

The Violation of Symmetry between Matter and Antimatter

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Lecture Themes

- Introduction
- Antimatter

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- Discrete Symmetries
- The Phenomena of CP Violation
- Electric and weak dipole moments
- The strong CP problem
- The discovery of *CP* violation in the kaon system
- CP Violation in the Standard Model
 - The CKM matrix and the Unitarity Triangle
 - **B** Factories
 - *CP* violation in the *B*-meson system and a global CKM fit
 - The Future at the LHC
- IV. CP Violation and the Genesis of a Matter World
 - Baryogenesis and CP violation
 - Models for Baryogenesis



CP Violation in the Model

We have learned that different types of *CP* violation have been observed ... we will later see that there is also *CP* violation in meson systems other than kaons.

ded at C

γ

Sir

ε_K

 $|V_{u}|$

α

All these phenomena can be described by a *unique* parameter in the Standard Model !

sol. w/ cos $2\beta < 0$ (excl. at CL > 0.95)

 Δm_d

The Standard Model

The Standard Model forces and their gauge bosons:

Electromagnetic interaction	⇔	Photons (γ)
Strong interaction (QCD)	\Leftrightarrow	Gluons (g)
Weak interaction	⇔	Neutral (Z ⁰) and charged (W [±])

Left-handed quarks are fermions organized in *doublets:*

up-type quarks (U_i) : down-type quarks (D_i) : $\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix} Q = +2/3$ Q = -1/3 ...and similar for the leptons.

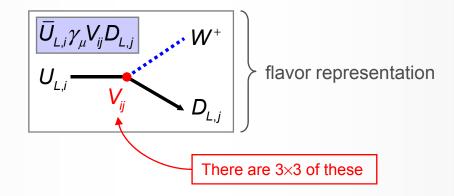
The charged weak current is of V-A type:

$$\overline{U}_{i}\gamma^{\mu}\left(1-\gamma_{5}\right)D_{i}=\overline{U}_{L,i}\gamma^{\mu}D_{L,i}$$

The operator projects upon left-handed particles (and right-handed antiparticles) – which means that the W^{\pm} boson is *blind* to the right-handed particles (and left-handed antiparticles)

Three-Generation Quark Mixing

The charged weak current generates transitions between generations, i.e., the flavoured quarks are not the same as the physical quarks:



Again: since mass and flavor eigenstates are not the same \rightarrow quark mixing:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \circ \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Quark mixing would simplify (= reduced parameter space) if some of the quarks had equal masses and would hence not be distinguishable !

Cabibbo-Kobayashi-Maskawa (CKM) matrix – 1973 (KM)

CP Violation in the Standard Model

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P-invariance

- What does *CP* or *T* conjugation with the Hamiltonian *H*?
 - Simple exercise:

Recall:

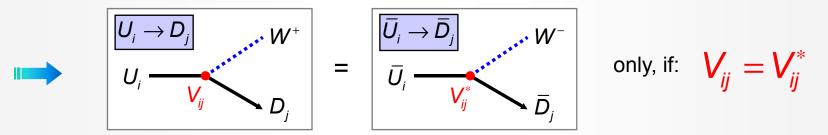
$$\begin{bmatrix}
 \hat{x}, \hat{p} \end{bmatrix} = i\hbar \implies \begin{cases}
 P[\hat{x}, \hat{p}]P^{-1} = PiP^{-1}\hbar \implies PiP^{-1} = i\\
 T\hat{x} = \hat{x}, T\hat{p} = -\hat{p}
 \end{cases}$$

$$\begin{bmatrix}
 \hat{x}, \hat{p}\end{bmatrix} = i\hbar \implies \begin{cases}
 P[\hat{x}, \hat{p}]P^{-1} = PiP^{-1}\hbar \implies PiP^{-1} = i\\
 T[\hat{x}, \hat{p}]T^{-1} = TiT^{-1}\hbar \implies TiT^{-1} = -i
 \end{cases}$$

 \rightarrow The T (and CP) operations are **anti-unitary**, which is **complex conjugation** !



Since $H = H(V_{ij})$, complex V_{ij} would generate $[T,H] \neq 0 \rightarrow CP$ violation



The Quark-Mixing Matrix

The $|V_{ij}|^2$ are transition probabilities and hence the matrix must be unitary

For example, a *t* quark can decay into a *d*, *s*, or *b* quark and nothing else; thus, the sum of the decay probabilities into these quarks must be one:

$$|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2 = 1$$

Unitarity condition:

$$\bigvee VV^{\dagger} = 1 \iff \sum_{j} V_{ij} V_{jk}^{*} = \delta_{ik}$$

The unitarity condition sets strong constraints on the V_{ij}, which initially has 2N² unknowns (N is number of generations)

Quark-Mixing Matrices for Different Generations



- 2 Unknowns module and phase: |V|e^{iφ}
- Unitarity determines |V| = 1

The phase is arbitrary (non-physical): $\overline{U}_L \gamma_\mu e^{i\phi} D_L \rightarrow \overline{U}_L \gamma_\mu D'_L$...with same physics

No phase, no CPV

Example for N = 2 generations:

- 8 Unknowns 4 moduli and 4 phases
- Unitarity gives 4 constraints : $VV^{\dagger} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
- For 4 quarks, we can adjust 3 relative phases

 \rightarrow Only 1 parameter, a rotation (= Cabibbo) angle left: no phase \rightarrow no CPV

Quark-Mixing Matrices for Different Generations

Example for N = 3:

- 18 Unknowns 9 moduli and 9 phases
- Unitarity gives 9 constraints
- For 6 quarks, we can adjust 5 relative phases

→ 4 Unknown parameters left, 3 rotation (Euler) angles and 1 phase → CPV !

Example for N = 4:

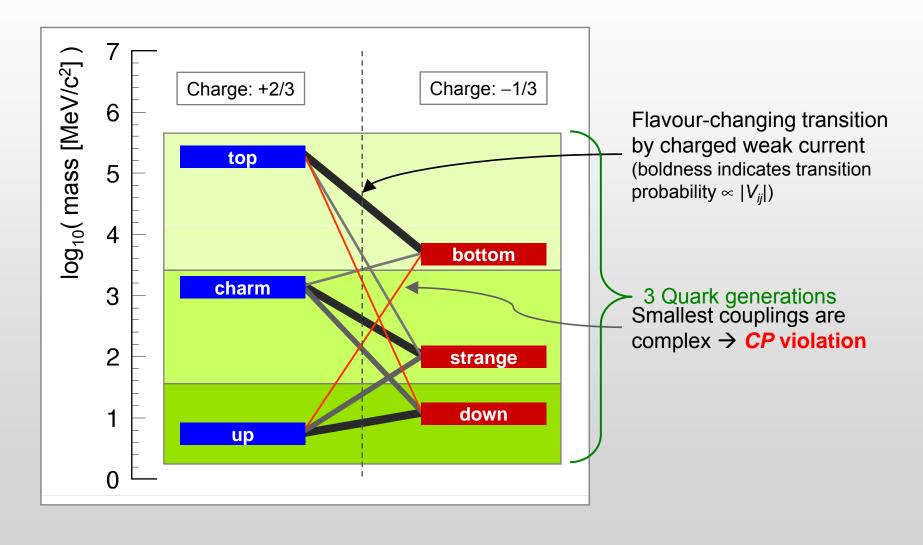
32 Unknowns, 16 unitarity constraints, 7 arbitrary phases

 \Rightarrow 9 Unknown parameters left, 6 rotation angles and 3 phases \rightarrow lots of CPV !

For *N* generations: $\begin{cases} \text{Number of rotation angles} : \frac{1}{2}N(N-1) \\ \text{Number of phases} : \frac{1}{2}(N-1)(N-2) \end{cases}$

Quark Flavours in the Standard Model

Quarks (as leptons) in the SM are organized in 3 generations:



The CKM Matrix in the Wolfenstein Parameterization

- The 3-generation CKM matrix has 4 unknowns, one of which is a phase
- Flavor-changing transitions between families are allowed, but are <u>small</u>
- We can develop the CKM matrix elements around the small flavor-changing transition between the 1st and the 2nd family (the Cabibbo mixing), denoted λ ≈ 0.2 :

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \implies \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3 (\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3 (1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

Decay-rate measurements give: $\Gamma(i \to j \overline{\ell} v) \propto |V_{ij}|^2 \times (F^2(i \to j))$

 $(|V|)_{ij} = \begin{pmatrix} 0.9738 \pm 0.0003 & 0.2257 \pm 0.0021 & 0.0043 \pm 0.0003 \\ 0.230 \pm 0.011 & 0.96 \pm 0.10 & 0.0416 \pm 0.0006 \\ - & - & > 0.78^{[95\% \text{ C.L.}]} \end{pmatrix}$

• How can we determine the *CP*-violating phase ?

Strong-interaction form factor (taken

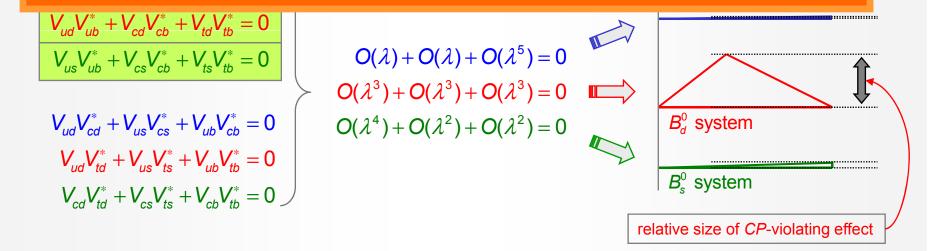
from theory)

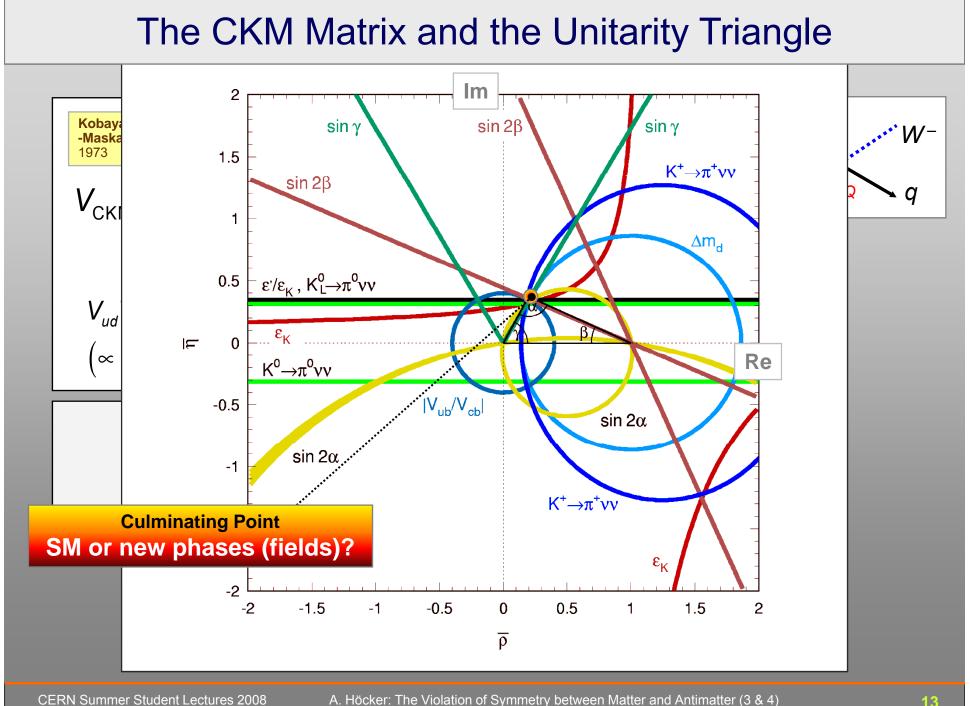
The CKM Matrix and the "Unitarity Triangle(s)"

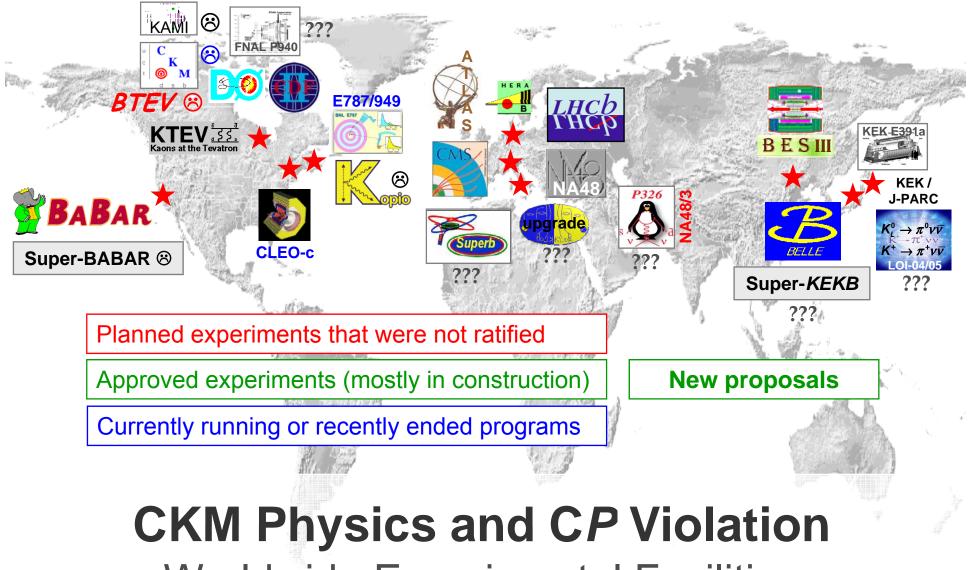
The 9 unitarity conditions of the 3×3 generations CKM matrix: multiplytiplytiply

CKM-type *CP* violation is <u>always</u> a rare phenomenon:

- 1. Either the CP asymmetry is small
- 2. Or/and the decay rate is suppressed







Worldwide Experimental Facilities

The B-Meson System

The study of *CP* violation, mixing and rare decays of *B* mesons allows to over-determine the Unitarity Triangle (UT)

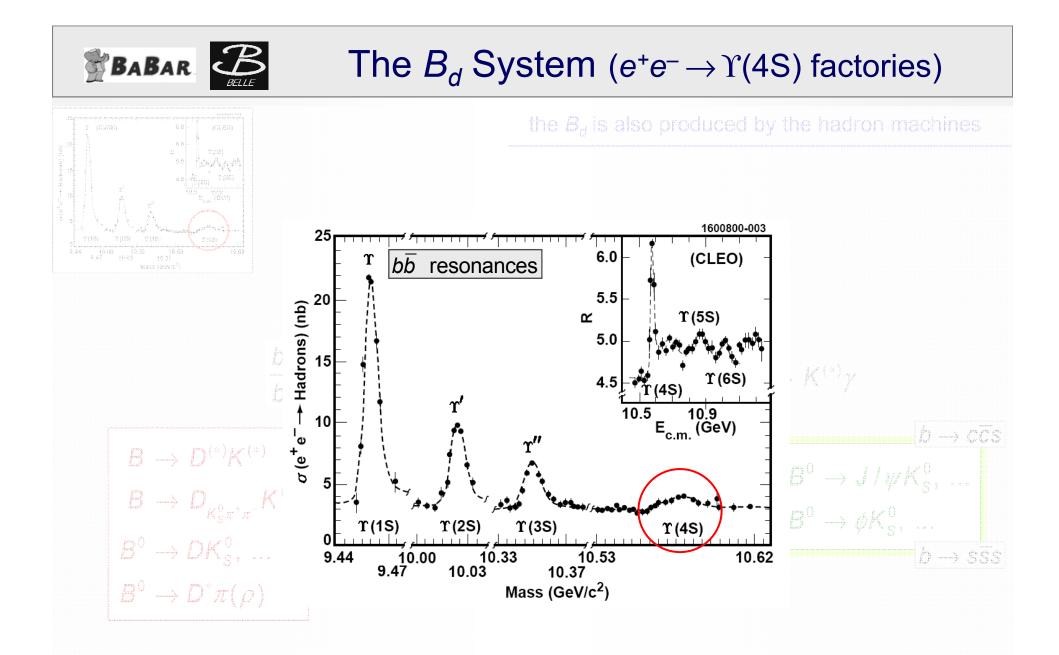
- 1. Relative CP-violating effects are expected to be large
- 2. Requires dedicated experiments

 α = arg

3. Goal: measure all three angles, α , β , γ , and the sides of the UT

$$\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \qquad \beta = \arg\left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right) \qquad \gamma = \arg\left(-\frac{V_{ud}V_{cb}^*}{V_{td}V_{tb}^*}\right)$$

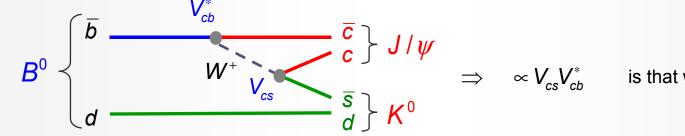
concentrate lecture on this measurement



The Measurement of β (... or more precisely: sin2 β)

We need to identify the processes that involve the CKM matrix elements that occur in the definition of β :

1. The decay $b \rightarrow c$:



 $eta = \arg igg(- rac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} igg)$

is that what we want? 😐

2. Like for the K^0 , the B^0 can first mix and then decay into the "CP eigenstate (?)" $J/\psi K^0$

$$B^{0} \begin{cases} \overline{b} & V_{tb}^{*} & V_{td} \\ t & W^{+} & \overline{t} & \overline{d} \\ d & V_{td}^{-} & V_{tb}^{-} & b \\ V_{td}^{-} & V_{tb}^{*} & b \end{cases} \Rightarrow \propto \left(V_{td}V_{tb}^{*}\right)^{2} \text{ not bad } \mathbb{S}$$

2. Also the K^0 in the decay must mix for interference $\Rightarrow \propto \left(V_{cd}V_{cs}^*\right)^2$ good \odot

A controversy...

Why do you call these **Penguin diagrams**? They don't look like penguins!

> I've never seen a **Feynman diagram** that looks like **you** ③

CALTECH

Mirror image of Richard Feynman

Courtesy: G. Hamel de Monchenault

CERN Summer Student Lectures 2008 A. Hö

A. Höcker: The Violation of Symmetry between Matter and Antimatter (3 & 4)

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What are the Experimental Requirements ?

The Observable :

$$A_{CP}(t) = \frac{\Gamma(\overline{B}^{0}(t) \to J/\psi K_{S}) - \Gamma(B^{0}(t) \to J/\psi K_{S})}{\Gamma(\overline{B}^{0}(t) \to J/\psi K_{S}) + \Gamma(B^{0}(t) \to J/\psi K_{S})} = \sin(2\beta) \cdot \sin(\Delta m_{d}t)$$

- We need to measure:
 - 1. Identify a final state that is *CP* **eigenstate** (e.g., $J/\psi K_S$)
 - 2. Determine the **flavour** of the **decaying** B^0 (assume here it is a B^0)
 - 3. How can we do this if $J/\psi K_s$ can be reached by both *B* flavors ?
 - If we could produce the B⁰B⁰ pairs in a coherent quantum state, we could "tag" the flavor of the decaying B⁰ from the flavor of the other B, not decaying into a CP eigenstate → see later
 - 5. Since the coherence is destroyed once one of the two *B*'s decays, we **need** the **decay time difference between the two** *B***'s** to calculate the flavor of the tagged *B* at the time when the B^0 decayed: $t \rightarrow \Delta t$

We must determine the decay time difference of the *B*'s by measuring their decay vertices

digression: Quantum Mechanics for $\Upsilon(4S) \rightarrow BB$ Decay

$$\begin{split} e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^0 \overline{B}^0 & \vec{p}^* \quad t_1 \\ \hline J^{PC} = 1^{--} & e^+ \\ \hline \\ \blacksquare & antisymmetric \text{ wave function} & t_2 \\ \blacksquare & \text{initial state:} \\ \hline & \left[\Upsilon(4S) \rightarrow B^0 \overline{B}^0 \right\rangle \propto \left(|B^0, \vec{p}^*\rangle | \overline{B}^0, -\vec{p}^*\rangle - |\overline{B}^0, \vec{p}^*\rangle | B^0, -\vec{p}^*\rangle \right) \\ &= \left(|B_H, \vec{p}^*\rangle |B_L, -\vec{p}^*\rangle - |B_L, \vec{p}^*\rangle |B_H, -\vec{p}^*\rangle \right) \frac{1}{2pq} \end{split}$$

 $t \equiv \left(t_1 + t_2\right)/2$

proper times:

$$\Delta t \equiv t_2 - t_1$$

flavor and mass eigenstates:

$$|B^{0}\rangle = \frac{1}{2p}(|B_{L}\rangle + |B_{H}\rangle)$$
$$|\overline{B}^{0}\rangle = \frac{1}{2q}(|B_{L}\rangle - |B_{H}\rangle)$$

double proper-time wave function: ٠

*

$$\left| \left(\Upsilon(4S) \to \mathcal{B}^{0} \overline{\mathcal{B}}^{0} \right)_{\text{phys}} (t, \Delta t) \right\rangle \propto e^{-2i\mu t} \begin{pmatrix} + e^{+i\Delta\mu\Delta t/2} \left| \mathcal{B}_{H}, \vec{p}^{*} \right\rangle \left| \mathcal{B}_{L}, -\vec{p}^{*} \right\rangle \\ - e^{-i\Delta\mu\Delta t/2} \left| \mathcal{B}_{L}, \vec{p}^{*} \right\rangle \left| \mathcal{B}_{H}, -\vec{p}^{*} \right\rangle \end{pmatrix}$$

$$\mu = M - i\Gamma/2$$
$$\Delta \mu = \Delta M - i\Delta\Gamma/2$$

Quantum Coherence at $\Upsilon(4S) \rightarrow BB$ Decay

Quantum coherence (due to synchronous evolution) for $\Delta t = 0$, the system is the superposition of:

```
oneB^0and one\overline{B}^0oneB_Hand oneB_LoneB_{CP=+1}and oneB_{CP=-1}
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An Einstein-Podolsky-Rosen phenomenon:

The measurement of the flavor (or *CP*) of one meson (*e.g.* from its decay products) determines the flavor (or *CP*) of the other meson at the same proper time (it is opposite)

For the study of time evolution, one needs to measure Δt .

However, at the $\Upsilon(4S)$:

 $p_B^* = 340 \text{ MeV/c}$ $(\beta \gamma)_B^* = 0.064$ flight distance $d^* \sim 30 \text{ }\mu\text{m}$ (beyond experimental reach)

Cannot perform decay-time-dependent measurements ?

Pier Oddone's Clever Idea (1987)

Why not produce the Υ (4S) with a strong boost? One could deduce the Δt from the distance between the two *B* vertices along the boost axis. What we need is an asymmetric-energy *B* Factory with peak luminosity of order 5×10^{33} cm⁻²s⁻¹



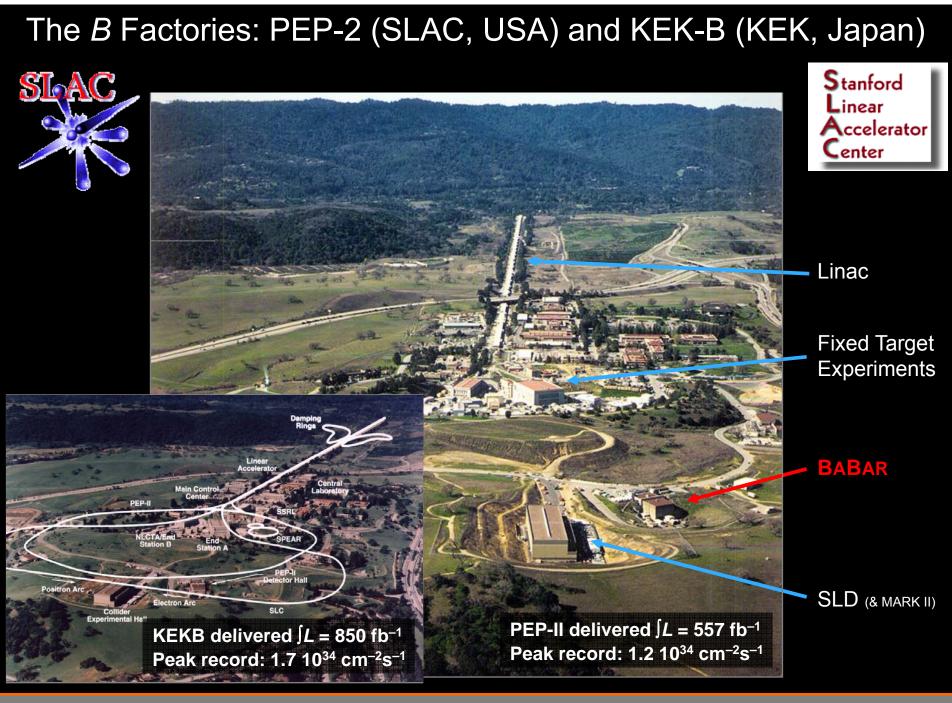
PEP-II: 9 GeV e⁻ on 3.1 GeV e⁺ :

- Coherent neutral *B* pair production and decay (*P*-wave)
- Boost of $\Upsilon(4S)$ in lab frame : $\beta \gamma = 0.56$

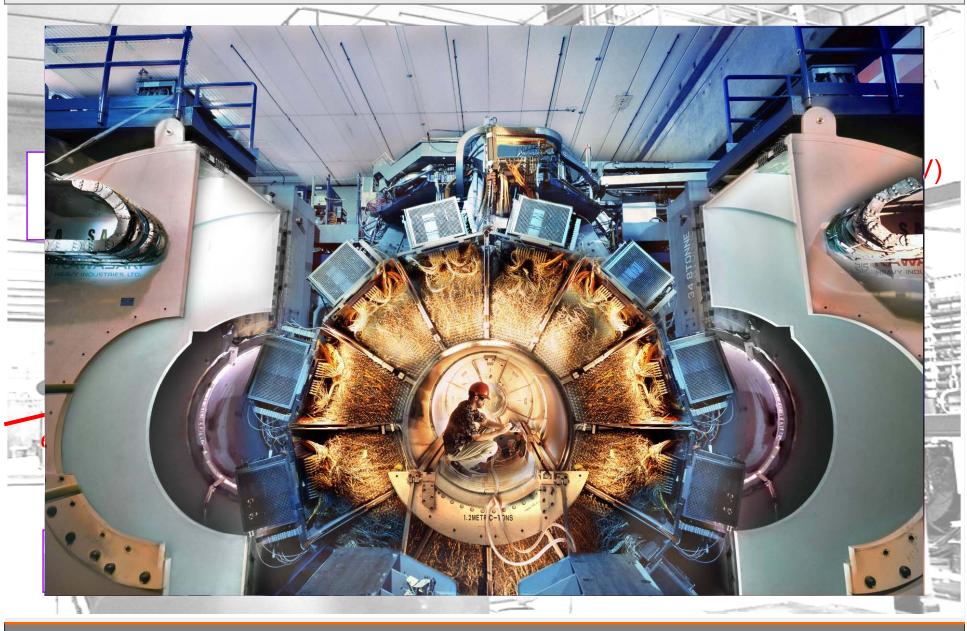


Oddone & Dorfan in PEP-II Tunnel, 2003

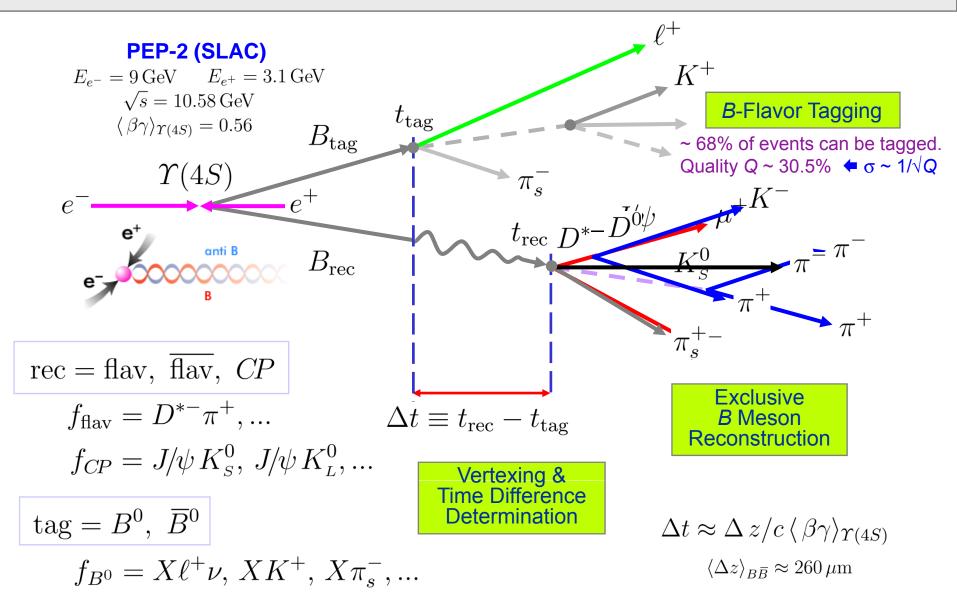
10 years later exist two asymmetric *B* Factories : PEP-II at SLAC and KEKB at KEK

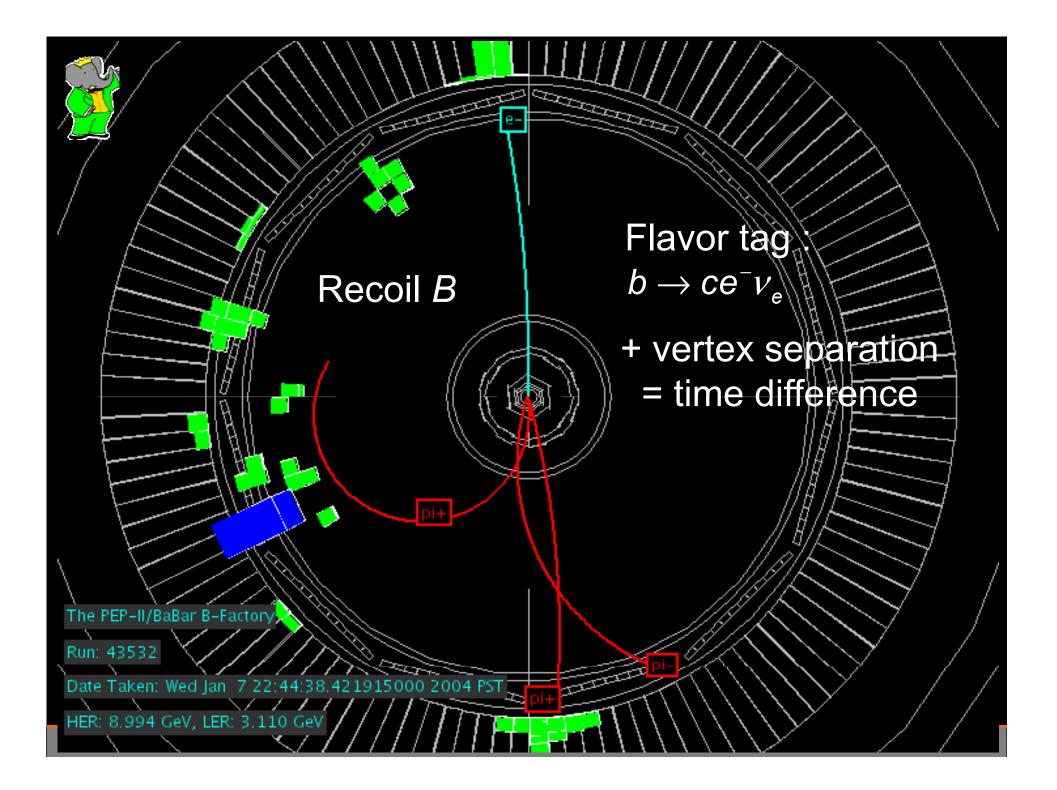


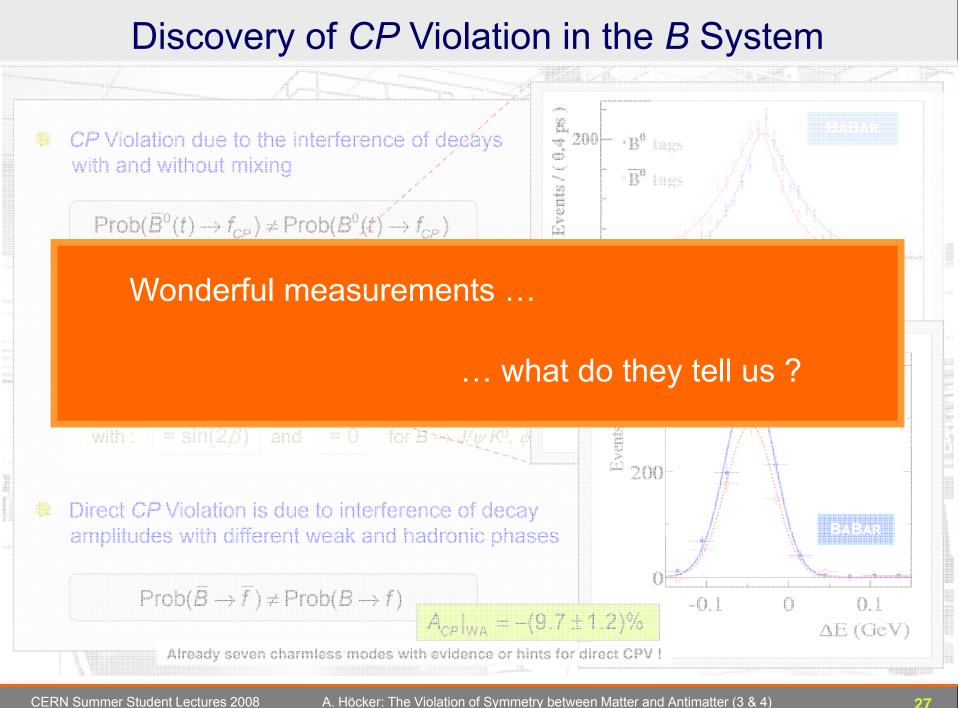
The BABAR Detector

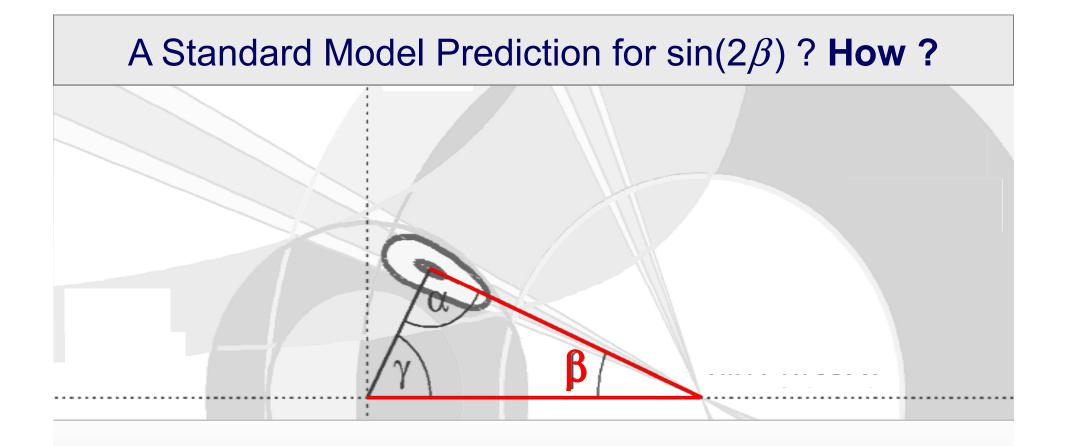


Analysis Technique at the B Factories









Since the CKM matrix describes all *CP*-violating effects by a single phase, and the complete quark-mixing matrix depends only on 4 parameters, we can constrain it (for example, using the *CP* measurements in the kaon sector) and hence obtain a prediction for $sin(2\beta)$.

We can even **overconstrain** the CKM matrix by a global fit using all the available information, and thus **search for inconsistencies that would reveal the presence of new physics** !

The Global CKM Fit

To determine (and then predict) the phase of the CKM matrix we need to measure processes that involve the matrix elements V_{ub} and V_{td}, i.e.: <u>*p* and </u><u>n</u>

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \Leftrightarrow \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3 (\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3 (1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

Some processes are already well established:

- 1. The rate of $b \rightarrow u$ transitions determine $|V_{ub}|$
- 2. Indirect *CP* Violation in the kaon system (ε) is sensitive to V_{td}
- 3. Neutral B_d mixing determines $|V_{td}|$ (reduce theory uncertainty by also using neutral B_s mixing)
- 4. Mixing-induced *CP* violation in *B* system determines $sin(2\beta)[arg(V_{td})]$

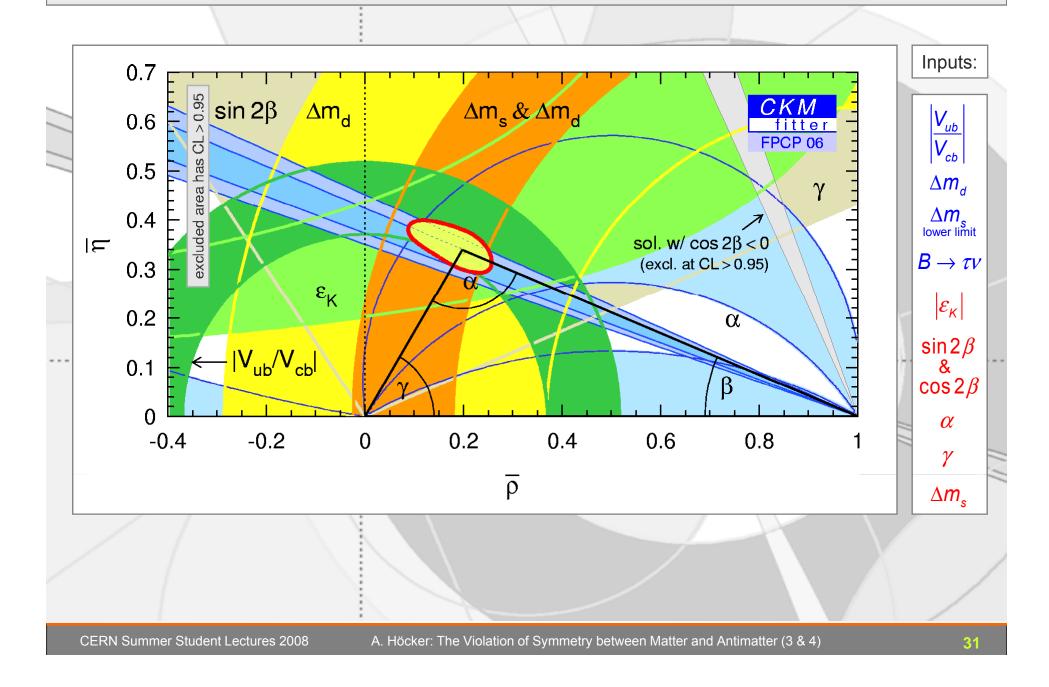
Some processes need larger data samples, now approached by the *B* factories:

- 1. *CP*-violation measurements in $B^0 \to \pi^+\pi^-$, $\rho^+\pi^- \rho^+\rho^-$ determine $\alpha(\overline{\rho},\overline{\eta})$
- 2. Direct-*CP*-violation measurements in $B \rightarrow DK$ determine $\gamma = \arctan\left(\frac{\overline{\eta}}{\overline{\rho}}\right)$
- 3. The rates of $b \rightarrow d$ loop transitions determine $|V_{td}|$
- 4. The leptonic decay $B^+ \to \tau^+ \nu$ ($\overline{b}d \to W^+$ "tree annihilation") determines $|V_{ub}|$



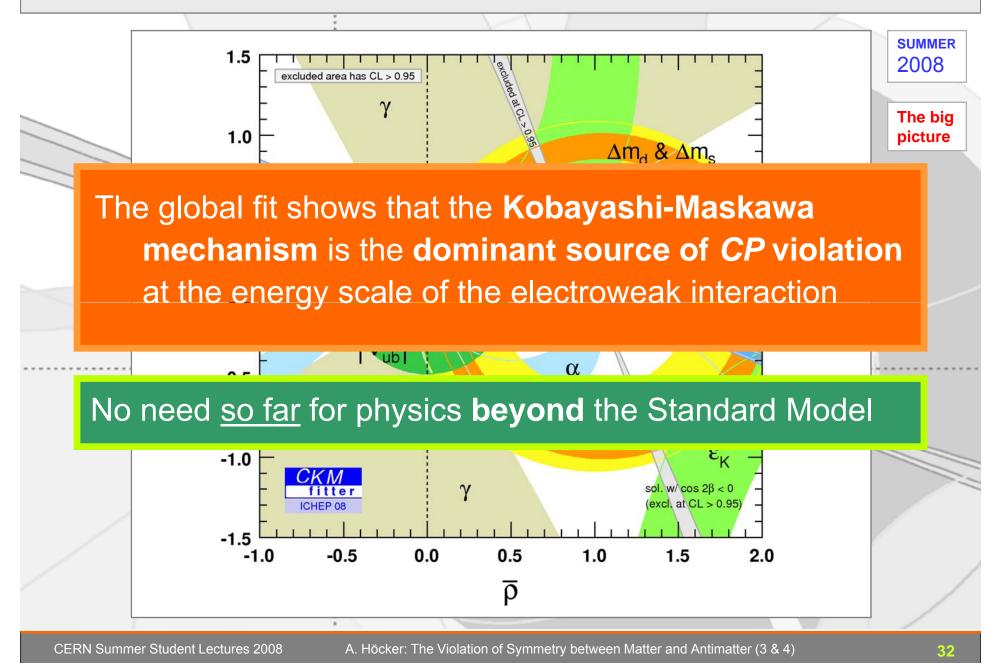
The Unitarity Triangle

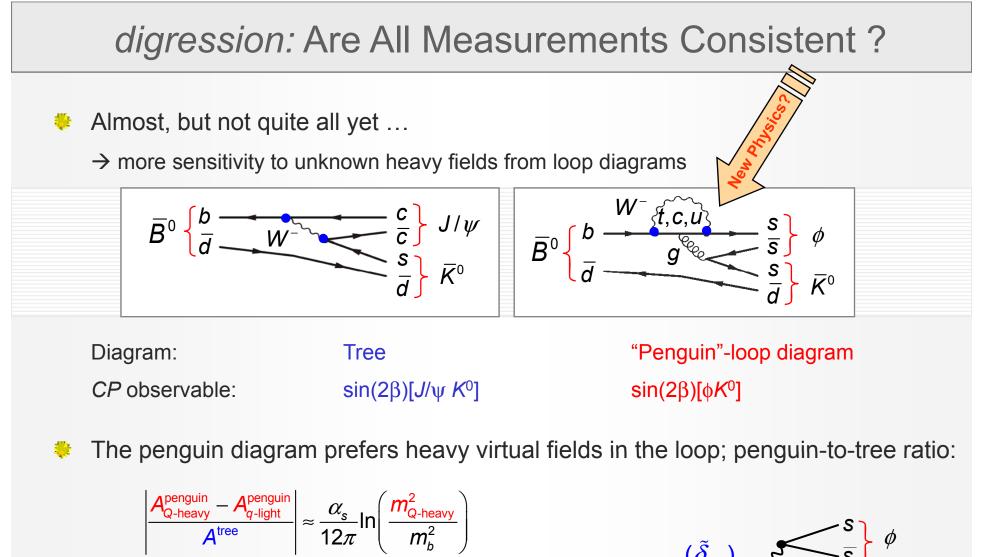
from the global CKM fit



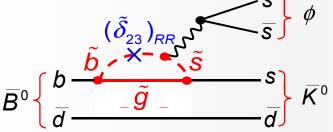
The Unitarity Triangle

from the global CKM fit

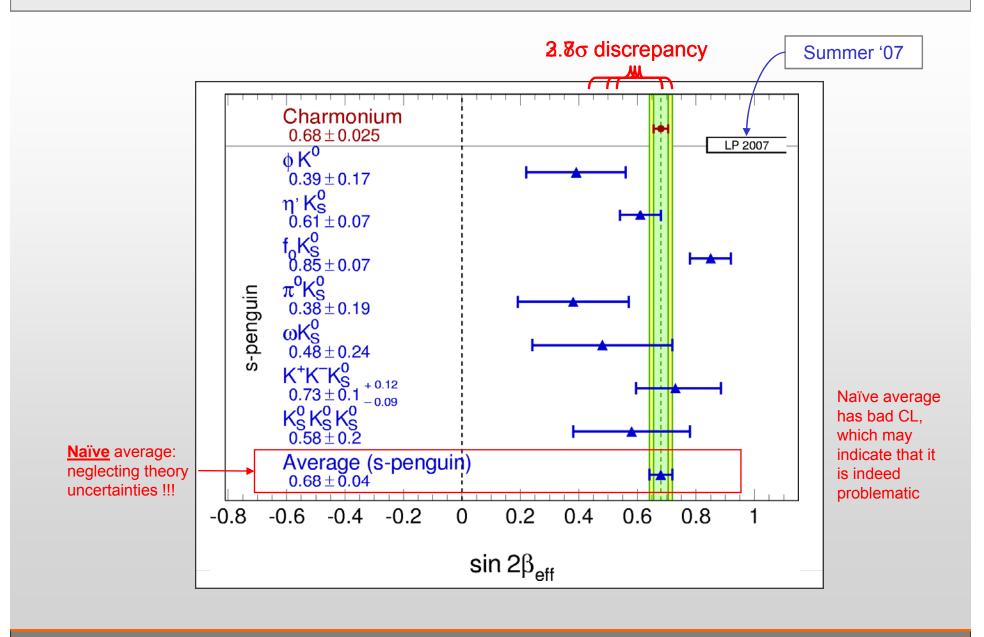




GUT-inspired example for SUSY penguin diagram:



digression: CP Violation in Penguin Modes

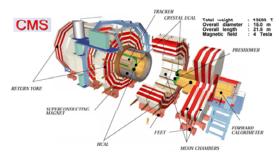


The Future of *B* Physics and *CP* Violation at the LHC

ATLAS

CMS





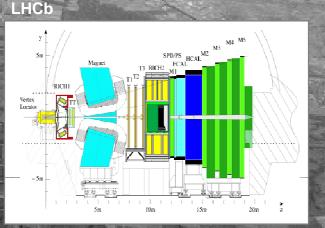
ALTAS and CMS concentrate on "high- p_{τ} " discovery physics.

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Their *B*-physics potential relies on the low- p_T performance of the Trigger systems.

LHCb is **not** a fixed-target experiment (looks like one). It concentrates on low- $p_T B$ physics.

Virtues over ATLAS & CMS: Low- p_T track trigger, particle ID & better mass resolution

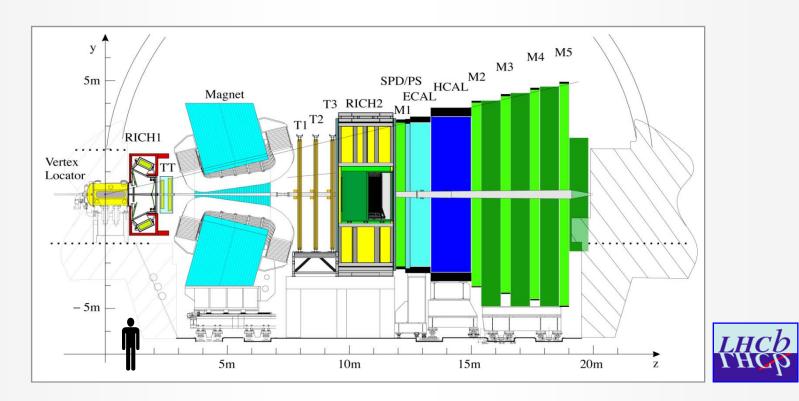


B Physics at Tevatron and LHC



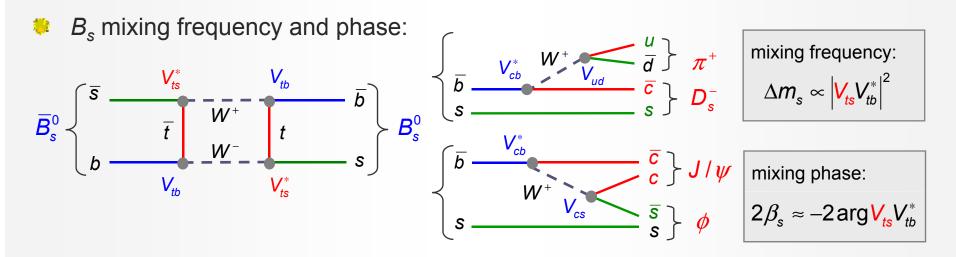
B physics at hadron colliders is complementary to the e^+e^-B factories.

- **Strengths:** High statistics; accesses the B_s ; sensitive to very rare modes, if clean signature; production of *b* baryons and B_c mesons
- **Weaknesses:** Worse tagging (no quantum coherence) and background; no rare modes with neutrinos can be reconstructed; less efficient for π^0 ;



digression: B Physics at Tevatron and LHC

Prime Measurements: (many, many more interesting measurements to be done!)



Frequency: just measured by CDF! CKM fit prediction not very precise yet (needs γ)

<u>Phase</u>: not measured yet, but precisely known in SM: excellent probe for new physics

B_s → $\mu^+\mu^-$: FCNC (box & EW-penguin-mediated) rare decay (BR ~ 3 ·10⁻⁹; current limit (CDF) < 5.8 ·10⁻⁸ at 95% CL)

