
Determination of properties of a Higgs-like resonance at LHC: separation of spin hypotheses

S. Bolognesi^(a), Y. Gao^(c), A. Gritsan^(a), K. Melnikov^(a),
M. Schulze^(b), N. Tran^(c), A. Whitbeck^(a)

(a) Johns Hopkins University,

(b) Argonne National Laboratory,

(c) Fermi National Laboratory



**36th International Conference
on High Energy Physics**

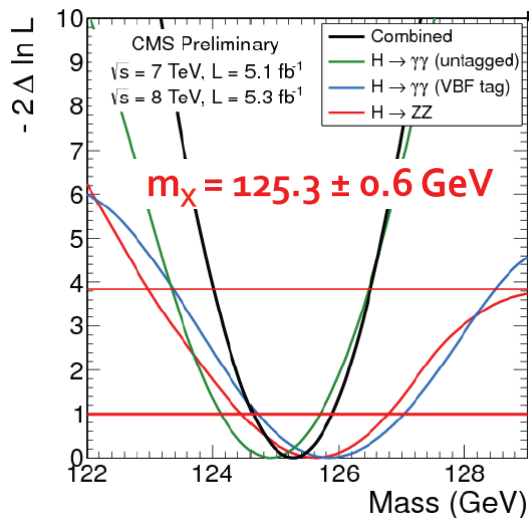
4 – 11 July 2012

Melbourne Convention and Exhibition Centre

Properties measurement

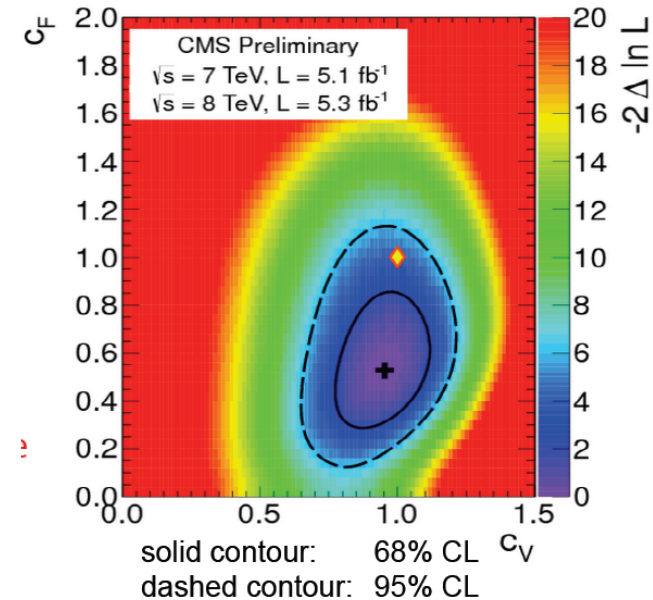
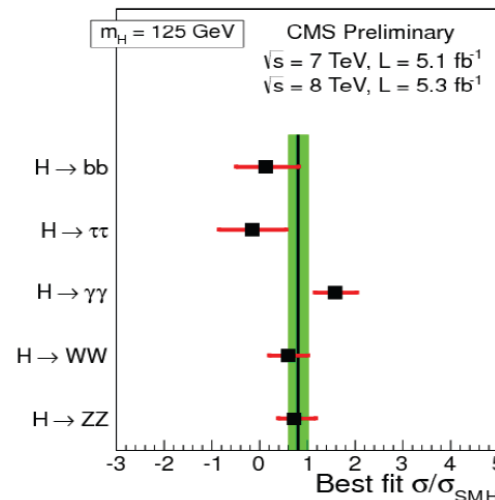
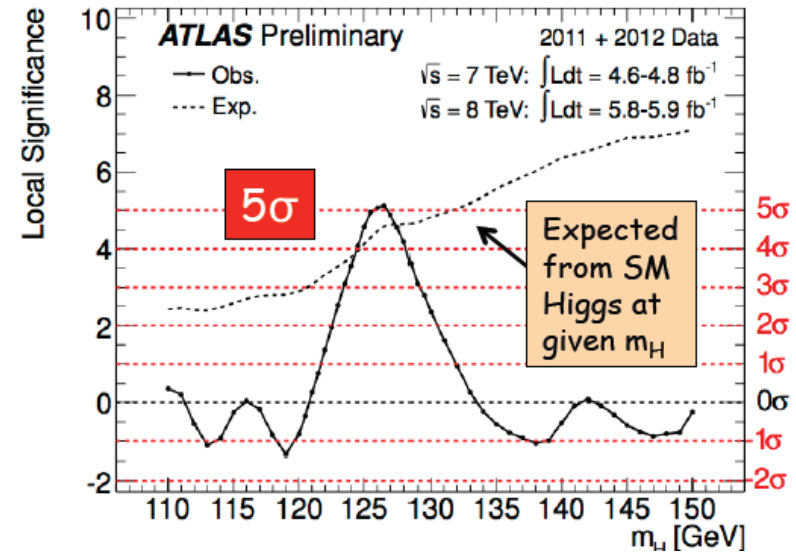
□ The signal observation is just the beginning ... long road ahead of us: **properties measurement**

- observation of an excess -> **mass and width**
- measure amplitude in different channels -> **xsec, branching ratios and couplings to V and f**



- differential distributions -> study tensor structure of the amplitudes: **spin/parity and couplings**

□ All properties are correlated



“Higgs-like” most general amplitude

□ Same amplitude for production (VV→X) and decay (X→VV):

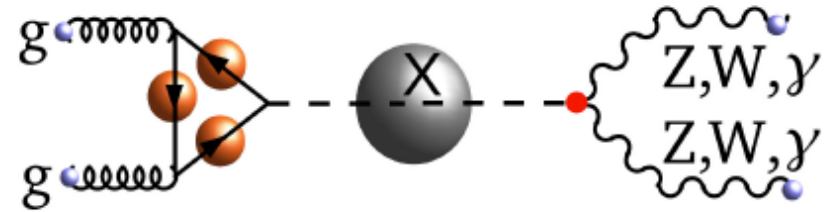
▪ **Spin 0:** $A(X \rightarrow V_1 V_2) = v^{-1} \epsilon_1^{*\mu} \epsilon_2^{*\nu} \left(a_1 g_{\mu\nu} M_X^2 + a_2 q_{1\mu} q_{2\nu} + a_3 \epsilon_{\mu\nu\alpha\beta} q_1^\alpha q_2^\beta \right)$

▶ SM Higgs→ZZ,WW:

$a_1 \neq 0, a_2 \sim O(10^{-2}), a_3 \sim O(10^{-11})$

▶ SM Higgs→γγ: $a_1 = -a_2/2 \neq 0$

▶ BSM pseudo-scalar Higgs $a_3 \neq 0$



▪ **Spin 1:** $A(X \rightarrow ZZ) = g_1^{(1)} [(\epsilon_1^* q)(\epsilon_2^* \epsilon_X) + (\epsilon_2^* q)(\epsilon_1^* \epsilon_X)] + g_2^{(1)} \epsilon_{\alpha\mu\nu\beta} \epsilon_X^\alpha \epsilon_1^{*,\mu} \epsilon_2^{*,\nu} \tilde{q}^\beta.$

▪ **Spin 2:** $A(X \rightarrow ZZ) = \Lambda^{-1} e_1^{*\mu} e_2^{*\nu} \left[c_1 (q_1 q_2) t_{\mu\nu} + c_2 g_{\mu\nu} t_{\alpha\beta} \tilde{q}^\alpha \tilde{q}^\beta + c_3 \frac{q_{2\mu} q_{1\nu}}{m_X^2} t_{\alpha\beta} \tilde{q}^\alpha \tilde{q}^\beta + 2c_4 (q_{1\nu} q_2^\alpha t_{\mu\alpha} + q_{2\mu} q_1^\alpha t_{\nu\alpha}) + c_5 t_{\alpha\beta} \frac{\tilde{q}^\alpha \tilde{q}^\beta}{m_X^2} \epsilon_{\mu\nu\rho\sigma} q_1^\rho q_2^\sigma + c_6 t^{\alpha\beta} \tilde{q}_\beta \epsilon_{\mu\nu\alpha\rho} q^\rho + \frac{c_7 t^{\alpha\beta} \tilde{q}_\beta}{m_X^2} (\epsilon_{\alpha\mu\rho\sigma} q^\rho \tilde{q}^\sigma q_\nu + \epsilon_{\alpha\nu\rho\sigma} q^\rho \tilde{q}^\sigma q_\mu) \right].$

▪ **Similarly for decay into fermions:** $A(X_{J=0} \rightarrow q\bar{q}) = \frac{m_q}{v} \bar{u}_{q_1} \left(\rho_1^{(0)} + \rho_2^{(0)} \gamma_5 \right) v_{q_2},$

$$A(X_{J=1} \rightarrow q\bar{q}) = \epsilon^\mu \bar{u}_{q_1} \left(\gamma_\mu \left(\rho_1^{(1)} + \rho_2^{(1)} \gamma_5 \right) + \frac{m_q \tilde{q}_\mu}{\Lambda^2} \left(\rho_3^{(1)} + \rho_4^{(1)} \gamma_5 \right) \right) v_{q_2},$$

$$A(X_{J=2} \rightarrow q\bar{q}) = \frac{1}{\Lambda} t^{\mu\nu} \bar{u}_{q_1} \left(\gamma_\mu \tilde{q}_\nu \left(\rho_1^{(2)} + \rho_2^{(2)} \gamma_5 \right) + \frac{m_q \tilde{q}_\mu \tilde{q}_\nu}{\Lambda^2} \left(\rho_3^{(2)} + \rho_4^{(2)} \gamma_5 \right) \right) v_{q_2},$$

(arXiv:1001.3396)

From couplings to angular analysis

- General amplitudes implemented in JHU MC -> able to generate any spin hypothesis !!!

QCD LO production but NLO correction to decay can be included in effective couplings a_i

(arXiv:1011.3396, <http://www.pha.jhu.edu/spin/>)

$$A(X \rightarrow V_1 V_2) = v^{-1} \epsilon_1^{*\mu} \epsilon_2^{*\nu} \left(a_1 g_{\mu\nu} M_X^2 + a_2 q_{1\mu} q_{2\nu} + a_3 \epsilon_{\mu\nu\alpha\beta} q_1^\alpha q_2^\beta \right)$$

- Analytical computation of helicity amplitudes

$$A_{00} = -\frac{M_X^4}{v} \left(a_1 x + a_2 \frac{M_{Z1} M_{Z2}}{M_X^2} (x^2 - 1) \right)$$

$$A_{\pm\pm} = \frac{M_X^2}{v} \left(a_1 \pm i a_3 \frac{M_{Z1} M_{Z2}}{M_X^2} \sqrt{x^2 - 1} \right)$$

$$x = \frac{M_X^2 - M_{Z1}^2 - M_{Z2}^2}{2 M_{Z1} M_{Z2}}$$

- Amplitudes parameterize angular distributions -> they can be extracted from data

eg, 0+ angular distribution:

$$4(1 - f_{++} - f_{--}) \sin^2 \theta_1 \sin^2 \theta_2$$

$$+ (f_{++} + f_{--}) ((1 + \cos^2 \theta_1)(1 + \cos^2 \theta_2) + 4 R_1 R_2 \cos \theta_1 \cos \theta_2)$$

$$- 2(f_{++} - f_{--}) (R_1 \cos \theta_1 (1 + \cos^2 \theta_2) + R_2 (1 + \cos^2 \theta_1) \cos \theta_2)$$

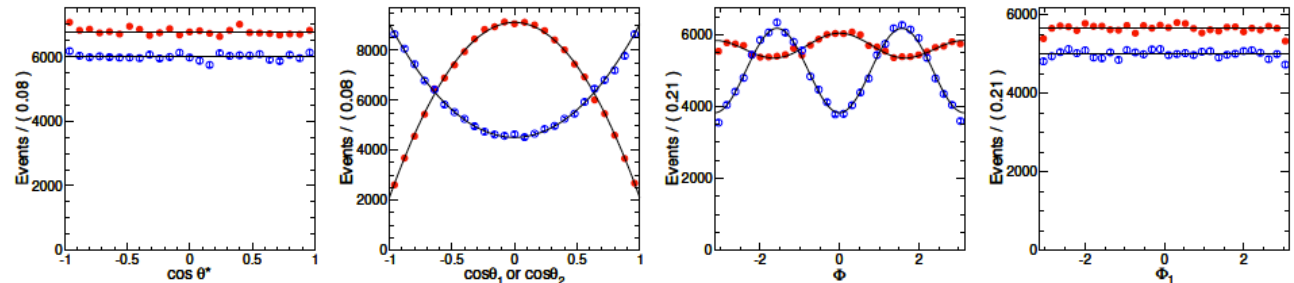
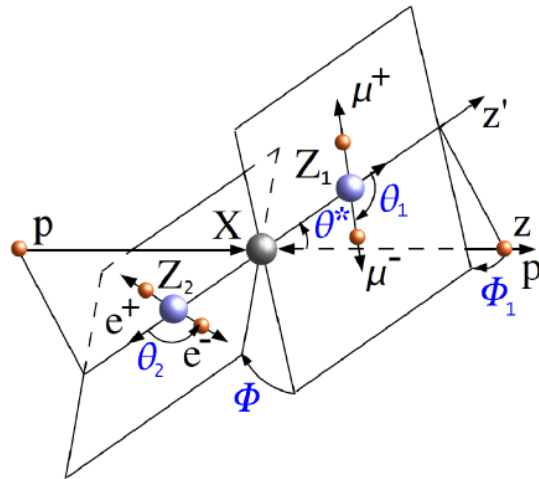
$$+ 4 \sqrt{f_{++} (1 - f_{++} - f_{--})} (R_1 - \cos \theta_1) \sin \theta_1 (R_2 - \cos \theta_2) \sin \theta_2 \cos(\Phi + \phi_{++})$$

$$+ 4 \sqrt{f_{--} (1 - f_{++} - f_{--})} (R_1 + \cos \theta_1) \sin \theta_1 (R_2 + \cos \theta_2) \sin \theta_2 \cos(\Phi - \phi_{--})$$

$$+ 2 \sqrt{f_{++} f_{--}} \sin^2 \theta_1 \sin^2 \theta_2 \cos(2\Phi + \phi_{++} - \phi_{--})$$

$$f_{ij} = |A_{ij}|^2, \phi_{ij} = \arg(A_{ij}/A_{00}), R_{1,2} = \frac{2c_A/c_V}{1+c_A^2/c_V^2} (= .15 \text{ for leptons})$$

Angular distributions for $X \rightarrow ZZ$ (250 GeV)



SM Higgs, Pseudo-Scalar (generator from arxiv.org:1001.3396)

5 / 19

1D projections for Vector, Pseudo-Vector
(generator from arxiv.org:1001.3396)

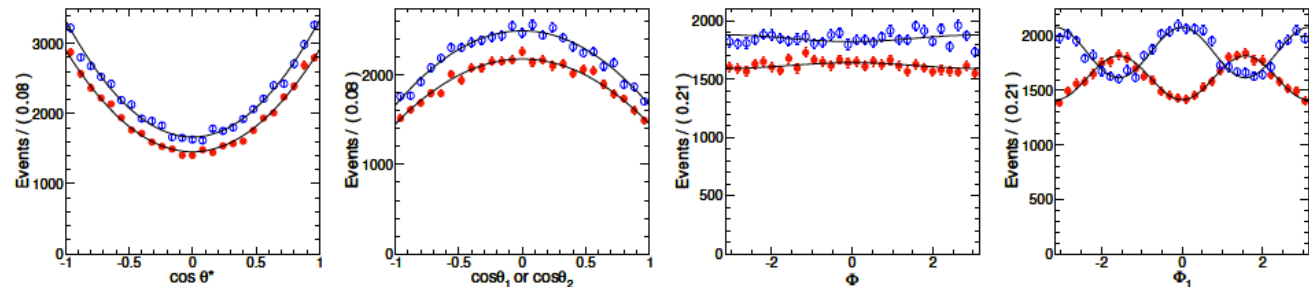
• “production” angles:
 θ^*, ϕ_1

• decay angles:
 θ_1, θ_2, ϕ

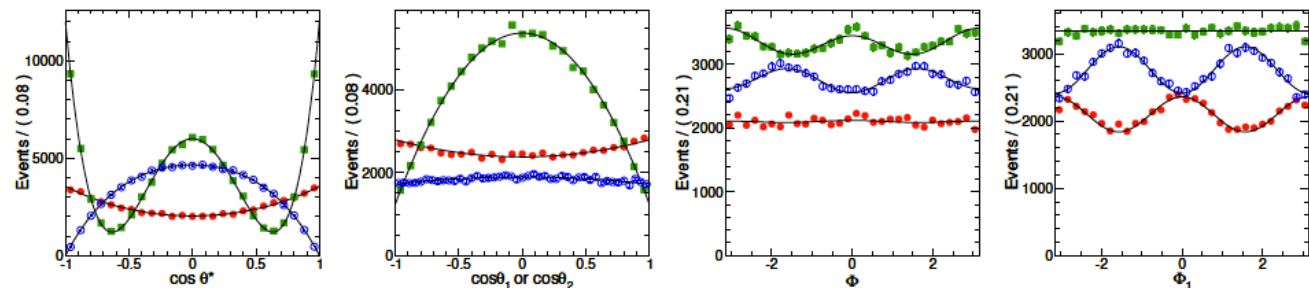
lines = analytical
computation

dots = MC generation

(much info also
from correlations!)



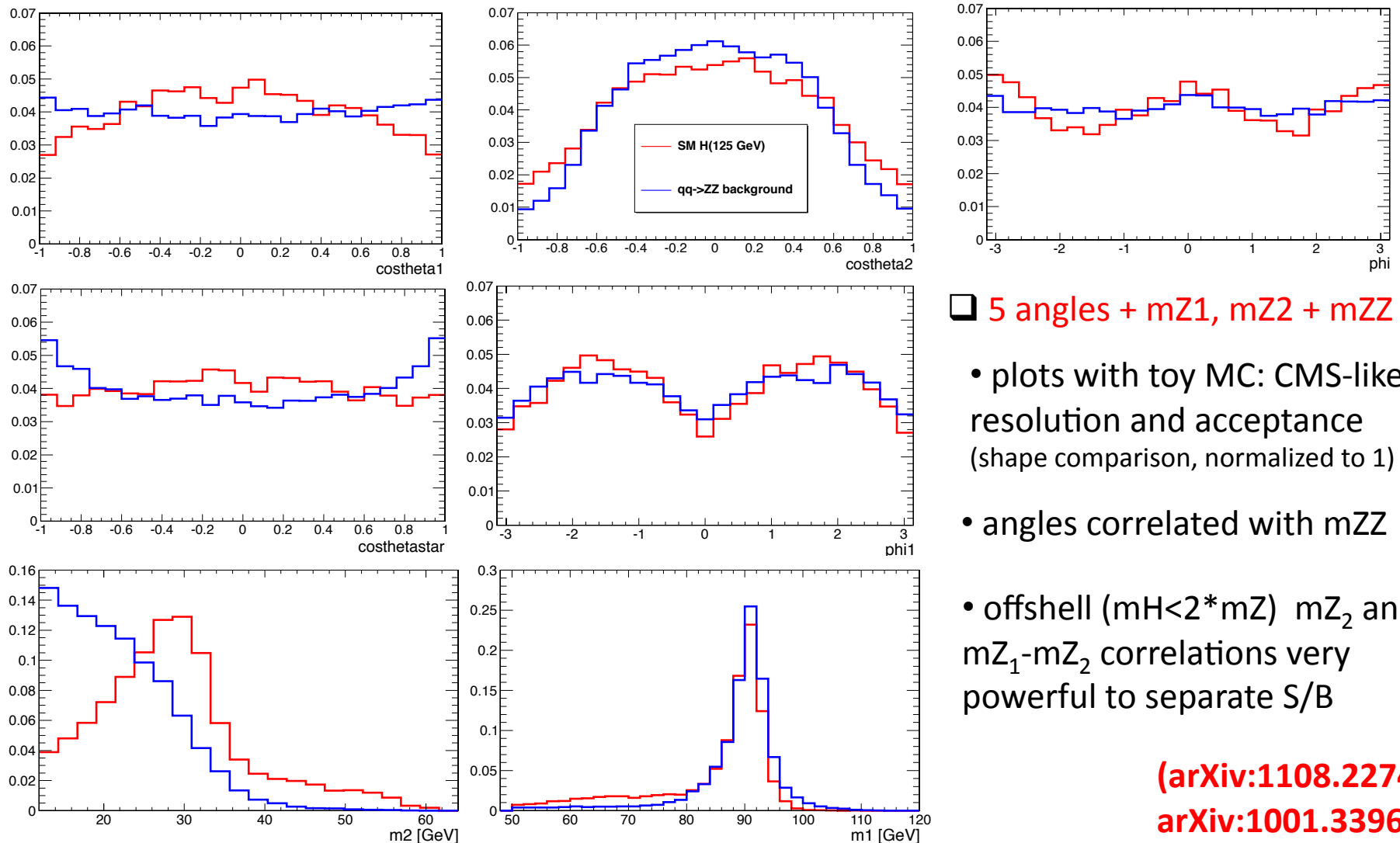
1D projections for $J^P = 2_M^+, 2_L^+, 2^-$
(generator from arxiv.org:1001.3396)



Angular analysis for Higgs- $\rightarrow$ ZZ search

Signal vs background -> Higgs search

Angular information can be used to separate Higgs signal from ZZ background



5 angles + m_{Z1} , m_{Z2} + m_{ZZ}

- plots with toy MC: CMS-like resolution and acceptance (shape comparison, normalized to 1)
- angles correlated with m_{ZZ}
- offshell ($m_H < 2 \cdot m_Z$) m_{Z_2} and $m_{Z_1} - m_{Z_2}$ correlations very powerful to separate S/B

(arXiv:1108.2274
arXiv:1001.3396)

MELA for Higgs search

□ Matrix Element Likelihood Approach:

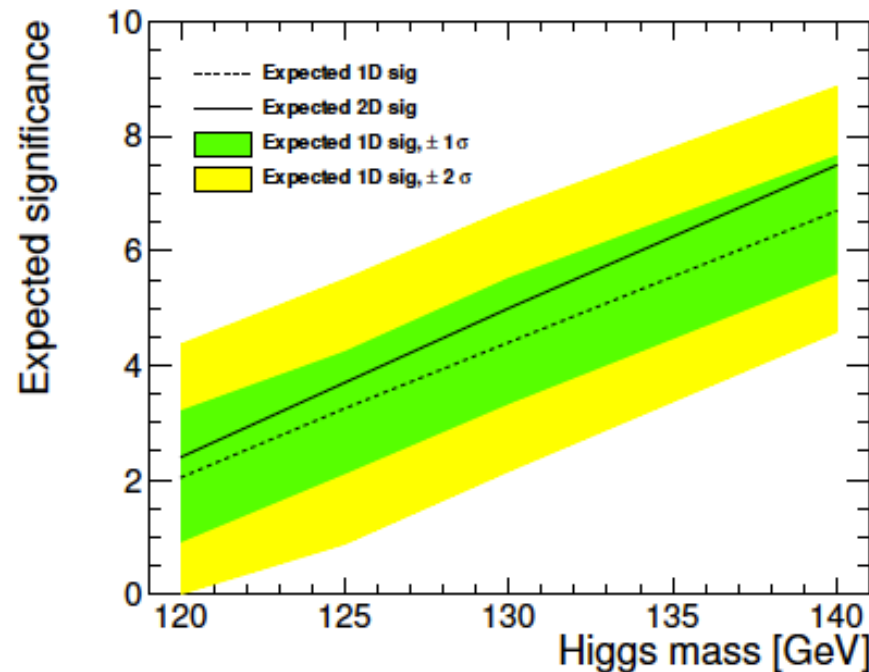
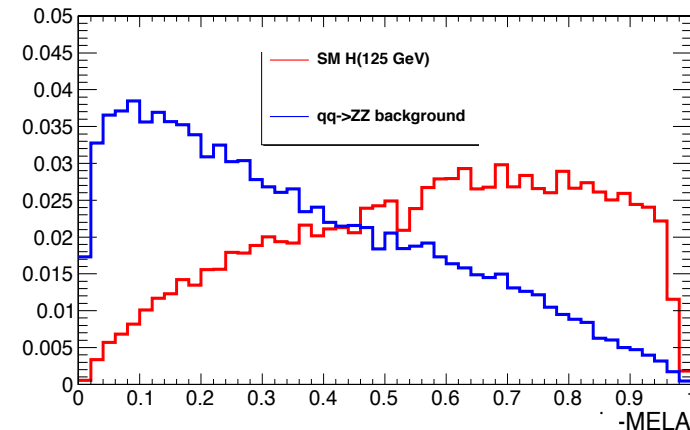
**analytical
likelihood built
from angular
distributions**

$$\text{MELA} = \frac{P_{\text{sig}}}{P_{\text{sig}} + P_{\text{bkg}}}$$

- acceptance effects cancel in the ratio to first order
- unaccounted effects make likelihood suboptimal

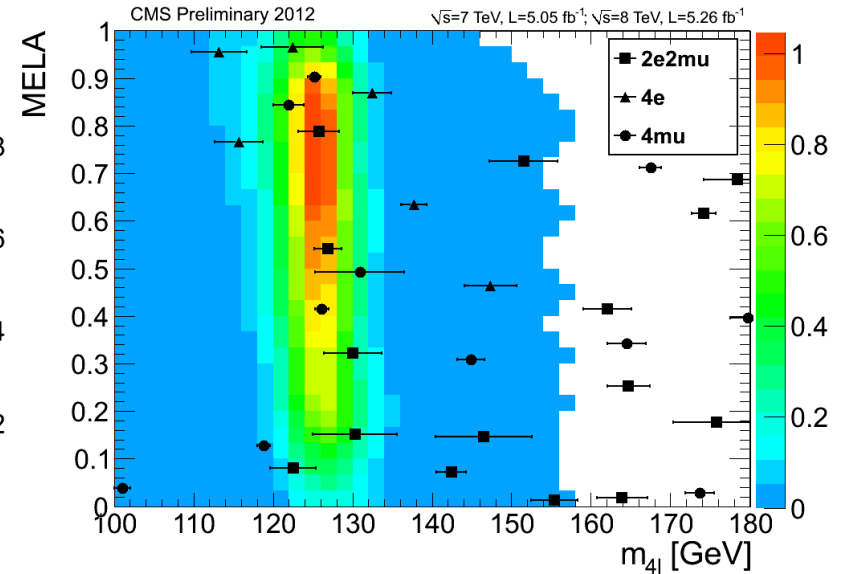
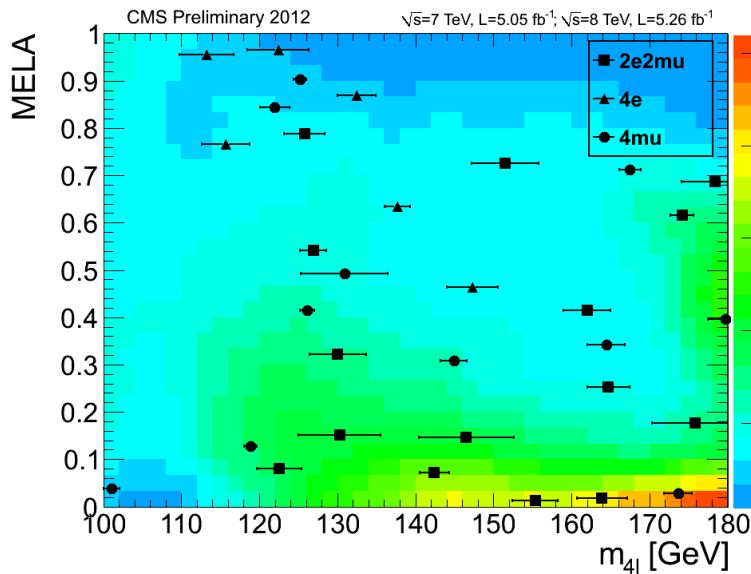
□ Toy analysis with MC applying CMS-like resolution and acceptance effects:

increase in significance 15%-30%
from low to high Higgs mass



Example from CMS: $H \rightarrow ZZ \rightarrow 4\text{lep}$ angular analysis

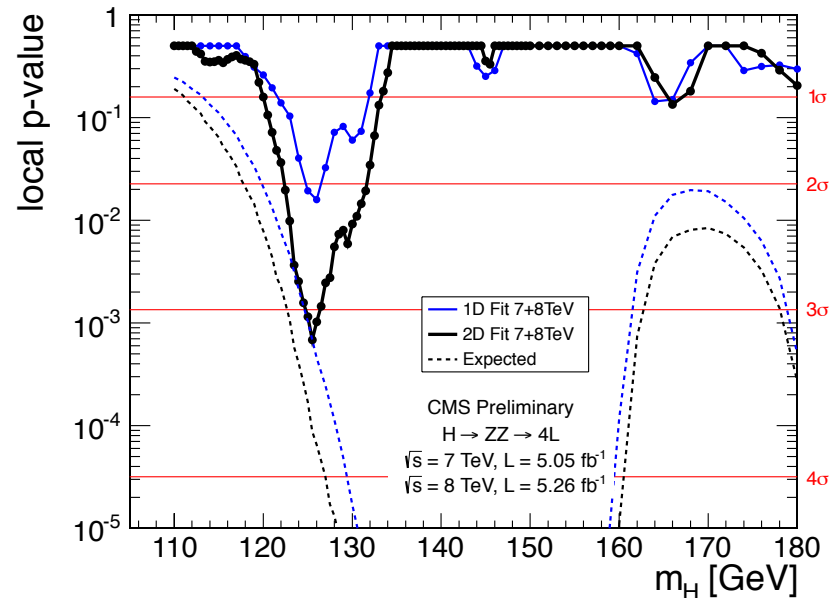
□ Signal extraction from 2D fit: $m(4l)$ vs MELA



□ Significance with 10 fb^{-1}

	1D	2D
expected	3.2	3.8
observed	2.2	3.2

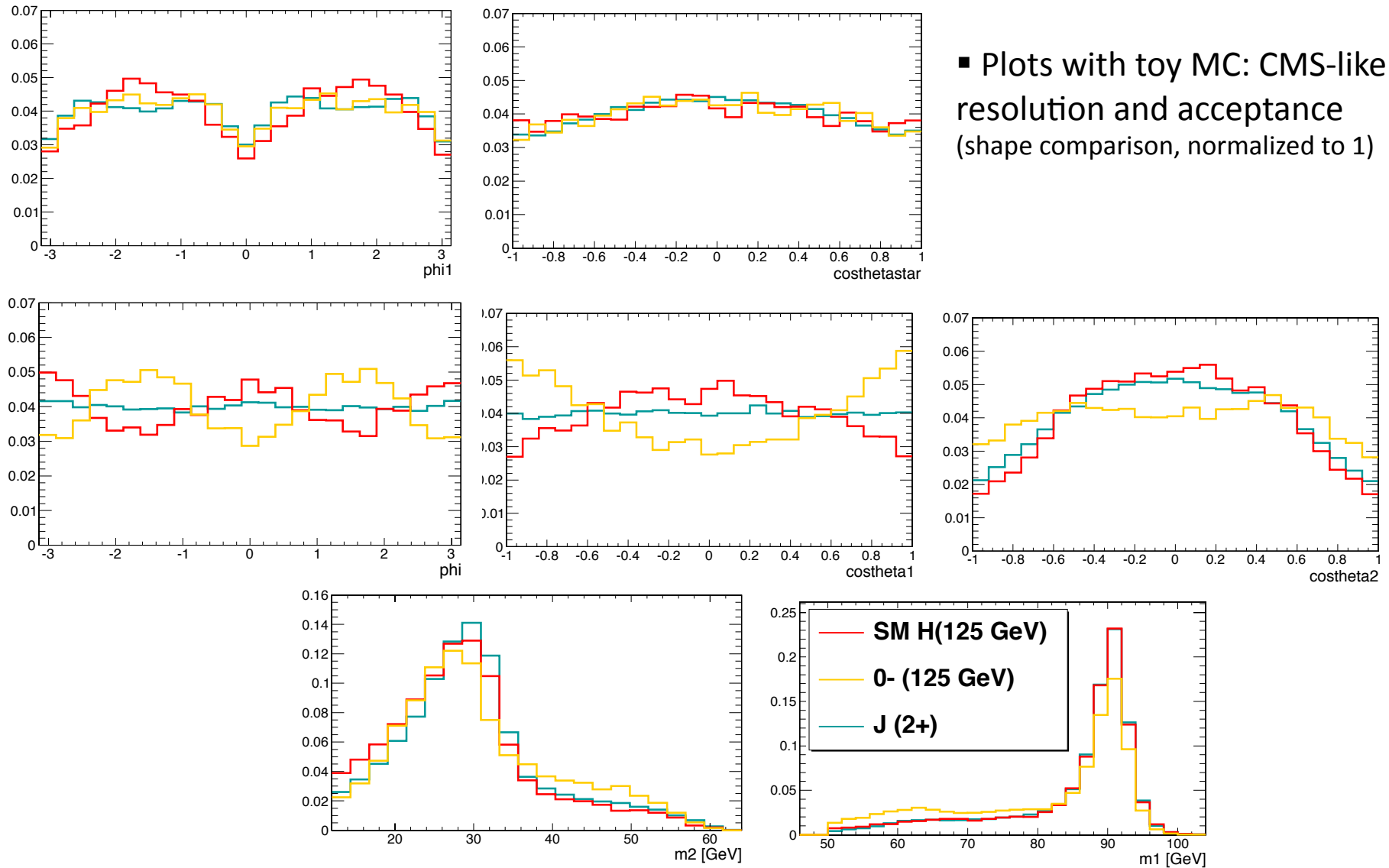
see: M.Klute talk, CMS HIG-12-016



Analysis for $X \rightarrow ZZ$ spin / parity measurement

Different spin/parity for $X \rightarrow ZZ$ (m_X 125 GeV)

■ Plots with toy MC: CMS-like resolution and acceptance (shape comparison, normalized to 1)

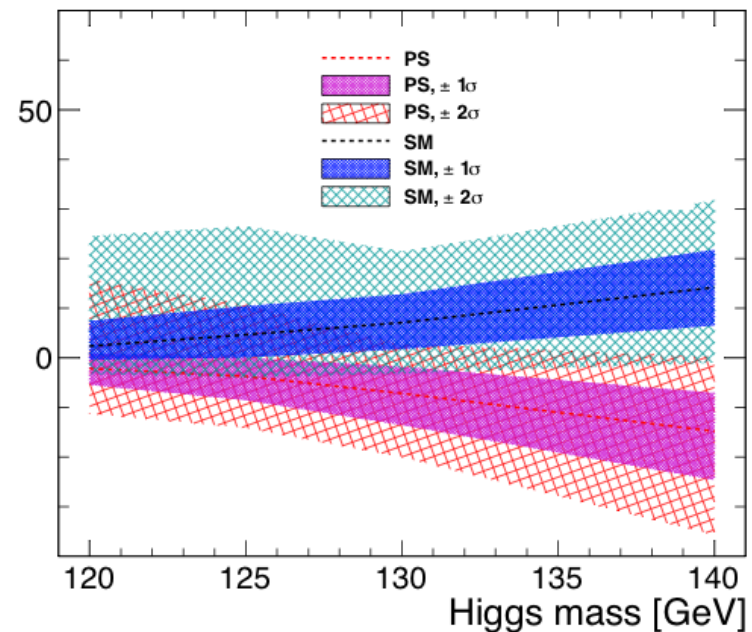
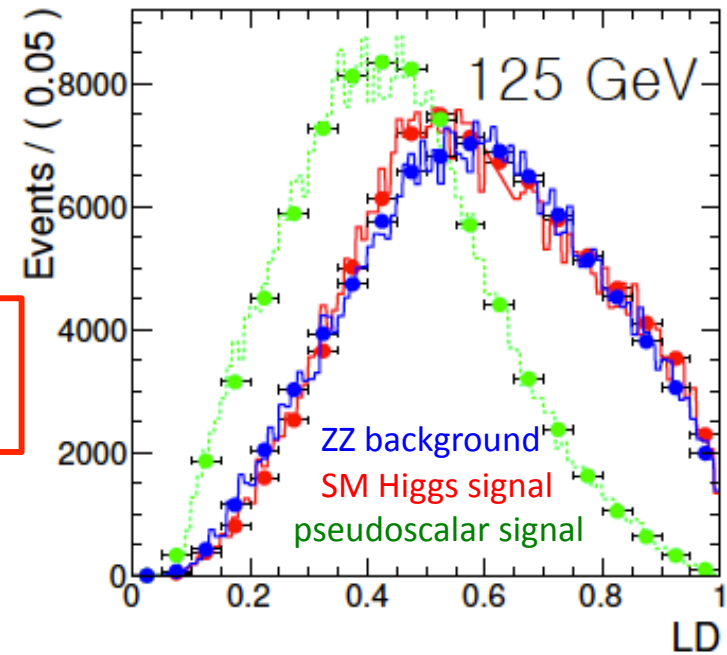
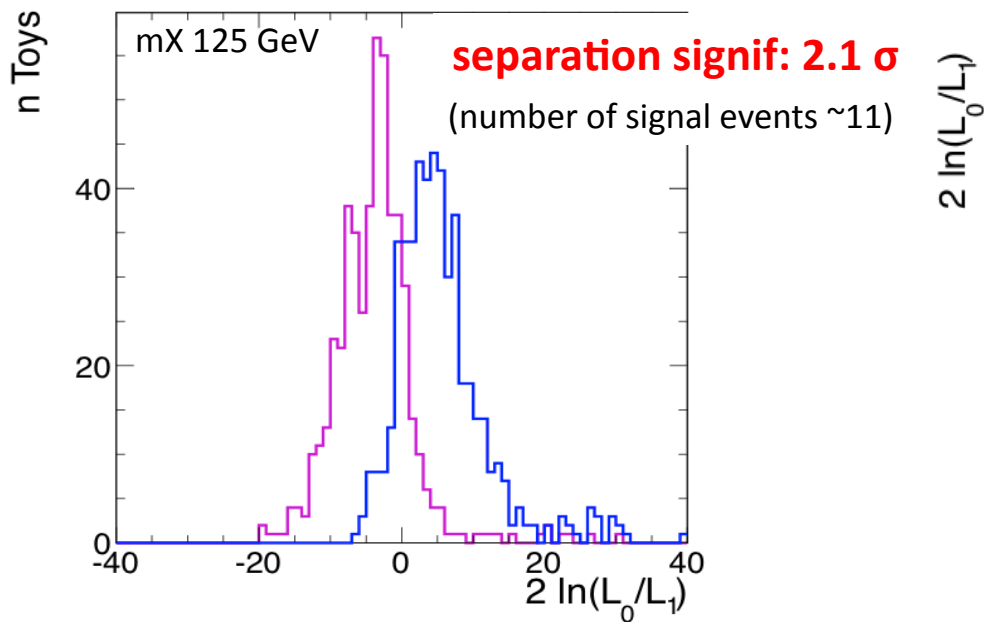


PseudoMELA: scalar vs pseudoscalar

□ Similar approach
for spin-hypothesis
separation

$$\text{pseudoMELA} = \frac{P_{0+}}{P_{0+} + P_{0-}}$$

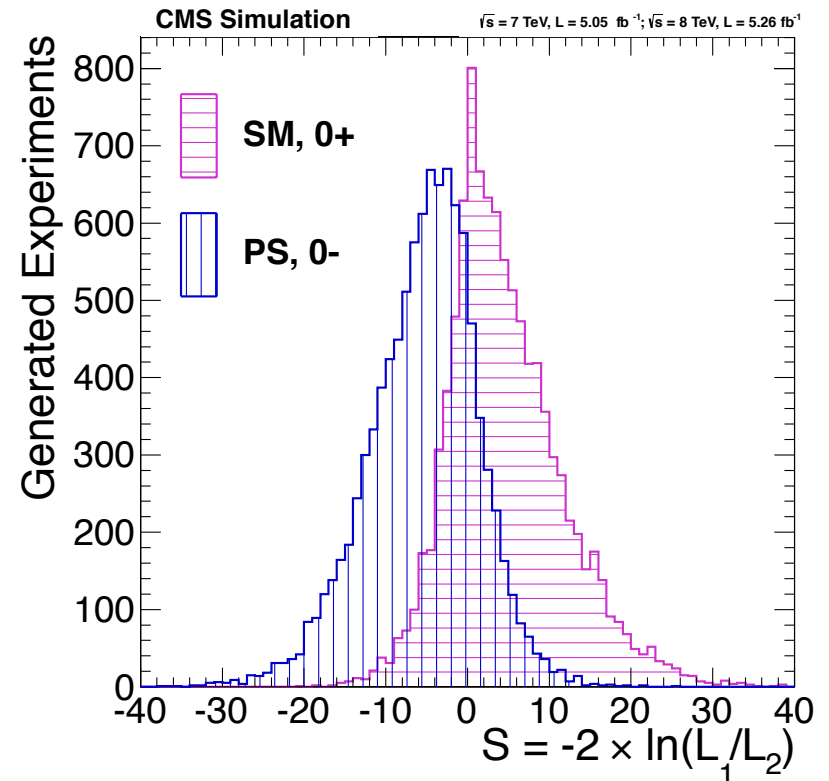
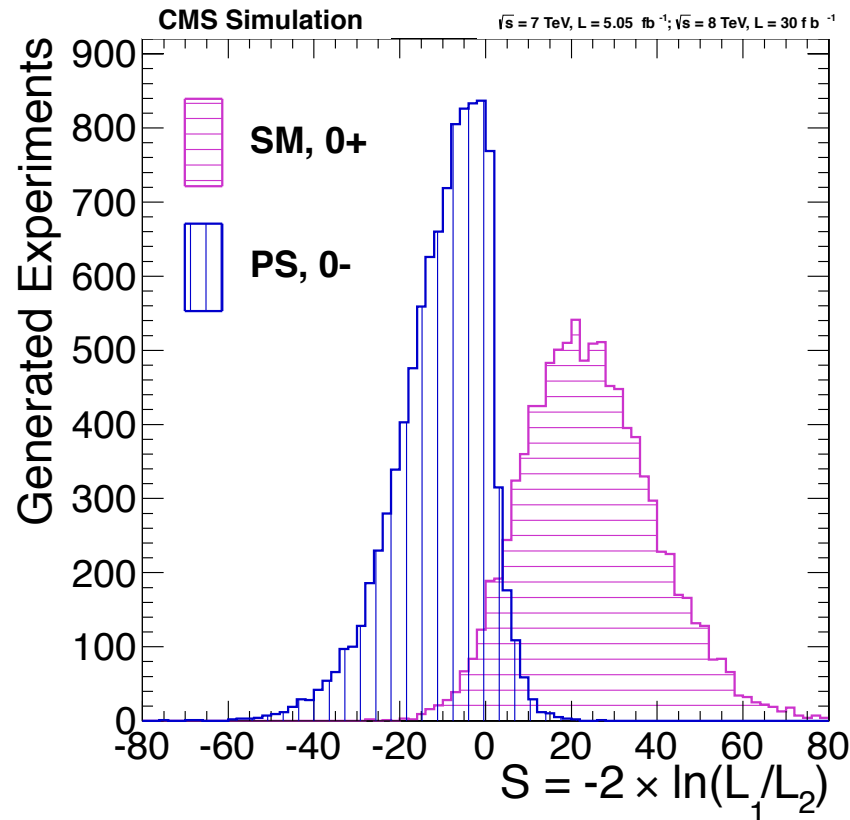
Toy results: hypothesis separation with 20 fb^{-1}
(assume same signal strength as SM)



Example from CMS

□ Full CMS simulation, with complete H→ZZ analysis (as published)

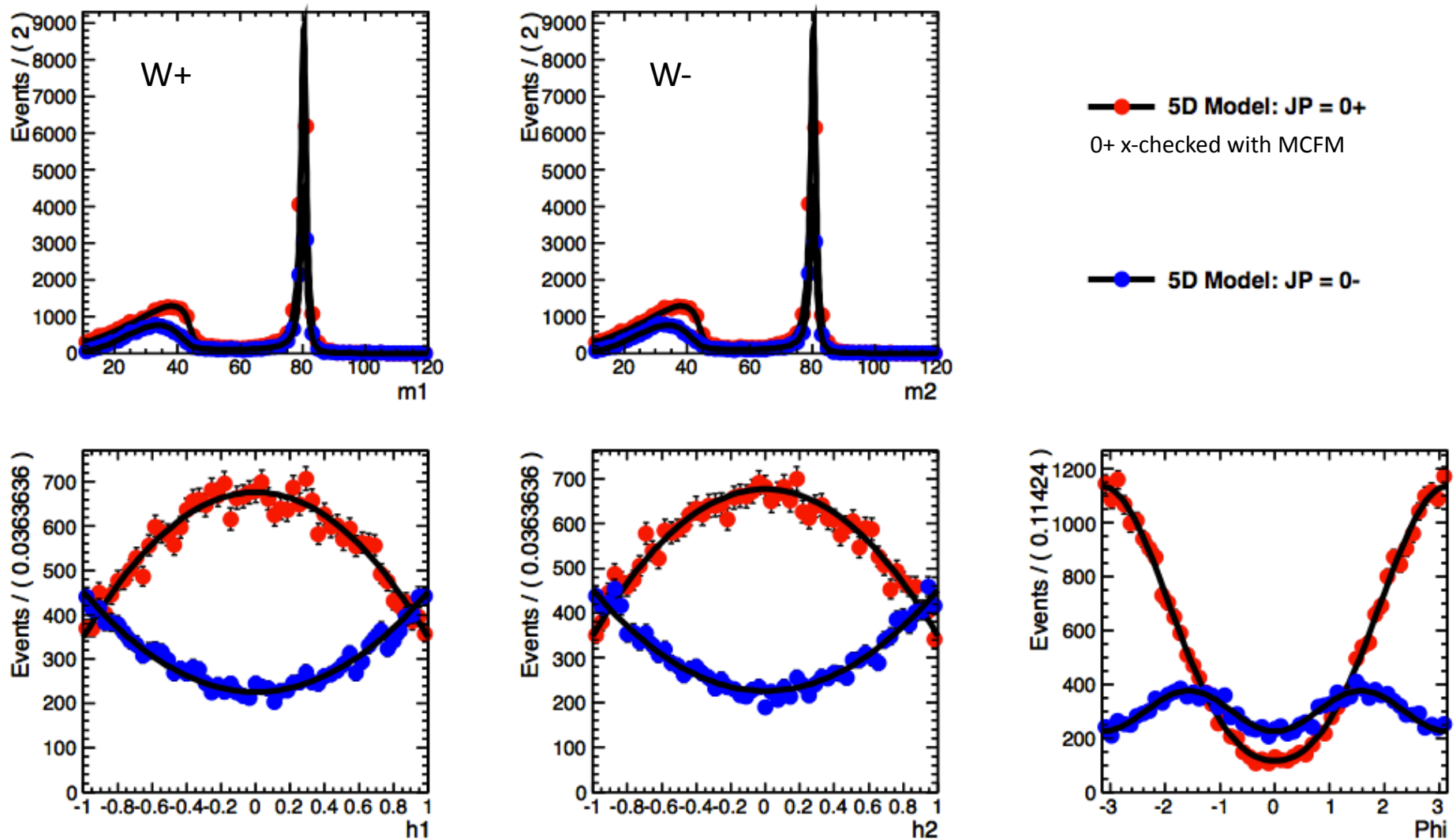
- status: **1.6 σ** expected separation with 5+5 fb⁻¹
- prospects: **3 σ** separation before shutdown



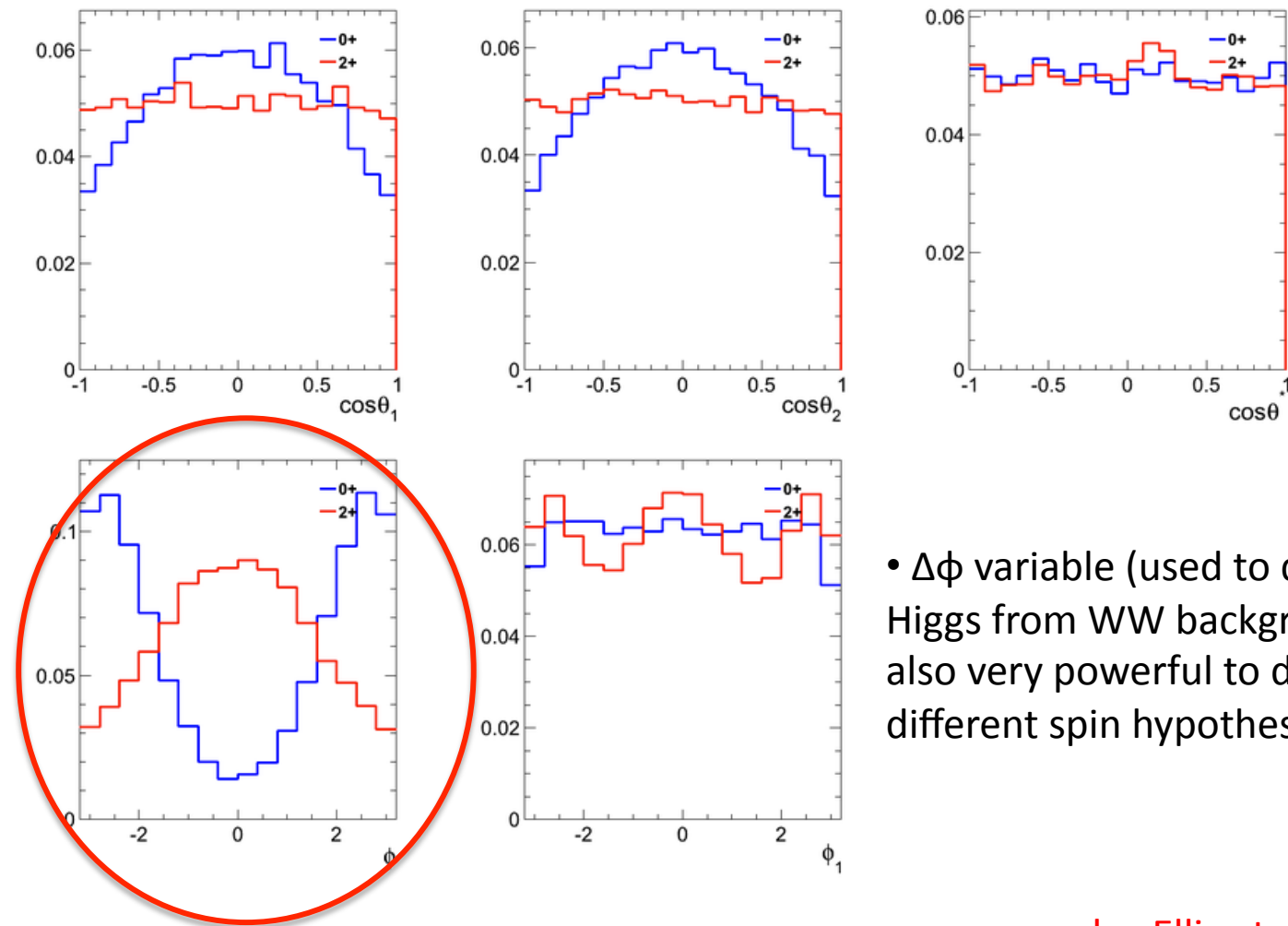
Integ. Lumi. 7 (8) TeV	Expected Separation
5/fb (5/fb)	1.6 σ
5/fb (20/fb)	2.6 σ
5/fb (30/fb)	3.1 σ

Spin/parity analysis in $X \rightarrow WW$ channel

0^+ vs 0^- in WW channel (125 GeV)



0+ vs 2+m in WW channel (125 GeV)



- $\Delta\phi$ variable (used to discriminate Higgs from WW background)
also very powerful to discriminate different spin hypothesis

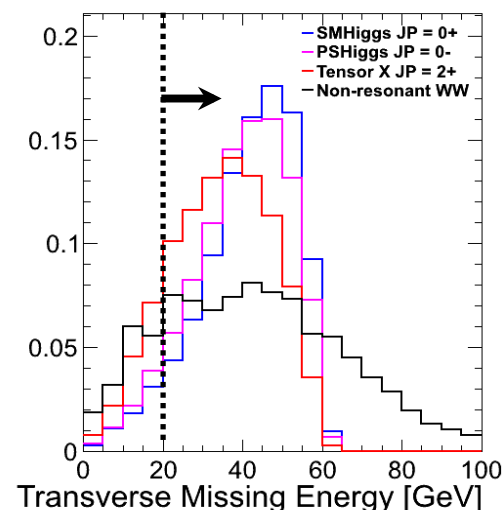
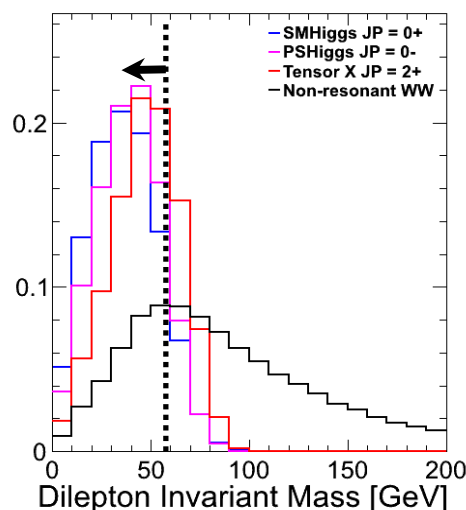
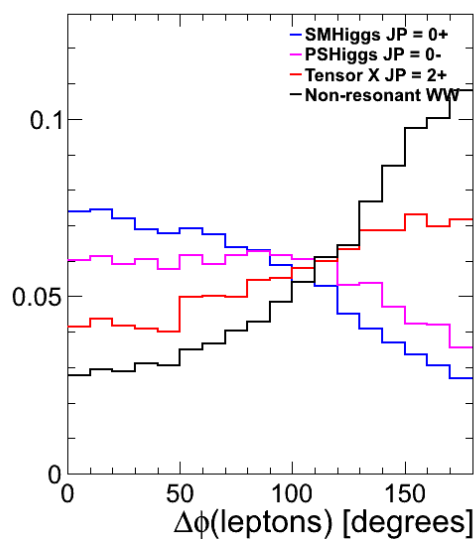
see also Ellis et al. [arXiv:1202.6660](https://arxiv.org/abs/1202.6660)

2D fit: $\Delta\phi$, $m(\ell\ell)$ or m_T

❑ **Toy studies:** only partial info available (kinematic not fully reconstructable)

CMS-like acceptance cuts, only 0-jets opposite-flavor channel

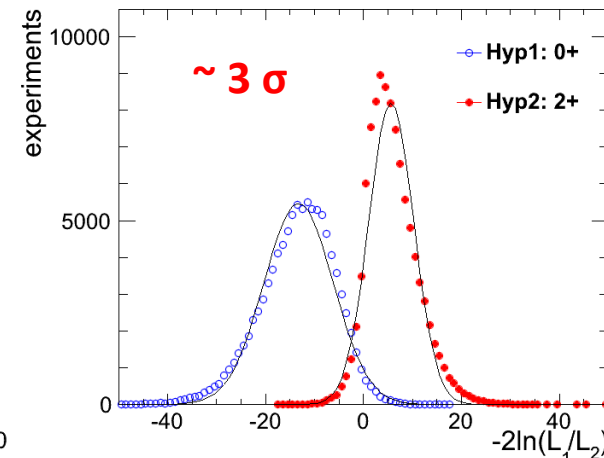
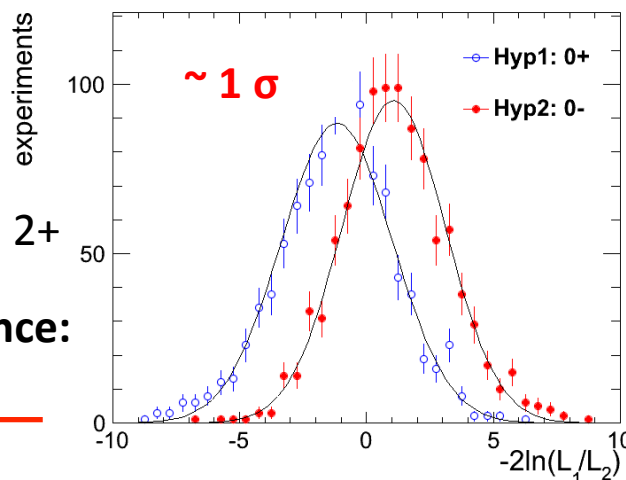
loose cuts to avoid sculpting distribution $\rightarrow$ 25/250 signal/background events per fb^{-1}



$\rightarrow$ 2D fit:
 $m_{\ell\ell}$, m_T

❑ **10 fb^{-1} , NO SYSTEMATICS**
only WW background

- **Signal significance:**
 ~ 4.5 for spin 0, ~ 3 for spin 2+
- **Spin separation significance:**

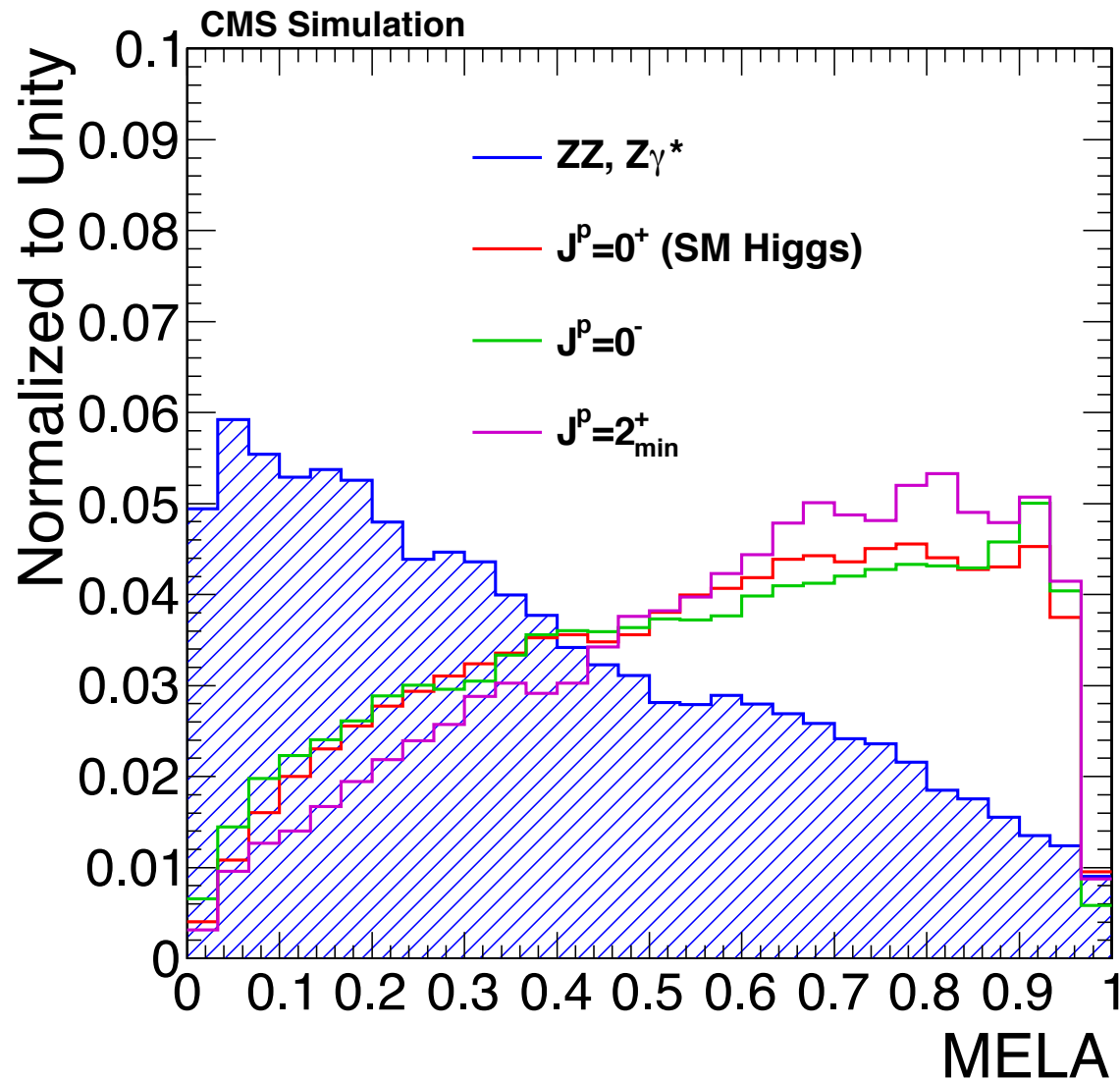


Conclusions and prospects

- ❑ JHU MC available for **any spin $VV \rightarrow X \rightarrow VV$**
- ❑ Angular analysis based with analytical likelihood (MELA) successfully used
 - **to boost signal search in $X \rightarrow ZZ$: $3\sigma \rightarrow 4\sigma$**
 - **to separate X spin hypothesis: 3σ separation $0+/0-$ before shutdown**
- ❑ **Combination of various channels (eg ZZ , WW):**
 - increase signal sensitivity
 - complementary information
- ❑ All models can be tested, **starting from most general couplings**

BACKUP

MELA for S/B: model independent



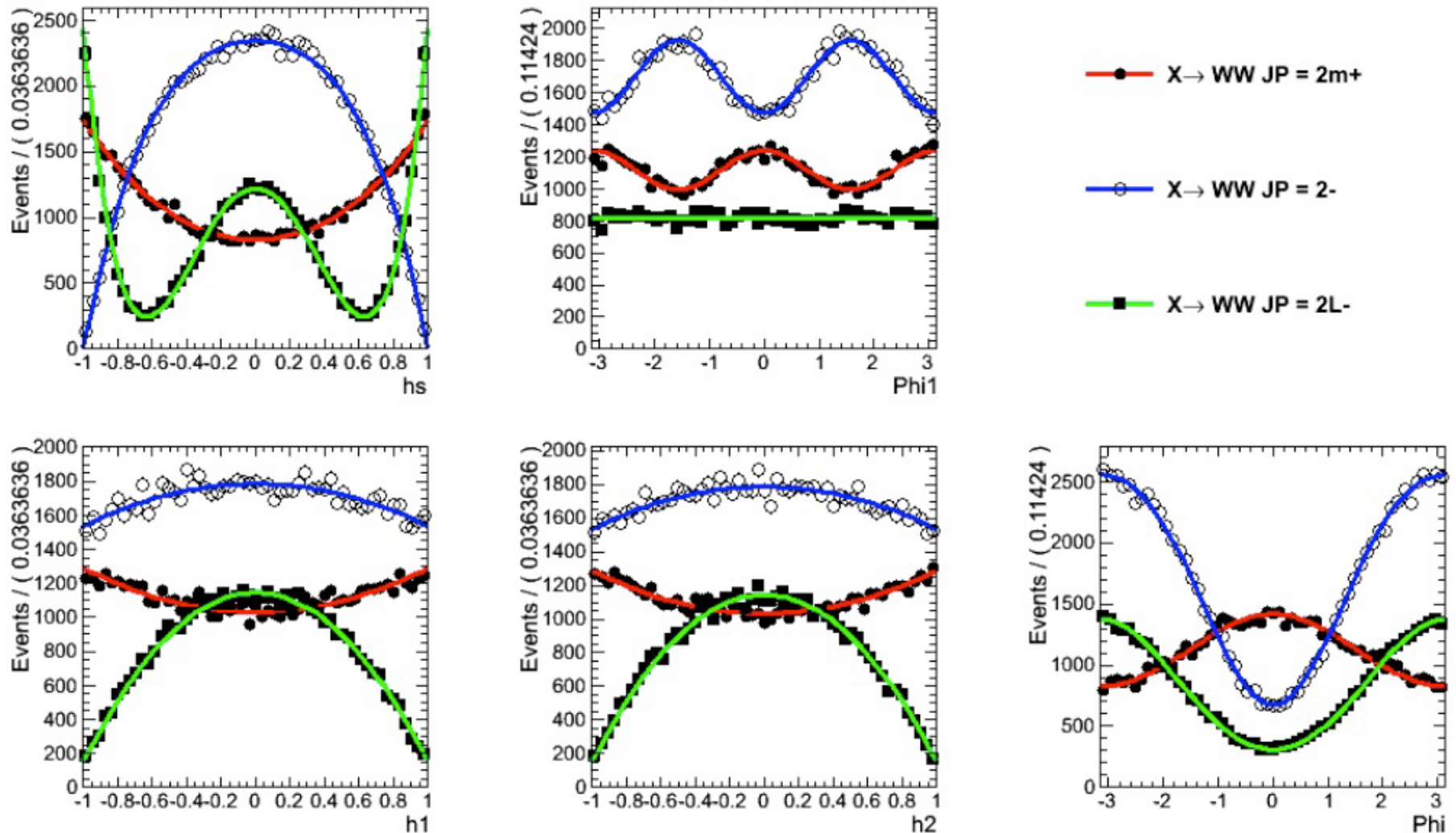
Scenarios studied in **arXiv:1001.3396**

TABLE I: The list of scenarios chosen for the analysis of the production and decay of an exotic X particle with quantum numbers J^P . For the two 2^+ cases, the superscripts m (minimal) and L (longitudinal) distinguish two scenarios, as discussed in the last column. When relevant, the relative fraction of gg and $q\bar{q}$ production is taken to be 1:0 at $m_X = 250$ GeV and 3:1 at $m_X = 1$ TeV. The spin-zero X production mechanism does not affect the angular distributions and therefore is not specified.

scenario (J^P)	$X \rightarrow ZZ$ decay parameters	X production parameters	comments
0^+	$a_1 \neq 0$ in Eq. (2)	$gg \rightarrow X$	SM Higgs-like scalar
0^-	$a_3 \neq 0$ in Eq. (2)	$gg \rightarrow X$	pseudo-scalar
1^+	$g_{12} \neq 0$ in Eq. (4)	$q\bar{q} \rightarrow X: \rho_{11}, \rho_{12} \neq 0$ in Eq. (9)	exotic pseudo-vector
1^-	$g_{11} \neq 0$ in Eq. (4)	$q\bar{q} \rightarrow X: \rho_{11}, \rho_{12} \neq 0$ in Eq. (9)	exotic vector
2_m^+	$g_1^{(2)} = g_5^{(2)} \neq 0$ in Eq. (5)	$gg \rightarrow X: g_1^{(2)} \neq 0$ in Eq. (5) $q\bar{q} \rightarrow X: \rho_{21} \neq 0$ in Eq. (10)	Graviton-like tensor with minimal couplings
2_L^+	$c_2 \neq 0$ in Eq. (6)	$gg \rightarrow X: g_2^{(2)} = g_3^{(2)} \neq 0$ in Eq. (5) $q\bar{q} \rightarrow X: \rho_{21}, \rho_{22} \neq 0$ in Eq. (10)	Graviton-like tensor longitudinally polarized and with $J_z = 0$ contribution
2^-	$g_8^{(2)} = g_9^{(2)} \neq 0$ in Eq. (5)	$gg \rightarrow X: g_1^{(2)} \neq 0$ in Eq. (5) $q\bar{q} \rightarrow X: \rho_{21}, \rho_{22} \neq 0$ in Eq. (10)	“pseudo-tensor”

WW: JHU generator validation (J=2)

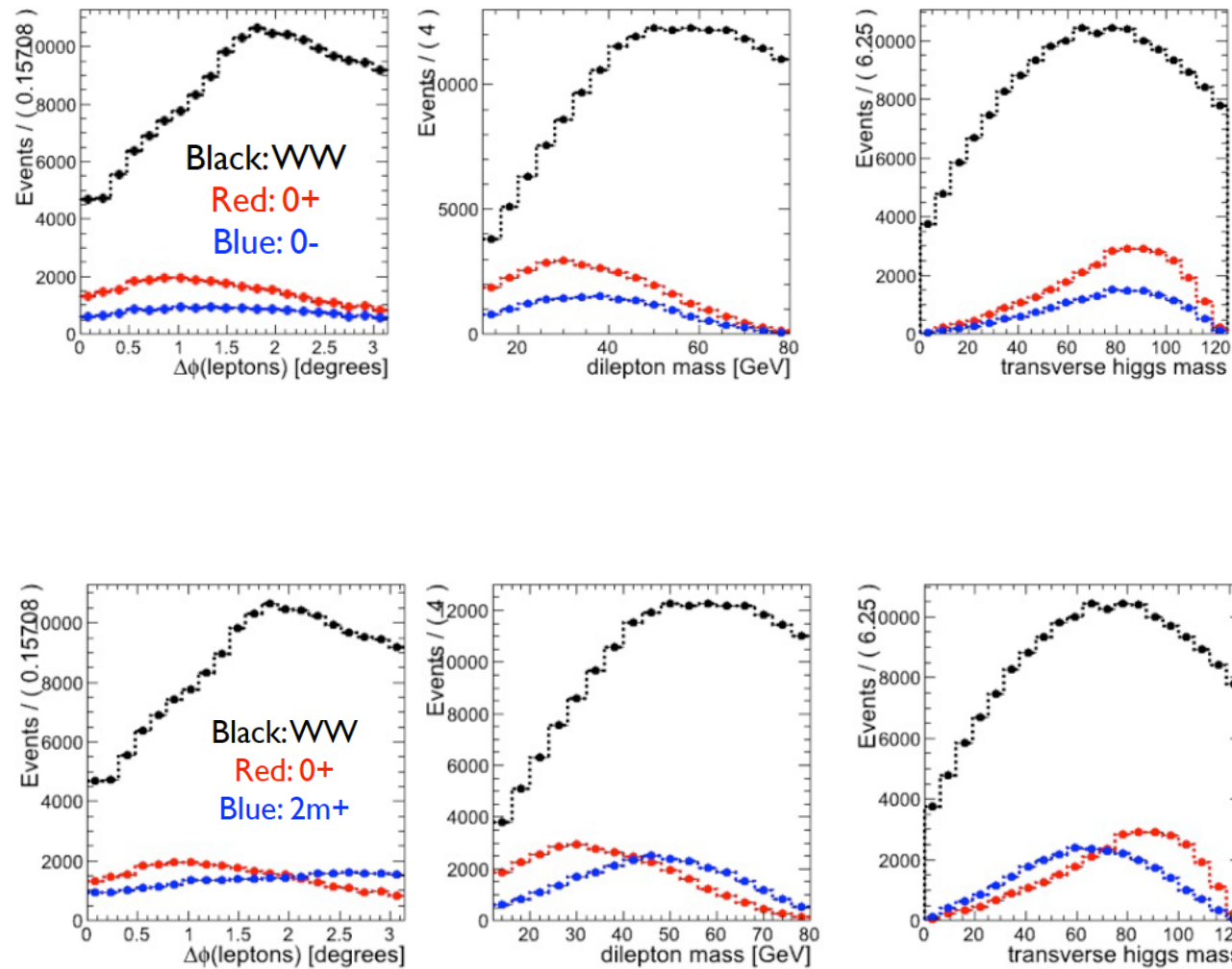
MX = 250 GeV (MC validation)



WW

- Define a minimal selections for the hypothesis separations
 - Lepton acceptance (20, 10) selections
 - dilepton mass range [12-80] GeV
 - transverse higgs mass [0 - 125] GeV
- With this selection the number of events per luminosity at 8 TeV
 - Signal: 25
 - Background: 250

Hypothesis separation in WW



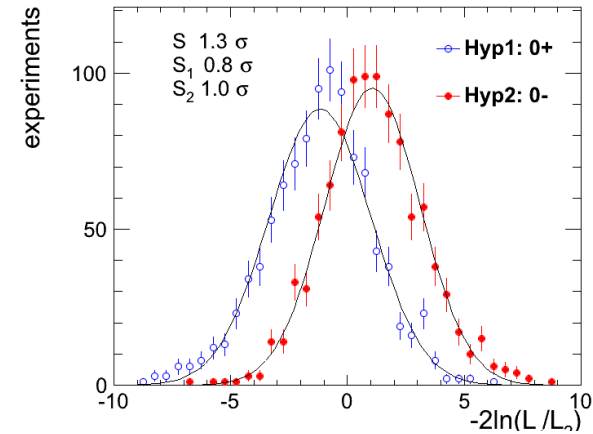
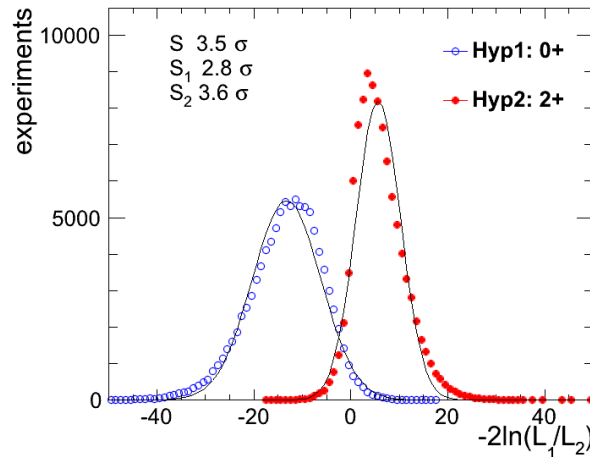
Hypothesis separation in WW

signal
significance

	2D (mll/ MT)	2D ($\Delta\Phi$ / MT)
0+	4.6 ± 1.0	3.2 ± 1.0
0-	4.4 ± 1.0	2.8 ± 1.0

	2D (mll/MT)	2D ($\Delta\Phi$ / MT)
0+	4.6 ± 1.0	3.0 ± 1.0
2+	3.0 ± 1.1	2.5 ± 1.0

2D: mll/MT



2D: $\Delta\Phi$ /MT

