



Exploration of Hot QCD Matter

The Next Decade

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August 16 - September 10, 2010

Phases of exploration

Phases of exploration



Smoking Gun
Phase

Phases of exploration



Smoking Gun
Phase



Charting
the Territory
Phase

Phases of exploration



Smoking Gun
Phase



Charting
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Phase

Tourist
Attraction
Phase



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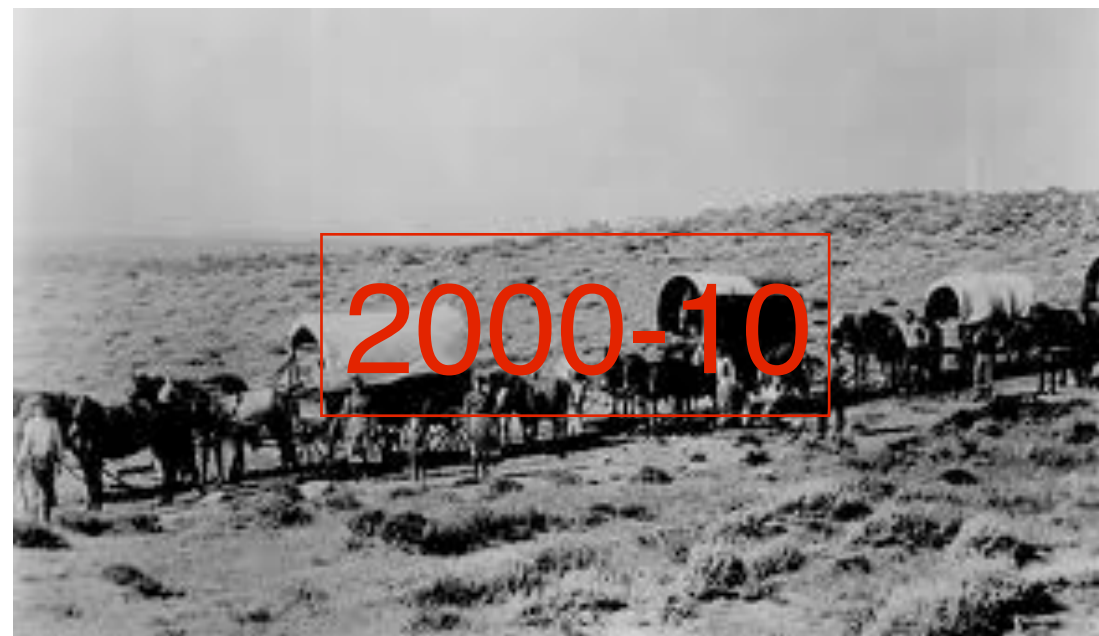
Tourist
Attraction
Phase



Phases of exploration

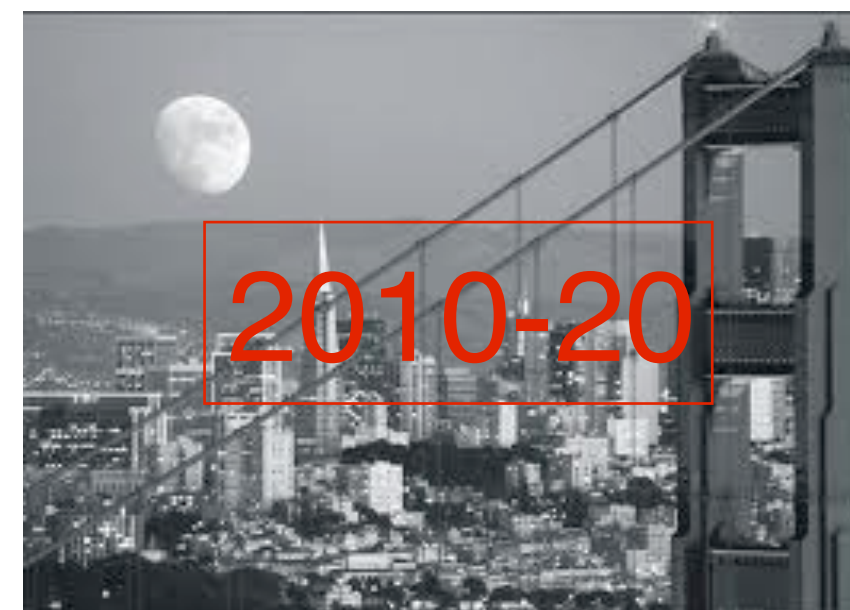


Smoking Gun
Phase



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Phases of exploration



Smoking Gun
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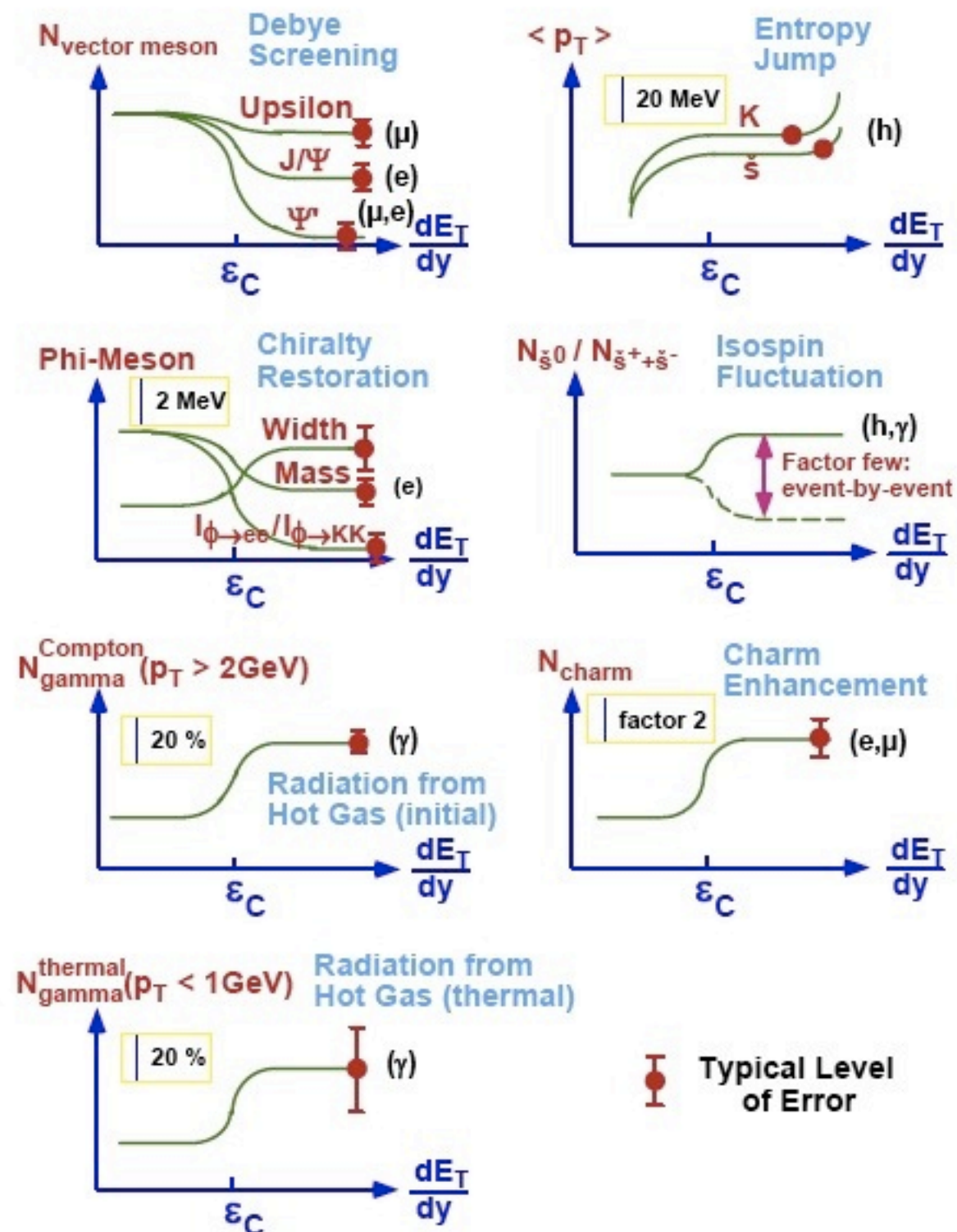


Charting
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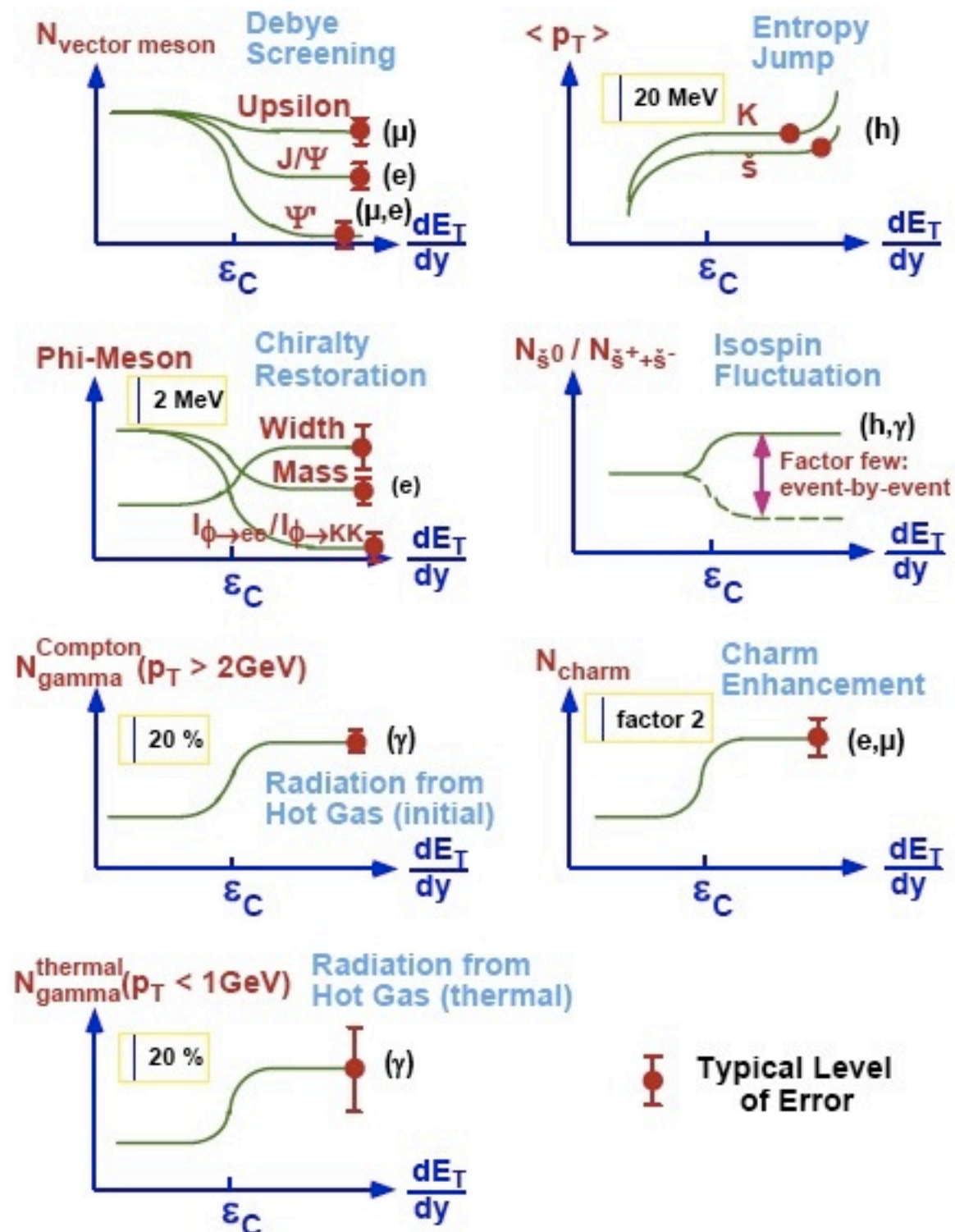
Tourist
Attraction
Phase



Smoking guns - NSAC style



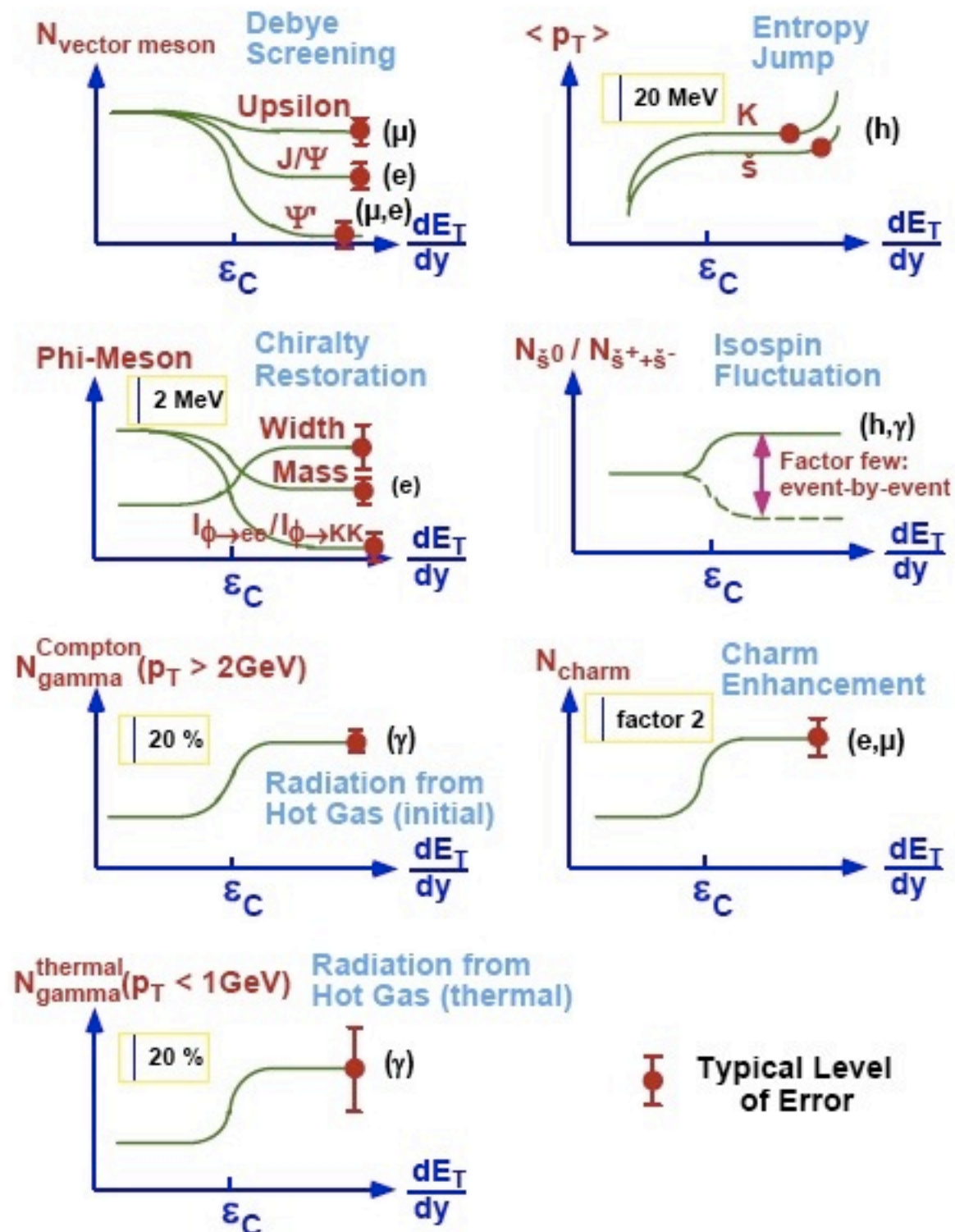
Smoking guns - NSAC style



But note what's missing:

- Jet quenching !
- Elliptic flow !!
- Quark recombination !!!
- Shear viscosity !!!!
- Critical point !!!!!

Smoking guns - NSAC style



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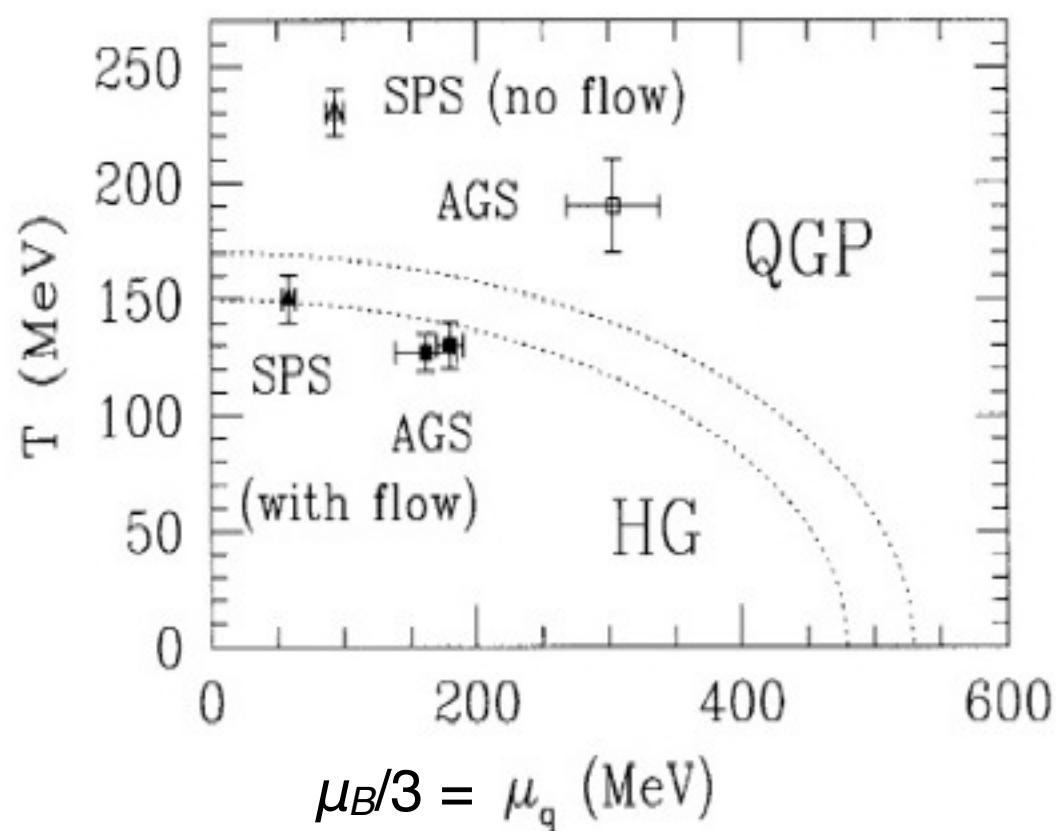
- Jet quenching !
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Disclaimer:

If the 1995 NSAC Committee could not accurately predict the future of heavy ion physics, would you expect **me** to be able to do so ???

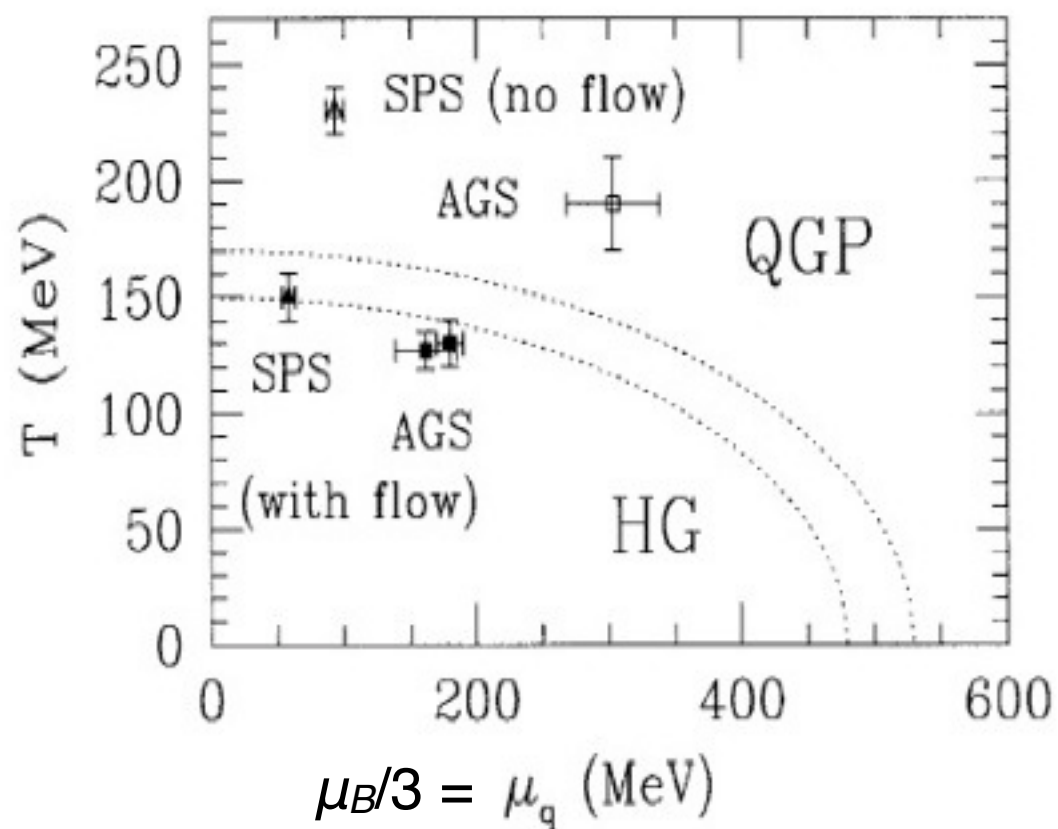
Charting the territory

Experimental evidence
for the QCD phase boundary
[B.M., NPA 590 (1995) 3c]

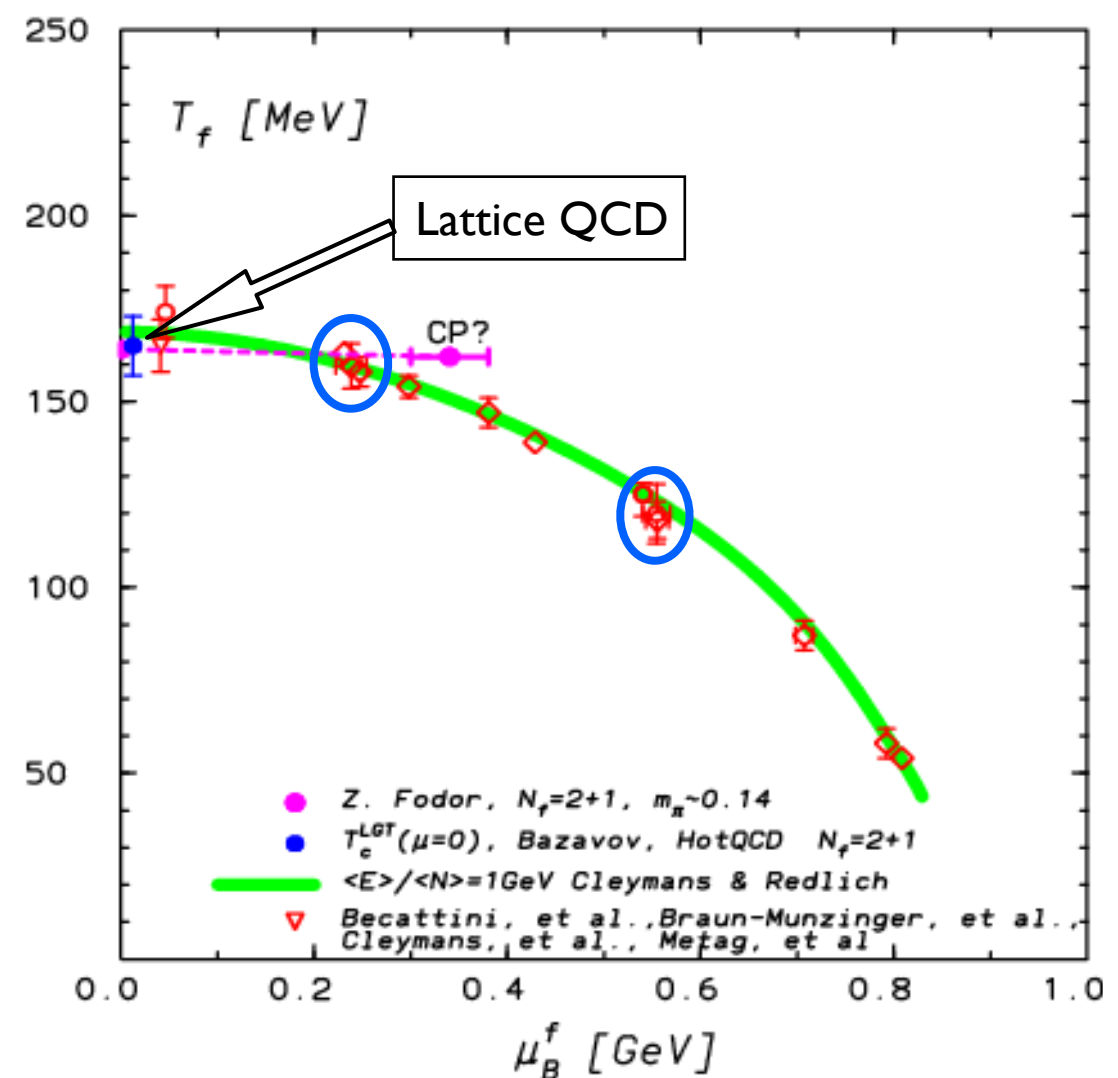


Charting the territory

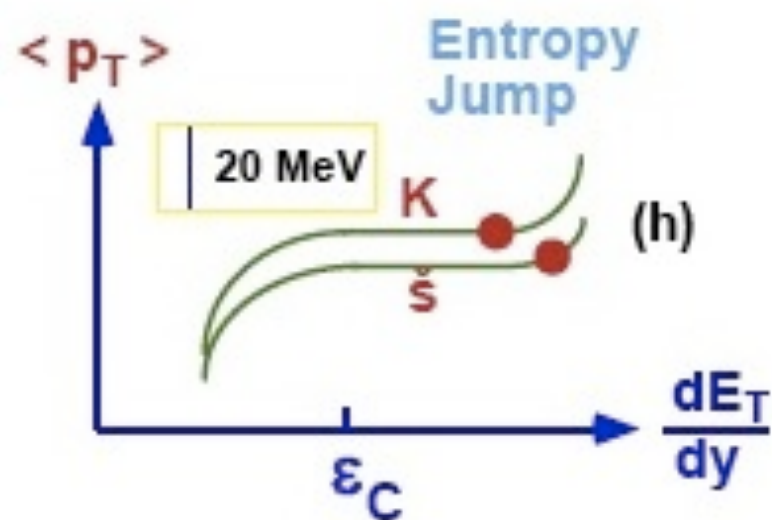
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Experimental evidence
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[K. Redlich, 2010]



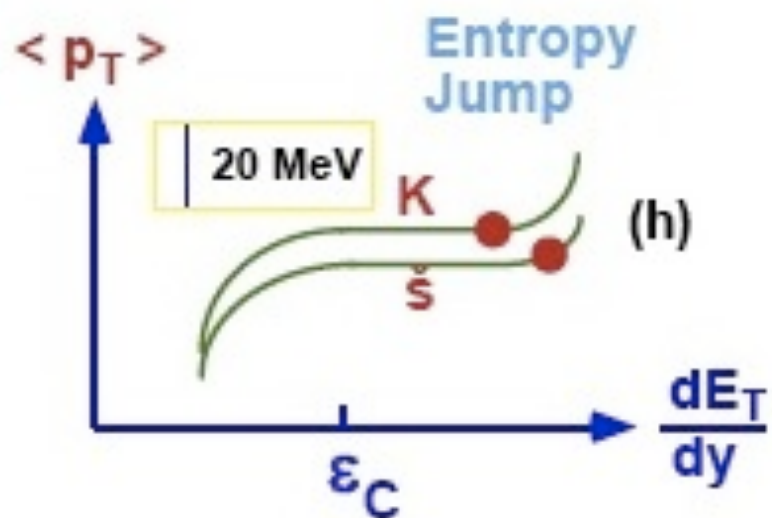
Was van Hove right?



Signal of a phase transformation:

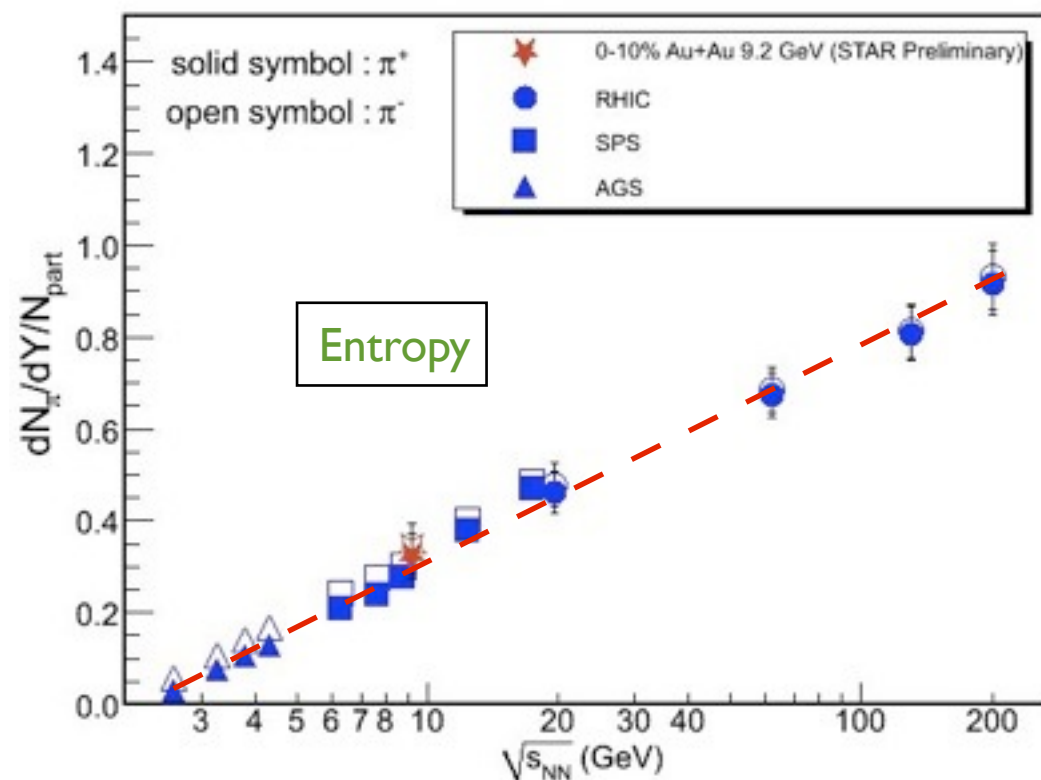
S-shaped relationship between $\langle p_T \rangle$ and energy density or entropy, where the flat region spans the domain in which frozen degrees of freedom (color) are unthawed.

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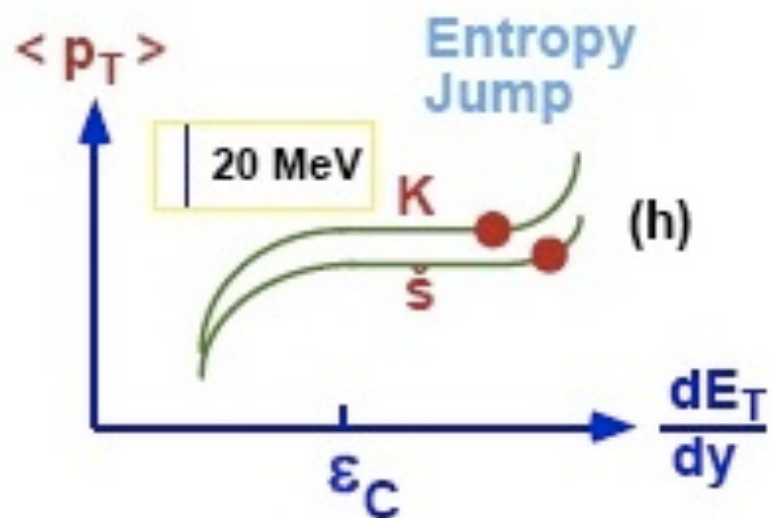


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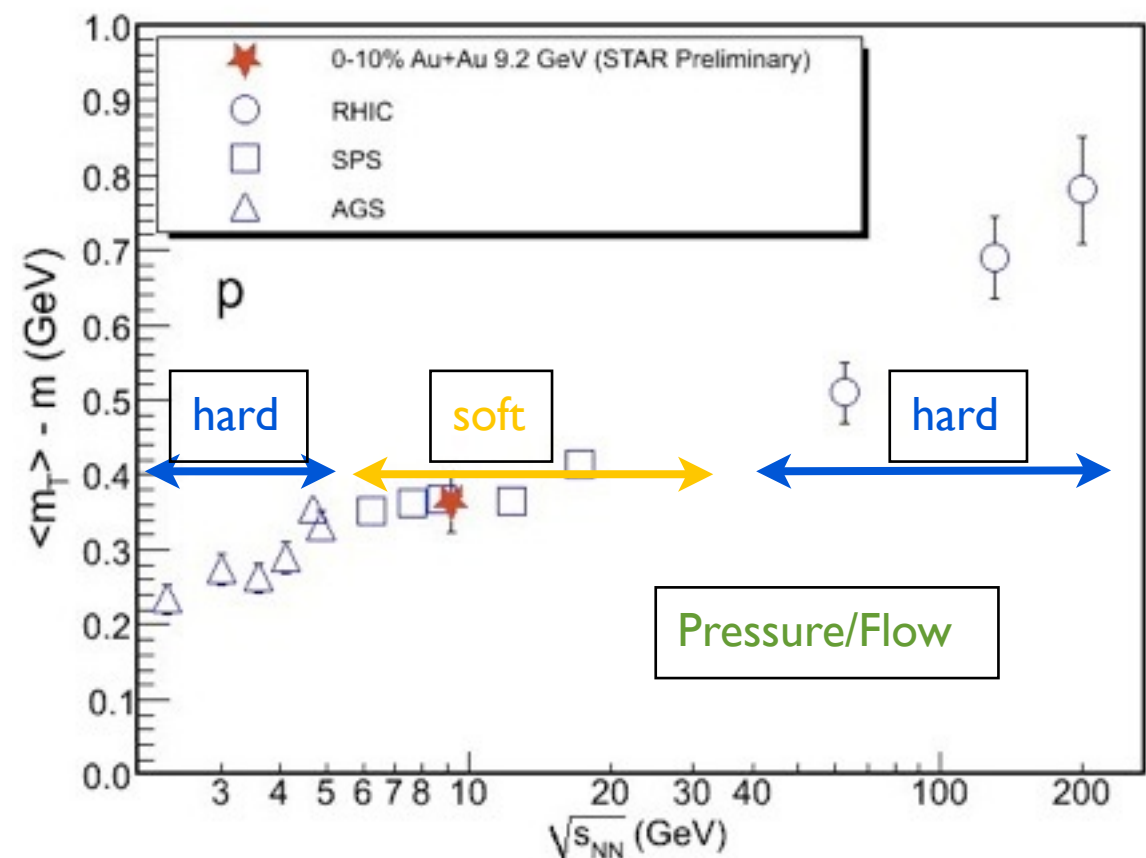
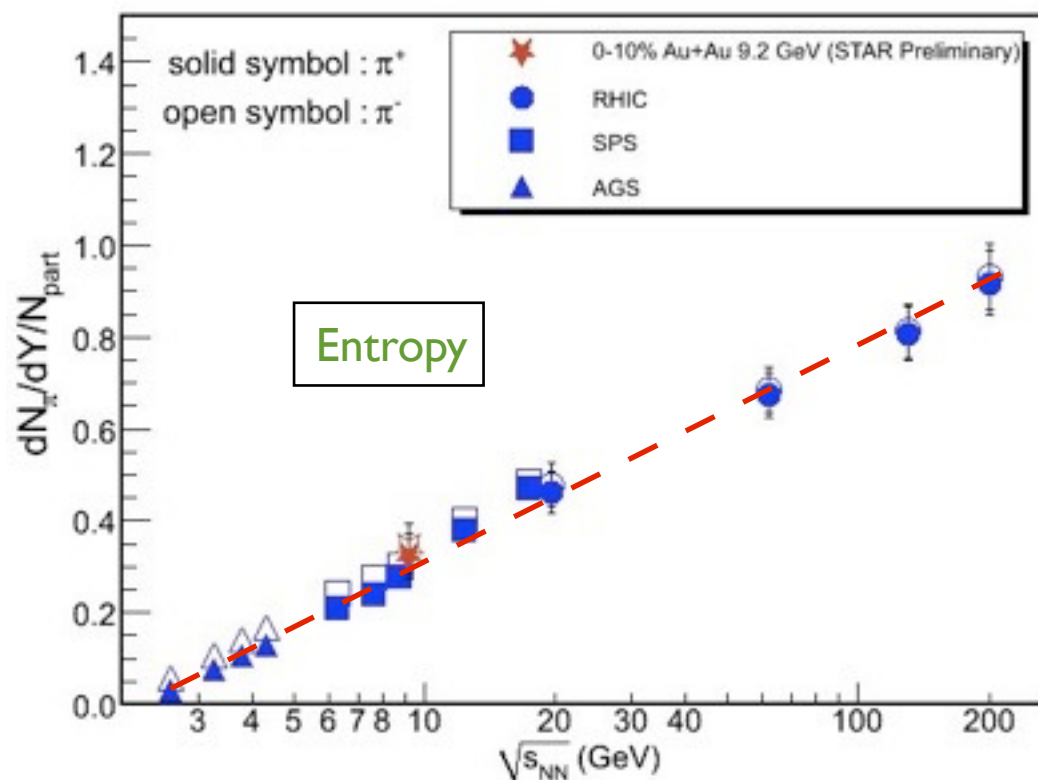


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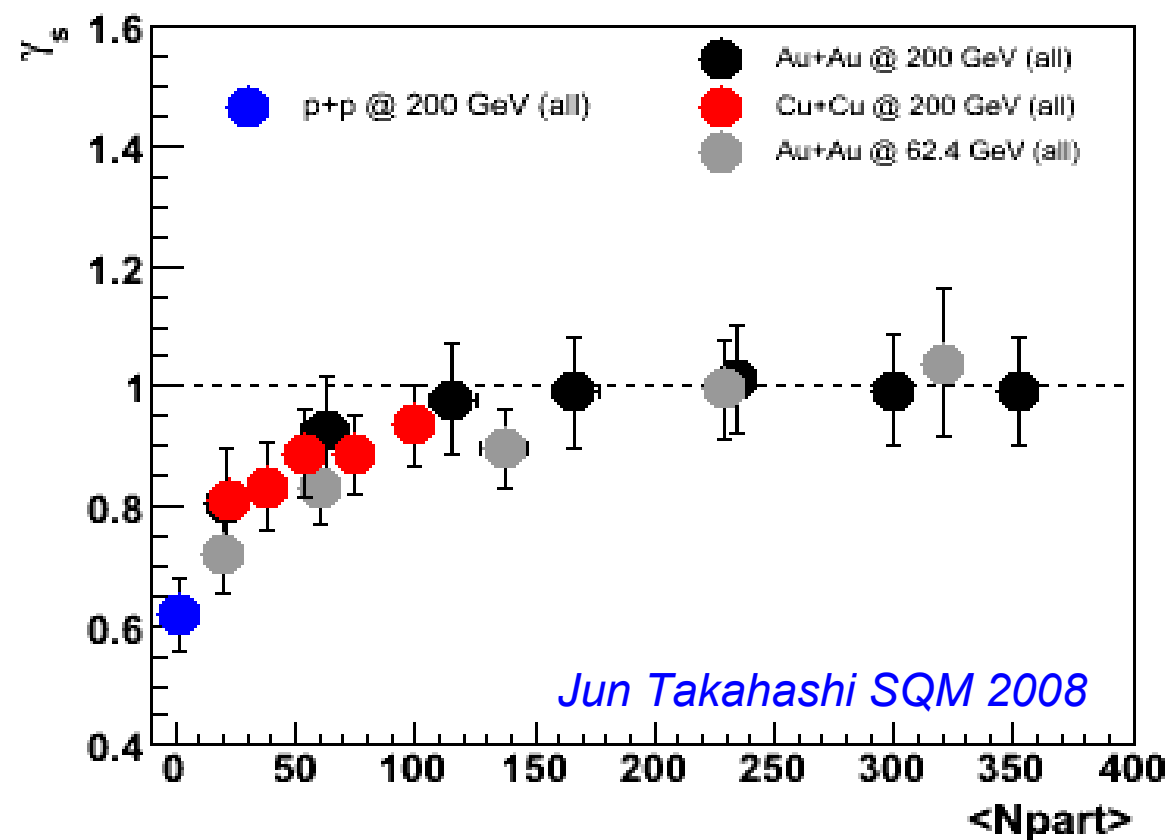
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Chemical tracers

Strange quarks *are* chemically equilibrated at hadronization of the quark-gluon plasma

Strangeness saturation

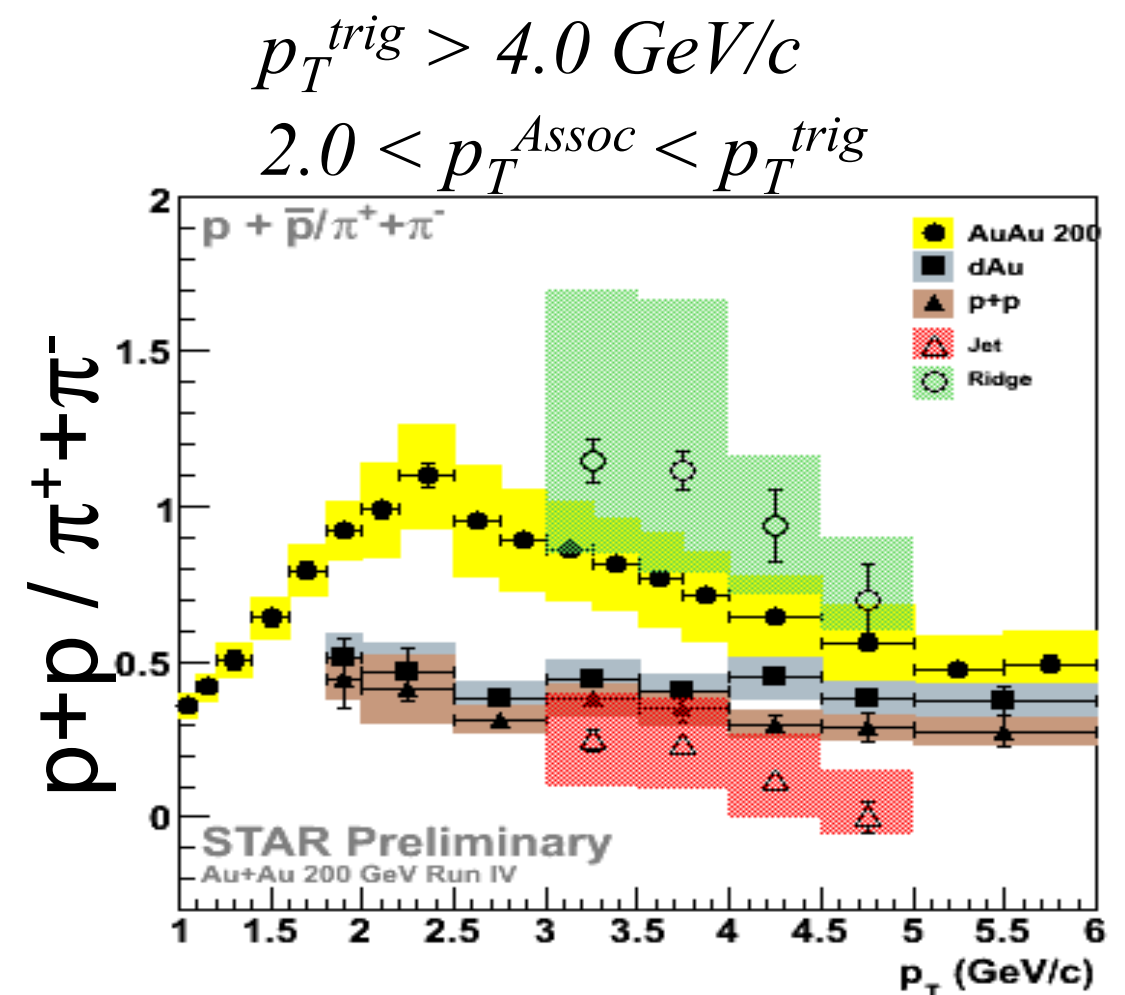
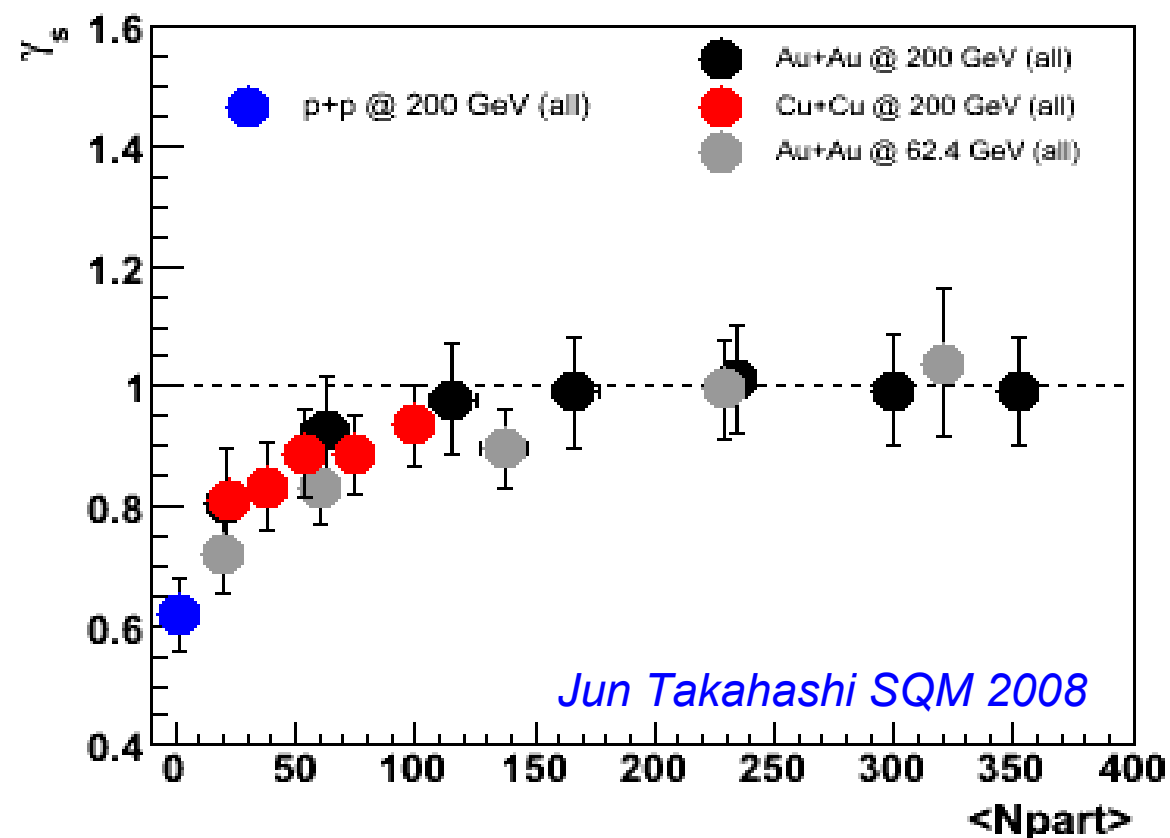


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Hadrochemistry was put to good use demonstrating that the “hard” ridge is composed of bulk matter, not jet fragments

Strangeness saturation





■ Theory breakthroughs of 2000-10:

- Application of gauge-gravity duality to strongly coupled plasma
- “Universal” quantum limit of (shear) viscosity
- Consistent theory of relativistic dissipative fluid dynamics
- *Ab initio* QCD equation of state at $\mu_B = 0$
- *Qualitative* connection between properties and observables
- *Conceptual* theory of the low- x parton structure of nuclei

Hot QCD matter (I)

Which **properties of hot QCD matter** can we hope to determine from relativistic heavy ion data (RHIC and LHC, maybe FAIR) ?

$$T_{\mu\nu} \Leftrightarrow \varepsilon, p, s \quad \text{Equation of state: spectra, coll. flow, fluctuations}$$

$$c_s^2 = \partial p / \partial \varepsilon \quad \text{Speed of sound: multiparticle correlations}$$

$$\eta = \frac{1}{T} \int d^4x \langle T_{xy}(x) T_{xy}(0) \rangle \quad \text{Shear viscosity: anisotropic collective flow}$$

$$\left. \begin{aligned} \hat{q} &= \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{a+i}(y^-) F_i^{a+}(0) \rangle \\ \hat{e} &= \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle i\partial^- A^{a+}(y^-) A^{a+}(0) \rangle \\ \hat{e}_2 &= \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{a+-}(y^-) F^{a+-}(0) \rangle \end{aligned} \right\} \quad \text{Momentum/energy diffusion: parton energy loss, jet fragmentation}$$

$$m_D = - \lim_{|x| \rightarrow \infty} \frac{1}{|x|} \ln \langle E^a(x) E^a(0) \rangle \quad \text{Color screening: Quarkonium states}$$

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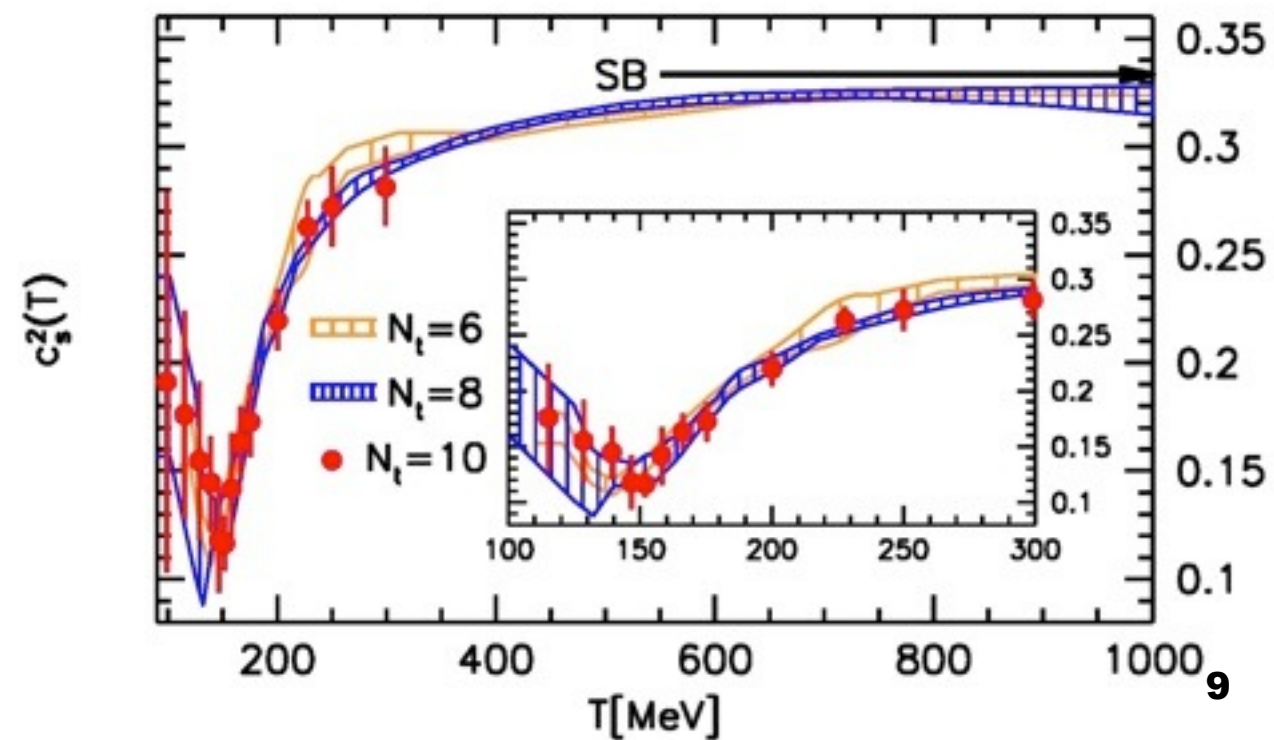
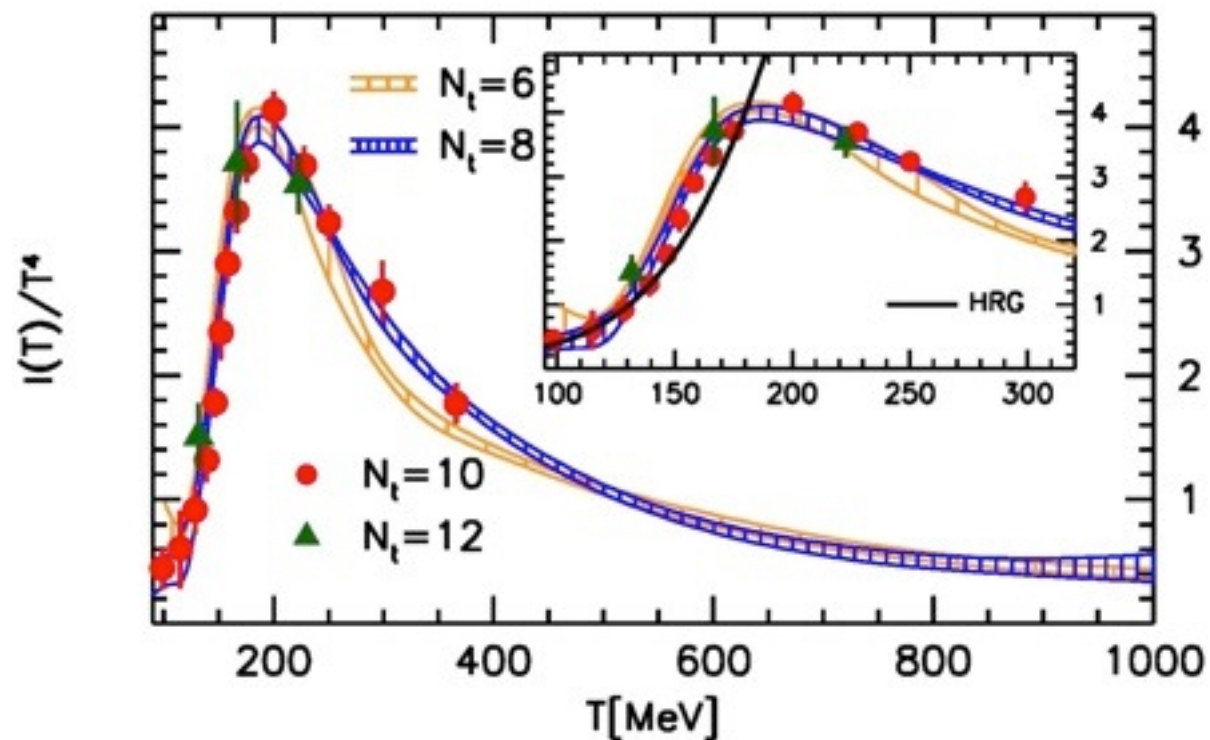
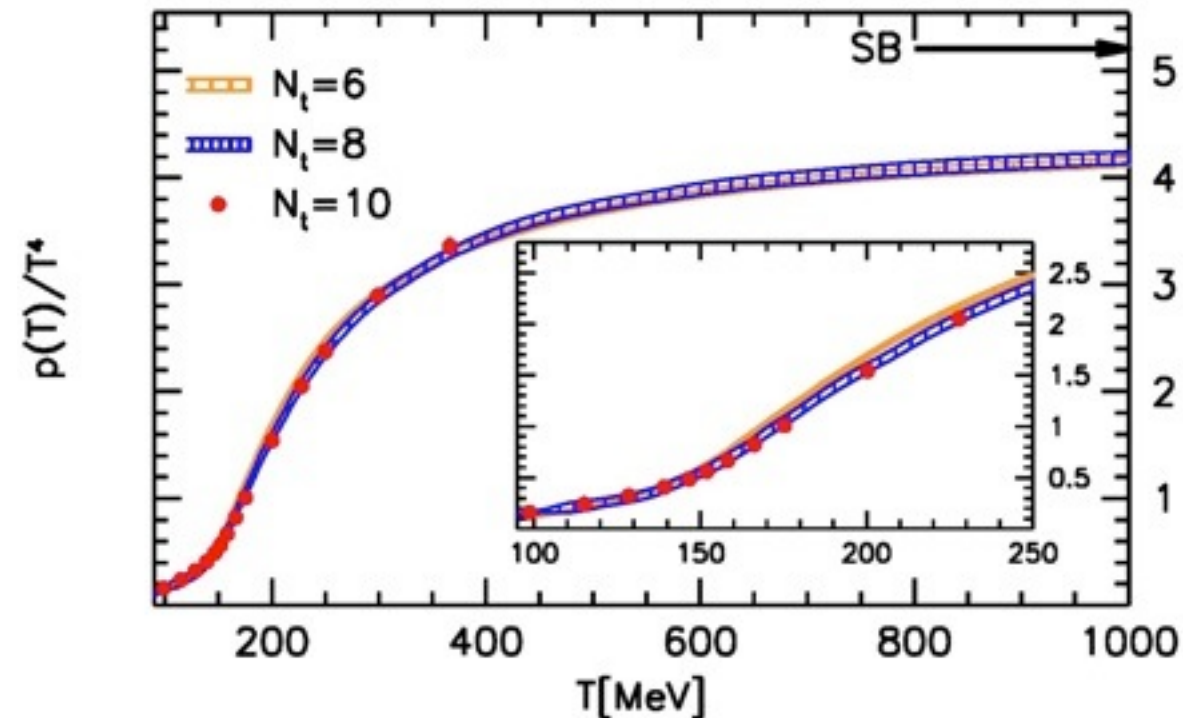
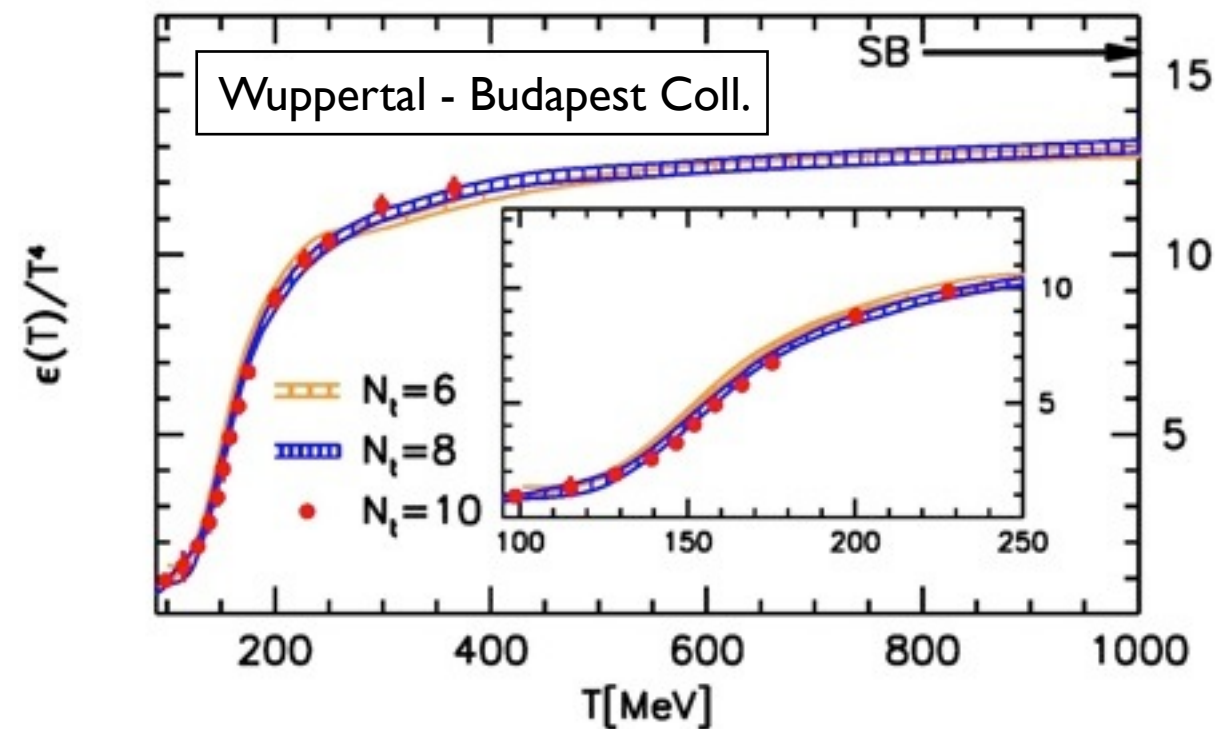
Momentum/energy diffusion:
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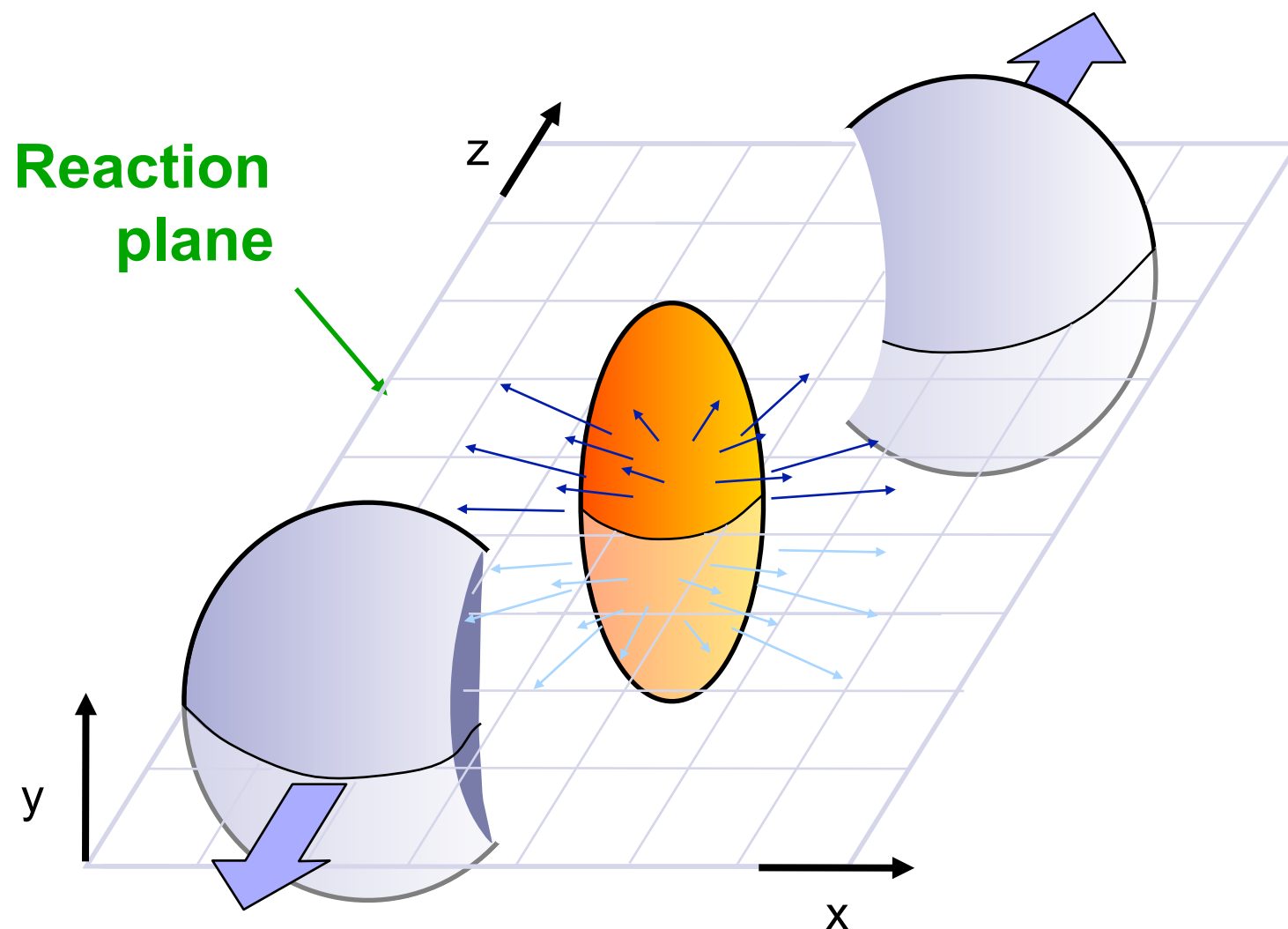
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Color screening: Quarkonium states

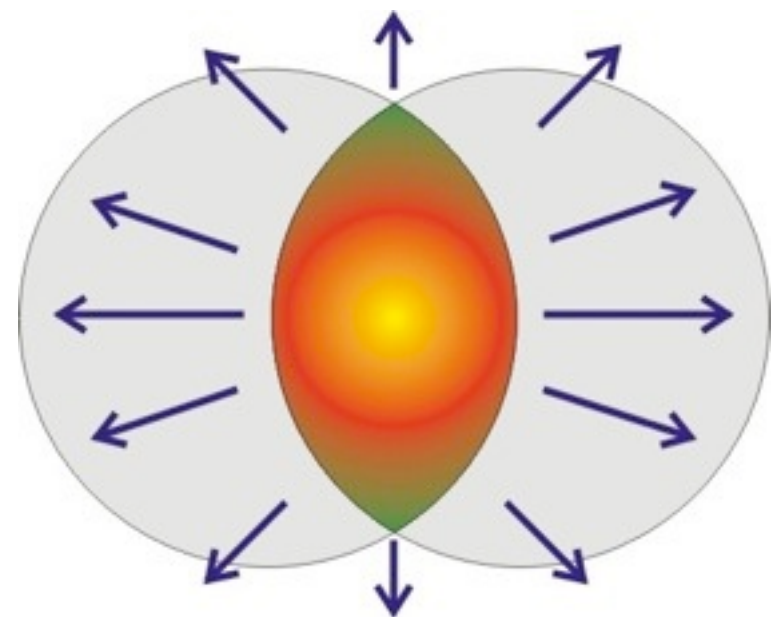
Lattice QCD - 2010



Elliptic Flow (v_2)



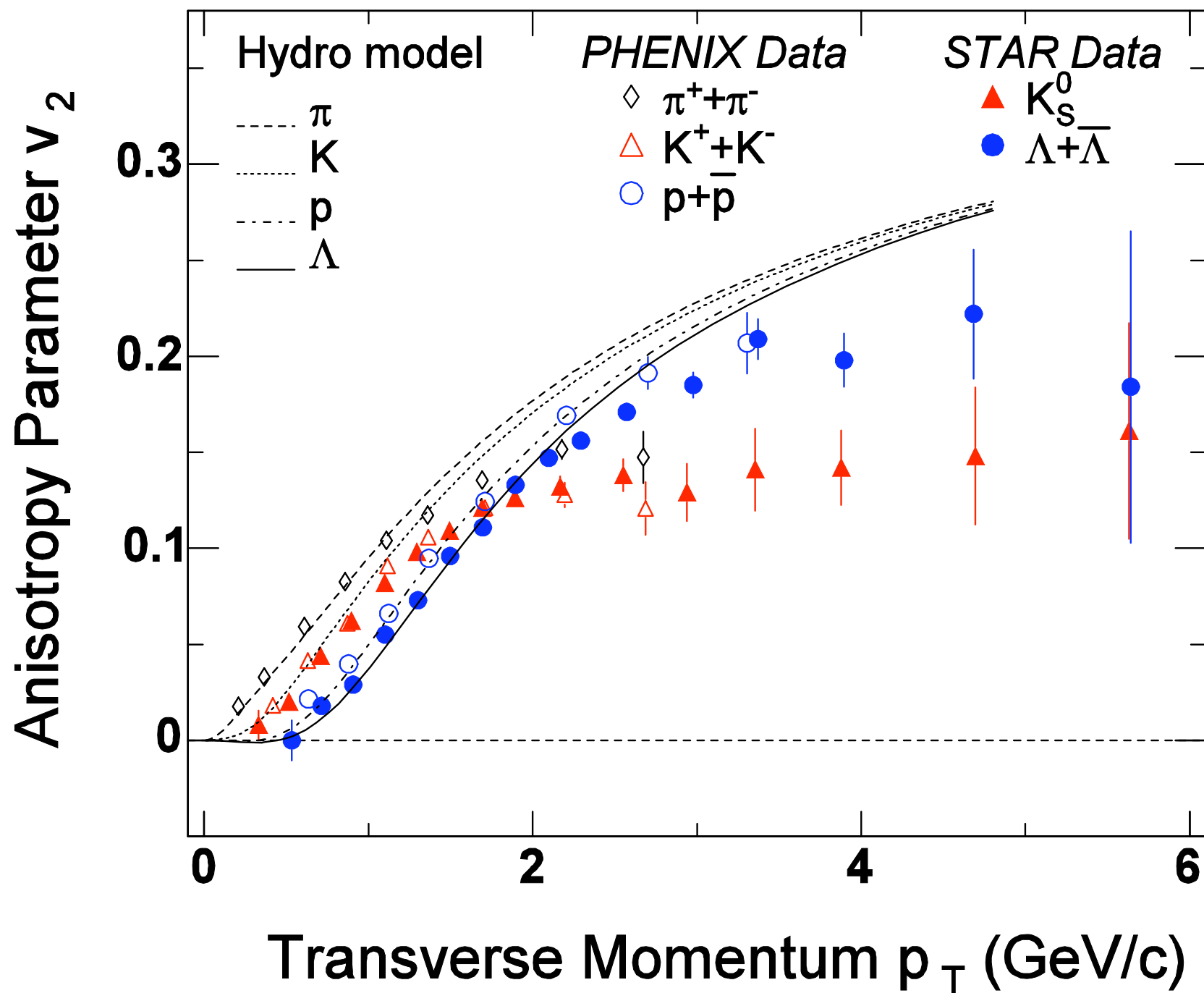
$v_2 = \cos(2\phi)$
coefficient of the
azimuthal distribution



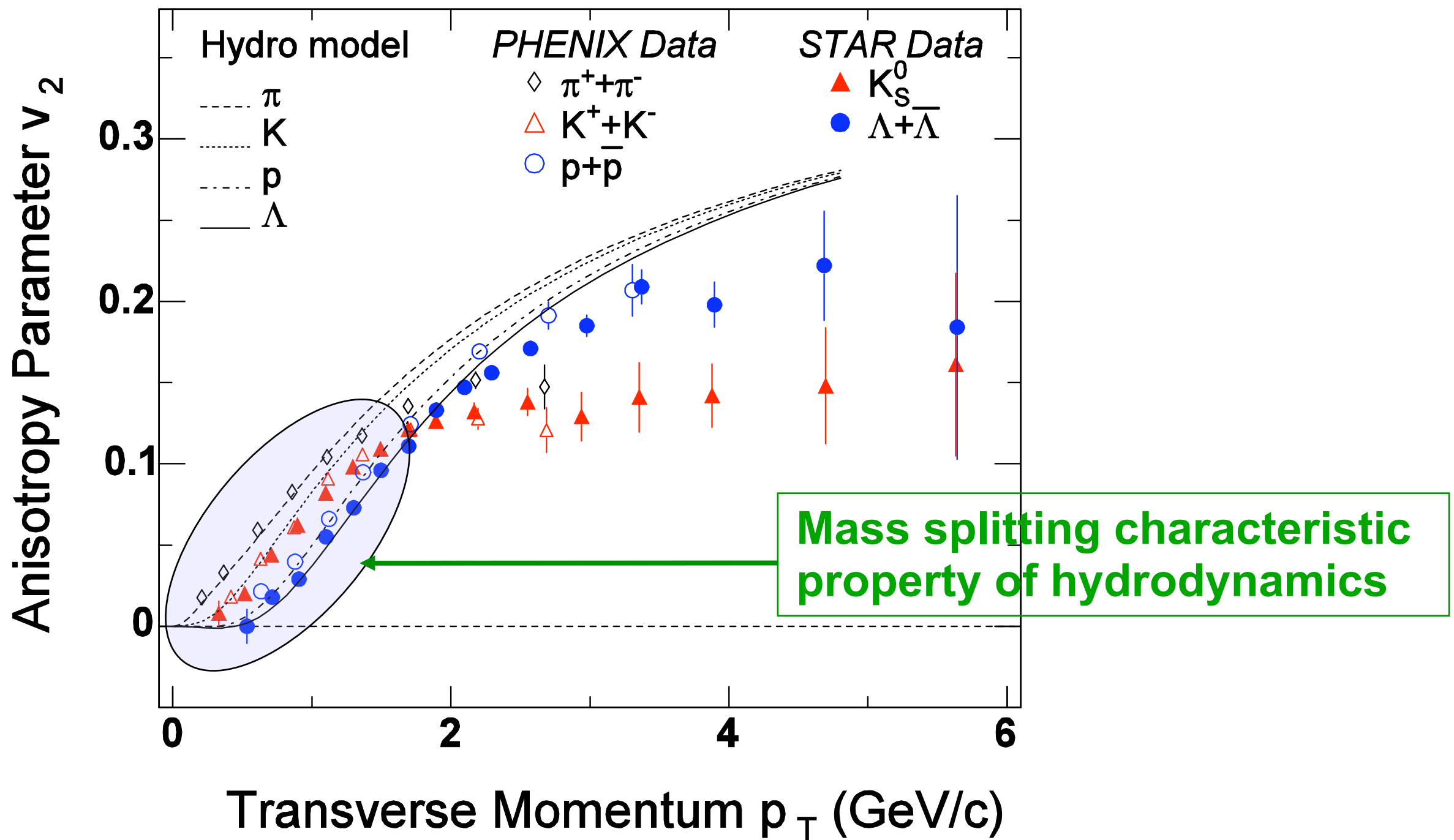
$$\nabla P(\leftrightarrow) > \nabla P(\updownarrow)$$

Hydrodynamics:
Flow is generated by ∇P

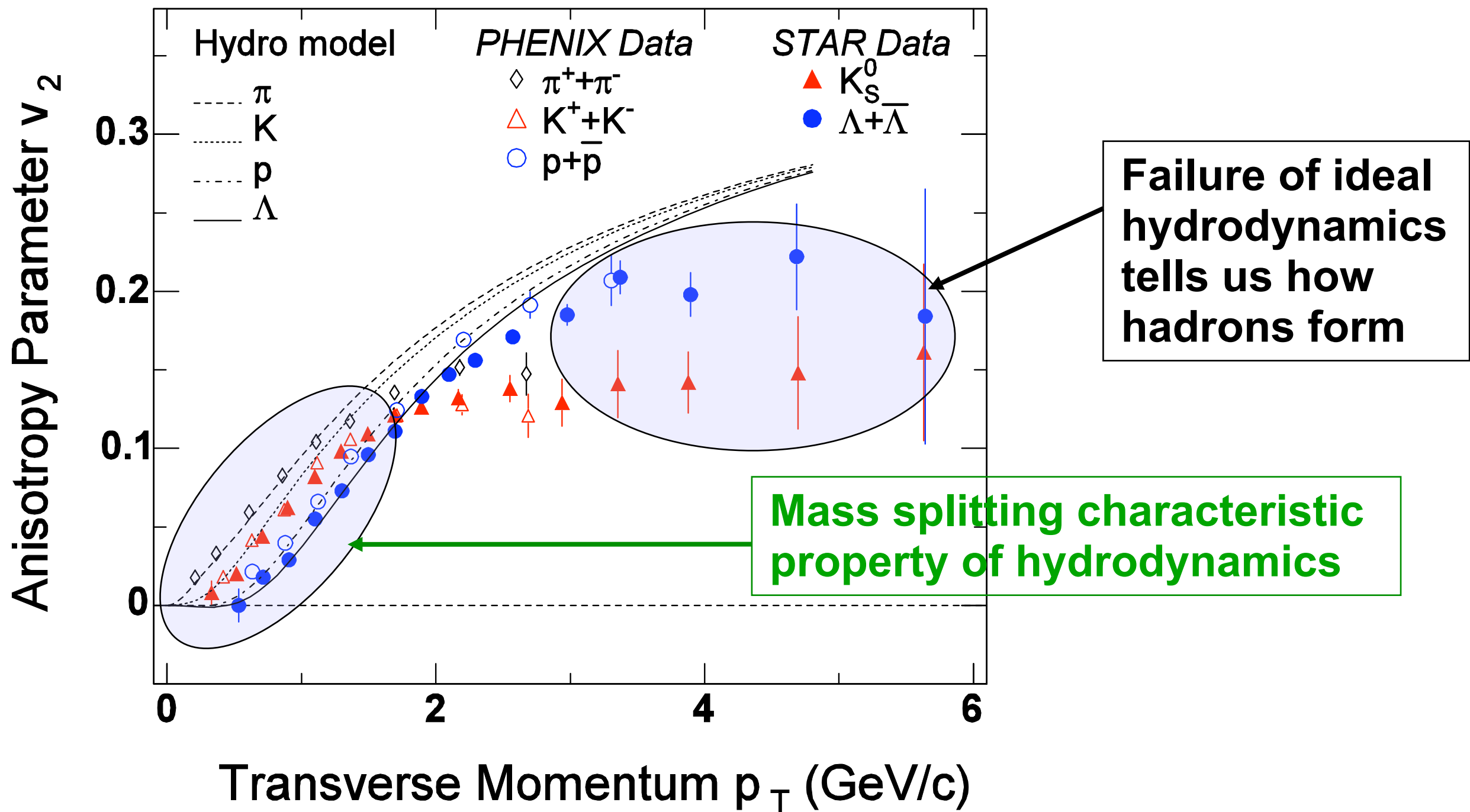
$v_2(p_T)$ vs. hydrodynamics



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Elliptic flow “measures” η_{QGP}

We finally have a **complete**,
causal formulation of
relativistic viscous
hydrodynamics:

$$\partial_\mu T^{\mu\nu} = 0 \quad \text{with} \quad T^{\mu\nu} = (\varepsilon + P)u^\mu u^\nu - P g^{\mu\nu} + \Pi^{\mu\nu}$$

$$\tau_\Pi \left[\frac{d\Pi^{\mu\nu}}{d\tau} + \left(u^\mu \Pi^{\nu\lambda} + u^\nu \Pi^{\mu\lambda} \right) \frac{du^\lambda}{d\tau} \right] = \underbrace{\eta}_{\text{Shear viscosity}} \left(\partial^\mu u^\nu + \partial^\nu u^\mu - \text{trace} \right) - \Pi^{\mu\nu}$$

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$$\begin{aligned} \Pi &= \Pi_{\text{NS}} - \tau_\Pi \dot{\Pi} \\ &+ \tau_{\Pi q} q \cdot \dot{u} - \ell_{\Pi q} \partial \cdot q - \zeta \hat{\delta}_0 \Pi \theta \\ &+ \lambda_{\Pi q} q \cdot \nabla \alpha + \lambda_{\Pi \pi} \pi^{\mu\nu} \sigma_{\mu\nu}, \end{aligned}$$

$$\begin{aligned} q^\mu &= q_{\text{NS}}^\mu - \tau_q \Delta^{\mu\nu} \dot{q}_\nu \\ &- \tau_{q\Pi} \Pi \dot{u}^\mu - \tau_{q\pi} \pi^{\mu\nu} \dot{u}_\nu + \ell_{q\Pi} \nabla^\mu \Pi - \ell_{q\pi} \Delta^{\mu\nu} \partial^\lambda \pi_{\nu\lambda} + \tau_q \omega^{\mu\nu} q_\nu - \frac{\kappa}{\beta} \hat{\delta}_1 q^\mu \theta \\ &- \lambda_{qq} \sigma^{\mu\nu} q_\nu + \lambda_{q\Pi} \Pi \nabla^\mu \alpha + \lambda_{q\pi} \pi^{\mu\nu} \nabla_\nu \alpha, \\ \pi^{\mu\nu} &= \pi_{\text{NS}}^{\mu\nu} - \tau_\pi \dot{\pi}^{<\mu\nu>} \\ &+ 2\tau_{\pi q} q^{<\mu} \dot{u}^{\nu>} + 2\ell_{\pi q} \nabla^{<\mu} q^{\nu>} + 2\tau_\pi \pi_\lambda^{<\mu} \omega^{\nu>\lambda} - 2\eta \hat{\delta}_2 \pi^{\mu\nu} \theta \\ &- 2\tau_\pi \pi_\lambda^{<\mu} \sigma^{\nu>\lambda} - 2\lambda_{\pi q} q^{<\mu} \nabla^{\nu>} \alpha + 2\lambda_{\pi\Pi} \Pi \sigma^{\mu\nu}, \end{aligned}$$

Complete set of causal, dissipative
relativistic hydrodynamics eqs.
(B. Betz & D. Rischke, JPG36, 2009)

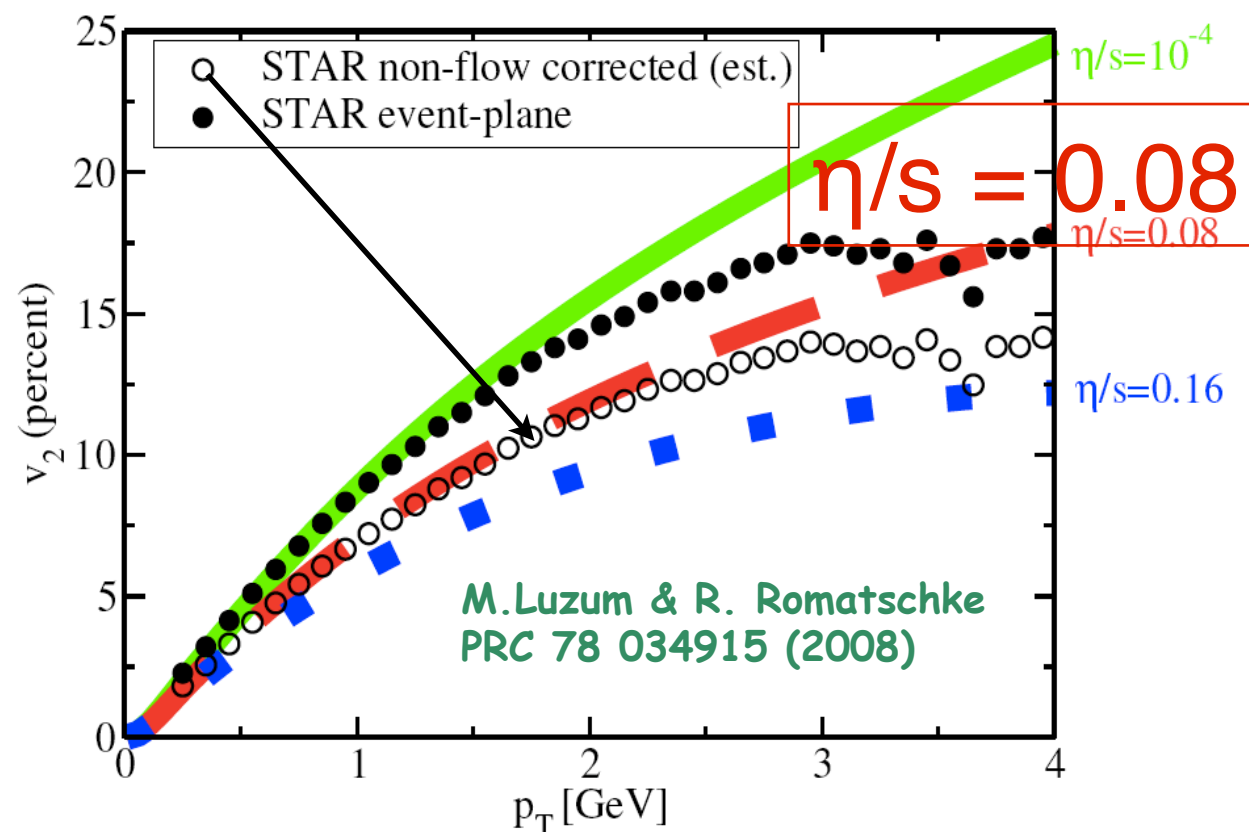
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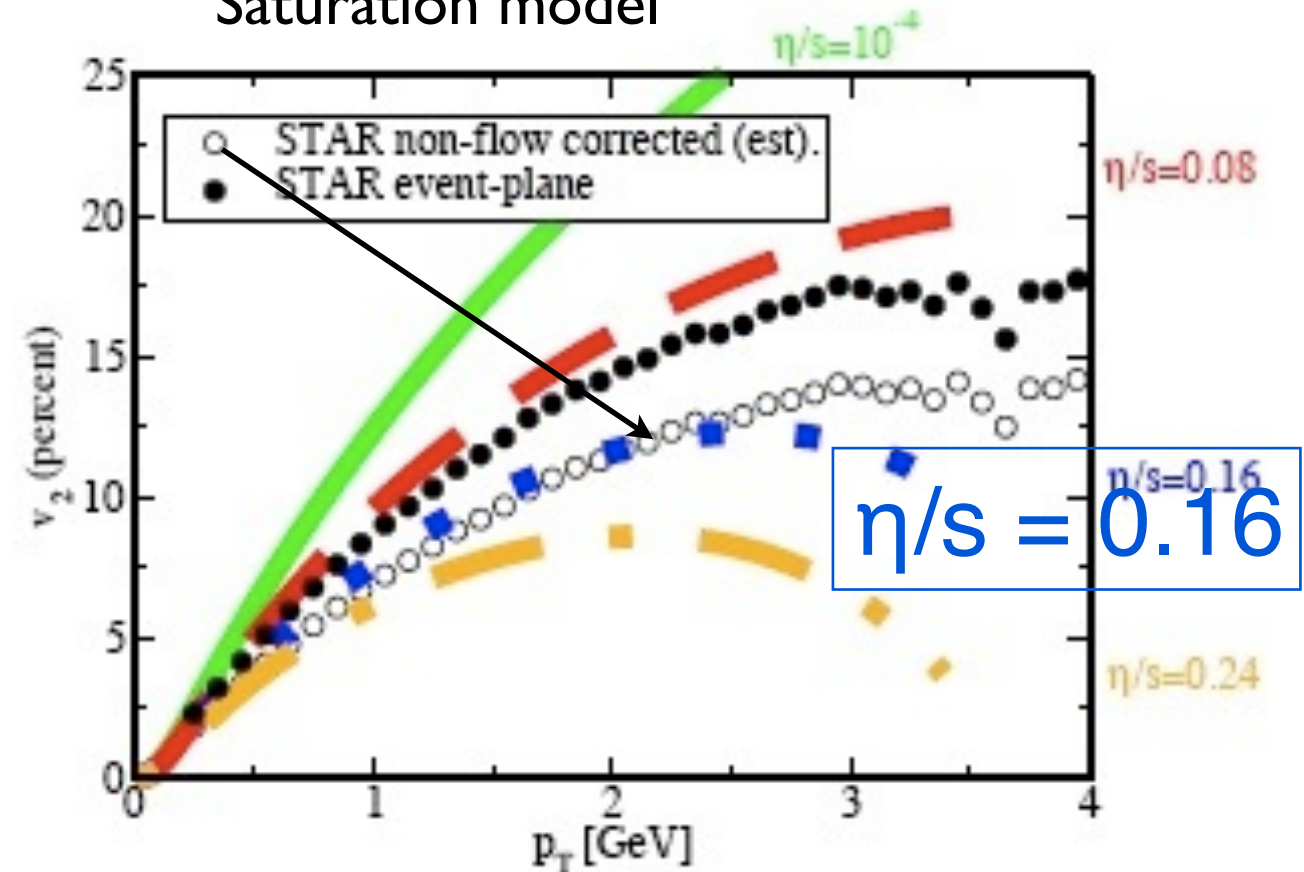
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Glauber model



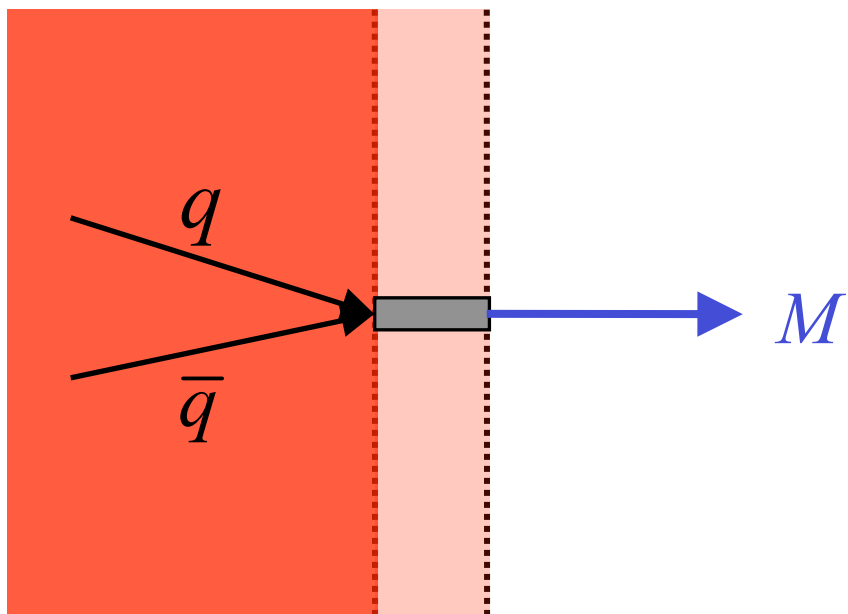
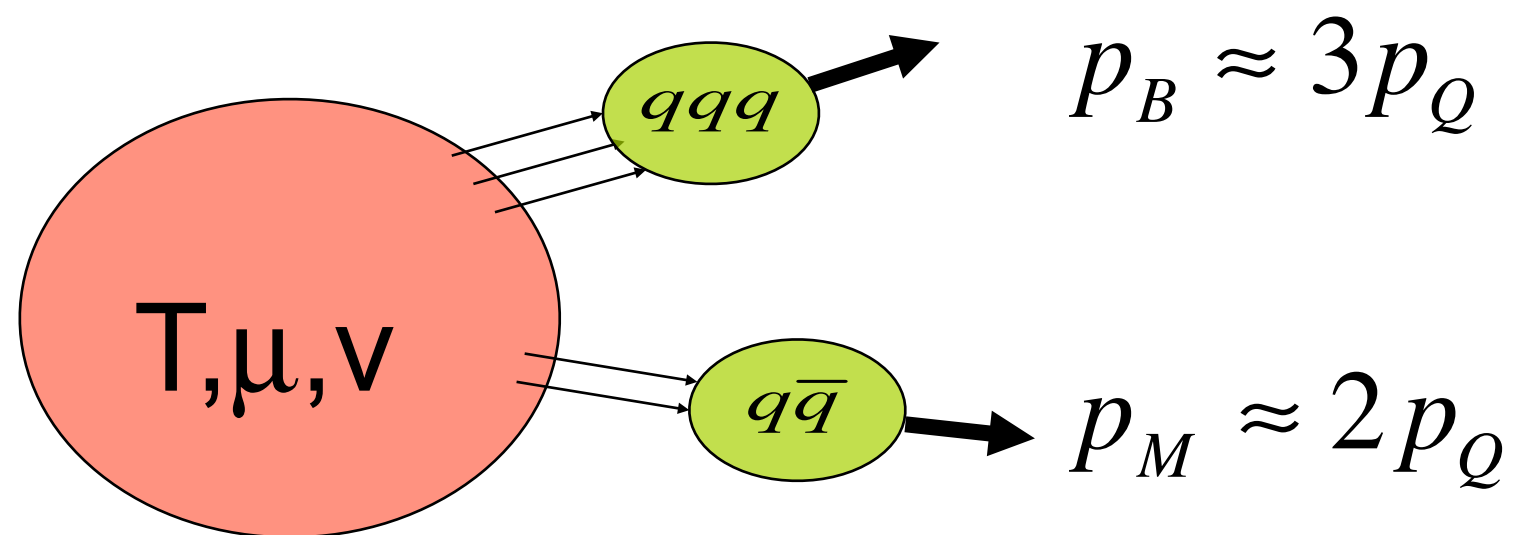
Saturation model



Bulk hadronization

Fast hadrons experience a rapid transition from medium to vacuum for fast hadrons

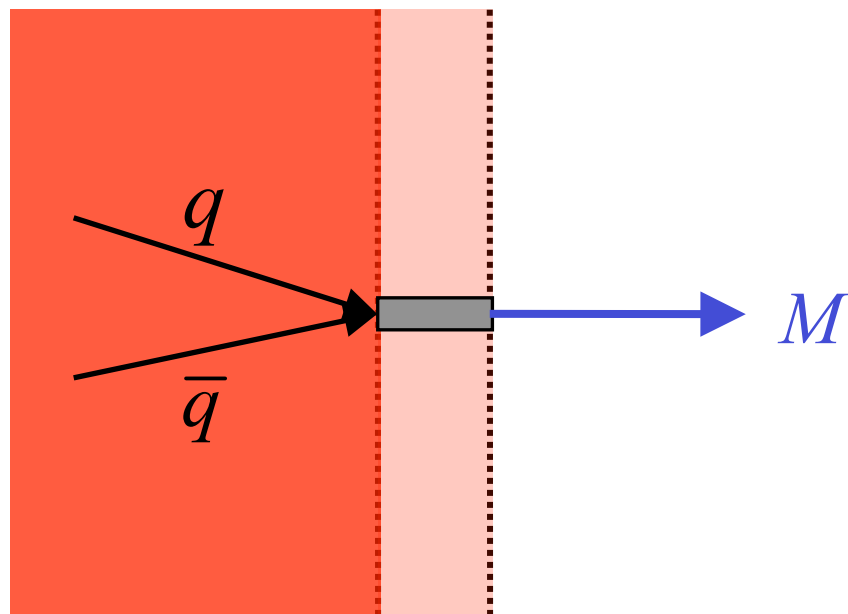
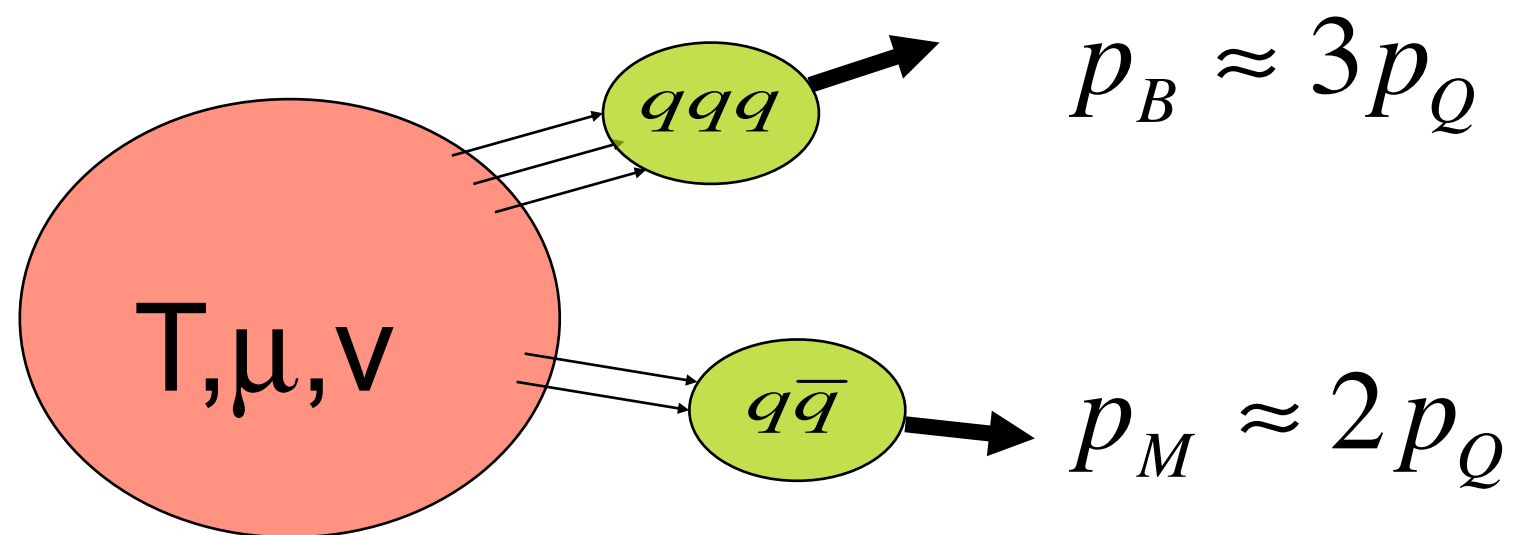
Sudden recombination



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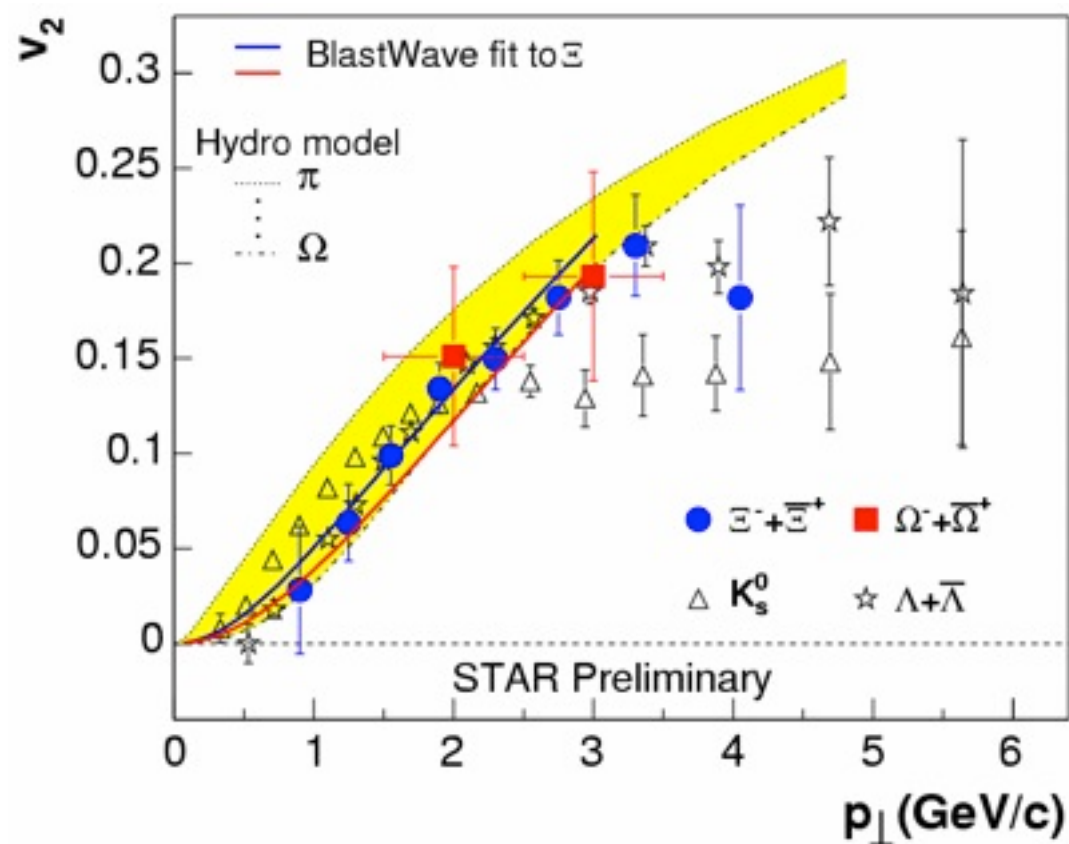
$$v_2^M(p_t) = 2v_2^Q\left(\frac{p_t}{2}\right)$$

$$v_2^B(p_t) = 3v_2^Q\left(\frac{p_t}{3}\right)$$

Quark number scaling of v_2

$$\frac{1}{2} v_2^M(p_t) = v_2^Q \left(\frac{p_t}{2} \right)$$

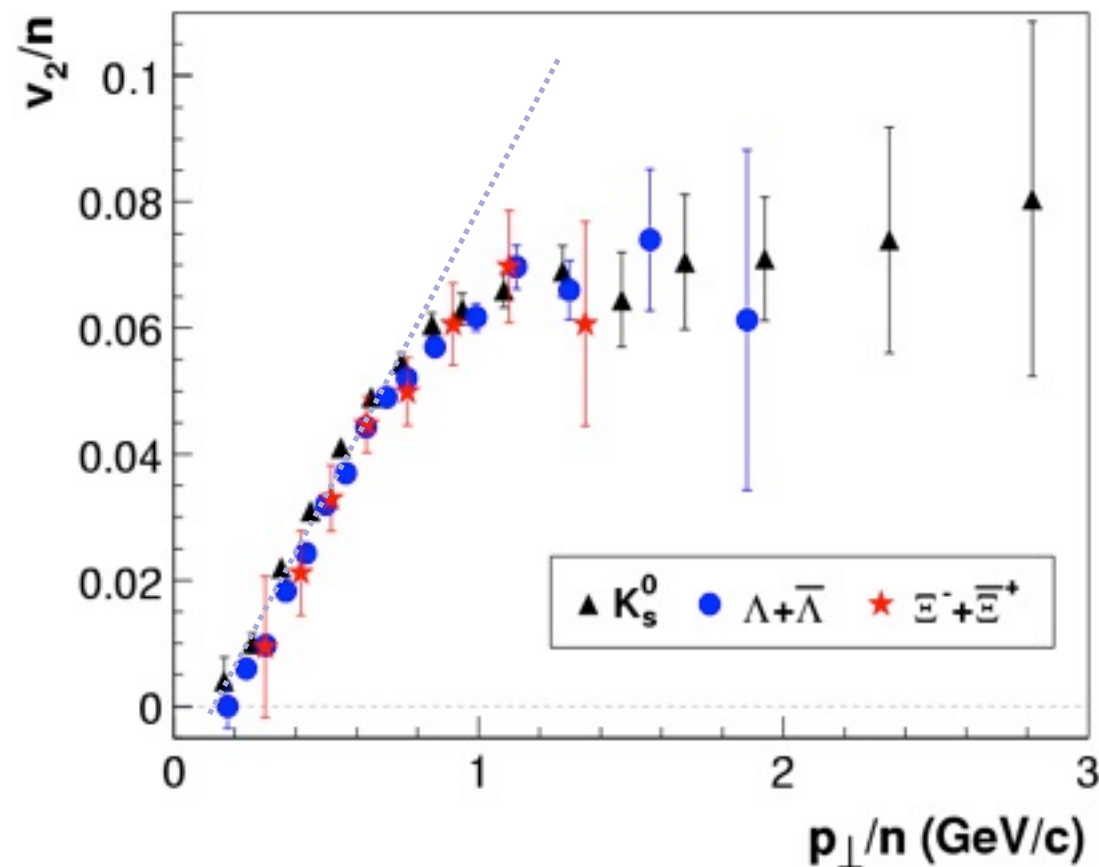
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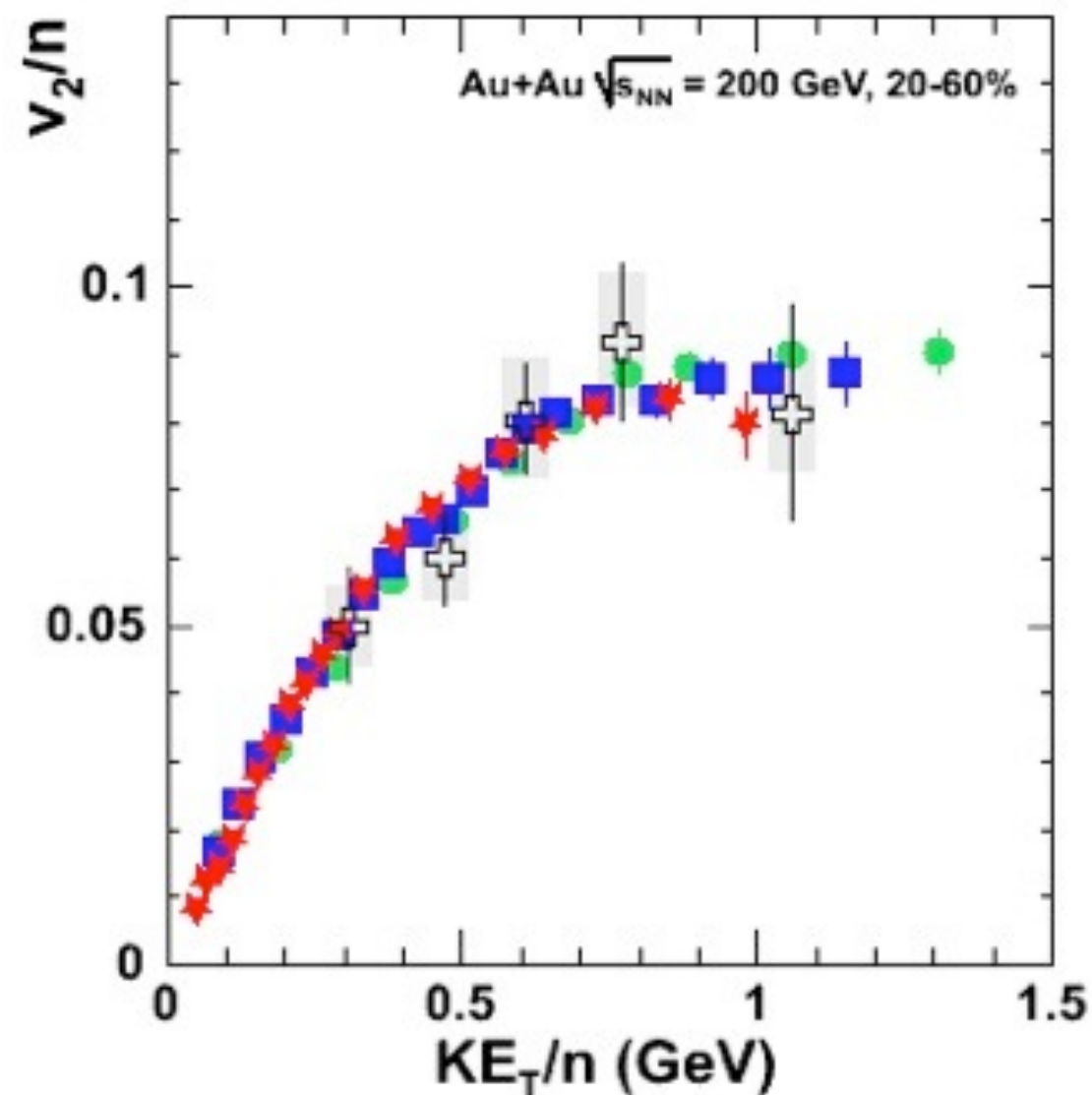
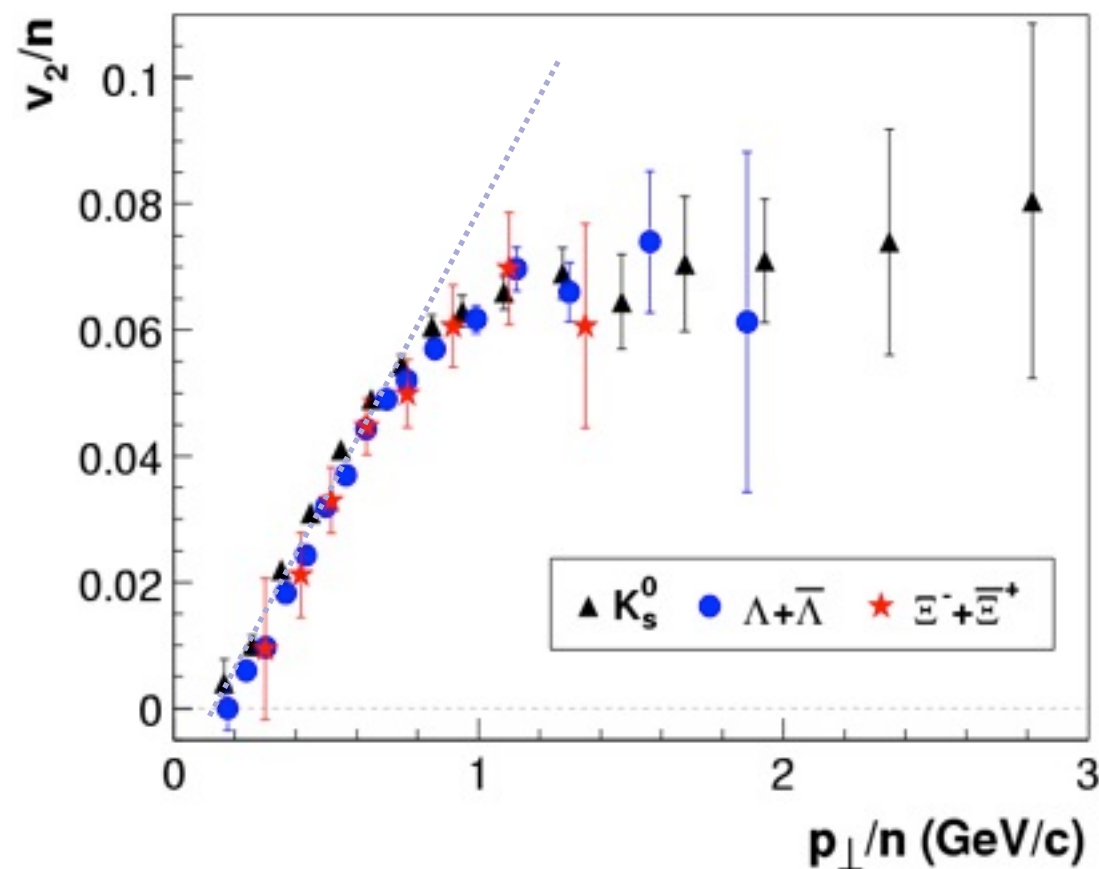


Emitting medium is composed of unconfined, flowing quarks.

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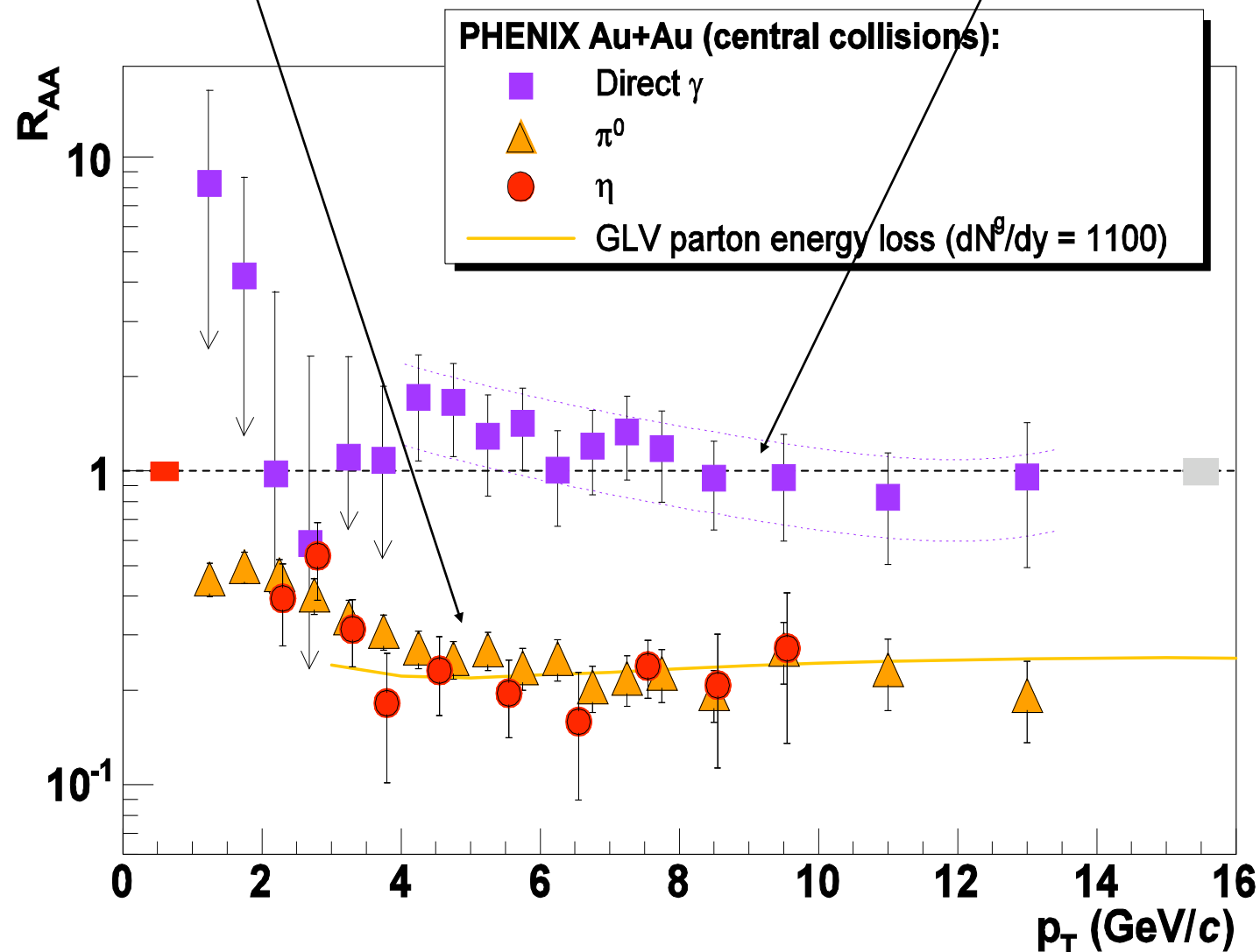


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Jet quenching in Au+Au

No suppression for photons

Suppression of hadrons



Yield in A+A

$$R_{AA}(p_T) = \frac{d^2 N_{AA} / dp_T dy}{T_{AA} (d^2 \sigma_{NN} / dp_T dy)}$$

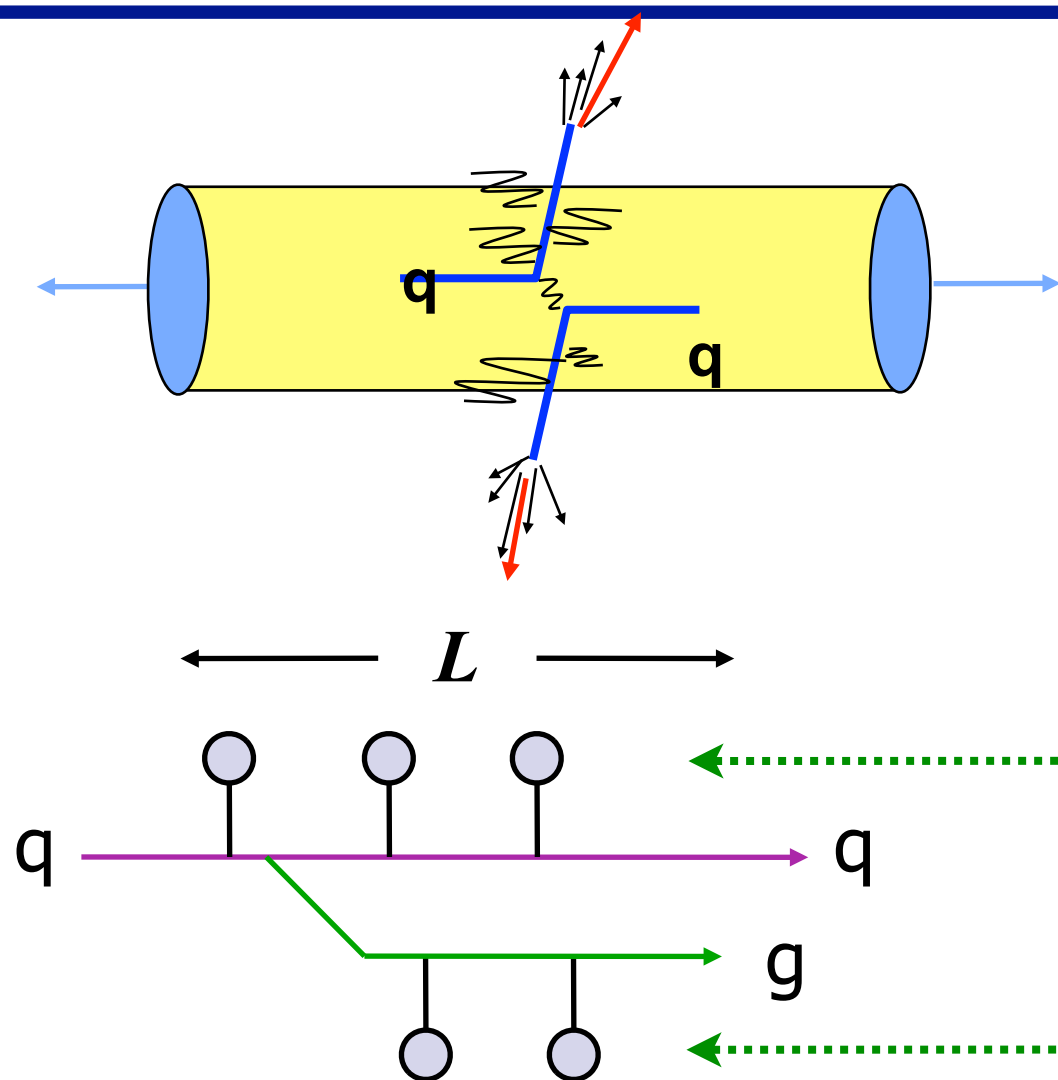
Area density
of p+p coll's
in A+A

Cross section
in p+p coll's

Without nuclear effects:

$$R_{AA} = 1.$$

Radiative energy loss



$$\Delta E \sim \rho L^2 \langle k_T^2 \rangle$$

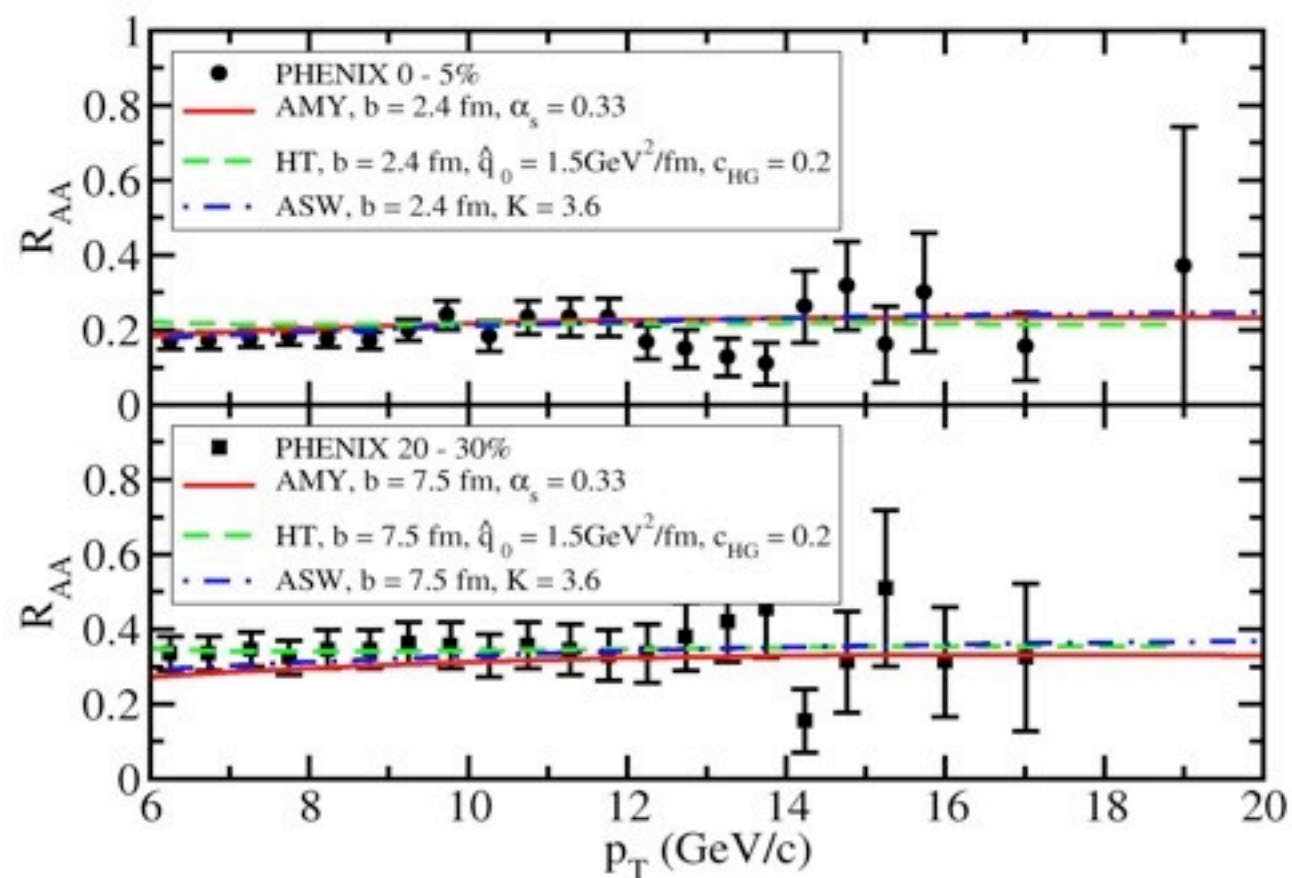
Scattering centers
= color charges

$$\hat{q} = \rho \int q^2 dq^2 \frac{d\sigma}{dq^2} = \int dx^- \langle F_i^+(x^-) F^{+i}(0) \rangle$$

Towards measuring \hat{q}

Good fits for light hadrons are obtained for all rad. energy loss models in 3-D hydrodynamics

Bass, Gale, Majumder, Nonaka, Qin, Renk & Ruppert

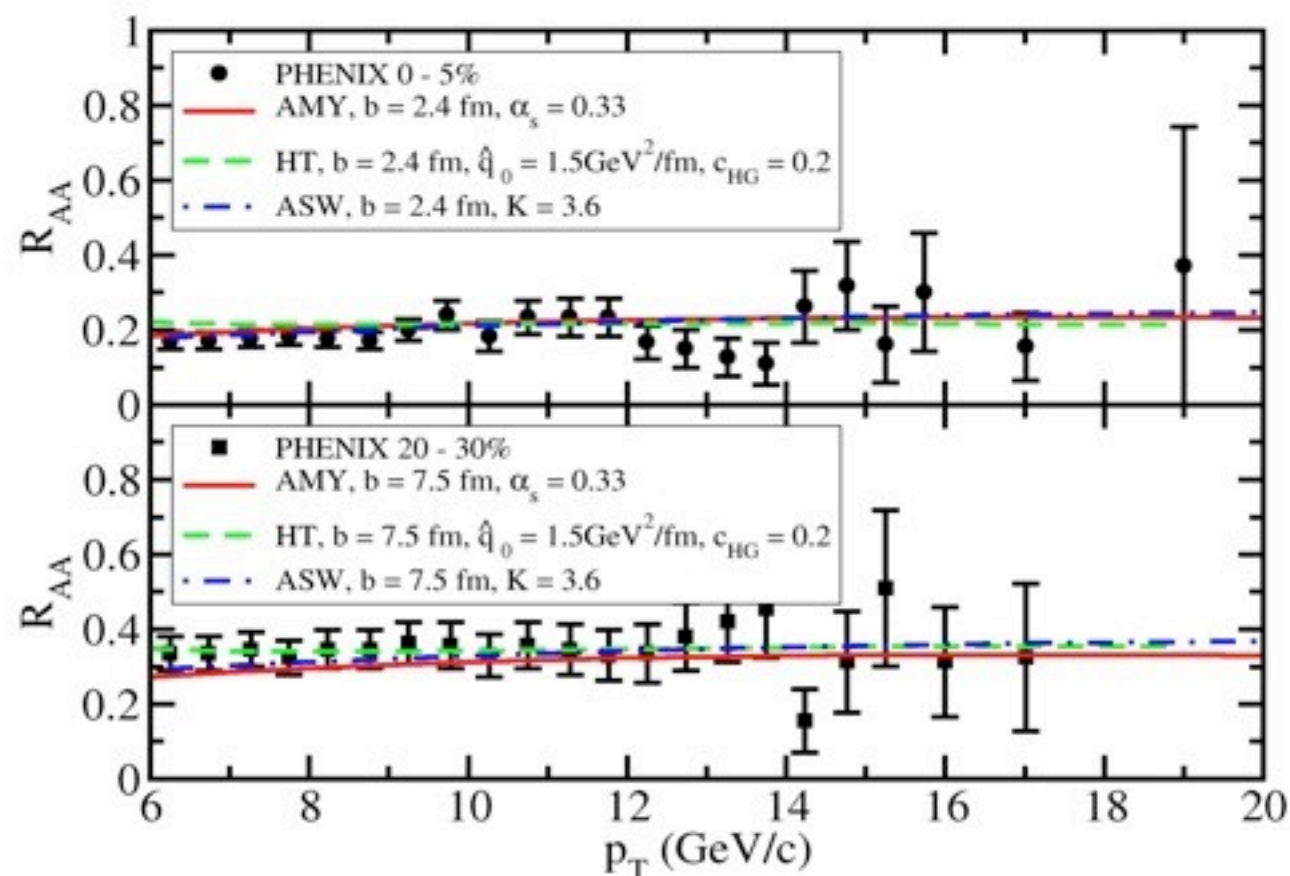


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Good fits for light hadrons are obtained for all rad. energy loss models in 3-D hydrodynamics

Transport parameter \hat{q} deviates by more than factor 2 between different implementations.

Bass, Gale, Majumder, Nonaka, Qin, Renk & Ruppert



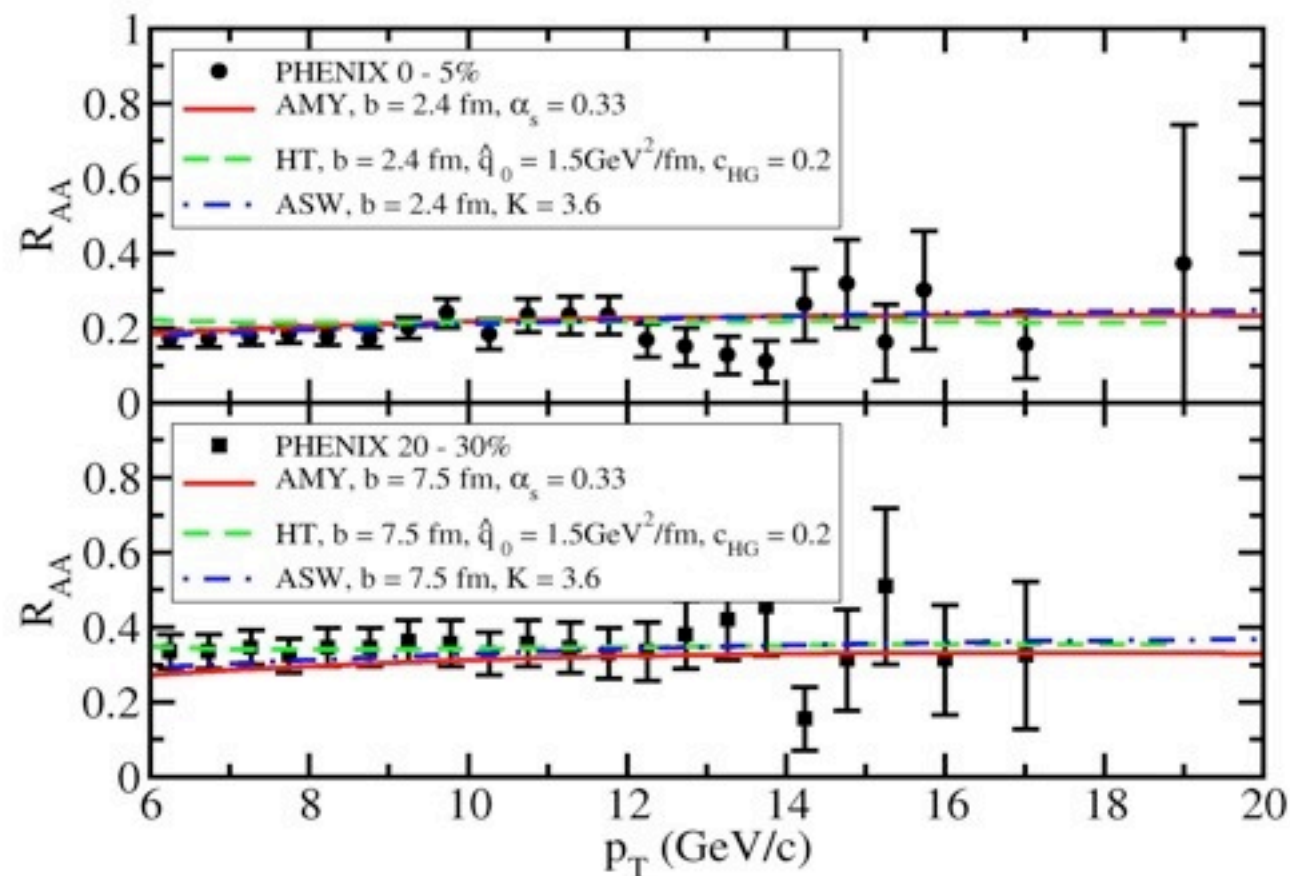
Caused by differences in the cut-offs in collinear approximation used in all implementations of gluon radiation.

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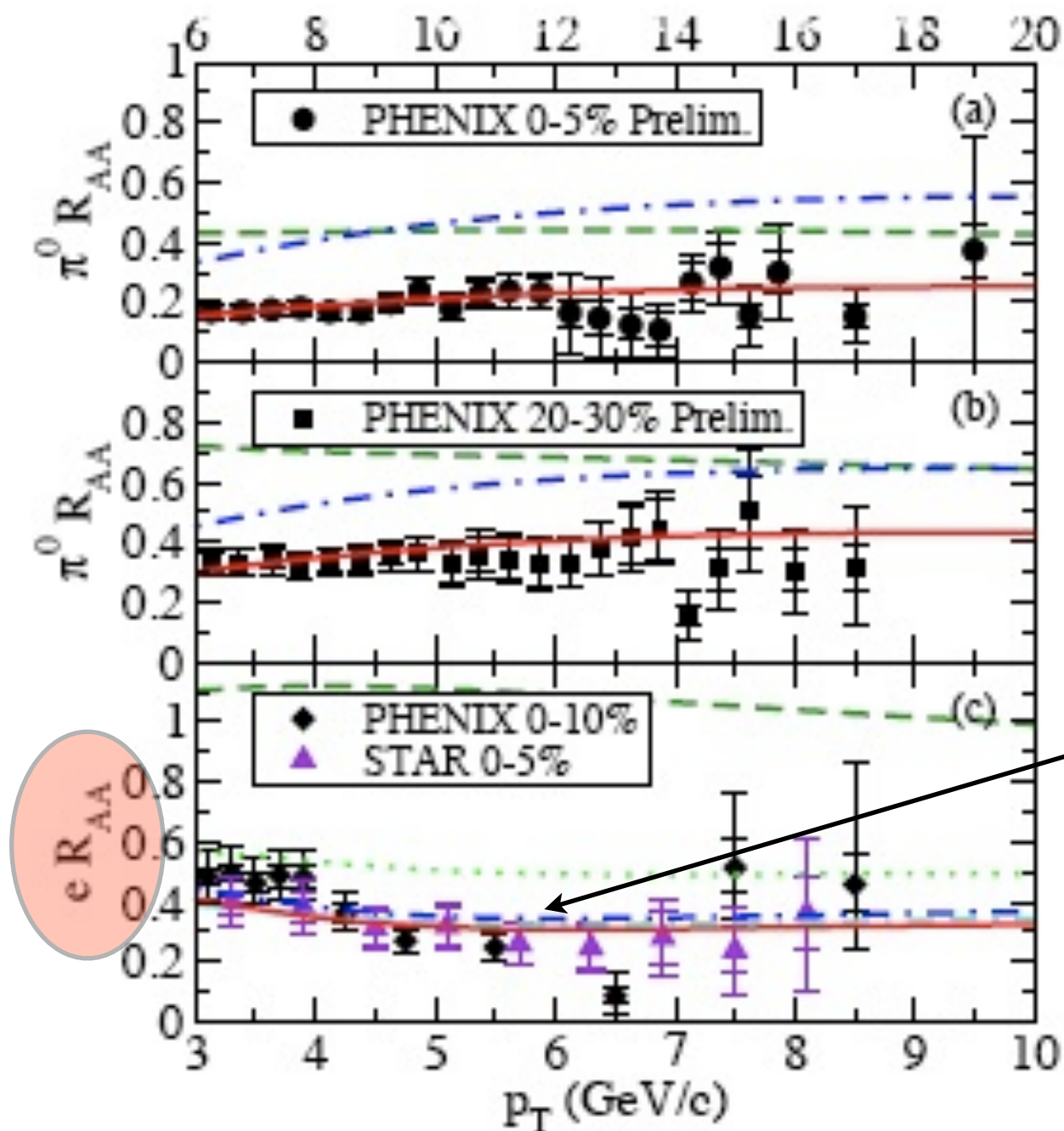


Caused by differences in the cut-offs in collinear approximation used in all implementations of gluon radiation.

Generalized, robust new approach needed.

The heavy quark conundrum

GY Qin & A Majumder



Heavy quark (c, b) energy loss deduced from suppression of weak decay electron spectrum

Suppression stronger than expected.

3 parameters: \hat{q} , \hat{e} , \hat{e}_2

Fit: $\frac{\hat{q}_c}{\hat{q}_{u/d/g}} \approx 1.1$ $\frac{\hat{q}_b}{\hat{q}_{u/d/g}} \approx 1.6$

contrary to expectations for a weakly coupled QGP.

Toward higher energies...



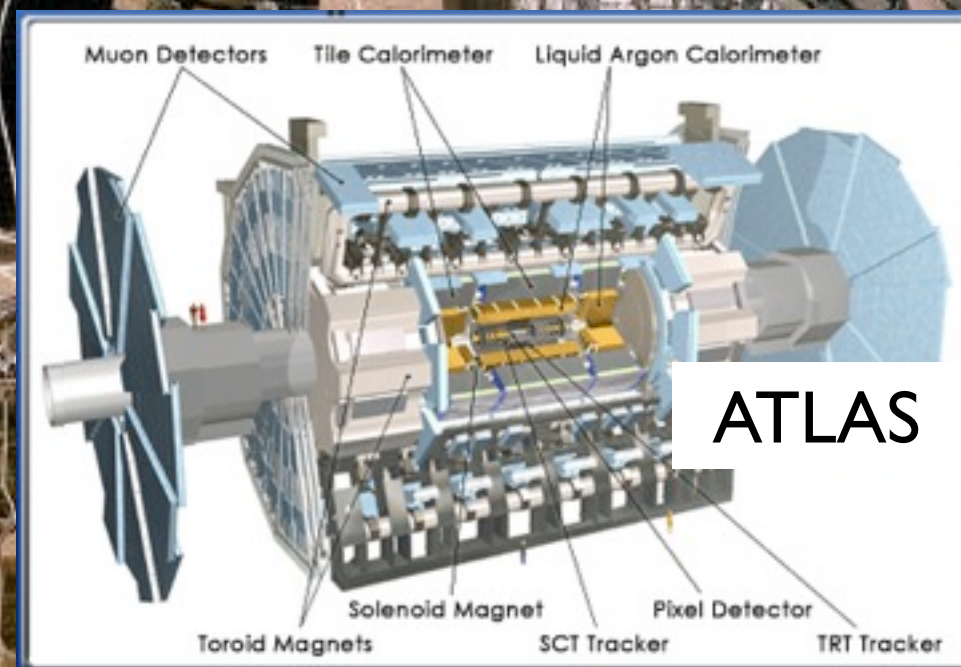
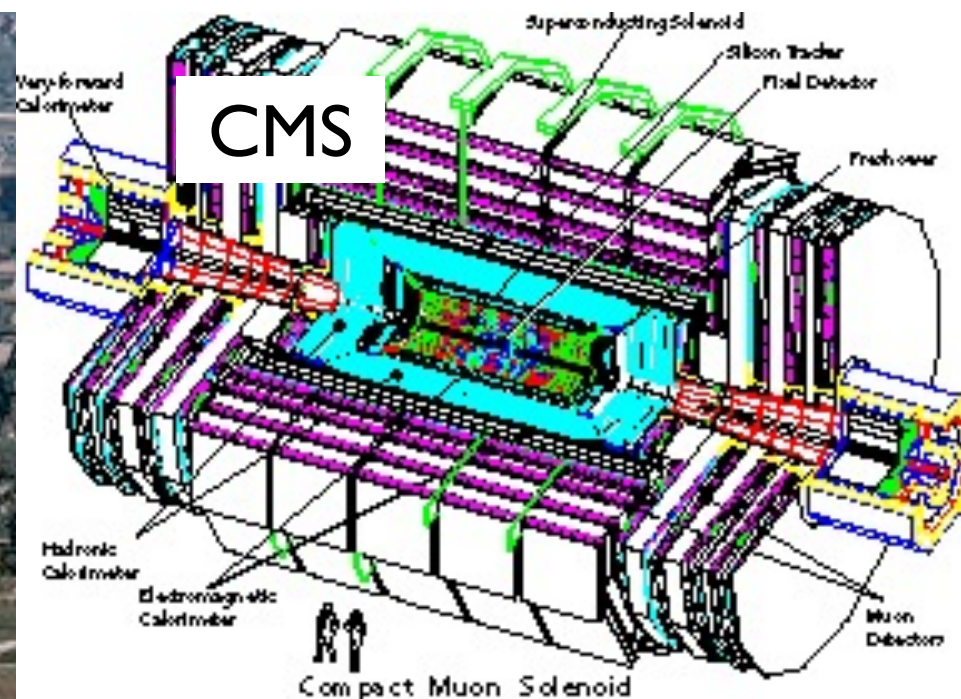
Toward higher energies...

LHC

CMS

ALICE

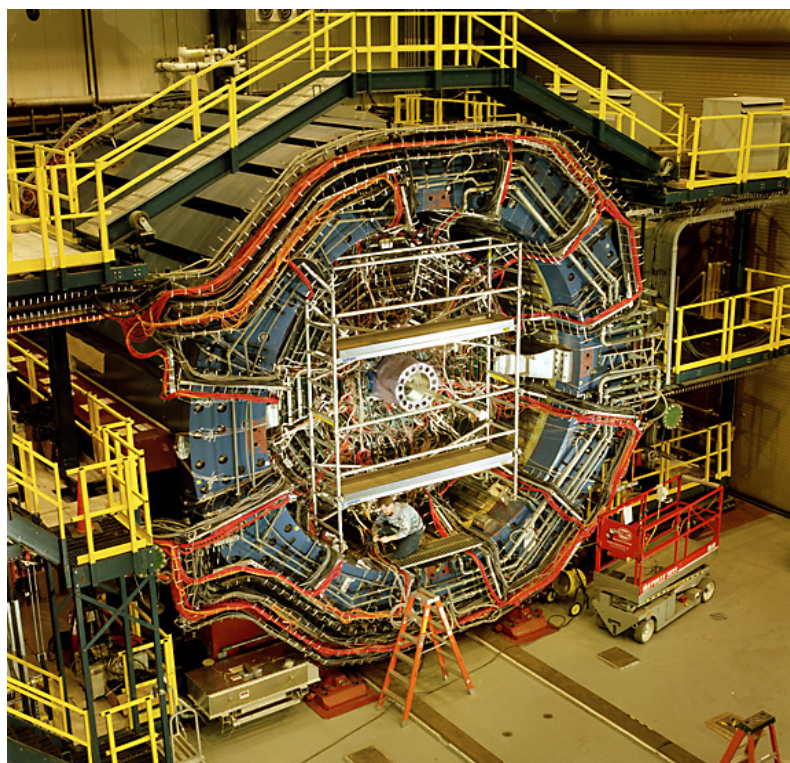
ATLAS



Toward rarer probes

RHIC detector upgrades

STAR



forward meson spectrometer

DAQ & TPC electronics
Time of Flight barrel

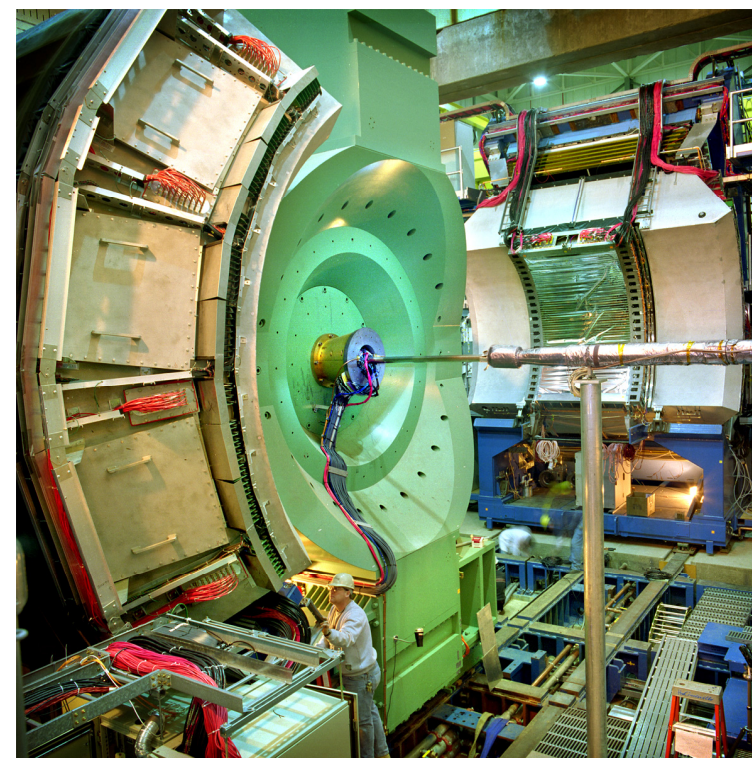
heavy flavor tracker
barrel silicon tracker
forward tracker

-completed –

ongoing

in preparation

PHENIX



hadron blind detector

muon Trigger
silicon vertex barrel (VTX)

forward silicon
forward EM calorimeter

Toward more powerful theory

Toward more powerful theory



https://wiki.bnl.gov/TECHQM/index.php/Main_Page

Toward more powerful theory



https://wiki.bnl.gov/TECHQM/index.php/Main_Page



THE UNIVERSITY
of NORTH CAROLINA
at CHAPEL HILL



<http://mo.pa.msu.edu/~scottepratt/madai/>

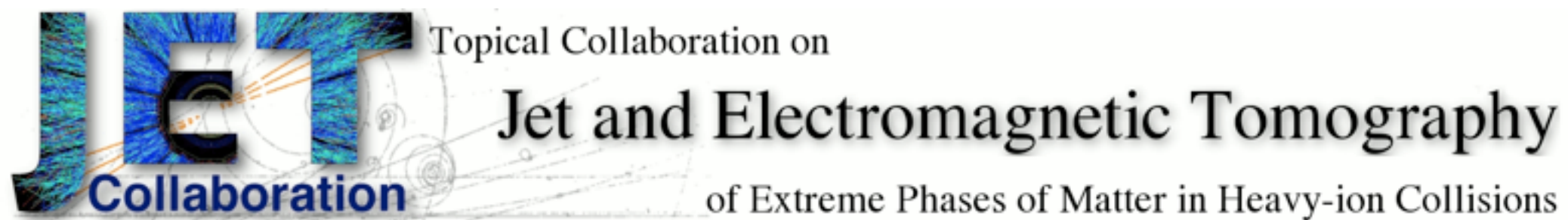
Toward more powerful theory



https://wiki.bnl.gov/TECHQM/index.php/Main_Page

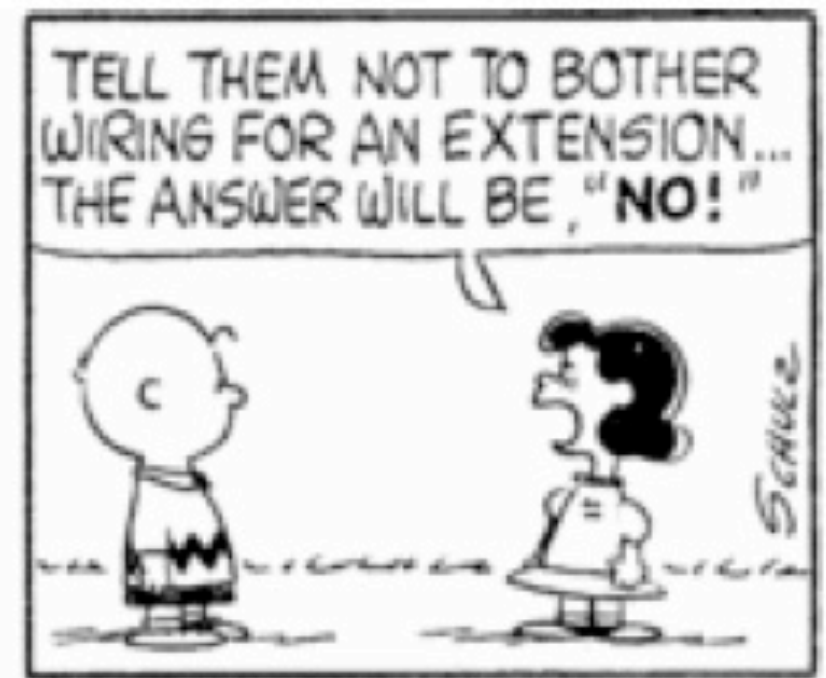
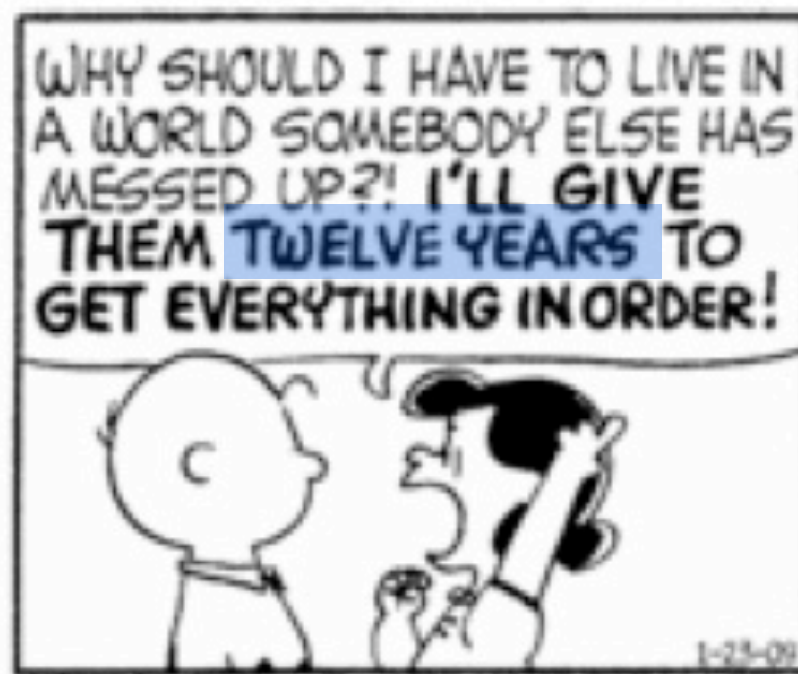


<http://mo.pa.msu.edu/~scottepratt/madai/>



<http://www-nsdth.lbl.gov/jet/>

The challenge



The challenge

Can we beat the deadline
and prove that
the world was once
(13.7×10^9 years ago)
a perfect fluid ?

Observables revisited

Which properties of hot QCD matter can we hope to determine from relativistic heavy ion data ?

$T_{\mu\nu} \Leftrightarrow \varepsilon, p, s$ **Equation of state:** spectra, collective flow

$c_s^2 = \partial p / \partial \varepsilon$ **Speed of sound:** multiparticle correlations

$\eta = \frac{1}{T} \int d^4x \langle T_{xy}(x) T_{xy}(0) \rangle$ **Shear viscosity:** anisotropic collective flow

$\hat{q} = \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{a+i}(y^-) F_i^{a+}(0) \rangle$
 $\hat{e} = \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle i\partial^- A^{a+}(y^-) A^{a+}(0) \rangle$
 $\hat{e}_2 = \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{a+-}(y^-) F^{a+-}(0) \rangle$

Momentum/energy diffusion:
parton energy loss
modified jet fragmentation

Color screening: Quarkonium states

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Speed of sound: multiparticle correlations

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Shear viscosity: anisotropic collective flow

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Momentum/energy diffusion:
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23

Ready for
a serious
attempt

Observables revisited

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Ready for
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Speed of sound: multiparticle correlations

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Shear viscosity: anisotropic collective flow

Serious
theoret.
develop-
ments
needed

$$\hat{q} = \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{a+i}(y^-) F_i^{a+}(0) \rangle$$

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Momentum/energy diffusion:

parton energy loss
modified jet fragmentation

$$m_D = - \lim_{|x| \rightarrow \infty} \frac{1}{|x|} \ln \langle E^a(x) E^a(0) \rangle$$

Color screening: Quarkonium states

23

Challenge #1

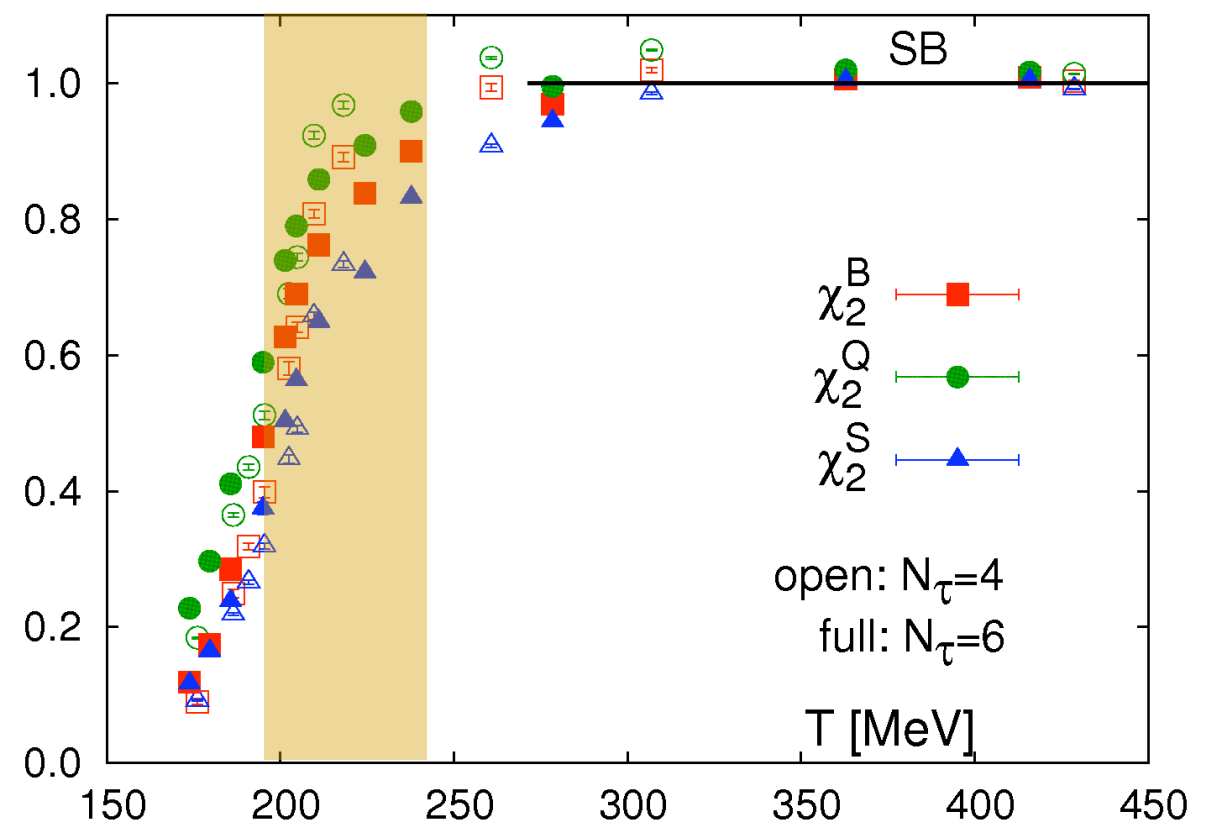
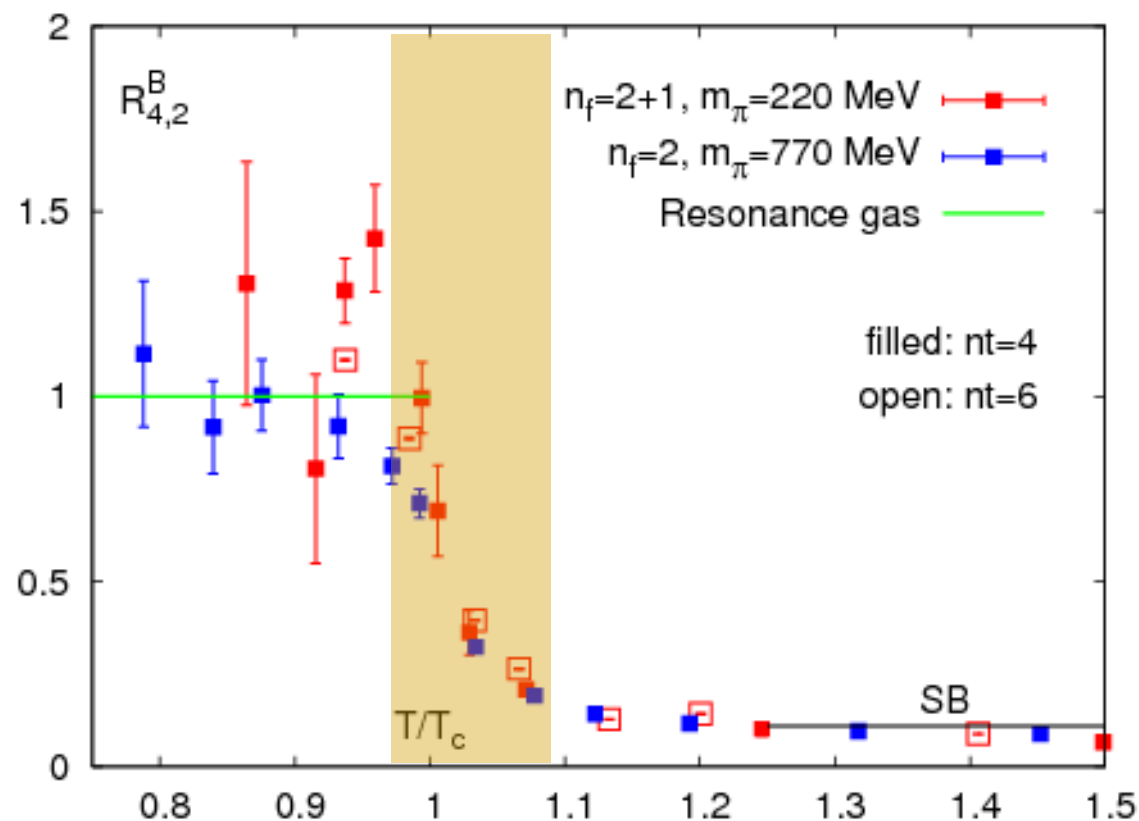
The Strong Coupling “Conundrum”

Conserved charges

$$R_{4,2}^B = \frac{1}{9} \frac{c_4}{c_2} \quad \frac{c_4^q}{c_2^q} = \frac{\langle (\delta N_q)^4 \rangle}{\langle (\delta N_q)^2 \rangle} - 3 \langle (\delta N_q)^2 \rangle$$

B = baryon number
 Q = electric charge
 S = strangeness

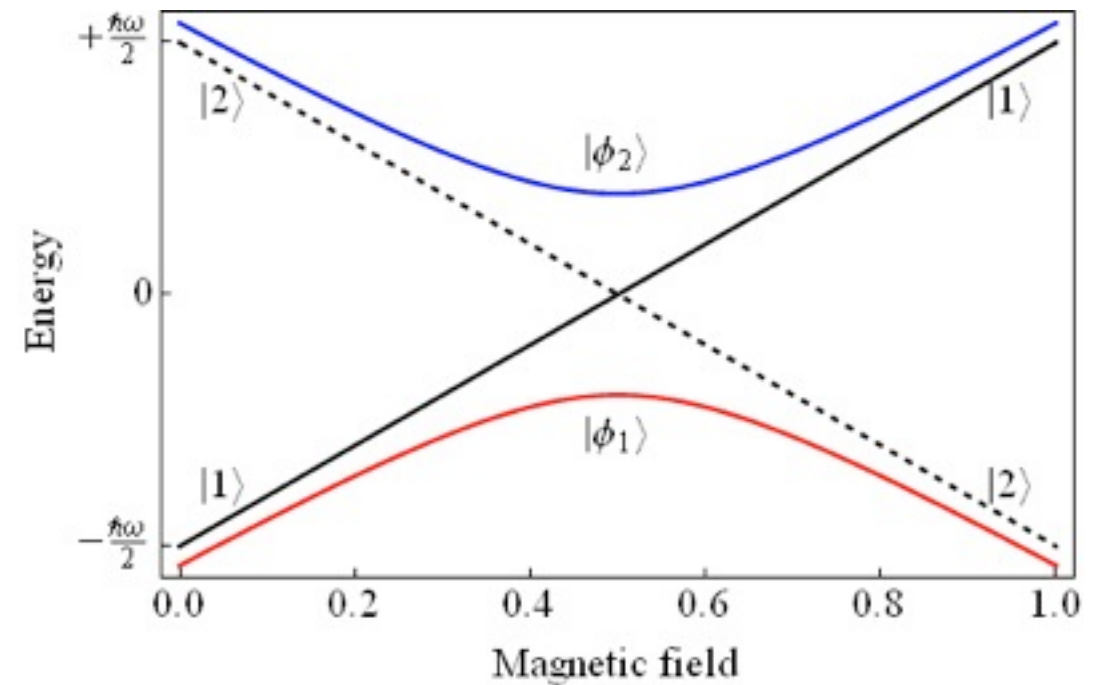
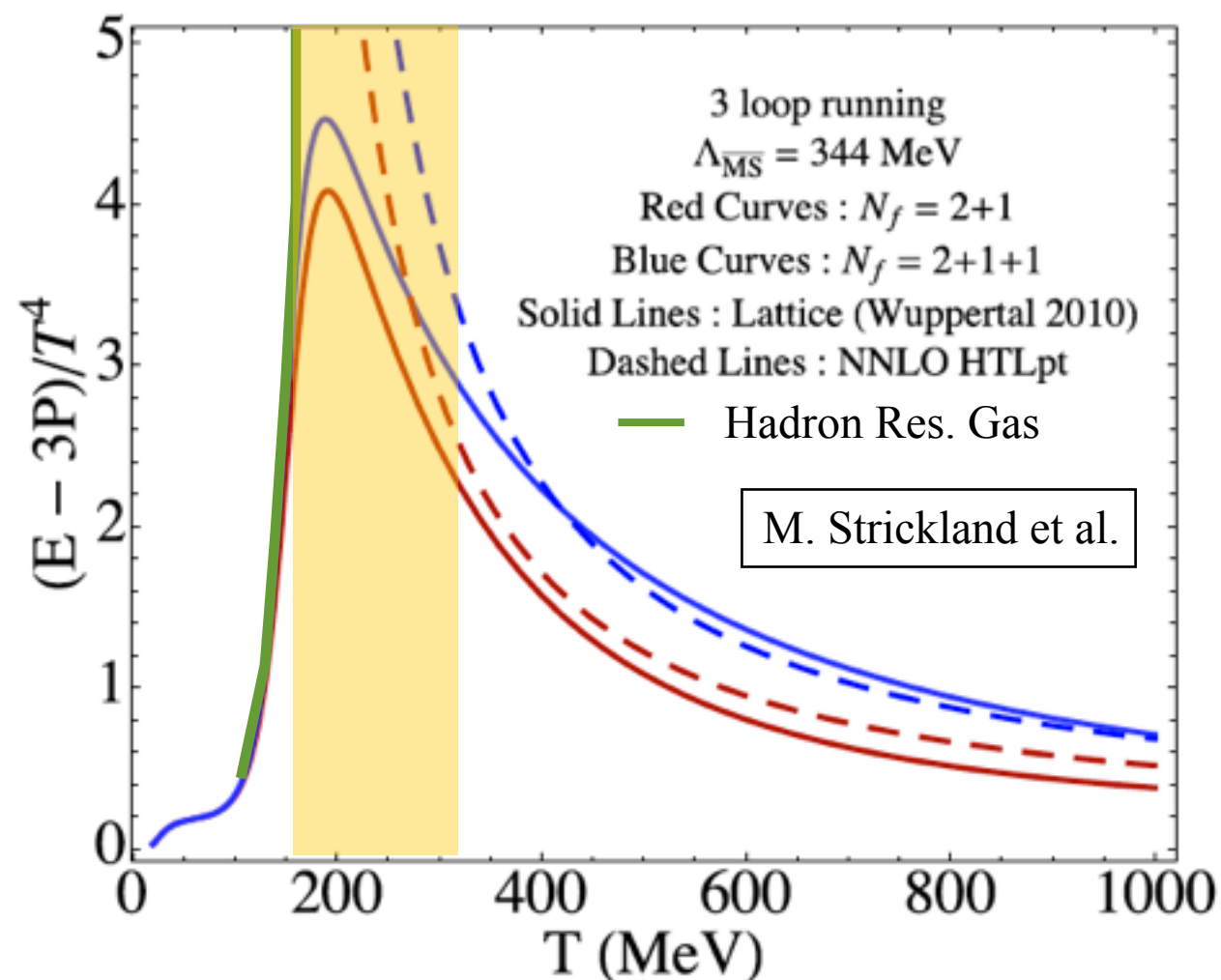
Baryon number kurtosis



Question: Are these properties compatible with “strong coupling”? Is the dependence of thermodynamic quantities on conserved quantum numbers “oblivious” to interactions?

Crossing the “wall”?

Possible scenario:
HRG works up to $0.9 T_c$;
HTL-QGP works above $2 T_c$
or even lower.



Is there an analogy to the Landau-Zener formula of ordinary QM in QFT ?

Can one construct a model in which the transition between two quasi-particle regimes occurs smoothly by “mixing” ?

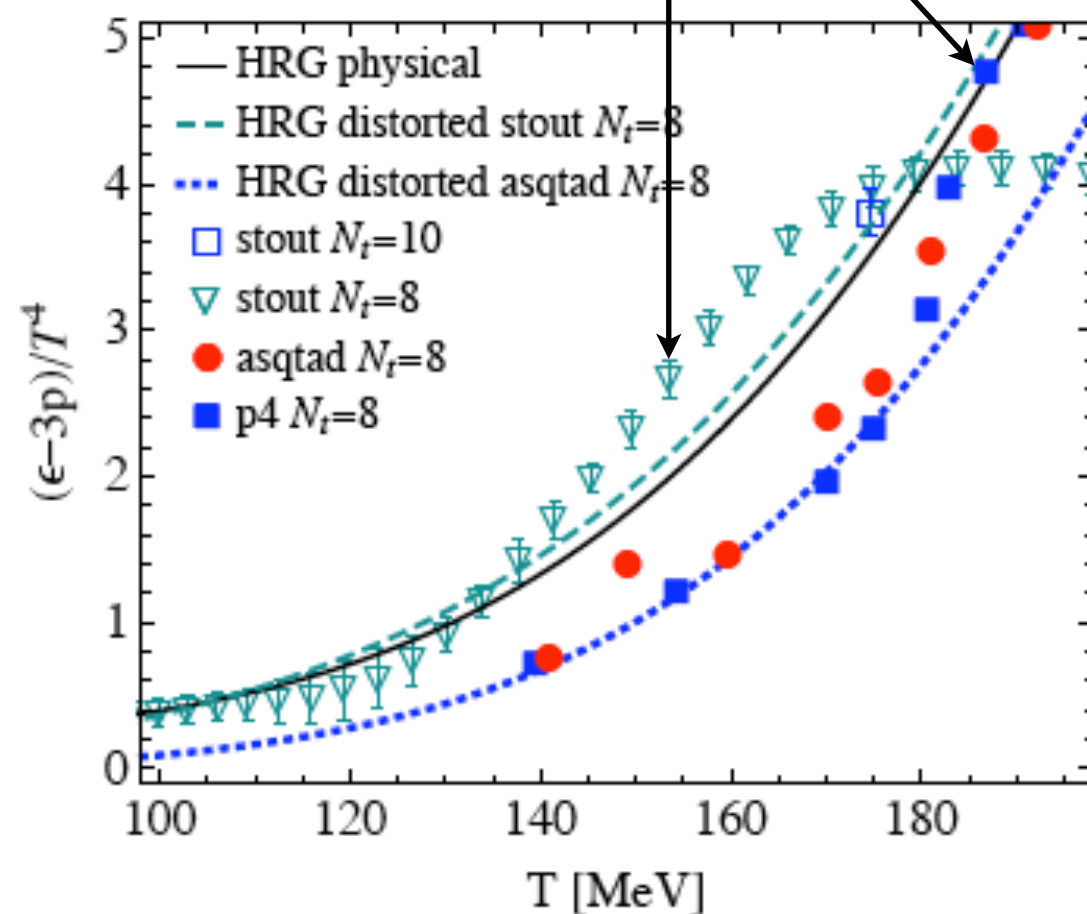
Can the transition be explained without a need for “strong coupling” ?

Exploring the hadron mass spectrum

Lines: Hadron resonance gas (HRG)

Data points: Lattice QCD

LQCD lies **above** HRG for $T > 140$ MeV

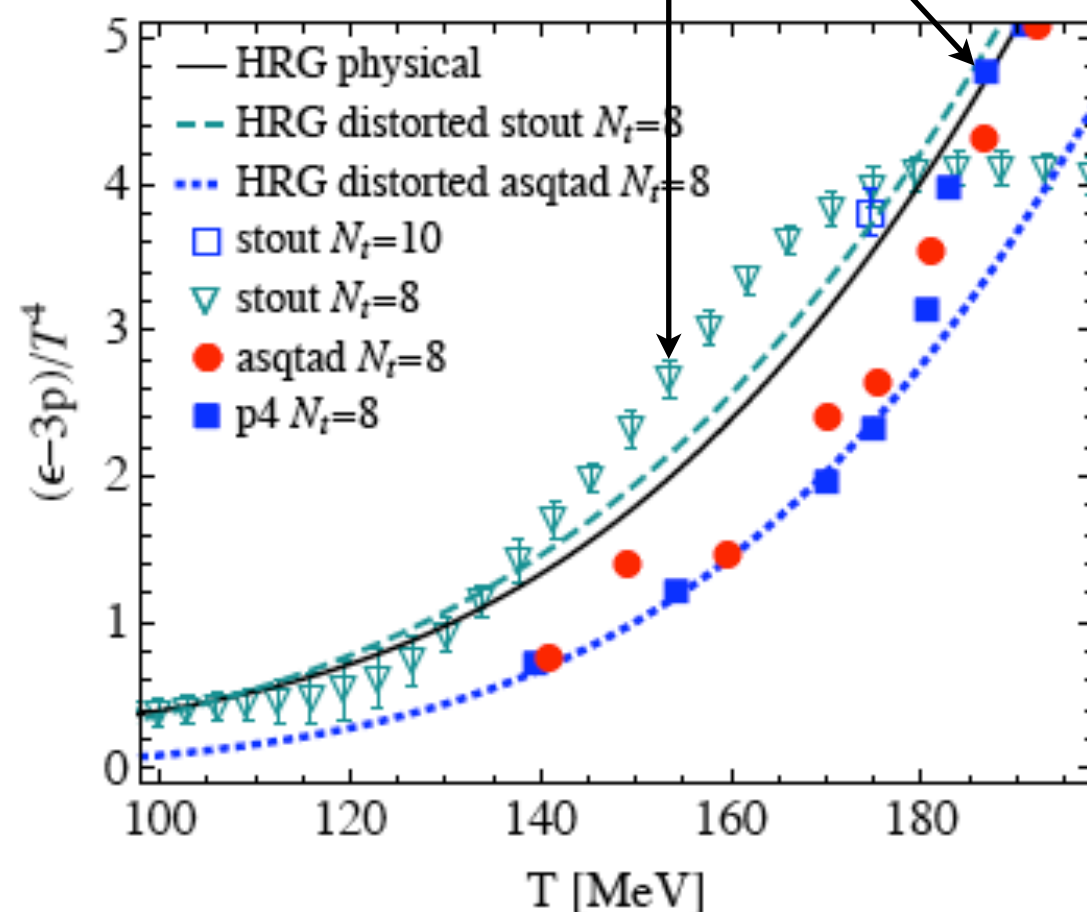


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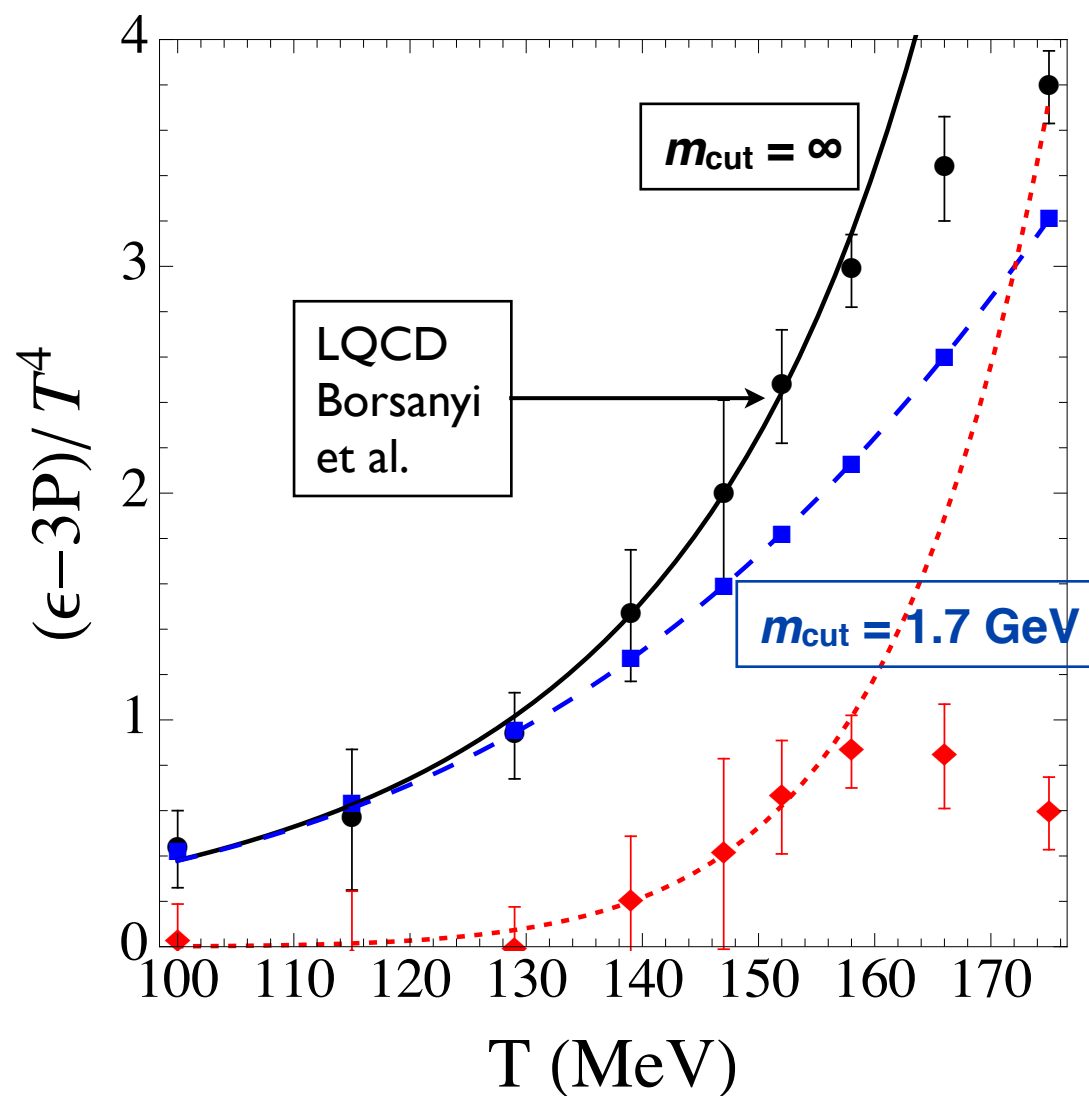
Three possible explanations:

1. Lattice artifact
2. Hadronic interactions
(e.g. in-medium mass changes)
3. Many presently unknown hadrons
with masses > 1.7 GeV

$(\epsilon-3p)$ measures the level density of massive hadronic excitations of the QCD vacuum. Are there many more Baryons? Hybrids? Glueballs?

Note: The JLab (Halls B & D) program studies precisely this question!

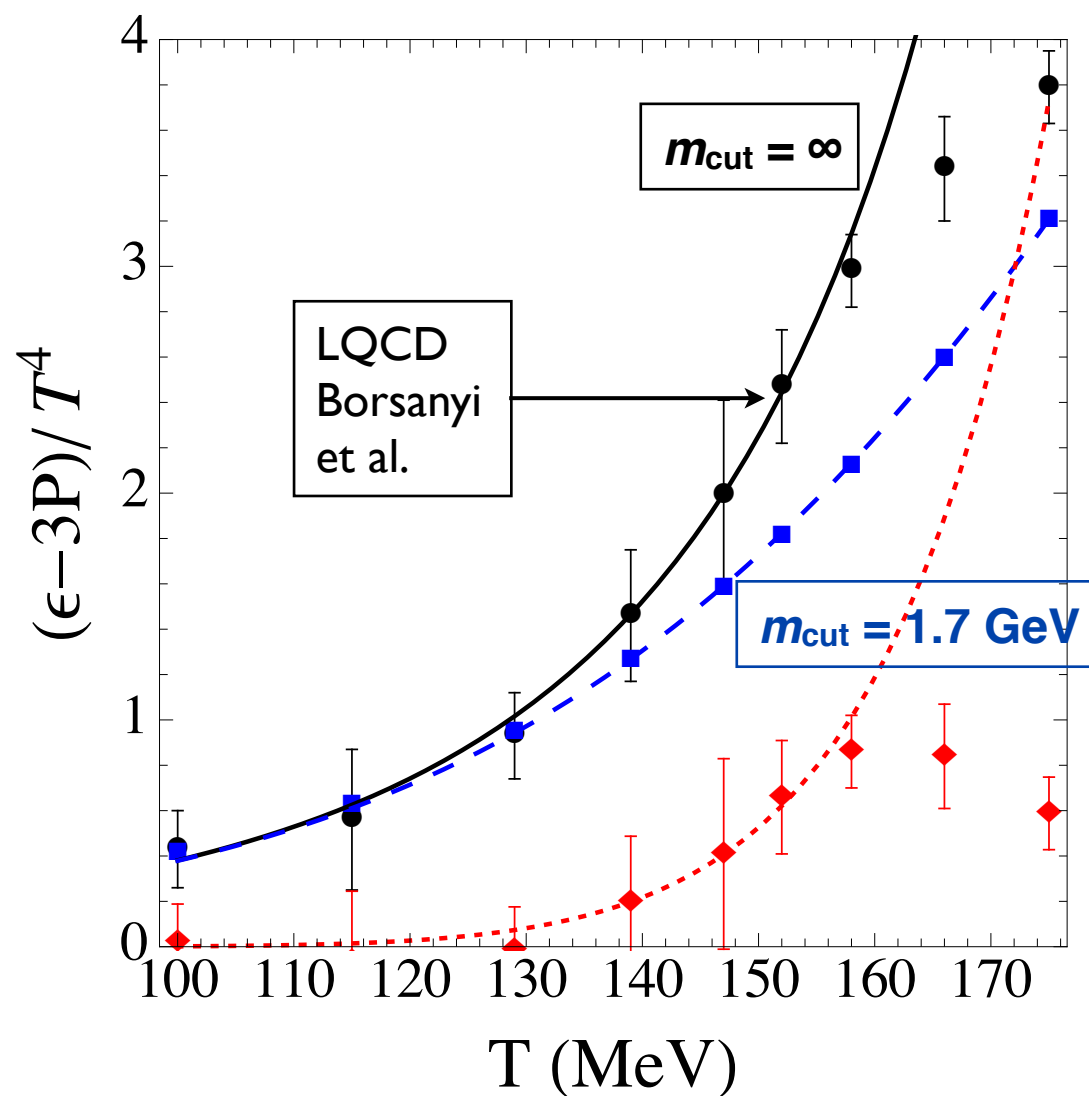
LQCD & hadron spectrum



$$\rho(m) = A e^{bm}$$

A. Majumder & B.M. (arXiv:1008.1747)

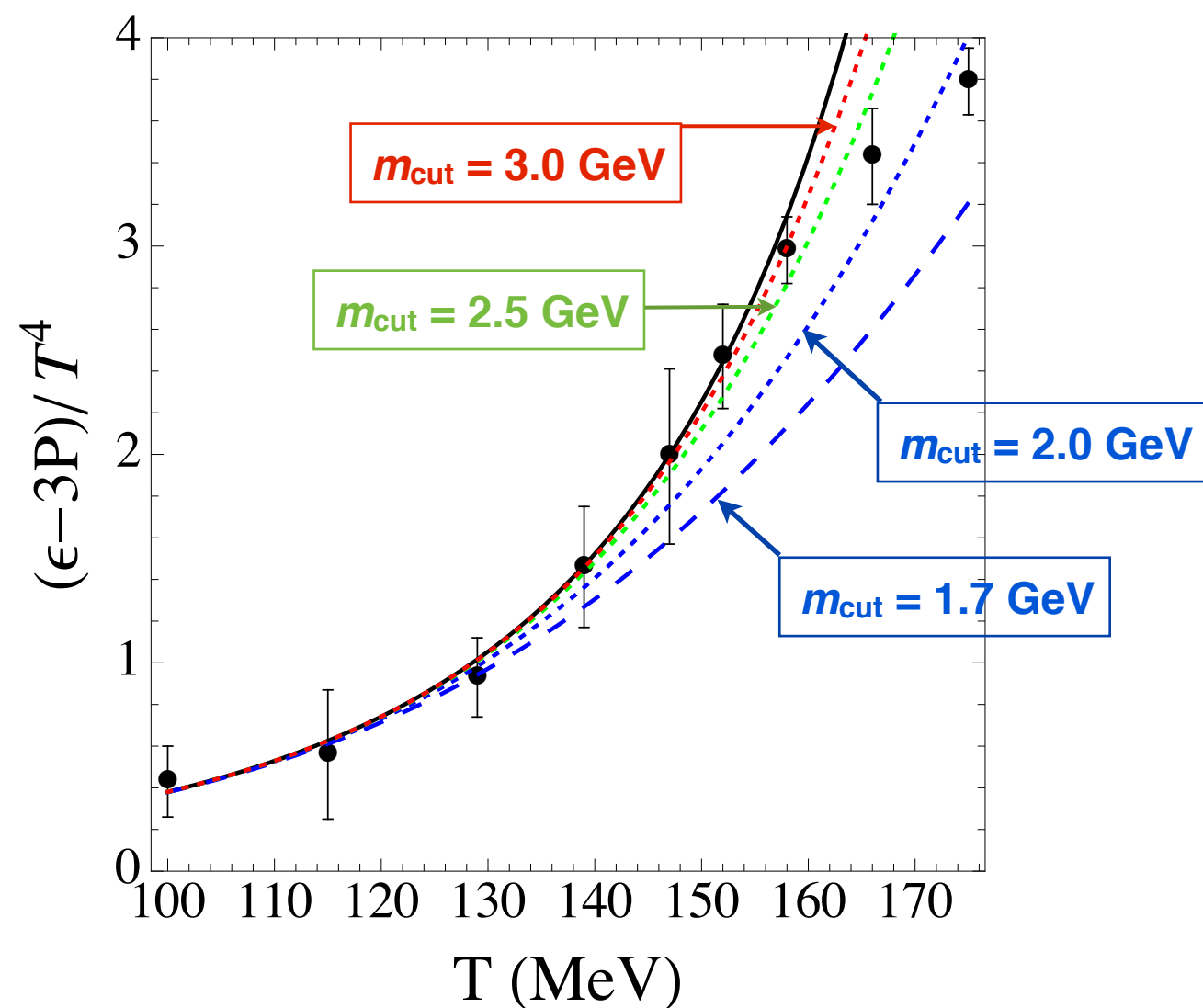
LQCD & hadron spectrum



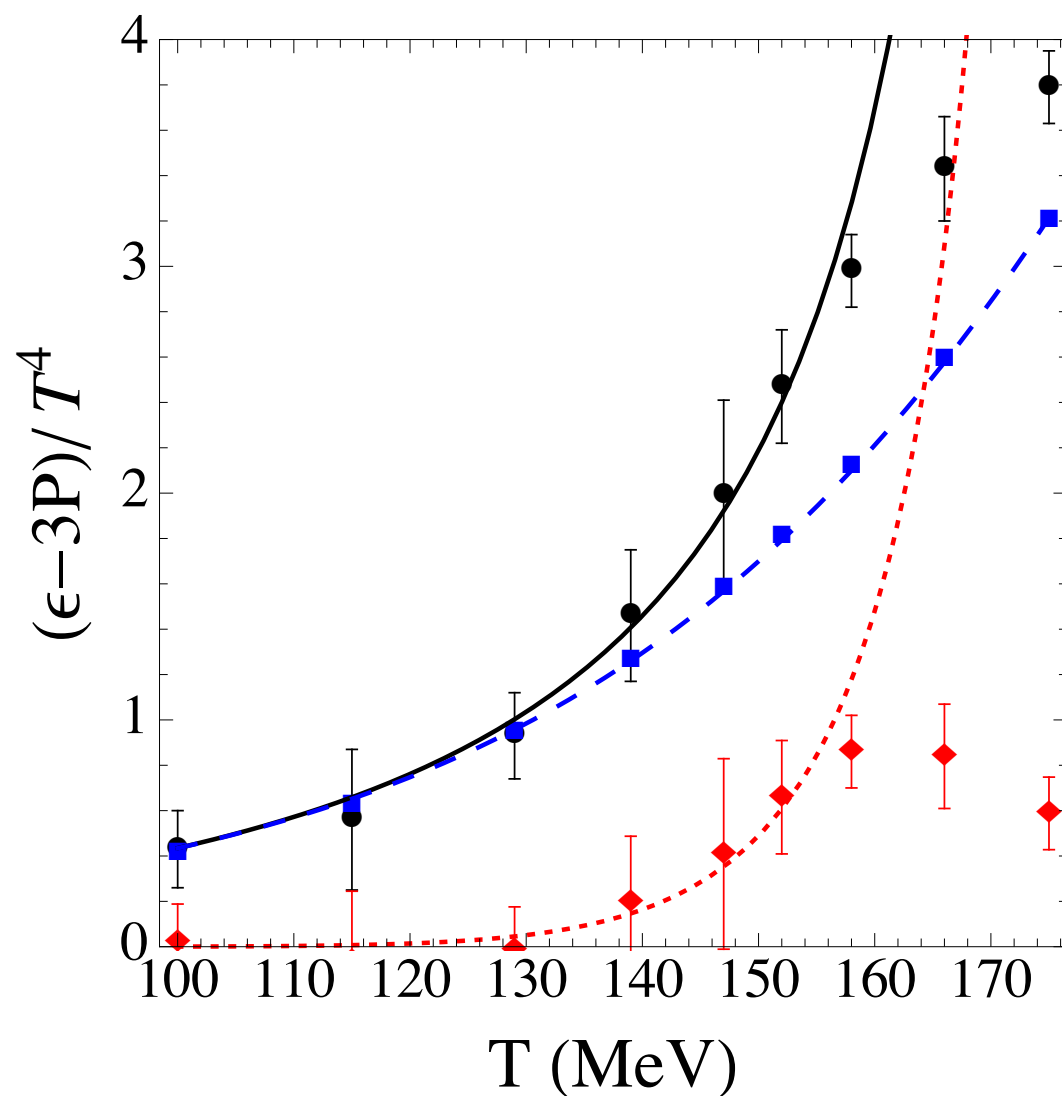
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Hadrons up to at least 2.5 GeV
(maybe 3 GeV) mass contribute



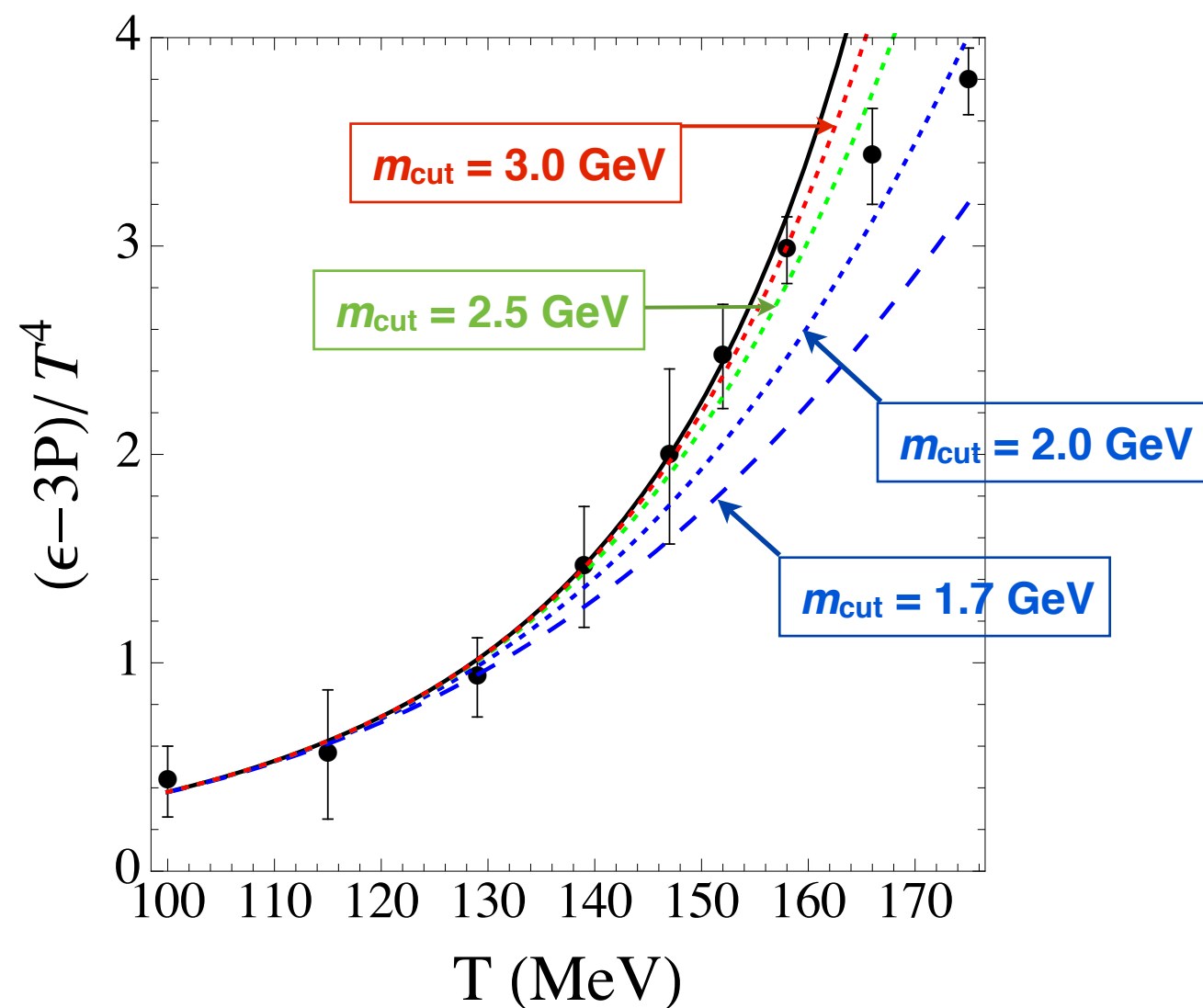
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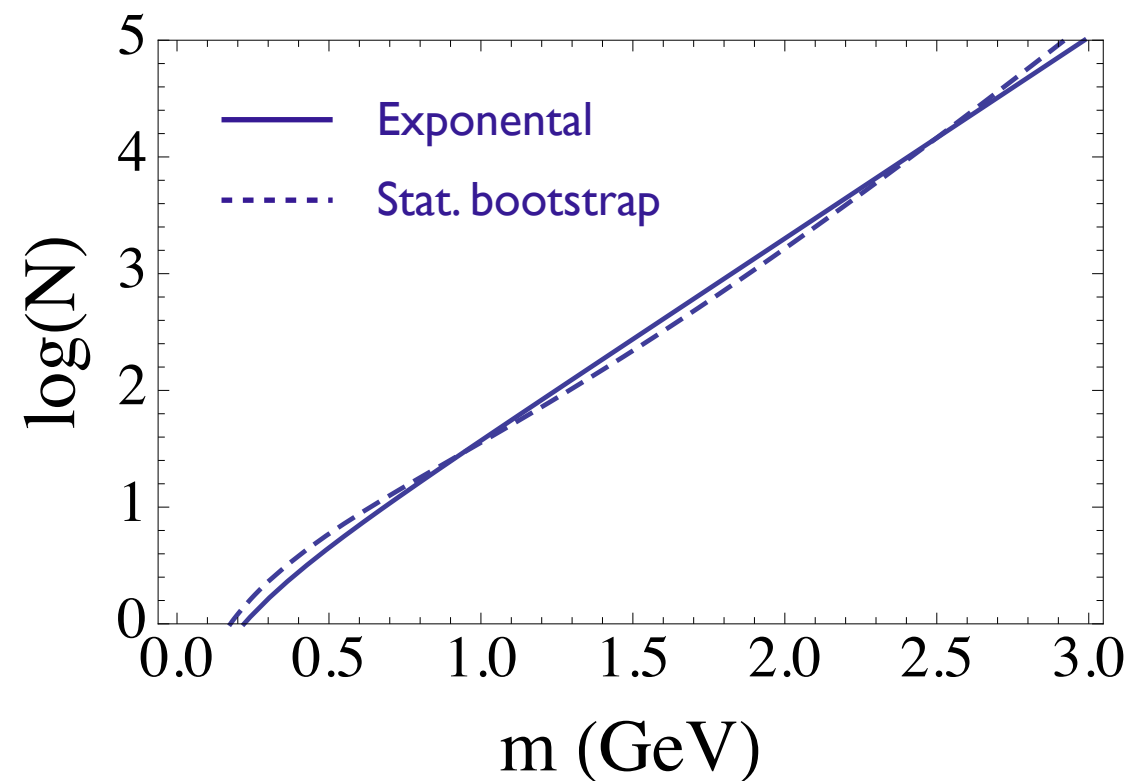
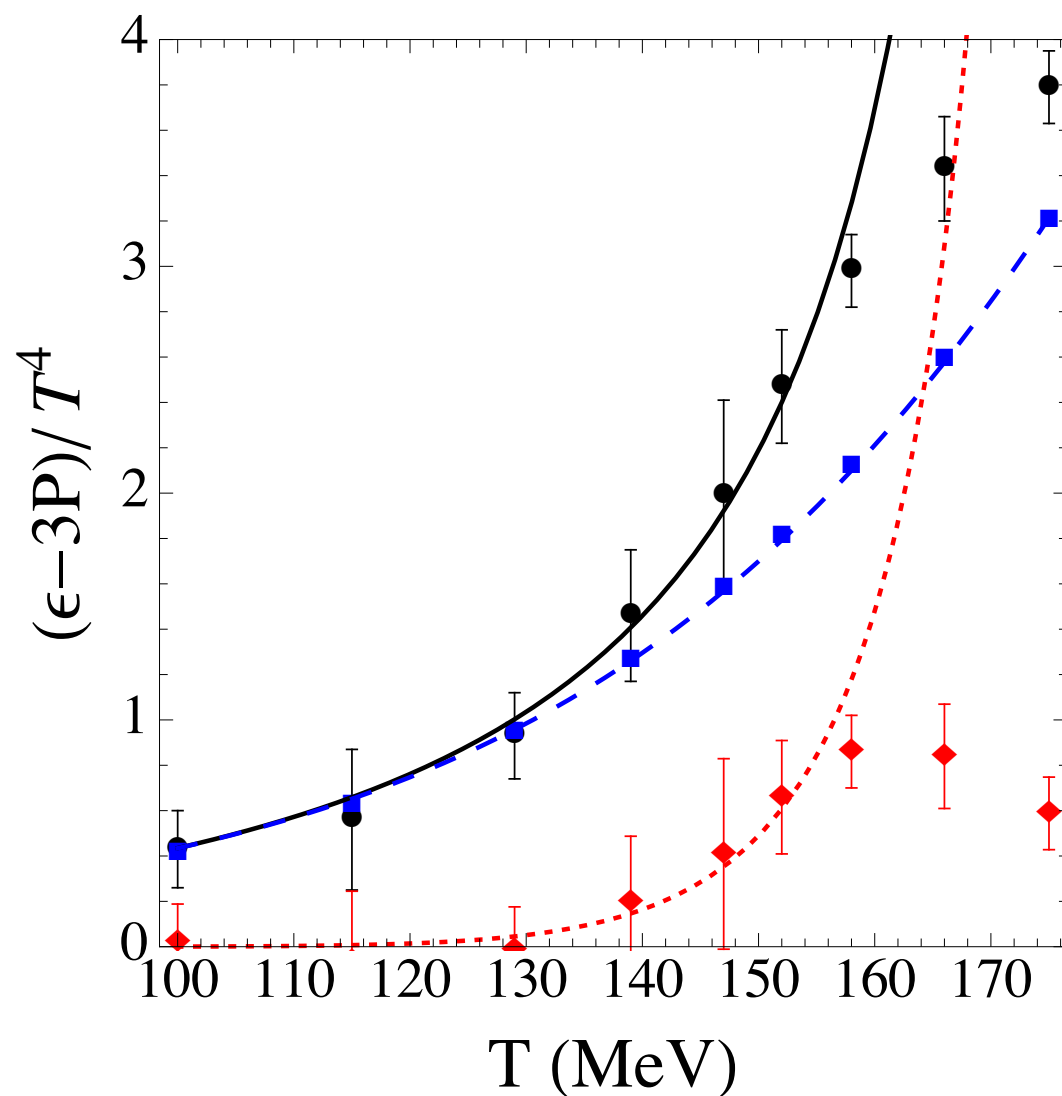
$$\rho(m) = A (m^2 + m_0^2)^{-5/4} e^{bm}$$

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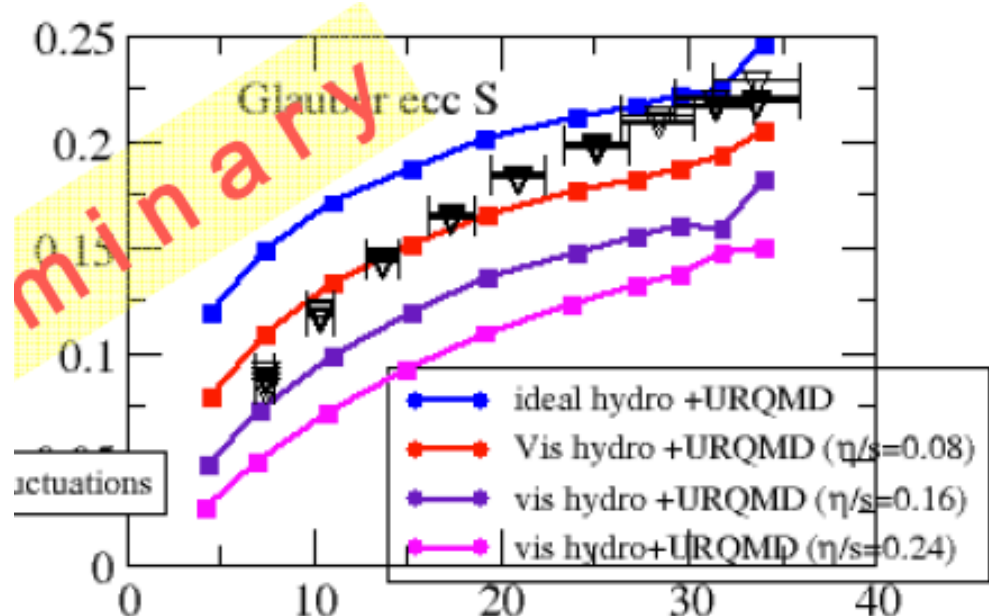
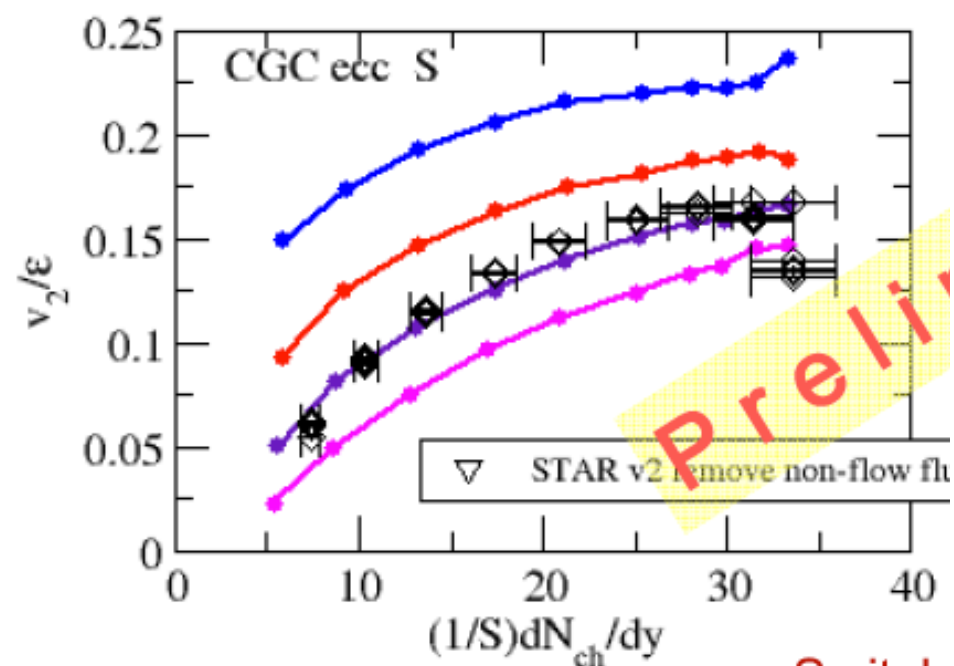
A. Majumder & B.M. (arXiv:1008.1747)

Challenge #2

The Perfect Fluid

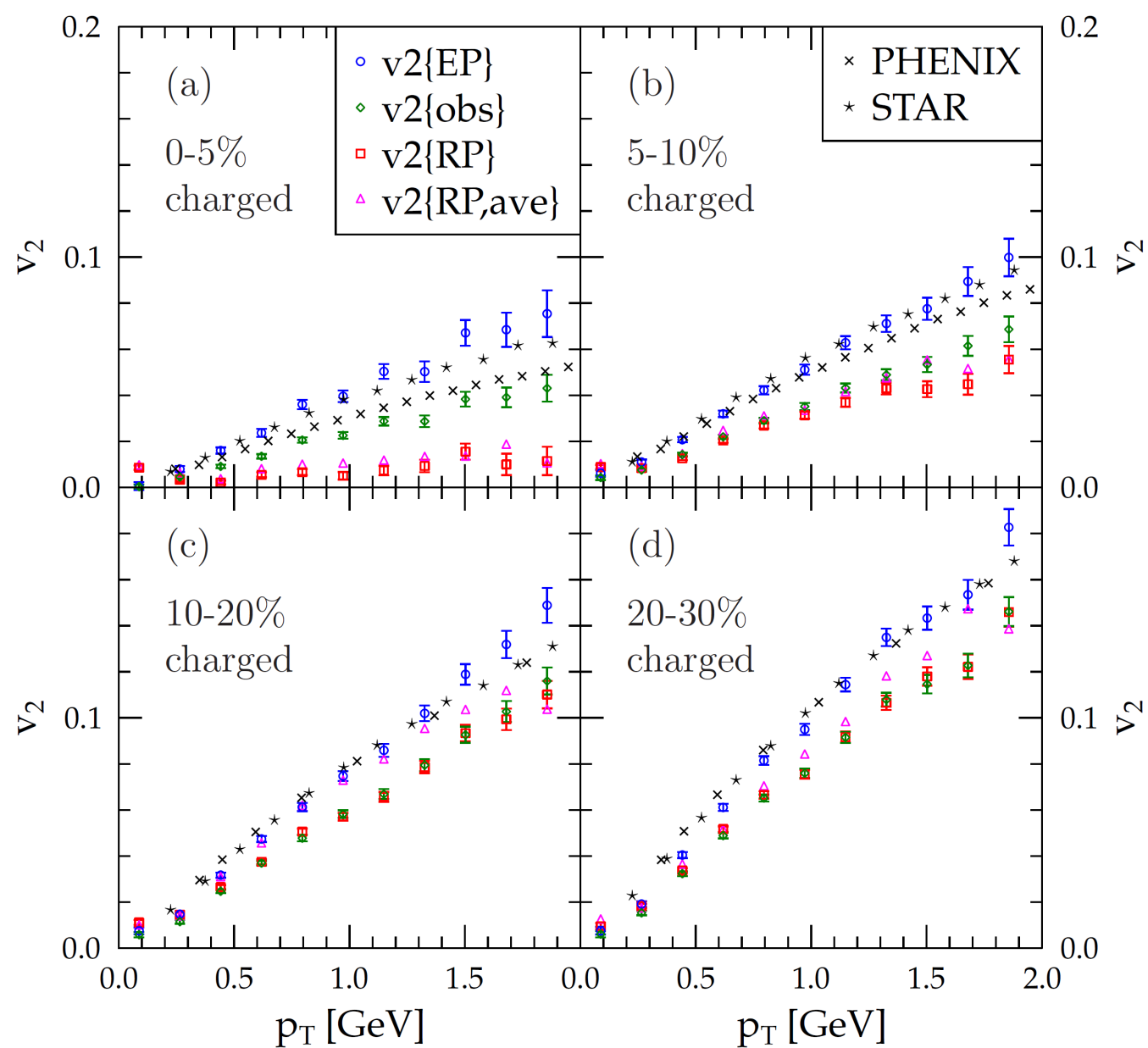
Deducing η/s from the data

H. Song, U. Heinz, et al.



ing temperature $T_{sw}=160$ MeV.

K.Eskola, H. Holopainen, H. Niemi



Deducing η/s from the data

Five effects have been identified as important ingredients:

- Shear viscosity
- Equation of state
- Differential freeze-out
- Initial transverse profile
- Initial-state fluctuations

Any compelling extraction of η/s from the data must account for **all five** !

Multiple dependencies require more than v_2 data; also spectra, identified particle data, HBT, etc.

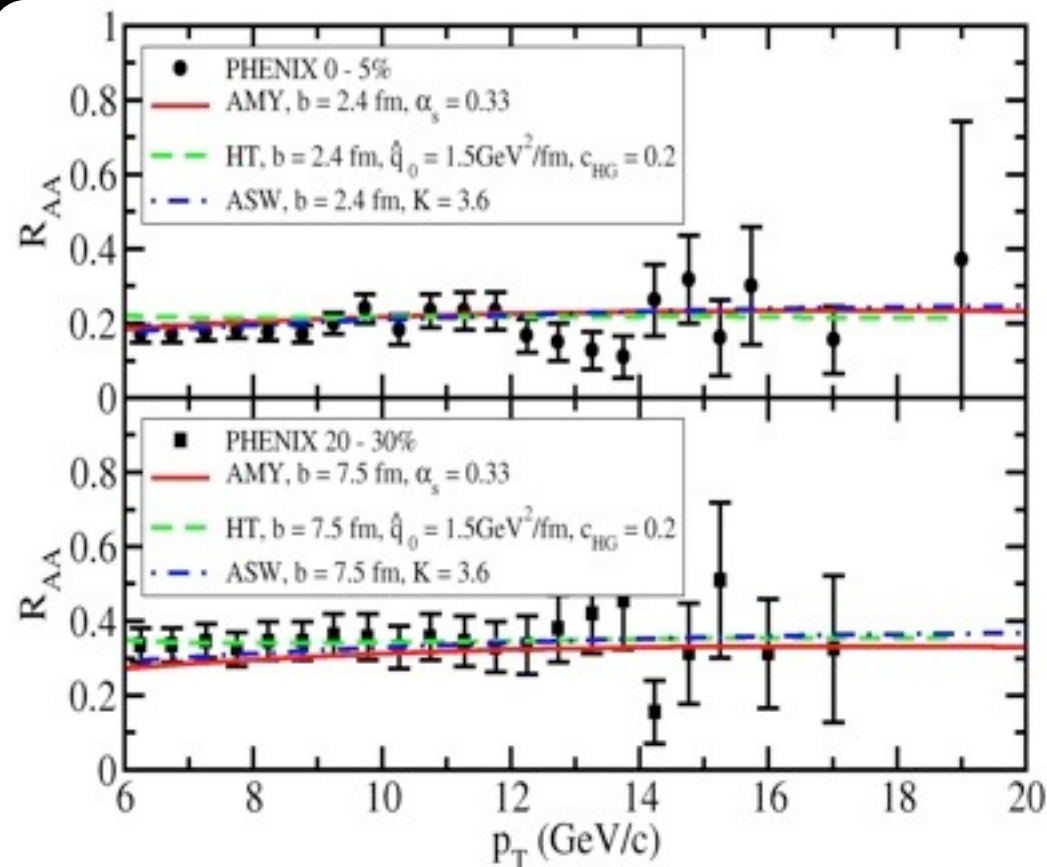
In other words, global description of bulk “soft” observables.

MADAI collaboration will do it - but a competitor would be good.

Challenge #3

Jet quenching

Deducing q^\wedge from the data



same 3D-hydro medium, 3 different schemes:

- R_{AA} in (semi-)central collisions is well described by all jet energy-loss schemes
- parameters reflect response of medium structure hard-wired into schemes
- large variation in extracted q^\wedge : 4-18 !!

How does the transport coefficient scale with the thermodynamic properties of the medium? Does the choice of T , ϵ or s matter?

- EoS for ideal QGP
- common choices for scaling:
 $\hat{q} \sim T^3$ $\hat{q} \sim \epsilon^{3/4}$ $\hat{q} \sim s$
- for non-ideal EoS, value is affected by choice of scaling variable!

q_0 [$\text{GeV}^2/$	ASW	HT	AMY
T	10	2.3	4.1
ϵ	18.5	4.5	X
s		4.3	X

Deducing q^\wedge from data

Any compelling extraction of q^\wedge from the data requires:

- Convergence of jet quenching schemes
- Improvement over eikonal-collinear approximation
- Realistic simulation of the bulk medium
- Treatment of elastic and radiative energy loss on equal terms
- Multi-gluon correlations?
- Explanation for large v_2 at large p_T

Is there a *golden channel* for energy loss theory?

B -quark energy loss at $p_T(b) = 50$ GeV could be it: p_T , m_b , are large scales, $p_T/m_b \gg 1$ ensures hadronization outside the medium.

Ideal measurement for the LHC. State of the art theory are needed !

Challenge #4

Quarkonium

Q-Qbar effective theory

Up to order $m\alpha_s^5$ [J. Giglieri, N. Brambilla, et al., arXiv:1007.4156]

$$\begin{aligned}
 \delta E_{n,l} = & \frac{\pi}{9} N_c C_F \alpha_s^2 T^2 \frac{a_0}{2} [3n^2 - l(l+1)] + \frac{\pi}{3} C_F^2 \alpha_s^2 T^2 a_0 \\
 & + \frac{E_n \alpha_s^3}{3\pi} \left[\log \left(\frac{2\pi T}{E_1} \right)^2 - 2\gamma_E \right] \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left[\frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right] \right. \\
 & \quad \left. + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \right\} + \frac{2E_n C_F^3 \alpha_s^3}{3\pi} L_{n,l} \\
 & + \frac{a_0^2 n^2}{2} [5n^2 + 1 - 3l(l+1)] \left\{ - \left[\frac{3}{2\pi} \zeta(3) + \frac{\pi}{3} \right] C_F \alpha_s T m_D^2 \right. \\
 & \quad \left. + \frac{2}{3} \zeta(3) N_c C_F \alpha_s^2 T^3 \right\} \\
 \\
 \Gamma_{n,l} = & \frac{1}{3} N_c^2 C_F \alpha_s^3 T + \frac{4}{3} \frac{C_F^2 \alpha_s^3 T}{n^2} (C_F + N_c) \\
 & + \frac{2E_n \alpha_s^3}{3} \left\{ \frac{4C_F^3 \delta_{l0}}{n} + N_c C_F^2 \left[\frac{8}{n(2l+1)} - \frac{1}{n^2} - \frac{2\delta_{l0}}{n} \right] + \frac{2N_c^2 C_F}{n(2l+1)} + \frac{N_c^3}{4} \right\} \\
 & - \left[\frac{C_F}{6} \alpha_s T m_D^2 \left(\ln \frac{E_1^2}{T^2} + 2\gamma_E - 3 - \log 4 - 2 \frac{\zeta'(2)}{\zeta(2)} \right) + \frac{4\pi}{9} \ln 2 N_c C_F \alpha_s^2 T^3 \right] \\
 & \quad \times a_0^2 n^2 [5n^2 + 1 - 3l(l+1)] \\
 & + \frac{8}{3} C_F \alpha_s T m_D^2 a_0^2 n^4 I_{n,l}
 \end{aligned}$$

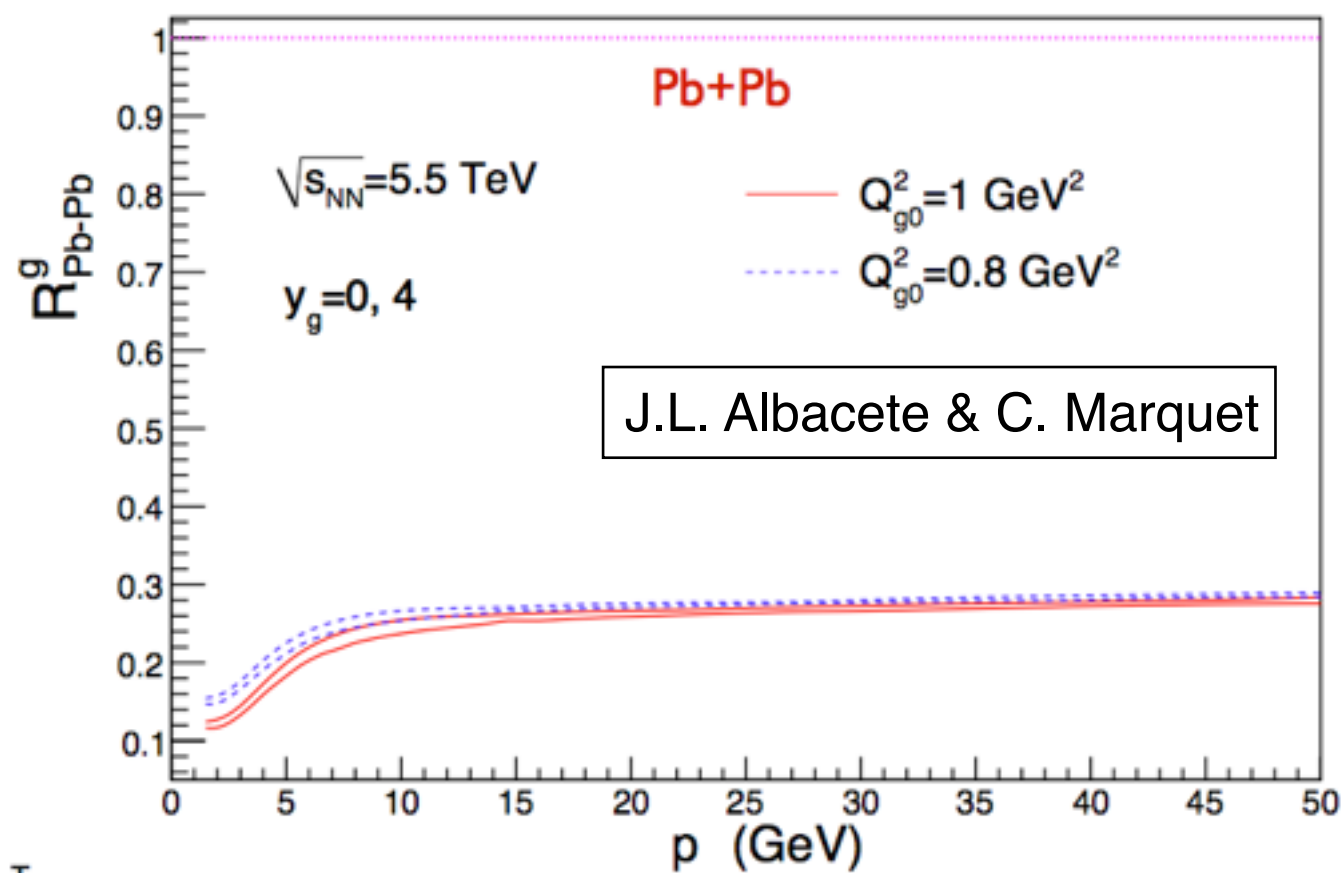
Lattice QCD etc:
See M. Asakawa's
and H. Satz' talks
next week.

Challenge #5

CGC or not CGC
...that is the question...

Gluon shadowing

Nuclear gluon density suppression at LHC
in the NLO CGC formalism.



Critical (?) test:

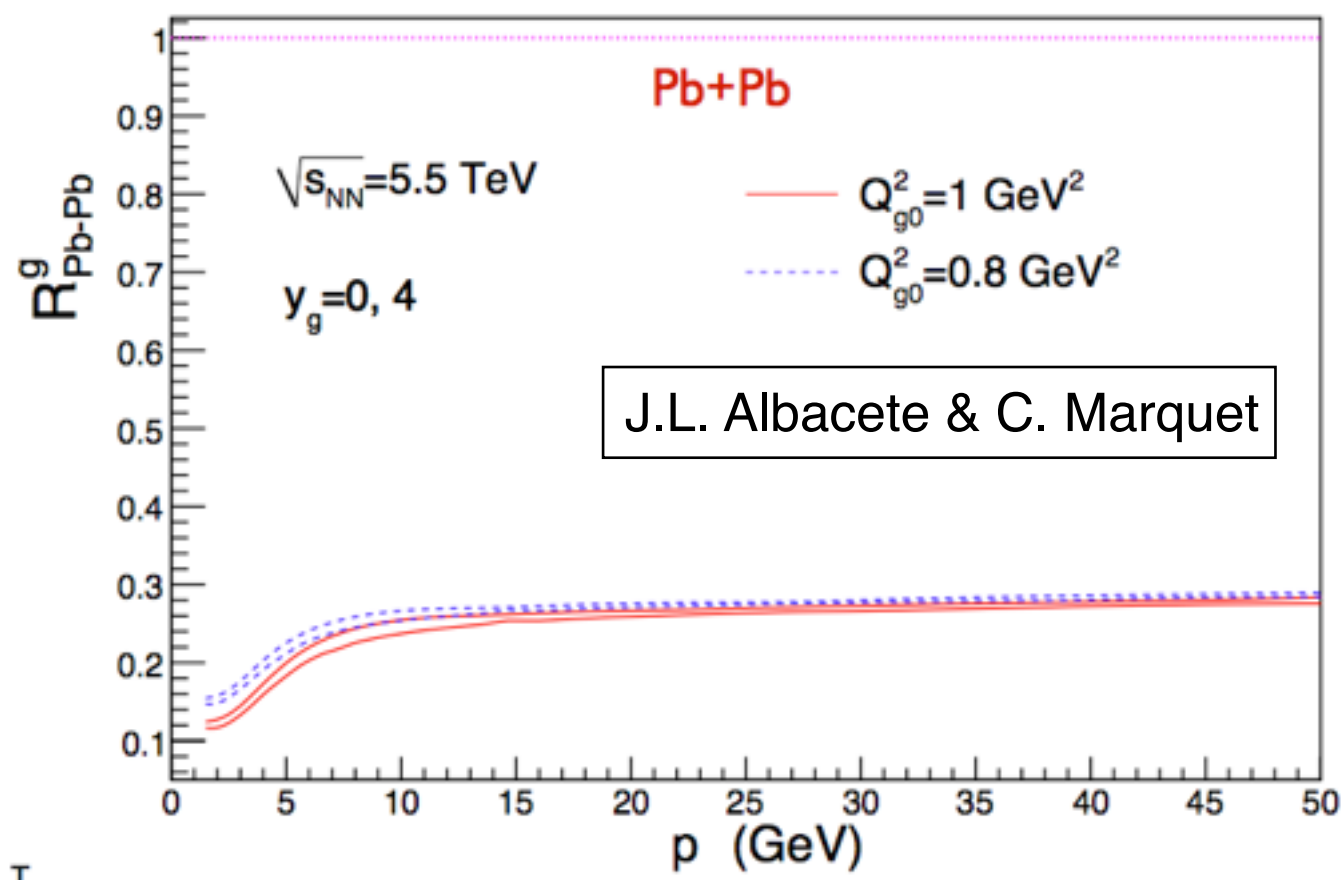
Calculate direct photon yield in
Pb+Pb at $p_T = 30 \text{ GeV}/c$ in

- the k_T -factorized NLO CGC formalism;
- the collinear pQCD formalism with HT-generated shadowing;
- other formalisms.

Should be done before LHC
data become available!

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If this test does not provide clarity, we may need to wait for p+Pb.

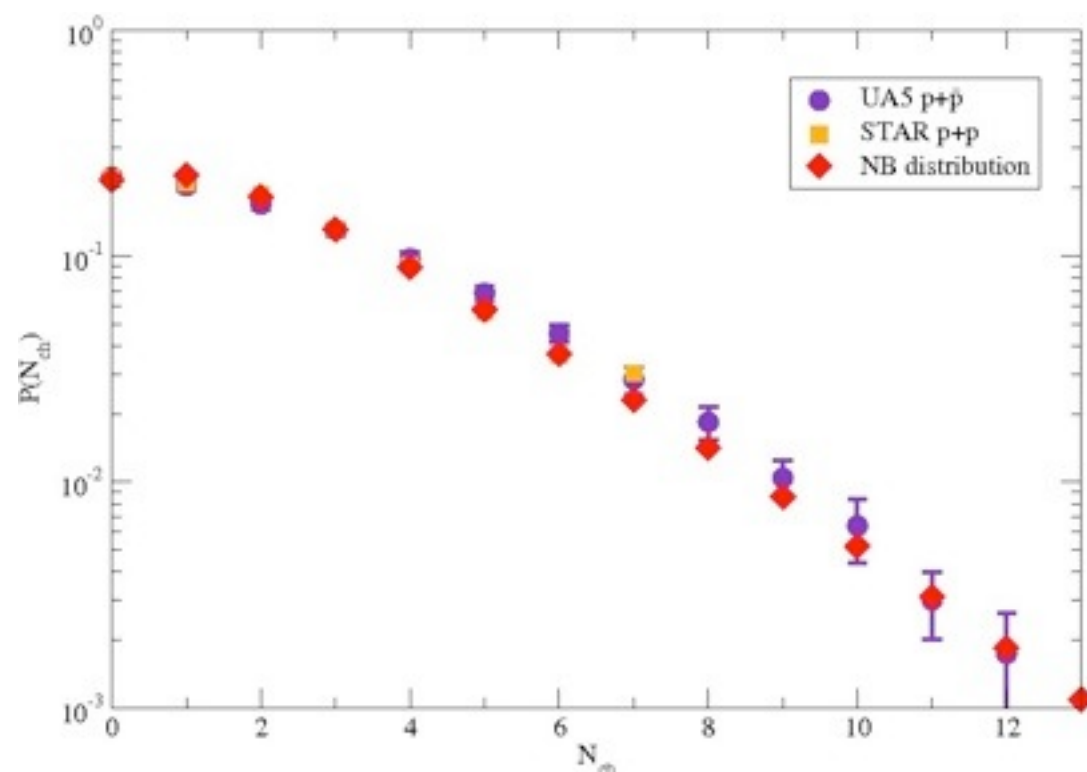
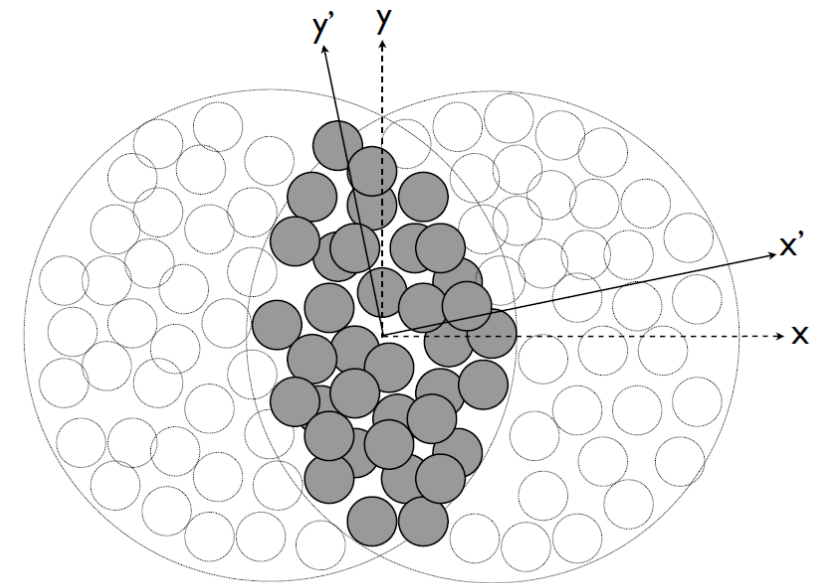
Challenge #6

One event at a time...

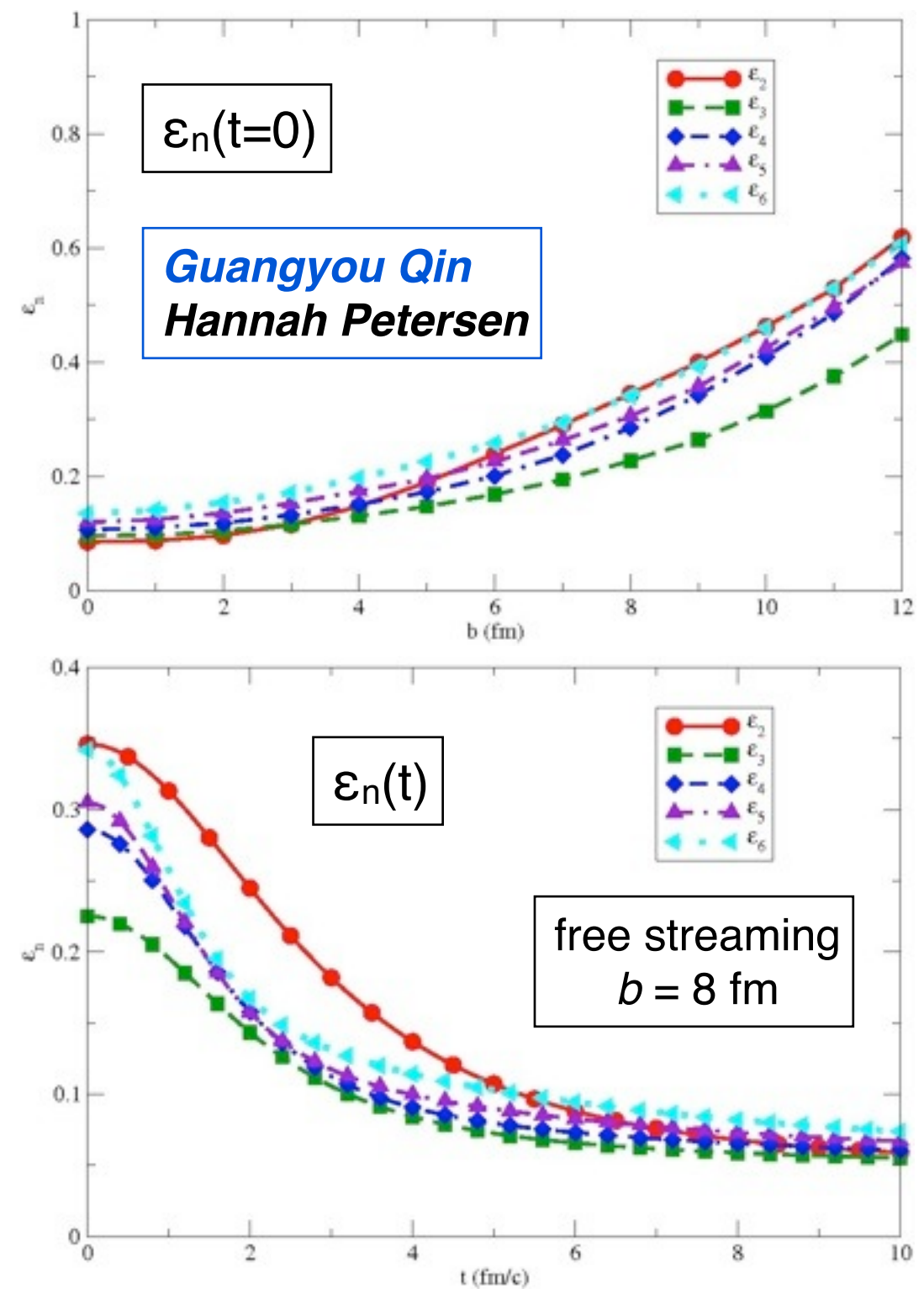
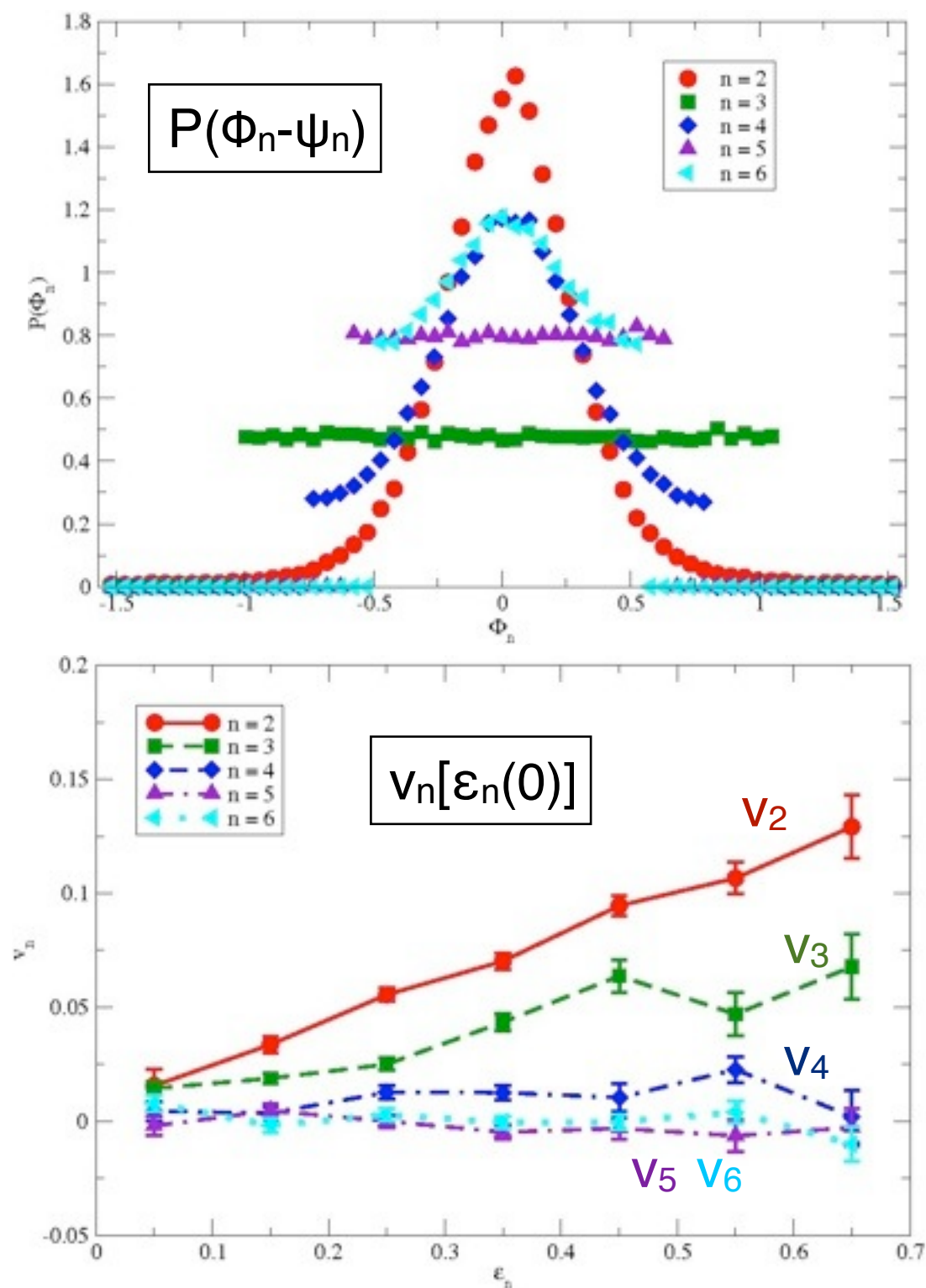
Initial state fluctuations

... need to account for fluctuations in:

- the locations of nucleons in colliding nuclei
- the NN cross section
- the energy deposition in NN collisions
- or, the leading color charge distributions (CGC).

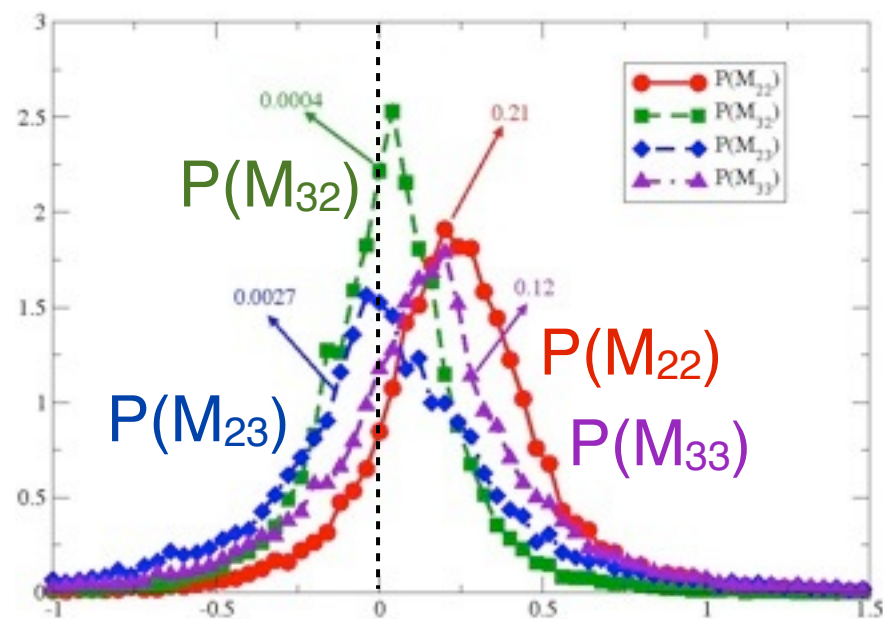
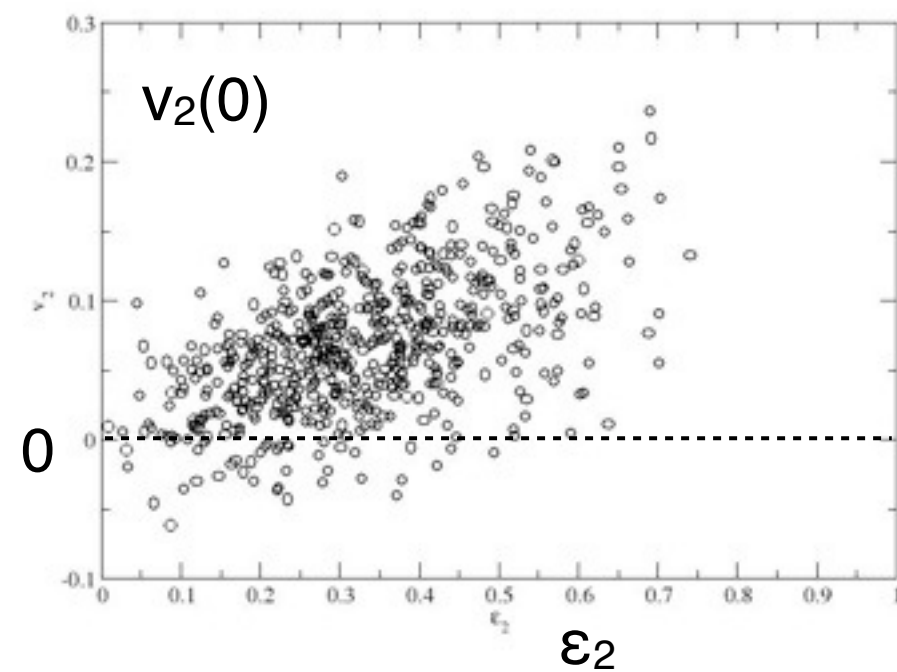
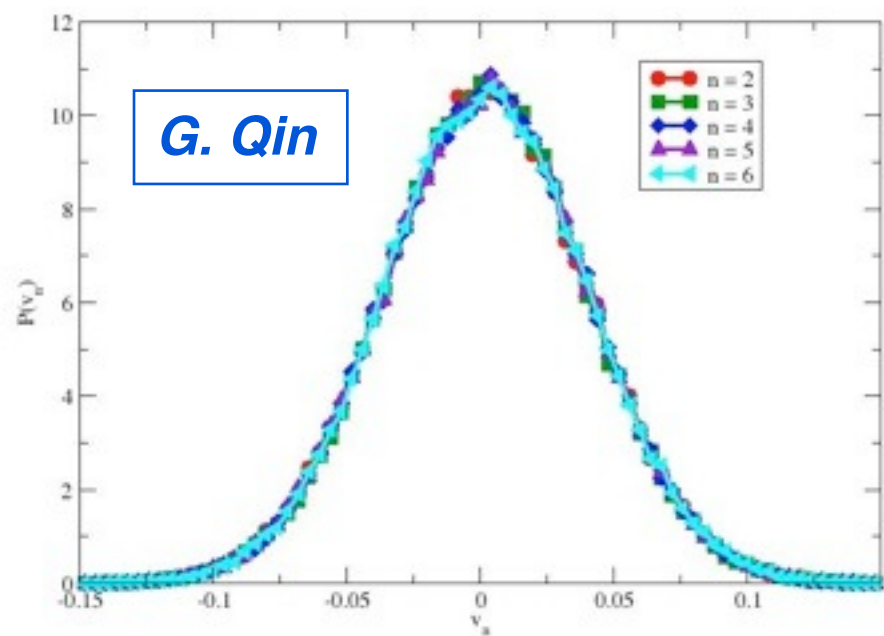


Multipole analysis



Initial v_n

Finite particle number (invoking “hadron-parton duality”) implies that $v_n(0) \neq 0$!



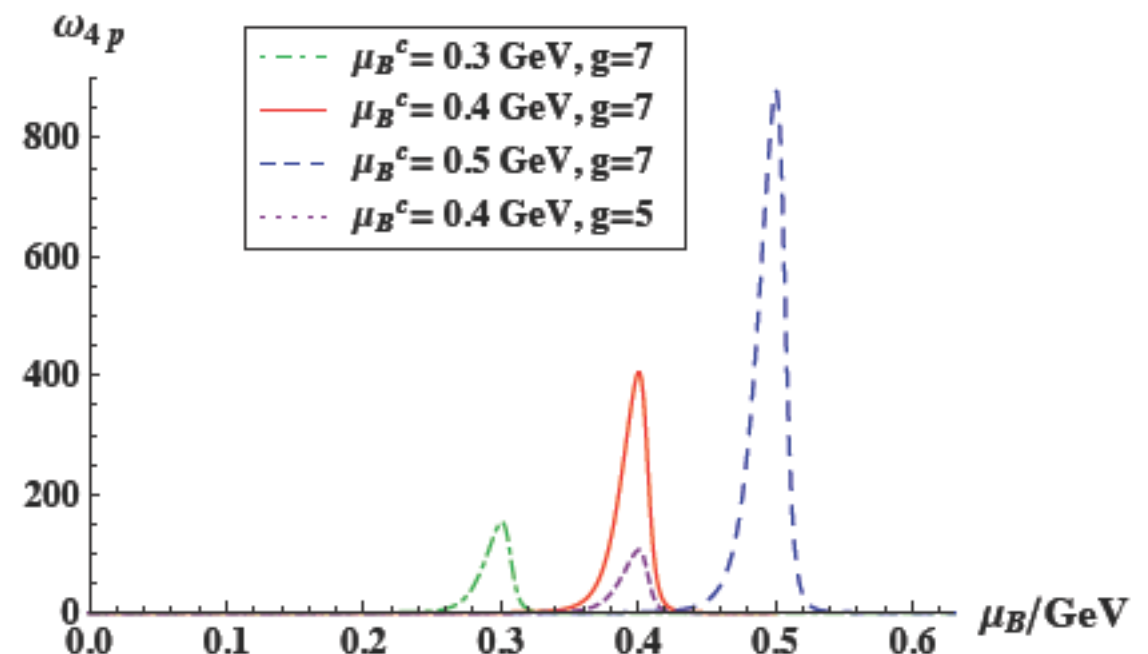
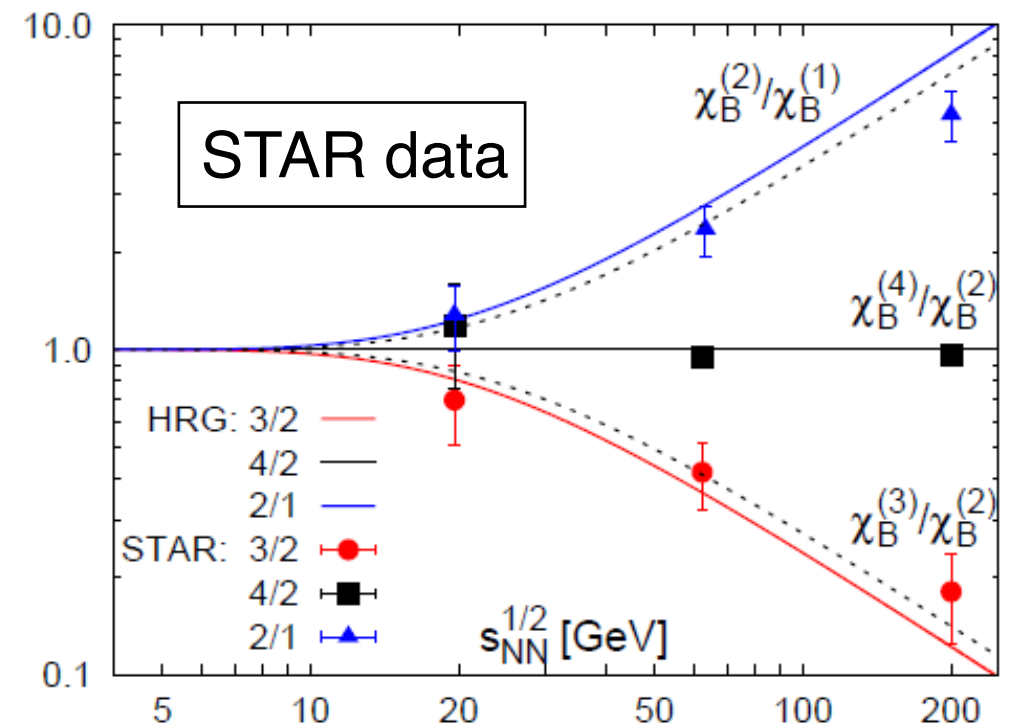
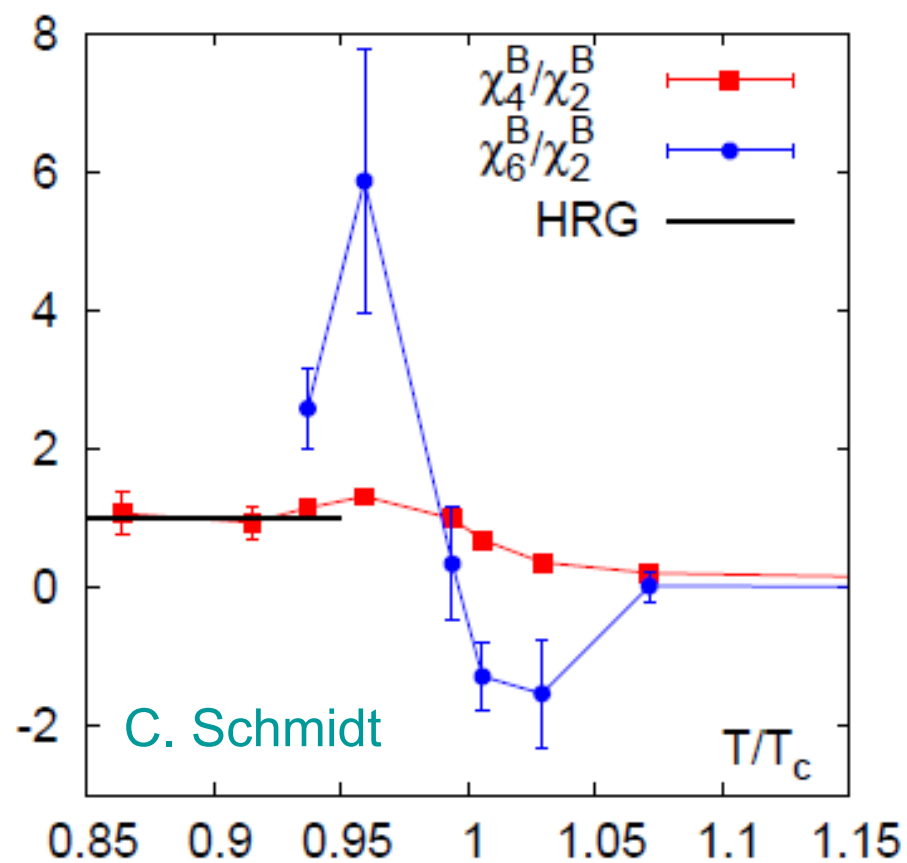
Correlation between v_n and ϵ_n :

$$\begin{pmatrix} v_2 \\ v_3 \end{pmatrix} = \begin{pmatrix} M_{22} & M_{23} \\ M_{32} & M_{33} \end{pmatrix} \begin{pmatrix} \epsilon_2 \\ \epsilon_3 \end{pmatrix}$$

Final-state fluctuations

Ratios of susceptibilities are good probes of QCD critical point (Karsch, Redlich)

Ratios of cumulants of particle yields are experimental analogue (Athanasίου, Rajagopal, Stephanov)



■ Challenges for the 2010's:

- *Quantitative* connection between matter properties and observables
- *Ab initio* QCD equation of state at $\mu_B \neq 0$, critical point
- *Ab initio* calculation of transport coefficients
- Theoretical understanding of QCD at intermediate coupling
- *Quantitative* theory of the low- x parton structure of nuclei

Paths to progress

Progress in the exploration of hot QCD matter in the coming decade will require:

- Consensus among theorists about the “valid” approaches to problems
- Resolution of limitations of formalisms
- Realistic simulations of observables
- Collaboration among champions of different approaches (TEC-HQM may be a good model)
- Of course, there is always the traditional alternative....

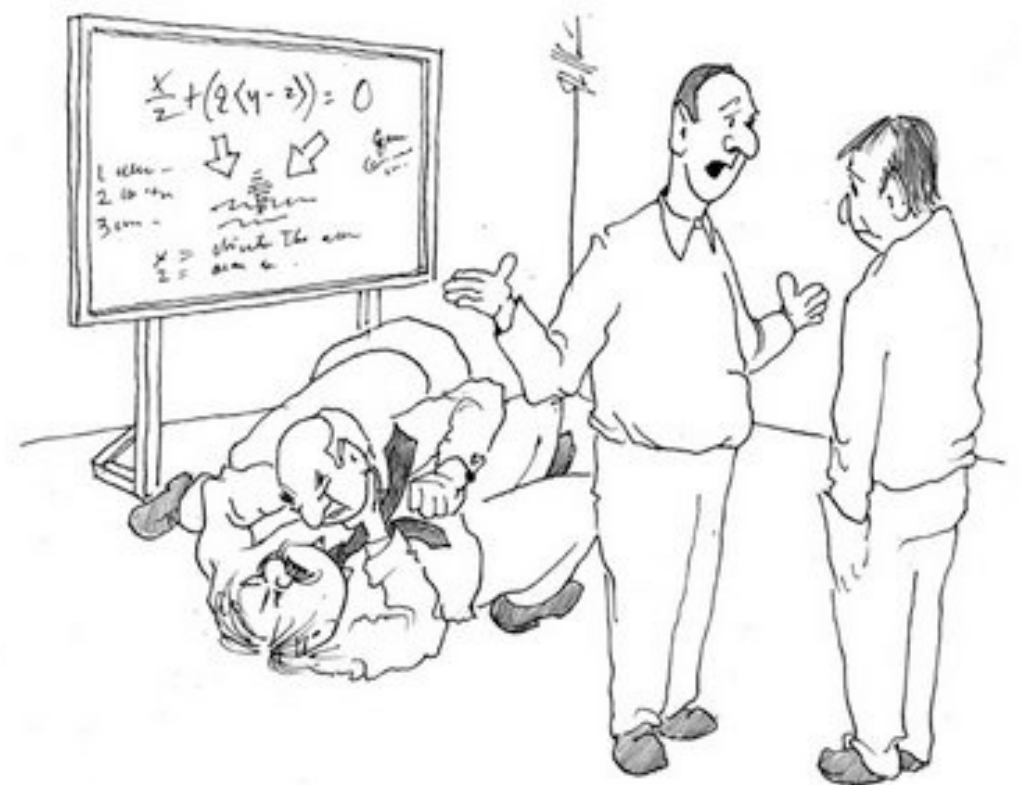
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The world before TEC-HQM

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“Hey, that’s scientists for you. Keswick and Murphy just can’t seem to agree on the theory of jet quenching.”