# **Particle Detectors**

Summer Student Lectures 2008 Werner Riegler, CERN, werner.riegler@cern.ch

- ♦ History of Instrumentation ↔ History of Particle Physics
- The 'Real' World of Particles
- Interaction of Particles with Matter
- Tracking Detectors, Calorimeters, Particle Identification
- Detector Systems

# **Particle Detectors**

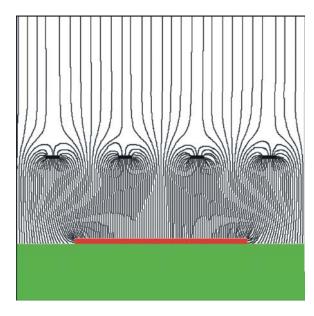
Detector-Physics: Precise knowledge of the processes leading to signals in particle detectors is necessary.

The detectors are nowadays working close to the limits of theoretically achievable measurement accuracy – even in large systems.

Due to available computing power, detectors can be simulated to within 5-10% of reality, based on the fundamental microphysics processes (atomic and nuclear crossections).

## **Particle Detector Simulation**

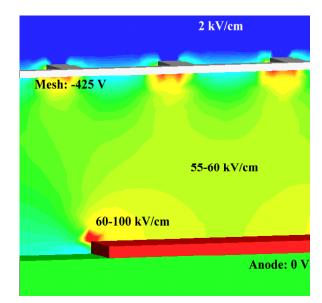
Electric Fields in a Micromega Detector



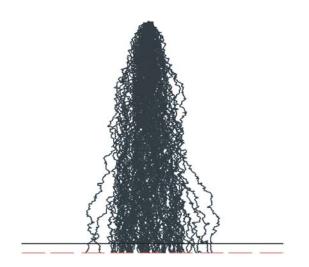
Very accurate simulations of particle detectors are possible due to availability of Finite Element simulation programs and computing power.

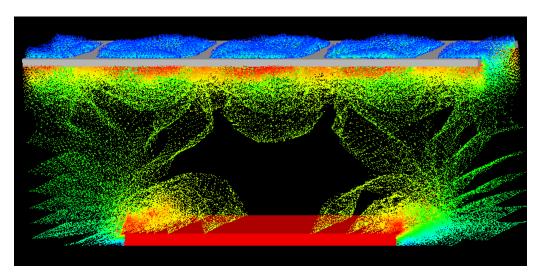
Follow every single electron by applying first principle laws of physics.

Electric Fields in a Micromega Detector



Electrons avalanche multiplication



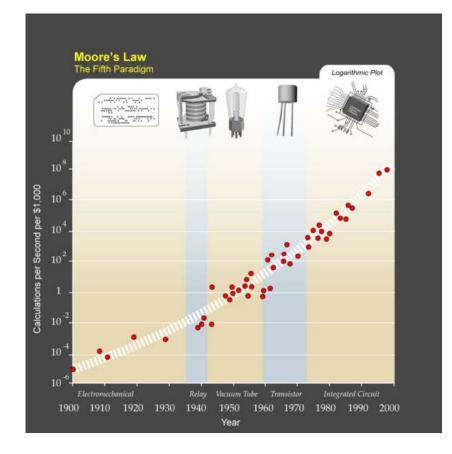


## **Particle Detector Simulation**

### I) C. Moore's Law: Computing power doubles 18 months.

II) W. Riegler's Law: The use of brain for solving a problem is inversely proportional to the available computing power.

 $\rightarrow$  I) + II) = ...



Knowing the basics of particle detectors is essential ...

## **Interaction of Particles with Matter**

Any device that is to detect a particle must interact with it in some way  $\rightarrow$  almost ...

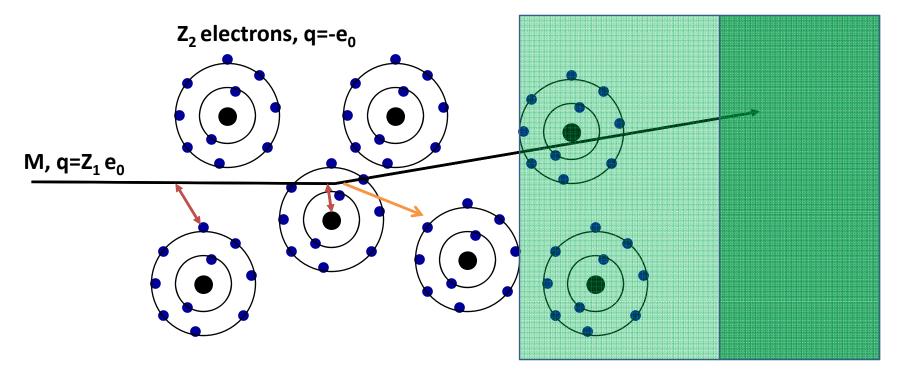
In many experiments neutrinos are measured by missing transverse momentum.

E.g.  $e^+e^-$  collider.  $P_{tot}=0$ , If the  $\Sigma p_i$  of all collision products is  $\neq 0 \rightarrow$  neutrino escaped.

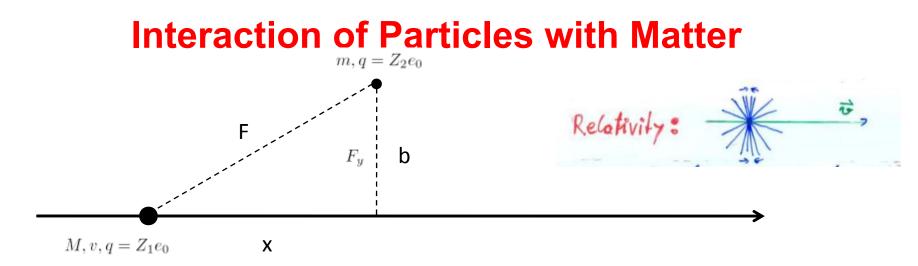


Claus Grupen, Particle Detectors, Cambridge University Press, Cambridge 1996 (455 pp. ISBN 0-521-55216-8) W. Riegler/CERN

## **Electromagnetic Interaction of Particles with Matter**



Interaction with the atomic electrons. The incoming particle loses energy and the atoms are <u>excited</u> or <u>ionized.</u> Interaction with the atomic nucleus. The particle is deflected (scattered) causing <u>multiple scattering of</u> the particle in the material. During this scattering a <u>Bremsstrahlung</u> photon can be emitted. In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as <u>Cherenkov Radiation</u>. When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.



While the charged particle is passing another charged particle, the Coulomb Force is acting, resulting in momentum transfer

$$F_y = \frac{Z_1 Z_2 e_0^2}{4\pi\varepsilon_0 (b^2 + v^2 t^2)} \frac{b}{\sqrt{b^2 + v^2 t^2}} \qquad \qquad \Delta p = \int_{-\infty}^{\infty} F_y(t) dt = \frac{2Z_1 Z_2 e_0^2}{4\pi\varepsilon_0 v b}$$

The relativistic form of the transverse electric field doesn't change the momentum transfer. The transverse field is stronger, but the time of action is shorter

$$F_{y} = \frac{\gamma Z_{1} Z_{2} e_{0}^{2} b}{4\pi\varepsilon_{0} (b^{2} + \gamma^{2} v^{2} t^{2})^{3/2}} \qquad \Delta p = \int_{-\infty}^{\infty} F_{y}(t) dt = \frac{2Z_{1} Z_{2} e_{0}^{2}}{4\pi\varepsilon_{0} v b}$$
The transferred energy is then
$$\Delta E = \frac{(\Delta p)^{2}}{2m} = \frac{Z_{2}^{2}}{m} \frac{2Z_{1}^{2} e_{0}^{4}}{(4\pi\varepsilon_{0})^{2} v^{2} b^{2}}$$

$$\Delta E(electrons) = Z_{2} \frac{1}{m_{e}} \frac{2Z_{1}^{2} e_{0}^{4}}{(4\pi\varepsilon_{0})^{2} v^{2} b^{2}} \qquad \Delta E(nucleus) = \frac{Z_{2}^{2}}{2Z_{2} m_{p}} \frac{2Z_{1}^{2} e_{0}^{4}}{(4\pi\varepsilon_{0})^{2} v^{2} b^{2}} \qquad \frac{\Delta E(electrons)}{\Delta E(nucleus)} = \frac{2m_{p}}{m_{e}} \approx 4000$$

### $\rightarrow$ The incoming particle transfer energy only (mostly) to the atomic electrons !

7/8/2008

The

## **Interaction of Particles with Matter**

Target material: mass A, Z<sub>2</sub>, density  $\rho$  [g/cm<sup>3</sup>], Avogadro number N<sub>A</sub>

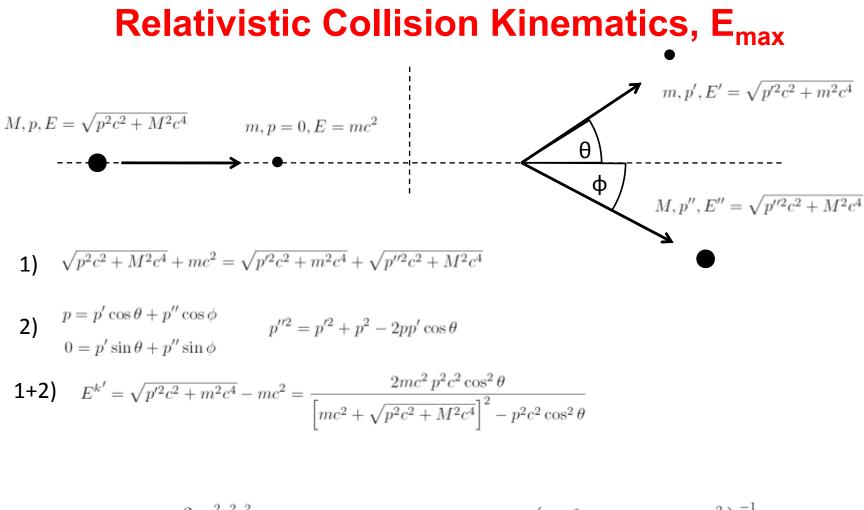
A gramm  $\rightarrow$  N<sub>A</sub> Atoms:Number of atoms/cm³<br/>Number of electrons/cm³n<sub>a</sub> = N<sub>A</sub>  $\rho$ /A[1/cm³]<br/>n<sub>e</sub> = N<sub>A</sub>  $\rho$ Z<sub>2</sub>/A $\Delta E(electrons) = \frac{2Z_2Z_1^2m_ec^2}{\beta^2b^2} \frac{e_0^4}{(4\pi\varepsilon_0m_ec^2)^2} = \frac{2Z_2Z_1^2m_ec^2}{\beta^2b^2} r_e^2$  $\widetilde{\rho}^2$ 

$$dE = -\int_{b_{min}}^{b_{max}} n_e \Delta E dx 2b\pi db = -\frac{4\pi Z_2 Z_1^2 m_e c^2 r_e^2}{\beta^2} \frac{N_A \rho}{A} \int_{b_{min}}^{b_{max}} \frac{db}{b}$$

With  $\Delta E(b) \rightarrow db/b = -1/2 dE/E \rightarrow E_{max} = \Delta E(b_{min}) E_{min} = \Delta E(b_{max})$ 

$$\frac{dE}{dx} = -2\pi r_e^2 m_e^2 c^2 \frac{Z_1^2}{\beta^2} \frac{N_A Z_2 \rho}{A} \int_{E_{min}}^{E_{max}} \frac{dE}{E} \qquad = \qquad -2\pi r_e^2 m_e^2 c^2 \frac{Z_1^2}{\beta^2} \frac{N_A Z_2 \rho}{A} \ln \frac{E_{max}}{E_{min}} \frac{dE}{E}$$

## $E_{min} \approx I$ (Ionization Energy)



$$E^{k'}_{max} = \frac{2mc^2 p^2 c^2}{(m^2 + M^2)c^4 + 2m\sqrt{p^2 c^2 + M^2 c^4}} = 2mc^2 \beta^2 \gamma^2 F \qquad F = \left(1 + \frac{2m}{M}\sqrt{1 + \beta^2 \gamma^2} + \frac{m^2}{M^2}\right)^{-1}$$

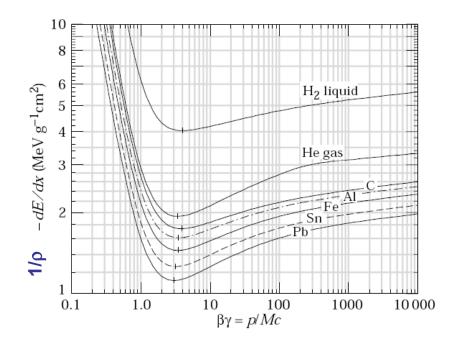
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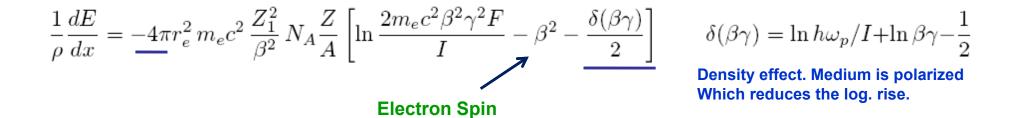
### **Classical Scattering on Free Electrons**

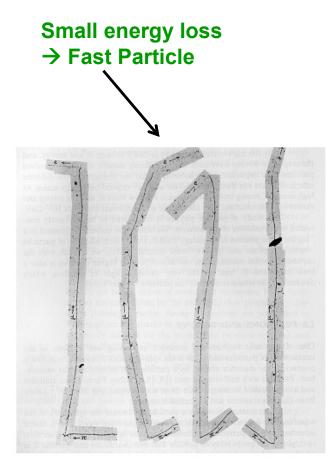
$$\frac{1}{\rho}\frac{dE}{dx} = -2\pi r_e^2 m_e c^2 \frac{Z_1^2}{\beta^2} N_A \frac{Z}{A} \ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I}$$

This formula is up to a factor 2 and the density effect identical to the precise QM derivation  $\rightarrow$ 

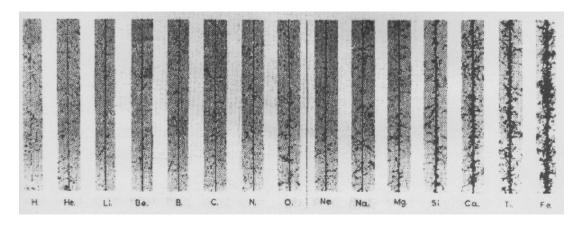
### **Bethe Bloch Formula**



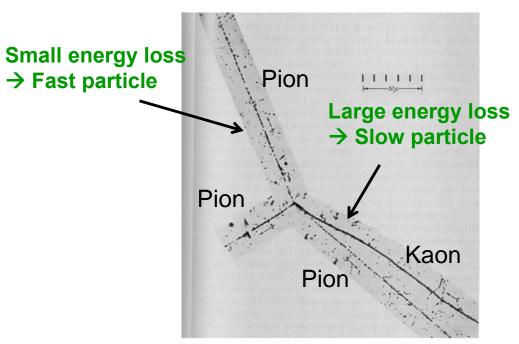




Discovery of muon and pion



### Cosmis rays: dE/dx $\alpha$ Z<sup>2</sup>



## **Bethe Bloch Formula**

$$\frac{1}{\rho}\frac{dE}{dx} = -4\pi r_e^2 \, m_e c^2 \, \frac{Z_1^2}{\beta^2} \, N_A \frac{Z}{A} \left[ \ln \frac{2m_e c^2 \beta^2 \gamma^2 F}{I} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

Für Z>1, I ≈16Z <sup>0.9</sup> eV

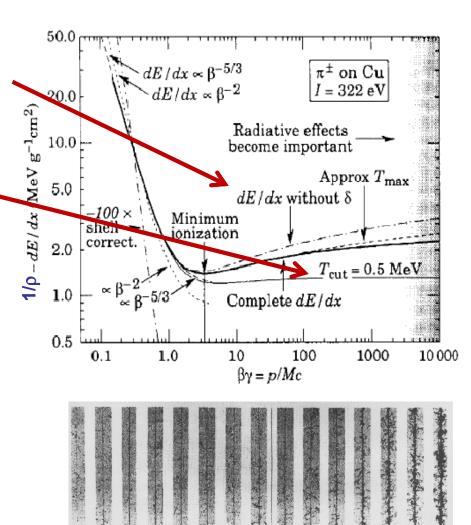
For Large  $\beta\gamma$  the medium is being polarized by the strong transverse fields, which reduces the rise of the energy loss  $\rightarrow$  density effect

At large Energy Transfers (delta electrons) the liberated electrons can leave the material. In reality,  $E_{max}$  must be replaced by  $E_{cut}$  and the energy loss reaches a plateau (Fermi plateau).

Characteristics of the energy loss as a function of the particle velocity ( $\beta\gamma$ )

The specific Energy Loss 1/p dE/dx

- firts decreaes as  $1/\beta^2$
- increases with In  $\gamma$  for  $\beta$  =1
- is  $\approx$  independent of M (M>>m<sub>e</sub>)
- is proportional to Z<sub>1</sub><sup>2</sup> of the incoming particle.
- is  $\approx$  independent of the material (Z/A  $\approx$  const)
- shows a pleateau at large  $\beta\gamma$  (>>100)
- •dE/dx  $\approx$  1-2 x  $\rho$  [g/cm<sup>3</sup>] MeV/cm



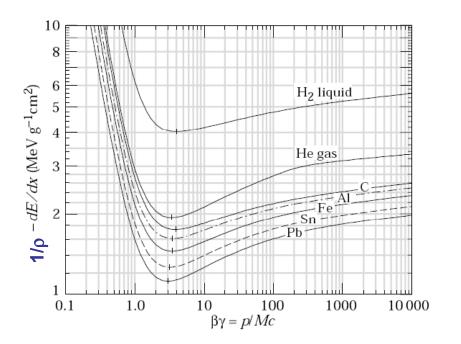
### **Bethe Bloch Formula**

Bethe Bloch Formula, a few Numbers:

For Z  $\approx$  0.5 A 1/ $\rho$  dE/dx  $\approx$  1.4 MeV cm <sup>2</sup>/g for  $\beta\gamma \approx$  3

Example : Iron: Thickness = 100 cm;  $\rho$  = 7.87 g/cm<sup>3</sup> dE  $\approx$  1.4 \* 100\* 7.87 = 1102 MeV

→ A 1 GeV Muon can traverse 1m of Iron



This number must be multiplied with  $\rho$  [g/cm<sup>3</sup>] of the Material  $\rightarrow$  dE/dx [MeV/cm]

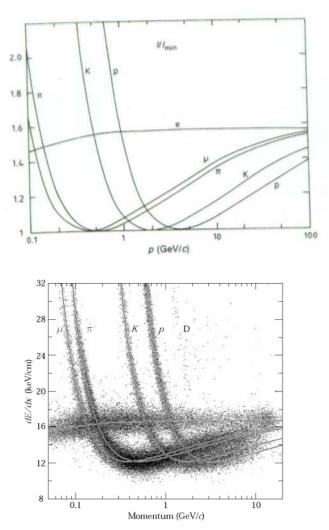
### **Energy Loss as a Function of the Momentum**

Energy loss depends on the particle velocity and is ≈ independent of the particle's mass M.

The energy loss as a function of particle Momentum  $P = Mc\beta\gamma$  IS however depending on the particle's mass

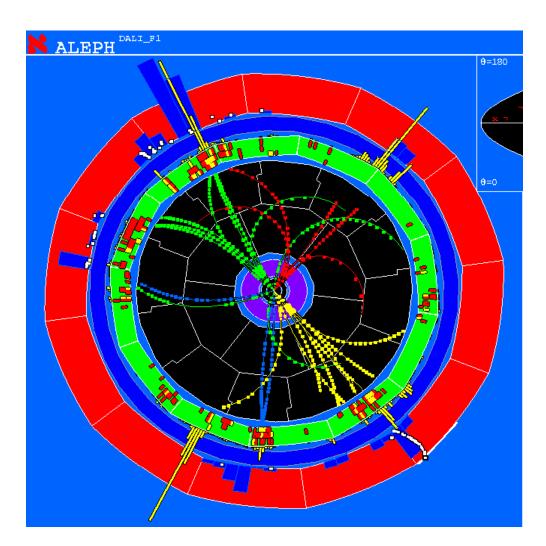
By measuring the particle momentum (deflection in the magnetic field) and measurement of the energy loss on can measure the particle mass

### → Particle Identification !



$$\frac{1}{\rho}\frac{dE}{dx} = -4\pi r_e^2 m_e c^2 Z_1^2 \frac{p^2 + M^2 c^2}{p^2} N_A \frac{Z}{A} \left[ \ln \frac{2m_e c^2 F}{I} \frac{p^2}{M^2 c^2} - \frac{p^2}{p^2 + M^2 c^2} \right]$$

### **Energy Loss as a Function of the Momentum**



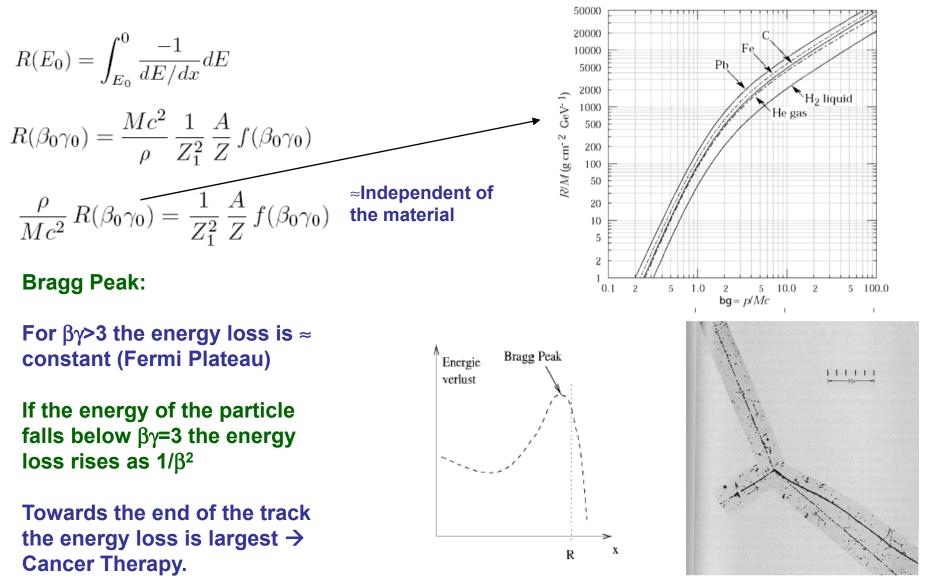
Measure momentum by curvature of the particle track.

Find dE/dx by measuring the deposited charge along the track.

→Particle ID

## **Range of Particles in Matter**

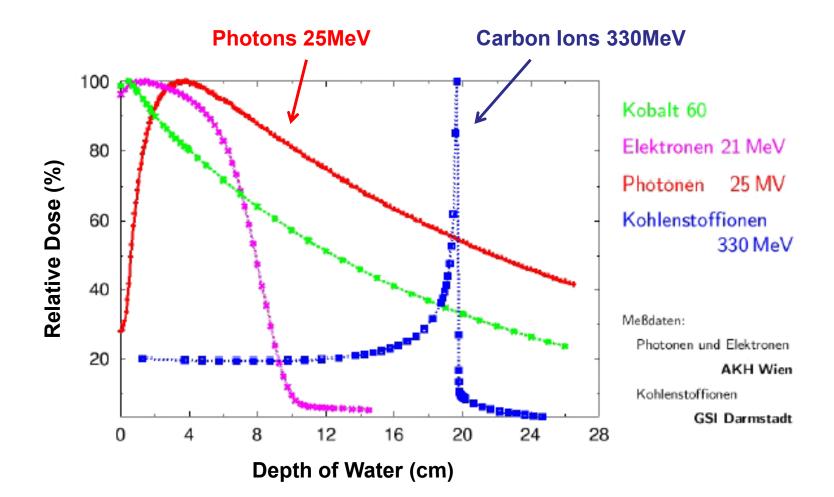
# Particle of mass M and kinetic Energy E<sub>0</sub> enters matter and looses energy until it comes to rest at distance R.



### **Range of Particles in Matter**

### Average Range:

Towards the end of the track the energy loss is largest  $\rightarrow$  Bragg Peak  $\rightarrow$  Cancer Therapy

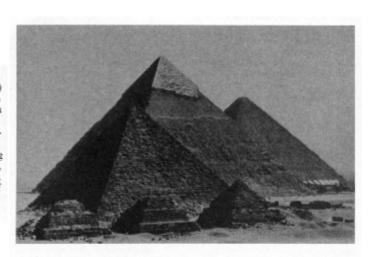


## Search for Hidden Chambers in the Pyramids

The structure of the Second Pyramid of Giza is determined by cosmic-ray absorption.

Luis W. Alvarez, Jared A. Anderson, F. El Bedwei, James Burkhard, Ahmed Fakhry, Adib Girgis, Amr Goneid, Fikhny, Hassan, Dennis Iverson, Gerald Lynch, Zenab Miligy, Ali Hilmy Moussa, Mohammed-Sharkawi, Lauren Yazolino Fig. 2 (bottom right). Cross sections of (a) the Great Pyramid of Cheops and (b) the Pyramid of Chephren, showing the known chambers: (A) Smooth limestone cap. (B) the Belzoni Chamber, (C) Belzoni's entrance, (D) Howard-Vyse's entrance, UN descending passageway, (F) ascending passageway, (G) underground chamber, (/-1) Grand Gallery, (J) King's Chamber, (J) Queen's Chamber, (K) center line of the pyramid.

6 FEBRUARY 1970



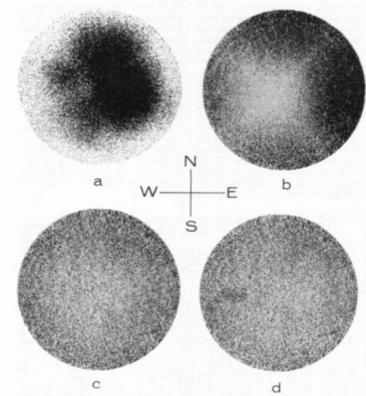
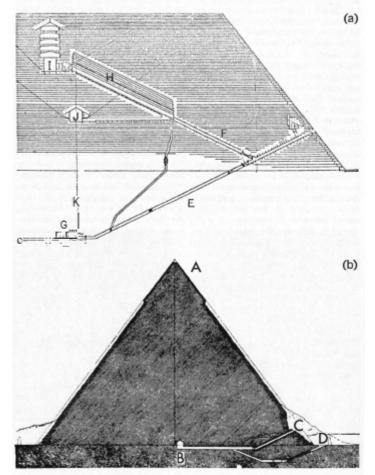


Fig. 13. Scatter plots showing the three stages in the combined analytic and visual analysis of the data and a plot with a simulated chamber, (a) Simulated "x-ray photograph" of uncorrected data. (b) Data corrected for the geometrical acceptance of the apparatus. (c) Data corrected for pyramid structure as well as geometrical acceptance. (d) Same as (c) but with simulated chamber, as in Fig. 12.

W. Riegler, Particle Detectors Luis Alvarez used the attenuation of muons to look for chambers in the Second Giza Pyramid → Muon Tomography

He proved that there are no chambers present.



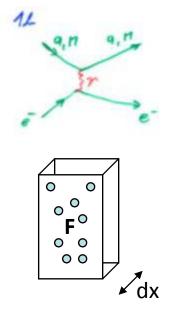
## **Intermezzo: Crossection**

Crossection  $\sigma$ : Material with Atomic Mass A and density  $\,\rho$  contains n Atoms/cm^3

$$n[\rm{cm}^{-3}] = \frac{N_A[\rm{mol}^{-1}]\,\rho[\rm{g/cm}^3]}{A[\rm{g/mol}]} \qquad N_A = 6.022 \times 10^{23}\,\rm{mol}^{-1}$$

E.g. Atom (Sphere) with Radius R: Atomic Crossection  $\sigma = R^2 \pi$ 

A volume with surface F and thickness dx contains N=nFdx Atoms. The total 'surface' of atoms in this volume is N  $\sigma$ . The relative area is  $p = N \sigma/F = N_A \rho \sigma /A dx =$ Probability that an incoming particle hits an atom in dx.



What is the probability P that a particle hits an atom between distance x and x+dx ? P = probability that the particle does NOT hit an atom in the m=x/dx material layers and that the particle DOES hit an atom in the  $m^{th}$  layer

$$P(x)dx = (1-p)^m p \approx e^{-m} p = \exp\left(-\frac{N_A\rho\sigma}{A}x\right) \frac{N_A\rho\sigma}{A}dx = \frac{1}{\lambda}\exp\left(-\frac{x}{\lambda}\right)dx \qquad \lambda = \frac{A}{N_A\rho\sigma}dx$$

**Mean free path** 
$$= \int_0^\infty x P(x) dx = \int_0^\infty \frac{x}{\lambda} e^{-\frac{x}{\lambda}} dx = \lambda$$

Average number of collisions/cm 
$$= \frac{1}{\lambda} = \frac{N_A \rho \sigma}{A}$$

## **Intermezzo: Differential Crossection**



**Differential Crossection:**  $\frac{d\sigma(E, E')}{dE'}$ 

→ Crossection for an incoming particle of energy E to lose an energy between E' and E'+dE'

Total Crossection: 
$$\sigma(E) = \int \frac{d\sigma(E, E')}{dE'} dE'$$

Probability P(E) that an incoming particle of Energy E loses an energy between E' and E'+dE' in a collision:

$$P(E, E')dE' = \frac{1}{\sigma(E)} \frac{d\sigma(E, E')}{dE'} dE'$$

Average number of collisions/cm causing an energy loss between E' and E'+dE' =  $\frac{N_A \rho}{A} \frac{d\sigma(E, E')}{dE'}$ 

Average energy loss/cm:

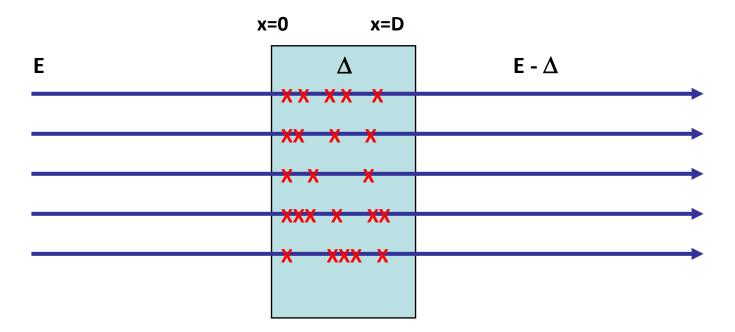
$$\frac{dE}{dx} = -\frac{N_A \rho}{A} \int E' \frac{d\sigma(E, E')}{dE'} dE'$$

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W. Riegler, Particle Detectors

## **Fluctuation of Energy Loss**

Up to now we have calculated the average energy loss. The energy loss is however a statistical process and will therefore fluctuate from event to event.



 $P(\Delta)$  = ? Probability that a particle loses an energy  $\Delta$  when traversing a material of thickness D

We have see earlier that the probability of an interaction ocuring between distance x and x+dx is exponentially distributed

$$P(x)dx = \frac{1}{\lambda}\exp\left(-\frac{x}{\lambda}\right)dx \qquad \lambda = \frac{A}{N_A\rho\sigma}$$

## **Probability for n Interactions in D**

We first calculate the probability to find n interactions in D, knowing that the probability to find a distance x between two interactions is  $P(x)dx = 1/\lambda \exp(-x/\lambda) dx$  with  $\lambda = A/N_A \rho \sigma$ 

Probability to have no interaction between 0 und D:

$$P(x > D) = \int_D^\infty P(x_1) dx_1 = e^{-\frac{D}{\lambda}}$$

Probability to have one interaction at  $x_1$  and no other interaction:

$$P(x_1, x_2 > D) = \int_D^\infty P(x_1) P(x_2 - x_1) dx_2 = \frac{1}{\lambda} e^{-\frac{D}{\lambda}}$$

Probability to have one interaction independently of  $x_1$ :

$$\int_0^D P(x_1, x_2 > D) = \frac{D}{\lambda} e^{-\frac{D}{\lambda}}$$

Probability to have the first interaction at  $x_1$ , the second at  $x_2$  .... the  $n^{th} \in x_n$  and no other interaction:

$$P(x_1, x_2...x_n > D) = \int_D^\infty P(x_1)P(x_2 - x_1)...P(x_n - x_{n-1})dx_n = \frac{1}{\lambda^n}e^{-\frac{D}{\lambda}}$$

Probability for *n* interactions independently of  $x_1, x_2...x_n$ 

$$\int_{0}^{D} \int_{0}^{x_{n-1}} \int_{0}^{x_{n-1}} \dots \int_{0}^{x_{1}} P(x_{1}, x_{2}..., x_{n} > D) dx_{1}...dx_{n-1} = \frac{1}{n!} \left(\frac{D}{\lambda}\right)^{n} e^{-\frac{D}{\lambda}}$$

## **Probability for n Interactions in D**

For an interaction with a mean free path of  $\lambda$  , the probability for n interactions on a distance D is given by

$$P(n) = \frac{1}{n!} \left(\frac{D}{\lambda}\right)^n e^{-\frac{D}{\lambda}} = \frac{\overline{n}^n}{n!} e^{-\overline{n}} \qquad \overline{n} = \frac{D}{\lambda} \qquad \lambda = \frac{A}{N_A \rho \sigma}$$

 $\rightarrow$  Poisson Distribution !

If the distance between interactions is exponentially distributed with an mean free path of  $\lambda \rightarrow$ the number of interactions on a distance D is Poisson distributed with an average of  $\bar{n}=D/\lambda$ .

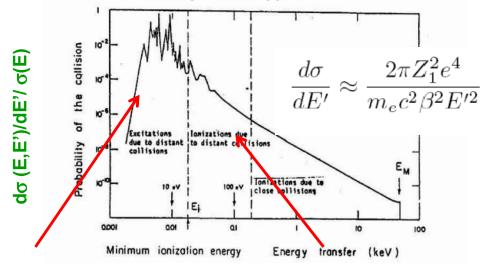
How do we find the energy loss distribution ?

If f(E) is the probability to lose the energy E' in an interaction, the probability p(E) to lose an energy E over the distance D ?

$$\begin{split} f(E) &= \frac{1}{\sigma} \frac{d\sigma}{dE} \\ p(E) &= P(1)f(E) + P(2) \int_0^E f(E-E')f(E')dE' + P(3) \int_0^E \int_0^{E'} f(E-E'-E'')f(E'')f(E')dE''dE' + \dots \\ F(s) &= \mathcal{L}\left[f(E)\right] = \int_0^\infty f(E)e^{-sE}dE \\ \mathcal{L}\left[p(E)\right] &= P(1)F(s) + P(2)F(s)^2 + P(3)F(s)^3 + \dots \\ &= \sum_{n=1}^\infty P(n)F(s)^n = \sum_{n=1}^\infty \frac{\overline{n}^n F^n}{n!} e^{-\overline{n}} = e^{\overline{n}(F(s)-1)} - 1 \approx e^{\overline{n}(F(s)-1)} \\ p(E) &= \mathcal{L}^{-1}\left[e^{\overline{n}(F(s)-1)}\right] = \frac{1}{2\pi i} \int_{\sigma-i\infty}^{\sigma+i\infty} e^{\overline{n}(F(s)-1)+sE} ds \end{split}$$

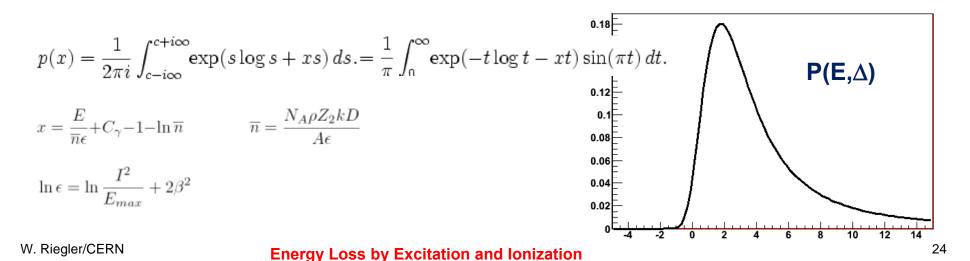
### **Fluctuations of the Energy Loss**

Probability f(E) for loosing energy between E' and E'+dE' in a single interaction is given by the differential crossection  $d\sigma$  (E,E')/dE'/  $\sigma$ (E) which is given by the Rutherford crossection at large energy transfers



Excitation and ionization

### Scattering on free electrons



## Landau Distribution

## Landau Distribution

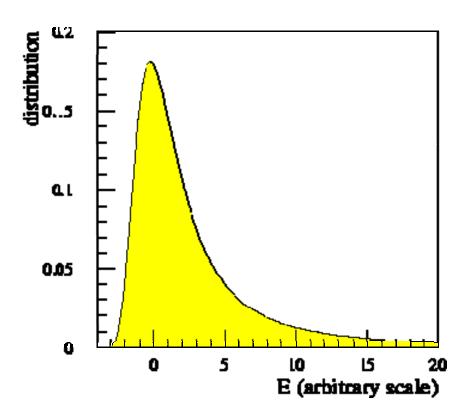
 $P(\Delta)$ : Probability for energy loss  $\Delta$  in matter of thickness D.

Landau distribution is very asymmetric.

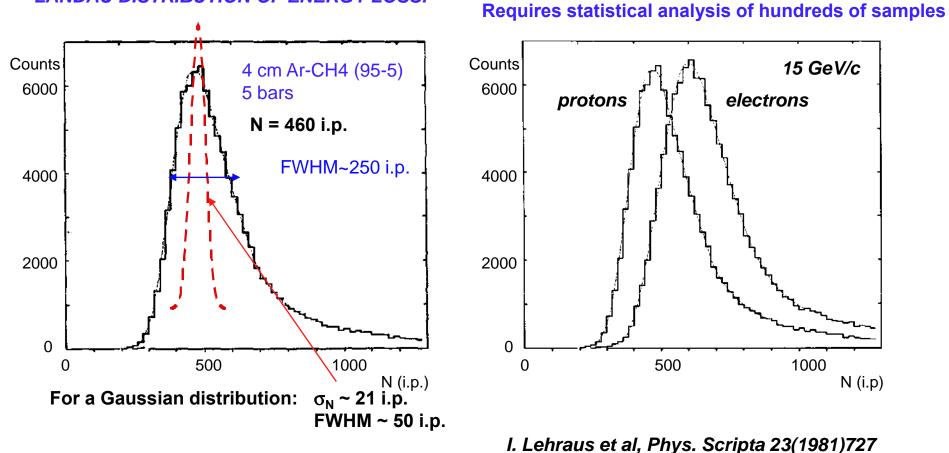
Average and most probable energy loss must be distinguished !

Measured Energy Loss is usually smaller that the real energy loss:

3 GeV Pion:  $E'_{max} = 450 \text{MeV} \rightarrow \text{A}$ 450 MeV Electron usually leaves the detector.



## Landau Distribution



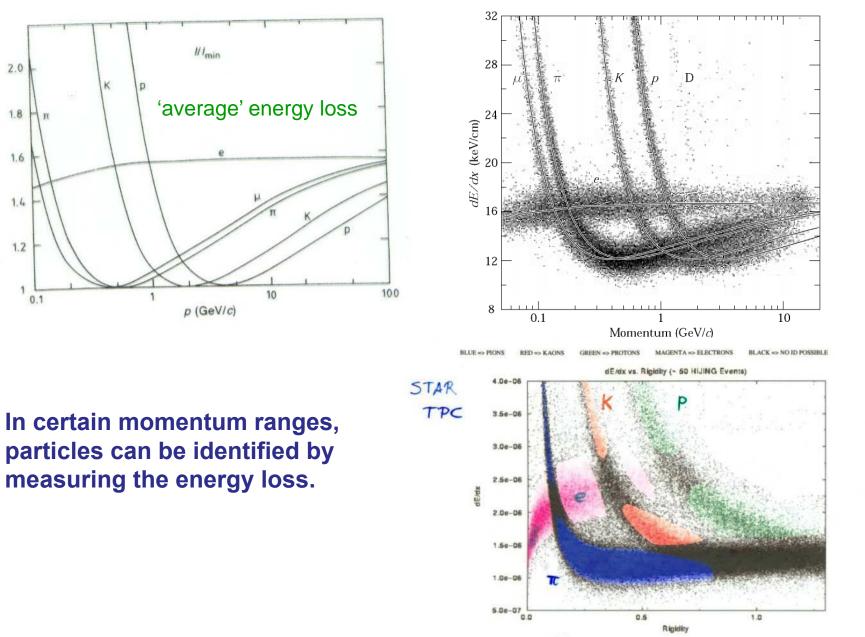
**PARTICLE IDENTIFICATION** 

### LANDAU DISTRIBUTION OF ENERGY LOSS:

W. Riegler/CERN

## **Particle Identification**

### Measured energy loss



2.0

1.8

1.6

1.4

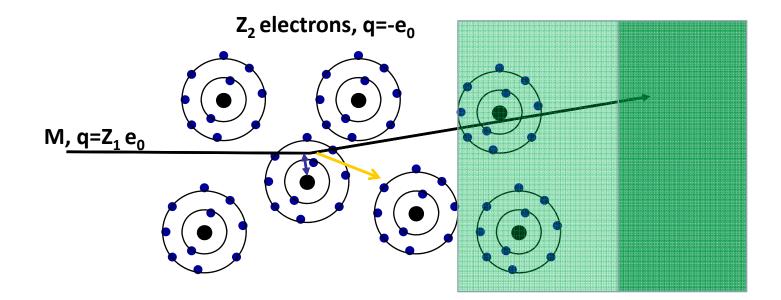
1.2

1

0.1

## **Bremsstrahlung**

A charged particle of mass M and charge  $q=Z_1e$  is deflected by a nucleus of charge Ze which is partially 'shielded' by the electrons. During this deflection the charge is 'accelerated' and it therefore radiated  $\rightarrow$  Bremsstrahlung.



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## **Bremsstrahlung, Classical**

$$q = \frac{2}{4\pi\epsilon}$$

A charged particle of mass M and charge  $q=Z_1e$  is deflected by a nucleus of Charge Ze.

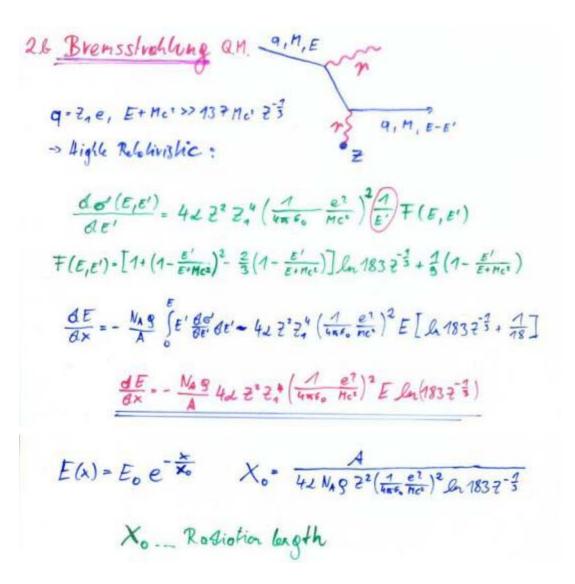
Because of the acceleration the particle radiated EM waves  $\rightarrow$  energy loss.

Coulomb-Scattering (Rutherford Scattering) describes the deflection of the particle.

Maxwell's Equations describe the radiated energy for a given momentum transfer.

 $\rightarrow$  dE/dx

## Bremsstrahlung, QM



**Proportional to Z<sup>2</sup>/A of the Material.** 

Proportional to Z<sub>1</sub><sup>4</sup> of the incoming particle.

Proportional to  $\rho$  of the material.

Proportional 1/M<sup>2</sup> of the incoming particle.

Proportional to the Energy of the Incoming particle  $\rightarrow$ 

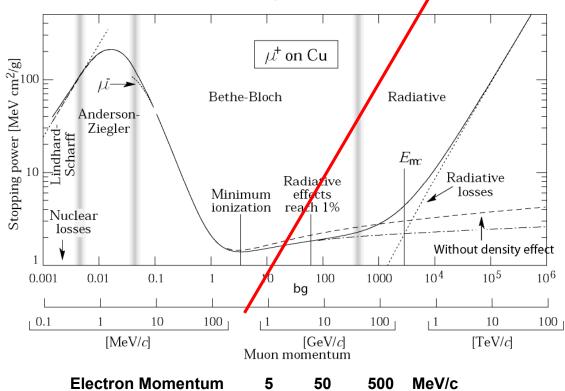
 $E(x)=Exp(-x/X_0) -$  'Radiation Length'

 $X_0 \propto M^2 A / (\rho Z_1^4 Z^2)$ 

 $X_0$ : Distance where the Energy  $E_0$  of the incoming particle decreases  $E_0Exp(-1)=0.37E_0$ .

# **Critical Energy**

such as copper to about 1% accuracy for energies between about 6 MeV and 6 GeV



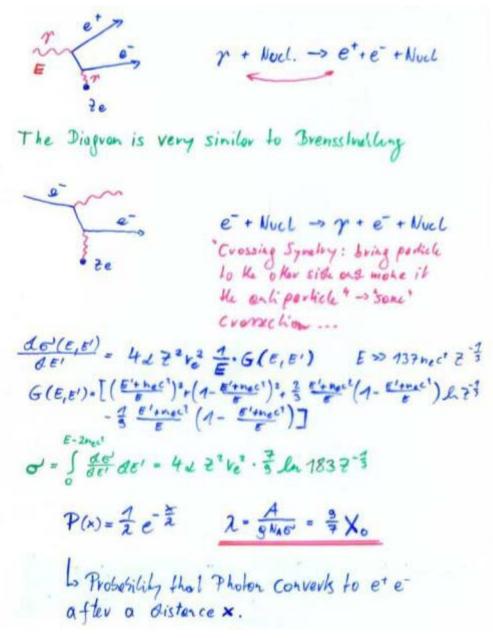
For the muon, the second lightest particle after the electron, the critical energy is at 400GeV.

The EM Bremsstrahlung is therefore only relevant for electrons at energies of past and present detectors.

Critical Energy: If dE/dx (Ionization) = dE/dx (Bremsstrahlung)

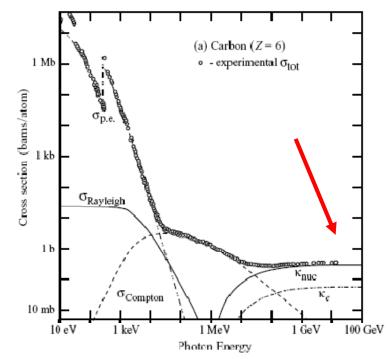
Myon in Copper: $p \approx 400 GeV$ Electron in Copper: $p \approx 20 MeV$ 

## **Pair Production, QM**

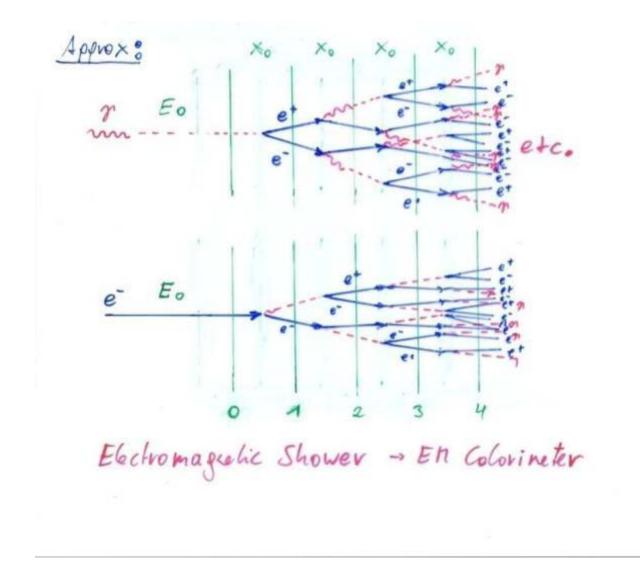


For  $E\gamma > m_e c^2 = 0.5 MeV : \lambda = 9/7X_0$ 

Average distance a high energy photon has to travel before it converts into an  $e^+ e^-$  pair is equal to 9/7 of the distance that a high energy electron has to travel before reducing it's energy from E<sub>0</sub> to E<sub>0</sub>\*Exp(-1) by photon radiation.



## Bremsstrahlung + Pair Production → EM Shower



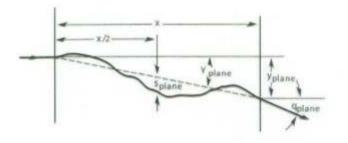
## **Multiple Scattering**

Statistical (quite complex) analysis of multiple collisions gives:

Probability that a particle is defected by an angle  $\theta$  after travelling a distance x in the material is given by a Gaussian distribution with sigma of:

$$\Theta_0 = \frac{0.0136}{\beta cp [\text{GeV/c}]} Z_1 \sqrt{\frac{x}{X_0}}$$

- X<sub>0</sub>... Radiation length of the material
- Z<sub>1</sub>... Charge of the particle
- p... Momentum of the particle



## **Multiple Scattering**

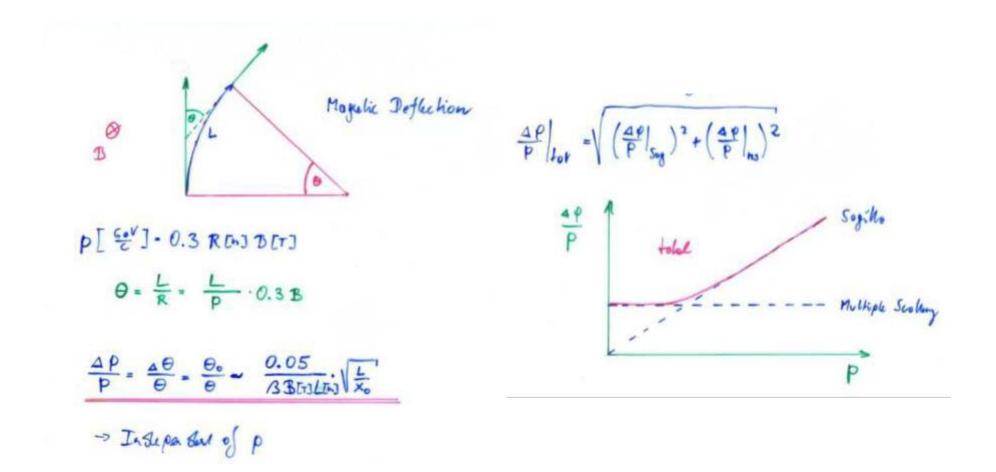
Magnetic Spectrometer: A charged particle describes a circle in a magnetic field:

$$\vec{B} \otimes L \left[\vec{s} \\ e^{-R} \\ e$$

Limit → Multiple Scattering

W. Riegler/CERN

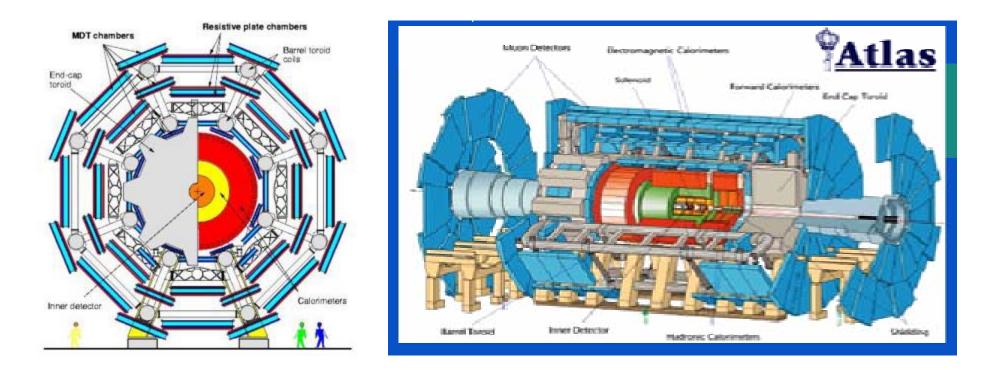
## **Multiple Scattering**



# **Multiple Scattering**

ATLAS Muon Spectrometer: N=3, sig=50um, P=1TeV, L=5m, B=0.4T

 $\Delta p/p \sim 8\%$  for the most energetic muons at LHC



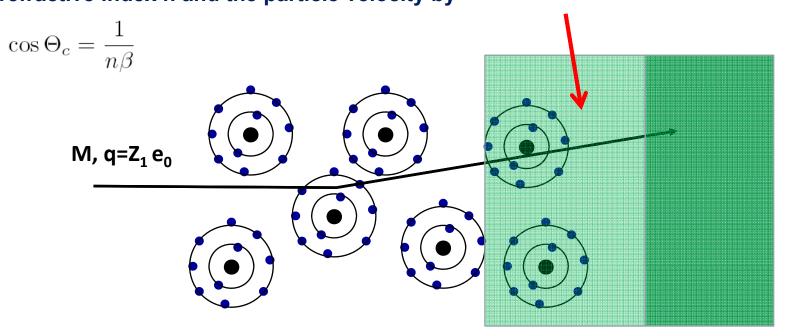
### **Cherenkov Radiation**

If we describe the passage of a charged particle through material of dielectric permittivity  $\mathbb{M}$  (using Maxwell's equations) the differential energy crossection is >0 if the velocity of the particle is larger than the velocity of light in the medium is

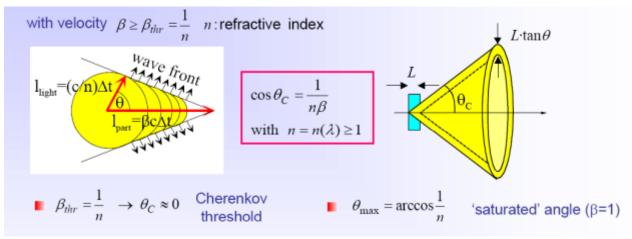
$$\frac{d\sigma}{dE} = \frac{\alpha}{\beta^2 \pi} \frac{A}{N_A \rho Z_2 \hbar c} \left( \beta^2 - \frac{1}{\epsilon_1} \right) \quad \rightarrow \quad \frac{N_A \rho Z_2}{A} \frac{d\sigma}{d\omega} \frac{d\omega}{dE} = \frac{\alpha}{c} \left( 1 - \frac{1}{\beta^2 n^2} \right) \qquad n = \sqrt{\epsilon_1} \qquad E = \hbar \omega$$

$$\frac{dE}{dx d\omega} \frac{1}{\hbar} = \frac{\alpha}{c} \left( 1 - \frac{1}{\beta^2 n^2} \right) \qquad \rightarrow \qquad \frac{dN}{dx d\lambda} = \frac{2\pi \alpha}{\lambda^2} \left( 1 - \frac{1}{\beta^2 n^2} \right) \qquad \omega = \frac{2\pi c}{\lambda}$$

N is the number of Cherenkov Photons emitted per cm of material. The expression is in addition proportional to  $Z_1^2$  of the incoming particle. The radiation is emitted at the characteristic angle  $\Box_c$ , that is related to the refractive index n and the particle velocity by

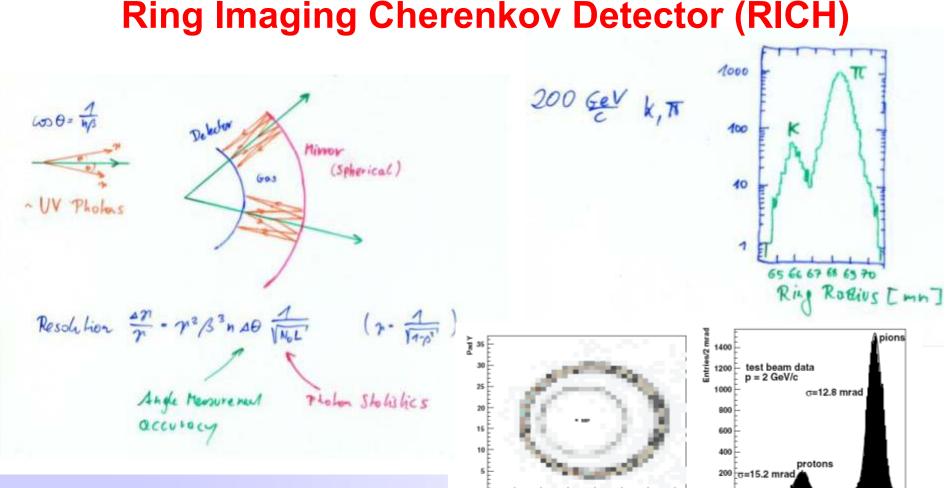


### **Cherenkov Radiation**



If the velocity of a charged particle is larger than the velocity of light in the westion  $t > \frac{1}{m} (m \dots Refrective Index of Natural)$ if emits 'Grenkor' radiation at a characteristic angle of  $\cos \theta_{c} = \frac{1}{m/3} (\beta = \frac{3}{c})$   $\frac{dN}{dx} \sim 2\pi d Z_{n}^{2} (1 - \frac{1}{\beta^{n}n^{2}}) \frac{\lambda_{2} - \lambda_{n}}{\lambda_{3} \cdot \lambda_{n}}$ - Number of emitted Pholons / larger with  $\lambda$  between  $\lambda_{n}$  and  $\lambda$ With  $\lambda_{n} = 490 (1 - \frac{1}{\beta^{2}m^{2}}) [\frac{1}{cm}]$ 

Maleriel	n-1	B throshold	In threshold
solid Sodium	3.22	0.24	1.029
lead gloss	0.67	0.60	1.25
water	0.33	0.75	1.52
silica aerogel	0.025-0.075	0.93-0.976	2.7 - 4.6
air	2.93-10-4	0.9957	41.2
He	3.3.10-5	0.99357	123



medium	n	$\theta_{max} \; (deg.)$	$N_{ph} (eV^{-1} cm^{-1})$
air*	1.000283	1.36	0.208
isobutane*	1.00127	2.89	0.941
water	1.33	41.2	160.8
quartz	1.46	46.7	196.4

There are only 'a few' photons per event →one needs highly sensitive photon detectors to measure the rings !

35

Pad X

0.4 0.45 0.5

0.55 0.6 0.65

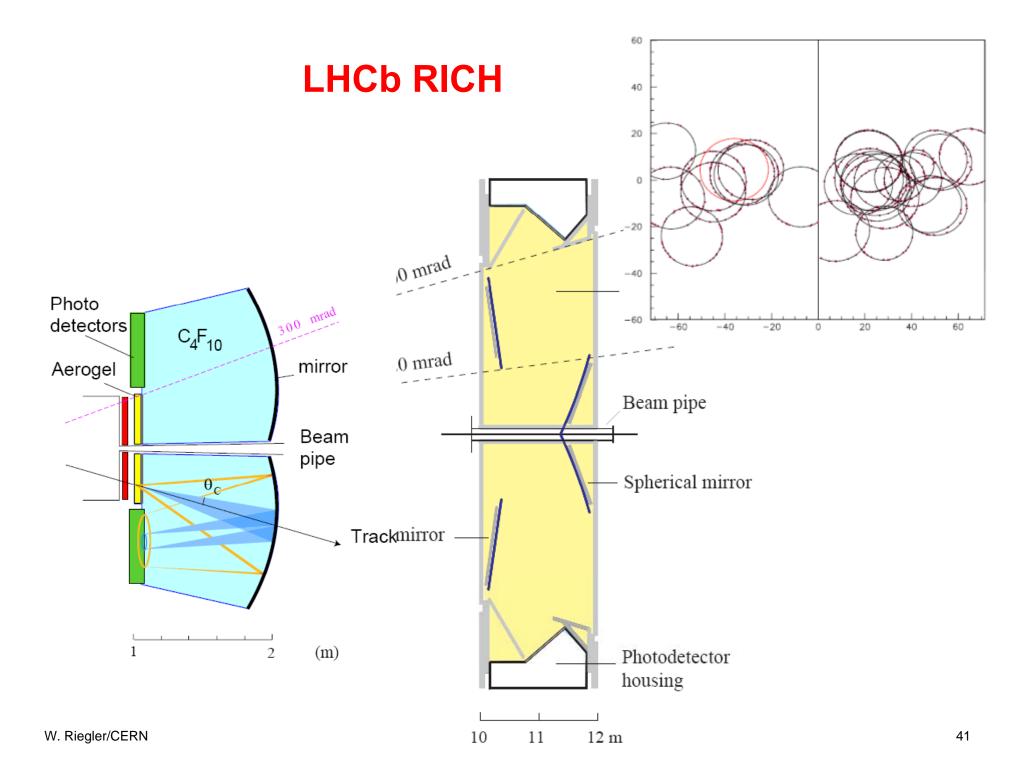
Single Cherenkov angle (rad)

0.7

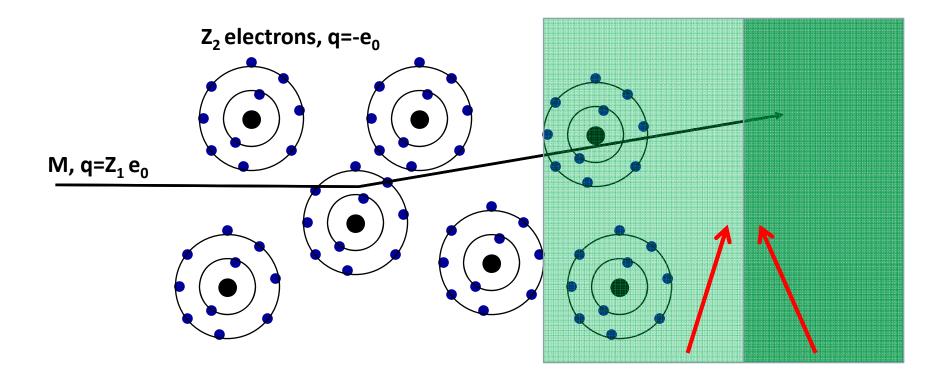
20

25 30

15



# **Transition Radiation**



When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.

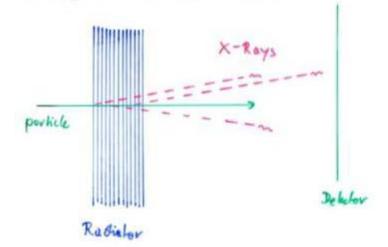
### **Transition Radiation**

Radiation (~ keV) enitted by cliva - velotivistic Porticles when Key traverse the boarder of 2 holenials of different Dielectric Permittivity (En.Ez) Vecum Eo Ez Hodium -q (ninror Charge) Clomical Picture  $q = Z_1 e$  $I = \frac{1}{3} d Z_n^2(hw_p) \gamma$  Radieled Evergy per Transition

thep .... plasma Frequency of the Medium ~20 eV for Styrene

About holf the Elevary is voliched between 0.1 thwpp < tww = thwpp E.g. p=1000 2-20 keV X-Rays Np ~ 3 2 ≥n<sup>2</sup> ~ 5.10<sup>3</sup>. ≥n<sup>2</sup> p-Dependence from hardering roker then Np Emission Angle ~ 7

The Number of Photons can be increased by placing many fails of Natural.



# **Electromagnetic Interaction of Particles with Matter**

#### **Ionization and Excitation:**

Charged particles traversing material are exciting and ionizing the atoms.

The average energy loss of the incoming particle by this process is to a good approximation described by the Bethe Bloch formula.

The energy loss fluctuation is well approximated by the Landau distribution.

**Multiple Scattering and Bremsstrahlung:** 

The incoming particles are scattering off the atomic nuclei which are partially shielded by the atomic electrons.

Measuring the particle momentum by deflection of the particle trajectory in the magnetic field, this scattering imposes a lower limit on the momentum resolution of the spectrometer.

The deflection of the particle on the nucleus results in an acceleration that causes emission of Bremsstrahlungs-Photons. These photons in turn produced e+e- pairs in the vicinity of the nucleus, which causes an EM cascade. This effect depends on the 2<sup>nd</sup> power of the particle mass, so it is only relevant for electrons.

# **Electromagnetic Interaction of Particles with Matter**

#### **Cherenkov Radiation:**

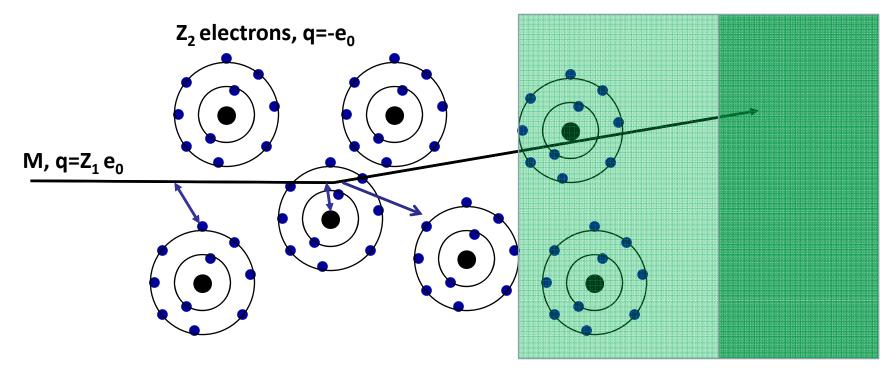
If a particle propagates in a material with a velocity larger than the speed of light in this material, Cherenkov radiation is emitted at a characteristic angle that depends on the particle velocity and the refractive index of the material.

#### **Transition Radiation:**

If a charged particle is crossing the boundary between two materials of different dielectric permittivity, there is a certain probability for emission of an X-ray photon.

→ The strong interaction of an incoming particle with matter is a process which is important for Hadron calorimetry and will be discussed later.

### **Electromagnetic Interaction of Particles with Matter**



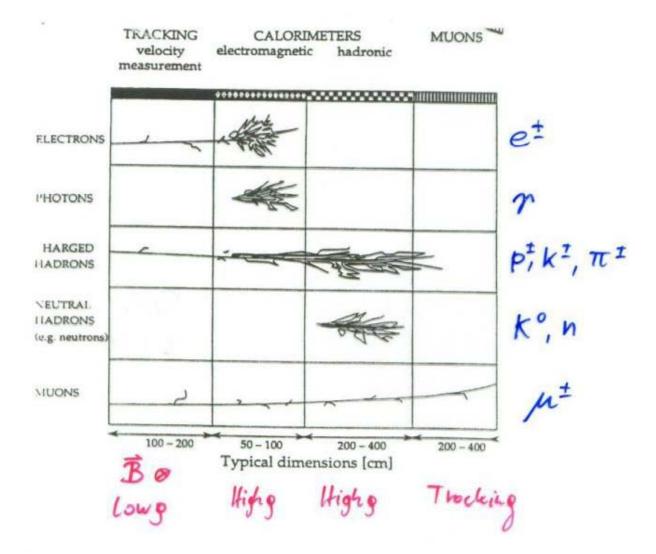
Now that we know all the Interactions we can talk about Detectors !

Interaction with the atomic electrons. The incoming particle loses energy and the atoms are <u>excited</u> or ionized.

7/8/2008

Interaction with the atomic nucleus. The particle is deflected (scattered) causing <u>multiple scattering</u> of the particle in the material. During this scattering a <u>Bremsstrahlung</u> photon can be emitted. In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as <u>Cherenkov Radiation</u>. When the particle crosses the boundary between two media, there is a probability of the order of 1% to produced and X ray photon, called <u>Transition radiation</u>.

### Now that we know all the Interactions we can talk about Detectors !



# Detectors based on registration of Ionization: Tracking in Gas and Solid State Detectors

Charged particles leave a trail of ions (and excited atoms) along their path: Electron-lon pairs in gases and liquids, electron hole pairs in solids.

The photons emitted by the excited atoms can be detected with photon detectors like photomultipliers or semiconductor photon detectors.

The produced charges can be registered  $\rightarrow$  Position measurement  $\rightarrow$  Tracking Detectors.

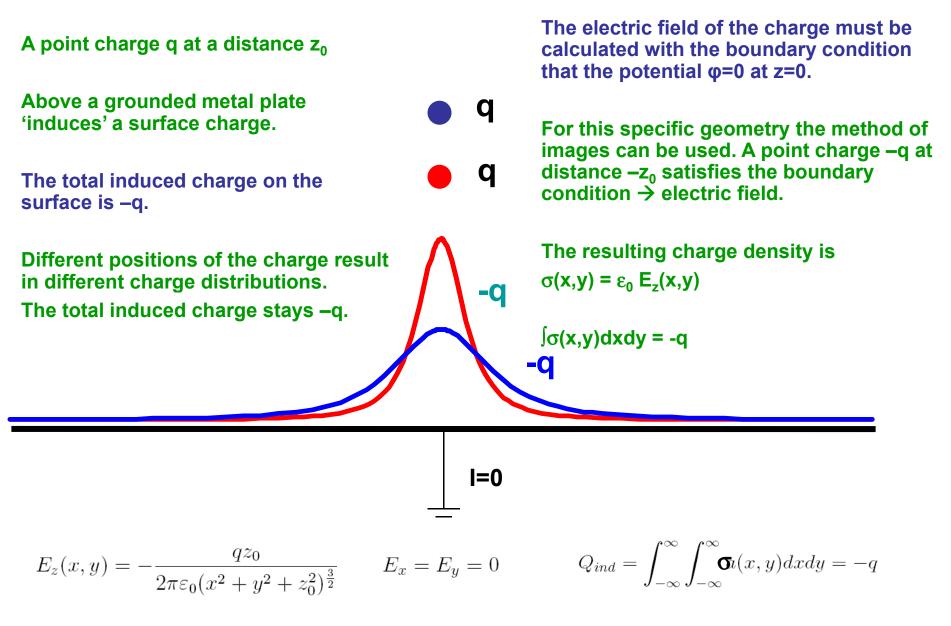
Cloud Chamber: Charges create drops → photography. Bubble Chamber: Charges create bubbles → photography. Emulsion: Charges 'blacked' the film.

Gas and Solid State Detectors: Moving Charges (electric fields) induce electronic signals on metallic electrons that can be read by dedicated electronics.

 $\rightarrow$ In solid state detectors the charge created by the incoming particle is sufficient.

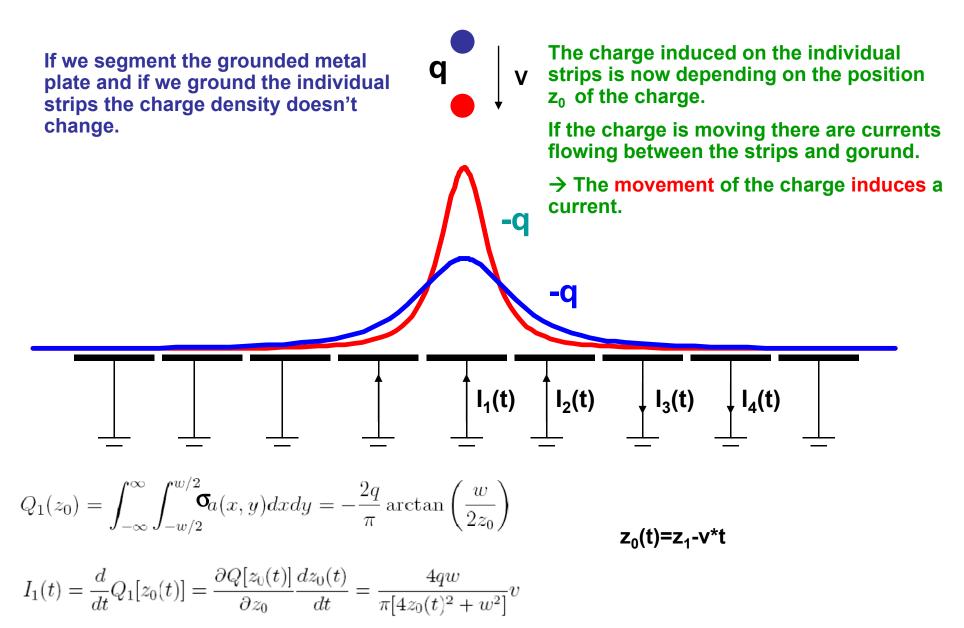
 $\rightarrow$ In gas detectors (e.g. wire chamber) the charges are internally multiplied in order to provide a measurable signal.

**Principle of signal induction by moving charges:** 



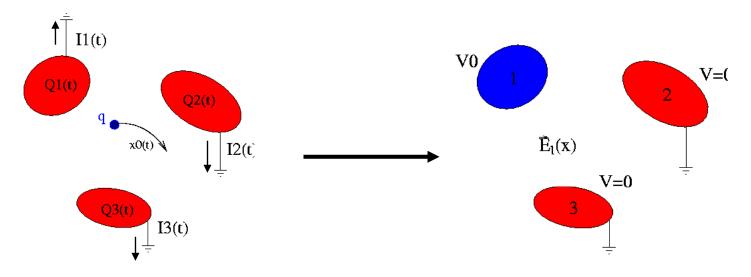
Signal induction by moving charges

### Principle of signal induction by moving charges:



Signal induction by moving charges

In order to calculate the signals the Poisson equation must be calculated for all different positions of the charge  $q \rightarrow$  difficult task.

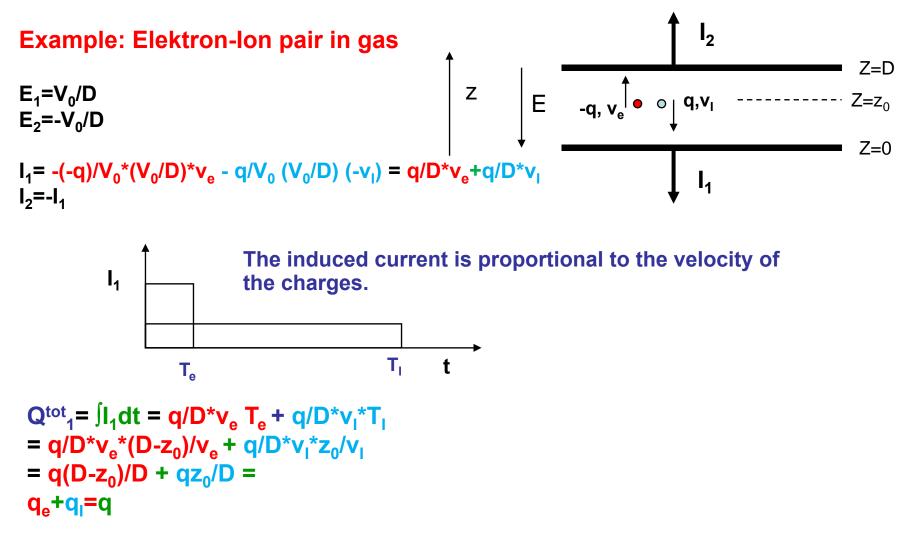


Theorem (1) (Reciprocity theorem, Ramotheorem): The current induced on a grounded electrode (n) by the movement of a charge q along a trajectory x(t) can be calculated the following way:

One removes the charge q and brings electrode (n) to potential  $V_0$  while keeping all the other electrodes at ground potential. This defined an electric field  $E_n(x)$  ('Weighting field' of electrode n). The induced current is then

$$I_n(t) = -\frac{q}{V_0} \vec{E_n}[\vec{x}(t)] \frac{d\vec{x}(t)}{dt} = -\frac{q}{V_0} \vec{E_n}[\vec{x}(t)] \vec{v}(t)$$

Signal induction by moving charges

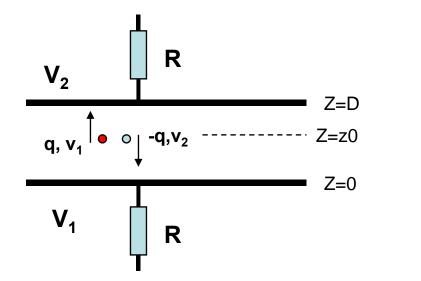


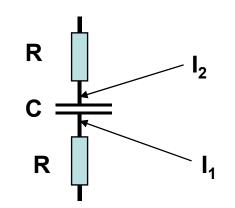
The induced charge depends on the position from where the charge starts moving.

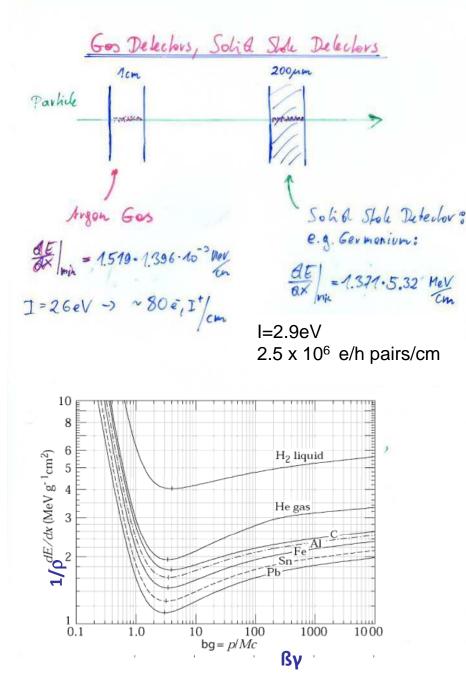
The total induced charge on a specific electrode, once all the charges have arrived at the electrodes, is equal to the charge that has arrived at this specific electrode.

### Theorem (2):

In case the electrodes are not grounded but connectd by arbitrary active or passive elements one first calculates the currents induced on the grounded electrodes and places them as ideal current sources on the equivalent circuit of the electrodes.







The induced signals are readout out by dedicated electronics.

The noise of an amplifier determines whether the signal can be registered. Signal/Noise >>1

The noise is characterized by the 'Equivalent Noise Charge (ENC)' = Charge signal at the input that produced an output signal equal to the noise.

ENC of very good amplifiers can be as low as 50e-, typical numbers are ~ 1000e-.

In order to register a signal, the registered charge must be q >> ENC i.e. typically q>>1000e-.

Gas Detector: q=80e- /cm  $\rightarrow$  too small.

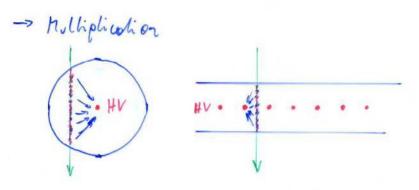
Solid state detectors have 1000x more density and factor 5-10 less ionization energy.  $\rightarrow$ Primary charge is 10<sup>4</sup>-10<sup>5</sup> times larger than is gases.

Gas detectors need internal amplification in order to be sensitive to single particle tracks.

Without internal amplification they can only be used for a large number of particles that arrive at the same time (ionization chamber).

### Wire Chamber

Since he Ionitotion density in Gooses is small, the signals induced by the moveman of the few e, It is small.



Electrons are Drifling forwards the wives (Wirds on positive HV)

Close to the wive the field is ~ 7

-> Multiplication -> electron Avolonche Geir ~ 103 - 106

-> Single Electron Servicity

By using thin wires, the electric fields close to the wires are very strong (e.g.100-300kV/cm).

In these large electric fields, the electrons gain enough energy to ionize the gas themselves  $\rightarrow$ Avalanche  $\rightarrow$  a primary electron produces 10<sup>3</sup>-10<sup>6</sup> electrons  $\rightarrow$  measurable signal.