

The background of the slide features four distinct cosmological images: a Mollweide projection of the Cosmic Microwave Background (CMB) in the top left; a deep-field view of distant galaxies in the top right; a 3D visualization of dark matter filaments in the middle left; and a field of galaxies in the bottom right.

A taste of cosmology

Licia Verde

<http://icc.ub.edu/~liciaverde>



Institut de Ciències
del Cosmos



OUTLINE

- The standard cosmological model
- The successes of cosmology over the past 10 years
- Cosmic Microwave Background
- Large-scale structure
- Inflation and outlook for the future

Lectures and additional material will appear at
<http://icc.ub.edu/~liciaverde/CLASHEP.html>

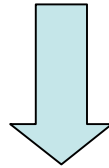
Outline 2



Last Judgment, Vasari, Florence Duomo

Successes of the Big Bang model

GR+cosmological principle



Hubble's law

CMB

Abundance of light elements

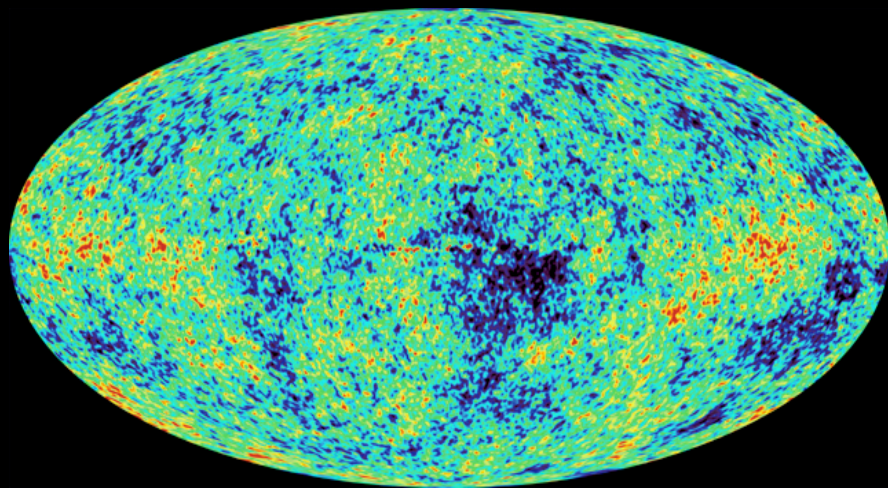
.. And problems

Flatness problem

Horizon problem

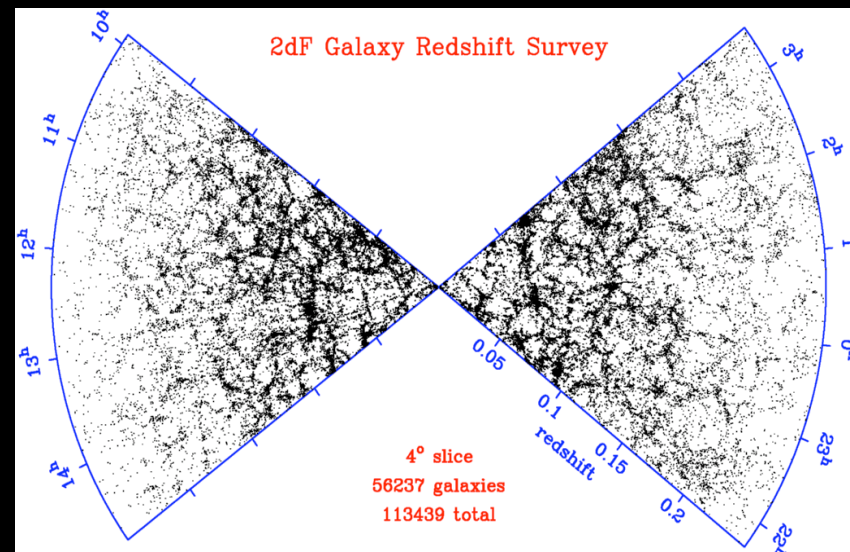
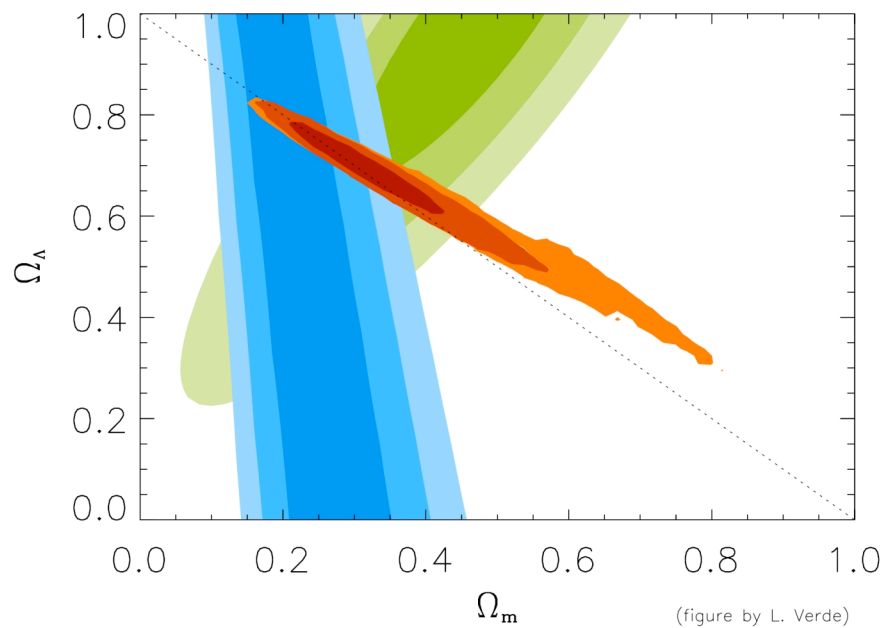
Monopole problem

Origin of perturbations



Horizon problem

Flatness problem



Structure Problem

Very quickly you find that early on $|1-\Omega| < 10^{-60}$

It is like balancing a pencil
on its tip, coming back
years later and still finding
it balancing on its tip



The Horizon problem

Different type of Horizons in Cosmology

Since light travels at a final speed & Universe is expanding

PARTICLE HORIZON: Maximum comoving distance light can have propagated in t_i to t_f

$$d_p(t) = \int_{t_i}^{t_f} \frac{dt}{a(t)}$$

Accounts for all the past expansion history

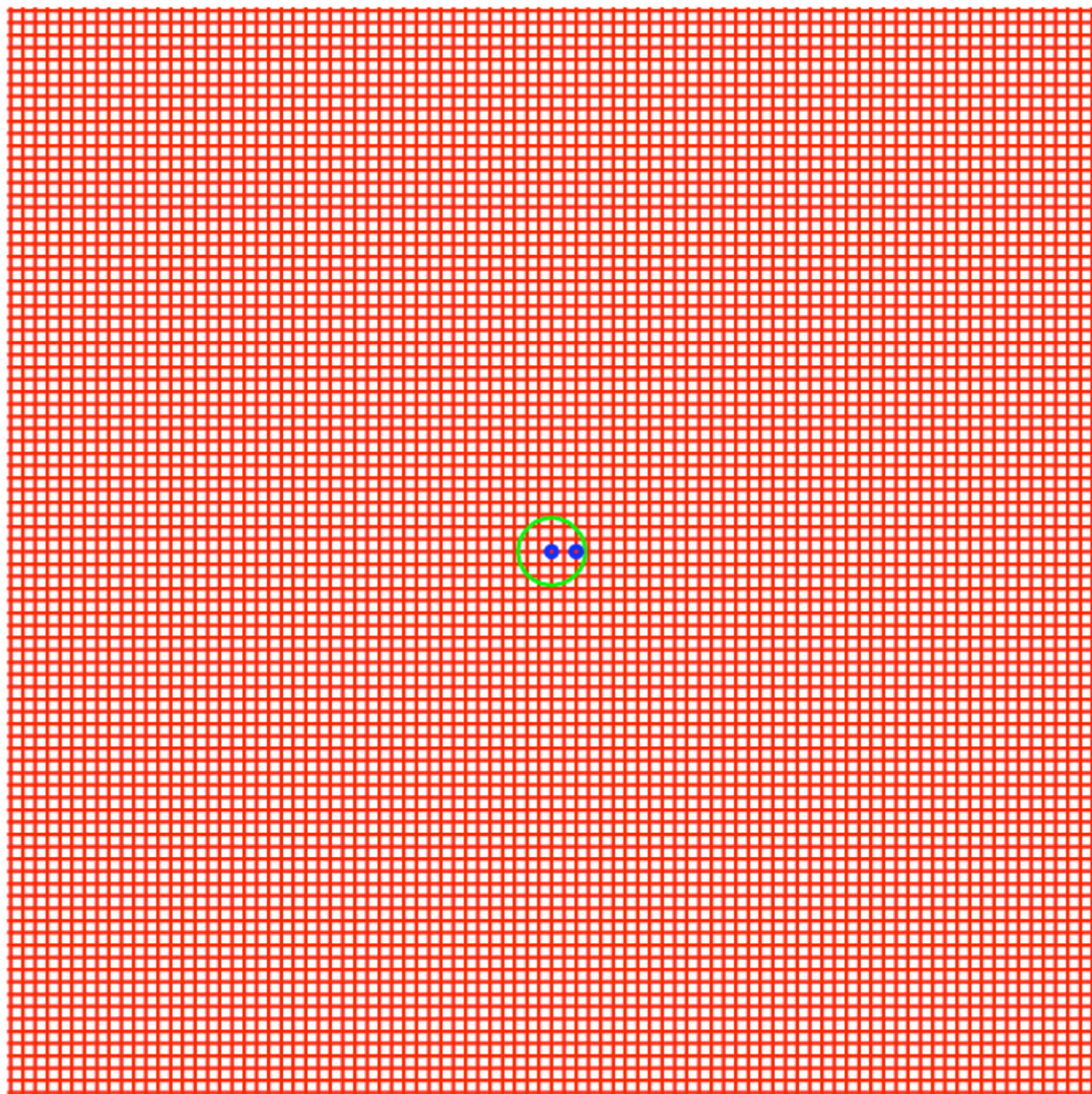
Given the same dt , dp can be very different if $a(t)$ is weird!

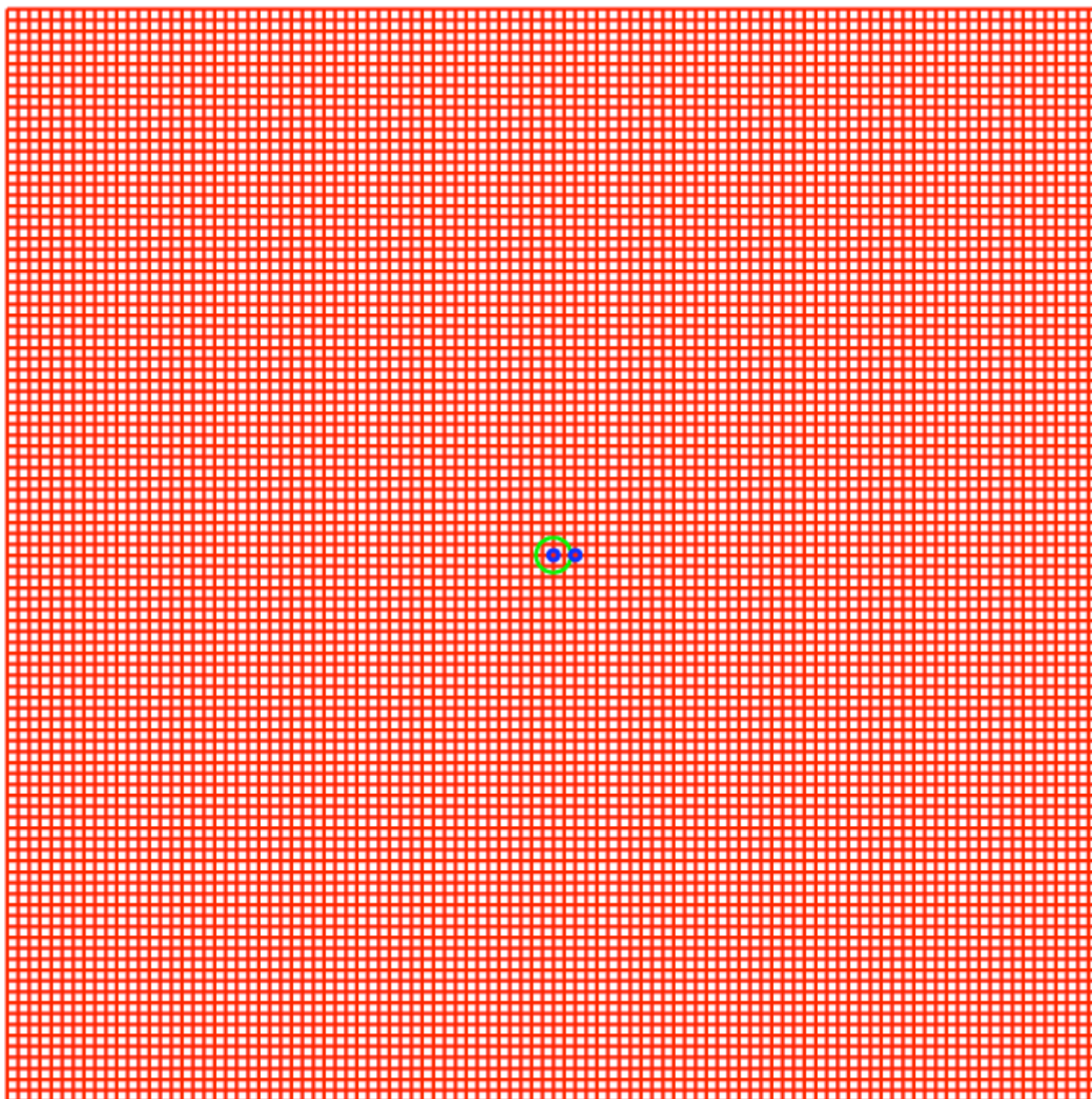
HUBBLE HORIZON: c/H or c/t_0 .

For normal expansion histories $dp \sim c/H$

For weird ones BEWARE!

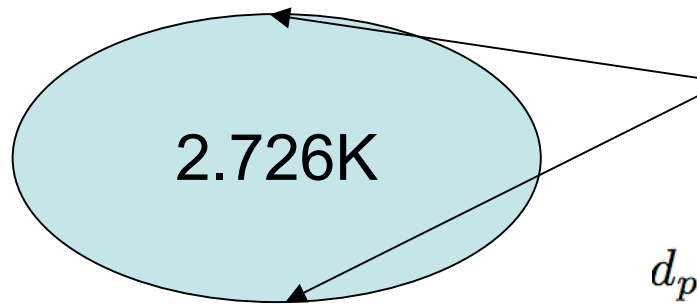
$$\frac{c}{H}$$





The Horizon problem

The universe is homogeneous and isotropic on large scales



Consider 2 antipodal points they are separated by $2d_H \sim 30000 \text{ Mpc}$

$$d_p(t_0) = c \int_{t_{cmb}}^{t_0} \frac{dt}{a(t)} \sim d_H(t_0); \quad t_{cmb} \ll t_0$$

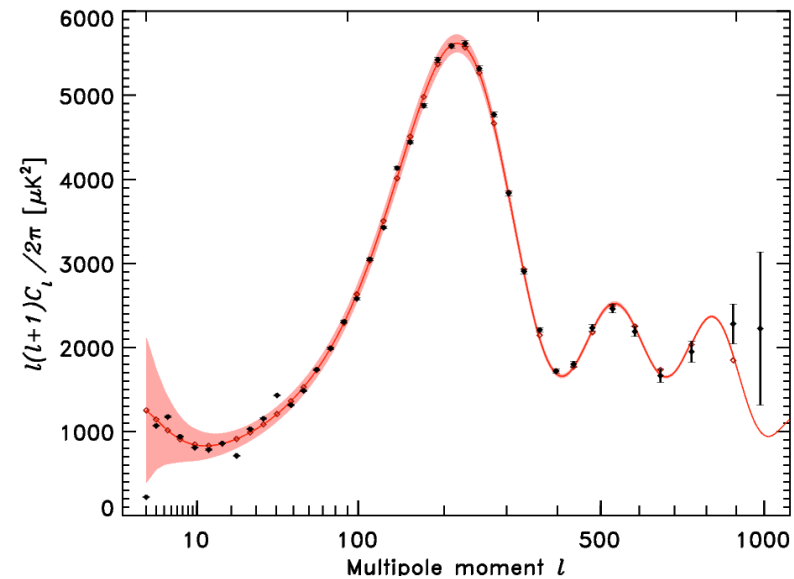
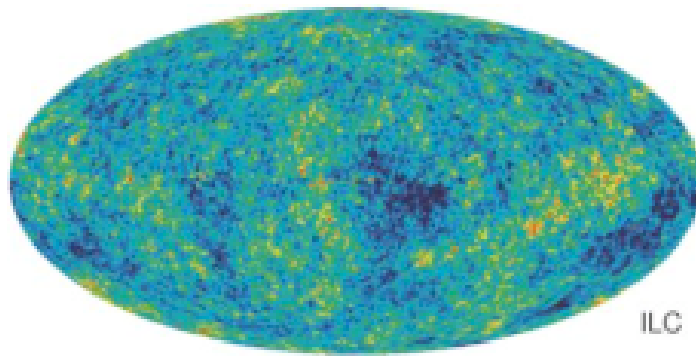
What was the Hubble radius (horizon) back then?

$$H(z)^2 \sim H_0^2 \Omega_{m,0} (1+z)^3 \longrightarrow \frac{c}{H_{z=1000}} \simeq 0.2 \text{ Mpc}$$

Only points at $\sim 0.2 \text{ Mpc}$ could have “talked”

Small aside

$$\theta_H(z_{CMB}) = \frac{d_H}{d_A} = \frac{d_H}{d_p/(1+z)} \sim 1^\circ \quad c_s \sim c$$



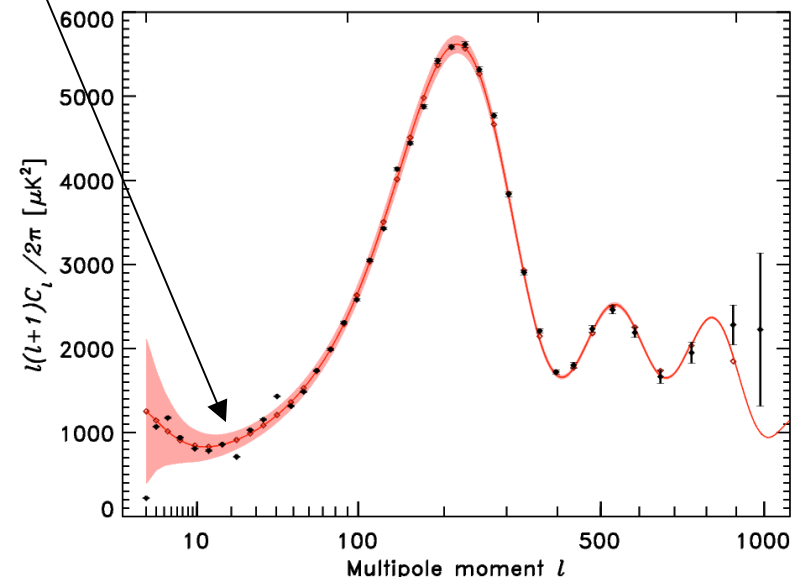
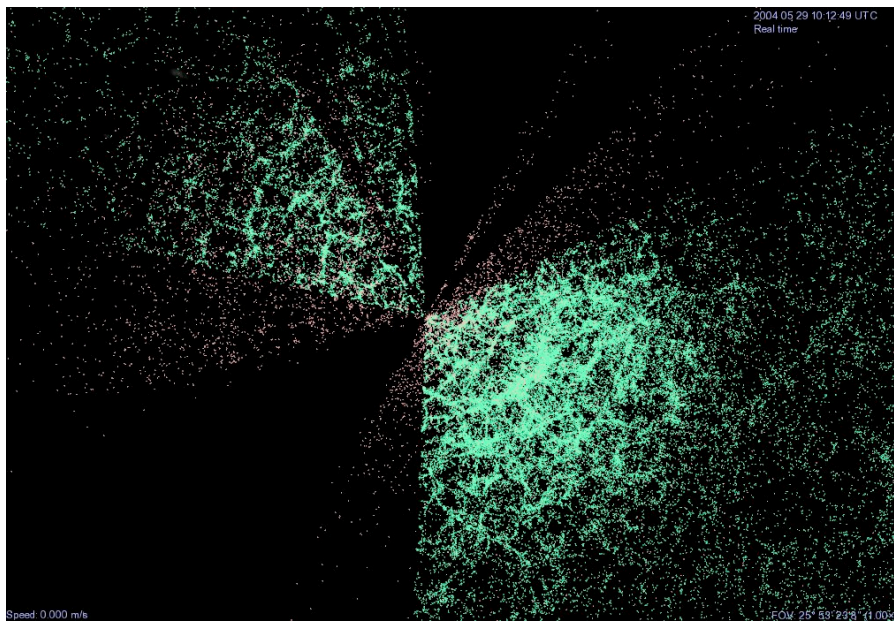
Compare with the size of the CMB spots!

The last scattering surface can be divided in 40000 patches of degree size I.e. 40000 “horizons”....

How could they all be at 2.726K?

Imagine 40000 students taking an exam, and all returning THE SAME exam down to the commas...

And where the heck these perturbations come from?

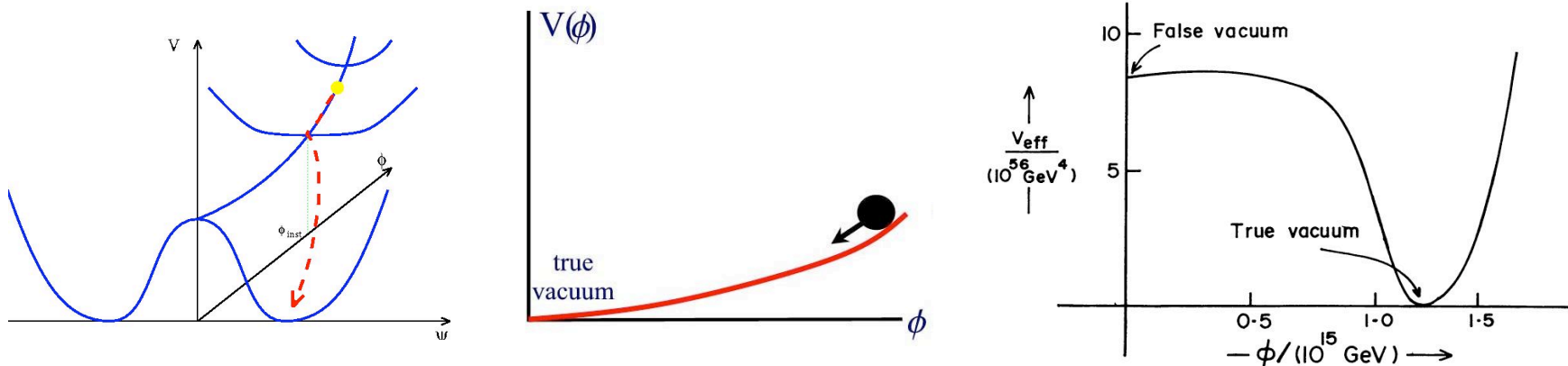


INFLATION to the rescue

Started in the 1980 with A. Guth, active research area.
Still a “paradigm” not a proven fact...

Postulate a period of accelerated expansion
at the very beginning!
Something like a cosmological constant

Different scenarios, particle-physics motivated (?)



Any weirdness like monopole

Would be diluted away!

Inflation solves the Flatness problem

Something like a Λ

$$H = \text{const}; \quad a \sim \exp(H_I t)$$

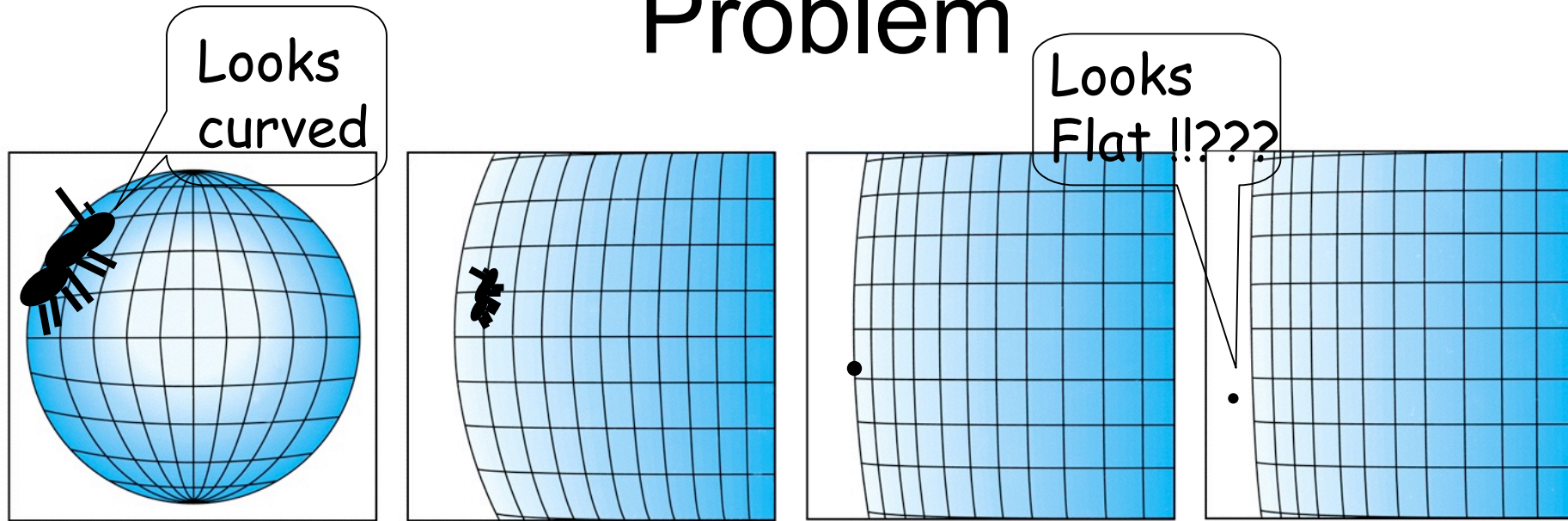
$$1 - \Omega(t) = \frac{c^2}{R_0^2 a^2 H^2}$$

$$\frac{a(t_f)}{a(t_i)} = e^N \quad N = H_i(t_f - t_i) \quad \text{number of e-foldings}$$

$$|1 - \Omega(t_f)| = \exp(-2N) |1 - \Omega(t_i)|$$

For $N \sim 100$ NOT BAD!

Inflation Solves the Flatness Problem



What made the Universe so flat?



What made the Universe so big?

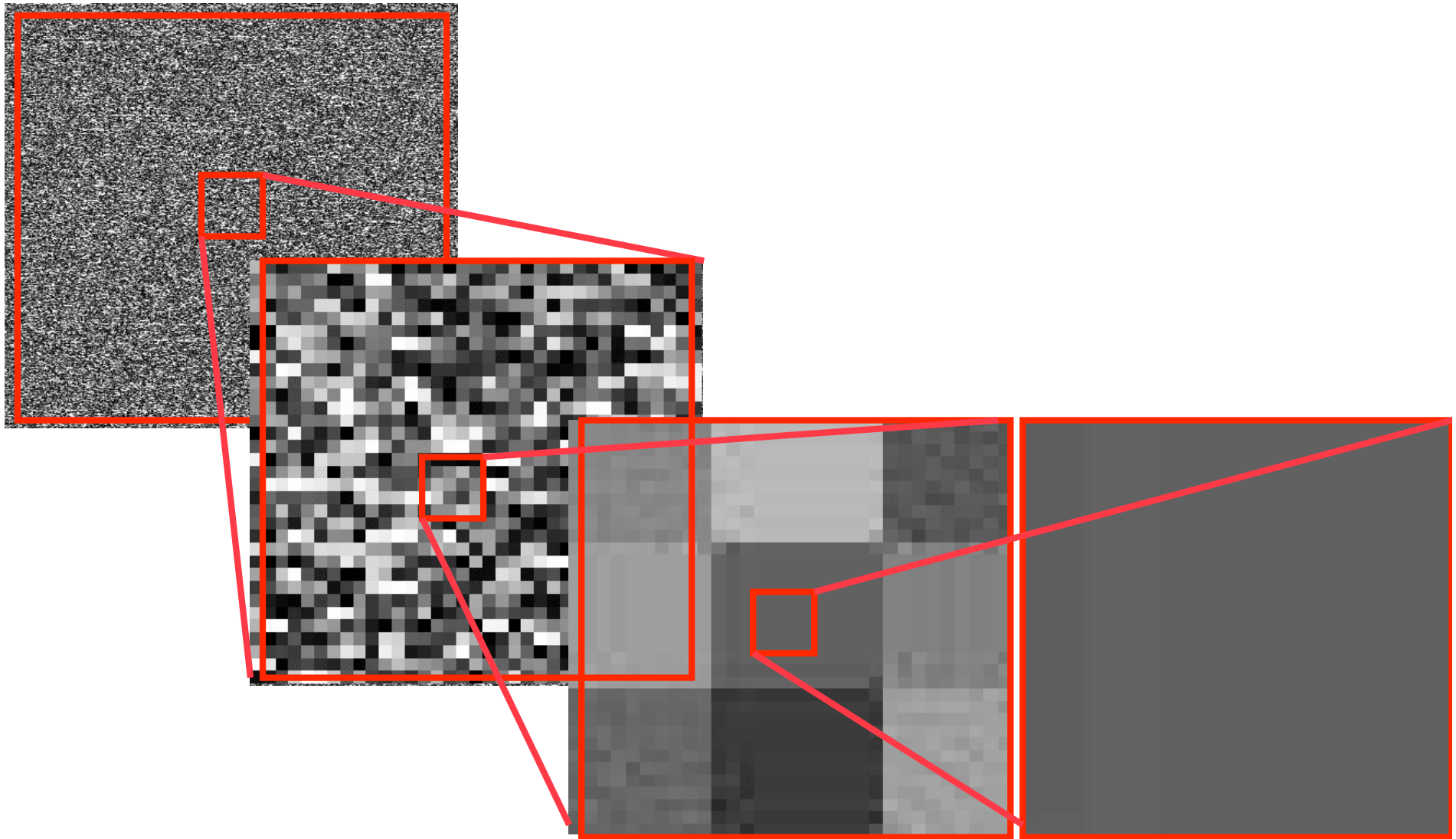


What made the universe so uniform?

What seeded the galaxies?

Why is the Universe so uniform?

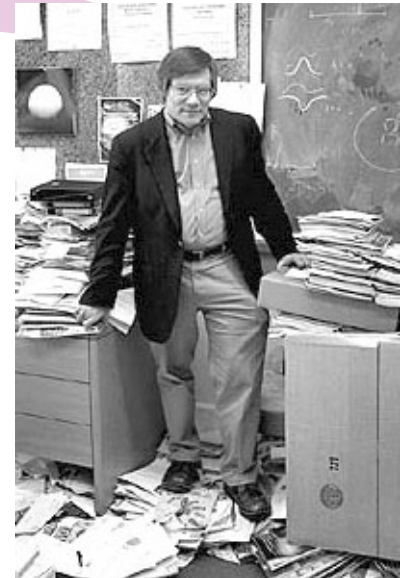
Inflation solves that



Inflation solves the Horizon problem

In an accelerated expansion the particle horizon and the Hubble horizon can be VERY DIFFERENT

Given the same dt , dp can be very different if $a(t)$ is weird!



As an added bonus:

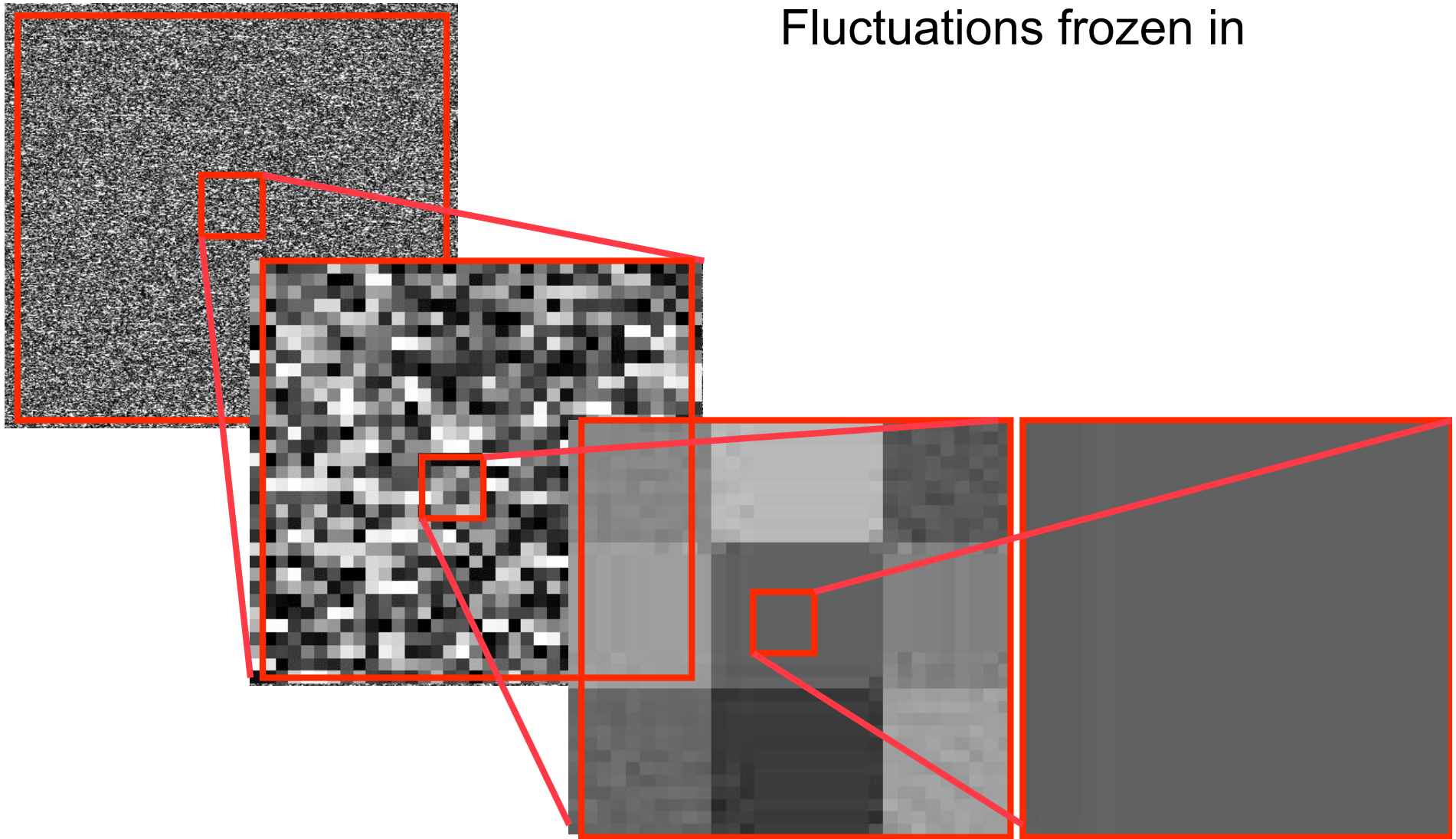
Inflation generates Gaussian perturbations: quantum fluctuations stretched to become classical by the expansion. The mechanism is similar to Hawking's radiation. (The event horizon being the complementary concept to the particle horizon...)

Turns out that the power spectrum of these perturbations will be a power law: different models of inflation predict slightly different power laws, but all close to “scale invariant”..

Perturbations outside the Horizon?

Inflation solves that

Fluctuations frozen in



CAN THIS BE TESTED?

flatness



Power law primordial power spectrum

Can even hope to distinguish specific models



Super horizon fluctuations (polarization)



Coming next

gaussianity



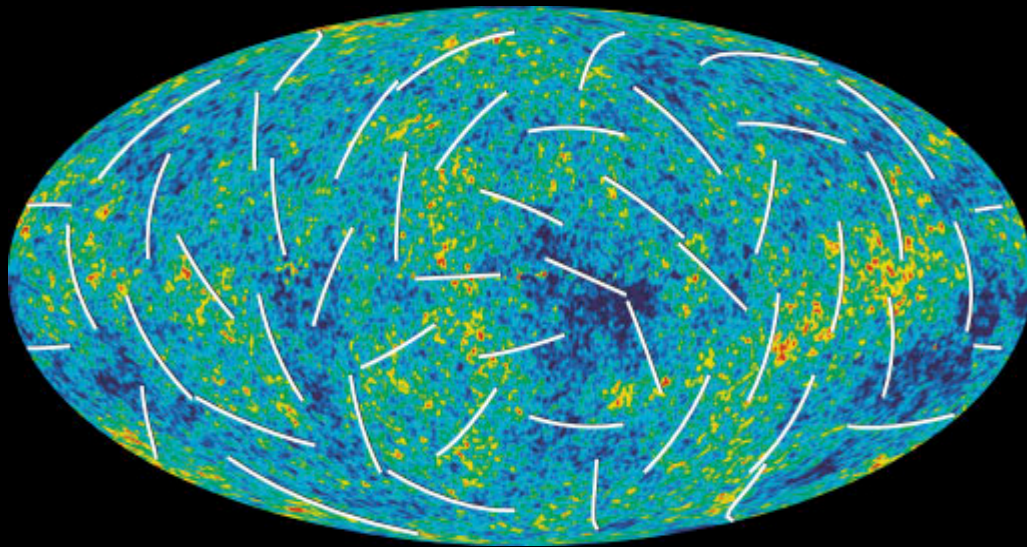
Can even hope to distinguish specific models

Stochastic background of gravity waves
(polarization)



There's more!

Polarization

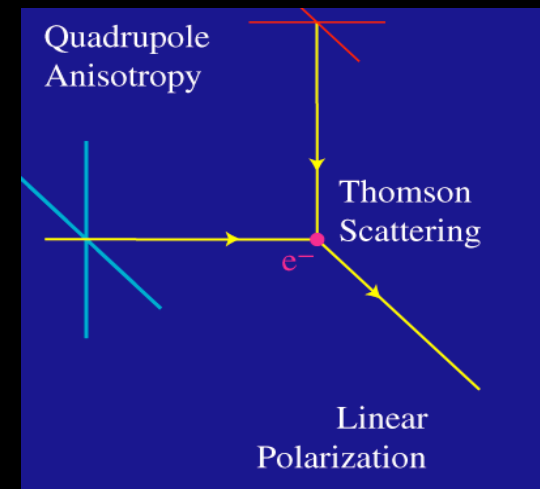
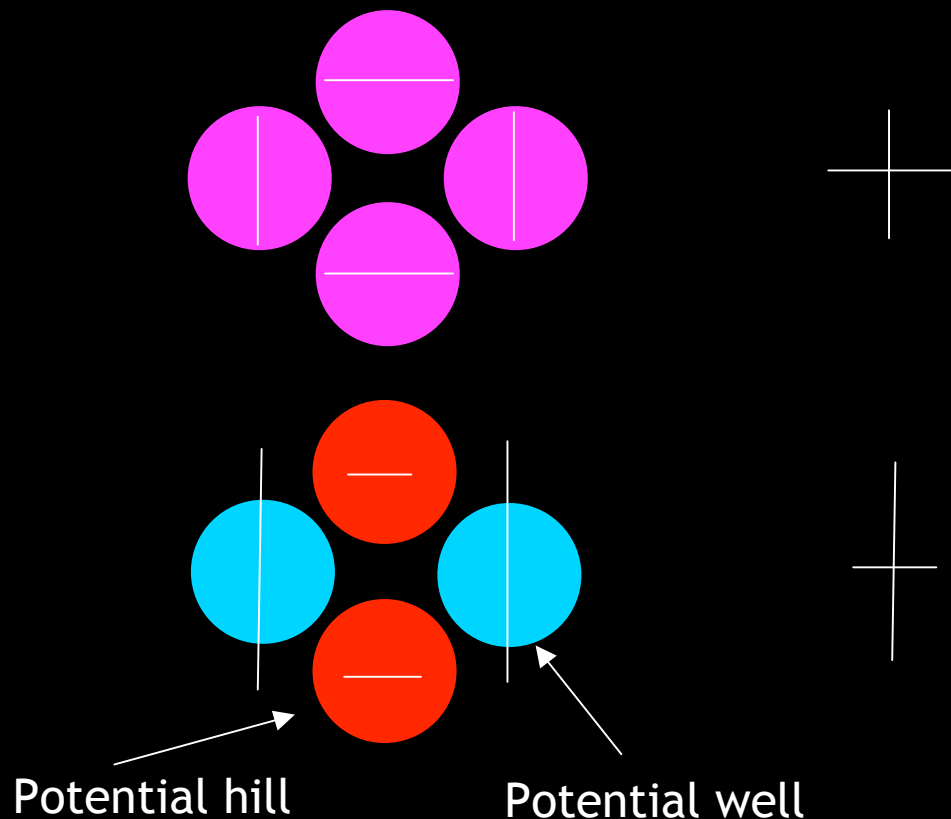


WMAP (2006)

First detected by DASI in 2002

Generation of CMB polarization

- Temperature quadrupole at the surface of last scatter generates polarization.



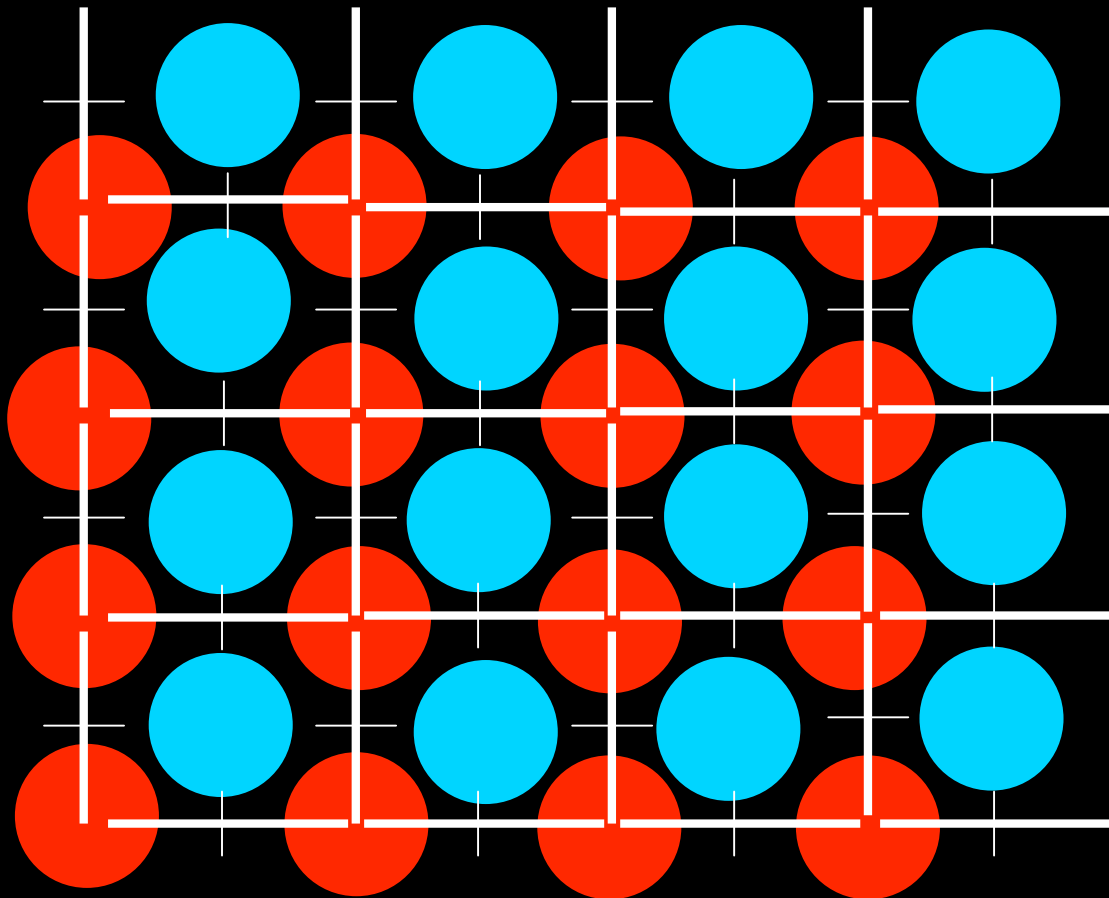
From Wayne Hu

YES, there is also
reionization

Rees 68, Coulson et al '94
..... Hu & White 97 (pedagogical)

Polarization for density perturbation

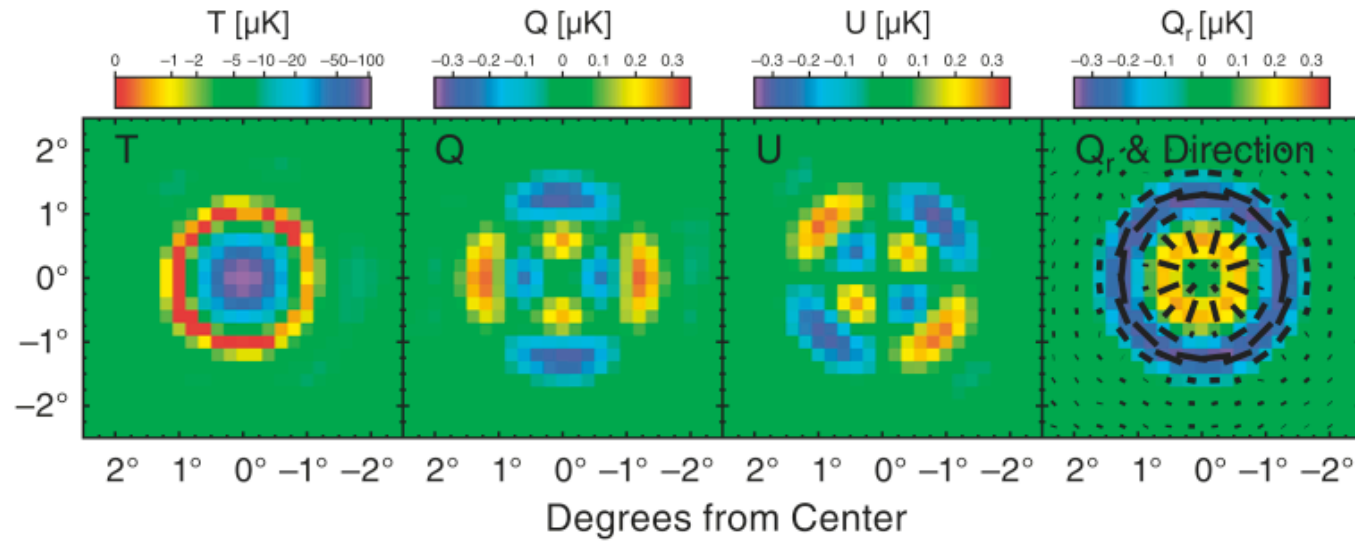
- Radial (tangential) pattern around hot (cold) spots.



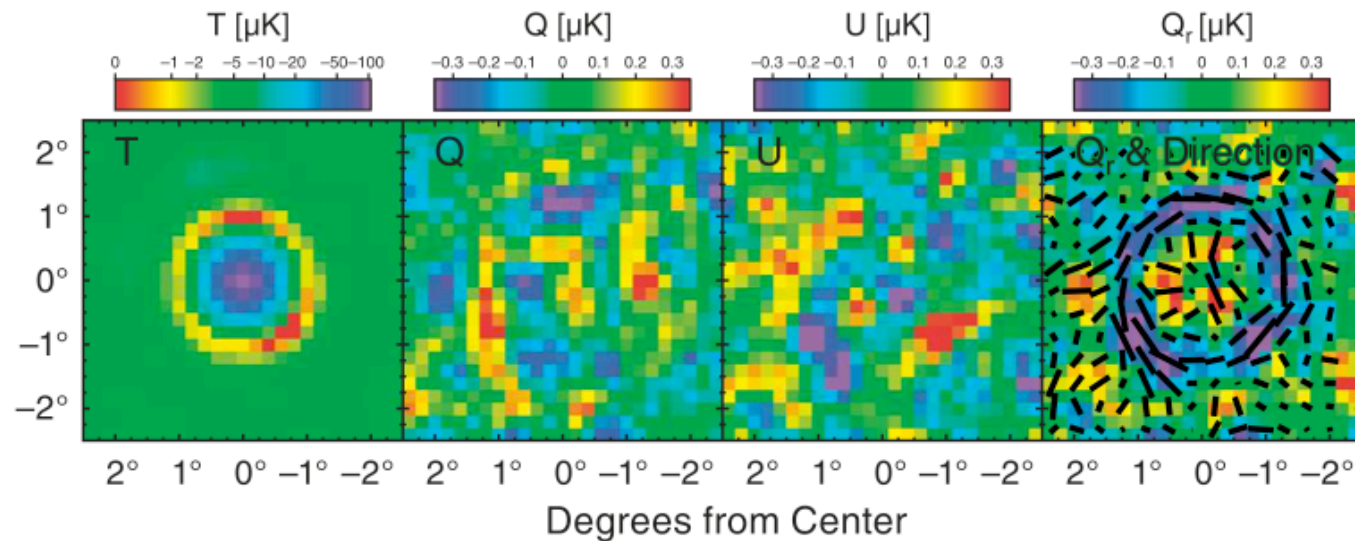
And it has been seen!

Komatsu, WMAP7yrs team (2010)

Theory
prediction

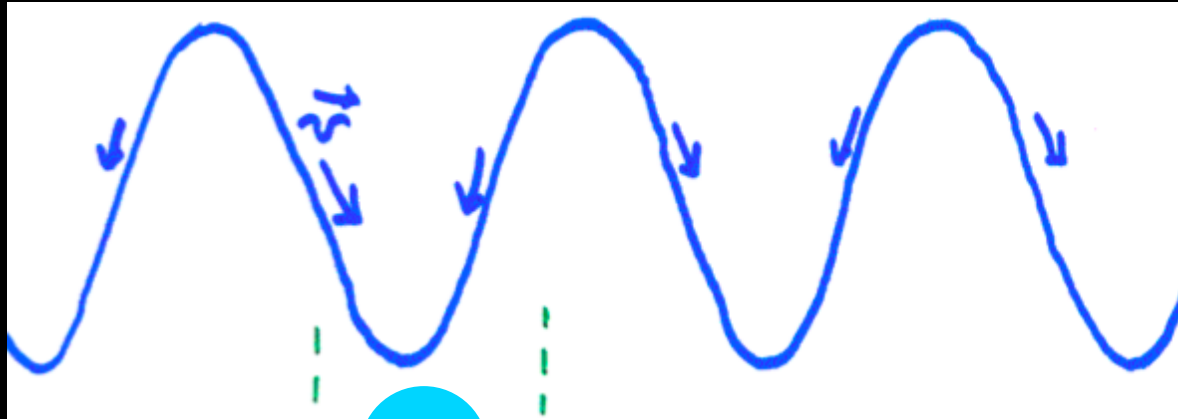


Observed



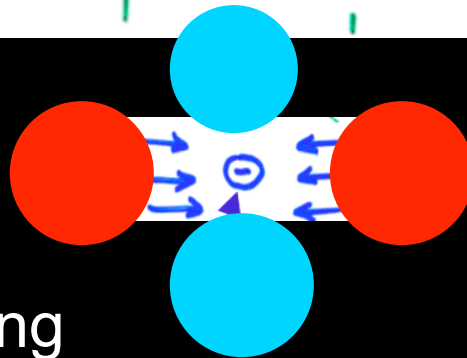
Large-scale TE anti correlation

Density mode



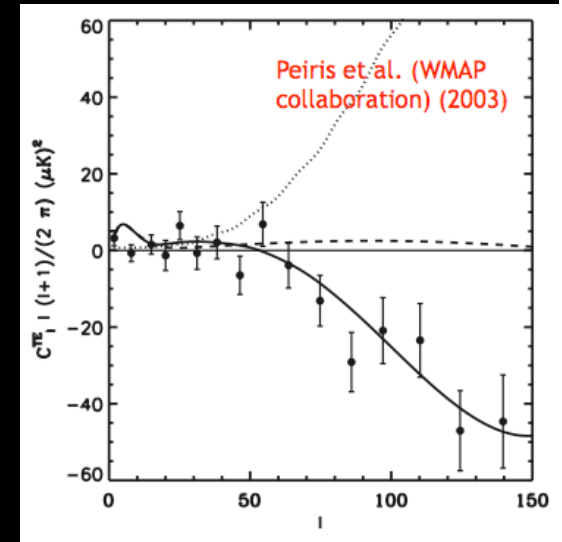
Velocities
(hot to cold)

During decoupling



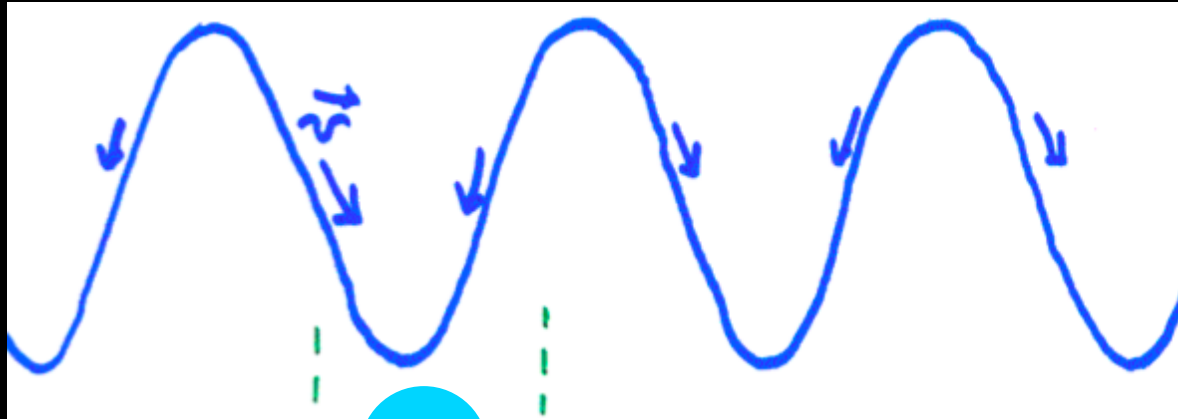
Hot due
to doppler

And it has been seen (2003)



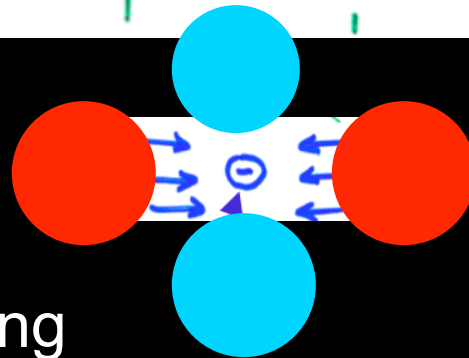
Large-scale TE anti correlation

Density mode



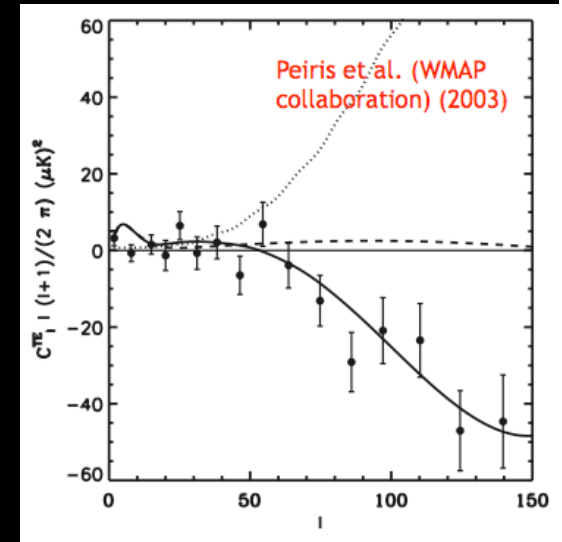
Velocities
(hot to cold)

During decoupling



Hot due
to doppler

Gravity waves (tensor) are different...



Gravity waves stretch space...

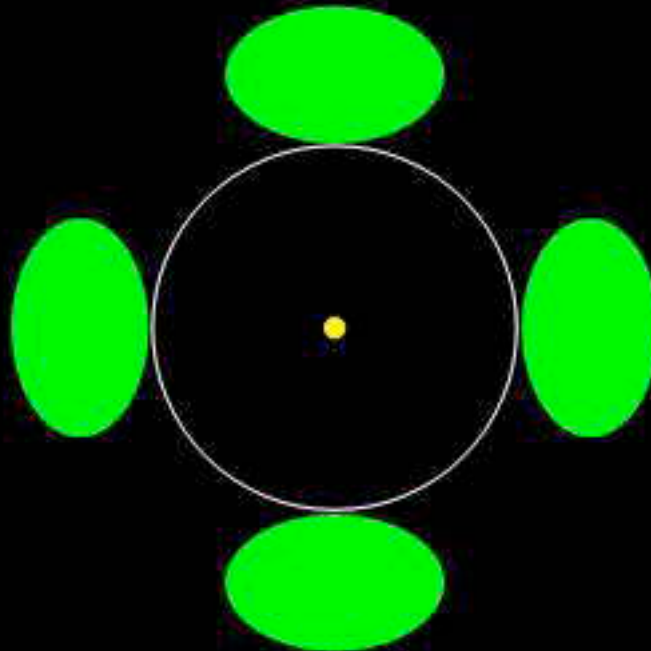


Image from J. Rhul.

... and create variations

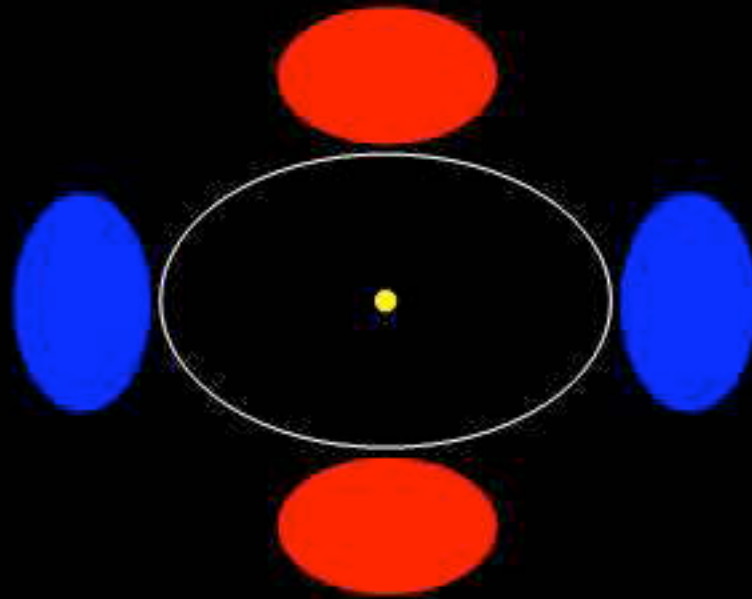
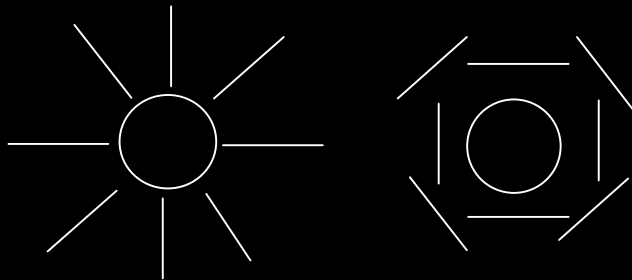


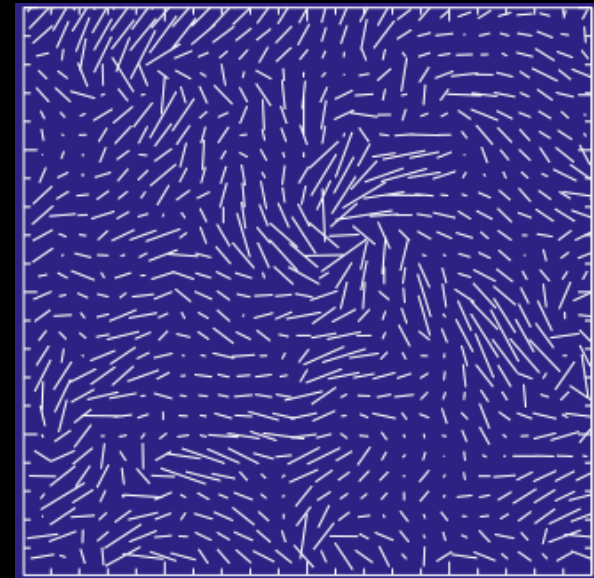
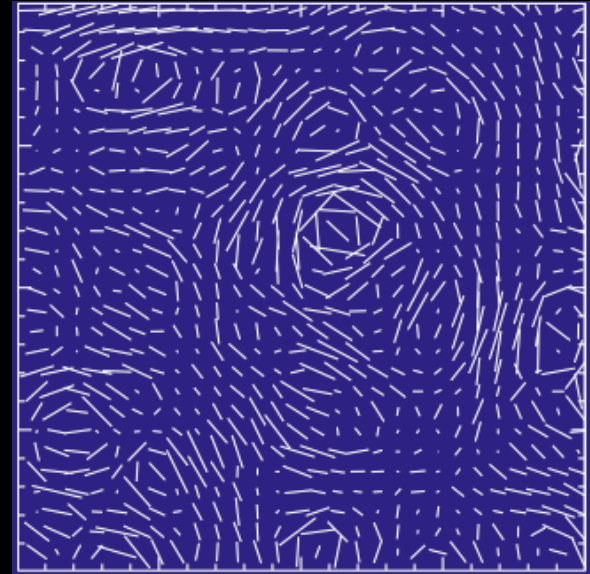
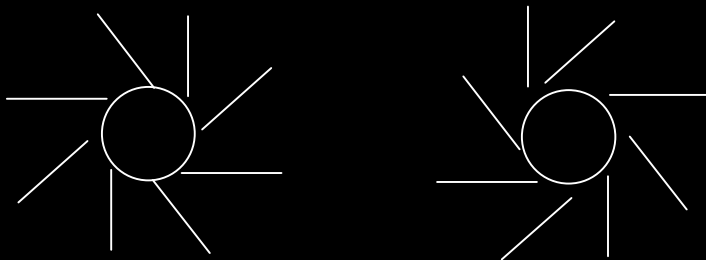
Image from J. Rhul.

E and B modes polarization

E polarization
from scalar, vector and tensor modes



B polarization only from (vector)
tensor modes



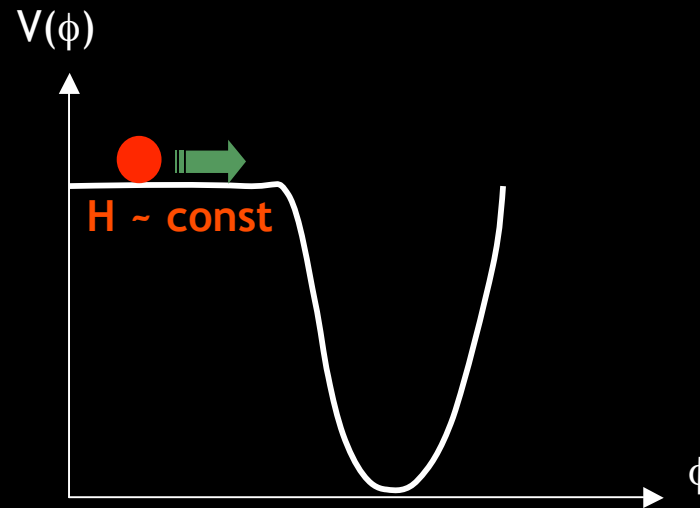
Seeing (indirectly) $z \gg 1100$

Information about the shape of the inflaton potential is enclosed in the shape and amplitude of the primordial power spectrum of the perturbations.

Information about the energy scale of inflation (the height of the potential) can be obtained by the addition of B modes polarization amplitude.

In general the observational constraints of $N_{\text{fold}} > 50$ requires the potential to be flat (not every scalar field can be the inflaton). But **detailed measurements of the shape of the power spectrum can rule in or out different potentials**. For example: Kahler inflation towards the KKLT minimum, or for multi-field other minima.

The inflationary solution



Accelerated expansion...

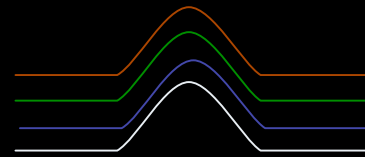
Factor 10^{26} in less than 10^{-34} s

Solves cosmological problems (Horizon, flatness).

Cosmological perturbations arise from quantum fluctuations, evolve classically.

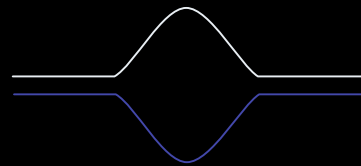
Guth (1981), Linde (1982), Albrecht & Steinhardt (1982), Sato (1981), Mukhanov & Chibisov (1981), Hawking (1982), Guth & Pi (1982), Starobinsky (1982), J. Bardeen, P.J. Steinhardt, M. Turner (1983), Mukhanov et al. 1992), Parker (1969), Birrell and Davies (1982)...

Perturbations: adiabatic



Photons
Neutrinos
Baryons(+electrons)
Dark matter
(dark energy negligible
early on)

(isocurvature)



Tensor
(gravitational waves)

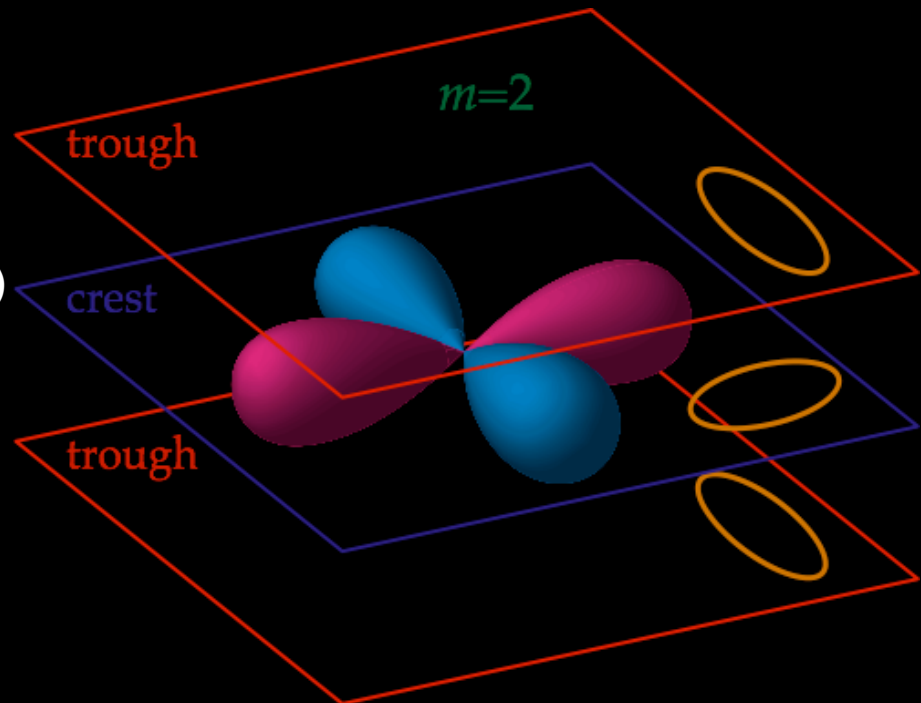


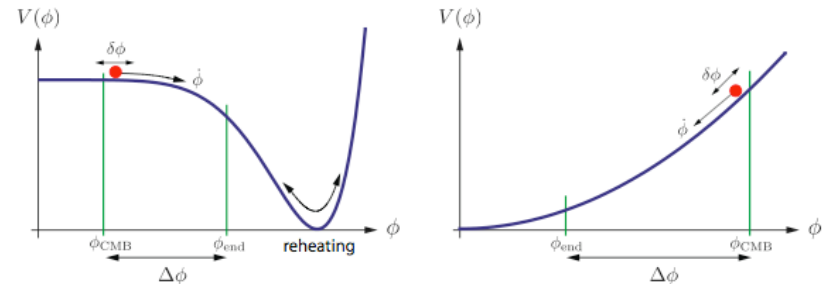
Fig. From W. Hu.

Inflationary cosmology

Friedmann equations, a is scale factor

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{3M_{\text{pl}}^2} \rho, \quad = \frac{1}{3M_{\text{pl}}^2} \left(\frac{1}{2} \dot{\phi}^2 + V(\phi) \right)$$

$$\dot{H} + H^2 = \frac{\ddot{a}}{a} = -\frac{1}{6M_{\text{pl}}^2} (\rho + 3p) = -\frac{1}{3M_{\text{pl}}^2} (\dot{\phi}^2 - V(\phi))$$



$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$. Single field slow roll inflation:
the simplest example

Inflate: $V \gg \dot{\phi}^2$, $a(t) \approx a(0)e^{Ht}$, $H \approx \text{const}$.

Sustain it $|\ddot{\phi}| \ll |V'|$. Process must terminate somehow

Restrictions in the form of the inflaton potential V :
SLOW ROLL PARAMETERS

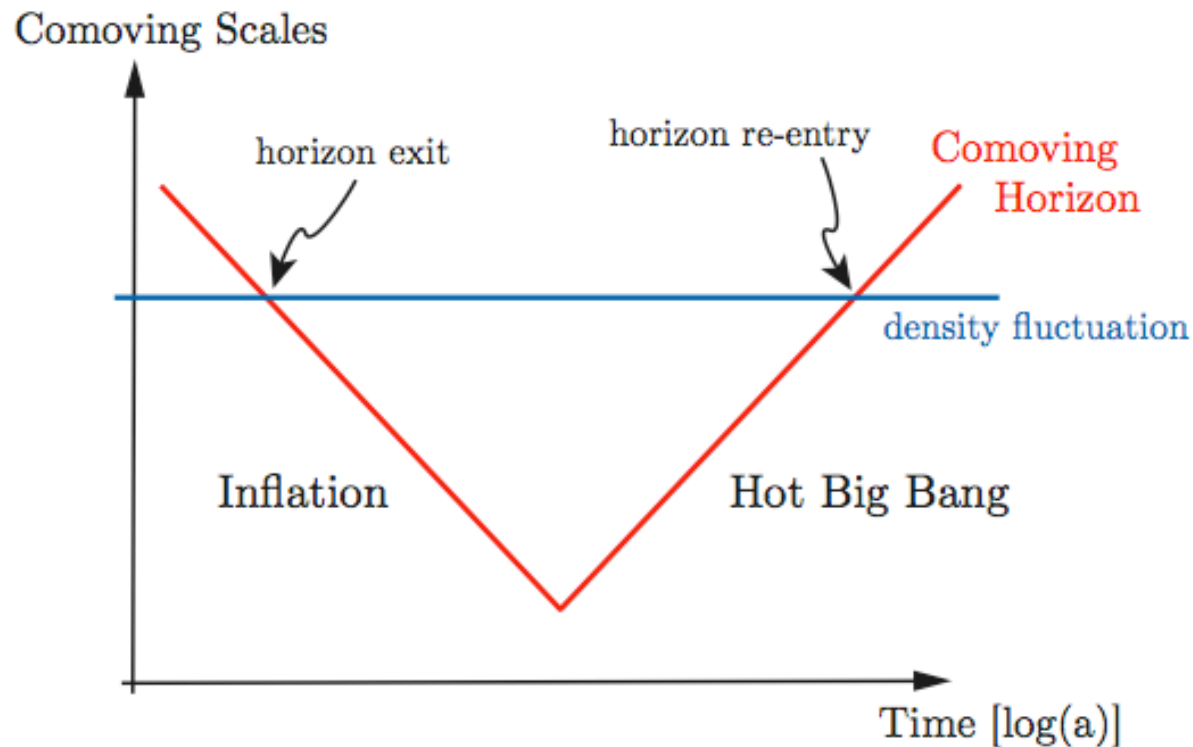
$$\epsilon \equiv -\frac{\dot{H}}{H^2} = \frac{M_{\text{pl}}^2}{2} \frac{\dot{\phi}^2}{H^2} \approx \frac{M_{\text{pl}}^2}{2} \left(\frac{V'}{V} \right)^2, \quad |\eta| \approx M_{\text{pl}}^2 \left| \frac{V''}{V} \right|$$

Inflationary cosmology

Physical wavelength of fluctuations is stretched by expansion

The physical horizon is time dependent

Physical wavelengths grow faster than the horizon



Origin of structure

Quantum fluctuations get stretched to become classical
and “super-horizon” because of the accelerated expansion

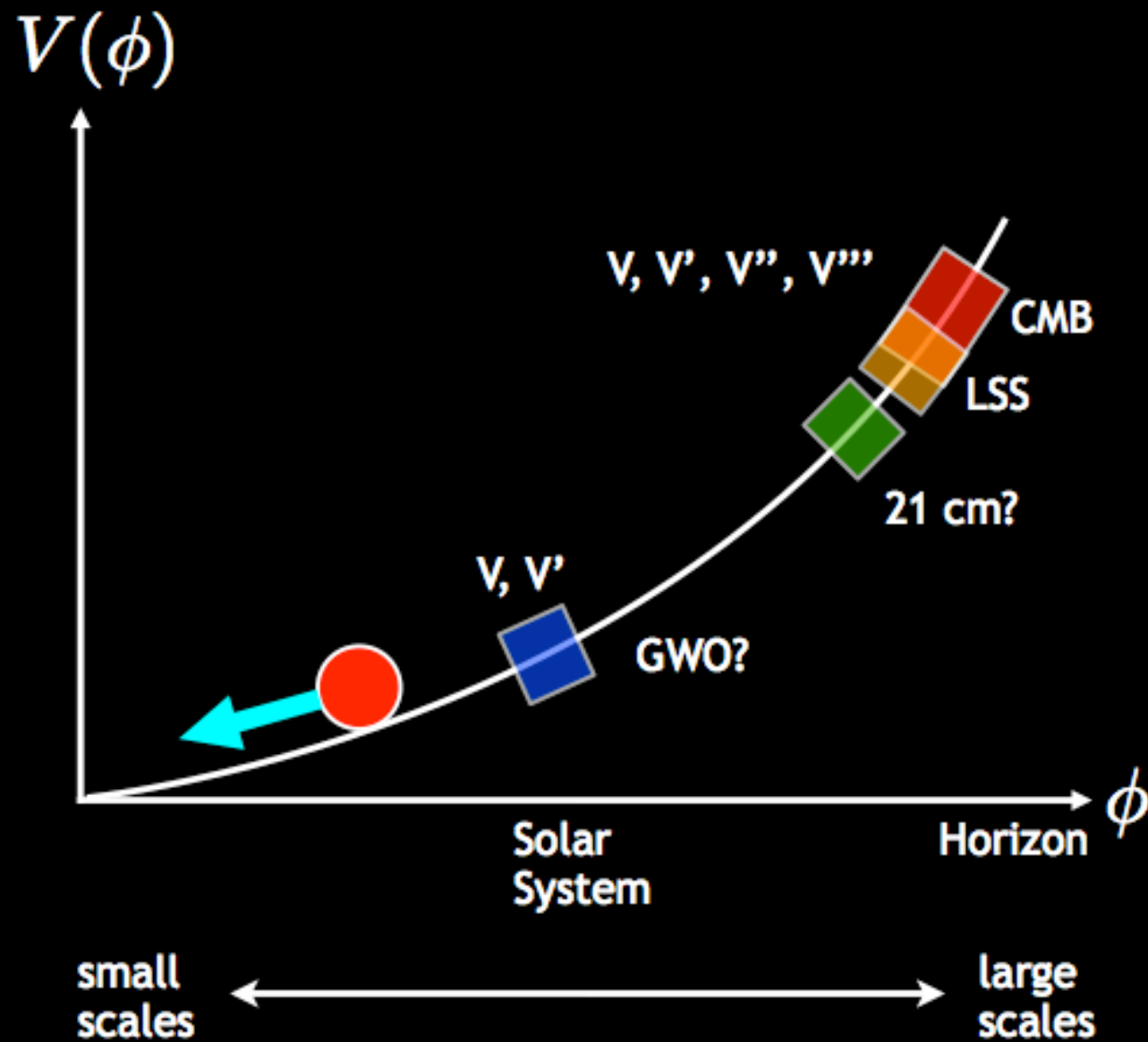
But the spacing of the fluctuations
(their power as a function of scale)
depend on how fast they exited the horizon (H)

Which in turns depend on the inflaton potential



The shape of the primordial power spectrum
encloses information on the shape of the inflaton potential!

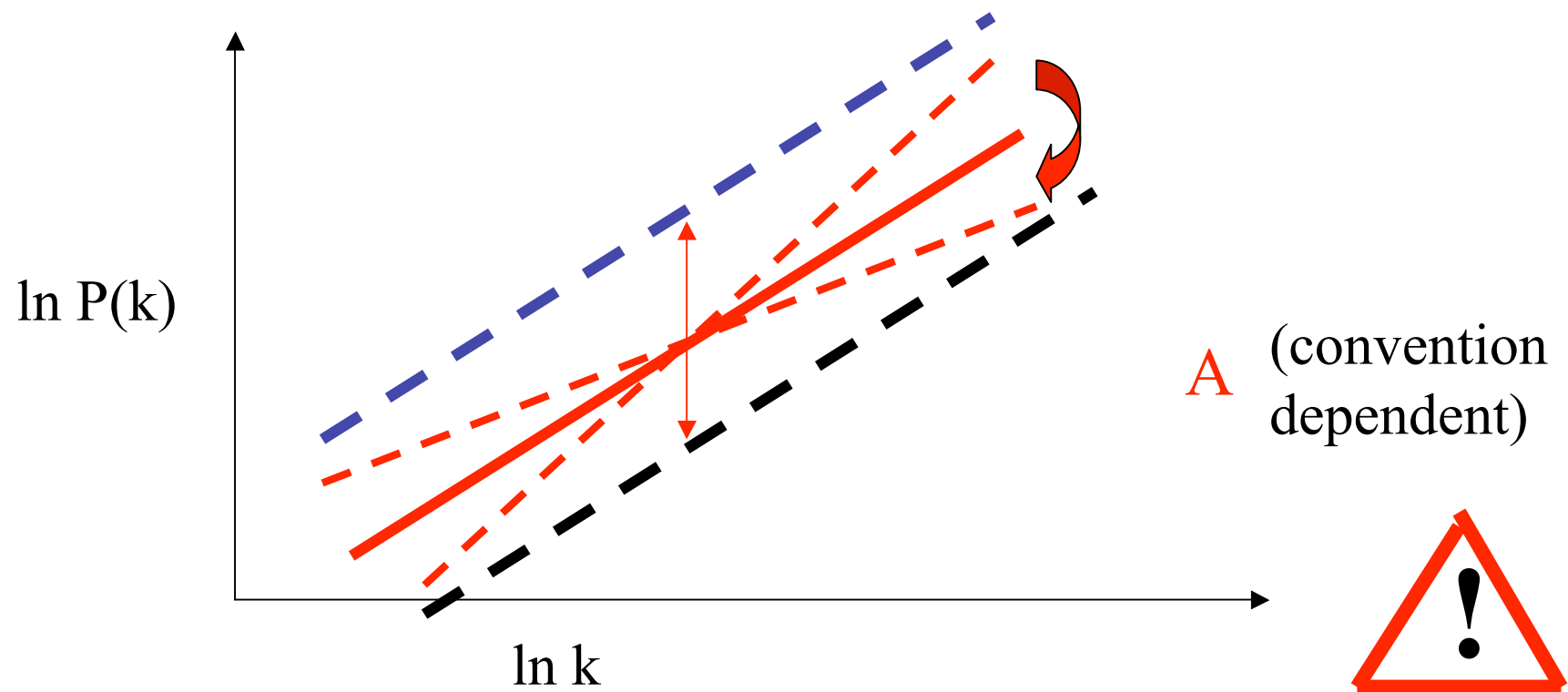
Fingerprints of the early universe



Primordial power spectrum = $A k^n$

slope

Amplitude of the power law



A (convention dependent)

Equal power per log k , $n=1$, scale invariant

Slow roll predictions

$$P_s(k) = \frac{1}{24\pi^2 M_{\text{pl}}^4} \frac{V}{\epsilon} \bigg|_{k=aH}, \quad n_s - 1 = 2\eta - 6\epsilon, \quad \epsilon \propto V'/V$$

$$P_t(k) = \frac{2}{3\pi^2} \frac{V}{M_{\text{pl}}^4} \bigg|_{k=aH}, \quad n_t = -2\epsilon, \quad r = 16\epsilon.$$

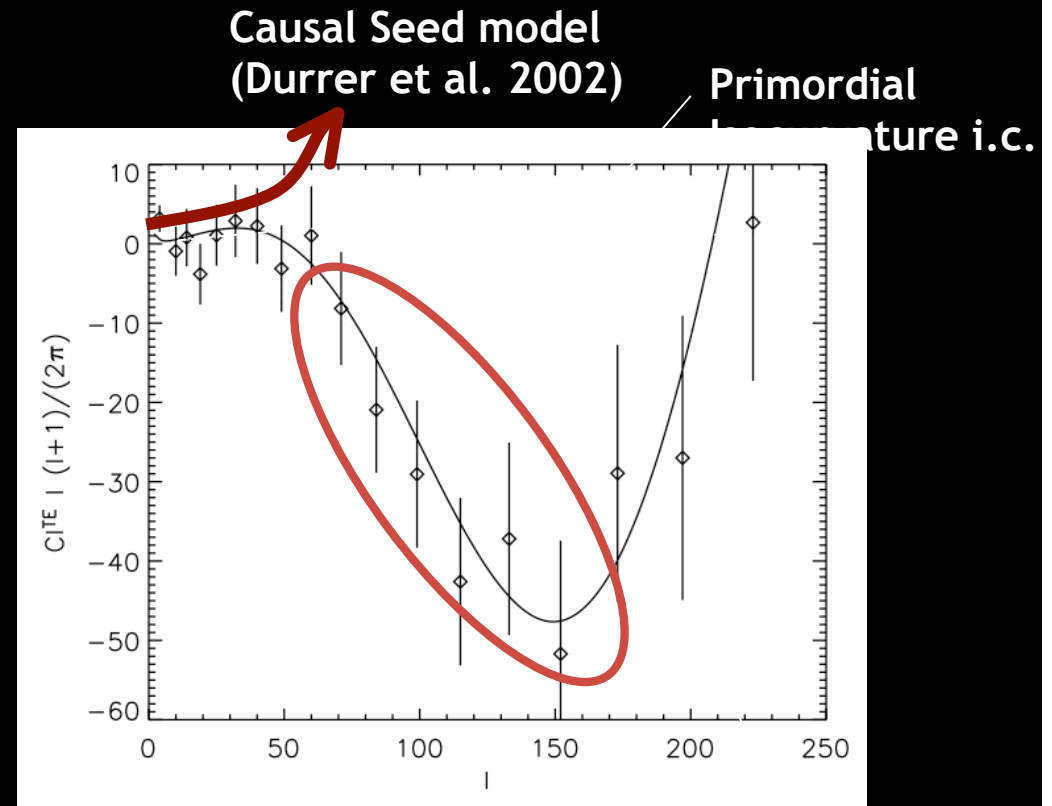
$$V(\phi) = V|_{\star} + V'|_{\star} (\phi - \phi_{\star}) + \frac{1}{2} V''|_{\star} (\phi - \phi_{\star})^2 + \frac{1}{3!} V'''|_{\star} (\phi - \phi_{\star})^3 + \dots,$$

Other models, of course

CMB Consistent with Simplest Inflationary Models

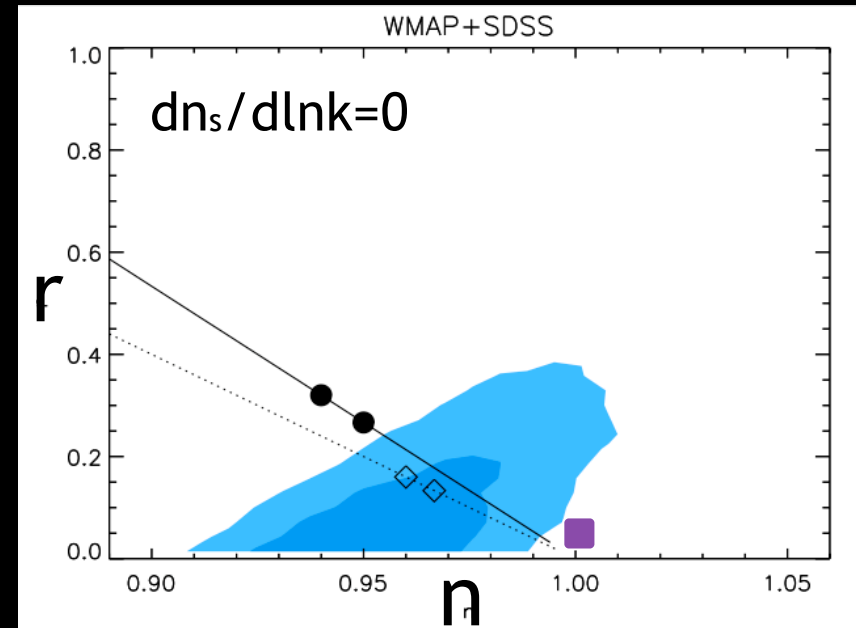
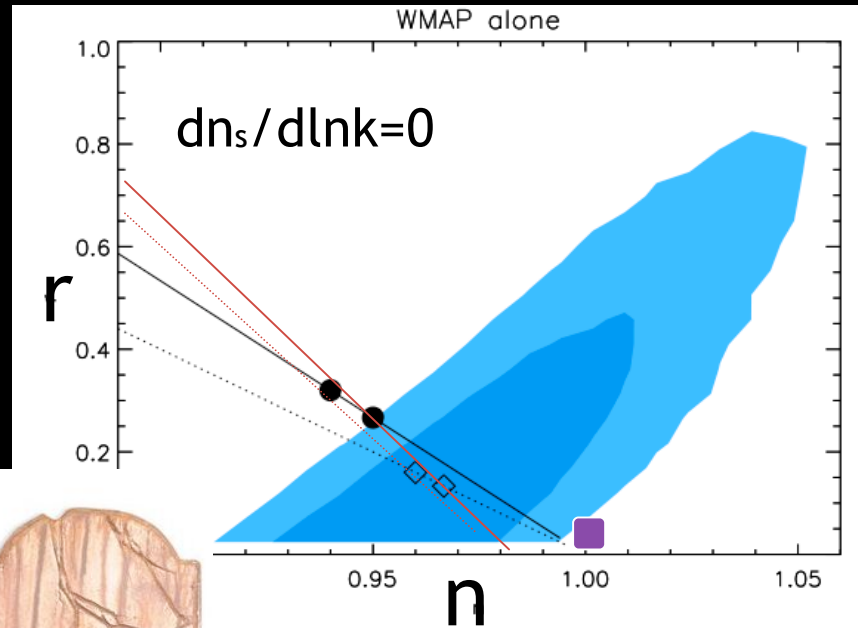
- Flat universe:
 $\Omega_{\text{tot}} = 1.0052 \pm 0.0064$
(with SN and BAO)
- Gaussianity: $-9 < f_{NL} < 111$
- Power Spectrum spectral index nearly scale-invariant:
 $n_s = 0.97 \pm 0.01$
- Adiabatic initial conditions
- Superhorizon fluctuations
(TE anticorrelations)

Still testing basic aspects of inflationary mechanism
rather than specific implementations



Hu & Sujiyama 1995
Zaldarriaga & Harari 1995
Spergel & Zaldarriaga 1997
Peiris et al 2003

Specific models critically tested



Models like $V(\phi) \sim \phi^p$

○ $p=4$

◆ $p=2$

For 50 and 60 e-foldings

■ HZ

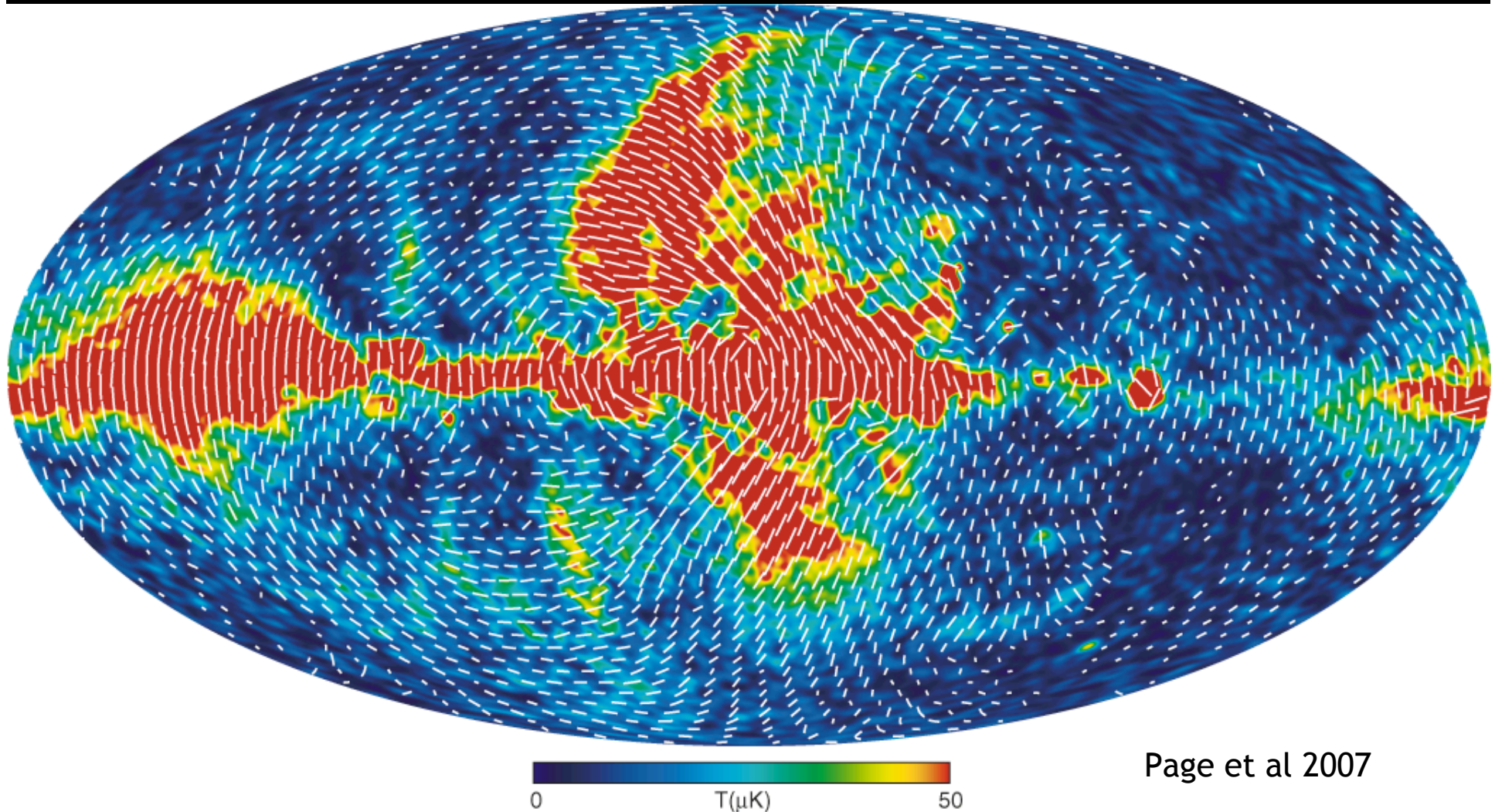
— p fix, N_e varies
— p varies, N_e fix

p fix, N_e varies
 p varies, N_e fix

We happen to live in a galaxy!

K Band (23 GHz)

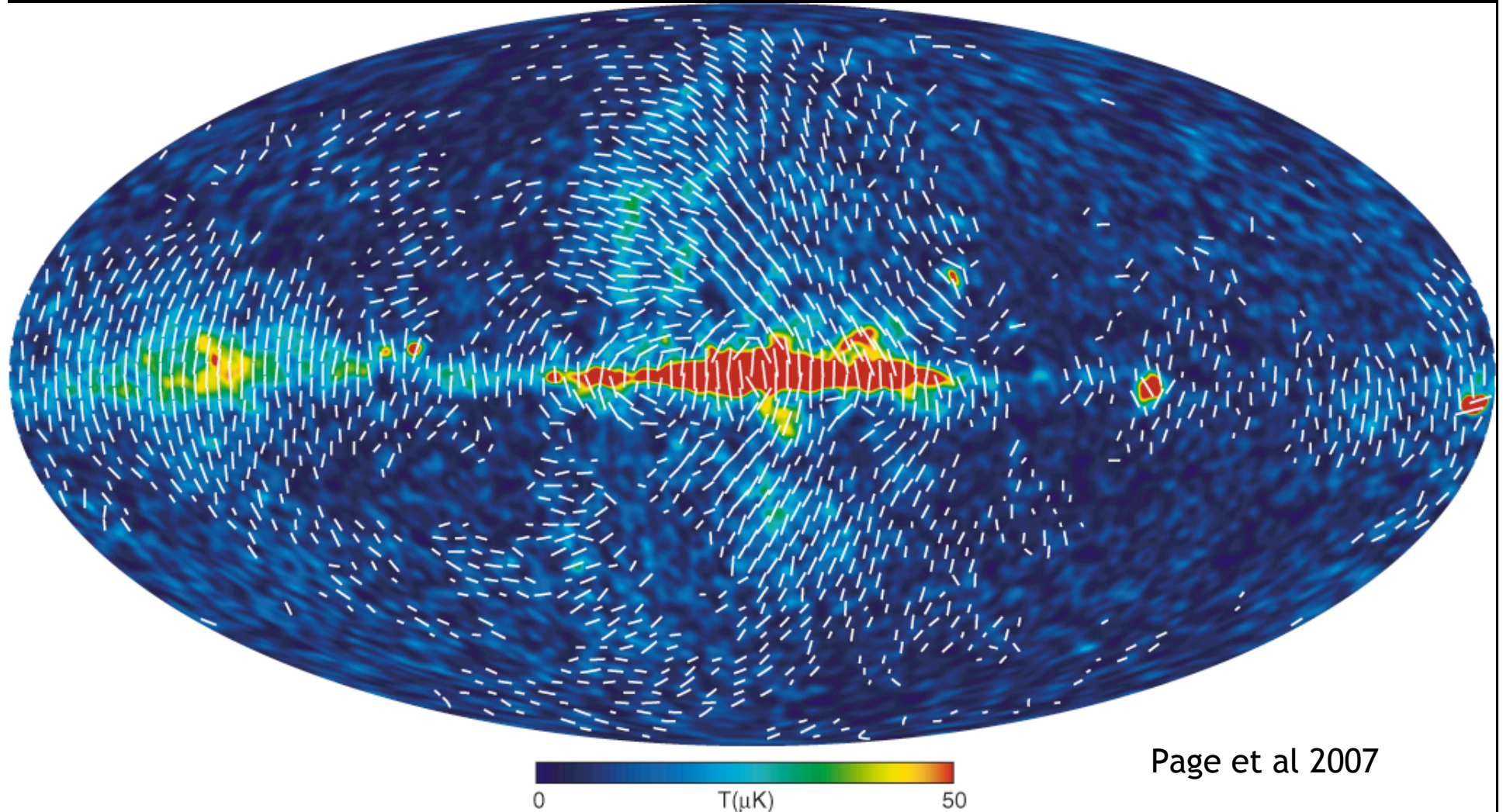
Dominated by synchrotron; Note that polarization direction is perpendicular to the magnetic field lines.



Page et al 2007

Ka Band (33 GHz)

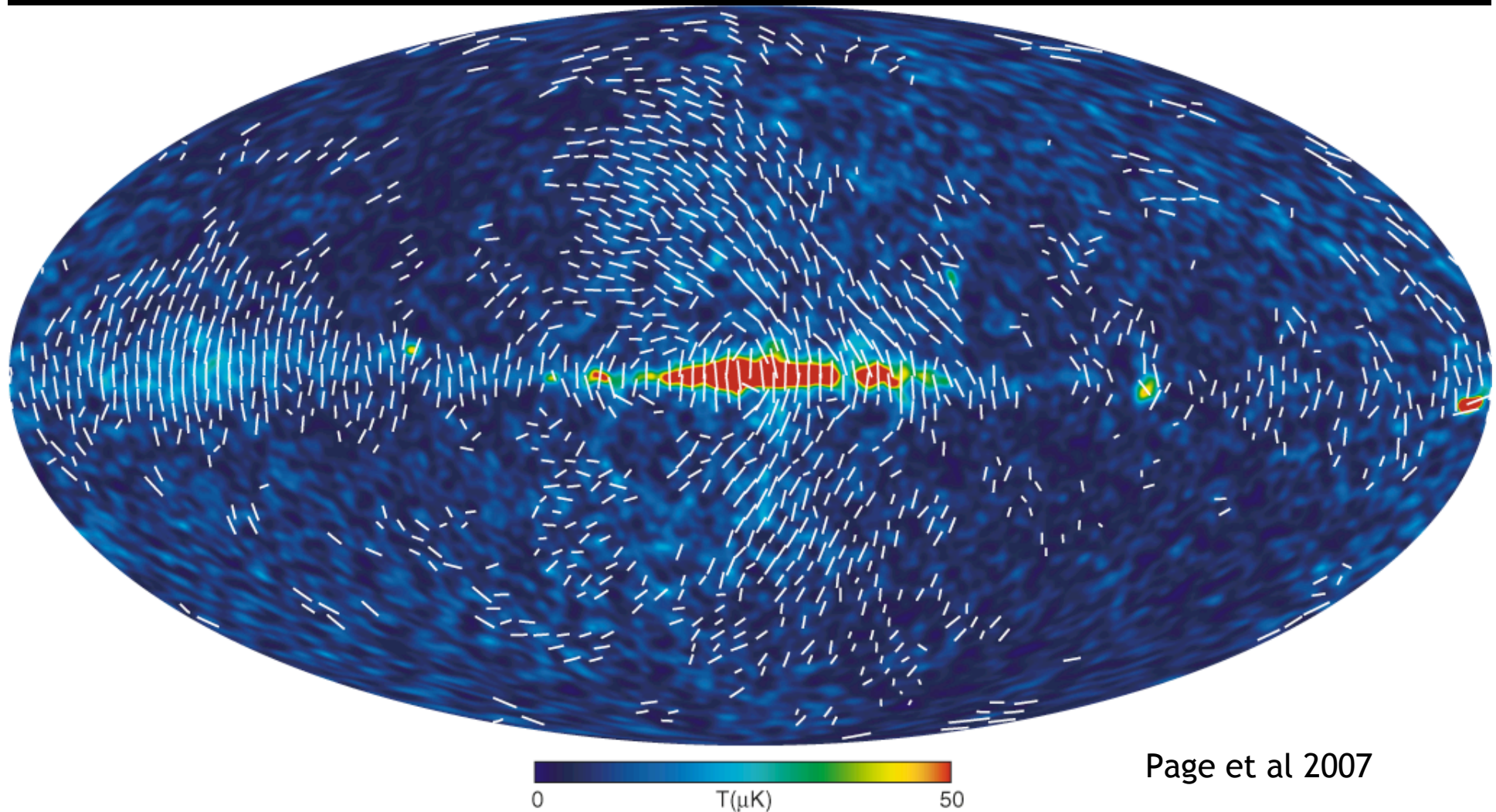
Synchrotron decreases as $n^{-3.2}$ from K to Ka band.



Page et al 2007

Q Band (41 GHz)

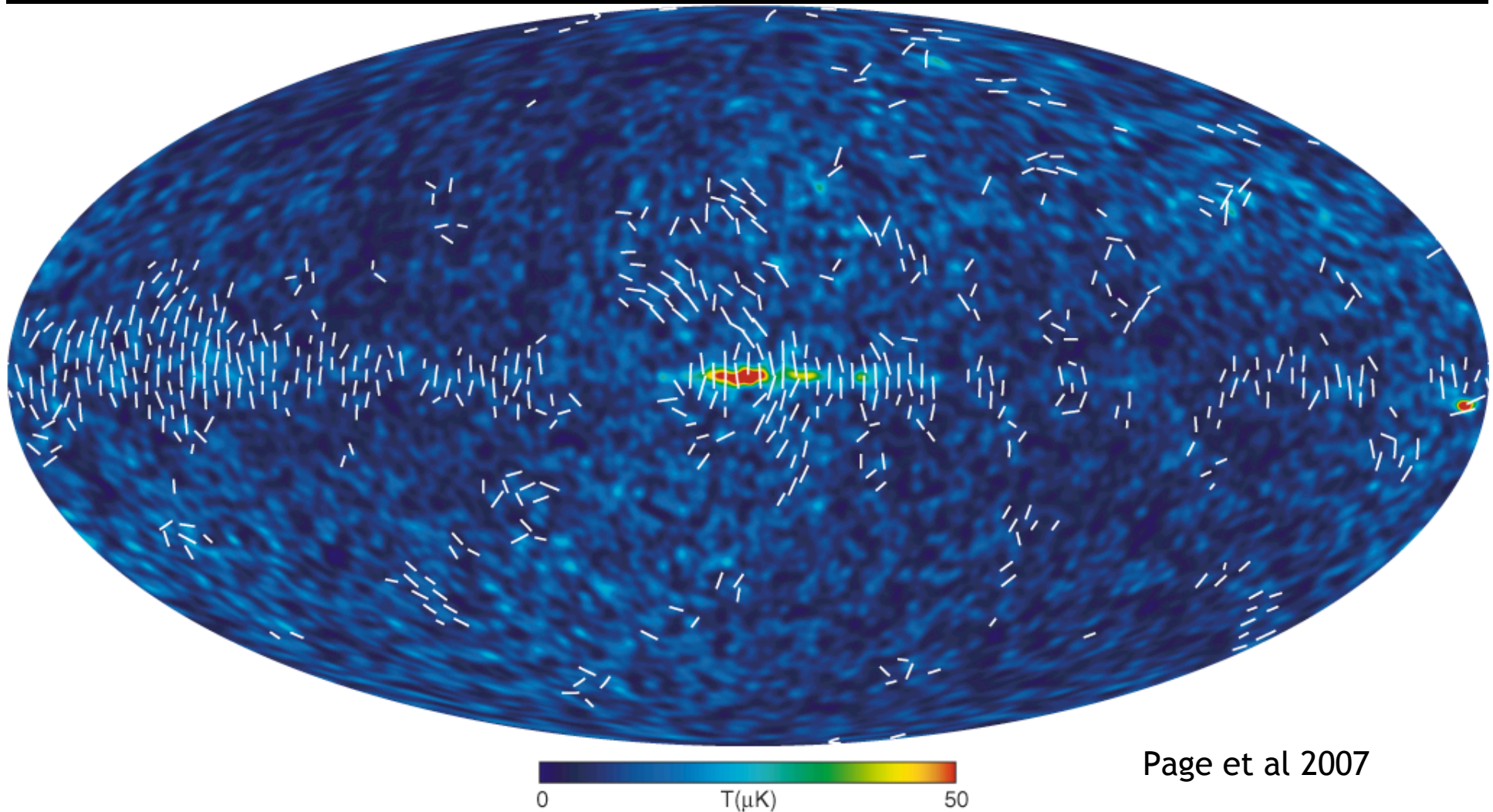
We still see significant polarized synchrotron in Q.



Page et al 2007

V Band (61 GHz)

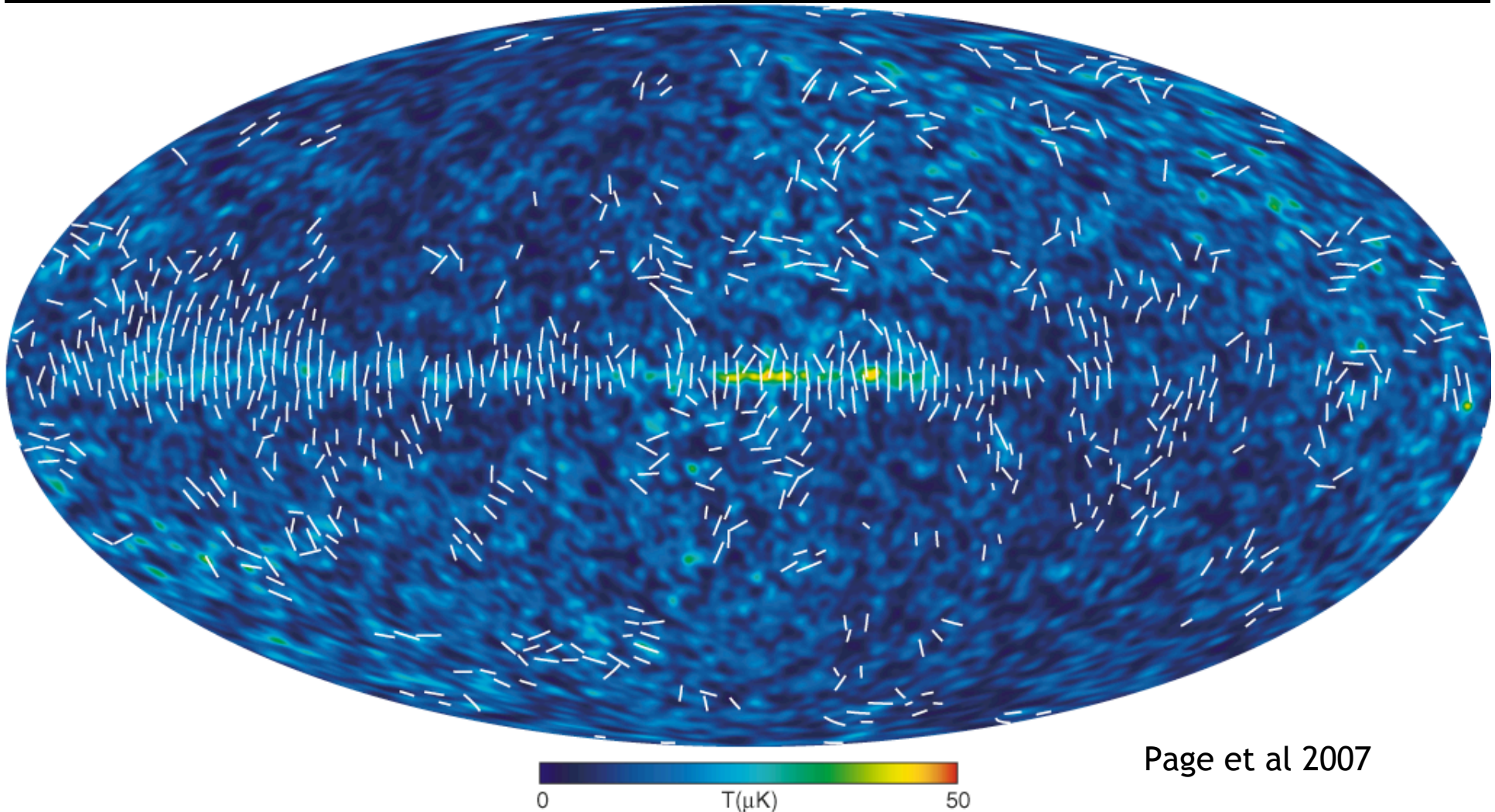
The polarized foreground emission is also smallest in V band.
We can also see that noise is larger on the ecliptic plane.



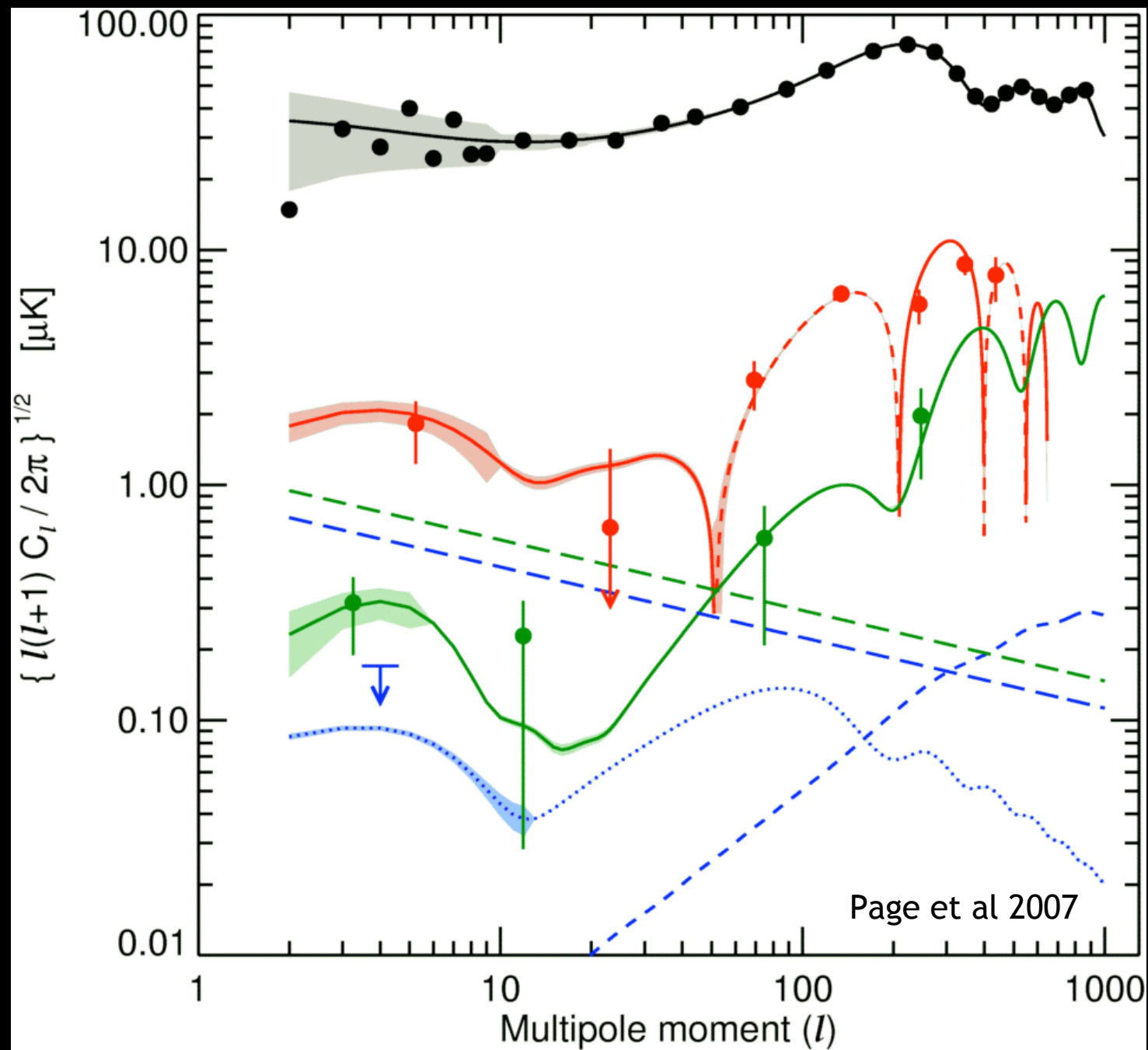
Page et al 2007

W Band (94 GHz)

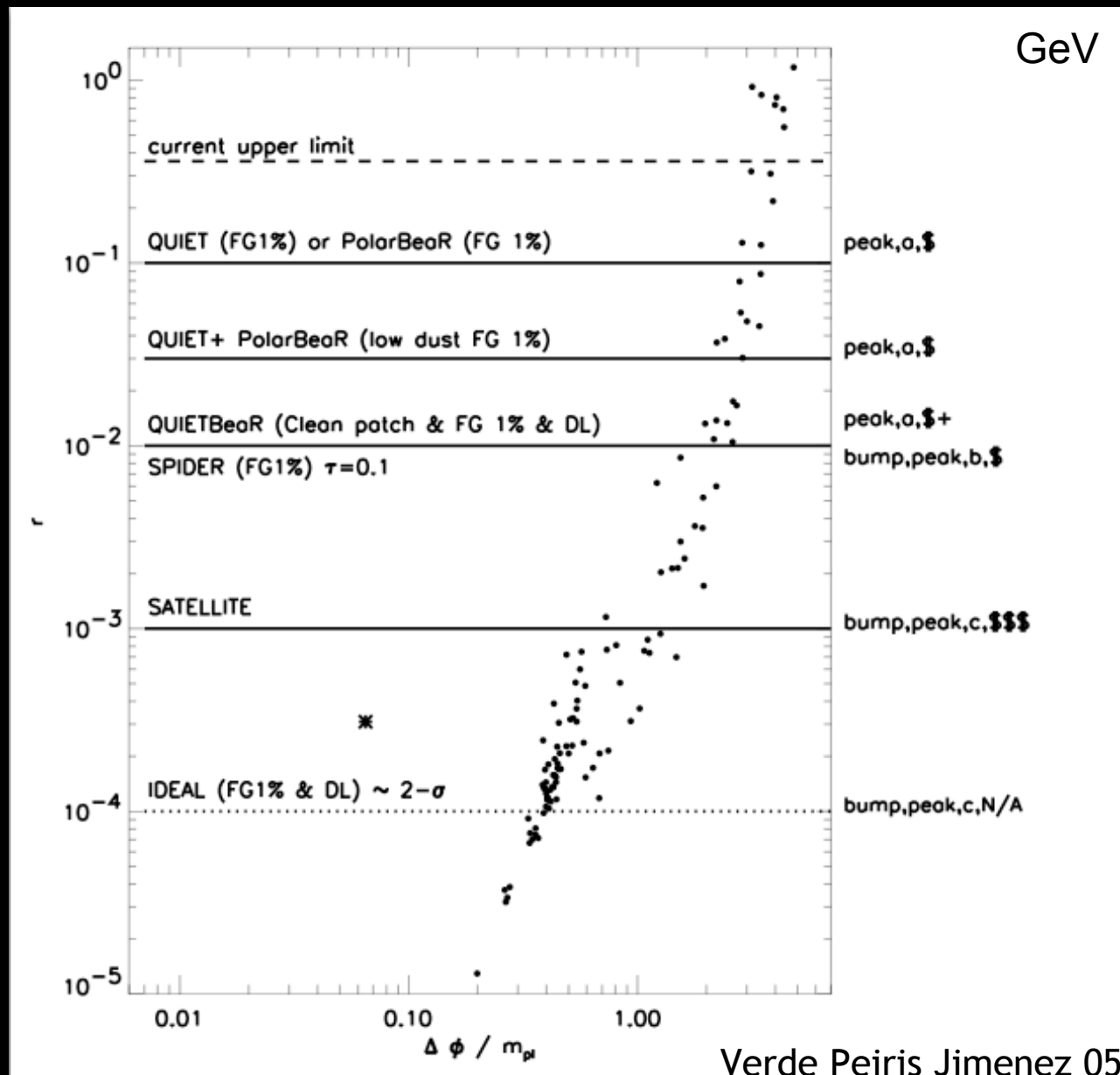
While synchrotron is the smallest in W, polarized dust (hard to see by eye) may contaminate in W band more than in V band.



Page et al 2007



The next frontier: gravity waves



Tev

$$3.2 \times 10^{16}$$

$$1.7 \times 10^{16}$$

$$9.7 \times 10^{15}$$

$$5.5 \times 10^{15}$$

$$3 \times 10^{15}$$

Windows into the primordial Universe

Recombination

380000 yrs

Atomic physics/GR

Nucleosynthesis

3 minutes

Nuclear physics

LHC

TeV energies

inflation

10^{-30} s (?)

GUT?

Big BANG



What next?

Polarization, the next frontier

Why measure CMB Polarization?

Directly measures dynamics in early universe

So far:

Critical test of the underlying theoretical framework for cosmology

Future: “How did the Universe begin?”

Improve cosmological constraints

Eventually, perhaps, test the theory of inflation.

Plans for the ultimate primary polarization CMB experiment
(CM)BPol

Inflation: Theoretical Front



"Inflation consists of taking a few numbers that we don't understand and replacing it with a function that we don't understand"

David Schramm 1945 - 1997

$V(\phi)$

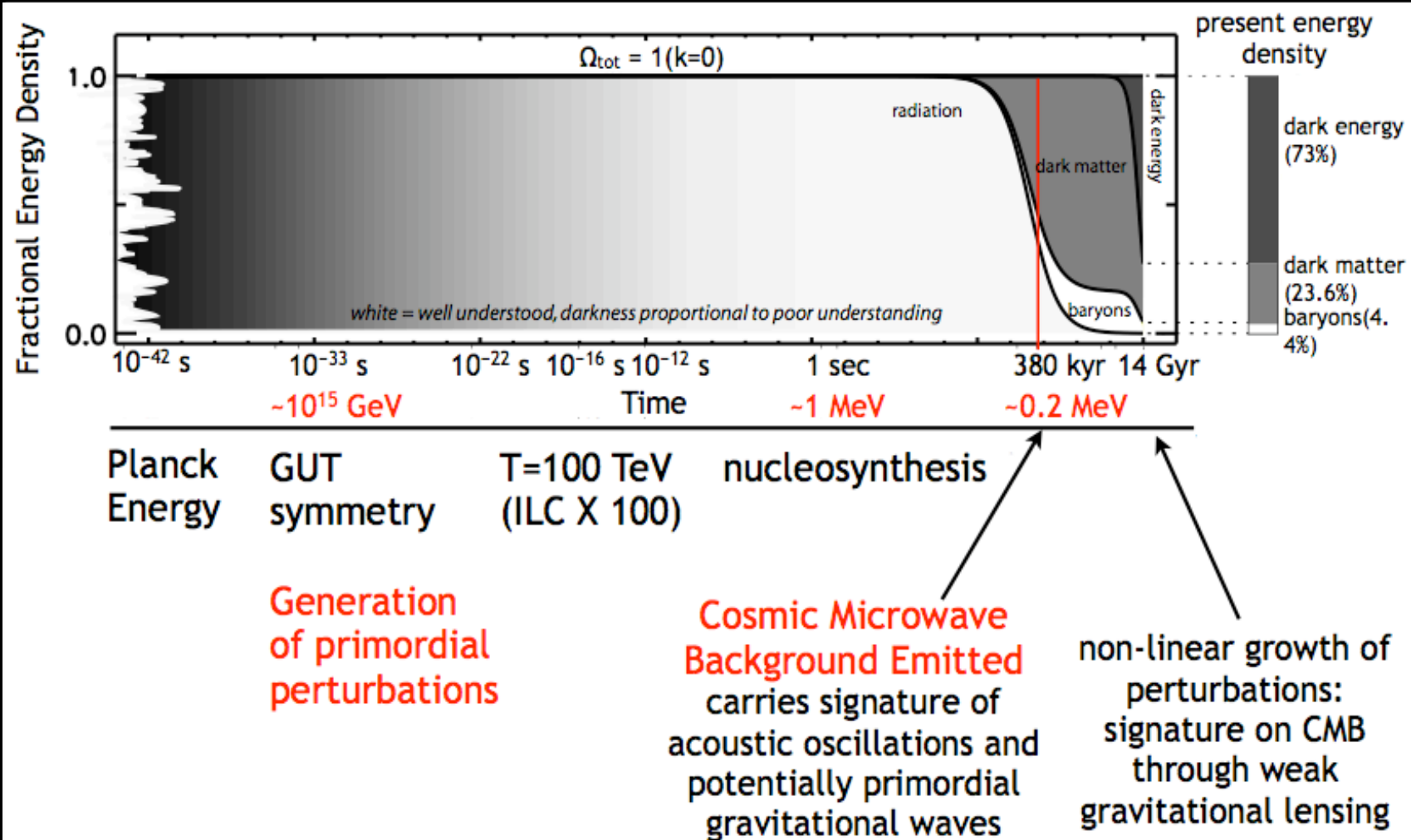
Why did the field start here?

Where did this function come from?

Why is the potential so flat?

How do we convert the field energy completely into particles?

Cosmic History / Cosmic Mystery



McMahon adapted by Peiris

Three important documents

(will probably shape observational cosmology for the next 10 years)

“Task force on CMB research” report
(to advise DoE, NSF, NASA):
Bock et al. 2006 (arXiv:astro-ph/0604101)

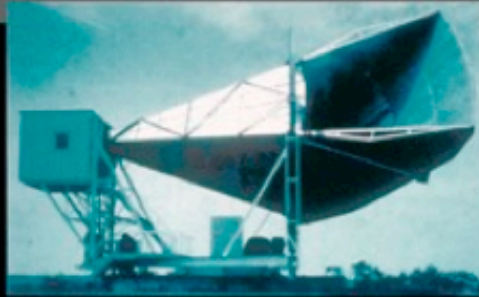
“The dark energy task force report”
(to advise DoE, NSF, NASA):
Albrecht et al. 2006 (arXiv:astro-ph/0609591)

“The report by the ESA-ESO Working Group on Fundamental Cosmology”
Peacock et al 2006 (astro-ph/0610906)

History of CMB temperature measurements

1965

Penzias and
Wilson

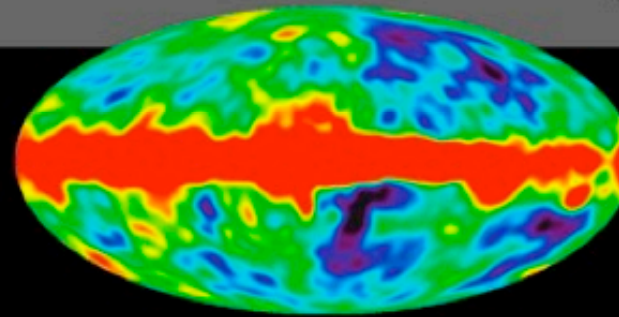


2.725 K



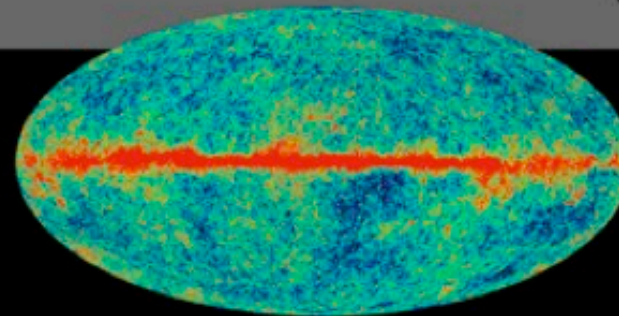
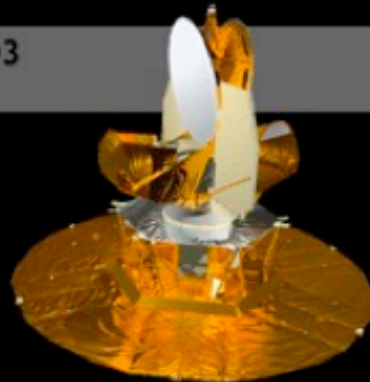
1992

COBE



2003

WMAP



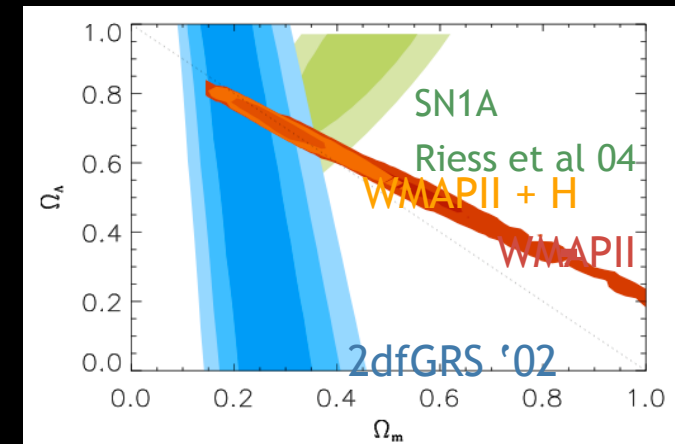
TOCO (1998) BOOMERANG (1998, 2003) MAXIMA (2000)
ARCHEOPS (2002) CBI (2002) ACBAR (2002) VSA (2002)

Origins of primordial fluctuations: Clues

- Flat universe:

WMAP + $h = 0.72 \pm 0.08$	-0.014 ± 0.017
WMAP + SDSS	$-0.0053^{+0.0068}_{-0.0060}$
WMAP + 2dFGRS	$-0.0093^{+0.0098}_{-0.0092}$
WMAP + SDSS LRG	-0.012 ± 0.010
WMAP + SNLS	-0.011 ± 0.012
WMAP + SNGold	-0.023 ± 0.014

Ω_K

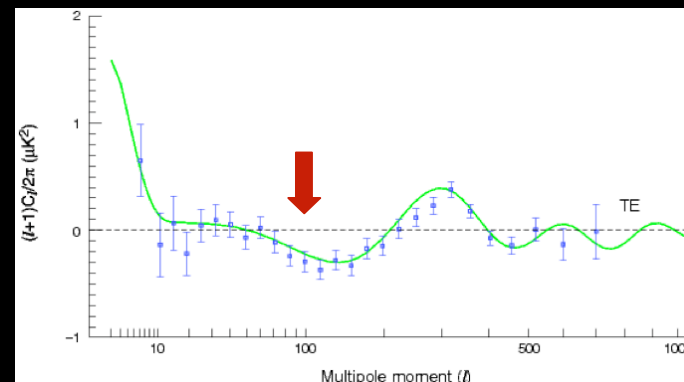


- Gaussianity: $-54 < f_{NL} < 114$
- Power Spectrum spectral index nearly scale-invariant:

n_s

WMAP	WMAP+CMB	WMAP+LSS
$0.951^{+0.015}_{-0.019}$	$0.947^{+0.014}_{-0.017}$	$0.948^{+0.014}_{-0.018}$

- Adiabatic initial conditions
- Superhorizon fluctuations (TE anticorrelations)



Observations Consistent with Simplest Inflationary Models