



New and conventional bottomonium states

Jin Li

Seoul National University

FPCP2012

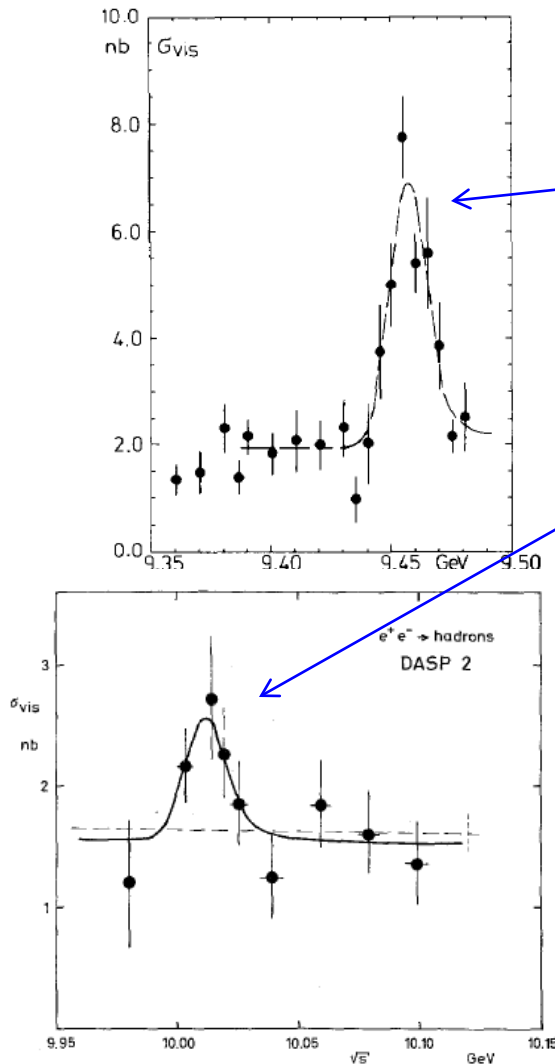


Υ discovery in 1978

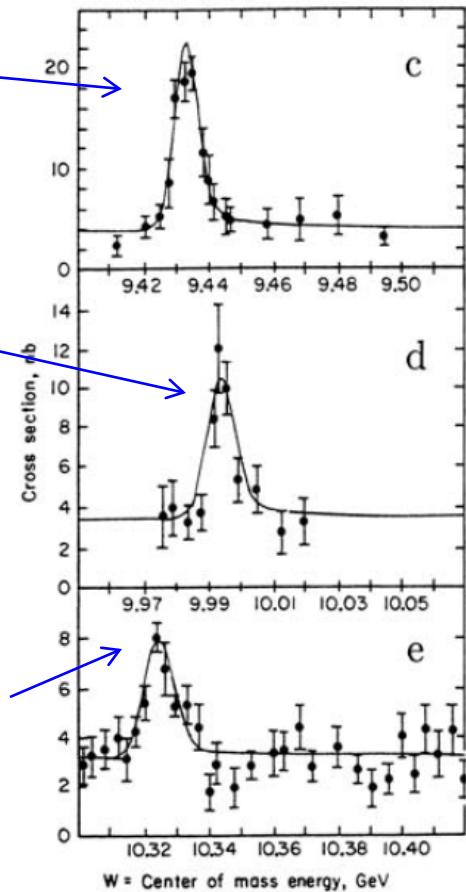
Υ, Υ' discovered in e^+e^- annihilation.

DORIS ring at DESY

CLEO group at CESR



Υ
 Υ'

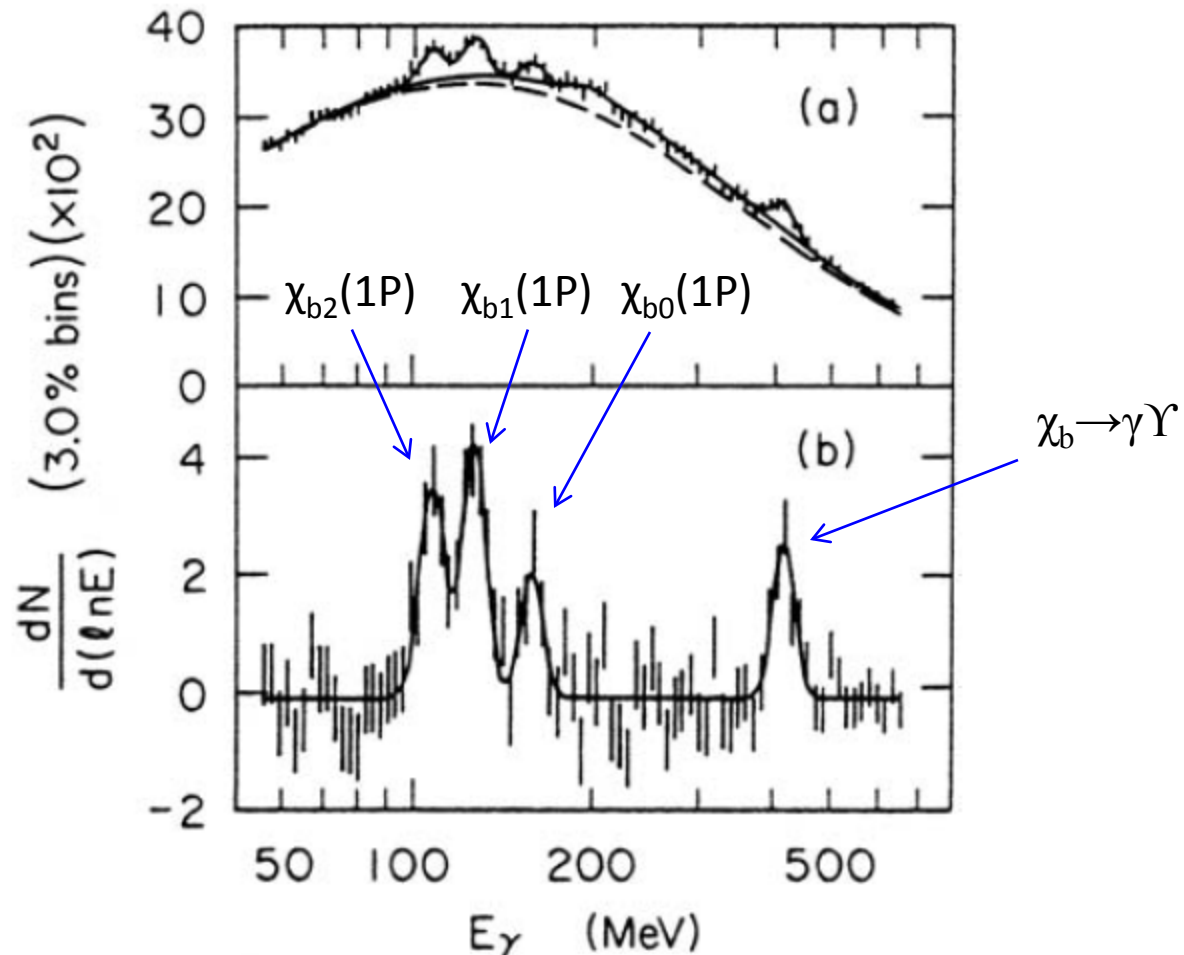


Υ''

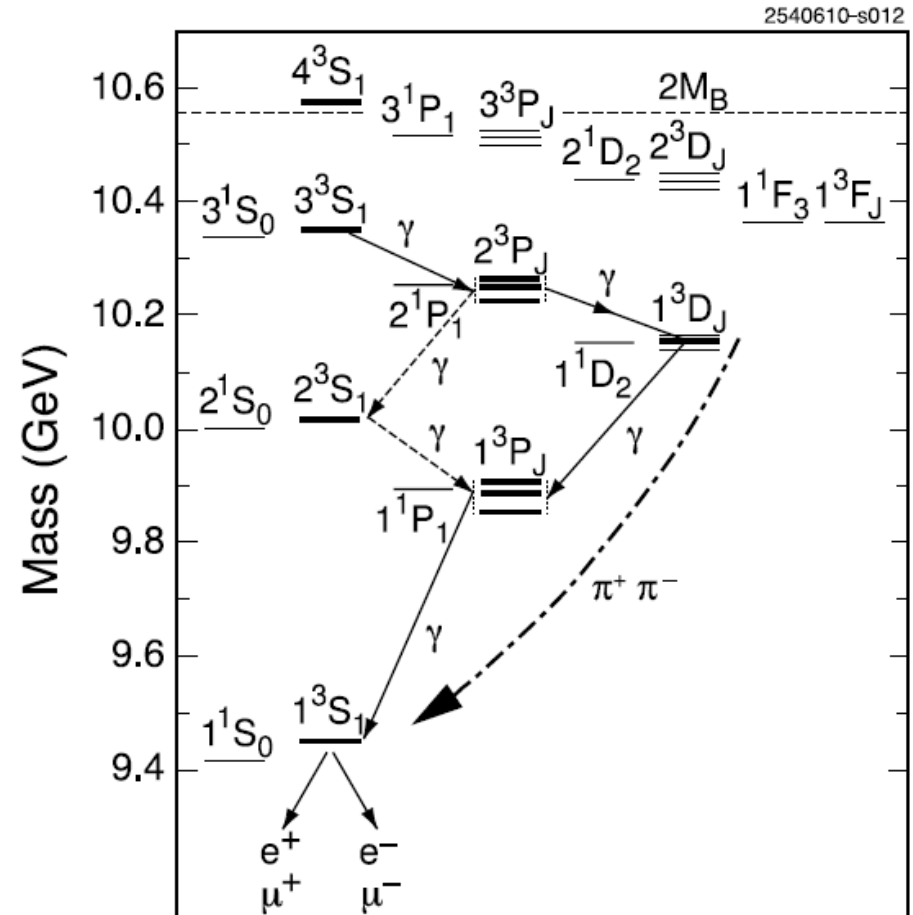
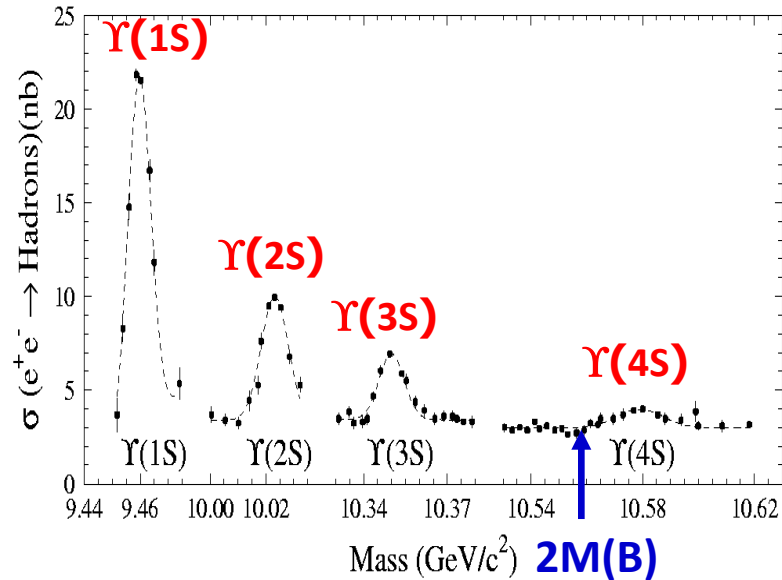
$\chi_b(^3P_{2,1,0})$ observation in 1985

Photon spectrum from Υ' decays.

Crystal Ball Collaboration at DORIS II.



The bottomonium family

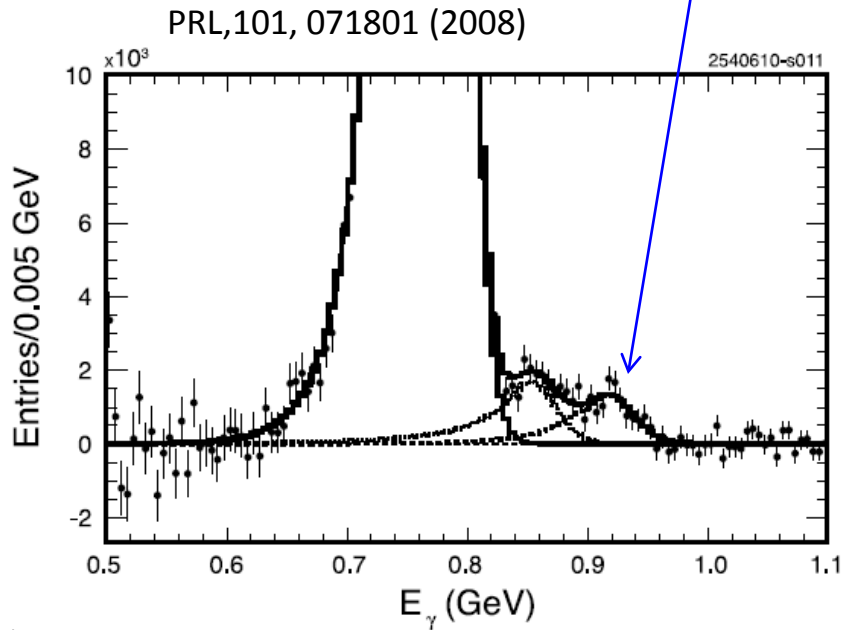


BaBar, CLEO collected large $\Upsilon(3S)$ data because its rich decay trees.

Old strategy: γ lineshape

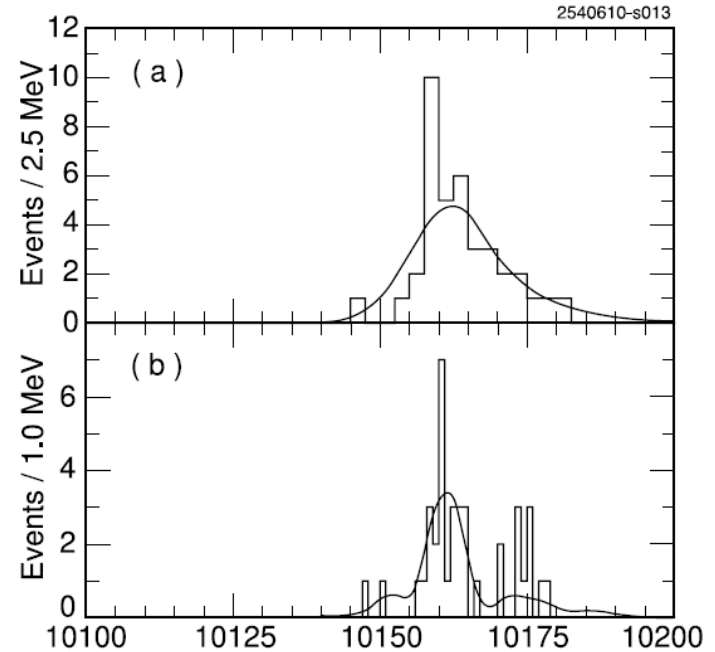
BaBar's η_b discovery

$$\Upsilon(3S) \rightarrow \gamma \eta_b$$



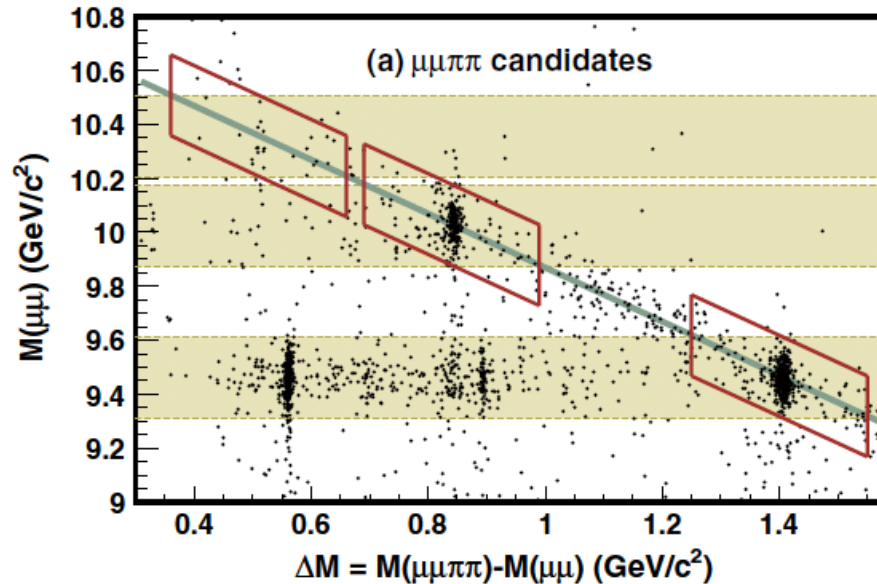
CLEO's $\Upsilon(1D)$ discovery

PRD,70, 032001 (2004)



Recoil mass of two soft γ from the $\Upsilon(3S) \rightarrow \gamma\gamma\gamma l^+ l^-$ events.

$\Upsilon(5S)$ is just different



$$e^+e^- \rightarrow \Upsilon(1S/2S/3S) \pi^+\pi^-$$

Process	$\Gamma_{\Upsilon(1S)\pi^+\pi^-}$
$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0060 MeV
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0009 MeV
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0019 MeV
$\Upsilon(10860) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.59 MeV

$\sim \times 100$



$\Upsilon(5S)$ result: (21.7fb^{-1})

Belle, K.F. Chen et al.

PRL 100, 112001 (2008)

Process	σ (pb)	Γ (MeV)
$\Upsilon(1S)\pi^+\pi^-$	$1.61 \pm 0.10 \pm 0.12$	$0.59 \pm 0.04 \pm 0.09$
$\Upsilon(2S)\pi^+\pi^-$	$2.35 \pm 0.19 \pm 0.32$	$0.85 \pm 0.07 \pm 0.16$
$\Upsilon(3S)\pi^+\pi^-$	$1.44^{+0.55}_{-0.45} \pm 0.19$	$0.52^{+0.20}_{-0.17} \pm 0.10$
$\Upsilon(1S)K^+K^-$	$0.185^{+0.048}_{-0.041} \pm 0.028$	$0.067^{+0.017}_{-0.015} \pm 0.013$

So Belle took large data at $\Upsilon(5S)$ resonance. **Now 121.4 fb^{-1} total.**

The $\pi^+\pi^-$ transition of $\Upsilon(5S)$

Missing mass technique



Good for study of unknown particles

Full reconstruction, when the decays of daughter particles are known.

$$\Upsilon(5S) \rightarrow \Upsilon(1S, 2S, 3S) \pi^+\pi^-$$



$$\Upsilon(nS) \rightarrow \mu^+ \mu^-$$

Missing mass technique:

$$\boxed{\Upsilon(5S)} \rightarrow h_b(nP) \boxed{\pi^+\pi^-}$$

$P(5S)$ from accelerator information

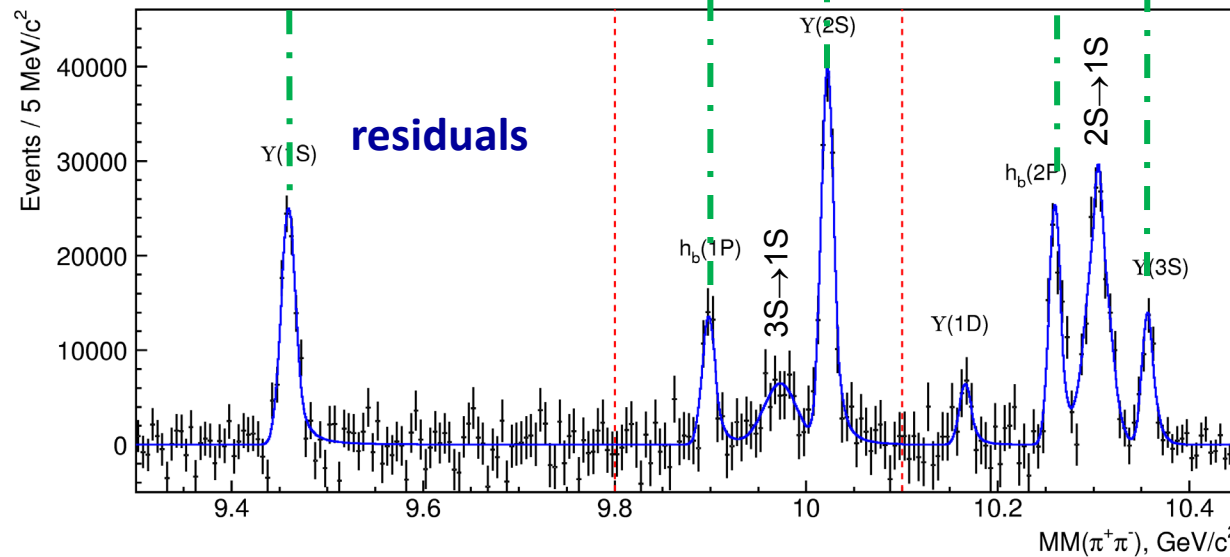
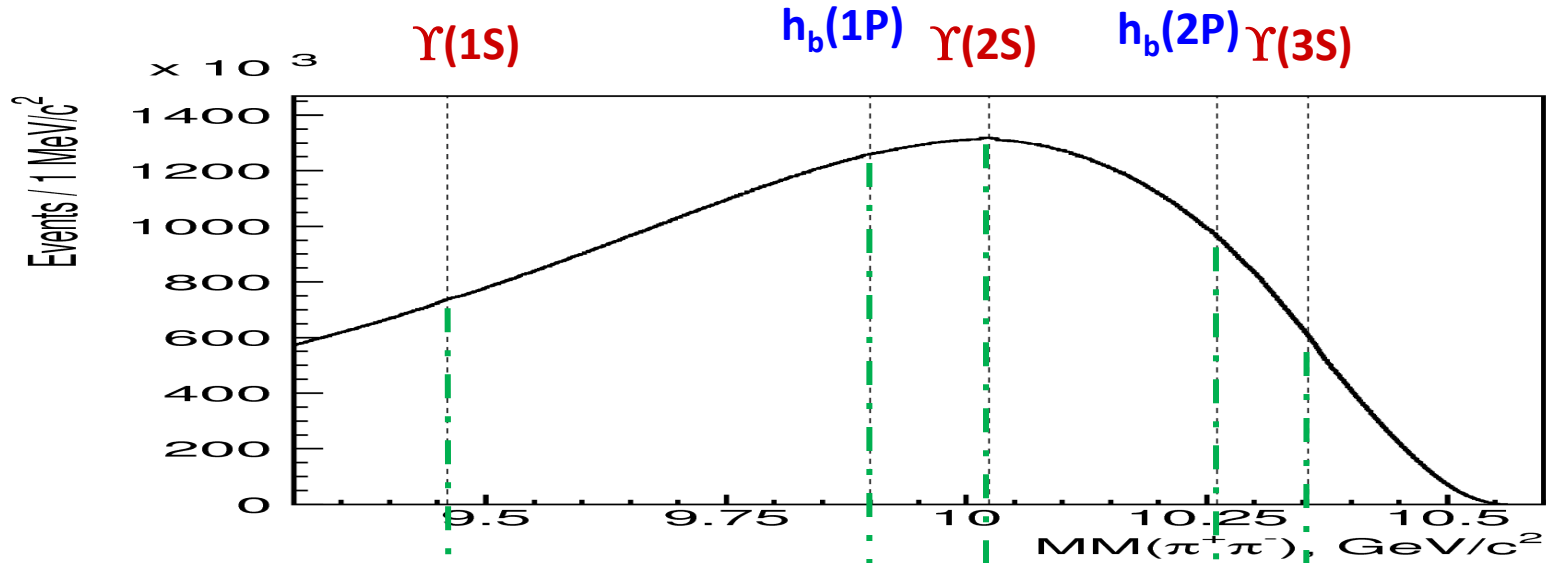
$P(\pi\pi)$ is reconstructed.

$$M(h_b) = \sqrt{(P(5S) - P(\pi^+\pi^-))^2} \equiv \textcolor{red}{MM}(\pi^+\pi^-)$$

missing mass of $\pi^+\pi^-$

Since we don't need to reconstruct h_b decays...

Results of $\pi^+\pi^-$ missing mass study



121.4 fb⁻¹

PRL 108 032001

**$h_b(1,2P) J^{PC}=1^{+-}$
1st observations**

$h_b(1,2P)$ mass

$(b\bar{b}) : S=0 \ L=1 \ J^{PC}=1^{+-}$

Belle PRL 108, 032001

Expected mass: center-of-gravity

$$\approx (M\chi_{b0} + 3 M\chi_{b1} + 5 M\chi_{b2}) / 9$$

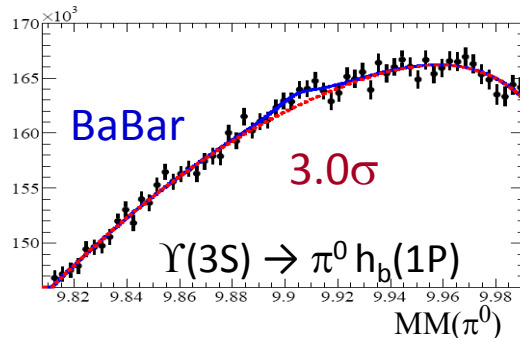
$\Delta M_{\text{HF}} \Rightarrow$ test of hyperfine interaction

Deviations from expected masses

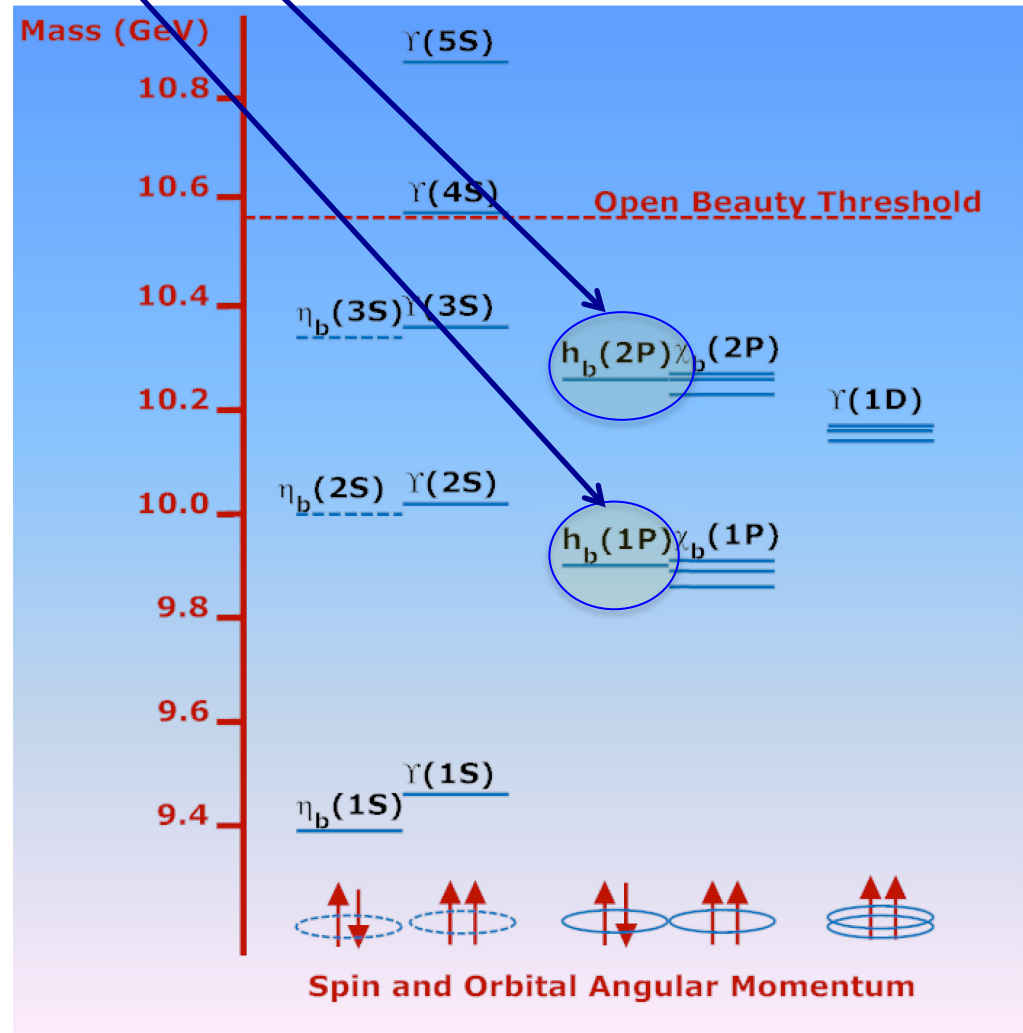
$$\left. \begin{array}{l} h_b(1P) \quad (1.7 \pm 1.5) \text{ MeV}/c^2 \\ h_b(2P) \quad (0.5^{+1.6}_{-1.2}) \text{ MeV}/c^2 \end{array} \right\}$$

Agrees with expectations

Previous search



arXiv:1102.4565



Large $\Upsilon(5S) \rightarrow h_b(nP) \pi^+ \pi^-$ rate

$S=1$ for $\Upsilon(5S)$; $S=0$ for h_b

$$\frac{\Gamma(\Upsilon(5S) \rightarrow h_b(nP) \pi^+ \pi^-)}{\Gamma(\Upsilon(5S) \rightarrow \Upsilon(2S) \pi^+ \pi^-)} = \begin{cases} 0.407 \pm 0.079^{+0.043}_{-0.076} & h_b(1P) \\ 0.78 \pm 0.09^{+0.22}_{-0.10} & h_b(2P) \end{cases}$$

Spin-flip
↙
No spin-flip
↘

Process with spin-flip of heavy quark is not suppressed

⇒ Mechanism of $\Upsilon(5S) \rightarrow h_b(nP) \pi^+ \pi^-$ decay is exotic

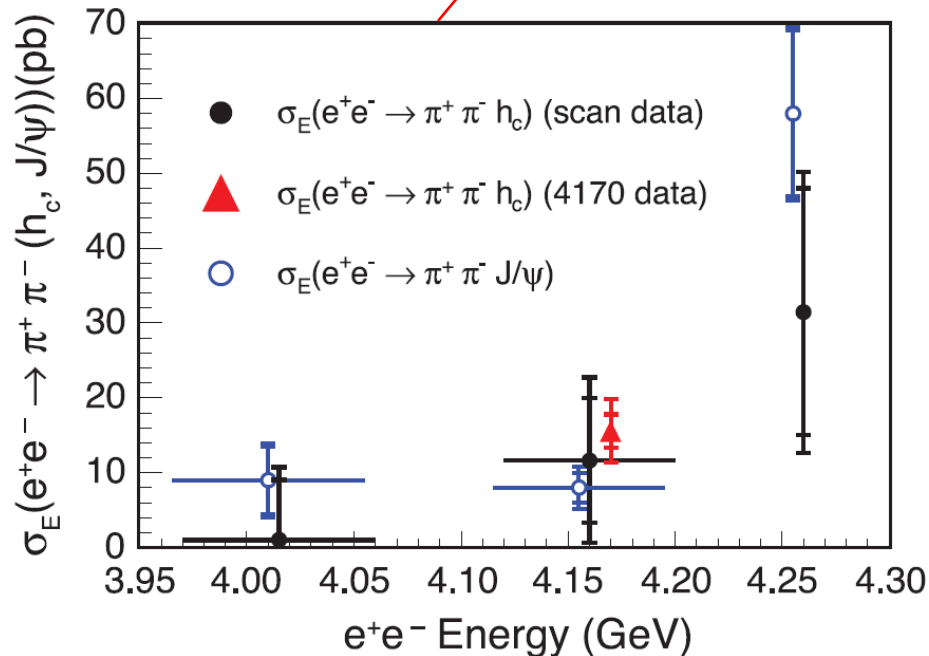
CLEO-c's $e^+e^- \rightarrow \pi^+\pi^- h_c$ cross section

An interesting comparison!

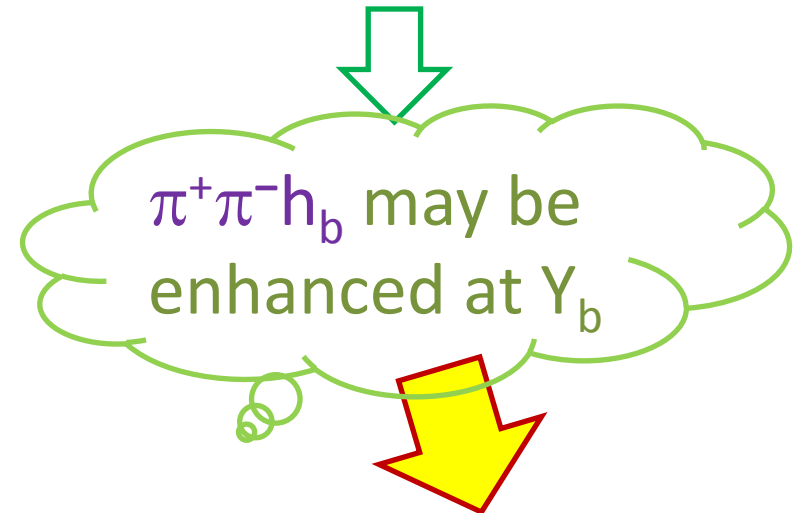
- $\sigma(h_c \pi^+\pi^-) \cong \sigma(J/\psi \pi^+\pi^-)$
- $\Gamma(Y(4260) \rightarrow J/\psi \pi^+\pi^-) > 508 \text{ keV} @ 90\% \text{ C.L.}$
- $\Rightarrow$ **Large!!** X. H. Mo et al., Phys. Lett. B 640 (2006) 182

PRL107, 041803 (2011)

arXiv:1102.3424



$\pi^+\pi^- h_c$ production is enhanced at $Y(4260)$



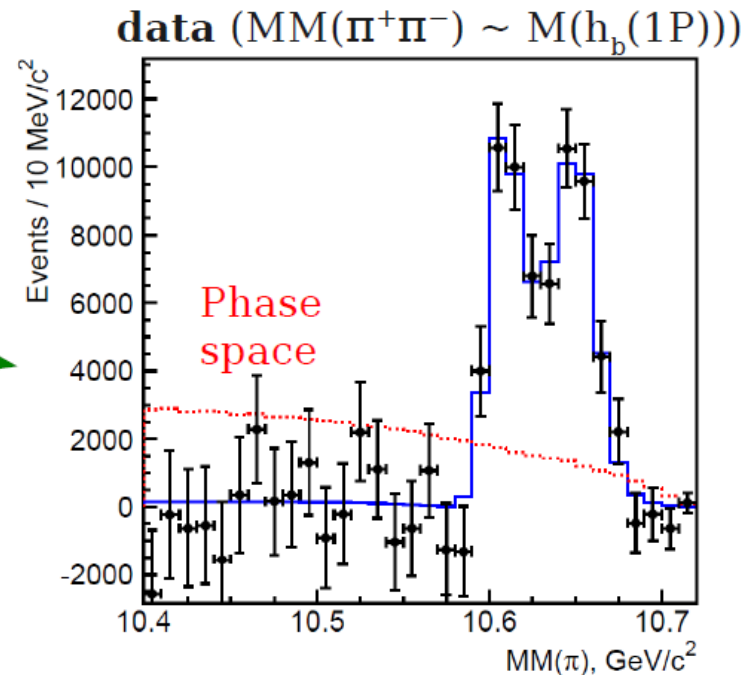
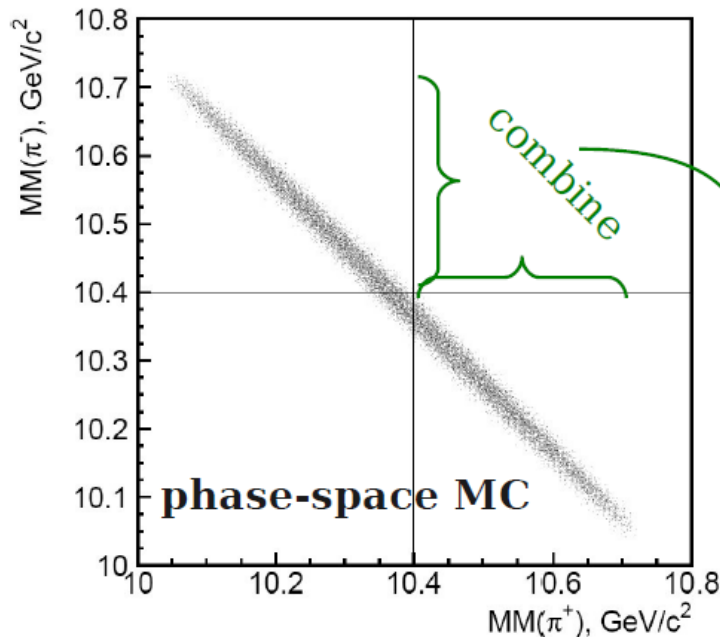
Substructure of $\pi^+\pi^- h_c$ in $Y(4260)$ has **not** been studied.

Substructure of $\pi^+\pi^- h_b$: Enough statistics in Belle's $Y(5S)$ data.

Original Motivation for h_b search

Resonant substructure of $h_b(nP)\pi^+\pi^-$

Now look at the missing mass of a single pion π^- , then $MM(\pi^-) = M(h_b \pi^+)$



Fit Function: $|BW(s, M_1, \Gamma_1) + ae^{i\phi} BW(s, M_2, \Gamma_2) + be^{i\psi}|^2 \frac{qp}{\sqrt{s}}$

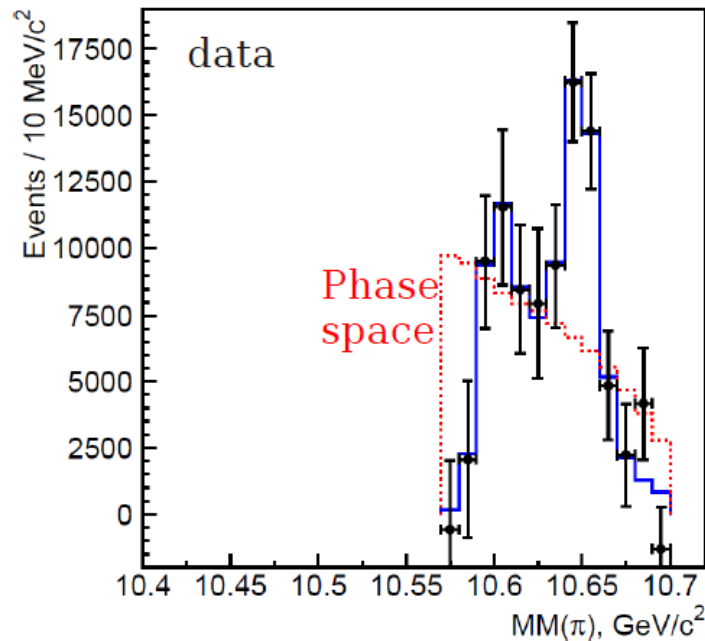
Significances with systematic: 1 resonance v.s. 0: **6.6 σ**
2 resonances v.s. 0: **16 σ**

Similar analysis for $h_b(2P)\pi^+\pi^-$

Significances: For $h_b(2P)$ yields in $MM(\pi^-)$ bins, the allowed phase space is smaller.

1 resonance v.s. 0: **1.9 σ**

2 resonances v.s. 0: **4.7 σ**



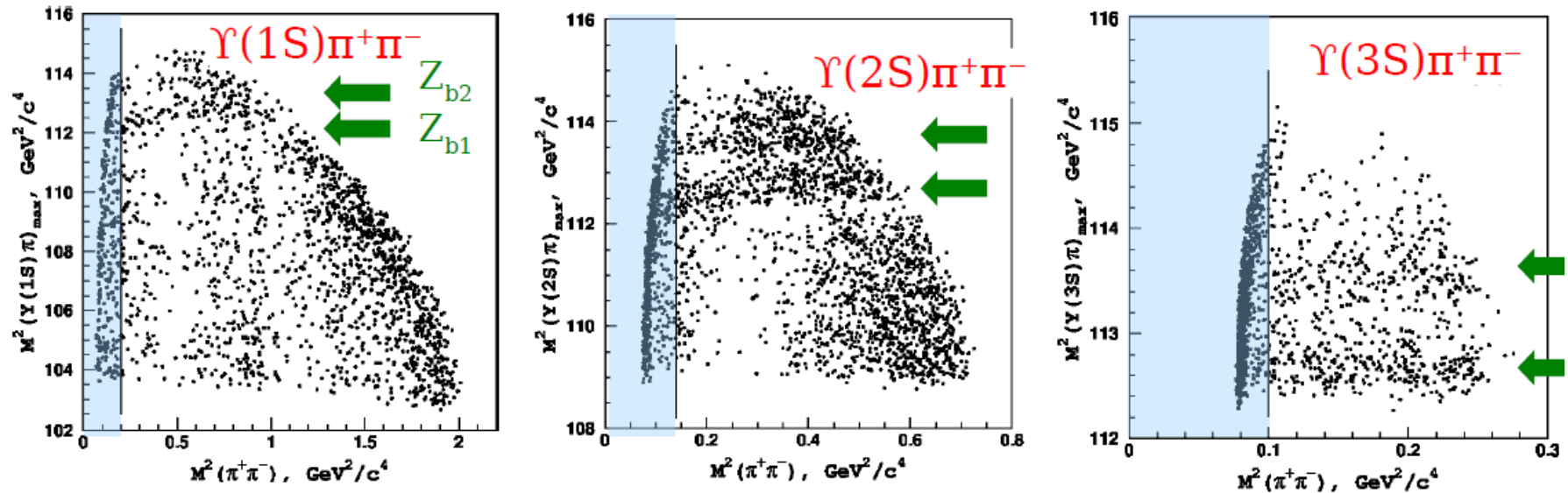
	$h_b(1P)\pi^+\pi^-$	$h_b(2P)\pi^+\pi^-$
$M_{Z_{b1}}$	$10605.1 \pm 2.2^{+3.0}_{-1.0}$	$10596 \pm 7^{+5}_{-2}$
$\Gamma_{Z_{b1}}$	$11.4^{+4.5+2.1}_{-3.9-1.2}$	16^{+16+13}_{-10-4}
$M_{Z_{b2}}$	$10654.5 \pm 2.5^{+1.0}_{-1.9}$	$10651 \pm 4 \pm 2$
$\Gamma_{Z_{b2}}$	$11.4^{+5.4+2.1}_{-4.7-5.7}$	12^{+11+8}_{-9-2}
a	$1.8^{+1.0+0.1}_{-0.7-0.5}$	$1.3^{+3.1+0.4}_{-1.1-0.7}$
ϕ	188^{+44+4}_{-58-9}	$255^{+56+12}_{-72-183}$
NR	~ 0	~ 0

Mass/width in MeV($/c^2$), phase in degrees

- Good agreement between $h_b(1P)$ and $h_b(2P)$.
- Non resonant part ~ 0 : Nearly all produced through

$$\Upsilon(5S) \rightarrow Z^\pm \pi^\mp \rightarrow h_b(nP) \pi^\pm \pi^\mp$$

Dalitz Plots of $\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$



Exclude high background from photon conversions

$$S(s_1, s_2) = |A_{Z_{b1}} + A_{Z_{b2}} + A_{NR} + A_{f_0(980)} + A_{f_2(1270)}|^2$$

$$s_i = M_{\Upsilon \pi_i}^2$$

Isospin symmetry

$$A_{Z_{bk}} = a_k e^{i\phi_k} \left(\frac{\sqrt{M_k \Gamma_k}}{M_k^2 - s_1 + iM_k \Gamma_k} + \frac{\sqrt{M_k \Gamma_k}}{M_k^2 - s_2 + iM_k \Gamma_k} \right)$$

$$A_{NR} = c_1 + c_2 M_{\pi\pi}^2$$

A. Voloshin, PRD74,054022 (2006)

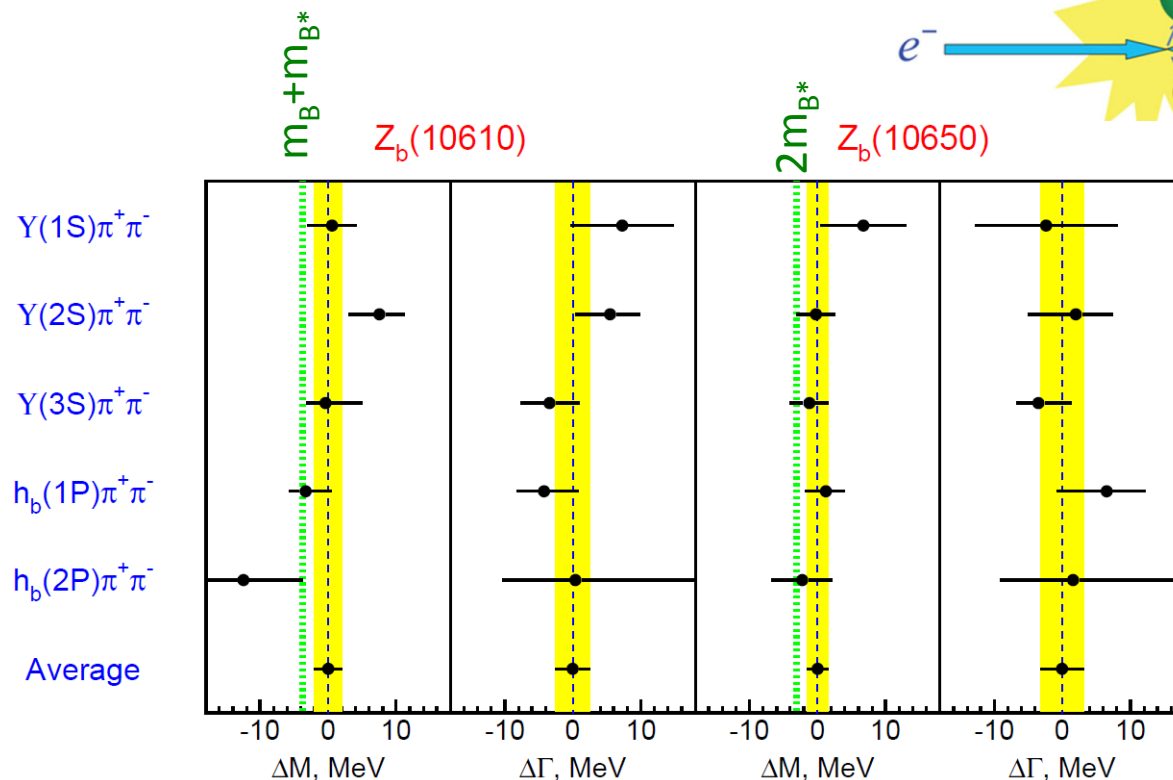
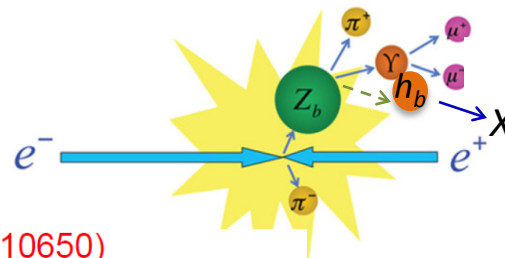
Prog. Part. Nucl. Phys. 61,455 (2008)

↑
Flatté

↑
D-Wave
Breit-Wigner

Summary of parameter measurements

Belle PRL 108, 122001



$Z_b(10610)$

$Z_b(10650)$

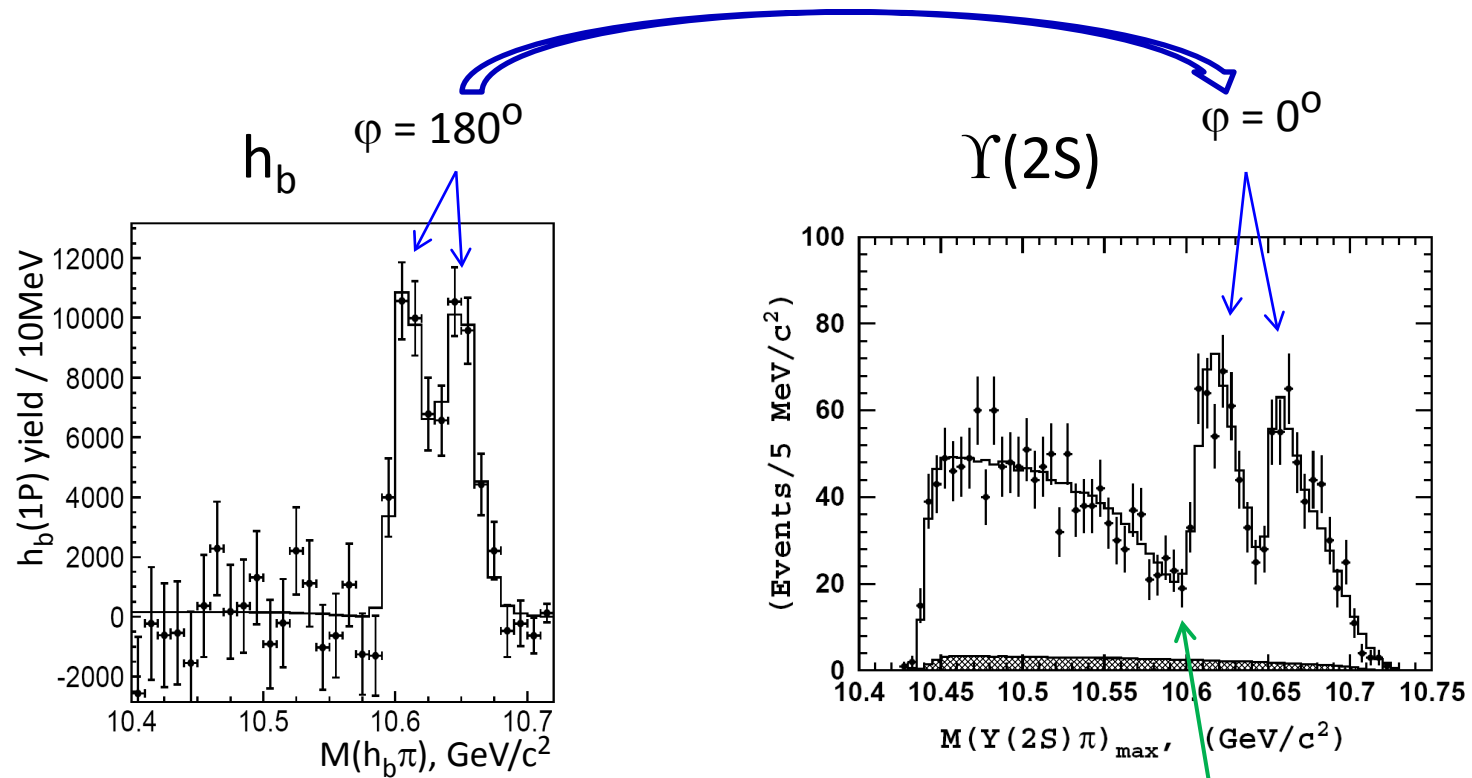
$M=10607.2 \pm 2.0$ MeV

$M=10652.2 \pm 1.5$ MeV

$\Gamma=18.4 \pm 2.4$ MeV

$\Gamma=11.5 \pm 2.2$ MeV

Projections of $\Upsilon(5S) \rightarrow [\Upsilon(nS), h_b] \pi^+ \pi^-$



Dip due to destructive interference with non-resonant amplitude.
 $\Rightarrow$ Information on J^P of Z_b ?

Introduction to η_b

h_b has large expected radiative η_b decay

$$h_b(1P) \rightarrow ggg (57\%), \eta_b(1S)\gamma (41\%), \gamma gg (2\%)$$

Godfrey & Rosner, PRD66 014012 (2002)

$$h_b(2P) \rightarrow ggg (63\%), \eta_b(1S)\gamma (13\%), \eta_b(2S)\gamma (19\%), \gamma gg (2\%)$$

Large $h_b(mP)$ samples give opportunity to study $\eta_b(nS)$ states.

Reminder: Experimental status of η_b

$$M[\eta_b(1S)] = 9390.9 \pm 2.8 \text{ MeV (BaBar + CLEO)}$$

$$M[\Upsilon(1S)] - M[\eta_b(1S)] = 69.3 \pm 2.8 \text{ MeV}$$

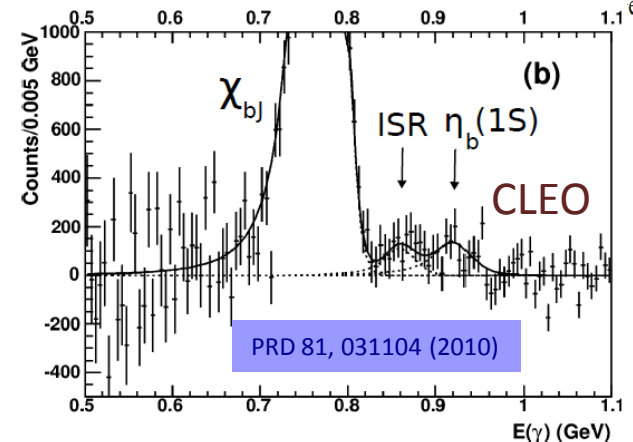
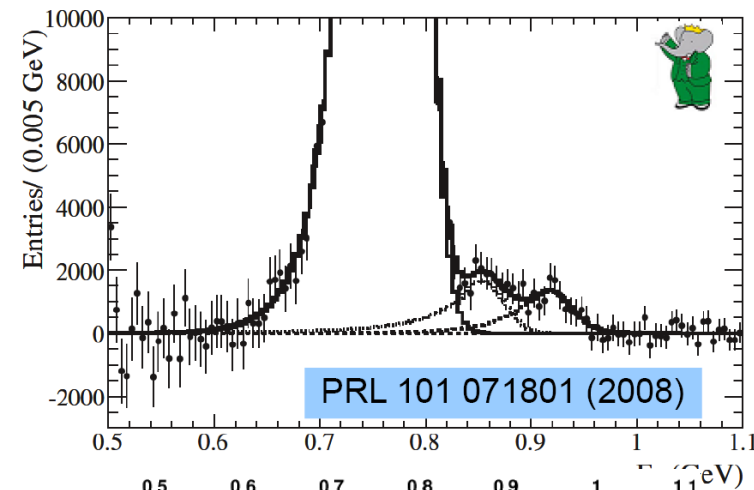
$$\text{pNRQCD: } 41 \pm 14 \text{ MeV} \quad \text{Lattice: } 60 \pm 8 \text{ MeV}$$

Kniehl et al., PRL92,242001(2004)

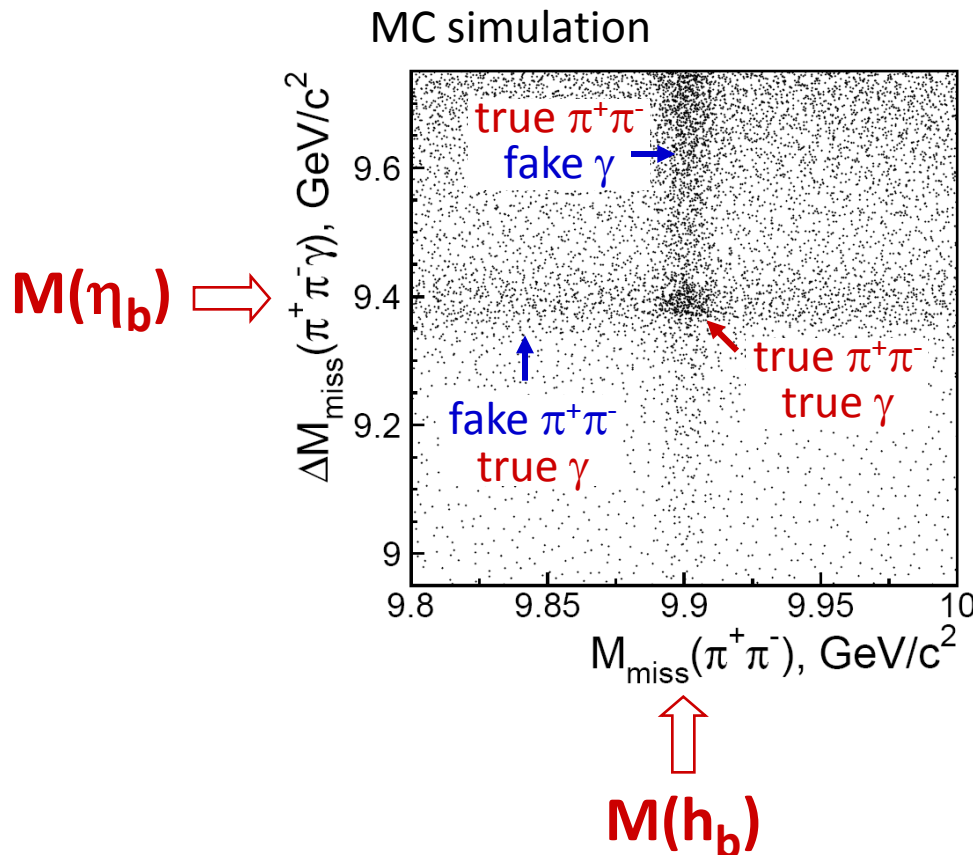
Meinel, PRD82,114502(2010)

Width of $\eta_b(1S)$: no information

$\Upsilon(3S) \rightarrow \eta_b(1S) \gamma$



Method of signal extraction



$$\Delta M_{\text{miss}}(\pi^+ \pi^- \gamma) \equiv M_{\text{miss}}(\pi^+ \pi^- \gamma) - M_{\text{miss}}(\pi^+ \pi^-) + M[h_b]$$

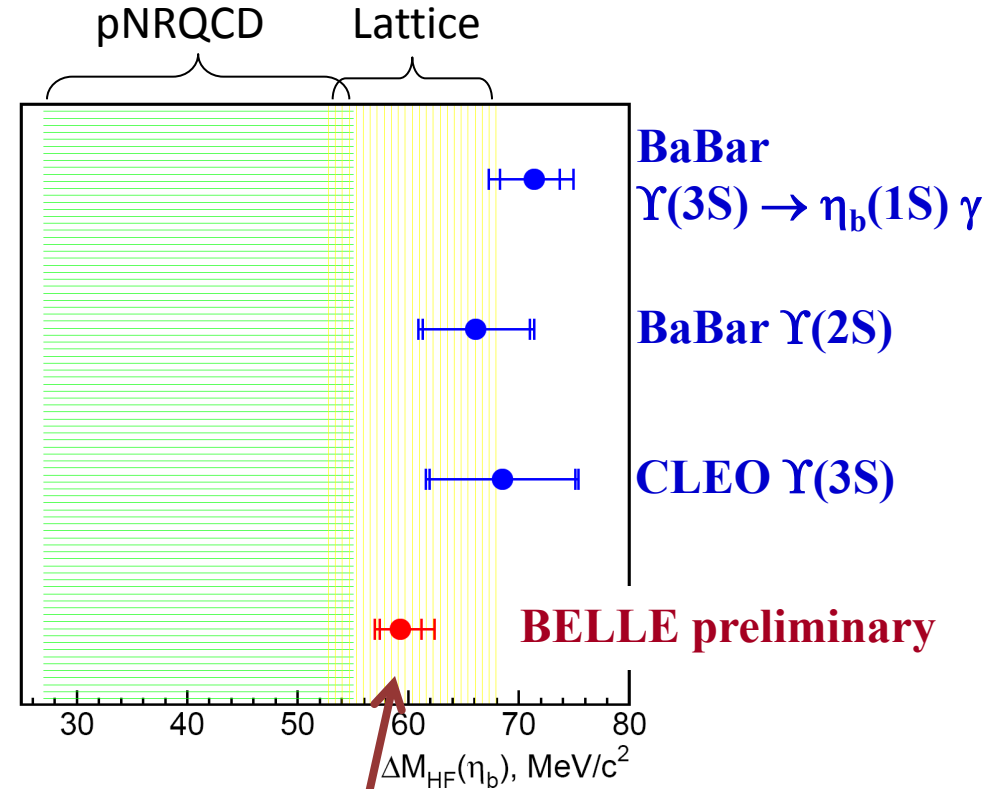
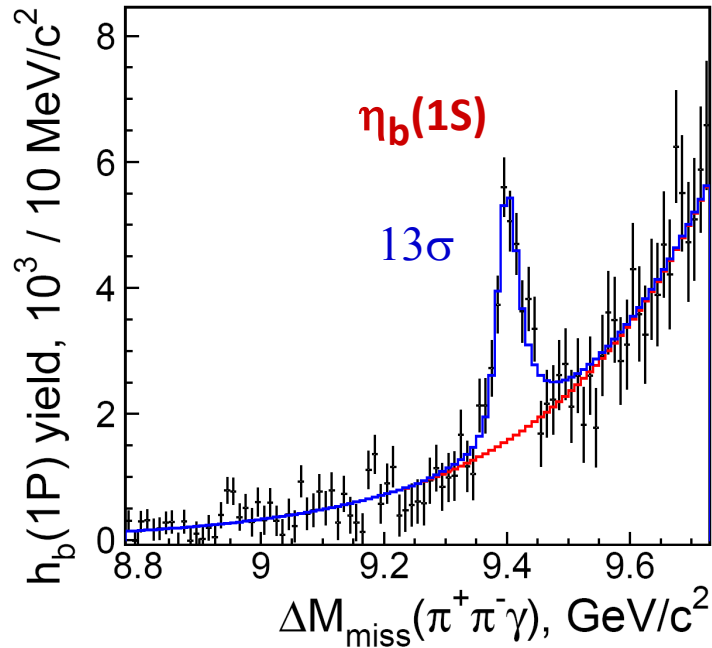
- rectangular bg bands
- no correlation

Approach:

fit $M_{\text{miss}}(\pi^+ \pi^-)$ spectra
in $\Delta M_{\text{miss}}(\pi^+ \pi^- \gamma)$ bins

Observation of $h_b(1P) \rightarrow \eta_b(1S) \gamma$

N.Brambilla et al., Eur.Phys.J.
C71(2011) 1534 (arXiv:1010.5827)



$$N[\eta_b(1S)] \quad (21.9 \pm 2.0^{+5.6}_{-1.7}) \cdot 10^3$$

$$M[\eta_b(1S)] \quad (9401.0 \pm 1.9^{+1.4}_{-2.4}) \text{ MeV}/c^2$$

$$\Gamma[\eta_b(1S)] \quad (12.4^{+5.5+11.5}_{-4.6-3.4}) \text{ MeV}$$

$$\text{Godfrey \& Rosner : BF} = 41\% \quad \mathcal{B}[h_b(1P) \rightarrow \eta_b(1S) \gamma] = (49.8 \pm 6.8^{+10.9}_{-5.2})\%$$

First observation of the $\eta_b(2S)$

$h_b(2P) \rightarrow \gamma \eta_b(2S)$: same method

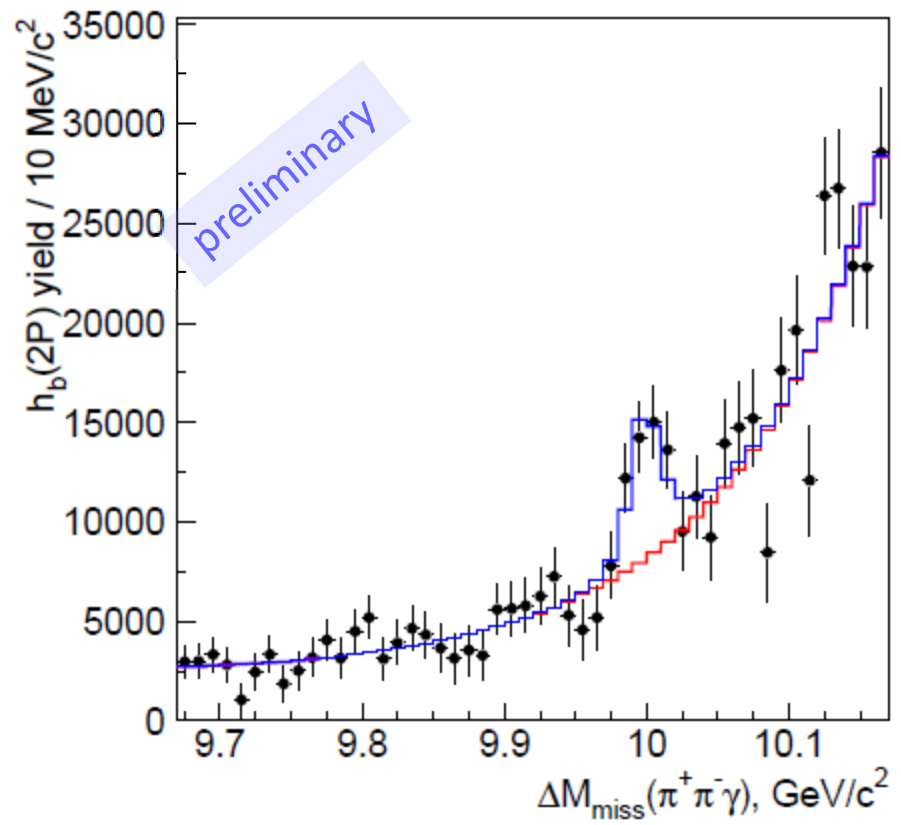
$$M[\eta_b(2S)] = 9999.0 \pm 3.5^{+2.8}_{-1.9} \text{ MeV}$$

$$\text{Bf}[h_b(2P) \rightarrow \gamma \eta_b(2S)] = 47.5 \pm 10.5^{+6.8}_{-7.7} \%$$

$$\Delta M_{\text{hfs}}(2S) = 24.3 \pm 3.5^{+2.8}_{-1.9} \text{ MeV}$$

Lattice Meinel PRD82,114502(2010)

$$\Delta M_{\text{HF}} = 23.5 \pm 4.7 \text{ MeV}$$

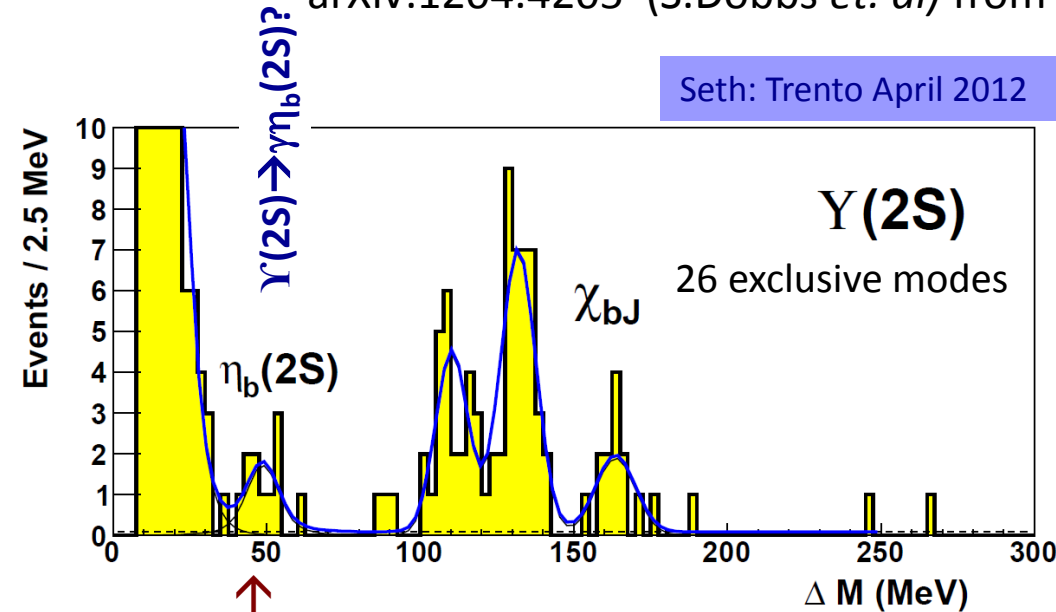


Comparison: $\eta_b(2S)$ “signals”

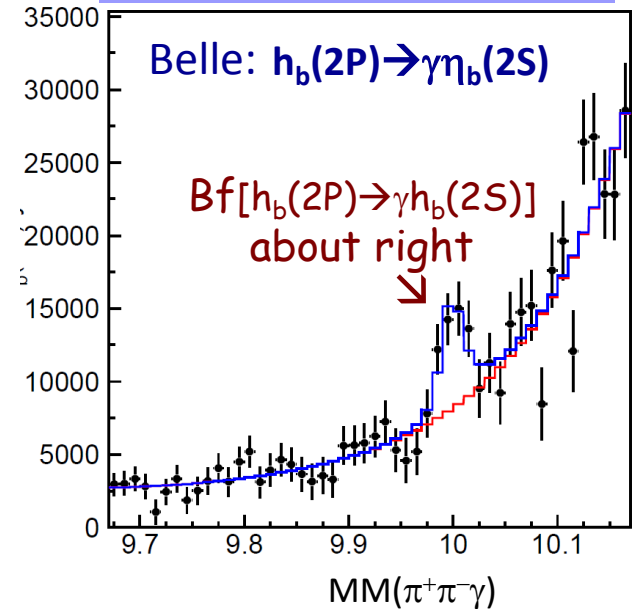
arXiv:1204.4205 (S.Dobbs *et. al*) from CLEO data

Seth: Trento April 2012

Belle: IWHSS'12 April, 2012



↑
anomalously large
production rate
($\sim 0.2 \times \chi_{b1}$ rate)



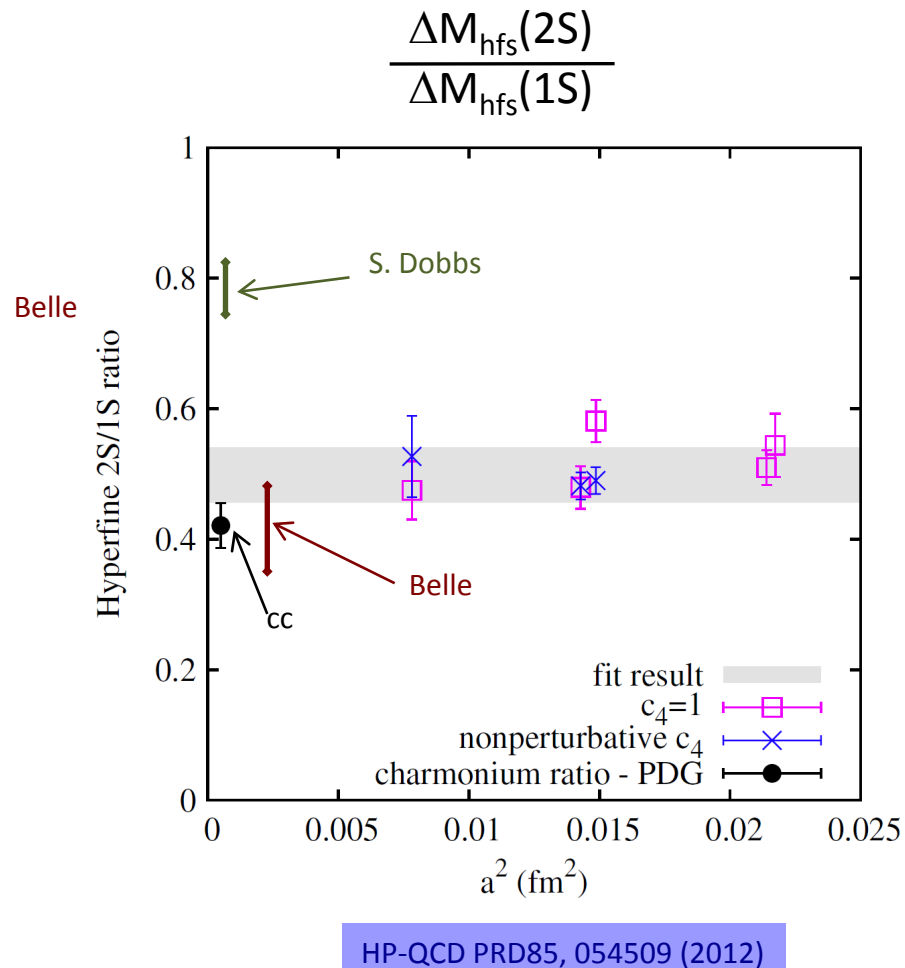
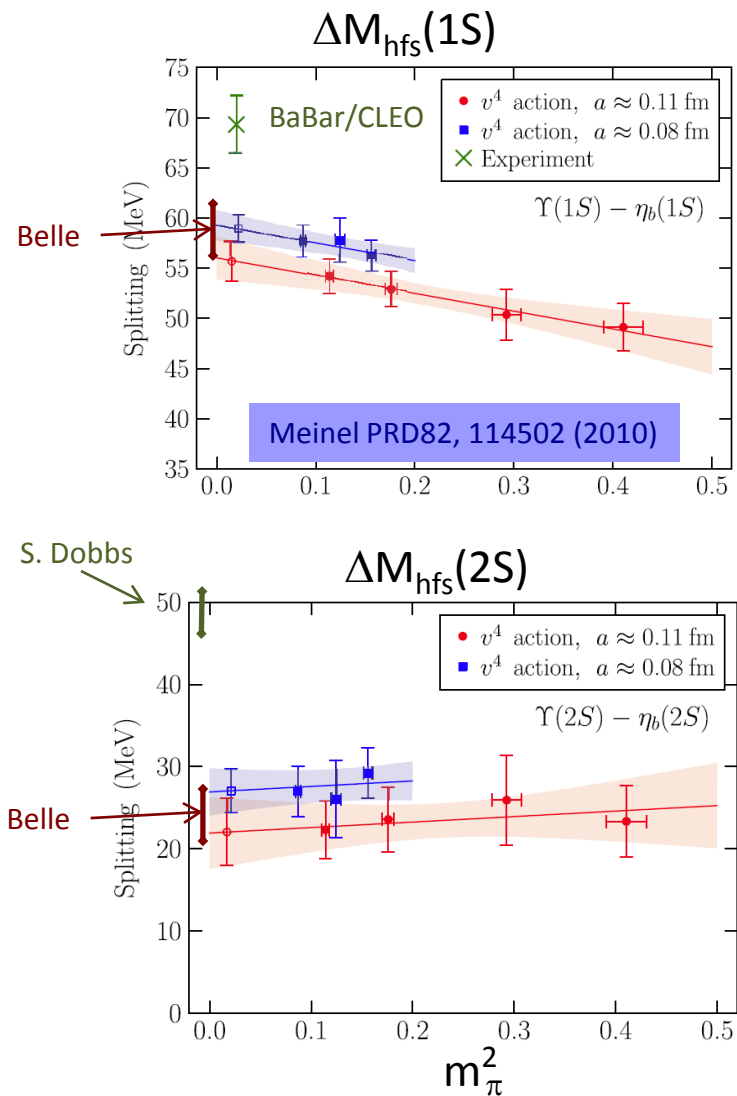
Expt	$\Delta M_{hfs}(2S) \text{ (MeV)}$
S. Dobbs	48.7 ± 2.7
Belle	24.3 ± 4.3

← strong disagreement with theory

← agrees with theory

↗
 $\approx 5\sigma$ discrepancy

LQCD predictions for $\Delta M_{\text{hfs}}(1,2S)$

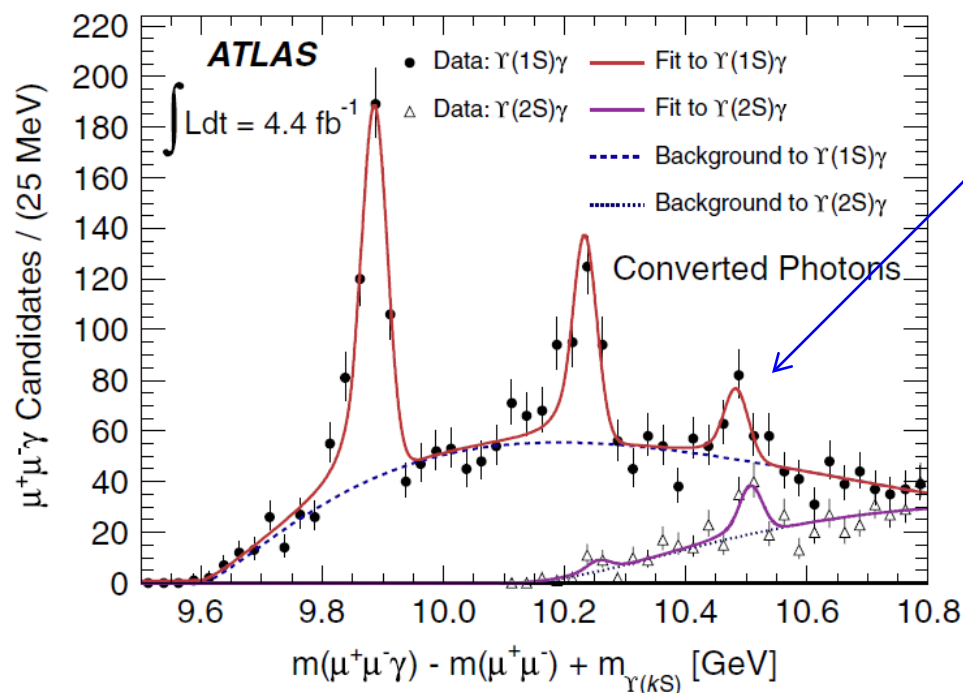


Observation of $\chi_b(3P)$

Converted photon is used for mass determination

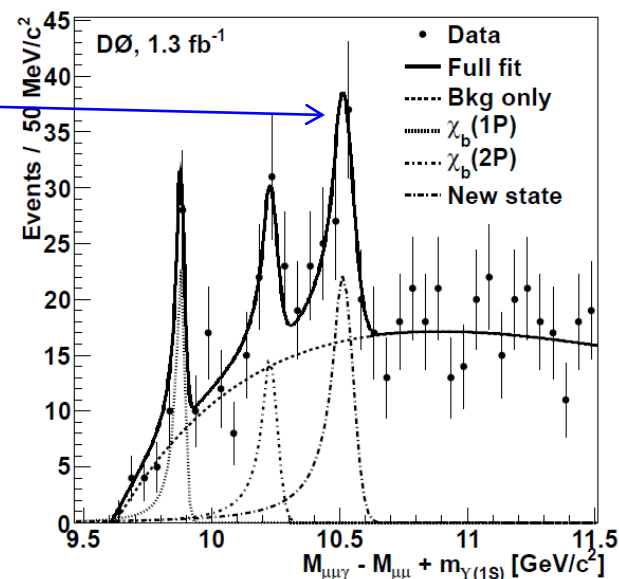
$\chi_b(3P) \rightarrow \Upsilon(1,2S)\gamma$ first by ATLAS:

PRL 108,152001



Confirmed by D0:

arXiv:1203.6034



Spin-weighted mass for $\chi_b(3P)$:

	$10.530 \pm 0.005 \pm 0.009 \text{ GeV}$	ATLAS
	$10.551 \pm 0.014 \pm 0.017 \text{ GeV}$	D0
	10.5439	(Potential model, arXiv: 1201.4096)

$\Upsilon(nS) \rightarrow \eta \Upsilon(mS)$ Status

$\Upsilon(nS) \rightarrow \eta \Upsilon(mS)$: E1M2
transition, spin-flip

M. B. Voloshin, Prog. Part. Nucl. Phys. 61, 455-511 (2008).
Y. -P. Kuang, Front. Phys. China 1, 19-37 (2006).

QCD multipole formalism:
• spin-flip amplitude scale as $1/m_b$.
• η transition suppressed compared to $\pi\pi$ transition.

Scale from $\psi' \rightarrow \eta J/\psi$

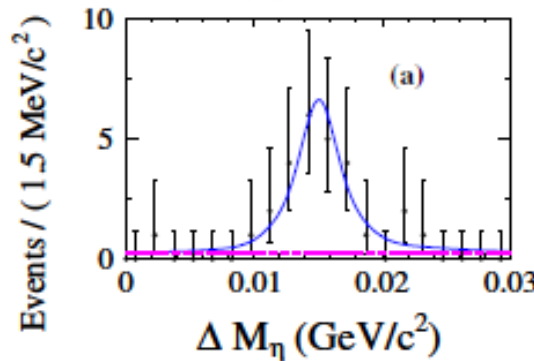
$$B[Y(2S) \rightarrow Y(1S)\eta] \sim 8 \times 10^{-4}$$

Experiment:

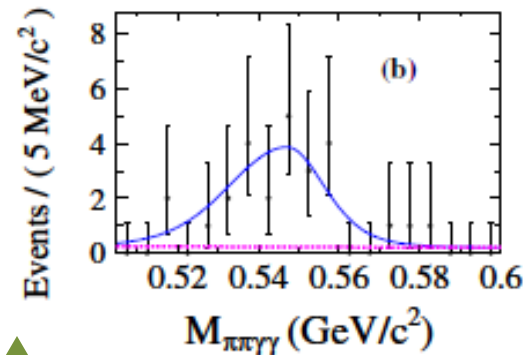
$$(2.39 \pm 0.31 \pm 0.14) \times 10^{-4}$$

$$(2.1 \pm 0.7 \pm 0.4) \times 10^{-4}$$

(CLEO, PRL101,192001)



$\eta \rightarrow \pi^+ \pi^- \pi^0$



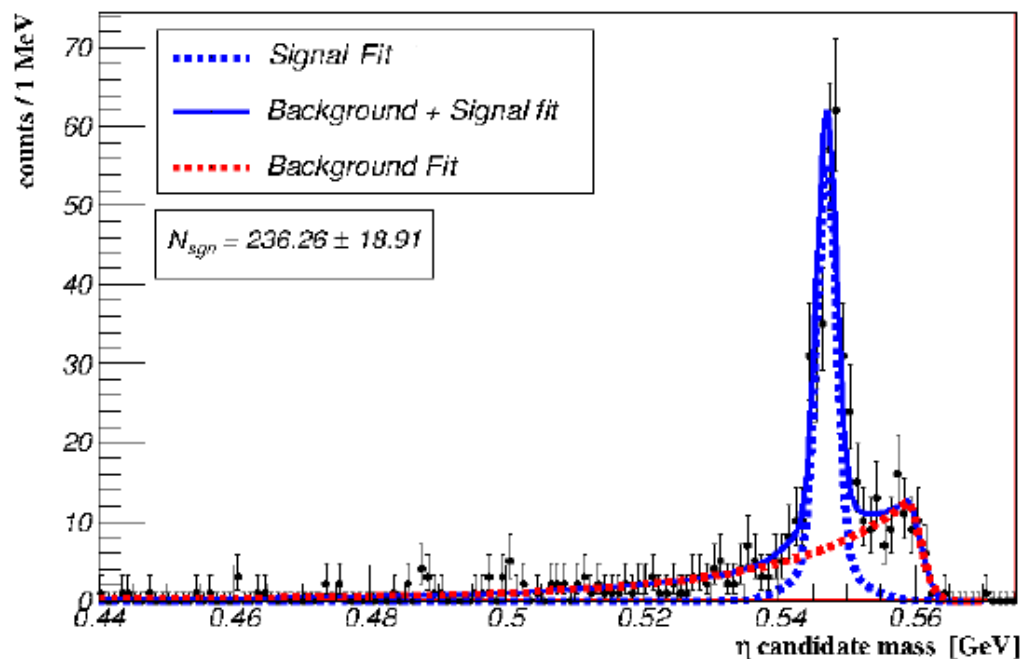
$\eta \rightarrow \gamma\gamma$

Phys.Rev.D 84 092003

$$B[Y(3S) \rightarrow Y(1S)\eta] < 1.0 \times 10^{-4}$$

$\Upsilon(2S) \rightarrow \eta, \pi^0 \Upsilon(1S)$

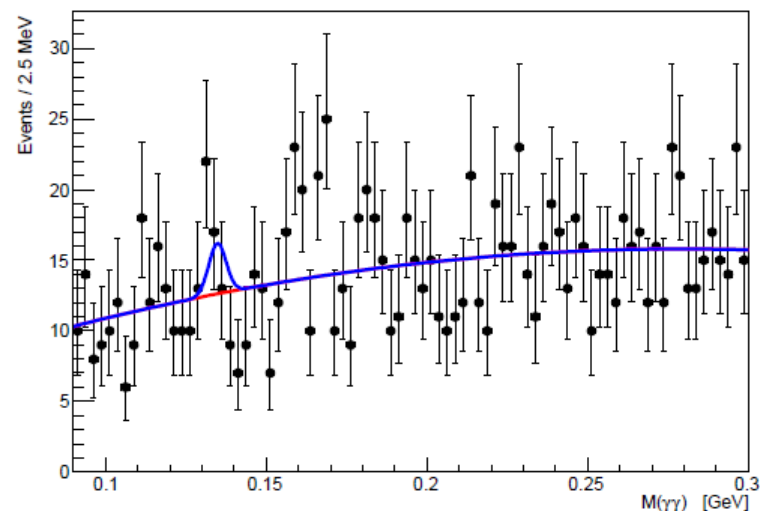
Preliminary



$$B[\Upsilon(2S) \rightarrow \Upsilon(1S)\eta] = (3.41 \pm 0.28 \pm 0.35) \times 10^{-4}$$

Still < half of theory prediction

- Exclusive analysis
- Normalized to $\Upsilon(2S) \rightarrow \pi^+ \pi^- \Upsilon(1S)$



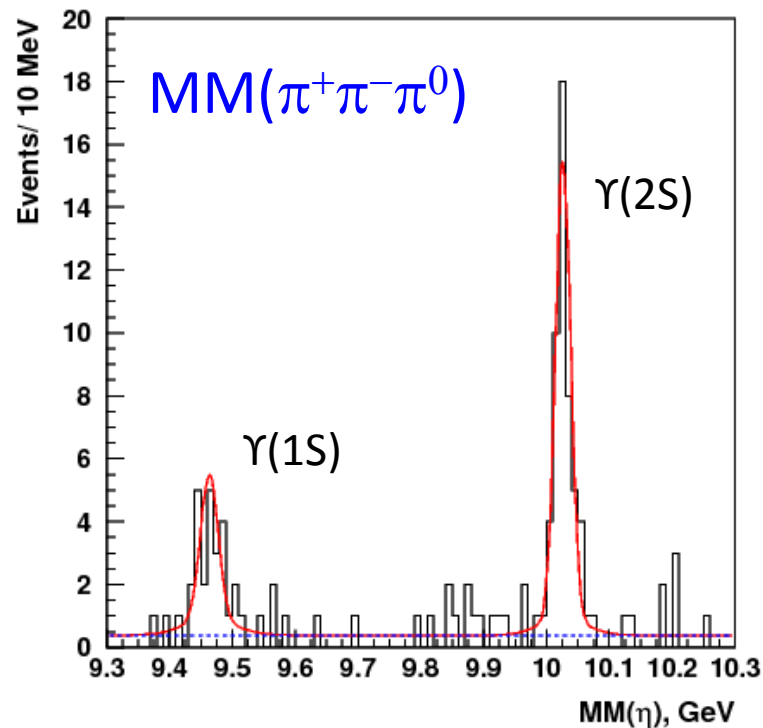
$$B(\Upsilon(2S) \rightarrow \pi^0 \Upsilon(1S)) < 0.43 \times 10^{-4} \text{ (90\% CL)}$$

$$\sim 6 \times 10^{-4} \text{ (Theory)}$$



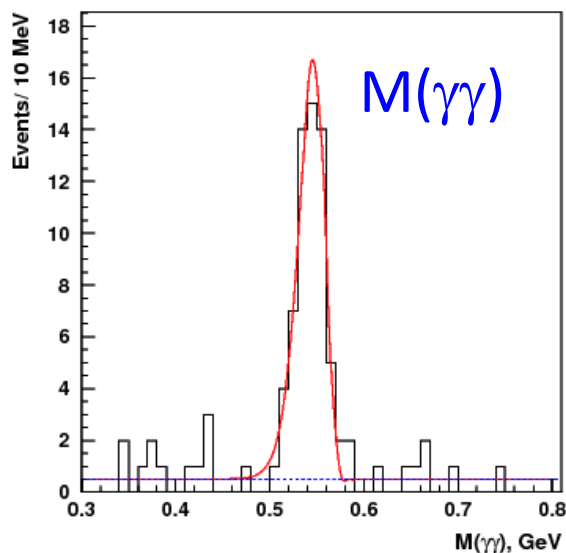
Scale from $\psi' \rightarrow \eta J/\psi$

Observation of $Y(5S) \rightarrow Y(1,2S)\eta$



- Three modes:
 - $Y(1,2S)[\mu^+\mu^-] \eta[\pi^+\pi^-\pi^0]$
 - $Y(2S)[Y(1S)\pi^+\pi^-] \eta[\gamma\gamma]$
 - $Y(1S)[\mu^+\mu^-] \eta'[\eta\pi^+\pi^-]$

preliminary

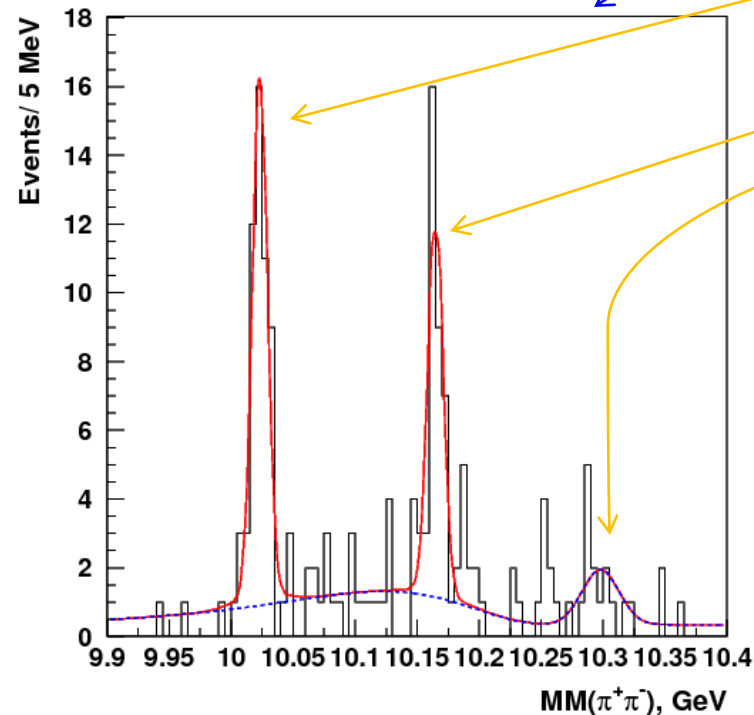
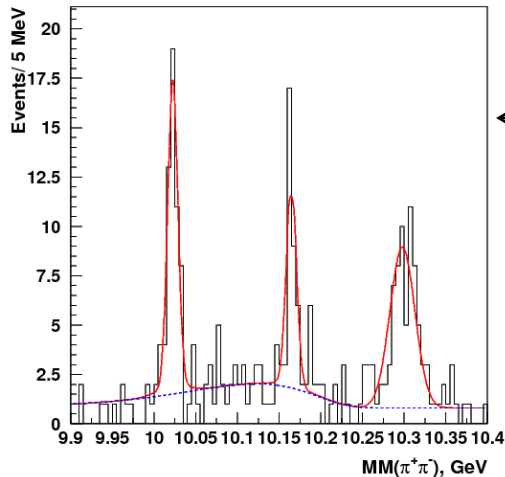


$$B[Y(5S) \rightarrow Y(1S)\eta] = (7.3 \pm 1.6 \pm 0.8) 10^{-4}$$

$$B[Y(5S) \rightarrow Y(2S)\eta] = (38 \pm 4 \pm 5) 10^{-4}$$

$$B[Y(5S) \rightarrow Y(1S)\eta'] < 1.2 10^{-4}$$

Observation of $Y(5S) \rightarrow Y(1D)\pi^+\pi^-$



- $Y(1S)[\mu^+\mu^-]\pi^+\pi^-\gamma\gamma$ final state

After $\chi_b(1P) \rightarrow Y\gamma$ selection

- Three peaks in $MM(\pi^+\pi^-)$:
- $Y(2S) \pi^+\pi^-$
- $Y(1D) \pi^+\pi^-$
- $Y(2S)[Y\pi^+\pi^-]\eta[\gamma\gamma]$ reflection

statistical significance 9σ

$$B[Y(5S) \rightarrow Y(2S)\pi^+\pi^-] = (7.5 \pm 1.1 \pm 0.8) \cdot 10^{-3} \text{ (cross check)}$$

$$B[Y(5S) \rightarrow Y(1D)\pi^+\pi^-] B[Y(1D) \rightarrow \chi_b(1P)\gamma \rightarrow Y(1S)\gamma\gamma] = (2.0 \pm 0.4 \pm 0.3) \times 10^{-4}$$

P.S. : An evidence of $Y(1D)$ was seen in inclusive $MM(\pi^+\pi^-)$ spectra

Summary

Belle's large $\Upsilon(5S)$ data gives unexpectedly new results.

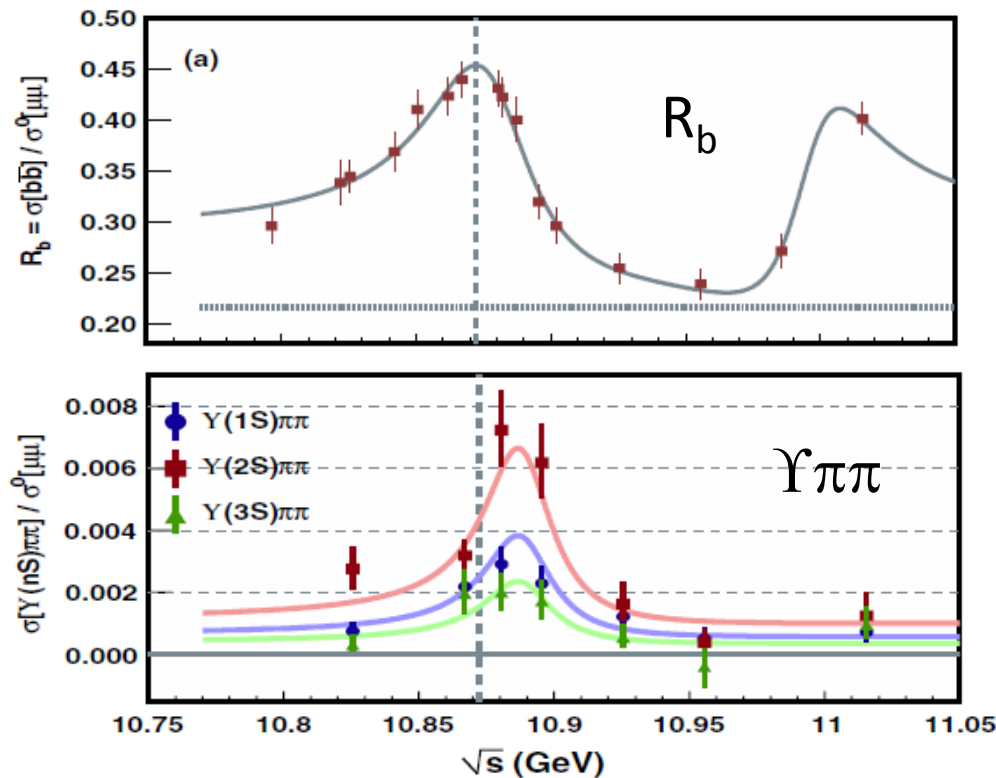
Inclusive $\gamma, \pi^0, \pi^+\pi^-$ spectrum is the main method in discovery of new states.

More results from exclusive reconstruction method.

- 
- $\Upsilon(5S)$
- Observation of $h_b(1P), h_b(2P), Z_{b1}^+, Z_{b2}^+$.
 - Exclusive method in final states $\Upsilon(nS)\pi^+\pi^-$.
 - Charm counterpart in $\Upsilon(4260)$ decay?
 - Observation of $h_b(1P) \rightarrow \eta_b(1S)\gamma$.
 - **Observation of $\eta_b(2S)$ from Belle and CLEO (S. Dobbs).**
 - Belle: $\Delta M_{\text{hfs}}(2S) = 24.3 \pm 4.3 \text{ MeV}$ $\text{Bf}[h_b(2P) \rightarrow \gamma \eta_b(2S)] = 47 \pm 13\%$
 - S. Dobbs (CLEO): $\Delta M_{\text{hfs}}(2S) = 48.7 \pm 2.7 \text{ MeV}$, no BF info.
 - Disagreement on the $\Delta M_{\text{hfs}}(2S)$.
 - Observation of $\chi_b(3P)$ from ATLAS and D0.
 - Observation of $\Upsilon(5S) \rightarrow \Upsilon(1,2S)\eta$. First measurement.
 - Observation of $\Upsilon(5S) \rightarrow \Upsilon(1D)\pi^+\pi^-$. First measurement.
 - Measurement of $\Upsilon(2S) \rightarrow \eta \Upsilon(1S)$ from Belle. Still smaller than theory.

BACKUP

(2) $\Upsilon(nS)\pi\pi$ production shape



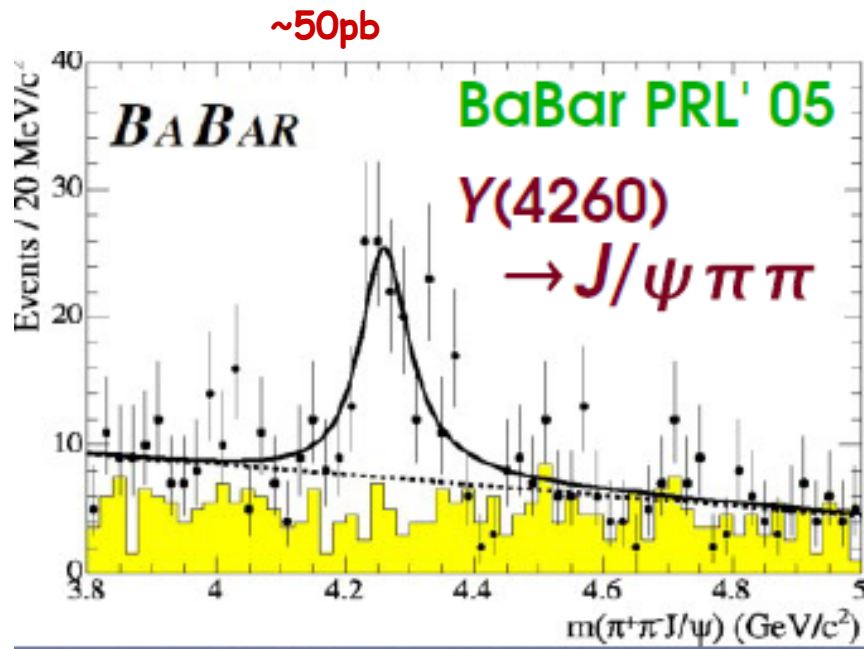
Belle, Phys.Rev., D82, 091106R (2010)

Energy scan $\Rightarrow$
mean of shapes of $\sigma(Y\pi\pi)$
and hadronic cross section R_b
shapes differ by 2.0σ

$$\mu_{Y\pi\pi} - \mu_{10860} = 9 \pm 4 \text{ MeV}/c^2$$

$Y(1S)\pi^+\pi^-\sigma_{\text{peak}}$ (pb)	$2.78^{+0.42}_{-0.34} \pm 0.23$
$Y(2S)\pi^+\pi^-\sigma_{\text{peak}}$ (pb)	$4.82^{+0.77}_{-0.62} \pm 0.66$
$Y(3S)\pi^+\pi^-\sigma_{\text{peak}}$ (pb)	$1.71^{+0.35}_{-0.31} \pm 0.24$
μ (MeV/ c^2)	$10888.4^{+2.7}_{-2.6} \pm 1.2$
Γ (MeV/ c^2)	$30.7^{+8.3}_{-7.0} \pm 3.1$

Reminder of $\Upsilon(4260)$



- Observed from initial state radiation events: $e^+e^- \rightarrow \gamma J/\psi \pi \pi$.
- Mass far above $D\bar{D}^{(*)}$ threshold.
- Width ~ 100 MeV (quite narrow).
- $J^{PC} = 1^{--}$ from production mechanism.

$$e^+e^- \rightarrow \gamma(\pi^+\pi^- J/\psi)$$



BaBar, Phys. Rev. Lett. **95**, 142001 (2005).
 arXiv:0808.1543v2.
 Belle, Phys. Rev. Lett. **99**, 182004 (2007).

$$e^+e^- \rightarrow \pi^+\pi^- J/\psi$$

$$e^+e^- \rightarrow \pi^0\pi^0 J/\psi$$



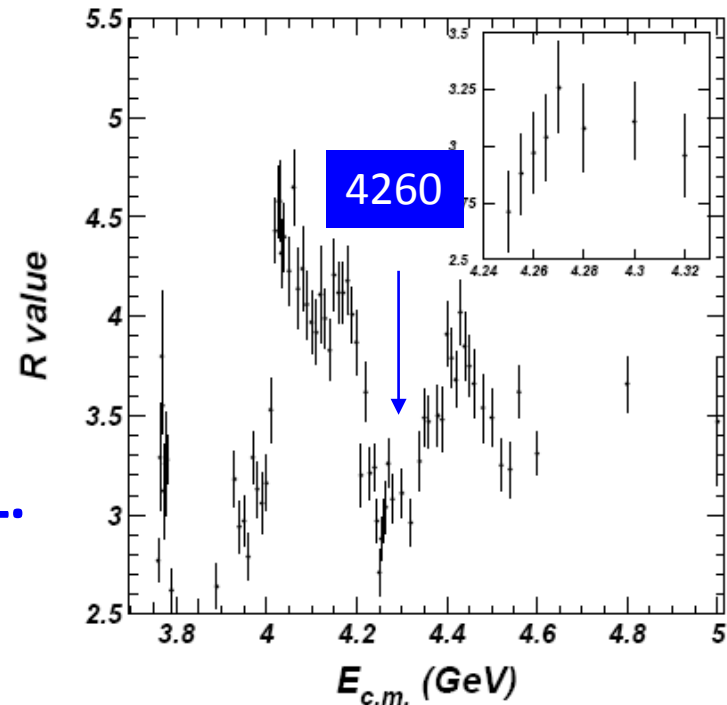
CLEO, Phys. Rev. Lett. **96**, 162003 (2006).

$\Upsilon(4260)$ notes

- Decay to $D\bar{D}^{(*)}$ not seen.
- Small coupling to e^+e^- ,
 $\text{BR}(J/\psi\pi^+\pi^-) \times \Gamma(e^+e^-)$
 $= 7.5 \pm 0.9 \pm 0.8 \text{ eV}$. BaBar, arXiv:0808.1543
- Small coupling to $p\bar{p}$
 $\text{BR}(\Upsilon(4260) \rightarrow p\bar{p}) /$
 $\text{BR}(\Upsilon(4260) \rightarrow J/\psi\pi^+\pi^-) < 0.13$.
BaBar, Phys.Rev.D73,012005(2006)
- $\Gamma(\Upsilon \rightarrow J/\psi\pi^+\pi^-) > 508 \text{ keV @ 90\% C.L.}$
 $\Rightarrow \text{Large !!}$

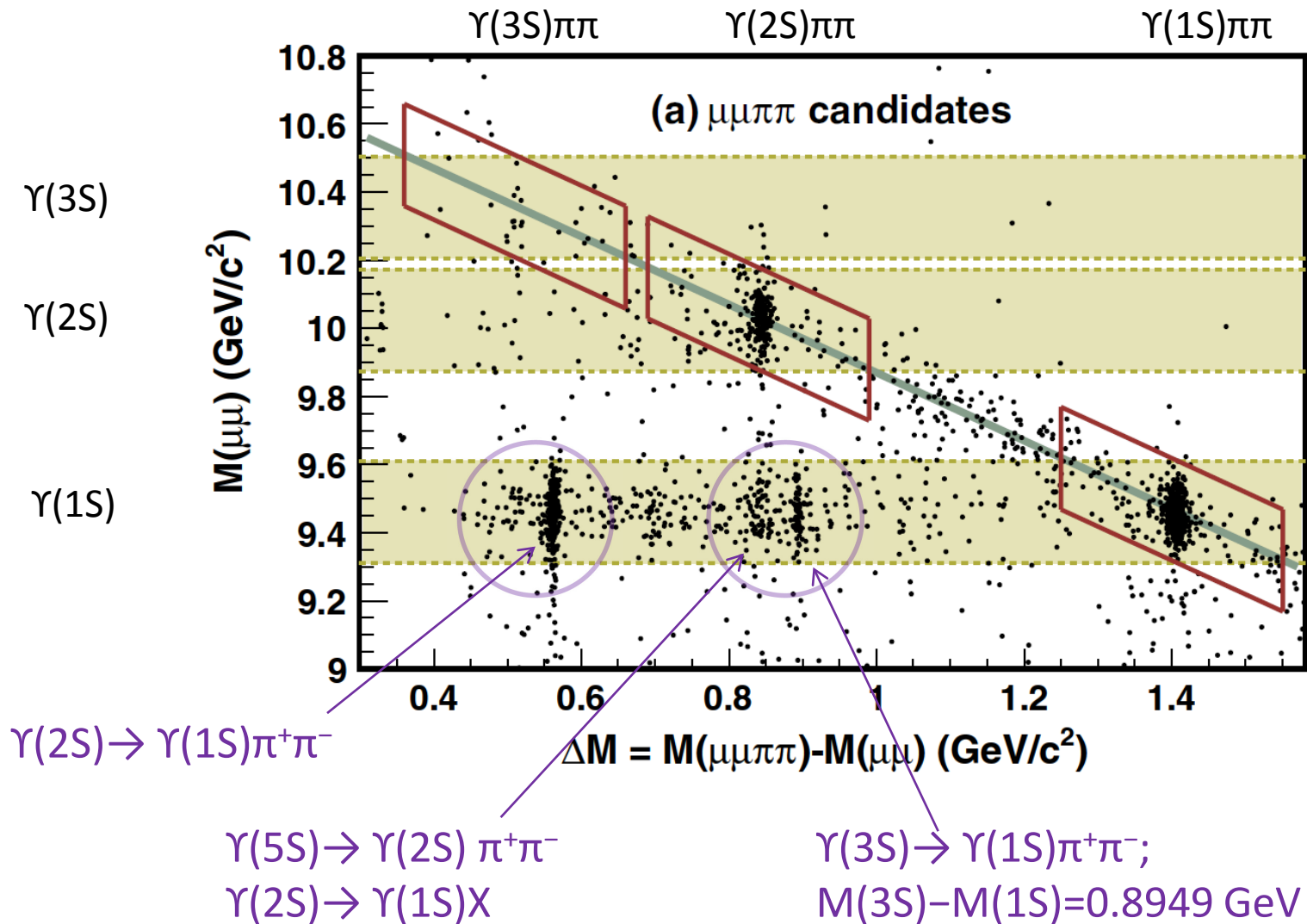
X. H. Mo et al., Phys. Lett. B 640 (2006) 182

BES, Phys.Rev.Lett.88.101802(2002)
At a dip in $\sigma(e^+e^-) \rightarrow \text{hadrons}$

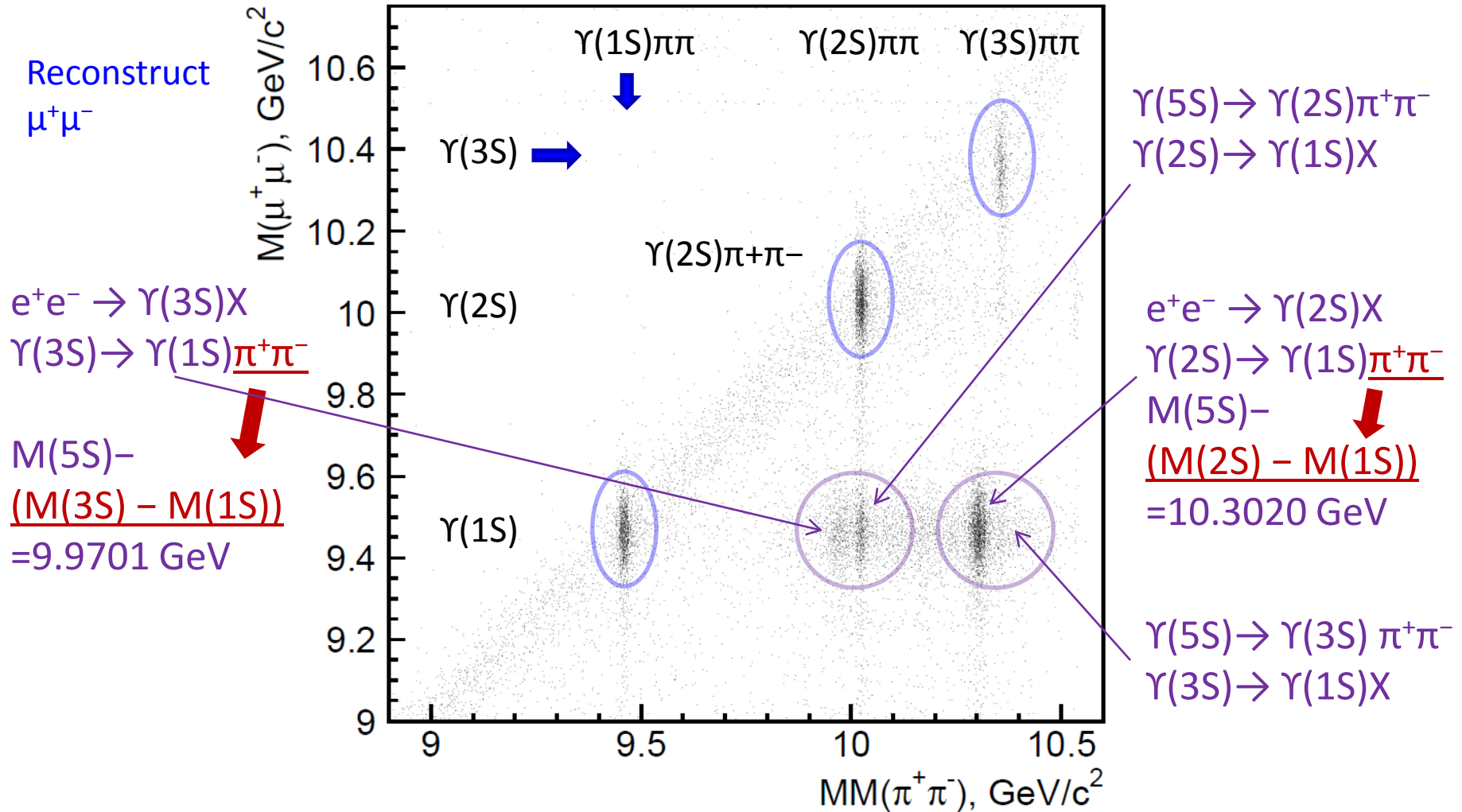


In b-sector, may be there also exists a counterpart Υ_b which has also large h_b branching fraction.

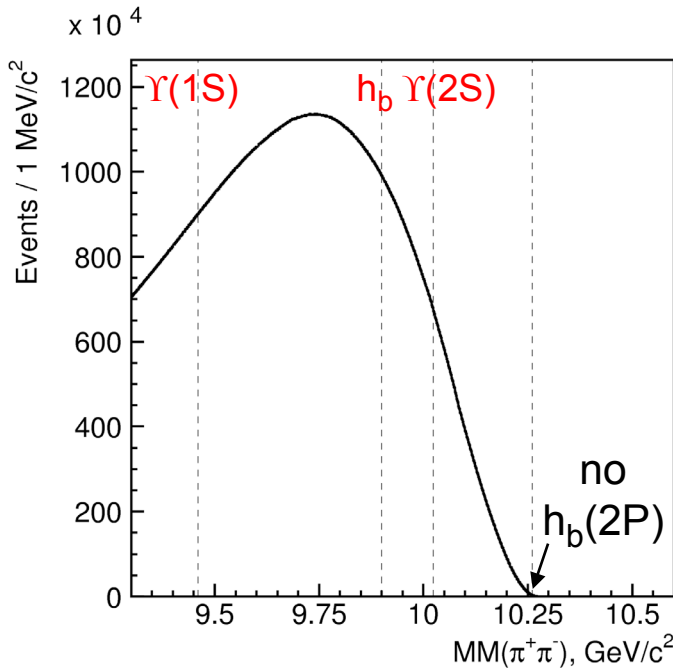
Exclusive (full) reconstruction



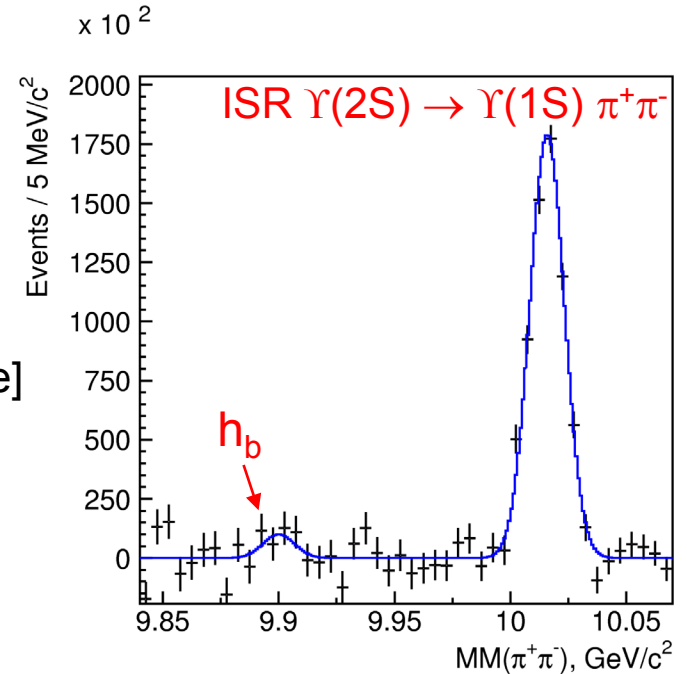
Missing mass technique: Calibration sources in $\Upsilon(5S)$ events



h_b in $\Upsilon(4S)$ data



$L = 711\text{fb}^{-1}$
[$\times 6$ $\Upsilon(5S)$ sample]



No significant signal of $h_b(1P)$: $(34 \pm 20) \times 10^3$ (1.7σ)

$$\frac{\sigma[e^+e^- \rightarrow h_b(1P) \pi^+\pi^-] @ \Upsilon(4S)}{\sigma[e^+e^- \rightarrow h_b(1P) \pi^+\pi^-] @ \Upsilon(5S)} < 0.28 \text{ at } 90\% \text{C.L.}$$

$\Rightarrow$ $\Upsilon(4S)$ does not show anomalous properties

Angular Analysis

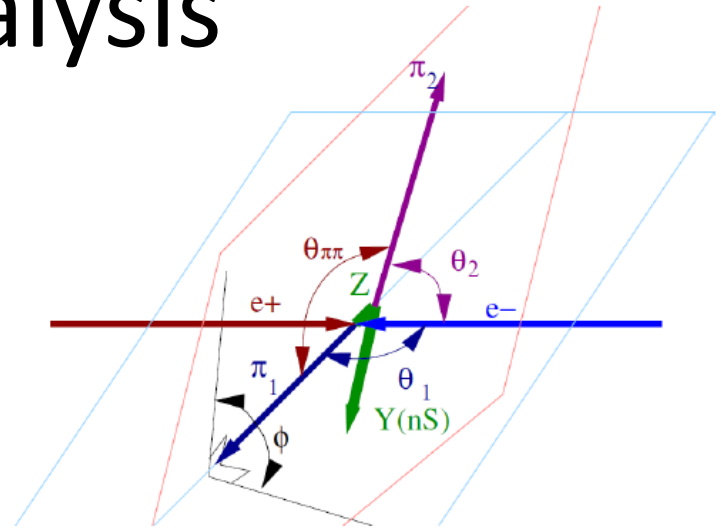
Z_b velocity is very small ($\beta < 0.02$) $\Rightarrow$ measure all pion momenta in the c.m. frame.

$$\Upsilon(5S) \rightarrow Z_b(\Upsilon(nS), h_b + \pi_1) \pi_2$$

$$\theta_1 = \angle(\pi_1, e^+)$$

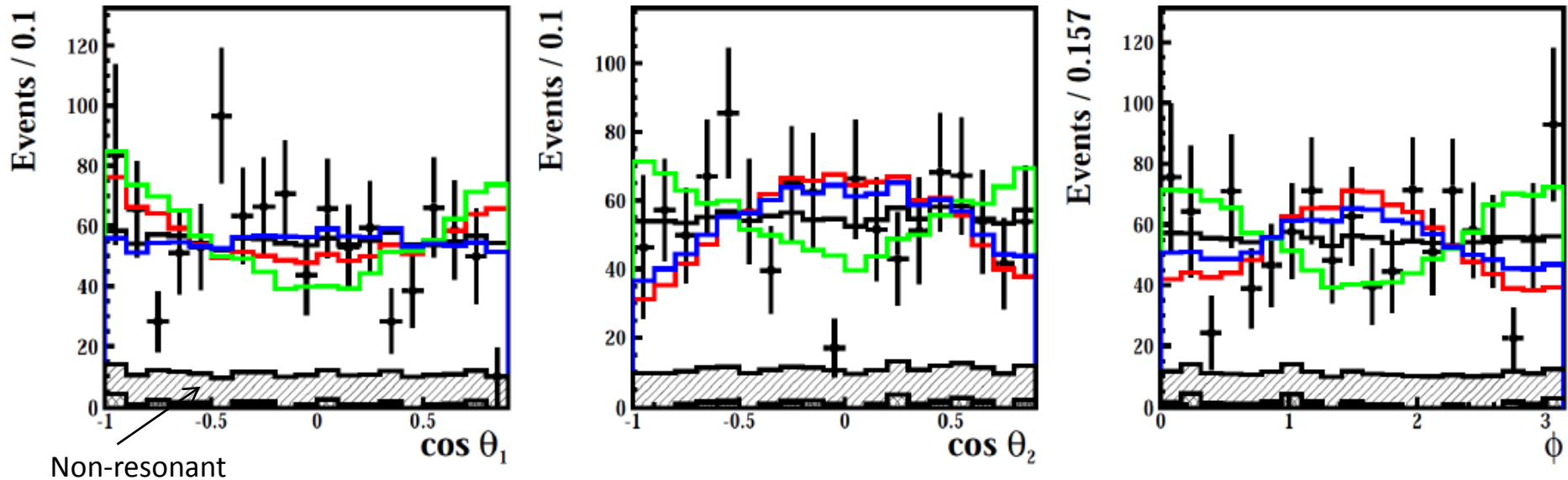
$$\theta_2 = \angle(\pi_2, e^+)$$

$$\phi = \angle(\text{plane}(\pi_1, e^+), \text{plane}(\pi_1, \pi_2))$$



$$J^P = 1^+, 1^-, 2^+, 2^-$$

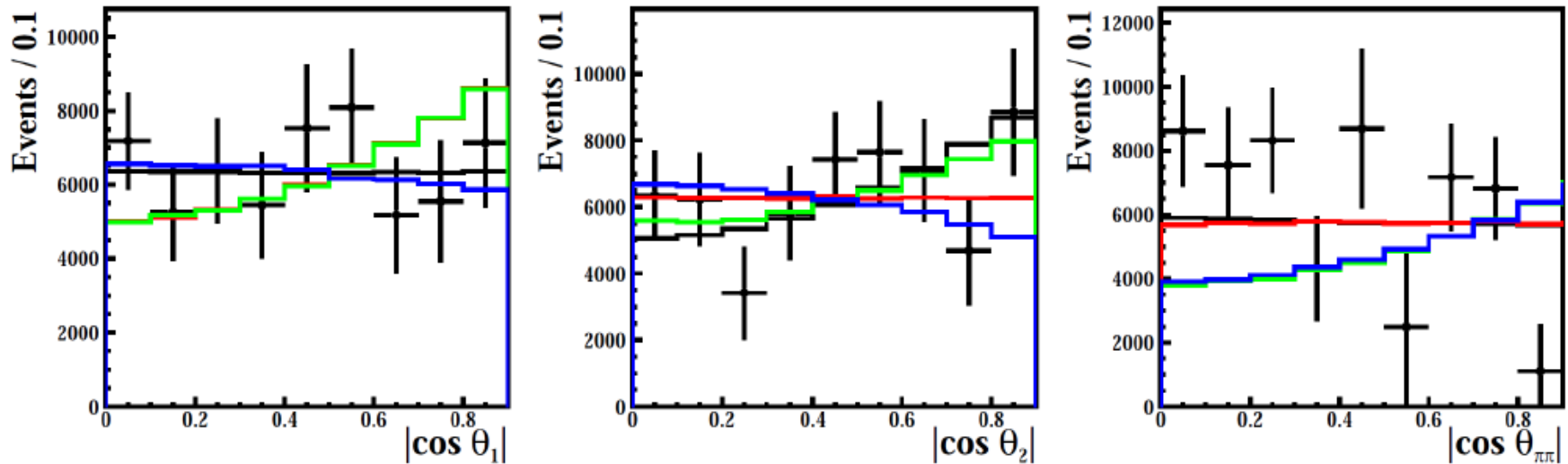
Example: $\Upsilon(5S) \rightarrow Z_b(10610) \pi_2 \rightarrow \Upsilon(2S) \pi_1 \pi_2$



Angular Analysis (h_b final state)

$J^P = 1^+, 1^-, 2^+, 2^-$

Example: $\Upsilon(5S) \rightarrow Z_b(10610) \pi_2 \rightarrow h_b(1P) \pi_1 \pi_2$



Probabilities at which other J^P hypotheses are disfavored with respect to 1^+

J^P	$Z_b(10610)$			$Z_b(10650)$		
	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$
1^-	3.6σ	0.3σ	0.3σ	3.7σ	2.6σ	2.7σ
2^+	4.3σ	3.5σ	4.3σ	4.4σ	2.7σ	2.1σ
2^-	2.7σ	2.8σ		2.9σ	2.6σ	

$J^P = 1^+$ is favored!

$$Y(5S) \rightarrow Y(1S) \eta'$$

