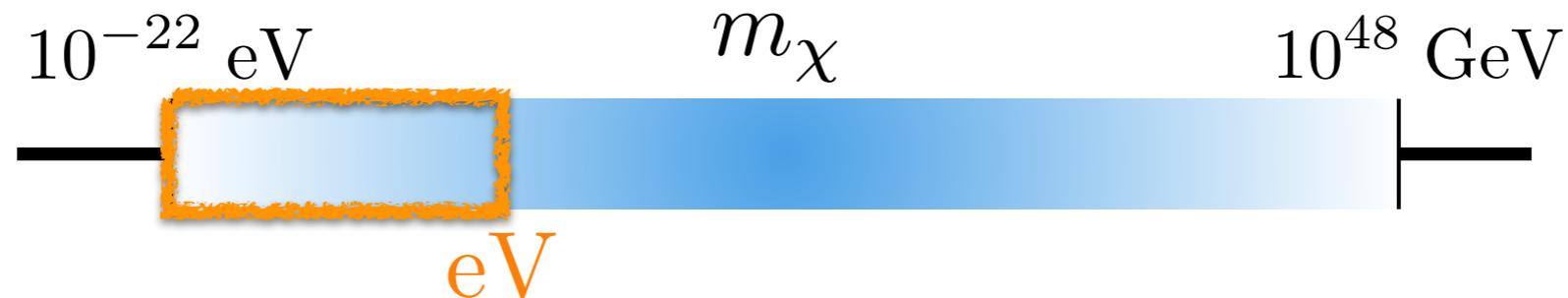


# A NEW CONCEPT FOR THE DETECTION OF AXION DARK MATTER

Raffaele Tito D'Agnolo - IPhT Saclay



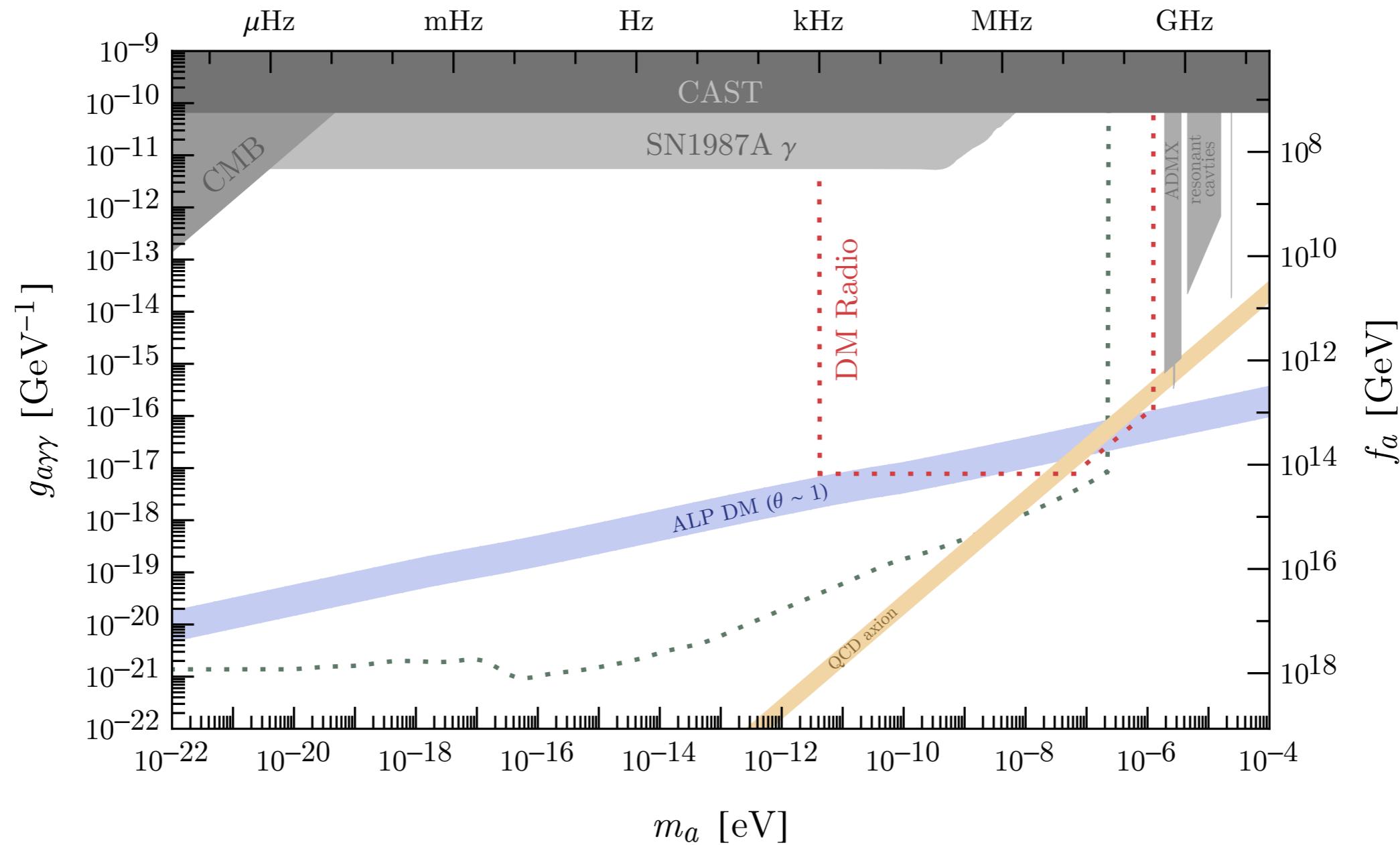


## Very good particle physics motivations:

Hui, Ostriker, Tremaine, Witten '17

- Top-Down from String Theory
- Strong CP Consistent with CMB
- Generically predicted in a class of solutions to the Hierarchy Problem
- Simple and predictive cosmology

$$\text{frequency} = m_a/2\pi$$

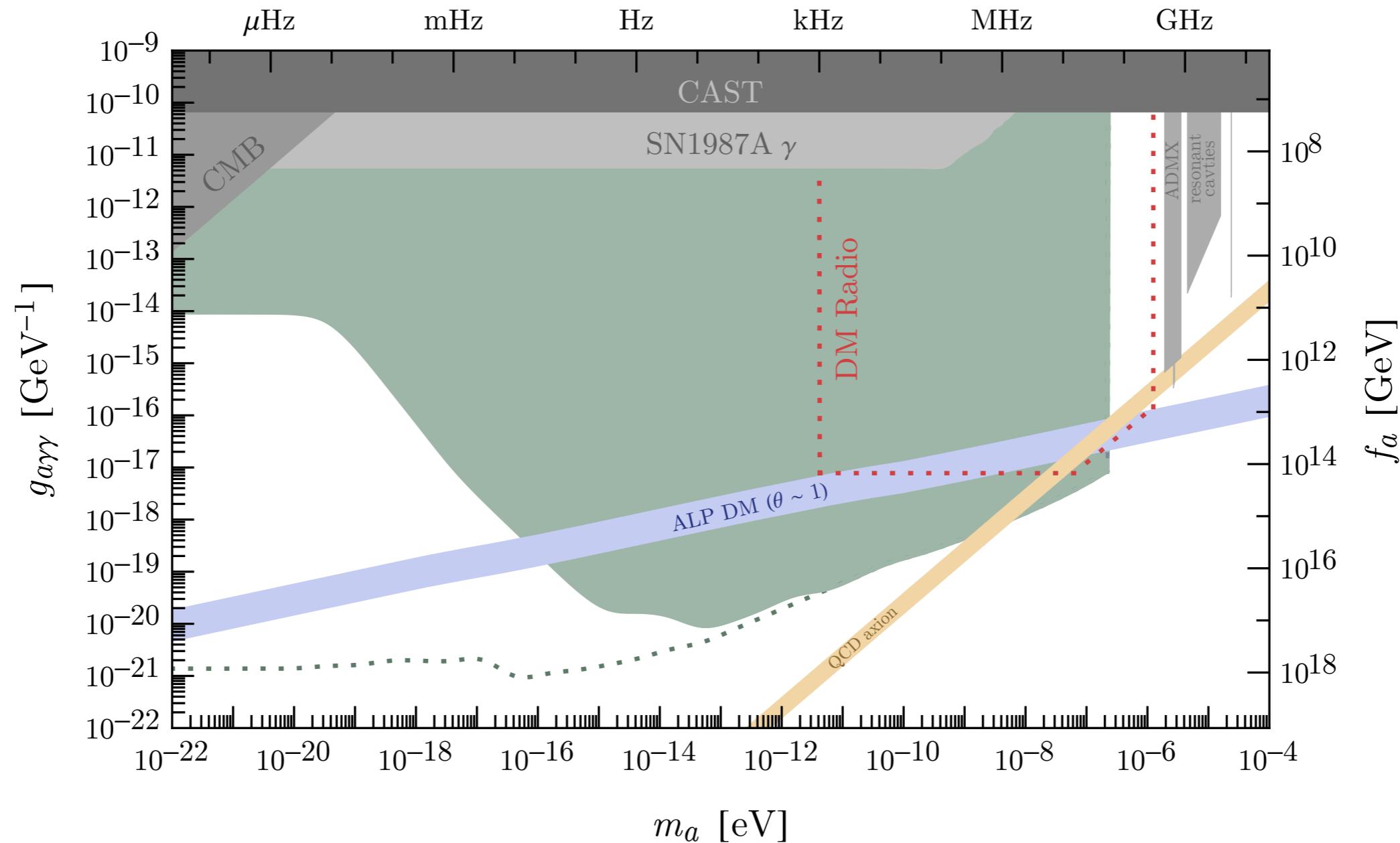




Our new experimental concept:

Initially developed with Superconducting Radio Frequency cavity experimentalists at SLAC

$$\text{frequency} = m_a/2\pi$$



A.Berlin, **RTD**, S. Ellis, C. Nantista, J. Nielson, P. Schuster, S. Tantawi, N. Toro, K. Zhou '19

A.Berlin, **RTD**, S. Ellis, K. Zhou '20

# AXION DM IN THE LABORATORY

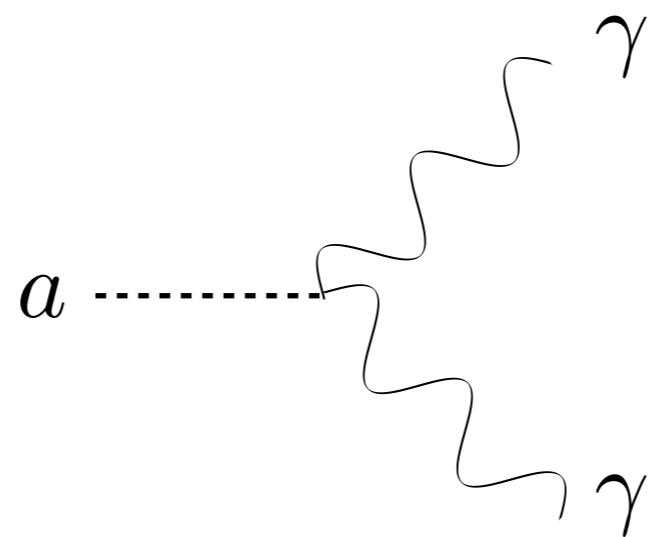
$$a(t) \simeq \frac{\sqrt{2\rho_{\text{DM}}}}{m_a} \cos(\omega_a t + \phi)$$

**Frequency:**  $\omega_a \simeq \text{GHz} \frac{m_a}{10^{-6} \text{ eV}}$

**Coherence:**  $\tau_a \simeq \text{ms} \frac{10^{-6} \text{ eV}}{m_a}$

**Max Exp. Size:**  $\lambda_a \simeq 200 \text{ m} \frac{10^{-6} \text{ eV}}{m_a}$

# AXION DETECTION



$$\nabla \times \mathbf{B} \simeq \partial_t \mathbf{E} + \mathbf{J} + \underline{g_{a\gamma\gamma} \mathbf{B} \partial_t a}$$

$$J_{\text{eff}}(t) \sim g_{a\gamma\gamma} B_0(t) \sqrt{\rho_{\text{DM}}} \cos m_a t$$

## Cavity:

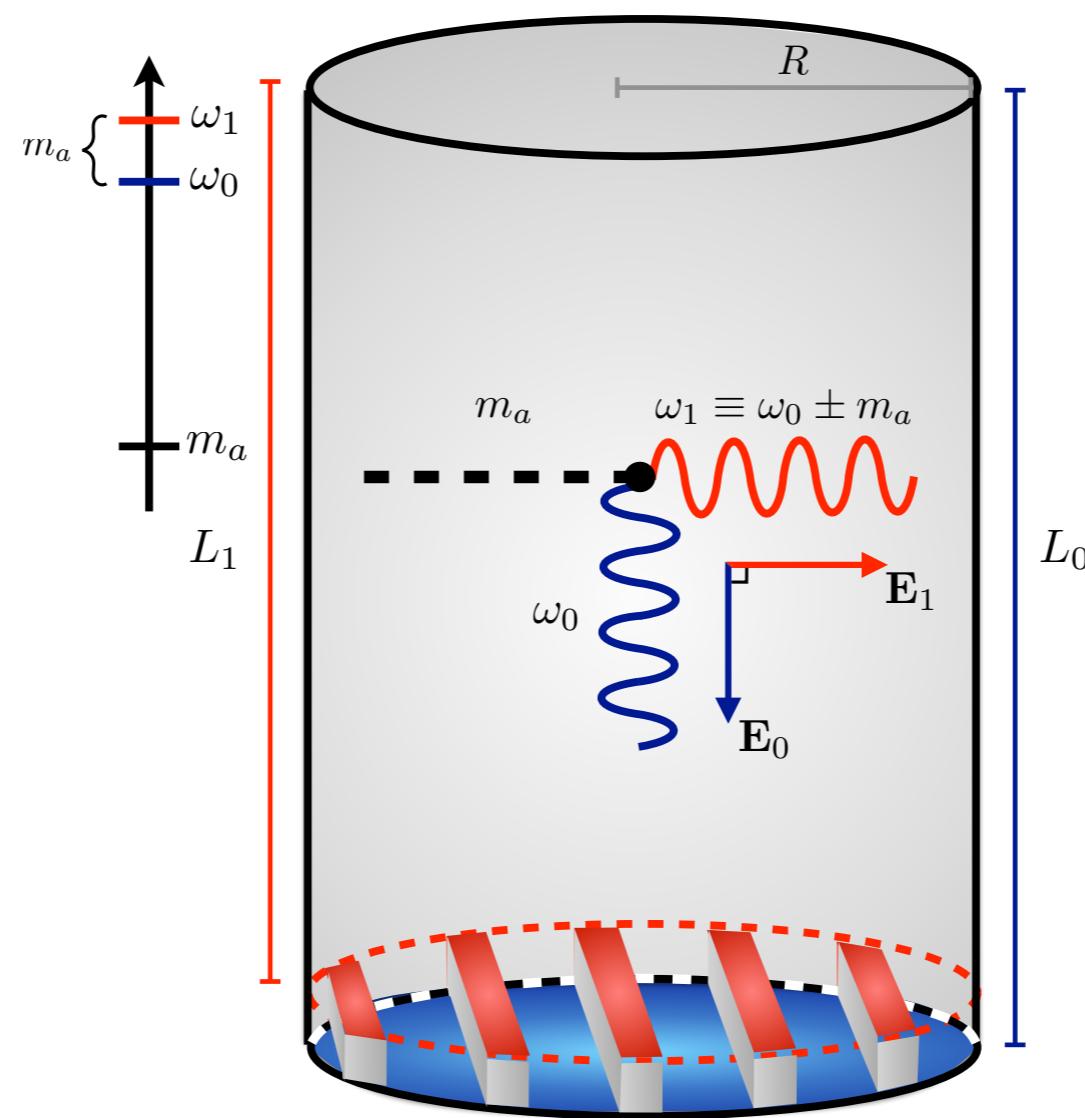
$$\sum_n \left( \partial_t^2 + \frac{\omega_n}{Q_n} \partial_t + \omega_n^2 \right) \mathbf{E}_n = \underline{g_{a\gamma\gamma} \partial_t(\mathbf{B} \partial_t a)}$$

$$\omega_1 \simeq m_a \quad \partial_t(\mathbf{B}) \simeq 0$$

## Problems:

**Cavity size**  $\sim 1/m_a$

**Signal power** decreases with  
axion mass



A.Berlin, **RTD**, S. Ellis, C. Nantista, J. Nielson, P. Schuster, S. Tantawi, N. Toro, K. Zhou '19

A.Berlin, **RTD**, S. Ellis, K. Zhou '20

$$\sum_n \left( \partial_t^2 + \frac{\omega_n}{Q_n} \partial_t + \omega_n^2 \right) \mathbf{E}_n = \underline{g_{a\gamma\gamma} \partial_t(\mathbf{B} \partial_t a)}$$

$$\omega_1 \simeq \omega_0 + m_a \quad \partial_t(\mathbf{B}) \simeq i\omega_0 \mathbf{B}$$

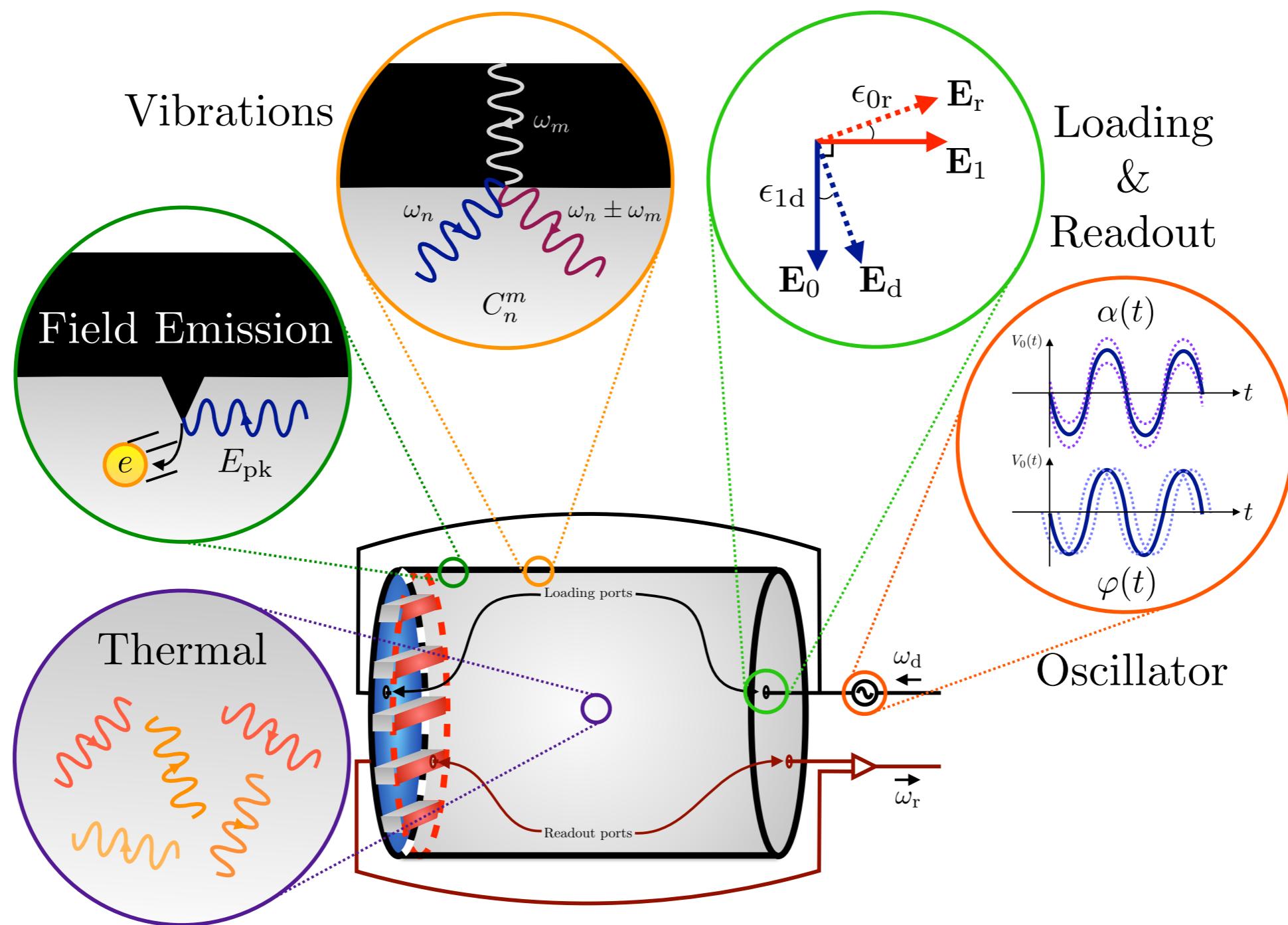
**Static:**

$$\mathbf{E}_1 \sim \frac{\cancel{m_a} g_{a\gamma\gamma} \sqrt{\rho_{\text{DM}}} \mathbf{B}}{m_a^2 - \omega_1^2 + i \frac{m_a \omega}{Q_1}}$$

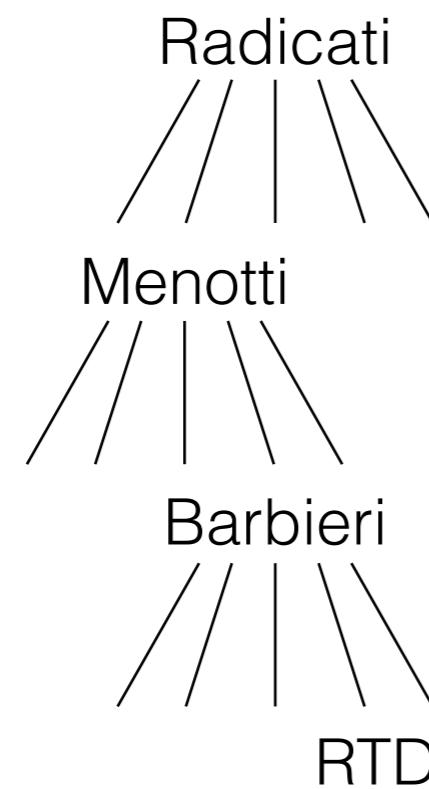
**Oscillating:**

$$\mathbf{E}_1 \sim \frac{\cancel{\omega_0} g_{a\gamma\gamma} \sqrt{\rho_{\text{DM}}} \mathbf{B}}{(\omega_0 + m_a)^2 - \omega_1^2 + i \frac{(\omega_0 + m_a)\omega}{Q_1}}$$

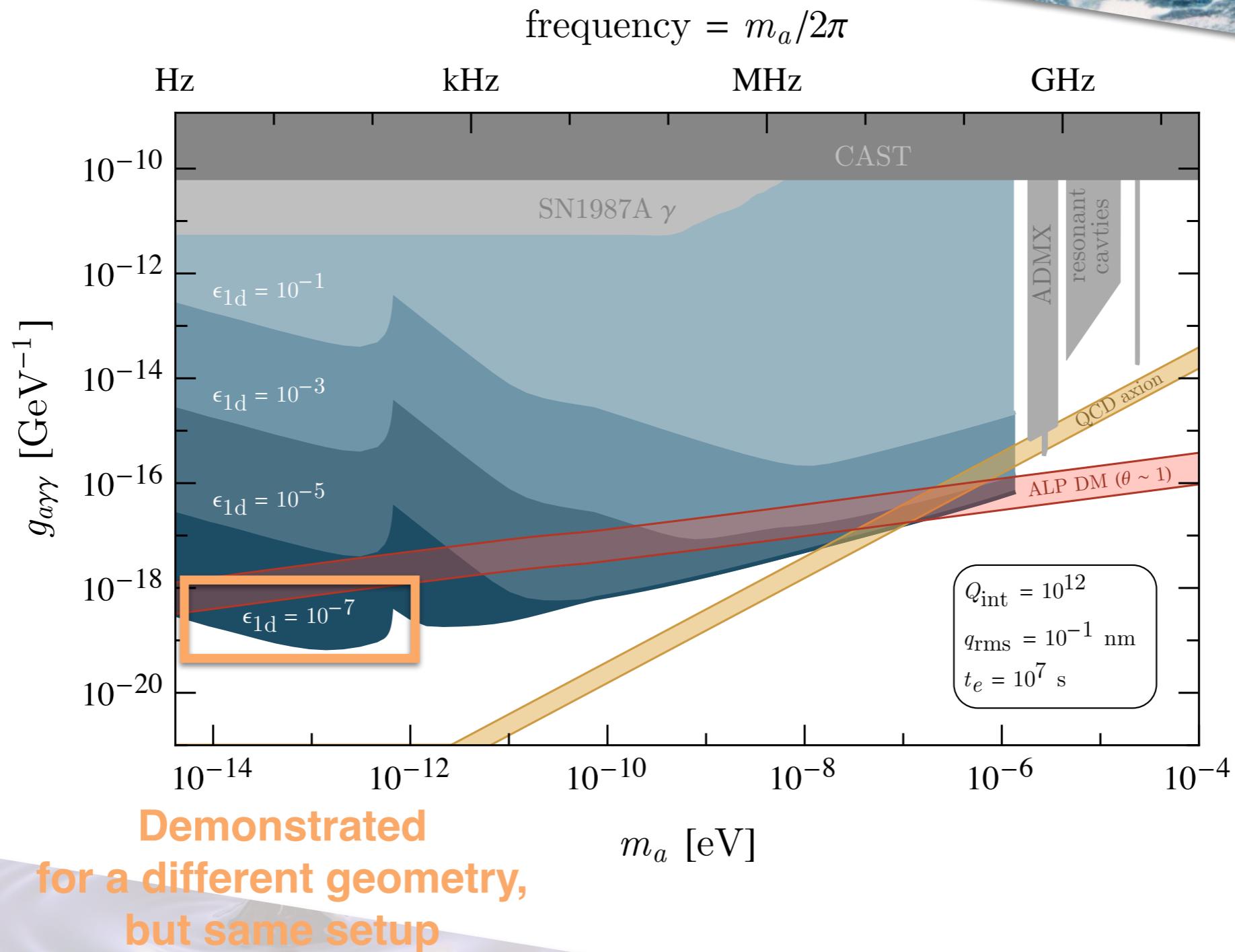
# NOISE



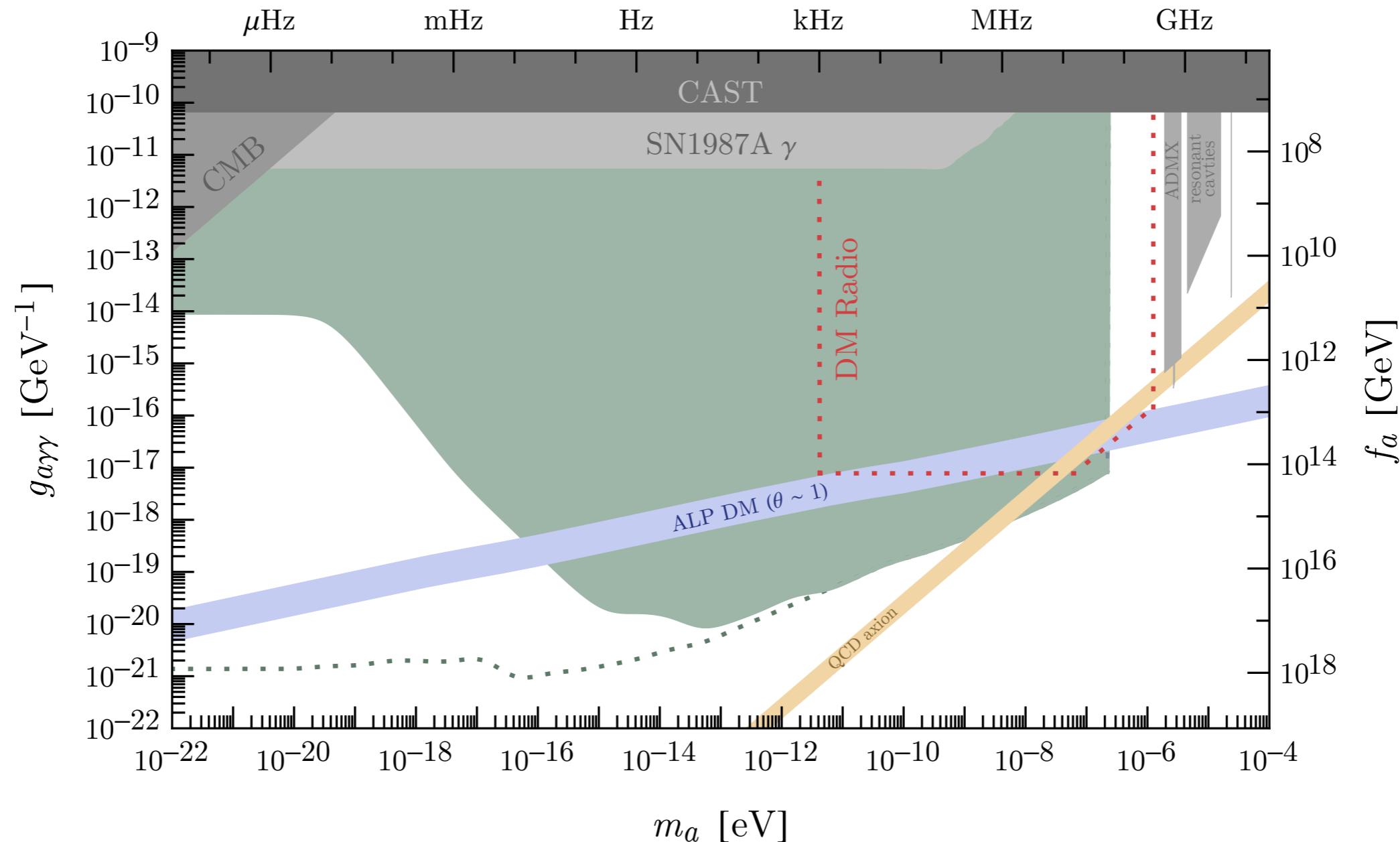
**A similar cavity already exists!**  
**Very well tested technology**  
Radicati, Pegoraro, Picasso '78



# ROBUSTNESS TO LOADING



$$\text{frequency} = m_a/2\pi$$

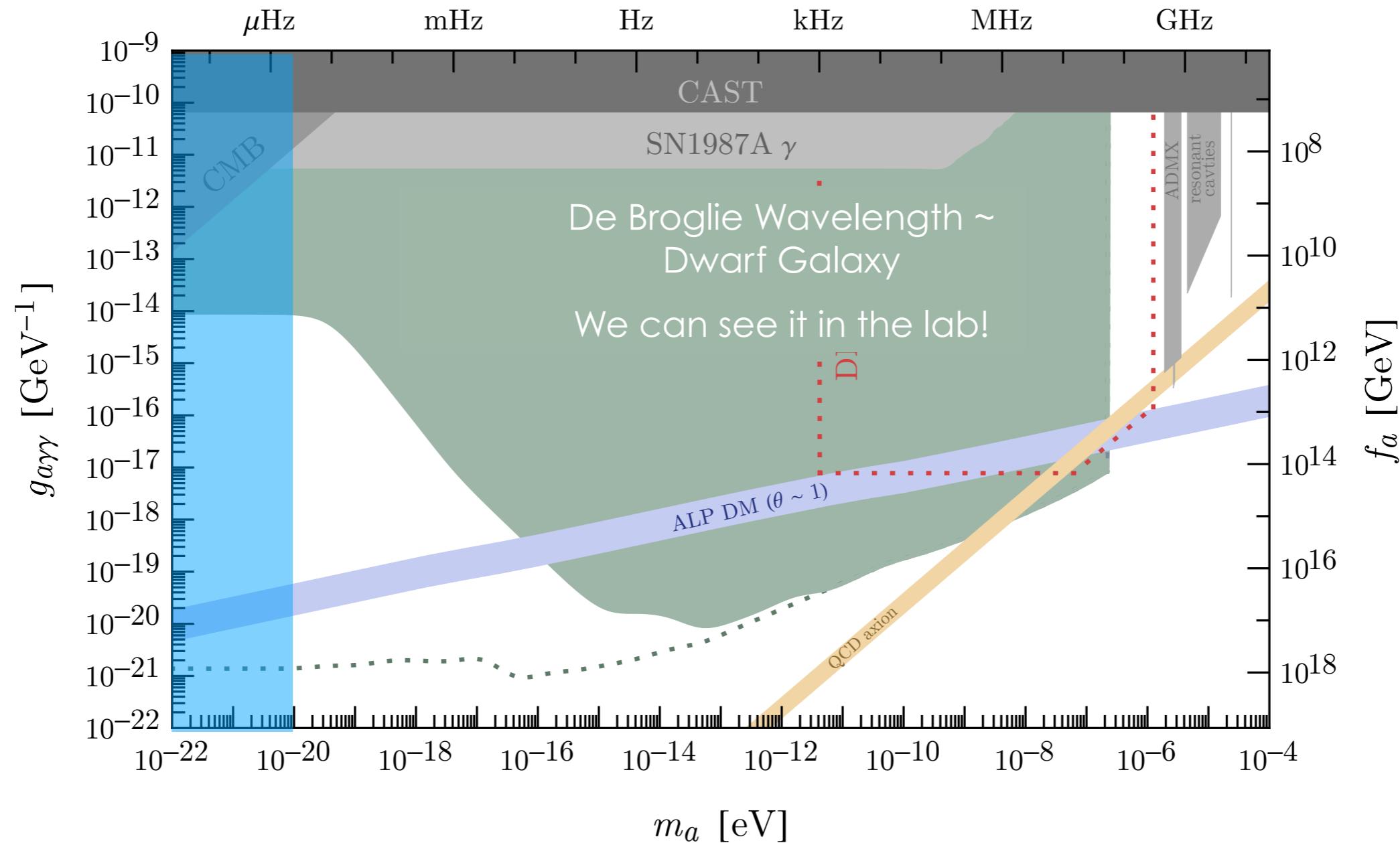


A.Berlin, **RTD**, S. Ellis, C. Nantista, J. Nielson, P. Schuster, S. Tantawi, N. Toro, K. Zhou '19

A.Berlin, **RTD**, S. Ellis, K. Zhou '20

# BACKUP

$$\text{frequency} = m_a/2\pi$$



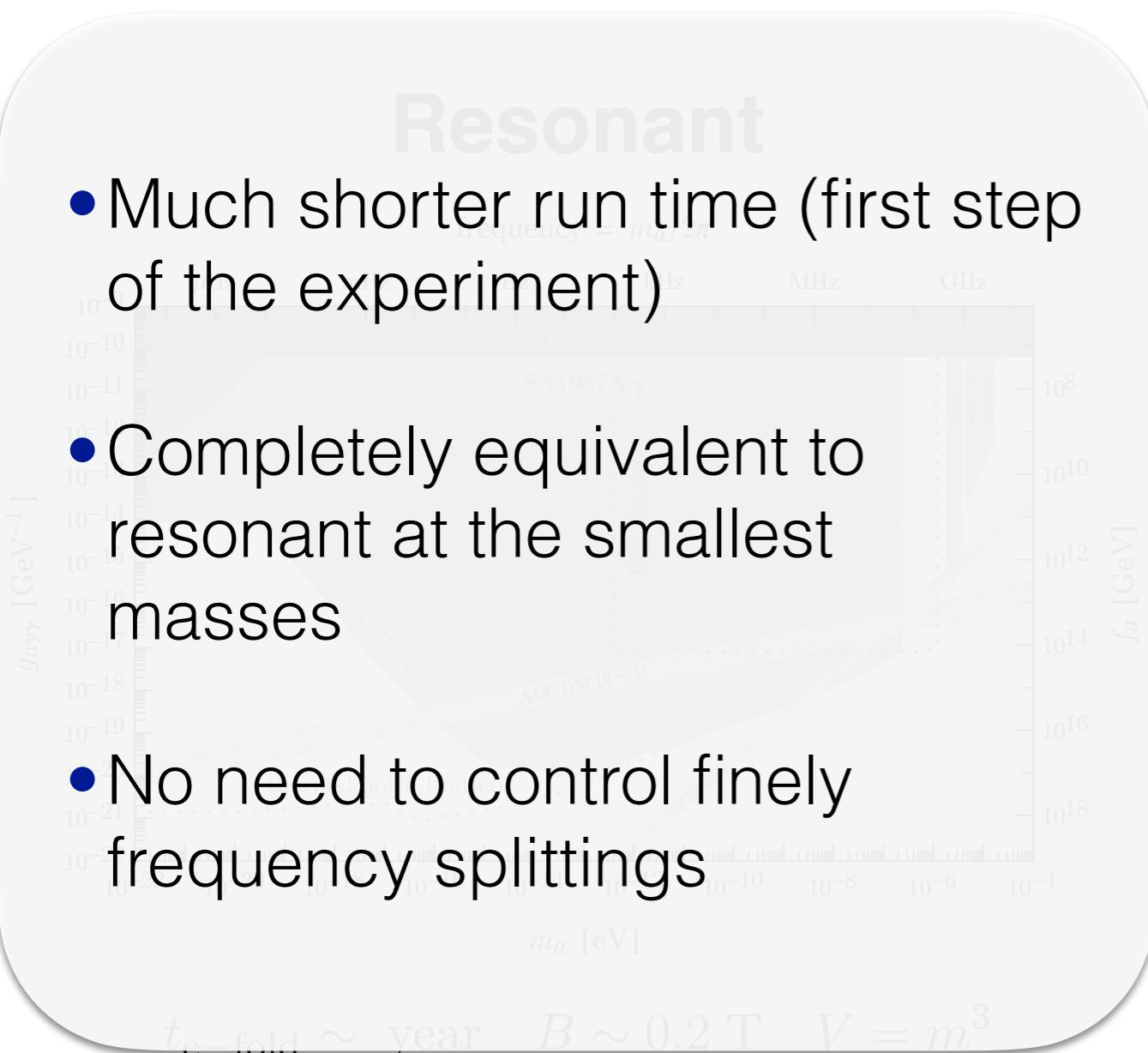
A.Berlin, **RTD**, S. Ellis, C. Nantista, J. Nielson, P. Schuster, S. Tantawi, N. Toro, K. Zhou '19

A.Berlin, **RTD**, S. Ellis, K. Zhou '20

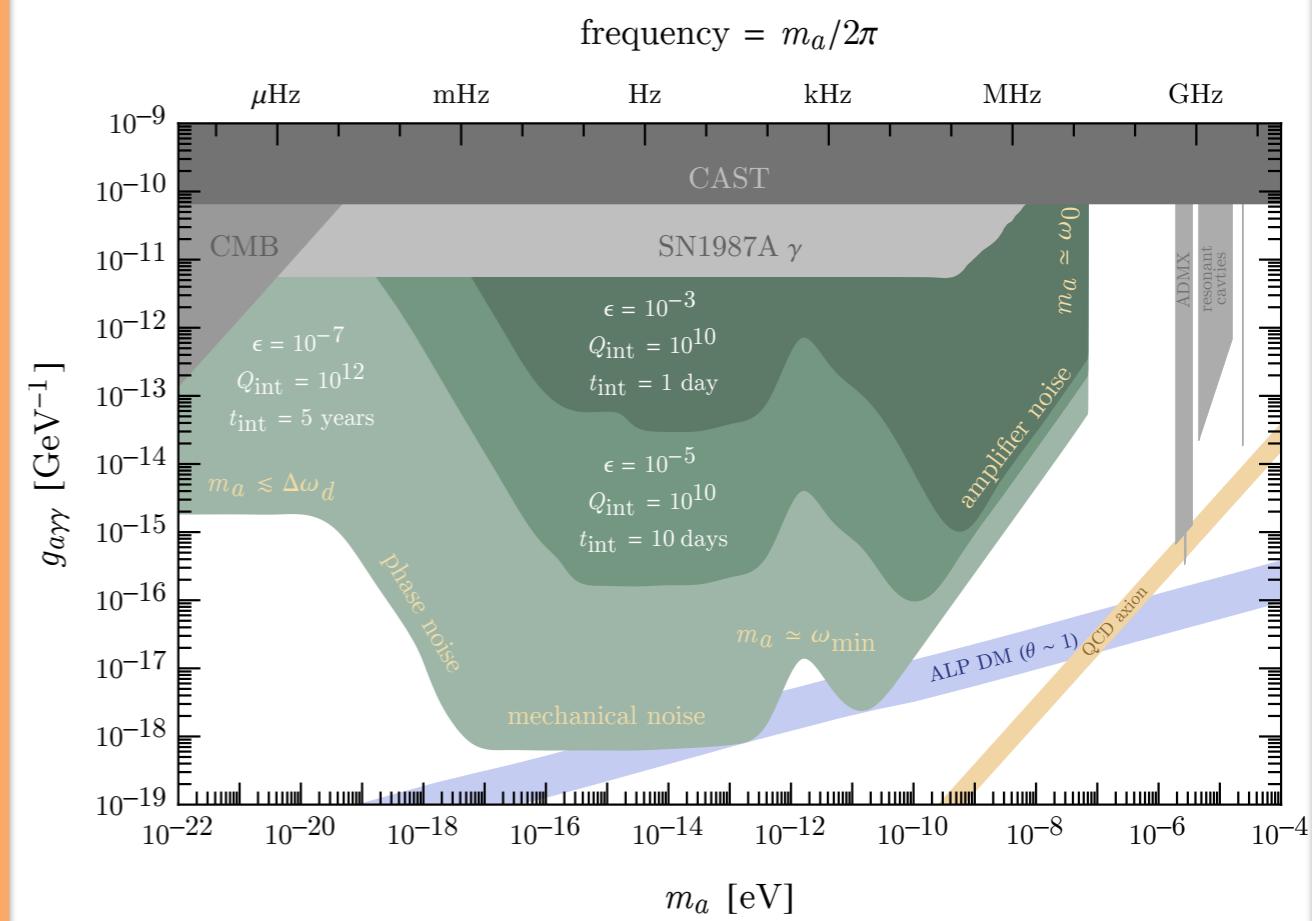
# SNEAK PREVIEW

## Resonant

- Much shorter run time (first step of the experiment)
- Completely equivalent to resonant at the smallest masses
- No need to control finely frequency splittings



## Broadband



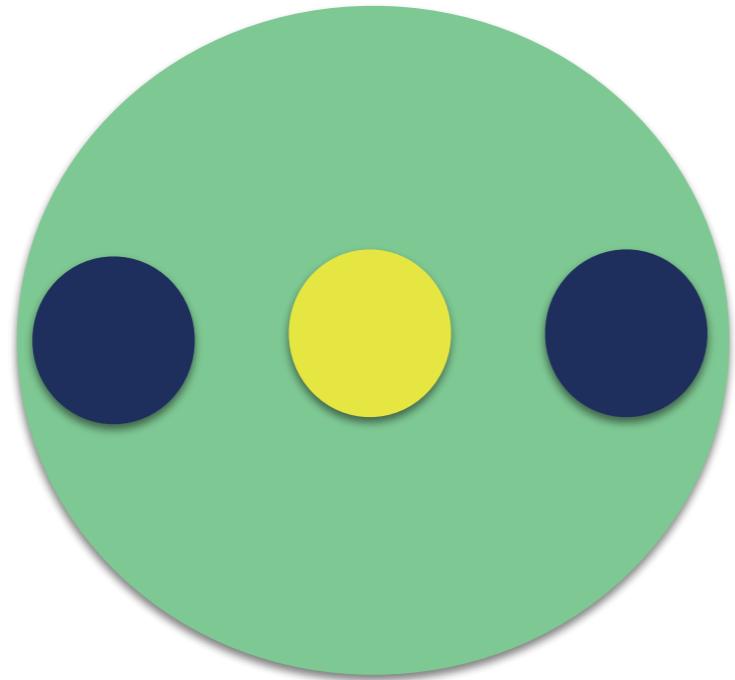
# AXION BASICS



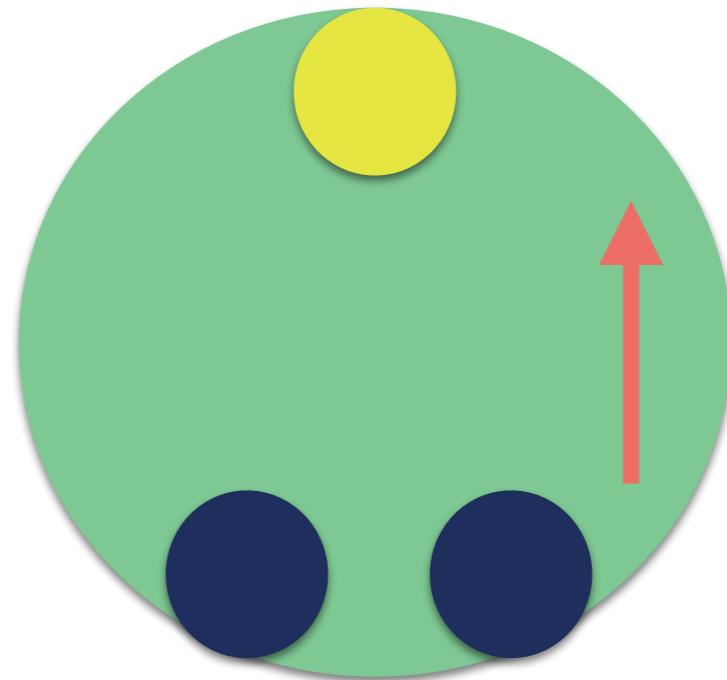
# CP IN QCD

$$\theta G\tilde{G}$$

Neutron  $\theta = 0$



Neutron  $\theta \neq 0$



Electric  
Dipole

$|\theta| \lesssim 10^{-10}$  **Experimentally**

# THE AXION FROM ABOVE

Introduce a new **global symmetry at  $f_a$**

$$\theta G\tilde{G} \longrightarrow \left(\theta + \frac{a}{f_a}\right) G\tilde{G}$$

**At the minimum**

$$\langle a \rangle = -\theta f_a$$

# AXION BASICS 3

QCD Phase Transition

$$\frac{a}{f_a} G \tilde{G}$$



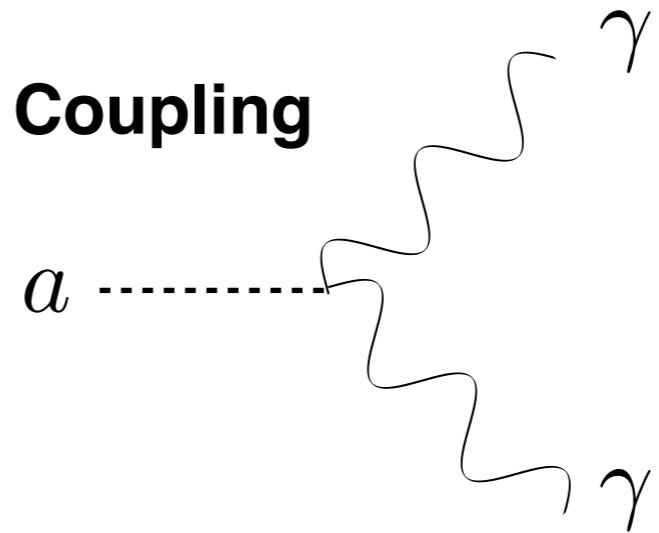
$$\frac{a}{f_a} \frac{\pi}{f_\pi} + \dots$$

**Mass**

$$m_a \sim \frac{m_\pi^2}{f_a} \sim 10^{-2} \text{ eV} \frac{10^9 \text{ GeV}}{f_a}$$

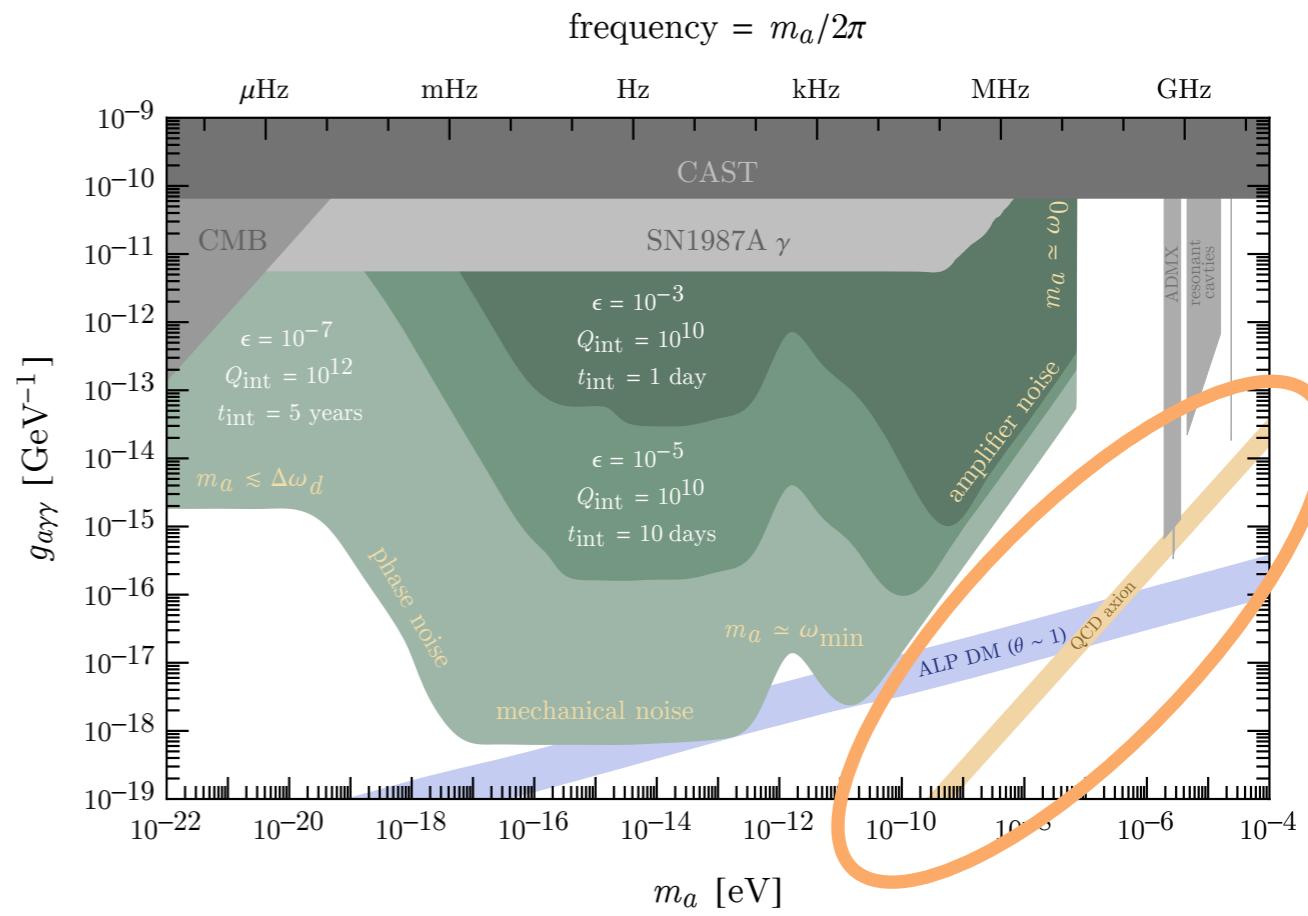
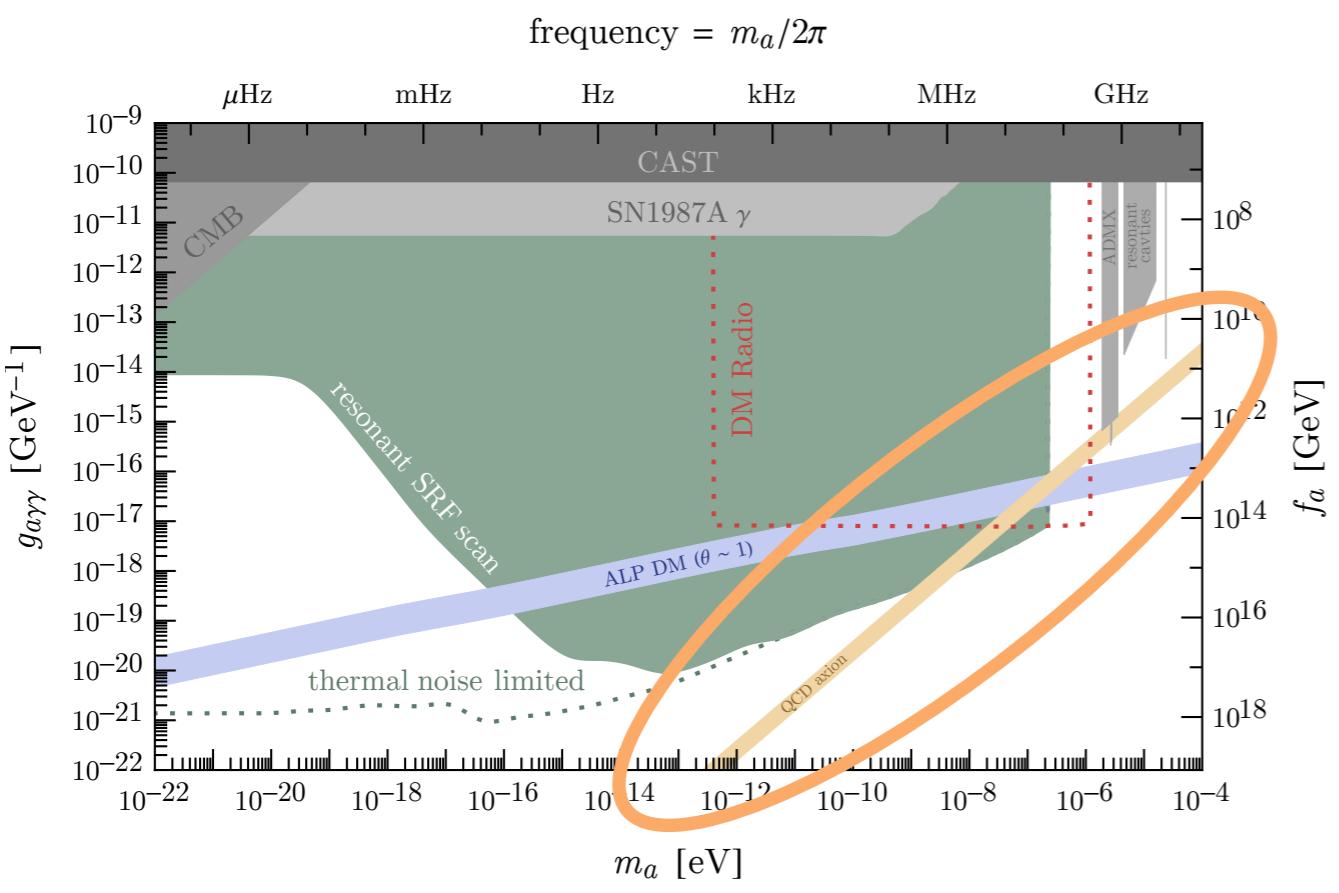
**Relevant Coupling**

$$\frac{a}{f_a} \mathbf{E} \cdot \mathbf{B}$$



# SNEAK PREVIEW: QCD AXION

Relevant to  
QCD Theta Angle



MACS J0416.1-2403

MACS J0152.5-2852

MACS J0

Abell 370

Abell 2744

AXION DARK MATTER

# MISALIGNMENT PRODUCTION

PQ breaking before inflation  
(for simplicity)



$$T \gg \Lambda_{\text{QCD}}$$

$$V(a) = 0$$

# MISALIGNMENT PRODUCTION

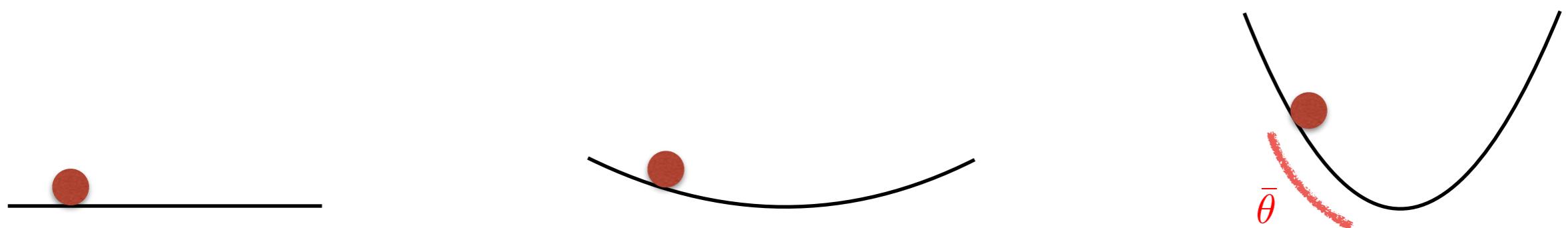
PQ breaking before inflation  
(for simplicity)



$$m_a(T) \approx 0.1 m_a \left( \frac{\Lambda_{\text{QCD}}}{T} \right)^4$$

# MISALIGNMENT PRODUCTION

PQ breaking before inflation  
(for simplicity)



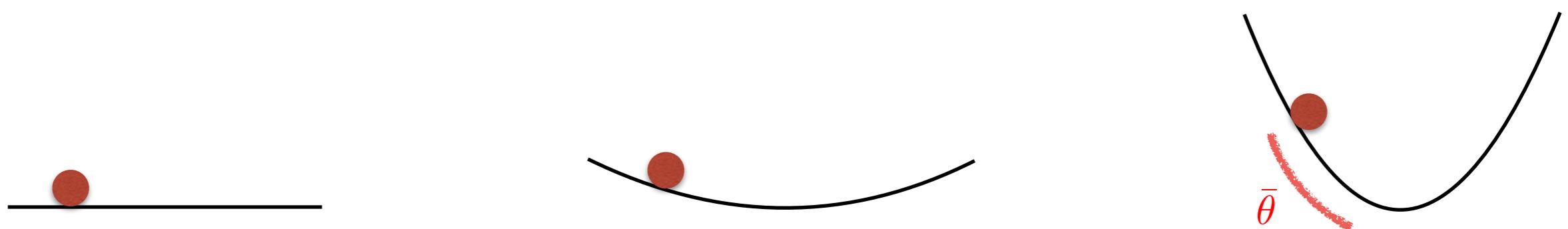
$$\rho_a = \frac{m_a^2 f_a^2 \bar{\theta}^2}{2}$$

# MISALIGNMENT PRODUCTION

Huge occupation number in a De Broglie volume (+ coherent state)

=

classical field

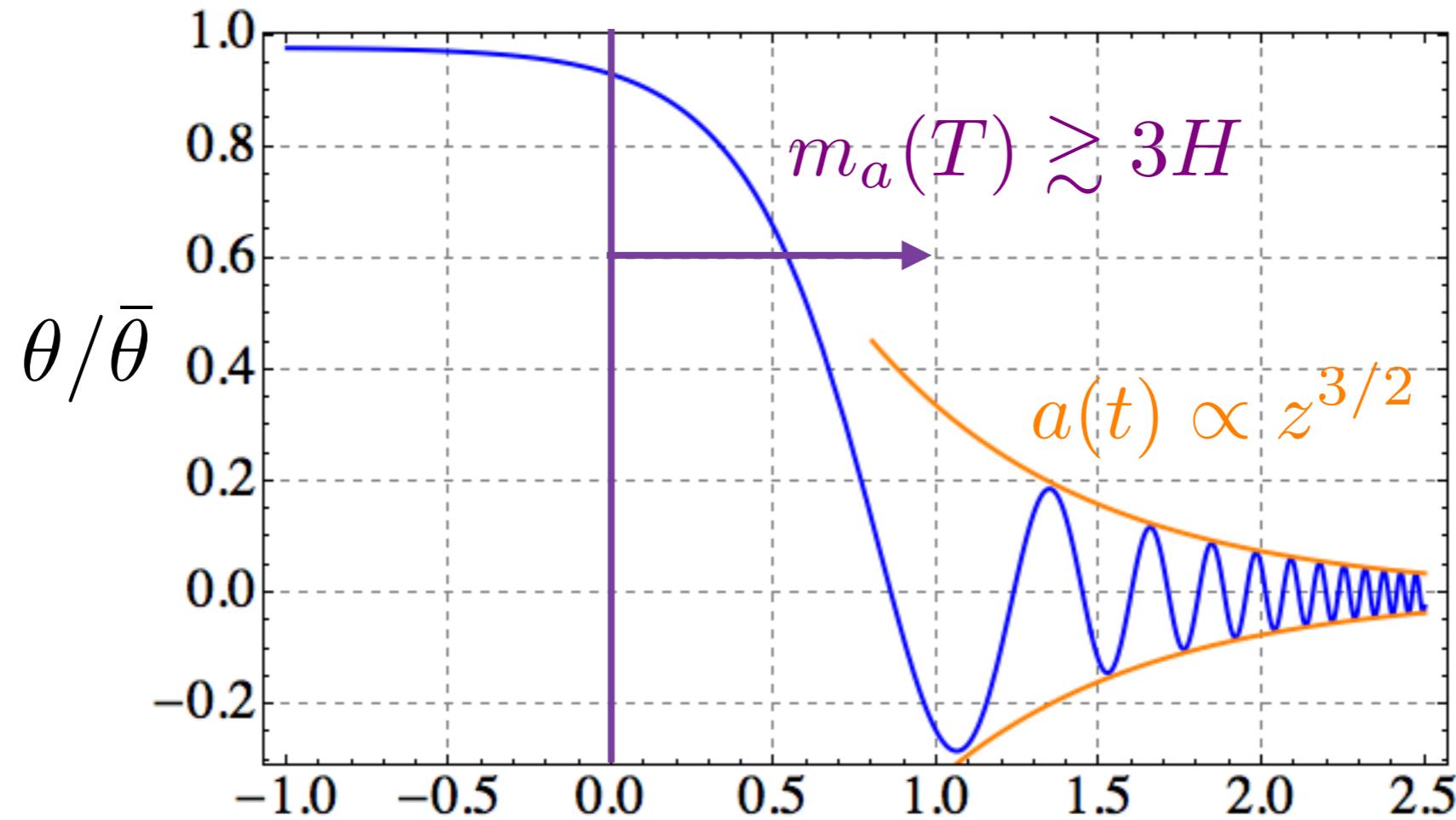


$$\theta \equiv a/f_a$$

$$\ddot{\theta} + 3H\dot{\theta} + m_a^2(T)\theta = 0$$

# AXION COSMOLOGY

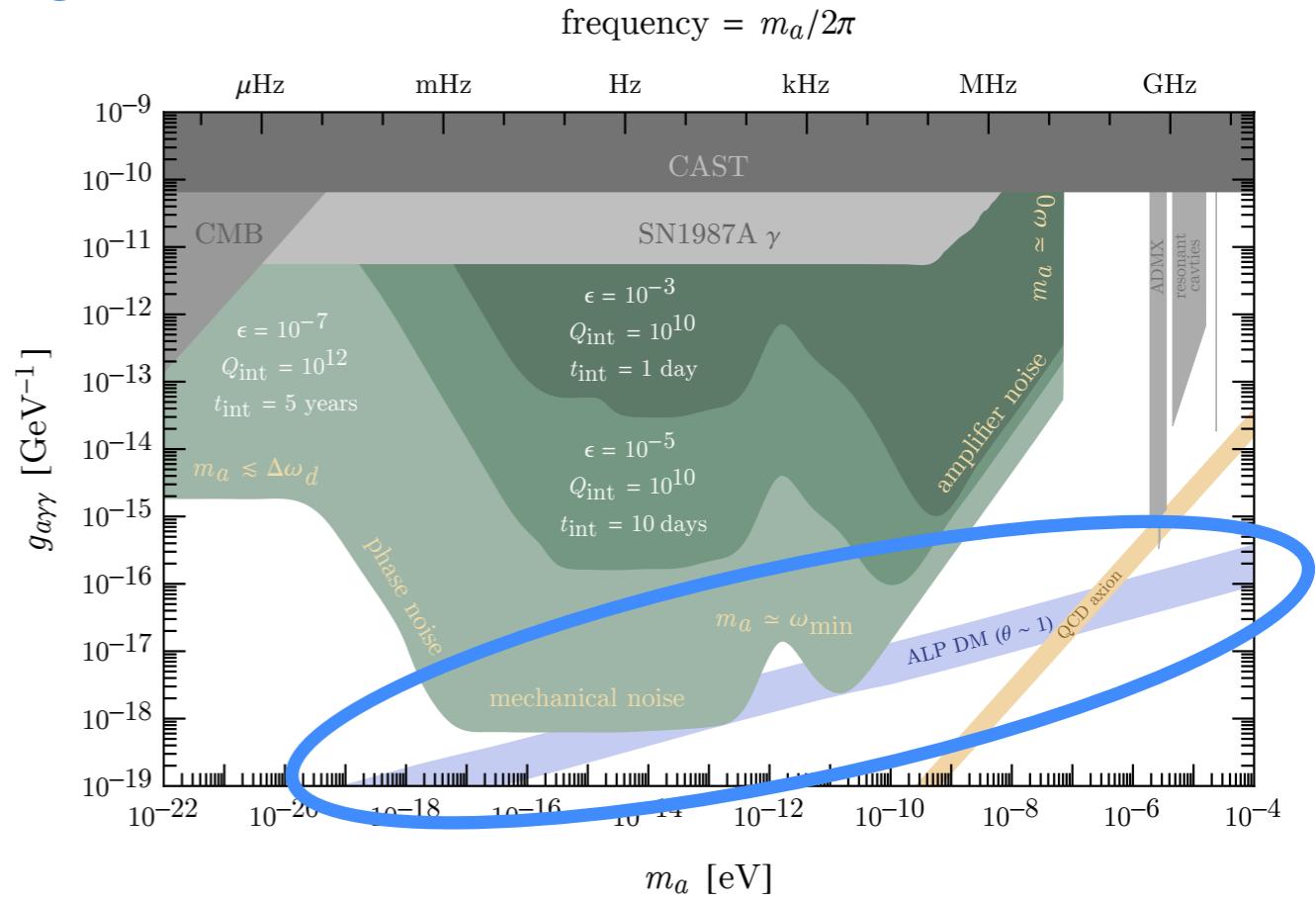
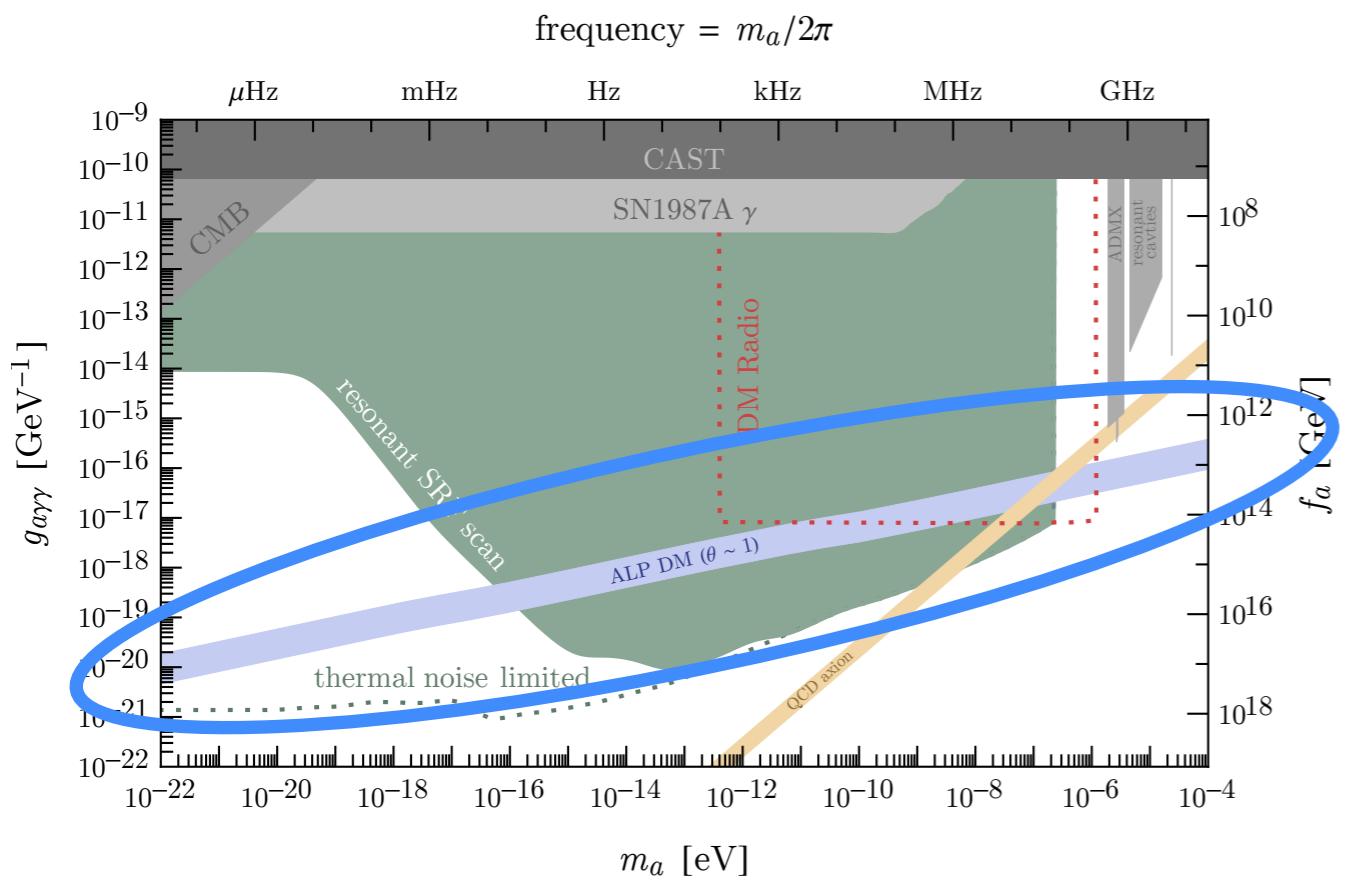
$$\ddot{\theta} + 3H\dot{\theta} + m_a^2(T)\theta = 0$$



$$\log(\sqrt{m_\phi M_{\text{Pl}}}/T)$$

# SNEAK PREVIEW: SIMPLEST ALP

**“Simplest ALP”  
T-independent mass  
Natural misalignment**



N.B. Many ways to populate the rest of the parameter space

Agrawal, Marques-Tavares, Xue '17

Graham, Scherlis '18

Marques-Tavares, Mao '18

# AXION DARK MATTER DETECTION



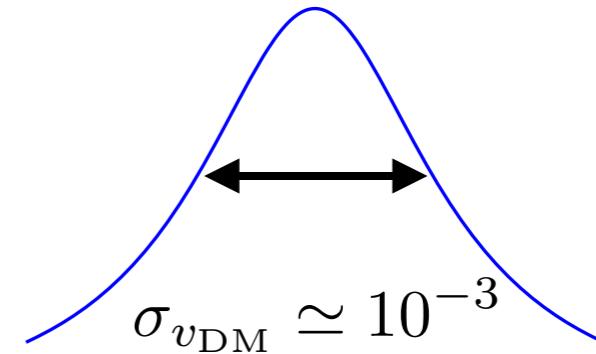
# AXION DM IN THE LABORATORY

**Produced Colder** than the SM (even if not via misalignment)

$$E_a \approx m_a$$

It acquires a **small velocity dispersion** from virialization **in the Milky Way**

$$E_a \simeq m_a \left( 1 + \frac{v_{\text{DM}}^2}{2} \right)$$

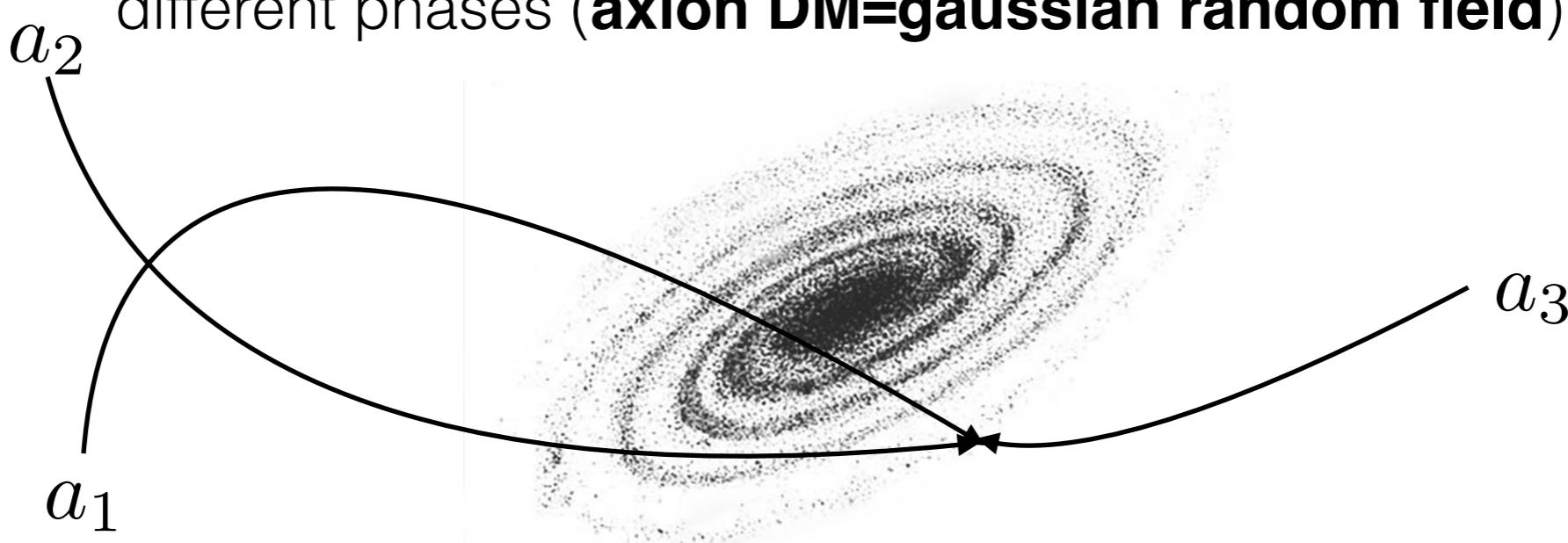


**Lots of axions** in each frequency bin that we can resolve (even more in a De Broglie volume):

$$\Delta N_a \simeq \frac{\rho_{\text{DM}} V}{m_a^2 t_{\text{int}} v_{\text{DM}}^2} \simeq 10^{24} \left( \frac{10^{-14} \text{ eV}}{m_a} \right)^2 \left( \frac{\text{year}}{t_{\text{int}}} \right) \left( \frac{V}{\text{m}^3} \right)$$

# AXION DM IN THE LABORATORY

In each experimental bin we are **summing over a multitude of plane waves with different phases (axion DM=gaussian random field)**:



$$a(t) = a_0 \left[ \cos \left( m_a \left( 1 + \frac{v_1^2}{2} \right) t + \phi_1 \right) + \cos \left( m_a \left( 1 + \frac{v_2^2}{2} \right) t + \phi_2 \right) + \dots \right]$$

$$\simeq a_0 \cos(m_a t + \phi) [\cos(\delta\omega_a t + \phi') + \dots]$$

$$\delta\omega_a \simeq \frac{1}{m_a \langle v_{\text{DM}}^2 \rangle} \simeq \frac{10^6}{m_a}$$

Effectively: very **slow modulation** of an approximately **monochromatic field**

# AXION DM IN THE LABORATORY

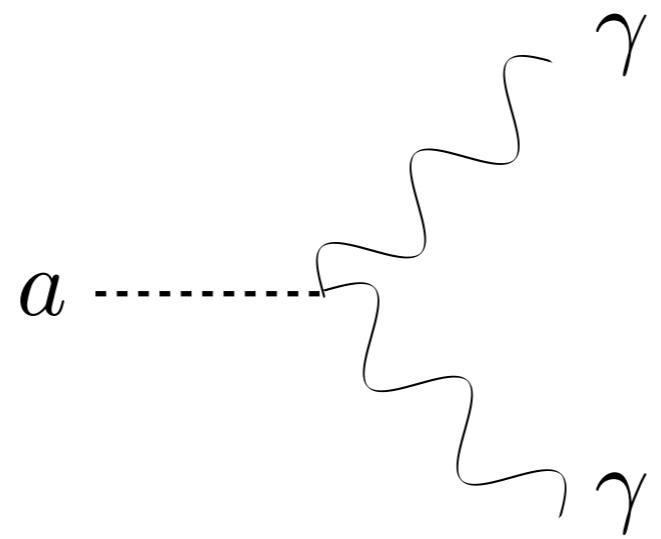
$$a(t) \simeq \frac{\sqrt{2\rho_{\text{DM}}}}{m_a} \cos(\omega_a t + \phi)$$

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**Coherence:**  $\tau_a \simeq \text{ms} \frac{10^{-6} \text{ eV}}{m_a}$

**Max Exp. Size:**  $\lambda_a \simeq 200 \text{ m} \frac{10^{-6} \text{ eV}}{m_a}$

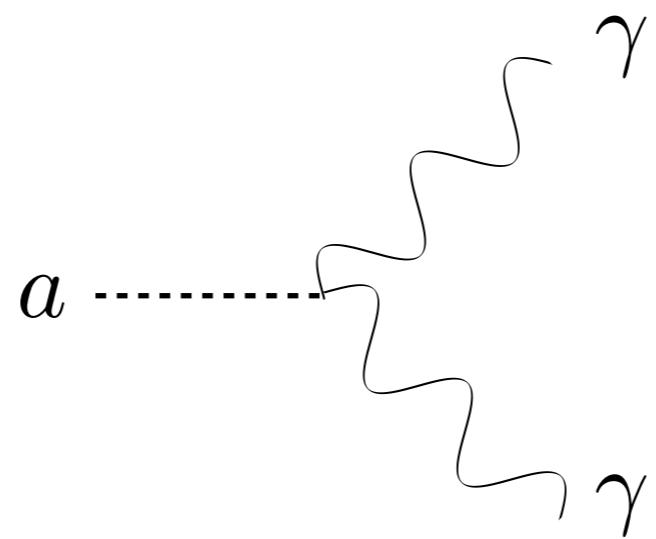
# AXION DETECTION



$$\nabla \times \mathbf{B} \simeq \partial_t \mathbf{E} + \mathbf{J} + \underline{g_{a\gamma\gamma} \mathbf{B} \partial_t a}$$

$$J_{\text{eff}}(t) \sim g_{a\gamma\gamma} B_0(t) \sqrt{\rho_{\text{DM}}} \cos m_a t$$

# AXION DETECTION



$$J_{\text{eff}} \sim 10^{-15} \text{ A/cm}^2 \left( \frac{g_{a\gamma\gamma}}{10^{-12} \text{ GeV}^{-1}} \right) \left( \frac{B_0}{4 \text{ T}} \right)$$

—  
10<sup>4</sup> A/cm<sup>2</sup>    10<sup>7</sup> A/cm<sup>2</sup>    10<sup>8</sup> A/cm<sup>2</sup>  
Flashlamp              Copper              Graphene

# AXION DETECTION

$$\nabla \times \mathbf{B} \simeq \partial_t \mathbf{E} + \mathbf{J} + g_{a\gamma\gamma} \mathbf{B} \partial_t a$$

$$\nabla \times \mathbf{E} = -\partial_t \mathbf{B}$$

**Cavity:**

$$\sum_n \left( \partial_t^2 + \frac{\omega_n}{Q_n} \partial_t + \omega_n^2 \right) \mathbf{E}_n = g_{a\gamma\gamma} \partial_t (\mathbf{B} \partial_t a)$$

# AXION DETECTION

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$$\omega_1 \simeq m_a \quad \partial_t (\mathbf{B}) \simeq 0$$

# AXION DETECTION

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$$\left( \partial_t^2 + \frac{m_a}{Q_1} \partial_t + m_a^2 \right) \mathbf{E}_1 = g_{a\gamma\gamma} \mathbf{B} \sqrt{\rho_{\text{DM}}} m_a \cos m_a t$$

# AXION DETECTION

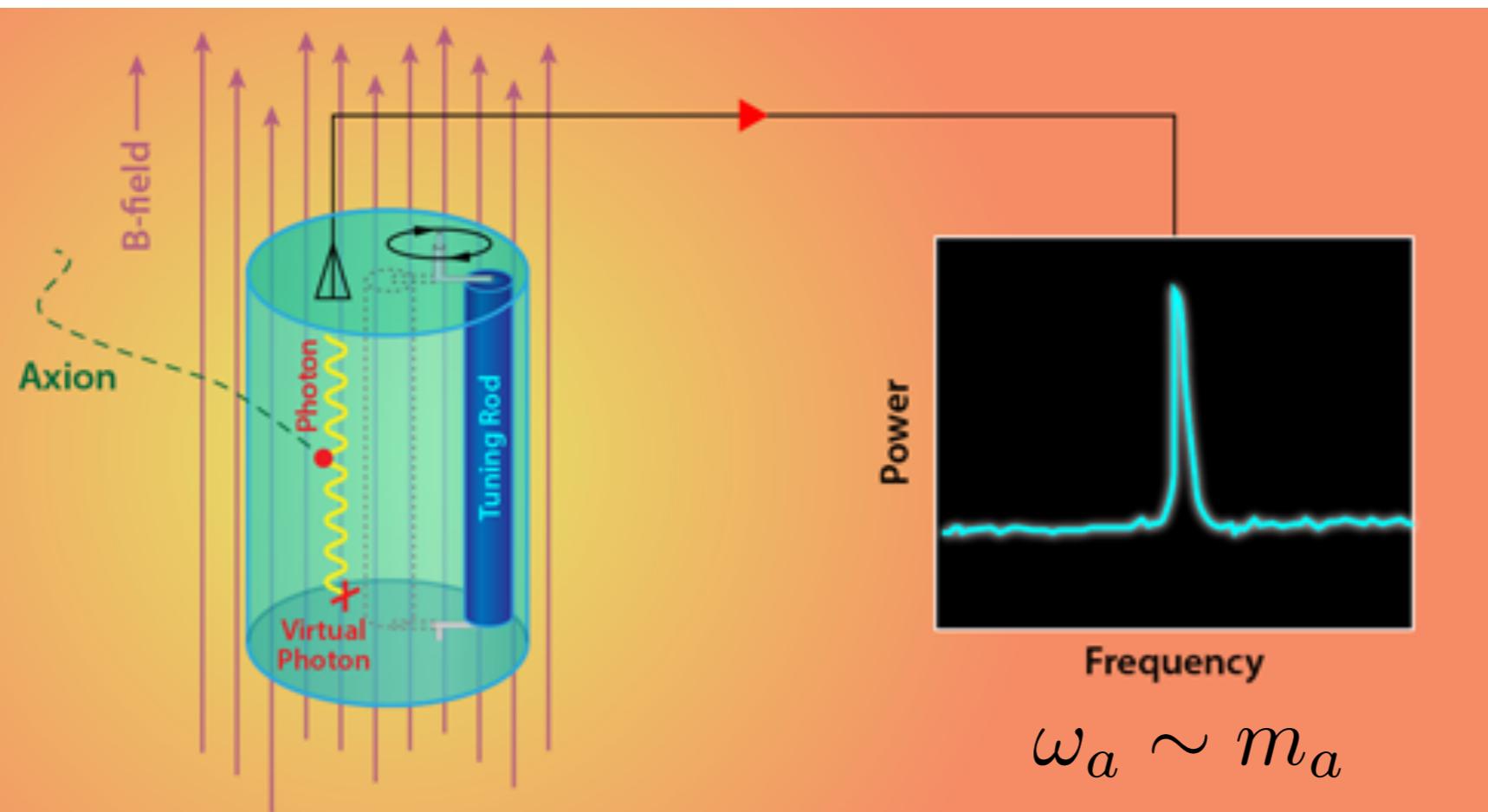
$$\left( \partial_t^2 + \frac{m_a}{Q_1} \partial_t + m_a^2 \right) \mathbf{E}_1 \sim m_a \cos m_a t$$

Resonant for many cycles

$$Q_a \sim 10^6$$

Ideal for

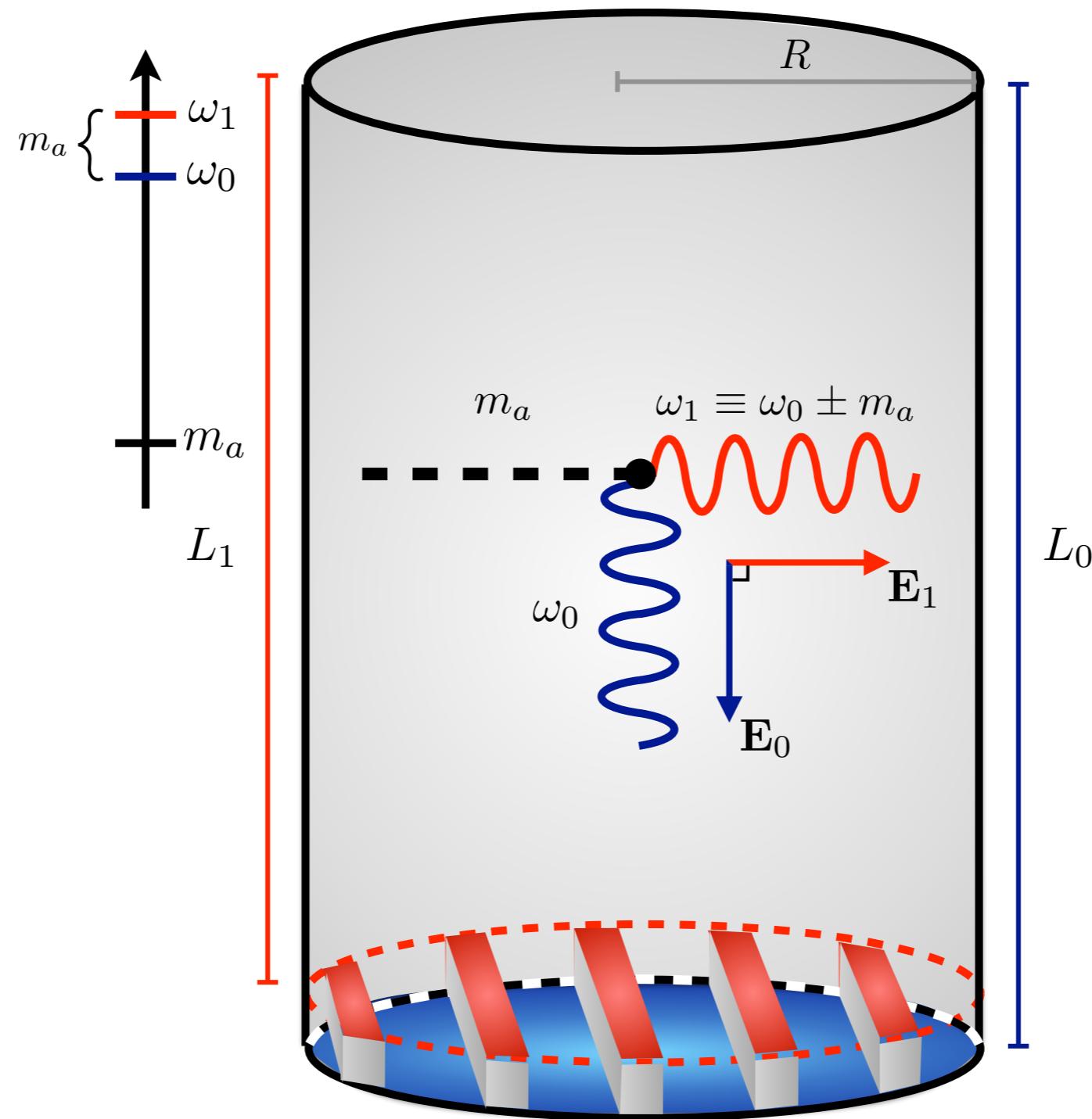
$$m_a \sim \text{GHz} \sim 10^{-6} \text{ eV}$$



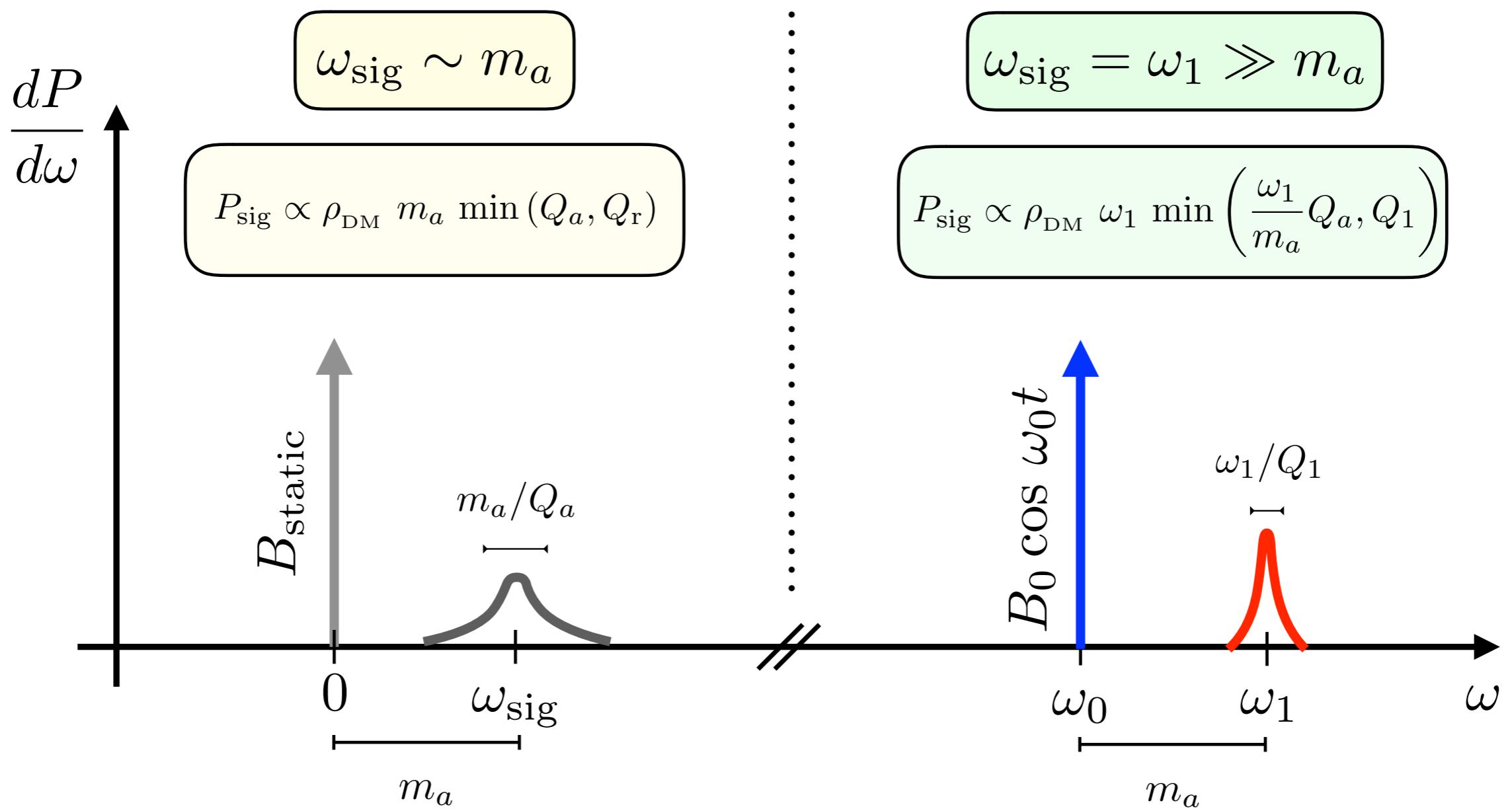
## Problems:

1. **Cavity size**  $\sim (\text{axion mass})^{-1}$
2. **Signal power** decreases with axion mass

# LOW MASS AXION DETECTION



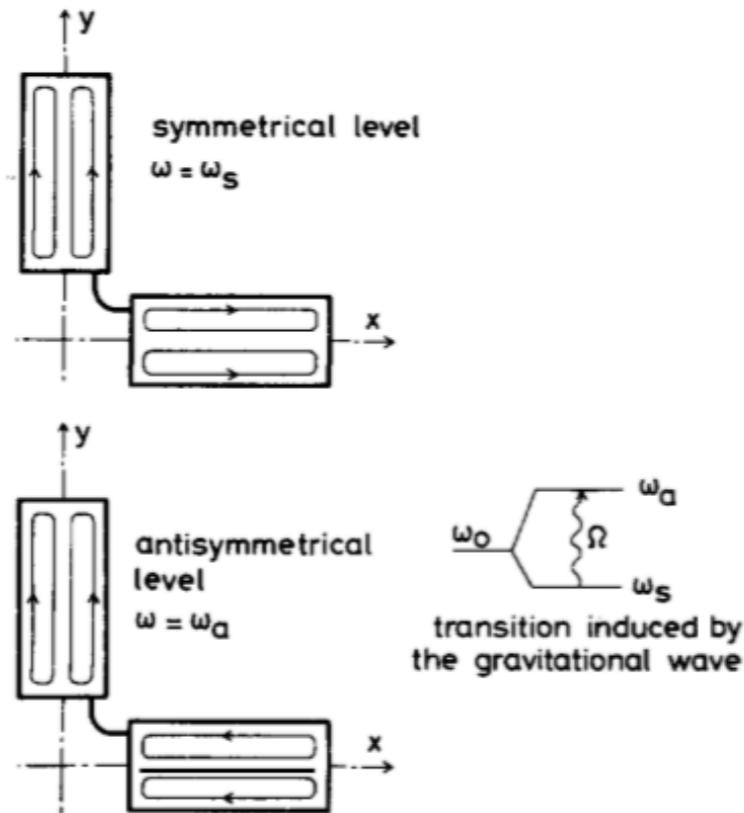
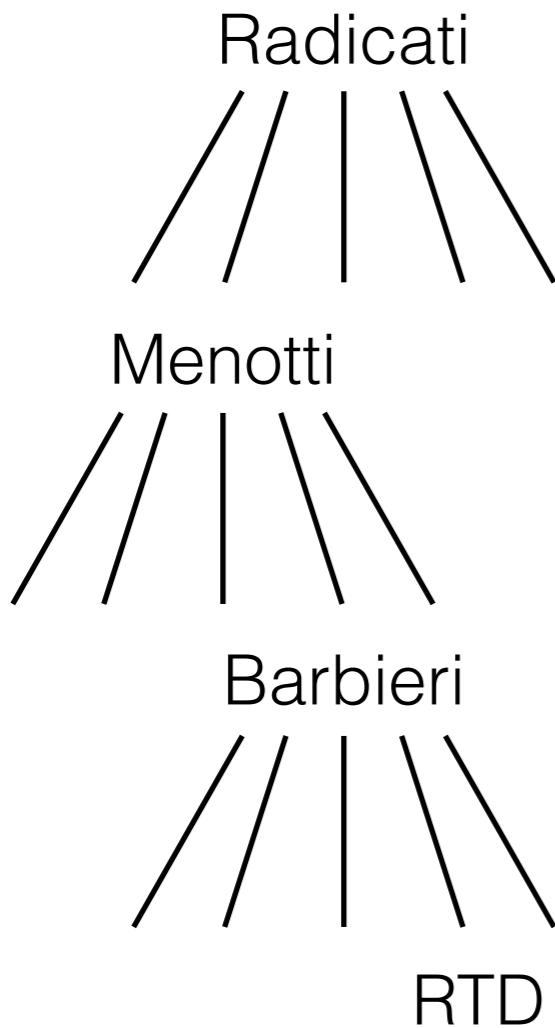
# LOW MASS AXION DETECTION



# OUR ANCESTORS HUNTING FOR GWs

With a different geometry,  
**viable also for gravitational waves!**

Radicati, Pegoraro, Picasso '78



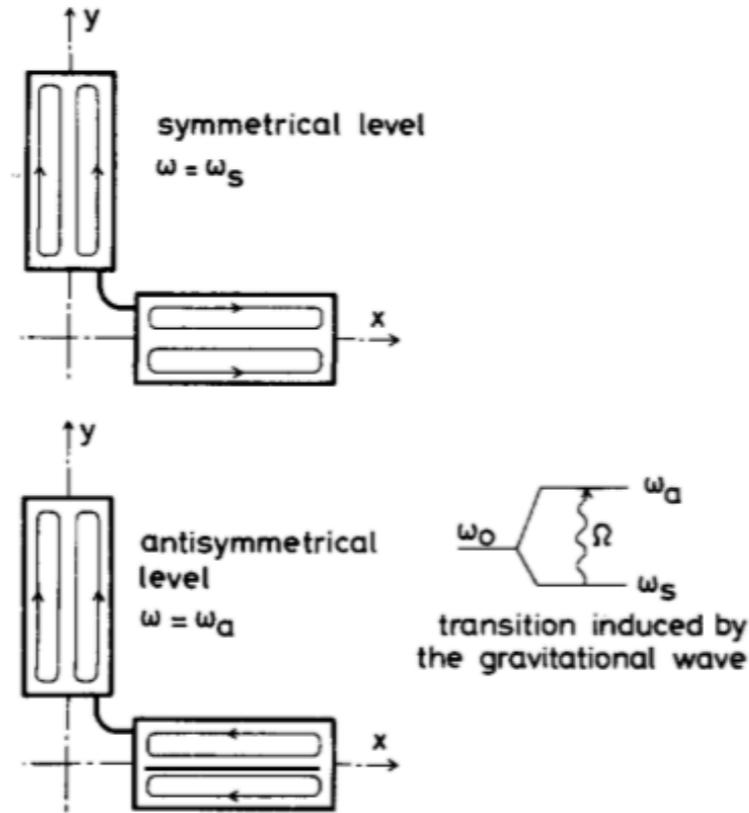
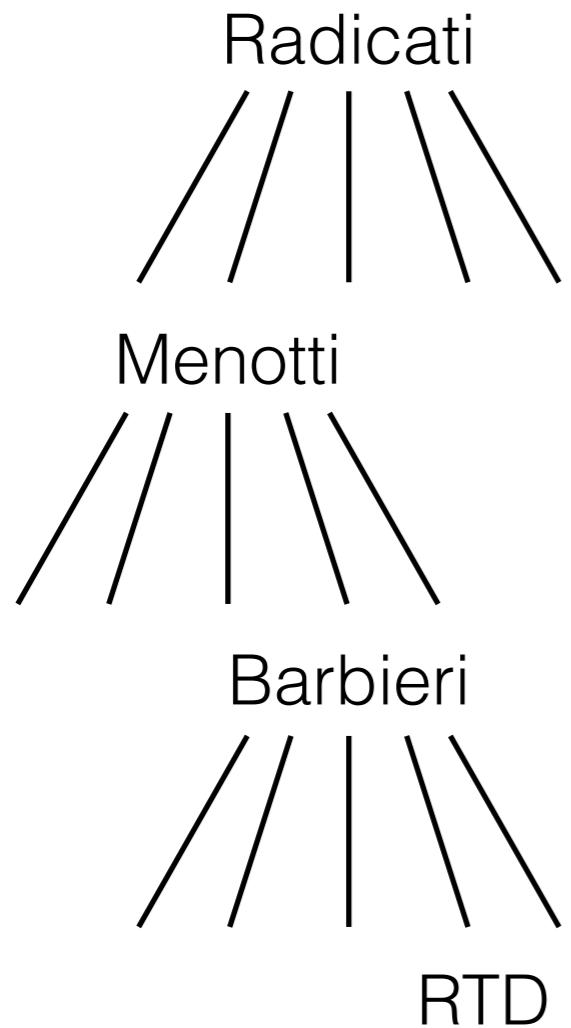
**MAGO '05**



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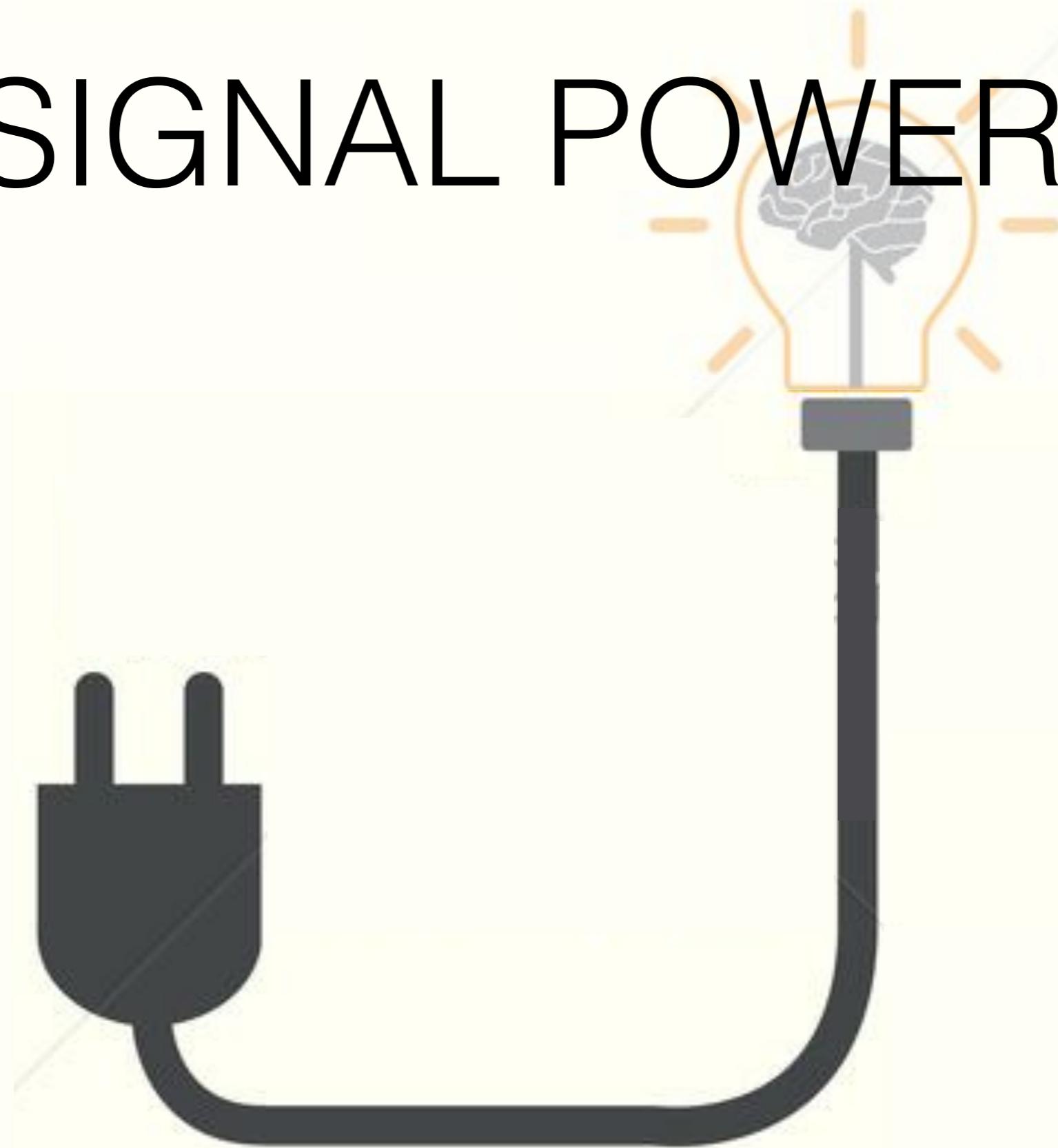
Radicati, Pegoraro, Picasso '78



MAGO '05

Other Interesting Proposals  
for SRF cavities as NP detectors:  
Berlin, Hook '20  
Bogorad, Hook, Kahn, Soreq '19

# SIGNAL POWER



# SIGNAL POWER AT LOW MASSES

$$\sum_n \left( \partial_t^2 + \frac{\omega_n}{Q_n} \partial_t + \omega_n^2 \right) \mathbf{E}_n = g_{a\gamma\gamma} \partial_t (\mathbf{B} \partial_t a)$$

$$\omega_1 \simeq \omega_0 + m_a \quad \partial_t (\mathbf{B}) \simeq i\omega_0 \mathbf{B}$$

**Static:**

$$\mathbf{E}_1 \sim \frac{m_a g_{a\gamma\gamma} \sqrt{\rho_{\text{DM}}} \mathbf{B}}{m_a^2 - \omega_1^2 + i \frac{m_a \omega}{Q_1}}$$

**Oscillating:**

$$\mathbf{E}_1 \sim \frac{\omega_0 g_{a\gamma\gamma} \sqrt{\rho_{\text{DM}}} \mathbf{B}}{(\omega_0 + m_a)^2 - \omega_1^2 + i \frac{(\omega_0 + m_a)\omega}{Q_1}}$$

# SIGNAL POWER AT LOW MASSES

Power = Energy/Time

Time

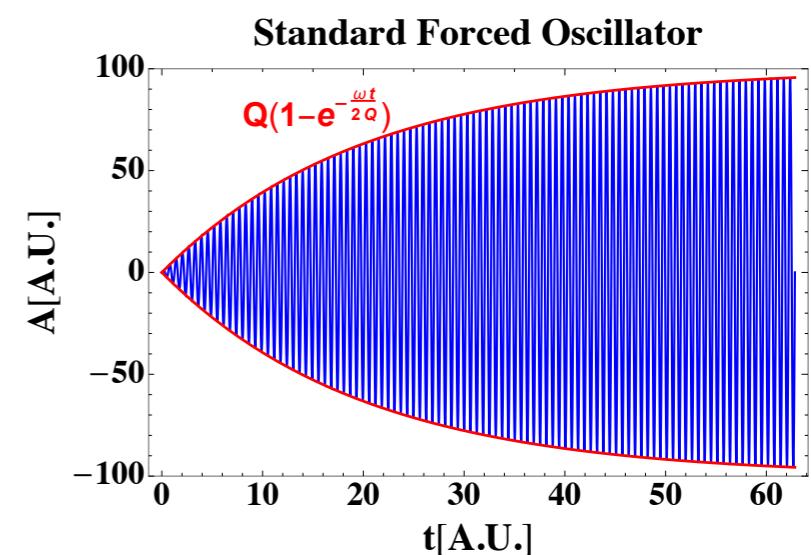
$$\min[\tau_a, \tau_r] = \min \left[ \frac{Q_a}{m_a}, \frac{Q_1}{\omega_1} \right]$$

$$t = \tau_a = \frac{Q_a}{m_a}$$

Axion stops being monochromatic

$$t = \tau_r = \frac{Q_1}{\omega_1}$$

Steady State



# SIGNAL POWER AT LOW MASSES

**Power = Energy/Time**

Energy

$$\omega_1^2 B_a^2 V \min \left[ \frac{Q_a^2}{m_a^2}, \frac{Q_1^2}{\omega_1^2} \right]$$

Time

$$\min[\tau_a, \tau_r] = \min \left[ \frac{Q_a}{m_a}, \frac{Q_1}{\omega_1} \right]$$

**Static:**  $\omega_1 \simeq m_a$

$$P \simeq m_a B_a^2 V \min[Q_a, Q_1]$$

**Naively no reason to build resonators with  $Q > 10^6$**

# SIGNAL POWER AT LOW MASSES

**Power = Energy/Time**

Energy

$$\omega_1^2 B_a^2 V \min \left[ \frac{Q_a^2}{m_a^2}, \frac{Q^2}{\omega_1^2} \right]$$

Time

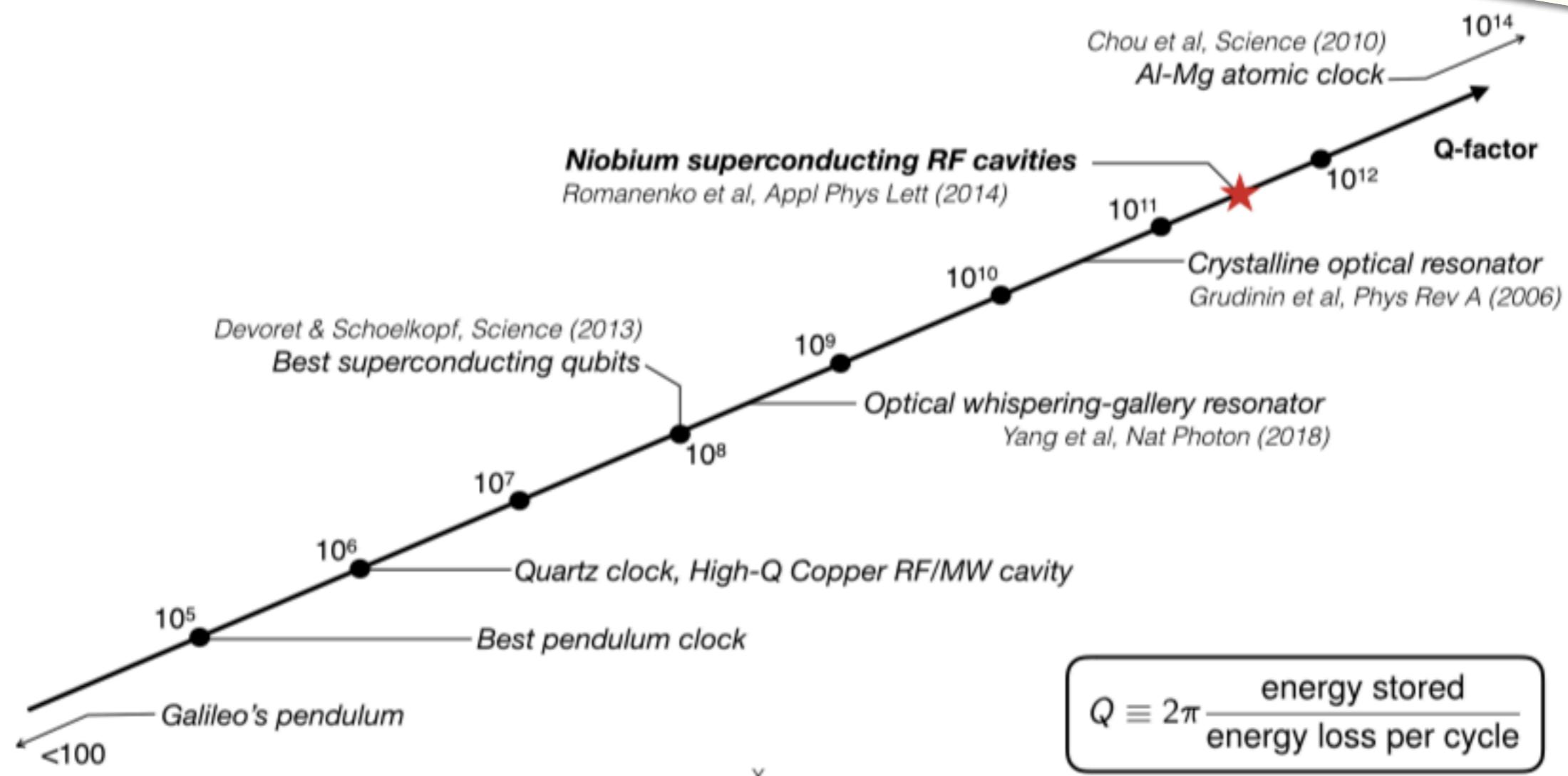
$$\min[\tau_a, \tau_r] = \min \left[ \frac{Q_a}{m_a}, \frac{Q_1}{\omega_1} \right]$$

**Oscillating:**  $\omega_1 > m_a$

$$P \simeq \omega_1 B_a^2 V \min[Q_a(\omega_1/m_a), Q_1]$$

**Great advantage of high-Q resonators at low  $m_a$**

# SUPERCONDUCTING RADIOFREQUENCY CAVITIES

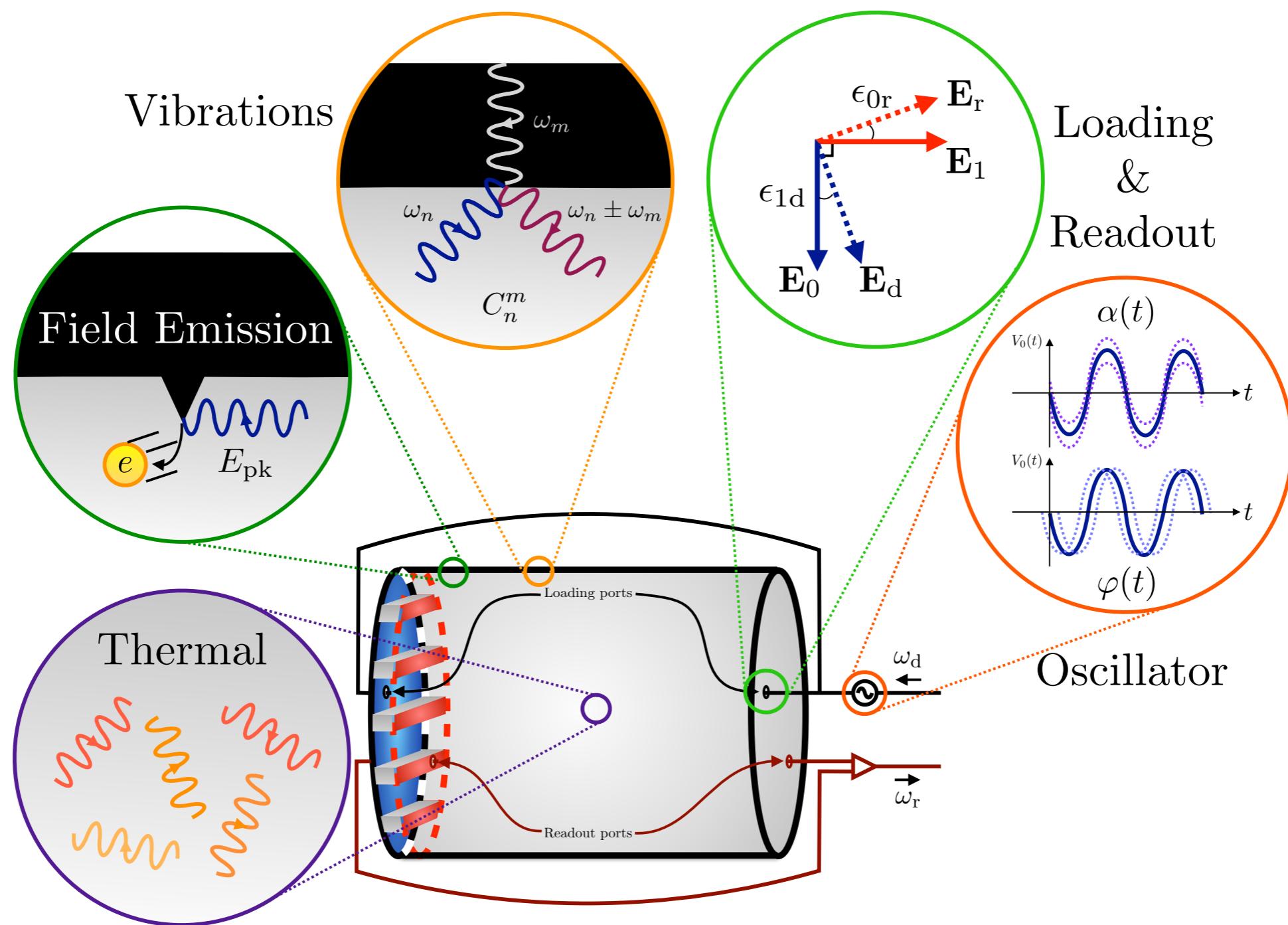


From Anna Grassellino, Fermilab



NOISE AND SENSITIVITY

# NOISE



# OSCILLATOR NOISE

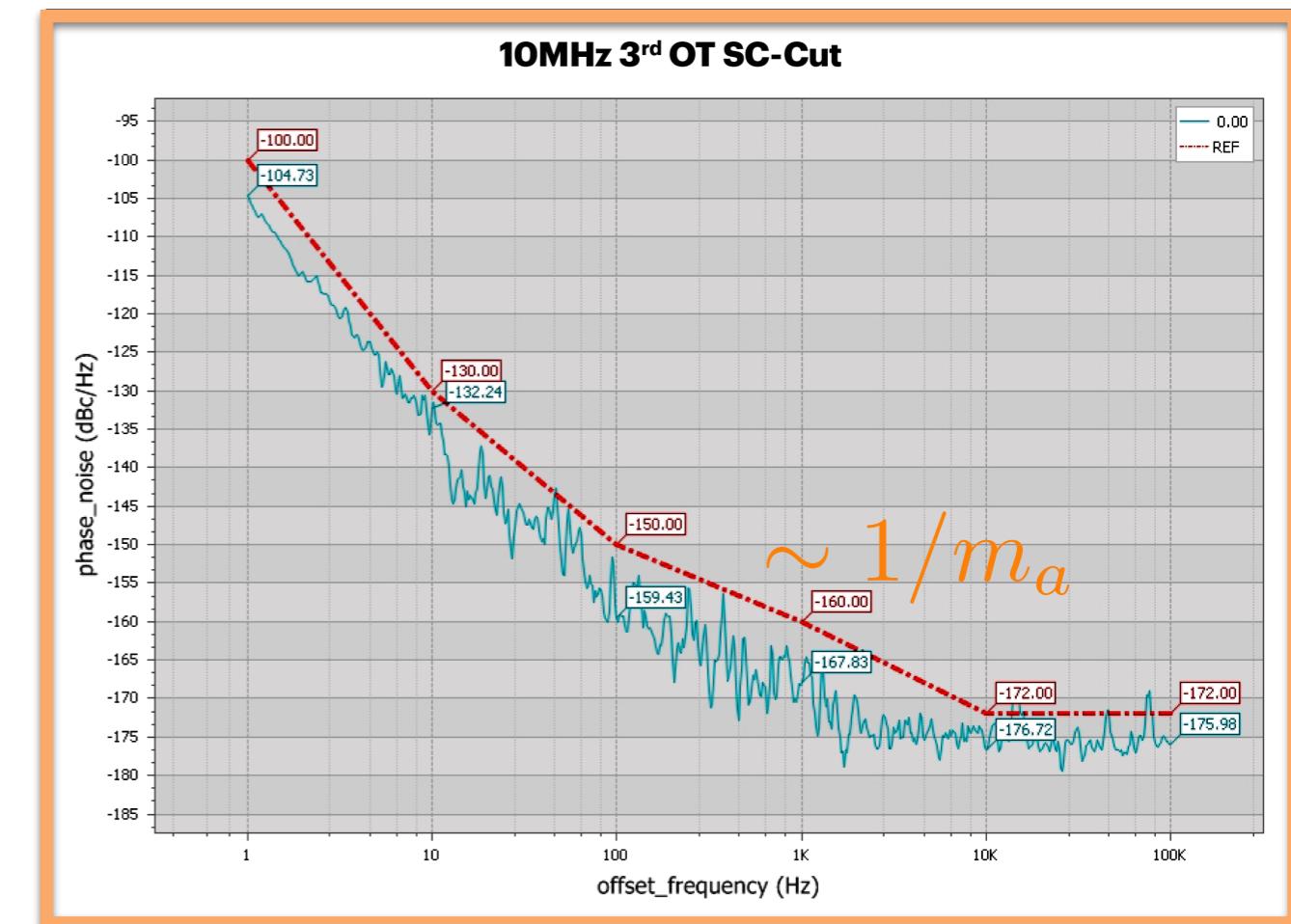
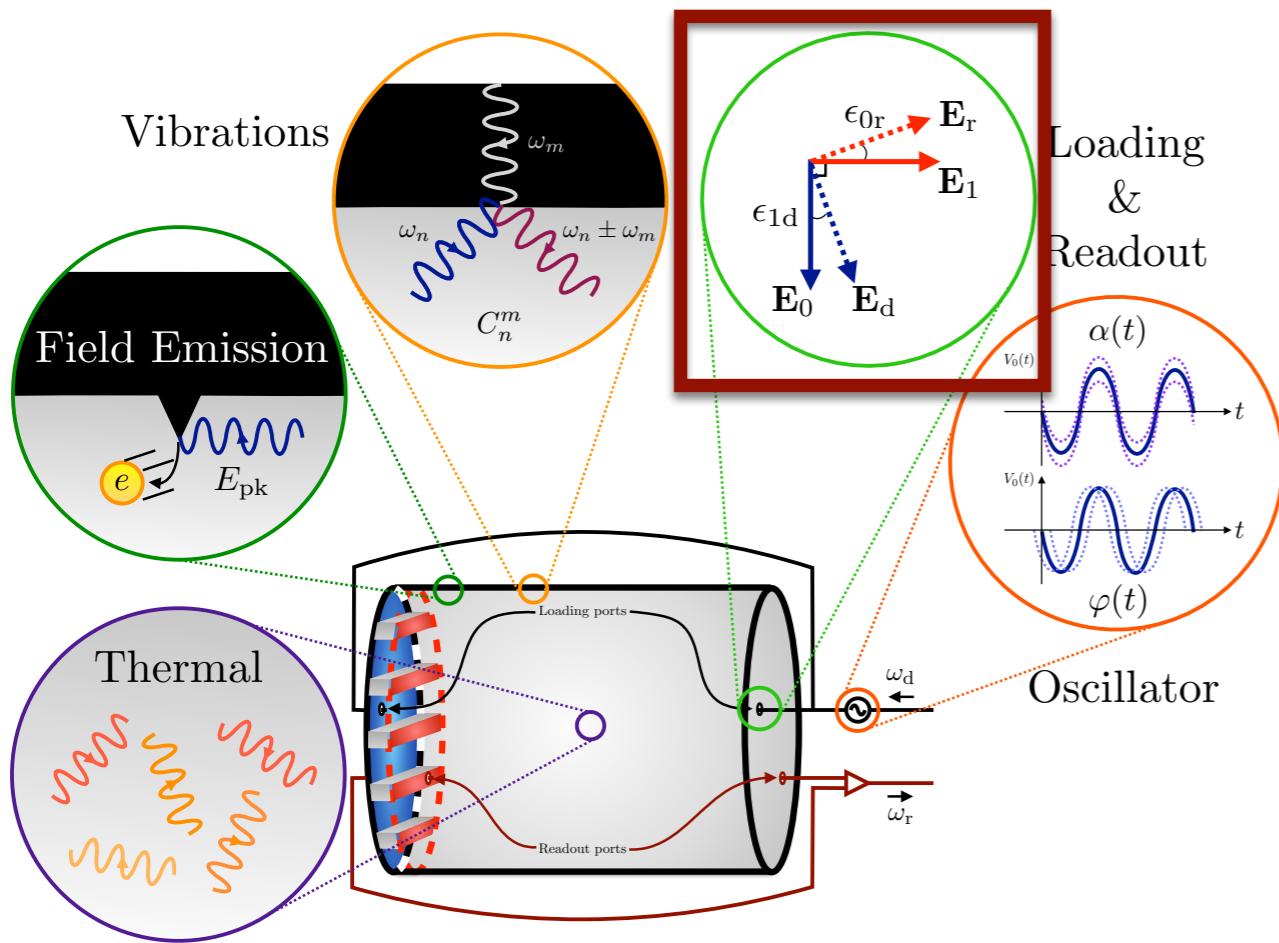
$$S_{\text{phase}}(\omega) \simeq \frac{1}{2} \epsilon_{1d}^2 S_\phi(\omega - \omega_0)$$

$$\frac{(\omega \omega_1/Q_1)^2}{(\omega^2 - \omega_1^2)^2 + (\omega \omega_1/Q_1)^2}$$

$$\frac{\omega_0 Q_1}{\omega_0 Q_0} P_{\text{in}}$$

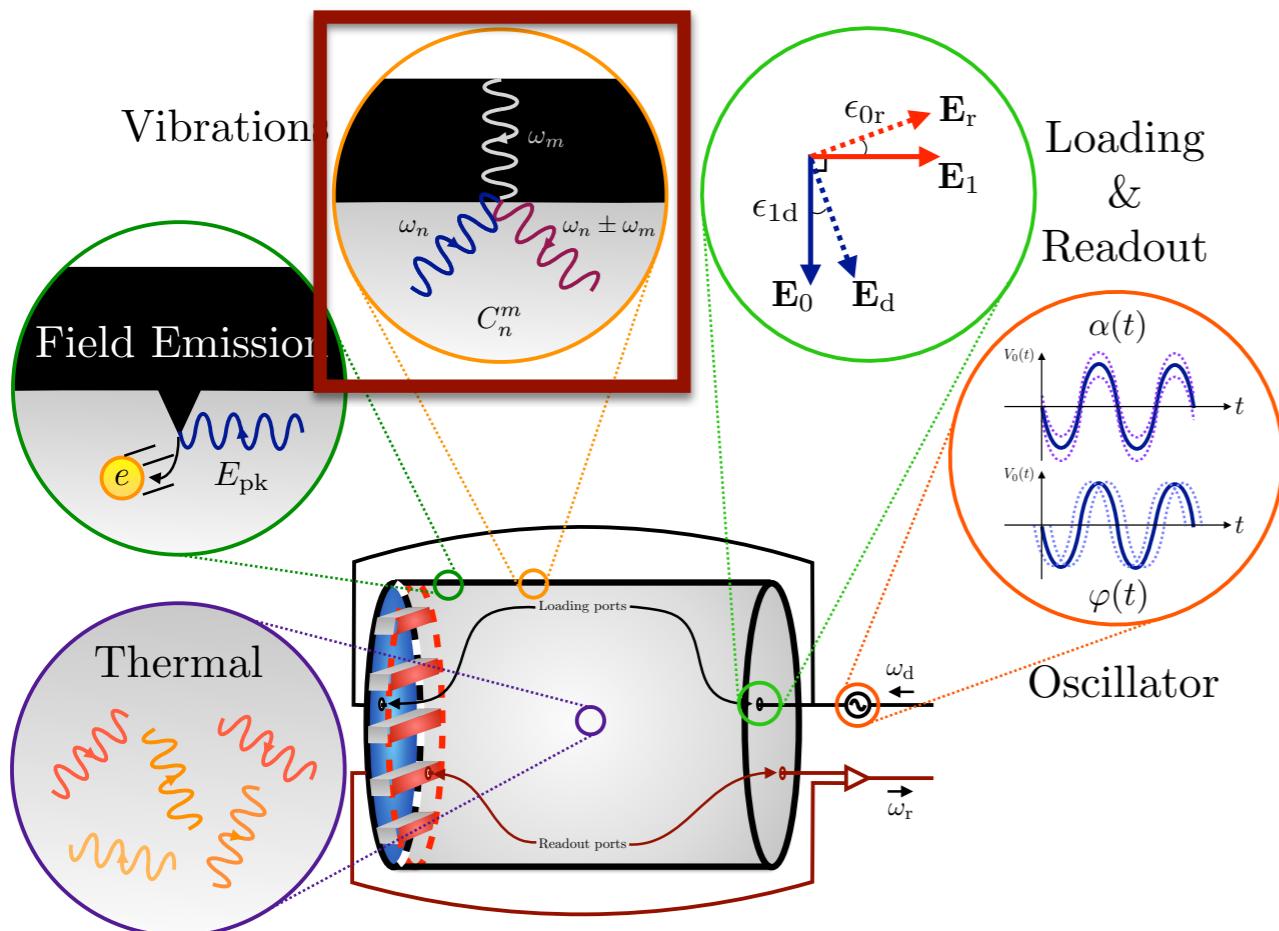
$\sim 1/m_a$

## Cavity Response



# VIBRATIONAL NOISE

$$S_{\text{mech}}(\omega) = \sum_{n=0,1} S_{\text{mech}}^{(n)}(\omega) \simeq \boxed{\frac{\epsilon_{1d}^2}{4} \frac{\omega_0}{Q_0} P_{\text{in}}} \sum_{n=0,1} \frac{(S_{q_m}(\omega - \omega_0)/V^{2/3}) (\omega_n/Q_n) \omega_n^4 \omega^2}{[(\omega^2 - \omega_n^2)^2 + (\omega \omega_n/Q_n)^2] [(\omega_0^2 - \omega_n^2)^2 + (\omega_0 \omega_n/Q_n)^2]}$$



**Wall Displacement**

$$S_{q_m}(\omega) \simeq \frac{1}{M^2} \frac{S_{f_m}(\omega)}{(\omega^2 - \omega_m^2)^2 + (\omega_m \omega/Q_m)^2}$$

**On Resonance**

$$\sim 1/m_a^4$$

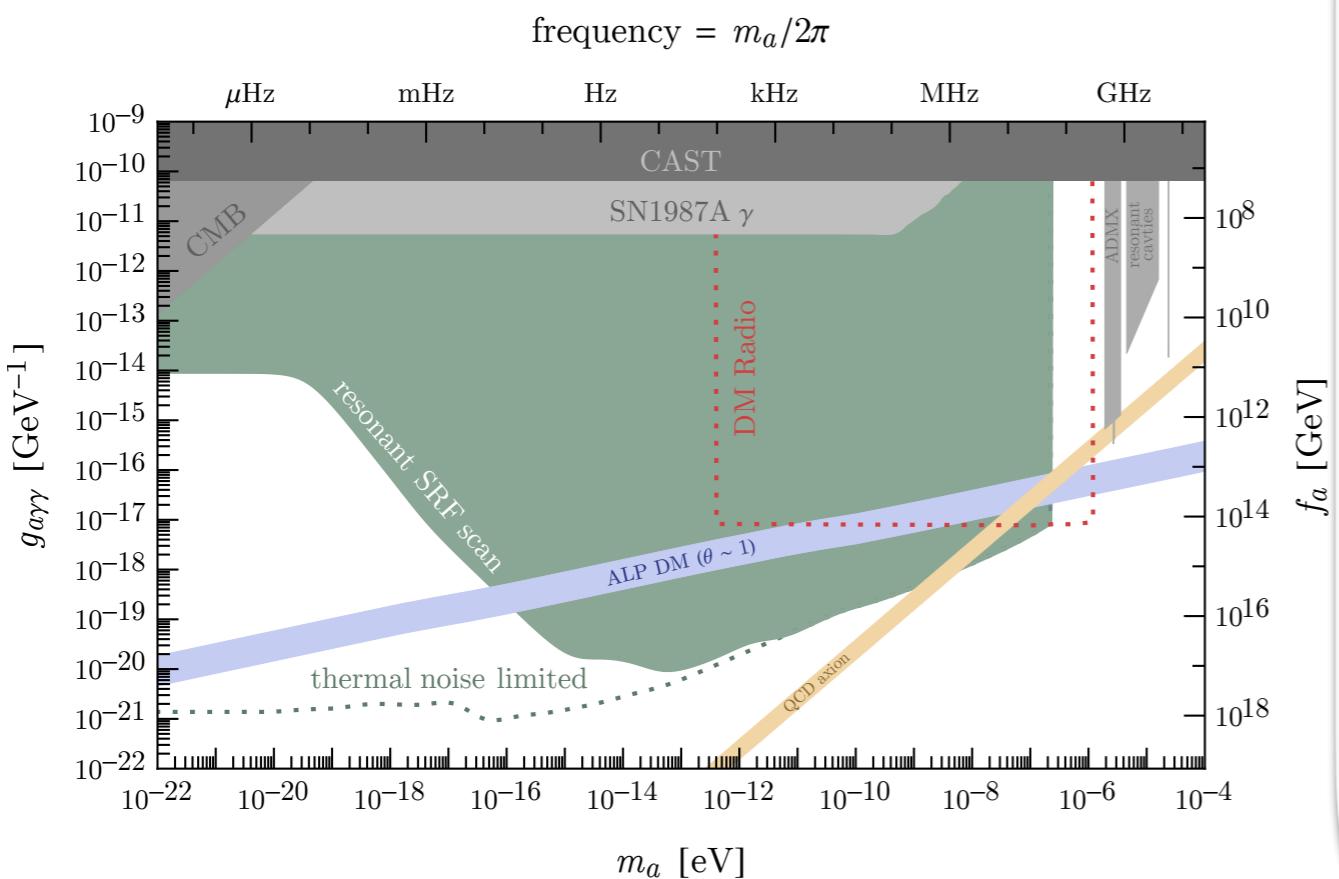
**Off Resonance**

$$\sim 1/m_a^2$$

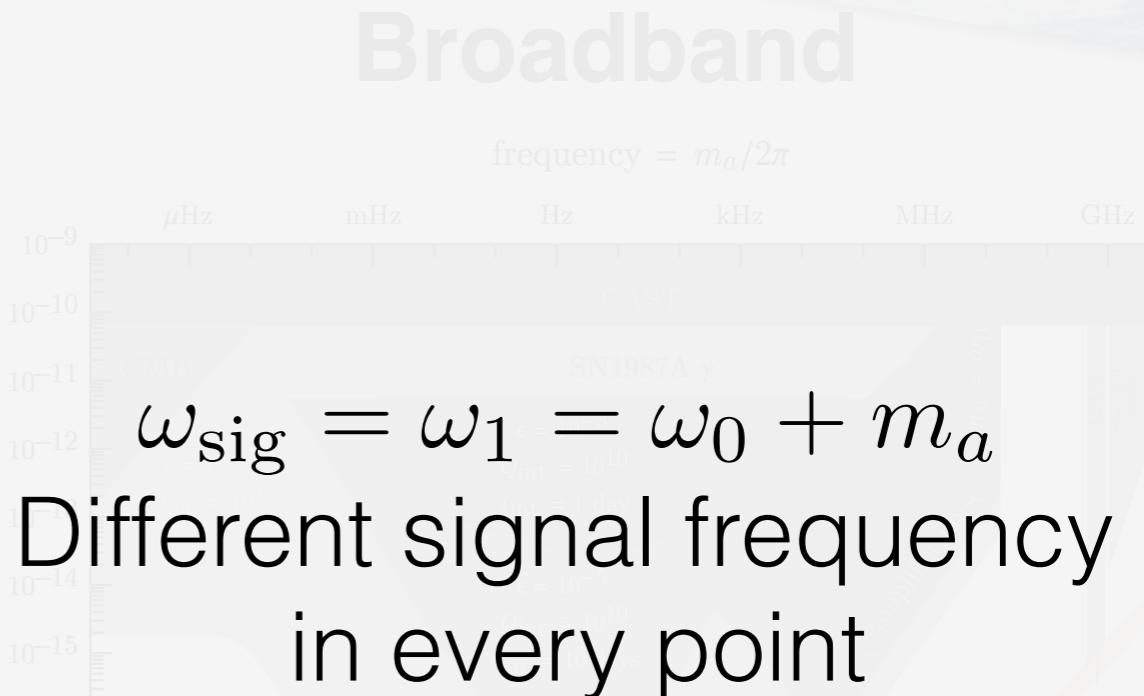
$$\omega_m^{\min} \simeq \text{kHz}$$

# RESONANT VS BROADBAND

## Resonant

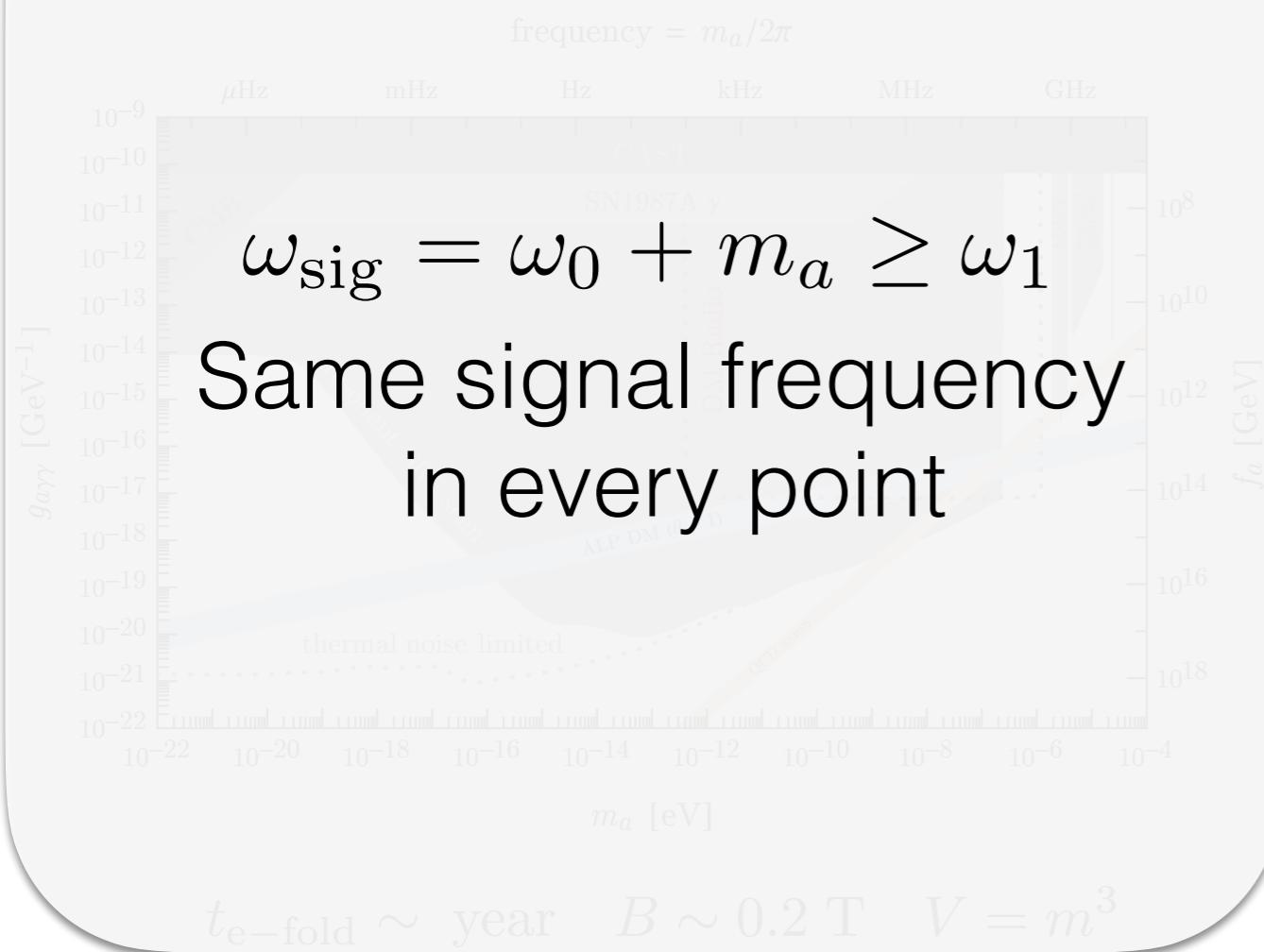


$$t_{\text{e-fold}} \sim \text{year} \quad B \sim 0.2 \text{ T} \quad V = m^3$$

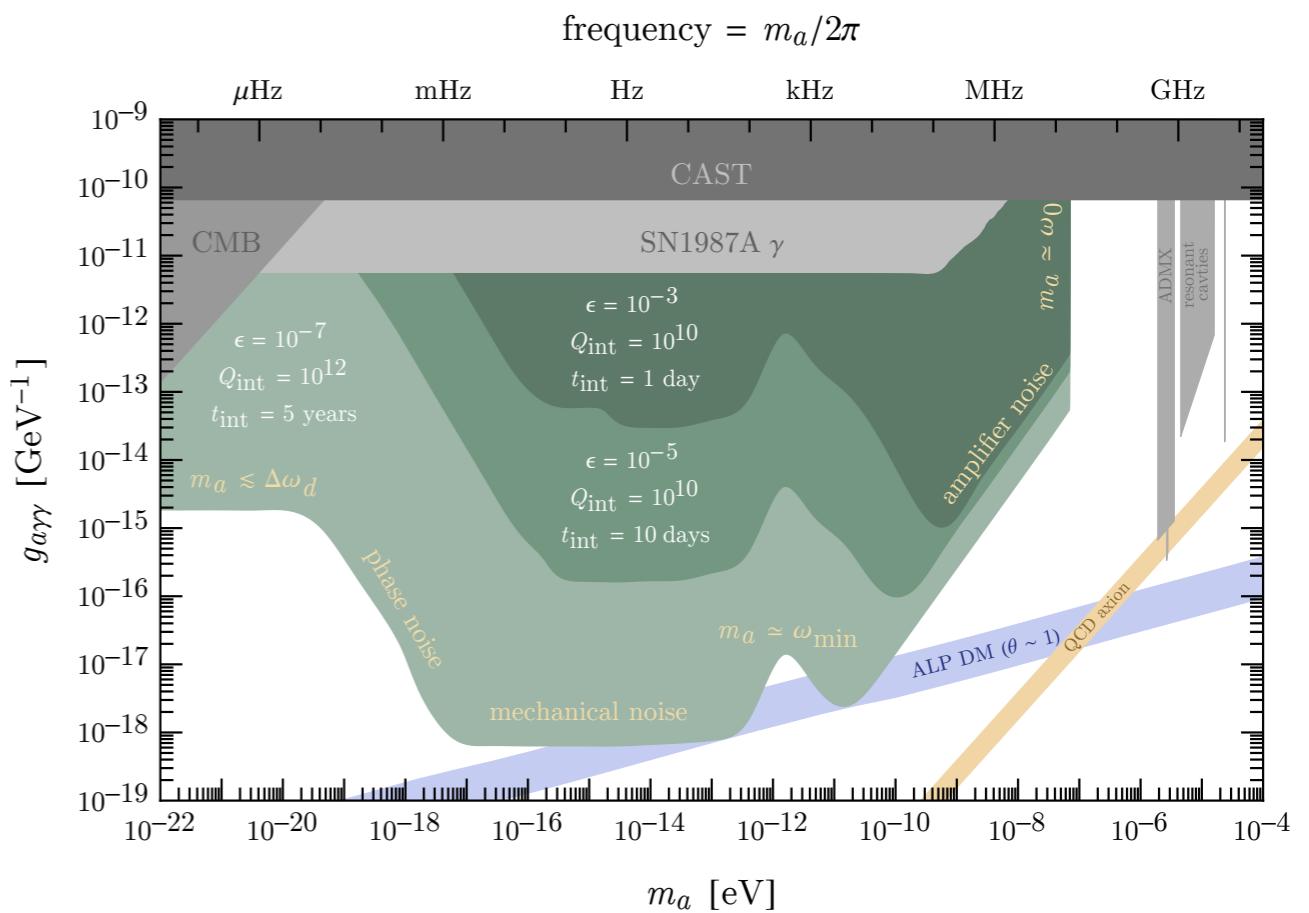


# RESONANT VS BROADBAND

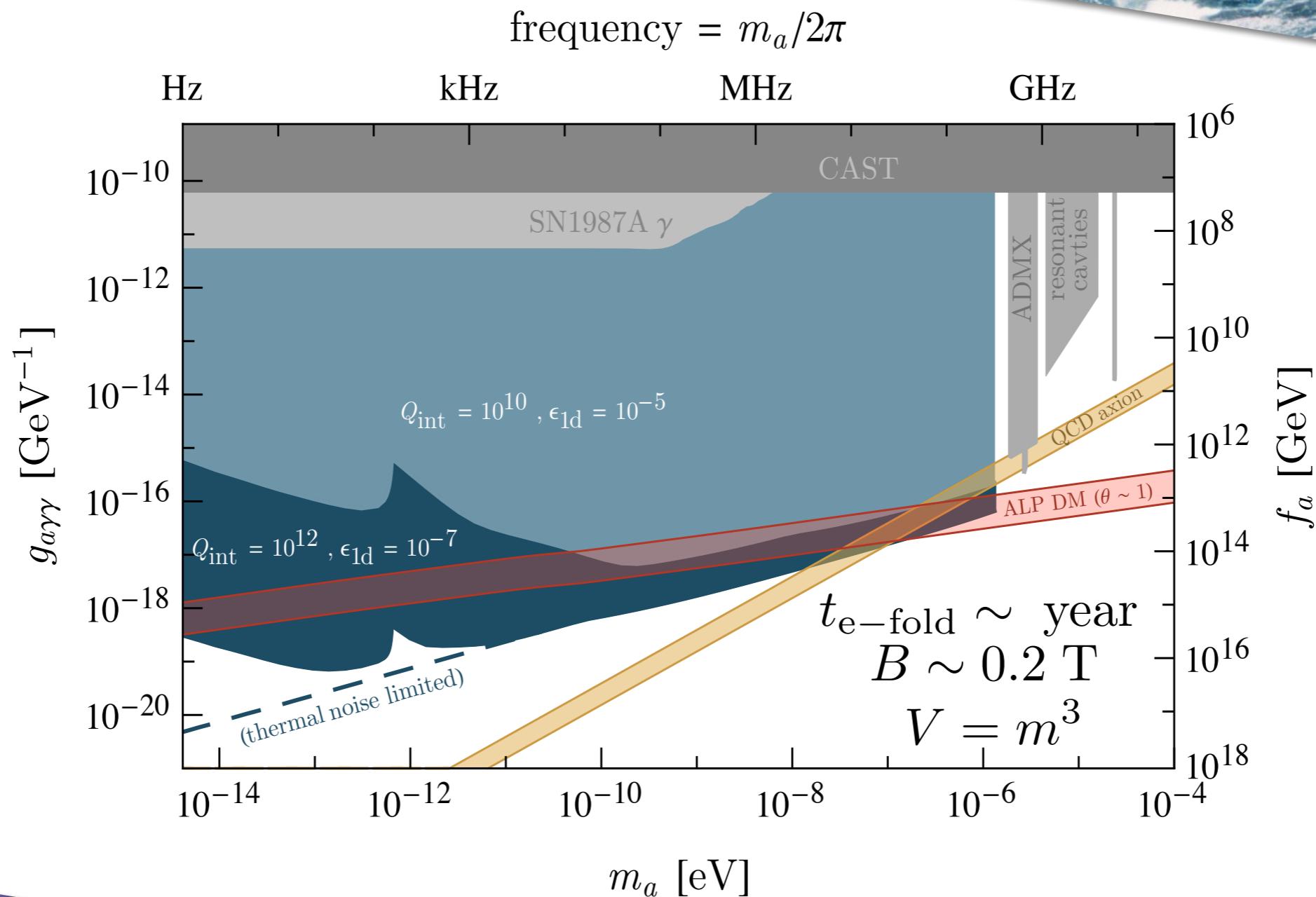
## Resonant



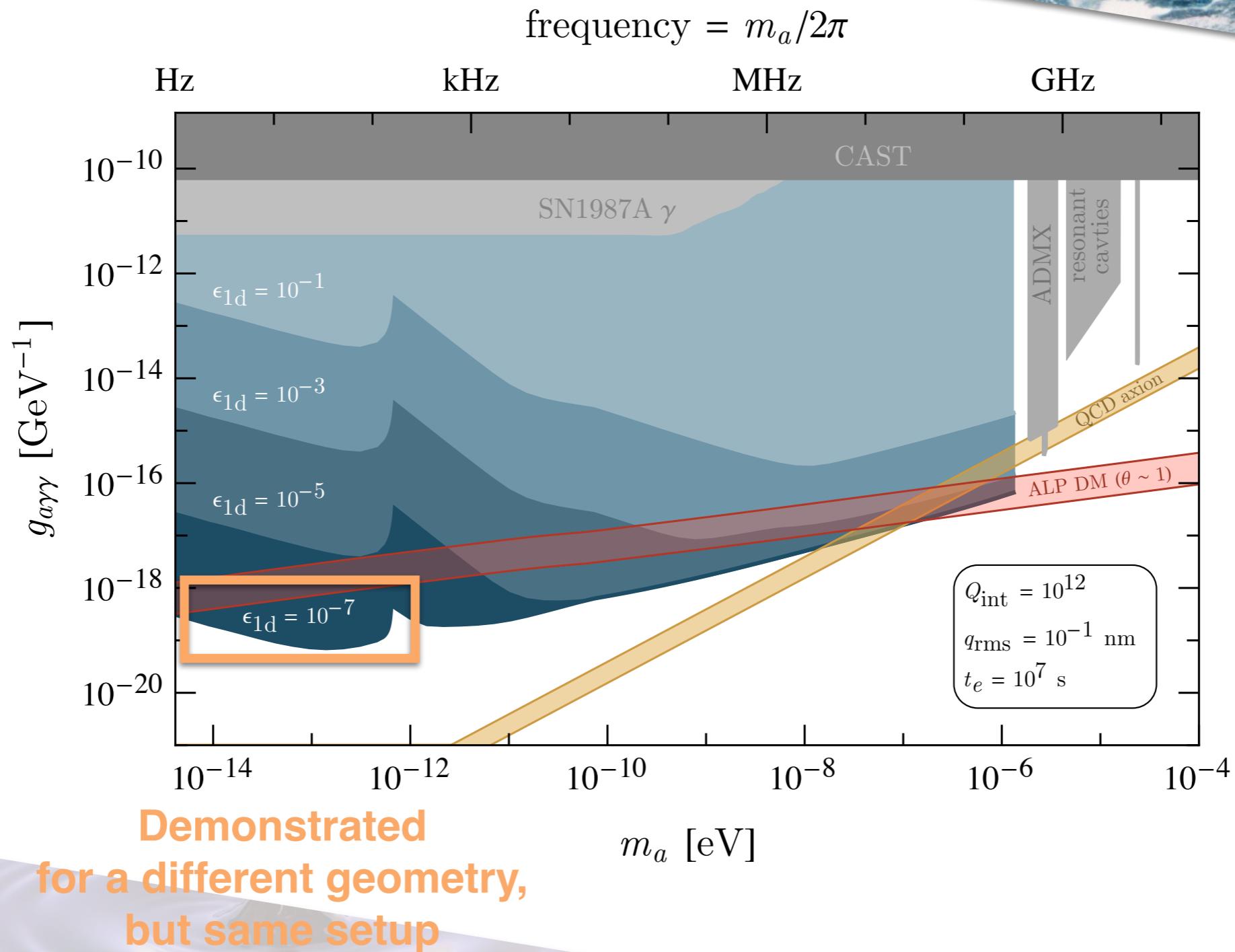
## Broadband



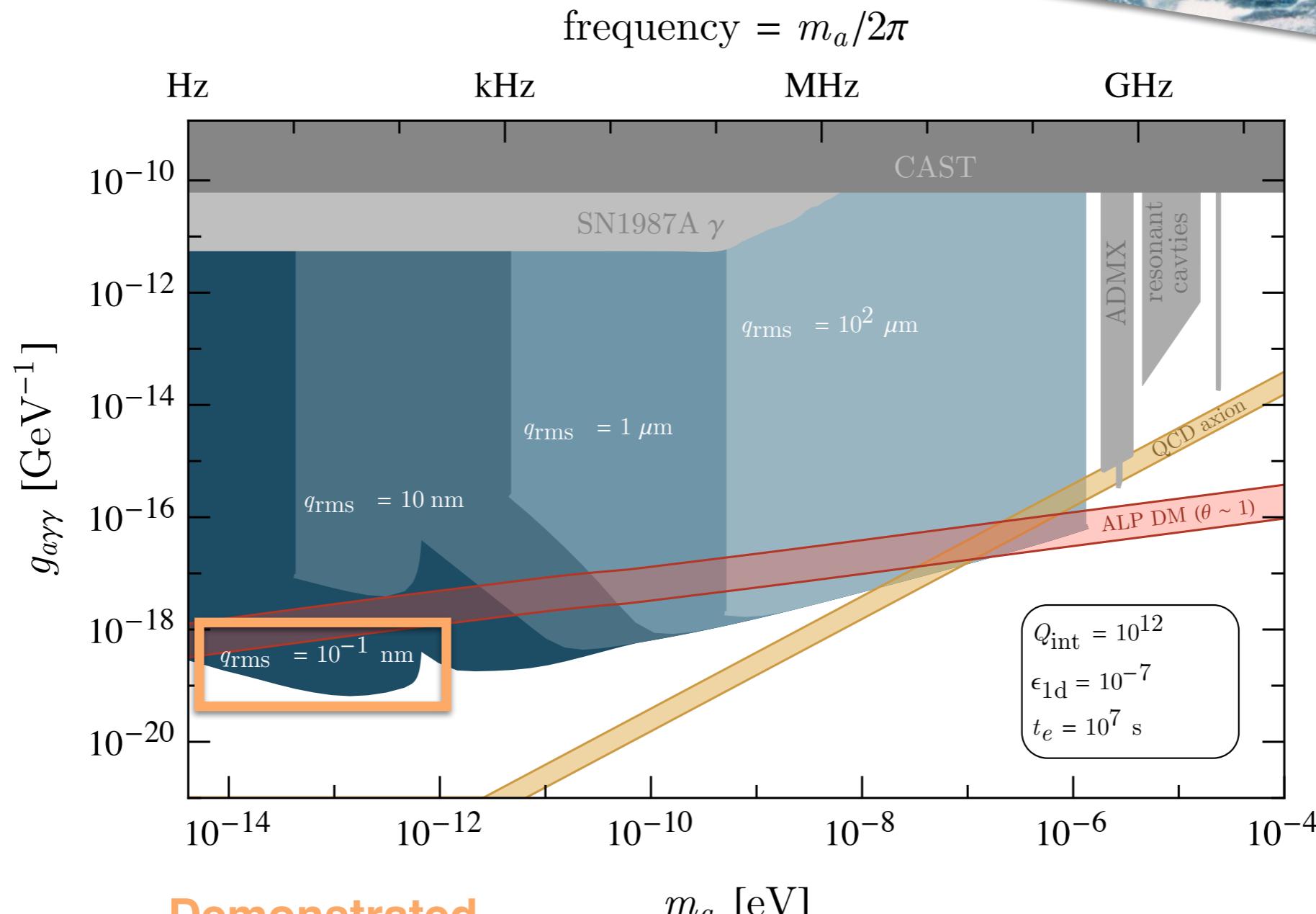
# SENSITIVITY (RESONANT)



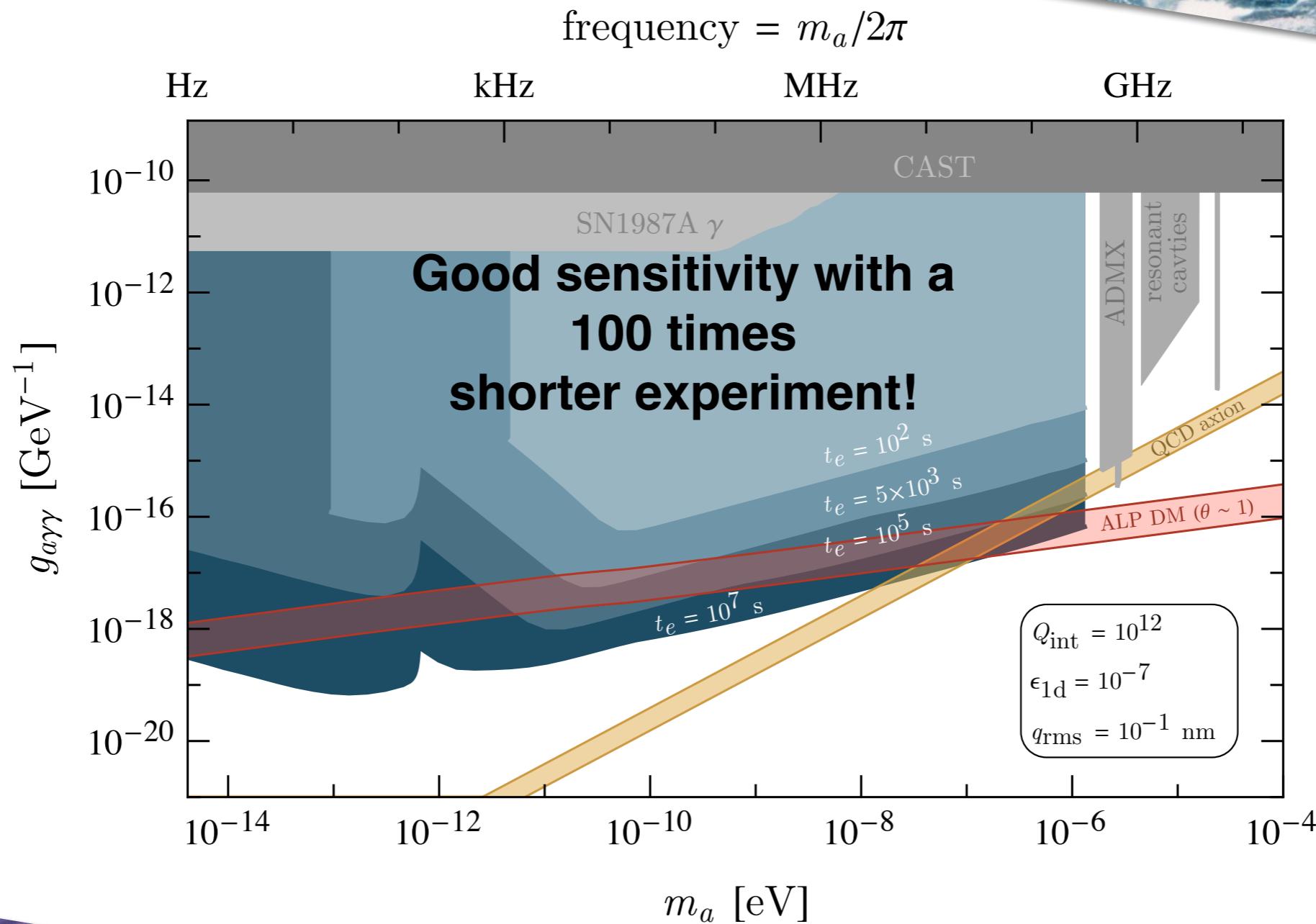
# ROBUSTNESS TO LOADING



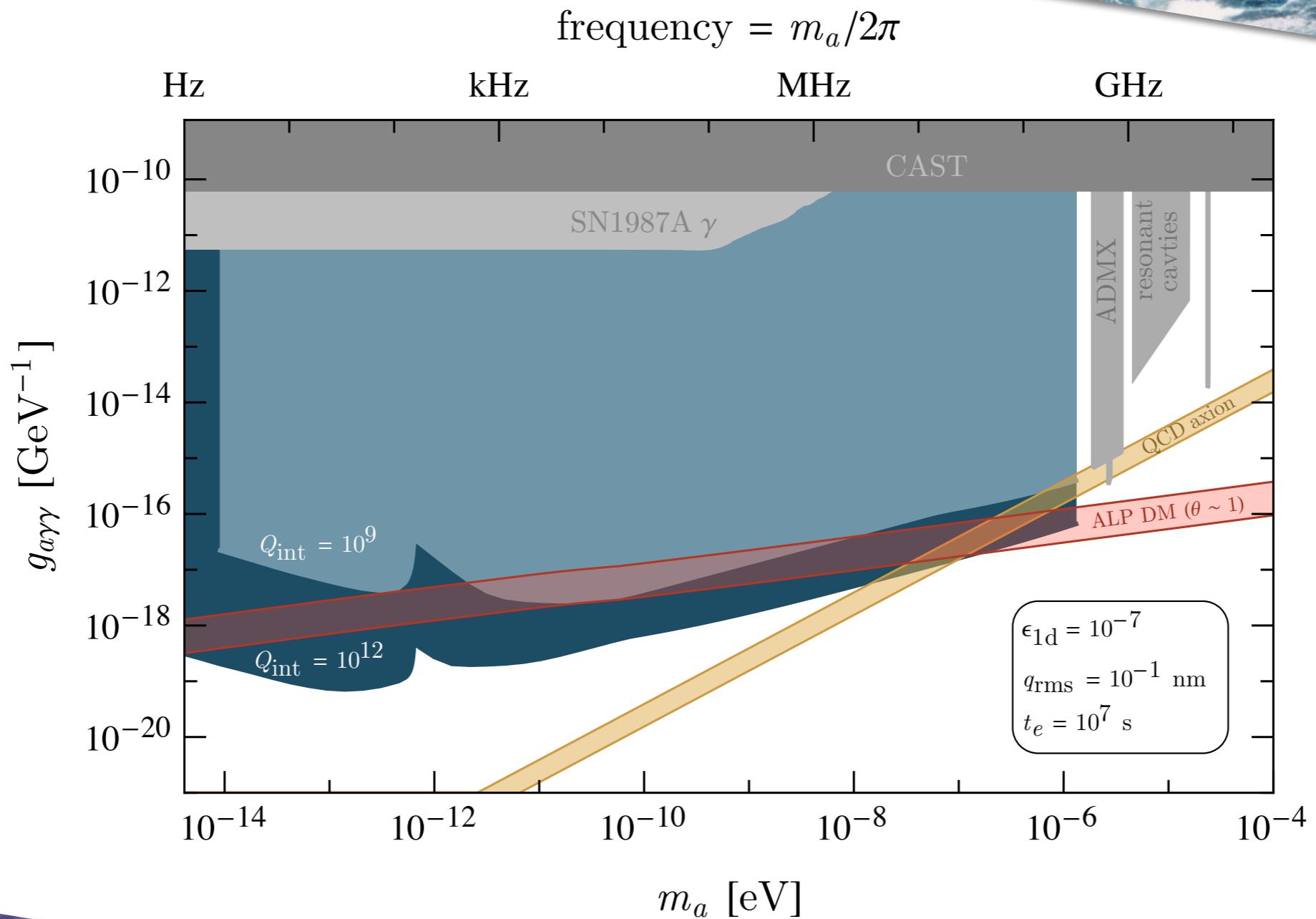
# ROBUSTNESS TO ATTENUATION OF VIBRATIONS



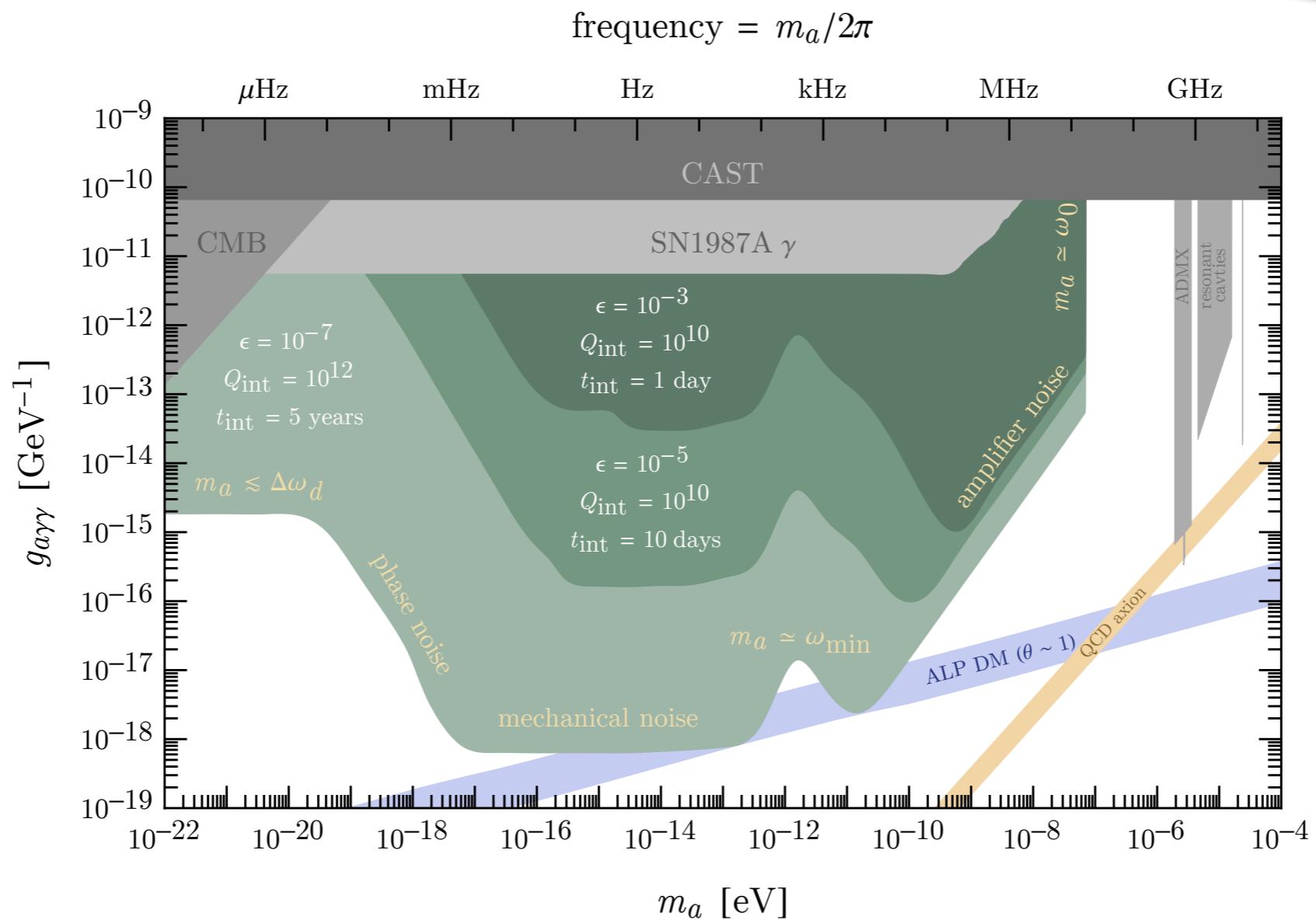
# INTEGRATION TIME



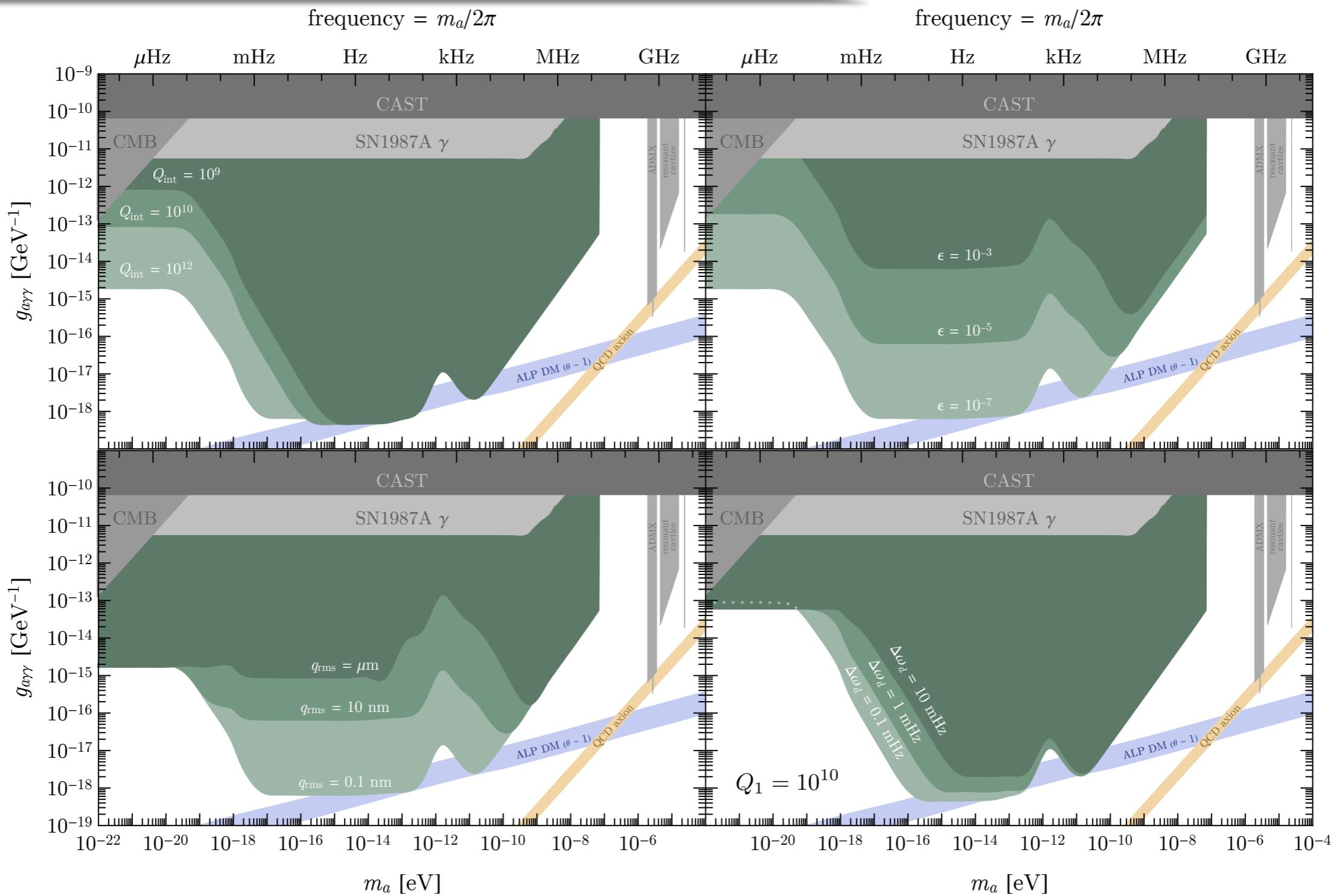
# THE POWER OF Q



# SENSITIVITY (BROADBAND)



# ROBUSTNESS TO EXPERIMENTAL DETAILS (BROADBAND)



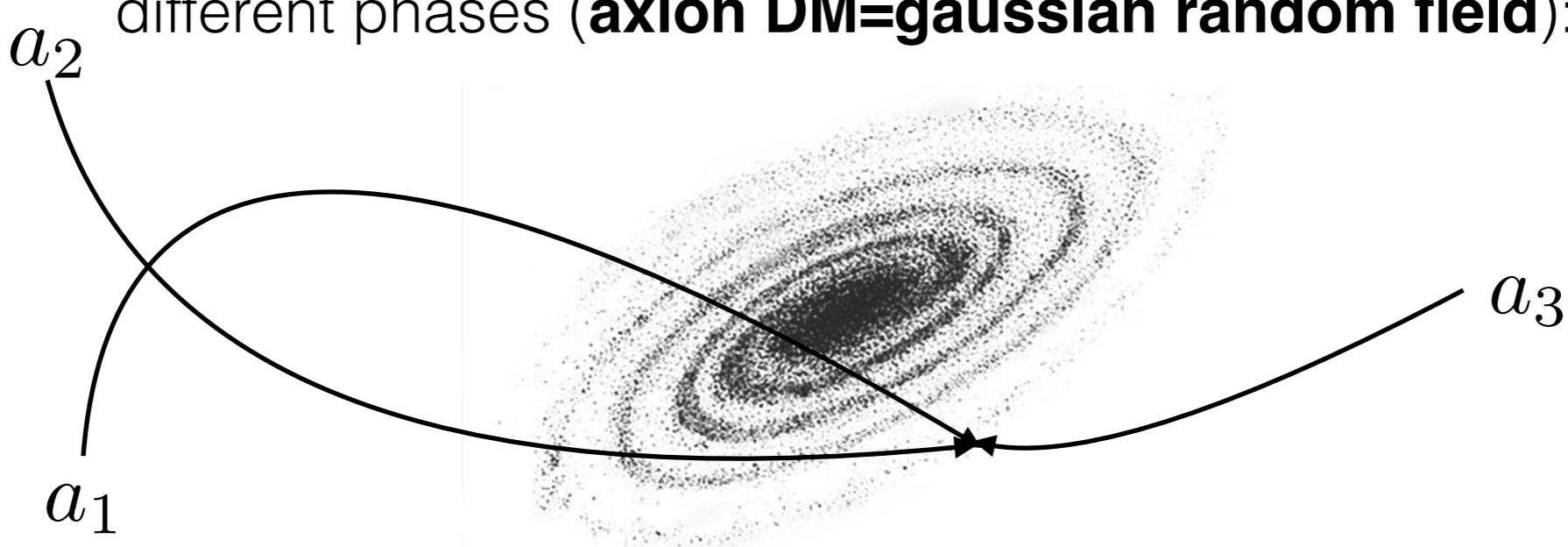
# CONCLUSION

- Light Dark Matter candidates behaving as a classical field are appealing theoretically (strong CP problem, Higgs mass, generically expected from string theory), maybe as appealing as WIMPs were in the past
- We are just starting to explore them experimentally (in this talk **new concept for axion dark matter detection**)

# BACKUP

# AXION DM IN THE LABORATORY

In each experimental bin we are summing over a multitude of plane waves with different phases (**axion DM=gaussian random field**):



$$a(t) \simeq a_0 \cos(m_a t + \phi) [\cos(\delta\omega_a t + \phi') + \dots]$$

$$t_{\text{int}} \gg \frac{1}{\delta\omega_a} \gg \frac{1}{m_a} \rightarrow a_0 = \frac{\sqrt{2\rho_{\text{DM}}}}{m_a} \quad \phi \text{ Irrelevant}$$

$$\frac{1}{\delta\omega_a} \gtrsim t_{\text{int}} \gg \frac{1}{m_a} \rightarrow a_0 < \frac{\sqrt{2\rho_{\text{DM}}}}{m_a} \quad \phi \text{ Irrelevant}$$

# STATISTICS INTERLUDE

**Time:** Gaussian Random Field

$$\langle a(t + \tau) a(t' + \tau) \rangle = \langle a(t) a(t') \rangle$$

**Mean**  $\langle a(t) \rangle = 0$

**Variance**  $\langle |a(t)|^2 \rangle = \frac{\rho_{\text{DM}}}{m_a^2}$

**Frequency:** Gaussian Random Field

**Mean**  $\langle a(\omega) \rangle = 0$

**Variance**  $\langle a(\omega) a^*(\omega') \rangle = \delta(\omega - \omega') S_a(\omega)$

# STATISTICS INTERLUDE

**Data:**  $d(\omega) = n(\omega) + s(\omega)$      $s(\omega) \sim a(\omega)$

**Noise:** Gaussian Colored     $\langle n(\omega) \rangle = 0$      $\langle n(\omega)n(\omega') \rangle = \delta(\omega - \omega')S_n(\omega)$

**Likelihood:**

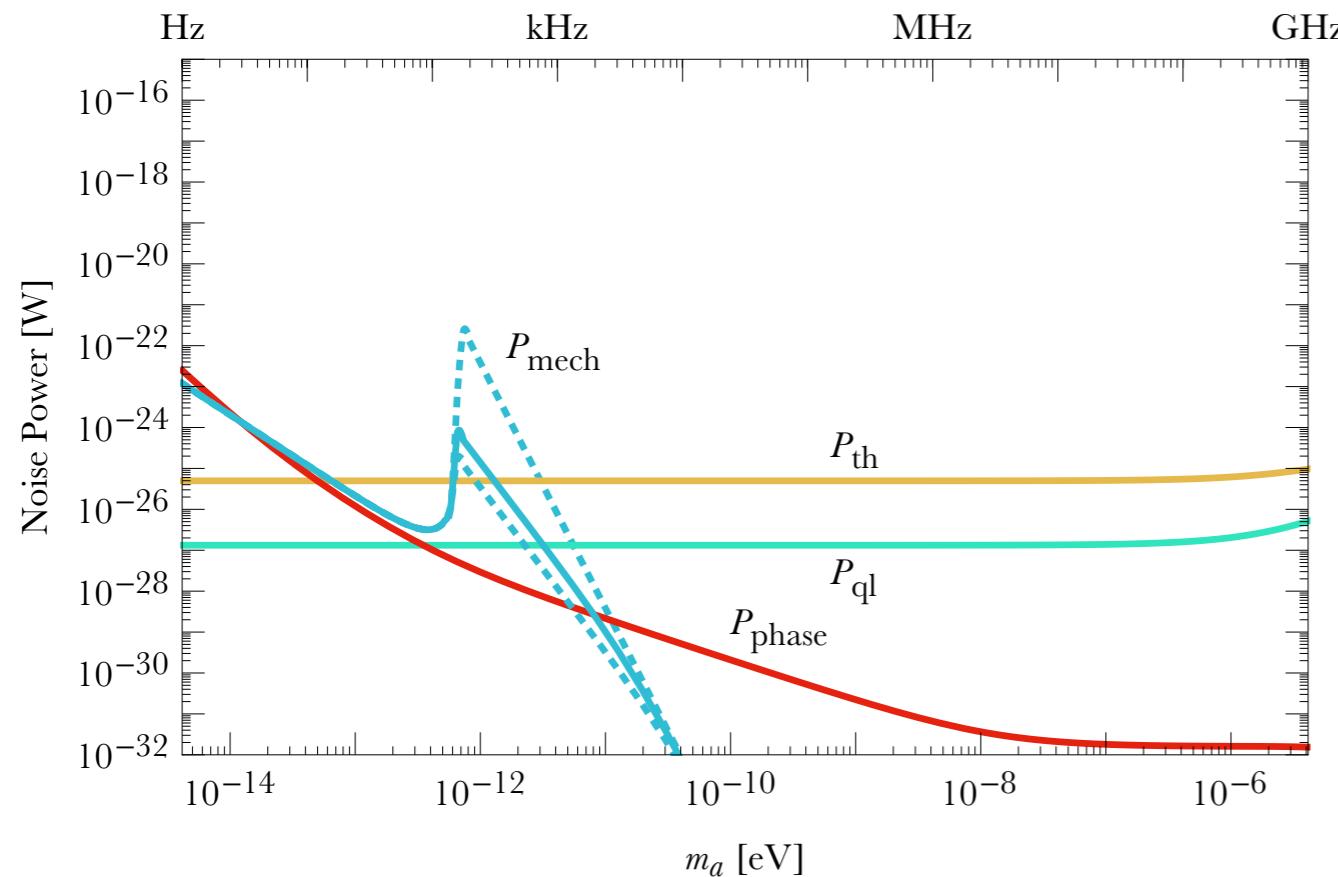
$$L[d(\omega)] = \frac{1}{Z} e^{-\int d\omega \frac{d(\omega)d^*(\omega)}{S_n(\omega) + S_{\text{sig}}(\omega)}}$$

**Only the average 2-point function matters.**

A ‘deterministic’ axion gives the same result (see next slide)

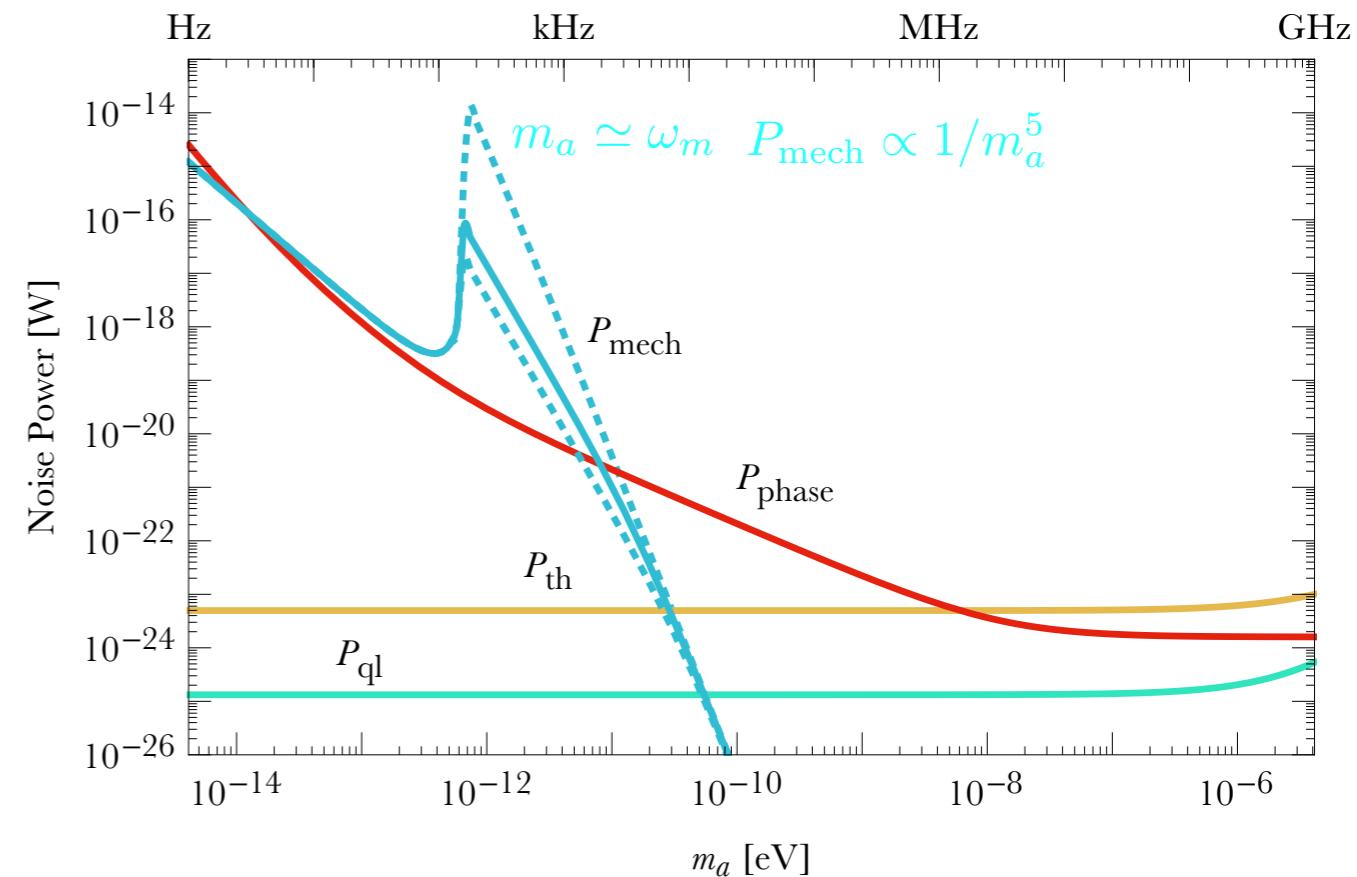
# NOISE (RESONANT)

frequency =  $m_a/2\pi$



$$\epsilon_{1d} = 10^{-7}, \quad Q = 10^{12}$$

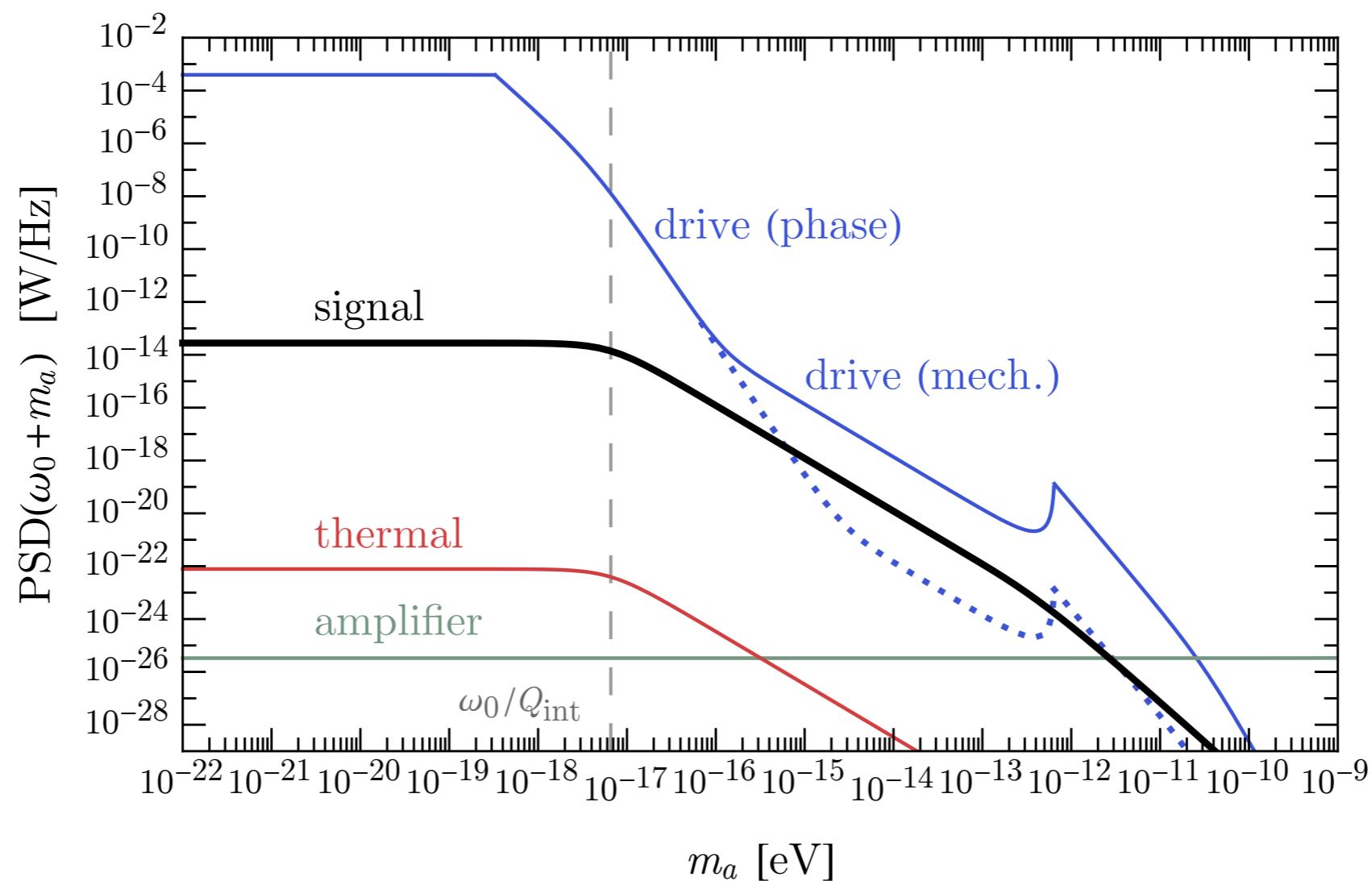
frequency =  $m_a/2\pi$



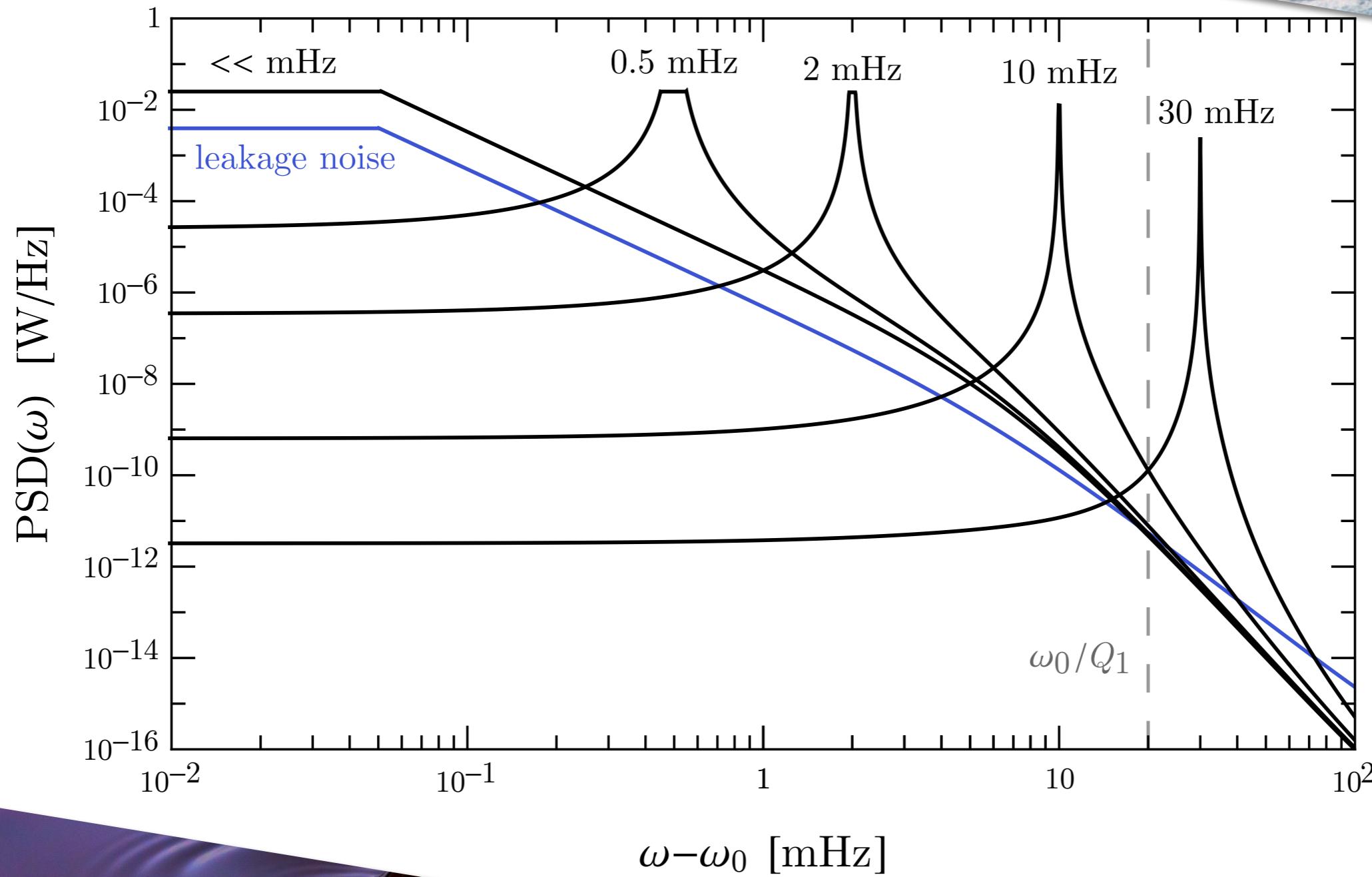
$$\epsilon_{1d} = 10^{-5}, \quad Q = 10^{10}$$

# NOISE (BROADBAND)

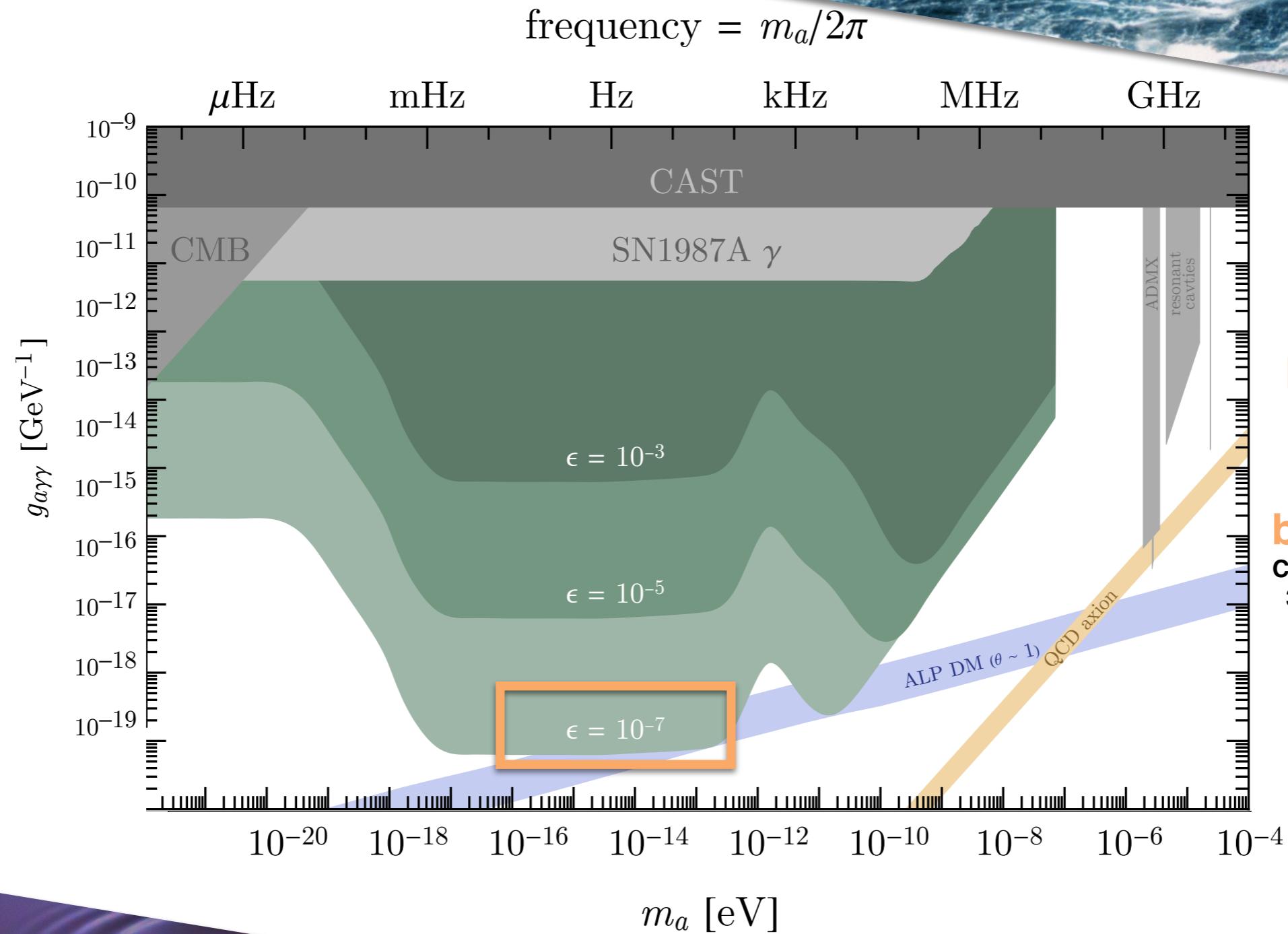
**PRELIMINARY!**



# MASS REACH (BROADBAND)



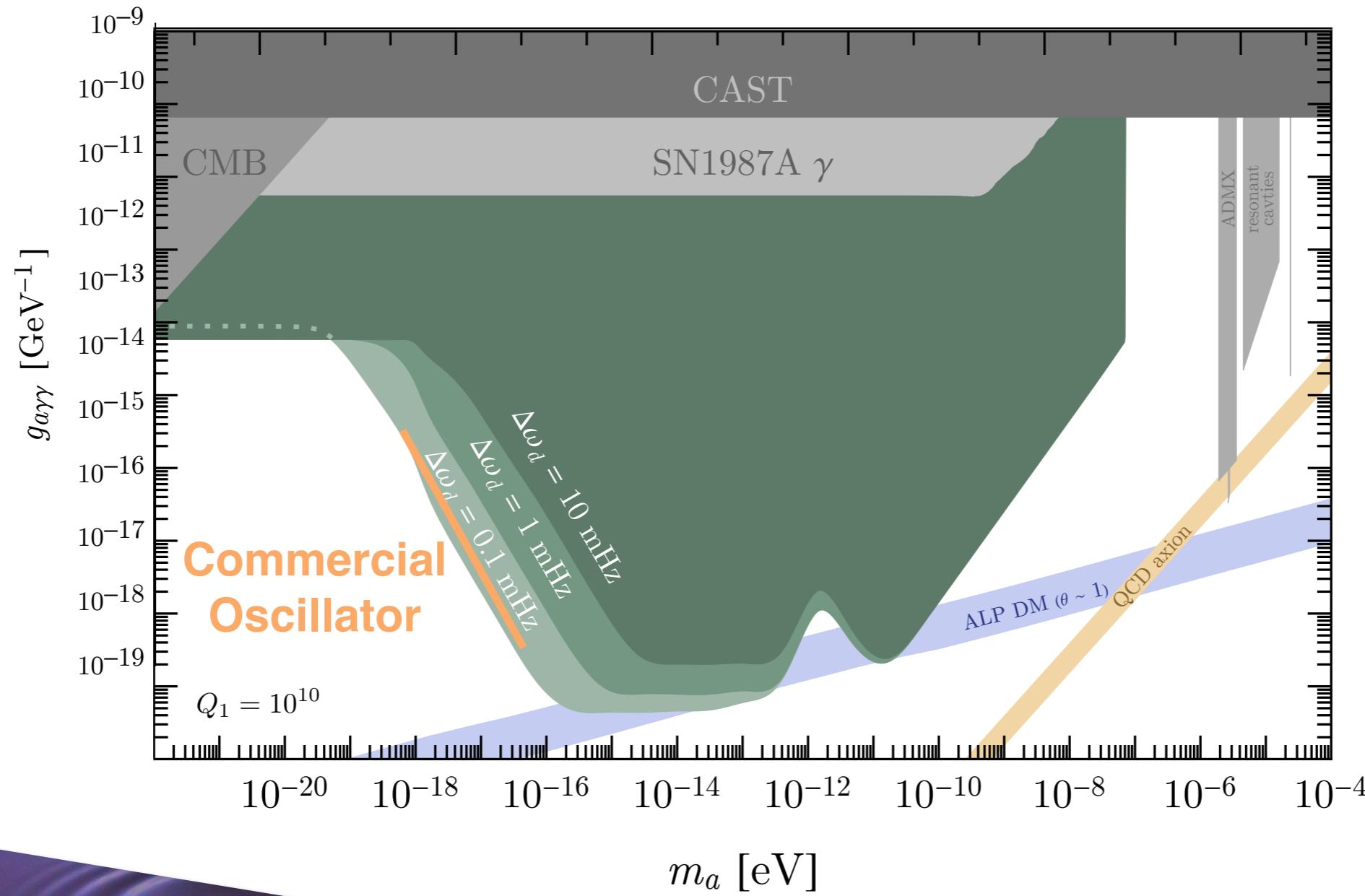
# ROBUSTNESS TO LOADING



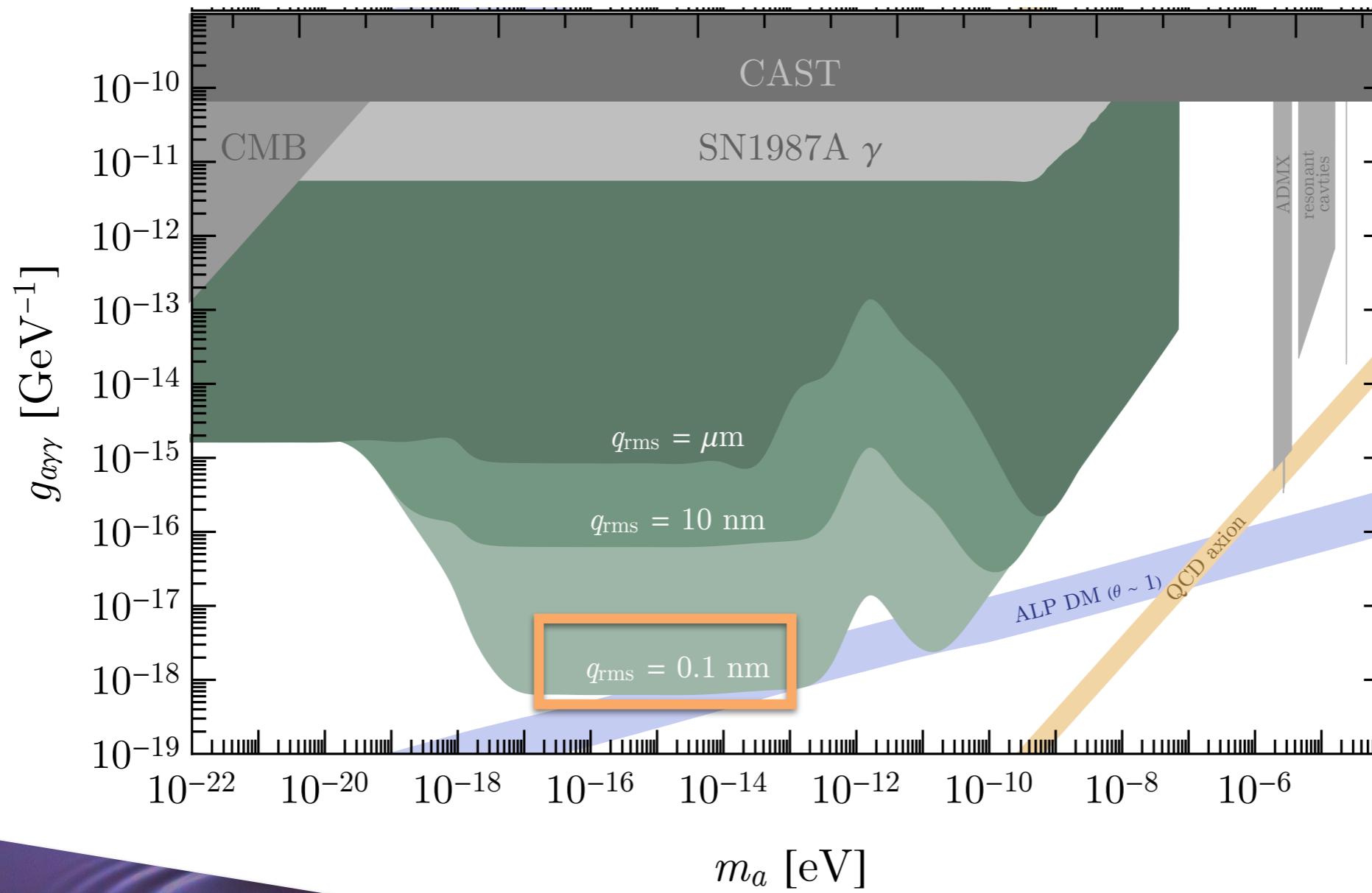
Demonstrated  
for a different  
geometry,  
but same setup

Class.Quant.Grav. 20 (2003)  
3505-3522, gr-qc/0502054

# ROBUSTNESS TO LOW FREQUENCY NOISE



# ROBUSTNESS TO ATTENUATION OF VIBRATIONS



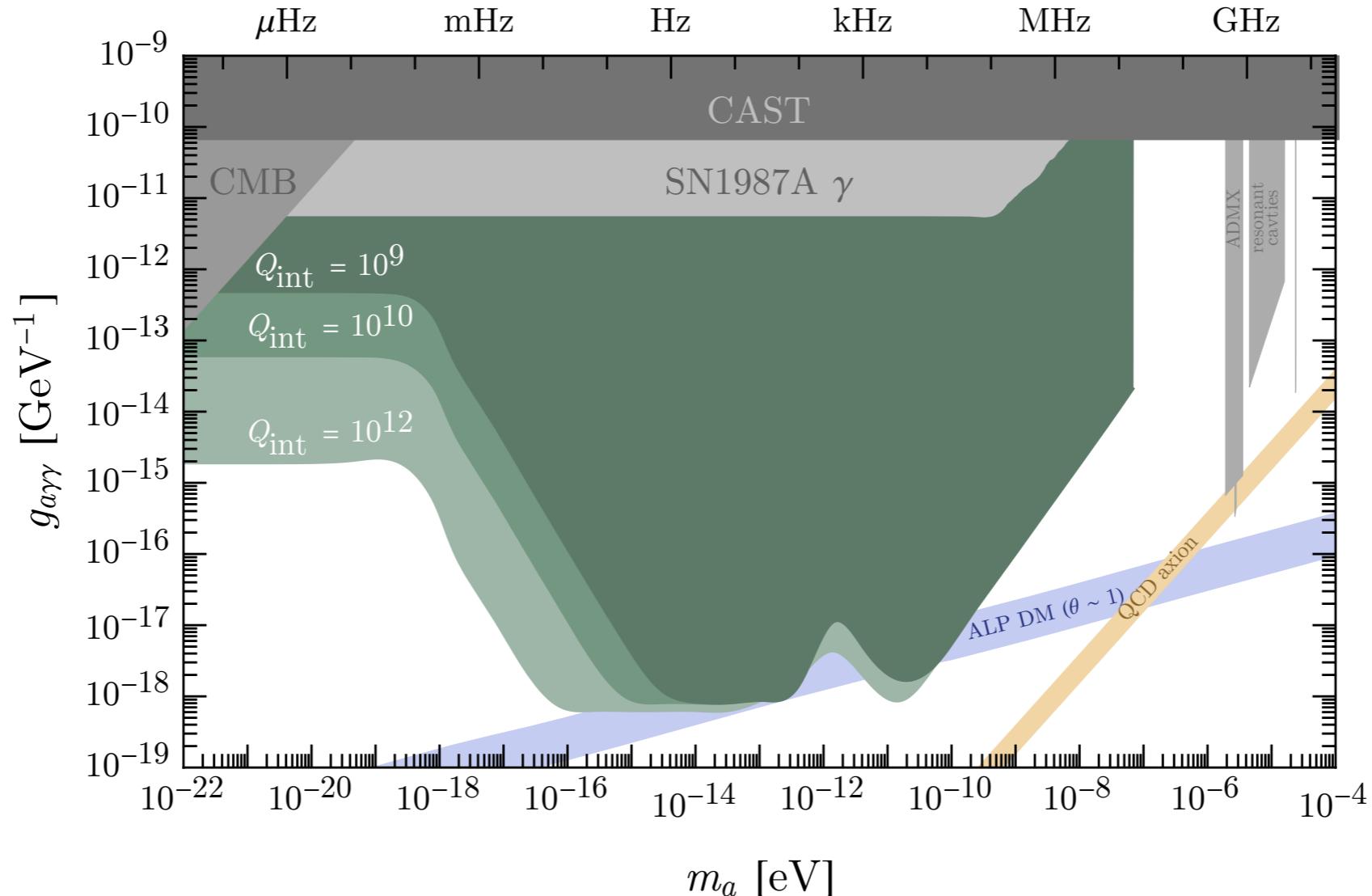
Demonstrated  
in similar  
cavities

[https://indico.physics.lbl.gov/indico/  
event/939/contributions/4371/  
attachments/2162/2812/DarkSRF-  
Aspen.pdf](https://indico.physics.lbl.gov/indico/event/939/contributions/4371/attachments/2162/2812/DarkSRF-Aspen.pdf)

# BROADBAND APPROACH

**PRELIMINARY!**

$$\text{frequency} = m_a/2\pi$$

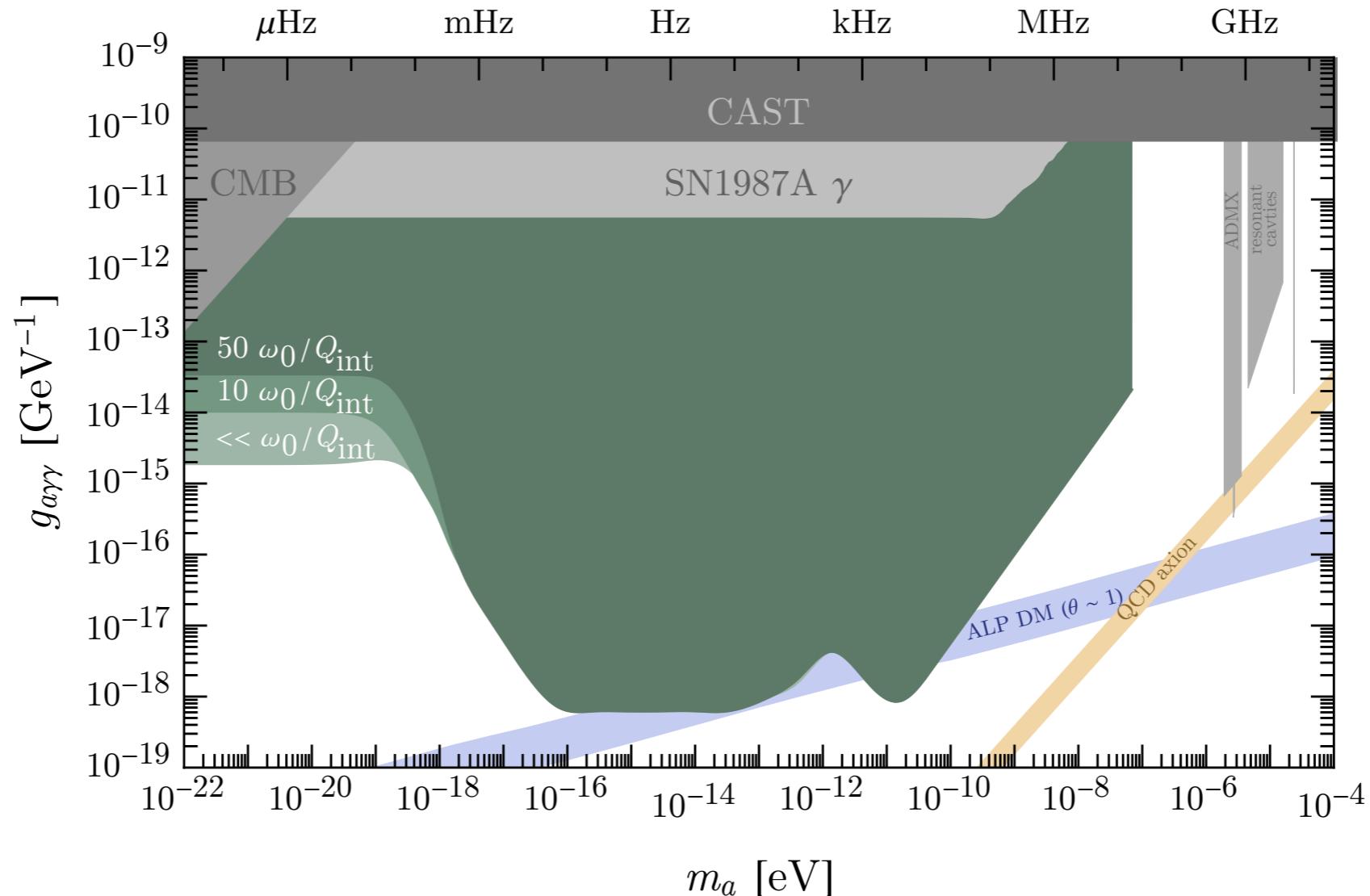


$$t_{\text{int}} \sim 5 \text{ years} \quad B \sim 0.2 \text{ T} \quad V = \text{m}^3$$

# BROADBAND APPROACH

**PRELIMINARY!**

$$\text{frequency} = m_a/2\pi$$



$$t_{\text{int}} \sim 5 \text{ years} \quad B \sim 0.2 \text{ T} \quad V = \text{m}^3$$

# OVERCOUPLING

$$S_{\text{sig}}(\omega) \rightarrow \frac{Q_1}{Q_{\text{cpl}}} S_{\text{sig}}(\omega)$$

**Quantum noise floor  
(amplifier)**

$$S_{\text{noise}}(\omega) = \boxed{S_{\text{ql}}(\omega)} + \frac{Q_1}{Q_{\text{cpl}}} \left( S_{\text{th}}(\omega) + S_{\text{phase}}(\omega) + S_{\text{mech}}^{(1)}(\omega) \right) + \frac{Q_0}{Q_{\text{cpl}}} S_{\text{mech}}^{(0)}(\omega)$$

**Overcoupling preserves the SNR in each frequency bin, but allows for bigger scan steps**