

### Superconducting magnets

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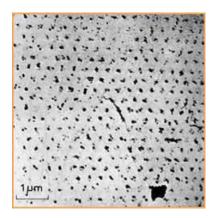


- The science of superconducting magnets is a exciting, fancy and dirty mixture of physics, engineering, and chemistry
  - Chemistry and material science: the quest for superconducting materials with better performances
  - Quantum physics: the key mechanisms of superconductivity
  - Classical electrodynamics: magnet design
  - Mechanical engineering: support structures
  - Electrical engineering: powering of the magnets and their protection
  - Cryogenics: keep them cool ...
- The cost optimization also plays a relevant role
  - Keep them cheap ...





- An example of the variety of the issues to be taken into account
  - The field of the LHC dipoles (8.3 T) is related to the critical field of Niobium-Titanium (Nb-Ti), which is determined by the microscopic quantum properties of the material



Quantized fluxoids penetrating a superconductor used in accelerator magnets



A 15 m truck unloading a 27 tons LHC dipole

- The length of the LHC dipoles (15 m) has been determined by the maximal dimensions of (regular) trucks allowed on European roads
- This makes the subject complex, challenging and complete for the formation of a (young) physicist or engineer



- The size of our objects
  - Length of an high energy physics accelerator: ~Km







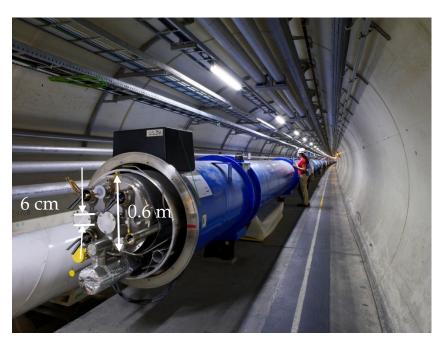
Main ring at Fermilab, Chicago, US



- The size of our objects
  - Length of an accelerator magnet: ~10 m
  - Diameter of an accelerator magnet: ~m
  - Beam pipe size of an accelerator magnet: ~cm



Unloading a 27 tons dipole



Dipoles in the LHC tunnel, Geneva, CH



A stack of LHC dipoles, CERN, Geneva, CH



#### **CONTENTS**

Introduction: the synchrotron and its magnets

Why do we need Km long accelerators to get TeV energies?

What are the physical limits to create strong magnetic fields?

- Hints on coil lay-out and normal conducting electromagnets
- Advantages of superconducting magnets, and basics of superconductivity (Nb-Ti limit: 13-14 T)

What are the practical limits imposed by magnet design and operation?

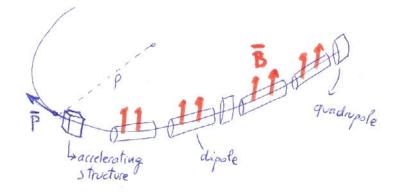
- Coil lay-out and operational margins (Nb-Ti limit: 8-9 T)
- Hints on Nb<sub>3</sub>Sn: towards 15-17 T?
- Cables

Some features of magnets for detectors



## 1. INTRODUCTION: PRINCIPLES OF A SYNCHROTRON

- Electro-magnetic field accelerates particles
- Magnetic field steers the particles in a closed (~circular) orbit

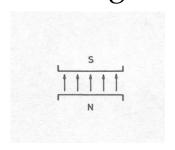


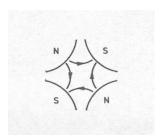
- To drive particles through the same accelerating structure several times
- As the particle is accelerated, its energy increases and the magnetic field is increased ("synchro") to keep the particles on the same orbit
- What are the limitations to increase the energy?
  - Proton machines: the maximum field of the dipoles (LHC, Tevatron, SPS ...)
  - Electron machines: the synchrotron radiation due to bending trajectories (LEP)

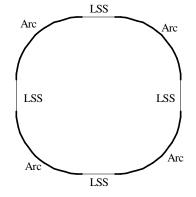


### 1. INTRODUCTION: NEEDED MAGNETIC FIELDS

The arcs: region where the beam is bent





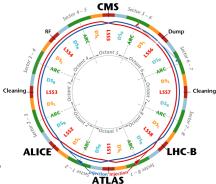


<u>Dipoles</u> for bending <u>Quadrupoles</u> for focusing

Sextupoles, octupoles ... for correcting

[see talk about accelerator physics by S. Gilardoni and E. Metral]

A schematic view of a synchrotron



The lay-out of the LHC

Long straight sections (LSS)

- Interaction regions (IR) housing the experiments
  - Solenoids (detector magnets) acting as spectrometers
- Regions for other services
  - Beam injection and dump (dipole kickers)
  - Accelerating structure (RF cavities) and beam cleaning (collimators)



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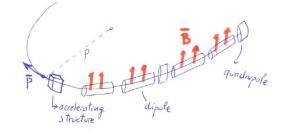
## 2. WHY DO WE NEED MANY Km TO GET A FEW TeV?

- Kinematics of circular motion
- Relativistic dynamics

$$\vec{p} = m \gamma \vec{v}$$

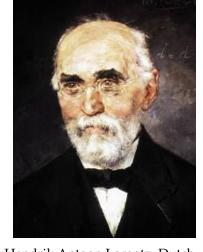
$$\left| \frac{d\vec{v}}{dt} \right| = \frac{v^2}{\rho}$$

$$\vec{F} = e\vec{v} \times \vec{B}$$



$$F = evB$$

$$\vec{F} = \frac{d}{dt} p = m \frac{d}{dt} (\gamma v) \sim m \gamma \frac{d}{dt} v$$



Hendrik Antoon Lorentz, Dutch
(18 July 1853 – 4 February 1928),
painted by Menso Kamerlingh Onnes,
brother of Heinke, who discovered
superconductivity

$$F = m\gamma \left| \frac{d\vec{v}}{dt} \right| = m\gamma \frac{v^2}{\rho}$$

$$eB = m\gamma \frac{v}{\rho} = \frac{p}{\rho}$$

$$p = eB\rho$$



### 2. WHY DO WE NEED MANY Km TO GET A FEW TeV?

• Relation momentum-magnetic field-orbit radius

$$p = eB\rho$$

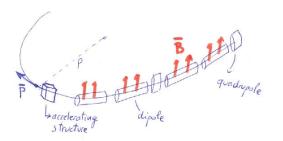
Preservation of 4-momentum

$$E^{2} - p^{2}c^{2} = m^{2}c^{4}$$
  $E = \sqrt{m^{2}c^{4} + p^{2}c^{2}}$ 

• Ultra-relativistic regime

$$pc \gg mc^2$$

$$E \sim pc$$



$$E = ceB\rho$$

Using practical units for a proton/electron, one has

$$E[GeV] = 0.3 \times B[T] \times \rho[m]$$

- Remember 1 eV=1.602×10<sup>-19</sup> J
- Remember 1 e=  $1.602 \times 10^{-19}$  C

The magnetic field is in Tesla ...

		r [m]	B [T]	E [TeV]
FNAL	Tevatron	758	4.40	1.000
DESY	HERA	569	4.80	0.820
<b>IHEP</b>	UNK	2000	5.00	3.000
SSCL	SSC	9818	6.79	20.000
BNL	RHIC	98	3.40	0.100
CERN	LHC	2801	8.33	7.000
CERN	LEP	2801	0.12	0.100



#### TESLA INTERLUDE

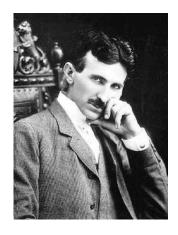
#### Nikolai Tesla (10 July 1856 - 7 January 1943)

- Born at midnight during an electrical storm in Smiljan near Gospić (now Croatia)
- Son of an orthodox priest
- A national hero in Serbia, Croatia and Bosnia

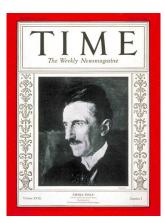
#### Career

- Polytechnic in Gratz (Austria) and Prague
- Emigrated in the States in 1884
- Electrical engineer
- Inventor of the alternating current induction motor (1887)
- Author of 250 patents

A rather strange character, a lot of legends on him ... (check on wikipedia)



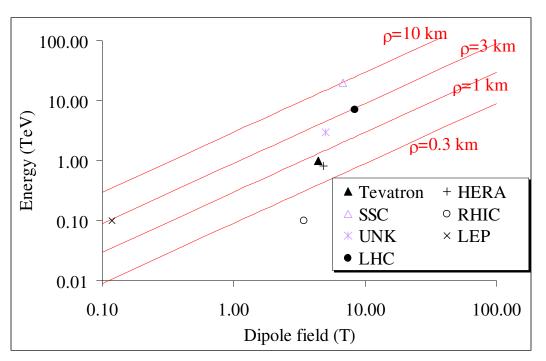




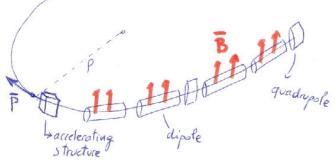


## 2. WHY DO WE NEED MANY Km TO GET A FEW TeV?

- Relation momentum-magnetic field-orbit radius
  - Having 8 T magnets, we need 3 Km curvature radius to have 7 TeV
  - If we would have 800 T magnets, 30 m would be enough ...
  - We will now show why 8 T is the present limit



$$E[GeV] = 0.3 \times B[T] \times \rho[m]$$





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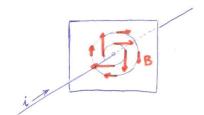
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## 3. ULTIMATE LIMITS TO STRONG FIELDS: BIOT-SAVART LAW

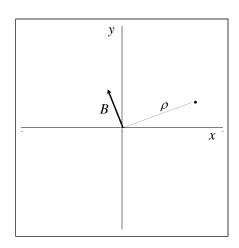
- A magnetic field is generated by two mechanisms
  - An electrical charge in movement (macroscopic current)
  - Coherent alignment of atomic magnetic momentum (ferromagnetic domains)

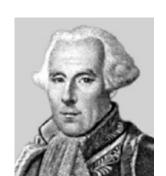


Biot-Savart law: magnetic field generated by a current line is

$$|B| = \frac{I\mu_0}{2\pi\rho}$$

- Proportional to current
- Inversely proportional to distance
- Perpendicular to current direction and distance





Félix Savart, French (June 30, 1791-March 16, 1841)



Jean-Baptiste Biot, French (April 21, 1774 – February 3, 1862)



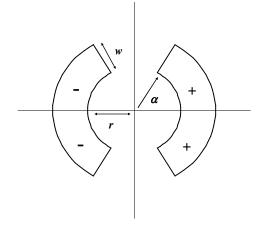
### 3. ULTIMATE LIMITS TO STRONG FIELDS: FIELD OF A WINDING

- Magnetic field generated by a winding
  - We compute the central field given by a sector dipole with uniform current density j

$$|B| = \frac{I\mu_0}{2\pi\rho} \qquad I \to j\rho d\rho d\theta$$

$$B = -4 \frac{j\mu_0}{2\pi} \int_{0}^{\alpha} \int_{r}^{r+w} \frac{\cos\theta}{\rho} \rho d\rho d\theta = -\frac{2j\mu_0}{\pi} w \sin\alpha$$

• Setting  $\alpha$ =60° one gets a more uniform field



- $B \propto \text{current density (obvious)}$
- $B \propto \text{coil width } w \text{ (less obvious)}$
- *B* is independent of the aperture *r* (much less obvious)

$$B[T] \approx 7 \times 10^{-4} j[\text{A/mm}^2] w[\text{mm}]$$

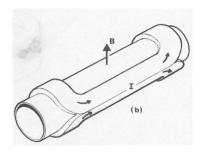


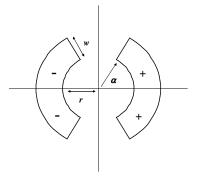
### 3. ULTIMATE LIMITS TO STRONG FIELDS: SUPERCONDUCTORS VERSUS NORMAL CONDUCTORS

Magnetic field generated by a winding of width w

$$B[T] \approx 7 \times 10^{-4} j[\text{A/mm}^2] w[\text{mm}]$$

- Superconductors allow current densities in the sc material of  $\sim 1000 \, [A/mm^2]$ 
  - Example: LHC dipoles have  $j_{sc} \sim 1500 \text{ A/mm}^2$   $j \sim 350 \text{ A/mm}^2$ , ( $\sim \frac{1}{4}$  of the cable made by sc!) Coil width  $w \sim 30 \text{ mm}$ , B $\sim 8 \text{ T}$
- The current density in copper for typical wires used in transmission lines is ~ 5 [A/mm²]
- Using special techniques for cooling one can arrive up to ~ 100 [A/mm²]
- There is still a factor 10, and moreover the normal conducting consumes a lot of power ...









### 3. ULTIMATE LIMITS TO STRONG FIELDS: SUPERCONDUCTORS VERSUS NORMAL CONDUCTORS

- Iron-dominated electromagnets
  - Normal conducting magnets for accelerators are made with a copper winding around a ferromagnetic core that greatly enhances the field
    - This is a very effective and cheap design

- From Mormal conducting coils
- The shape of the pole gives the field homogeneity
- The limit is given by the iron saturation, i.e. 2 T
  - This limit is due to the atomic properties, i.e. it looks like a hard limit
- Therefore, superconducting magnets today give a factor ~4-5 larger field than normal conducting not so bad anyway ...
  - LHC with 2 T magnets would be 100 Km long, and it would not fit between the lake and the Jura mountains ...



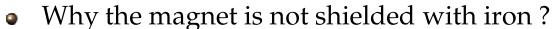
### INTERLUDE: THE TERMINATOR-3 ACCELERATOR

We apply some concepts to the accelerator shown in Terminator-3 [Columbia Pictures, 2003]

Estimation of the magnetic field

$$E[GeV] = 0.3 \times B[T] \times \rho[m]$$

- Energy = 5760 GeV
- Radius ~30 m
- Field =  $5760/0.3/30 \sim 700 \text{ T (a lot !)}$  Energy of the machine (left) and size of the accelerator (right)



- Assuming a bore of 25 mm radius, inner field of 700 T, iron saturation at 2 T, one needs 700\*25/2=9000 mm=9 m of iron ... no space in their tunnel!
- In the LHC, one has a bore of 28 mm radius, inner field of 8 T, one needs 8\*25/2=100 mm of iron
- Is it possible to have 700 T magnets ??







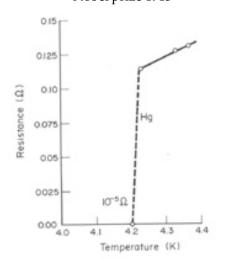
A magnet whose fringe field is not shielded



- In 1911, Kamerlingh Onnes discovers the superconductivity of mercury
  - Below 4.2 K, mercury has a non measurable electric resistance not very small, but zero!
  - This discovery has been made possible thanks to his efforts to liquifying Helium, a major technological advancement needed for the discovery
  - 4.2 K is called the critical temperature: below it the material is superconductor
  - Superconductivity has been discovered in other elements, with critical temperatures ranging from a few K (low temp. sc) to up to 150 K (high temperature sc)
  - The behaviour has been modeled later in terms of quantum mechanics
    - Electron form pairs (Cooper pairs) that act as a boson, and "freely" move in the superconductor without resistance
    - Several Nobel prizes have been awarded in this field ...

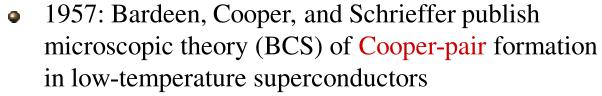


Heinke Kamerlingh Onnes (18 July 1853 – 4 February 1928) Nobel prize 1913





- 1950: Ginzburg and Landau propose a macroscopic theory (GL) for superconductivity
  - Nobel prize in 2003 to Ginzburg, Abrikosov, Leggett



Nobel prize in 1972

- 1986: Bednorz and Muller discover superconductivity at high temperatures in layered materials having copper oxide planes
  - Nobel prize in 1986 (a fast one ...)



Ginzburg and Landau (circa 1947)







Bardeen, Cooper and Schrieffer





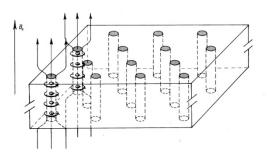
George Bednorz and Alexander Muller E. Todesco - Superconducting magnets 21



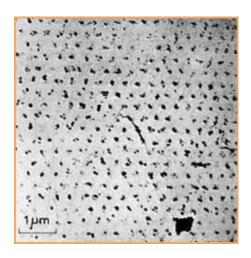
- Type I superconductors: they expel magnetic field (example: Hg)
  - They cannot be used for building magnets
- Type II superconductors: they do not expel magnetic field (example: Nb-Ti)
  - The magnetic field penetrates locally in very tiny quantized vortex

$$\phi_0 = \frac{h}{2e}$$

- The current acts on the fluxoids with a Lorentz force that must be balanced, otherwise they start to move, dissipate, and the superconductivity is lost
- The more current density, the less magnetic field, and viceversa → concept of critical surface
- The sc material is built to have a strong pinning force to counteract fluxoid motion
  - Pinning centers are generated with imperfections in the lattice
  - It is a very delicate and fascinating cooking ...



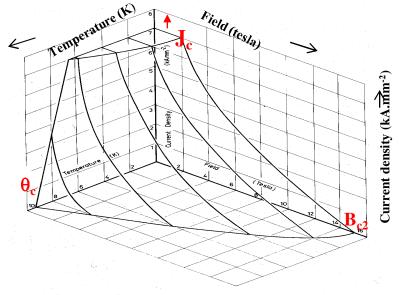
Artist view of flux penetration in a type II superconductor



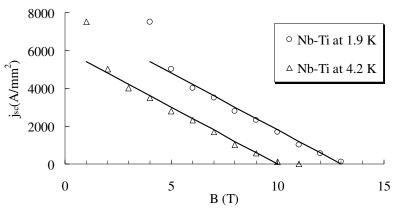
First image of flux penetration, U. Essmann and H. Trauble Max-Planck Institute, Stuttgart Physics Letters 24A, 526 (1967)



- The material is superconductor as long as B, j, and temperature stay below the critical surface
  - The maximum current density ~ 10 000 A/mm<sup>2</sup>, but this at zero field and zero temperature
  - In a magnet, the winding has a current density to create a magnetic field → the magnetic field is also in the winding → this reduces the current density
  - The obvious ultimate limit to Nb-Ti dipoles is 14 T at zero temperature and zero current density, and 13 T at 1.9 K
  - In reality, we cannot get 13 T but much less
     around 8 T in the LHC why?



Critical surface for Nb-Ti



Section of the Nb-Ti critical surface at 1.9 and 4.2 K, and linear fit



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Some features of magnets for detectors



### 4. LIMITS IN MAGNET DESIGN: COIL WIDTH AND MAGNET SIZE

- We compute what field can be reached for a sector coil of width *w* 
  - We characterize the critical surface by two parameters

$$j_c = \kappa c(B_{c2}^* - B)$$

and we added  $\kappa$  which takes into account that only a fraction ( $\sim$ <sup>1</sup>/<sub>4</sub>) of the coil is made up to superconductor

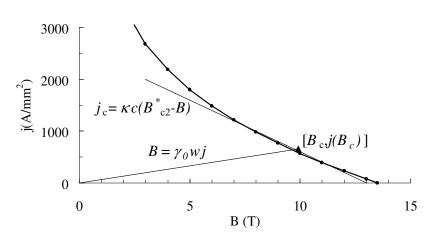
The relation between current density and field is  $B = \gamma_0 wj$ 

and the field that can be reached is given by  $B_c = \gamma_0 w j_c = \gamma_0 w \kappa c (B_{c2}^* - B_c)$ 

$$B_c = \gamma_0 w j_c = \gamma_0 w \kappa c (B_{c2}^* - B_c)$$

$$B_c = B_{c2}^* \frac{\kappa c \gamma_0 w}{1 + \kappa c \gamma_0 w}$$

The larger coil, the smaller  $j_c$ , the larger *B* 



Critical surface for Nb-Ti: j versus B and magnet loadline

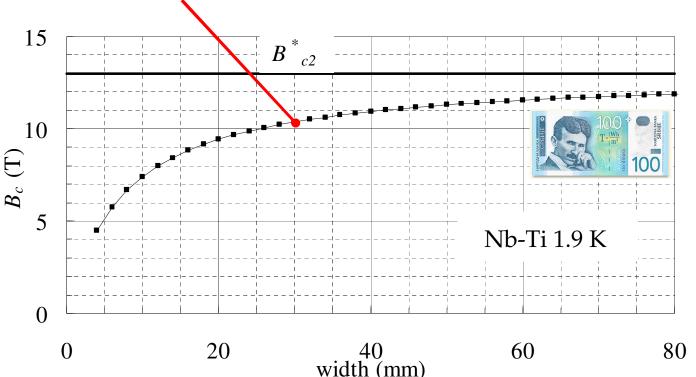


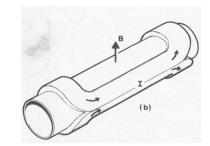
## 4. LIMITS IN MAGNET DESIGN: COIL WIDTH AND MAGNET SIZE

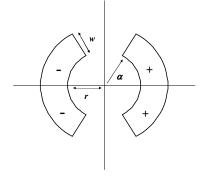
- We have computed what field can be reached for a sector coil of width w for Nb-Ti
  - There is a slow saturation towards 13 T

 $B_c = B_{c2}^* \frac{\kappa c \gamma_0 w}{1 + \kappa c \gamma_0 w}$ 

- The last Tesla are very expensive in terms of coil
- LHC dipole has been set on 30 mm coil width, giving ~10 T







Field versus coil thickness for Nb-Ti at 1.9 K



### 4. LIMITS IN MAGNET DESIGN: COIL WIDTH AND MAGNET SIZE

- One cannot work on the critical surface
  - Any disturbance producing energy (beam loss, coil movements under Lorentz forces) increases the temperature and the superconductivity is lost
    - In this case one has a transition called quench the energy must be dumped without burning the magnet
    - The energy in one circuit of the LHC dipoles is 1 GJ!

- One works at ~80-90% from the critical surface
  - LHC dipoles are giving the maximum field 10 T given by a reasonable amount of coil (30 mm) for Nb-Ti at 1.9 K
  - At 80% one goes from 10 T to 8 T which is the baseline value
  - Transverse size of the magnet: we will show that the needed aperture is ~25 mm, plus 30 mm of coil, mechanical structure and iron shield (100 mm) → ~one meter of diameter

5.76 TeV REQUIRED



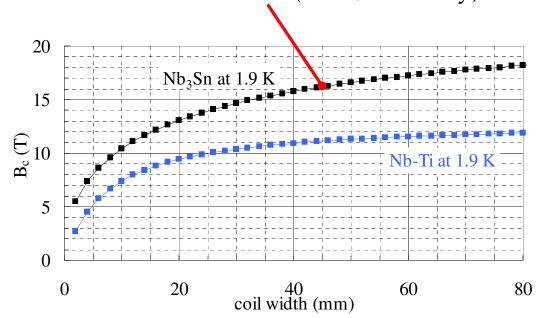
# 4. LIMITS IN MAGNET DESIGN: HINTS ON Nb<sub>3</sub>Sn

- Nb<sub>3</sub>Sn has a wider critical surface
  - But the material is more difficult to manufacture

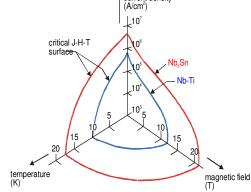
• It has never been used in accelerators, but tested successfully in short models and used in solenoids

• With Nb<sub>3</sub>Sn one could go up to 15-18 T

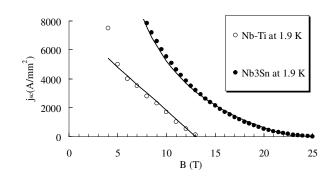
• World record is 16 T (HD1, Berkeley)



Field versus coil thickness for Nb-Ti and Nb<sub>3</sub>Sn at 1.9 K



Critical surface for Nb-Ti and Nb<sub>3</sub>Sn





### 4. LIMITS IN MAGNET DESIGN: HINTS ON CABLE GEOMETRY

- The superconducting cables are not bulk material but have a complex geometry
  - The cable is made of several (20-40) strands of ~1 mm diameter
    - This to carry more current and therefore to reduce the stored energy
  - The strands are made of superconducting filaments of ~5-50 μm diameter inside a copper matrix
    - to stabilize the superconductor
    - to minimize field distortions due to superconductor magnetization
    - to protect the superconductor when the superconductivity is lost (the current flows in the copper and does not burn the sc)
  - Filaments and the strands are twisted
    - to reduce coupling currents and AC losses

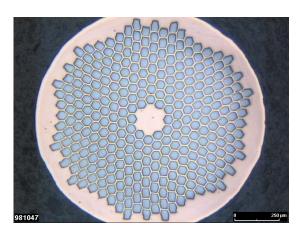




Sketch of superconducting cable and cross-section



Superconducting cable made of strands



Superconducting strand



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#### 5. MAGNETS FOR DETECTORS

- What is the beam size in an accelerator ?
  - Inverse proportional to the sqrt energy
    - The larger the energy, the smaller the beam!

$$\sigma = \sqrt{\frac{\mathcal{E}_n \mathcal{\beta}_f}{\gamma}}$$

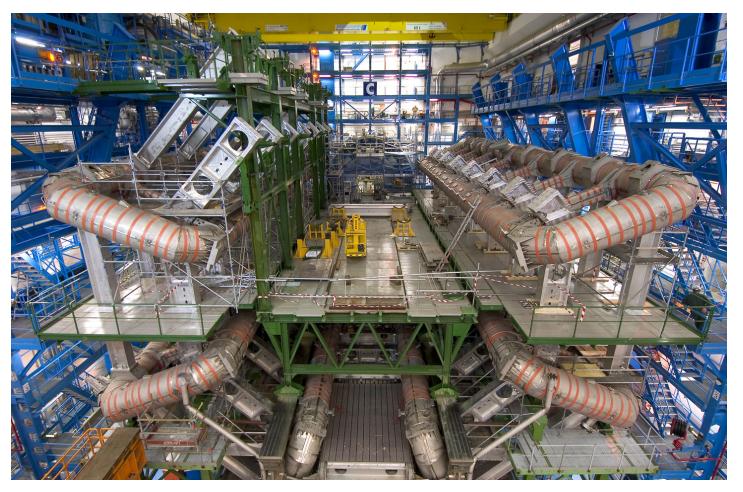
- Size of the beam pipe is given by the values at the injection energy
- Proportional to the sqrt of the emittance  $\varepsilon_n$  (property of the injectors)
- Proportional to the sqrt of the  $\beta$  function
  - This is related to the optics the  $\beta$  function in the arc is proportional to the distance L between quadrupoles

$$\beta_f = (2 + \sqrt{2})L \sim 3.4L$$

- Example: LHC
  - Injection energy 450 GeV,  $\gamma$ =480
  - Cell length L=50 m,  $\beta_f=170$  m
  - $\varepsilon_n = 3.75 \times 10^{-6} \text{m rad}$
  - The beam size  $\sigma$ =1.2 mm the magnet aperture (radius) is 28 mm to house  $10\sigma$  plus some margin



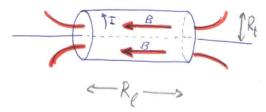
• The beam is small ... why are detectors so large?



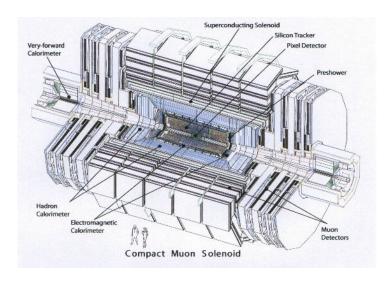
The toroidal coils of ATLAS experiment



- Detector magnets provide a field to bend the particles generated by collisions (not the particles of the beam!)
- The measurement of the bending radius gives an estimate of the charge and energy of the particle
- Different lay-outs
  - A solenoid providing a field parallel to the beam direction (example: LHC CMS, LEP ALEPH, Tevatron CDF)
    - Field lines perpendicular to (*x*,*y*)



Sketch of a detector based on a solenoid



Sketch of the CMS detector in the LHC

- A series of toroidal coils to provide a circular field around the beam (example: LHC ATLAS)
  - Field lines of circular shape in the (x,y) plane





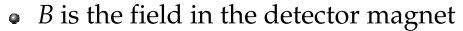
The solenoid of CMS experiment



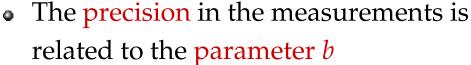
#### Detector transverse size

• The particle is bent with a curvature radius

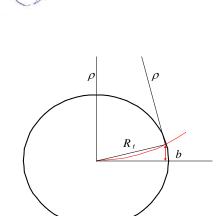
$$E = eB\rho$$







$$b = \frac{R_t^2}{2\rho} = \frac{e}{2} \frac{R_t^2 B}{E}$$



Detector

- The magnetic field is limited by the technology
- If we double the energy of the machine, keeping the same magnetic field, we must make a 1.4 times larger detector ...



- Detector transverse size
  - *B* is the field in the detector magnet
  - $R_t$  is the transverse radius of the detector magnet
  - The precision in the measurements is  $\propto 1/b$

$$b = \frac{R_t^2}{2\rho} = \frac{e}{2} \frac{R_t^2 B}{E}$$

$$b \sim 0.15 \frac{R_t^2 B}{E[\text{GeV}]}$$

- Examples
  - LEP ALEPH: E=100 GeV, B=1.5 T,  $R_t=6.5 \text{ m}$ ,  $R_t=2.65 \text{ m}$ , b=16 mm
    - that's why we need sizes of meters and not centimeters!
- The magnetic field is limited by technology
  - But fields are not so high as for accelerator dipoles (4 T instead of 8 T)
  - Note that the precision with  $BR_t^2$  better large than high field ...
- Detector longitudinal size
  - several issues are involved not easy to give simple scaling laws

# CERN

#### **SUMMARY**

- We recalled the principles of a synchrotron
  - Large magnetic field allow a more compact synchrotron or a higher energy
- Principles of magnets
  - Why superconducting magnets are very effective
  - Their present limitations
  - The mechanisms behind superconductivity
- Main features of the design
  - The coils
  - The cable
- Detector magnets
  - The reasons for their huge size



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- Google Earth for the images of accelerators in the world
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- Columbia Pictures for some images of "Terminator-3: The rise of machines"