



# Property Measurements of Higgs-like Single Resonance at LHC

## MELA and Spin Hypothesis Separation

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On behalf of CMS++

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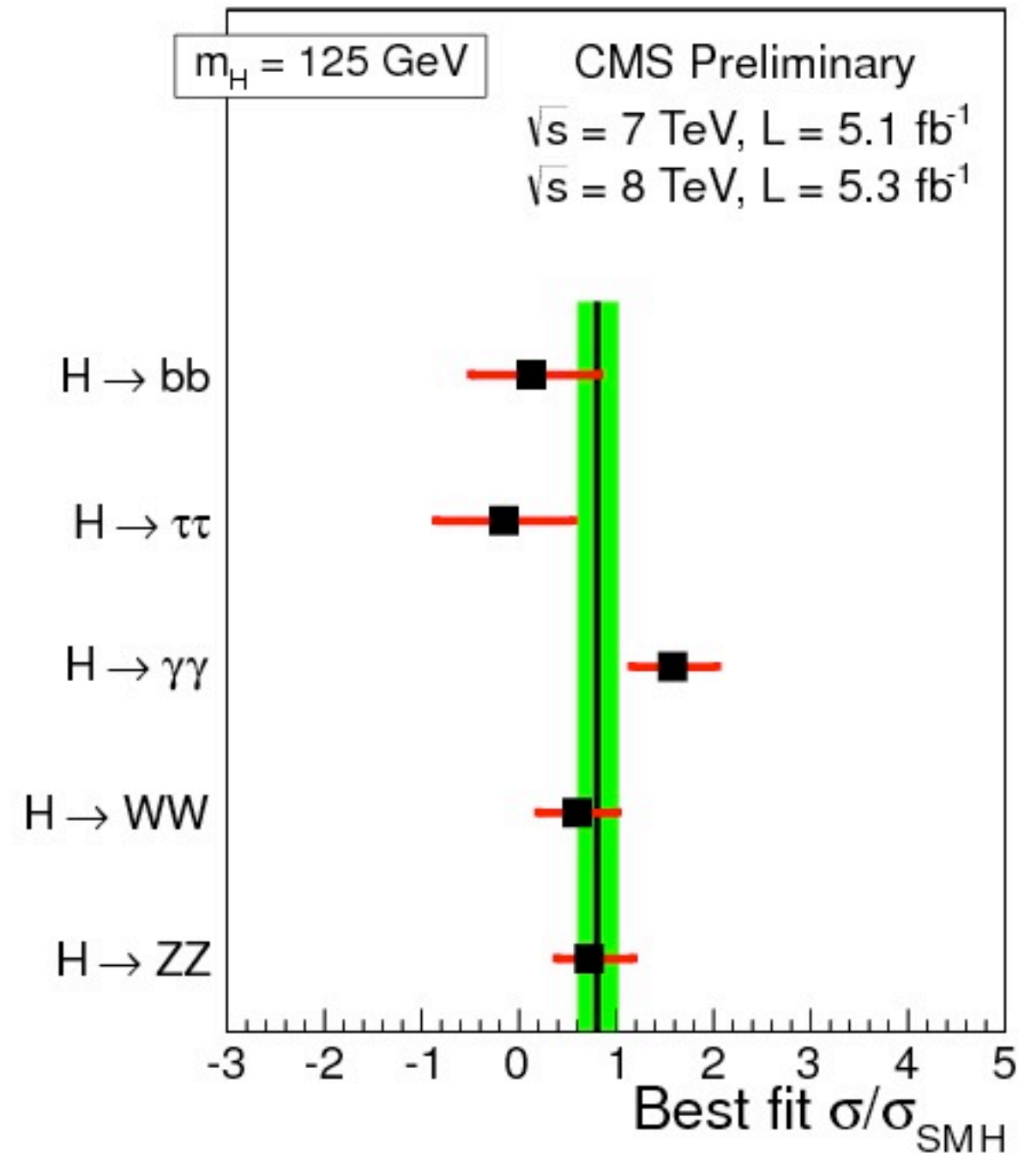
(a) Johns Hopkins University,

(b) Argonne National Laboratory,

(c) Fermi National Laboratory

# Motivation

- LHC has observed a single resonance with mass  $\sim 125$  GeV
  - Primarily driven in di-boson channels
- The spin/parity measurement is a crucial step to understand the resonance and its interactions with SM particles
  - Given the large contribution in  $\gamma\gamma$ , the spin-1 hypothesis is not favored
  - Among all other possibilities, consider the following interesting spin/parity hypotheses
    - Scalar:  $0^+$
    - Pseudo-scalar:  $0^-$
    - Tensor  $2^+$



# Outline

- An update of previous report by Nhan Tran
  - <https://indico.cern.ch/contributionDisplay.py?contribId=34&confId=162621>
- Brief reminder of the general  $pp \rightarrow X \rightarrow VV$  interactions and angular analysis
  - MC generator used to simulate the  $pp \rightarrow X \rightarrow VV$  interactions
- The Matrix Element Likelihood Analysis in  $X \rightarrow ZZ \rightarrow 4l$ 
  - Impact on the  $H \rightarrow ZZ \rightarrow 4l$  search
  - The spin/parity hypothesis test in the  $X \rightarrow ZZ \rightarrow 4l$
- The spin/parity hypothesis test in the  $X \rightarrow WW \rightarrow (lv)(lv)$
- Summary and conclusions

Describe  $pp \rightarrow X \rightarrow VV$   
Interactions

# $X \rightarrow VV$ Amplitude for Spin-0

- A general amplitude in terms of polarization vectors

$$A = v^{-1} \epsilon_1^{*\mu} \epsilon_2^{*\nu} \left( a_1 g_{\mu\nu} M_X^2 + a_2 q_\mu q_\nu + a_3 \epsilon_{\mu\nu\alpha\beta} q_1^\alpha q_2^\beta \right)$$

- This allows us to rewrite it in the form of the helicity amplitudes, which later can be connected to the experimental angular analysis

$$\begin{aligned} A_{00} &= -\frac{M_X^2}{v} \left( a_1 x + a_2 \frac{M_{V_1} M_{V_2}}{M_X^2} (x^2 - 1) \right) \\ A_{\pm\pm} &= +\frac{M_X^2}{v} \left( a_1 \pm i a_3 \frac{M_{V_1} M_{V_2}}{M_X^2} \sqrt{x^2 - 1} \right) \end{aligned} \quad \Leftarrow \quad x = \frac{M_X^2 - M_{V_1}^2 - M_{V_2}^2}{2M_{V_1} M_{V_2}}$$

- For the SM Higgs,  $a_1 = 1$

# X → VV Amplitude for Spin-2

- General amplitude in terms of both field strength tensor and polarization vectors

$$\begin{array}{l}
 \begin{array}{l} 2^+ \text{ } CP \\ 2^- \text{ } \overline{CP} \end{array} \\
 \begin{array}{l} 2^+ \text{ } \overline{CP} \\ 2^- \text{ } CP \end{array}
 \end{array}
 A = \frac{e_1^{*\mu} e_2^{*\nu}}{\Lambda} \left[ c_1 t_{\mu\nu}(q_1 q_2) + c_2 g_{\mu\nu} t_{\alpha\beta}(q_1 - q_2)^\alpha (q_1 - q_2)^\beta \right. \\
 + \frac{c_3 t_{\alpha\beta}}{M_X^2} q_{2\mu} q_{1\nu} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta + 2c_4 (t_{\mu\alpha} q_{1\nu} q_2^\alpha + t_{\nu\alpha} q_{2\mu} q_1^\alpha) \\
 + \frac{c_5 t_{\alpha\beta}}{M_X^2} (q_1 - q_2)^\alpha (q_1 - q_2)^\beta \epsilon_{\mu\nu\rho\sigma} q_1^\rho q_2^\sigma + c_6 t^{\alpha\beta} (q_1 - q_2)_\beta \epsilon_{\mu\nu\alpha\rho} q^\rho \\
 \left. + \frac{c_7 t^{\alpha\beta}}{M_X^2} (q_1 - q_2)_\beta (\epsilon_{\alpha\mu\rho\sigma} q^\rho (q_1 - q_2)^\sigma q_\nu + \epsilon_{\alpha\nu\rho\sigma} q^\rho (q_1 - q_2)^\sigma q_\mu) \right]$$

- Similarly we can write down helicity amplitudes to connect with the experimental angular analysis

$$\begin{aligned}
 A_{00} &= \frac{M_X^4}{M_V^2 \sqrt{6} \Lambda} \left[ (1 + \beta^2) \left( \frac{c_1}{8} - \frac{c_2}{2} \beta^2 \right) - \beta^2 \left( \frac{c_3}{2} \beta^2 - c_4 \right) \right] \\
 A_{\pm\pm} &= \frac{M_X^2}{\sqrt{6} \Lambda} \left[ \frac{c_1}{4} (1 + \beta^2) + 2c_2 \beta^2 \pm i\beta (c_5 \beta^2 - 2c_6) \right] \\
 A_{\pm 0} \equiv A_{0\pm} &= \frac{M_X^3}{M_V \sqrt{2} \Lambda} \left[ \frac{c_1}{8} (1 + \beta^2) + \frac{c_4}{2} \beta^2 \mp i\beta \frac{(c_6 + c_7 \beta^2)}{2} \right] \\
 A_{+-} \equiv A_{-+} &= \frac{M_X^2}{4\Lambda} c_1 (1 + \beta^2)
 \end{aligned}$$

- Examples include Z', KK gluons, RS graviton, etc.
  - For the RS graviton we consider the minimal coupling case where  $g_1 = g_5 = 1$

# Angular Analysis

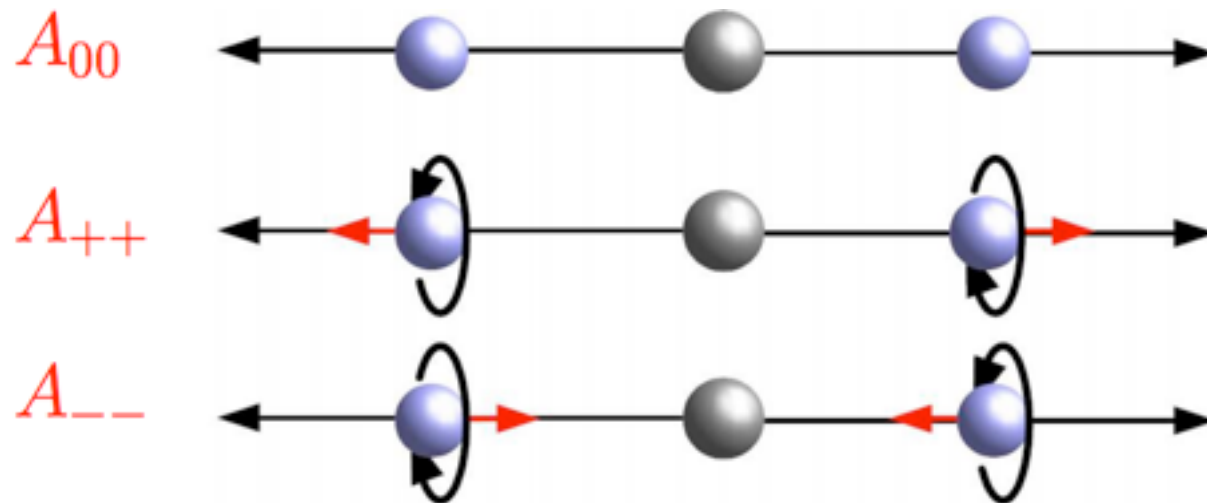
- The helicity amplitudes can be measured from angular analysis

$$d\sigma \propto \sum_{\chi, \mu, \tau} \left| \sum_{\lambda, m} A_{ab}(\{\Omega\}) \right|^2$$

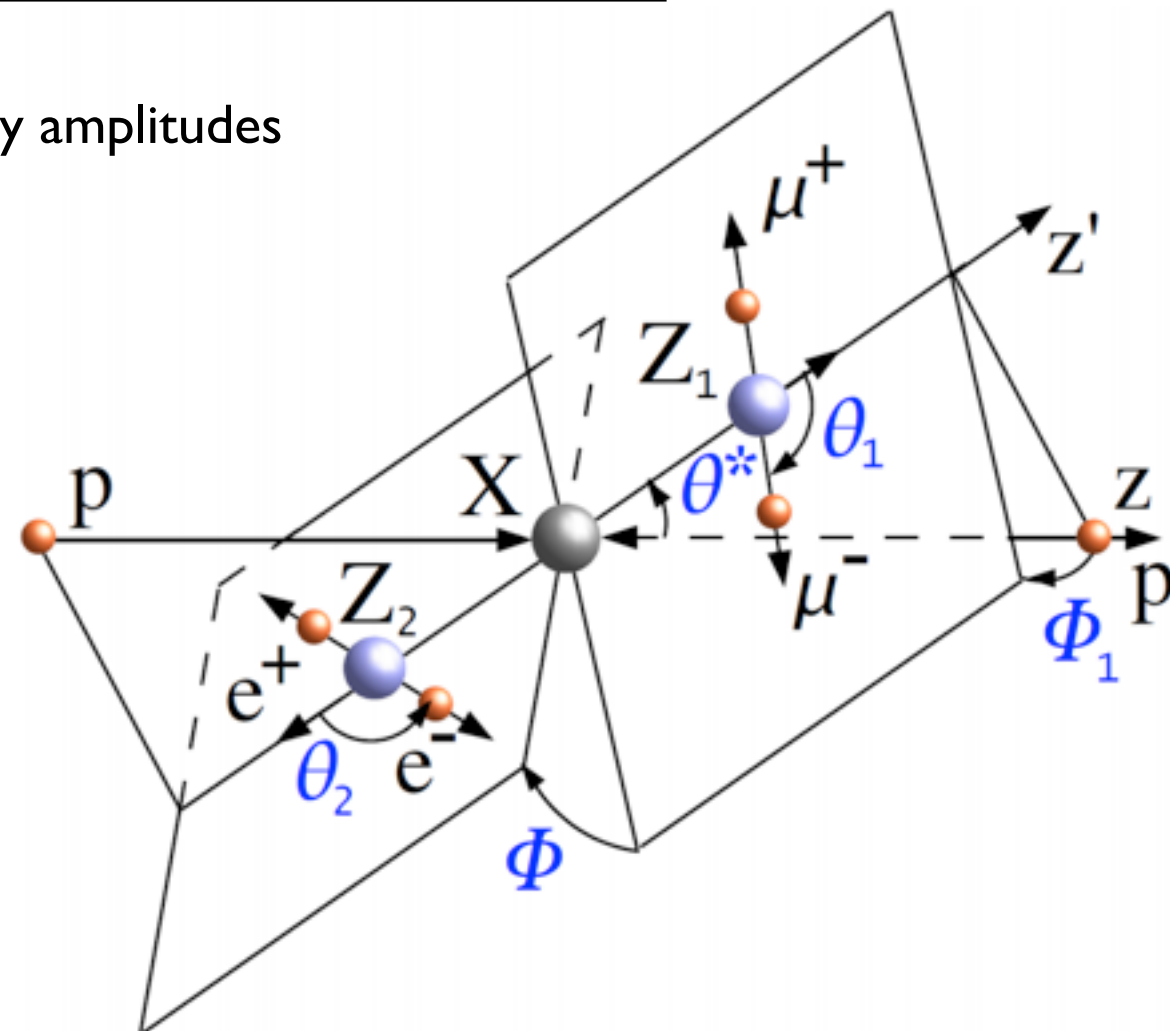
$$A_{ab} \propto D_{\chi_1 - \chi_2, m}^{J*}(\Omega^*) B_{\chi_1 \chi_2} \times D_{m, \lambda_1 - \lambda_2}^{J*}(\Omega) A_{\lambda_1 \lambda_2}$$

$$\times D_{\lambda_1, \mu_1 - \mu_2}^{S_1*}(\Omega_1) T(\mu_1, \mu_2) \times D_{\lambda_2, \tau_1 - \tau_2}^{S_2*}(\Omega_2) W(\tau_1, \tau_2)$$

- For example, a Higgs like spin 0 resonance has 3 helicity amplitudes



Need only 5 angles  $\{\theta_1, \theta_2, \theta^*, \Phi, \Phi_1\}$  to fully describe the production/decay



- Detailed expressions for the spin 1 and spin 2 can be found in the reference [\*PhysRevD.81.075022\*](#)

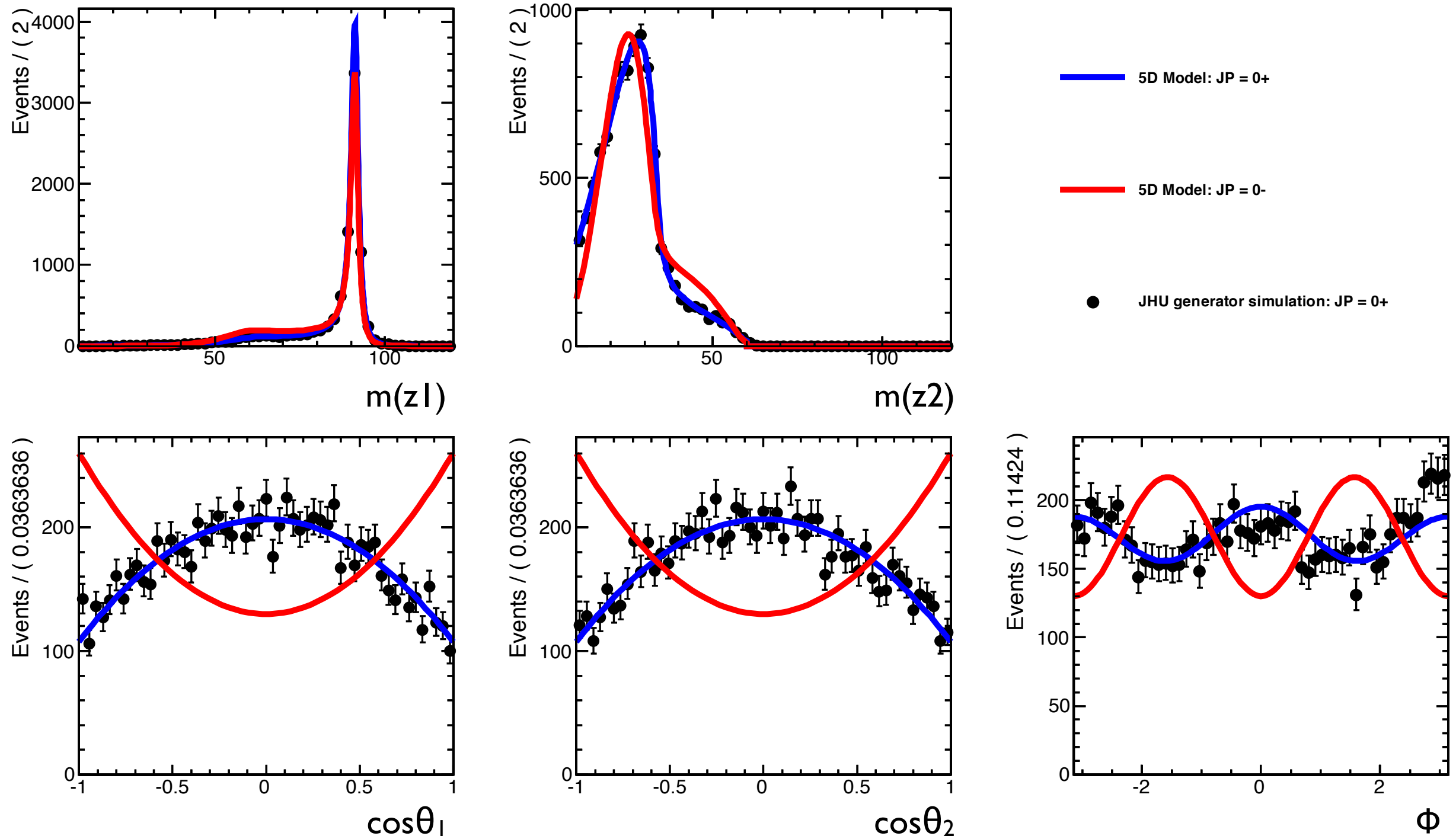
# The JHU Generator

- A MC program developed to simulate production and decay of  $X \rightarrow VV$  with  $X$  spin  $\leq 2$ 
  - $X \rightarrow ZZ \rightarrow 4l, 2l2\tau, 2l2\nu, 2l2q$
  - $X \rightarrow WW \rightarrow 2l2\nu, l\nu\tau\nu, l\nu qq$
  - $X \rightarrow \gamma\gamma$
- Includes all spin correlations and all possible couplings
  - Inputs are general dimensionless couplings - calculates matrix elements
- For the production of  $X$ , both  $gg$  and  $qq$  are considered
- Output in LHE format; e.g. can interface to Pythia for hadronization
- All code publicly available: [www.pha.jhu.edu/spin](http://www.pha.jhu.edu/spin)



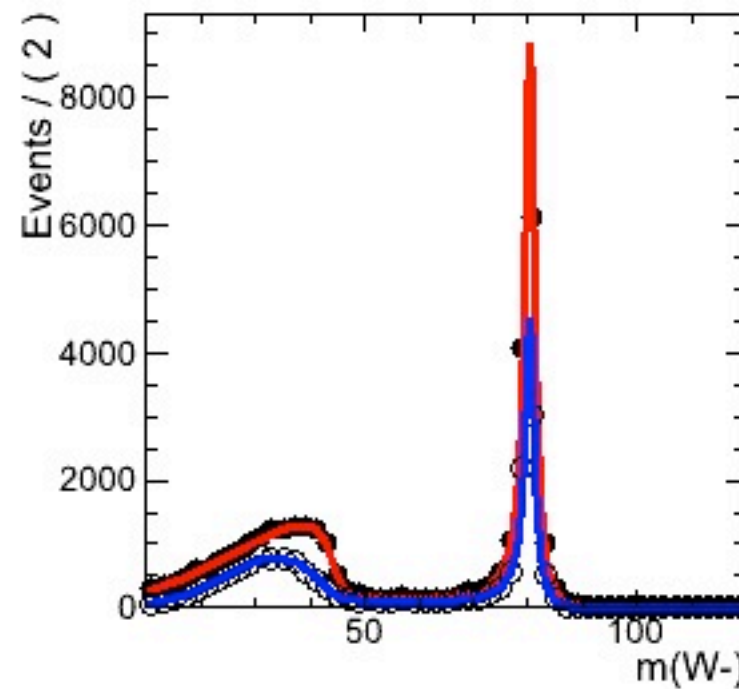
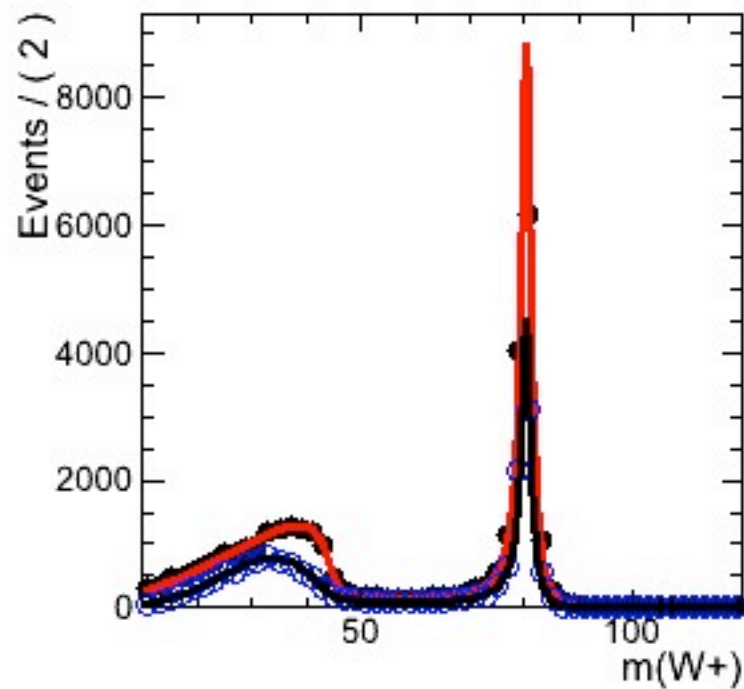
# Generator Validation ( $X \rightarrow ZZ$ Spin 0)

- In this test  $m_X = 125$  GeV



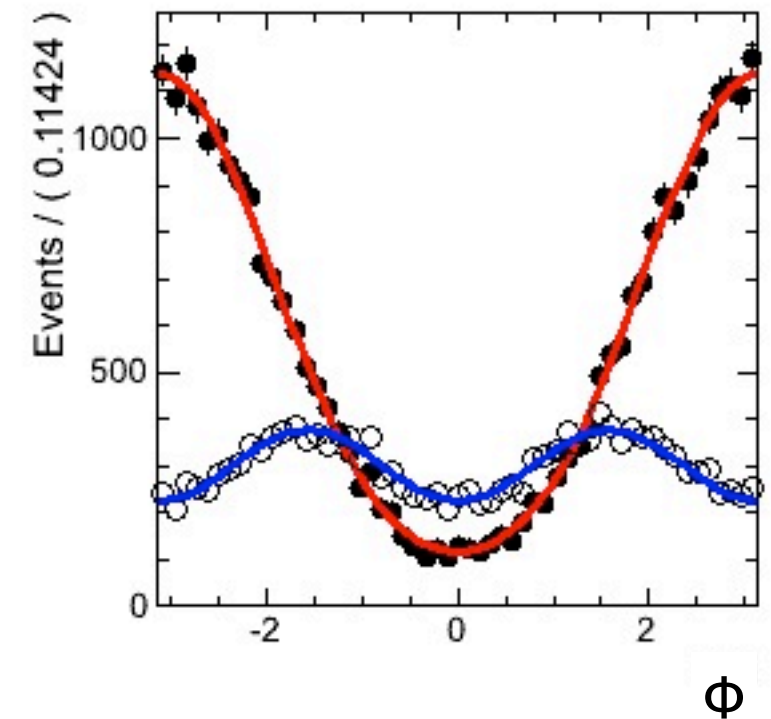
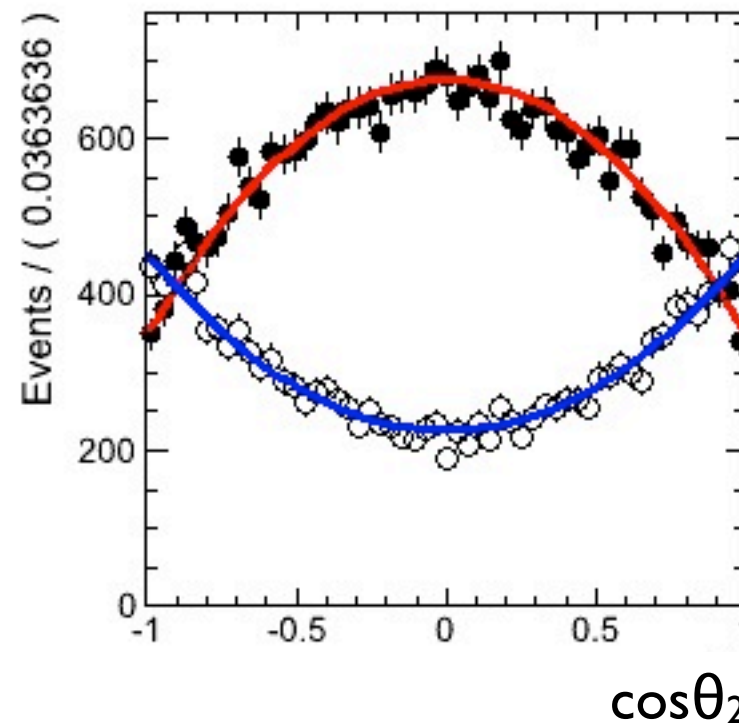
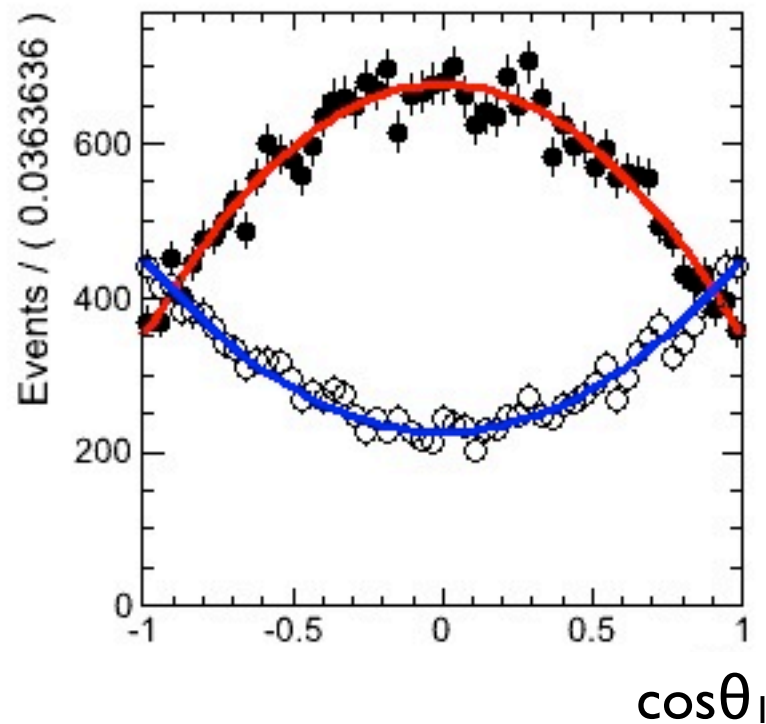
# Generator Validation ( $X \rightarrow WW$ Spin 0)

- In this test  $m_X = 125$  GeV



—●—  $X \rightarrow WW: JP = 0^+$

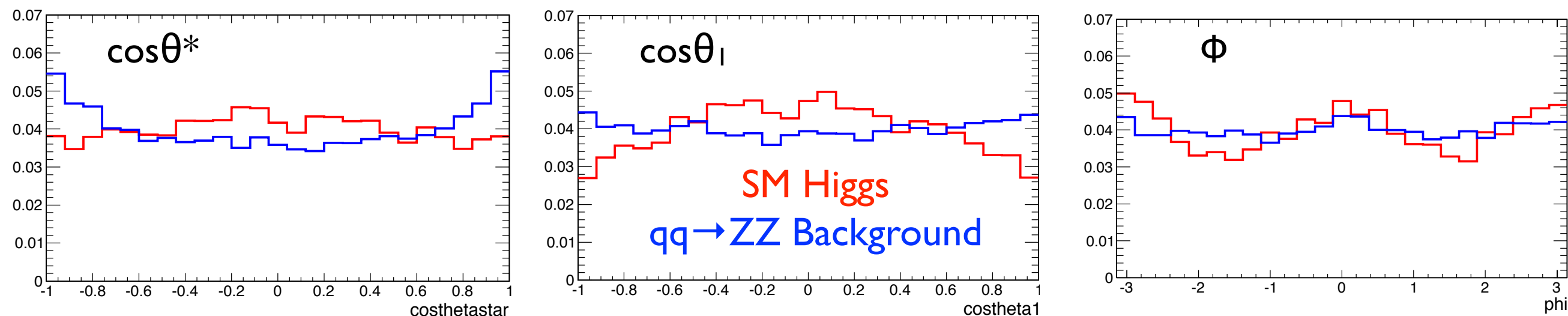
—○—  $X \rightarrow WW: JP = 0^-$



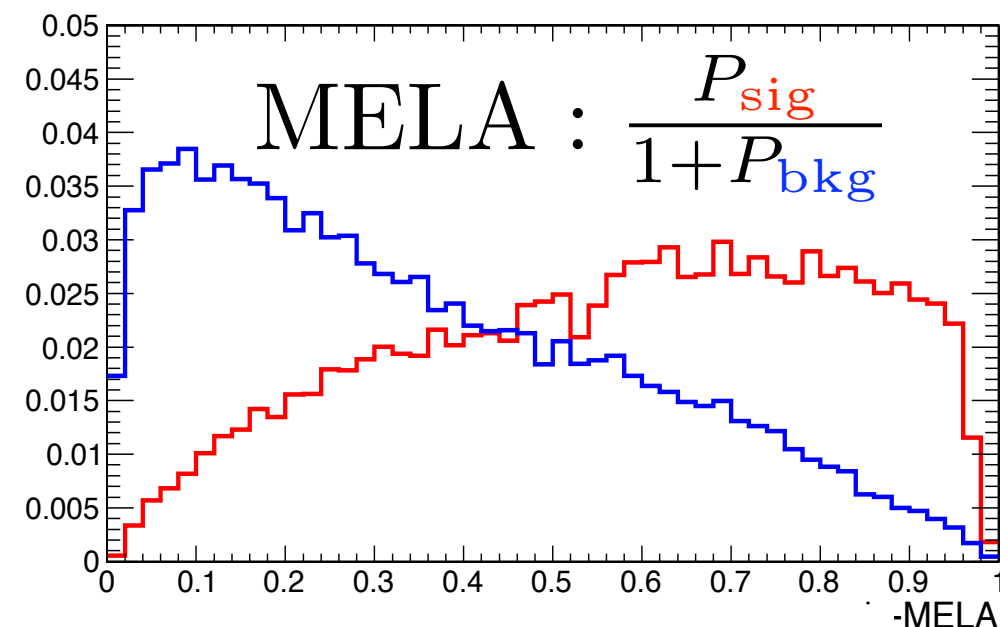
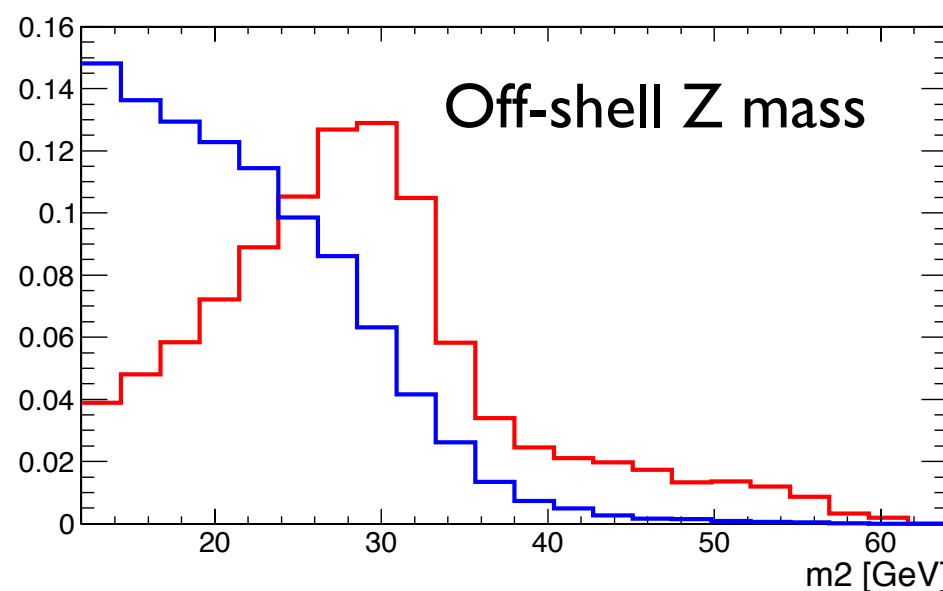
# The **M**atrix **E**lement **L**ikelihood **A**nalysis in $ZZ(4l)$ channel

# MELA in $H \rightarrow ZZ \rightarrow 4l$ Search

- The angular variables can be used to distinguish between Higgs signal and SM Background



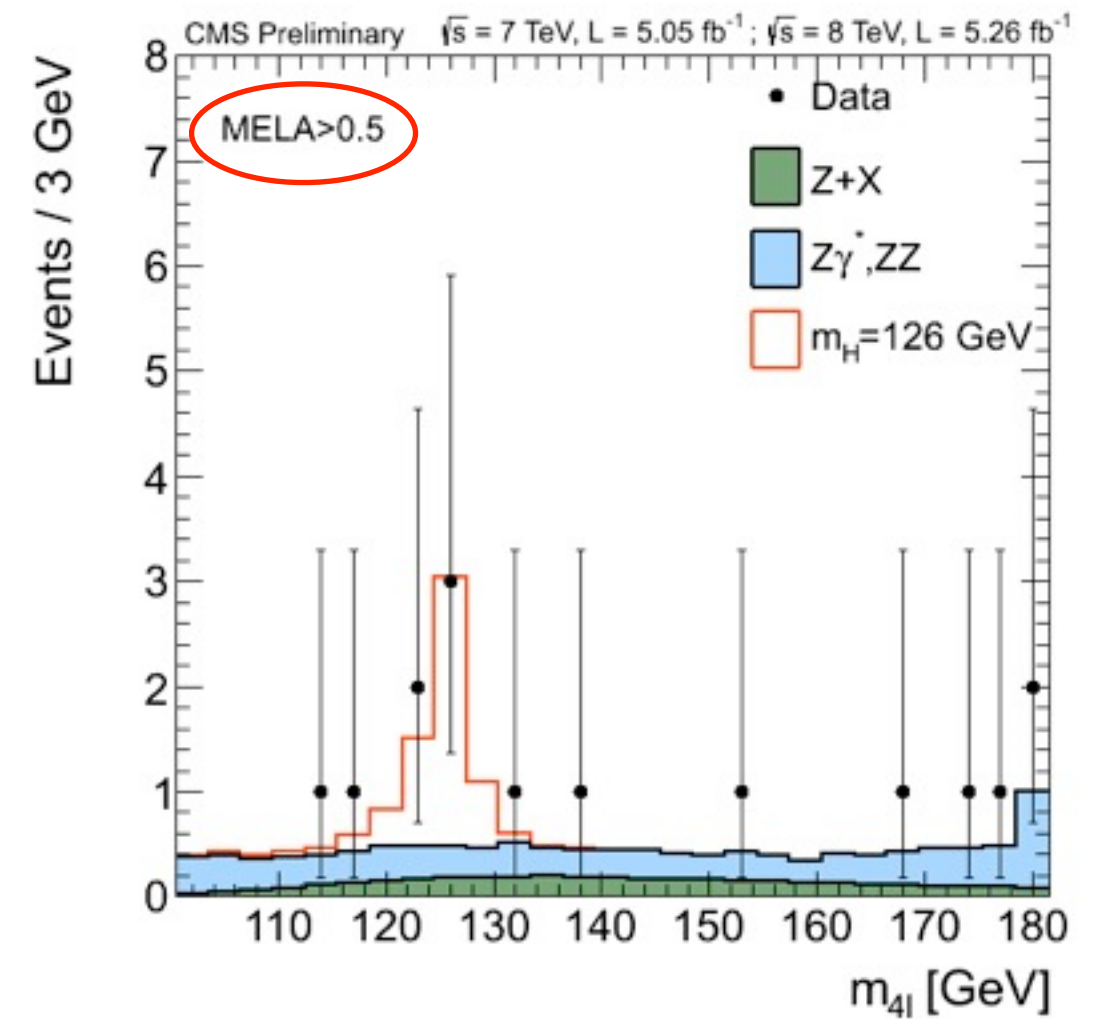
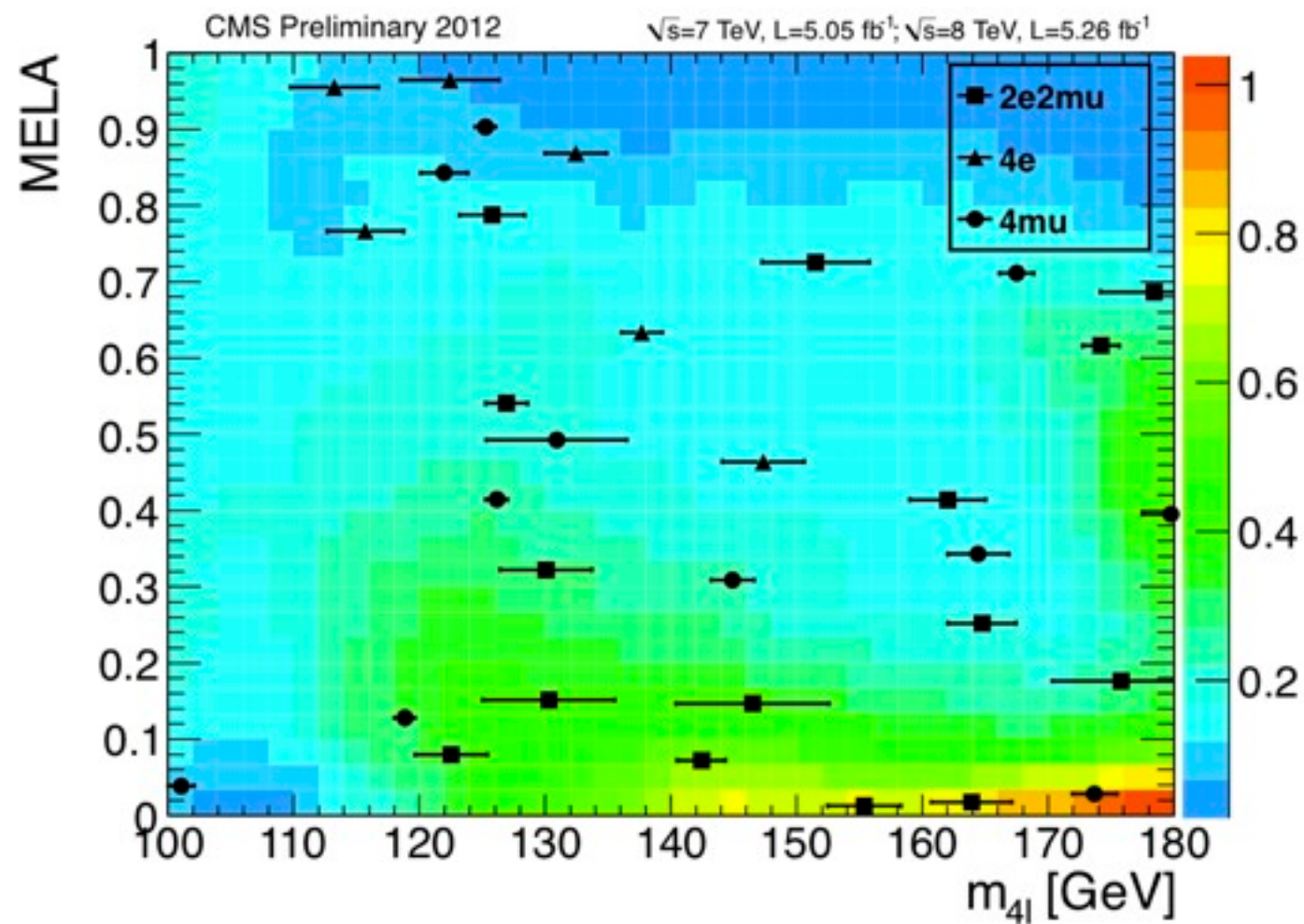
- We can build analytical likelihoods based on 5 angular variables and 2 on(off)-shell Zmass for sig/bkgd processes and construct a single distinguishing variable “MELA”



- A toy study using CMS-like analysis shows that using MELA increases the search sensitivity by  $\sim 15\text{-}30\%$  compared to using only the  $4l$  mass

Reference: [arXiv:1108.2274](https://arxiv.org/abs/1108.2274) [arXiv:1001.3396](https://arxiv.org/abs/1001.3396)

- The CMS HZZ(4l) search uses a 2D template based on  $[m(4l), \text{MELA}]$



# Spin/Parity Hypothesis Separations

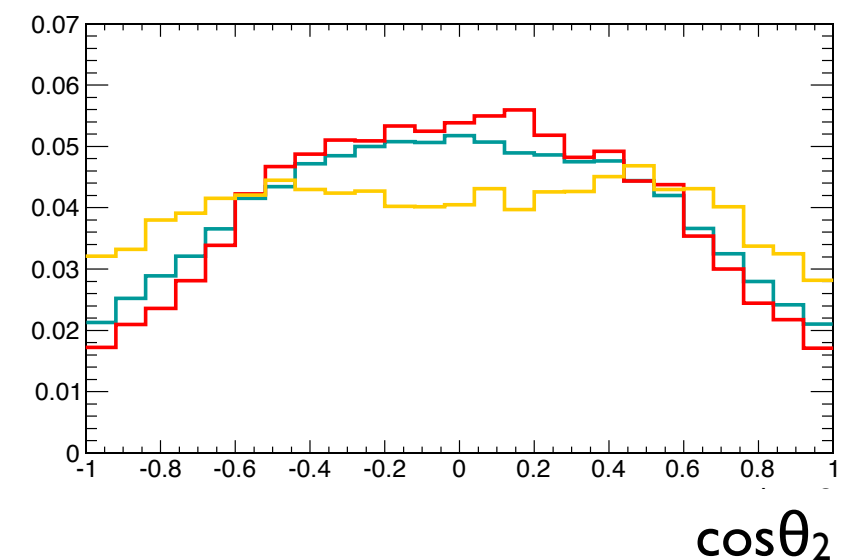
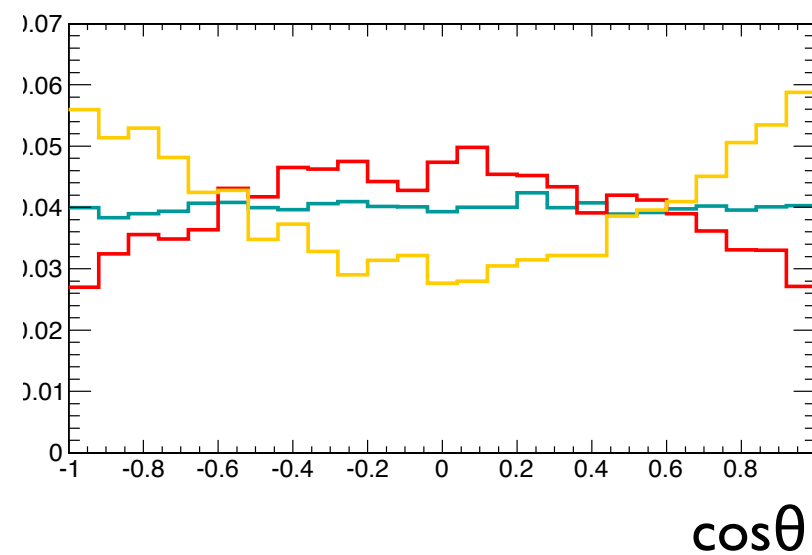
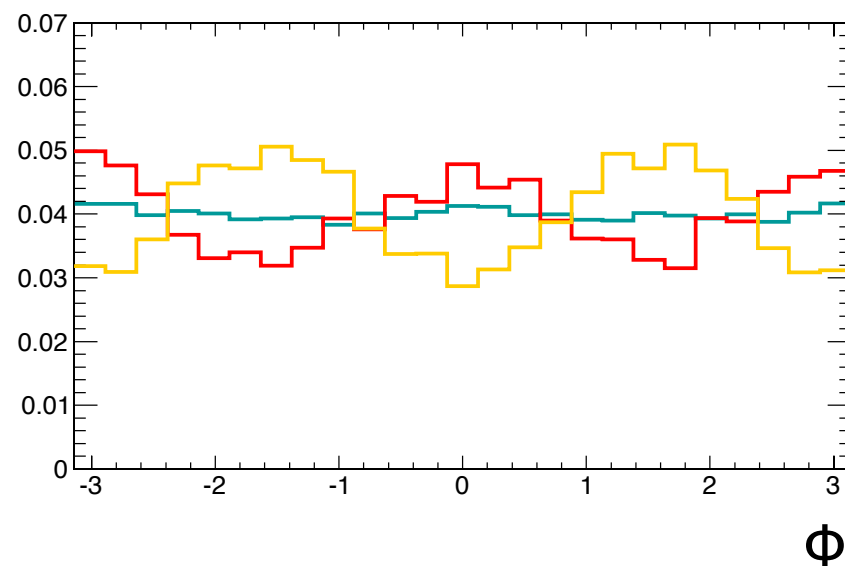
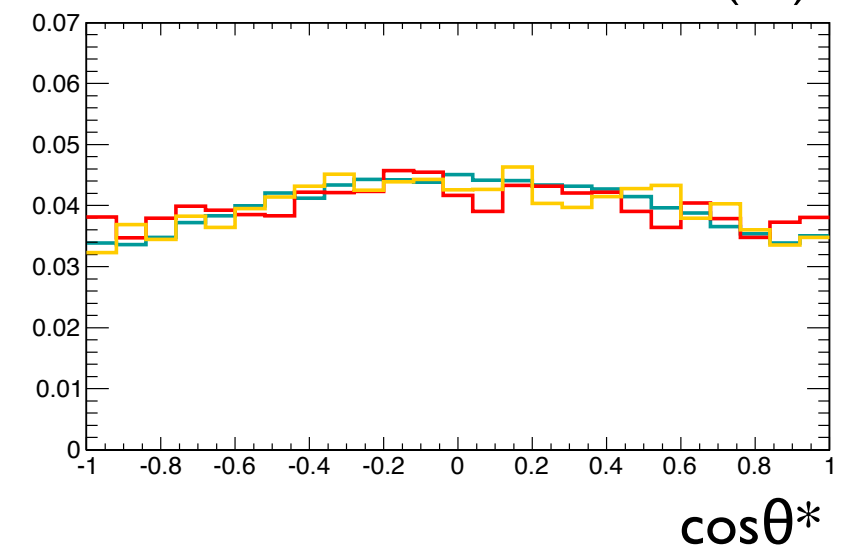
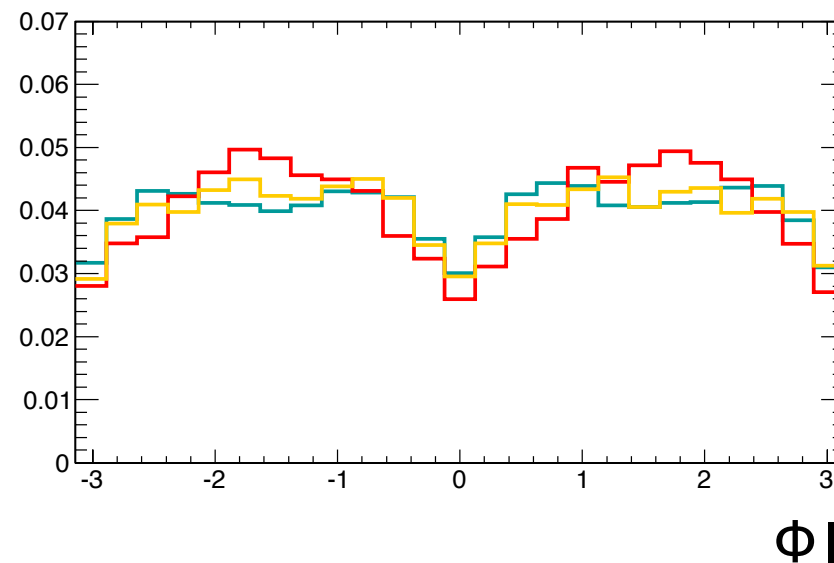
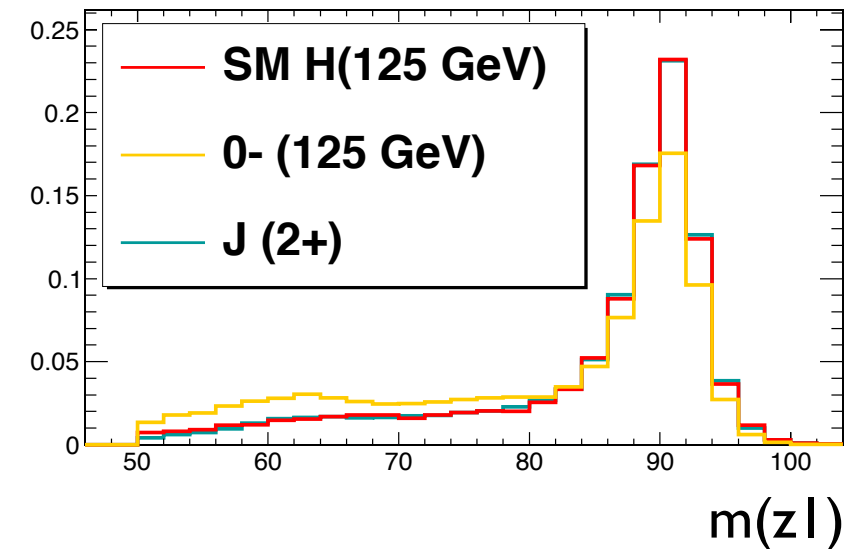
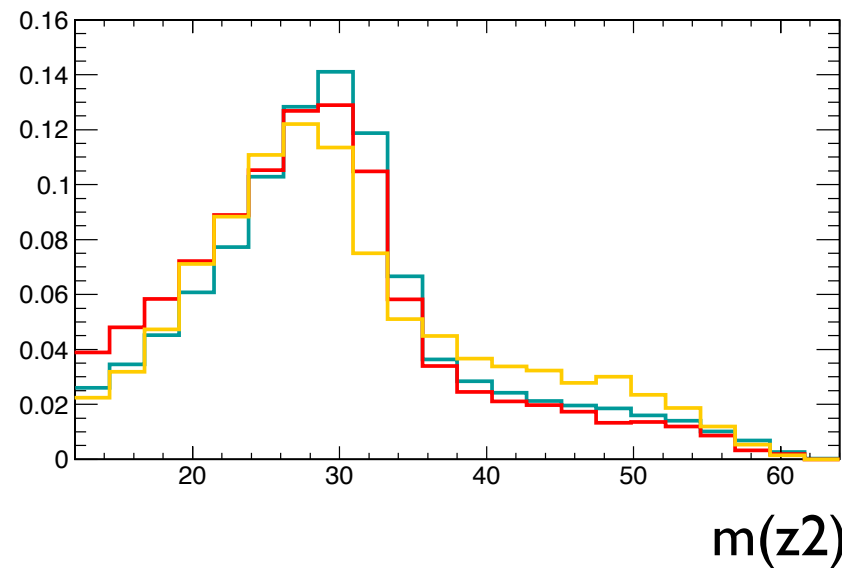
$$X \rightarrow ZZ \rightarrow 4l$$

# Kinematics for different spin/parity

- The full 7-D variables

- Good separations between  $0^+$  and  $0^-$

Pseudo-data with CMS like detector resolutions



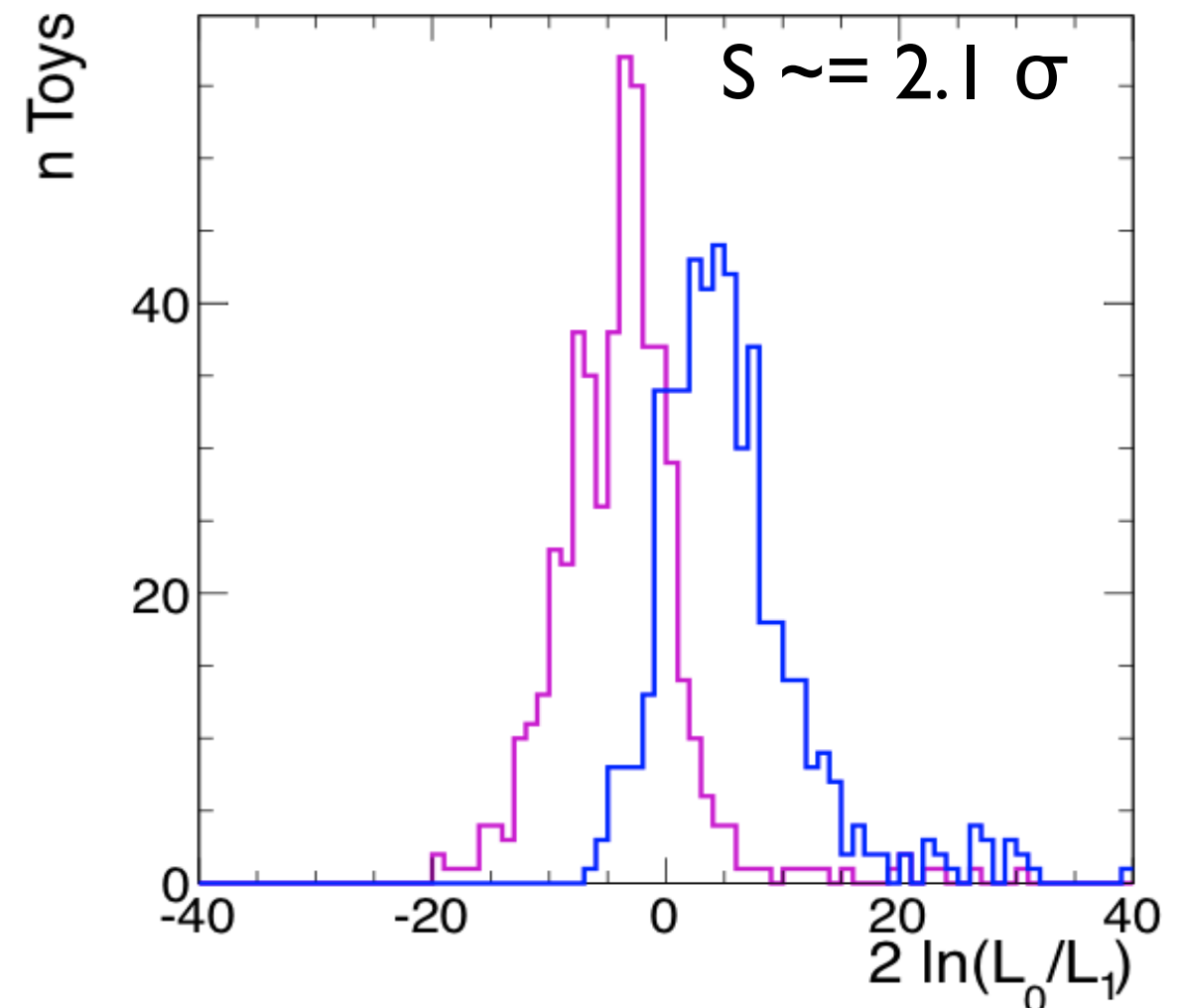
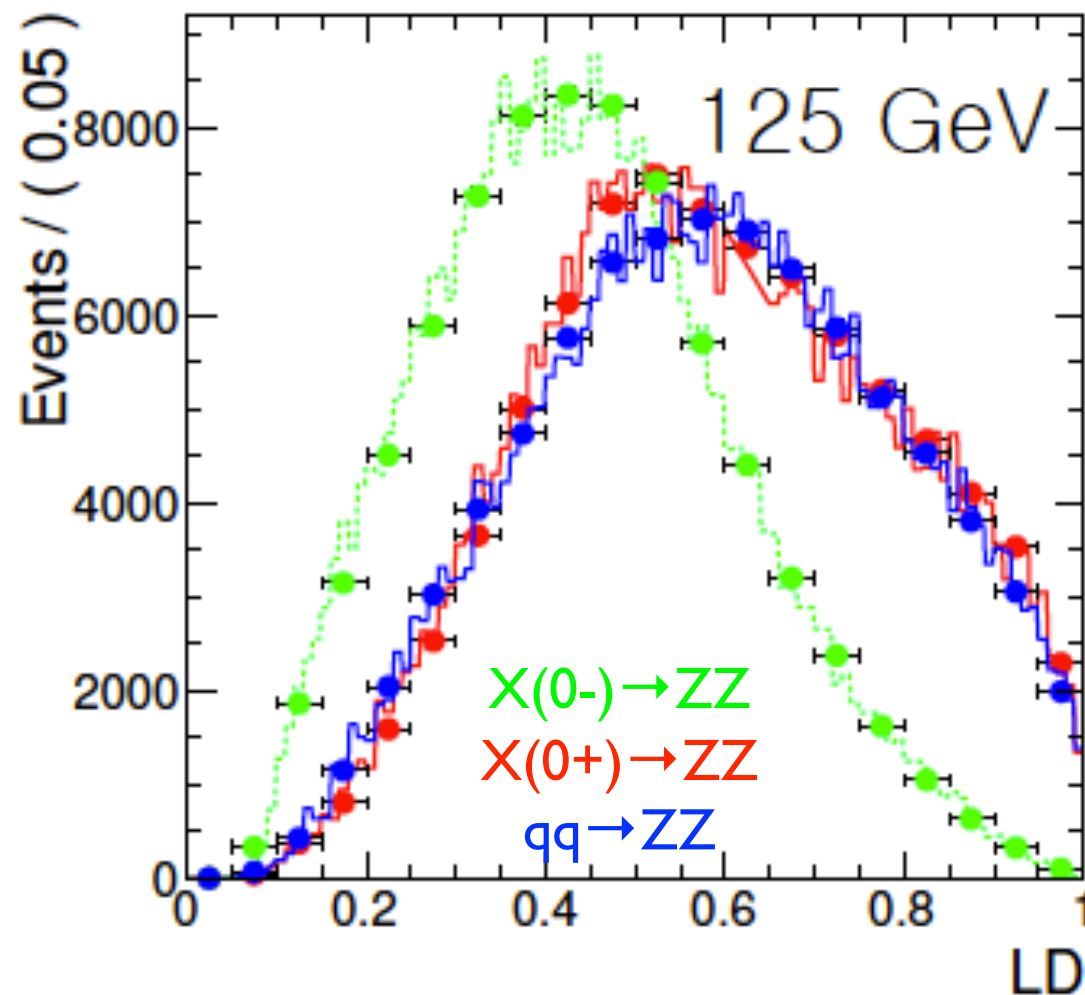


# PseudoMELA (0+ vs 0-)

- Construct similar likelihood that distinguishes 0- vs 0+

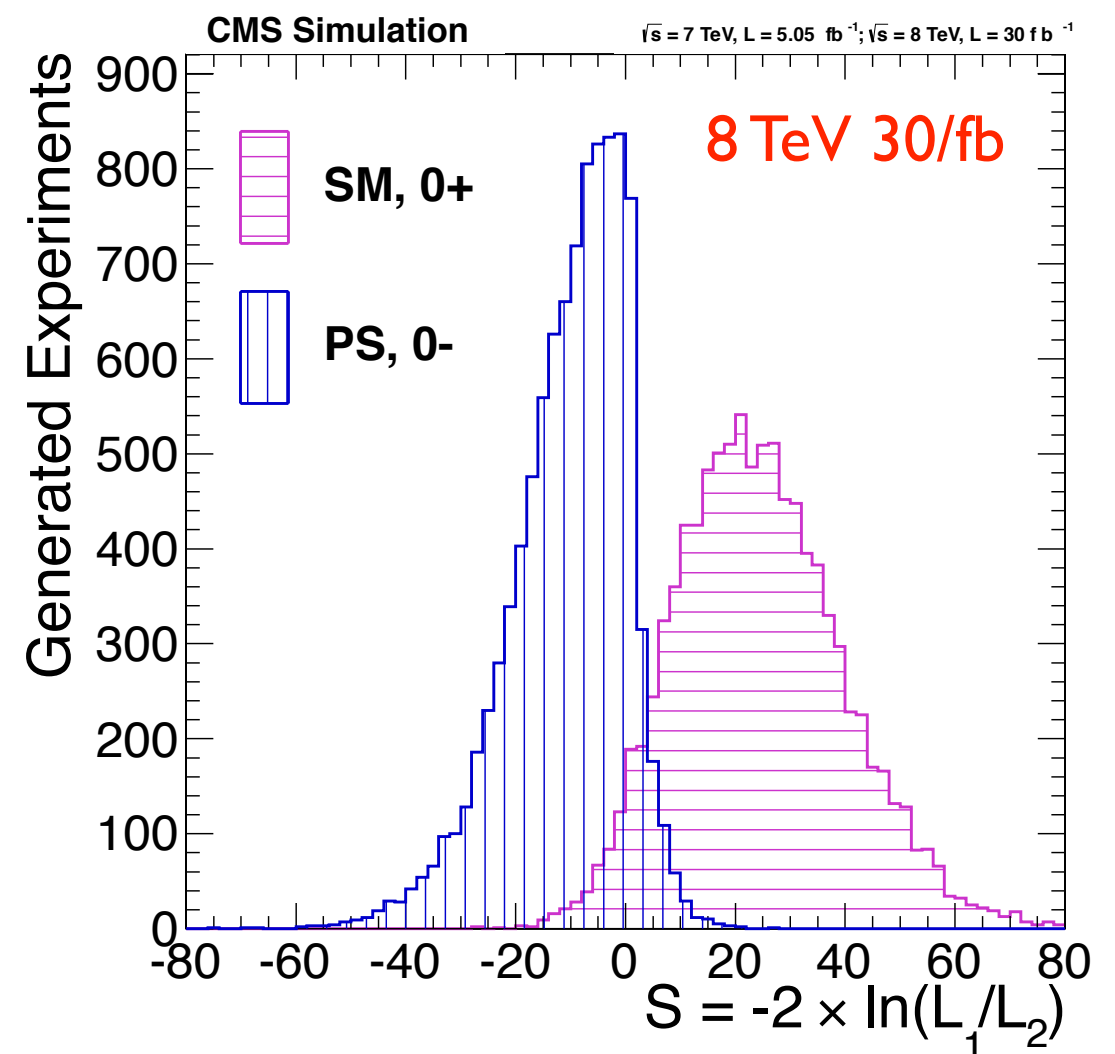
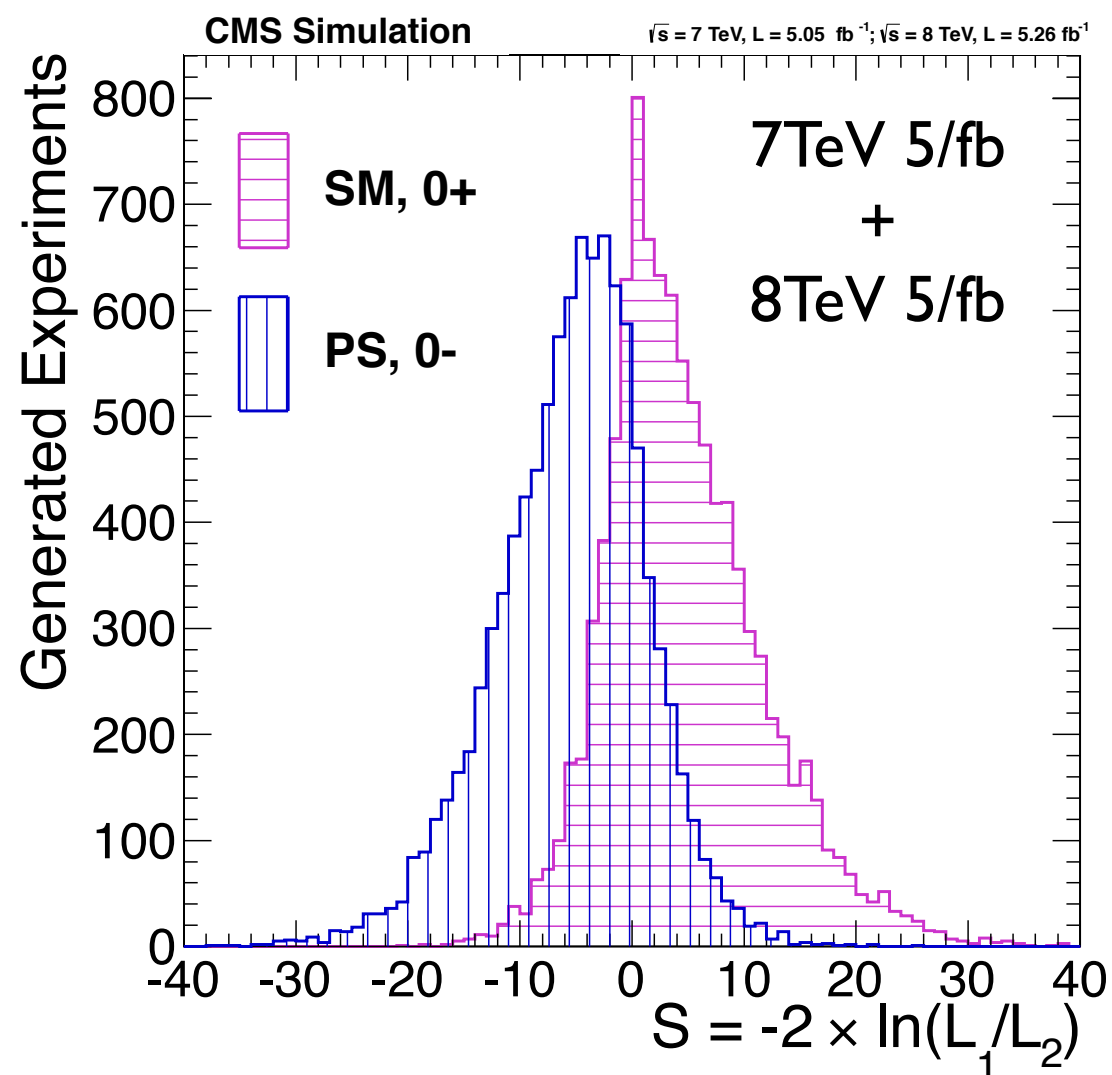
$$\text{PseudoMELA: } \frac{P_{0+}}{P_{0+} + P_{0-}}$$

- Using pseudoMELA we expect  $\sim 2\sigma$  separation between 0+ and 0- projected for 20/fb
  - Assume the 0+ and 0- the same signal strength as the SM Higgs
  - For 20/fb, we expect the separation significance  $\sim 2.1\sigma$





- PseudoMELA is fully implemented in CMS
  - **Current status:**  $1.6 \sigma$  expected separation using 5/fb 7 TeV + 5/fb 8 TeV data
  - **Projections for 30/fb at 8 TeV:**  $\sim 3 \sigma$  separation

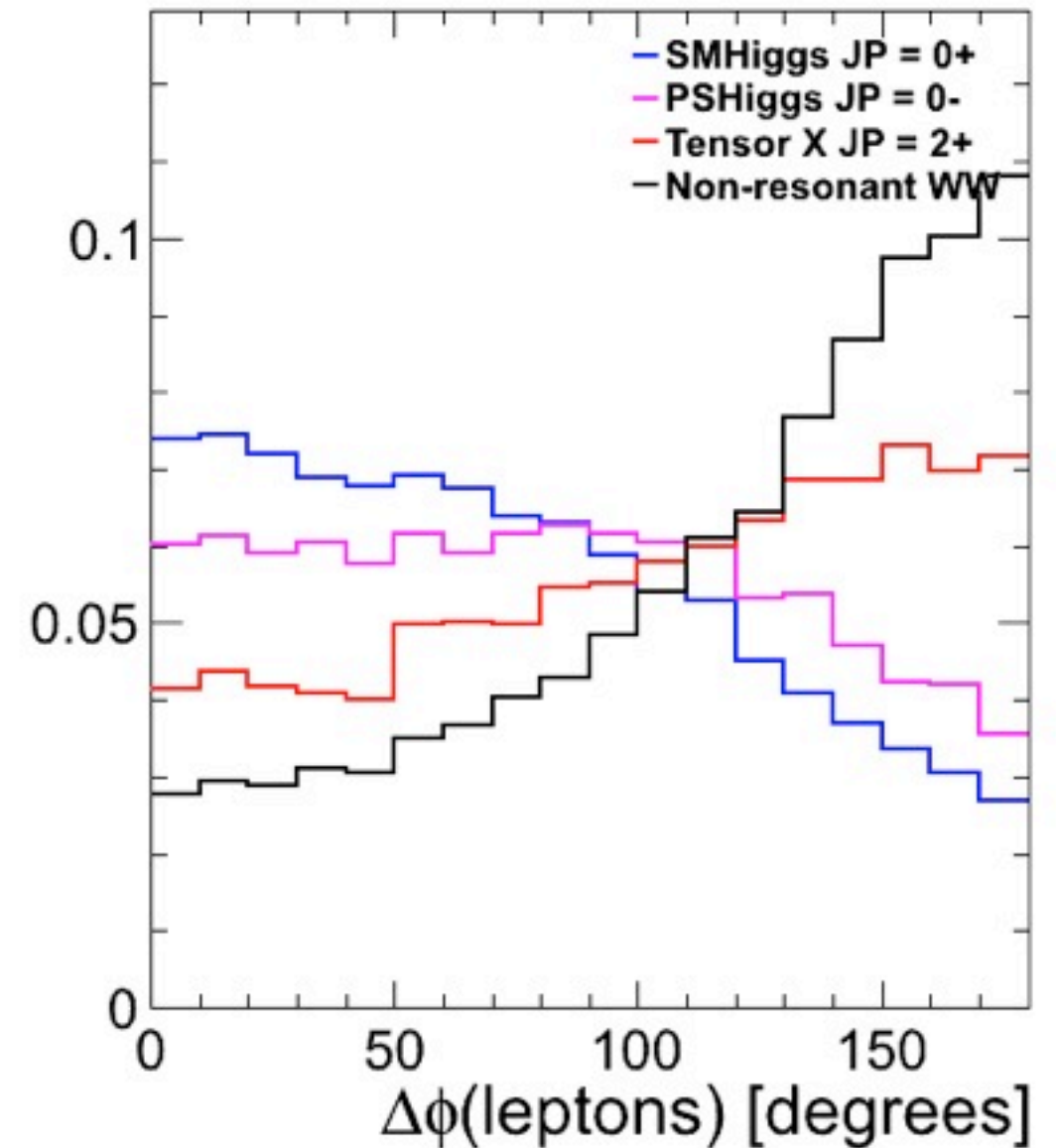


# Spin/Parity Hypothesis Separations

$$X \rightarrow WW \rightarrow (\ell\nu)(\ell\nu)$$

# The $X \rightarrow WW$ Analysis

- Due to the missing  $\nu$ s, the  $WW$  final state is not fully reconstructible
  - No reconstructed resonance mass
  - The full angular distributions are not available
- Experimental variables can still be used to distinguish different spin/parity
  - For instance the **opening angle between the two leptons** carry important message
  - See also J.Ellis et al. [\*arXiv:1202.6660\*](#)
- The CMS/ATLAS analyses are optimized for the scalar resonance
  - The selections may not be suitable for the hypothesis tests



For spin-2 we consider the minimal coupling model

# Explore more kinematic observables

- Select dilepton events with  $p_T[20,10]$  and within  $|\eta| < 2.5$

- Plots are normalized by area for the shape comparison

- Arrows indicate the shape-based analysis cuts in CMS

- For the  $XWW$  analysis

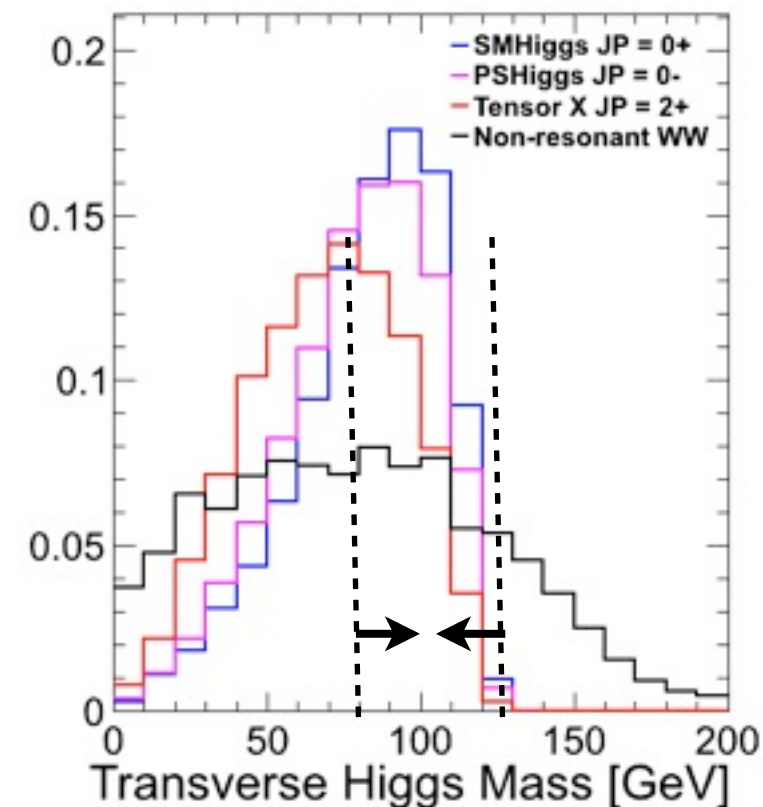
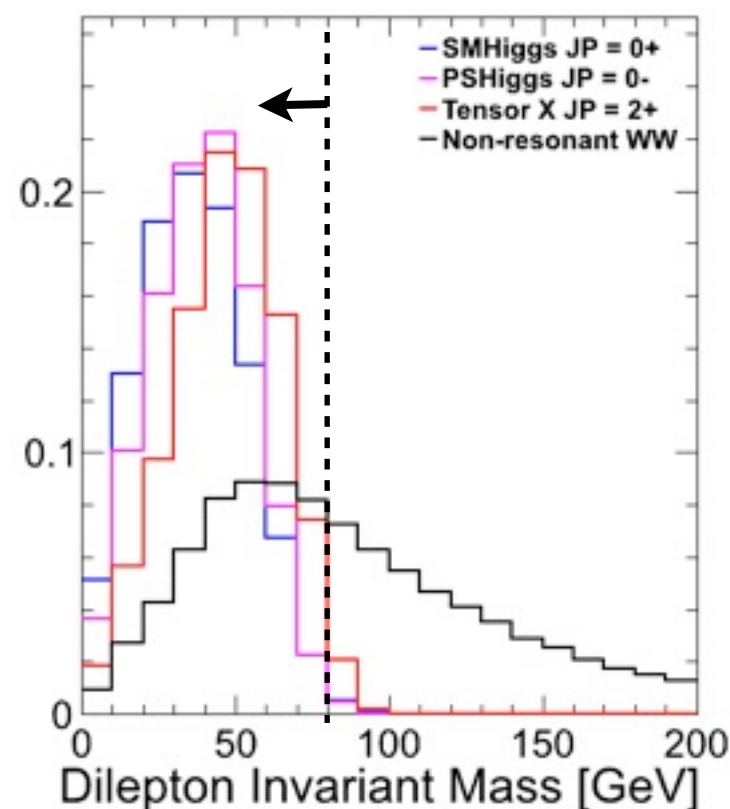
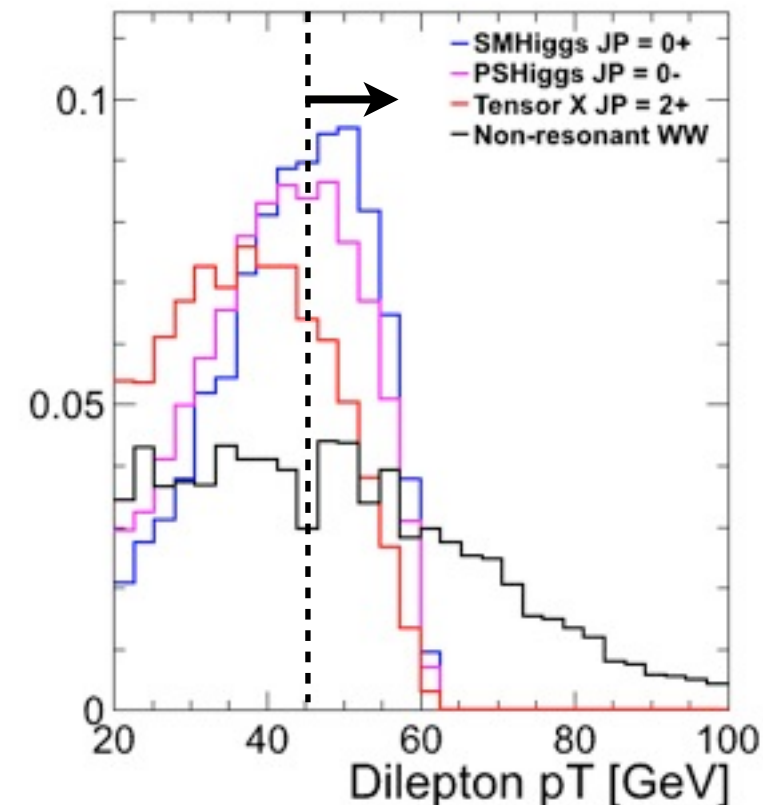
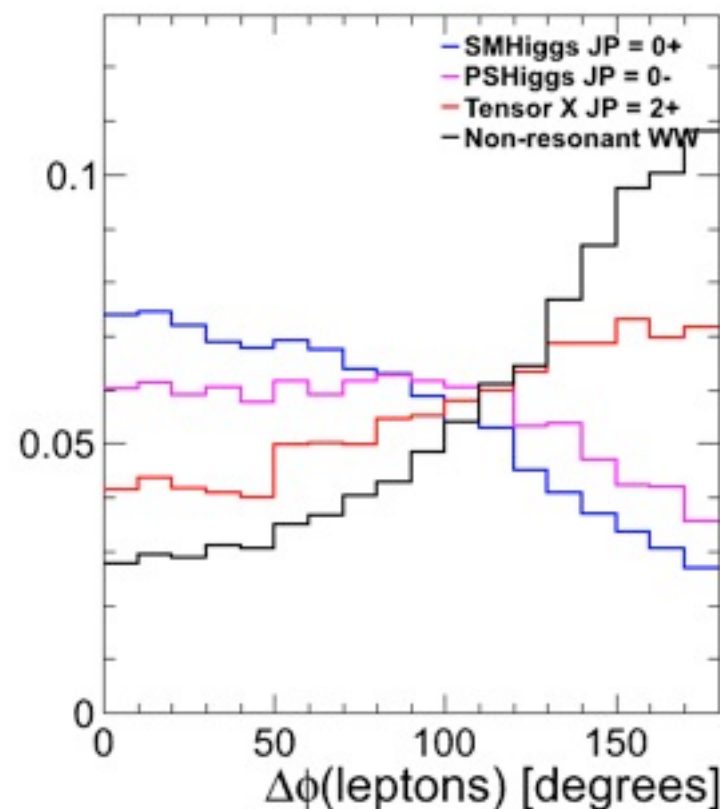
- Use only the purest channel,  $e\mu$  events with 0 jets

- Relax cuts on dilepton  $p_T$  and MET and  $m_T$

- For 10/fb at 8 TeV, we expect

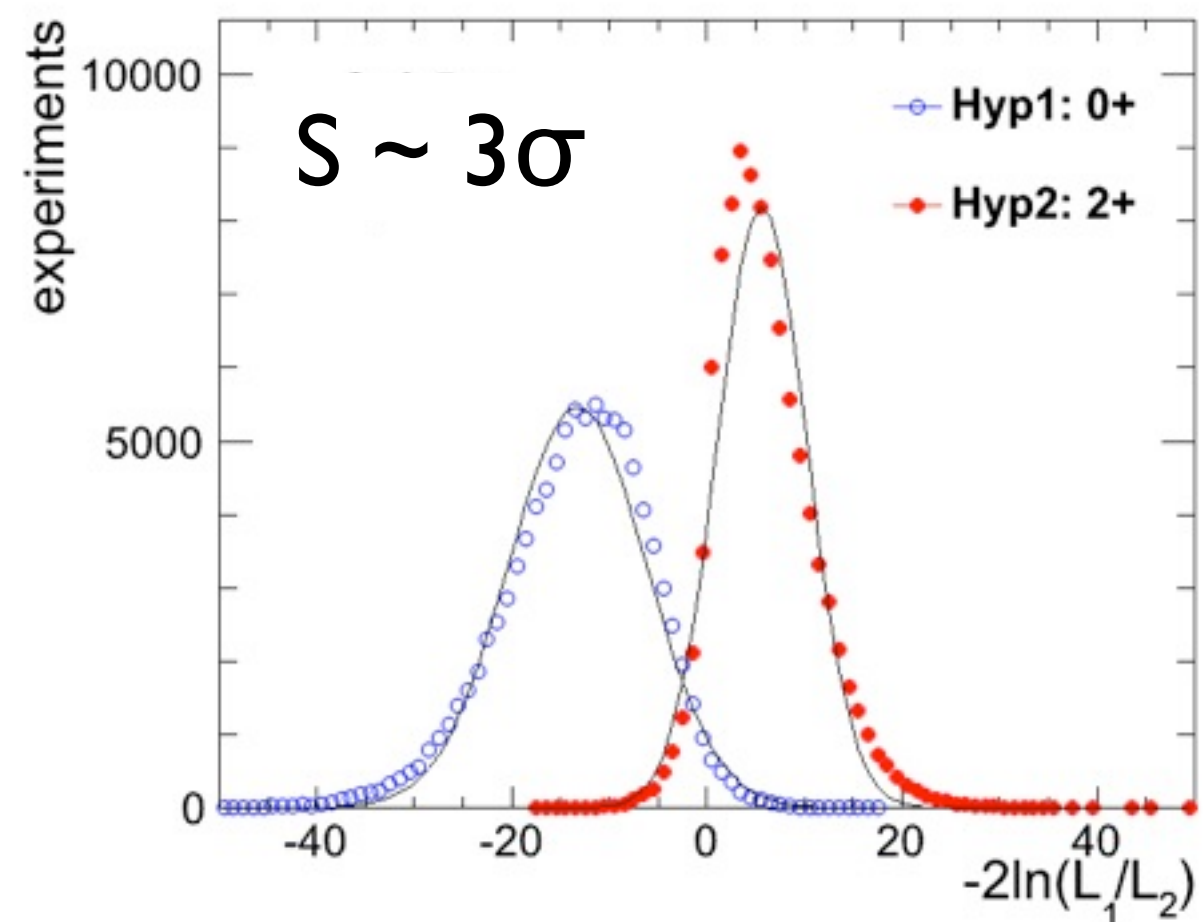
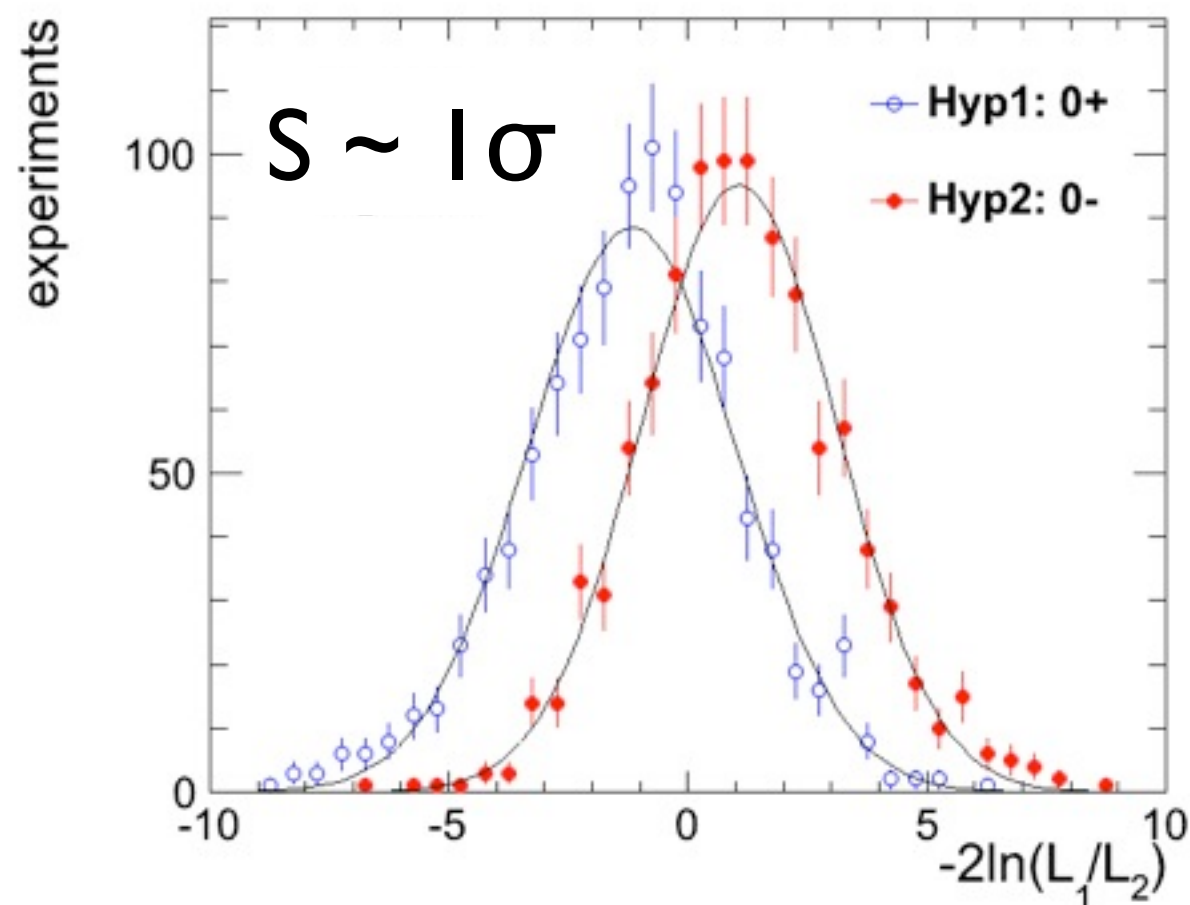
- 25 signal
- 250 background

- Assume it is all  $WW$



# Hypothesis Separation Results

- Consider an **ideal/optimistic scenario**
  - Ignore the systematics and assume the background is all WW
- Use the 2D template based on (mll, mT)
- For 10/fb we project  $\sim 1\sigma$  separation for  $0^+$  vs  $0^-$ , and  $\sim 3\sigma$  for  $0^+$  vs  $2^+$ 
  - The separation between  $0^+/2^+$  can reach  $\sim 5\sigma$  with  $\sim 30/\text{fb}$  data in this optimistic case
    - **Systematics and other bkgd will degrade the performance. By how much needs future studies.**



# Summary

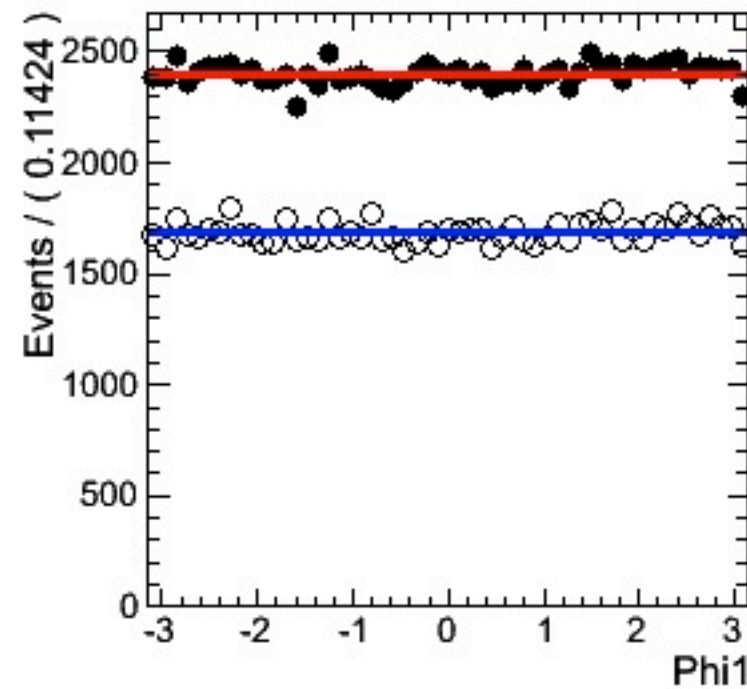
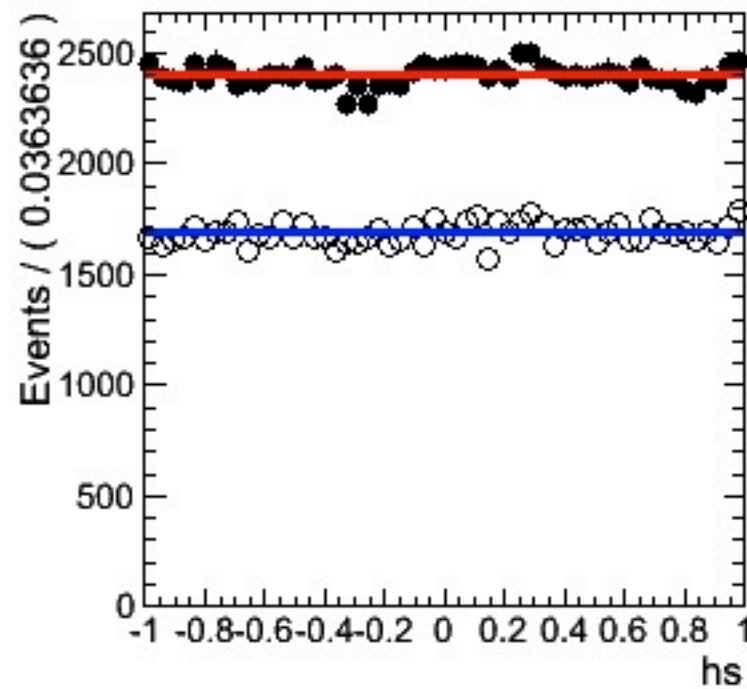
- An exciting “Higgs-like” resonance has been observed
  - Identifying the resonance’s spin and parity is crucial to pin down the nature of this resonance
- We reviewed the model-independent amplitude for  $X \rightarrow VV \rightarrow 4$  fermions interaction as well as a supporting MC generator as a baseline for spin/parity determinations
- We updated the MELO analysis used for both Higgs search and hypothesis separations
  - MELO is used in CMS HZZ(4l) analysis and shown improvement to the Higgs search sensitivity
  - A hypothesis separation based on MELO is also employed in CMS in the HZZ(4l) analysis
    - Expected  $0^+$  vs  $0^-$  separation at  $1.6 \sigma$  with current data, and  $\sim 3 \sigma$  for 30/fb data
- We introduced similar analysis for the  $X \rightarrow WW \rightarrow (l\nu l\nu)$  channel
  - Using variables ( $m_{ll}$ ,  $m_T$ ) this channel has promising sensitivity of  $0^+$  and  $2m^+$  separations
  - With 30/fb data with ideal condition, we expect  $\sim 5\sigma$  separation
    - WARNING: consider only GEN quantities and ignore non-WW background or systematics
    - We look forward to a realistic analysis from LHC

# Backup slides



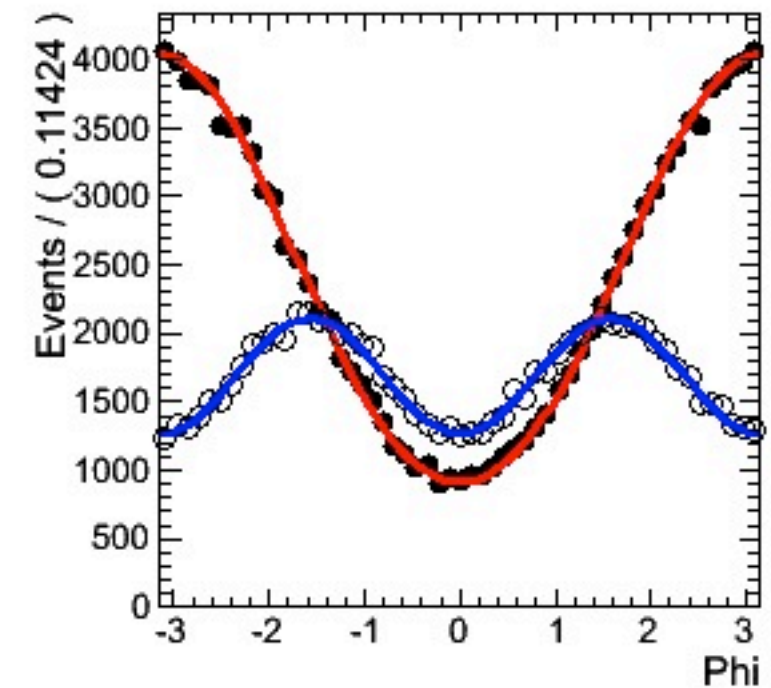
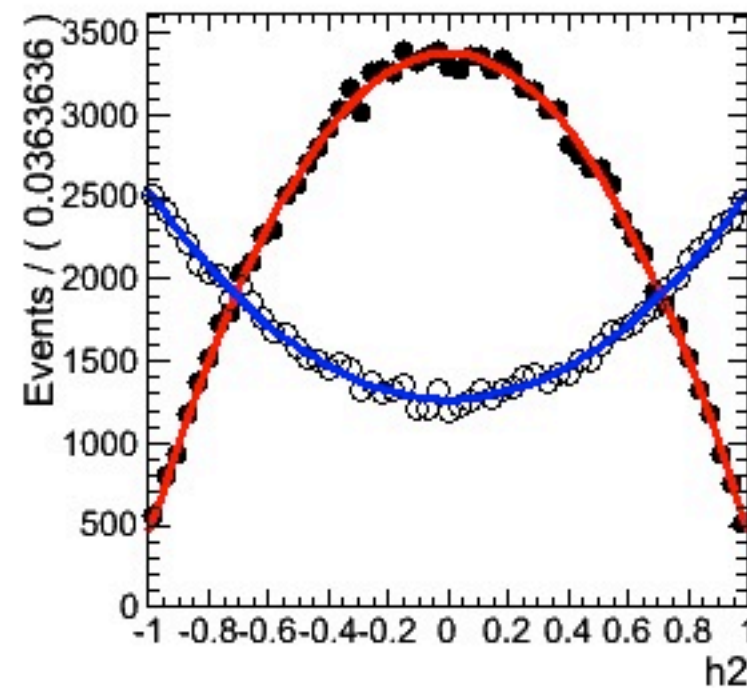
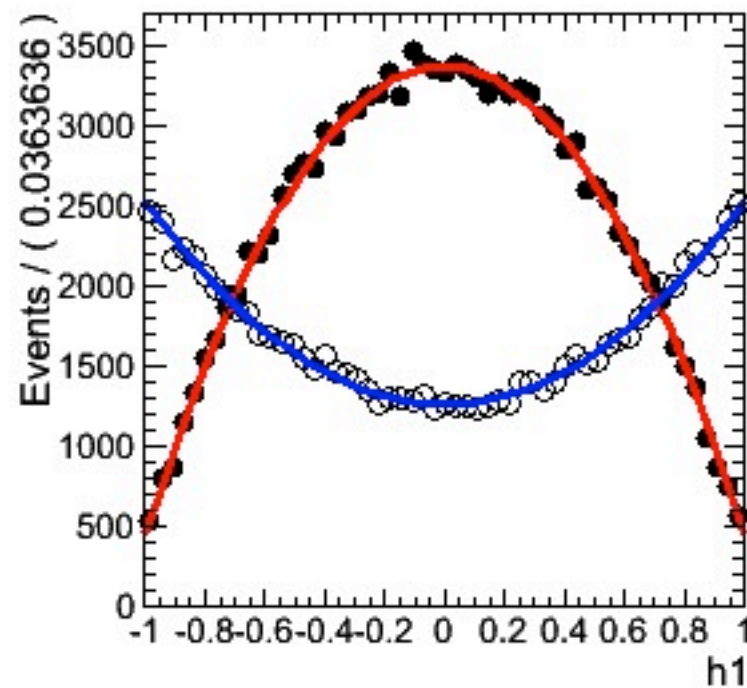
# Generator Validation ( $X \rightarrow WW$ Spin 0)

- In this test  $m_X = 250$  GeV



—●—  $X \rightarrow WW$  JP = 0+

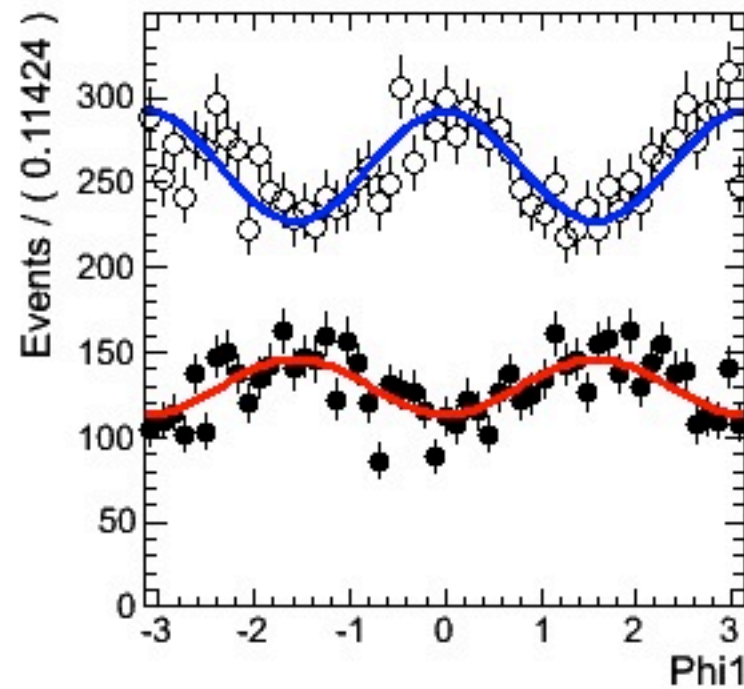
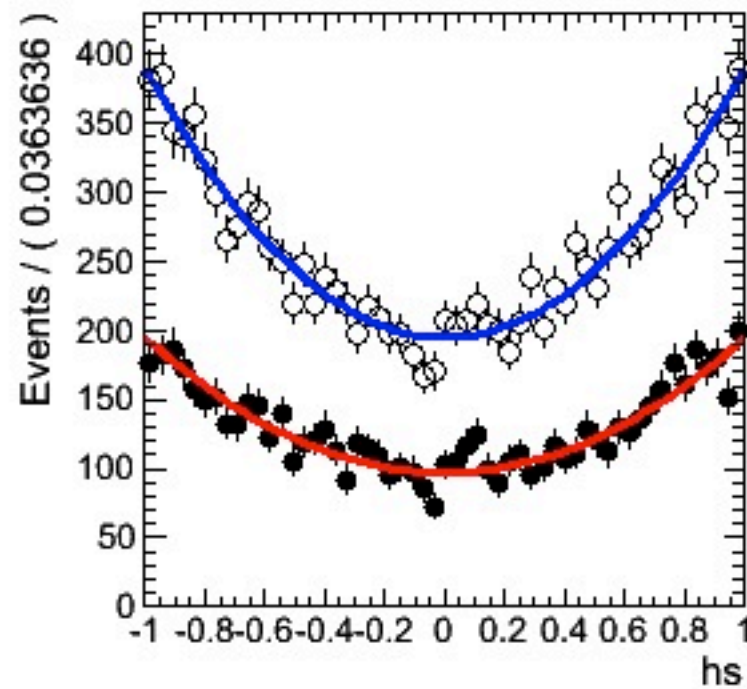
—○—  $X \rightarrow WW$  JP = 0-





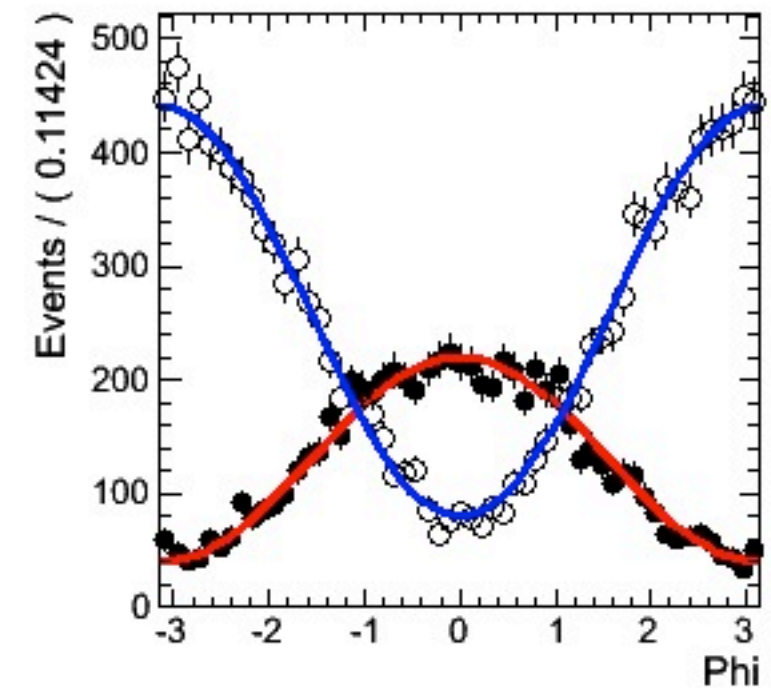
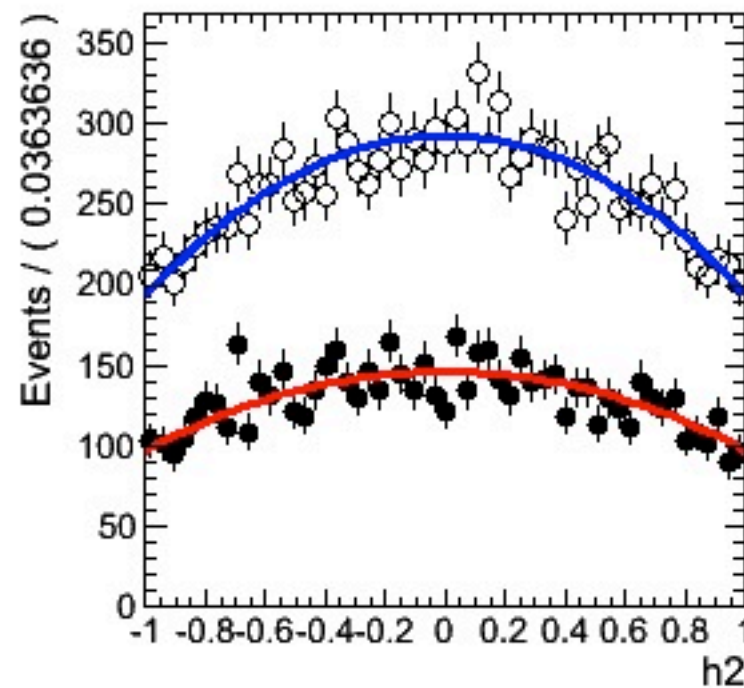
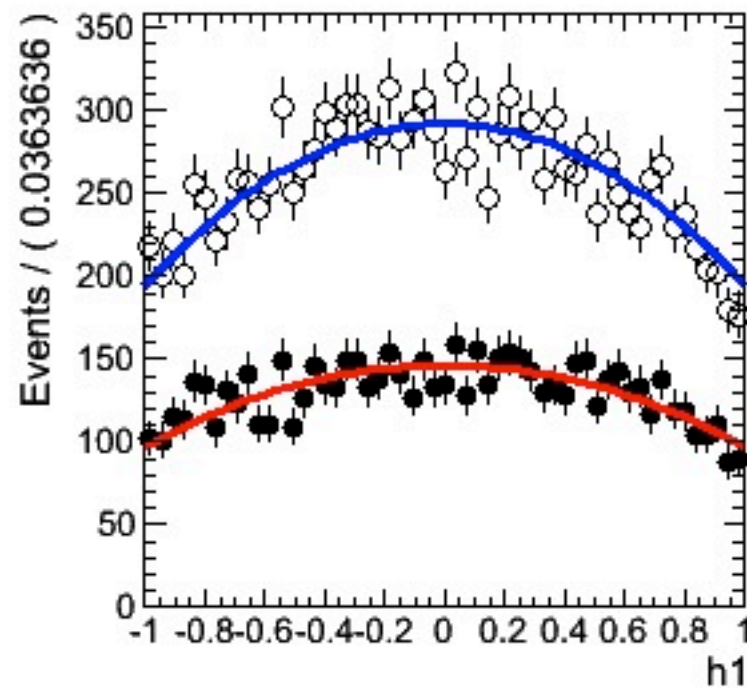
# Generator Validation ( $X \rightarrow WW$ Spin I)

- In this test  $m_X = 250$  GeV



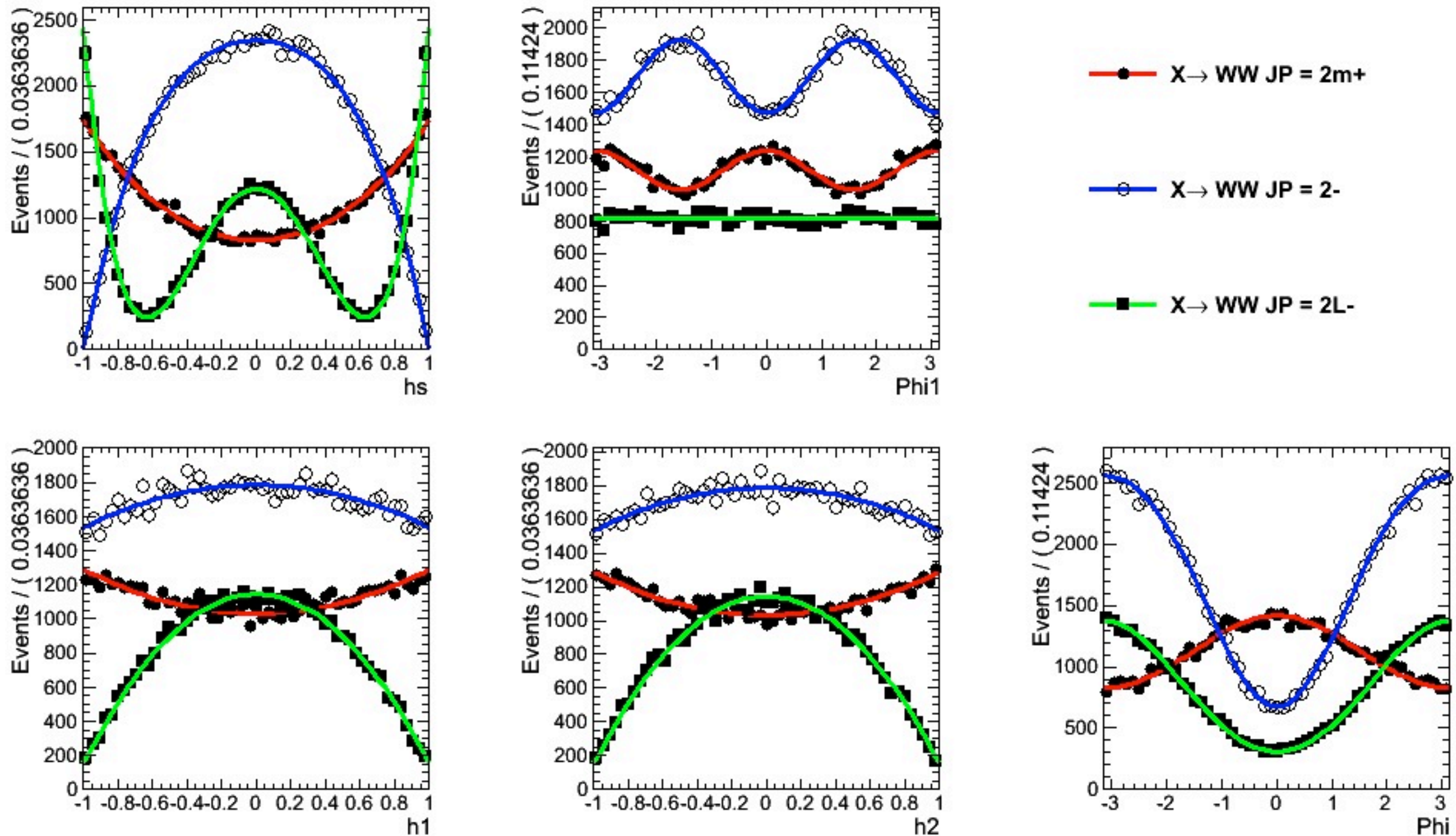
$\bullet$   $X \rightarrow WW$  JP = 1+

$\circ$   $X \rightarrow WW$  JP = 1-



# Generator Validation ( $X \rightarrow WW$ Spin 2)

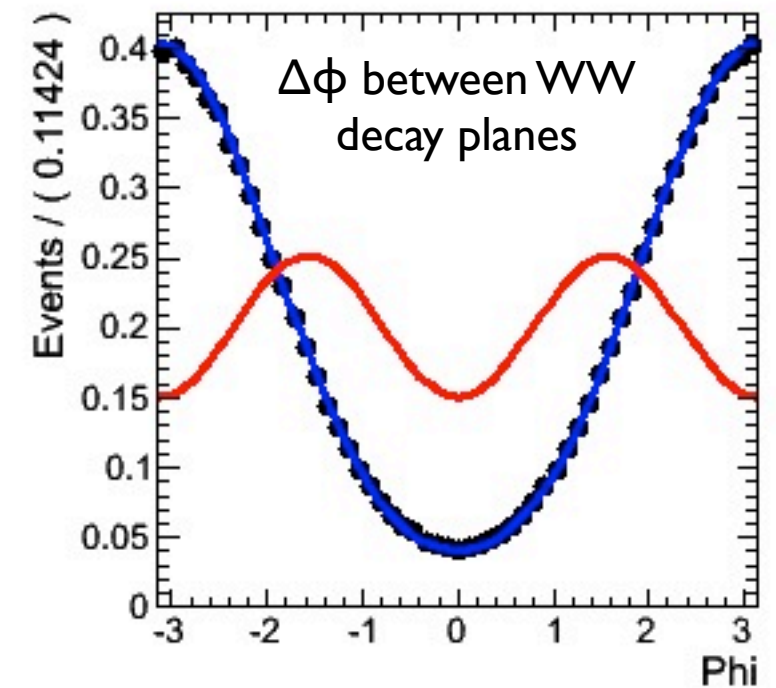
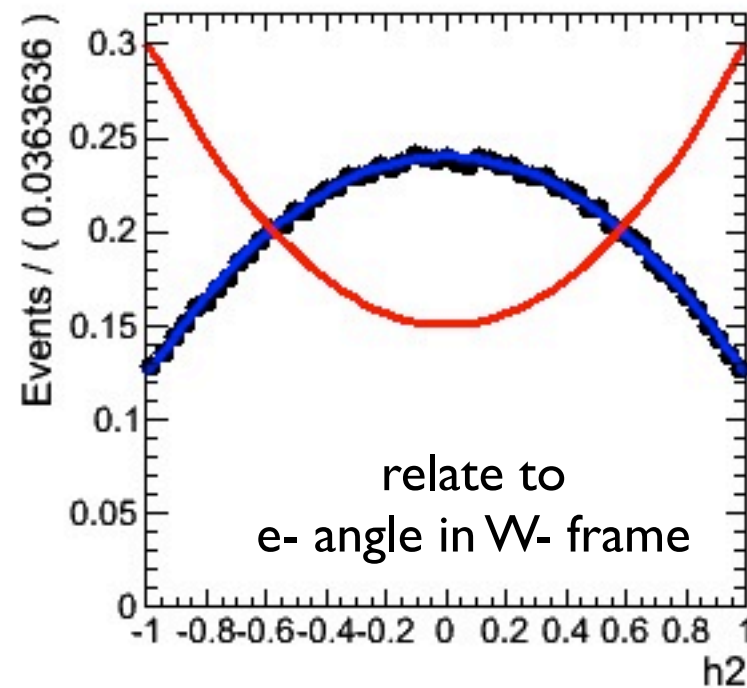
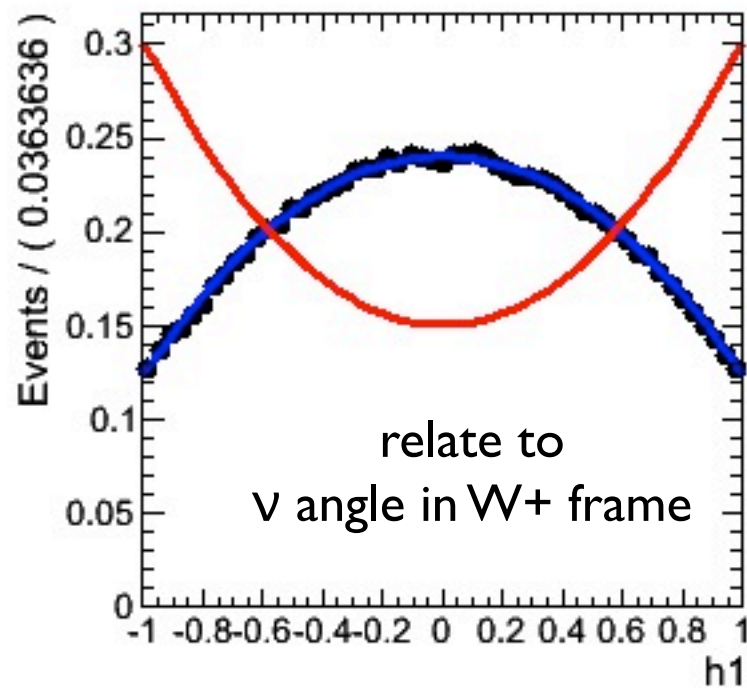
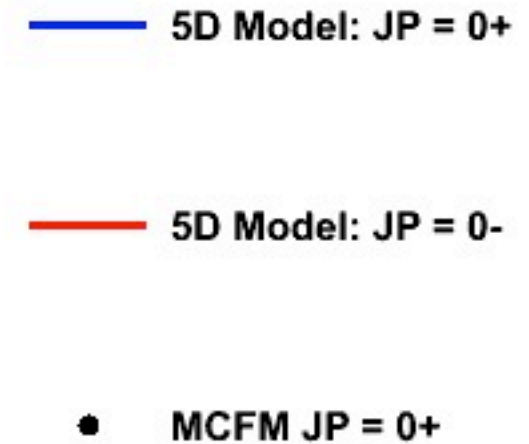
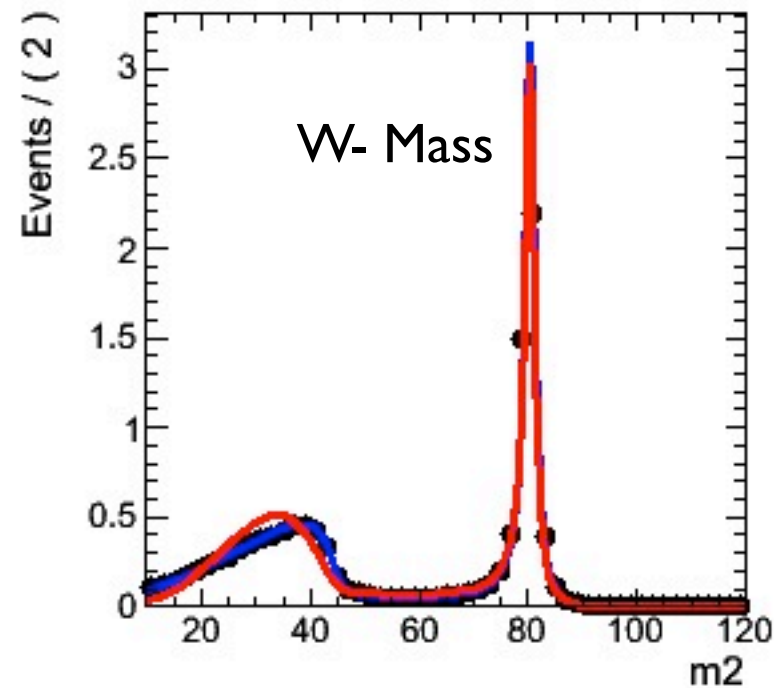
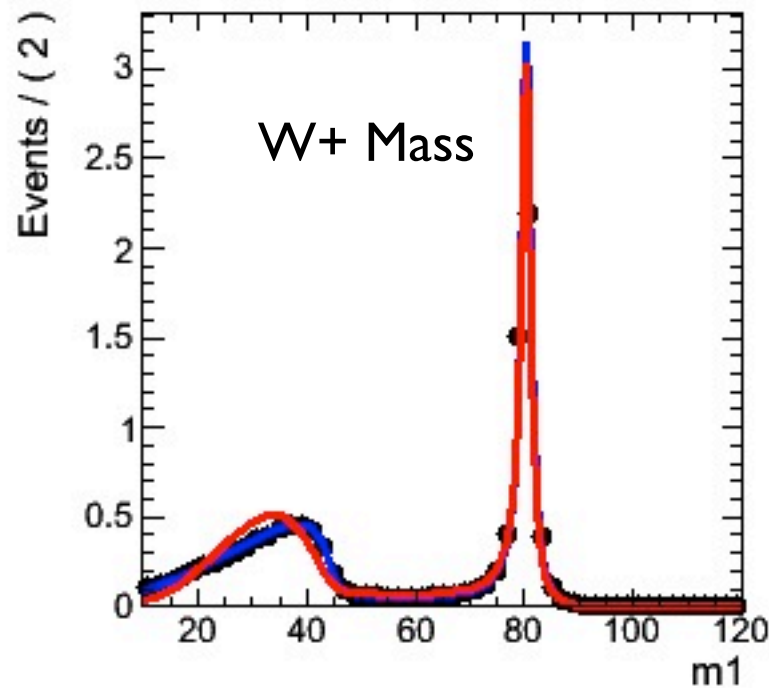
- In this validation,  $m_X = 250$  GeV





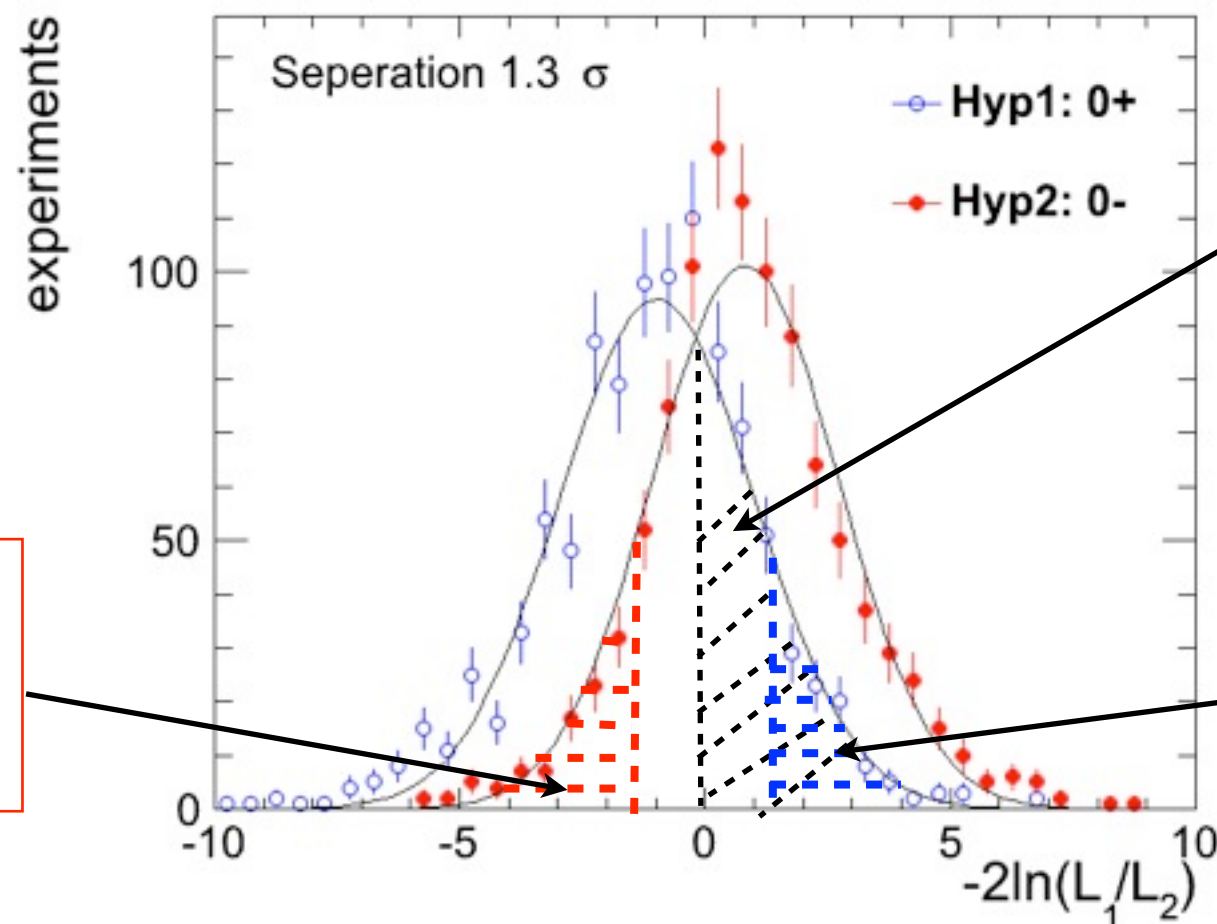
# Generator Validation (SM Higgs 125 GeV MCFM)

- In this test  $m_X = 125$  GeV



# Extract the hypothesis separation

- With a given dataset we calculate  $-2\ln(L_1/L_2)$ , where  $L_1/L_2$  are the fitted maximum likelihood based on the  $S_1+B$  and  $S_2+B$  templates
- We study  $-2\ln(L_1/L_2)$  for two sets of toy MCs generated with the two hypotheses independently, based on  $N$  toy experiments
- The exact separation depends on the interpretation
  - If the  $-2\ln(L_1/L_2)$  are gaussian distributed, the “separation” corresponds to the separation between the peaks of the two distributions



1) Average Separation ( $S$ )  
This area correspond to the one-sided Gaussian probability outside the  $S/2\sigma$  range

2)  $S_1$   
This quantifies the probability of Hyp1 faking the Hyp2

3)  $S_2$   
This quantifies the probability of Hyp2 faking the Hyp1