

# Cosmology Dark Matter

AESHEP Oct 25, 2012

Kavli IPMU, University of Tokyo

UC Berkeley, Lawrence Berkeley Laboratory

Hitoshi Murayama





How did the Universe begin?

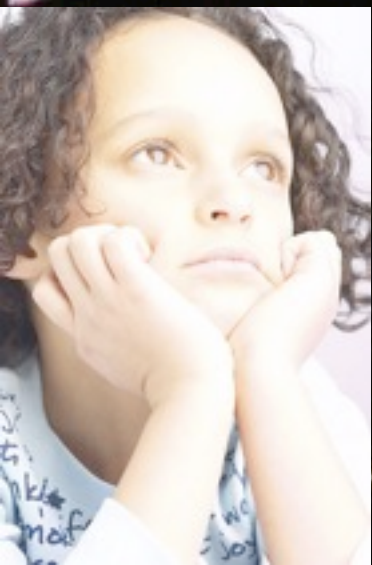
What is its fate?

What is it made of?

What are its fundamental laws?

Why do we exist?

interdisciplinary institute of  
astronomy, physics and mathematics  
10-year program by Japanese  
government since 2007



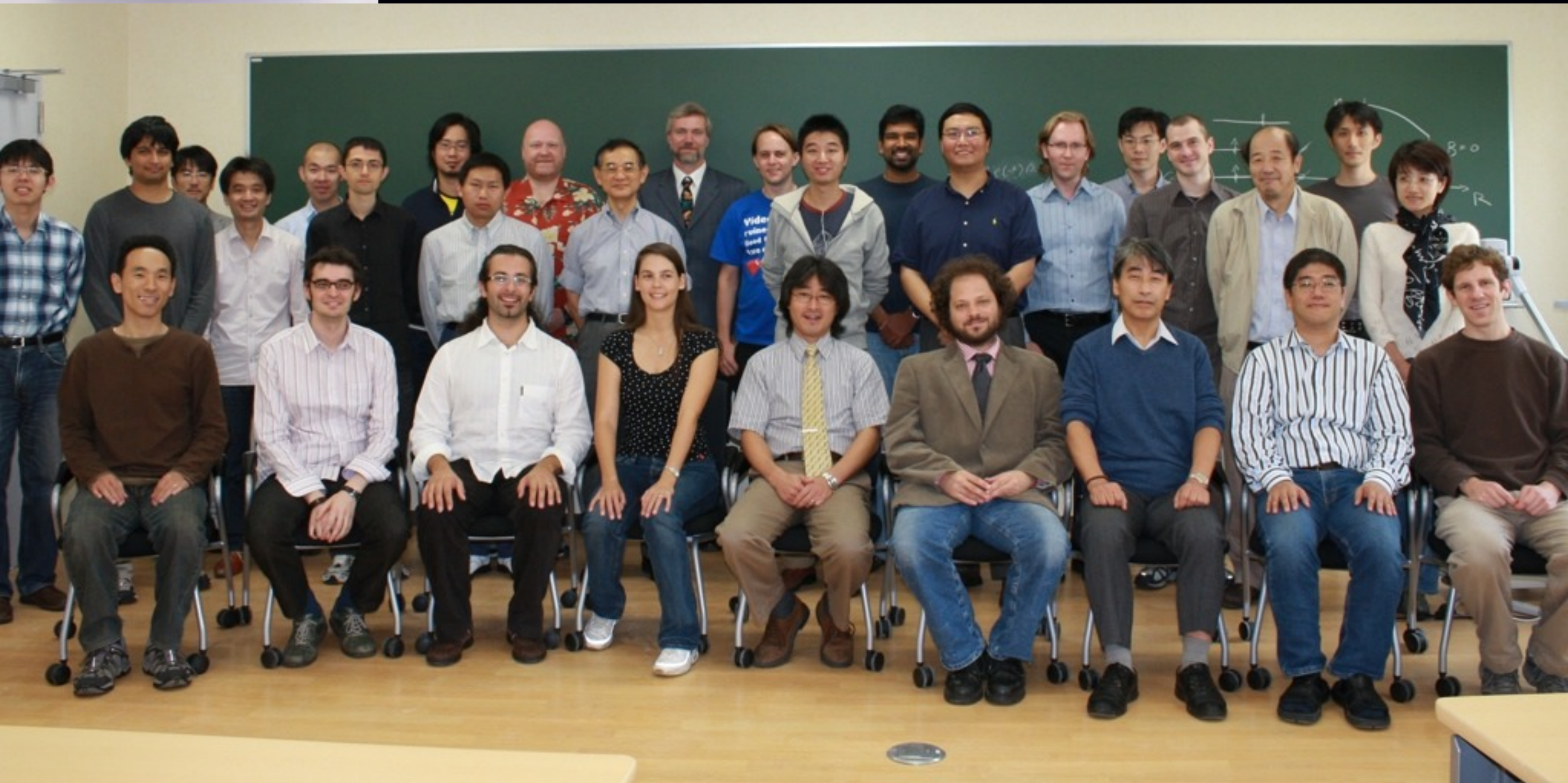


# Oct 2007





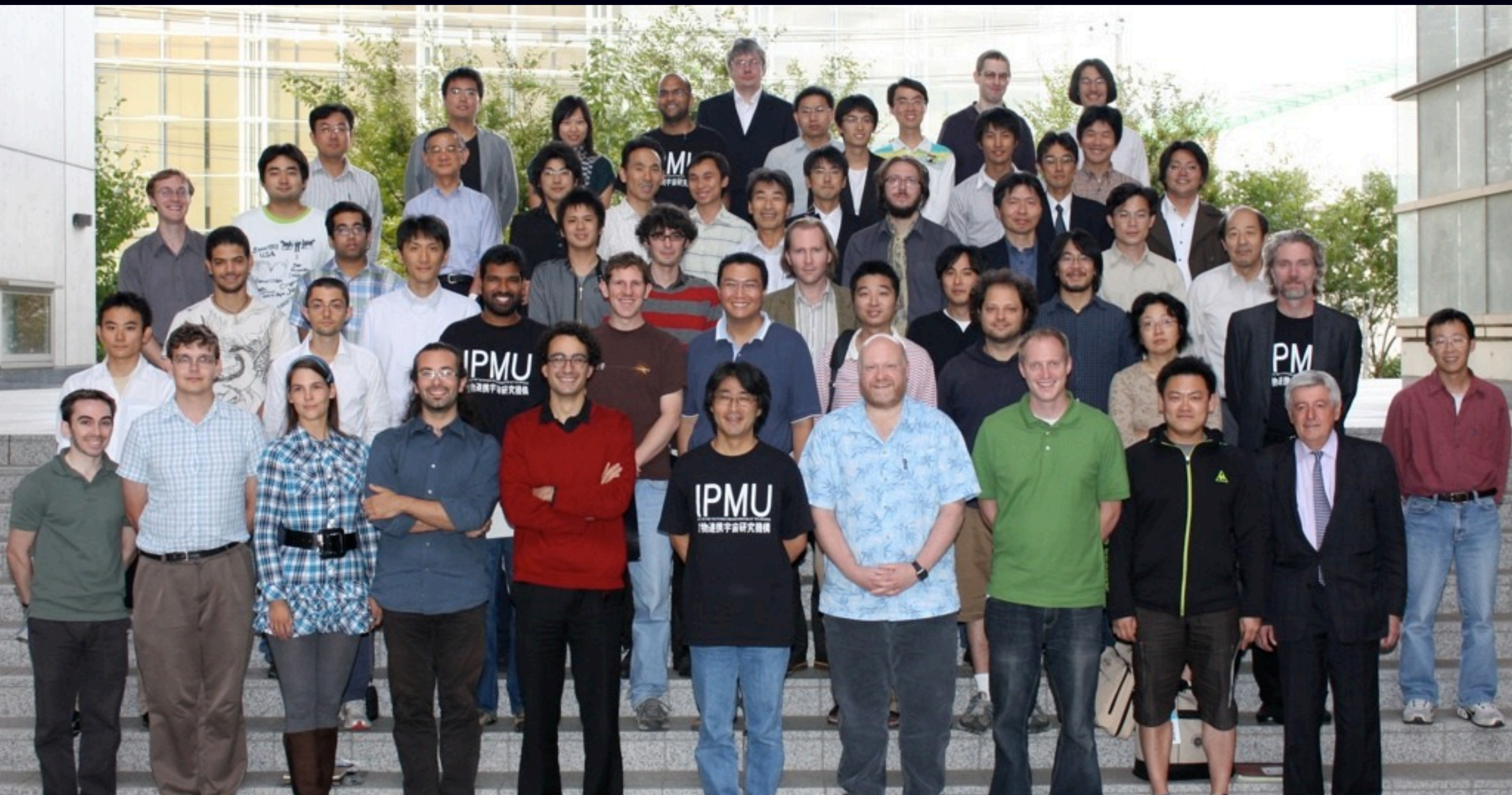
Oct 2008



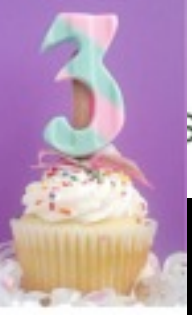




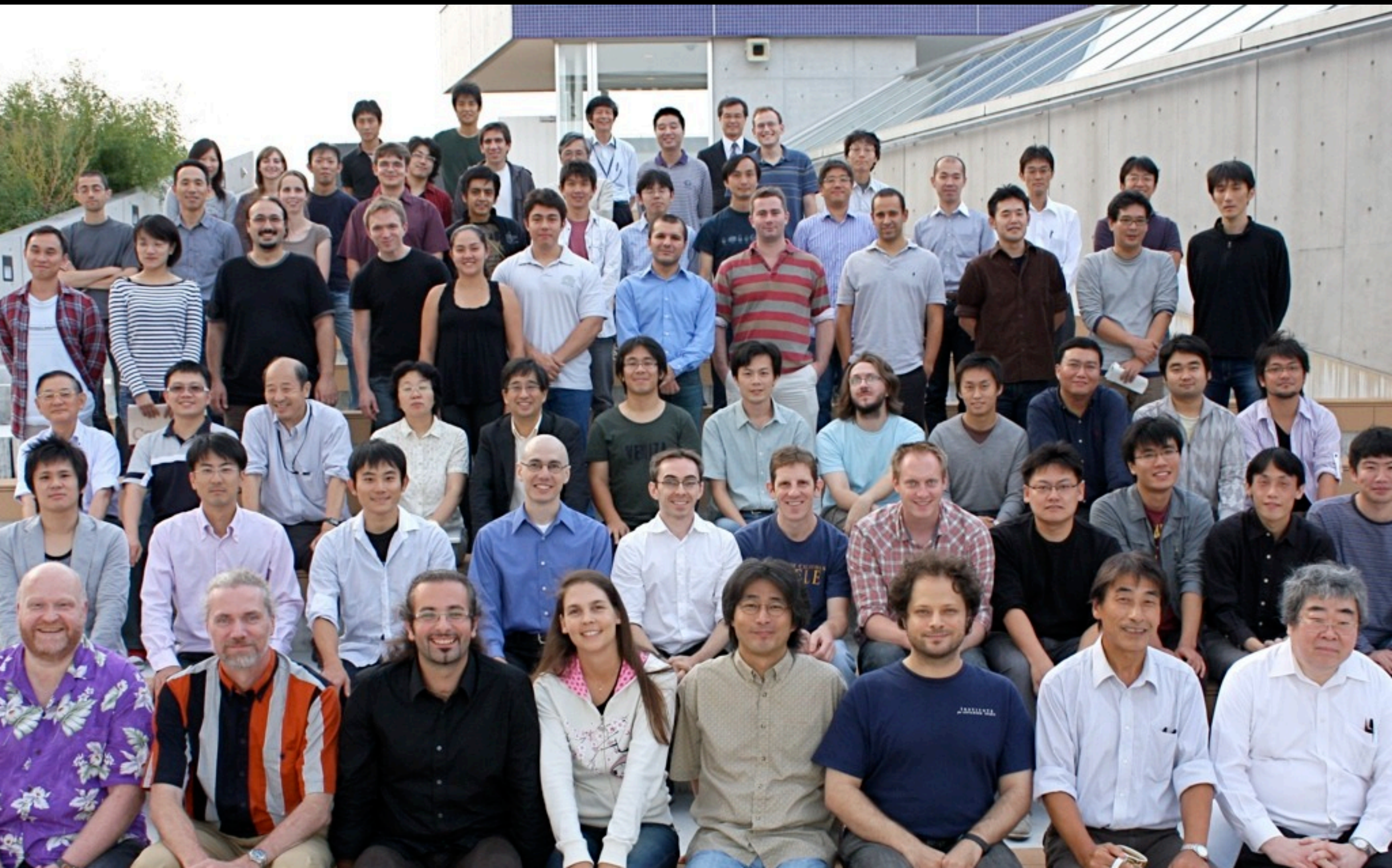
Oct 2009







Oct 2010







Oct 2011





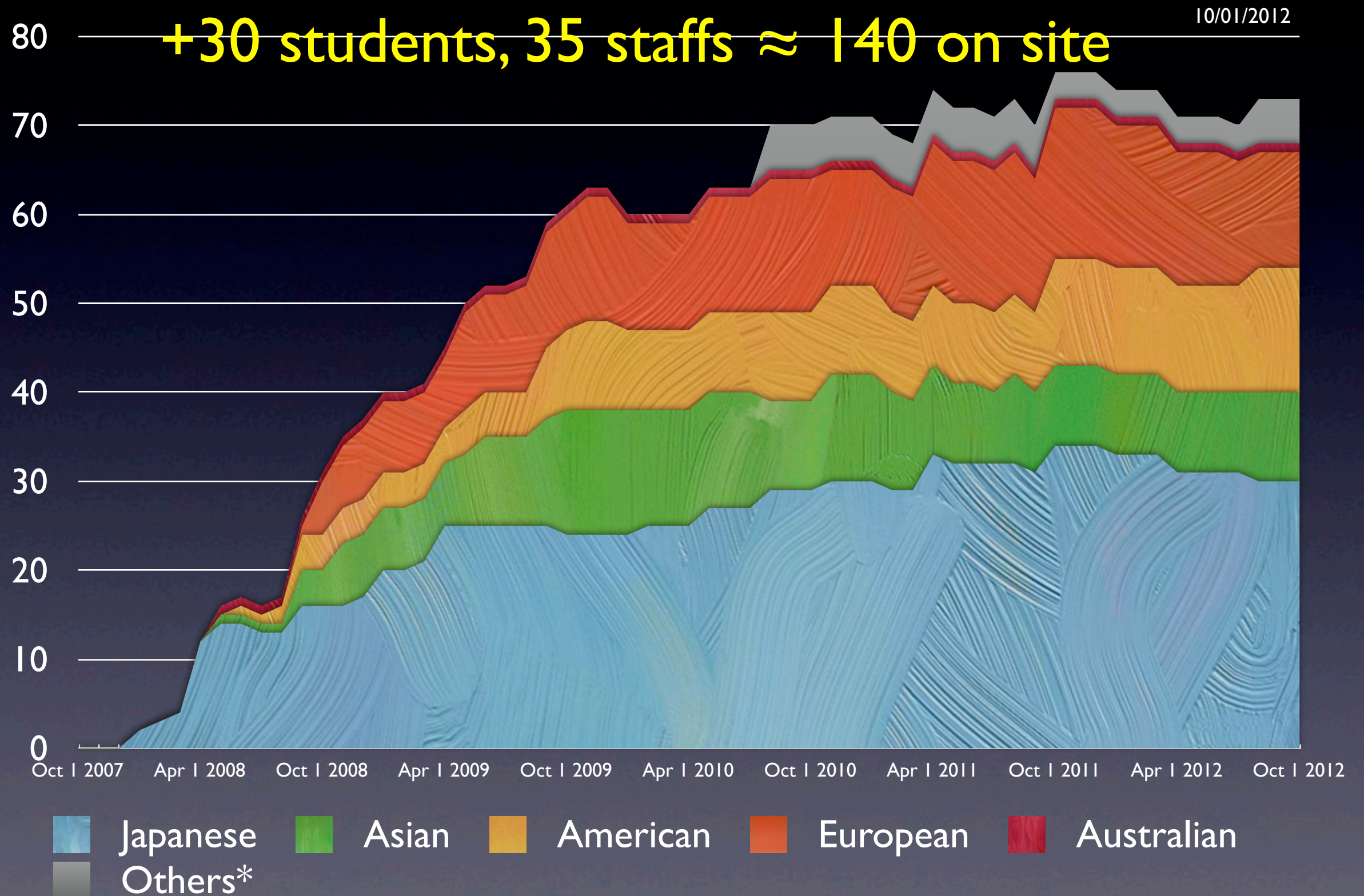


Oct 2012





# Full-time Scientists paid by IPMU



\*Argentina, Chile, Canada



brand-new building 2010

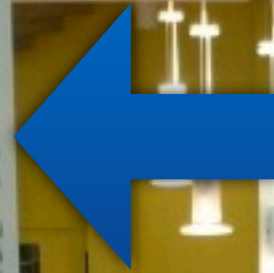




“European town square”

obelisk

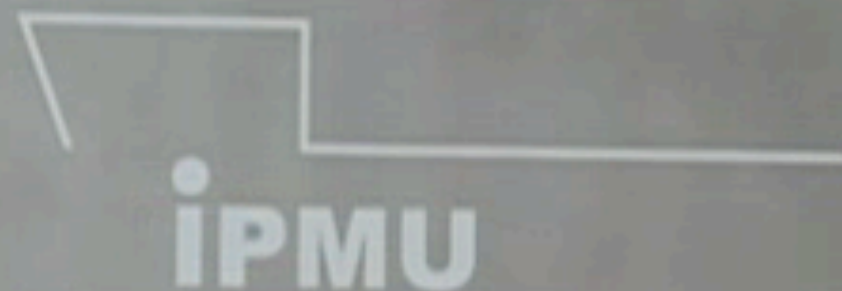
“L’Universo é scritto in  
lingua matematica”





日本の頭脳

挑む天才たち



Institute for the Physics and Mathematics of the Universe

数物連携宇宙研究機構

2007年設立

東京大学国際高等研究所数物連携宇宙研究機構

Institute for the Physics and Mathematics of the Universe

Asahi TV





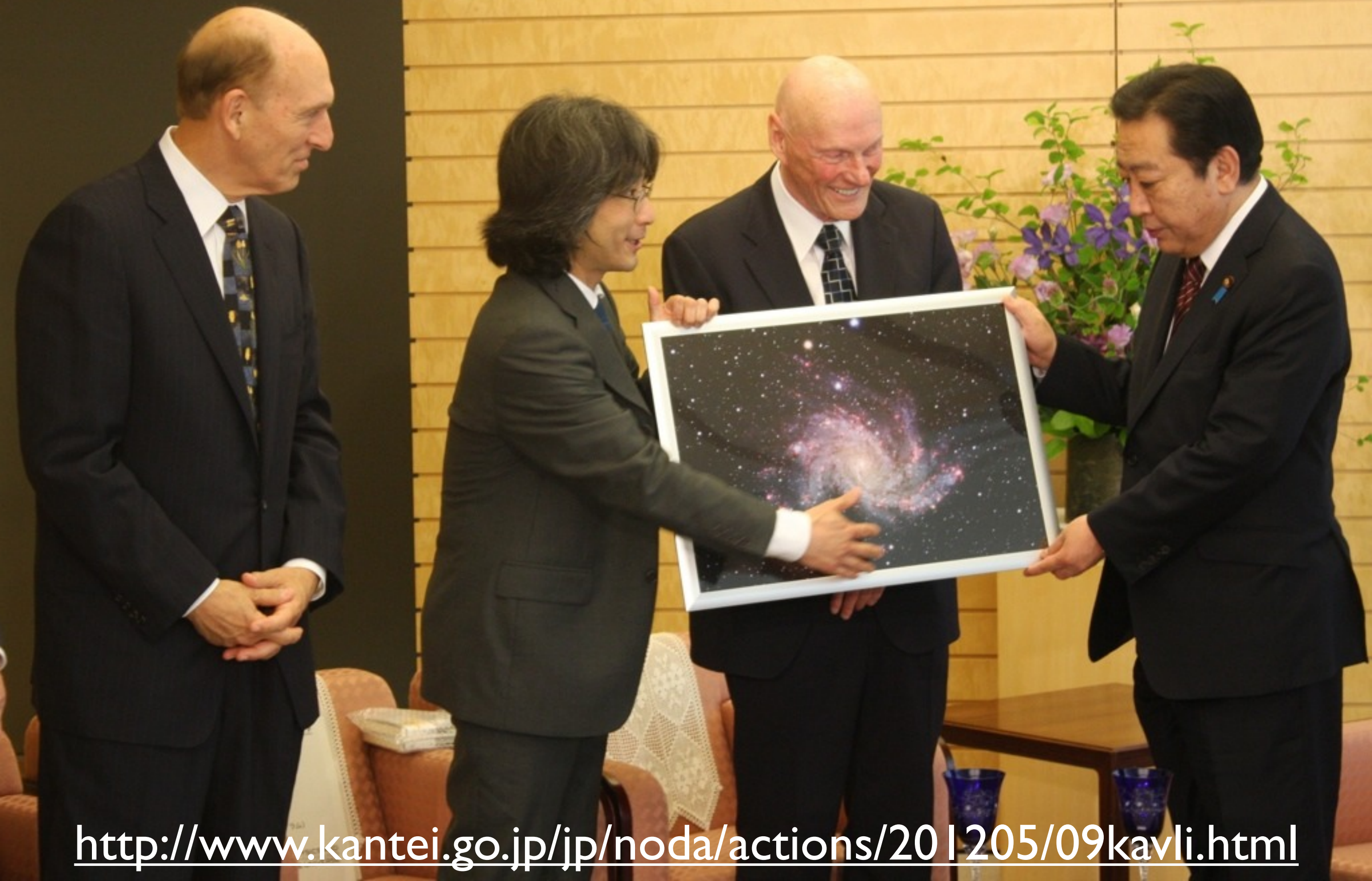
# THE KAVLI FOUNDATION



officially **Kavli IPMU** on April 1, 2012  
First research institute in Japan named  
after a donor, breaking new grounds



May 9, meeting with Prime Minister Noda



<http://www.kantei.go.jp/jp/noda/actions/201205/09kavli.html>



- *Basic research is very important, because it is a common resource shared by the whole humanity.*





# Cosmology Dark Matter

AESHEP Oct 25, 2012

Kavli IPMU, University of Tokyo

UC Berkeley, Lawrence Berkeley Laboratory

Hitoshi Murayama





*The whole  
Universe was  
smaller than  
an atom*

**Big Bang**

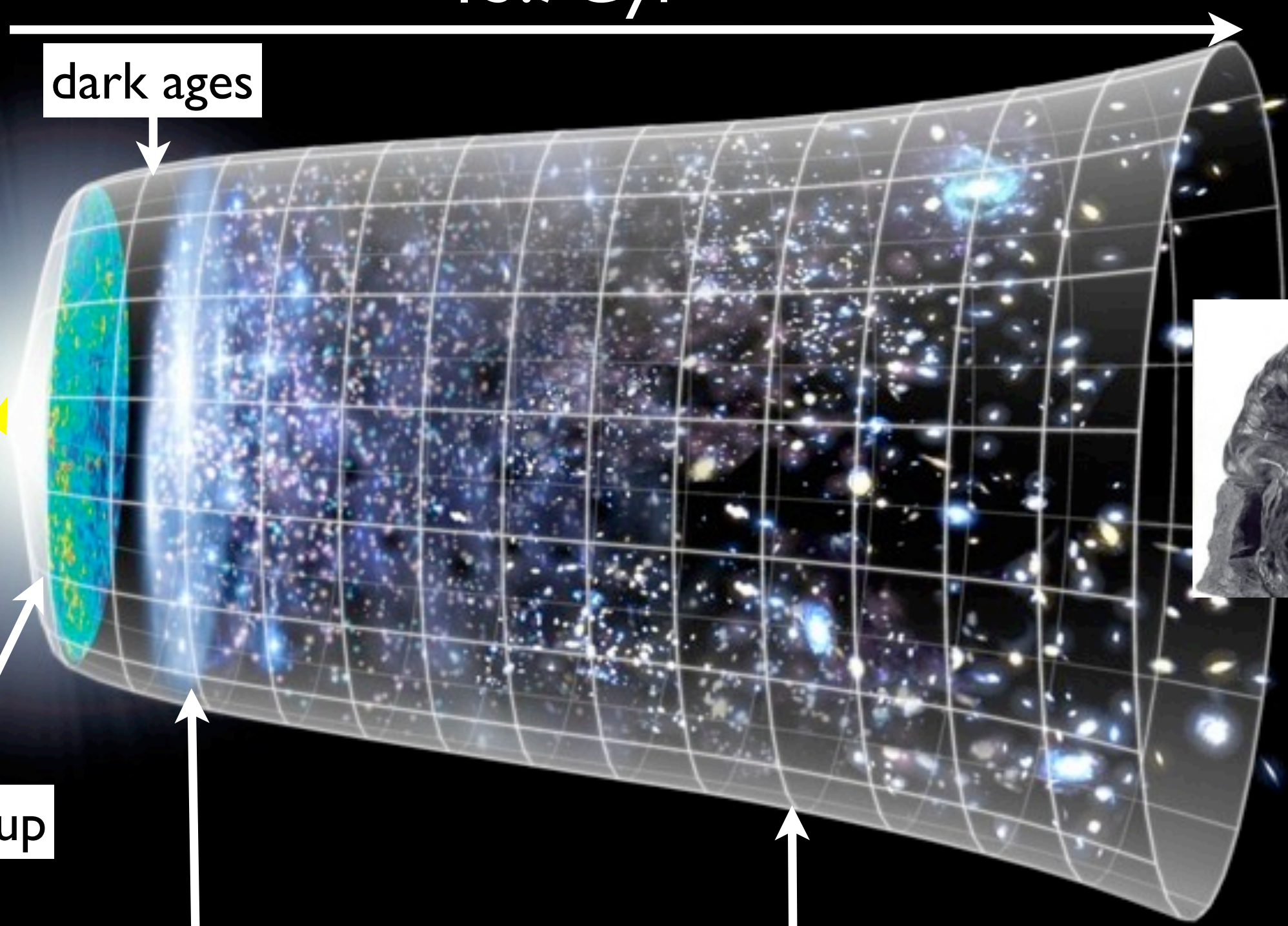
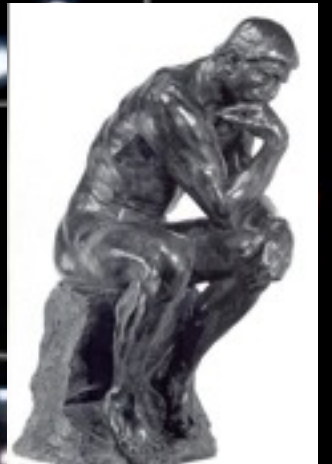
13.7Gyr

dark ages

particle soup

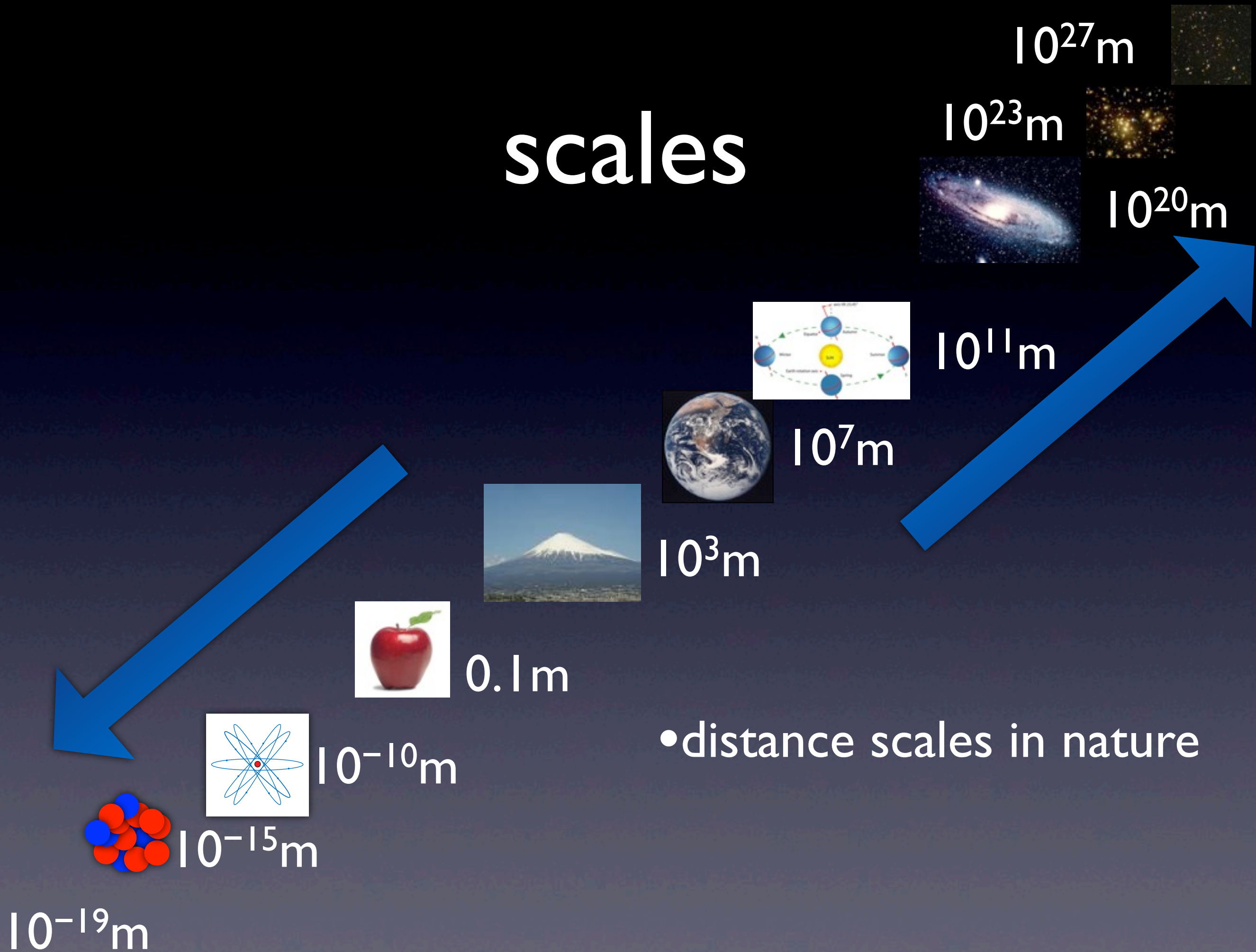
star

Earth



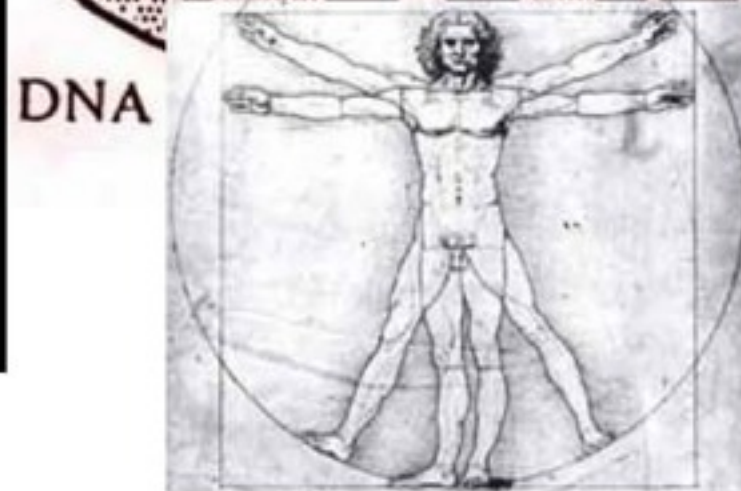
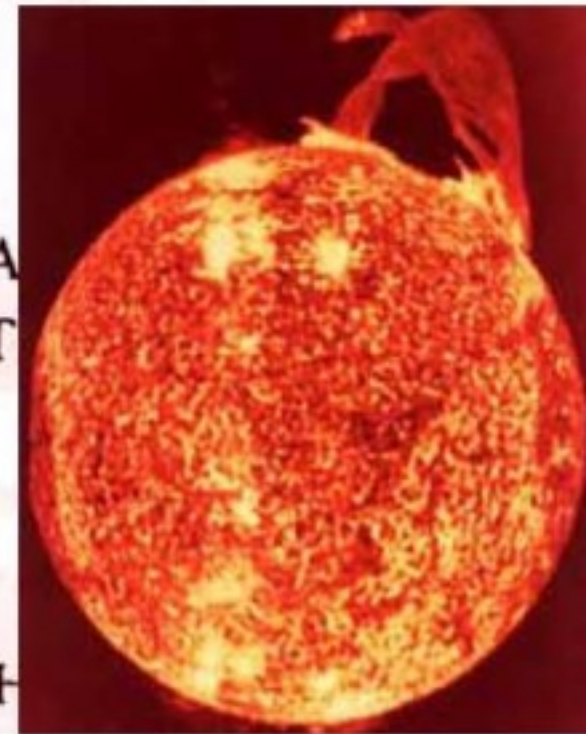
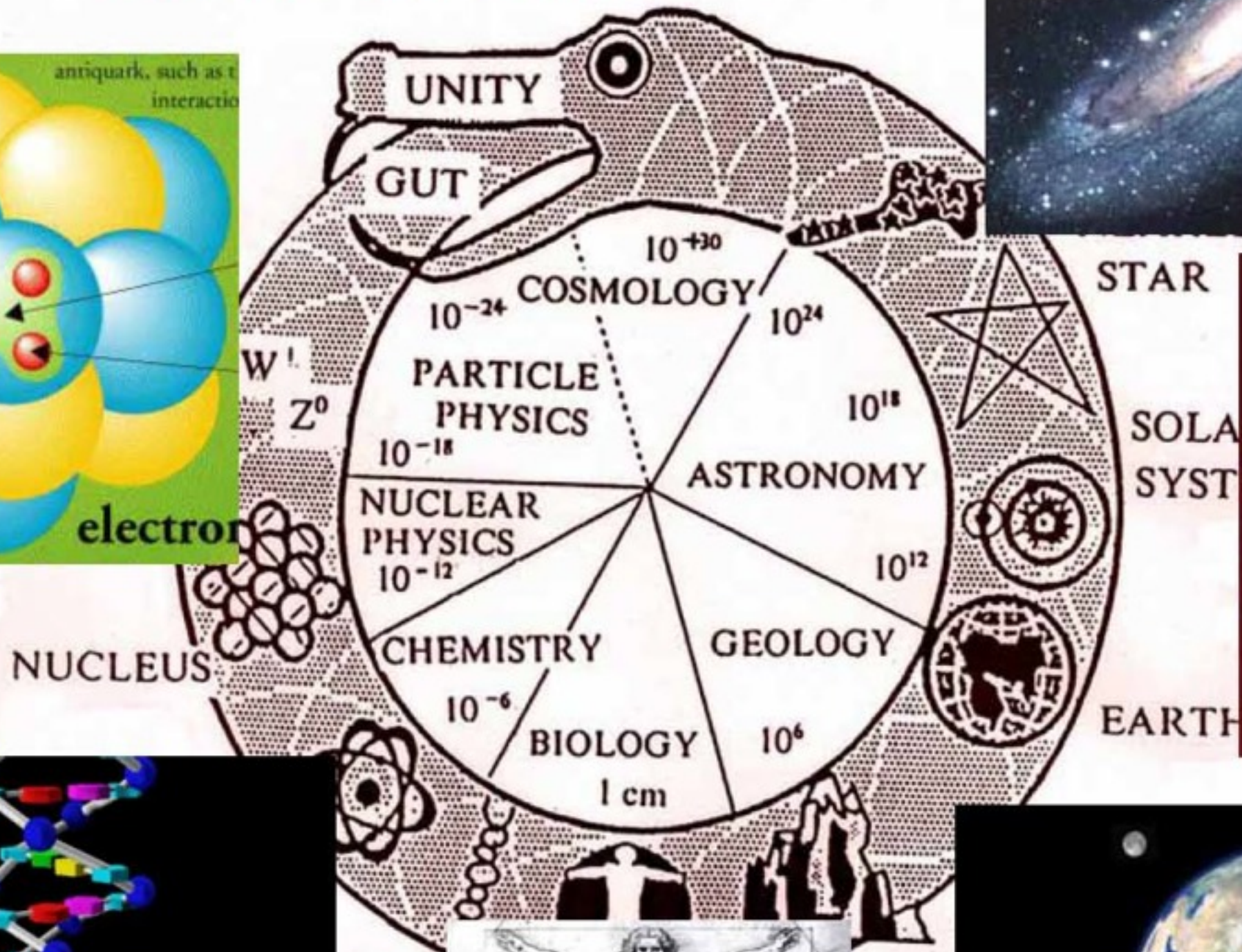
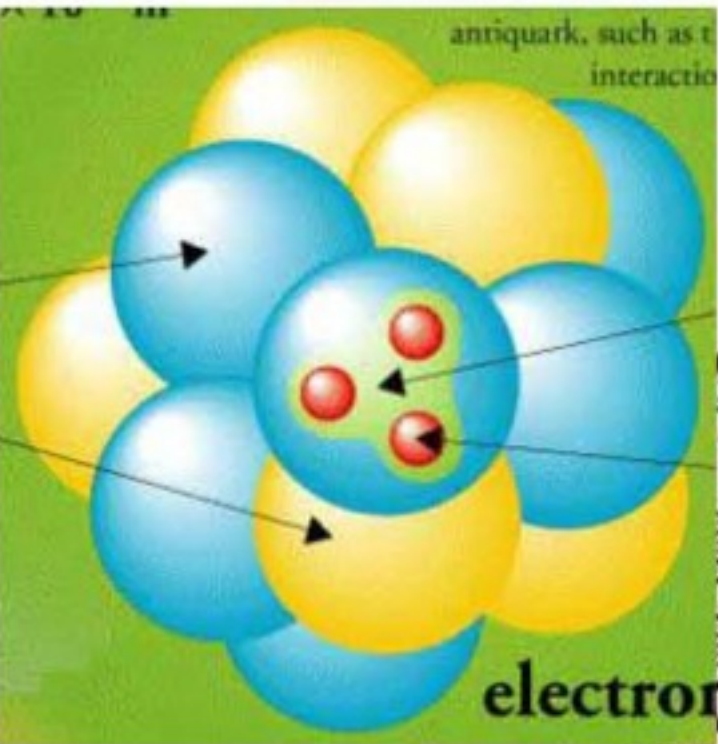


# scales





# Snake of Sizes



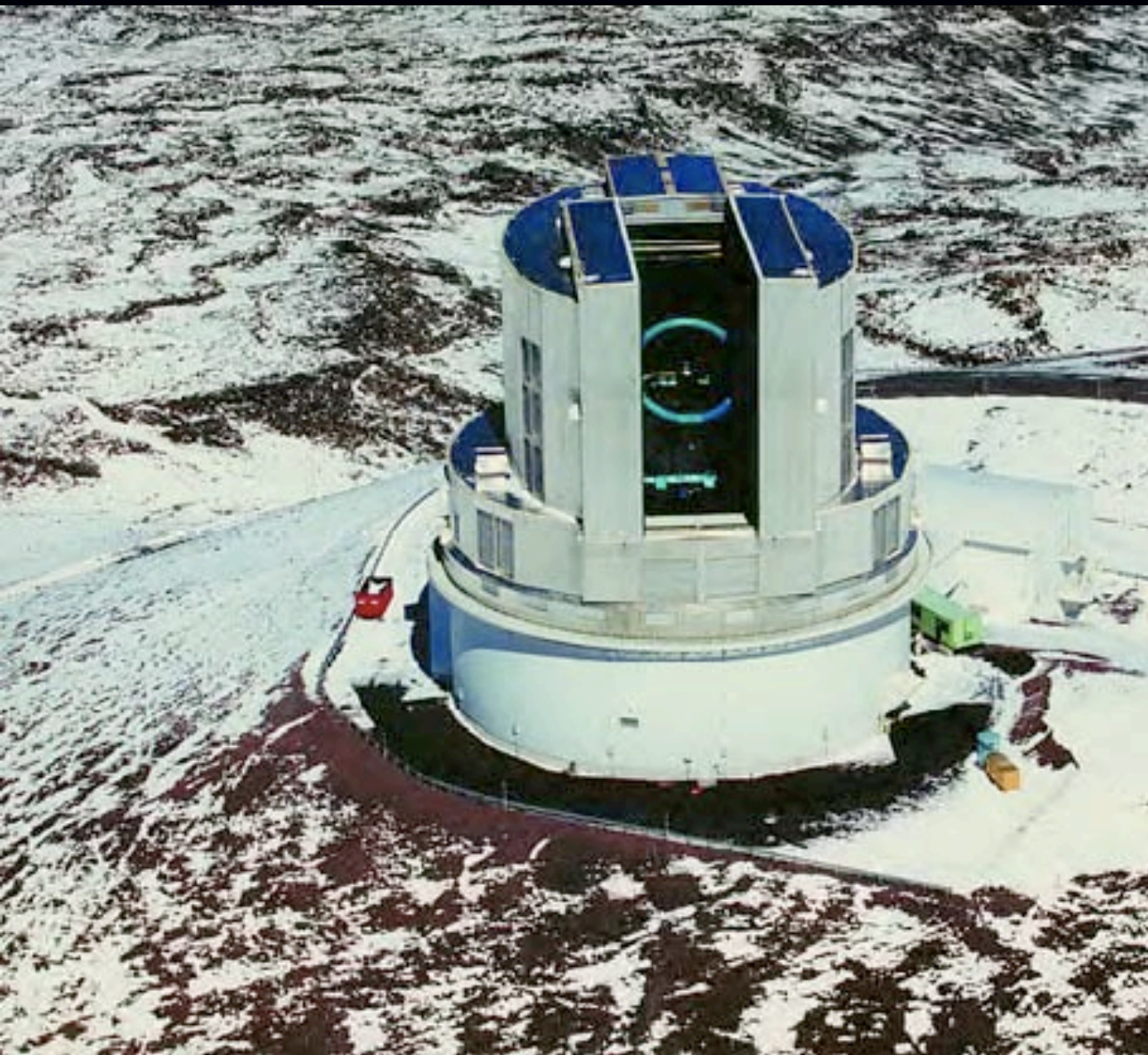


# Time Machine





# Time Machine





# Solar System









Apr 7 2012

375 km above ground

skin of peach



Sep 30, 2008  
Kaguya

380,000km  
= 1.3 light seconds



© JAXA/NHK



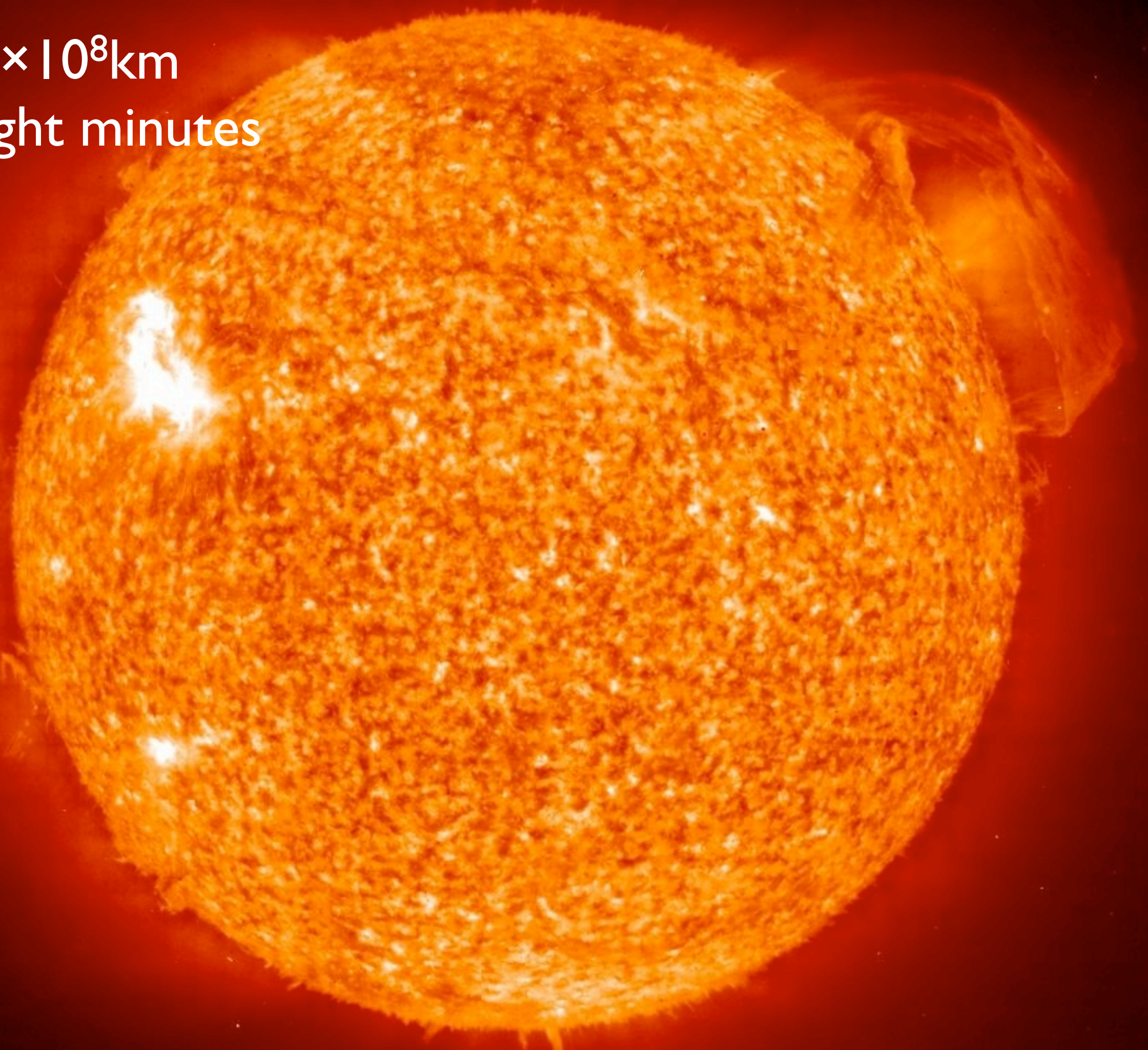
380,000km  
= 1.3 light seconds



© JAXA/NHI



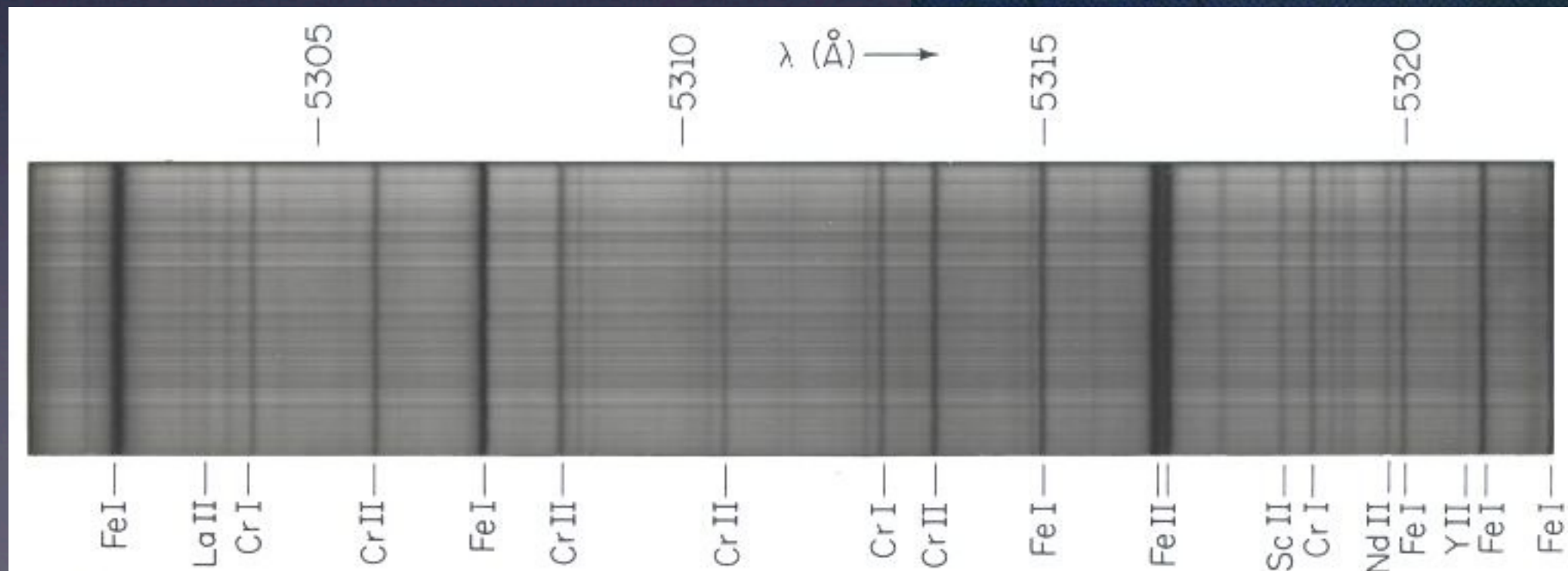
$1.5 \times 10^8 \text{ km}$   
= 8.3 light minutes





# Made of atoms

- everything around us is made of atoms
- stars are made of atoms, too
- spectroscopy



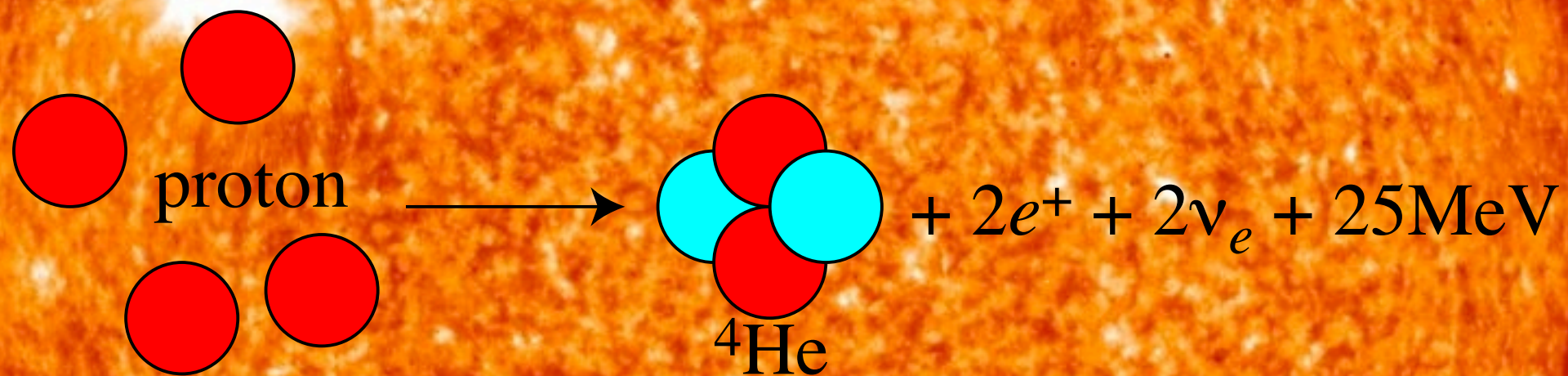


<http://www.ktf-split.hr/periodni/en/>

(1) Pure Appl. Chem., 73, No. 4, 667-683 (2001)  
Relative atomic mass is shown with five significant figures. For elements have no stable nuclides, the value enclosed in brackets indicates the mass number of the longest-lived isotope of the element.  
However three such elements (Th, Pa, and U) do have a characteristic terrestrial isotopic composition, and for these an atomic weight is tabulated.



$1.5 \times 10^8 \text{ km}$   
= 8.3 light minutes



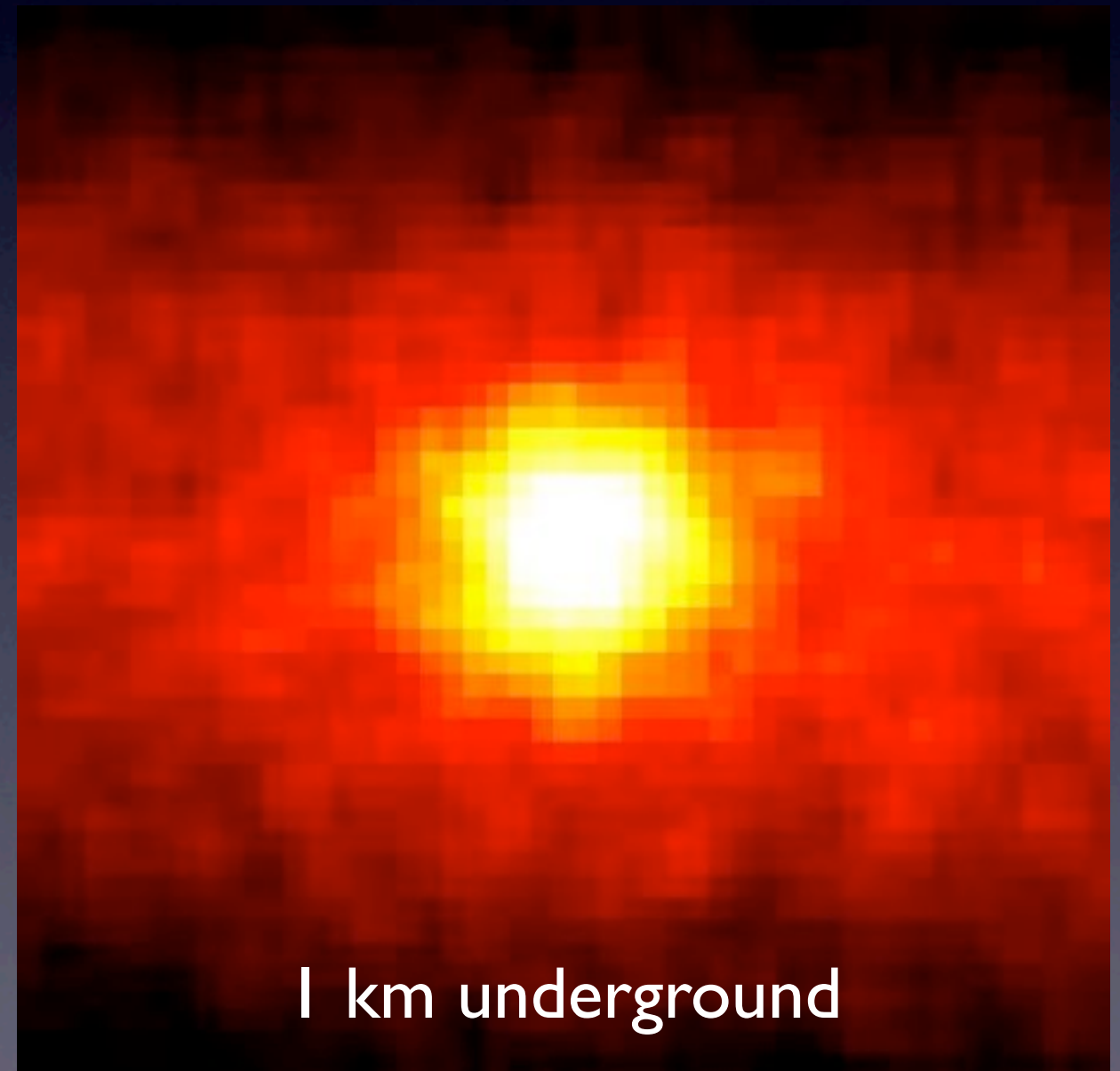
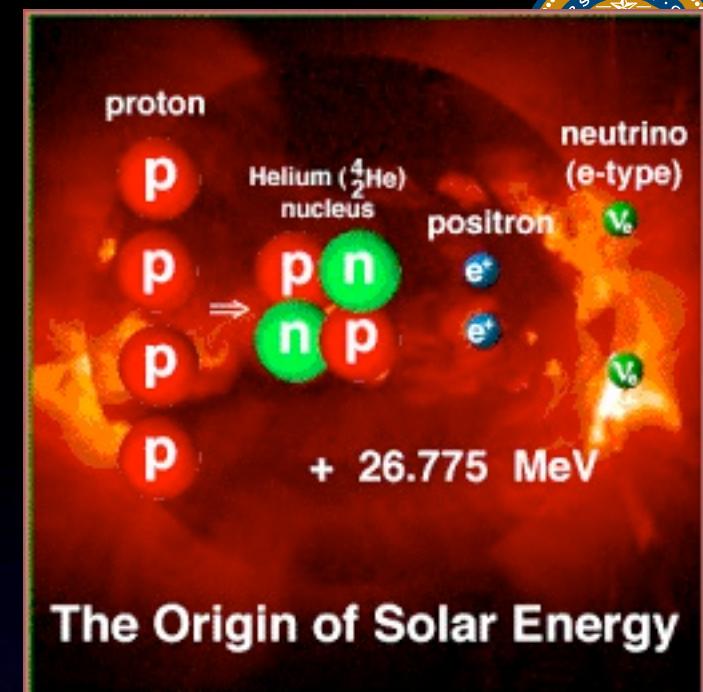
$$E=mc^2$$

5 Mt lighter every second  
turning mass to energy  
burning hydrogen



# proof

*nuclear fusion also produces neutrinos*  
*tens of trillions of neutrinos going through our body*  
*every second*

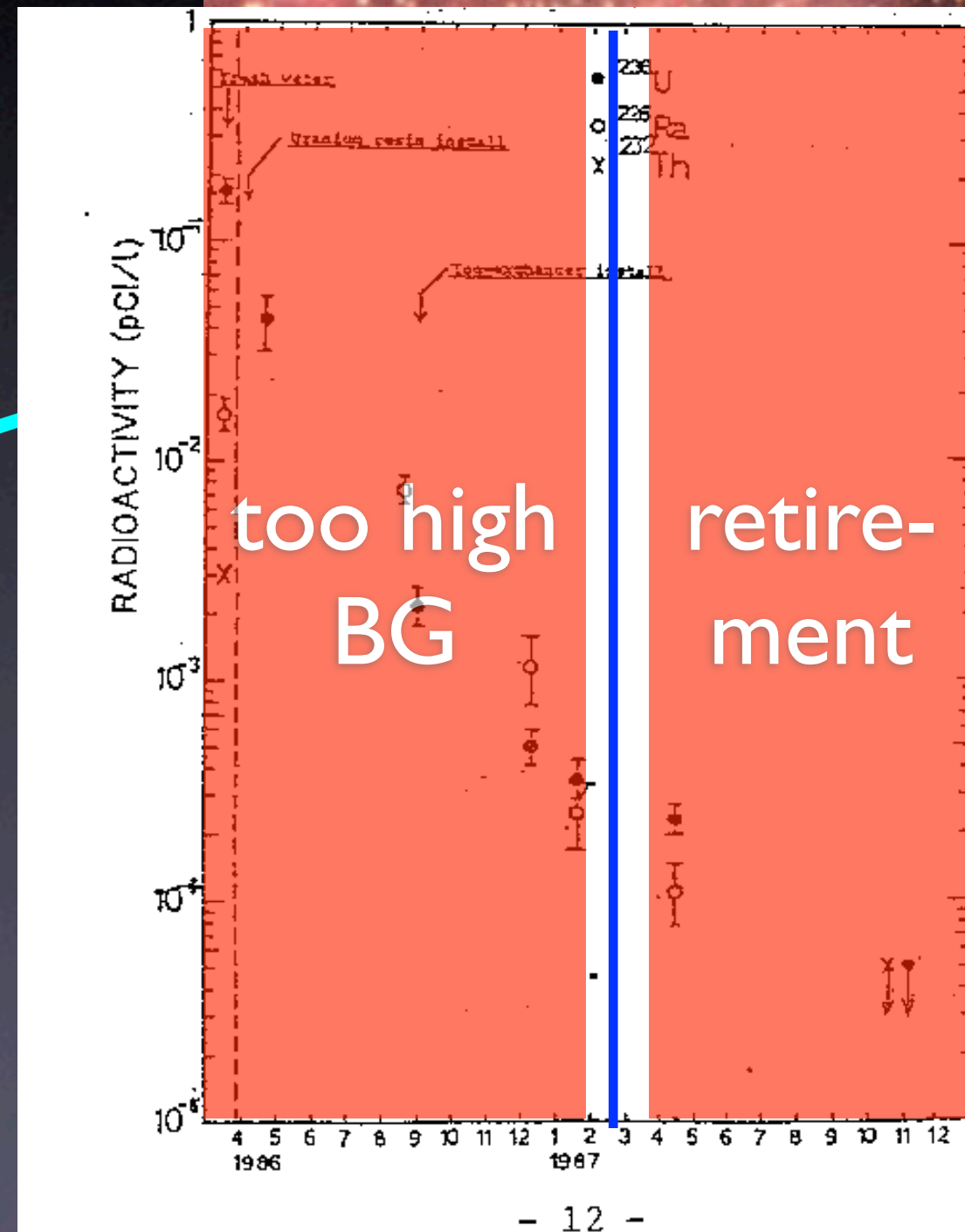
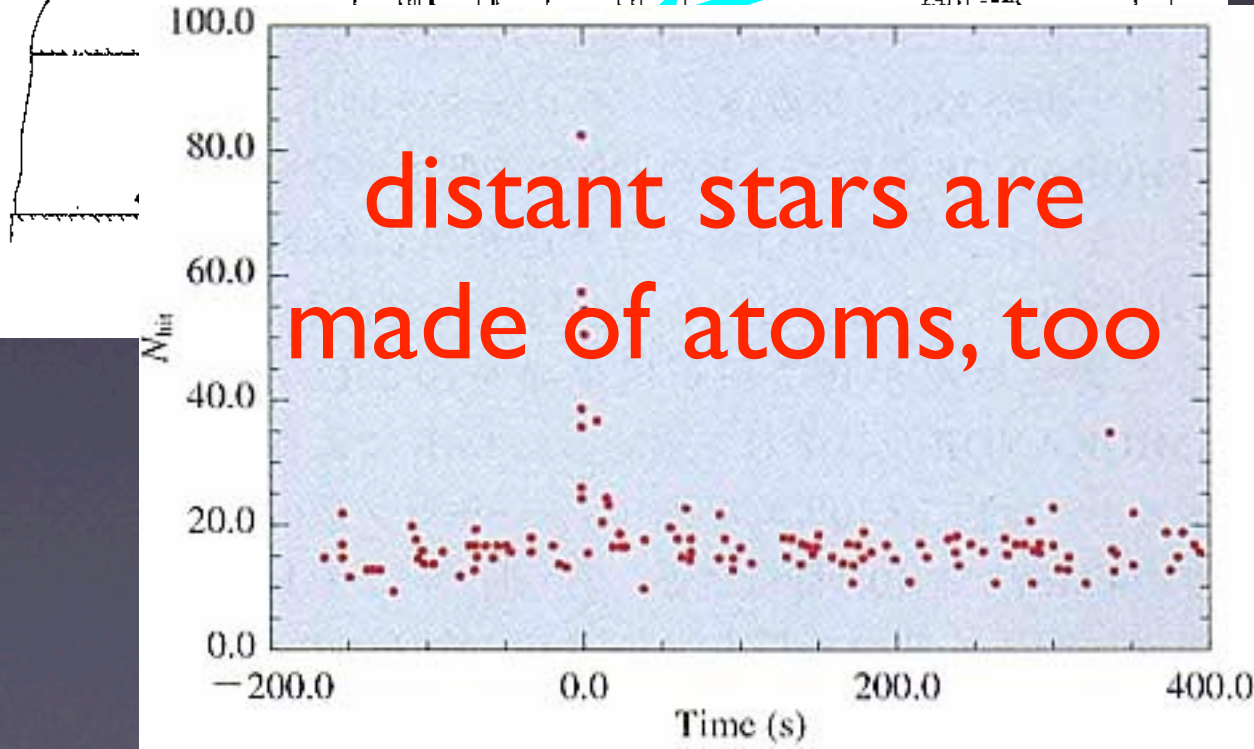
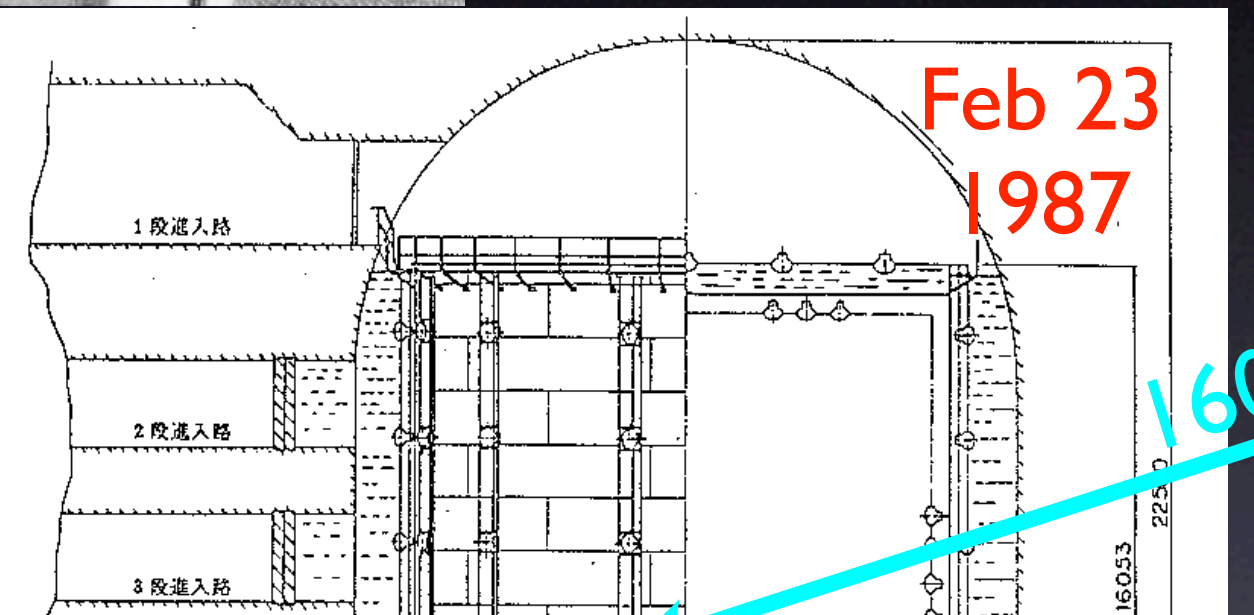


1 km underground





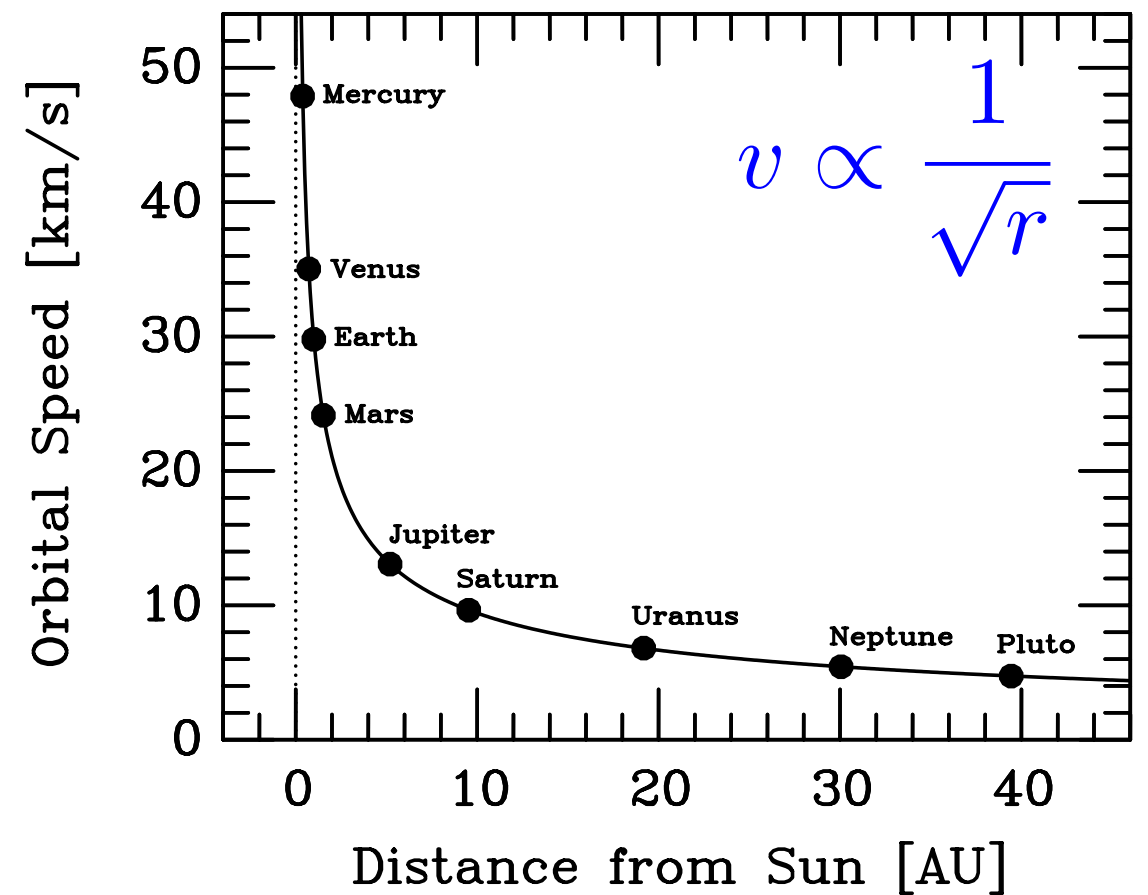
# luck





Neptune  
4 light hours

Solar



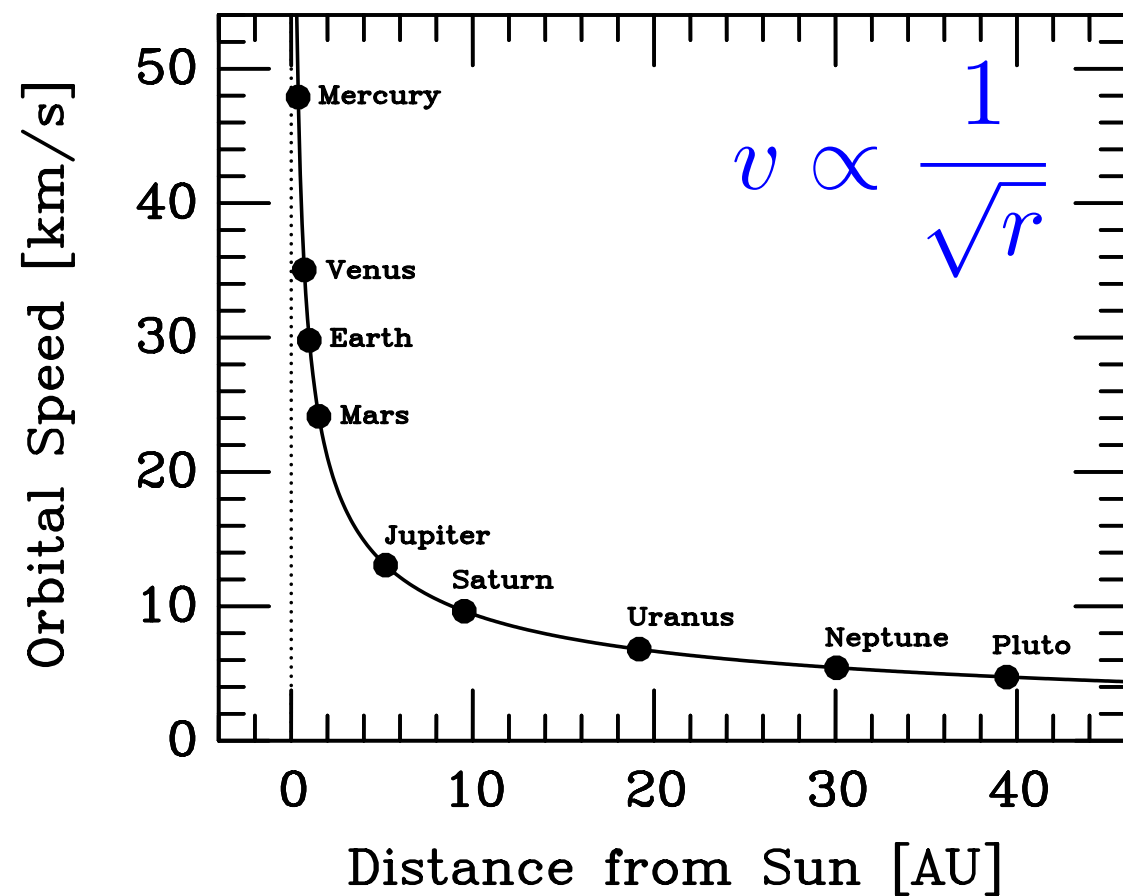
20 light minutes  
Ito Kawawa



Earth revolves around the Sun with 30km/sec



# High School physics



$$F = \frac{GM_{\odot}m}{r^2}$$

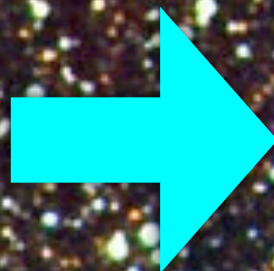
$$ma = m \frac{v^2}{r}$$

$$\frac{GM_{\odot}m}{r^2} = m \frac{v^2}{r}$$

$$v = \sqrt{\frac{GM_{\odot}}{r}} \propto \frac{1}{\sqrt{r}}$$



closest star



Proxima Centauri  
4.2 light years



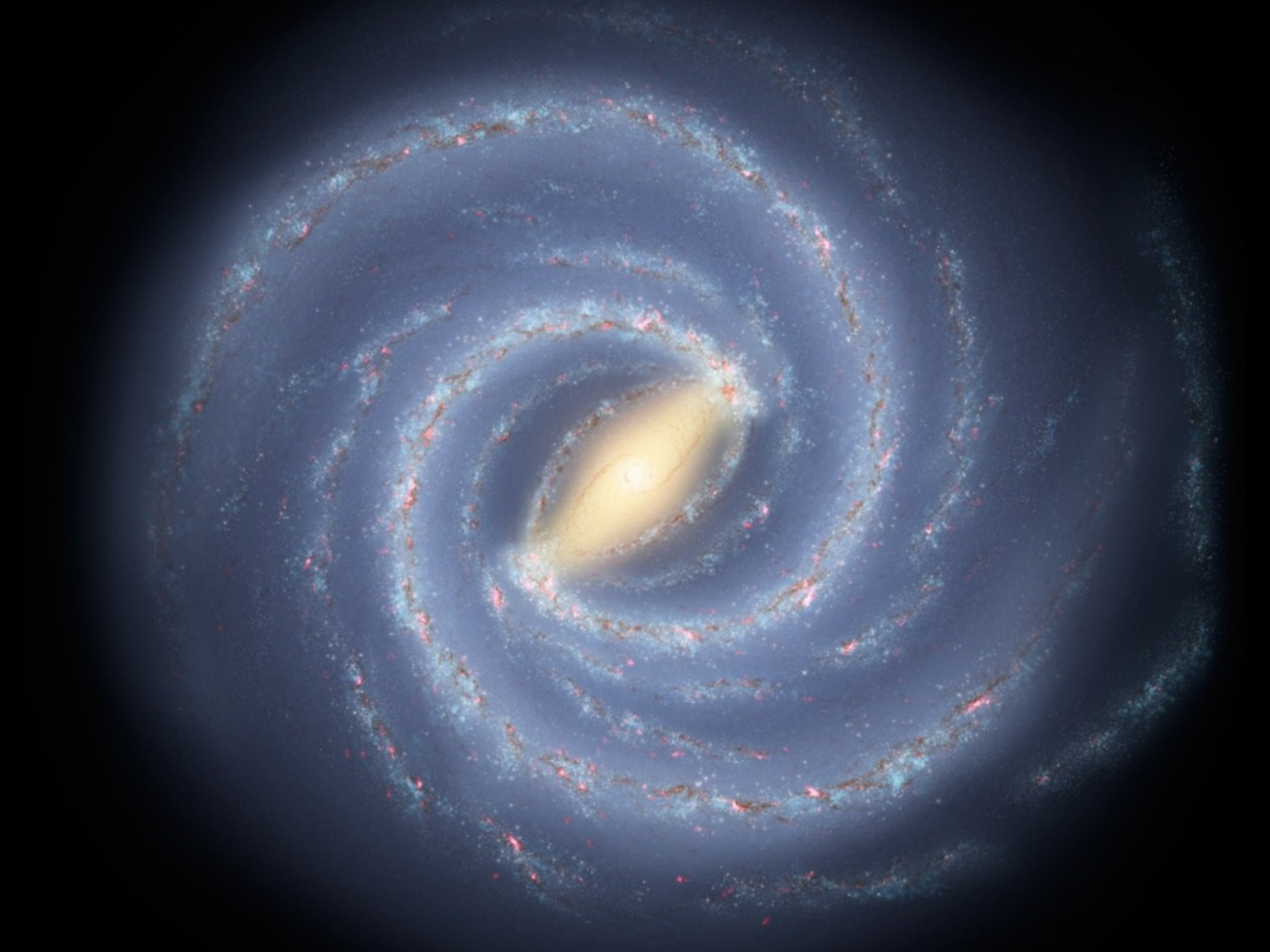


# Milky Way and Galaxies



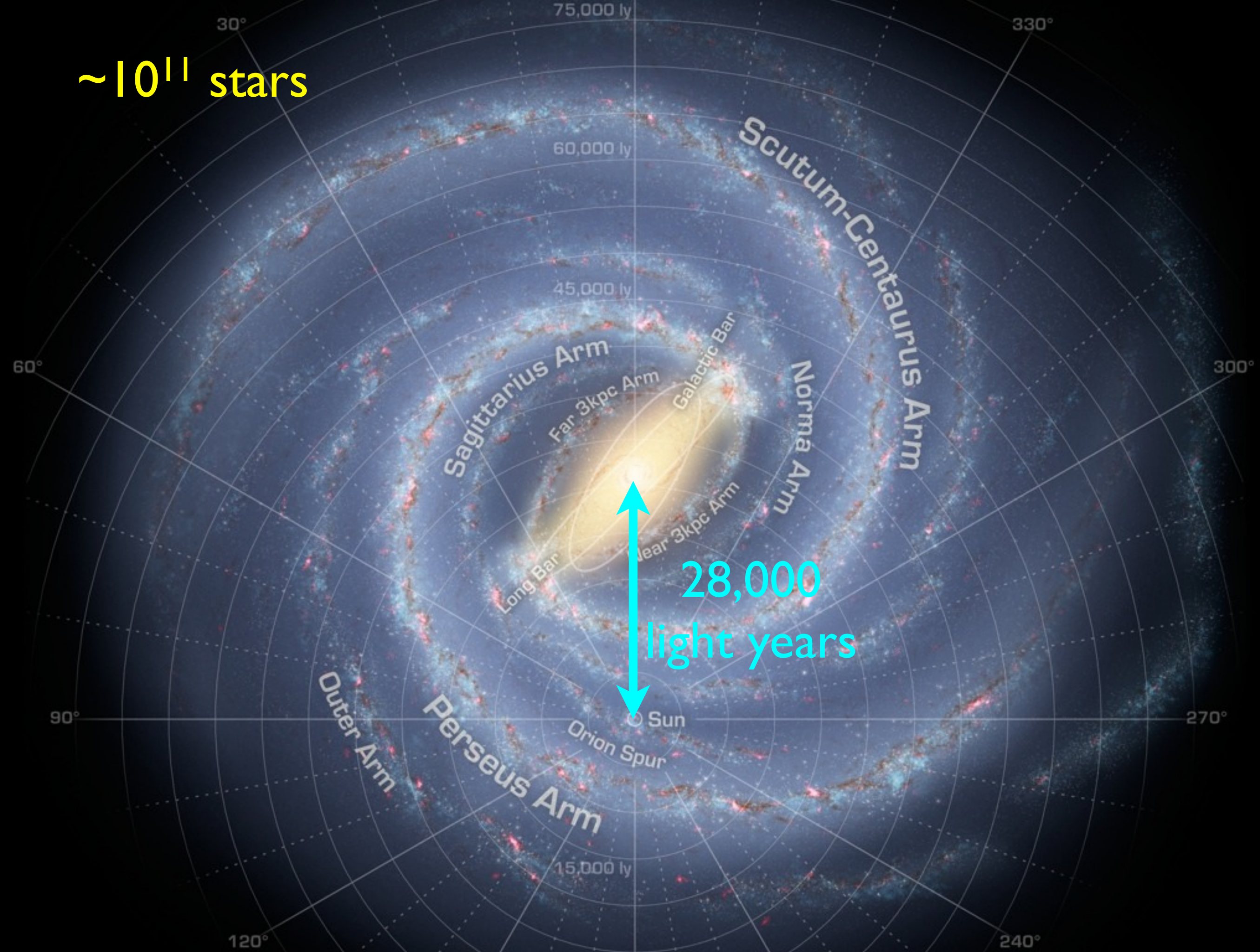




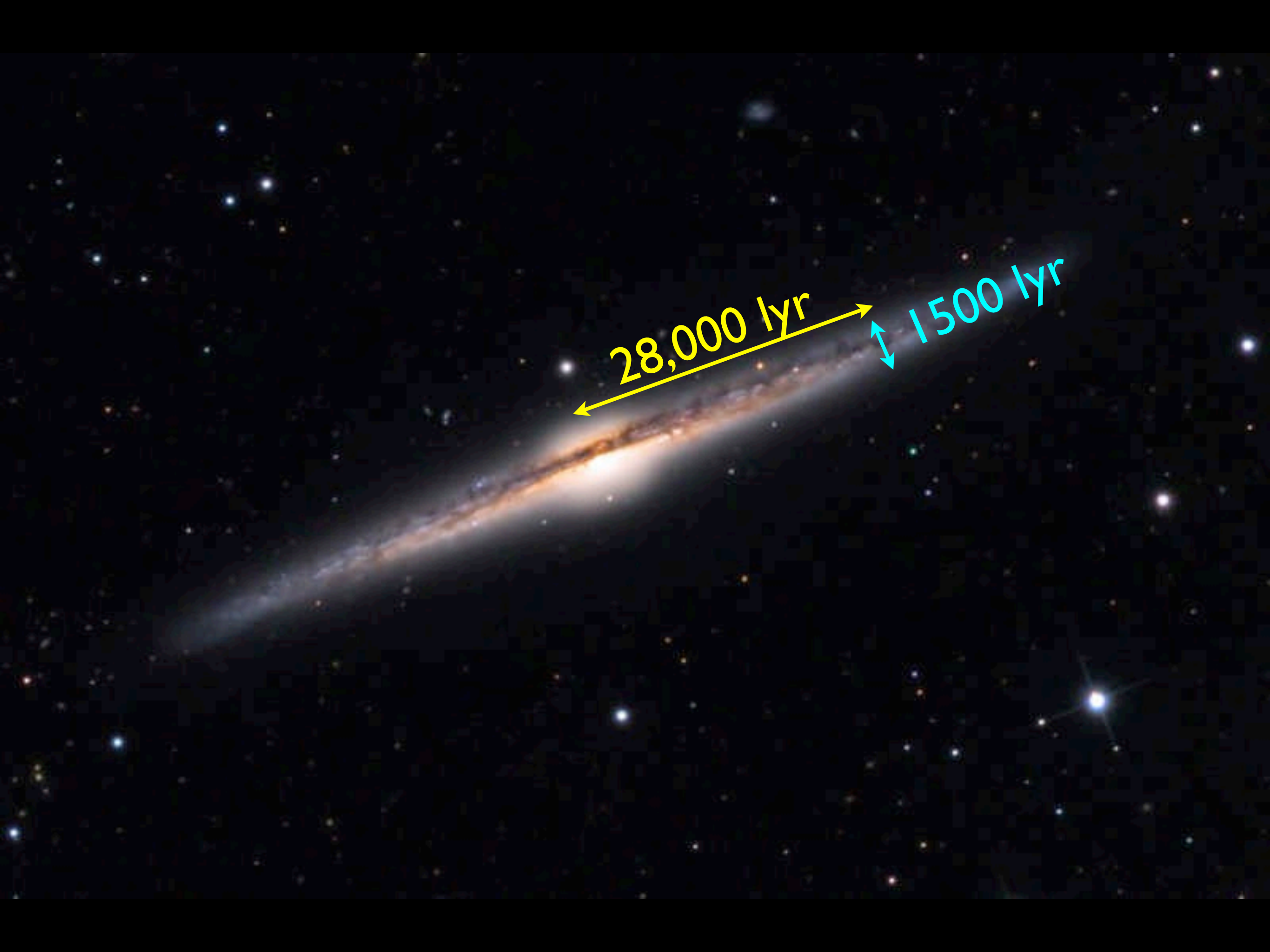




$\sim 10^{11}$  stars



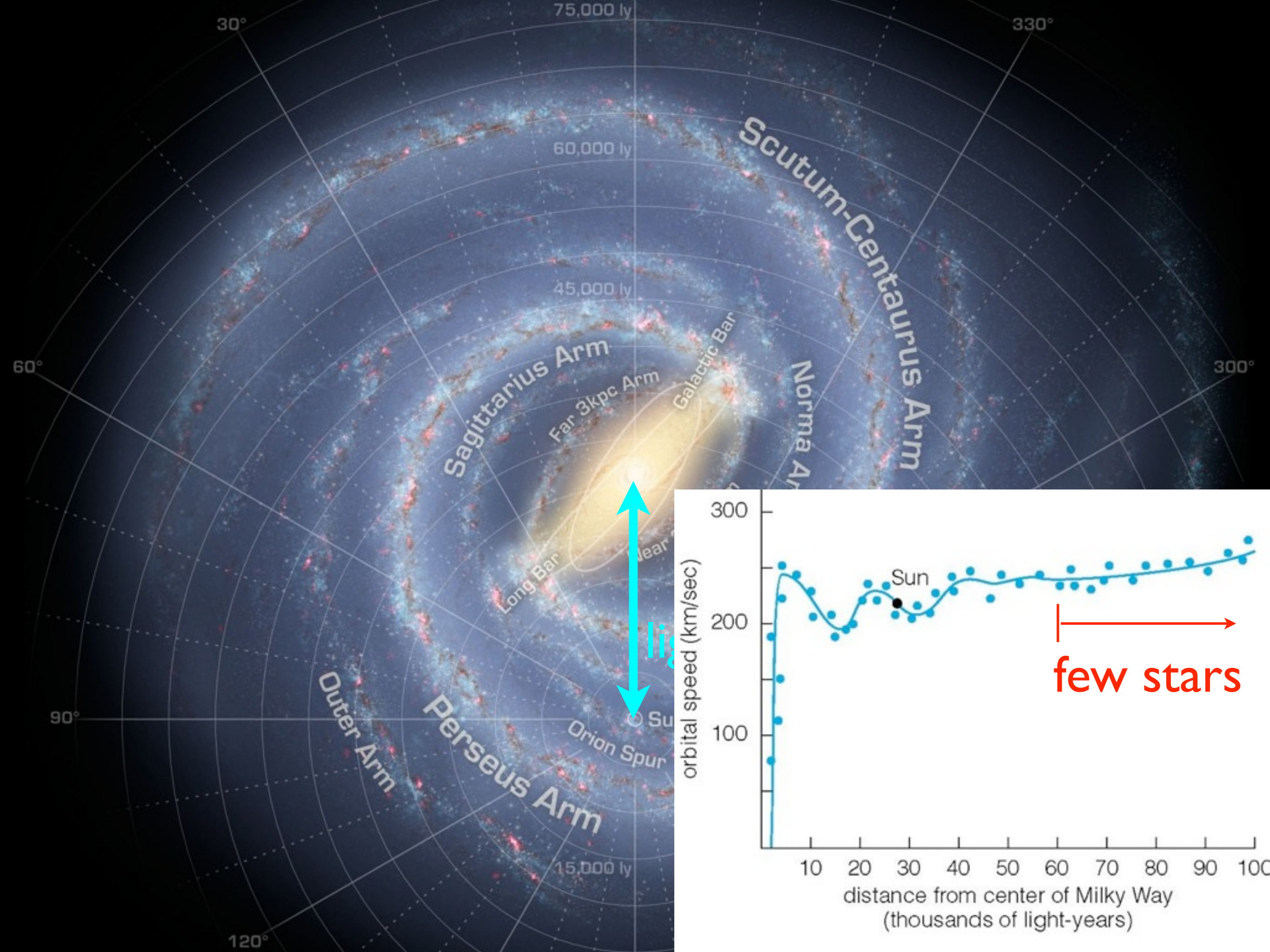




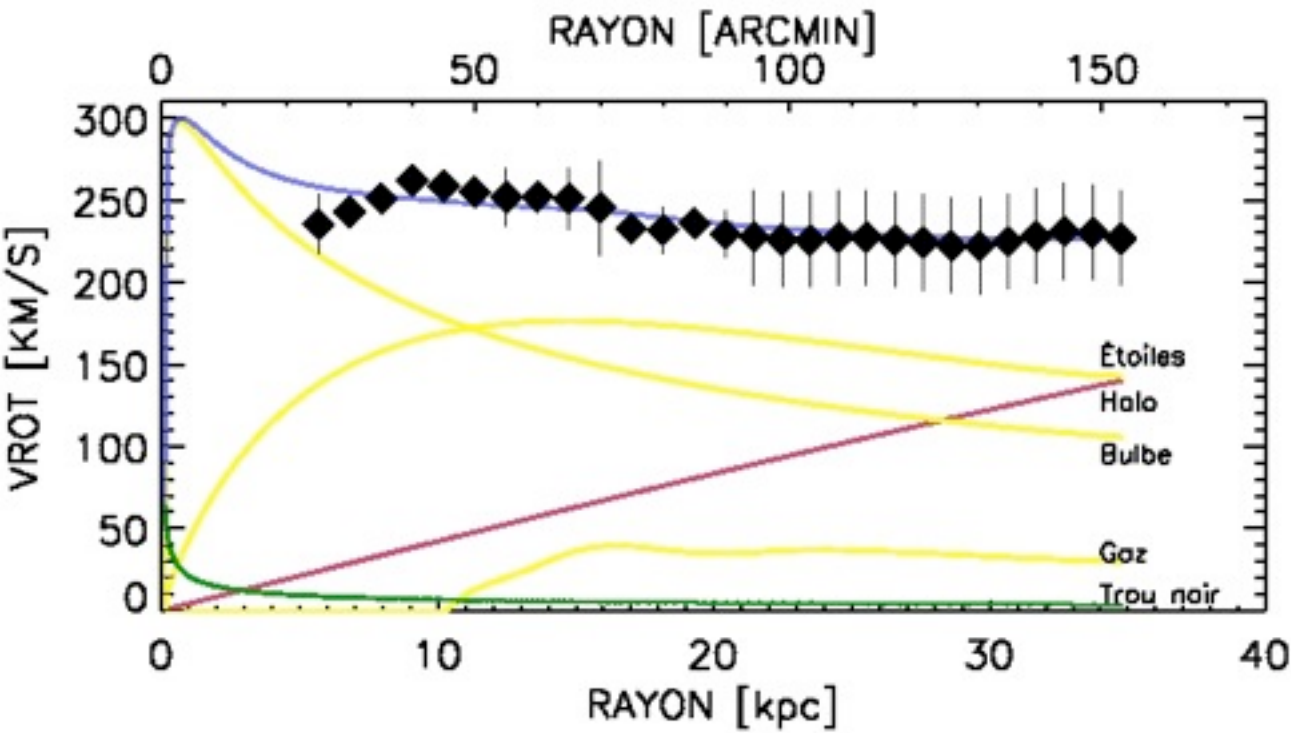
28,000 lyr

1500 lyr









will collide with us  
in 4.5 billion years

Andromeda M33 = 2.5M lyr

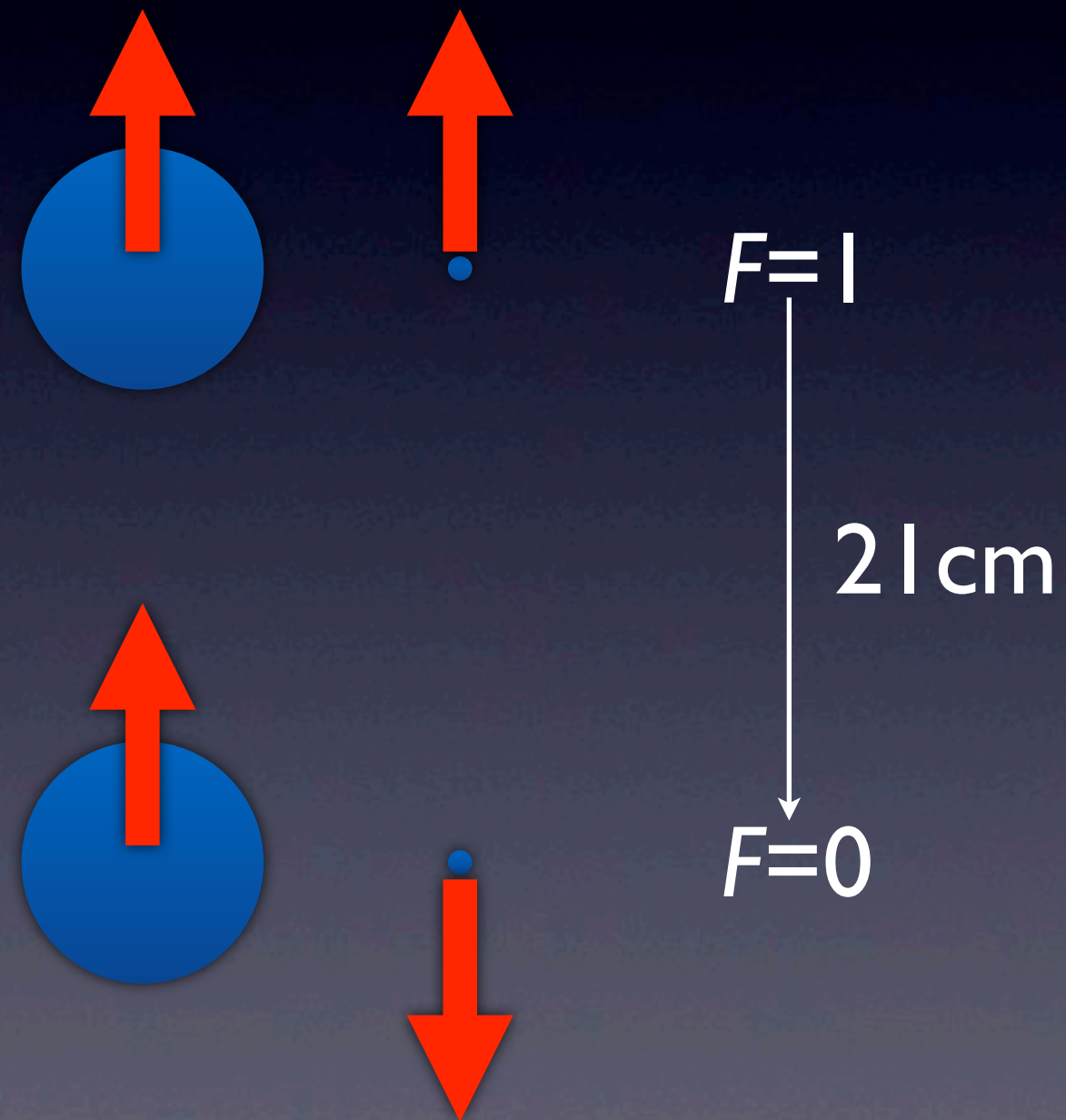


# How do we measure the rotation curve?

- Special relativity

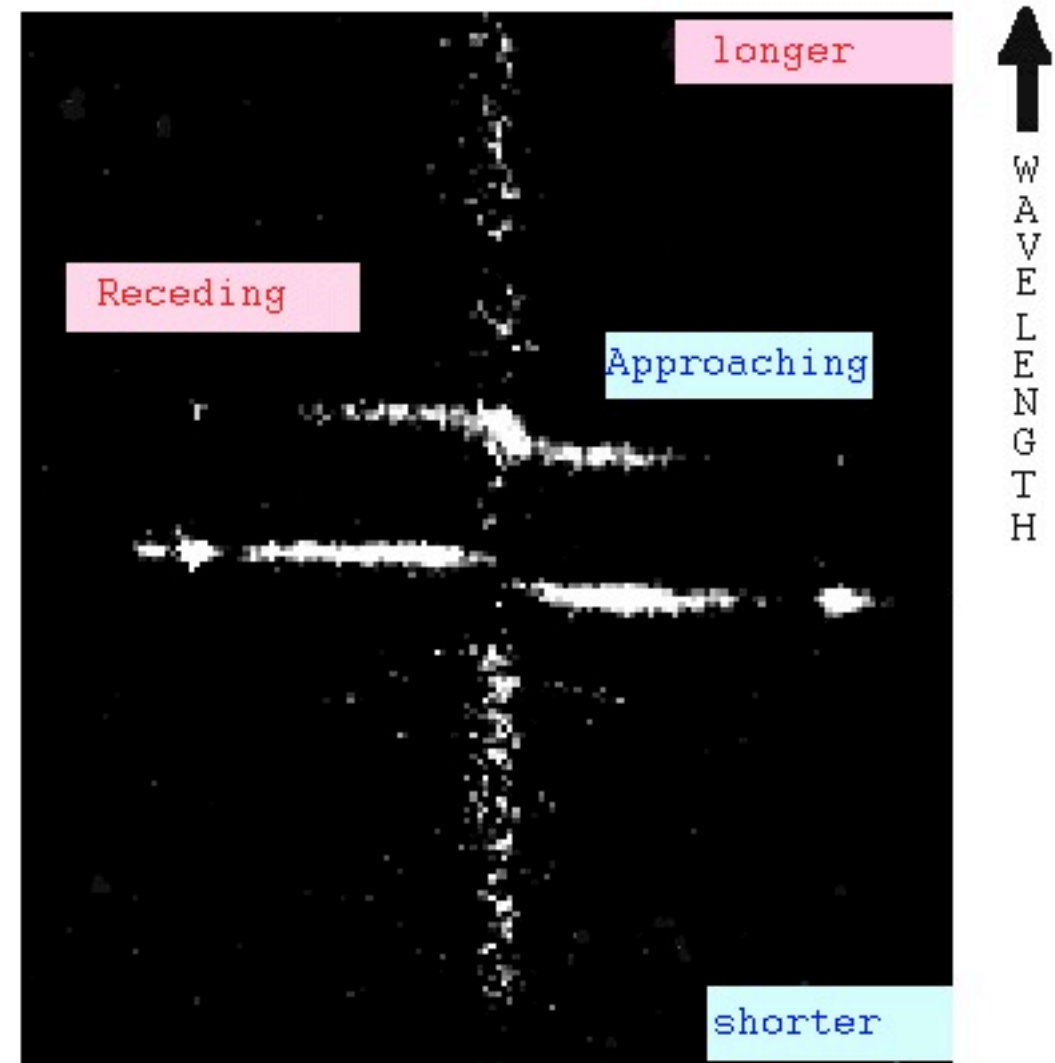
$$f' = \sqrt{\frac{c \mp v}{c \pm v}} f \approx \left(1 \mp \frac{v}{c}\right) f$$

- hyperfine splitting in neutral hydrogen
- 21cm line can be excited by the cosmic microwave background
- $kT_0 = 0.23 \text{ meV}$
- $h c / 21 \text{ cm} = 0.94 \text{ } \mu\text{eV}$





# Galaxy rotation curve



Distance along galaxy major axis →

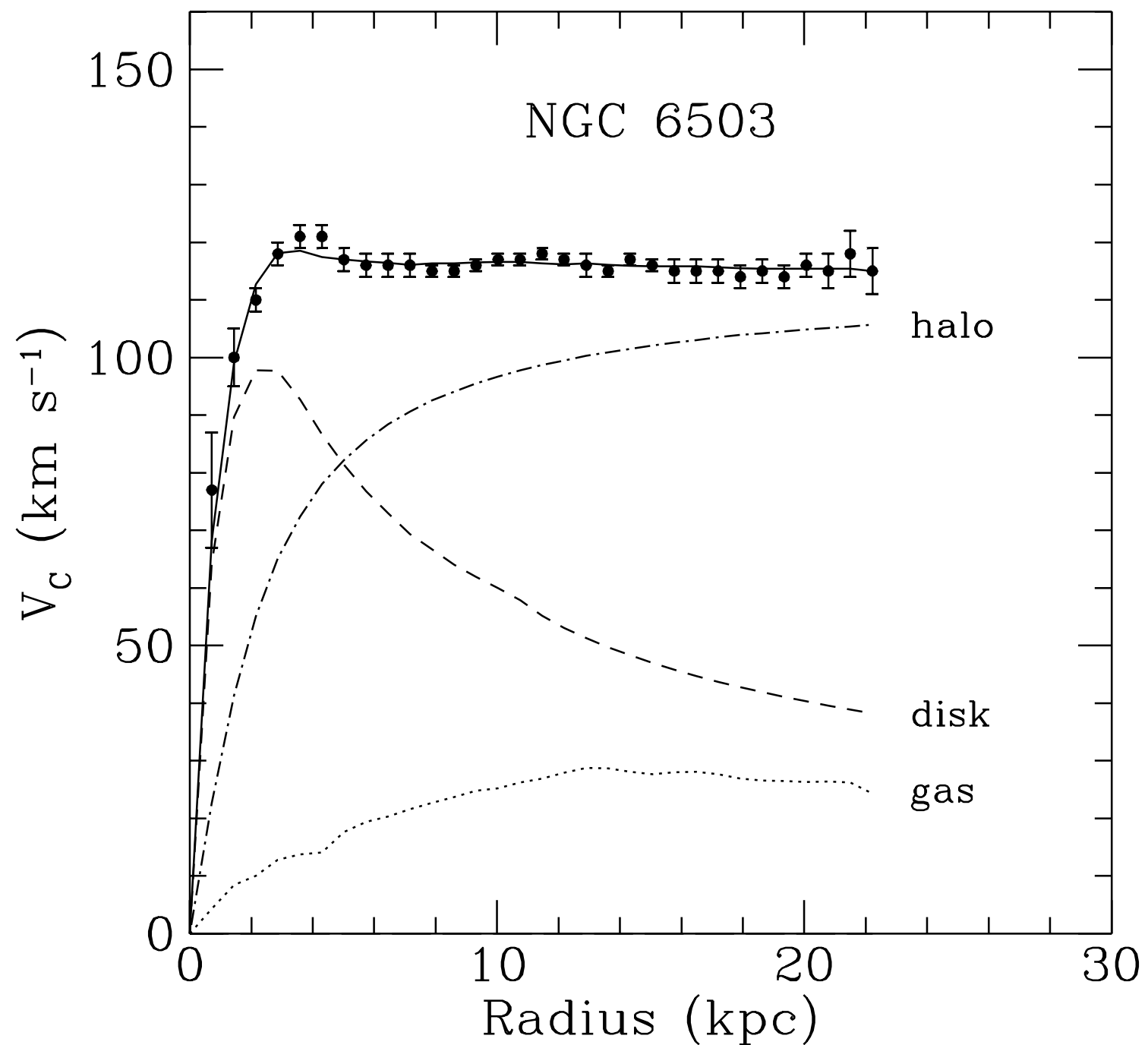
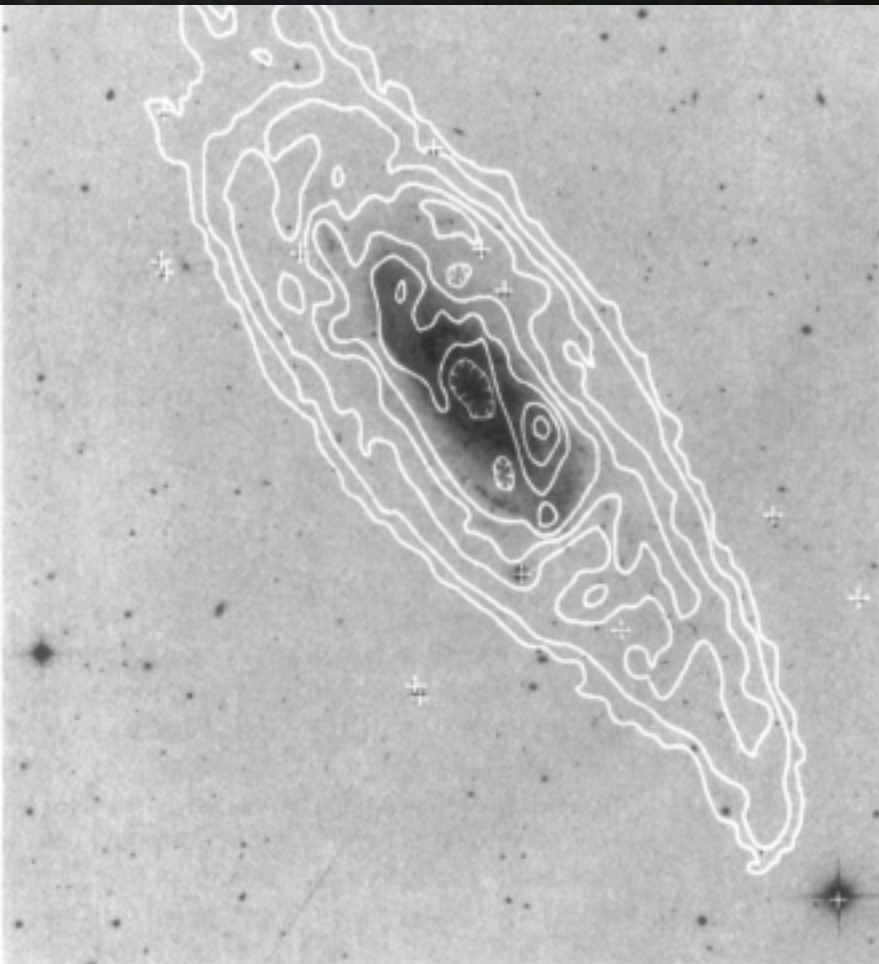




Vera  
Rubin

1960s







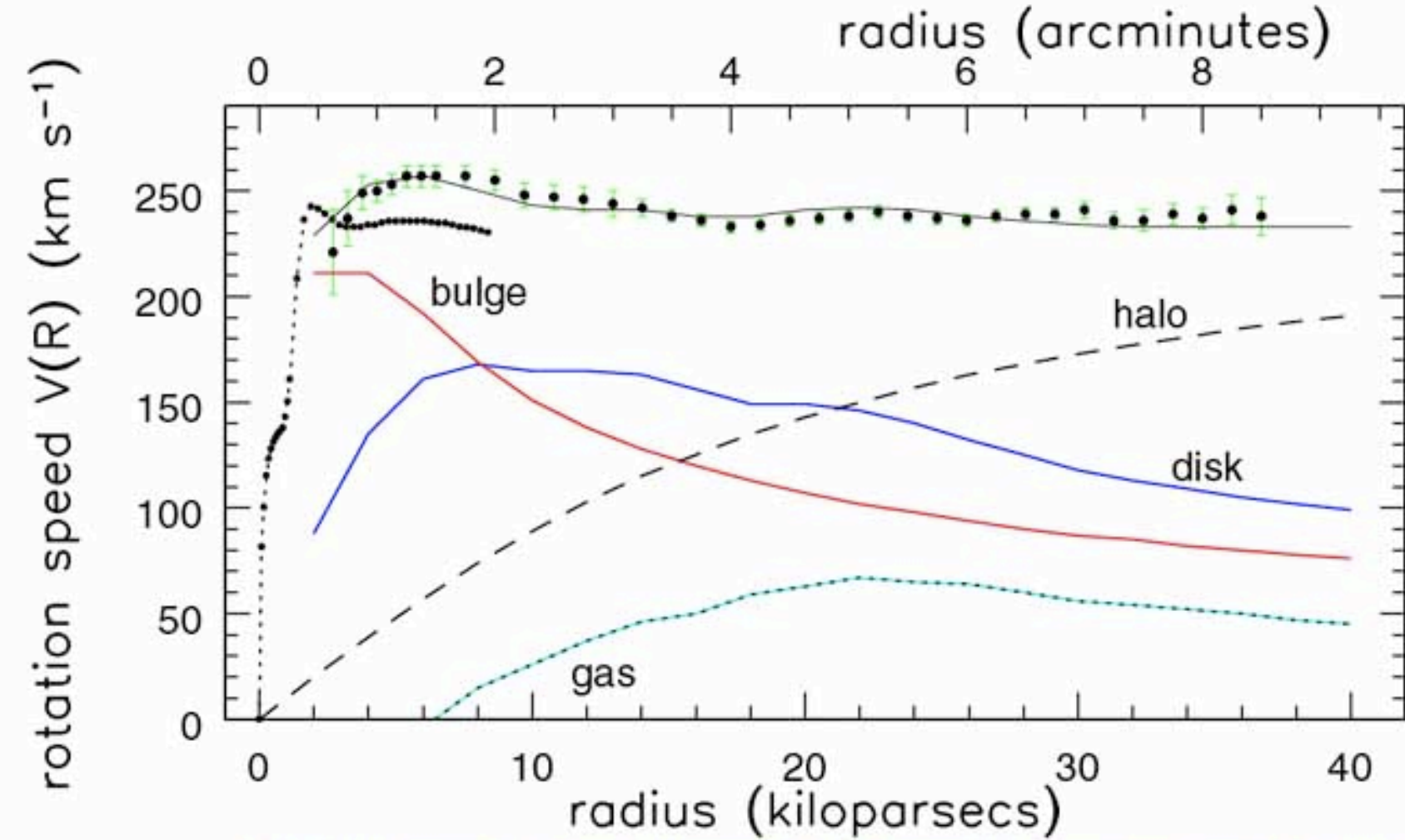
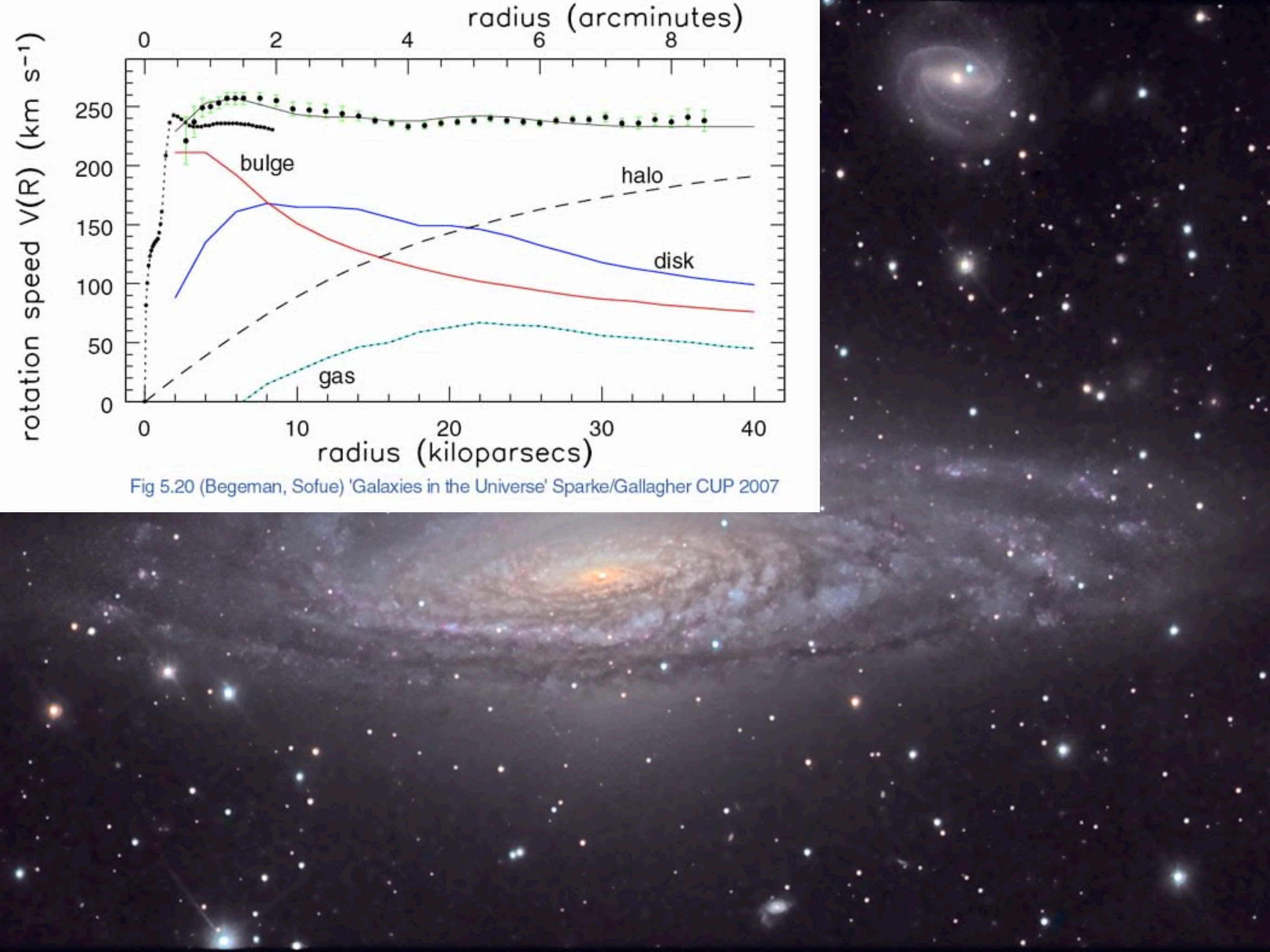
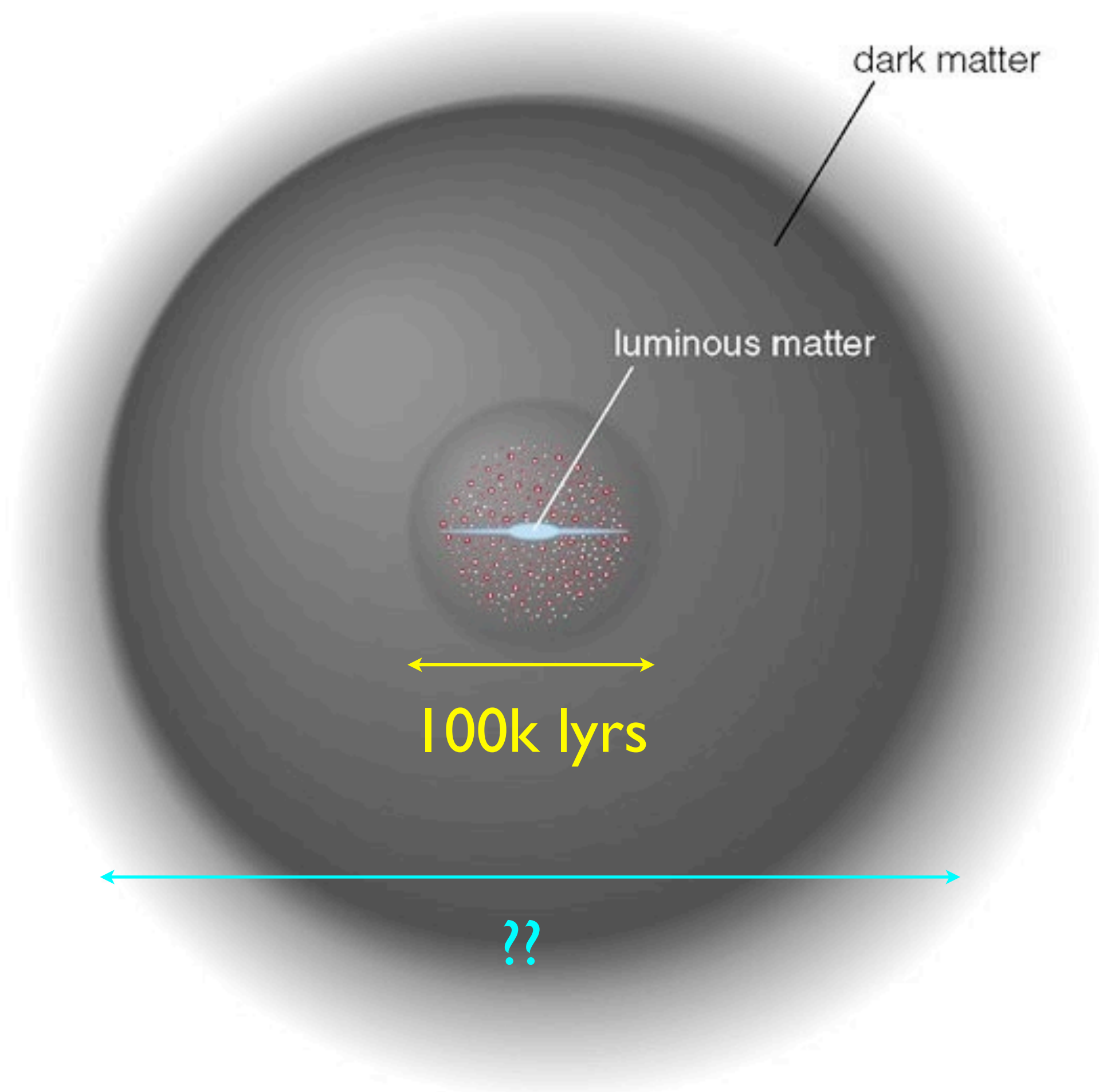


Fig 5.20 (Begeman, Sofue) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007









# connects galaxies

stacking 85k quasars near 20M galaxies

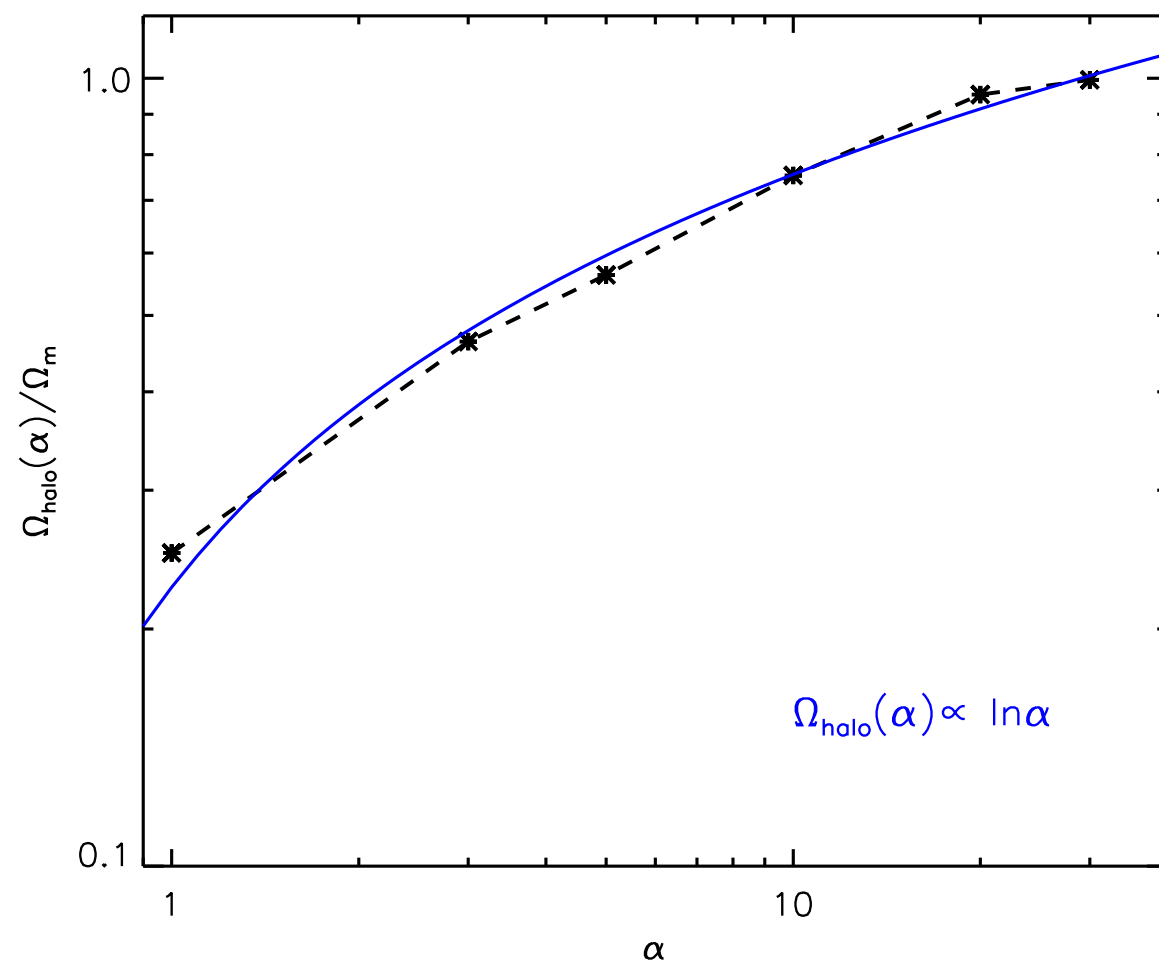
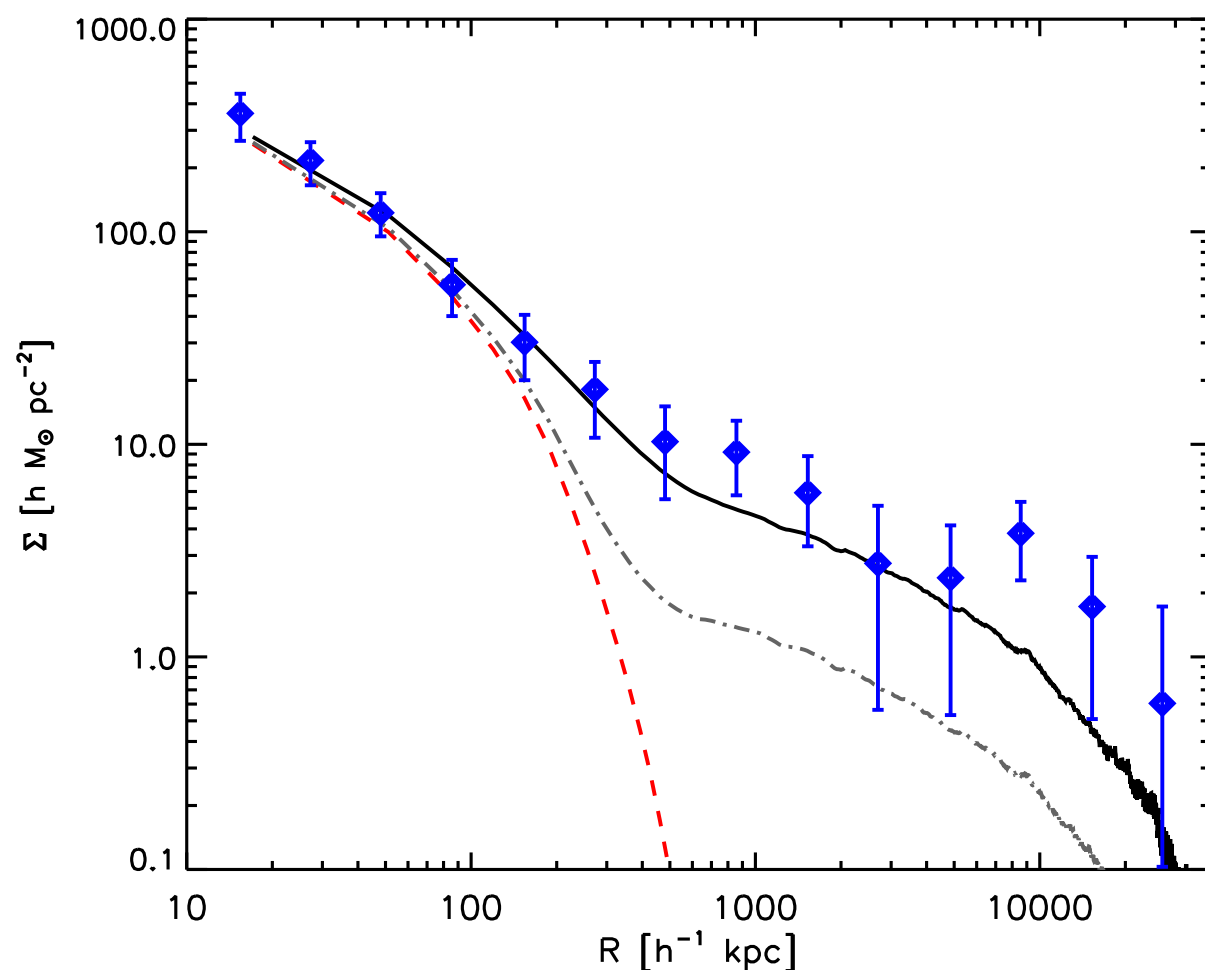


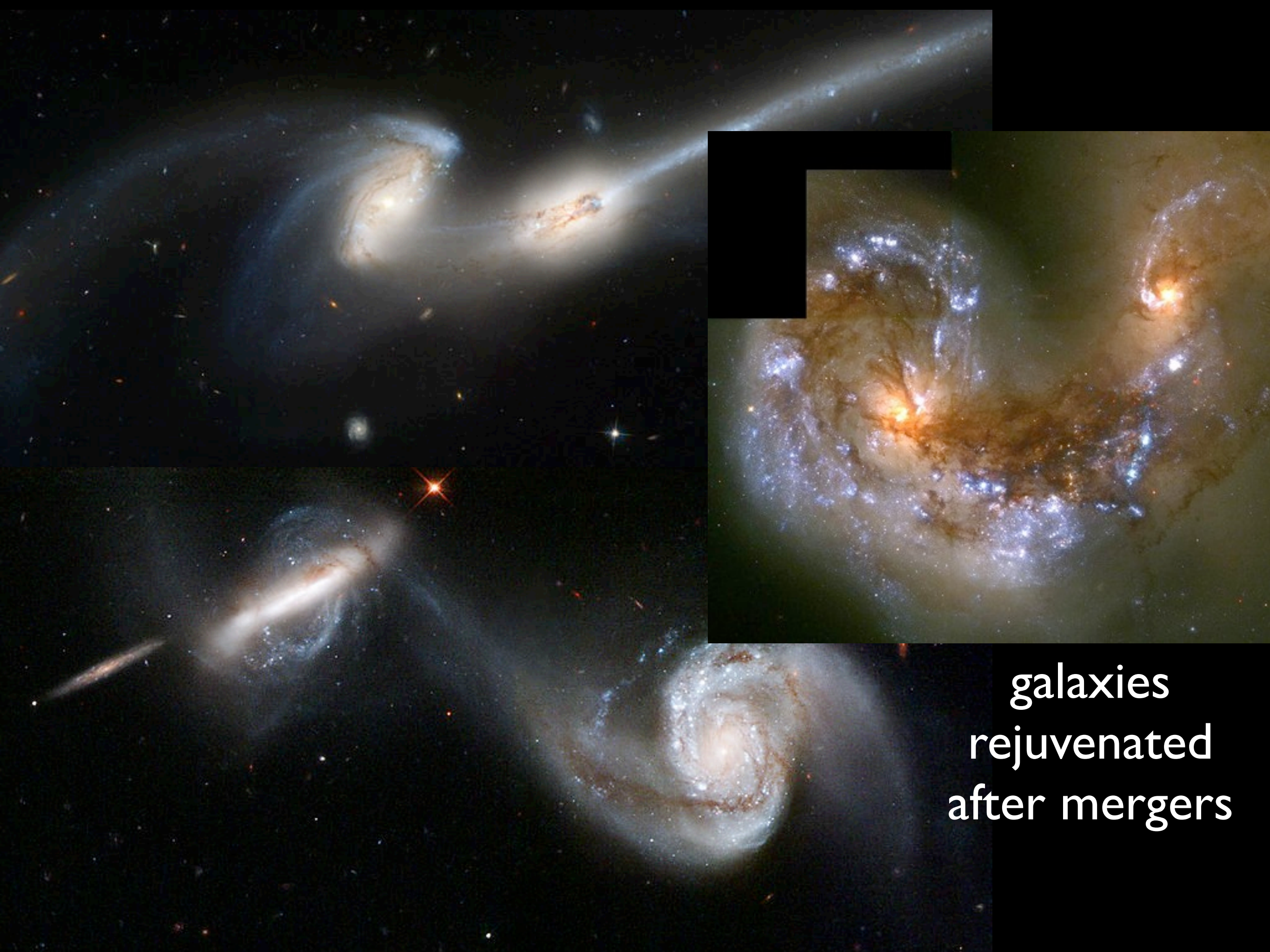
Fig. 2.— The mean surface mass density profile as a function of the distance from the centre of galaxies. The thick solid curve is the mean of all haloes above the mass threshold. The dash-dotted curve represents the contribution from particles bound to haloes, i.e., particles that reside within where  $R_{\text{vir}}$  is the pseudovirial radius and  $\alpha$  is the multiplier represented in the abscissa. The solid the virial radius of all haloes. The data with error bars are the observational estimate by MSFR curve is  $0.23 \ln + 0.23$  given in the text.

Fig. 4.— Fraction of mass contained in the sphere centred on individual haloes with radius  $\alpha R_{\text{vir}}$ , where  $R_{\text{vir}}$  is the pseudovirial radius and  $\alpha$  is the multiplier represented in the abscissa. The solid the virial radius of all haloes. The data with error bars are the observational estimate by MSFR curve is  $0.23 \ln + 0.23$  given in the text.

Ménard et al 2009

Masaki Fukugita Yoshida 2011





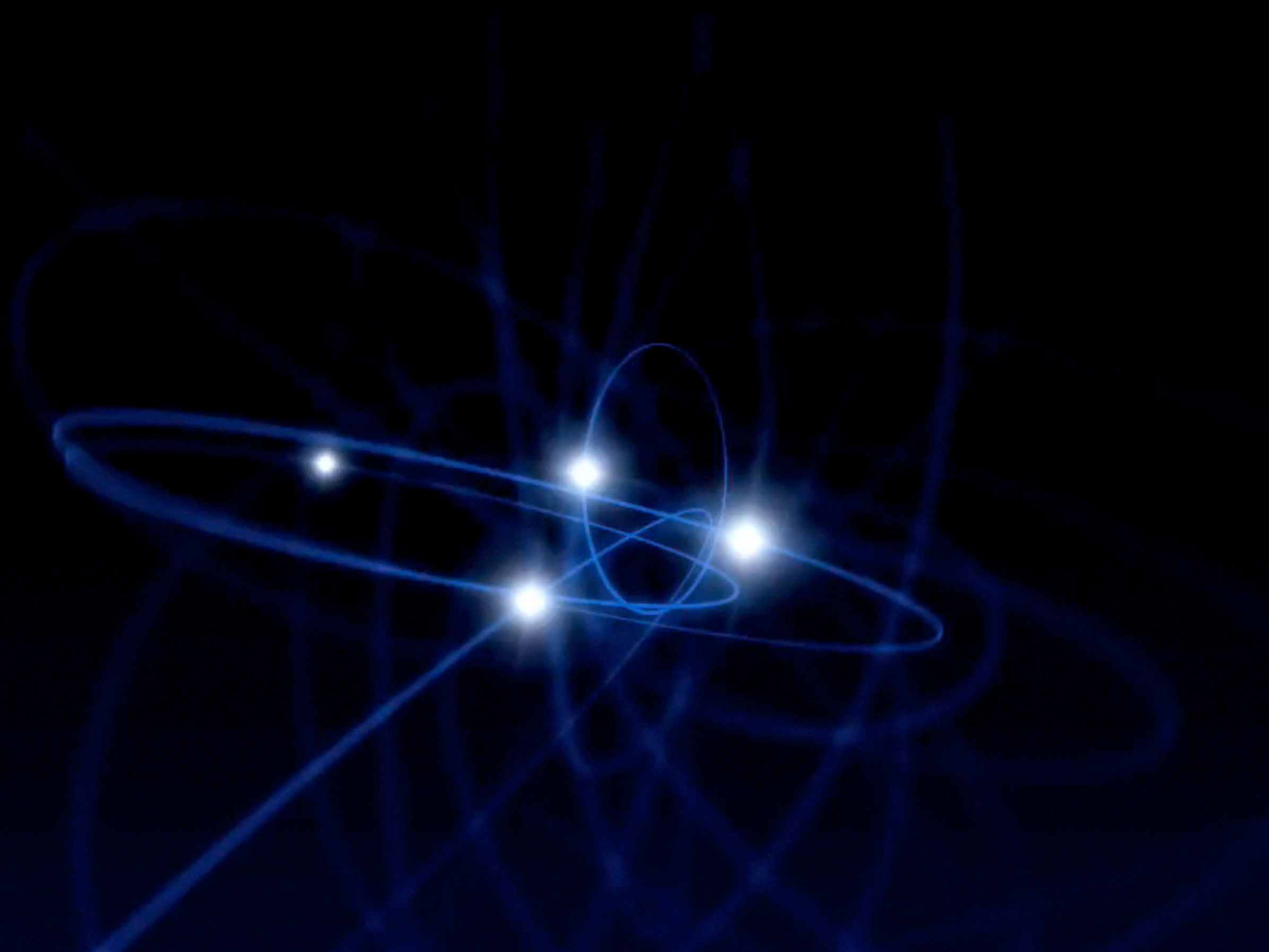
galaxies  
rejuvenated  
after mergers



# Center of Milky Way



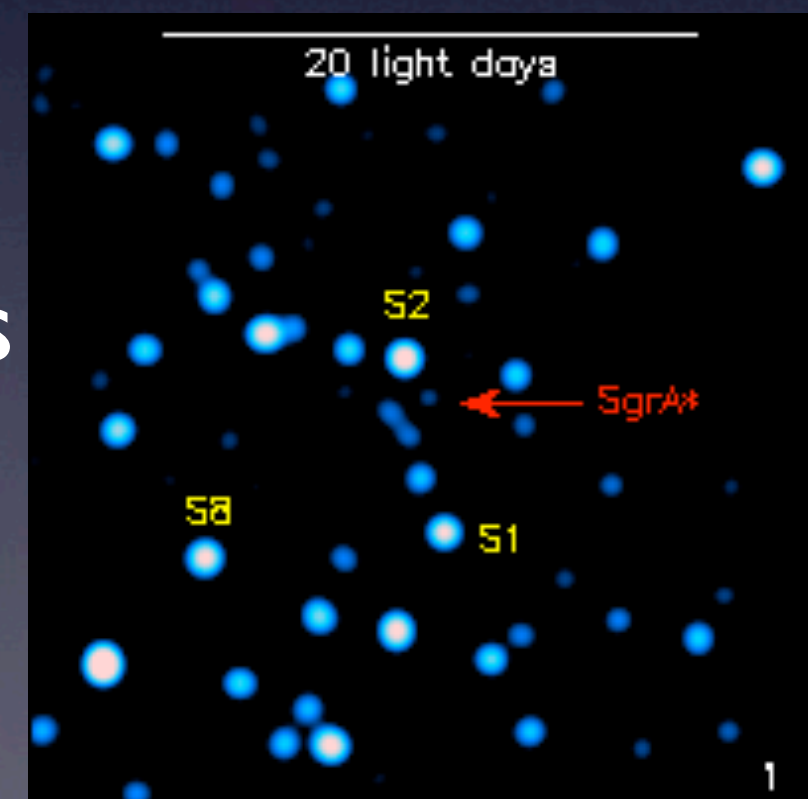






# Supermassive Black Hole

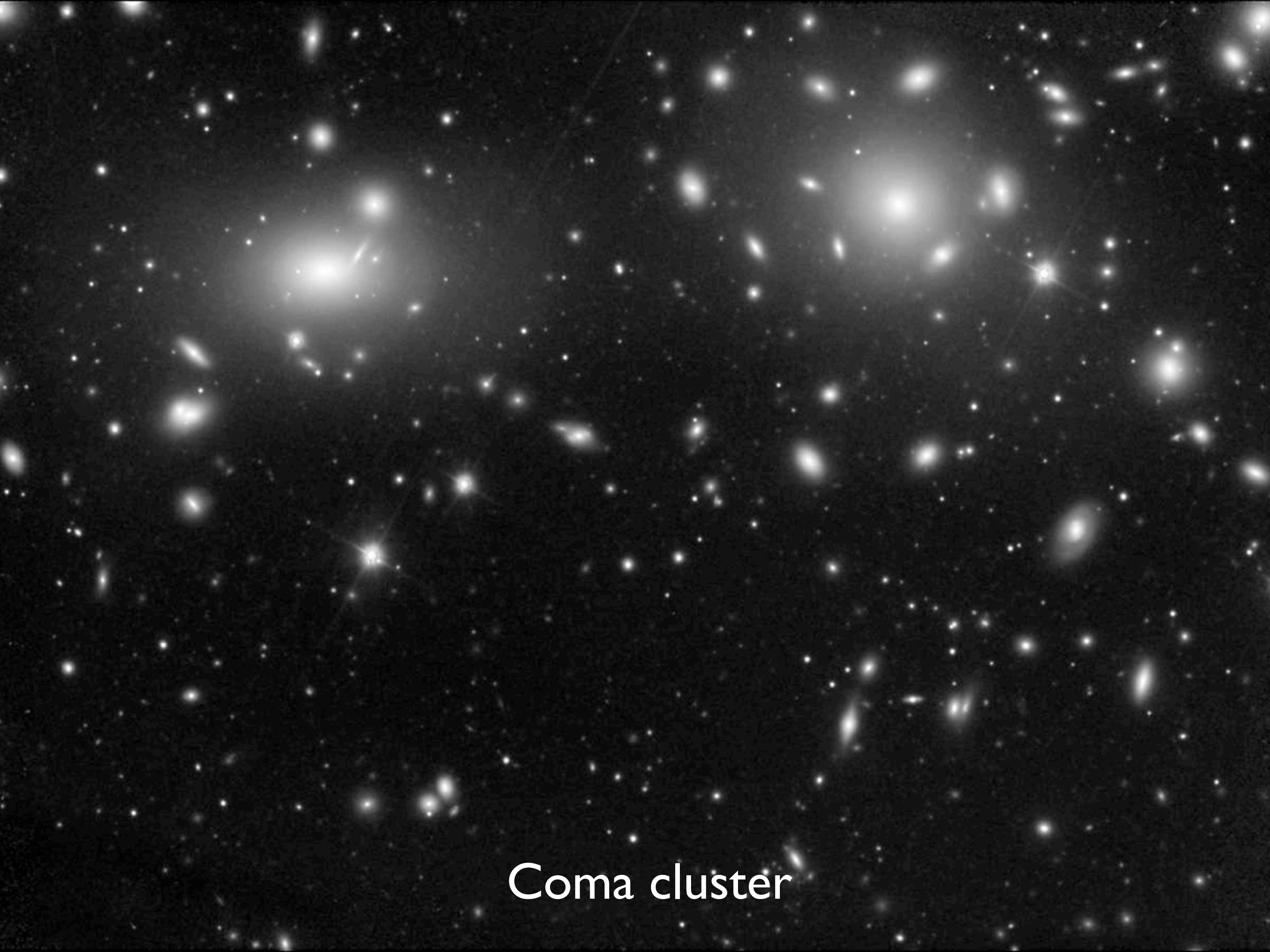
- supermassive blackhole of mass  $\sim 4M_{\text{sun}}$  at the center of Milky Way
- swallows gas around it
- “death cry” for about 30 min
- but can’t be dark matter, far less than 100billion stars





# Cluster of Galaxies



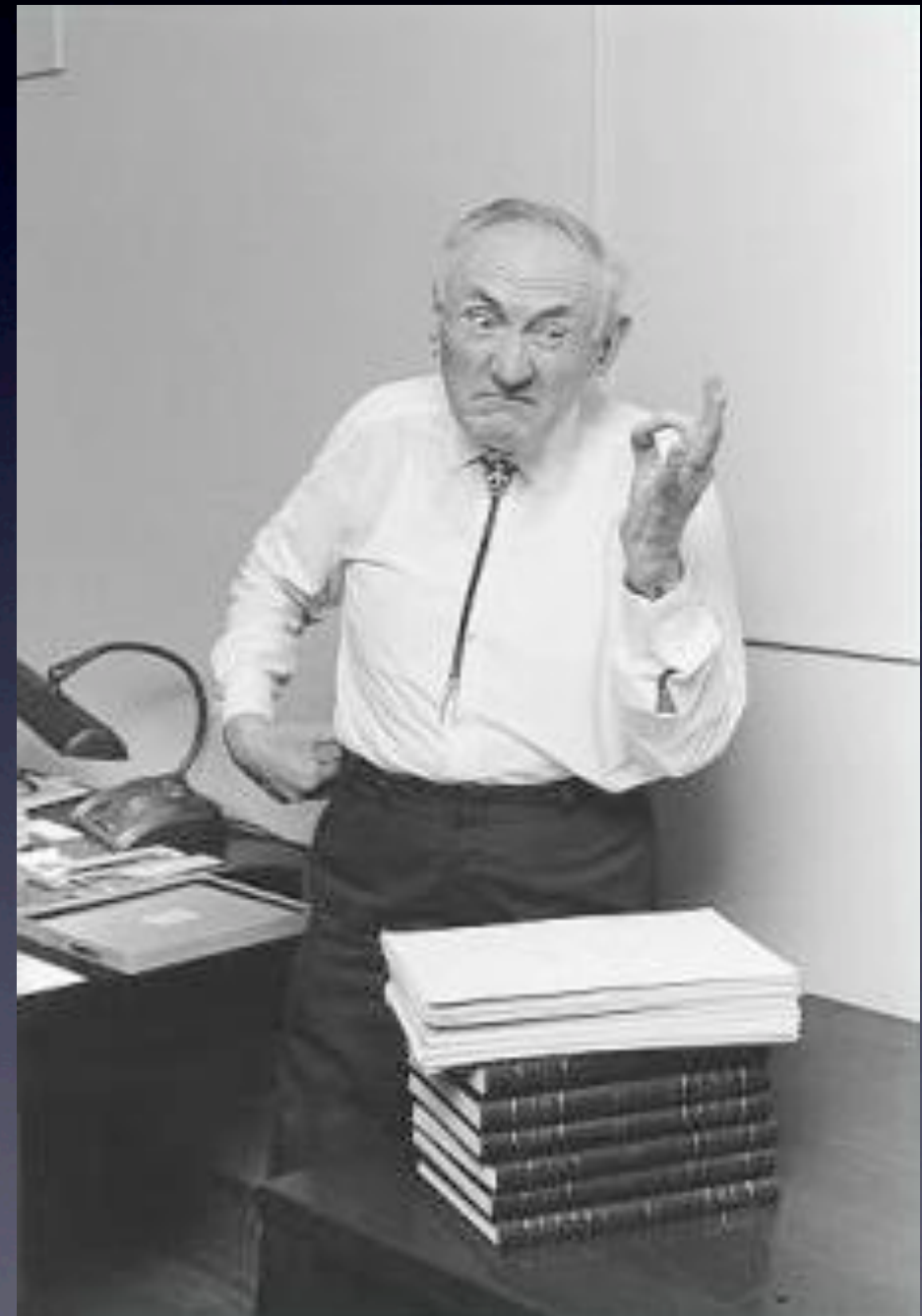


Coma cluster



# motion of galaxies

- galaxies are moving in the mutual gravitational potential
- assume virialized motion  $\langle v^2 \rangle = G_N M/r$
- but they are too fast, too
- first proposal of “dark matter”



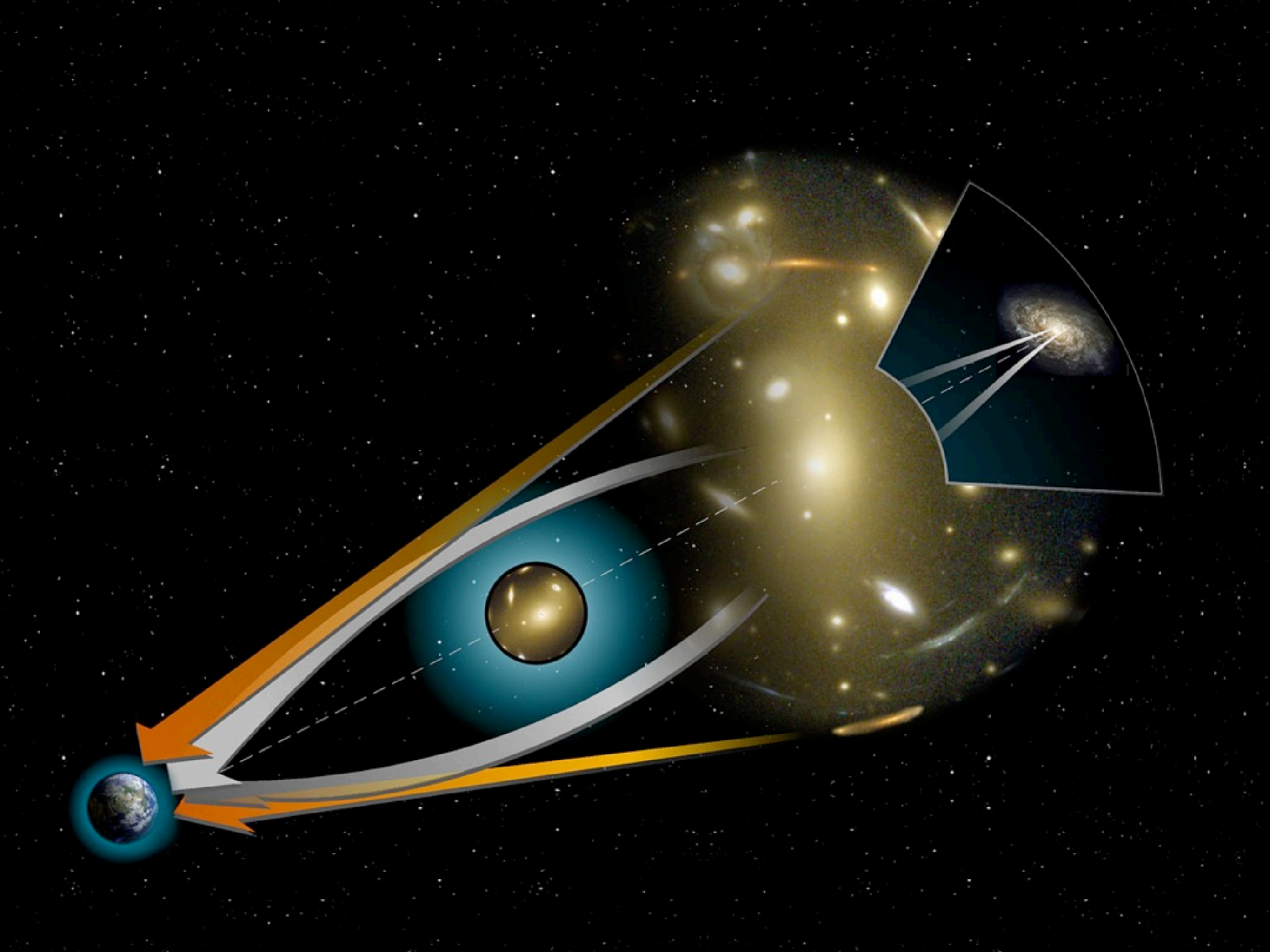
Fred Zwicky



# gravitational lensing

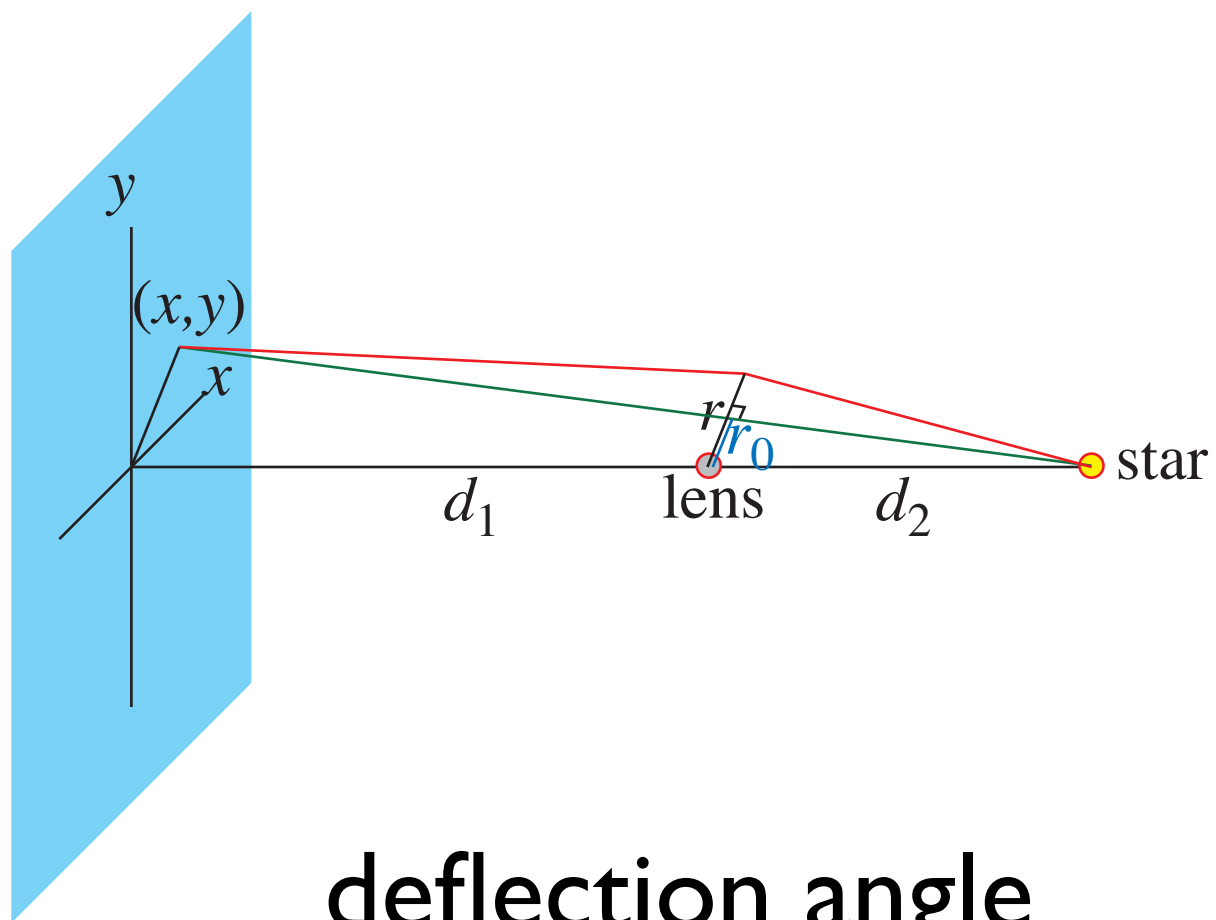






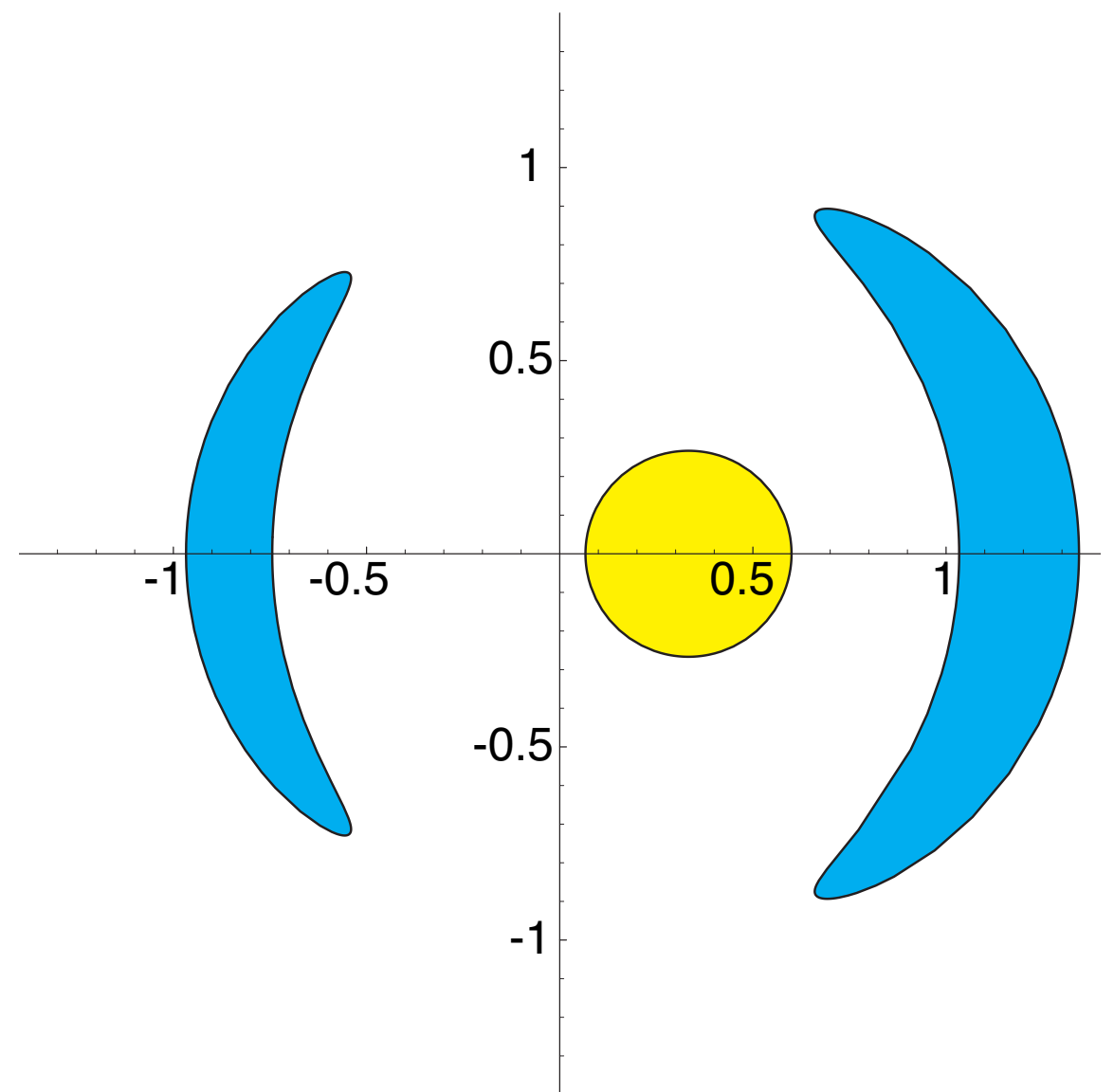


# gravitational lensing



deflection angle

$$\theta = 2 \frac{r_S}{r} = 4 \frac{G_N M}{c^2 r}$$





# gravitational lensing

$$ds^2 = \left(1 - \frac{r_S}{r}\right) c^2 dt^2 - \frac{dr^2}{1 - r_S/r} - r^2 d\theta^2 - r^2 \sin^2 \theta d\phi^2$$

$$g^{\mu\nu} \partial_\mu S \partial_\nu S = mc^2 = 0$$

$$S(t, r, \theta) = Et - L\theta + W(E, r, L)$$

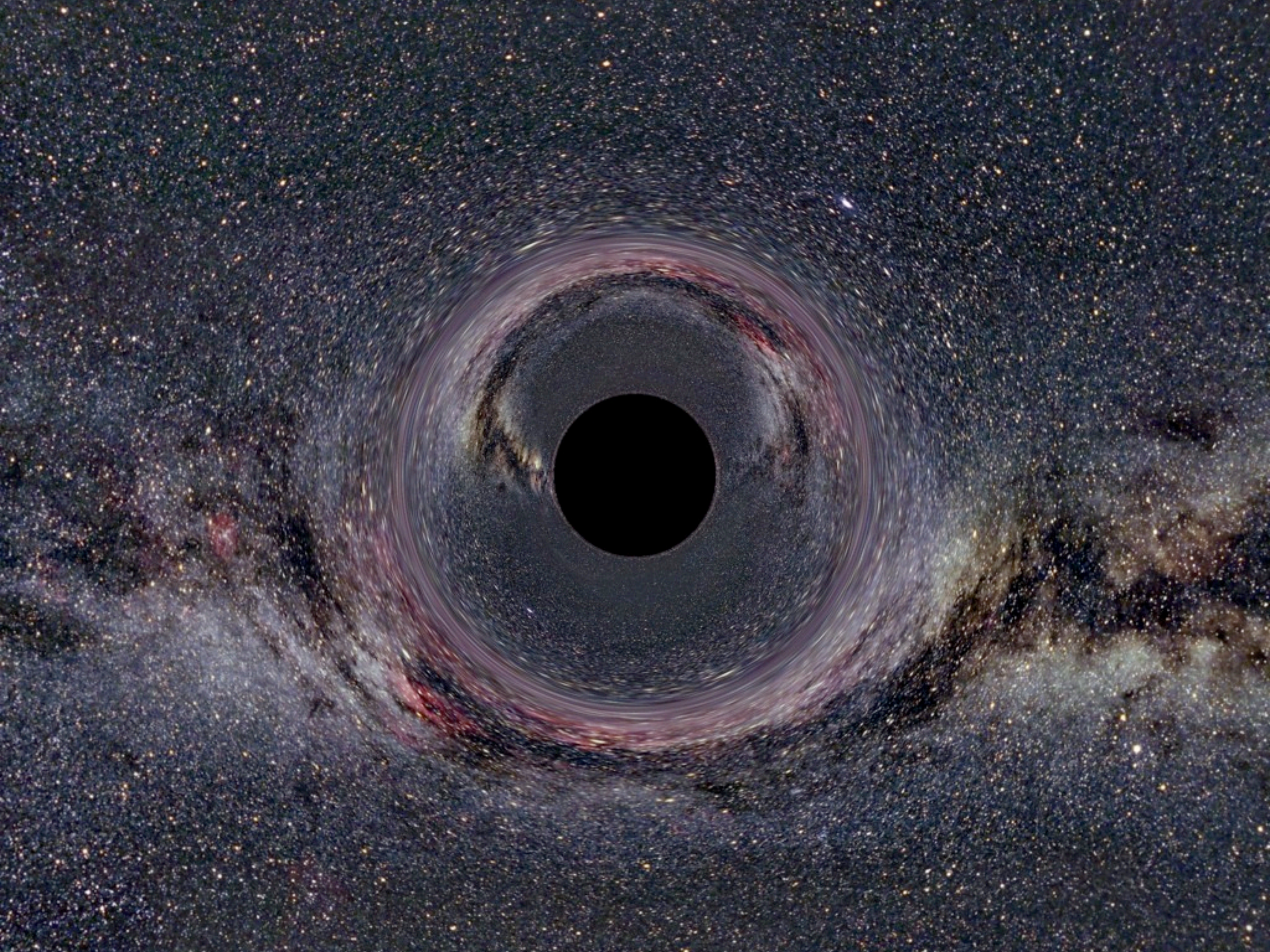
$$(\partial_r W)^2 = \left(1 - \frac{r_S}{r}\right)^{-2} \frac{E^2}{c^2} - \left(1 - \frac{r_S}{r}\right)^{-1} \frac{L^2}{r^2}$$

The closest approach  $r_c$  is where  $\partial_r W = 0$

$$E^2 = c^2 \left(1 - \frac{r_S}{r_c}\right) \frac{L^2}{r_c^2}$$

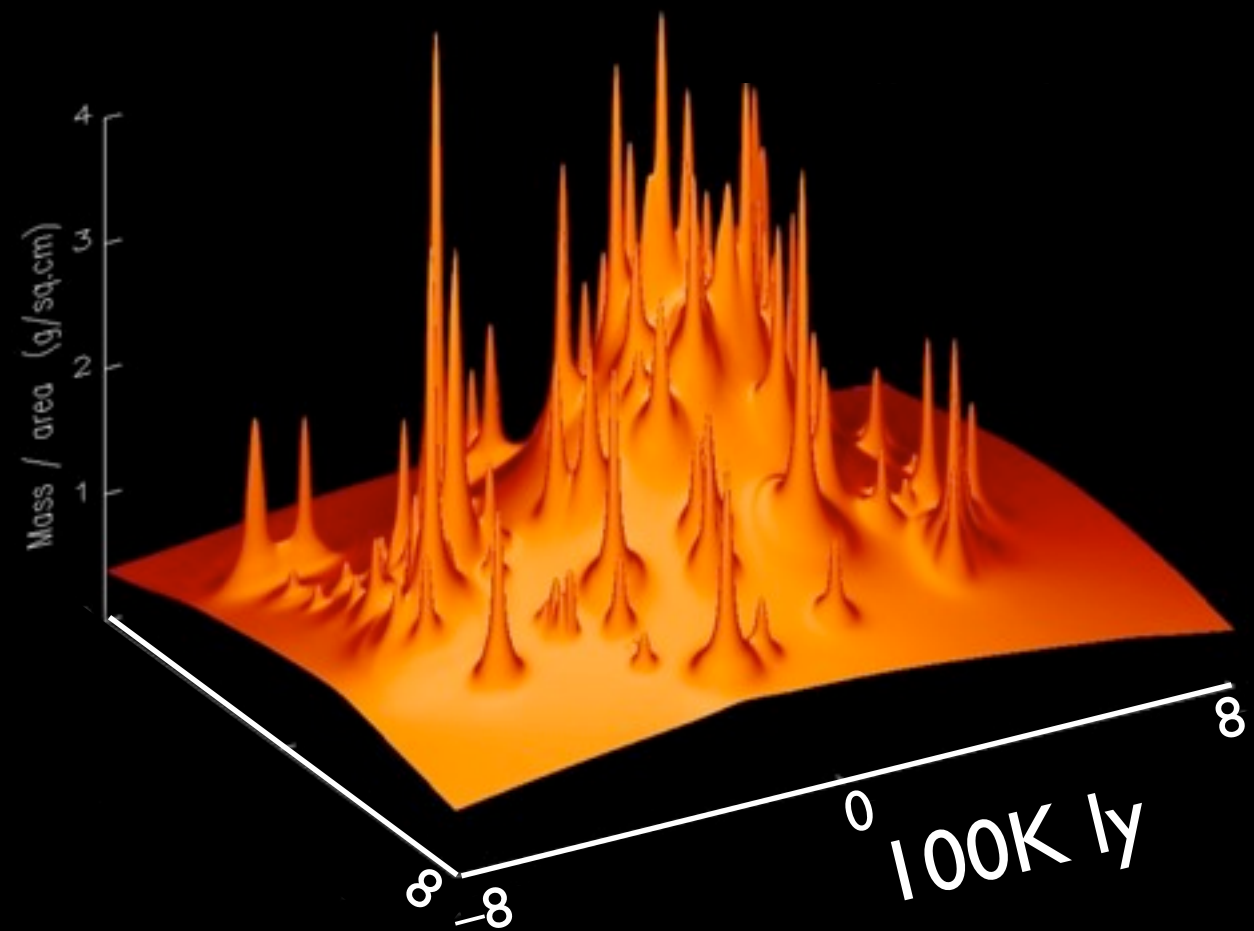
$$\pi + \Delta\theta = \partial_L W = 2 \int_{r_c}^{\infty} \frac{dr}{r \sqrt{\left(1 - \frac{r_S}{r_c}\right) \frac{r^2}{r_c^2} - \left(1 - \frac{r_S}{r}\right)}} = \pi + \frac{2r_S}{r_c} + O(r_S^2)$$



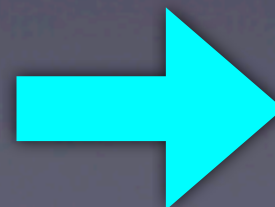




# Clusters of galaxies



distortion in **images** of BG galaxies



2D map of dark matter



“see” invisible dark matter



Subaru telescope



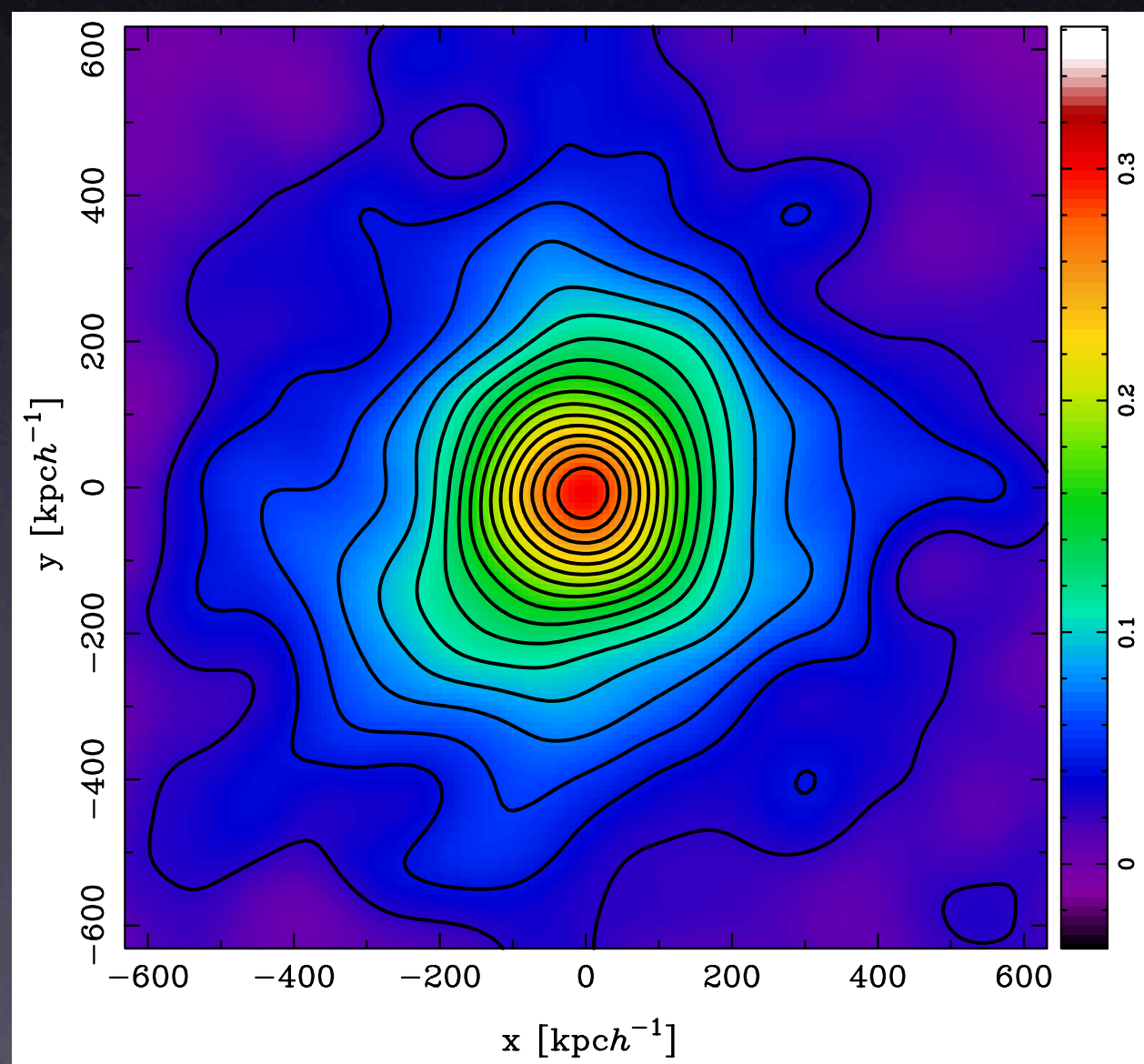
more than 80% of matter is not atoms!



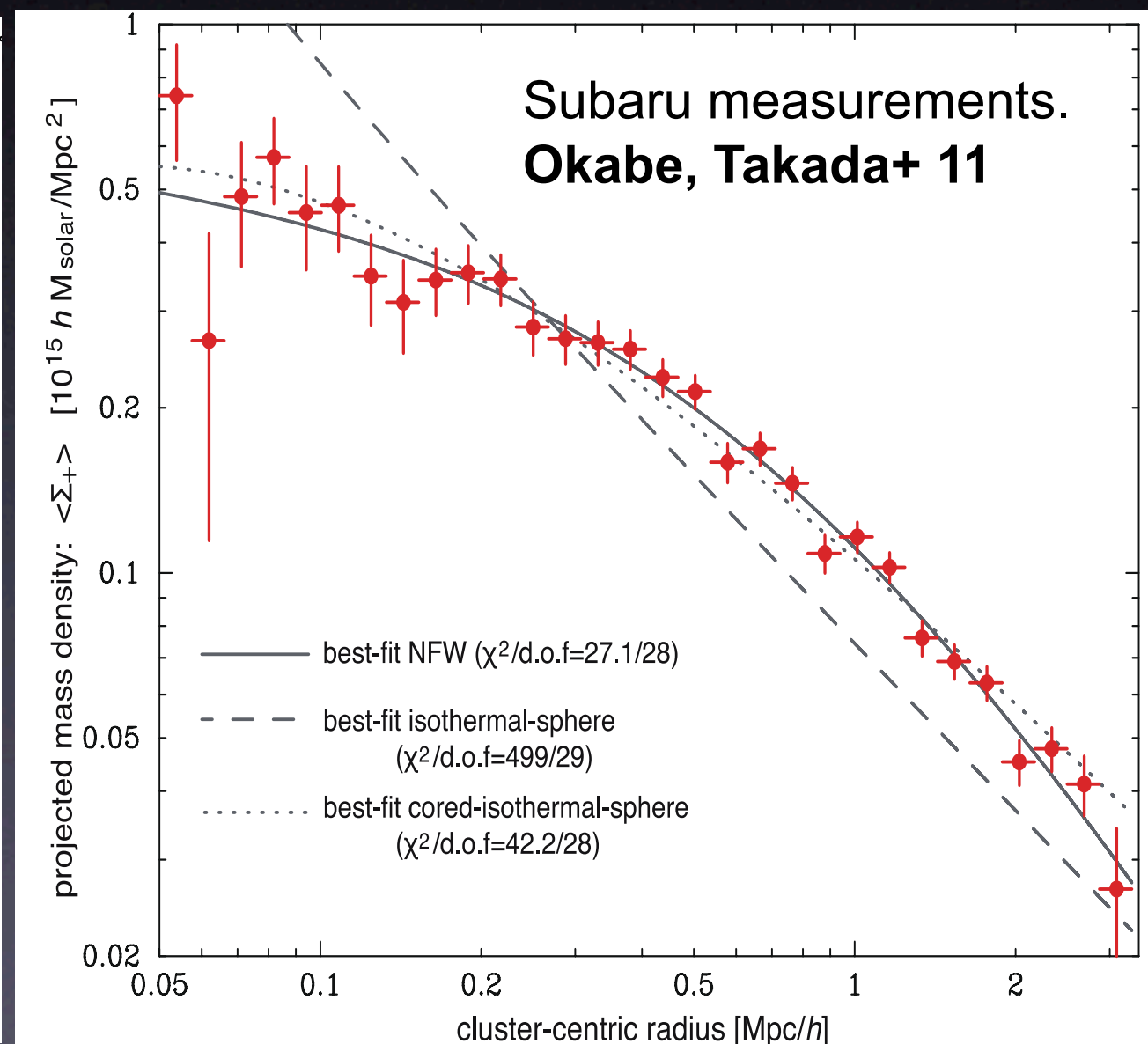




# as expected by theory



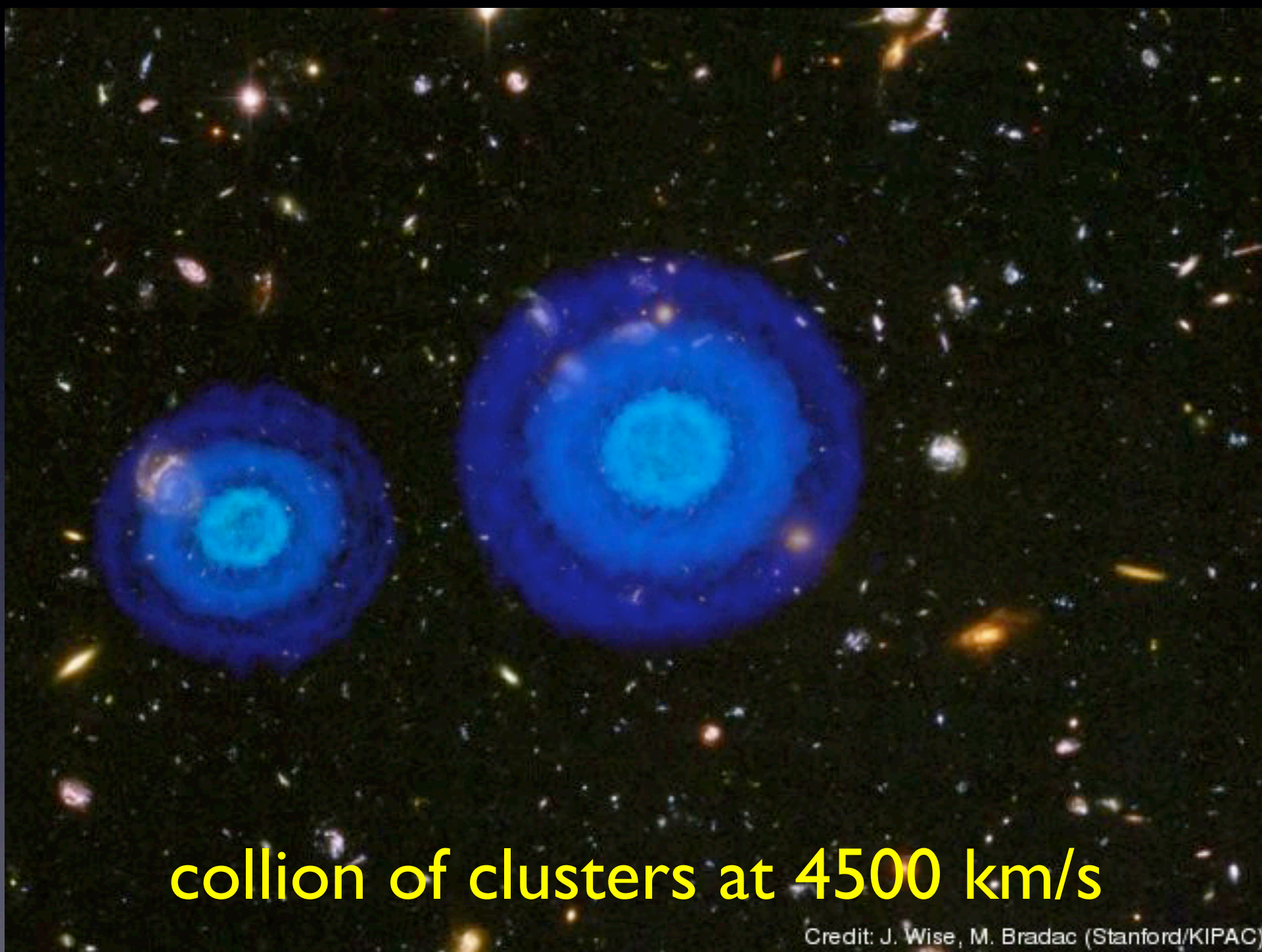
45 clusters stacked



consistent with NFW profile



# lucky we are not here



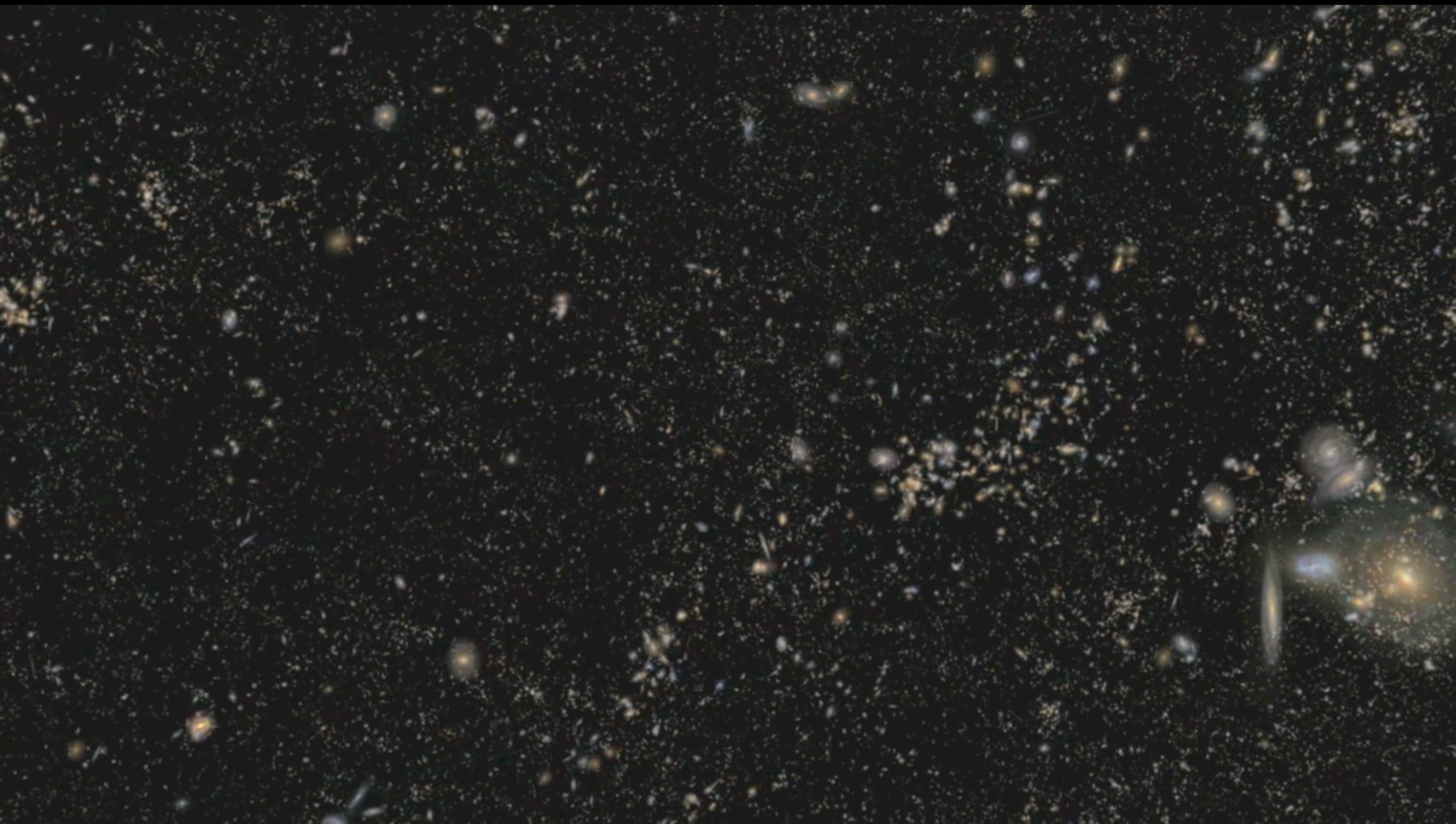
4 billion lyr away



# Dark Matter

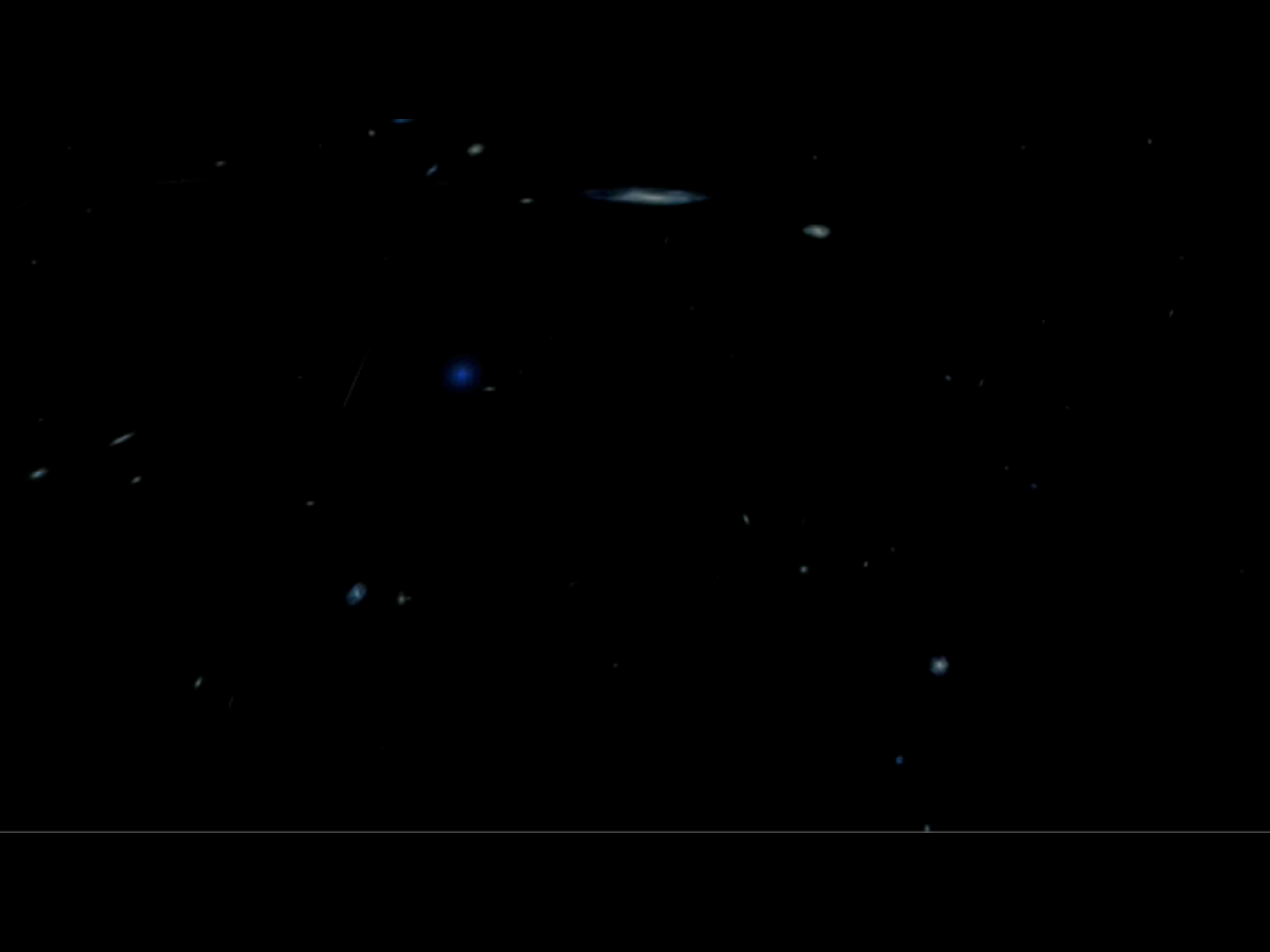






fly-through based on SDSS-III data







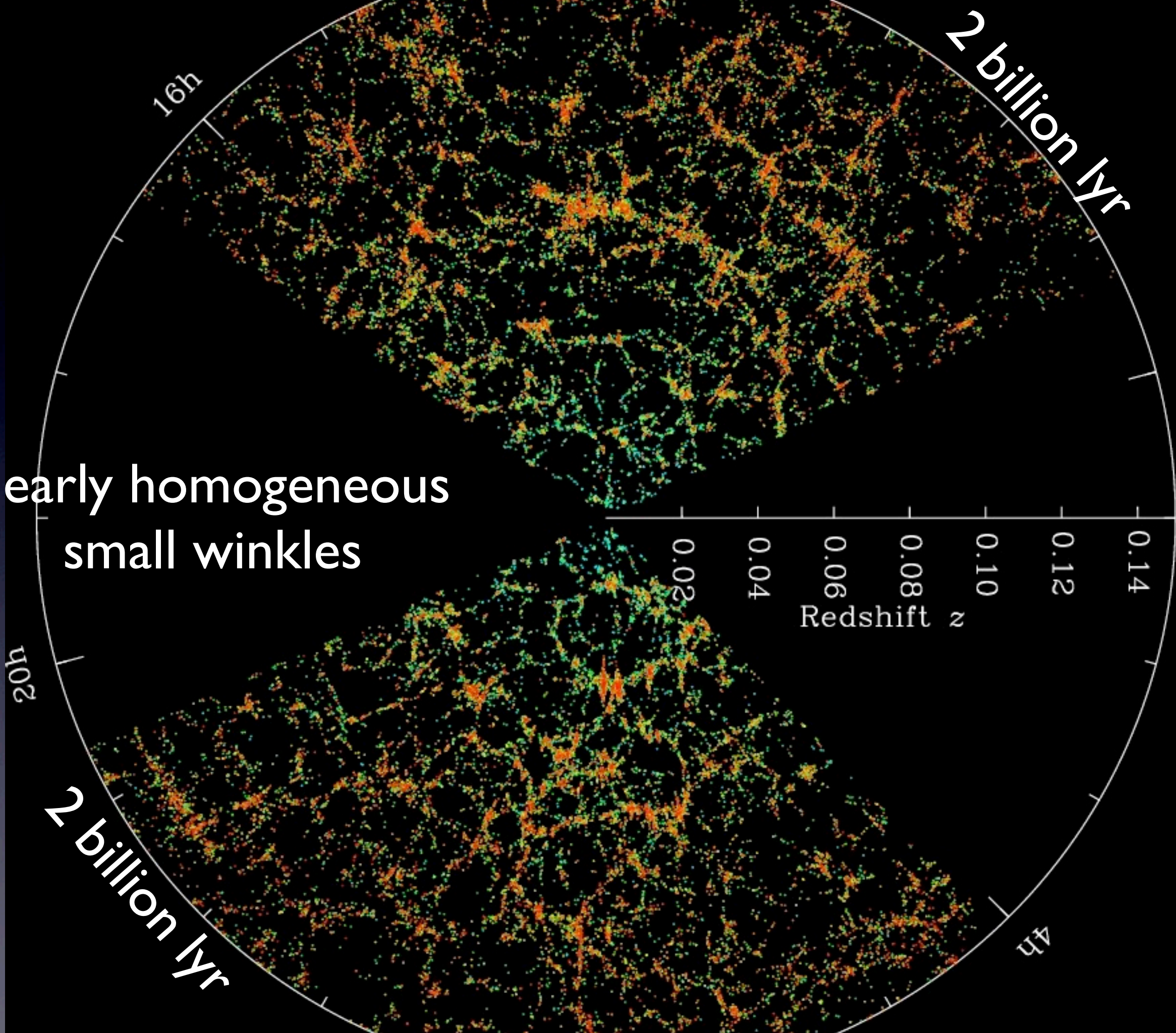
20 billion yr

2 billion yr

2 billion yr

Redshift  $z$

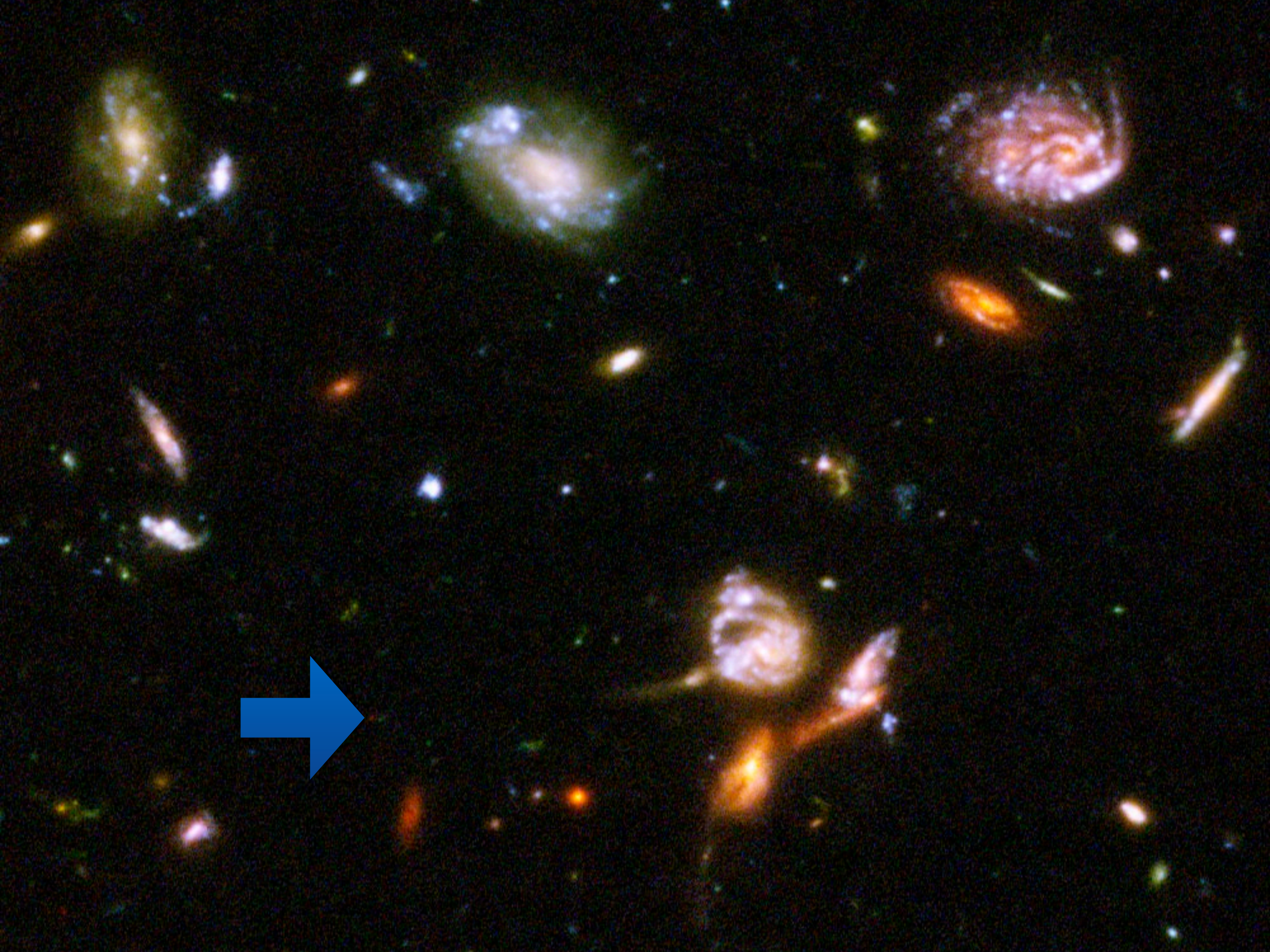
nearly homogeneous  
small winkles



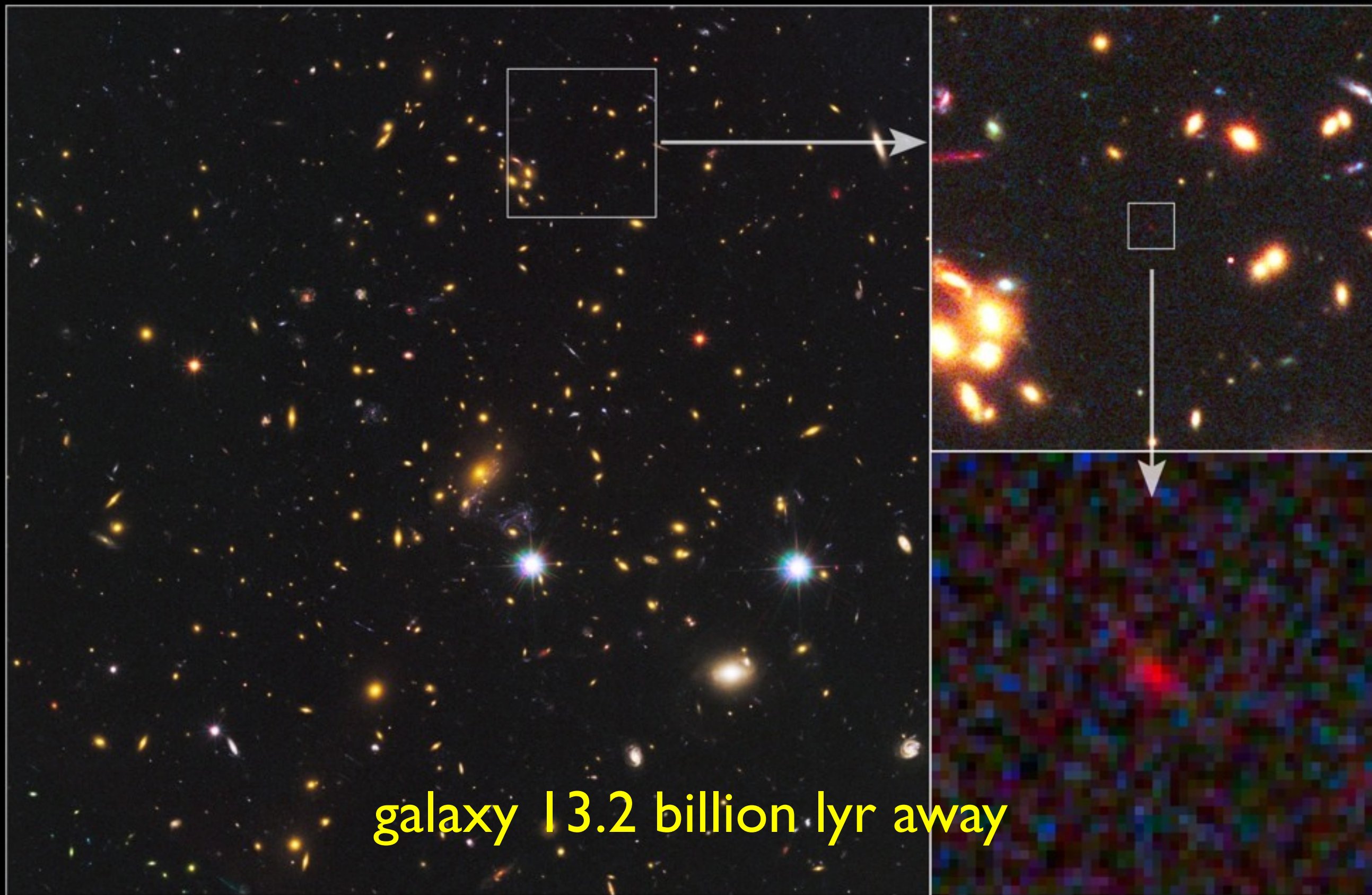












galaxy 13.2 billion lyr away

Galaxy Cluster MACS J1149+2223

High-Redshift Galaxy MACS1149-JD

A Distant Gravitationally-Lensed Galaxy at Redshift = 9.6

Hubble Space Telescope • ACS • WFC3

NASA / ESA / STScI / J. Hora (Harvard-Smithsonian CfA)

ssc2012-12a







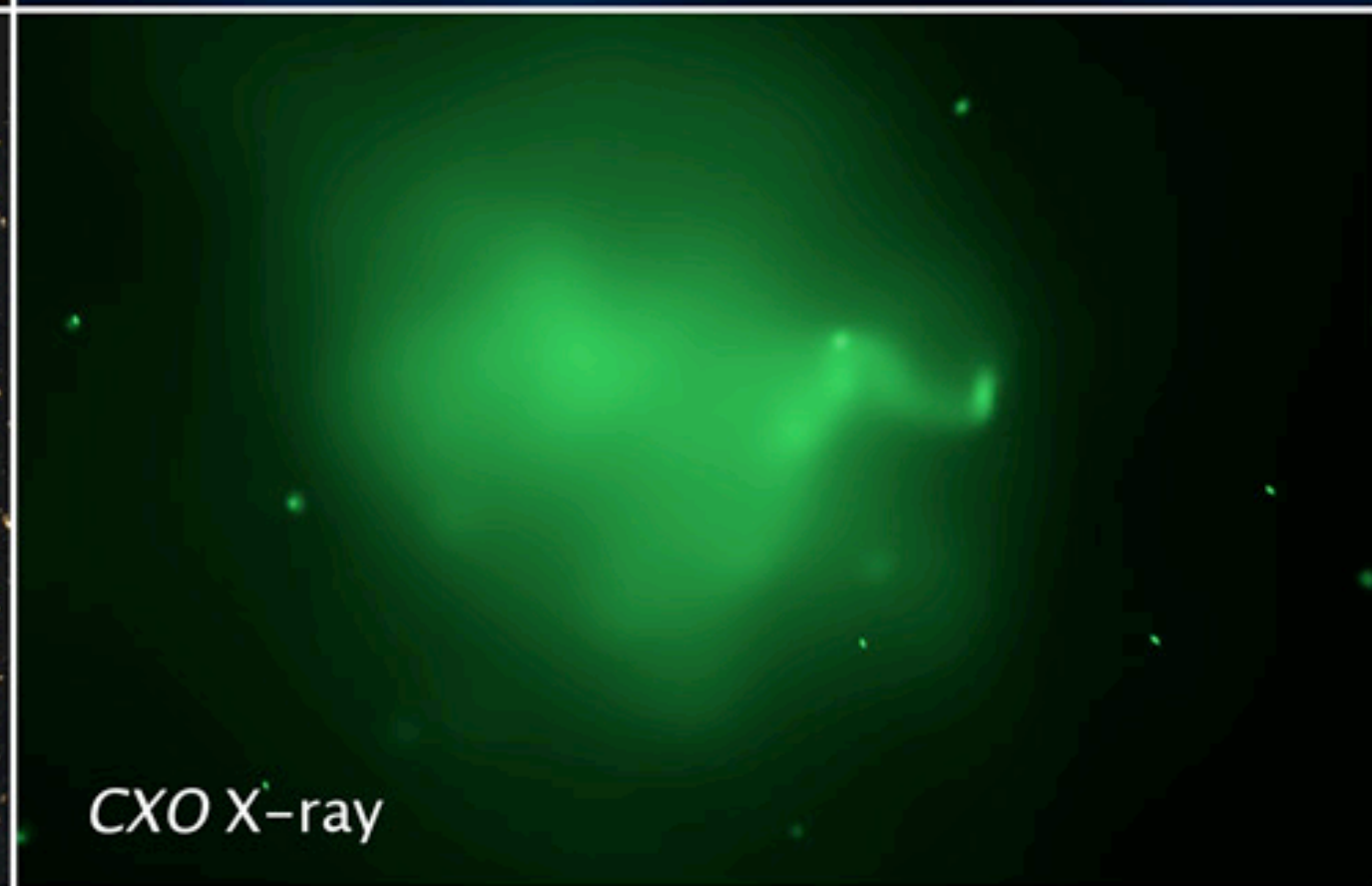
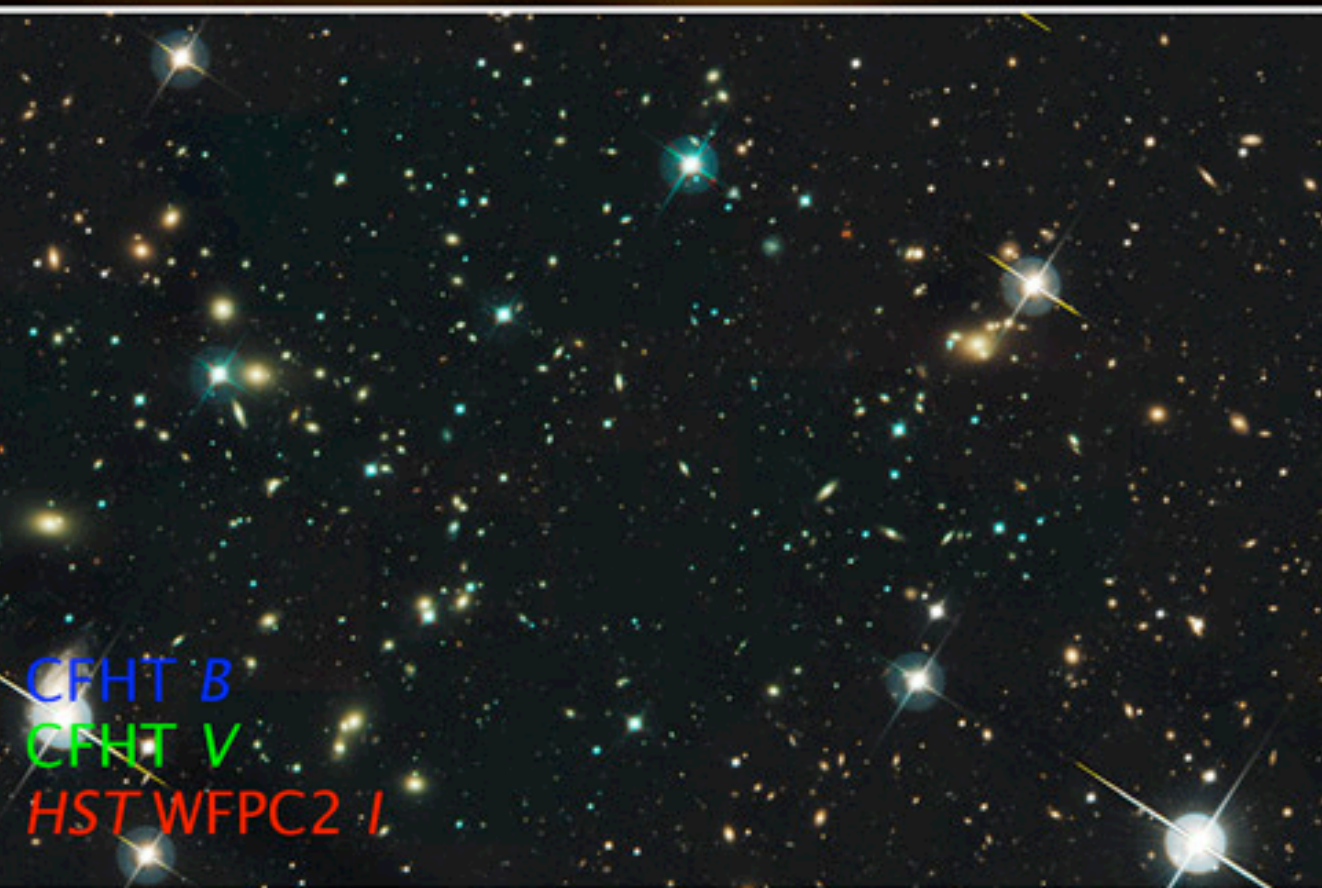
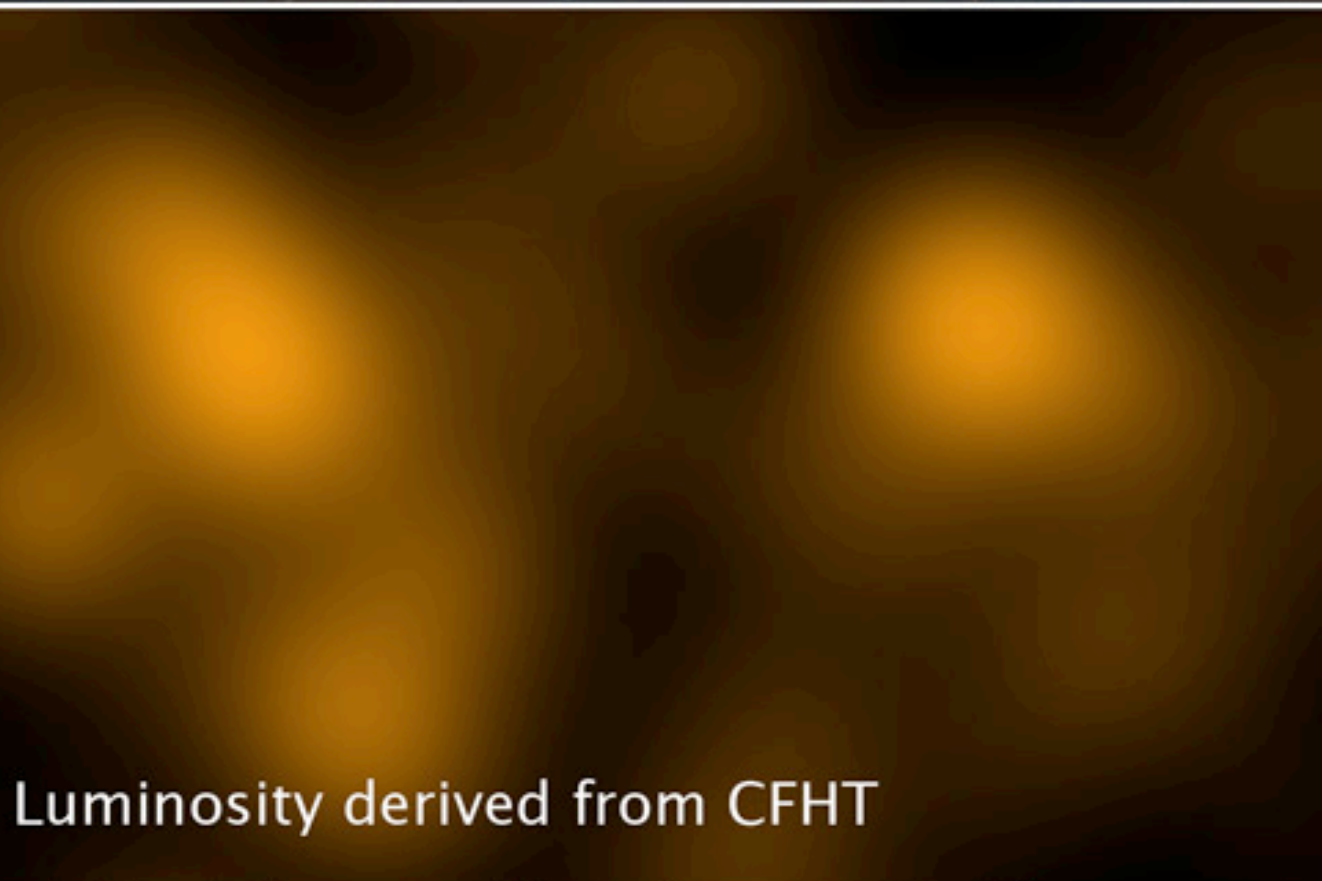
# Train Wreck Cluster

Abell 520





# Train Wreck Cluster







# Friedmann Universe



# Expanding space

- Hubble law:  $v = H_0 d$
- $\lambda = \lambda_0(1+z)$
- $z$ : redshift =  $R_0/R$
- adiabatic expansion  $\Rightarrow$

$$T \propto R^{-1}$$

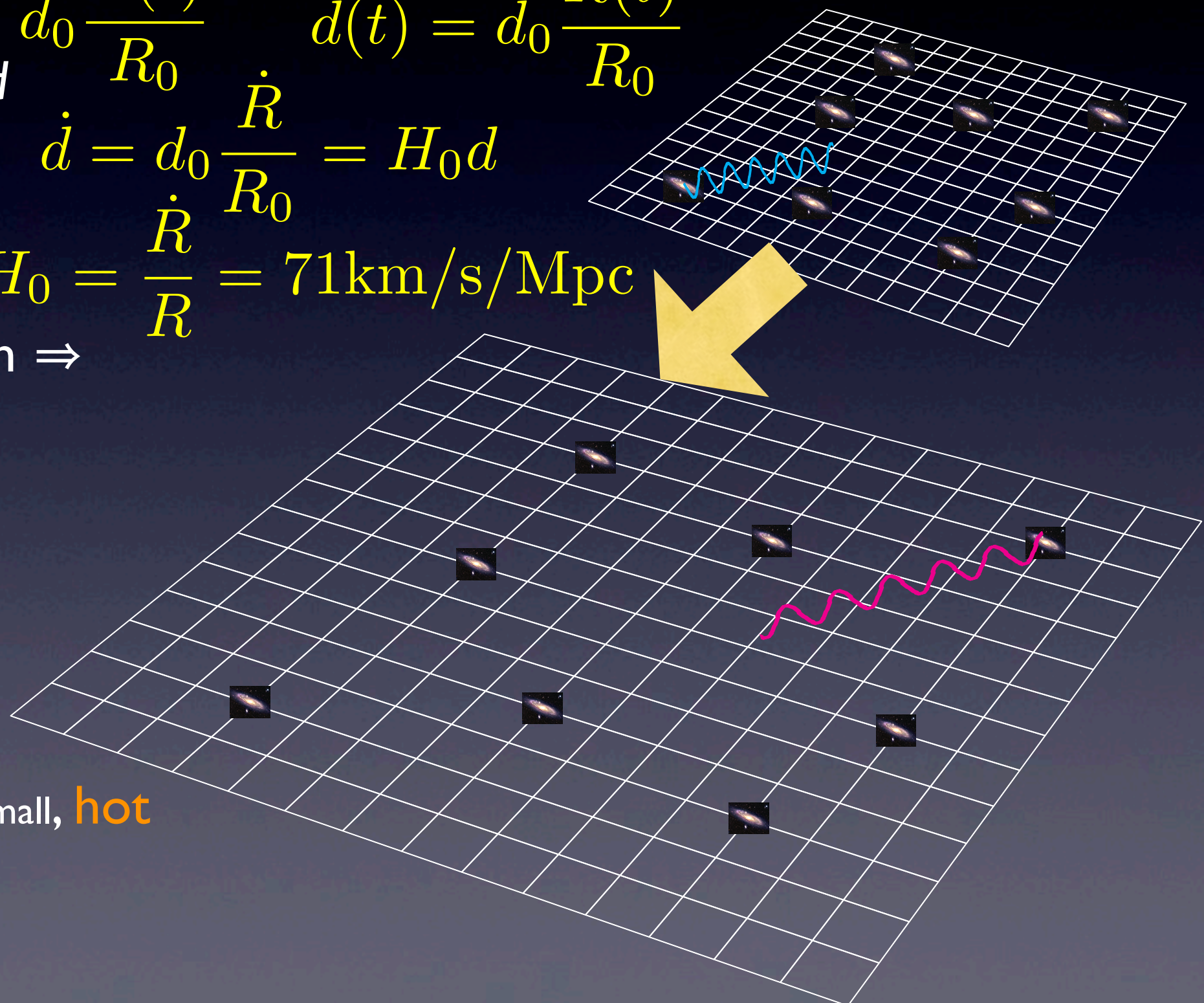
- $T = T_0(1+z)$
- bigger and colder
- Universe started small, hot

Big Bang!

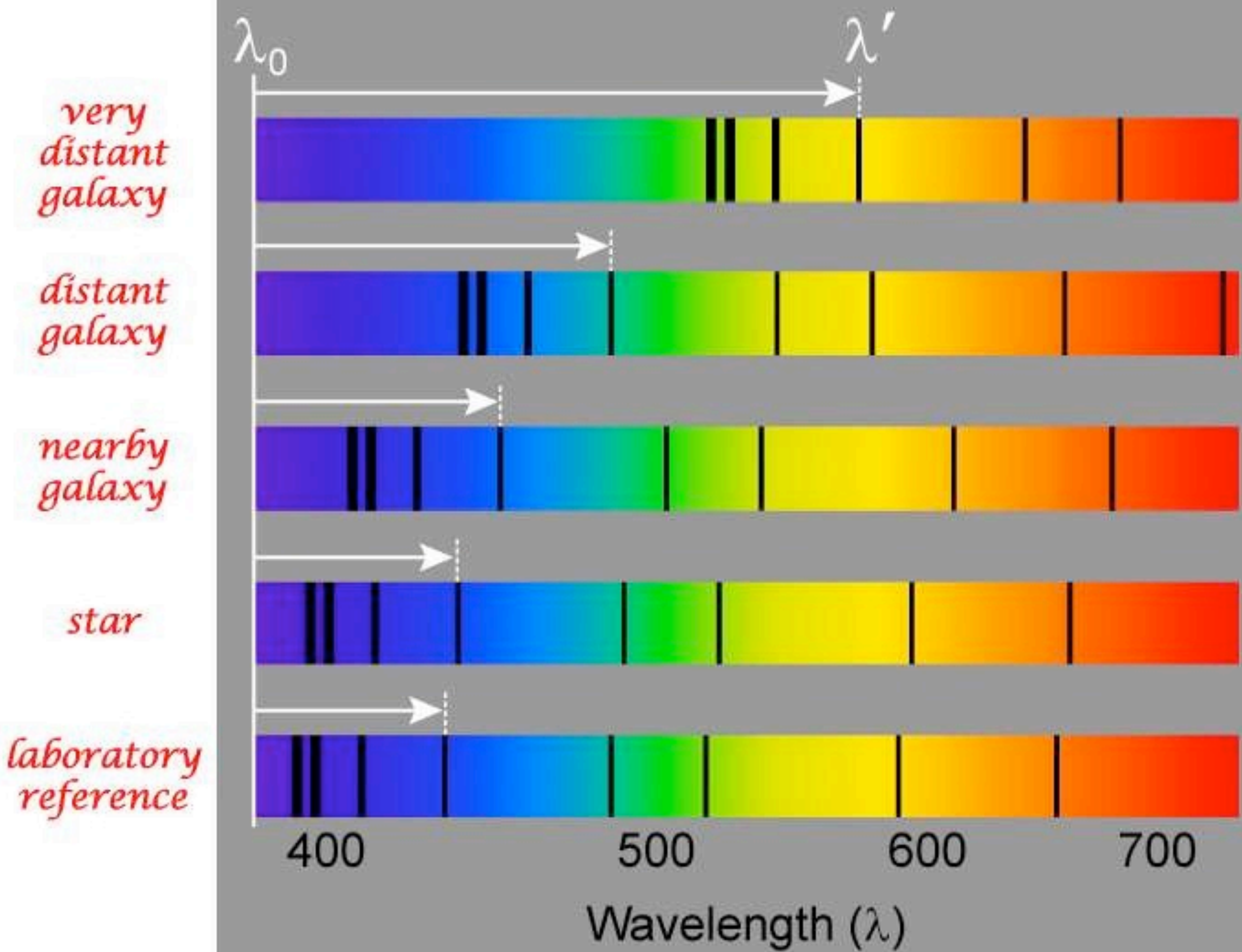
$$d = d_0 \frac{R(t)}{R_0} \quad \dot{d}(t) = d_0 \frac{\dot{R}(t)}{R_0}$$

$$\dot{d} = d_0 \frac{\dot{R}}{R_0} = H_0 d$$

$$H_0 = \frac{\dot{R}}{R} = 71 \text{ km/s/Mpc}$$









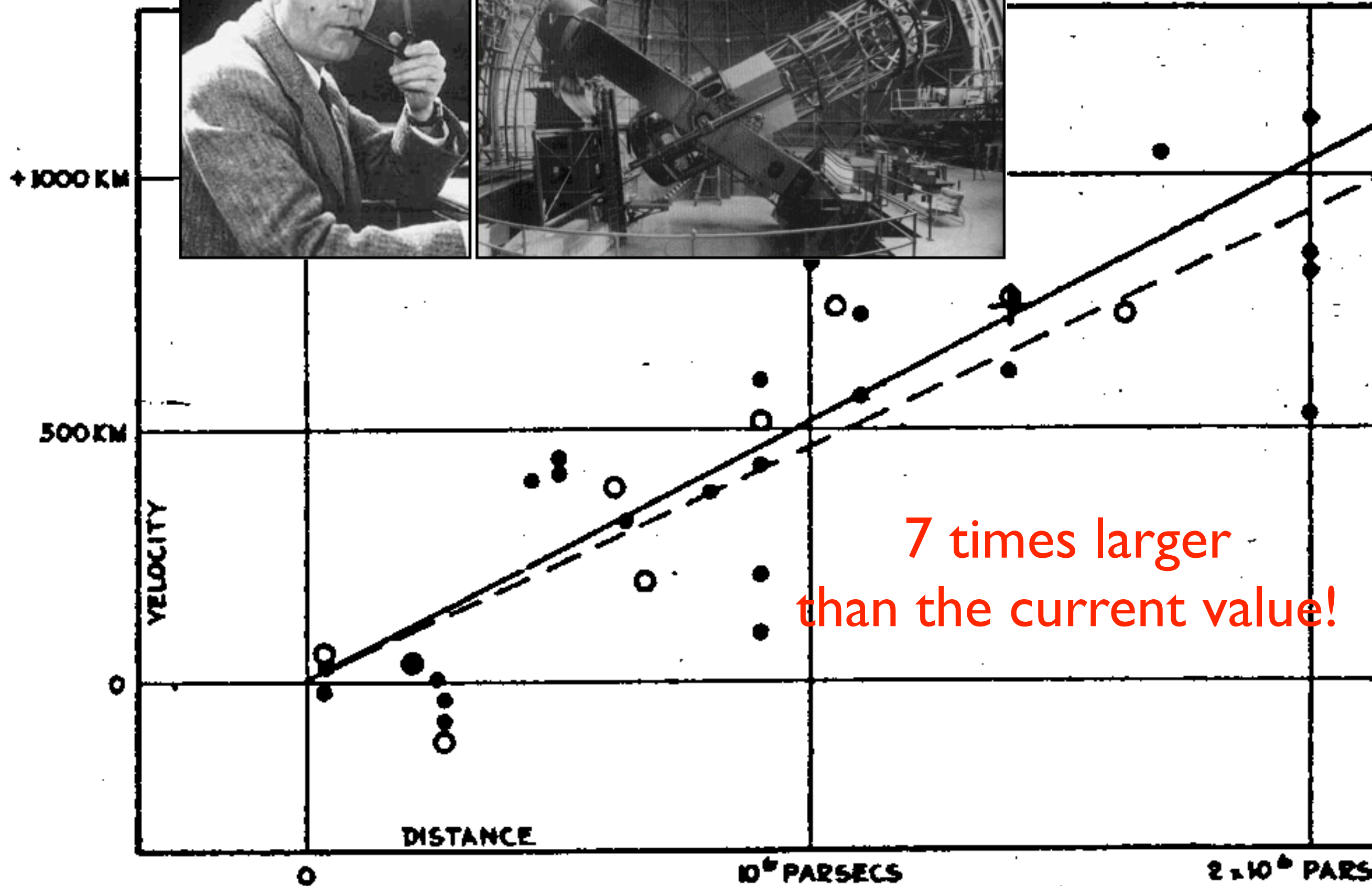
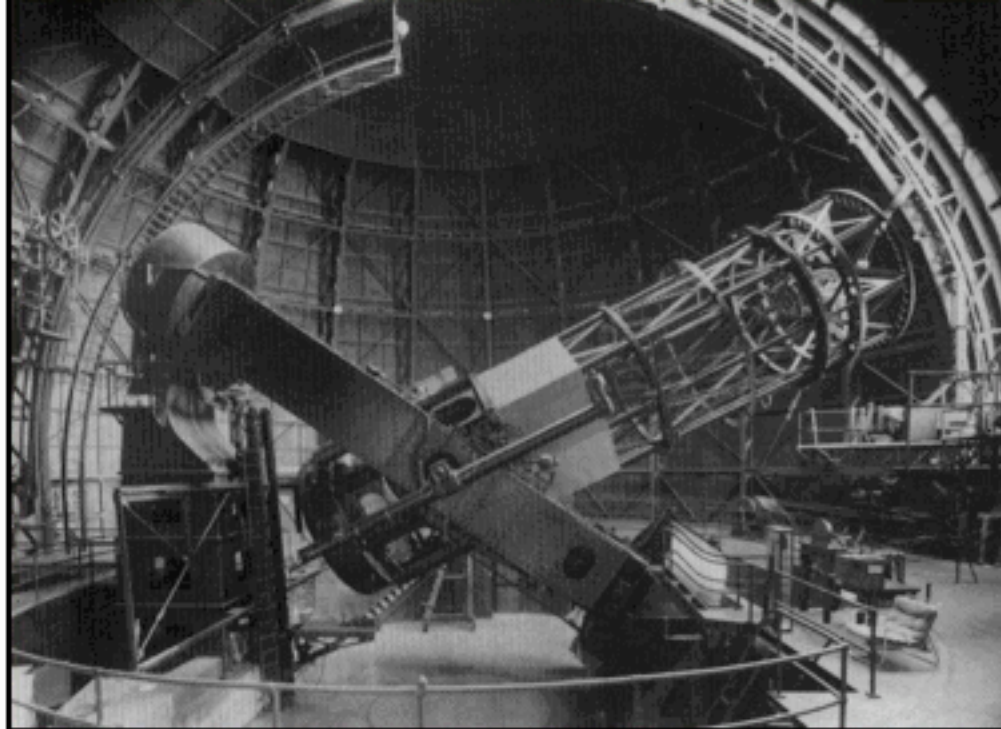
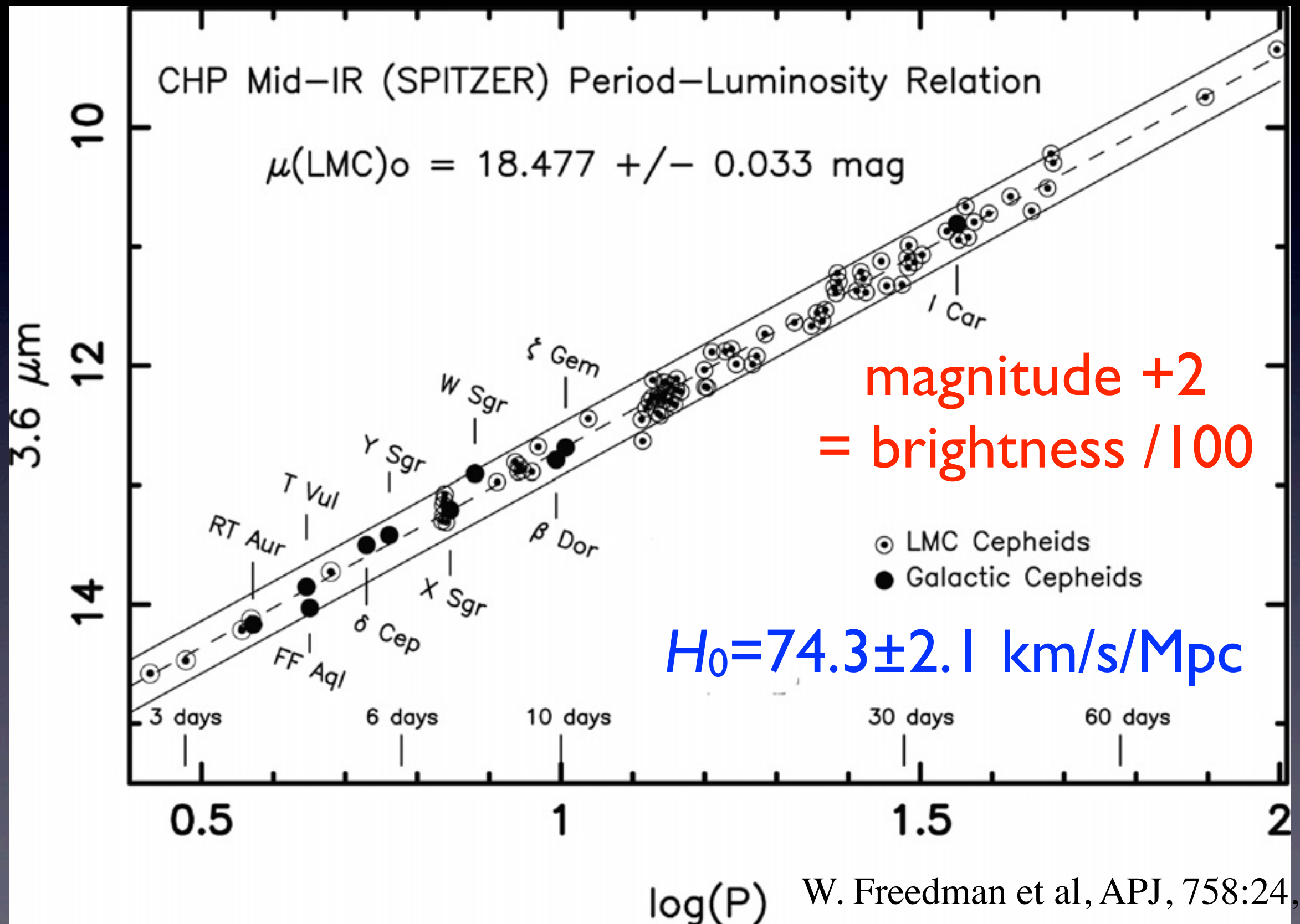


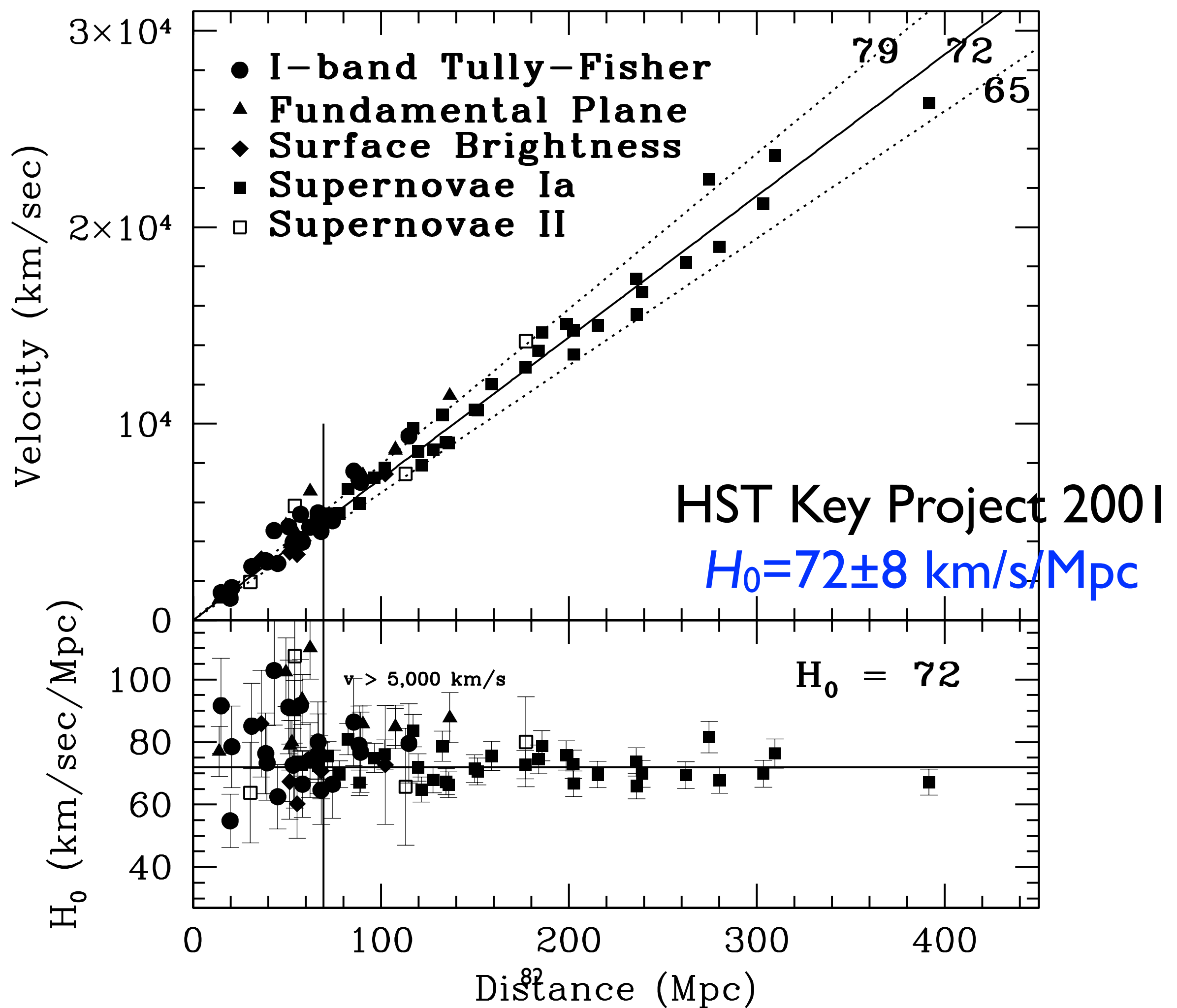
FIGURE 1



# Cepheids calibration



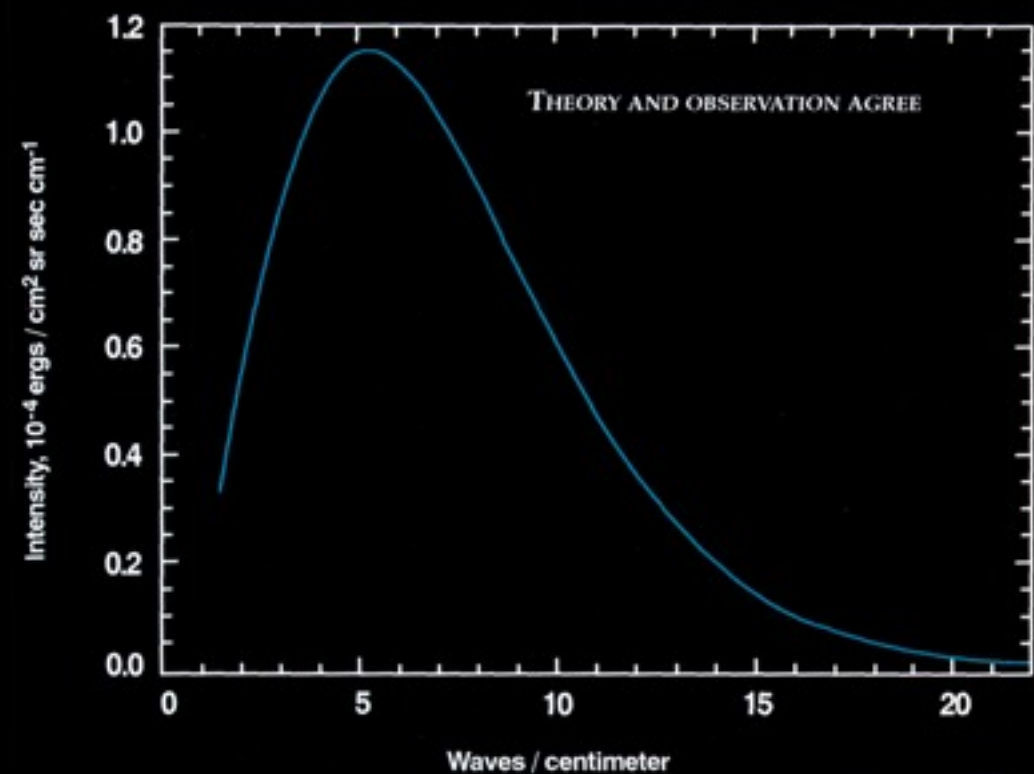
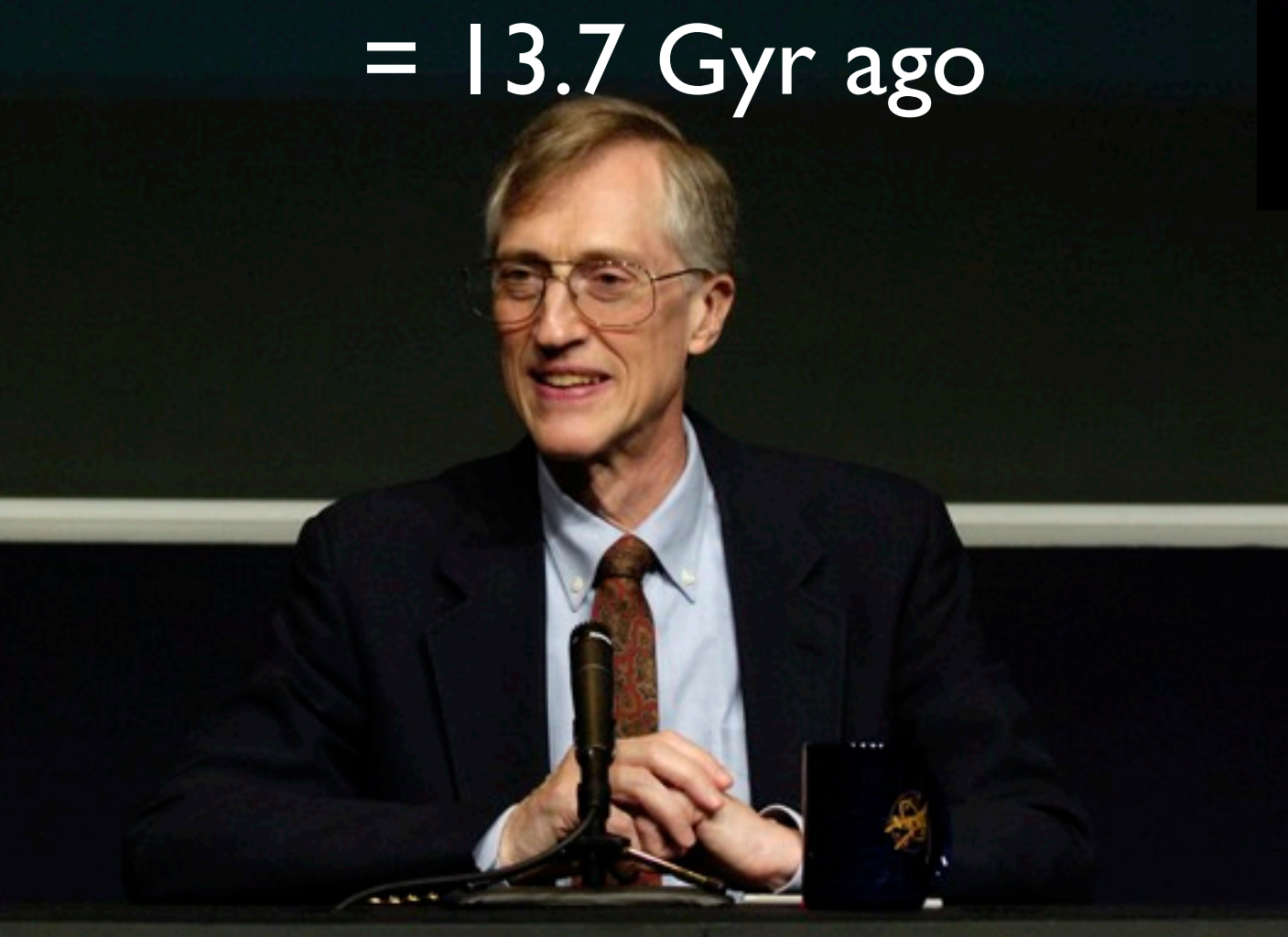






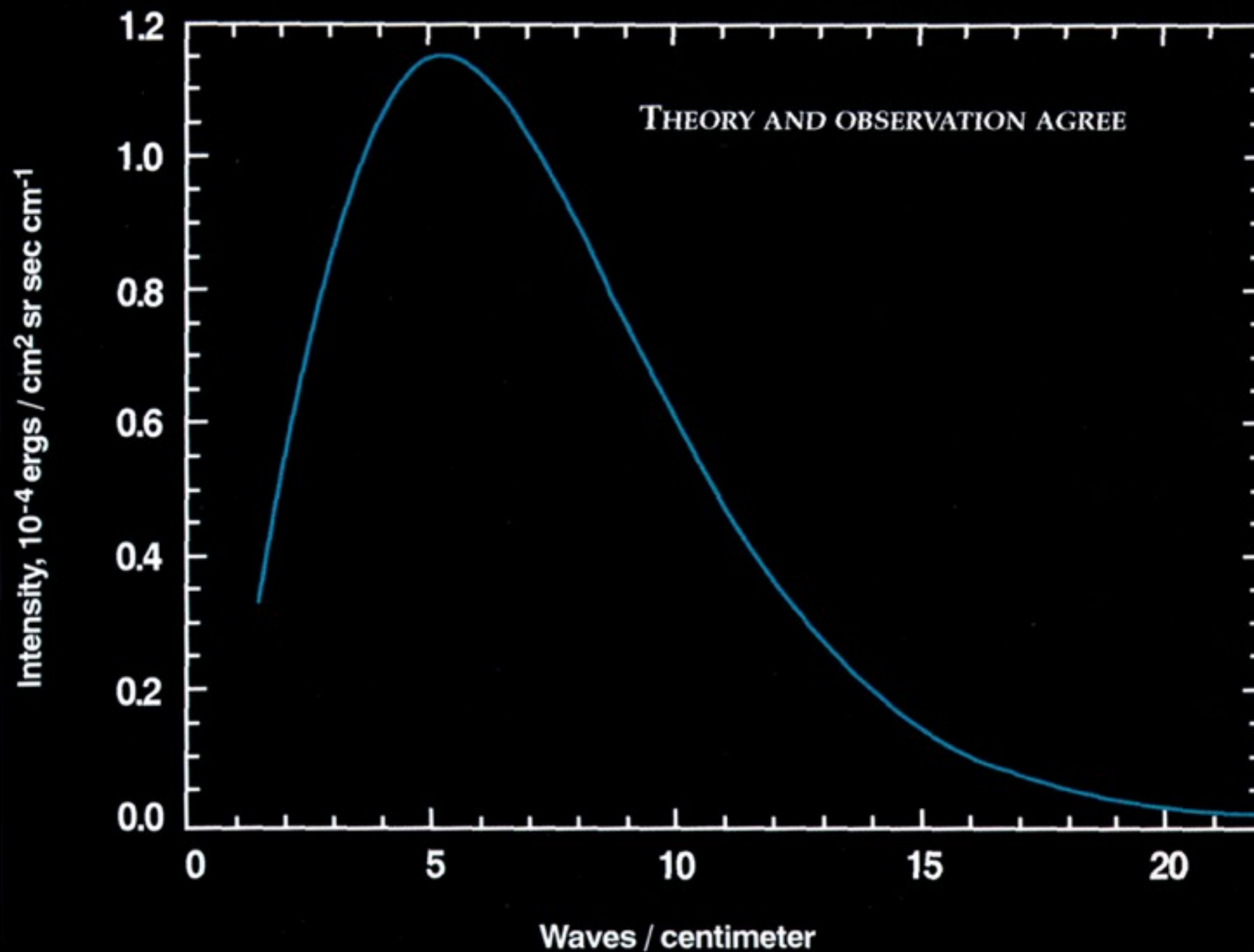


13.7 G lyr away  
= 13.7 Gyr ago





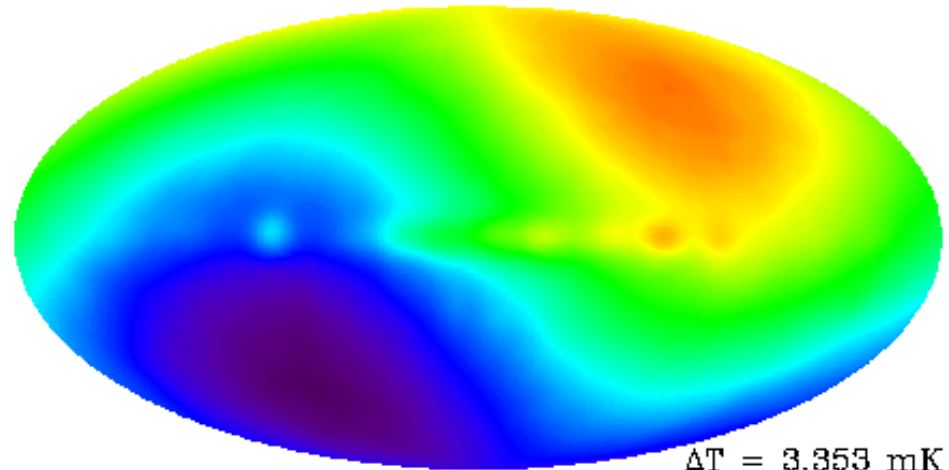
## COSMIC MICROWAVE BACKGROUND SPECTRUM FROM COBE



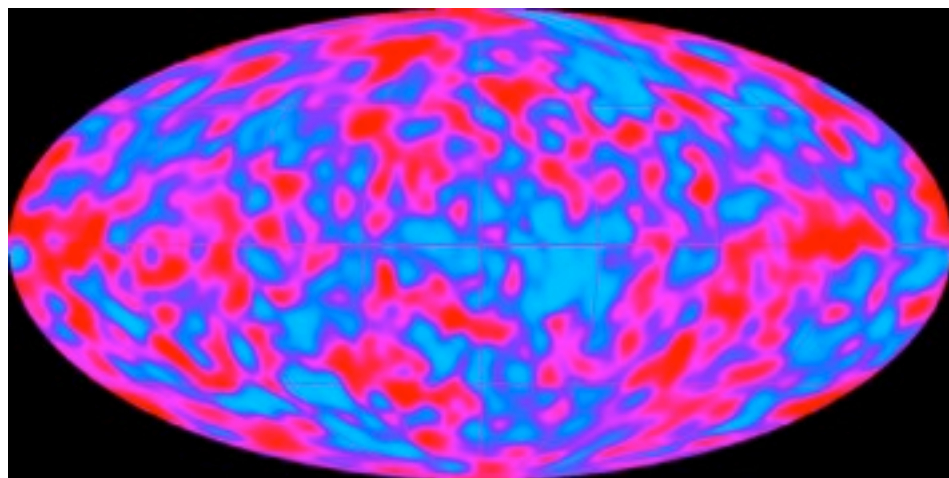




$T = 2.728 \text{ K}$



$\Delta T = 3.353 \text{ mK}$



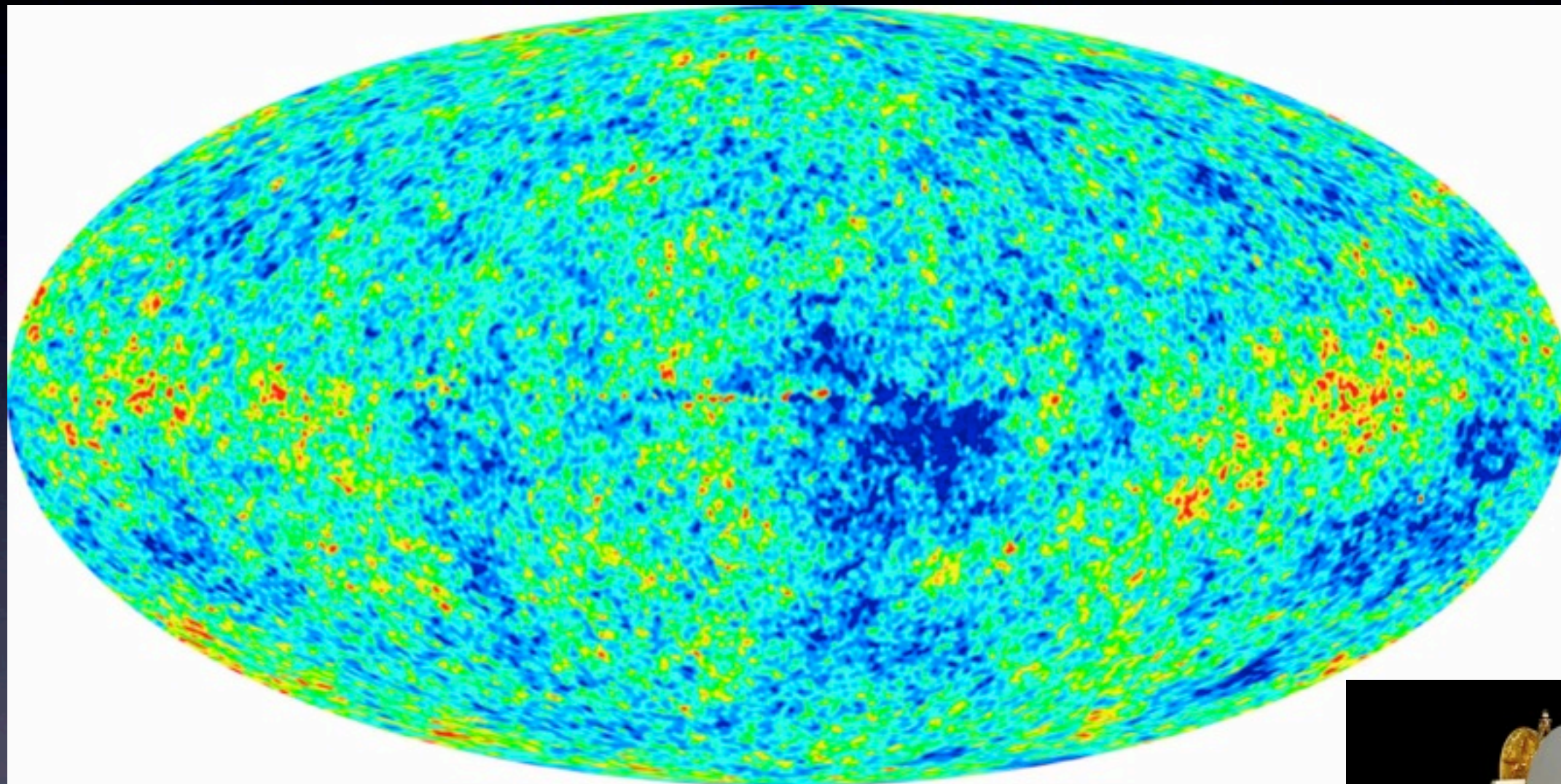
CMB temperature

CMB dipole  
we are moving at  
 $\sim 1\%$  of  $c$  relative to CMB

CMB anisotropy  
at  $\sim 10^{-5}$   
1mm ripple on 100m sea



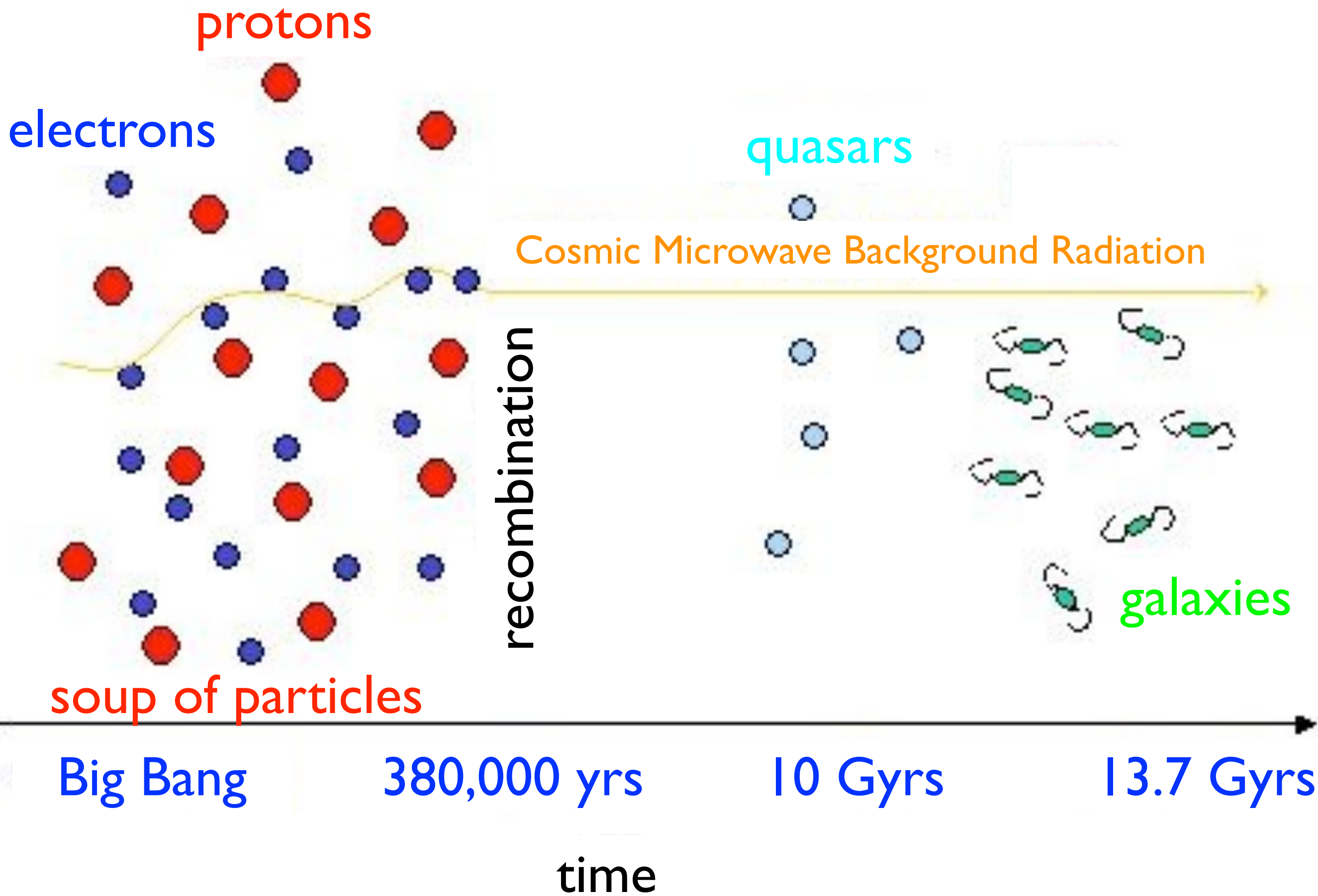
# *wall @ 13.7Glyr away*



You can never see beyond this wall  
using light

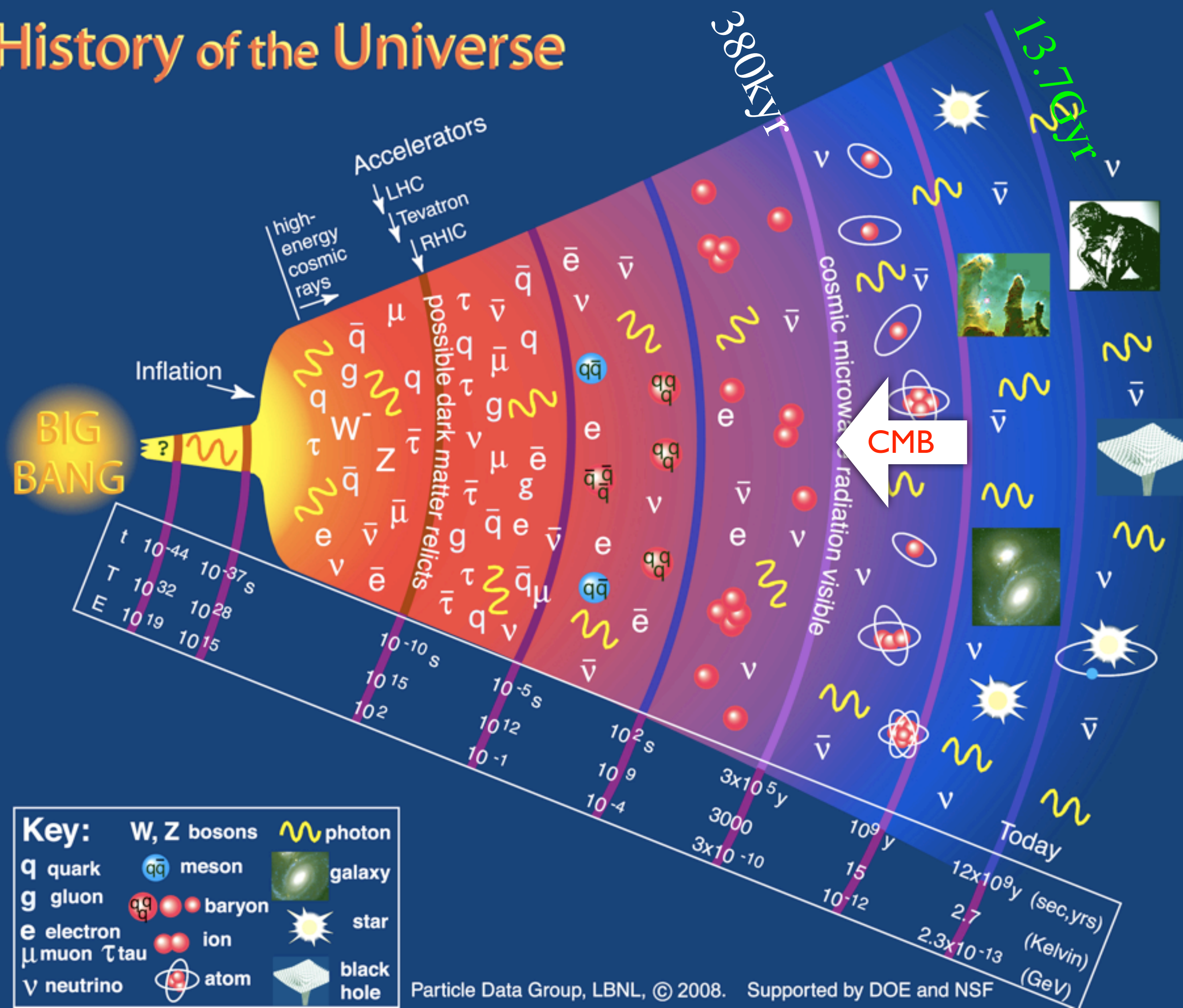








# History of the Universe







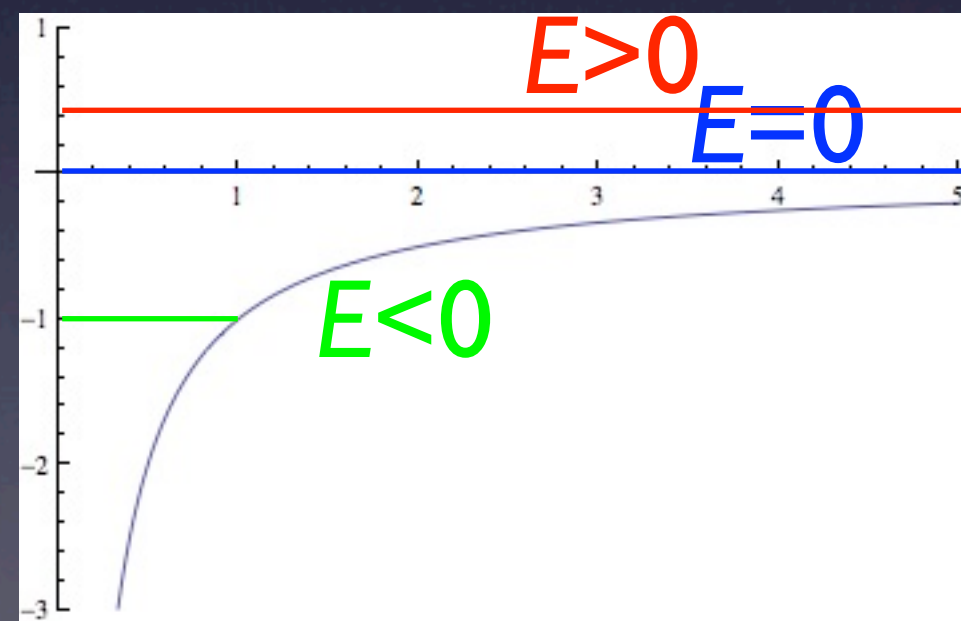
same as  
this ball

# Friedmann Equation

- “non-relativistic derivation”
- assume spherical distribution of mass density  $\rho$
- same as full relativistic equation with a curvature term  $k=-1, 0, 1$

$$E = \frac{m}{2} \dot{R}^2 - G_N \left( \frac{4\pi}{3} \rho R^3 \right) \frac{m}{R}$$

$$\left( \frac{\dot{R}}{R} \right)^2 = \frac{8\pi}{3} G_N \rho - \frac{k}{R^2}$$



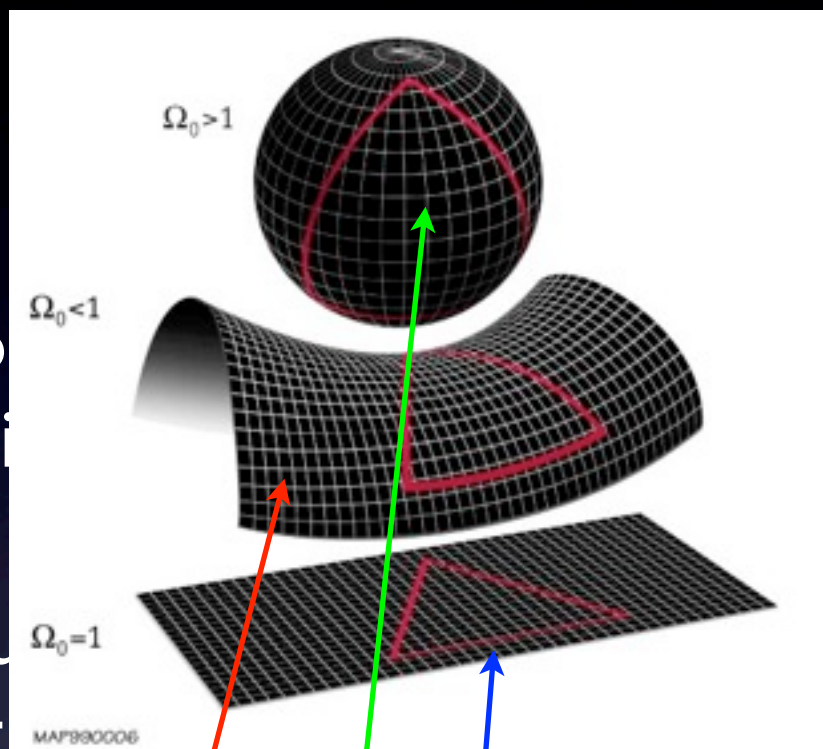
$$\frac{4\pi}{3} \rho R^3 = M$$





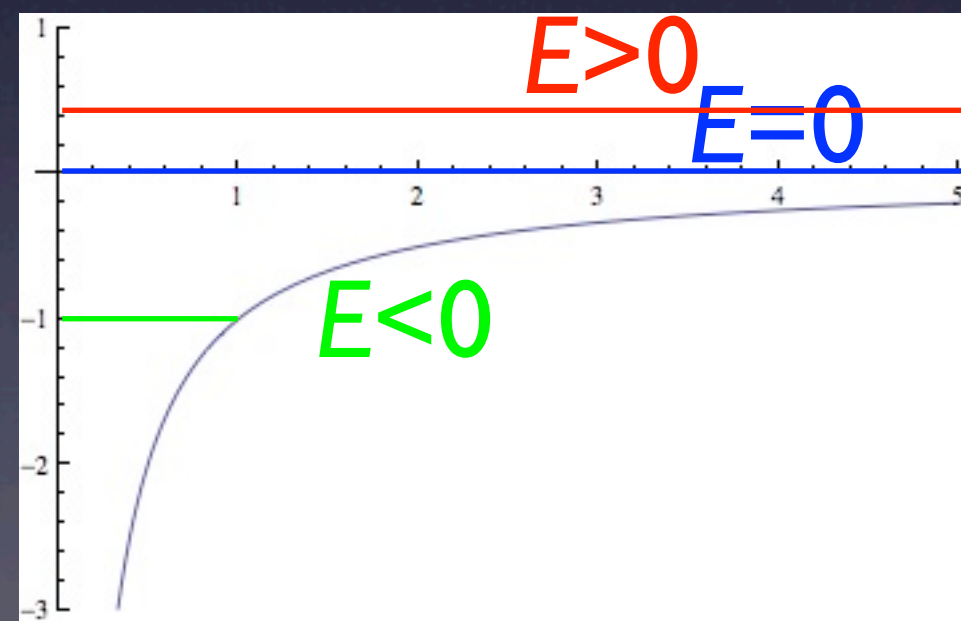
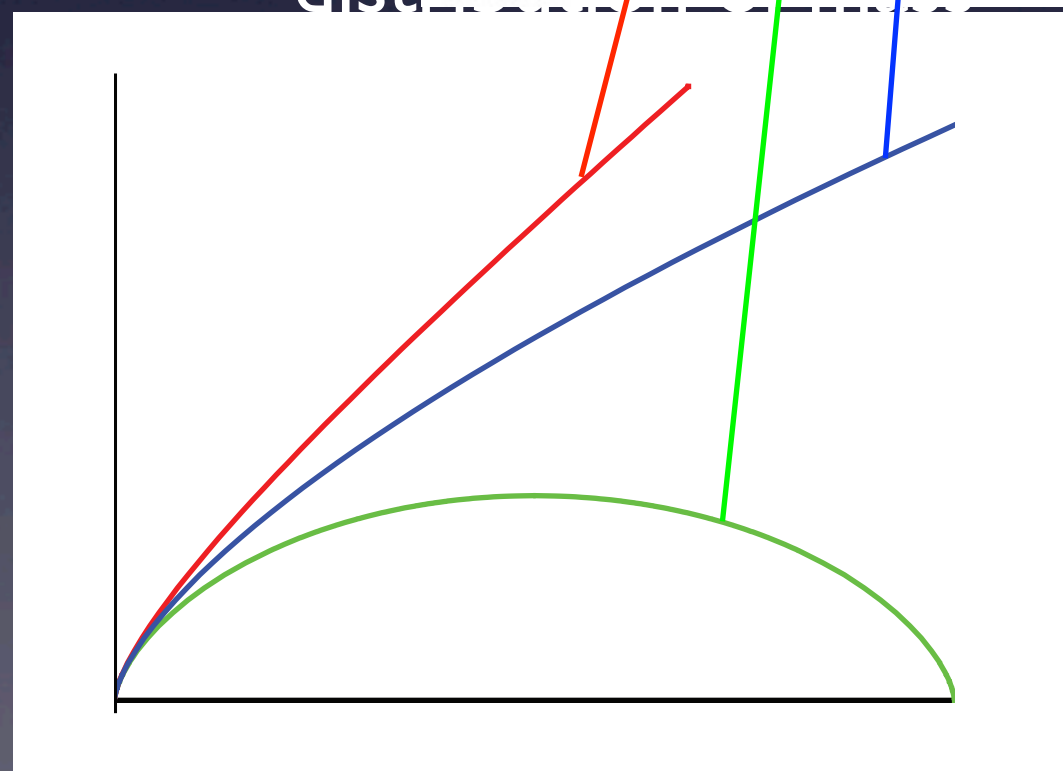
# Friedmann Equation

- “no  
deri
- assu  
dist



$$E = \frac{m}{2} \dot{R}^2 - G_N \left( \frac{4\pi}{3} \rho R^3 \right) \frac{m}{R}$$

$$\left( \frac{\dot{R}}{R} \right)^2 = \frac{8\pi}{3} G_N \rho - \frac{k}{R^2}$$



$$\frac{4\pi}{3} \rho R^3 = M$$



# Current Universe

- knowing the l.h.s. tells us the current energy density
- l.h.s. =  $H_0^2$  from Hubble law  $v=H_0 d$
- r.h.s. defines the *critical density*  $\rho_c$

$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3}G_N\rho - \frac{k}{R^2}$$

$$H_0 = \frac{\dot{R}}{R} = 71\text{km/s/Mpc}$$

$$\rho_c = \frac{3}{8\pi}G_N^{-1}H_0^2 = 5.3 \times 10^{-6}\text{GeVcm}^{-3}$$

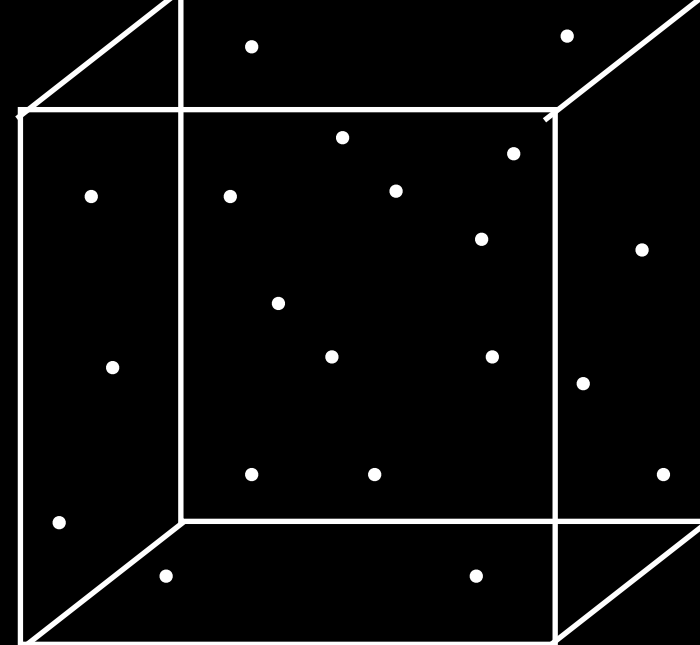
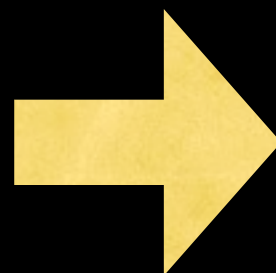
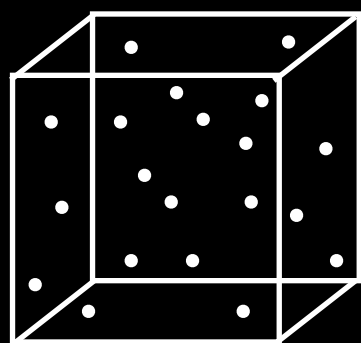
- define energy fraction  $\Omega_i=\rho_i/\rho_c$
- $\sum_i \Omega_i=1$

$$1 = \Omega_{\text{rad}} + \Omega_{\text{matter}} + \Omega_k + \Omega_\Lambda$$

$$\rho(z) = \rho_c(\Omega_{\text{rad}}(1+z)^4 + \Omega_{\text{matter}}(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda)$$

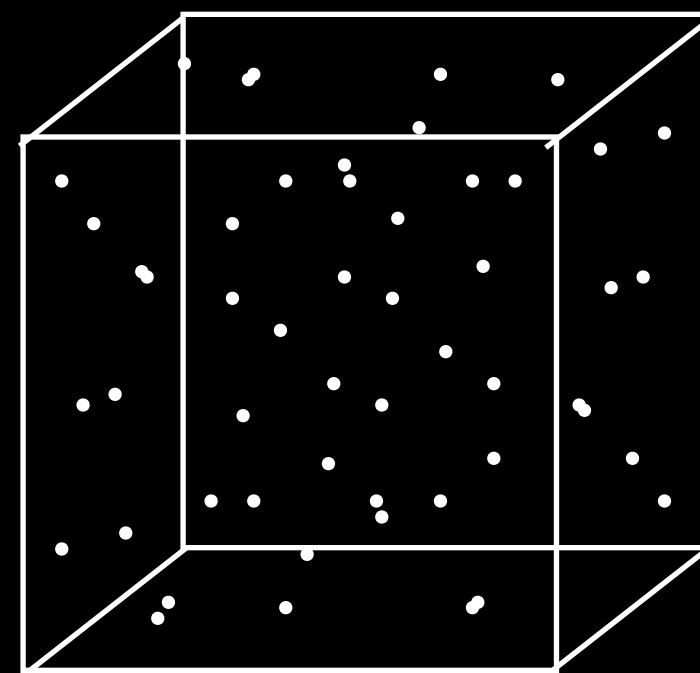
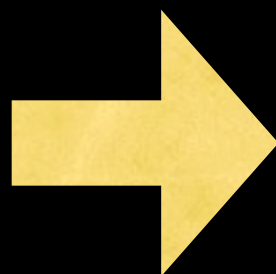
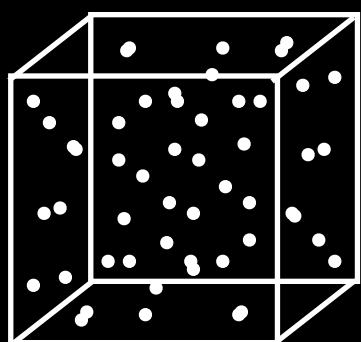


matter



$$\rho \propto R^{-3}$$

radiation

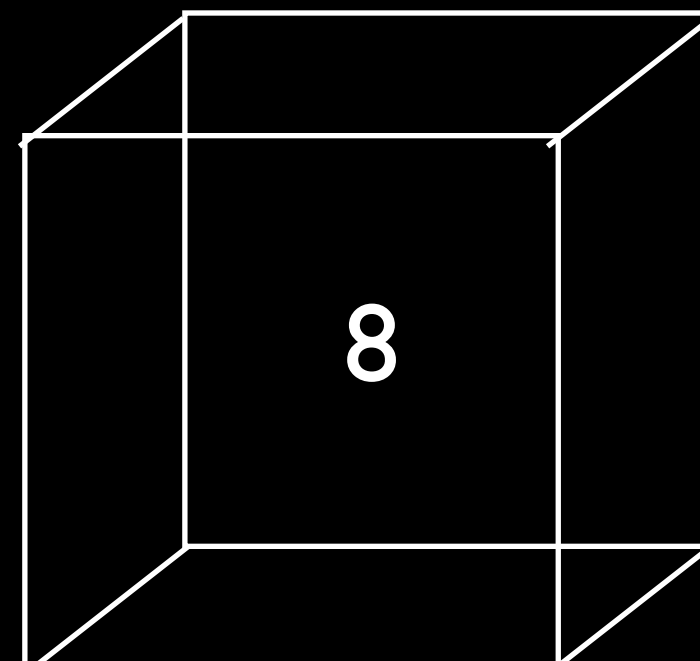
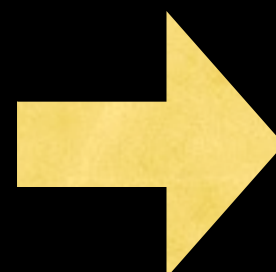
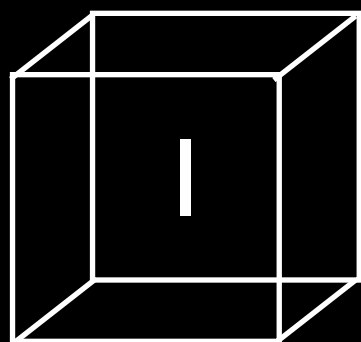


each one

$$E \propto R^{-1}$$

$$\rho \propto R^{-4}$$

vacuum  
energy  
74%



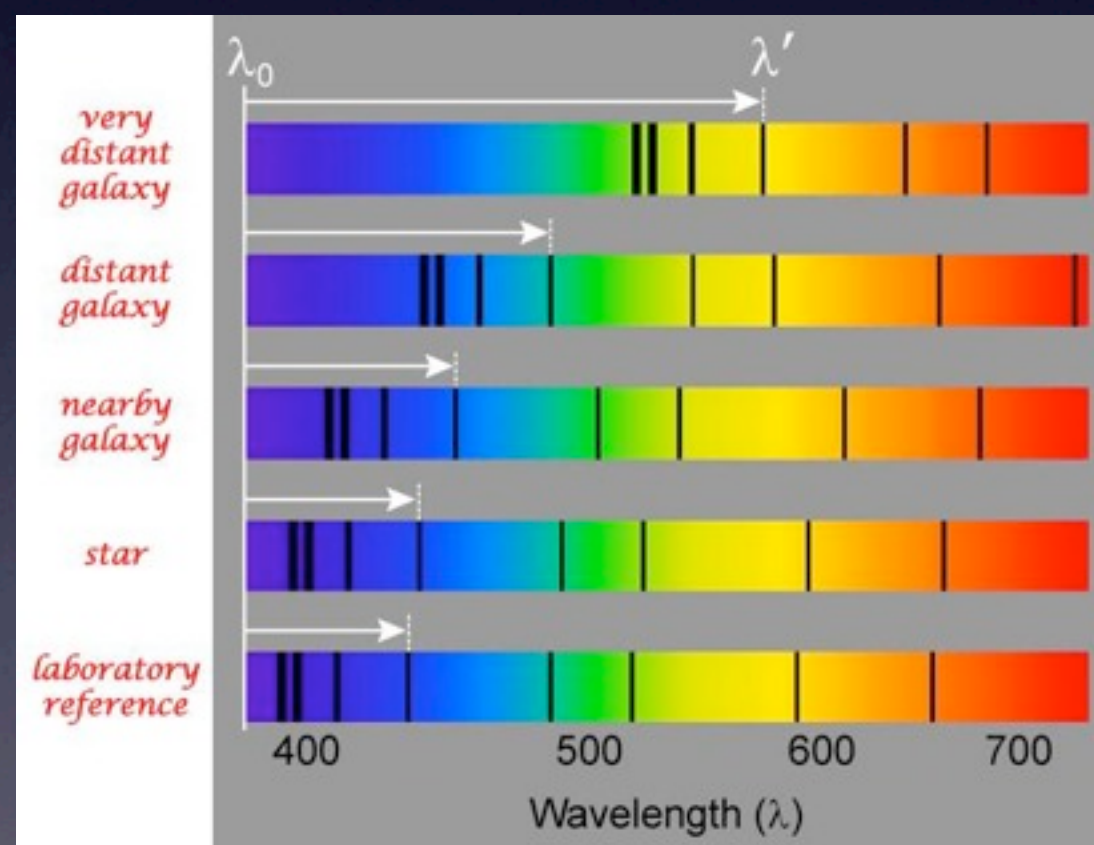
$$\rho \propto R^0$$



# Expanding Universe

$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3}G_N\rho - \frac{k}{R^2}$$

- $\lambda = \lambda_0(1+z)$
- $z$ : redshift
- $1+z = R_0/R = a(t)^{-1}$
- adiabatic expansion  $\Rightarrow$   
 $T \propto R^{-1}$
- $T = T_0(1+z)$



$$H(z)^2 = H_0^2(\Omega_{\text{rad}}(1+z)^4 + \Omega_{\text{matter}}(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda)$$



# distance

- luminosity distance
- comoving distance
- light travel distance
- angular diameter distance

$$d_L = \sqrt{L/4\pi S}$$

$$d_C(z) = c \int_t^{t_0} \frac{dt'}{a(t')}$$

$$c(t_0 - t)$$

$$d_A = x/\theta$$

$$\frac{\dot{a}}{a} = H$$

$$dt = \frac{1}{H} \frac{da}{a} = \frac{1}{H} \frac{dz}{1+z}$$

$$H(z)^2 = H_0^2 (\Omega_{\text{rad}}(1+z)^4 + \Omega_{\text{matter}}(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda)$$



# distance

- luminosity distance
- comoving distance
- light travel distance
- angular diameter distance

$$d_L = \sqrt{L/4\pi S}$$

$$d_C(z) = c \int_0^z \frac{dz'}{H(z')}$$

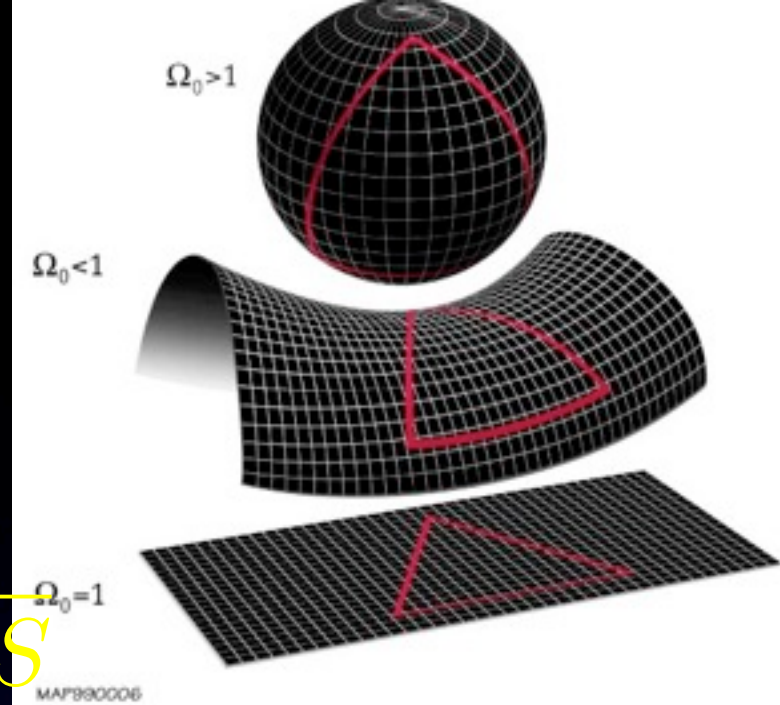
$$d_T(z) = c \int_0^z \frac{dz'}{(1+z')H(z')}$$

$$d_A = x/\theta$$

- transverse comoving distance

$$d_M(z) = \frac{c}{H_0} \frac{1}{\sqrt{\Omega_k}} \sinh \frac{\sqrt{\Omega_k} H_0 d_C(z)}{c}$$

$$H(z)^2 = H_0^2 (\Omega_{\text{rad}}(1+z)^4 + \Omega_{\text{matter}}(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda)$$





# distance

- luminosity distance

$$d_L(z) = (1 + z)d_M(z)$$

- comoving distance

$$d_C(z) = c \int_0^z \frac{dz'}{H(z')}$$

- light travel distance

$$d_T(z) = c \int_0^z \frac{dz'}{(1 + z')H(z')}$$

- angular diameter distance

$$d_A(z) = \frac{d_M(z)}{(1 + z)}$$

- transverse comoving distance

$$d_M(z) = \frac{c}{H_0} \frac{1}{\sqrt{\Omega_k}} \sinh \frac{\sqrt{\Omega_k} H_0 d_C(z)}{c}$$

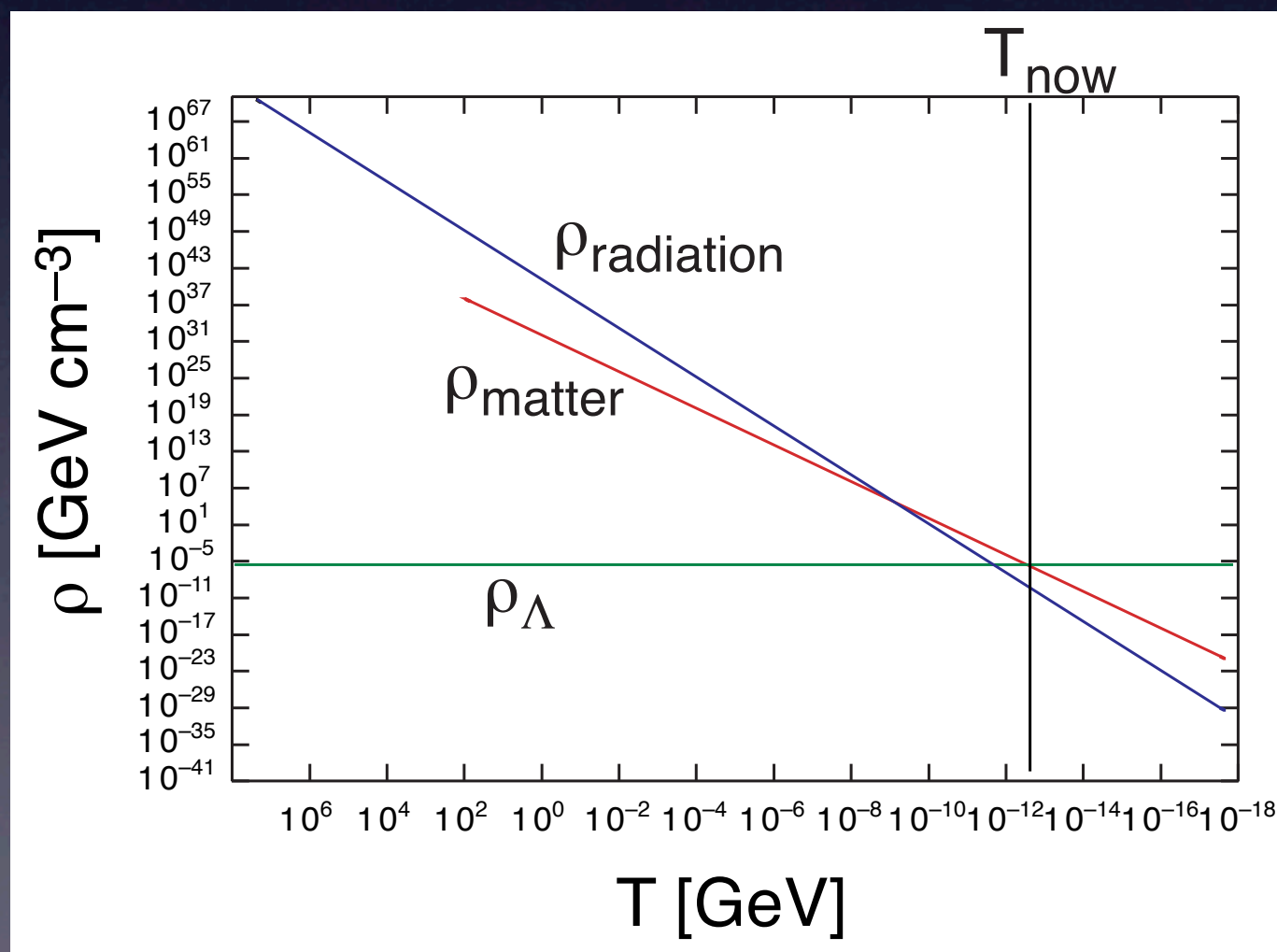
$$H(z)^2 = H_0^2 (\Omega_{\text{rad}}(1 + z)^4 + \Omega_{\text{matter}}(1 + z)^3 + \Omega_k(1 + z)^2 + \Omega_\Lambda)$$



# Early Universe

- temperature:  $T \propto (1+z)$
- matter:  $\rho \propto (1+z)^3$
- radiation (massless particles):  $\rho \propto (1+z)^4$   
matter-radiation equality:  $z \approx 3300$
- recombination:  $z \approx 1300$

$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3} G_N \rho - \frac{k}{R^2}$$





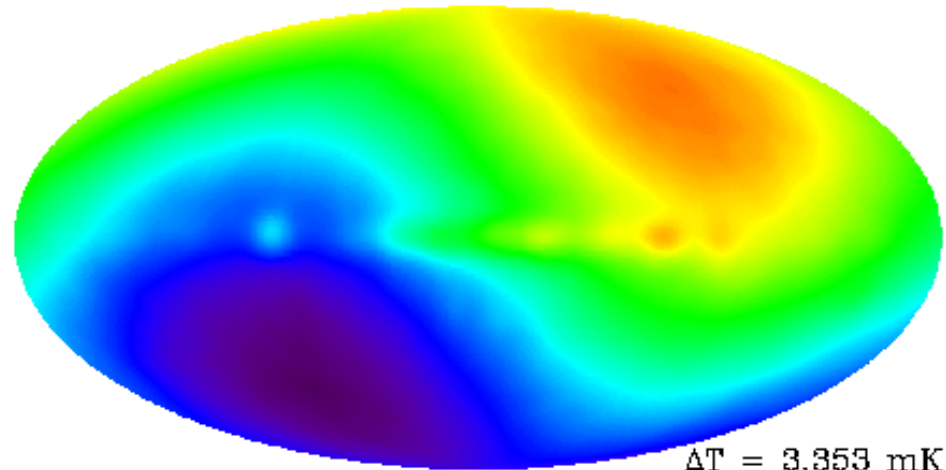


# Large-Scale Structure

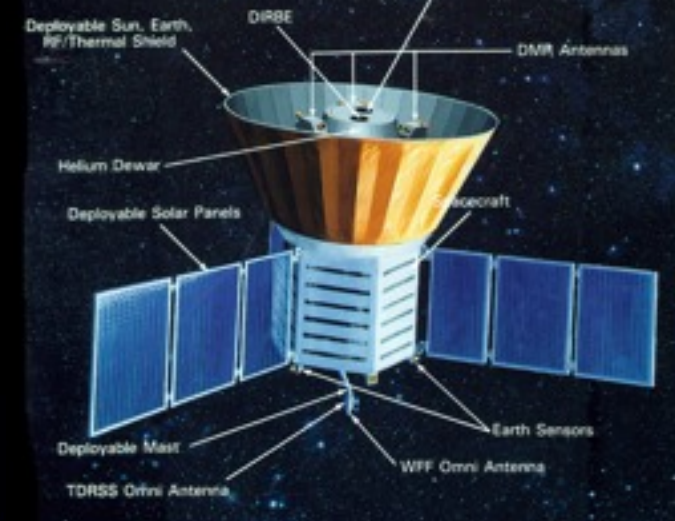
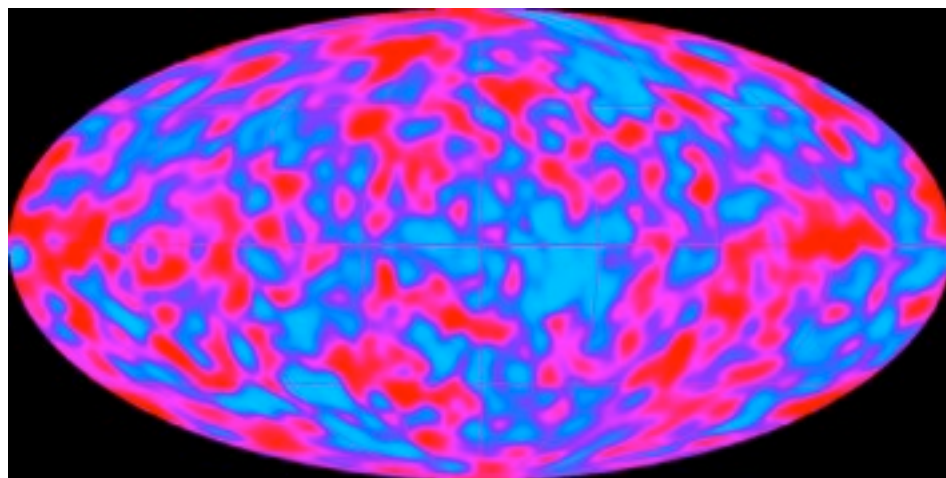




$T = 2.728 \text{ K}$



$\Delta T = 3.353 \text{ mK}$



# CMB temperature

CMB dipole  
we are moving at  
 $\sim 1\%$  of  $c$  relative to CMB

CMB anisotropy  
at  $\sim 10^{-5}$   
1mm ripple on 100m sea



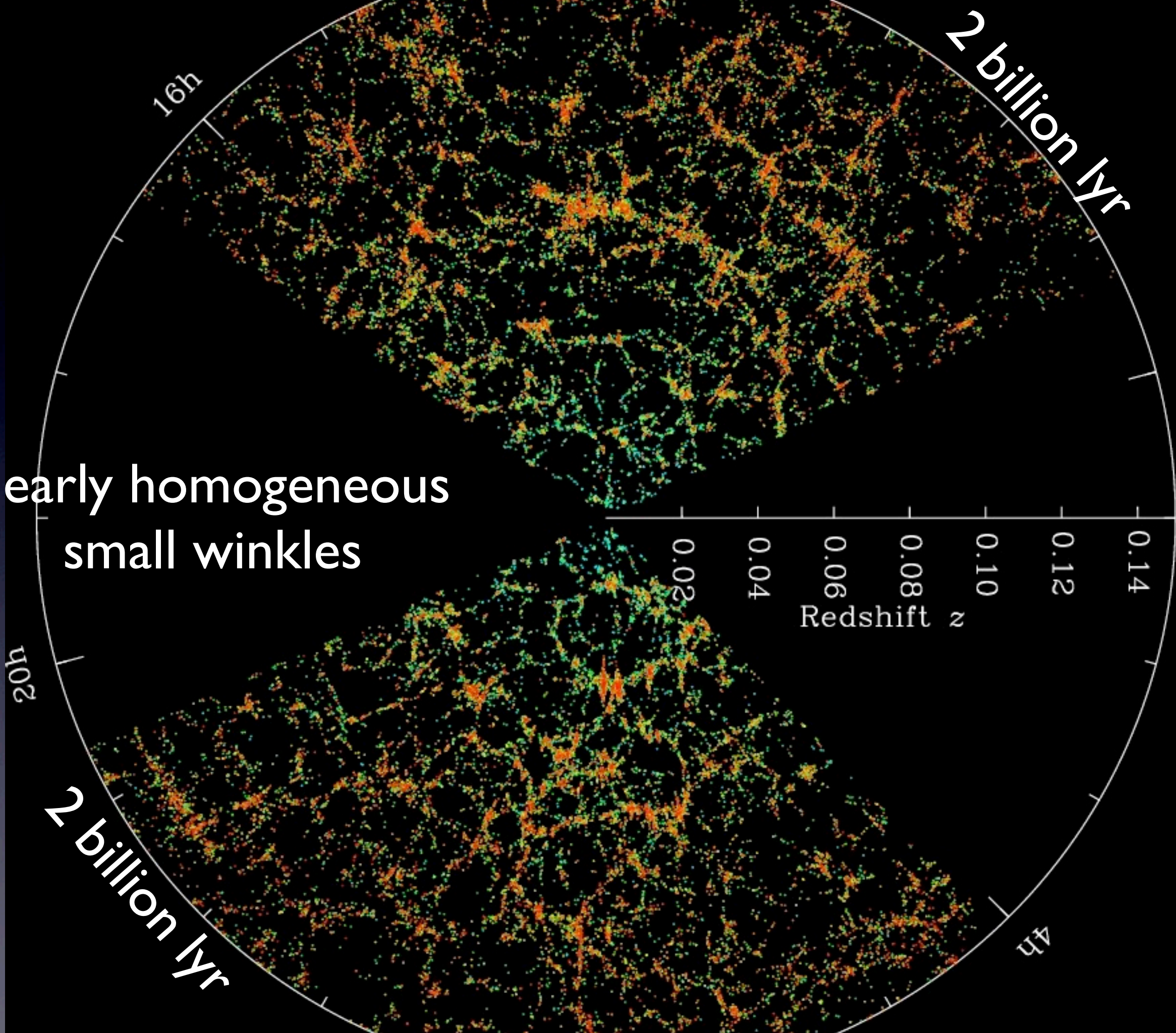
20 billion yr

2 billion yr

2 billion yr

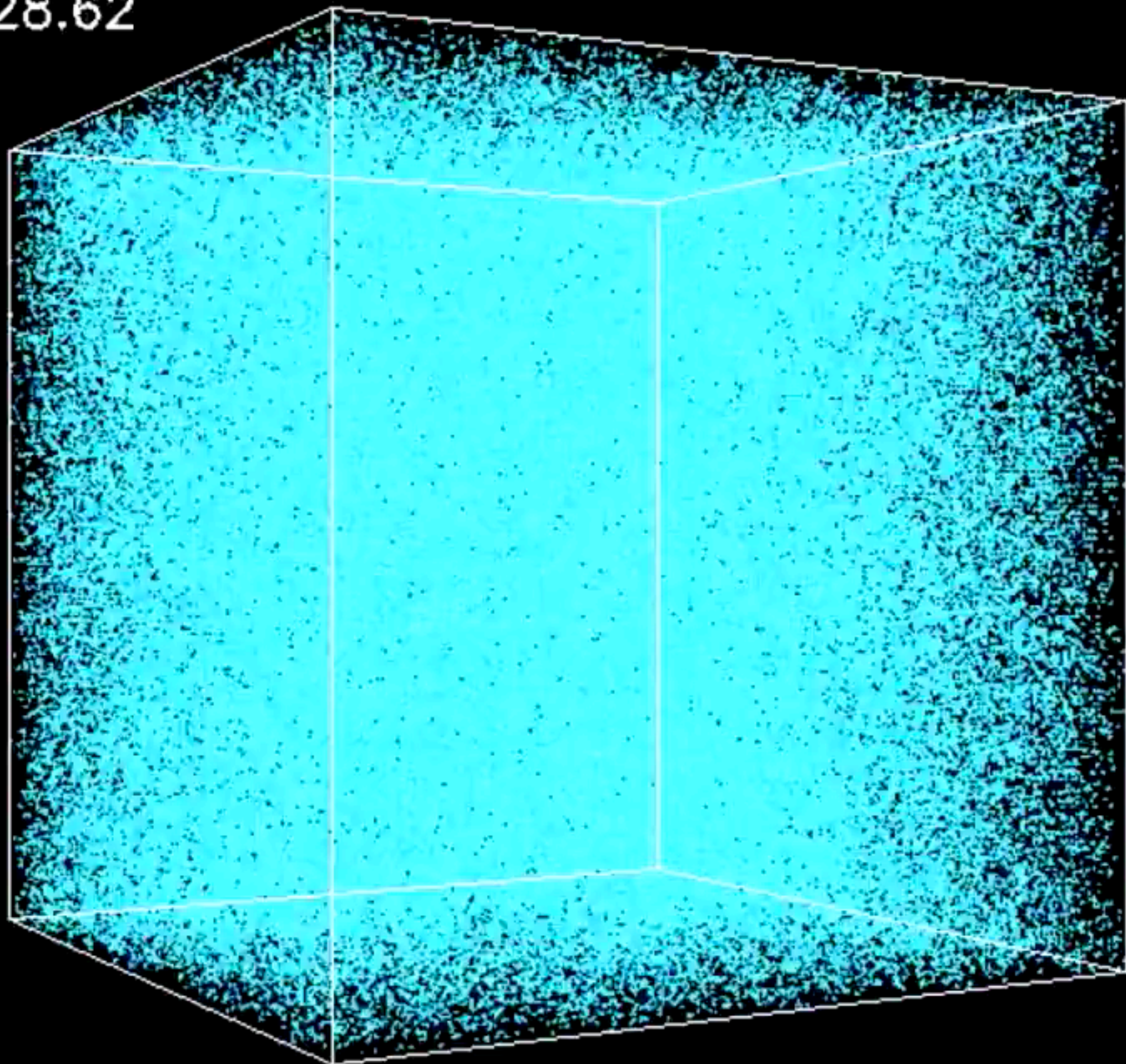
Redshift  $z$

nearly homogeneous  
small winkles





$Z=28.62$





# Dark Matter is our birth mother

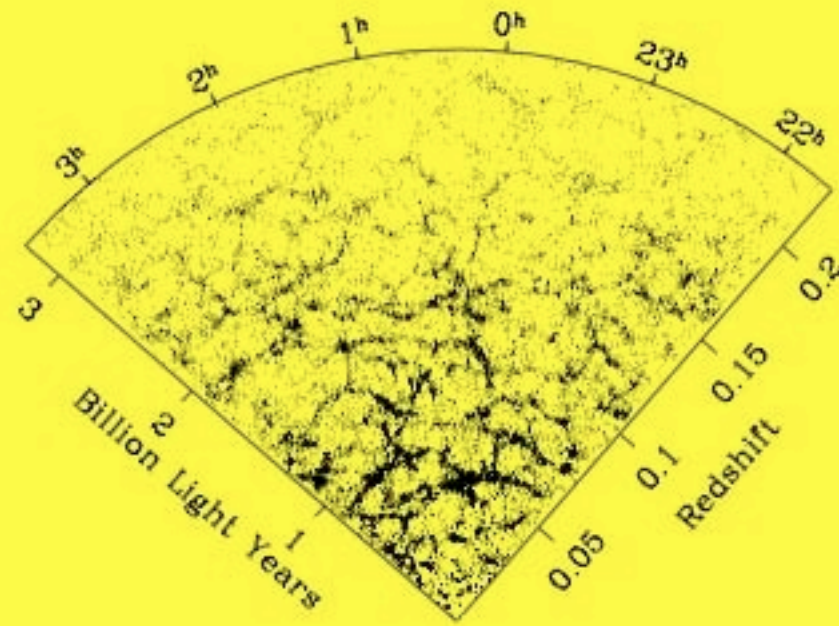
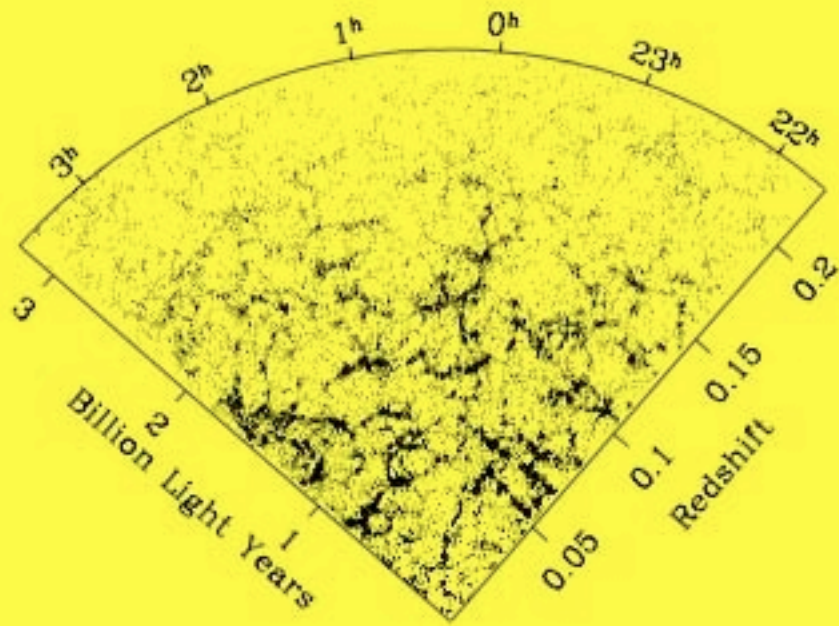
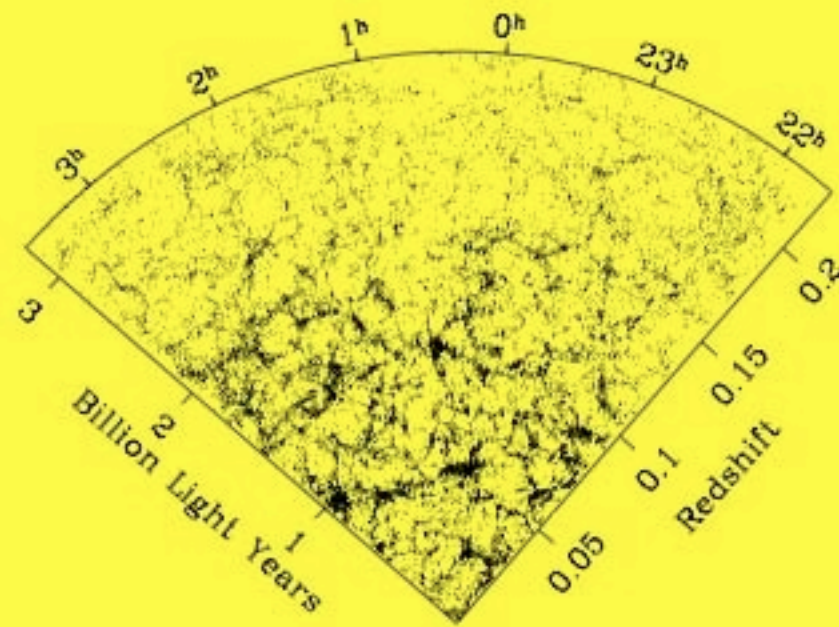
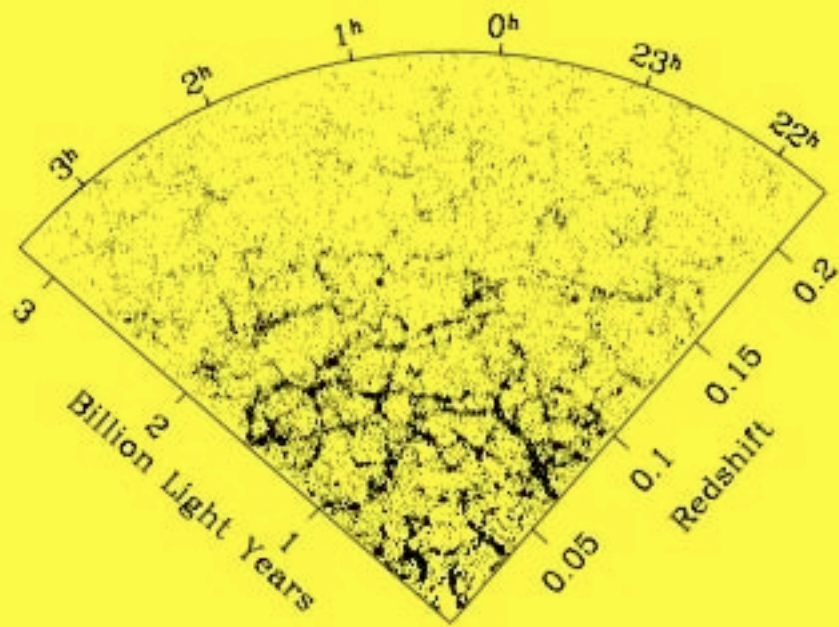


no dark matter

with dark matter



# one is real









# reenacting Big Ban with Cal Band





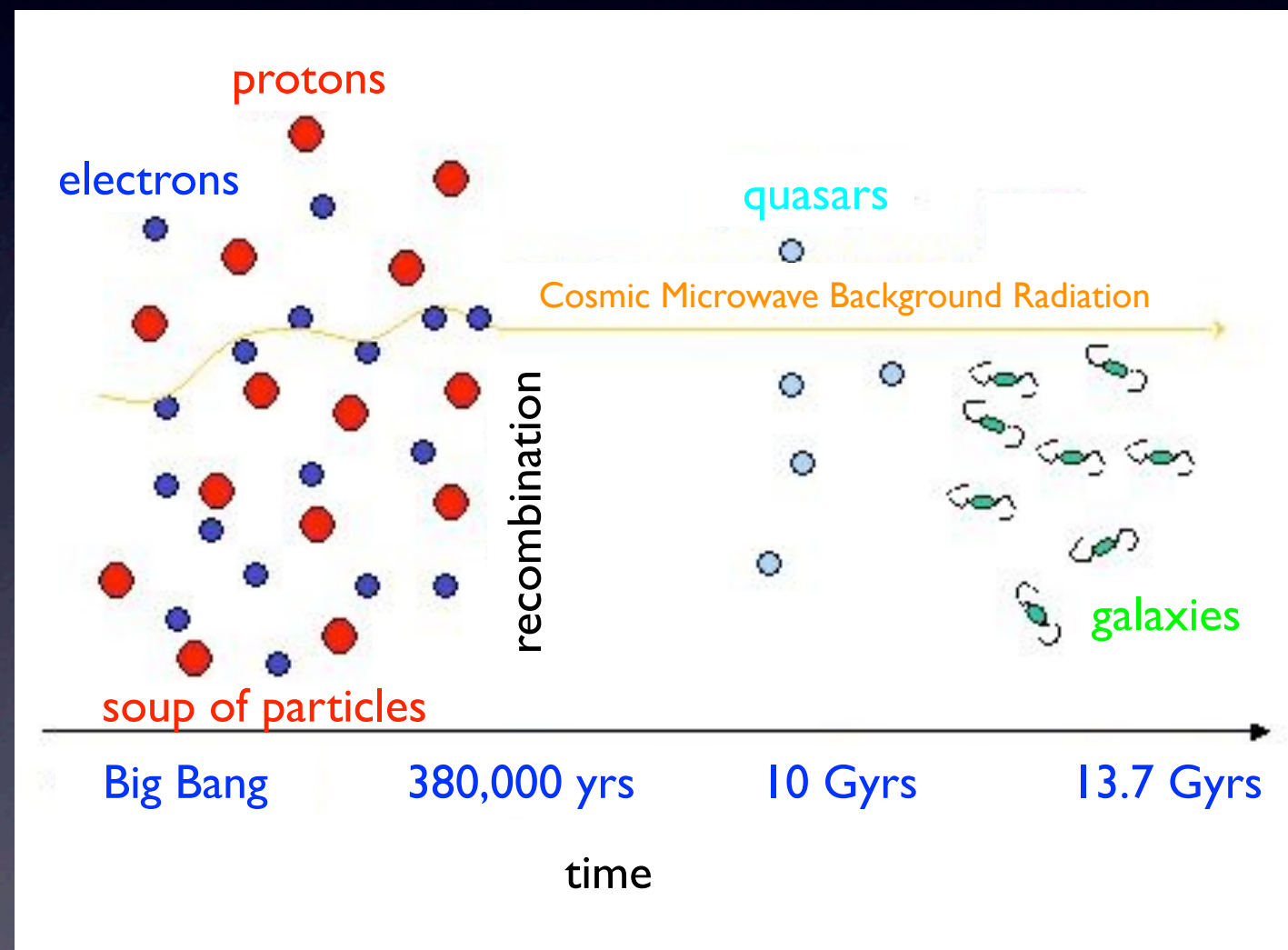


power spectrum



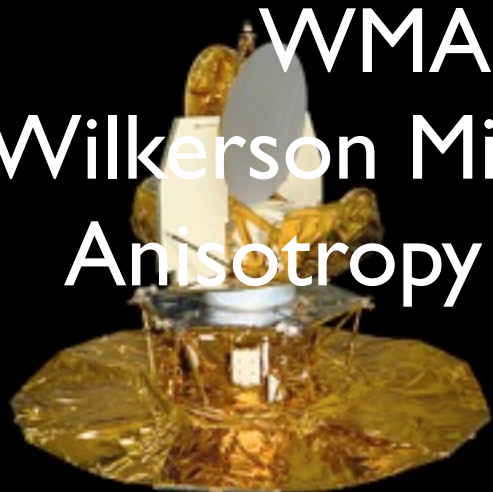
# CMB

- before recombination, there was a fluid of protons, electrons, photons, dark matter (and neutrinos)
- photon pressure  $\Rightarrow$  “sound waves”





# WMAP Wilkinson Microwave Anisotropy Probe

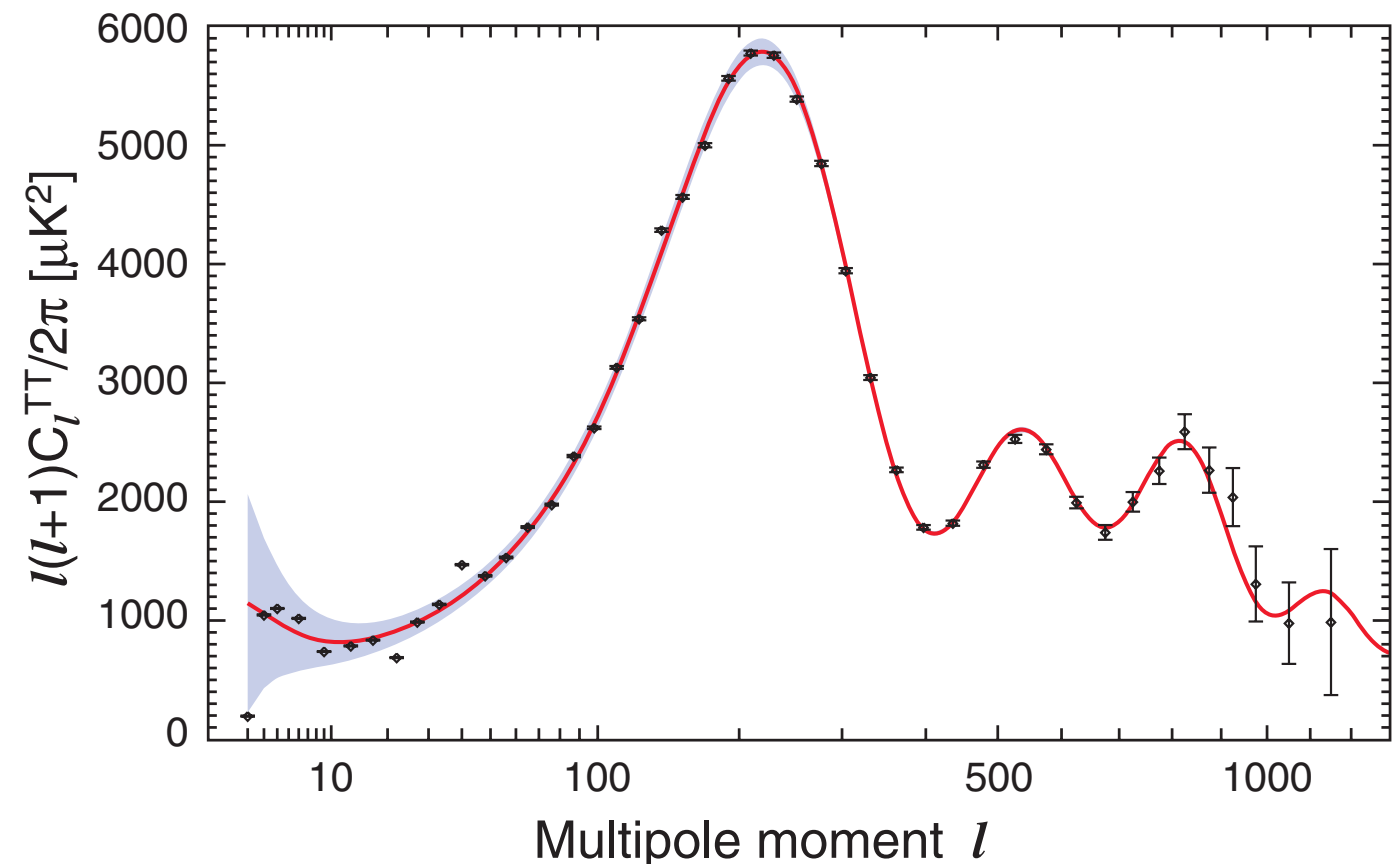
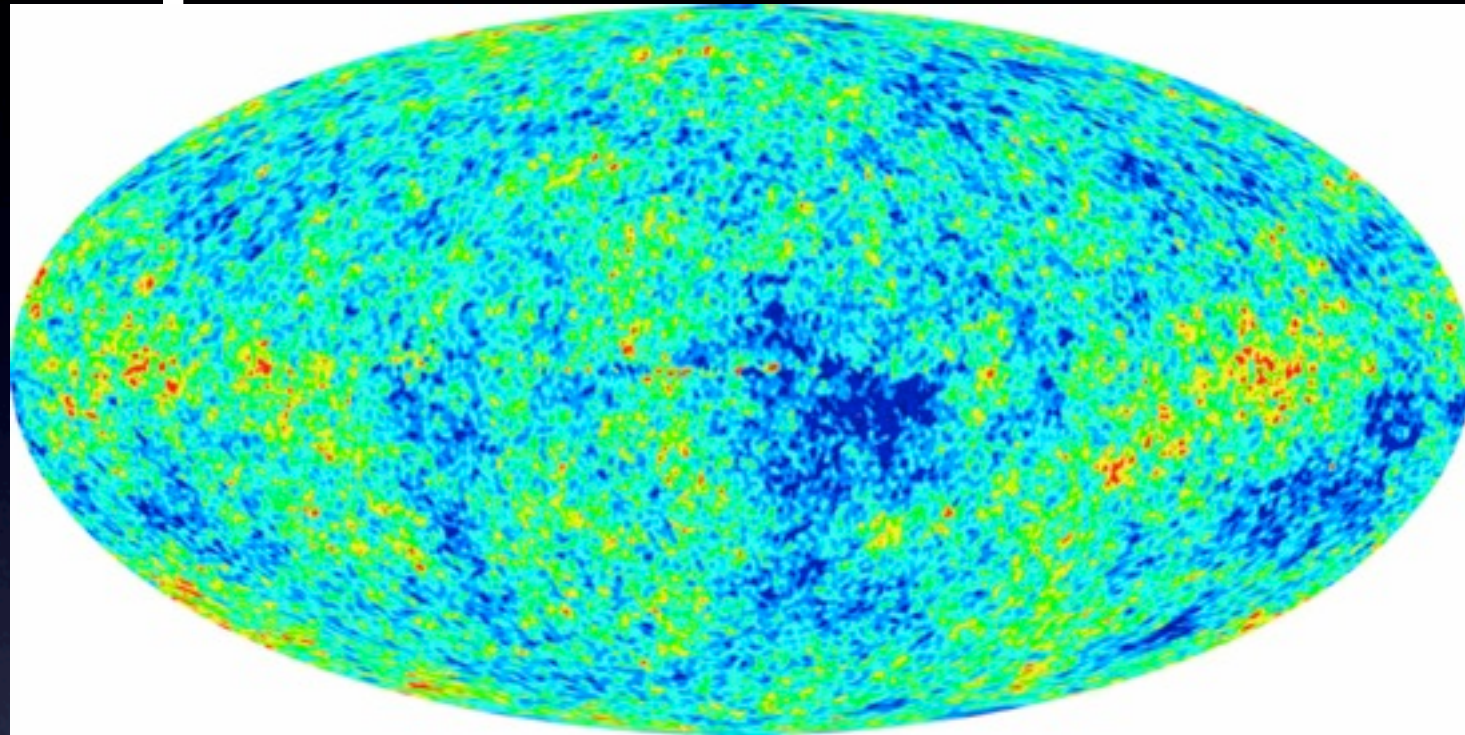


## assumption

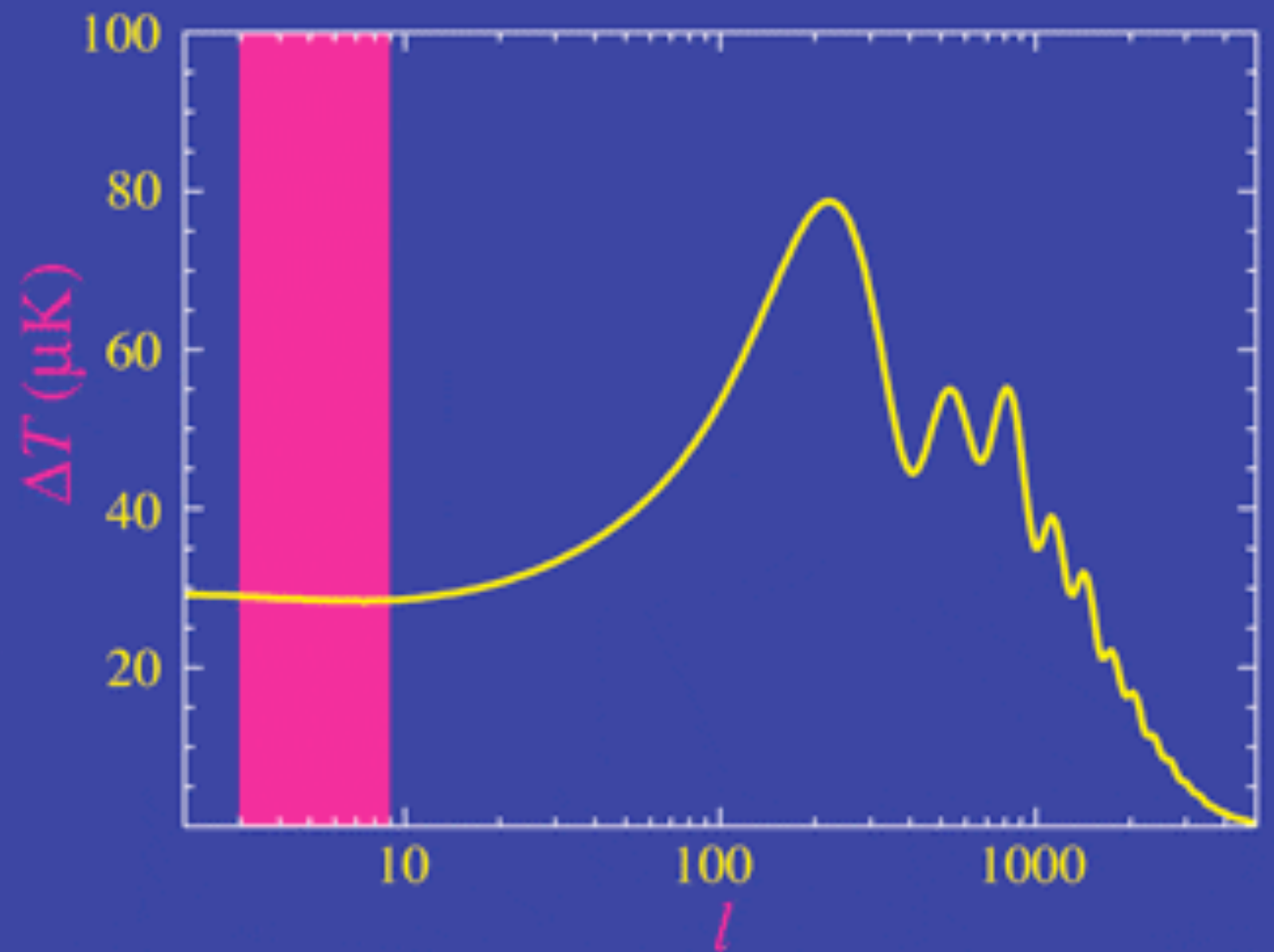
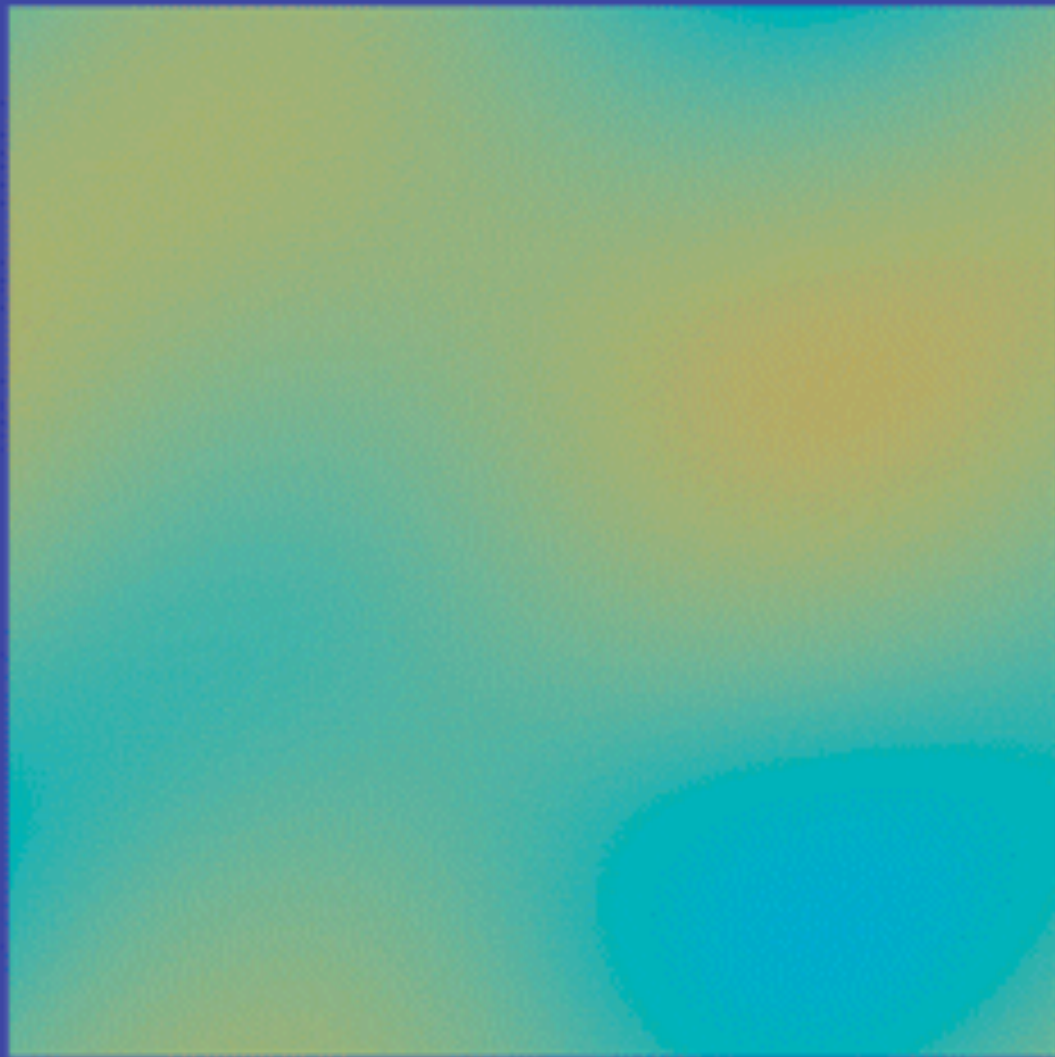
- a random density fluctuations  $\sim O(10^{-5})$  more-or-less **scale invariant**  $P(k) \propto k^{ns-1}$
- starts acoustic oscillation, amplified by gravitational attraction
- “knows” about everything between  $0 < z < 1300$

$$\delta T/T = a_{lm} Y_l^m$$

$$(2l+1)c_{lm} = \sum_m a_{lm}^* a_{lm}$$

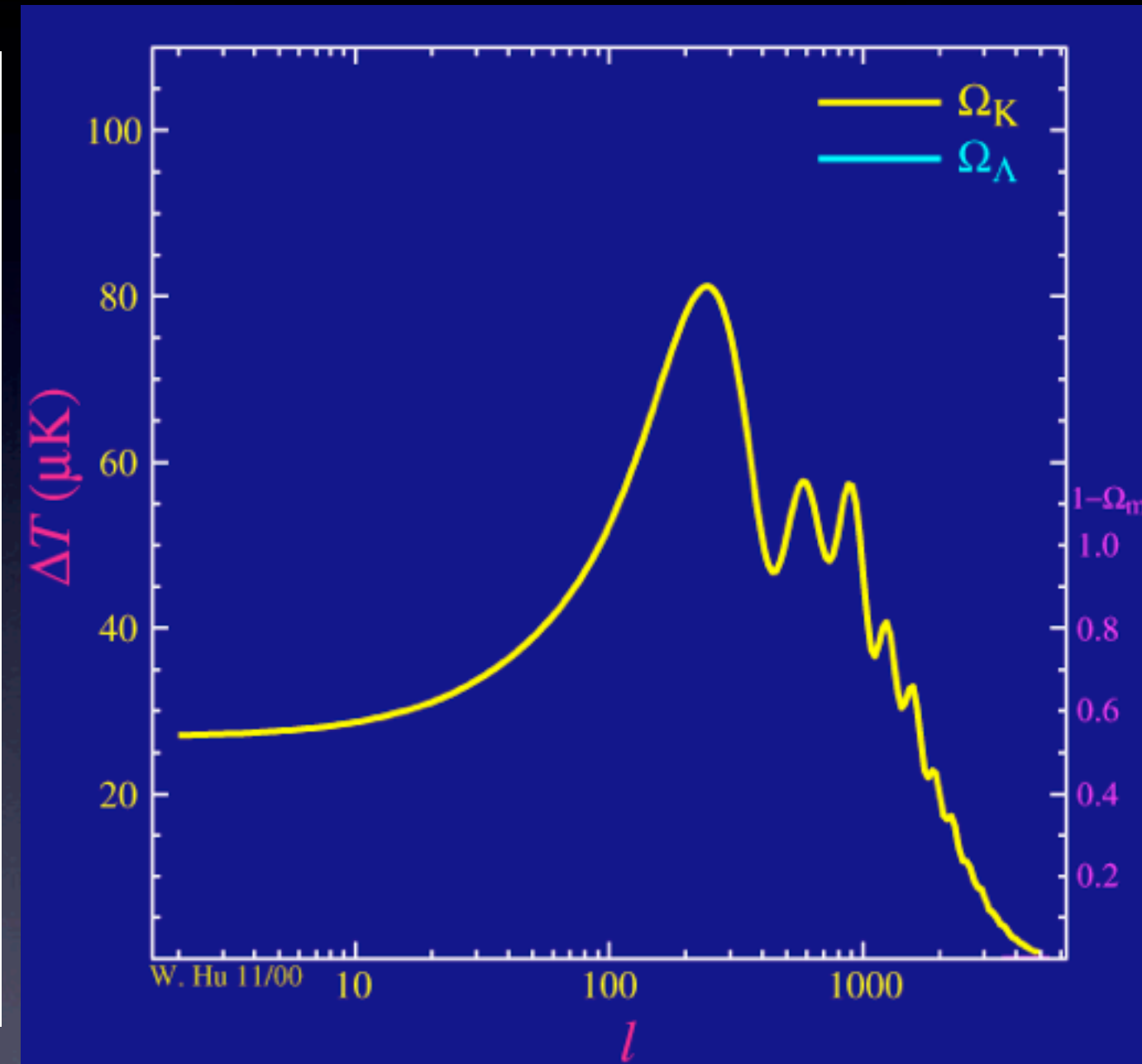
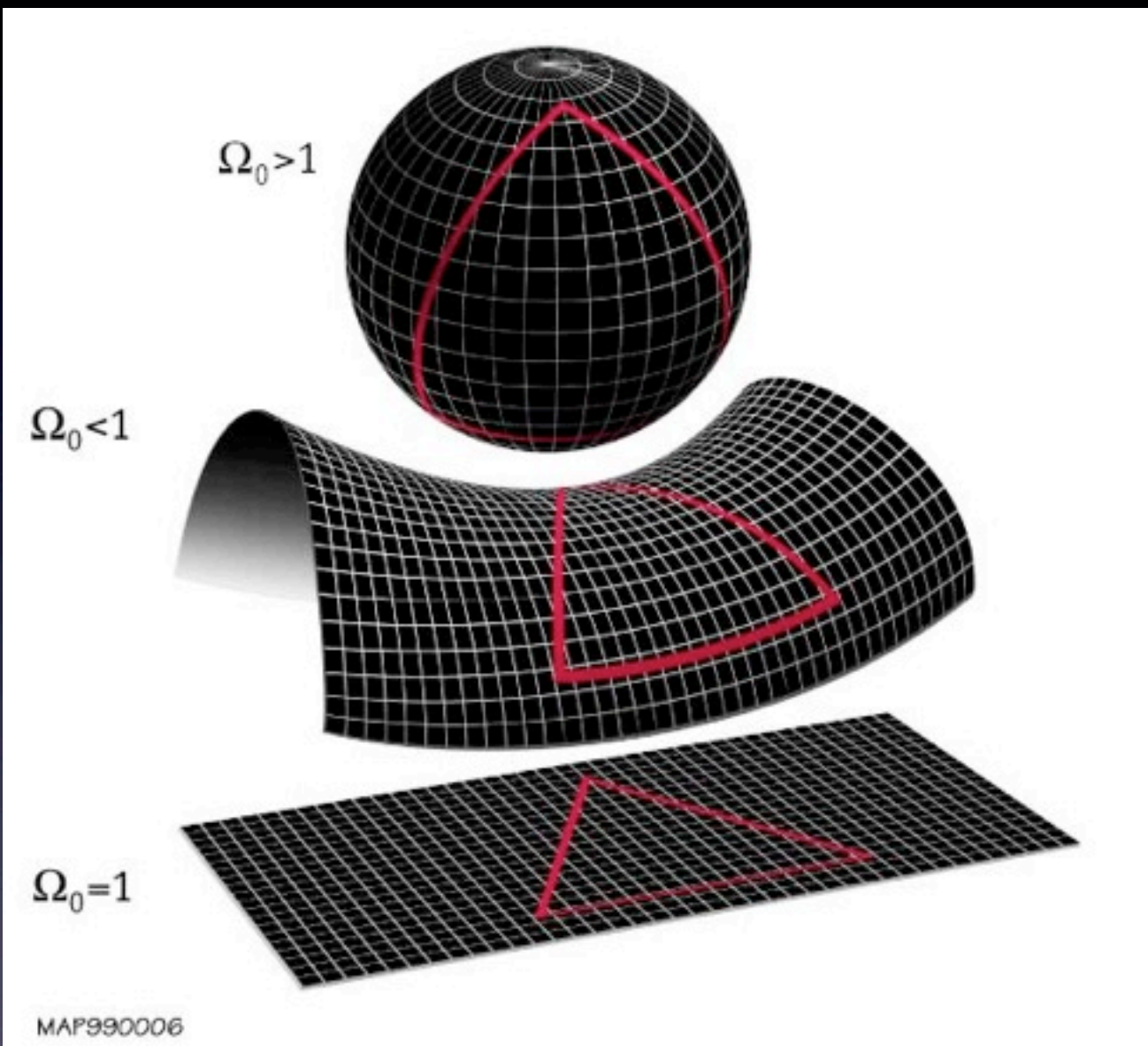






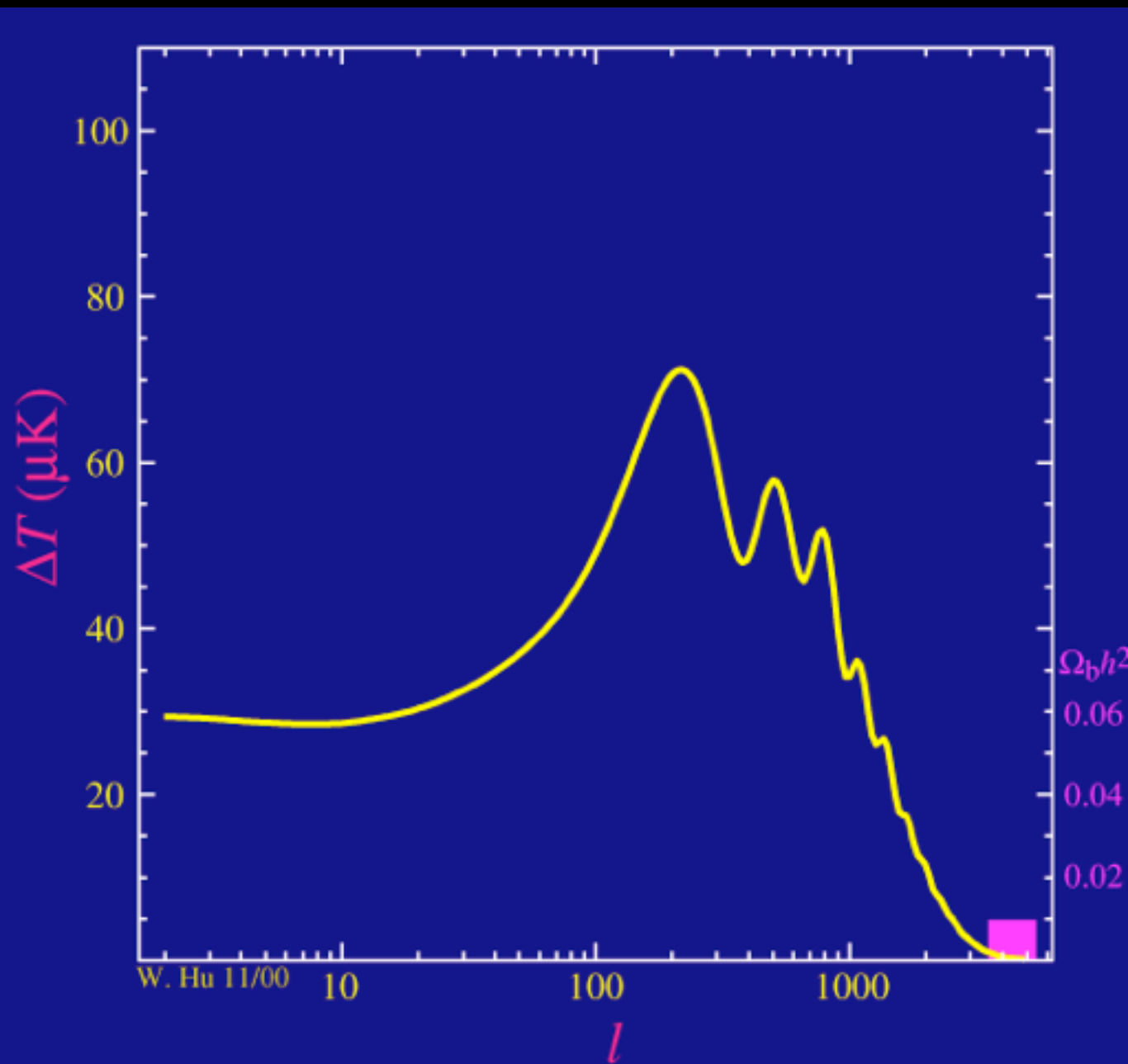
Wayne Hu



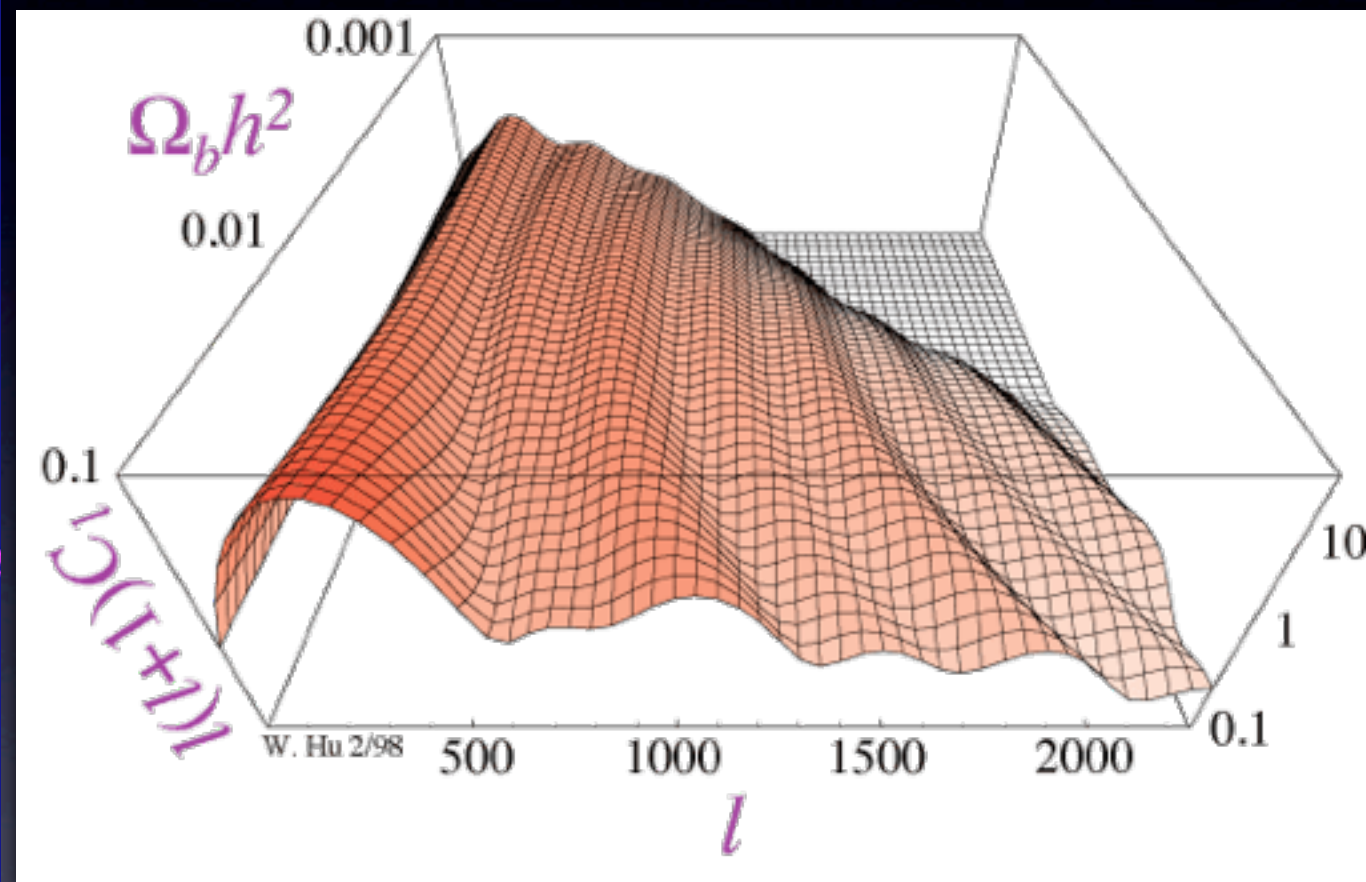


$\Omega_K$  changes  
the apparent angular size  
of the peak positions





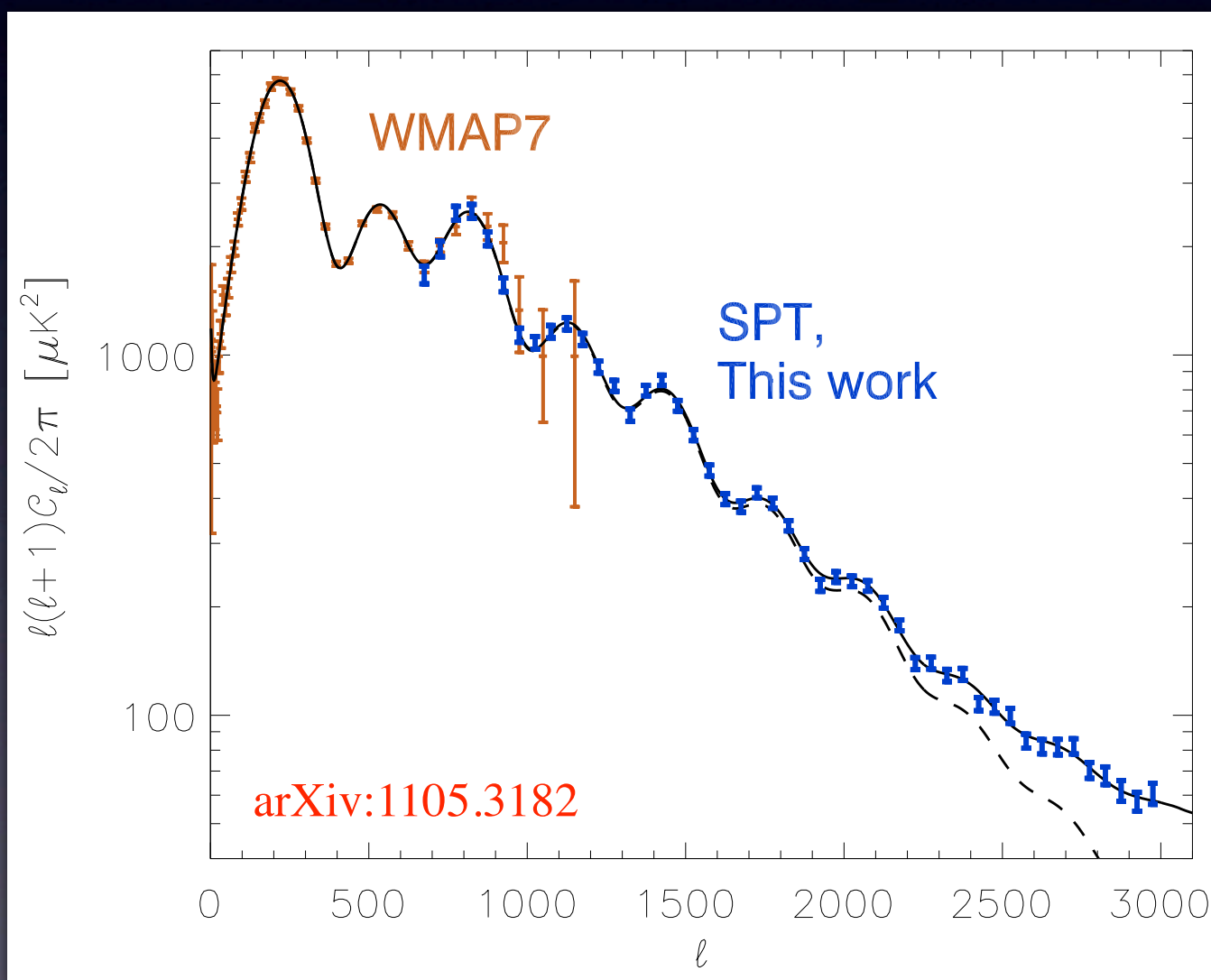
$\Omega_b$  changes  
the relative size of  
even and odd peaks



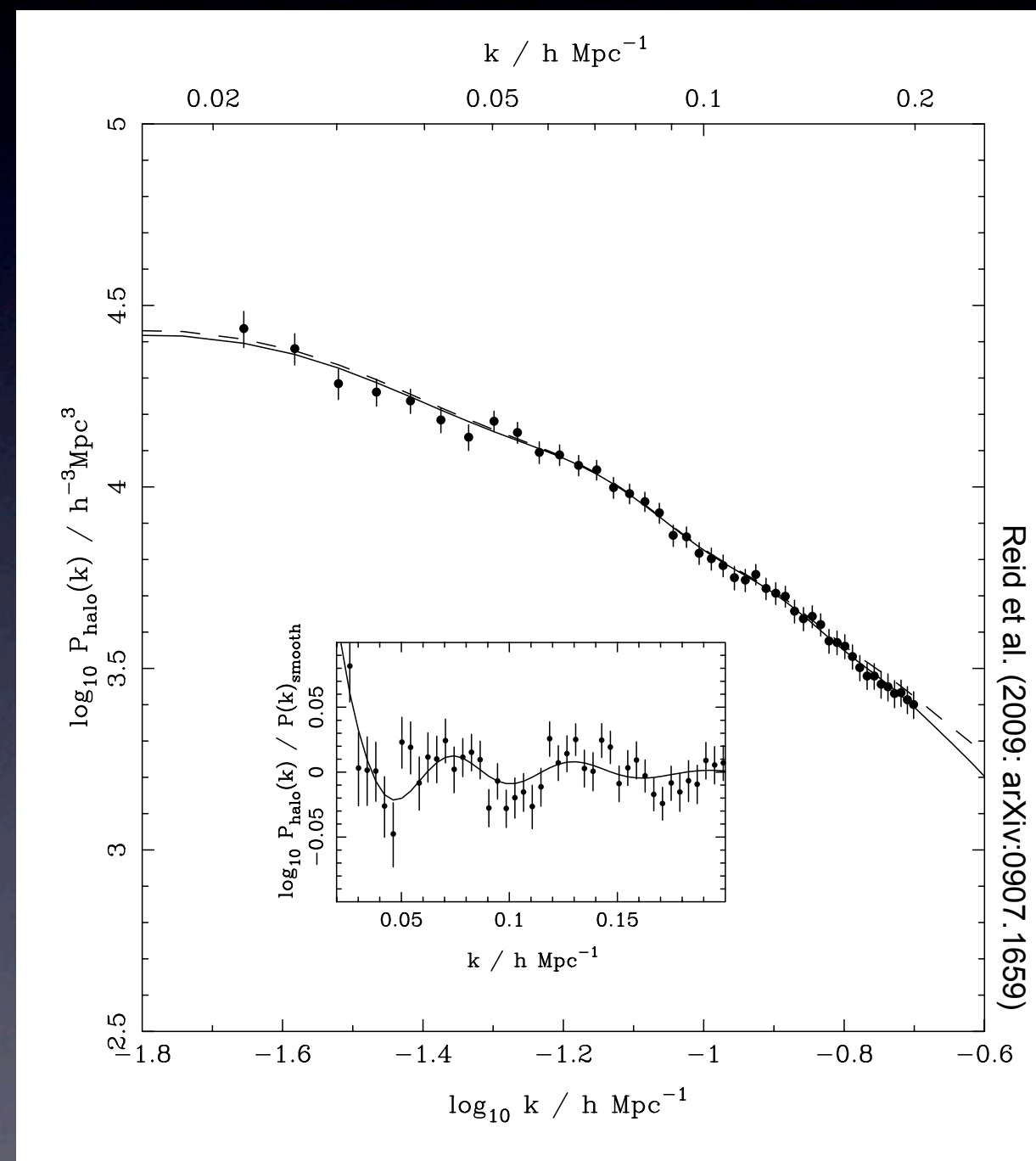


# standard cosmology $\Lambda$ CDM

works like SM @ LEP



CMB power spectrum



galaxy power spectrum



# standard cosmology

## $\Lambda$ CDM

- flat universe  $\Omega_k=0$
- perturbation  $P(k) \propto k^{n_s-1}$   
with single exponent  $n_s$   
for both scalar and  
tensor modes
- three massless neutrinos

**Table 3**  
Six-parameter  $\Lambda$ CDM Fit<sup>a</sup>

Parameter	Seven-year Fit
Fit parameters	
$10^2 \Omega_b h^2$	$2.258^{+0.057}_{-0.056}$
$\Omega_c h^2$	$0.1109 \pm 0.0056$
$\Omega_\Lambda$	$0.734 \pm 0.029$
$\Delta_{\mathcal{R}}^2$	$(2.43 \pm 0.11) \times 10^{-9}$
$n_s$	$0.963 \pm 0.014$
$\tau$	$0.088 \pm 0.015$
Derived parameters	
$t_0$	$13.75 \pm 0.13$ Gyr
$H_0$	$71.0 \pm 2.5$ km s <sup>-1</sup> Mpc <sup>-1</sup>
$\sigma_8$	$0.801 \pm 0.030$
$\Omega_b$	$0.0449 \pm 0.0028$
$\Omega_c$	$0.222 \pm 0.026$
$z_{\text{eq}}$	$3196^{+134}_{-133}$
$z_{\text{reion}}$	$10.5 \pm 1.2$

**Note.** <sup>a</sup> Models fit to *WMAP* data only. See Komatsu et al. for constraints.





# Known Facts about Dark Matter



# Cold and Neutral

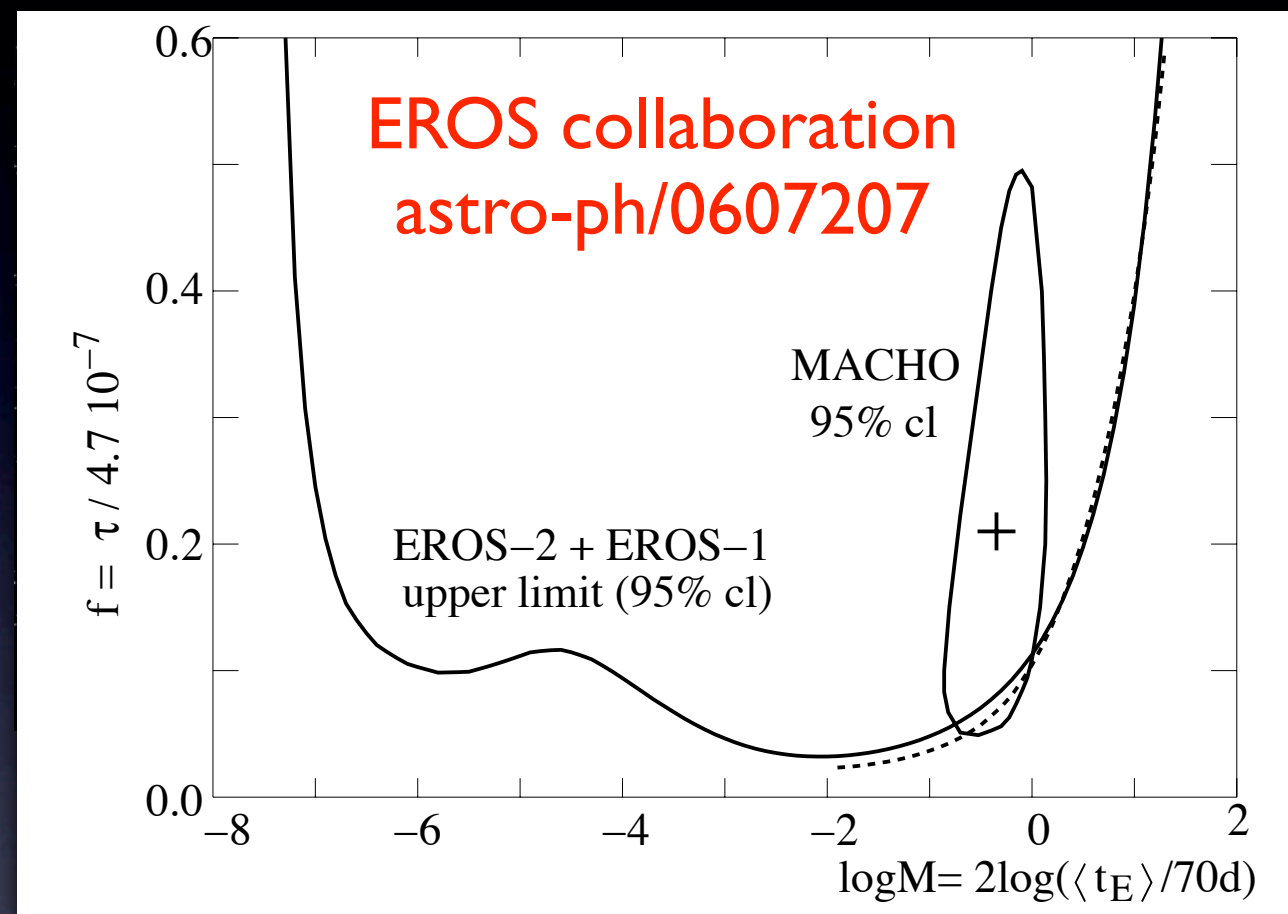
- By the time of matter-radiation equality and until now, dark matter must be non-relativistic and clump together by gravitational attraction
- must be electrically neutral



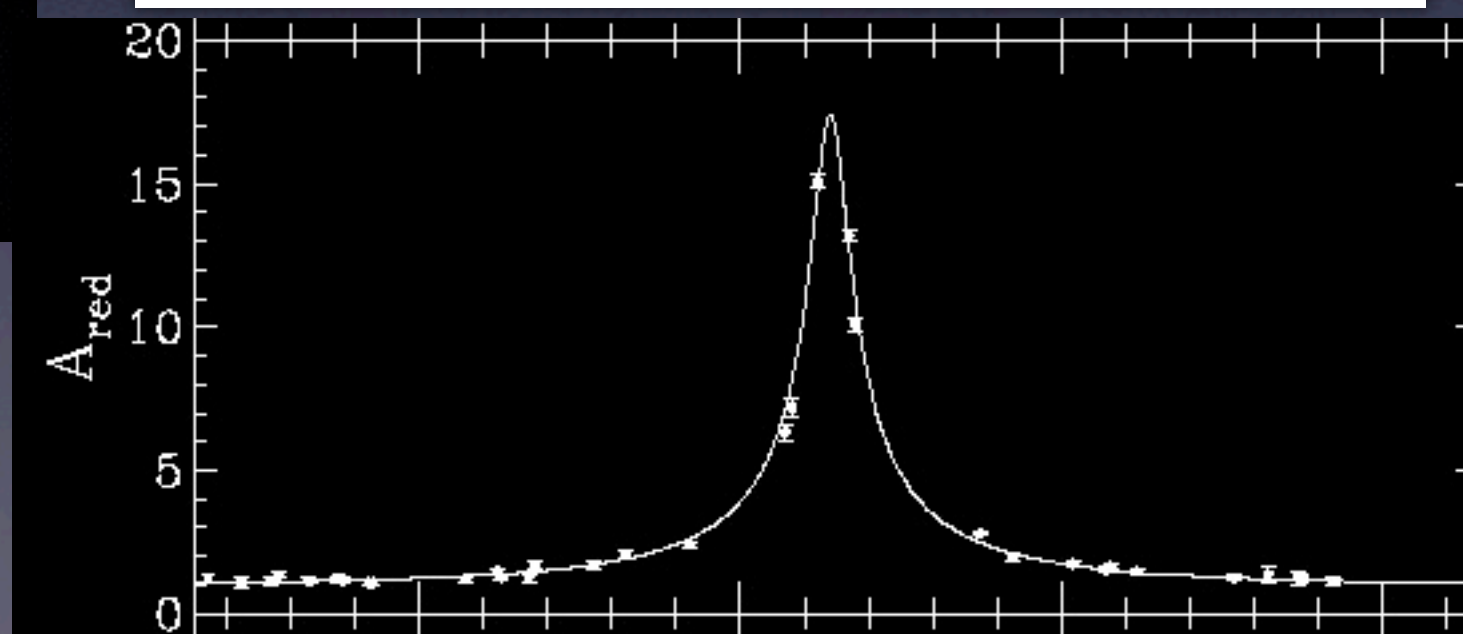
# Dim Stars?

Search for **MACHOs**  
(Massive Compact Halo Objects)

*Large Magellanic Cloud*



*Not enough of them!*





# Mass Limits

## “Uncertainty Principle”

- Clumps to form structure
- imagine  $V = G_N \frac{Mm}{r}$
- “Bohr radius”:  $r_B = \frac{\hbar^2}{G_N M m^2}$
- too small  $m \Rightarrow$  won’t “fit” in a galaxy!
- $m > 10^{-22}$  eV “uncertainty principle” bound  
(modified from Hu, Barkana, Gruzinov, astro-ph/0003365)



# Mass Limits

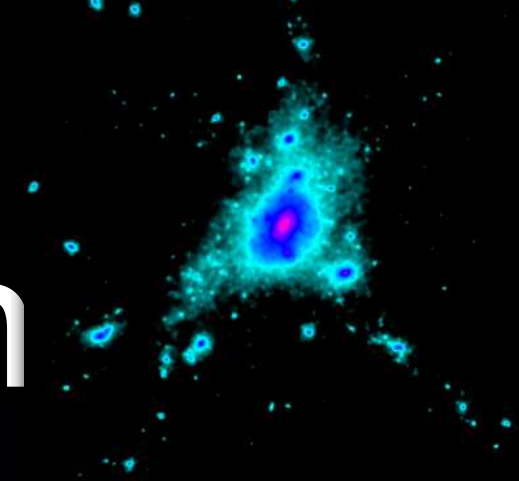
- $10^{-31}$  GeV to  $10^{50}$  GeV
- we narrowed it down to within 81 orders of magnitude
- a big progress in 70 years since Zwicky





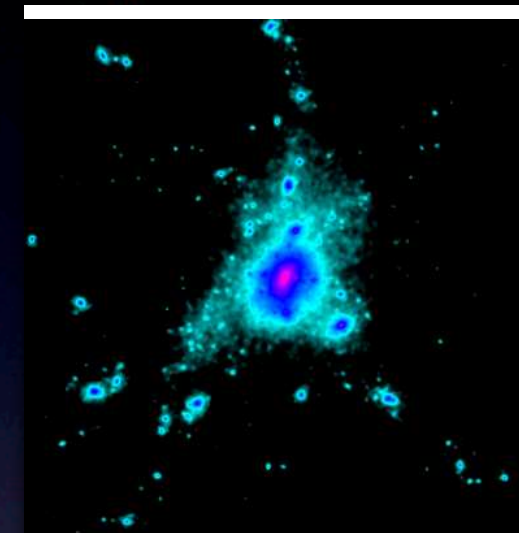
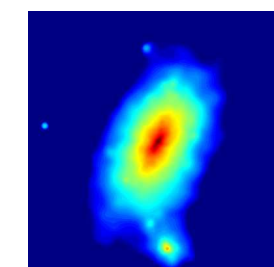
# Self-Couplin

- if self-coupling too big, will “smooth out” cuspy profile at the galactic center
- some people want it  
(Spergel and Steinhardt, astro-ph/9909386)
- need core  $< 35$  kpc/h from data  
 $\sigma < 1.7 \times 10^{-25} \text{ cm}^2 (\text{m/GeV})$   
(Yoshida, Springel, White, astro-ph/0006134)
- bullet cluster:  
 $\sigma < 1.7 \times 10^{-24} \text{ cm}^2 (\text{m/GeV})$   
(Markevitch et al, astro-ph/0309303)



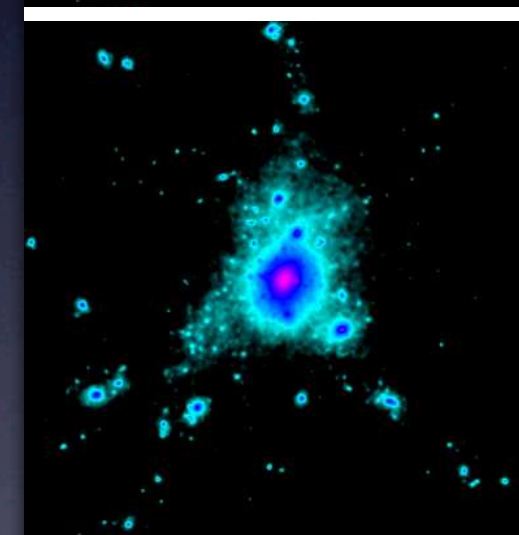
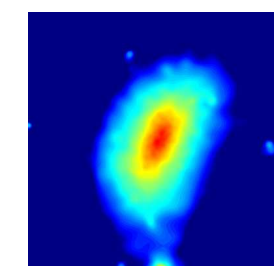
S1

1 : 0.82 : 0.65



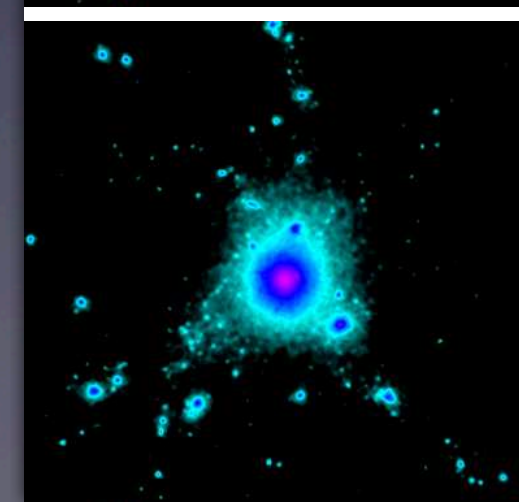
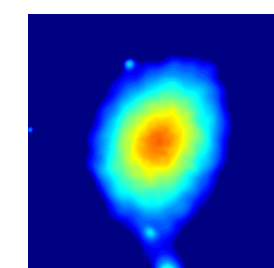
S1Wa

$\sigma^* = 0.1 \text{ cm}^2 \text{g}^{-1}$   
 $r_c = 40 h^{-1} \text{ kpc}$   
1 : 0.88 : 0.66



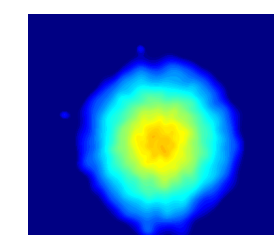
S1Wb

$\sigma^* = 1.0 \text{ cm}^2 \text{g}^{-1}$   
 $r_c = 100 h^{-1} \text{ kpc}$   
1 : 0.91 : 0.72



S1Wc

$\sigma^* = 10.0 \text{ cm}^2 \text{g}^{-1}$   
 $r_c = 160 h^{-1} \text{ kpc}$   
1 : 0.98 : 0.89



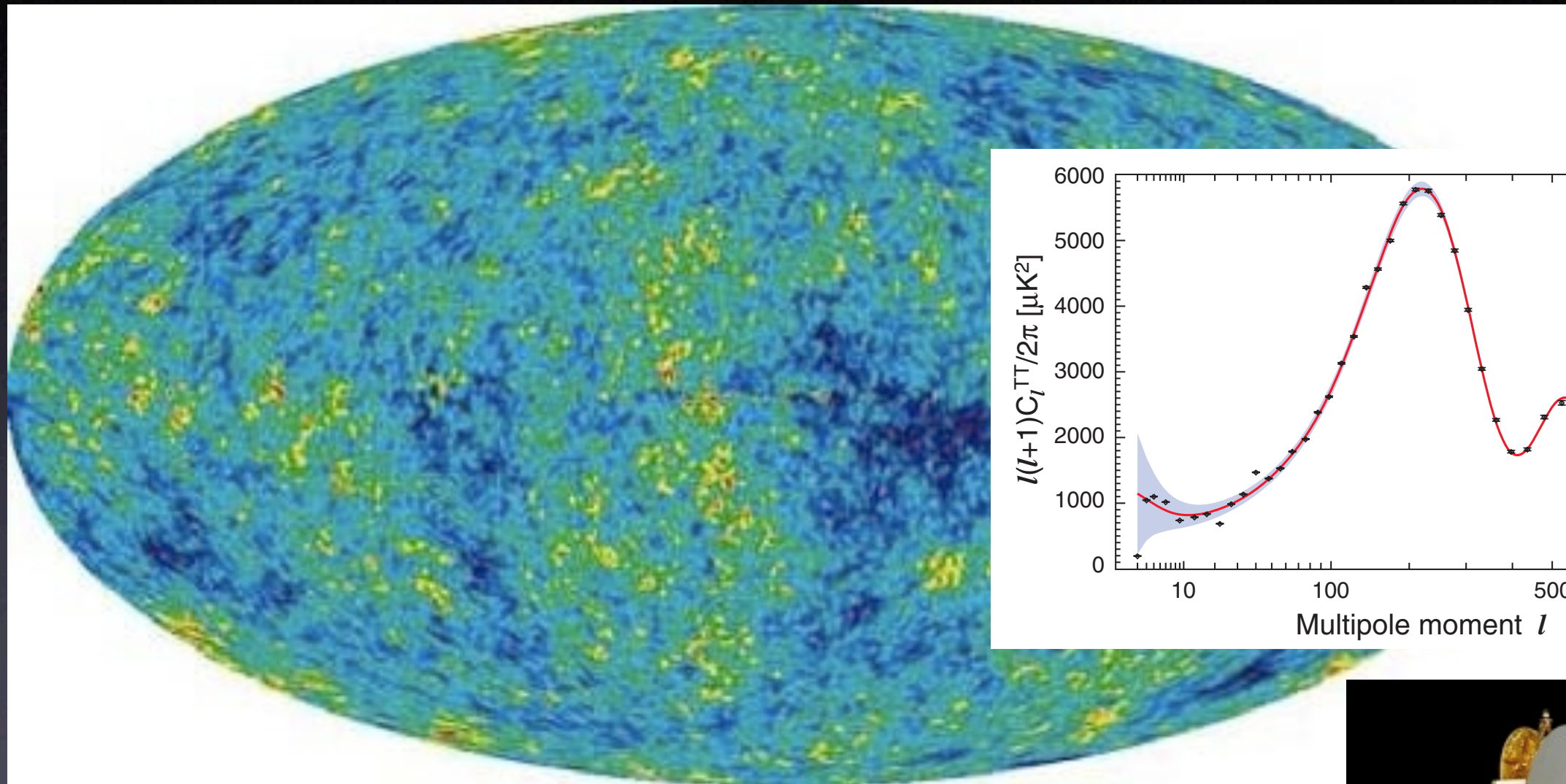


# Lifetime

- At least of the order of age of the universe  
14Gyr
- Beyond that, it depends on decay modes,  
branching fractions, all model-dependent



# Cosmological scales

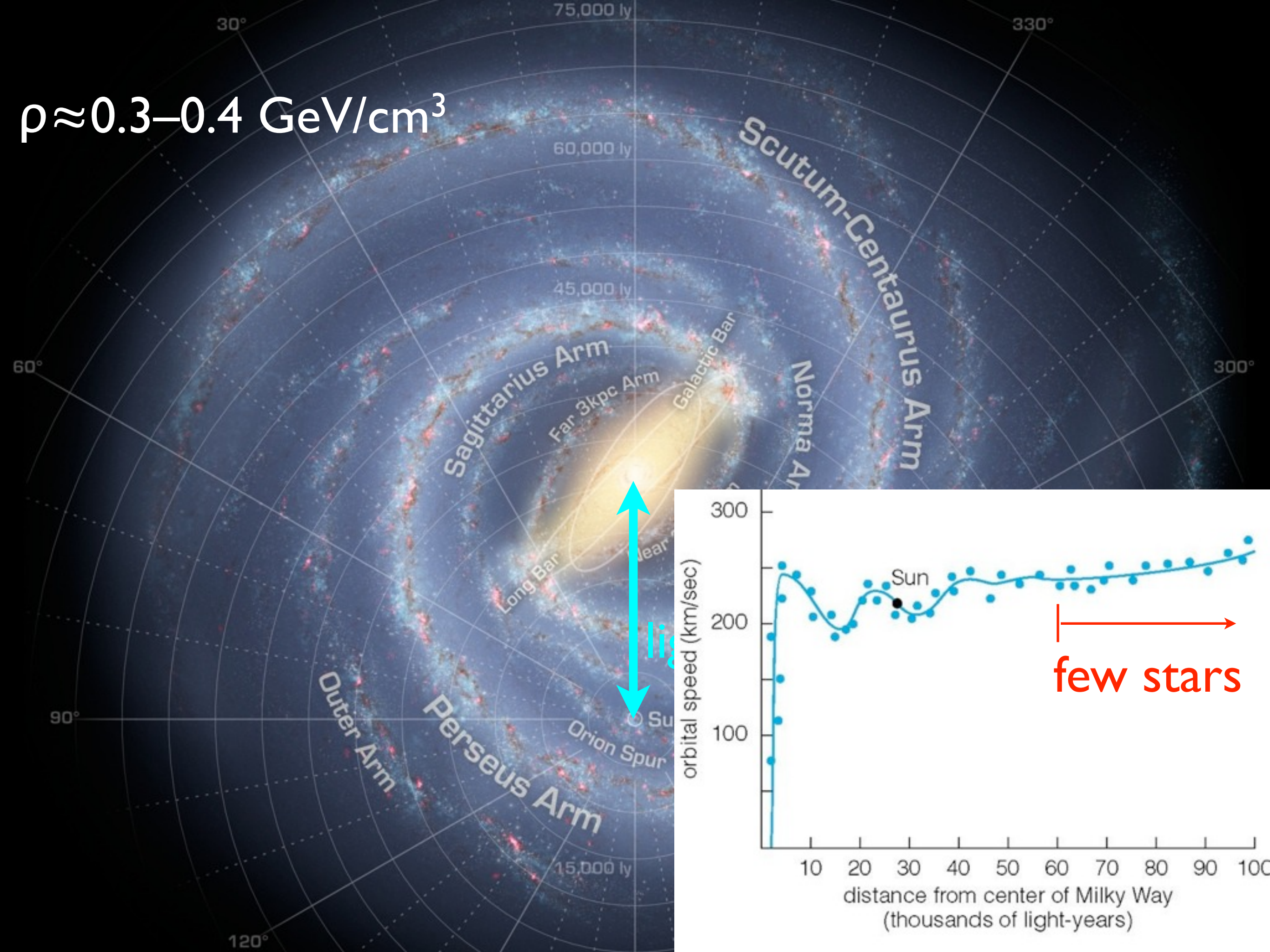


$$\frac{\text{matter}}{\text{all atoms}} = 5.70^{+0.39}_{-0.61}$$





$$\rho \approx 0.3 - 0.4 \text{ GeV/cm}^3$$



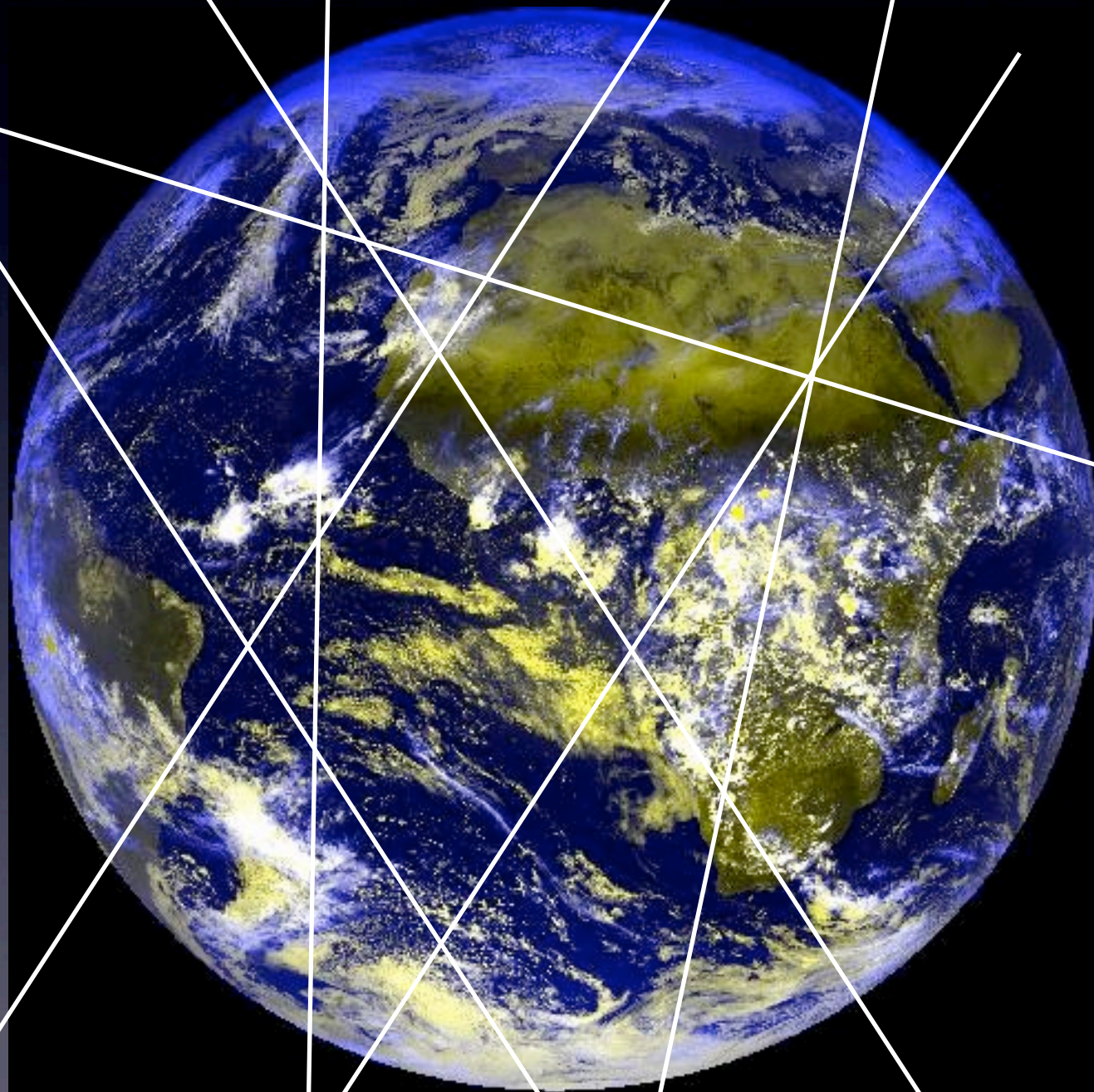




# WIMP paradigm



# MACHOs to WIMP



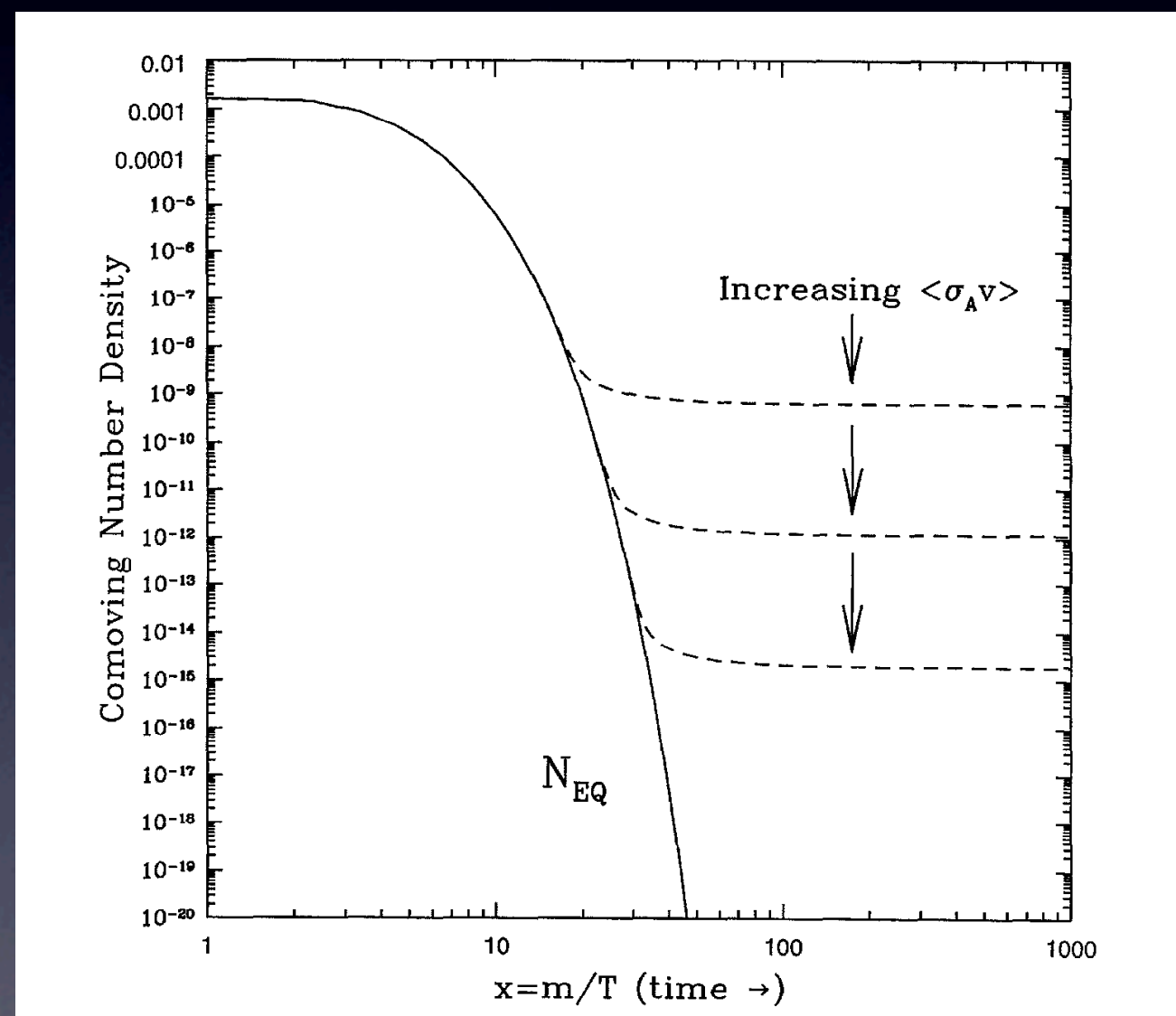
- *The dominant paradigm:*  
**WIMP** (Weakly Interacting  
Massive Particle)
- *Stable heavy particle  
produced in early  
Universe, left-over from  
near-complete annihilation*

$$\Omega_M = \frac{0.756(n+1)x_f^{n+1}}{g^{1/2}\sigma_{ann}M_{Pl}^3} \frac{3s_0}{8\pi H_0^2} \approx \frac{\alpha^2/(TeV)^2}{\sigma_{ann}}$$



# thermal relic

- thermal equilibrium when  $T > m_\chi$
- Once  $T < m_\chi$ , no more  $\chi$  created
- if stable, only way to lose them is annihilation
- but universe expands and  $\chi$  get dilute
- at some point they can't find each other
- their number in comoving volume "frozen"





# Freeze-out

- WIMP freezes out when the annihilation rate drops below the expansion rate
- Yield  $Y=n/s$  constant under expansion
- stronger annihilation  $\Rightarrow$  less abundance

$$H \approx g_*^{1/2} \frac{T^2}{M_{Pl}}$$

$$\Gamma_{\text{ann}} \approx \langle \sigma_{\text{ann}} v \rangle n$$

$$H(T_f) = \Gamma_{\text{ann}}$$

$$n \approx g_*^{1/2} \frac{T_f^2}{M_{Pl} \langle \sigma_{\text{ann}} v \rangle}$$

$$s \approx g_* T^3$$

$$Y = \frac{n}{s} \approx g_*^{-1/2} \frac{1}{M_{Pl} T_f \langle \sigma_{\text{ann}} v \rangle}$$

$$\Omega_\chi = \frac{m_\chi Y s_0}{\rho_c}$$

$$\approx g_*^{-1/2} \frac{x_f}{M_{Pl}^3 \langle \sigma_{\text{ann}} v \rangle} \frac{s_0}{H_0^2}$$



# Order of magnitude

- “Known”  $\Omega_\chi=0.23$  determines the WIMP annihilation cross section
- simple estimate of the annihilation cross section
- weak-scale mass!!!

$$\Omega_\chi \approx g_*^{-1/2} \frac{x_f}{M_{Pl}^3 \langle \sigma_{\text{ann}} v \rangle} \frac{s_0}{H_0^2}$$

$$\langle \sigma_{\text{ann}} v \rangle \approx \frac{1.12 \times 10^{-10} \text{GeV}^{-2} x_f}{g_*^{1/2} \Omega_\chi h^2}$$

$$\sim 10^{-9} \text{GeV}^{-2}$$

$$\langle \sigma_{\text{ann}} v \rangle \approx \frac{\pi \alpha^2}{m_\chi^2}$$

$$m_\chi \approx 300 \text{ GeV}$$

WIMP miracle



# therma

- Solve the Boltzmann eq

$$\frac{dn_1}{dt} + 3Hn_1 = - \int \prod_{i=1}^4 \frac{d^3 p_i}{(2\pi)^3 2E_i} |\mathcal{M}|^2$$

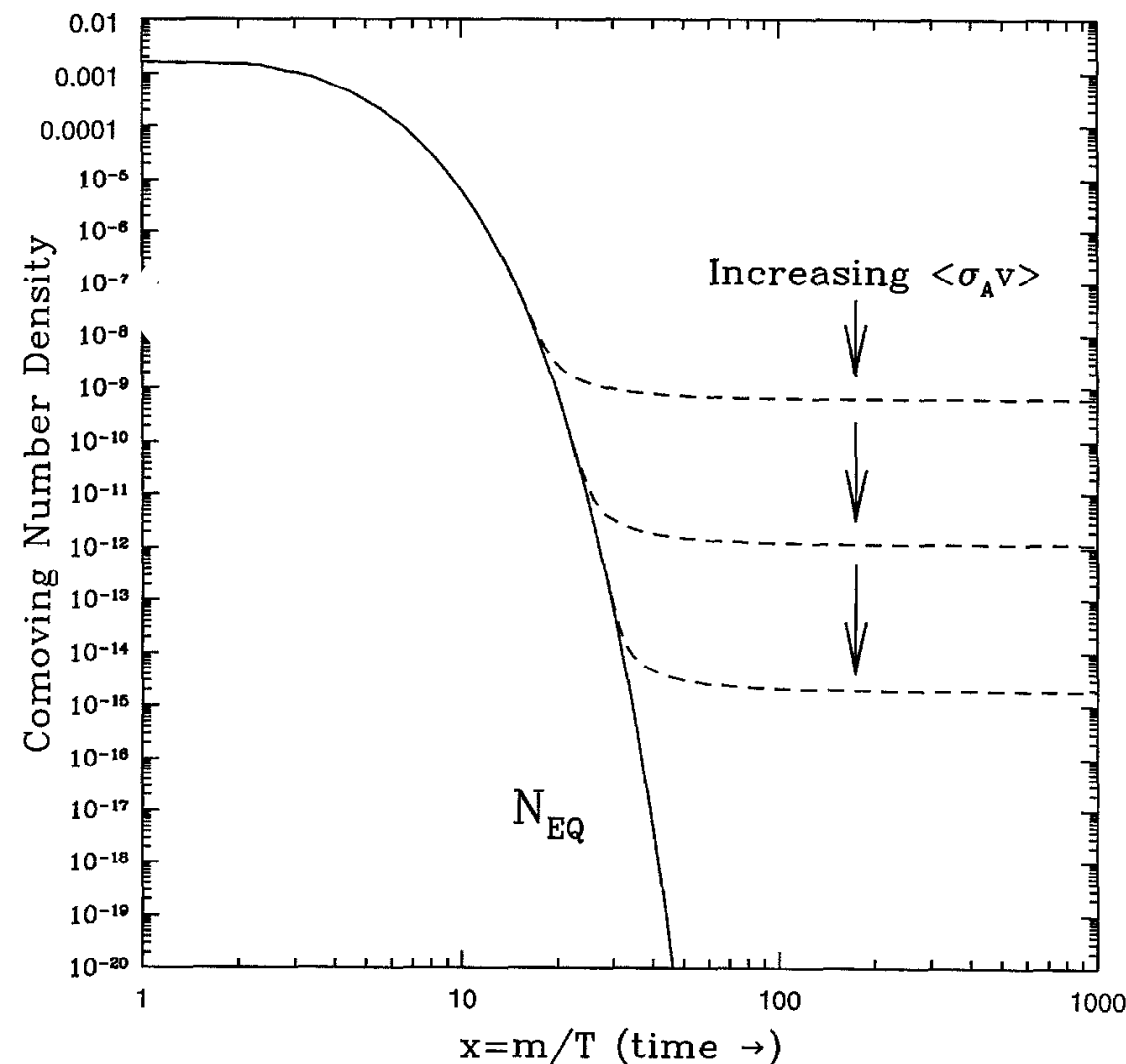
$$[f_1 f_2 (1 \pm f_3)(1 \pm f_4) -$$

- assume Maxwell distribution,  $\Gamma = \mathcal{L} = \chi$ ,  $E_1 = E_2 = m_\chi$

$$\frac{dn}{dt} + 3Hn = -\langle \sigma_{\text{ann}} v \rangle (n^2 - n_{eq}^2)$$

- Note momentum dependence may be important close to thresholds, resonances
- reproduce the estimate with

$$x_f \approx 24 + \ln \frac{m_\chi}{100 \text{ GeV}} + \ln \frac{\langle \sigma_{\text{ann}} v \rangle}{10^{-9} \text{ GeV}^{-2}} - \frac{1}{2} \ln \frac{g_*}{100}$$





# WIMP

- A stable particle at the weak scale with “EM-strength” coupling naturally gives the correct abundance
- This is where we expect new particles because of the hierarchy problem!
- Many candidates of this type: SUSY, little Higgs with  $T$ -parity, Universal Extra Dimensions, etc
- If so, we may even create dark matter at accelerators



# Minimal Model

- Dark Matter clearly a new degree of freedom
- The smallest degree of freedom you can add to the QFT is a real Klein-Gordon field  
S: **dof=1**
- assign odd  $Z_2$  parity to S, everything else even
- Most general renormalizable coupling

$$L_S = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{k}{2} |H|^2 S^2 - \frac{h}{4!} S^4.$$



- correct Dark Matter abundance 5.5–1800 GeV
- evades direct detection limits  $>60$  GeV
- satisfies triviality/instability limits from RGE
- consistent with precision electroweak data

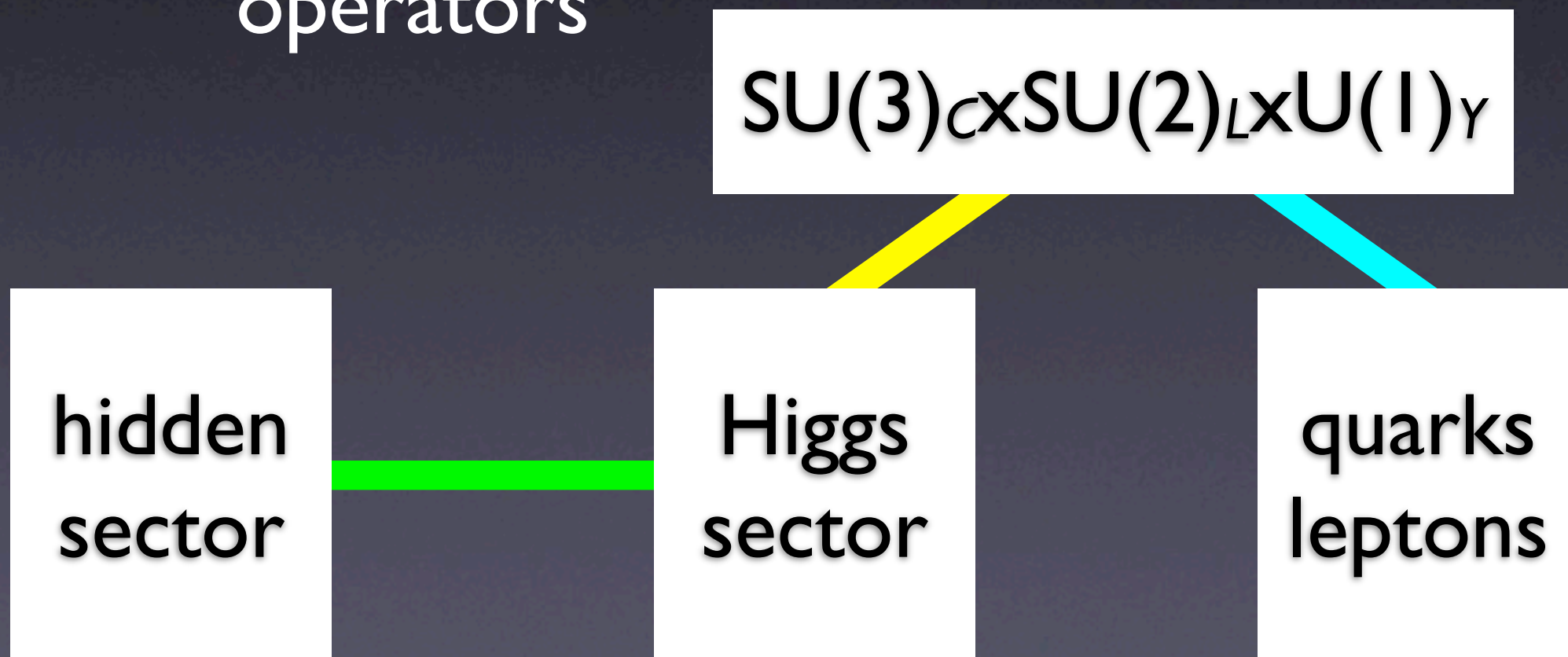




# Higgs as a portal

$$L_S = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{k}{2} |H|^2 S^2 - \frac{h}{4!} S^4.$$

- having discovered the Higgs?
- Higgs boson may connect the Standard Model to other “sectors” via lowest-dim operators

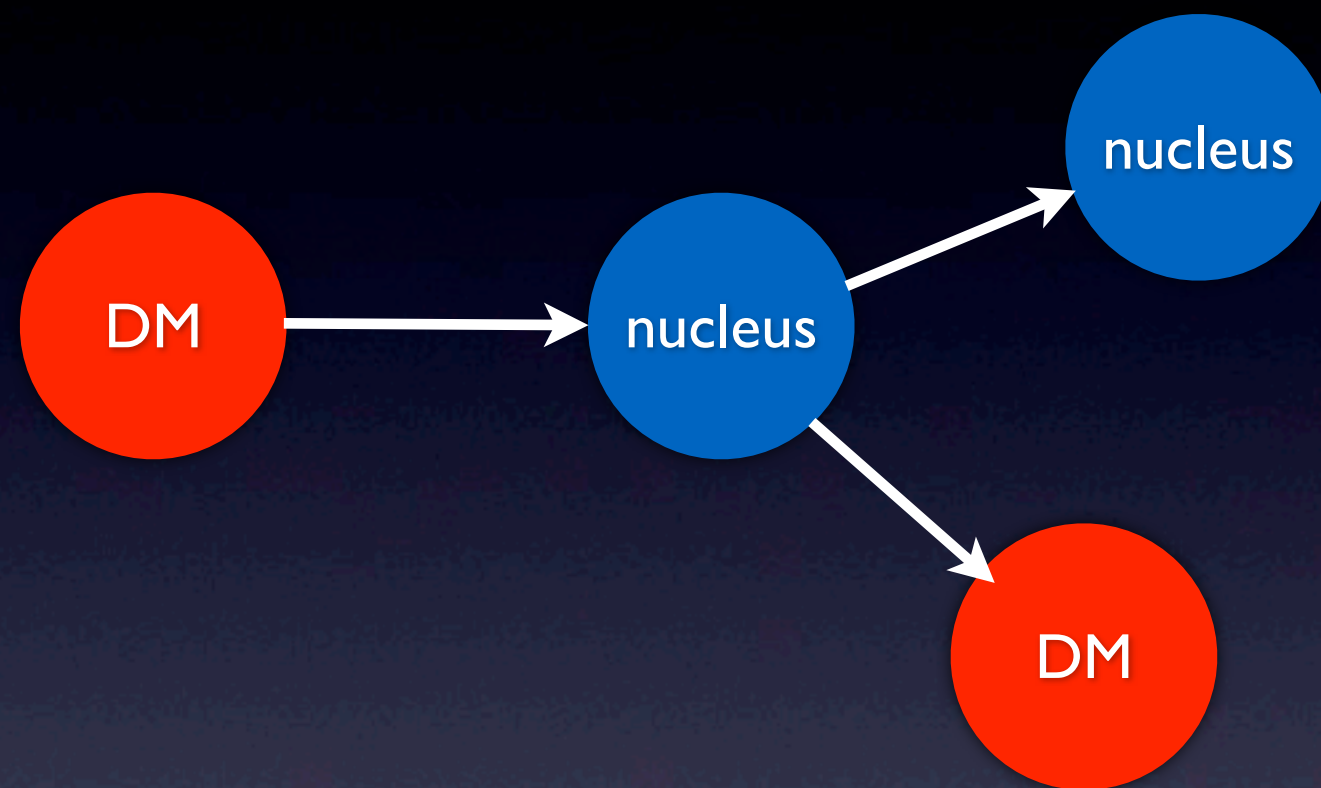


$$\mathcal{L} = \mathcal{O}_{hidden} H^\dagger H$$



# basic idea

- maximum energy transfer to nucleus when  $m_\chi \sim M_A$
- energy of the nucleus leads to a combination of
  - ionization
  - phonon
  - scintillation

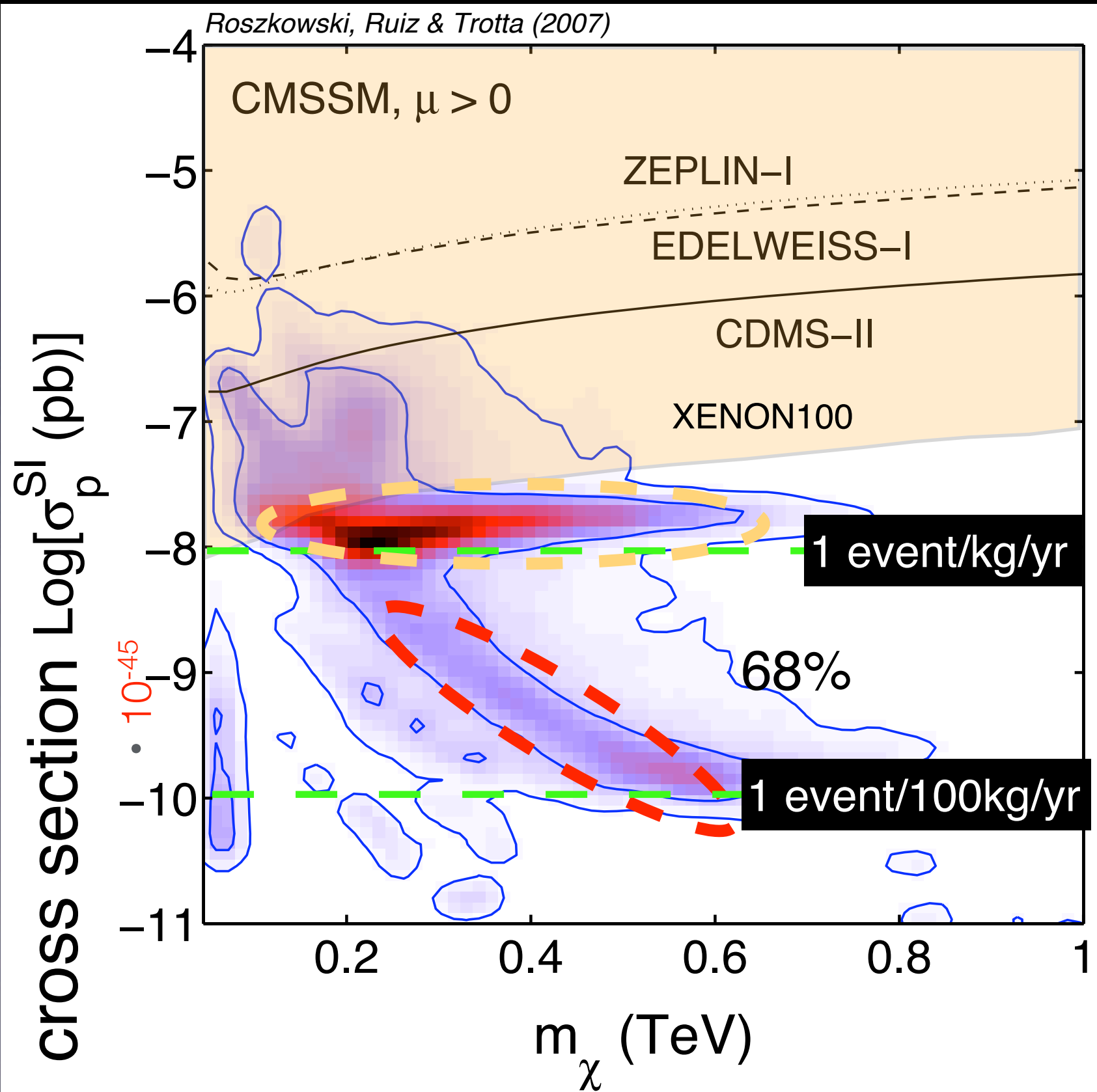


$$E_f = \frac{1}{2} m_\chi \frac{m_\chi M_A}{(m_\chi + M_A)^2} 2(1 - \cos \hat{\theta})$$



# Sensitivity and SUSY Parameter

Masaki Yamashita



CMSSM in 2007  
[hep-ph 0705.2012v1](#)  
Roszkowski et al.

near future

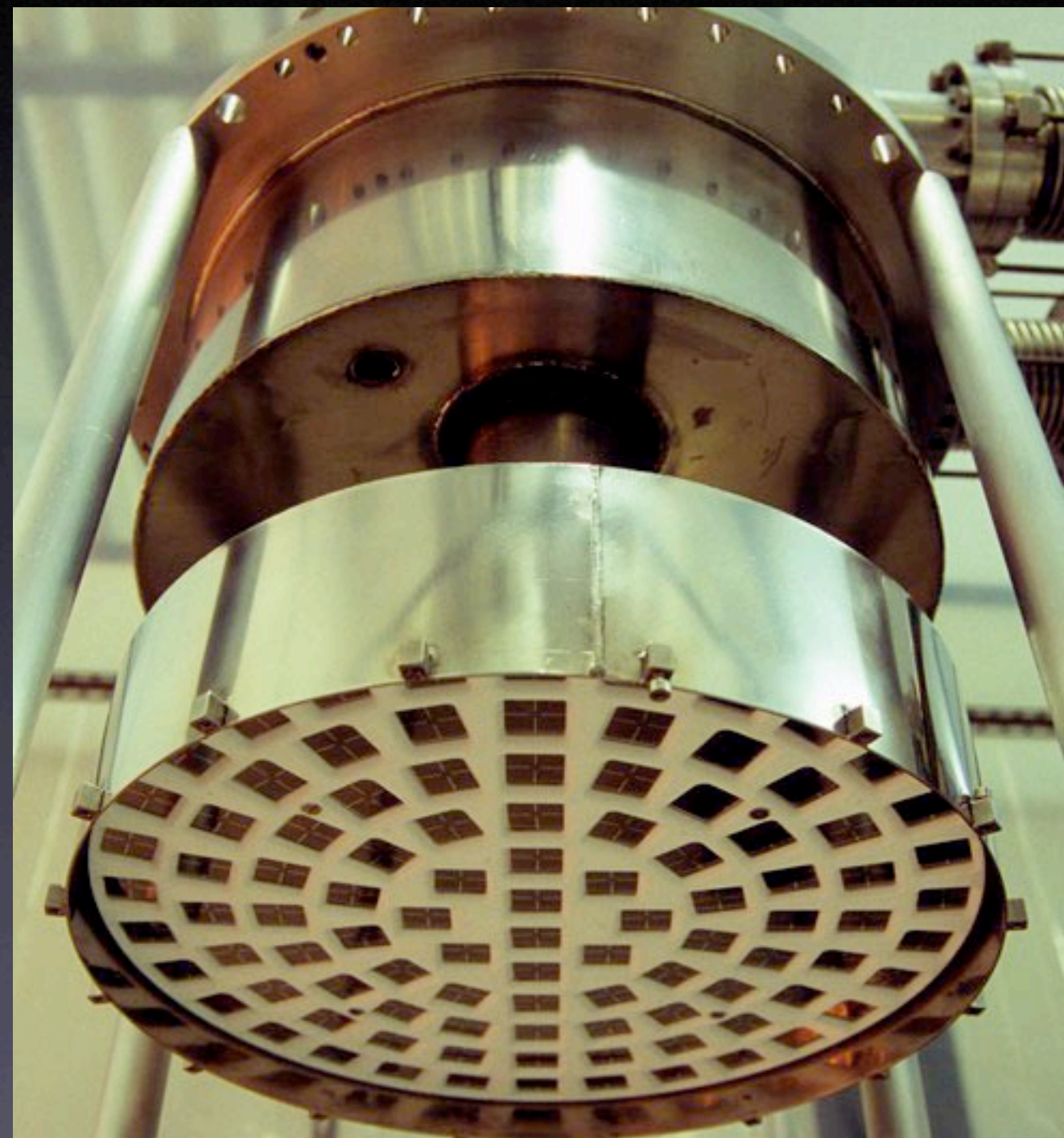
Super CDMS, XENON100, LUX,  
XMASS, COUPP, CRESST-II,  
EDELWEISS-II, ZEPLIN-III,...

Future experiments

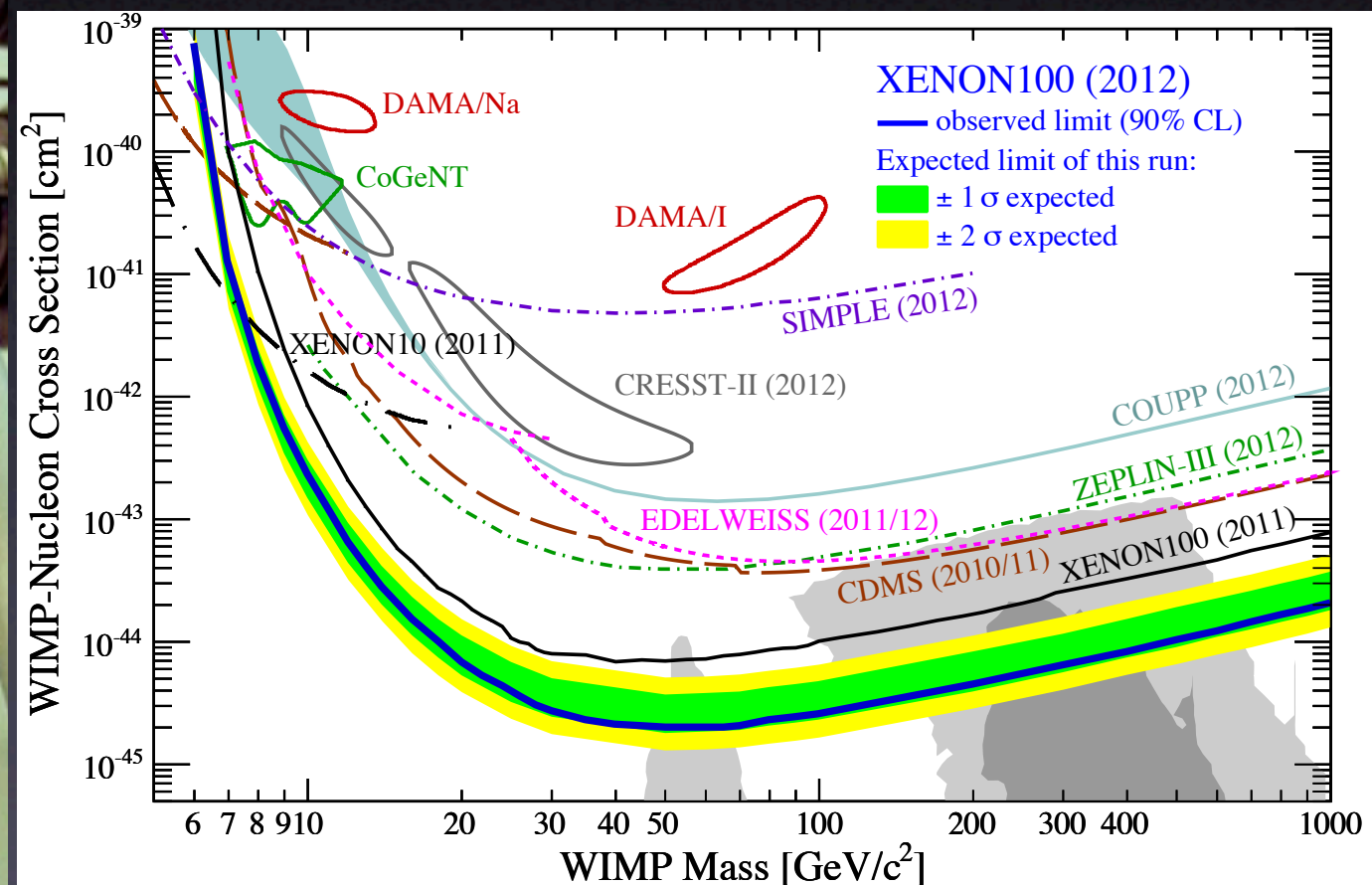
SuperCDMS1t, XENON1t, LZ, Darwin  
ArDM, XMASS 20T, ...



# direct search



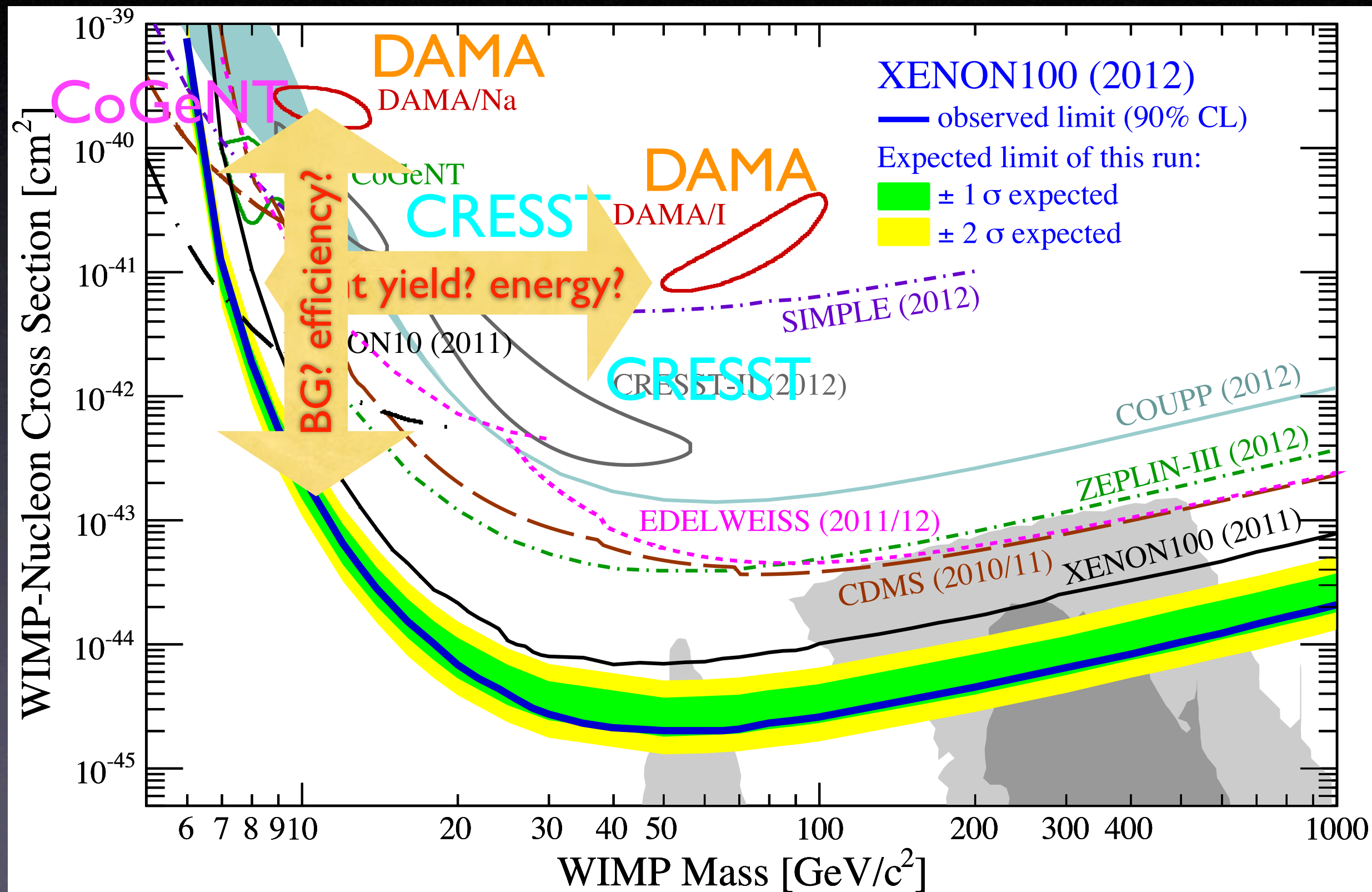
XENON 100



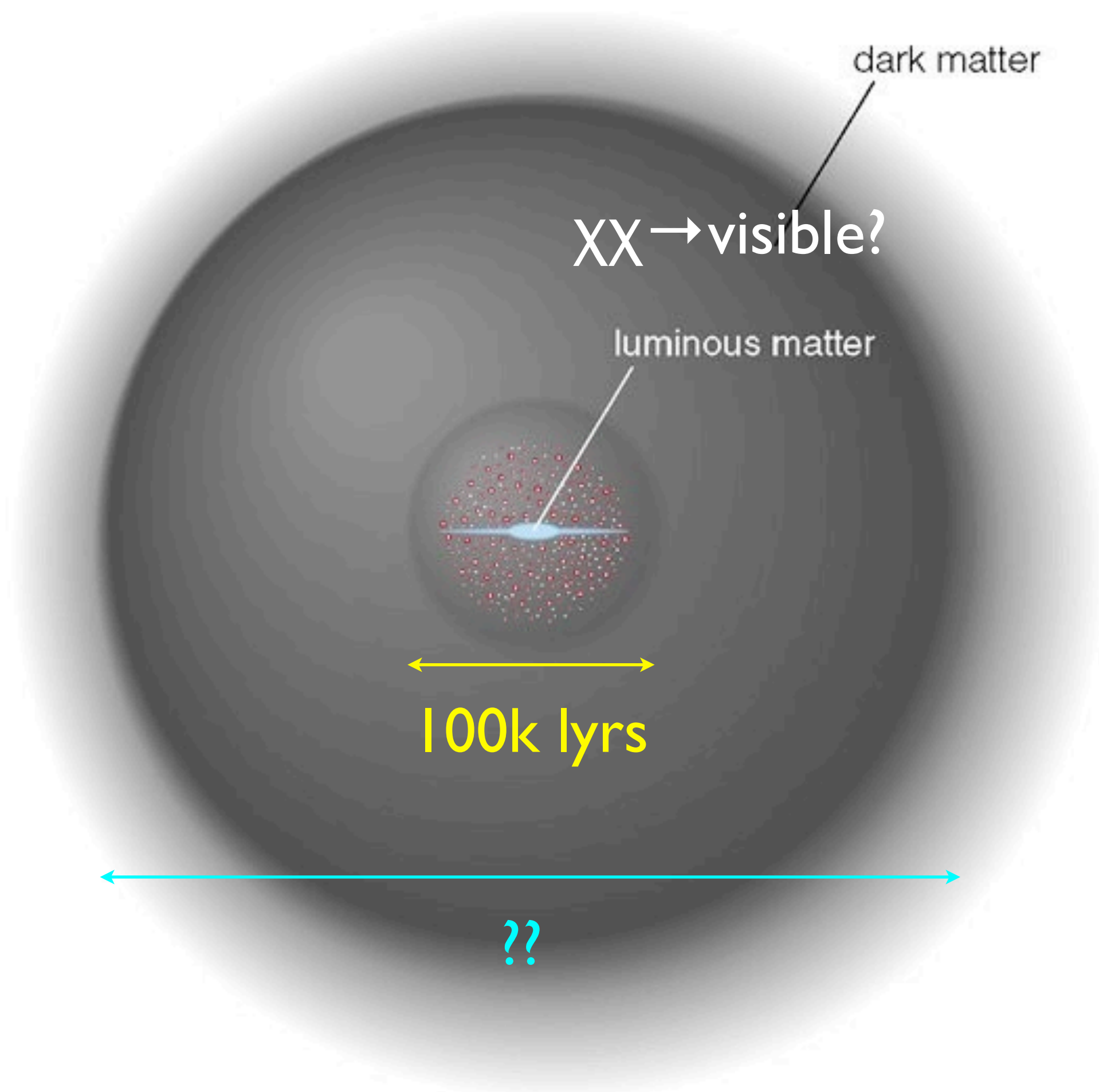
cf.  $\sigma \sim 10^{-36} \text{ cm}^2$   
for a heavy neutrino



# confusing

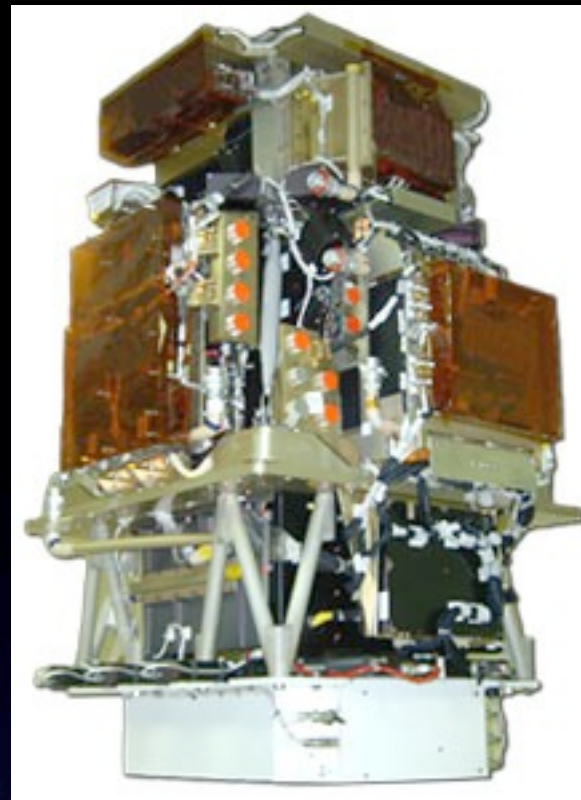




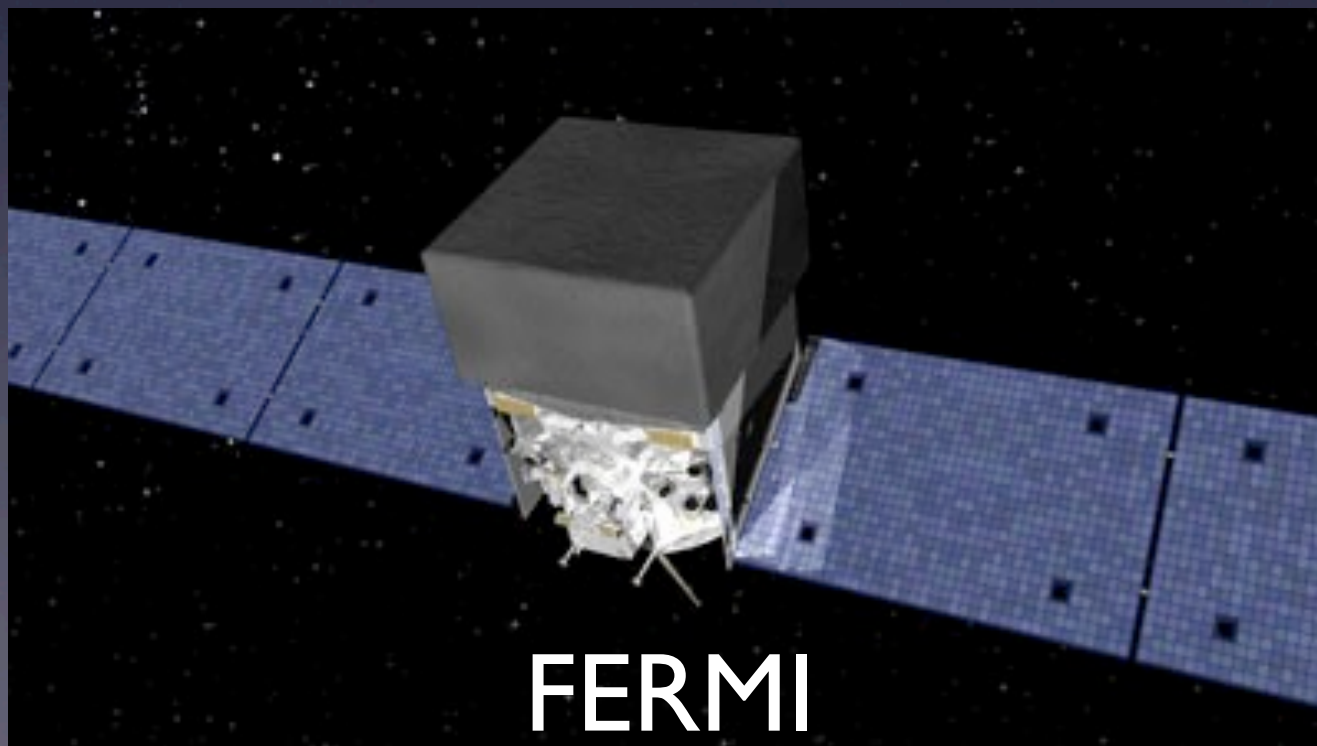
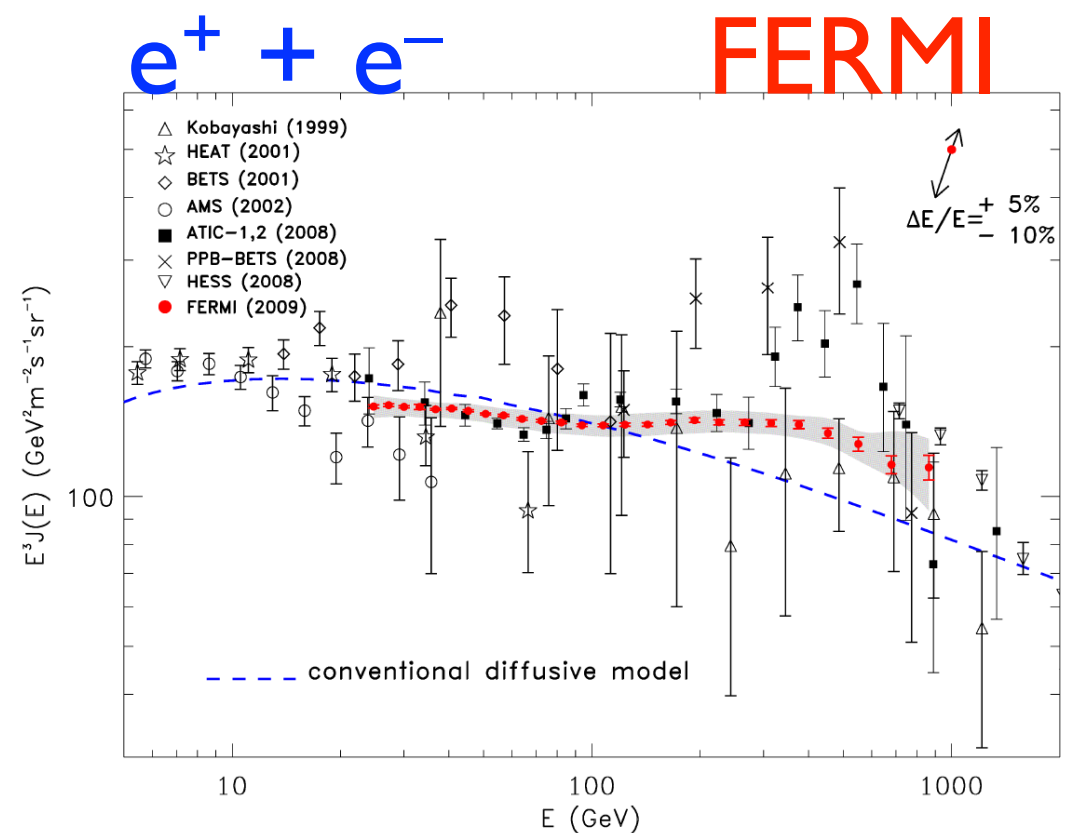
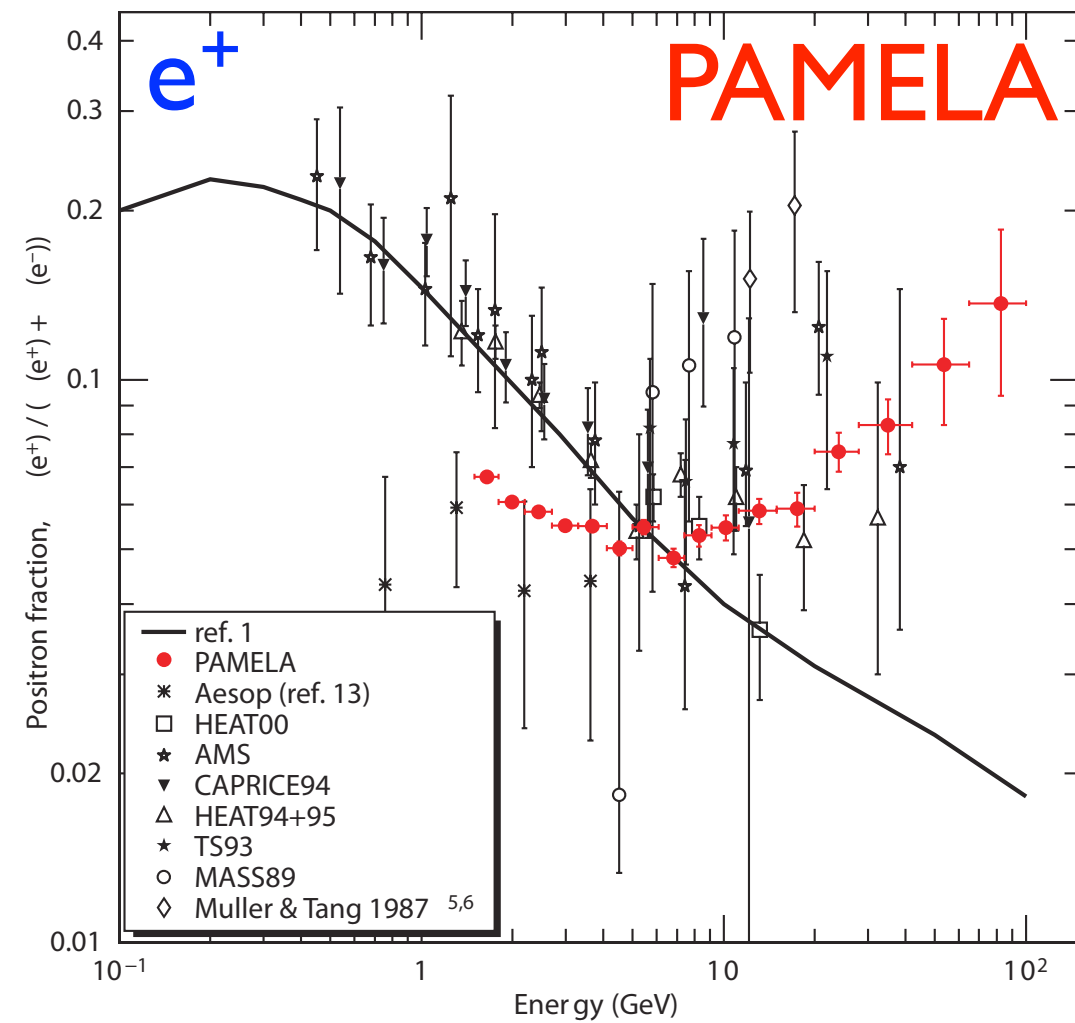




# PAMELA



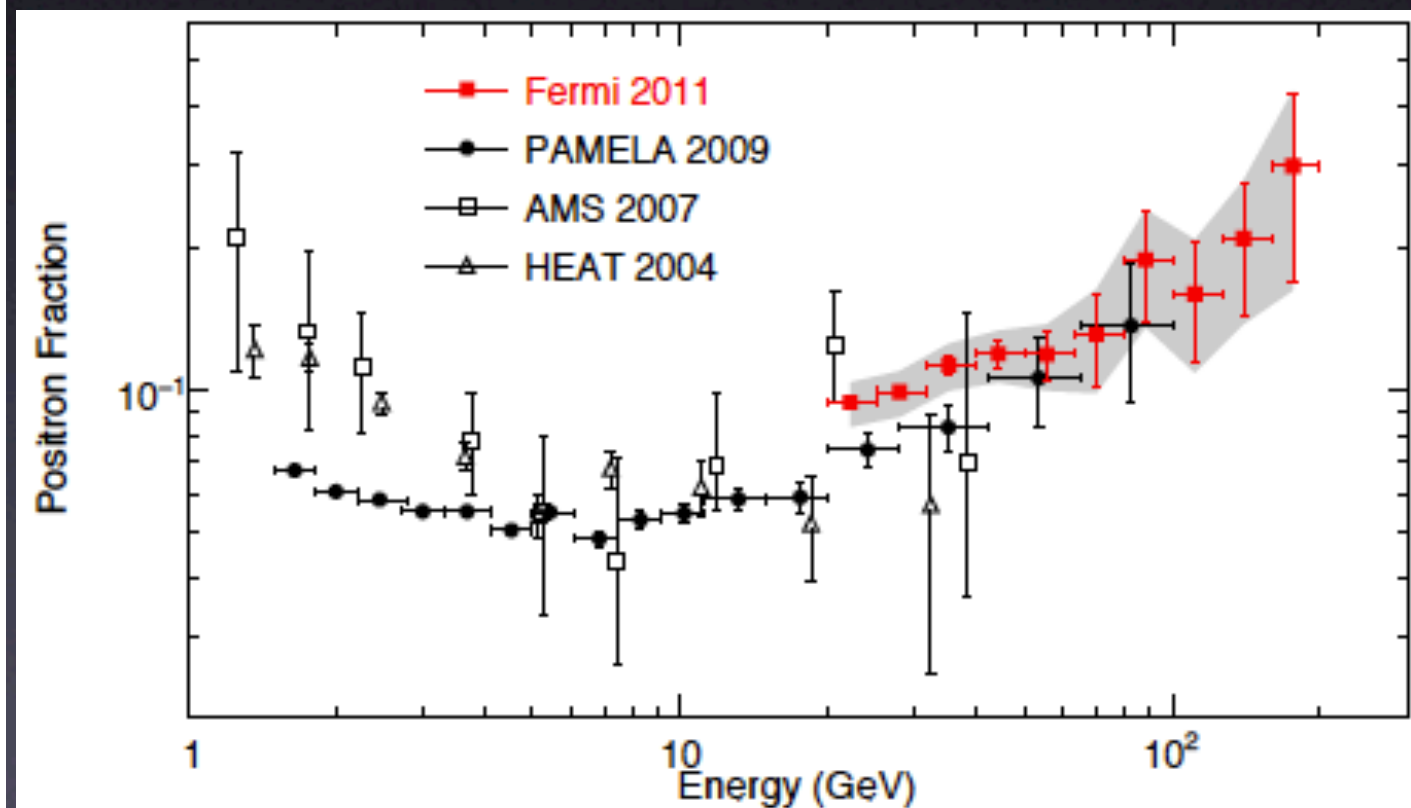
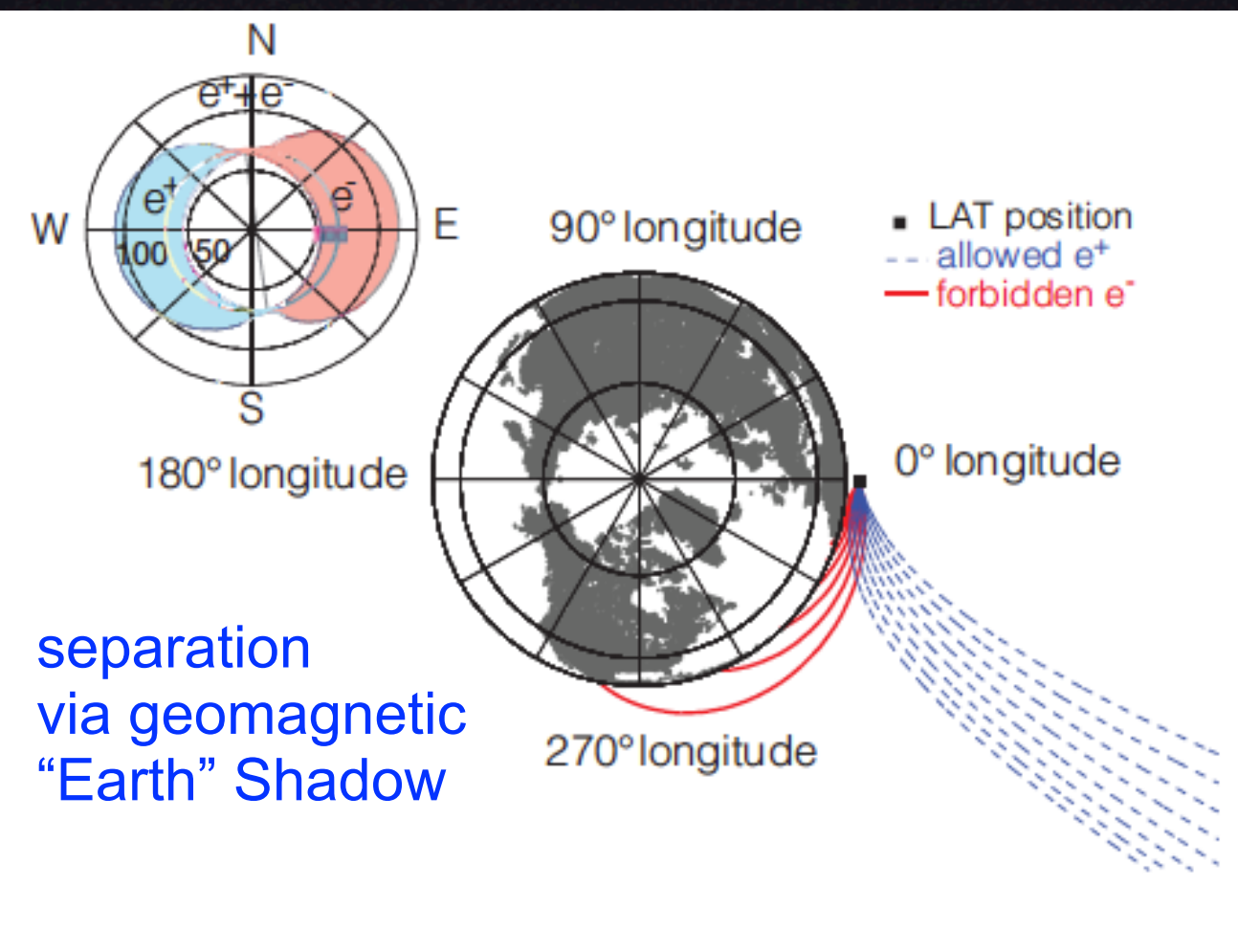
dark matter annihilation or decay  
in the galactic halo?



# FERMI

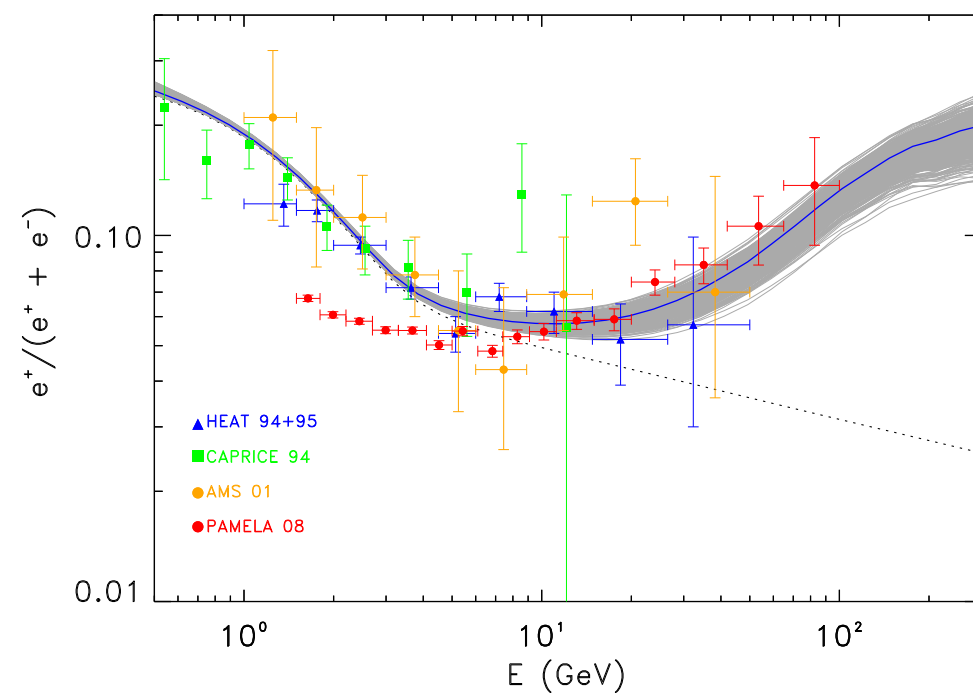
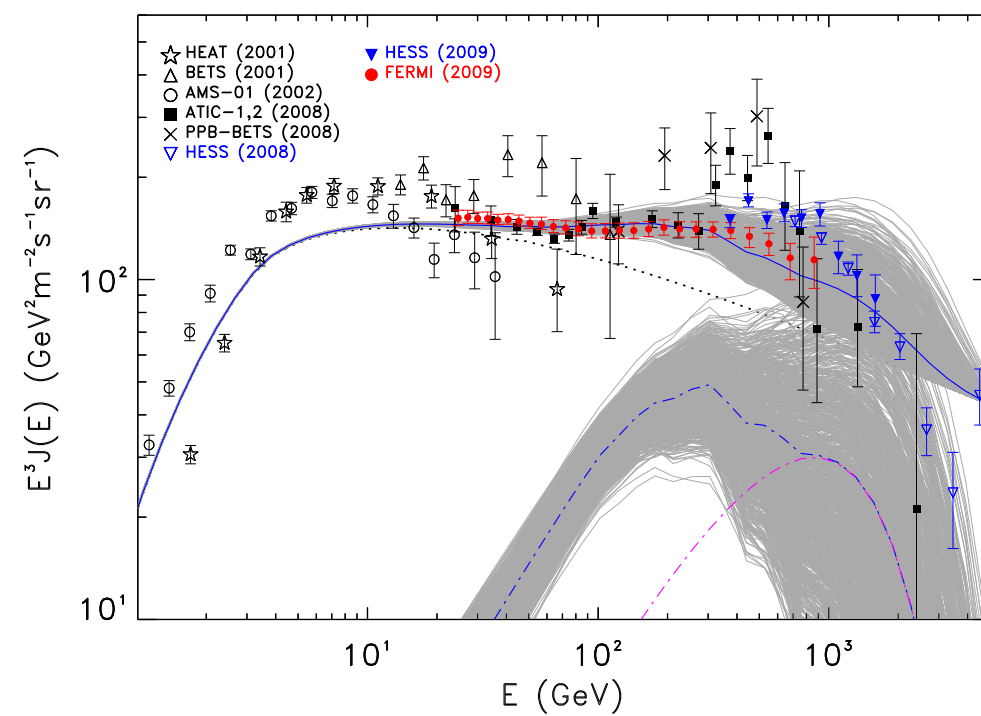


# rise in $e^+$ fraction confirmed by Fermi



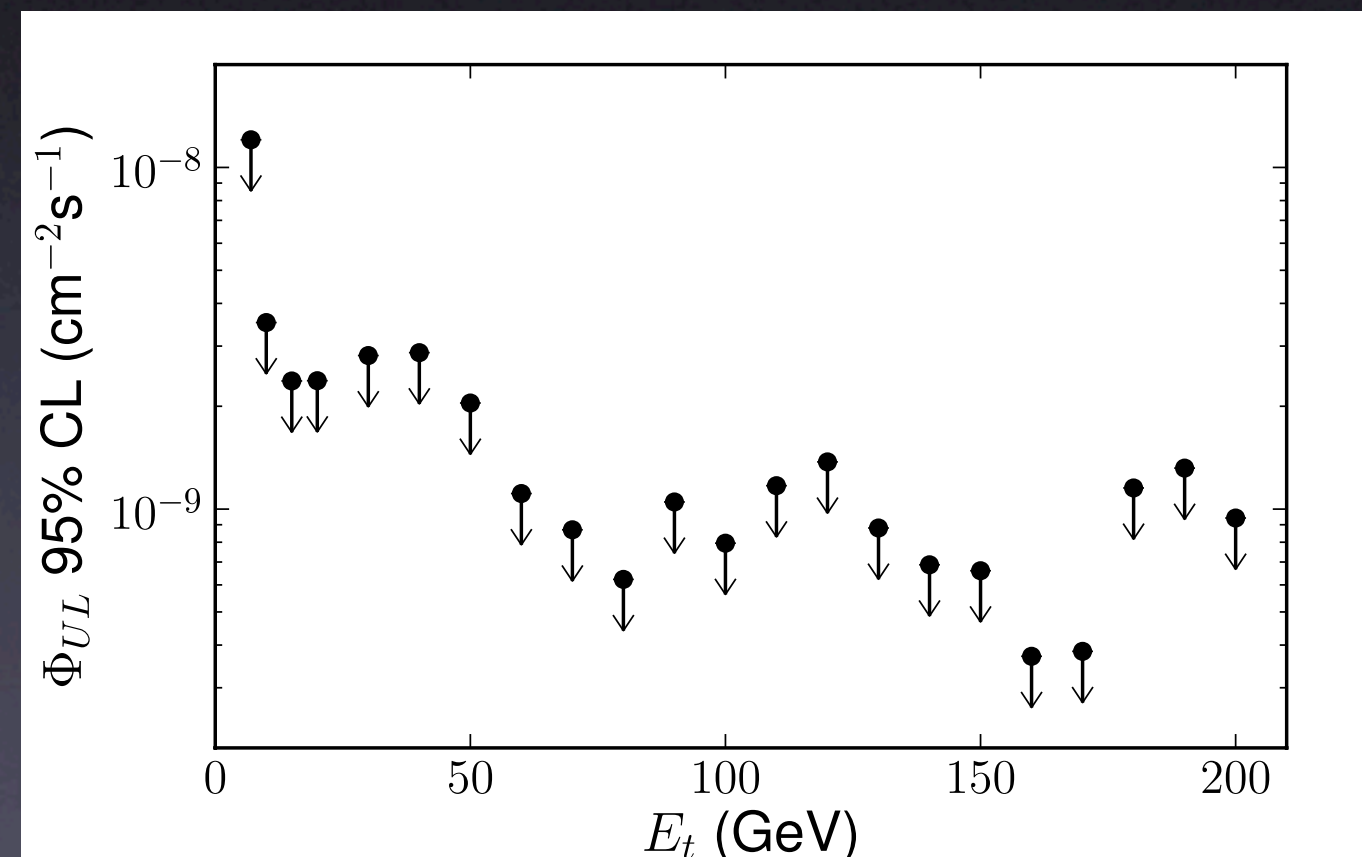
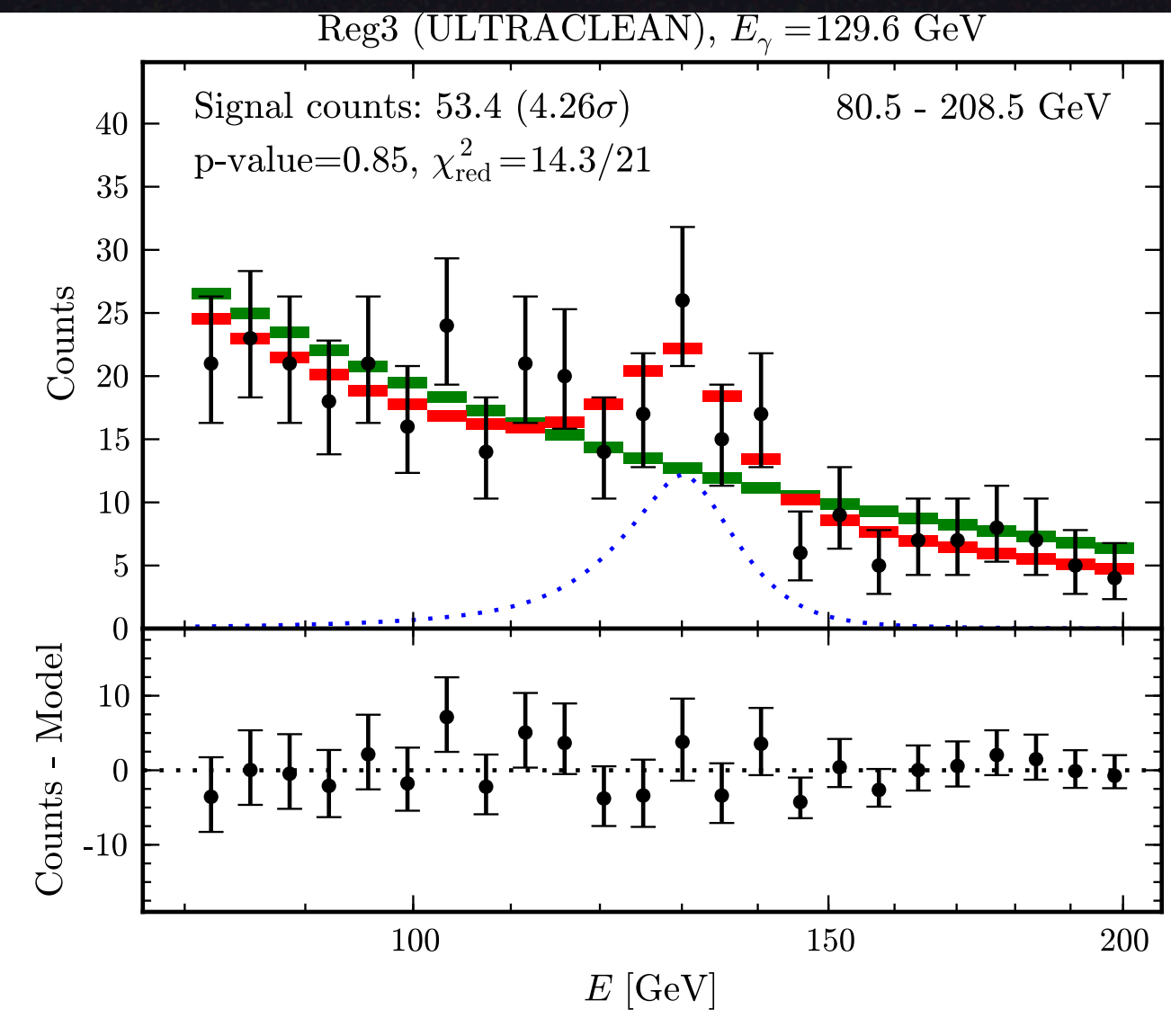
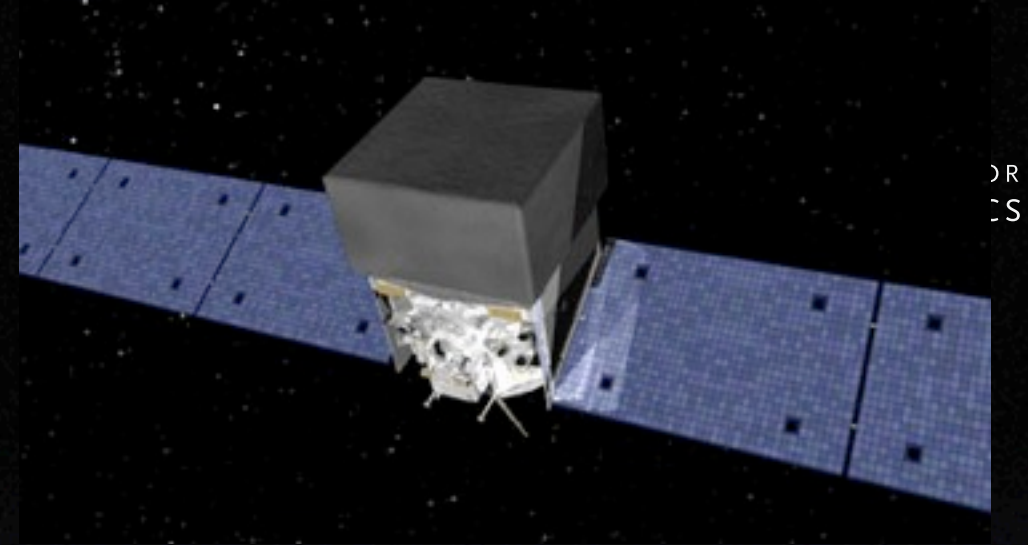


# pulsars?





# bump?



Christoph Weniger

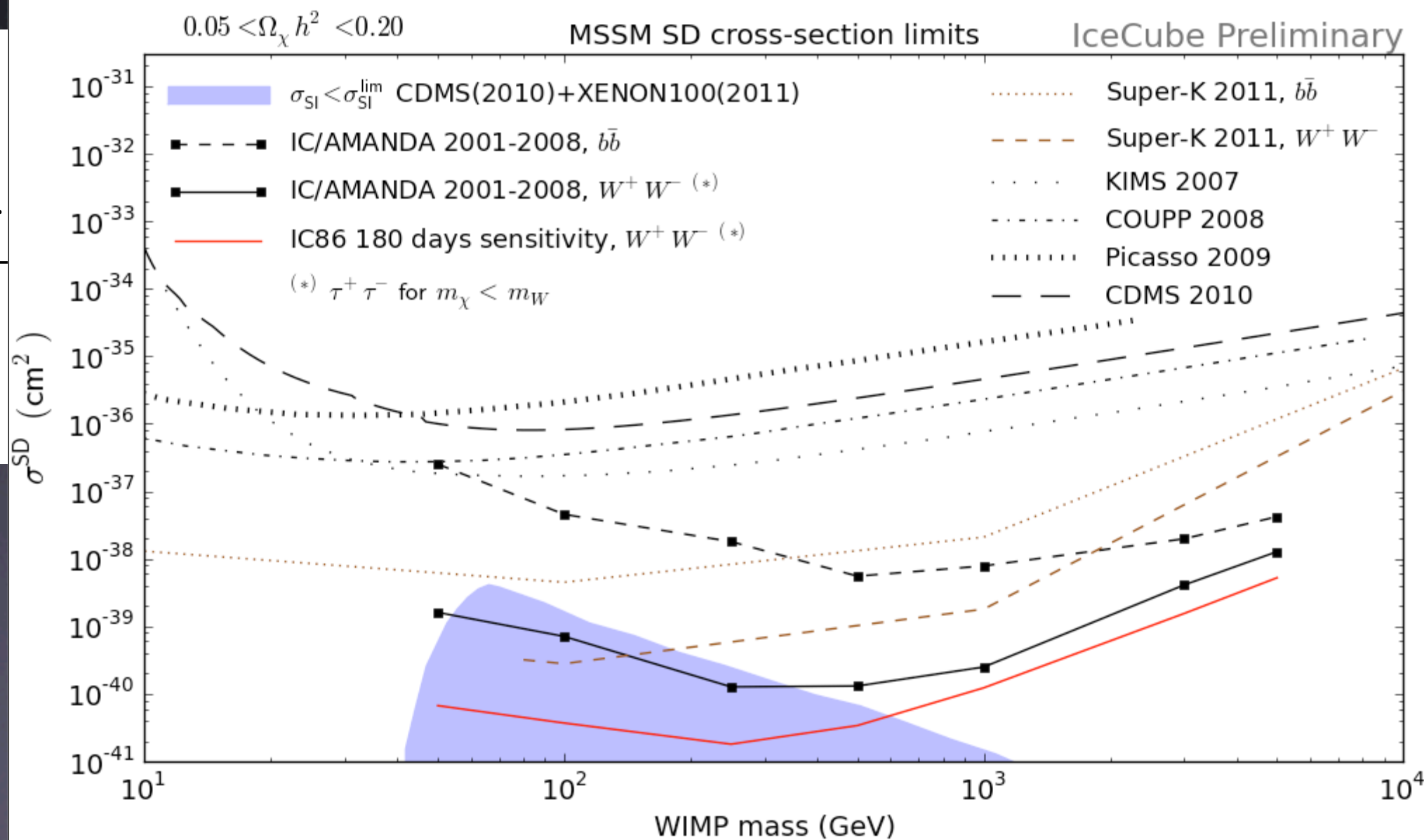
Fermi-LAT collab



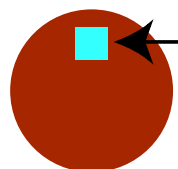
# Finding Dark Matter

## Indirect method

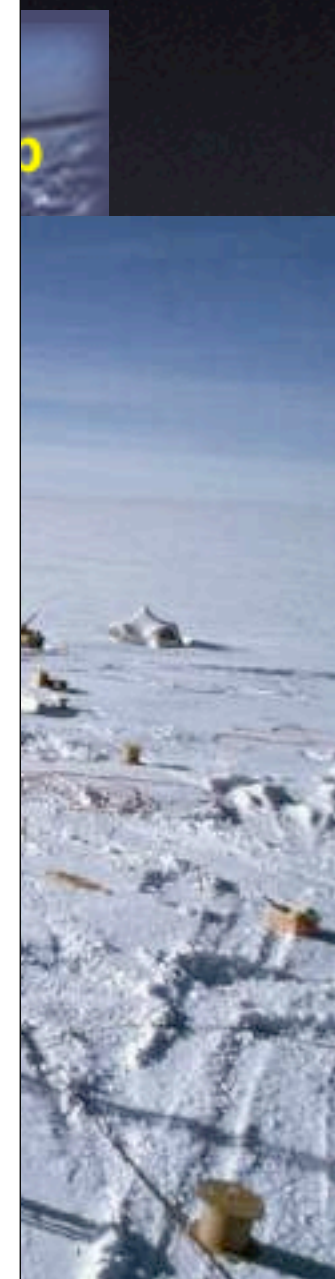
### Indirect search from the Sun: spin dependent x-section



$\nu$  detector



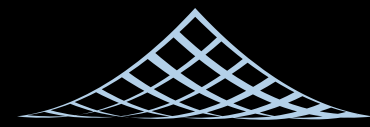
Earth







# Hadron Collider (LHC)



BERKELEY CENTER FOR  
THEORETICAL PHYSICS

*Recreating Big Bang*



*running!*

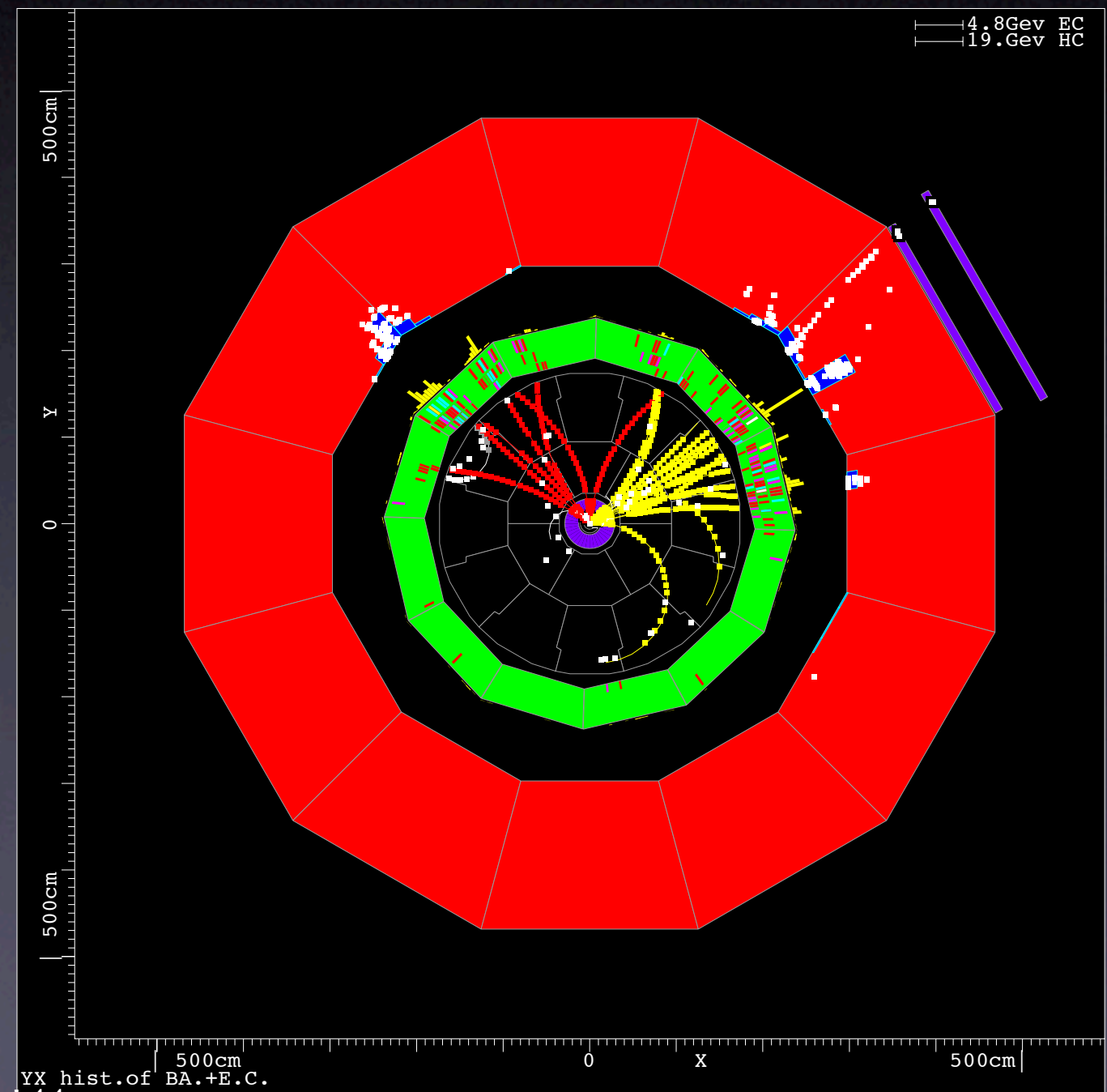


# Producing Dark Matter in the laboratory

- Mimic Big Bang in the lab
- Hope to create invisible Dark Matter particles
- Look for events where energy and momenta are unbalanced

“missing energy”  $E_{\text{miss}}$

- **Something** is escaping the detector  
⇒ **Dark Matter!?**





# How do we know what Dark Matter *is*?

- cosmological measurement of dark matter

- abundance  $\propto \sigma_{\text{ann}}^{-1}$

- detection experiments

- scattering cross section

- production at colliders

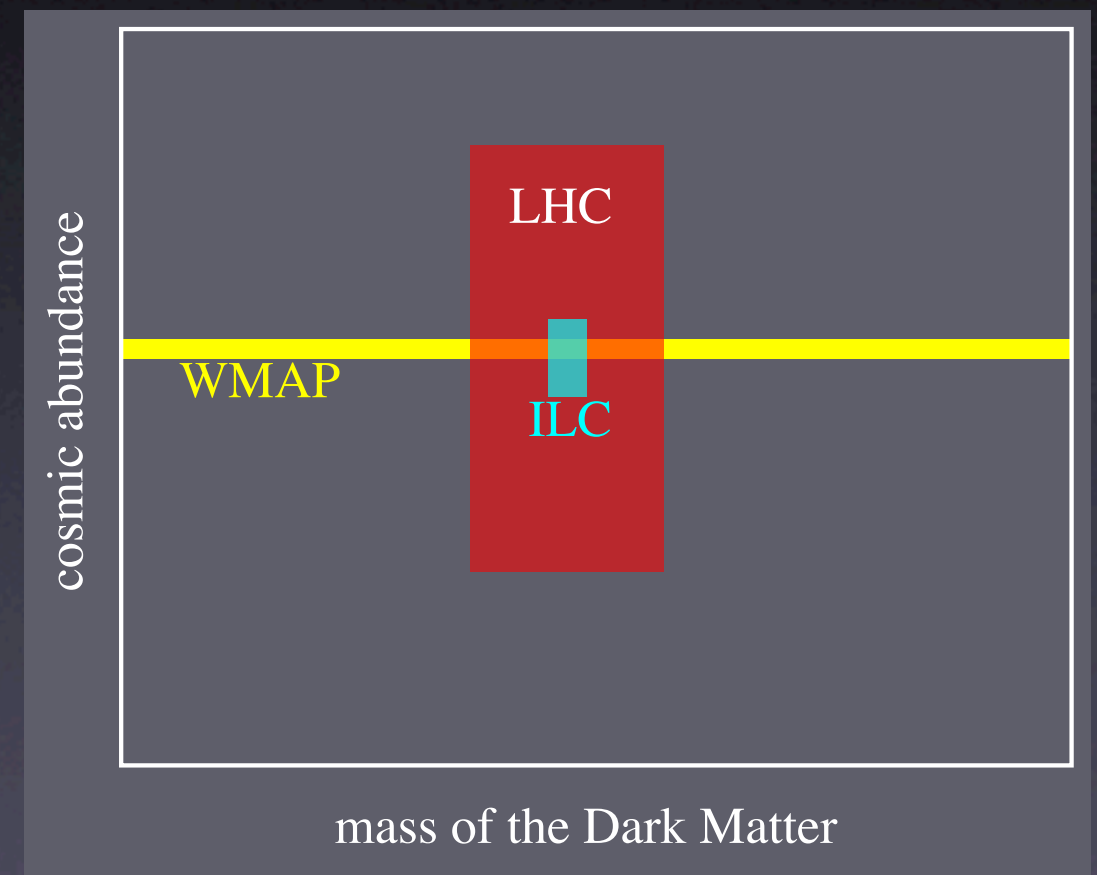
- mass, couplings

- can calculate cross sections

- If they agree with each other:

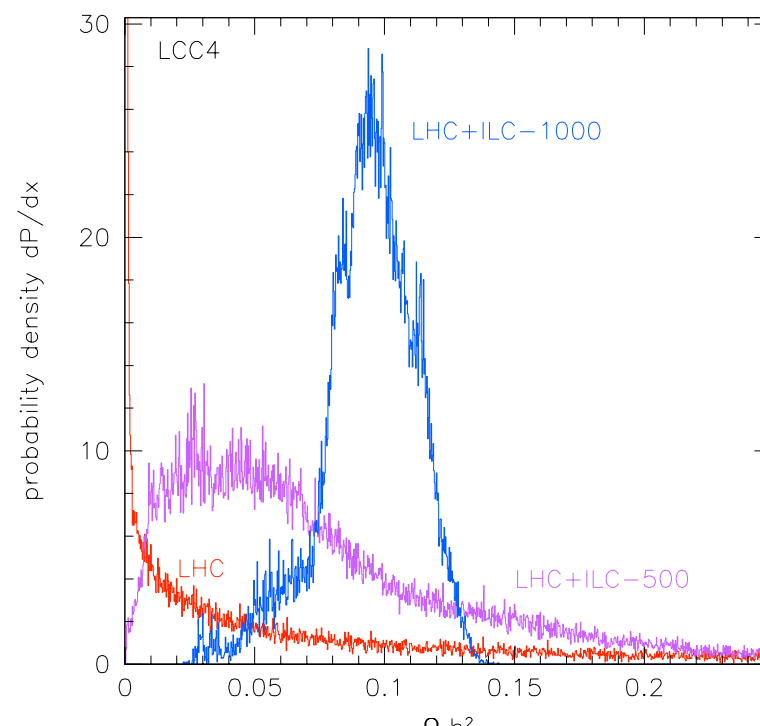
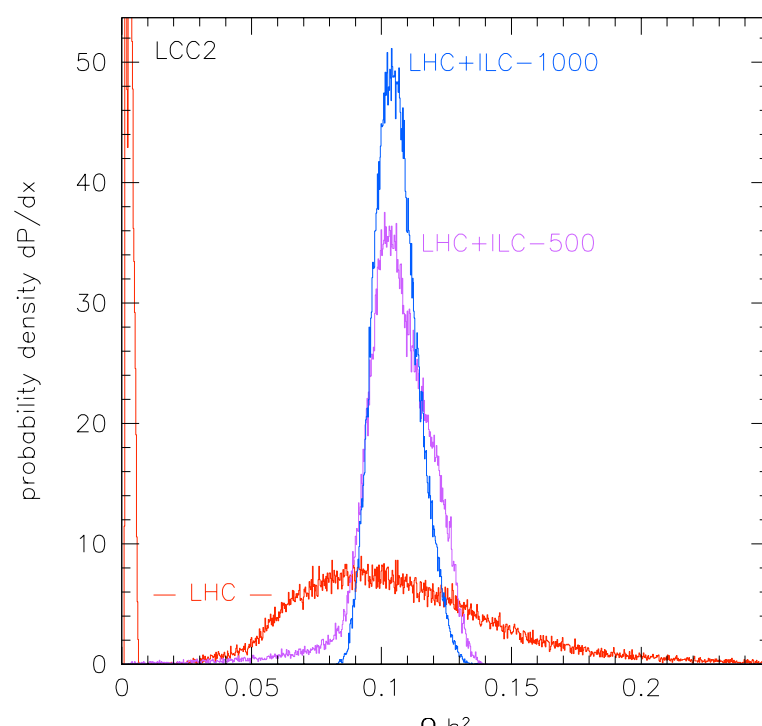
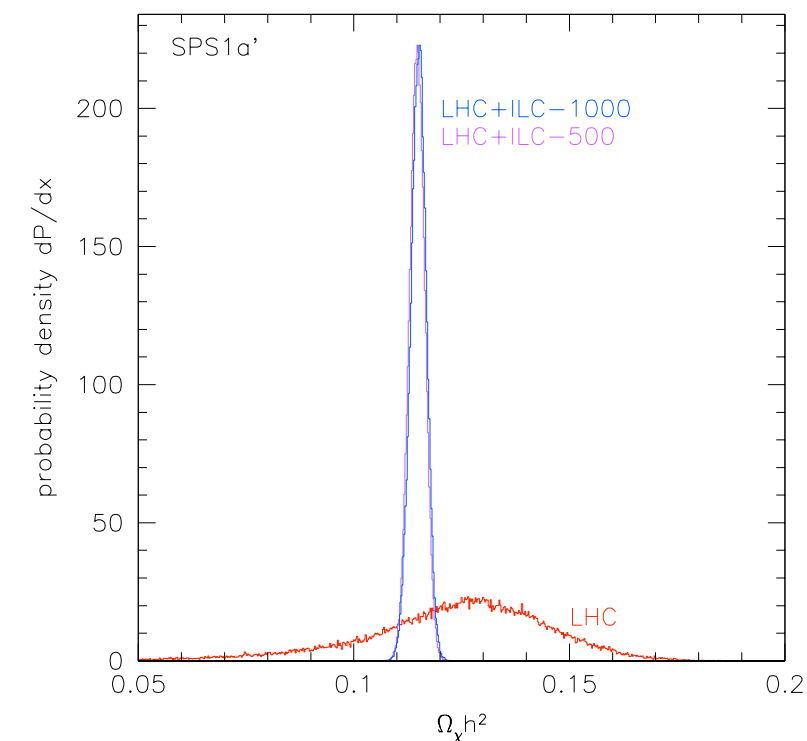
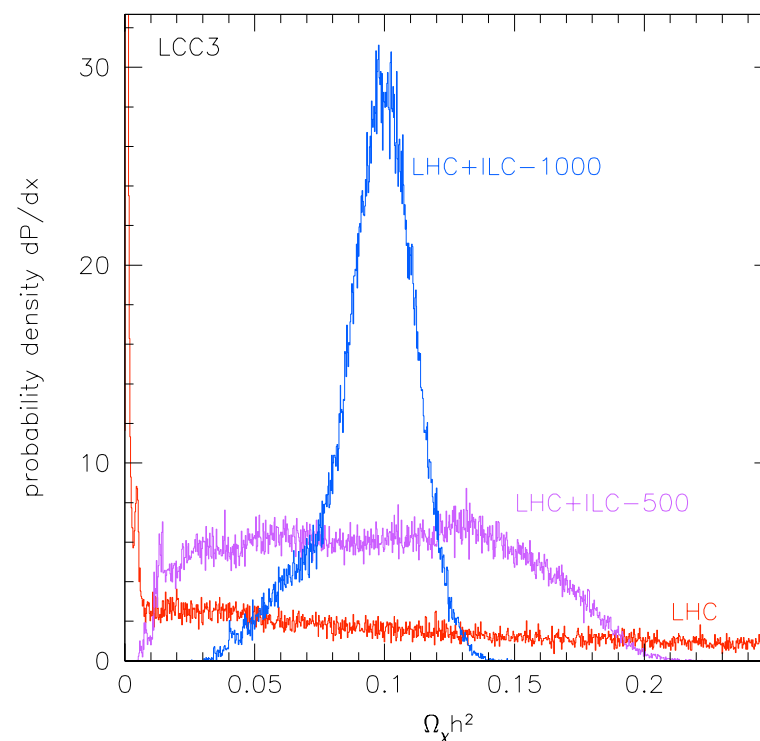
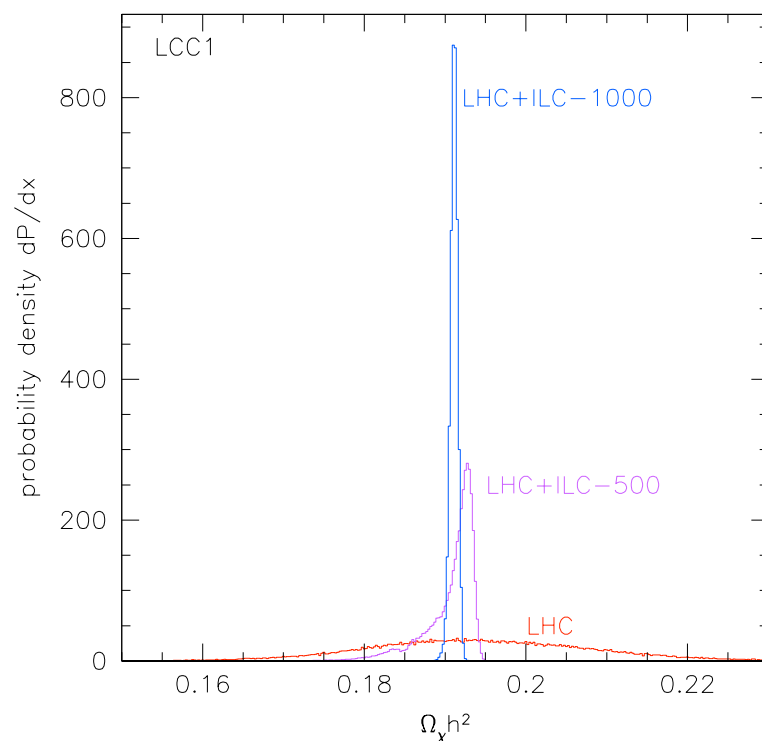
⇒ Will know *what Dark Matter is*

⇒ Will understand universe back to  $t \sim 10^{-10}$  sec





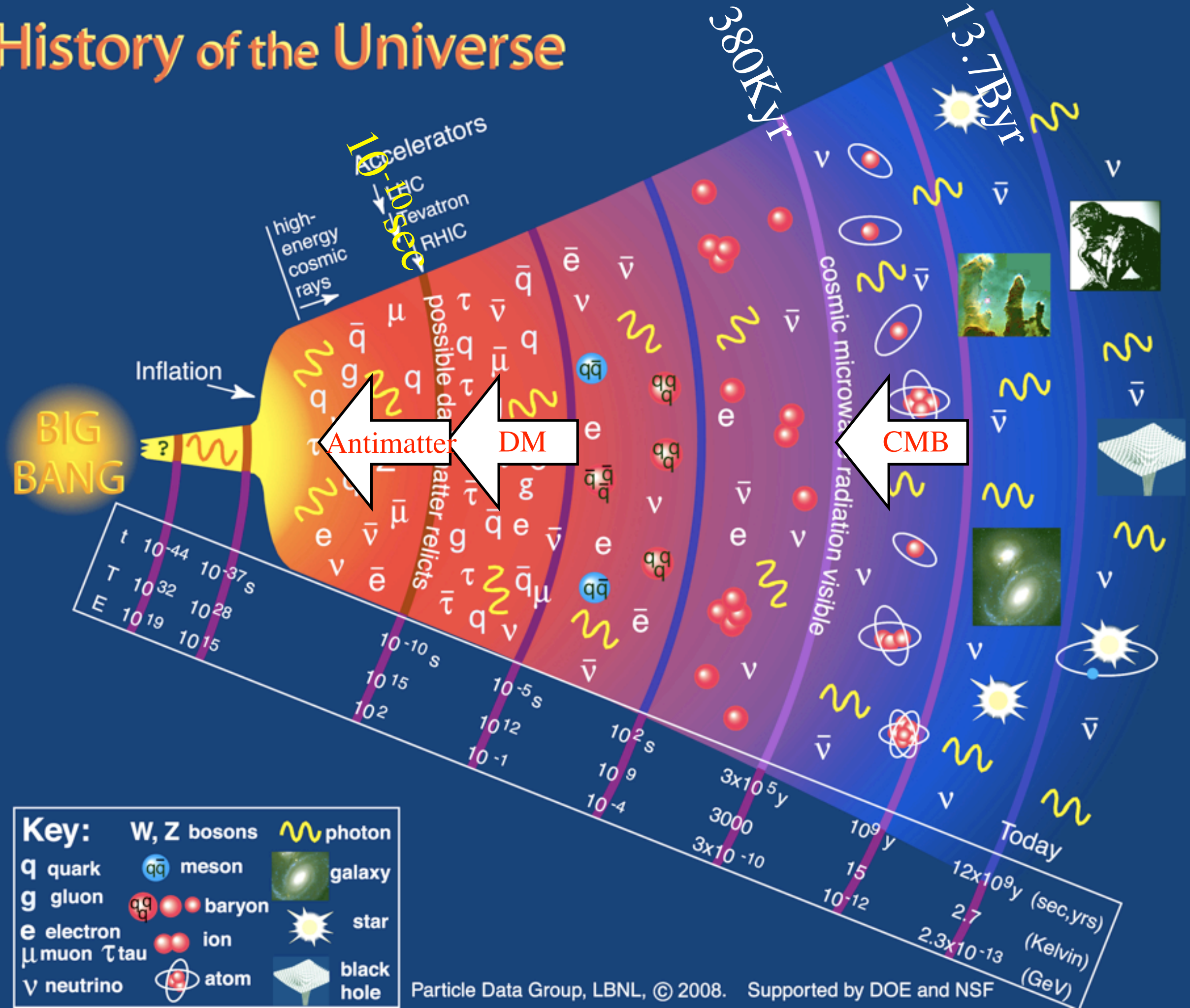
# Omega from colliders



**SUSY case study**  
**Baltz, Battaglia, Peskin,**  
**Wizansky hep-ph/0602187**



# History of the Universe



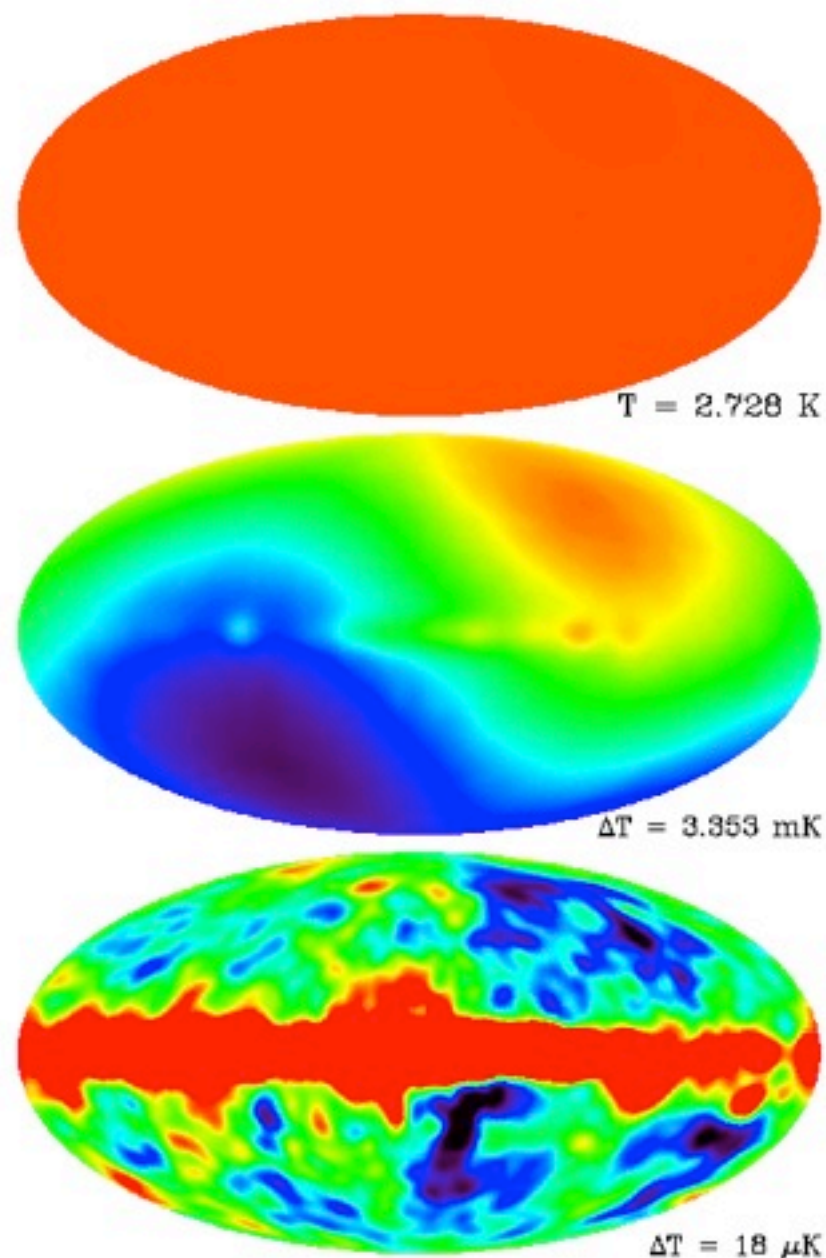


# Inflation





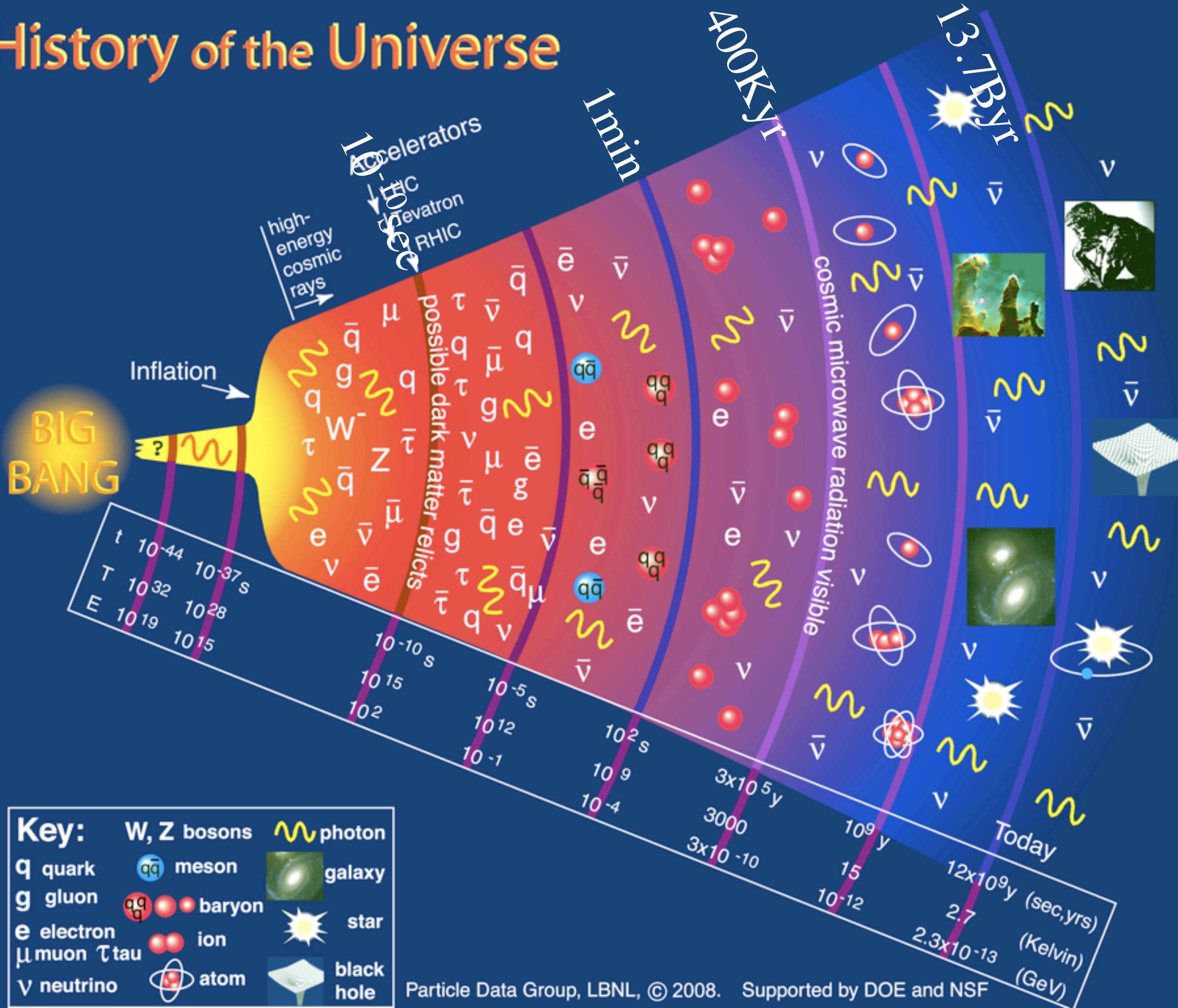
# Why do they all look the same?



- Like having discovered two remote islands in very different parts of the world, speaking the same language
- even the accents are nearly the same: one part in 100,000
- we suspect they had communication



# History of the Universe

















# inflaton

- scalar field with rather flat potential (compared to the Planck scale),  $\lambda \approx 10^{-11}$
- the equation of motion has a “friction term”

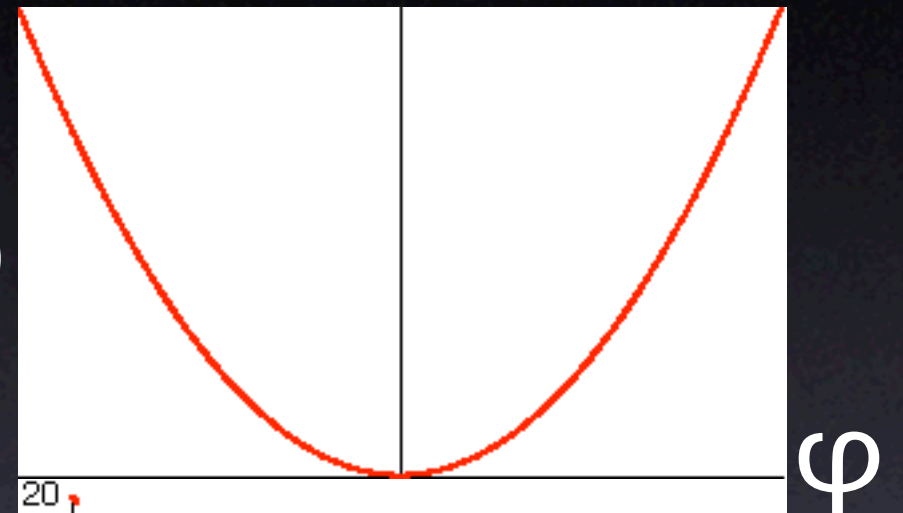
$$\ddot{\phi} + 3H\dot{\phi} = V'(\phi)$$

- slow-roll solution with more or less constant  $H$

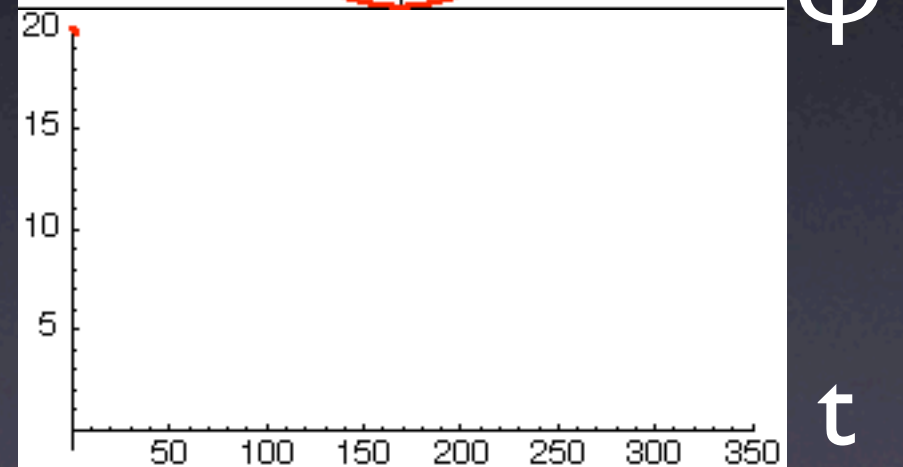
$$|\ddot{\phi}| \ll |\dot{\phi}| = V'(\phi) \quad H^2 = \frac{8\pi}{3} \frac{V}{M_{Pl}^2}$$

- Universe expands exponentially  $R(t) \propto e^{Ht}$
- need *e-folding*  $N=Ht > 60$  to solve the problem

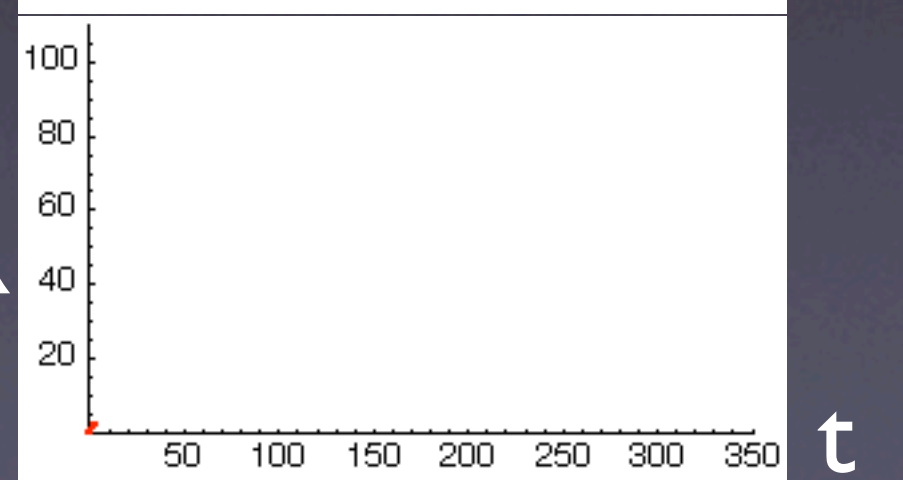
$V(\phi)$



$\phi$



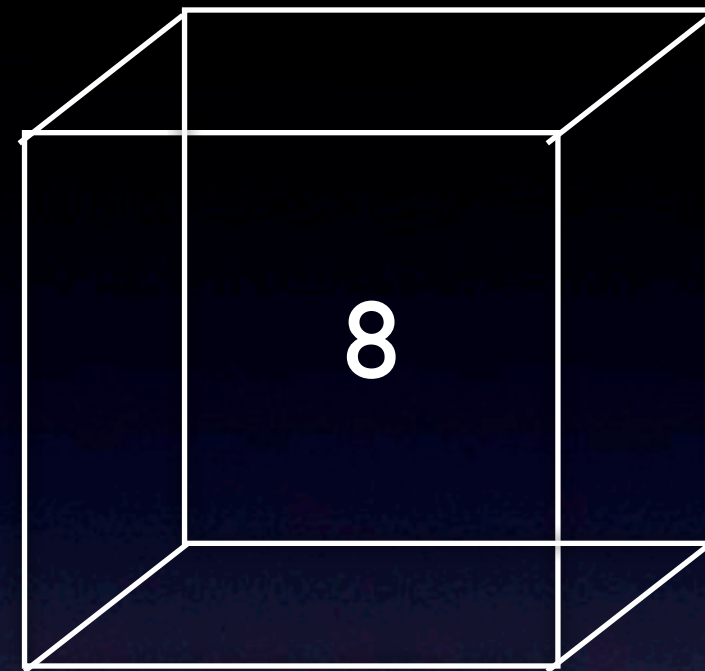
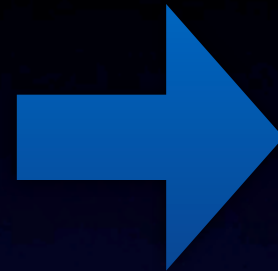
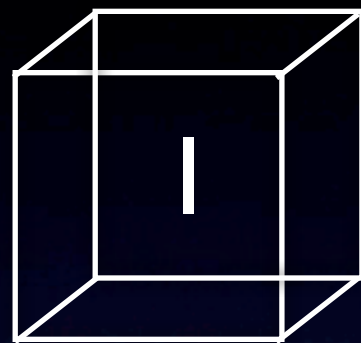
$\log R$





# Ultimate Free Lunch!

vacuum  
energy  
74%



$$\rho \propto R^0$$

total energy keeps growing like volume  $R(t)^3 \propto e^{3Ht}$





# near sighted

- What you are seeing one moment is *gone* by inflation the next moment
- feel very near-sighted
- “horizon”  $\approx H_I^{-1}$
- uncertainty principle: quantum fluctuation

$$\delta\varphi \approx H_I / 2\pi$$

$$\zeta = \frac{\delta\rho}{\rho + p} = \frac{V'\delta\varphi}{\dot{\phi}^2} = \frac{V'}{\dot{\phi}^2} \frac{H}{2\pi}$$

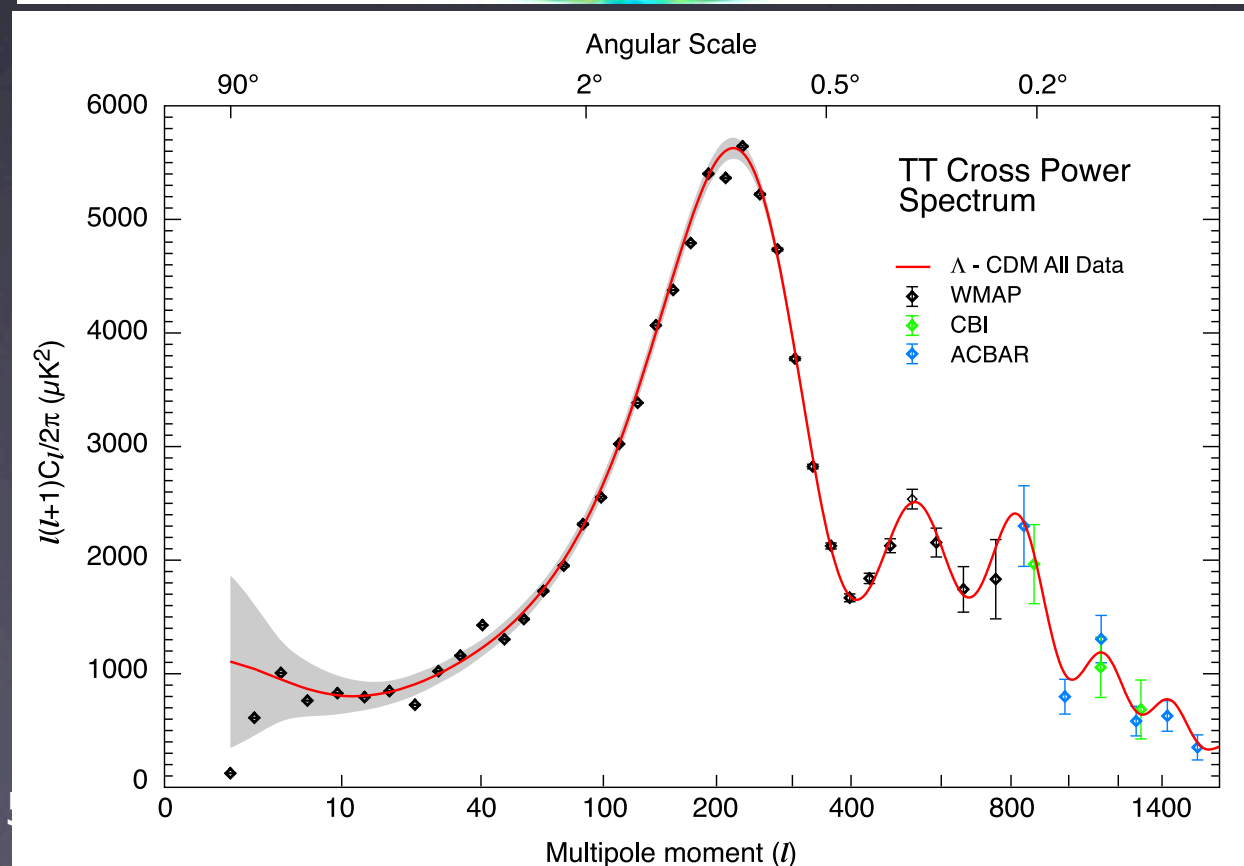
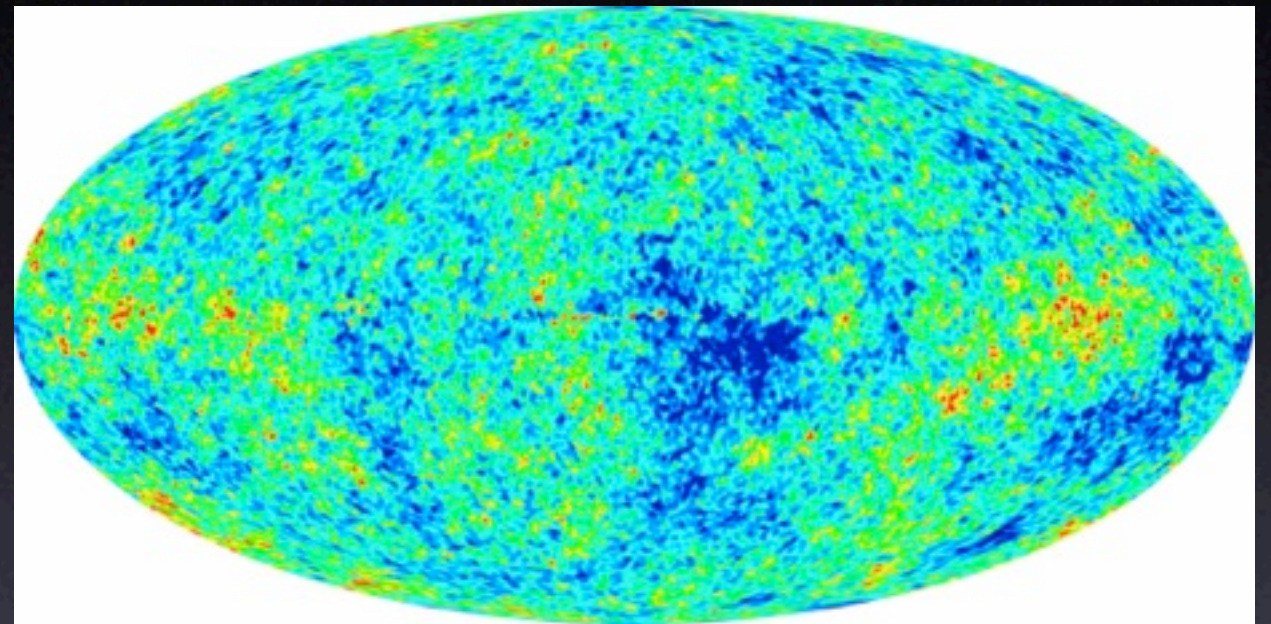
- nearly scale-invariant density fluctuation





# Seeds for structure

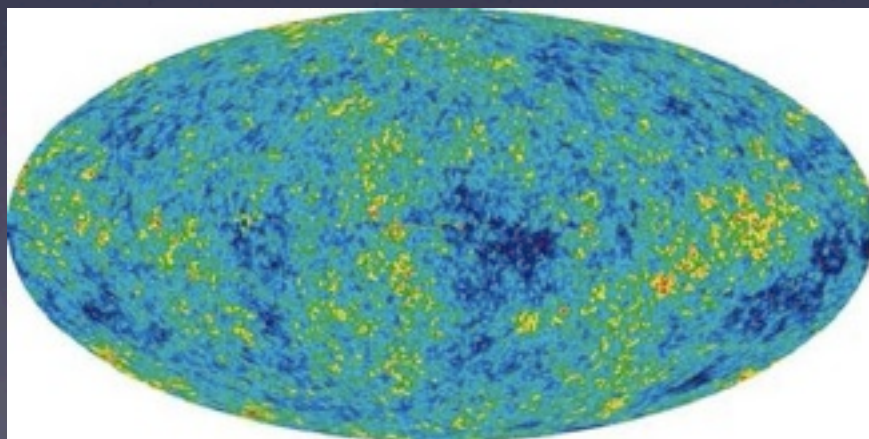
- **Cosmic Inflation** stretched the new-born microscopic space to our entire visible universe
- **Observed structure originates from quantum fluctuation of inflaton**
- Large-Scale Structure, CMB E-mode polarization consistent with this picture



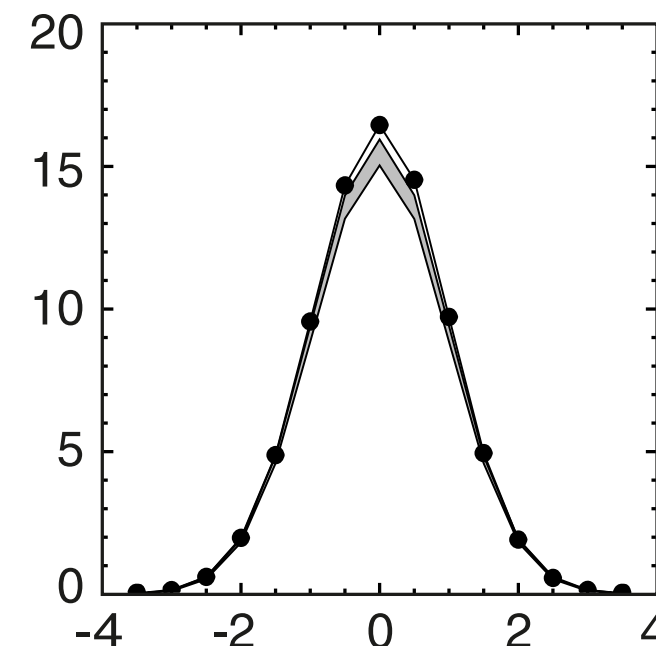
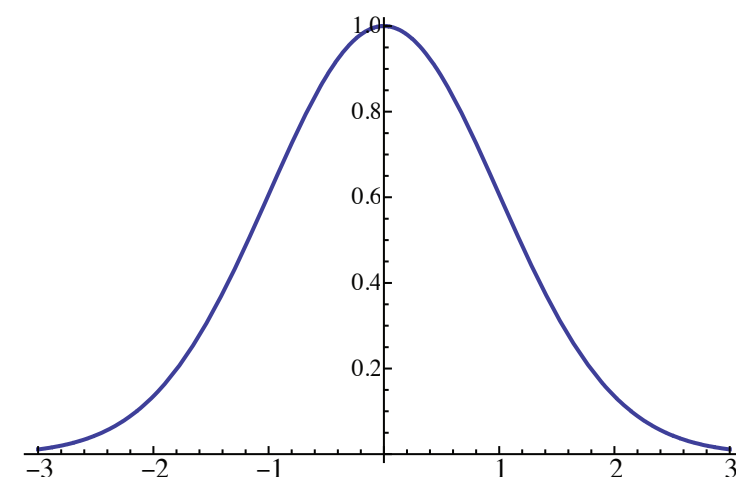


# Getting stronger

- If simple quantum fluctuation, it must be distributed as Gaussian
- Indeed!
- further tests of non-Gaussianity at Planck



distribution

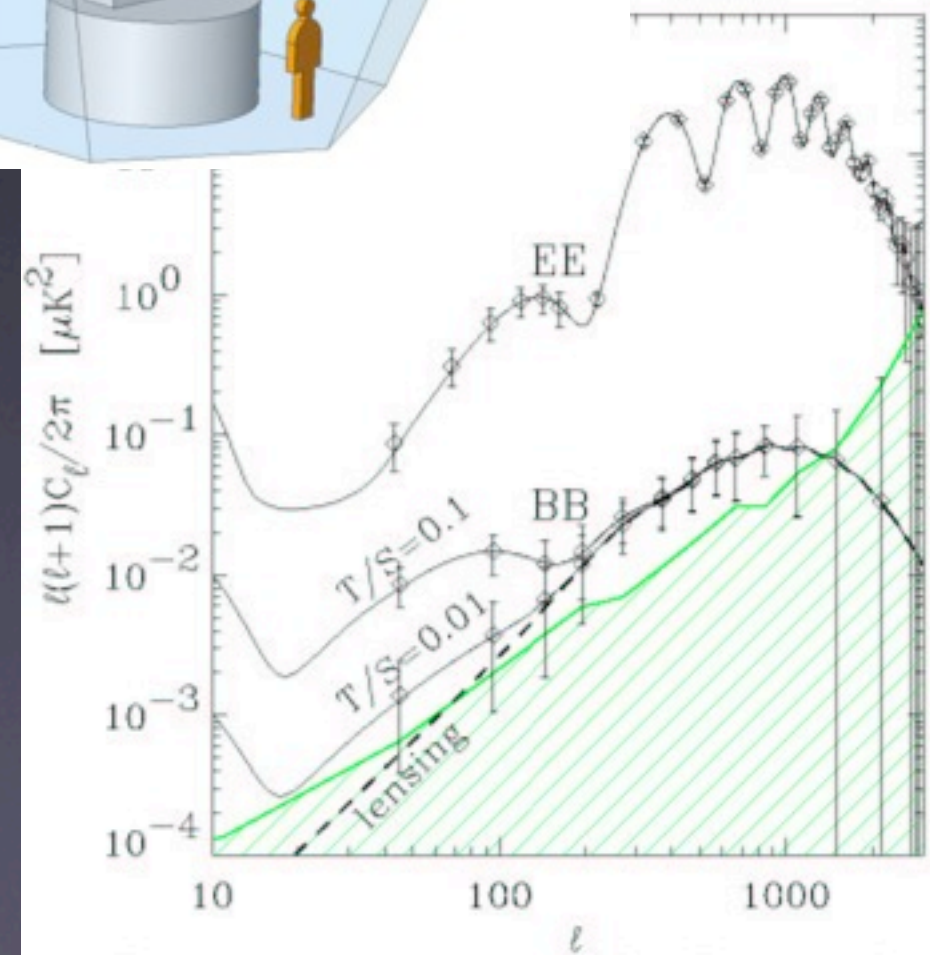
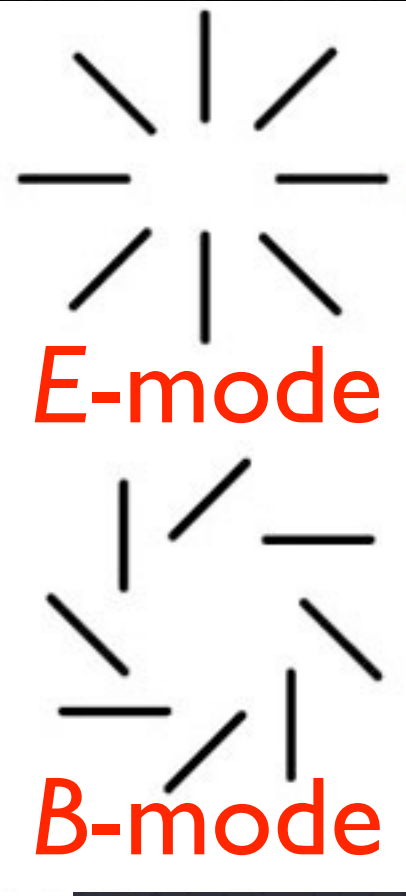
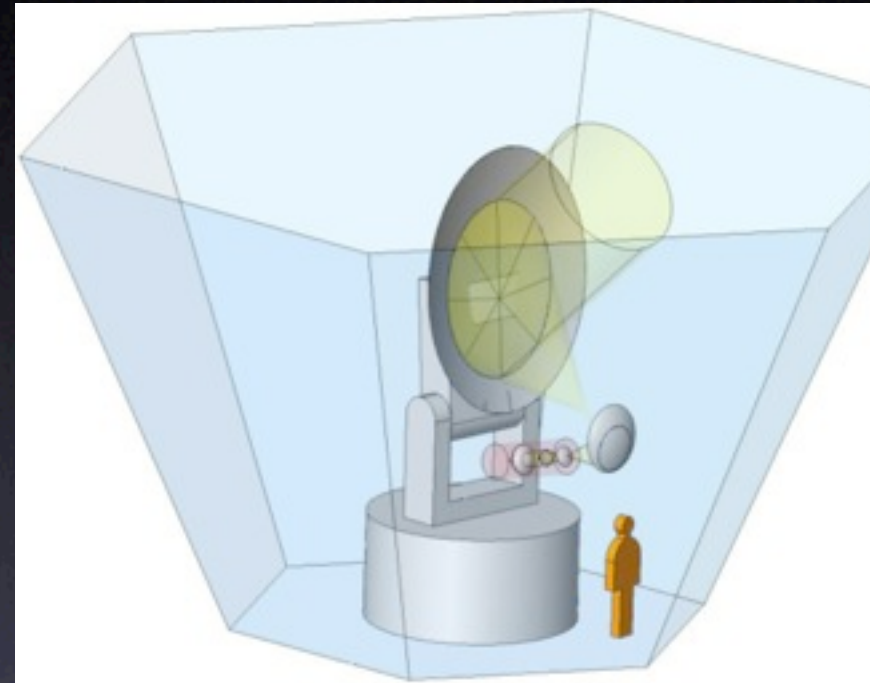


$\Delta T$



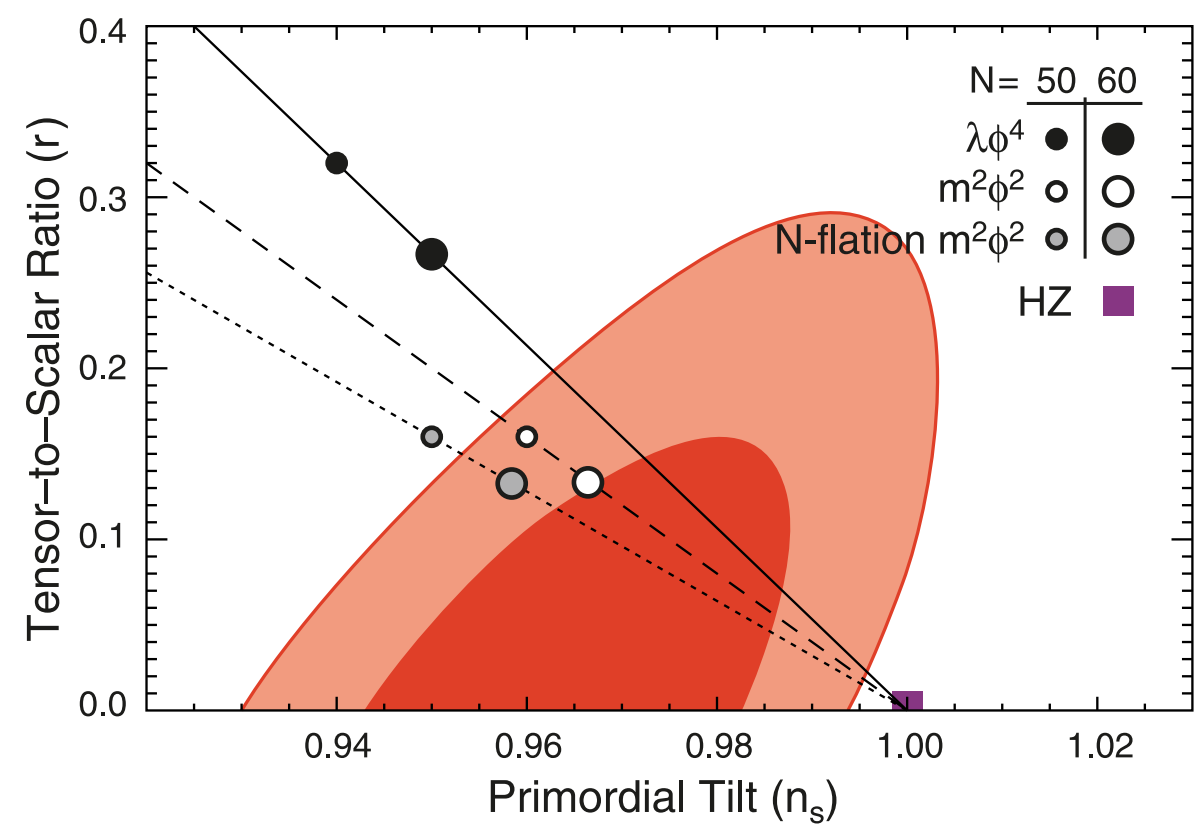
# How do we know it really happened?

- **everything** gets quantum fluctuation, including **gravitons**
- Gravitons from quantum fluctuation gives **B-mode polarization in CMB**
- The size is directly proportional to the **inflationary energy scale**  
 $\Rightarrow$  e.g., **Planck**, **POLARBEAR**, **Quiet**





su et al.

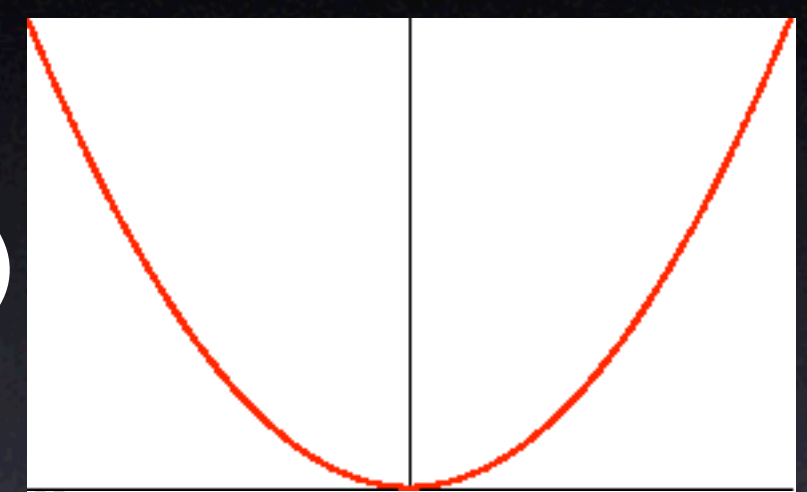


- quantum fluctuation source of later structure
- decays into both matter and anti-matter, but with a slight preference to matter
- decay products contain supersymmetry and hence Dark Matter

HM, Suzuki, Yanagida, Yokoyama

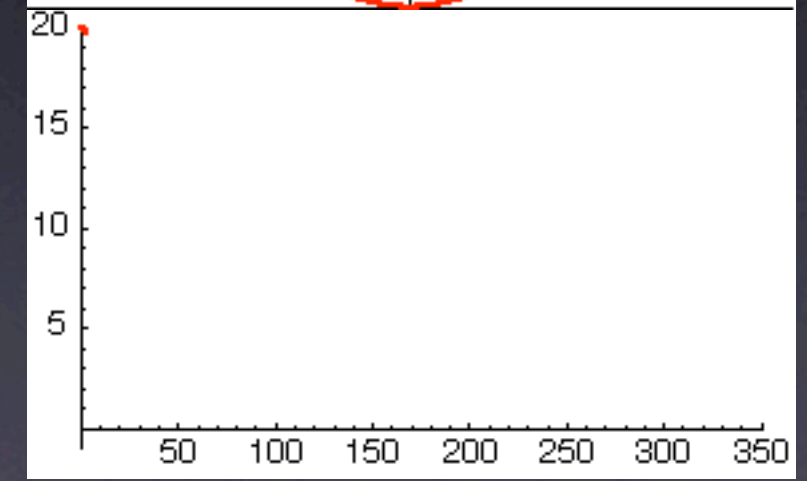
# m together

$V(\varphi)$



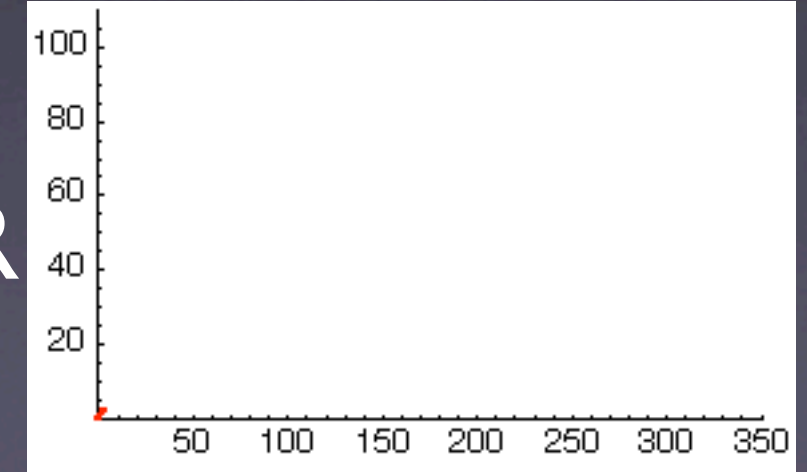
$\varphi$

$\varphi$



$t$

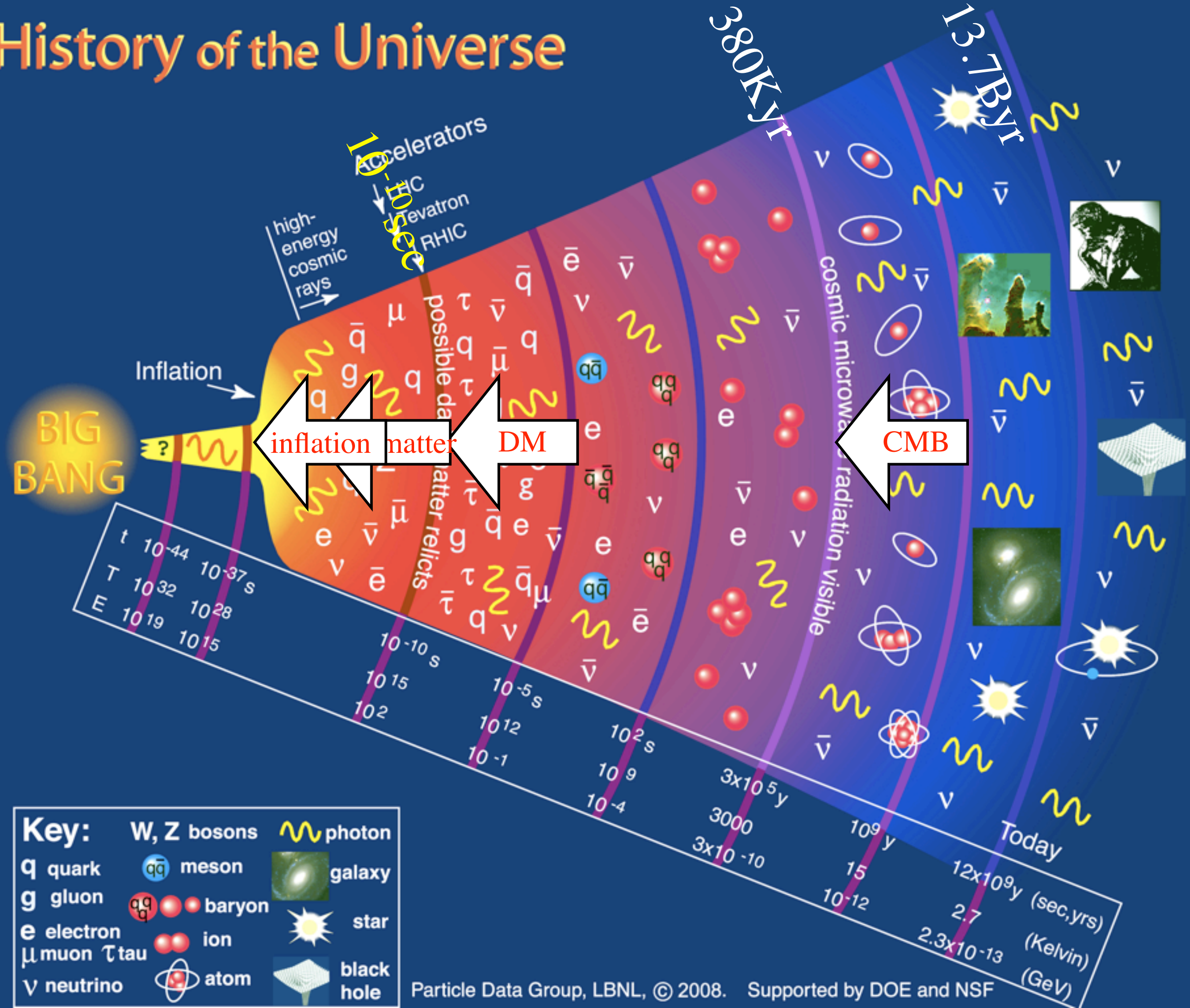
$\log R$



$t$



# History of the Universe



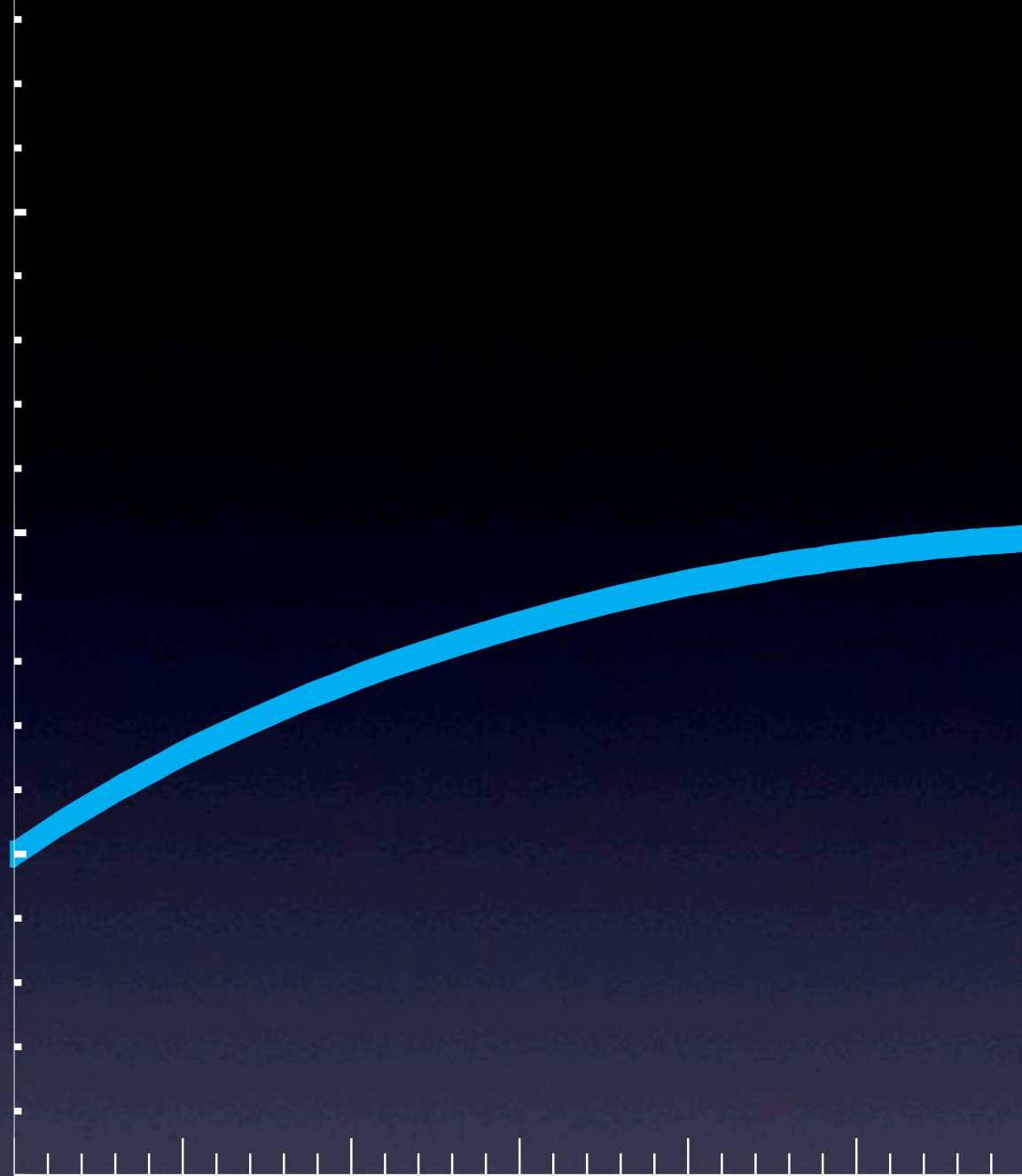
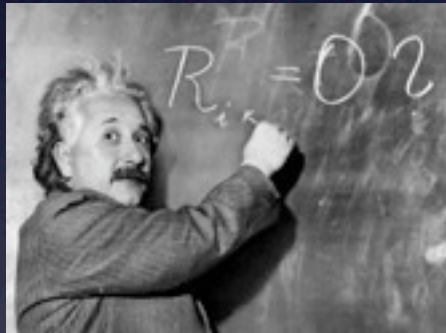




# fate of the Universe



expansion

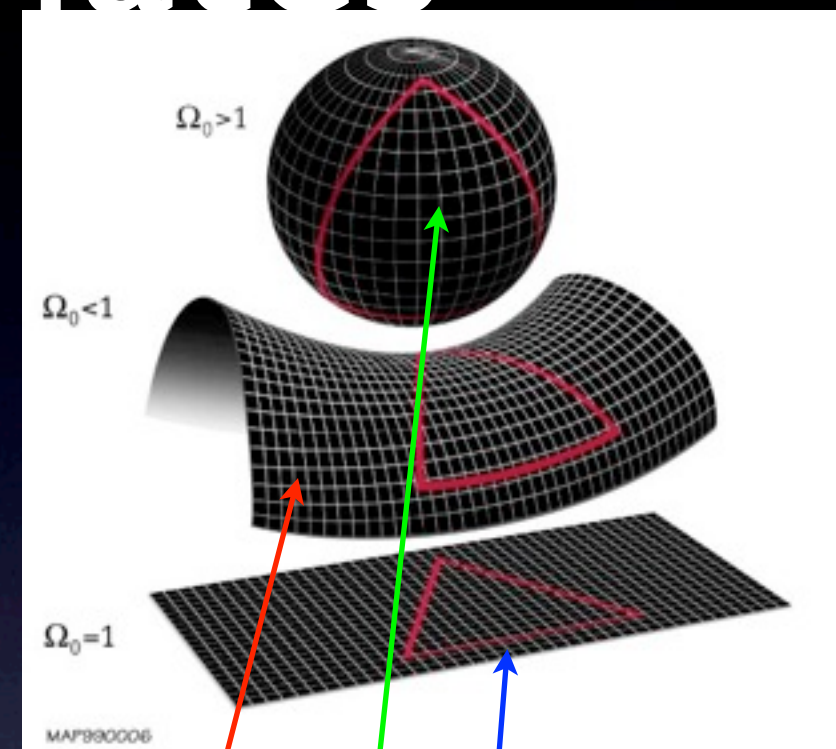


decceleration

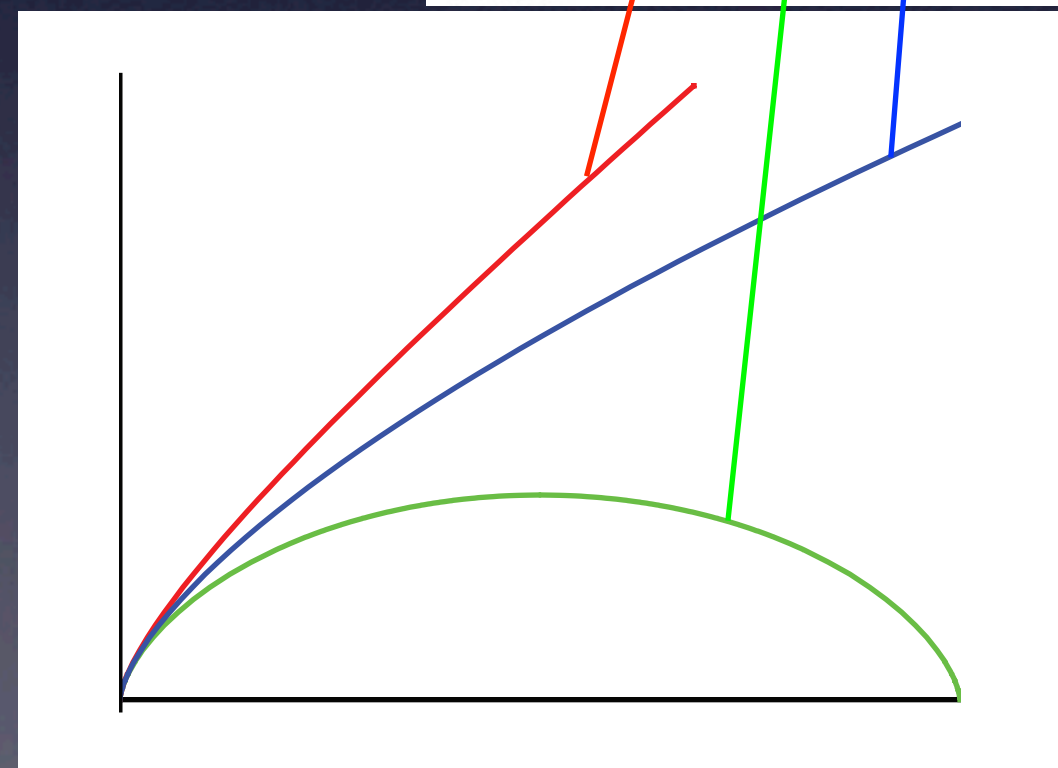


# three possible fates

- if large amount of matter, expansion stops and heads back to a Big Crunch
- if small amount of matter, expansion will go on forever
- study the expansion history and predict the future!



size of the Universe



time




# future observers

- as the Universe gets better, more and more galaxies come into sight
- observation becomes more fun!





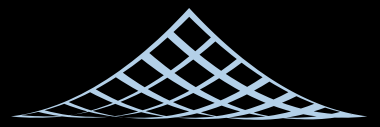


# Dark Energy



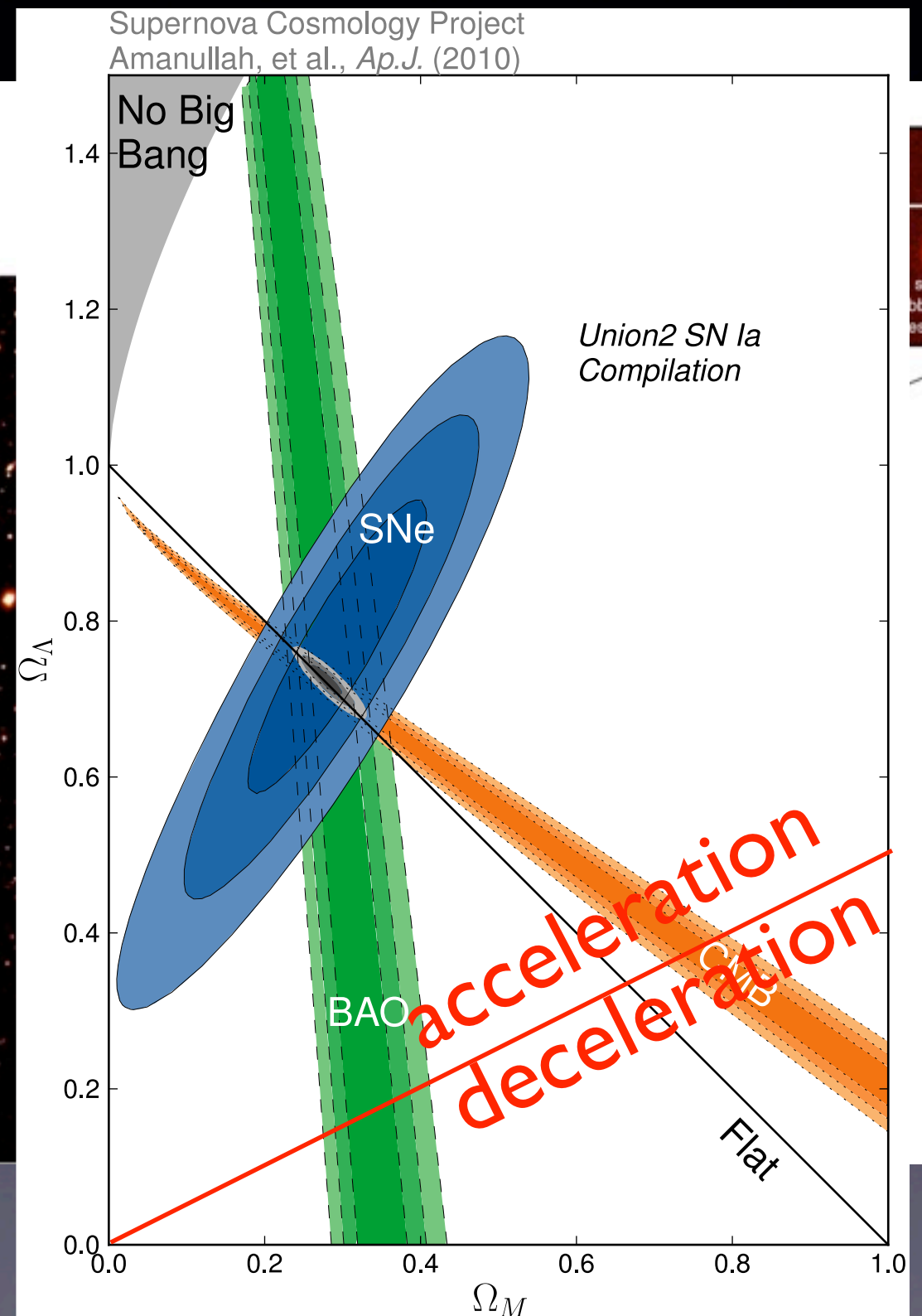




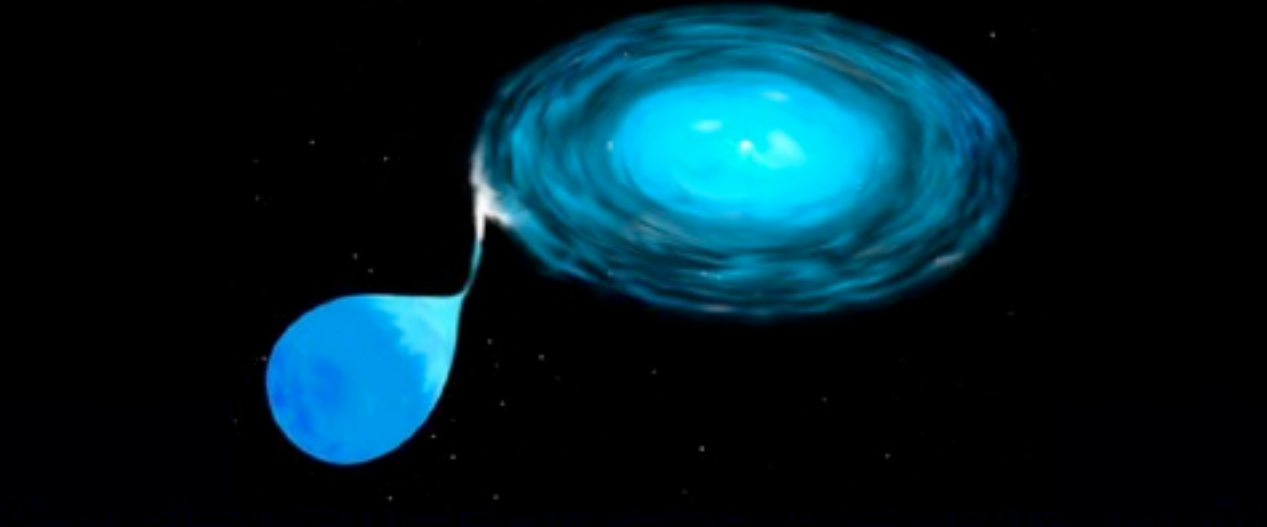


# Type-Ia supernovae

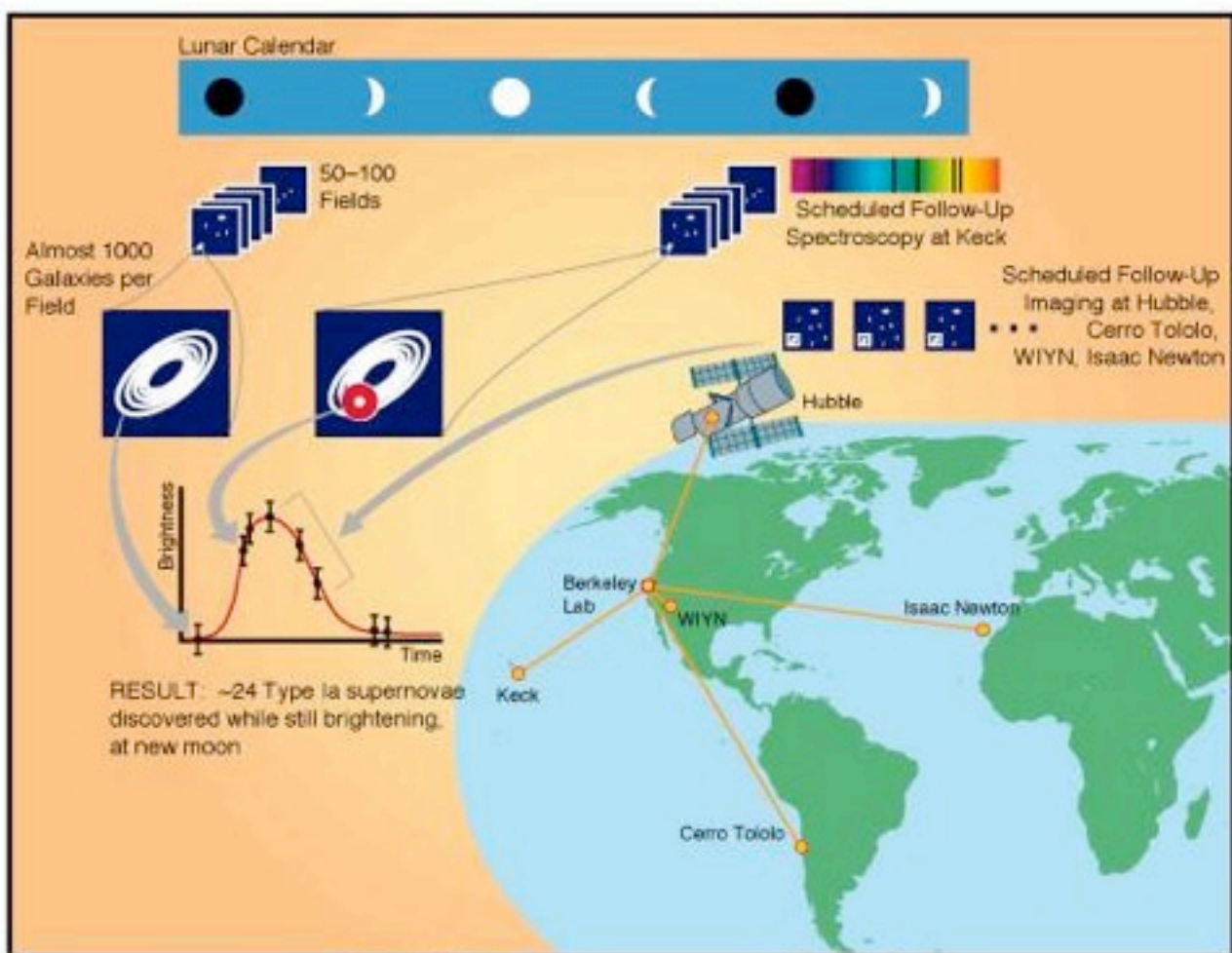
- Type-Ia supernova becomes brighter than the whole galaxy
- *How bright it looks*  
 $\Rightarrow$  *How far away*  
 $\Rightarrow$  *How far back in time*
- *How red it looks*  
 $\Rightarrow$  *How much expansion*
- Expansion of the Universe is getting faster!





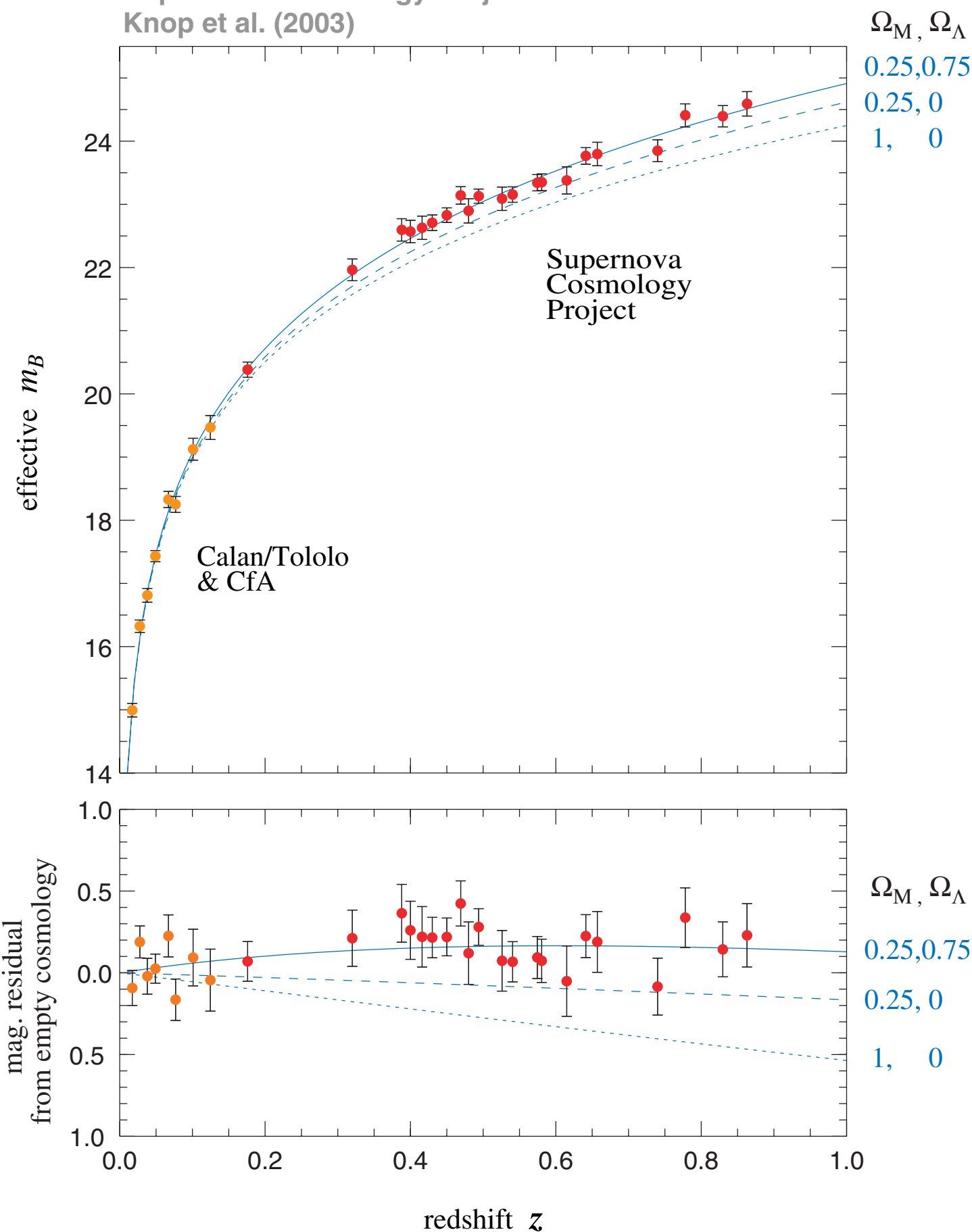


## Strategy



supernovae  
on demand

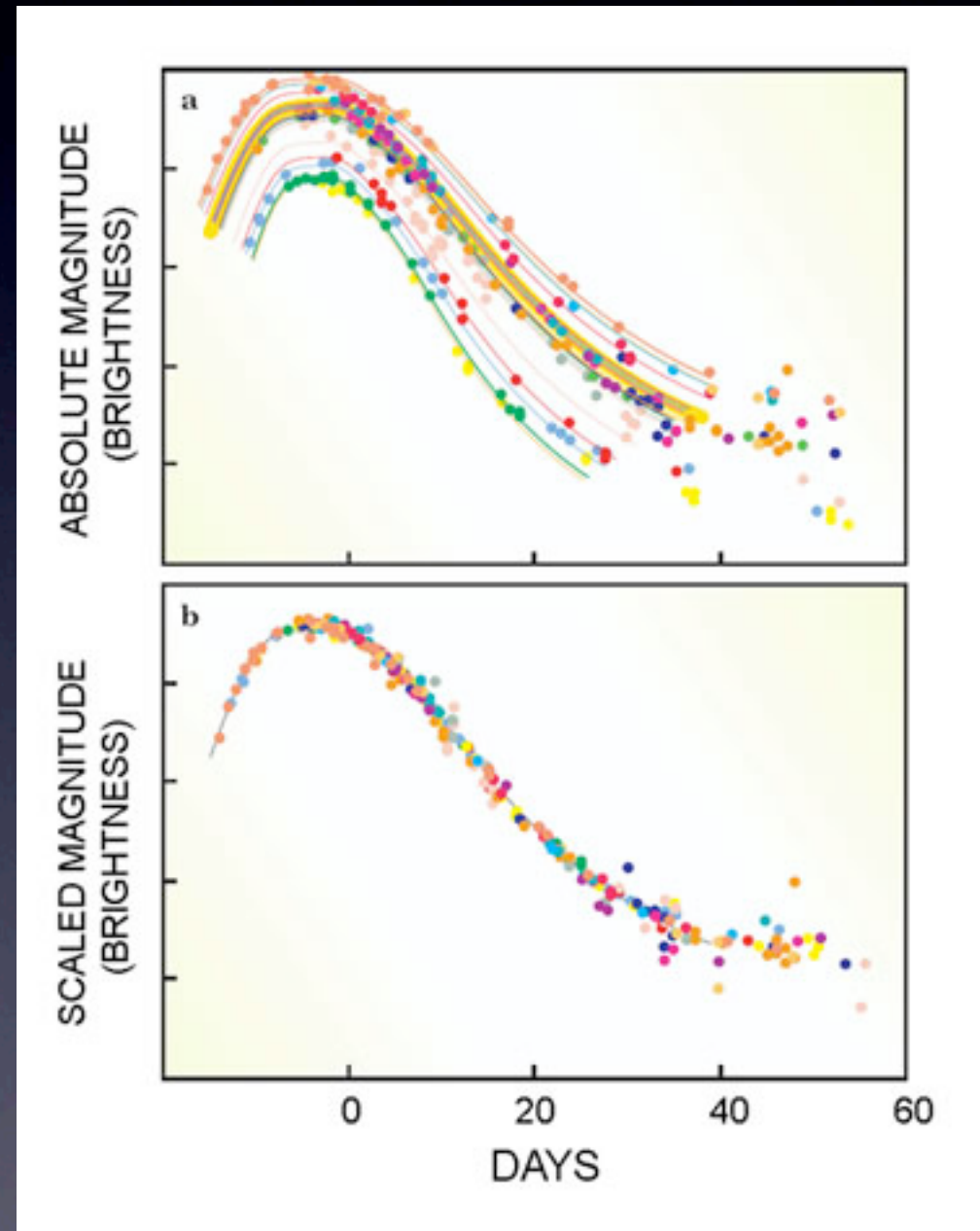
## Supernova Cosmology Project Knop et al. (2003)





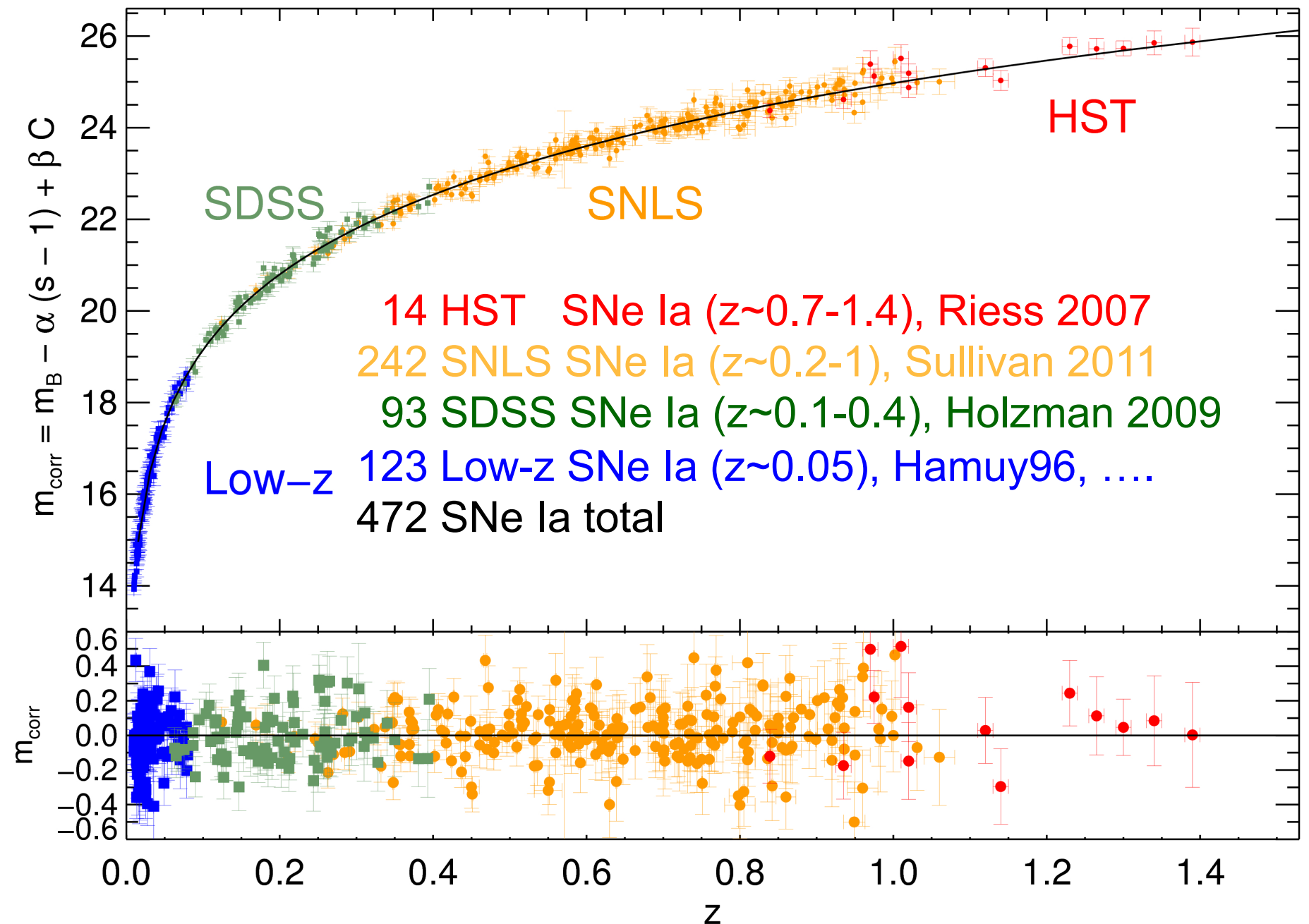
# stretch factor

- it is not quite standard
- correlation between duration time and the absolute brightness
- can be “fixed” by a “stretch factor”
- other smaller concerns with environment (metallicity), dust extinction, etc





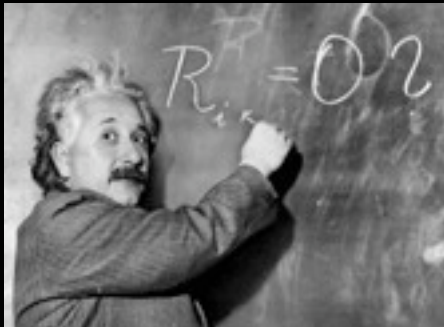
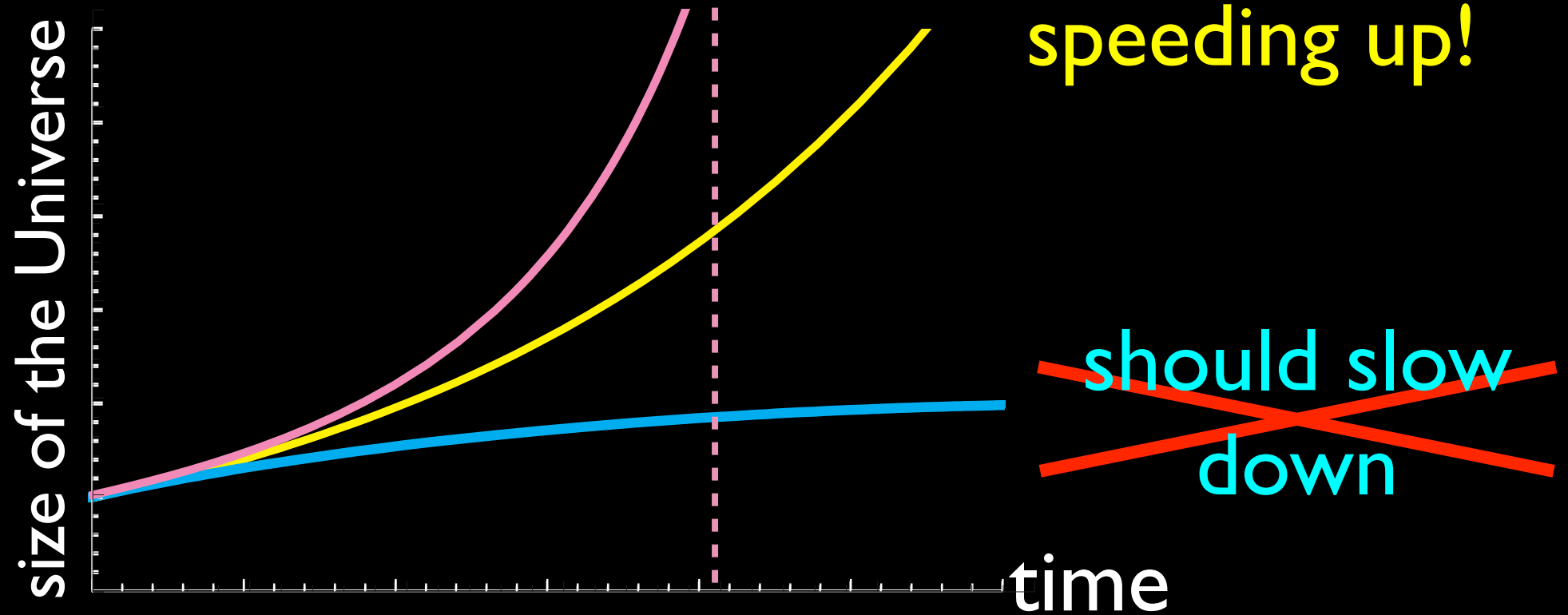
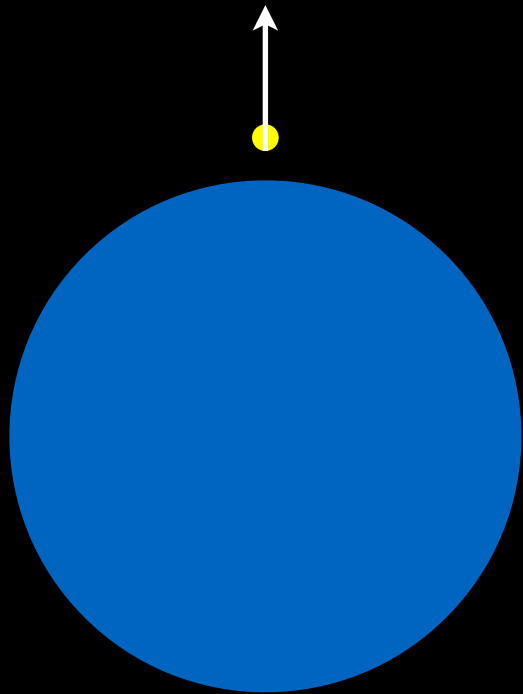
Stat  $\sim \times 10$  since the  
1998 discovery papers



Guy et al, 2010 – Conley et al 2010, Sullivan et al, 2011



expansion



- expansion started to speed up **recently** (~7Byr)
- **energy is increasing!**
- **infinite source of energy??** dark energy
- **Was Einstein wrong?**
- new paradigm of the Universe, fundamental laws
- If the rate of energy increase very quick, eventually the expansion becomes infinitely fast  
⇒ **Will the Universe end??**
- **Need to measure the rate of energy increase!**



# Acceleration

- $w$ : equation of state parameter

$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi}{3} G_N \rho$$

- radiation:  $w=1/3$

$$\rho = wp$$

- matter:  $w=0$

$$dU = d(\rho R^3) = -pdV = -wpdR^3$$

- vacuum energy:  $w=-1$

$$\rho \propto R^{-3(1+w)}$$

- acceleration:  $w < -1/3$

$$\ddot{R} \propto -(1 - 3w)$$



# Does the Universe end?

- If  $w < -1$ , the Universe ends in a **Big Rip**
- Expansion becomes **so fast** that galaxies, stars, eventually atoms and even nuclei get ripped apart
- **Universe ends** with an infinite speed and empty!
- or it may be “Inflation Strikes Back”,  $w > -1$
- We need to know the **equation of state**





衝撃の終末  
ビッグリップ







# Embarrassment

- A naïve estimate of the cosmological constant in Quantum Field Theory:

$$\rho_{\Lambda} \sim M_{Pl}^4 = G_N^{-2} \sim 10^{120} \text{ times observation}$$

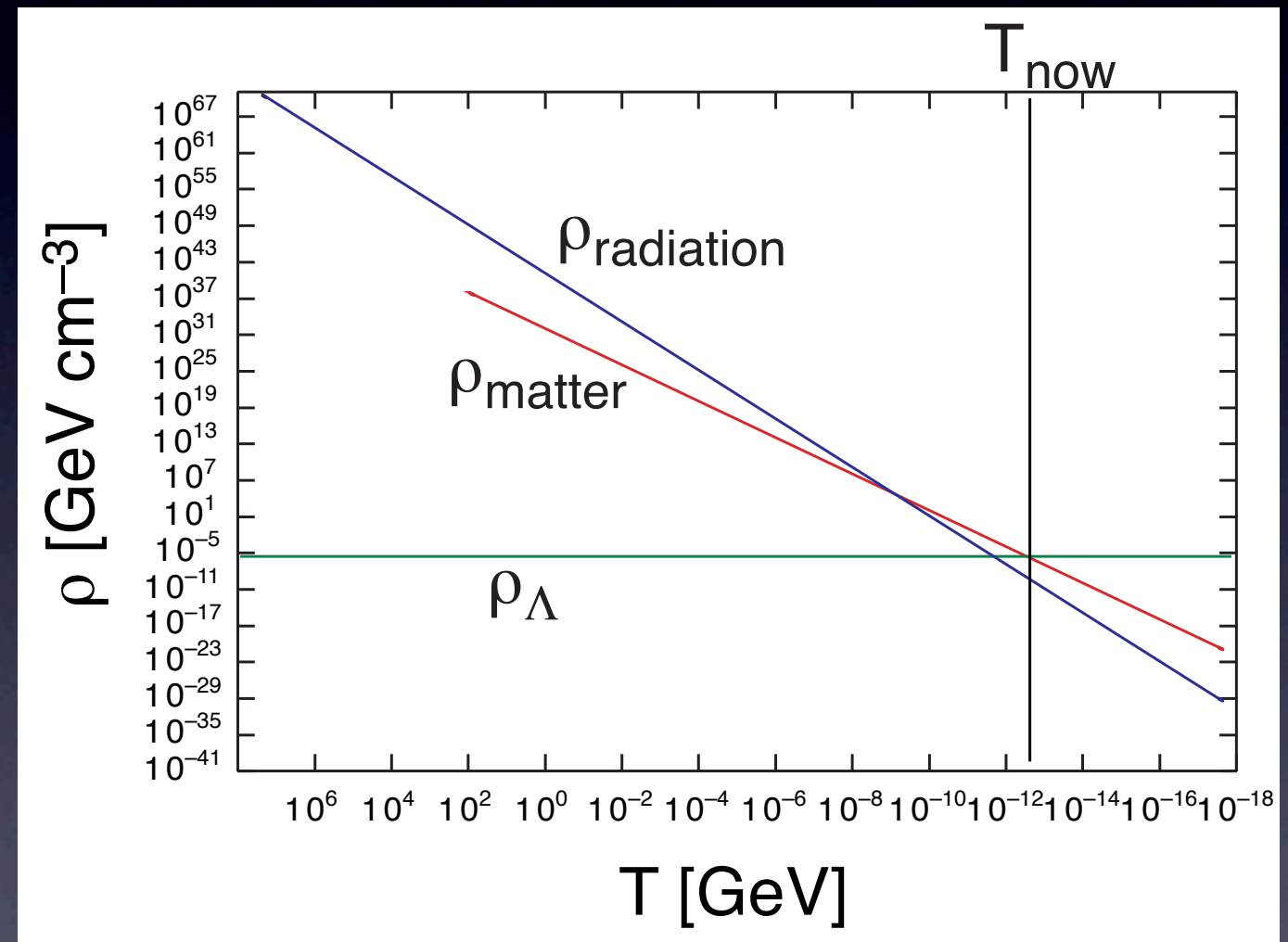
The worst prediction in theoretical physics!

- People had argued that there must be some mechanism to set it zero
- But now it seems finite???



# Cosmic Coincidence Problem

- Why do we see matter and cosmological constant almost equal in amount?
- “Why Now” problem
- Actually a *triple coincidence problem* including the radiation
- If there is a deep reason for  $\rho_\Lambda \sim ((\text{TeV})^2/M_{Pl})^4$ , coincidence natural



Arkani-Hamed, Hall, Kolda, HM





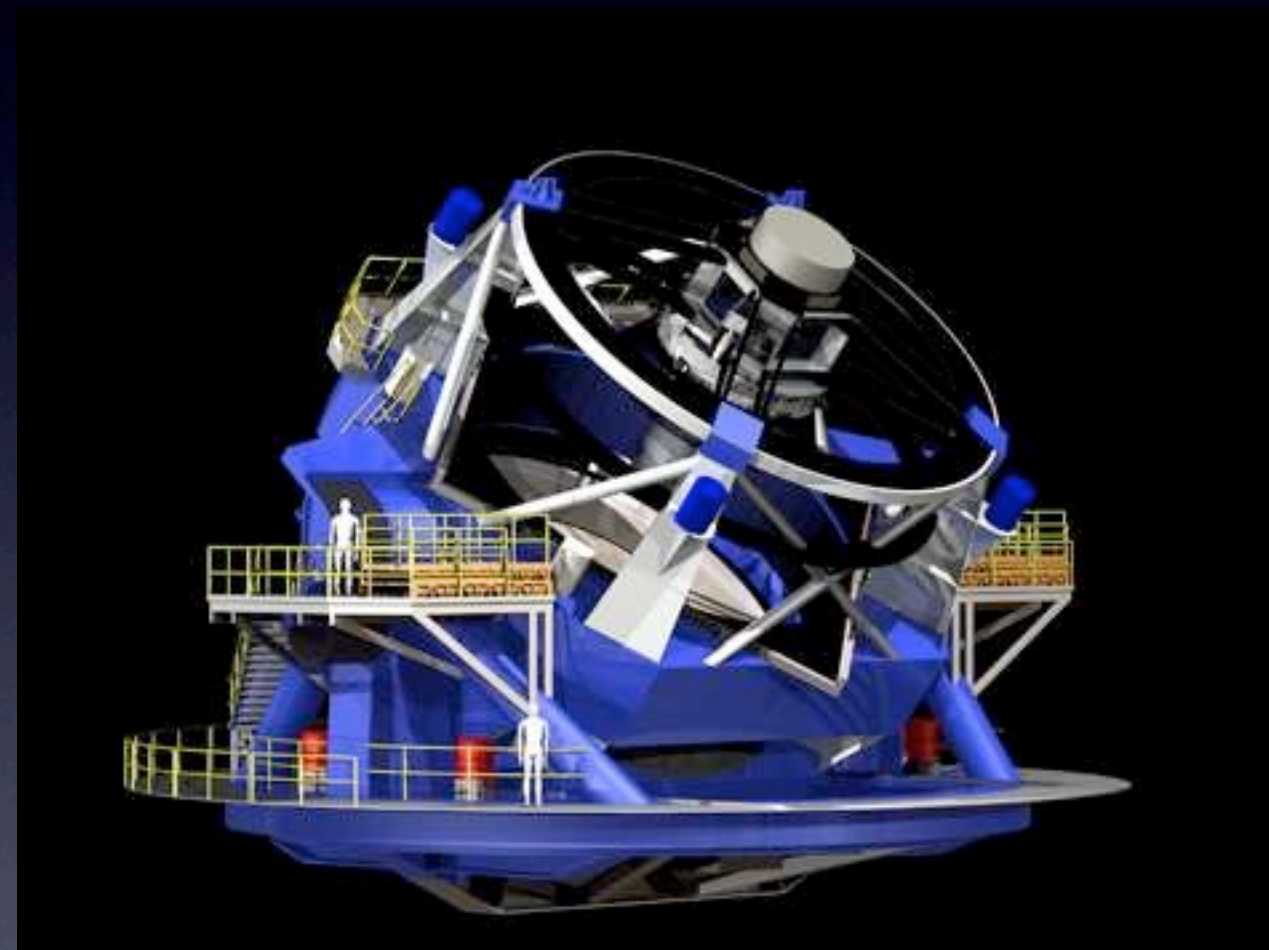
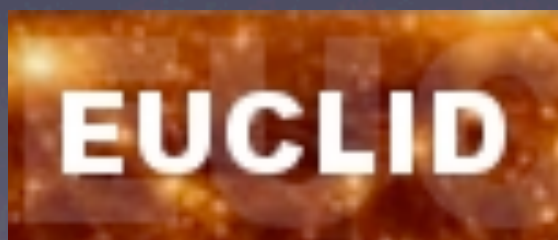
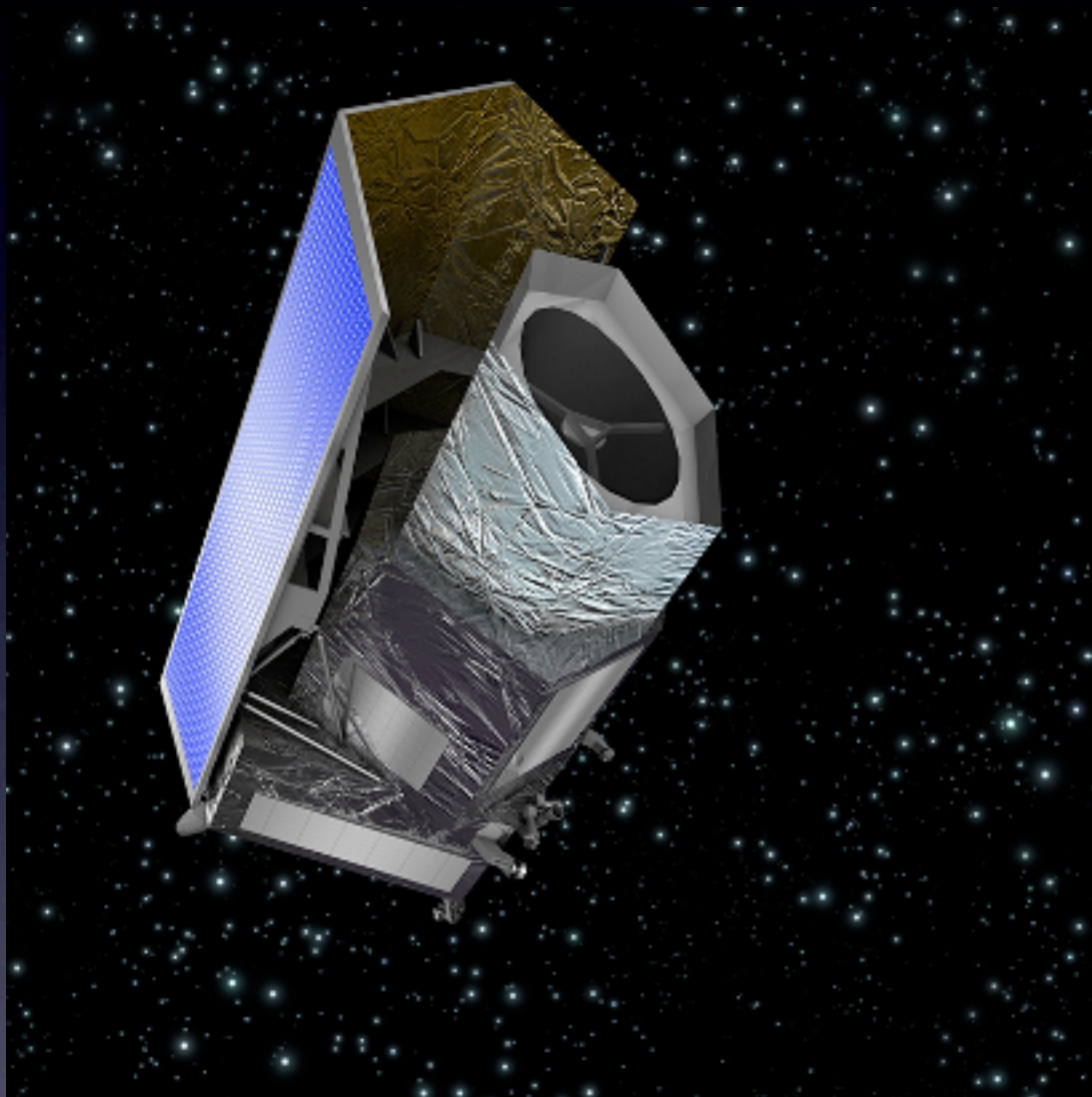


We can study cosmology only now.  
*Need funding ASAP.*





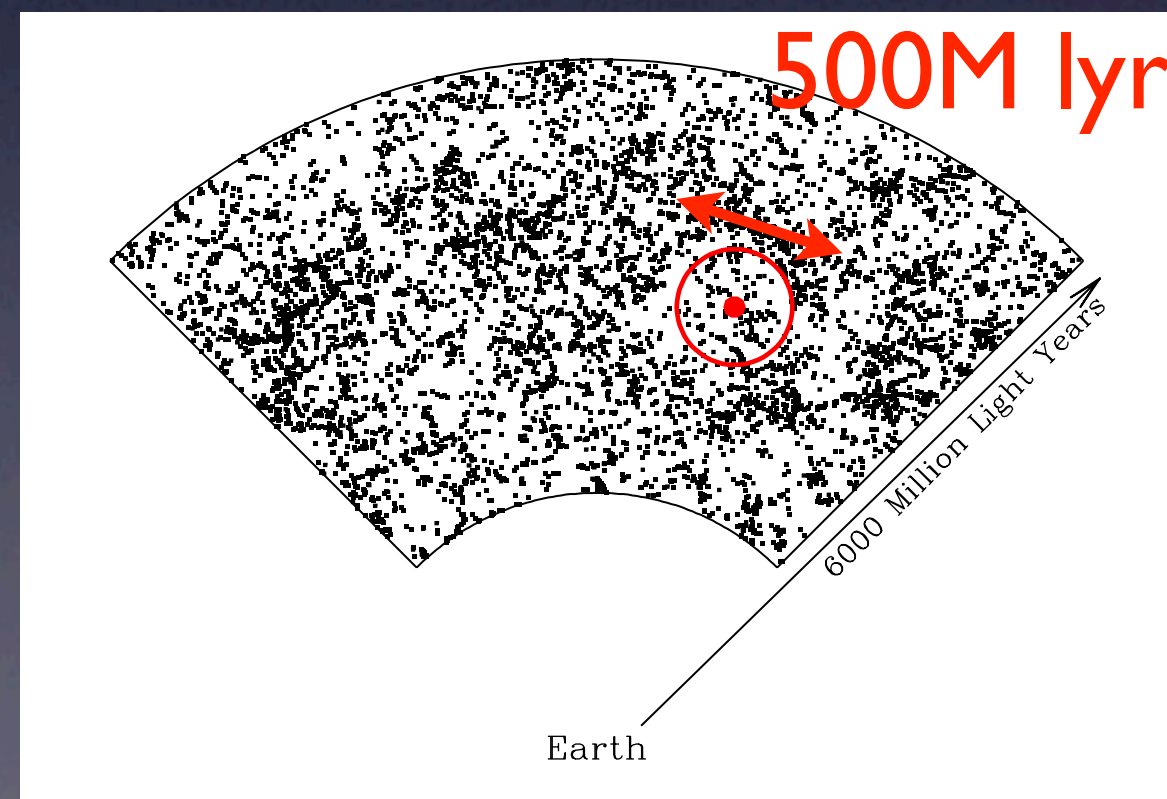
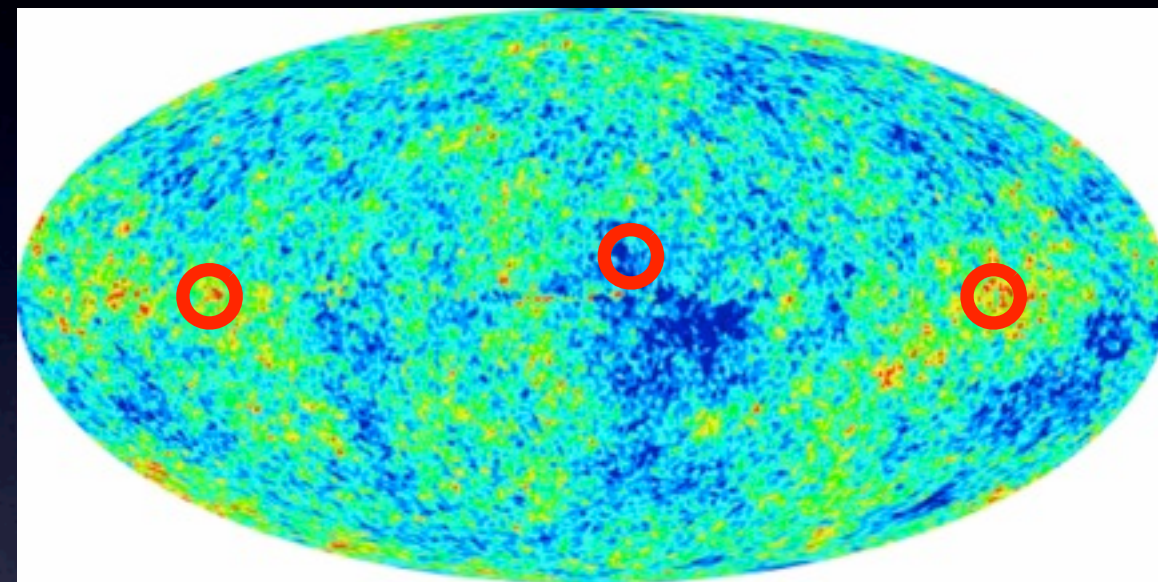
# big future players





# Standard Ruler

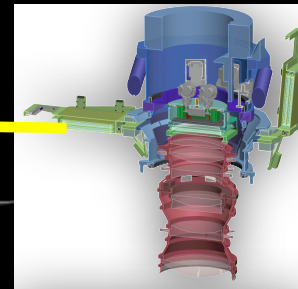
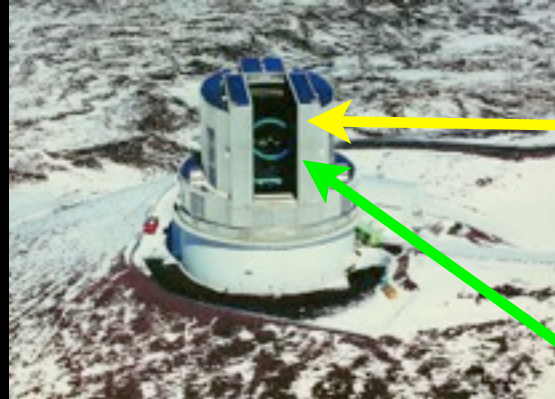
- characteristic scales for acoustic peaks
- acoustic peak shows up in galaxy distributions, too, at  $\sim 500\text{M lyr}$
- use this scale as a “standard ruler” to measure distances accurately
- Will the Universe end?



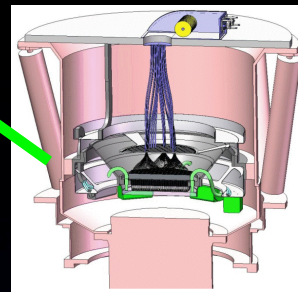


# SuMIRe

Subaru

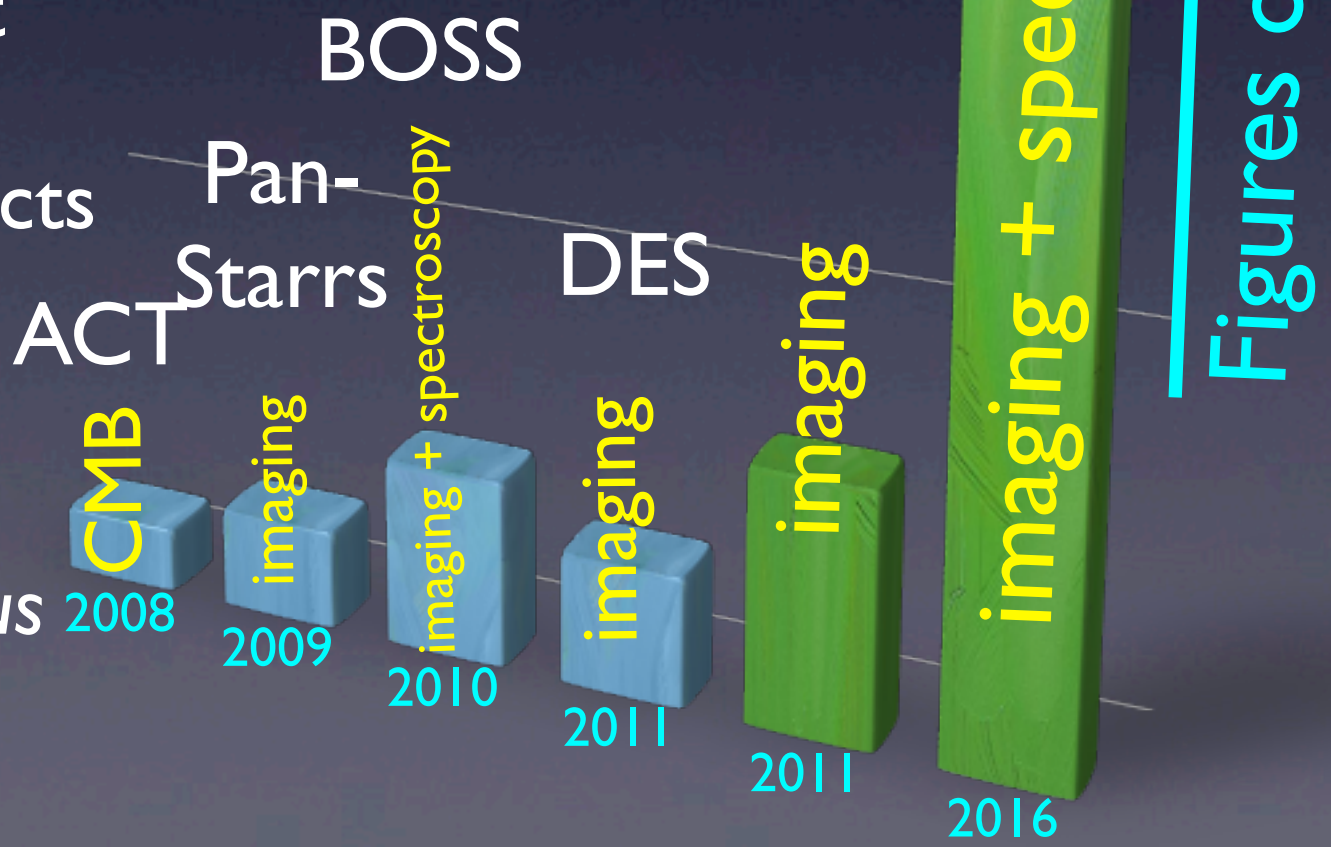


imaging  
(HSC)



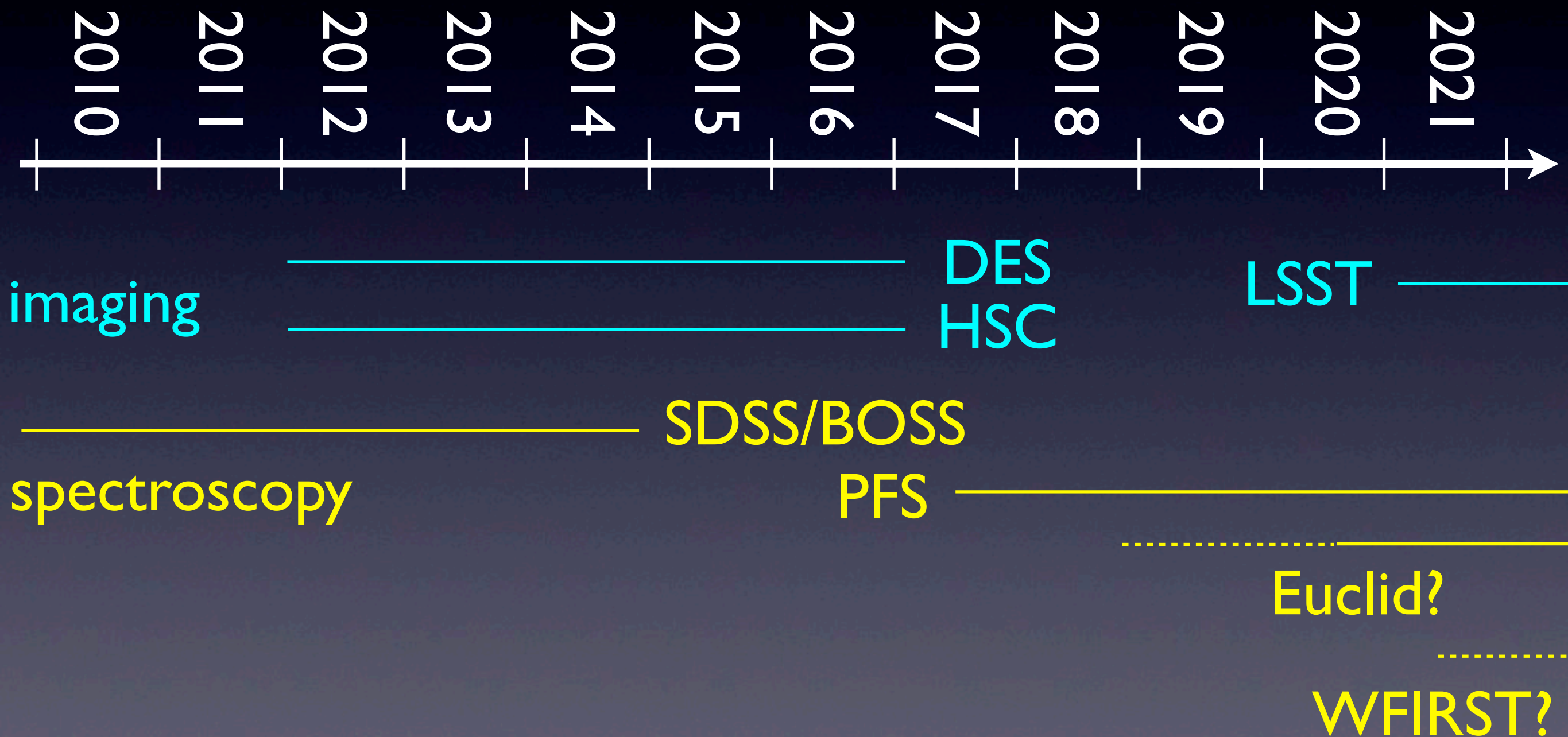
spectroscopy  
(PFS)

- *cosmic census*
- field of view  $\sim$  Hubble x1000
- Major study of dark energy
- Subaru Measurement of Images and Redshifts
  1. **imaging** with 0.9B-pixels 3t CCD camera from 2012
  2. **spectroscopy** of 2400 objects from 2017
- same telescope for both **imaging** and **spectroscopy**
- *galaxy survey with continuous redshift coverage*





# Timeline





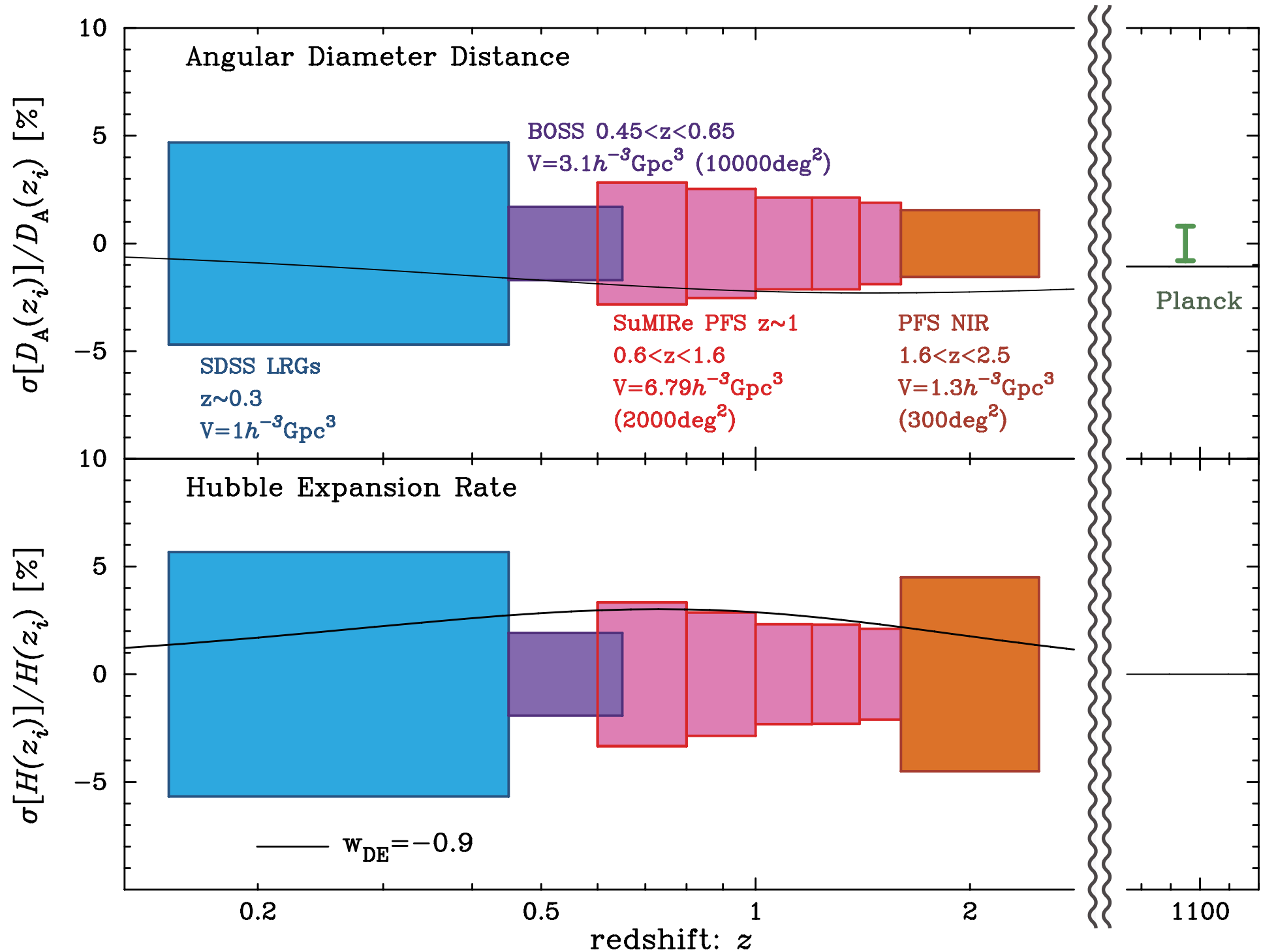
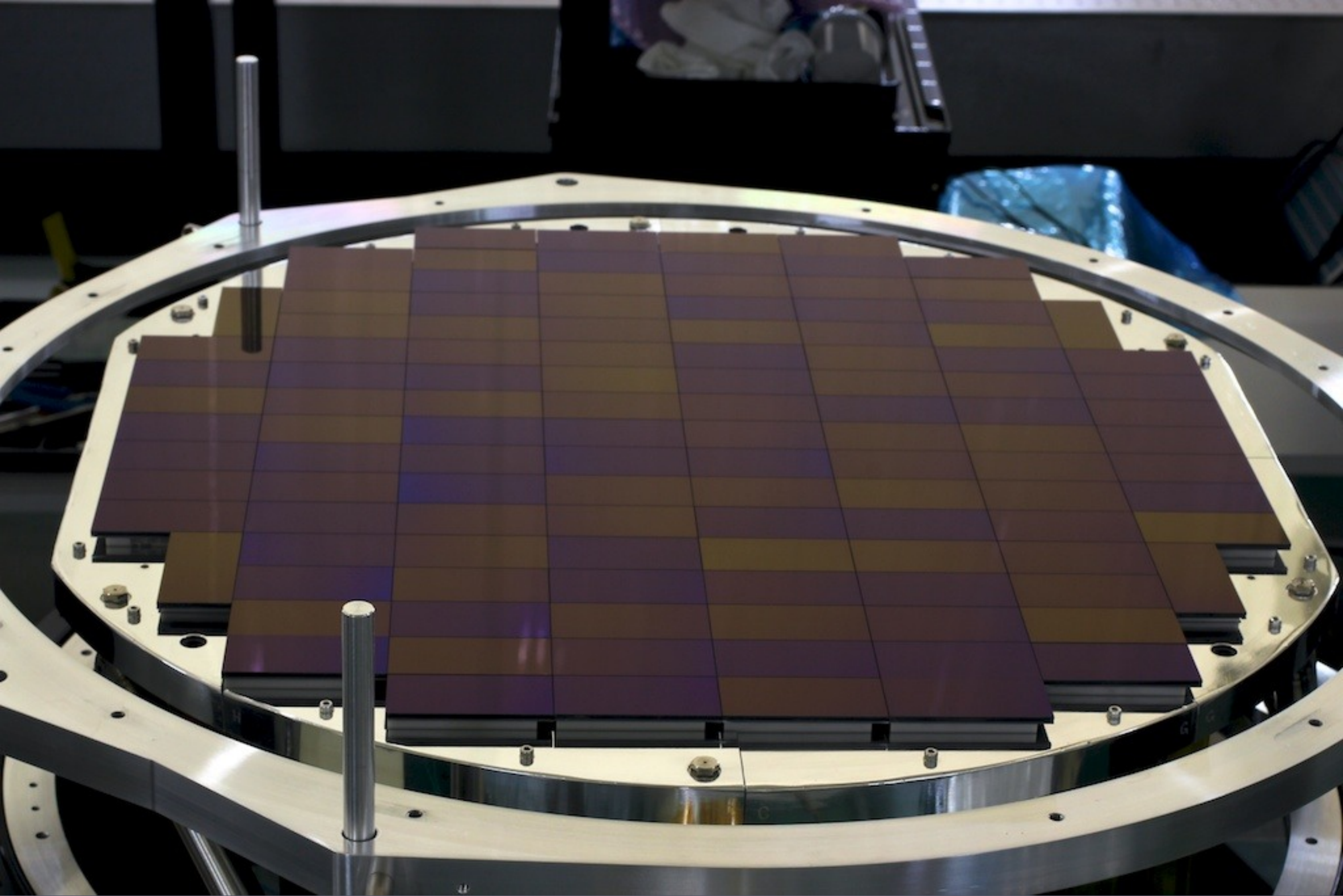


Figure 4.6: Fractional errors in measuring the angular diameter distance and the Hubble expansion rate for each redshift slices for the different BAO surveys, SDSS, BOSS and PFS. For the PFS survey we assumed survey parameters given in Table 4.3. The solid curves in each panel shows the fractional difference of  $D_A(z)$  or  $H(z)$  when changing the dark energy equation of state  $w$  to  $w = -0.9$  from  $w = -1$  ( $\Lambda\text{CDM}$  model).

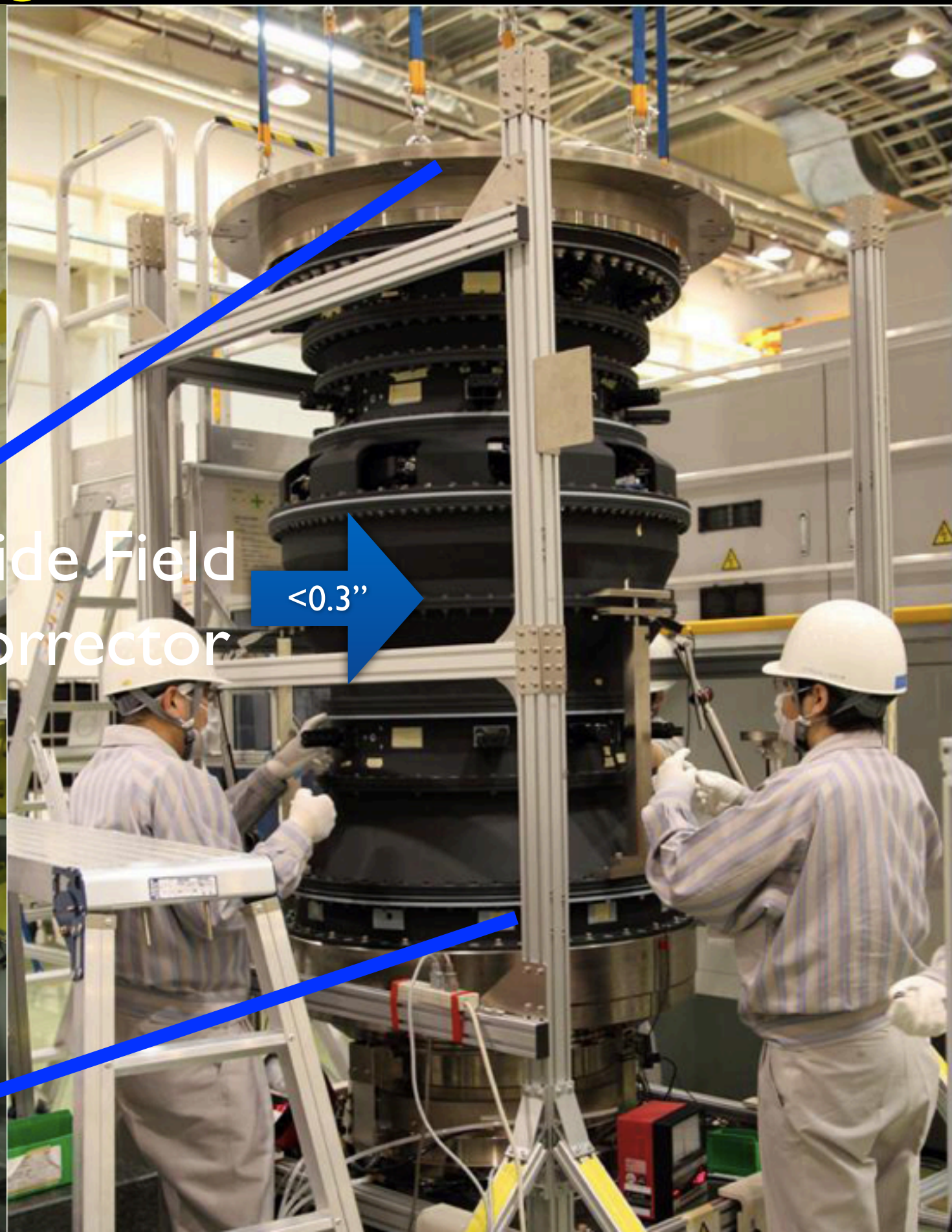
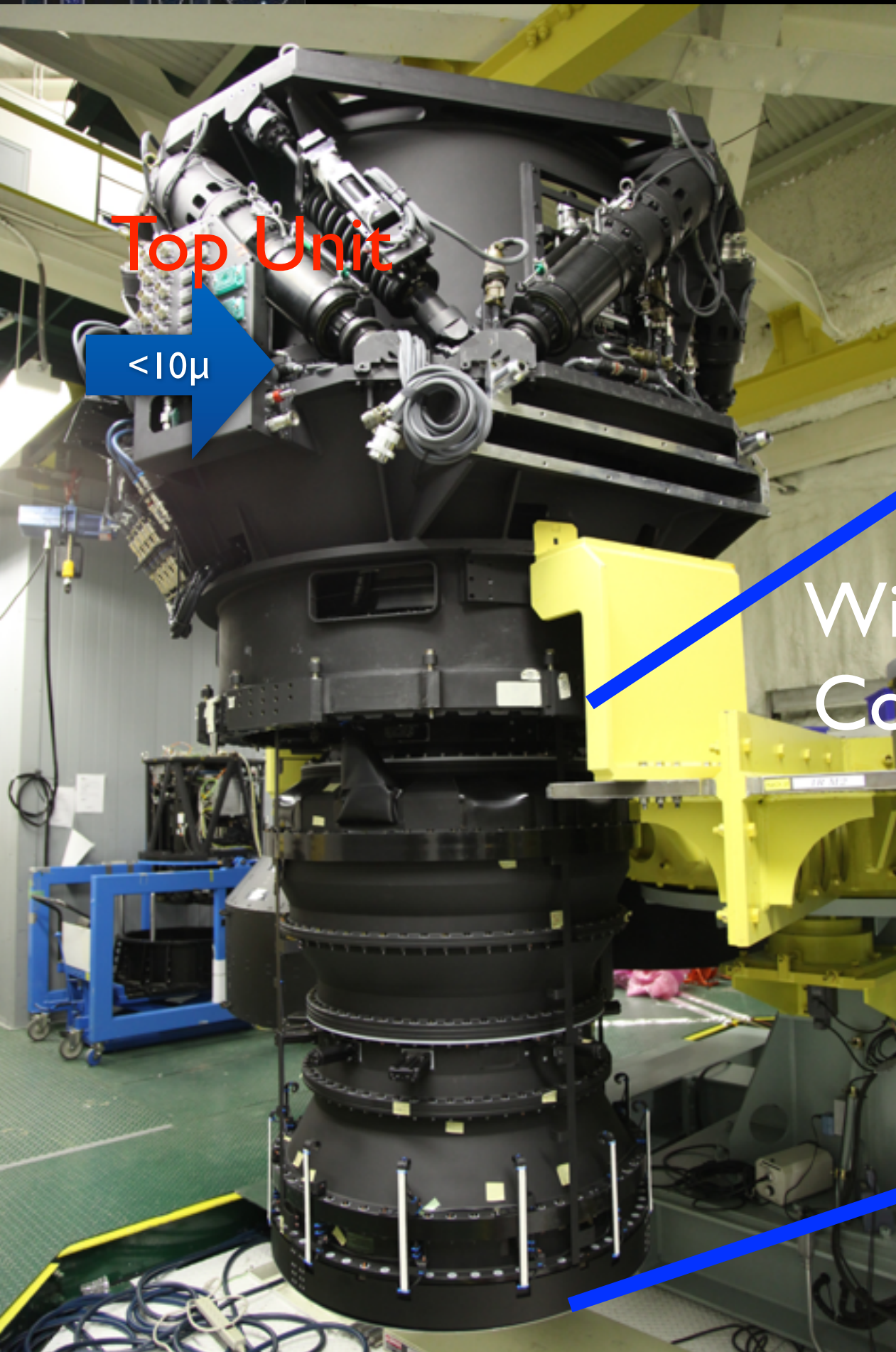




First Light later this year!



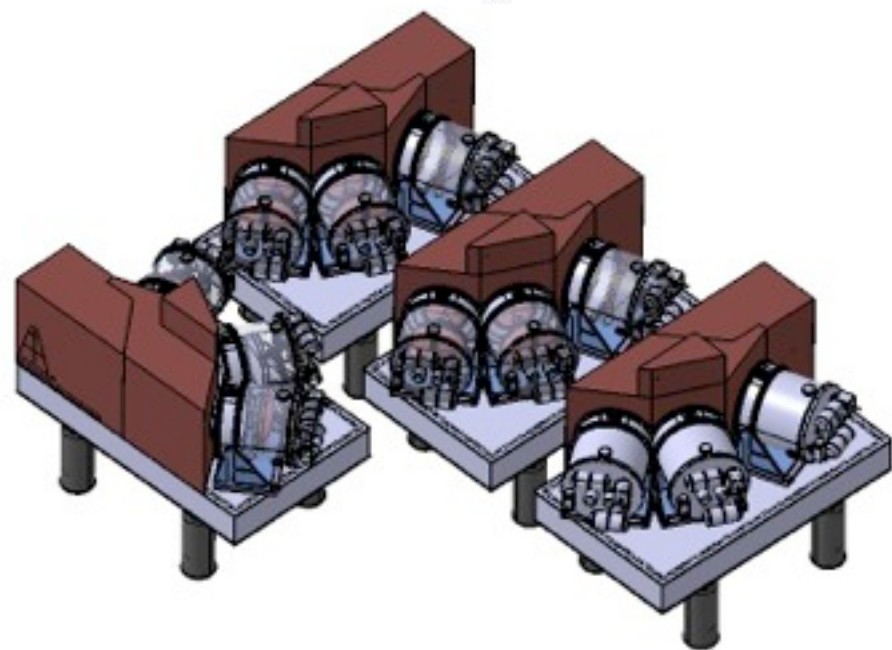
# World's Best Digital Camera: 3tons!





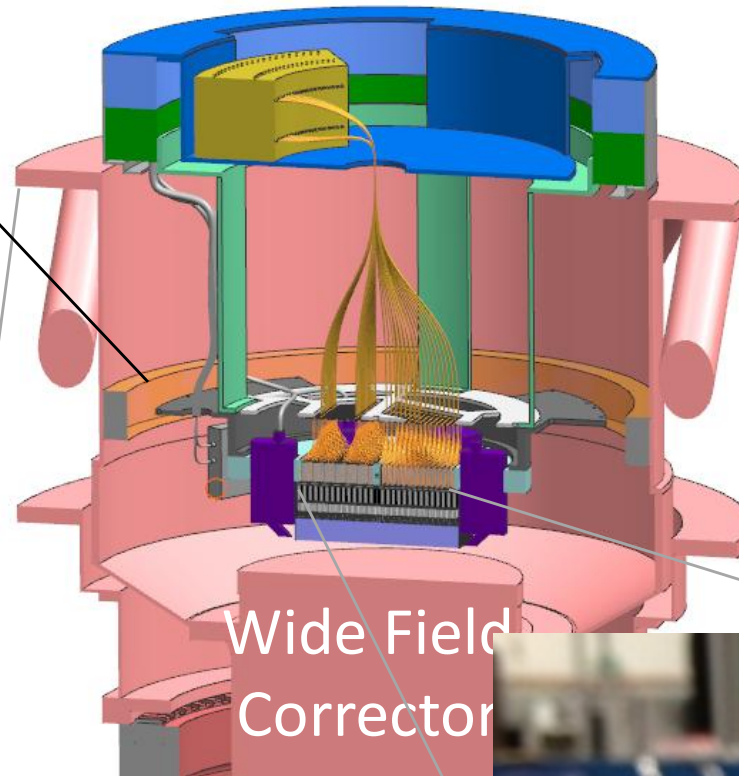
camera:  
Princeton, JHU

metrology: ASIAA



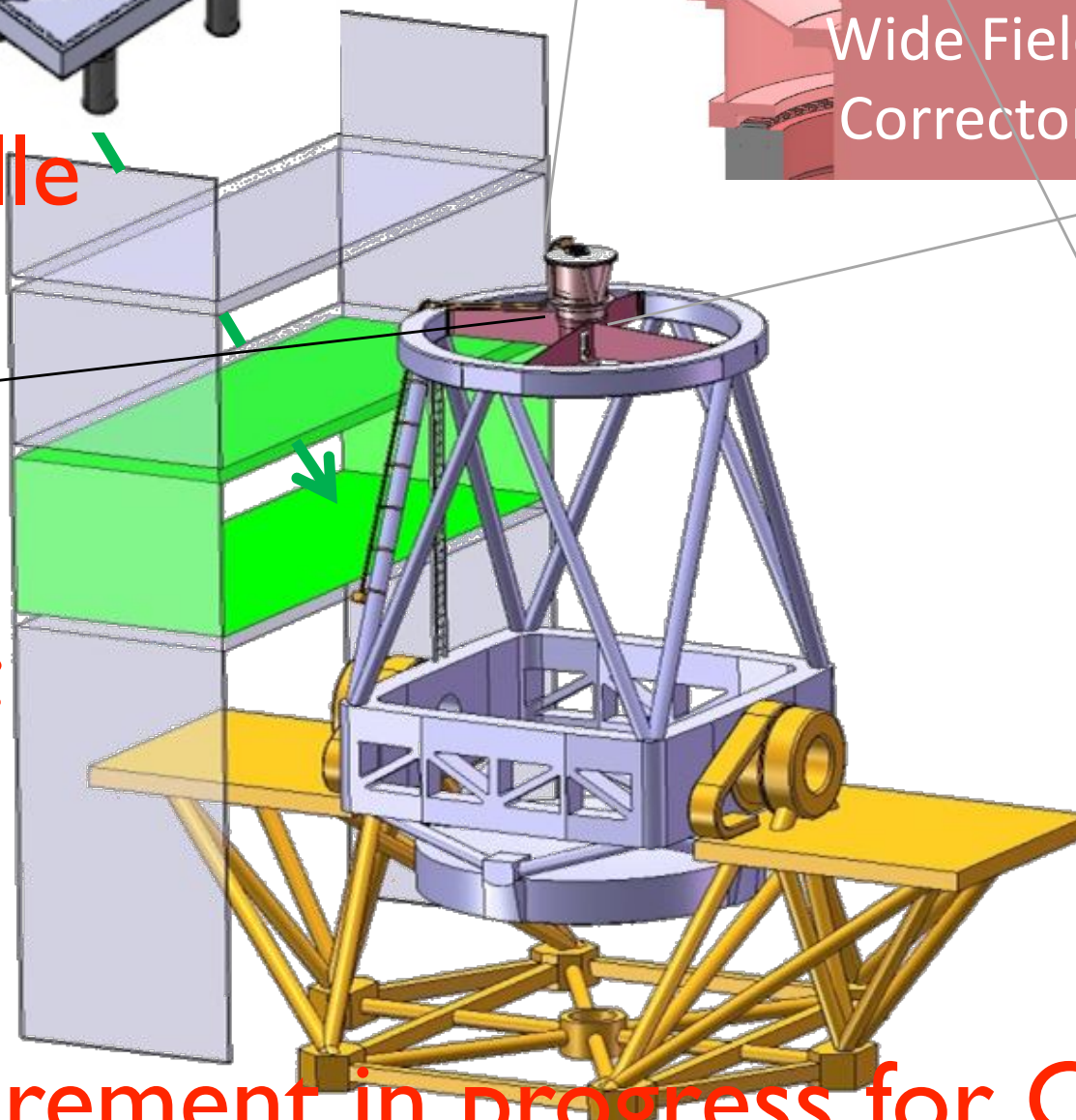
Prime Focus Instrument

Rotator



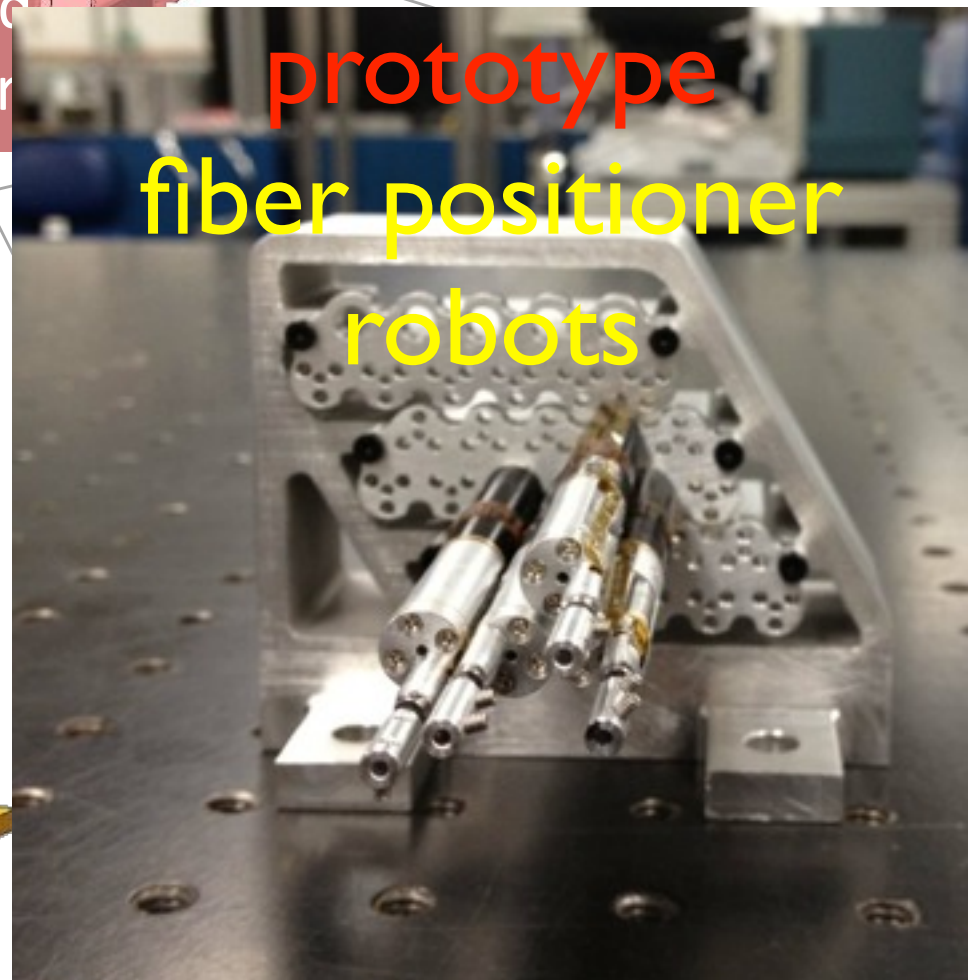
optics: Marseille

Fiber Connector



2400 fibers:  
Brazil

prototype  
fiber positioner  
robots



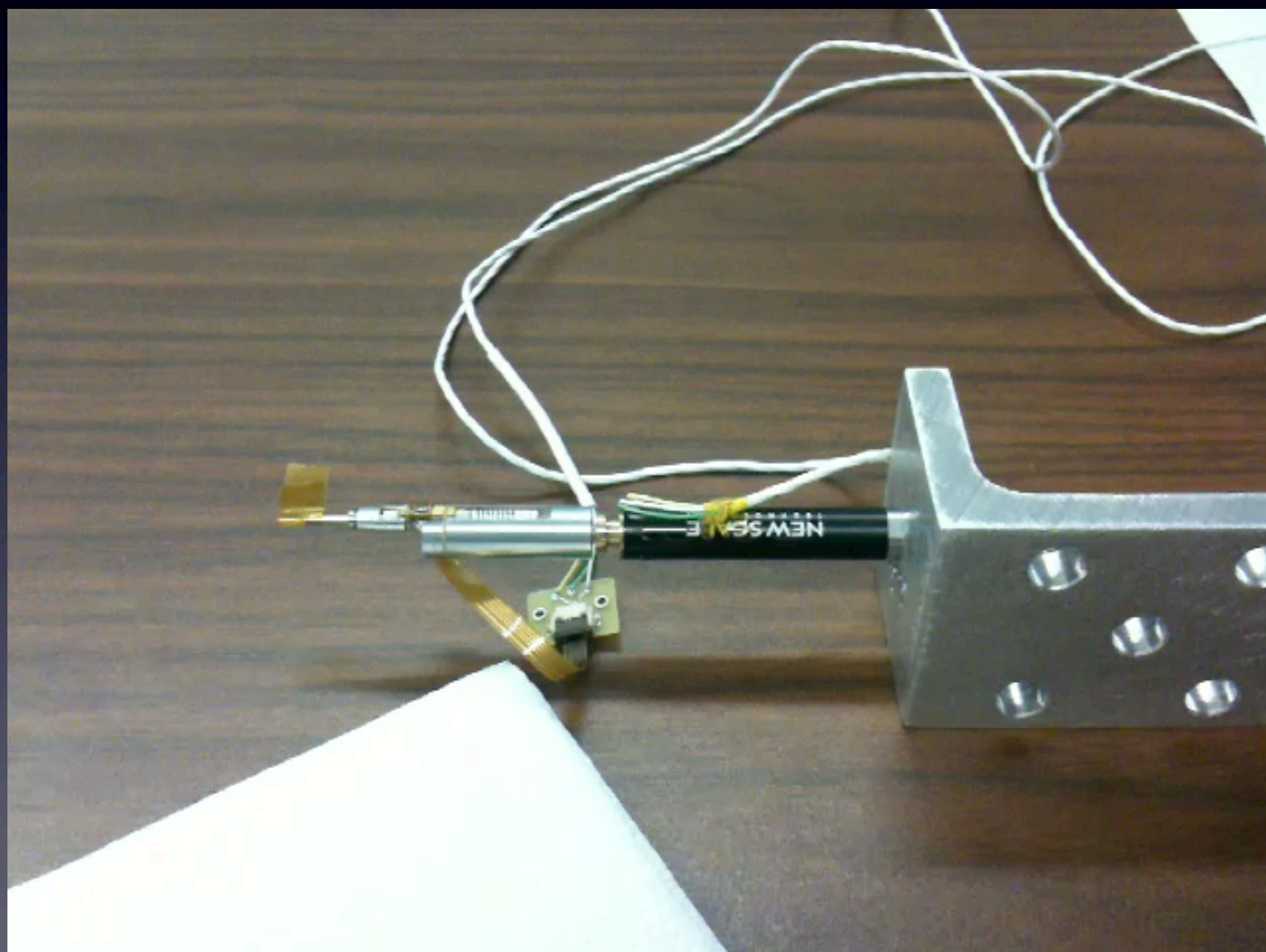
Fiber Positioner

Cobra

procurement in progress for CCD, gratings



# fiber positioner JPL Cobra design



pointing accuracy  $\sim 10\mu$  in  $\sim 40$  seconds



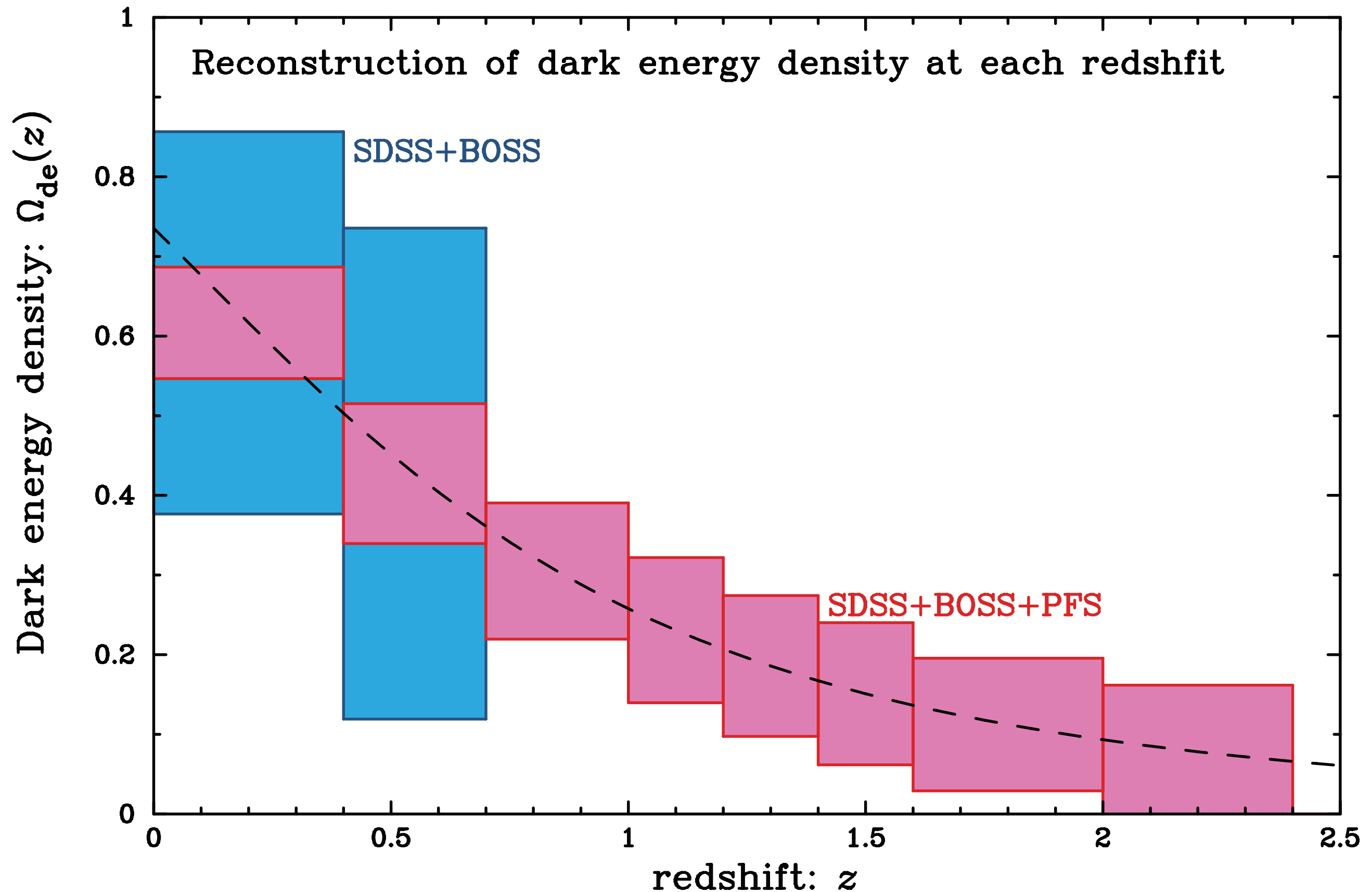
# 2nd PFS collaboration meeting 1/8, 9, 2012

## a big momentum building up!





# map out evolution history







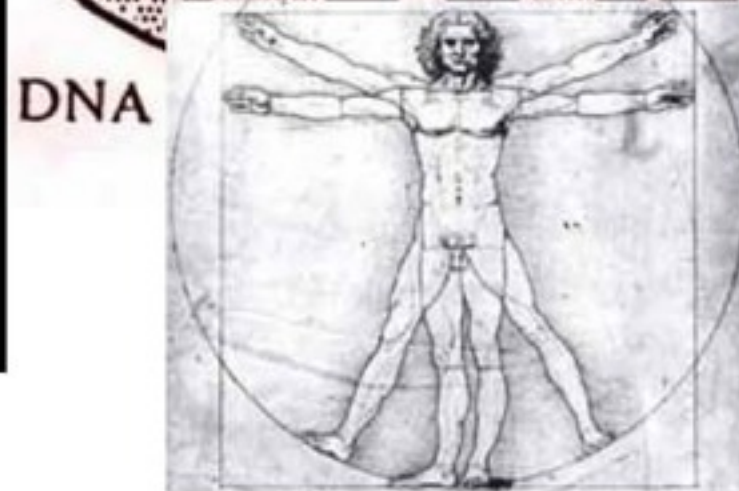
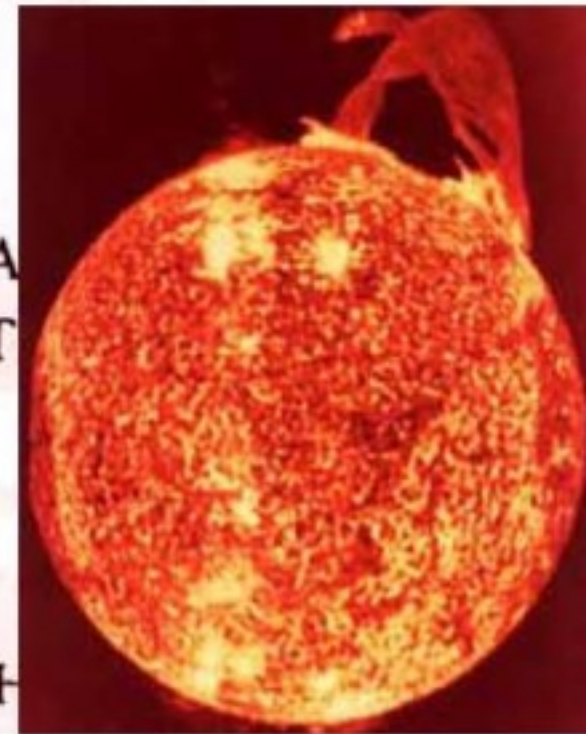
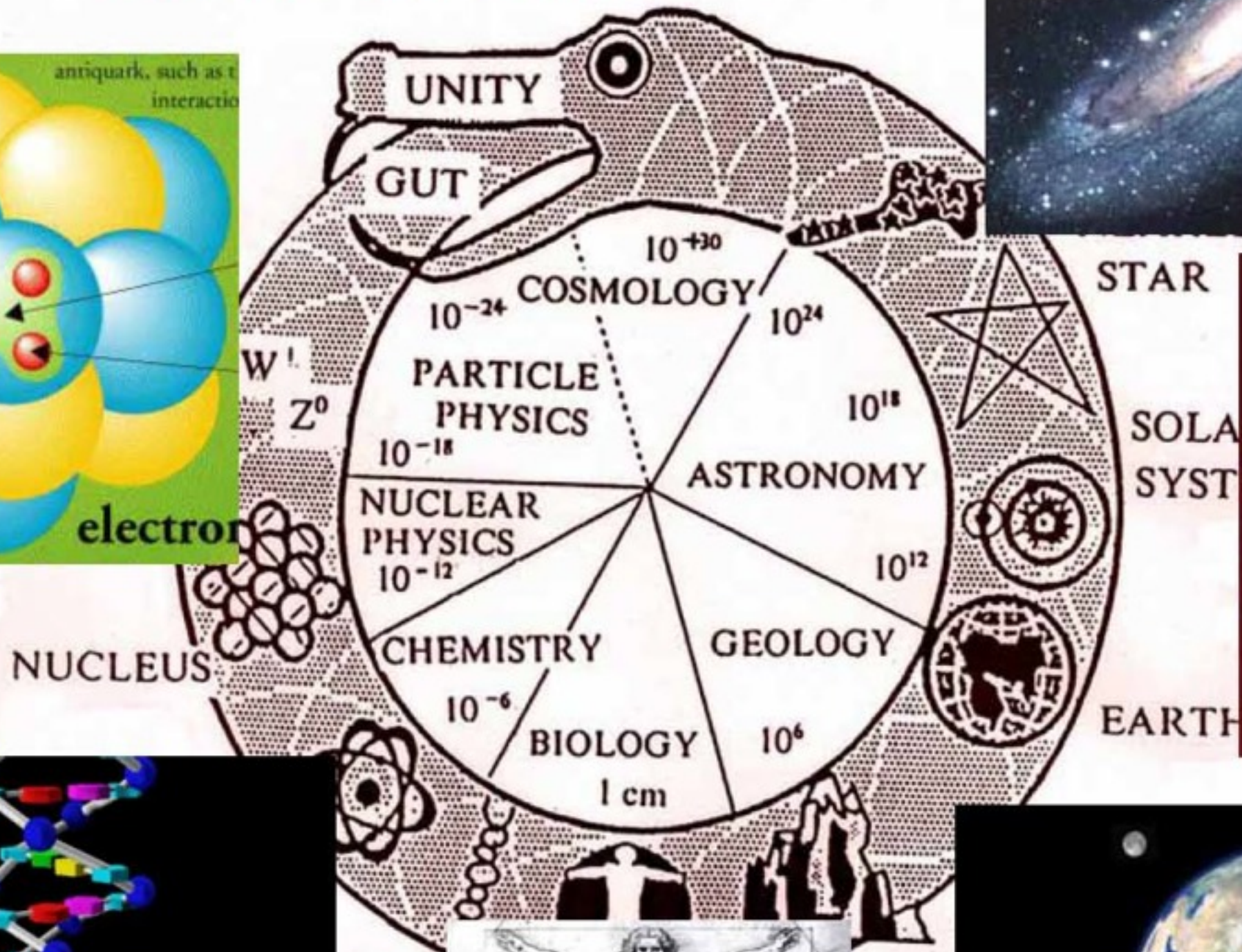
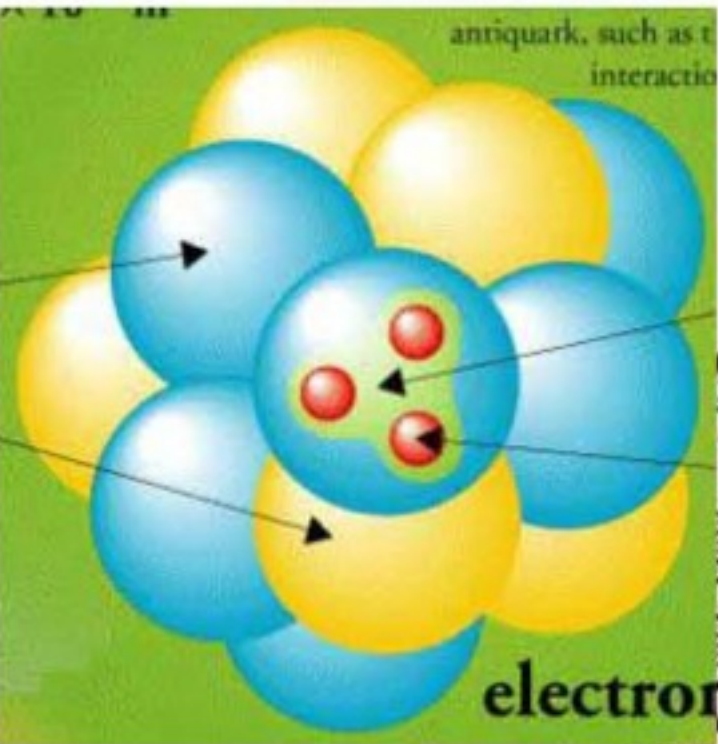
# PFS Rocks!

*Subaru Prime Focus Spectrograph*

<http://sumire.ipmu.jp/pfs/intro.html>



# Snake of Sizes







dark side

HEP  
astro