Beyond the Standard Model

Lecture 4

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Outline:

- Electroweak symmetry breaking (Lecture 1)
- Quark and lepton masses; vectorlike quarks (Lecture 2)
- New gauge bosons (Lecture 3)
- Extra dimensions; MSSM; WIMPs and cascade decays
 (Lectures 4 & 5)

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"New physics" at the TeV scale could change the basic hypotheses of the Standard Model:

local quantum field theory in 3 spatial + 1 time dimensions, invariant under SO(3,1) Lorentz transformations.

... "terra incognita" ... "uncharted waters" ...

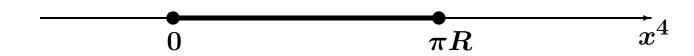
Theories with extra spatial dimensions:

- graviton only propagates in $n \ge 2$ flat extra dimensions (ADD) (rephrases the hierarchy problem)
- bosons only propagate in some flat extra dimensions (DDG)
 (allows gauge coupling unification at lower scales)
- ullet all particles propagate in some flat extra dimensions (UED) (has dark matter candidate; explains proton stability for n=2)
- graviton only propagates in a warped extra dimension (RS)
 (solves hierarchy problem)
- all particles propagate in a warped extra dimension
 (makes fermion masses exponentially sensitive to inputs)

• ...

Bosons in extra spatial dimensions

4D flat spacetime \perp one dimension of size $L = \pi R$:



A scalar field in the bulk, $\phi(x^{\alpha})$, $\alpha=0,1,...,4$:

$${\cal L}_{5D} = (\partial^{\mu}\phi)^{\dagger}\,\partial_{\mu}\phi - \left(\partial^{4}\phi
ight)^{\dagger}\,\partial_{4}\phi - m_{0}^{2}\phi^{\dagger}\phi \,\,, \qquad \qquad \mu = 0,1,2,3$$

$$\Rightarrow$$
 Equation of motion: $\left(\partial^{\mu}\partial_{\mu}-\partial^{4}\partial_{4}\right)\phi=m_{0}^{2}\phi$

 m_0 is the 5D mass of ϕ .

Neumann boundary conditions for "even" fields:

$$rac{\partial}{\partial x^4}\phi(x^\mu,0)=rac{\partial}{\partial x^4}\phi(x^\mu,\pi R)=0$$

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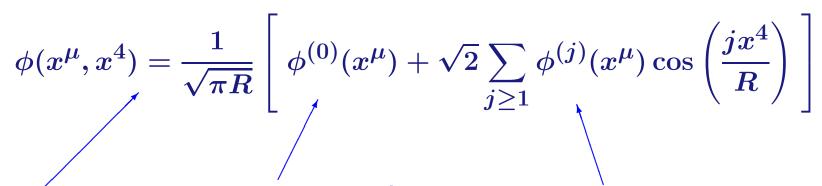
Solution to the equation of motion:

$$\phi(x^{\mu}, x^4) = rac{1}{\sqrt{\pi R}} \left[\; \phi^{(0)}(x^{\mu}) + \sqrt{2} \sum_{j \geq 1} \phi^{(j)}(x^{\mu}) \cos\left(rac{jx^4}{R}
ight) \;
ight]$$

Neumann boundary conditions for "even" fields:

$$rac{\partial}{\partial x^4}\phi(x^\mu,0)=rac{\partial}{\partial x^4}\phi(x^\mu,\pi R)=0$$

Solution to the equation of motion:



Kaluza-Klein decomposition

Zero-mode (wave function is constant along x^4)

Kaluza-Klein modes: particles of definite momentum along x^4

4D point of view: a tower of massive particles:

$${\cal L}_{4D} = \int_0^{\pi R} dx^4 \; {\cal L}_{5D} \qquad \Rightarrow \qquad m_j^2 = m_0^2 + rac{j^2}{R^2}$$

Dirichlet boundary conditions for "odd" fields:

$$\phi(x,0) = \phi(x,\pi R) = 0$$

KK decomposition:
$$\phi(x^\mu,x^4)=rac{\sqrt{2}}{\sqrt{\pi R}}\sum_{j\geq 1}\phi^{(j)}(x^\mu)\sin\left(rac{jx^4}{R}
ight)$$

There is no zero-mode.

The lightest KK mode is $\phi^{(1)}$, of mass $\sqrt{1/R^2+m_0^2}$

Homework: Check that the normalization condition for KK functions requires the factor of $\sqrt{2}$.

Why j < 0 is not allowed?

Gauge bosons in 5D:

 $A_{\mu}(x^{
u},x^4)$, $\mu,
u=0,1,2,3$, and

 $A_4(x^{\nu},x^4)$ – polarization along the extra dimension.

From the point of view of the 4D theory:

 $A_4(x^{\nu},x^4)$ is a tower of spinless KK modes.

Gauge invariance requires A_{μ} to have a zero-mode:

$$\partial_4 A_\mu(x^
u,0) = \partial_4 A_\mu(x^
u,\pi R) = 0$$

$$A_{\mu}(x^{
u},x^4) = rac{1}{\sqrt{\pi R}} \left[\ A_{\mu}^{(0)}(x^{
u}) + \sqrt{2} \sum_{j \geq 1} A_{\mu}^{(j)}(x^{
u}) \cos \left(rac{jx^4}{R}
ight) \
ight]$$

Dirichlet B.C: $A_4(x^{\nu}, 0) = A_4(x^{\nu}, \pi R) = 0$

$$ext{KK decomposition}: \quad A_4(x^
u, x^4) = \sqrt{rac{2}{L}} \sum_{j \geq 1} A_G^{(j)}(x) \sin\left(rac{jx^4}{R}
ight)$$

 $ightarrow A_4(x^
u,x^4)$ does not have a 0-mode! (Odd field)

Kaluza-Klein spectrum of gauge bosons

 $A_G^{(j)}(x^
u)$ becomes the longitudinal degree of freedom of the spin-1 KK mode $A_\mu^{(j)}(x^
u)$.

$$A^{(3)}_{\mu}$$
 \longrightarrow $\frac{3}{R}$ \longrightarrow $A^{(3)}_{G}$

$$A^{(2)}_{\mu}$$
 $\qquad \qquad \frac{2}{R}$ $\qquad \qquad A^{(2)}_{G}$

$$A^{(1)}_{\mu}$$
 — $\frac{1}{R}$ — $A^{(1)}_{G}$

$$A_{\mu}^{(0)}$$
 ——

Fermions in a compact dimension

Gamma matrices – require 5 anti-commuting matrices:

$$\gamma^{\mu}$$
, $\mu=0,1,2,3$, and $\gamma^4=i\gamma_5$

These are 4×4 matrices \rightarrow 5D fermions have 4 components.

⇒ 5D fermions are vector-like:

$$\chi(x^{\mu}, x^4) = \chi_L(x^{\mu}, x^4) + \chi_R(x^{\mu}, x^4)$$

Chiral boundary conditions:

$$\chi_L(x^\mu,0) = \chi_L(x^\mu,\pi R) = 0$$
 $rac{\partial}{\partial x^4}\chi_R(x^\mu,0) = rac{\partial}{\partial x^4}\chi_R(x^\mu,\pi R) = 0$

Dirac equation in 5D:

$$i\gamma^{\mu}\partial_{\mu}\chi_{R}=(\partial_{4}+m_{0})\chi_{L}$$
 $i\gamma^{\mu}\partial_{\mu}\chi_{L}=(-\partial_{4}+m_{0})\chi_{R}$

Dirac equation in 5D:

$$i\gamma^{\mu}\partial_{\mu}\chi_{R}=(\partial_{4}+m_{0})\chi_{L}$$

$$i\gamma^{\mu}\partial_{\mu}\chi_{L}=(-\partial_{4}+m_{0})\chi_{R}$$

Kaluza-Klein decomposition:

$$\chi = \frac{1}{\sqrt{\pi R}} \left\{ \chi_R^0(x^\mu) + \sqrt{2} \sum_{j \geq 1} \left[\chi_R^j(x^\mu) \cos \left(\frac{\pi j x^4}{L} \right) + \chi_L^j(x^\mu) \sin \left(\frac{\pi j x^4}{L} \right) \right] \right\}$$

0-mode is a chiral fermion!

KK modes are vectorlike fermions.

Homework: solve 5D Dirac equation when χ_R is odd and χ_L is even.

Kaluza-Klein spectrum of quarks and leptons

$$(t_L^{(3)},b_L^{(3)}) \qquad \qquad \frac{3}{R} - - - (T_R^{(3)},B_R^{(3)}) \qquad \qquad T_L^{(3)} - - - \frac{3}{R} - - - t_R^{(3)}$$

$$T_L^{(3)} - \frac{3}{R} - t_R^{(3)}$$

$$T_L^{(2)} - \frac{2}{R} - t_R^{(2)}$$

$$(t_L^{(1)},b_L^{(1)}) - \frac{1}{R} - (T_R^{(1)},B_R^{(1)}) - T_L^{(1)} - \frac{1}{R} - t_R^{(1)}$$

$$T_L^{(1)} - \frac{1}{R} - t_R^{(1)}$$

$$(t_L,b_L)$$
 ———

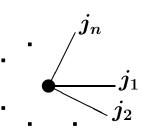
 $---t_R$

Universal Extra Dimensions

<u>All</u> Standard Model particles propagate in $D \geq 5$ dimensions.

Momentum conservation \rightarrow KK-number conservation

$$\mathcal{L}_{4D} = \int_0^{\pi R} dx^4 \; \mathcal{L}_{5D}$$



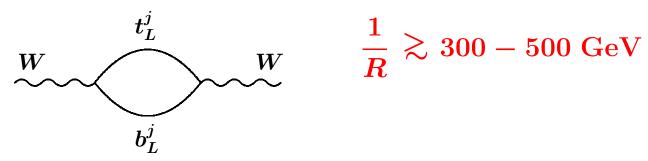
At each interaction vertex:

 $j_1 \pm j_2 \pm ... \pm j_n = 0$ for a certain choice of \pm

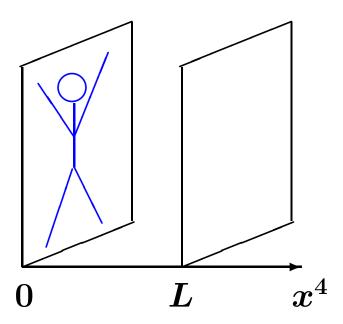
In particular: $0 \pm \cdots \pm 0 \neq 1$

- ⇒ tree-level exchange of KK modes does not contribute to currently measurable quantities
- ⇒ no single KK 1-mode production at colliders

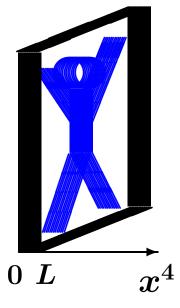
Bounds from one-loop shifts in W and Z masses, and other observables:



Bosons in 5D, localized fermions:

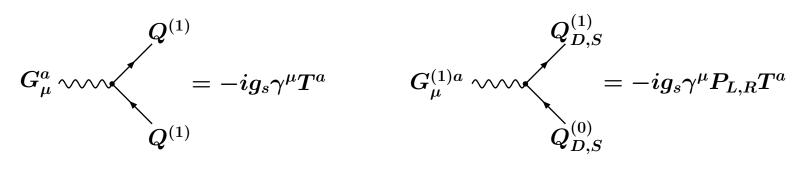


A 4-th universal spatial dimension:

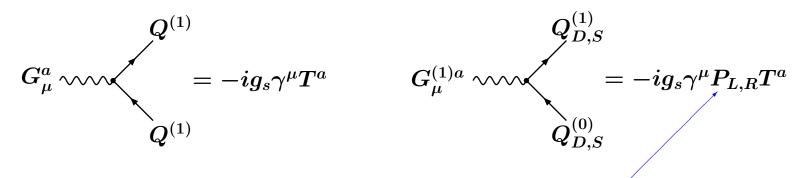


We all have a constant thickness in the 4th spatial dimension.

Feynman rules relevant for QCD production of KK particles at hadron colliders:

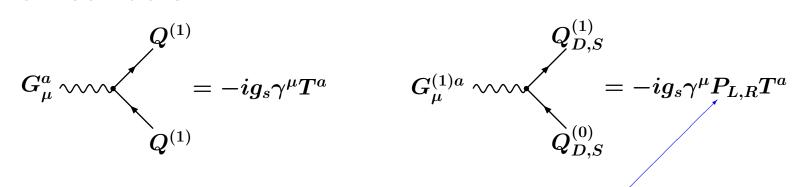


Feynman rules relevant for QCD production of KK particles at hadron colliders:



Interaction of a level-1 quark with a level-1 gluon is chiral

Feynman rules relevant for QCD production of KK particles at hadron colliders:



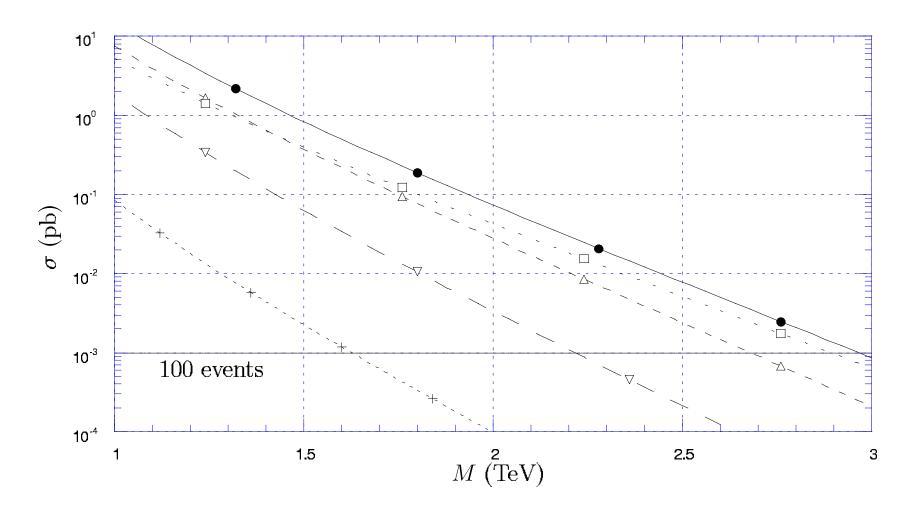
Interaction of a level-1 quark with a level-1 gluon is chiral

Feynman rules for interactions of standard-model gluons with KK modes are fixed by gauge invariance:

$$G_{\mu}^{a}$$
 $G_{
ho}^{(1)c}=-ig_{s}^{2}[f^{abe}f^{cde}(g^{\mu
ho}g^{
u\sigma}-g^{\mu\sigma}g^{
u
ho})+f^{ace}f^{bde}(g^{\mu
u}g^{
ho\sigma}-g^{\mu\sigma}g^{
u
ho}) \ +f^{ade}f^{bce}(g^{\mu
u}g^{
ho\sigma}-g^{\mu
ho}g^{
u\sigma})]$

$$G_
u^{b}$$
 ($G_
u^{(1)a}$) $G_
u^{b}$ ($G_
u^{(1)c}$) $G_
u^{(1)c}$ $G_
u^{(1)c}$ $G_
u^{(1)c}$

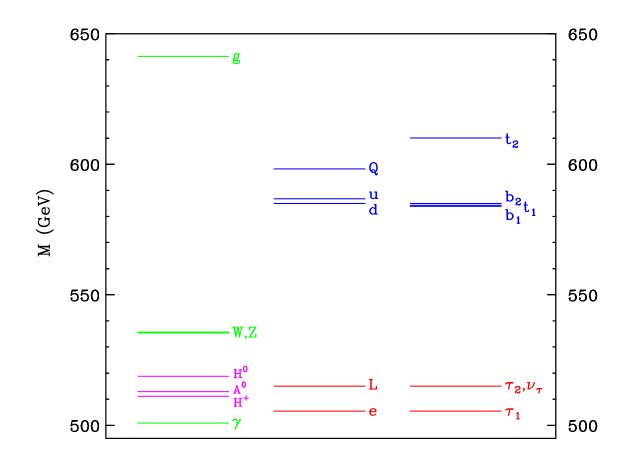
Cross section for production of a pair of level-1 particles at the LHC14, as a function of the compactification scale 1/R:



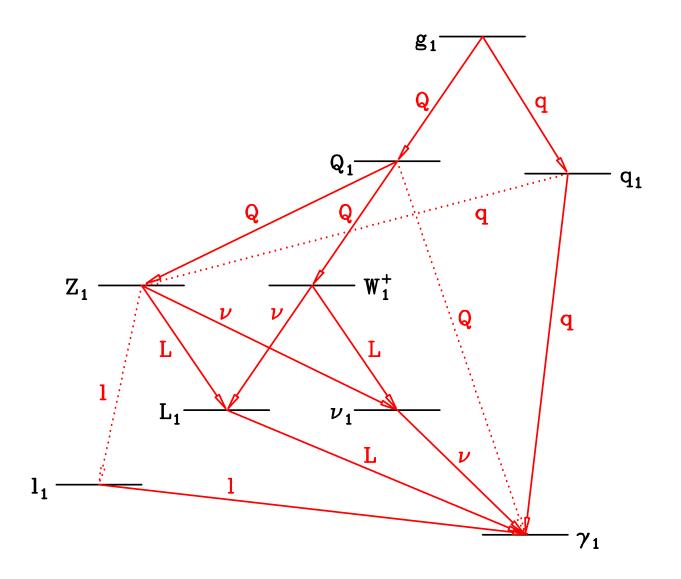
(Macesanu, McMullen, Nandi, hep-ph/0201300)

(1) modes have a tree-level mass of 1/R, and KK parity –. One-loop contributions (and electroweak symmetry breaking) split the spectrum (Cheng, Matchev, Schmaltz, hep-ph/0204342)

Mass spectrum of the (1) level:

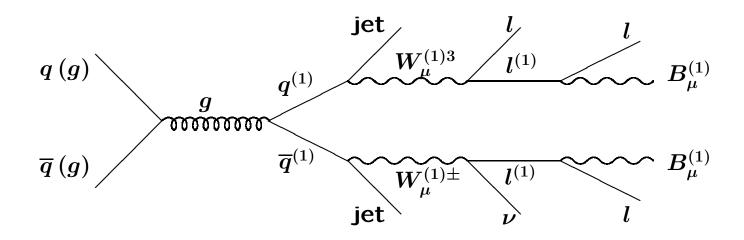


Decay modes of the KK particles:



Homework: compute the branching fractions of the level-1 particles.

Pair production of (1) modes at hadron colliders:



Look for: 2 hard leptons (~ 100 GeV) + 1 soft lepton (~ 10 GeV) + 2 jets (~ 50 GeV) + E_T

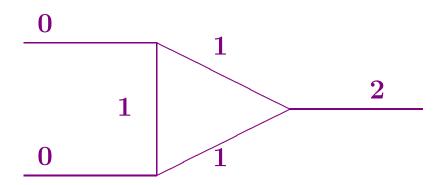
(Cheng, Matchev, Schmaltz, hep-ph/0205314; ...)

Homework: draw other diagrams which contribute to this signal.

CDF analysis of $3l + E_T$: 1/R > 280 GeV (Run I)

At one-loop level: $j_1 \pm j_2 \pm ... \pm j_n = \text{even}$

At colliders: s-channel production of the 2-modes



Kaluza-Klein parity: invariance under reflections with respect to the center of the compact dimension.

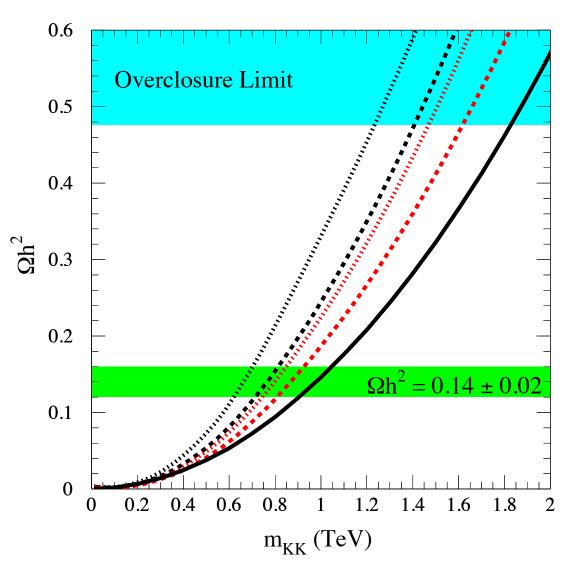
KK parity $(-1)^j$ is conserved \Rightarrow lightest KK-odd particle is stable. (only KK modes with odd j are odd under KK parity)



Lightest KK particle is stable in UED:

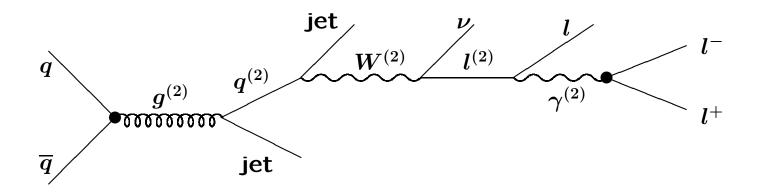
 $\gamma^{(1)}$ is a viable dark matter candidate

(from Servant, Tait, hep-ph/0206071)



Second-level masses: $\sim 2/R$.

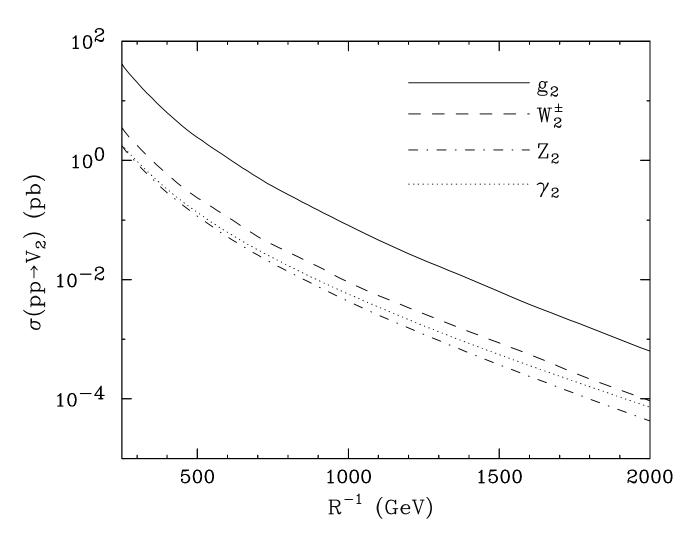
Cascade decay of the 2-mode is followed by $\gamma^{(2)}$ decay into hard leptons:



Allows discrimination of UED & MSSM

(A. Datta, K. Kong, K. Matchev, hep-ph/0509246)

Cross section for s-channel production of a level-2 boson (of mass 2/R + corrections) at the LHC14:



(A. Datta, K. Kong, K. Matchev, hep-ph/0509246)

Conclusions to Lecture 4

- ullet Any particle that propagates in $D \geq 5$ would appear in experiments as a tower of heavy 4-dimensional particles.
- Kaluza-Klein modes of the quarks and leptons are <u>vectorlike</u> fermions. Chirality of 0-modes arises due to boundary conditions.
- One Universal Extra Dimension
- compactification scale can be as low as ~ 500 GeV.
- lightest KK mode is a dark matter candidate
- Look for Kaluza-Klein modes at the Tevatron and the LHC:
- 3 soft leptons + jets + $\not\!\!E_T$
- series of narrow $\ell^+\ell^-$ resonances due to level-2 particles.