^2 + Q_T^2}{\alpha \bar{\alpha} s} \quad Q^2 = \frac{l_T^2}{\gamma \bar{\gamma}}$$



Interference effects

Remember BH-DVCS interference

BP, L.Szymanowski, Phys. Rev. Lett. 103, 072002



⇒ **Chiral-oddity** of photon **DA** → Interference builds a **proton transversity** dependent contribution

⇒ Charge conjugation properties : $\frac{d\Delta_T\sigma(l^-)-d\Delta_T\sigma(l^+)}{d^4Q d\Omega} = \frac{d\sigma_{\phi BH}}{d^4Q d\Omega}$

Crucial point : **CHIRAL-ODD** amplitude has an **absorptive part** :

$$\text{Amplitude } \mathcal{A}_\phi \sim \int_0^1 du \frac{\phi_\gamma(u)}{u - \frac{Q^2\alpha}{Q^2 + Q^2} - i\epsilon} = PV \int_0^1 du \frac{\phi_\gamma(u)}{u - \frac{Q^2\alpha}{Q^2 + Q^2}} + i\pi\phi_\gamma\left(\frac{Q^2\alpha}{Q^2 + Q^2}\right)$$

Cross section difference

$$d\bar{\sigma}_{\phi BH} = \frac{(4\pi\alpha_{em})^3}{4s} \frac{C_F 4\pi\alpha_s}{2N_c} \cdot \frac{\chi\langle\bar{q}q\rangle}{\vec{Q}_\perp^2} \int dx \sum_q Q_l^3 Q_q^3 h_1^q(x) 2\mathcal{R}e(\mathcal{I}_{\phi BH}) dLIPS$$

$$2\mathcal{R}e(\mathcal{I}_{\phi BH}) = \phi_\gamma \left[\frac{\alpha Q^2}{Q^2 + \vec{Q}_\perp^2} \right] \frac{32\pi\alpha^2\bar{\alpha}}{xs(\bar{\alpha}Q^2 + \vec{Q}_\perp^2)^2} \cdot (Q^2 + \vec{Q}_\perp^2) [\epsilon^{rksT} Q_T A_1 + \epsilon^{rksT} l_T A_2]$$

Result : INTERFERENCE DOESN'T VANISH

$$\sim \chi \phi_\gamma \left(\frac{Q^2 \alpha}{Q^2 + Q_T^2} \right) \cdot h_1 \left(\frac{\bar{\alpha} Q^2 + Q_T^2}{\alpha \bar{\alpha} s} \right)$$

⇒ may be singled out by the lepton azimuthal distribution

⇒ allows to **scan** $h_1(x)$ and $\Phi_\gamma(z)$

⇒ only nucleon is polarized, i.e. **SINGLE SPIN EFFECTS**

CONCLUSION

THERE IS MUCH PHYSICS TO BE STUDIED WITH
COMPASS, BOTH WITH HADRON and MUON
BEAMS

there is EVEN MORE than in the existing PROPOSALS

Thank you for your attention