

# Electroweak Corrections in the Vincia Parton Shower

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**In collaboration with Ronald Kleiss, Peter Skands, Helen Brooks**

# Overview

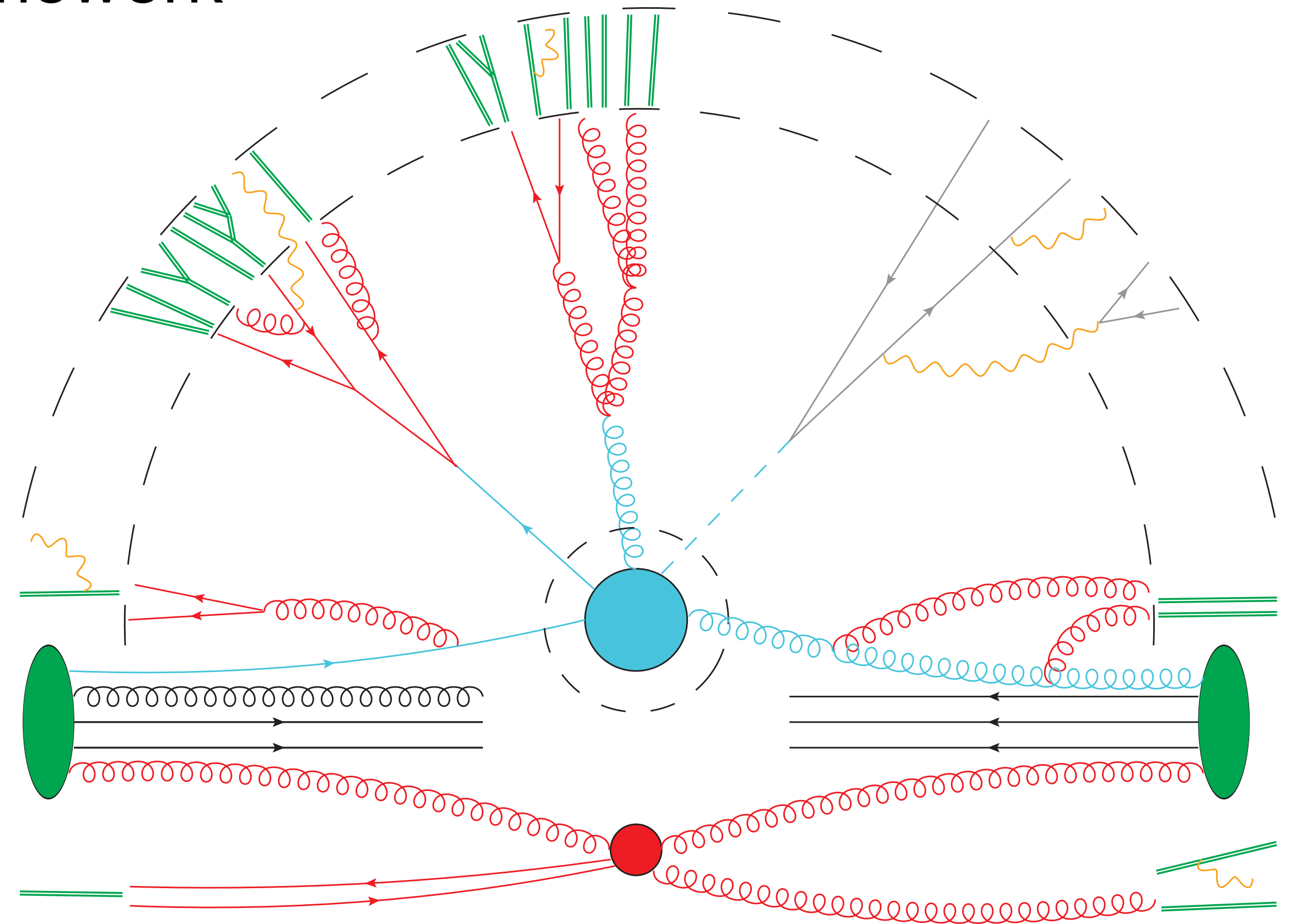
1. Parton shower overview
2. Electroweak showering
3. Novel features in the electroweak sector

# Parton shower overview



# Parton Showers

- Essential part of Monte Carlo event generators
- Process-independent resummation framework
- Fully differential
- Interface hard scattering (high scale) to hadronization (low scale)
- Many types with many differences

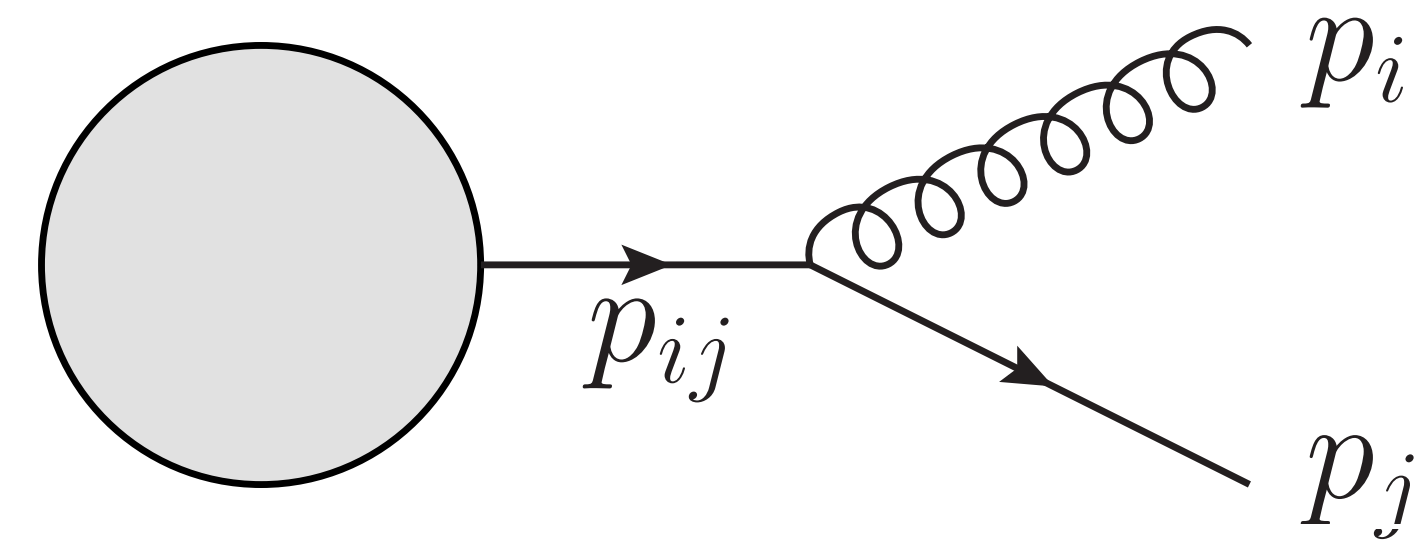


# Factorization

Based on factorisation properties of Matrix Element in singular limits

## 1. Quasi-collinear limit

$$p_i \cdot p_j \approx m_i^2, m_j^2 \text{ and } E_i^2, E_j^2 \gg p_i \cdot p_j$$



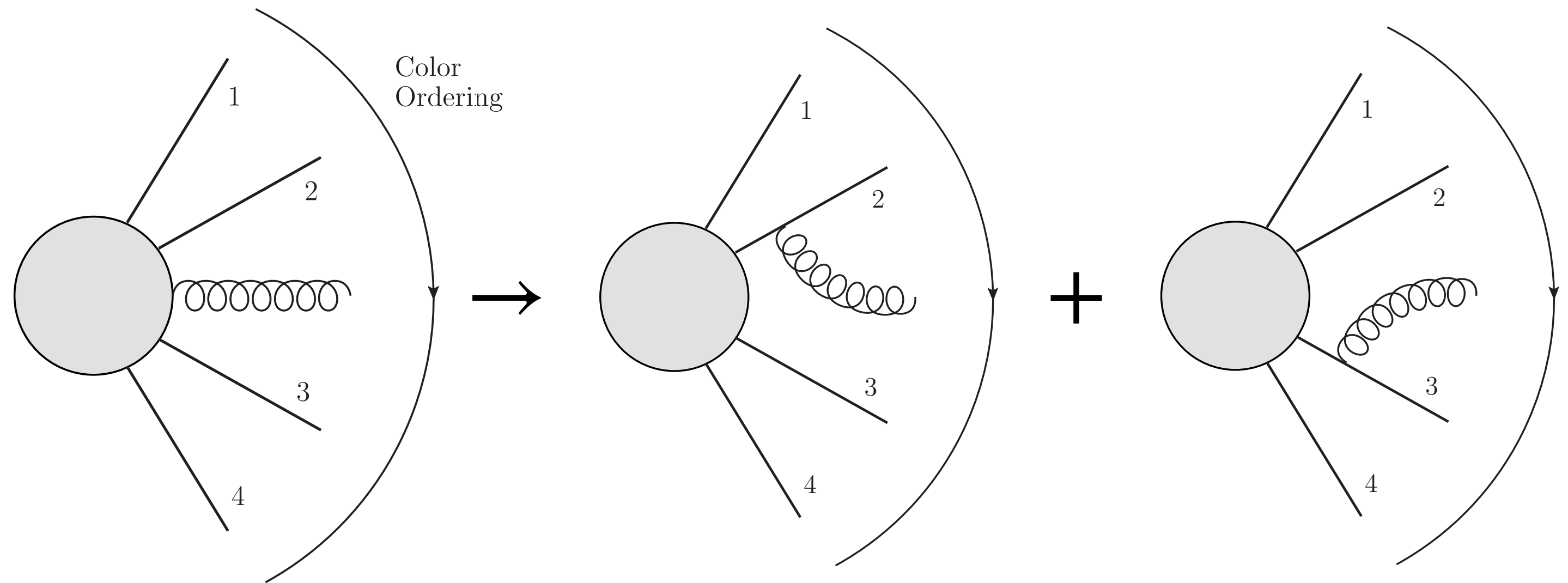
$$|M_{n+1}(\dots, p_i, p_j, \dots)|^2 \rightarrow 8\pi\alpha_s \frac{1}{(p_i + p_j)^2} P_{(ij) \rightarrow ij}(z) |M_n(\dots, p_{ij}, \dots)|^2$$

# Factorization

Based on factorisation properties of Matrix Element in singular limits

## 2. Soft limit

$$E_j \approx m_j \text{ and } E_i, E_k \gg E_j$$



$$|M_{n+1}(\dots, p_i, p_j, p_k \dots)|^2 \rightarrow 4\pi\alpha_s C \left[ 2 \frac{p_i \cdot p_k}{p_i \cdot p_j p_j \cdot p_k} - \frac{m_i^2}{(p_i \cdot p_j)^2} - \frac{m_k^2}{(p_j \cdot p_k)^2} \right] |M_n(\dots, p_i, p_k \dots)|^2 + \mathcal{O}(1/N_C^2)$$

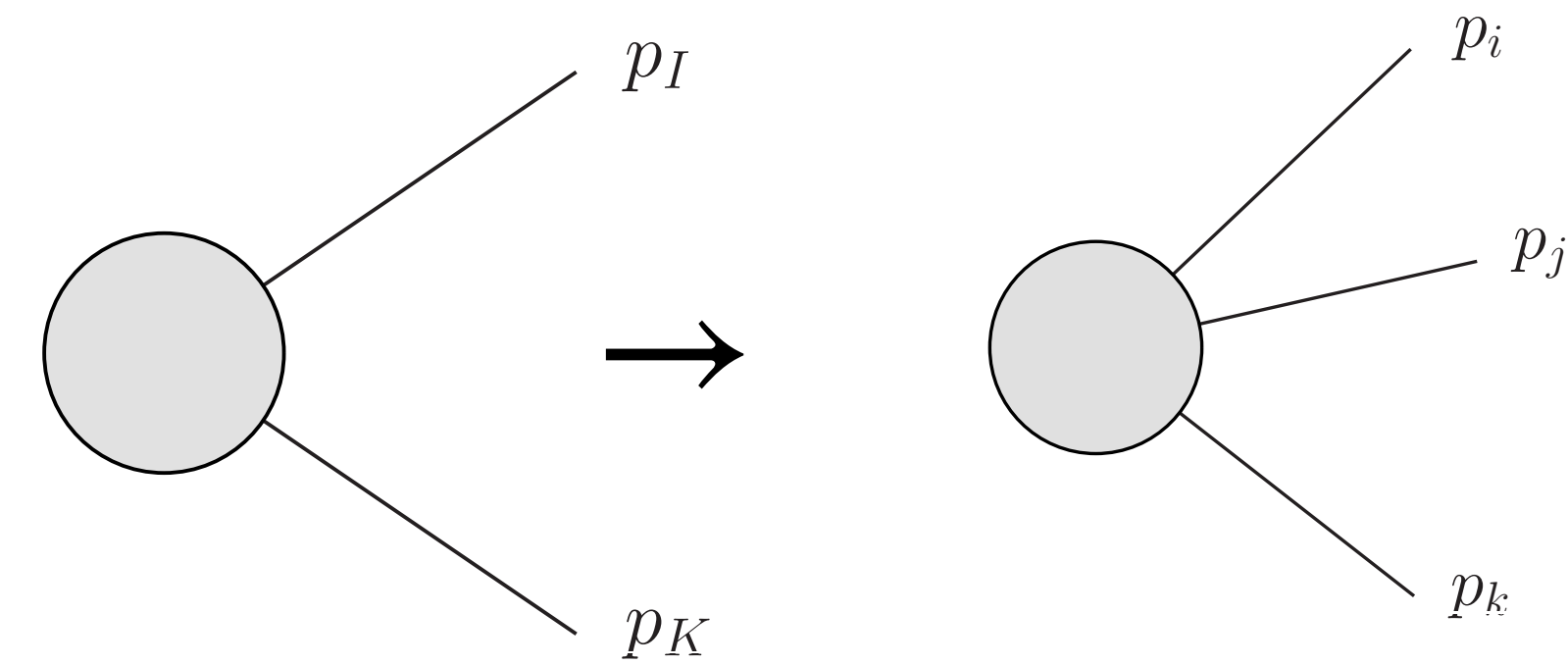
# Main Ingredients

## 1. Phase space factorisation

$$d\Phi_{n+1} = d\Phi_n \times d\Phi_{\text{ps}}$$



Comes with a **kinematic map**



## 2. Ordering scale

$$p_{\perp}^2(\Phi_{\text{ps}})$$

1. Momentum conservation

2. IR safety

## 3. Branching kernel

$$|M_{n+1}(\Phi_{n+1})|^2 \approx \sum_i B_i(\Phi_{\text{ps}}) \times |M_n(\Phi_n)|^2$$

# Parton Showers

Branching kernel (real corrections)



$$P_i(\Phi_{ps,i}) = B(\Phi_{ps,i}) \Theta(p_{\perp,i}^2 < p_{\perp,i-1}^2) \times \Delta(p_{\perp,i-1}^2, p_{\perp,i}^2)$$

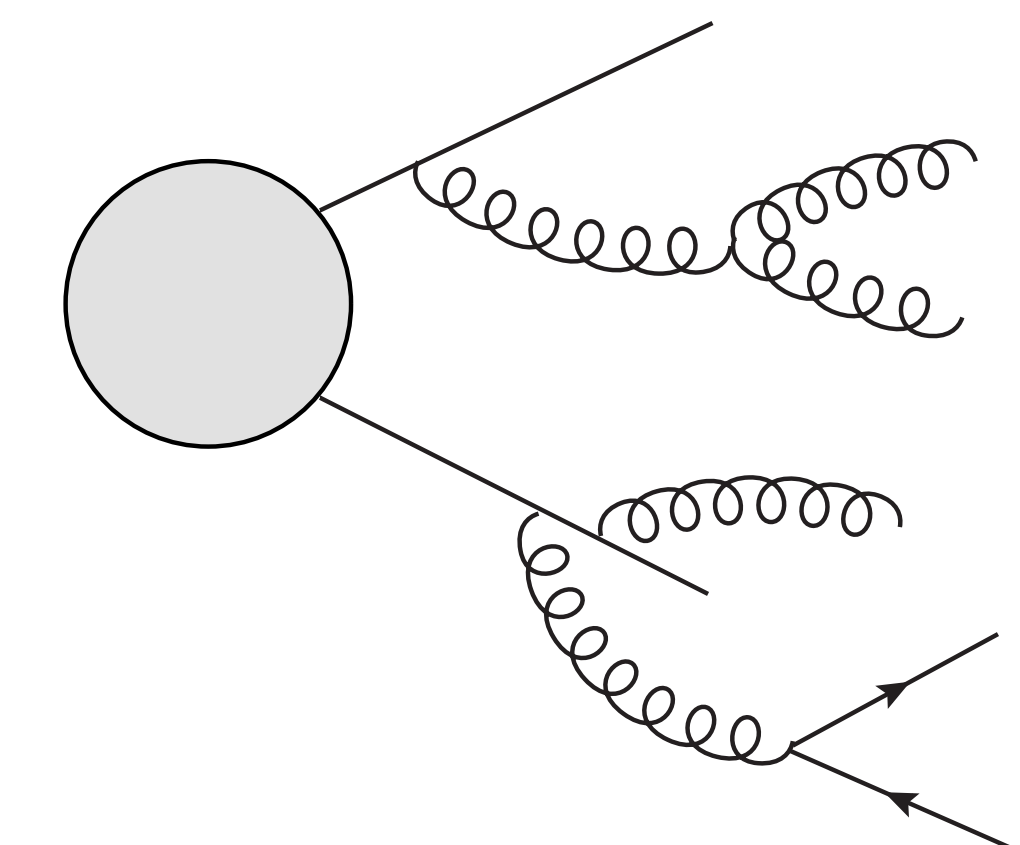
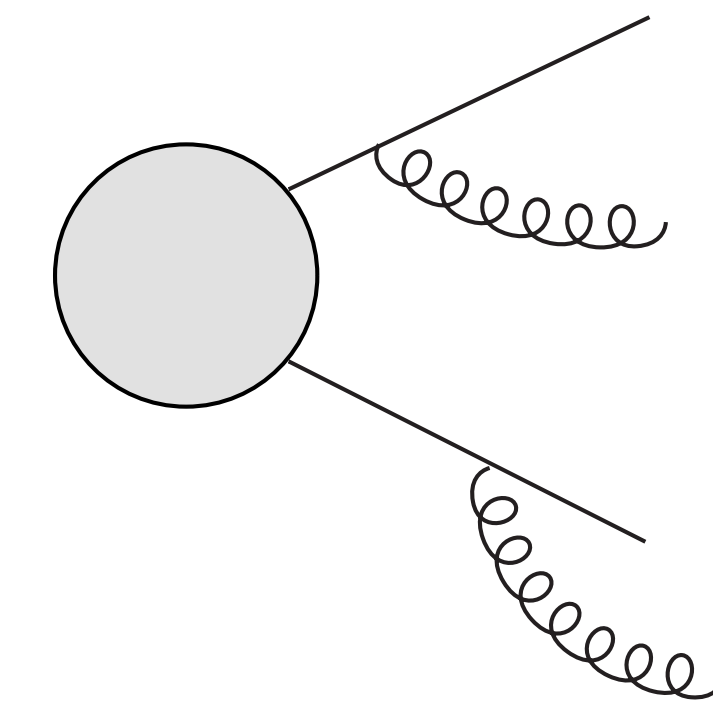
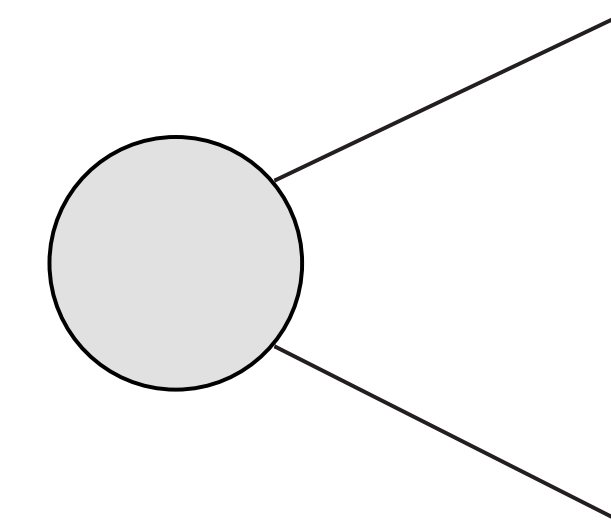


Sudakov factor (virtual corrections)

$$\Delta(p_{\perp,i-1}^2, p_{\perp,i}^2) = \exp \left( - \int_{p_{\perp,i}^2}^{p_{\perp,i-1}^2} d\Phi_{ps} B(\Phi_{ps}) \right)$$

Parton shower is *unitary*:  
cancellation of real and virtual corrections  
→  $\sigma_{inc}$  unaltered

$$p_{\perp} \approx Q_{fac}$$



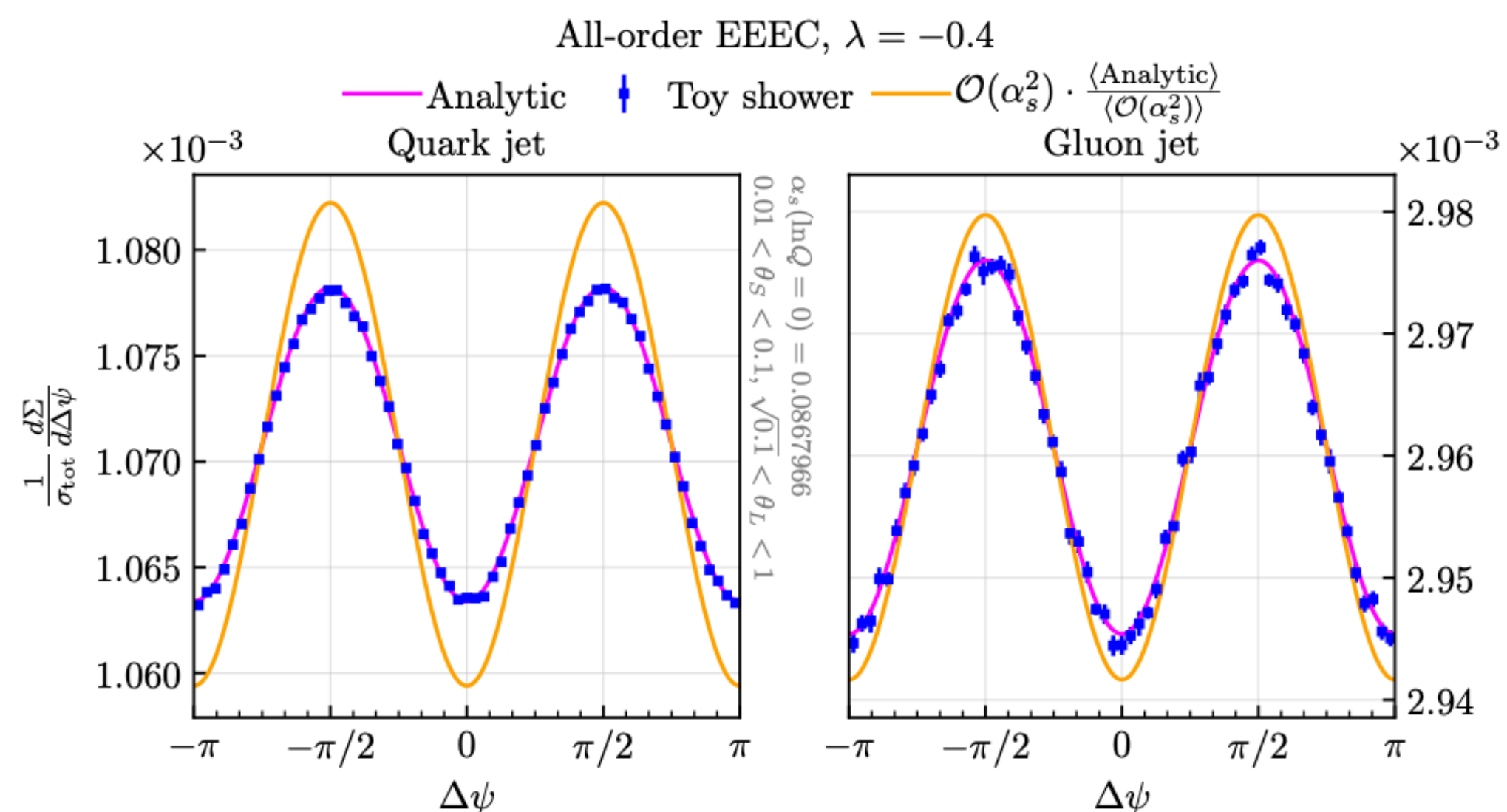
$$p_{\perp} \approx \Lambda_{QCD}$$



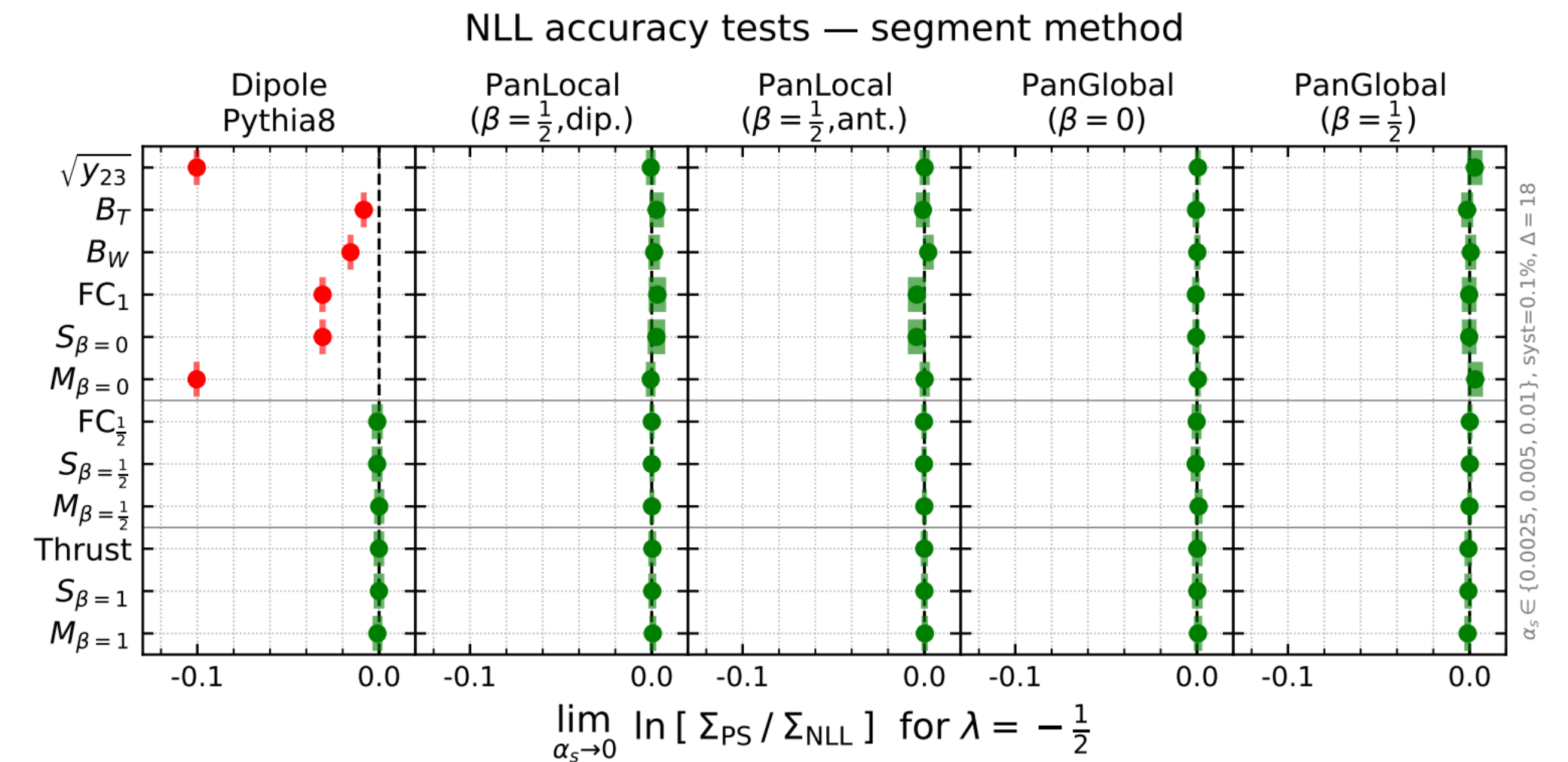


# Parton Shower Accuracy

- Formal NLL accuracy  
[Dasgupta, Dreyer, Hamilton, Monni, Salam, Soyez 2002.11114](#)  
[Nagy, Soper 2011.04773](#)  
[Forshaw, Holguin, Platzer 2003.06400](#)
- Inclusion of higher-order branching kernels  
 → Requirement for NNLL  
[Hoche, Krauss, Prestel 1705.00982](#)  
[Li, Skands 1611.00013](#)
- Spin correlations  
[Karlberg, Salam, Scyboz, RV 1611.00013](#)  
[Richardson, Webster 1807.01955](#)



- Subleading colour effects  $1/N_c^2 \sim 10\%$   
[Hamilton, Medves, Salam, Scyboz, Soyez 2011.10054](#)  
[Nagy, Soper 1501.00778](#)  
[Platzer, Sjo Dahl, Thoren 1808.00332](#)  
[Forshaw, Holguin, Platzer 1905.08686](#)  
[Isaacson, Prestel 1806.10102](#)



- Electroweak corrections  $\alpha/\alpha_s \sim 10\%$   
[Christiansen, Sjostrand arXiv:1401.5238](#)  
[Krauss, Petrov, Schoenherr, Spannowsky arXiv:1403.4788](#)  
[Chen, Han, Tweedie arXiv:1611.00788](#)  
[Kleiss, RV 2002.09248](#)

→ Rest of the talk

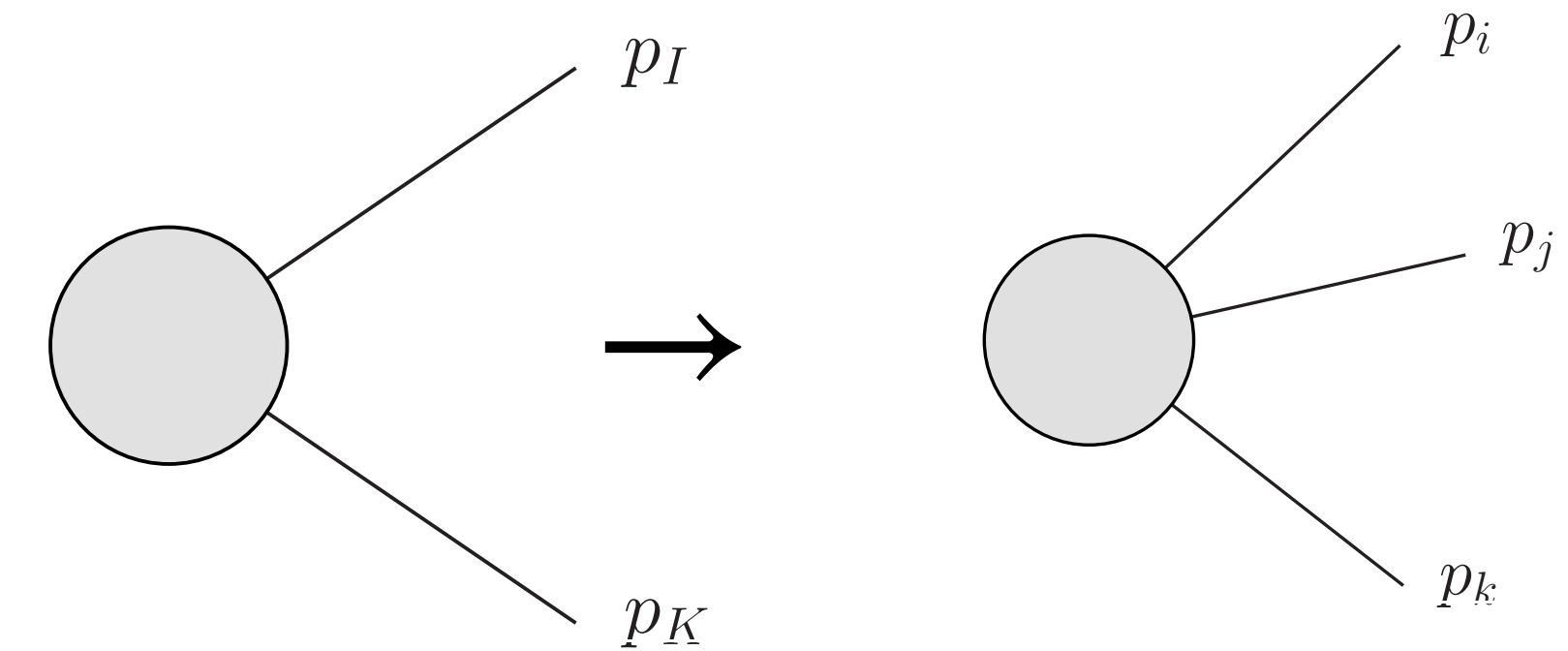
# Vincia: Three ingredients

$$s_{ab} = 2p_a \cdot p_b$$

$$m_{ab}^2 = (p_a + p_b)^2$$

## 1. Phase space factorisation

$$d\Phi_{\text{ps}} = \frac{1}{16\pi^2} \lambda^{\frac{1}{2}}(m_{IK}^2, m_I^2, m_K^2) ds_{ij} ds_{jk} \frac{d\varphi}{2\pi}$$

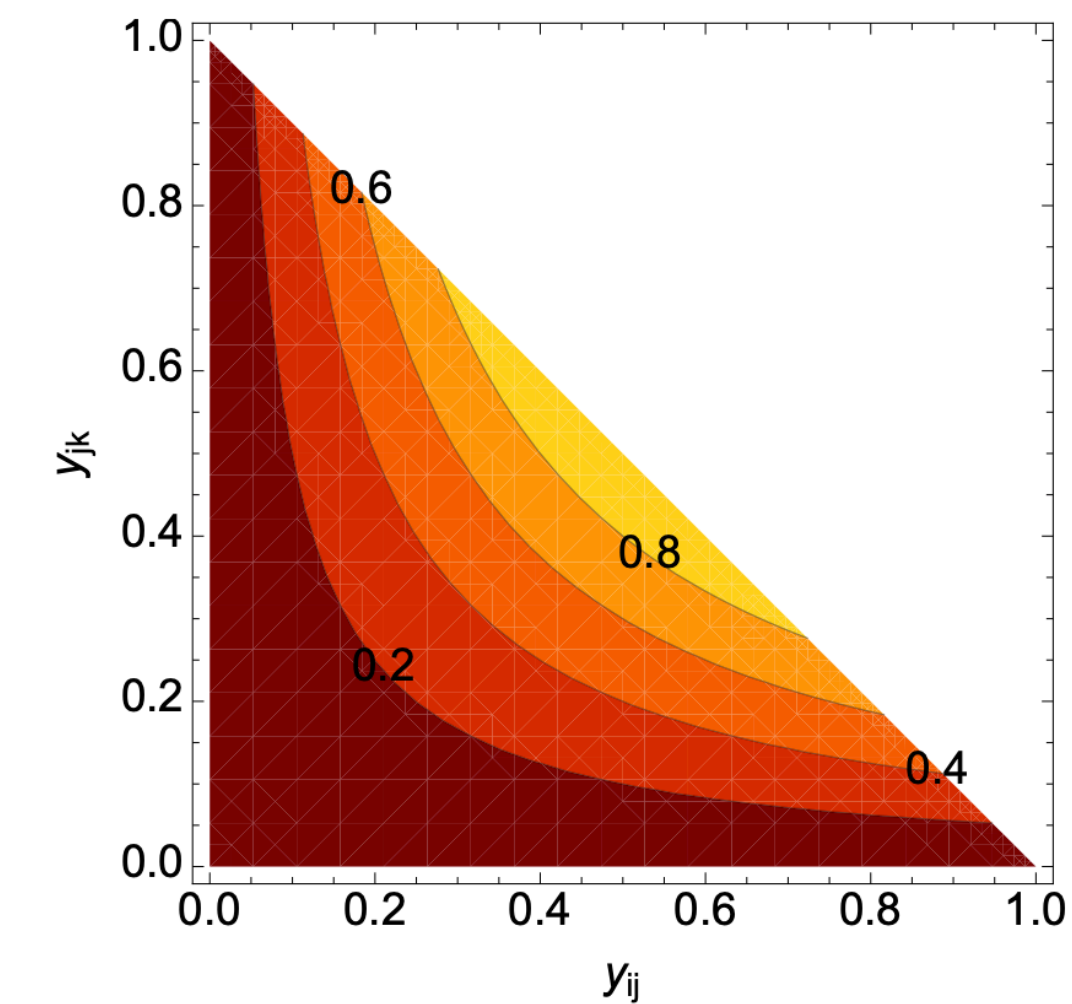


## 2. Ordering scale: Ariadne $p_{\perp}^2$

$$p_{\perp}^2 = \frac{s_{ij}s_{jk}}{s_{IK}}$$

## 3. Branching kernel: Antenna functions

$$a_{q\bar{q}}(s_{ij}, s_{jk}) = 4\pi\alpha_s C_F \left( 2 \frac{s_{ik}}{s_{ij}s_{jk}} - 2 \frac{m_i^2}{s_{ij}^2} - 2 \frac{m_k^2}{s_{jk}^2} + \frac{1}{s_{IK}} \left( \frac{s_{ij}}{s_{jk}} + \frac{s_{jk}}{s_{ij}} \right) \right)$$

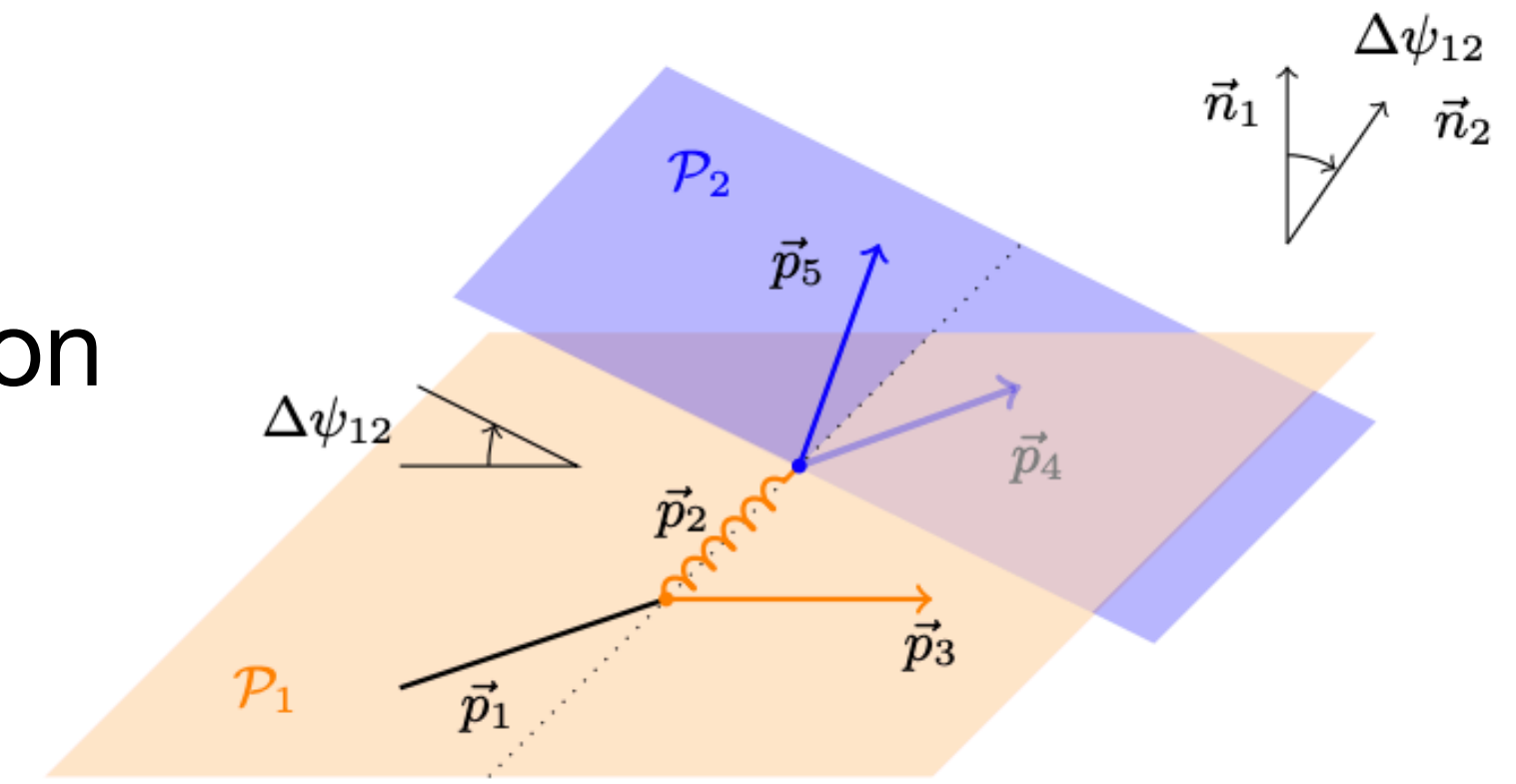


# Side note: Spin interference

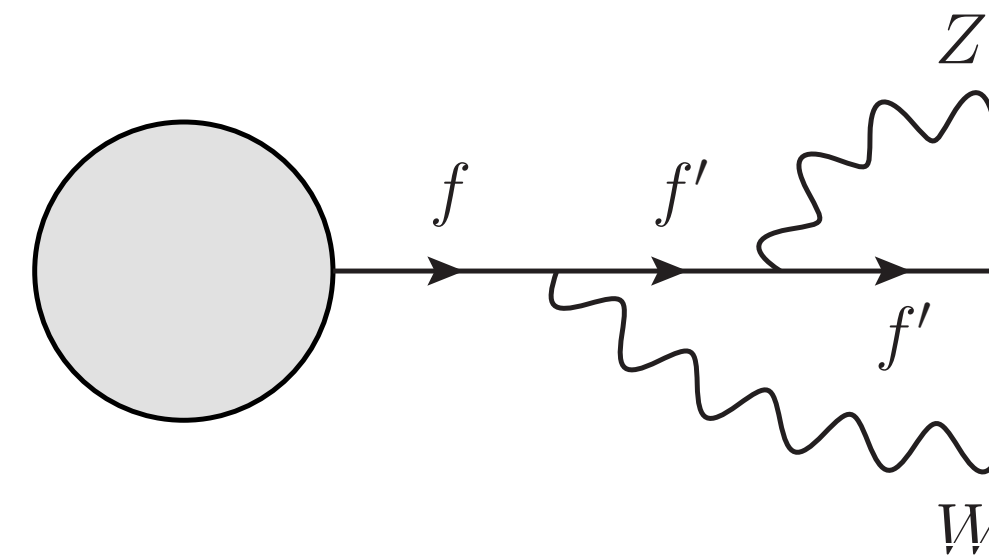
- In QCD, spin interference effects only lead to azimuthal modulation  
 → Integrates out of the Sudakov

$$\Delta(p_{\perp,i-1}^2, p_{\perp,i}^2) = \exp \left( - \int_{p_{\perp,i}^2}^{p_{\perp,i-1}^2} d\Phi_{ps} B(\Phi_{ps}) \right)$$

$\uparrow$   
 Azimuthal integral

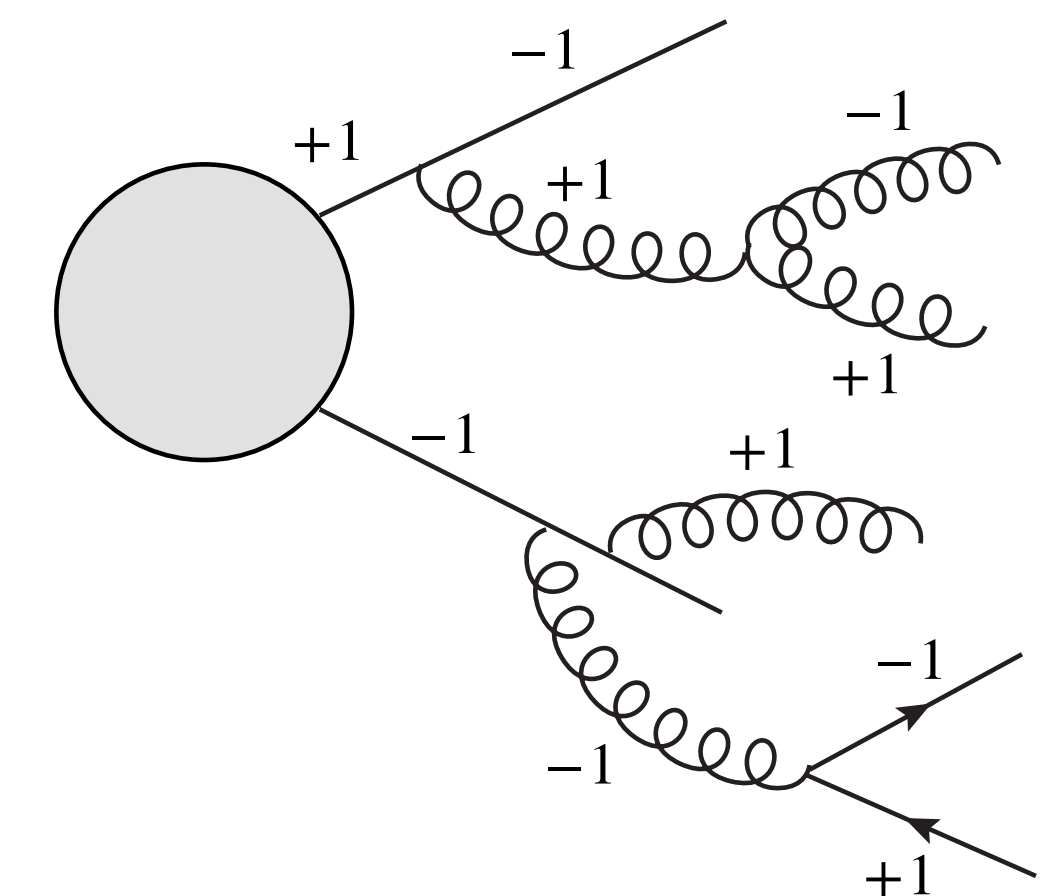


- In EW, spin influences the rate of emissions  
 → Does not integrate out of the Sudakov



Vincia's solution: Evolution of intermediate helicity states

- Should capture leading effects
- Needs separate branching kernels for every spin configuration



# Electroweak Showering

# Why EW Showers?

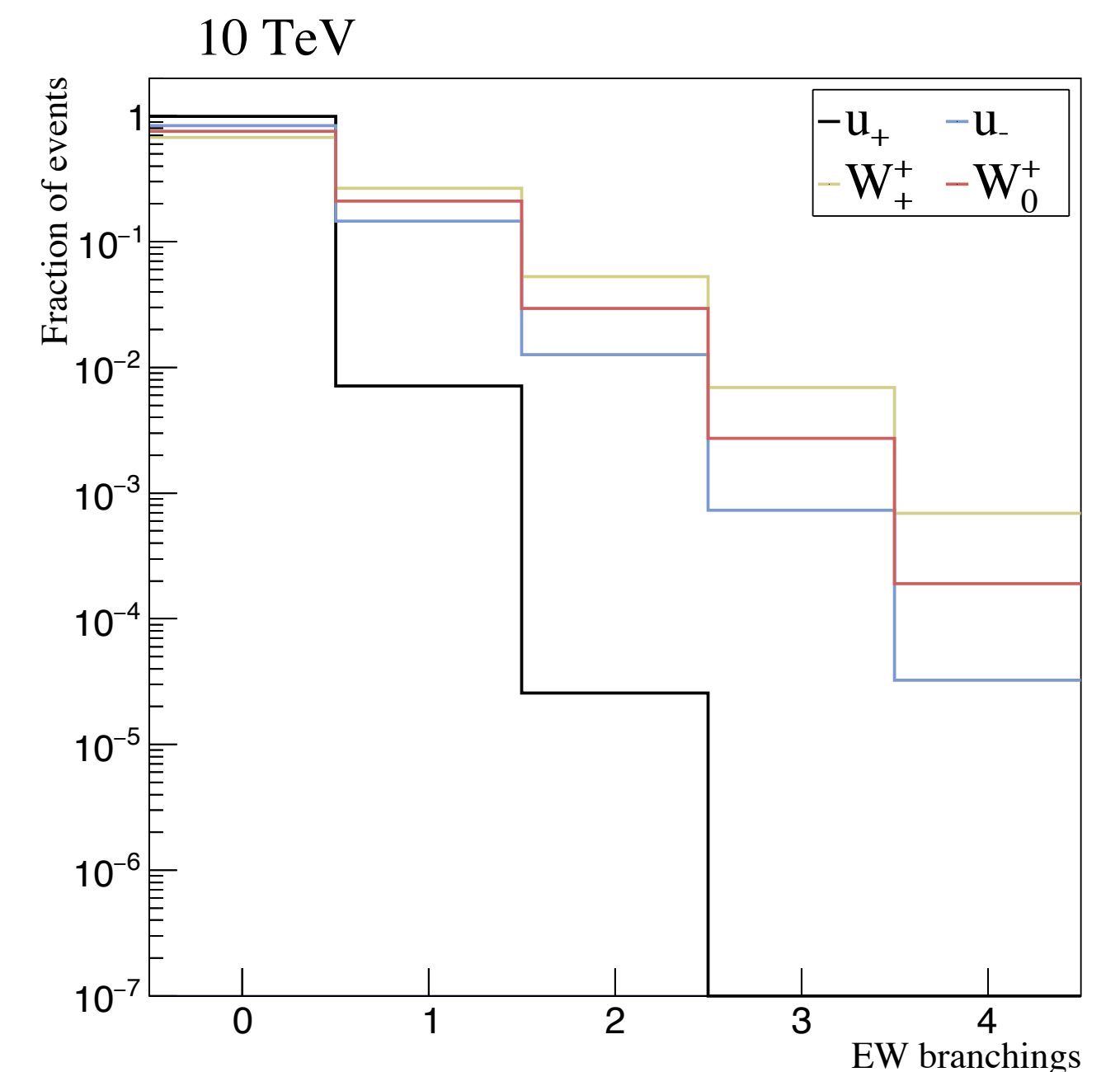
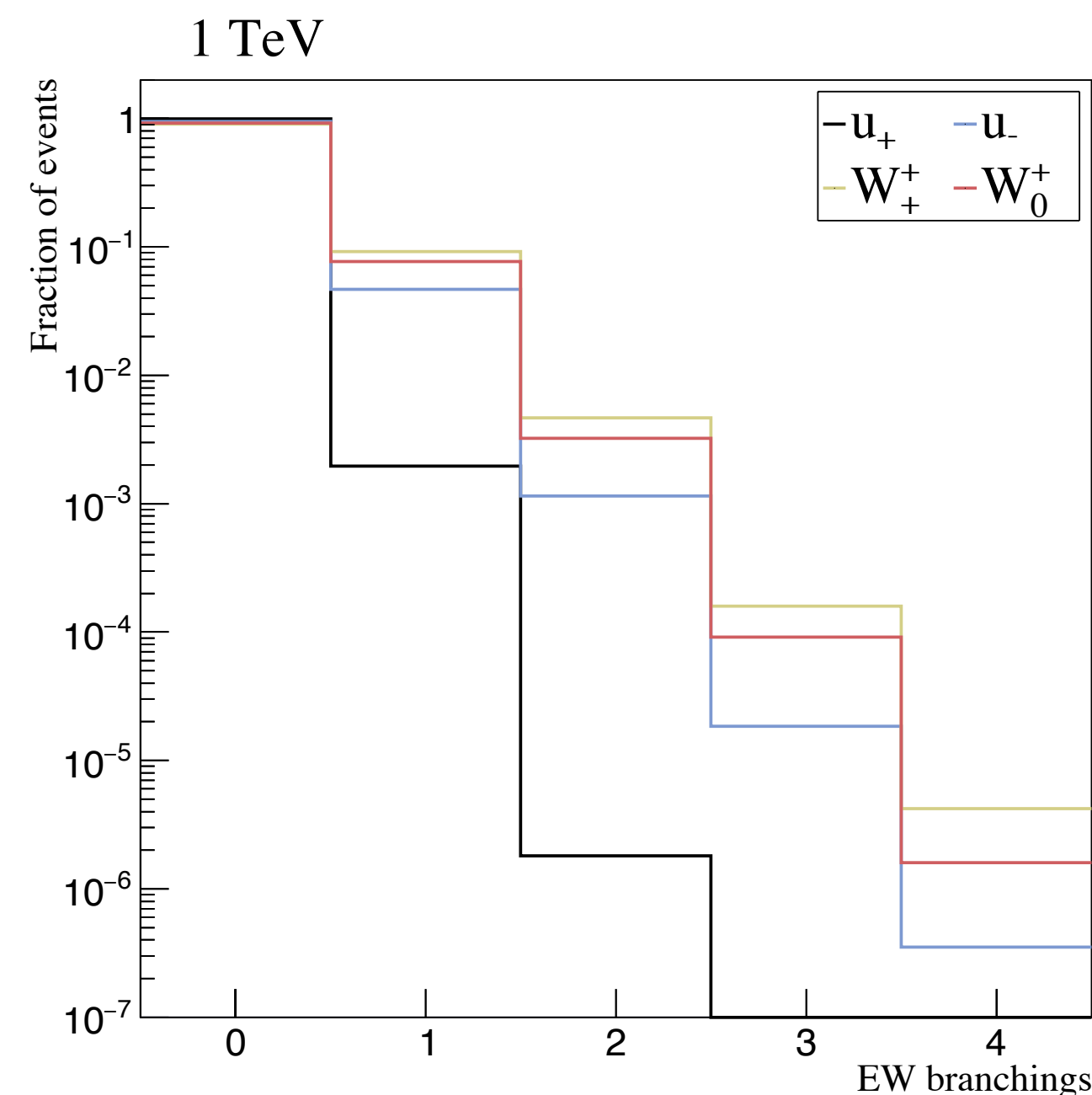
- Real corrections: EW gauge bosons, tops, Higgs part of jets
- Virtual corrections: Universal incorporation of Sudakov logs  $\frac{\alpha}{\pi} \ln^2 (s/Q_{EW}^2)$

## Applications

- (HL)-LHC [ATLAS 1609.07045](#)
  - Future colliders
  - DM spectra [Bauer, Rodd, Webber 2007.15001](#)
- Results later

## Existing implementations

- Only vector boson emissions [Christiansen, Sjostrand arXiv:1401.5238](#)  
[Krauss, Petrov, Schoenherr, Spannowsky arXiv:1403.4788](#)
- Full-fledged EW shower [Chen, Han, Tweedie arXiv:1611.00788](#)



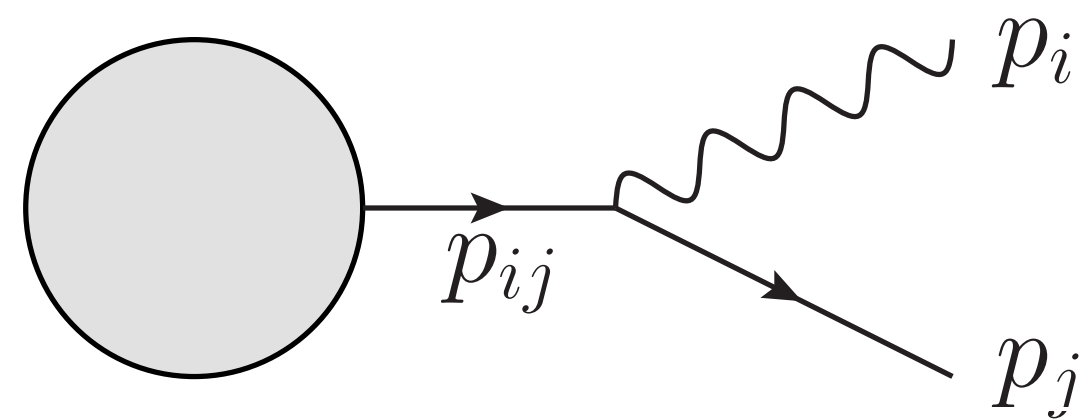
# Electroweak Branching Kernels

Use spinor-helicity formalism

$$M_{\lambda_{ij}, \lambda_i, \lambda_j}(p_i, p_j) = \begin{array}{c} p_i, \lambda_i \\ \diagup \\ p_{ij}, \lambda_{ij} \\ \diagdown \\ p_j, \lambda_j \end{array}$$

Transform to Vincia phase space

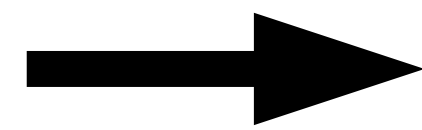
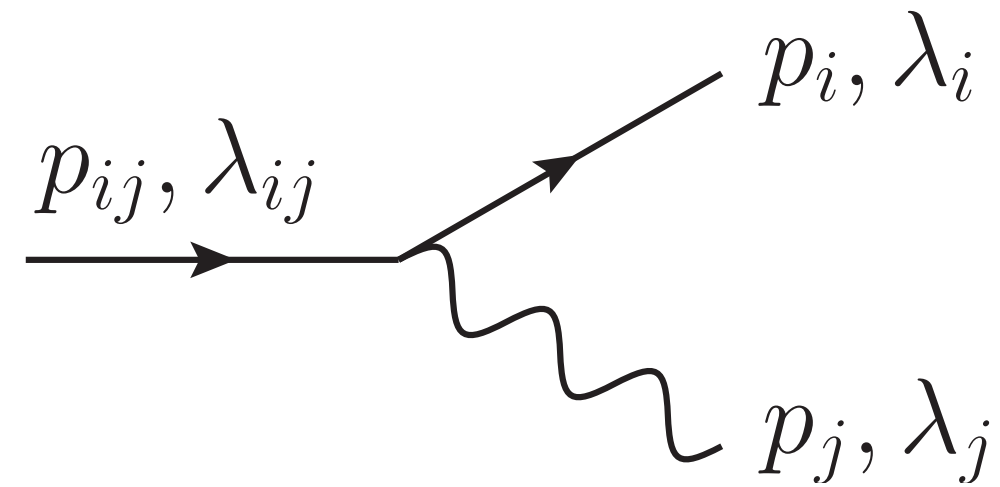
$$a_{\lambda_{ij}, \lambda_i, \lambda_j}(s_{ij}, s_{jk}) = \left[ \left| \frac{1}{Q^2} M_{\lambda_{ij}, \lambda_i, \lambda_j}(p_i, p_j) \right|^2 \right]_{(1-z) \rightarrow x_j}^{z \rightarrow x_i}$$



$$x_i = \frac{s_{ij} + s_{ik} + m_i^2}{m_{IK}^2} \quad x_j = \frac{s_{ij} + s_{jk} + m_j^2}{m_{IK}^2}$$

$$Q^2 = s_{ij} + m_i^2 + m_j^2 - m_{ij}^2$$

# Longitudinal Polarisation

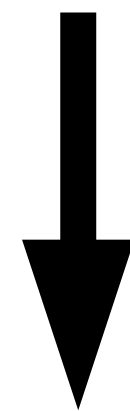
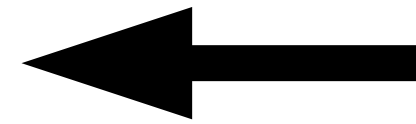


$$M_{\lambda_{ij}, \lambda_i, \lambda_j}(p_i, p_j) = \bar{u}_{\lambda_i}(p_i)(v + a\gamma^5)\not{\epsilon}_{\lambda_j}(p_j)u_{\lambda_{ij}}(p_{ij})$$

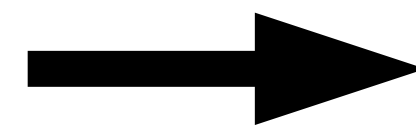


1. Insert spinor representations
2. Consider longitudinal polarisation
3. Do some Dirac algebra

$$M_{+,+,0}(p_i, p_j) \propto \frac{1}{m_j} \left( (Q^2 + m_{ij}^2)\not{p}_{ij} - m_i^2\not{p}_{ij} \right)$$



$Q^2$  drops out

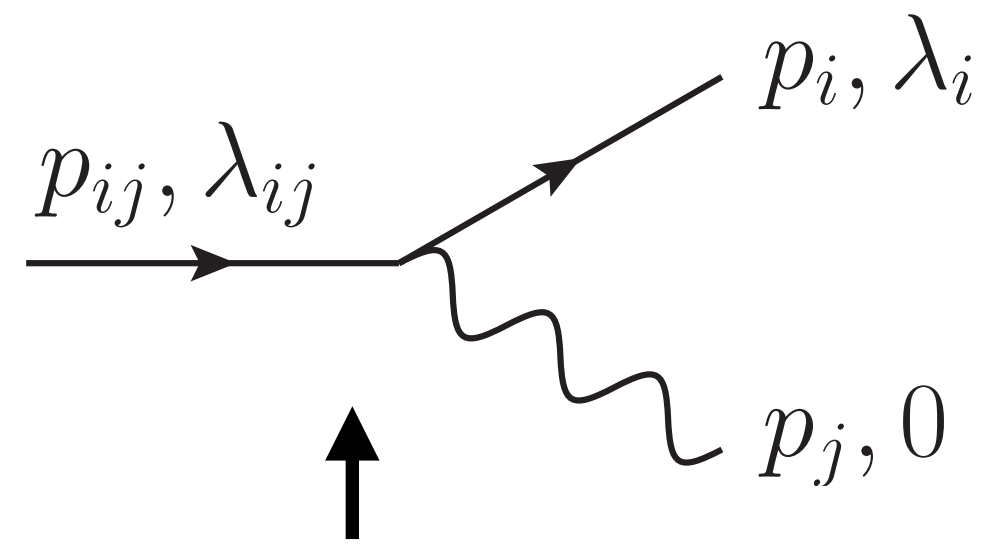


Unitarity violation

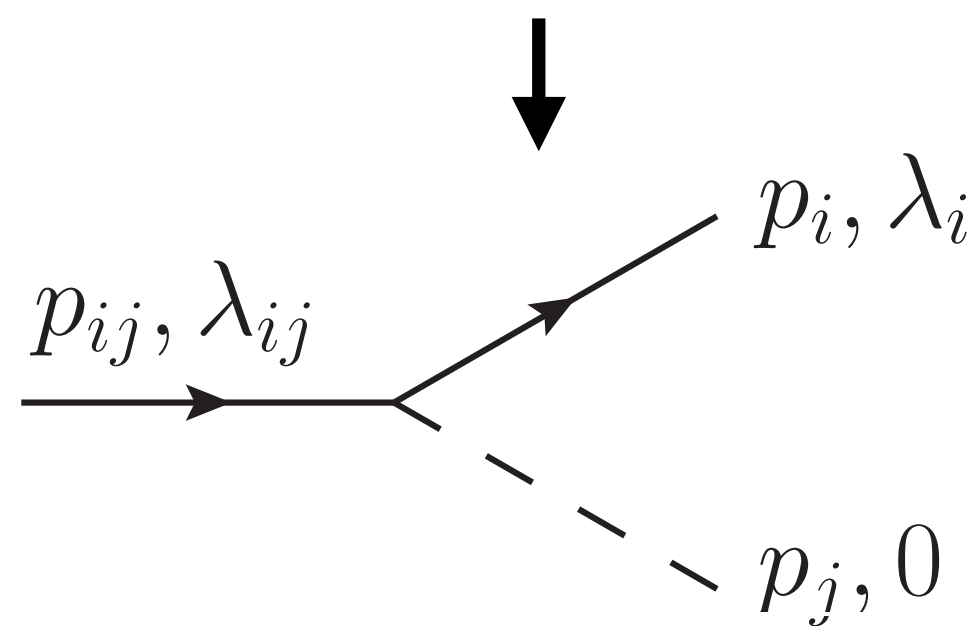


???

# Goldstone Bosons



$$\epsilon_0^\mu(p) = \frac{1}{m} \left( p^\mu - \frac{m^2}{p \cdot k} k^\mu \right)$$



**Goldstone piece actually couples to Yukawa**

Possible to solve with Goldstone equivalence and suitable gauge choice

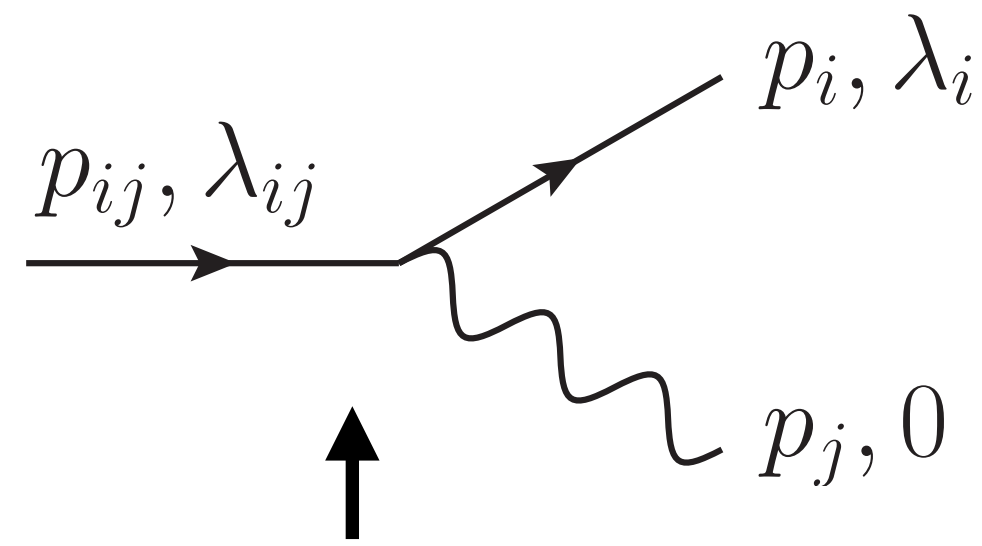
Spinor helicity formalism enables much simpler solution:

$$\frac{1}{m_j} \left( (Q^2 + m_{ij}^2) \not{p}_i - m_i^2 \not{p}_{ij} \right)$$

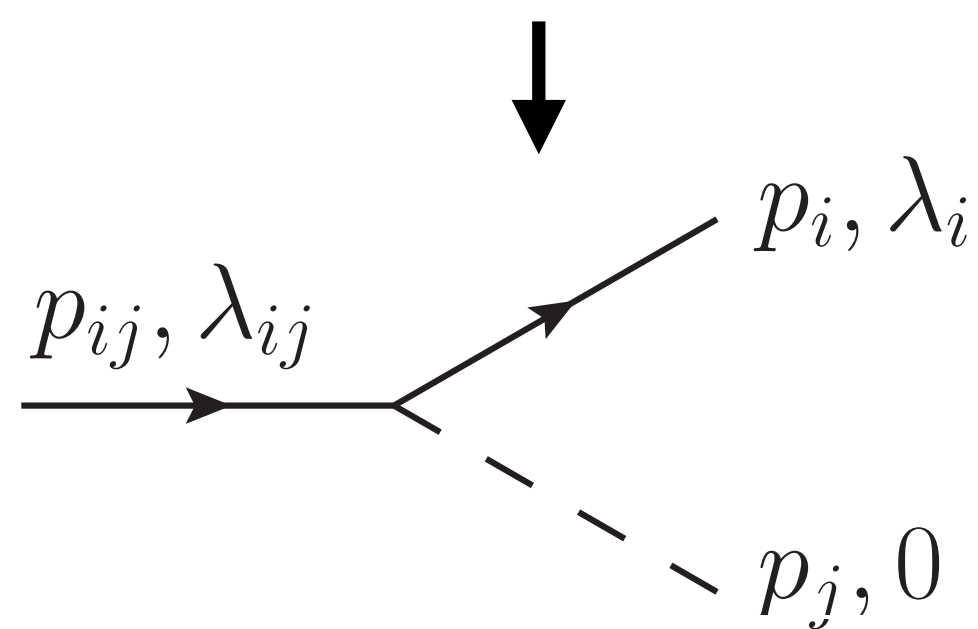
Yukawa couplings   
 ↑                    ↑   
 Off-shellness



# Goldstone Bosons



$$\epsilon_0^\mu(p) = \frac{1}{m} \left( p^\mu - \frac{m^2}{p \cdot k} k^\mu \right)$$



**Goldstone piece actually couples to Yukawa**

Possible to solve with Goldstone equivalence and suitable gauge choice

Spinor helicity formalism enables much simpler solution:

Yukawa couplings

$$\frac{1}{m_j} \left( \cancel{m_j^2} + m_{ij}^2 \right) \not{p}_i - m_i^2 \not{p}_{ij}$$

↓  
Off-shellness

# Collinear Limits

$\lambda_I$	$\lambda_i$	$\lambda_j$	$V \rightarrow f\bar{f}'$
$\lambda$	$\lambda$	$-\lambda$	$\sqrt{2}\lambda(v - \lambda a)\sqrt{\tilde{Q}^2}z$
$\lambda$	$-\lambda$	$\lambda$	$\sqrt{2}\lambda(v + \lambda a)\sqrt{\tilde{Q}^2}(1 - z)$
$\lambda$	$\lambda$	$\lambda$	$\sqrt{2}\lambda\left[m_i(v + \lambda a)\sqrt{\frac{1-z}{z}} + m_j(v - \lambda a)\sqrt{\frac{z}{1-z}}\right]$
$\lambda$	$-\lambda$	$-\lambda$	0
0	$\lambda$	$\lambda$	$\sqrt{\tilde{Q}^2}\left[\frac{m_i}{m_{ij}}(v + \lambda a) + \frac{m_j}{m_{ij}}(v - \lambda a)\right]$
0	$\lambda$	$-\lambda$	$(v - \lambda a)\left[2m_{ij}\sqrt{z(1-z)} - \frac{m_i^2}{m_{ij}}\sqrt{\frac{1-z}{z}} - \frac{m_j^2}{m_{ij}}\sqrt{\frac{z}{1-z}}\right] + (v + \lambda a)\frac{m_i m_j}{m_{ij}}\frac{1}{\sqrt{z(1-z)}}$

$\lambda_{ij}$	$\lambda_i$	$\lambda_j$	$f \rightarrow f'V$ and $\bar{f} \rightarrow \bar{f}'V$
$\lambda$	$\lambda$	$\lambda$	$\sqrt{2}\lambda(v - \lambda a)\sqrt{\tilde{Q}^2}\frac{1}{\sqrt{1-z}}$
$\lambda$	$\lambda$	$-\lambda$	$\sqrt{2}\lambda(v - \lambda a)\sqrt{\tilde{Q}^2}\frac{z}{\sqrt{1-z}}$
$\lambda$	$-\lambda$	$\lambda$	$\sqrt{2}\lambda\left[m_{ij}(v - \lambda a)\sqrt{z} - m_i(v + \lambda a)\frac{1}{\sqrt{z}}\right]$
$\lambda$	$-\lambda$	$-\lambda$	0
$\lambda$	$\lambda$	0	$(v - \lambda a)\left[\frac{m_{ij}^2}{m_j}\sqrt{z} - \frac{m_i^2}{m_j}\frac{1}{\sqrt{z}} - 2m_j\frac{\sqrt{z}}{1-z}\right] + (v + \lambda a)\frac{m_i m_{ij}}{m_j}\frac{1-z}{\sqrt{z}}$
$\lambda$	$-\lambda$	0	$\sqrt{\tilde{Q}^2}\sqrt{1-z}\left[\frac{m_i}{m_j}(v - \lambda a) - \frac{m_{ij}}{m_j}(v + \lambda a)\right]$

$\lambda_I$	$\lambda_i$	$(f \rightarrow fh$ and $\bar{f} \rightarrow \bar{f}h) \times \frac{e}{2s_w} \frac{m_f}{m_w}$
$\lambda$	$\lambda$	$m_f\left[\sqrt{z} + \frac{1}{\sqrt{z}}\right]$
$\lambda$	$-\lambda$	$\sqrt{1-z}\sqrt{\tilde{Q}^2}$

$\lambda_I$	$\lambda_i$	$V \rightarrow Vh \times g_h$
$\lambda$	$\lambda$	-1
$\lambda$	$-\lambda$	0
0	$\lambda$	$\frac{1}{m_{ij}}\frac{\lambda}{\sqrt{2}}\sqrt{\tilde{Q}^2}\sqrt{z(1-z)}$
$\lambda$	0	$\frac{1}{m_i}\frac{\lambda}{\sqrt{2}}\sqrt{\tilde{Q}^2}\sqrt{\frac{1-z}{z}}$
0	0	$\frac{1}{2}\frac{m_j^2}{m_i^2} + \frac{1-z}{z} + z$

$\lambda_i$	$\lambda_i$	$h \rightarrow VV \times g_V$
$\lambda$	$\lambda$	0
$\lambda$	$-\lambda$	-1
0	$\lambda$	$\frac{1}{m_i}\frac{\lambda}{\sqrt{2}}\sqrt{\tilde{Q}^2}\sqrt{\frac{1-z}{z}}$
$\lambda$	0	$\frac{1}{m_j}\frac{\lambda}{\sqrt{2}}\sqrt{\tilde{Q}^2}\sqrt{\frac{z}{1-z}}$
0	0	$\frac{1}{2}\frac{m_{ij}^2}{m_i^2} - 1 - \frac{1-z}{z} - \frac{z}{1-z}$

$\lambda_i$	$\lambda_j$	$h \rightarrow f\bar{f} \times \frac{e}{2s_w} \frac{m_f}{m_w}$
$\lambda$	$\lambda$	$\sqrt{\tilde{Q}^2}$
$\lambda$	$-\lambda$	$m_f\left[\sqrt{\frac{1-z}{z}} - \sqrt{\frac{z}{1-z}}\right]$

$\lambda_I$	$\lambda_i$	$\lambda_j$	$V \rightarrow V'V'' \times g_V$
$\lambda$	$\lambda$	$\lambda$	$\sqrt{2}\lambda\sqrt{\tilde{Q}^2}\sqrt{\frac{1}{z(1-z)}}$
$\lambda$	$\lambda$	$-\lambda$	$\sqrt{2}\lambda\sqrt{\tilde{Q}^2}z\sqrt{\frac{z}{1-z}}$
$\lambda$	$-\lambda$	$\lambda$	$\sqrt{2}\lambda\sqrt{\tilde{Q}^2}(1-z)\sqrt{\frac{1-z}{z}}$
$\lambda$	$-\lambda$	$-\lambda$	0
0	$\lambda$	$\lambda$	0
0	$\lambda$	$-\lambda$	$m_{ij}(2z - 1) + \frac{m_j^2}{m_{ij}} - \frac{m_i^2}{m_{ij}}$
$\lambda$	0	$\lambda$	$m_i\left(1 + 2\frac{1-z}{z}\right) + \frac{m_j^2}{m_i} - \frac{m_{ij}^2}{m_i}$
$\lambda$	0	$-\lambda$	0
$\lambda$	$\lambda$	0	$m_j\left(1 + 2\frac{z}{1-z}\right) + \frac{m_i^2}{m_j} - \frac{m_{ij}^2}{m_j}$
$\lambda$	$-\lambda$	0	0
$\lambda$	0	0	$\frac{\lambda}{\sqrt{2}}\frac{m_i^2 + m_j^2 - m_{ij}^2}{m_i m_j}\sqrt{\tilde{Q}^2}\sqrt{z(1-z)}$
0	$\lambda$	0	$\frac{\lambda}{\sqrt{2}}\frac{m_{ij}^2 + m_j^2 - m_i^2}{m_{ij} m_j}\sqrt{\tilde{Q}^2}\sqrt{\frac{1-z}{z}}$
0	0	$\lambda$	$\frac{\lambda}{\sqrt{2}}\frac{m_{ij}^2 + m_i^2 - m_j^2}{m_{ij} m_i}\sqrt{\tilde{Q}^2}\sqrt{\frac{z}{1-z}}$
0	0	0	$\frac{1}{2}\frac{m_{ij}^3}{m_i m_j}(2z - 1) - \frac{m_i^3}{m_{ij} m_j}\left(\frac{1}{2} + \frac{1-z}{z}\right) + \frac{m_j^3}{m_{ij} m_i}\left(\frac{1}{2} + \frac{z}{1-z}\right) + \frac{m_i m_j}{m_{ij}}\left(\frac{1-z}{z} - \frac{z}{1-z}\right) + \frac{m_{ij} m_i}{m_j}(1-z)\left(2 + \frac{1-z}{z}\right) - \frac{m_{ij} m_j}{m_i}z\left(2 + \frac{z}{1-z}\right)$

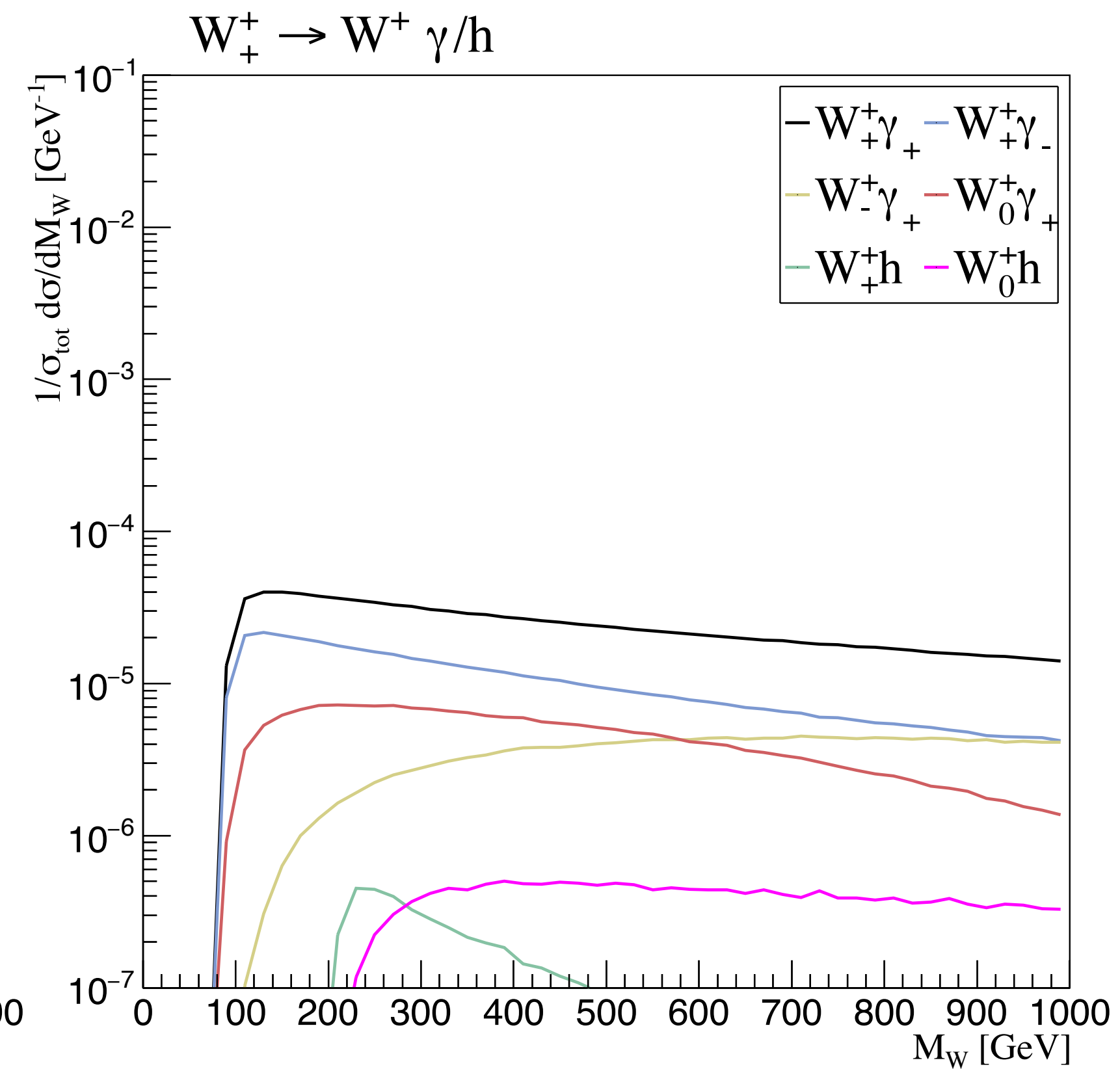
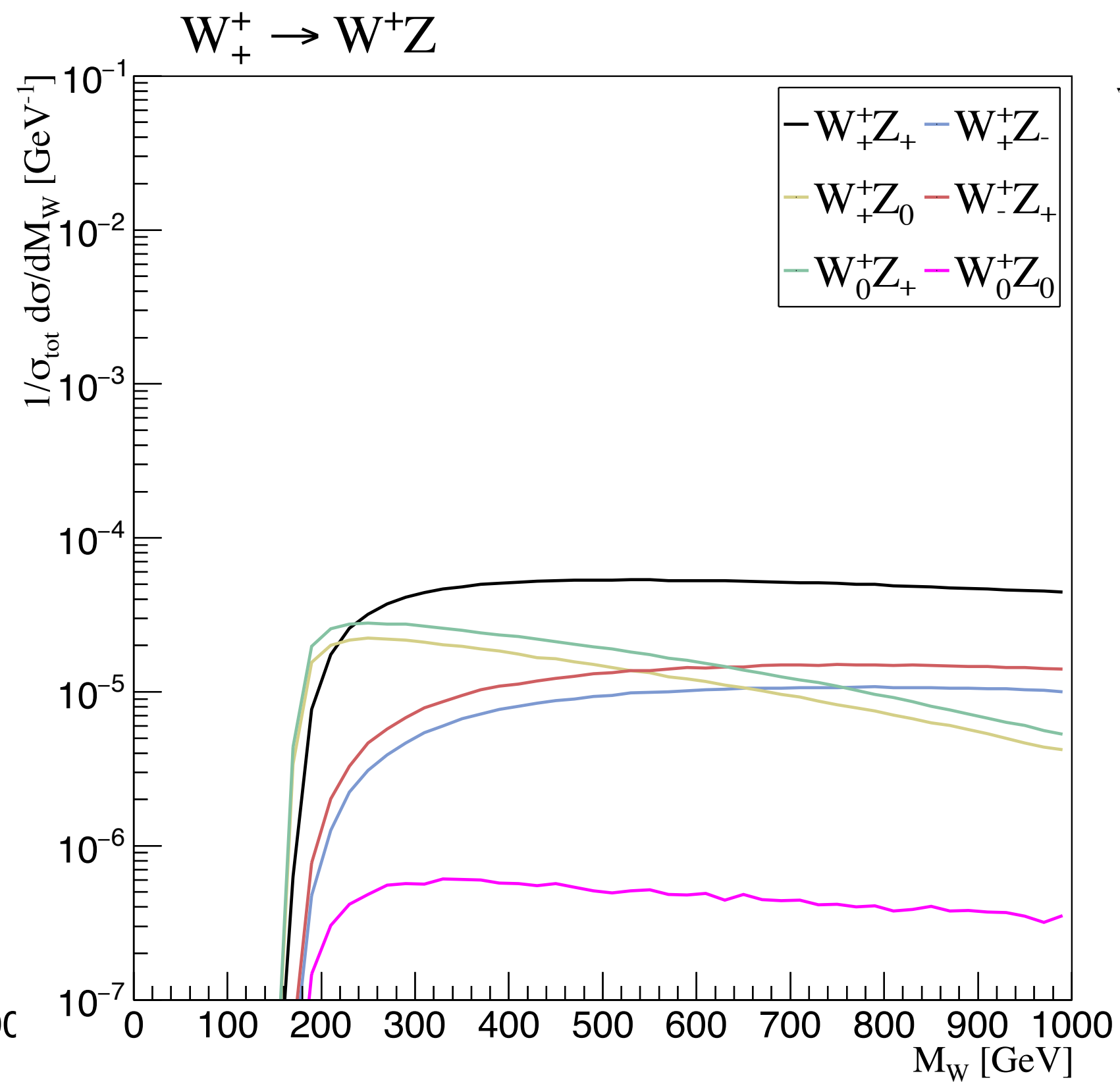
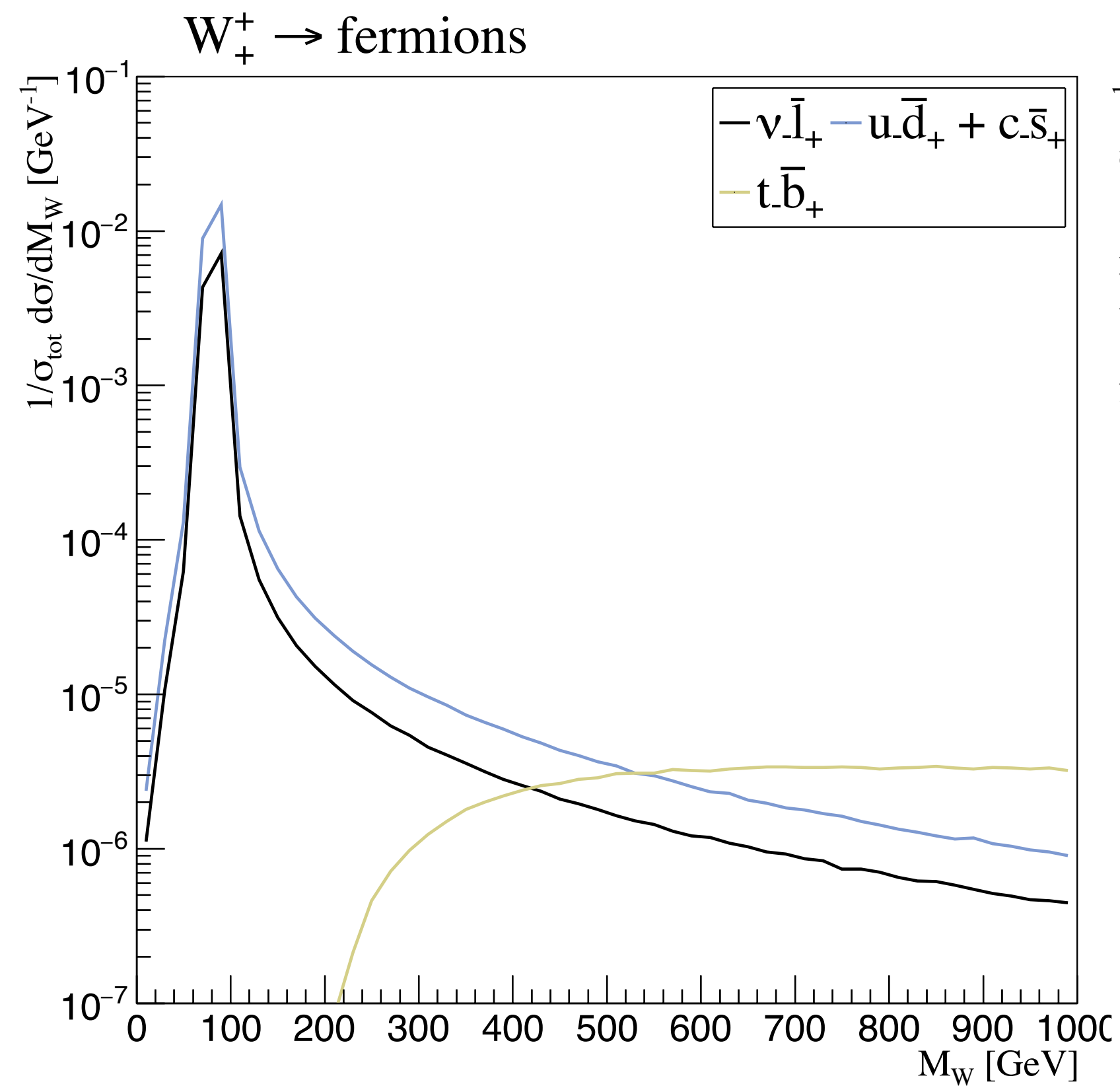
# Collinear Limits

$\lambda_{ij}$	$\lambda_i$	$\lambda_j$	$f \rightarrow f'V$ and $\bar{f} \rightarrow \bar{f}'V$	
$\lambda$	$\lambda$	$\lambda$	$\sqrt{2}\lambda(v - \lambda a)\sqrt{\tilde{Q}^2} \frac{1}{\sqrt{1-z}}$	$P(z) \propto \frac{\tilde{Q}^2}{Q^4} \frac{1+z^2}{1-z}$
$\lambda$	$\lambda$	$-\lambda$	$\sqrt{2}\lambda(v - \lambda a)\sqrt{\tilde{Q}^2} \frac{z}{\sqrt{1-z}}$	
$\lambda$	$-\lambda$	$\lambda$	$\sqrt{2}\lambda \left[ m_{ij}(v - \lambda a)\sqrt{z} - m_i(v + \lambda a)\frac{1}{\sqrt{z}} \right]$	$P(z) \propto \frac{m^2}{Q^4}$
$\lambda$	$-\lambda$	$-\lambda$	0	
$\lambda$	$\lambda$	0	$(v - \lambda a) \left[ \frac{m_{ij}^2}{m_j} \sqrt{z} - \frac{m_i^2}{m_j} \frac{1}{\sqrt{z}} - 2m_j \frac{\sqrt{z}}{1-z} \right]$ $+ (v + \lambda a) \frac{m_i m_{ij}}{m_j} \frac{1-z}{\sqrt{z}}$	
$\lambda$	$-\lambda$	0	$\sqrt{\tilde{Q}^2} \sqrt{1-z} \left[ \frac{m_i}{m_j} (v - \lambda a) - \frac{m_{ij}}{m_j} (v + \lambda a) \right]$	$P(z) \propto \frac{\tilde{Q}^2}{Q^4} (1-z)$

$$\tilde{Q}^2 = Q^2 + m_{ij}^2 - \frac{m_i^2}{z} - \frac{m_j^2}{1-z}$$

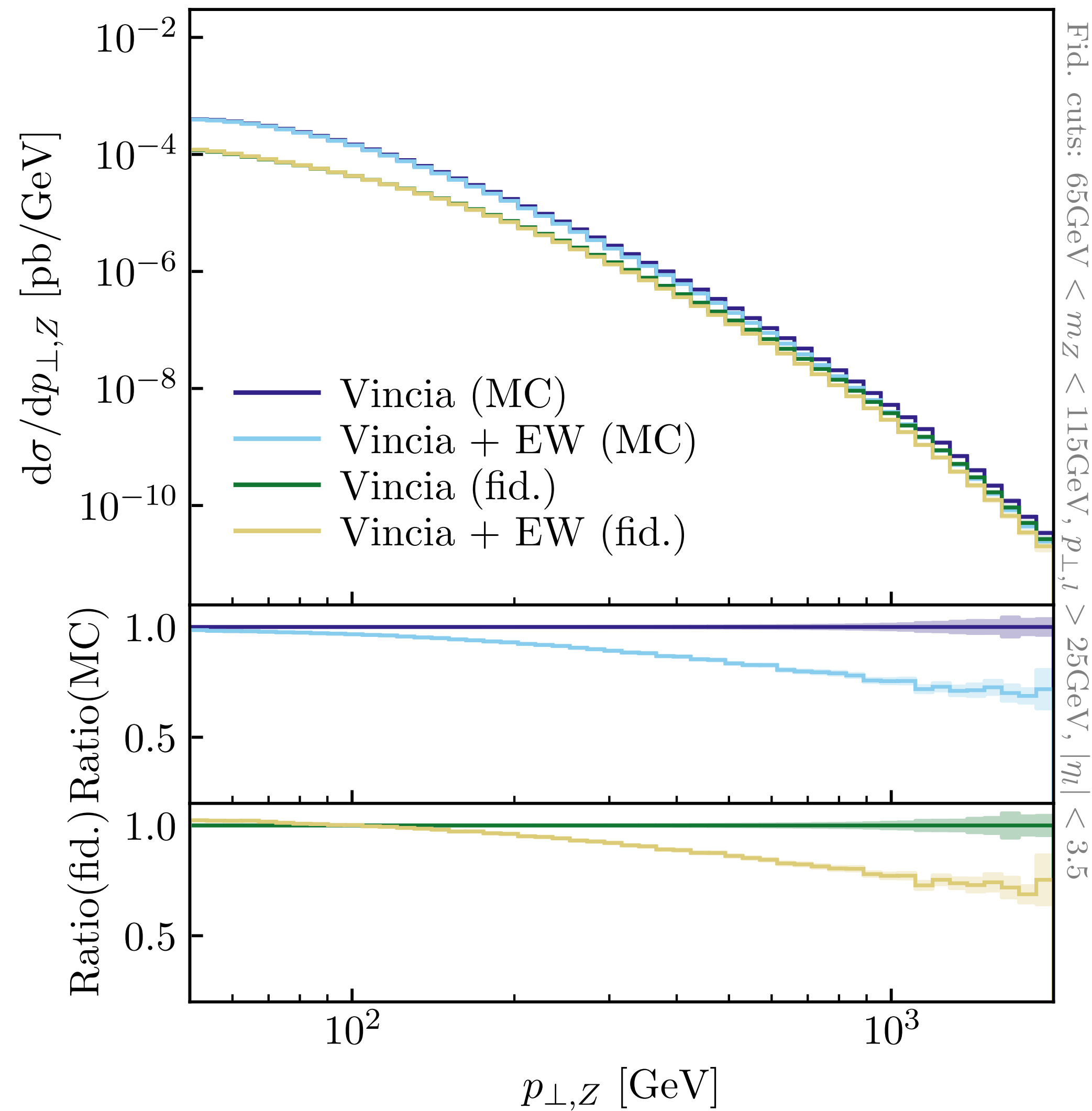
# The Electroweak Shower

$\mathcal{O}(1000)$  types of branchings (all FSR + ffV ISR)

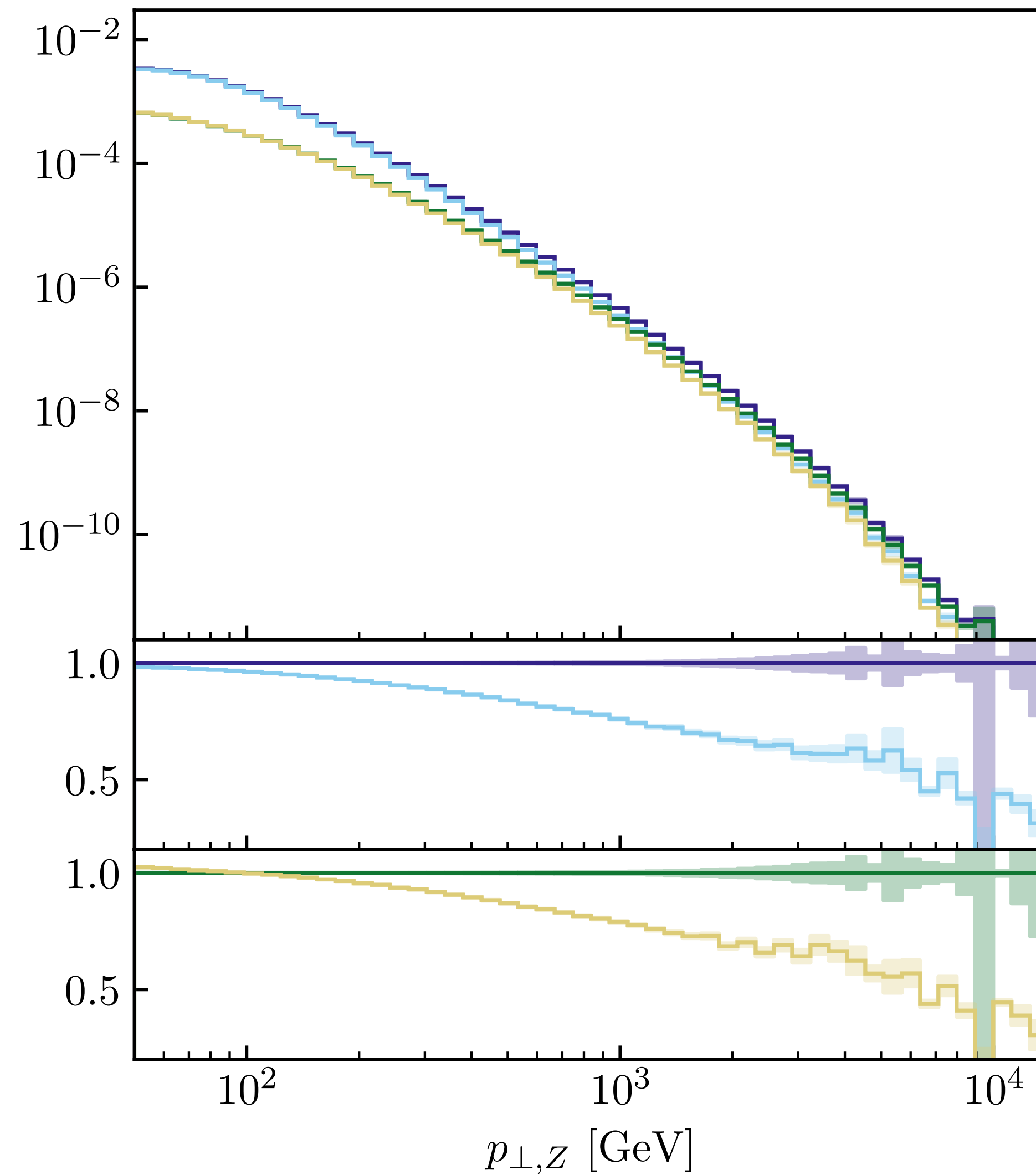


# Results: Virtual Sudakov logs

$pp \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^-$  (14 TeV)



$pp \rightarrow ZZ \rightarrow e^+e^-\mu^+\mu^-$  (100 TeV)

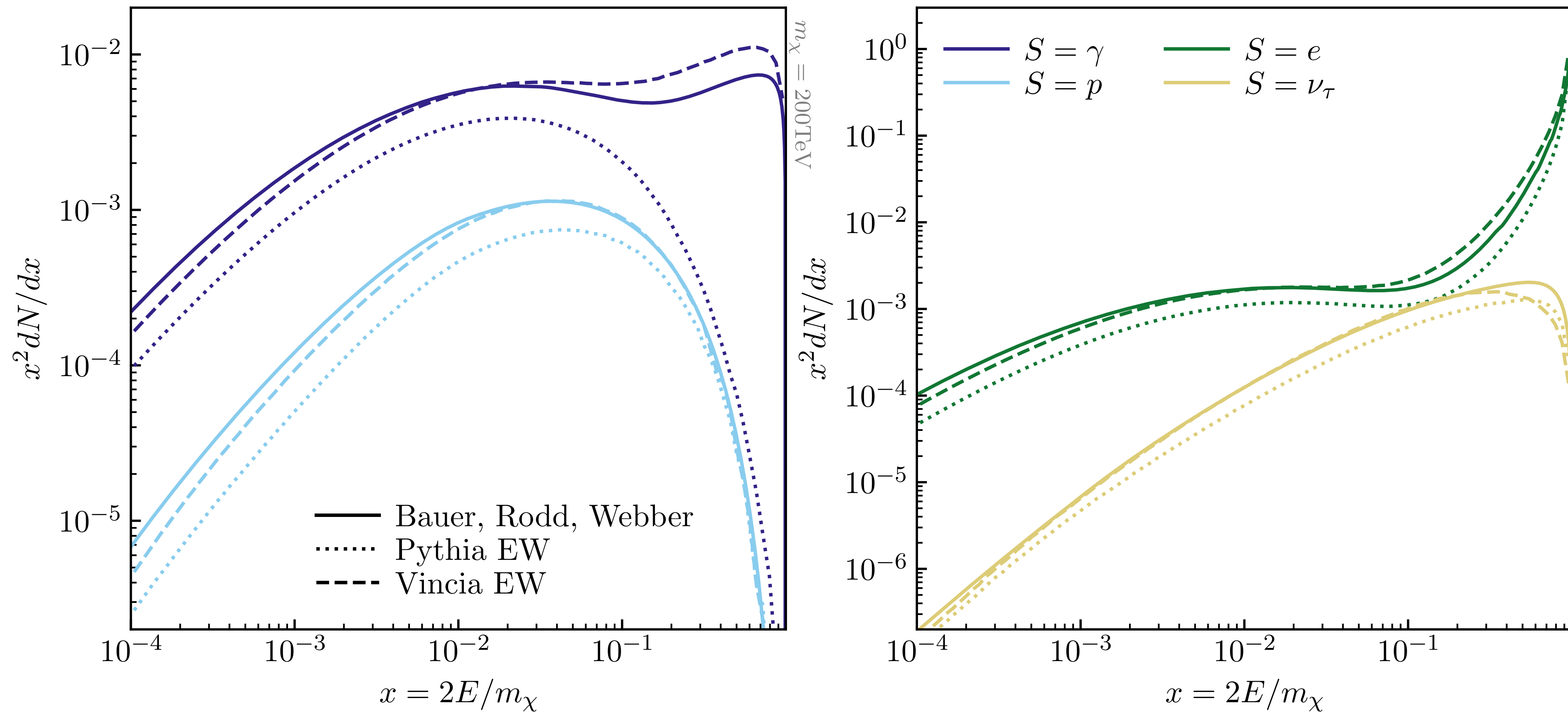


# Results: DM decay spectra

Comparison with analytic results

Bauer, Rodd, Webber 2007.15001

$$\chi \rightarrow \nu_e \bar{\nu}_e \rightarrow S$$



# Novel features in the Electroweak Sector

# Resonance Matching

Branchings like  $t \rightarrow bW$ ,  $Z \rightarrow q\bar{q}$  etc.

- Large scales:  
EW shower offers best description
- Small scales:  
Breit-Wigner distribution

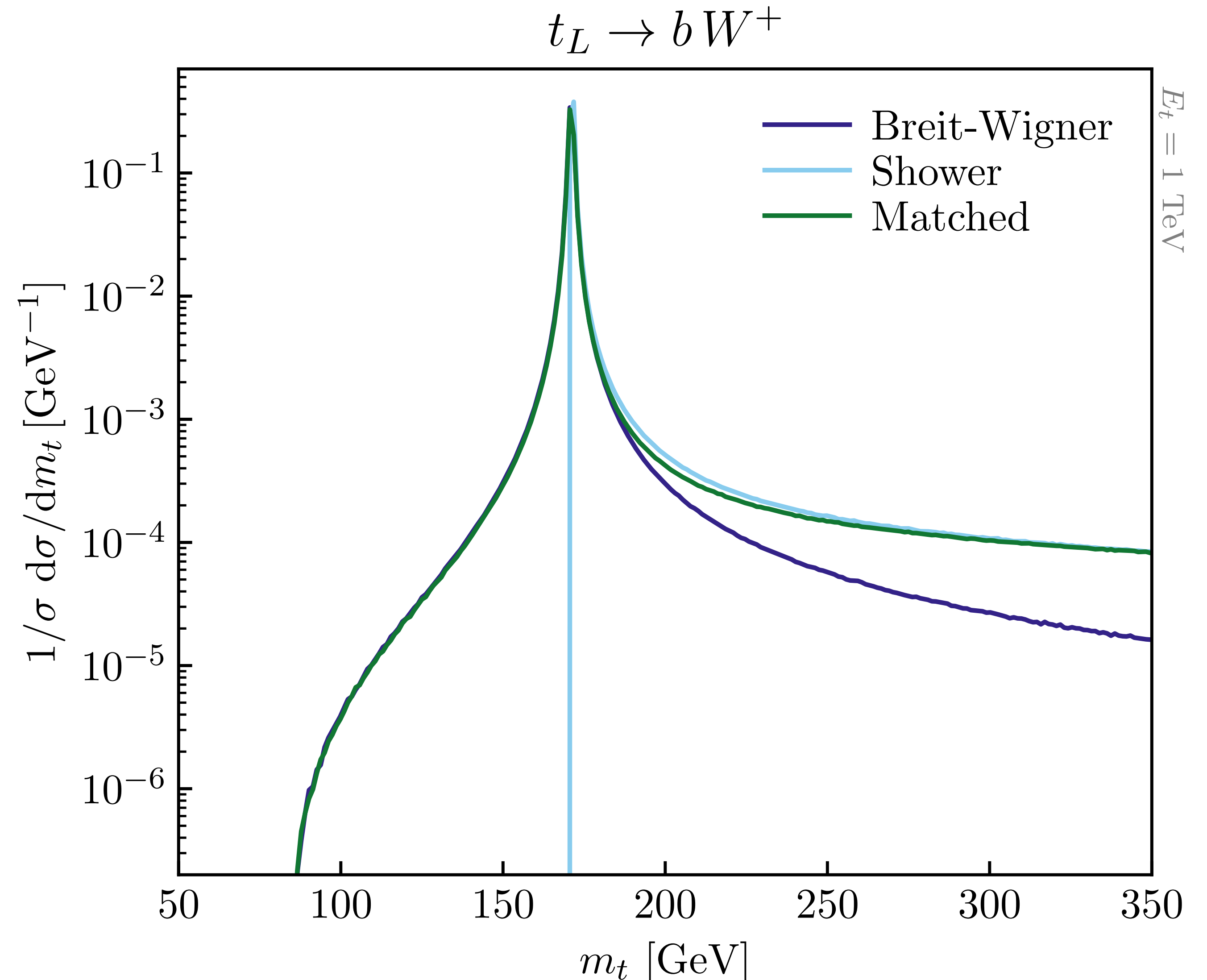
$$\text{BW}(Q^2) \propto \frac{m_0 \Gamma(m)}{Q^4 + m_0^2 \Gamma(m)^2}$$

**Matching:**

- Sample mass from Breit-Wigner upon production
- Suppress shower by factor

$$\frac{Q^4}{(Q^2 + Q_{\text{EW}}^2)^2}$$

- Decay when shower hits off-shellness scale

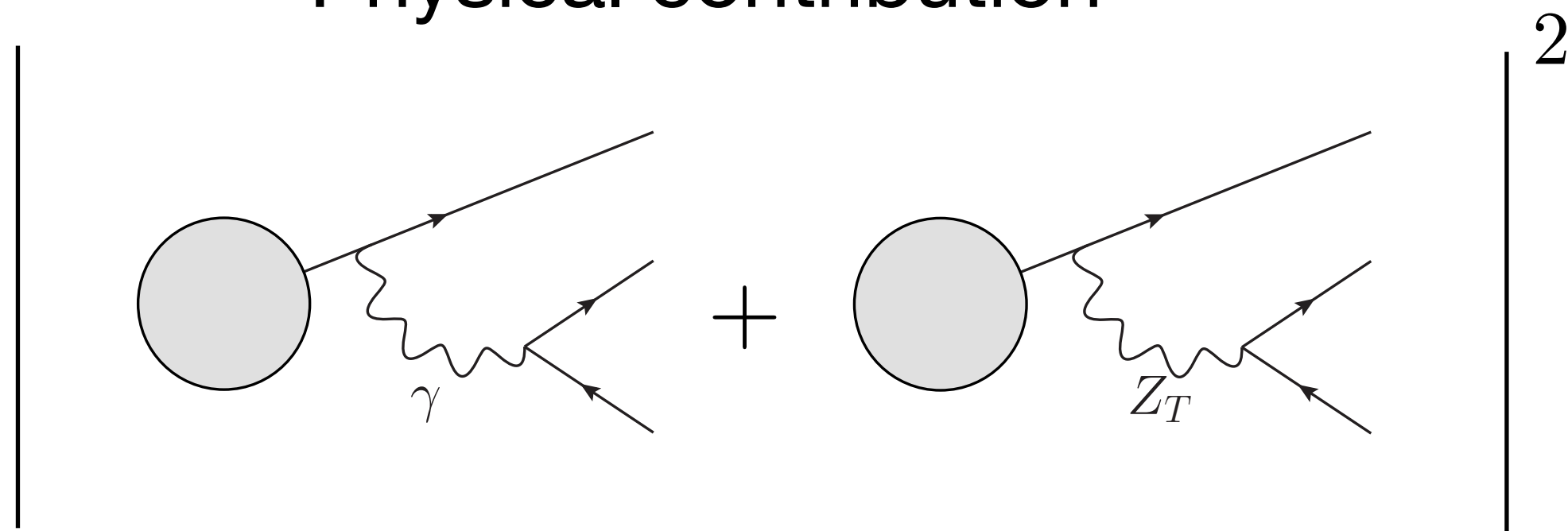




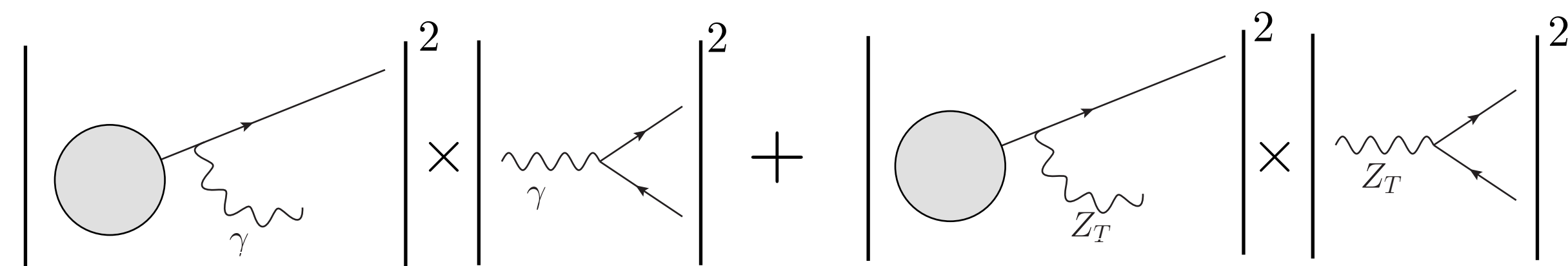
# Neutral Boson Interference

Interference between  $\gamma, Z_T$  and  $h, Z_L$

Physical contribution



Shower approximation

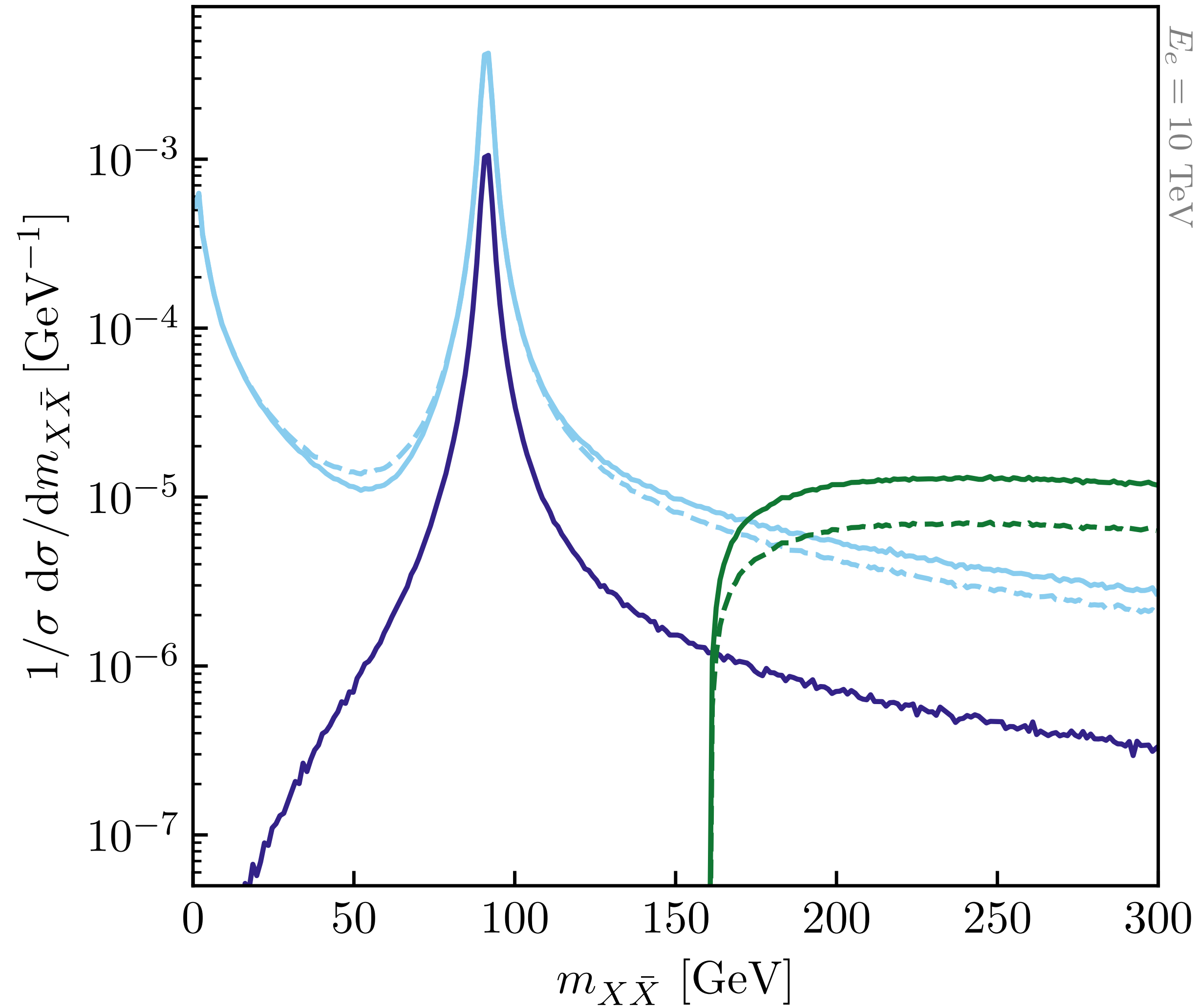


- Complicated solution: Evolve density matrices  
 → Very computationally expensive
- Simple solution: Apply event weight  
 → Does not get Sudakov right

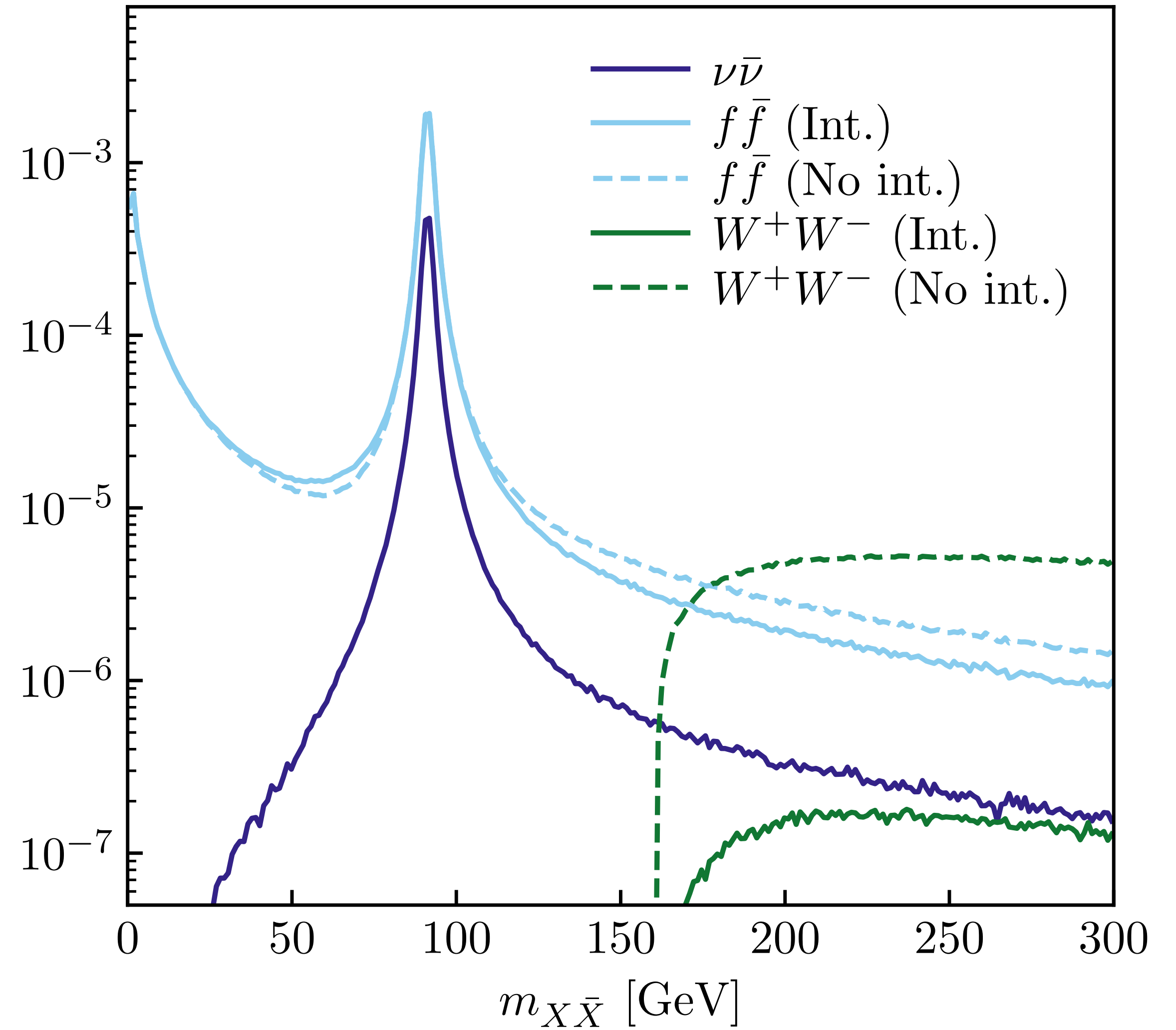
$$w = \frac{\left| \begin{array}{c} \text{grey circle} \\ \gamma \\ \times \\ \text{vertex} \end{array} \right|^2 + \left| \begin{array}{c} \text{grey circle} \\ Z_T \\ \times \\ \text{vertex} \end{array} \right|^2}{\left| \begin{array}{c} \text{grey circle} \\ \gamma \\ \times \\ \text{vertex} \end{array} \right|^2 + \left| \begin{array}{c} \text{grey circle} \\ Z_T \\ \times \\ \text{vertex} \end{array} \right|^2}$$

# Bosonic Interference

$$e_L \rightarrow e_L \gamma/Z_T \rightarrow e_L X \bar{X}$$

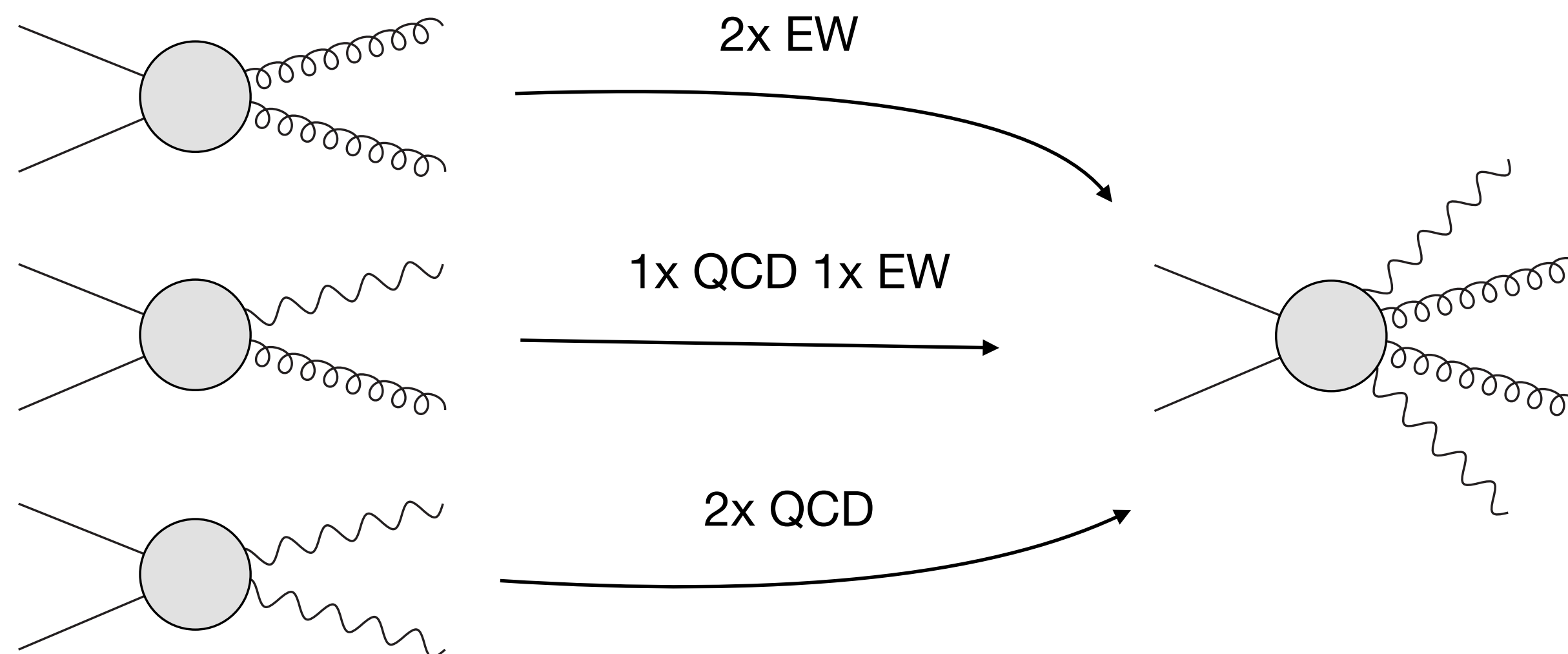


$$e_R \rightarrow e_R \gamma/Z_T \rightarrow e_R X \bar{X}$$

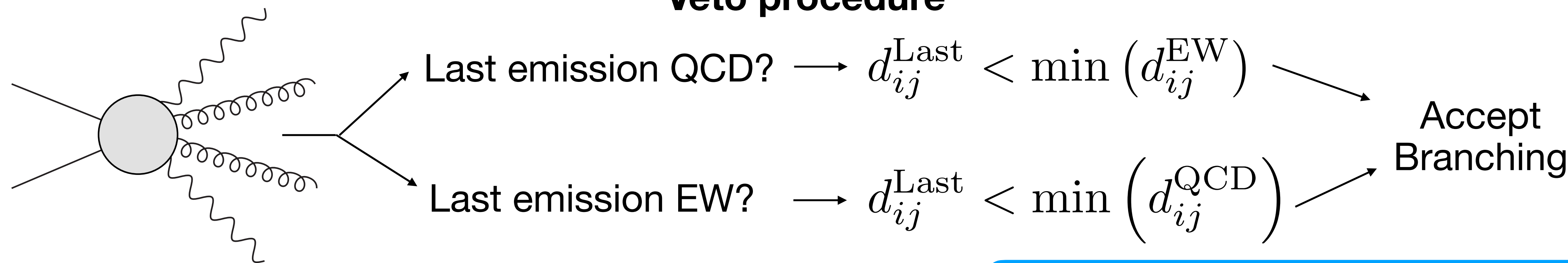


# Overlap Veto

## Double counting problem



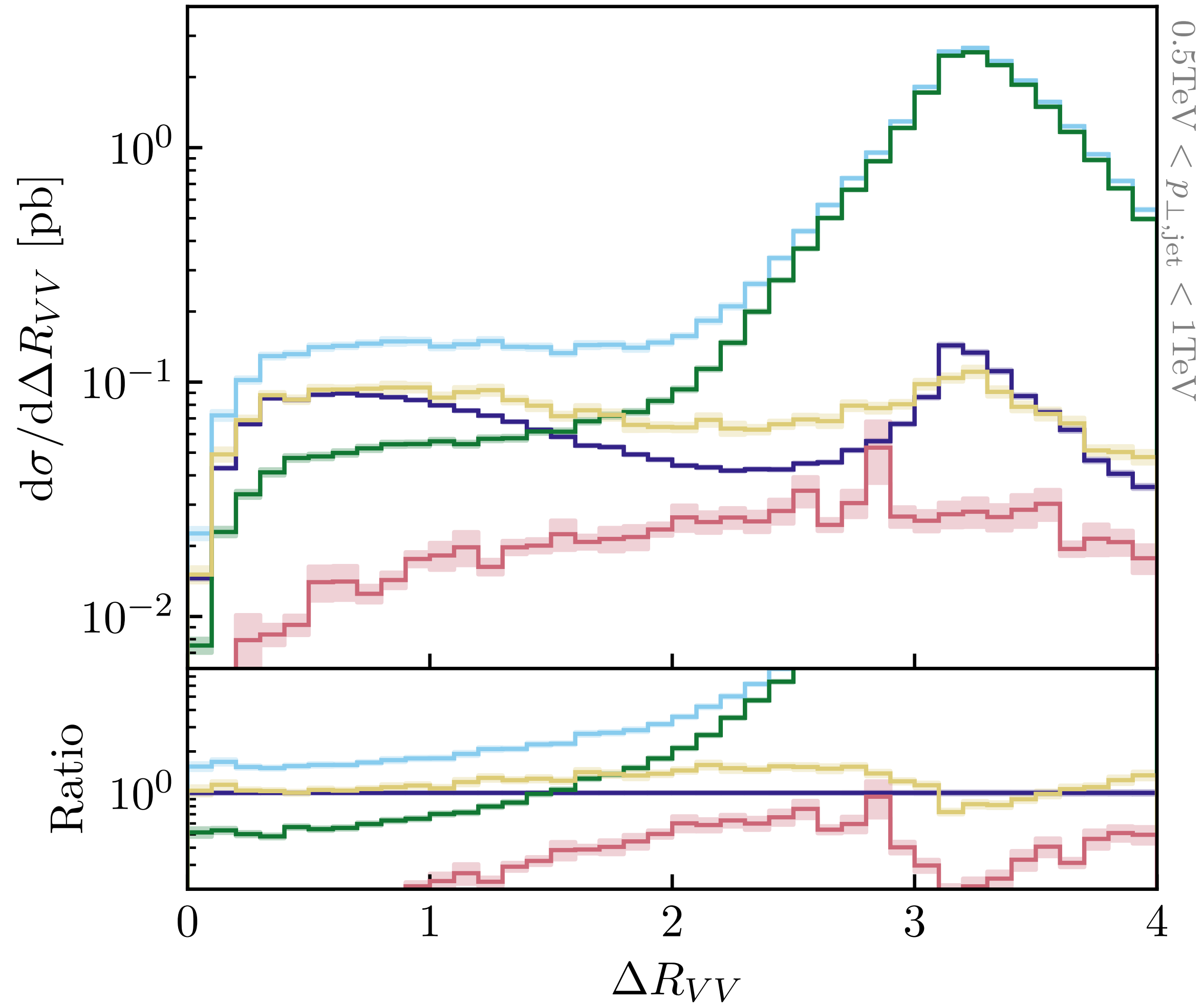
## Veto procedure



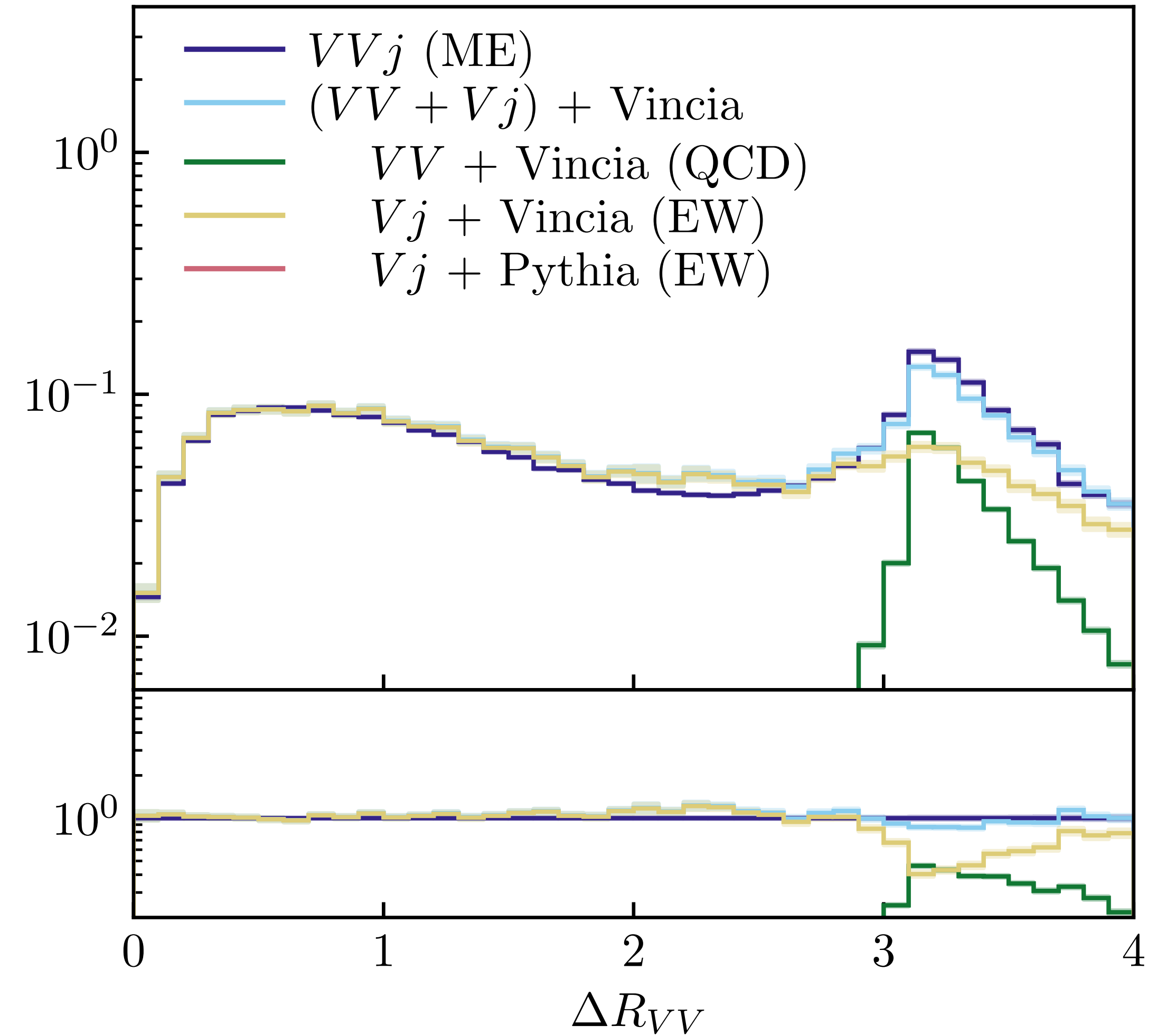
$$d_{ij} = \min(k_{T,i}^2, k_{T,j}^2) \frac{\Delta_{ij}}{R} + m_i^2 + m_j^2 - m^2$$

# Overlap Veto

$pp \rightarrow VVj$  (no overlap veto)



$pp \rightarrow VVj$  (overlap veto)



# Conclusions

- Universal EW radiative corrections relevant at (HL)-LHC and future colliders
- EW sector offers rich physics above the EW scale
- Many features unique to the EW sector
  - Matching to resonance decays
  - Neutral boson interference
  - Overlap between hard scatterings
- Many other features yet to implement
  - Treatment of soft & spin interference
  - Bloch-Nordsieck violations
- EW shower is available in Pythia 8.304 (released last week)

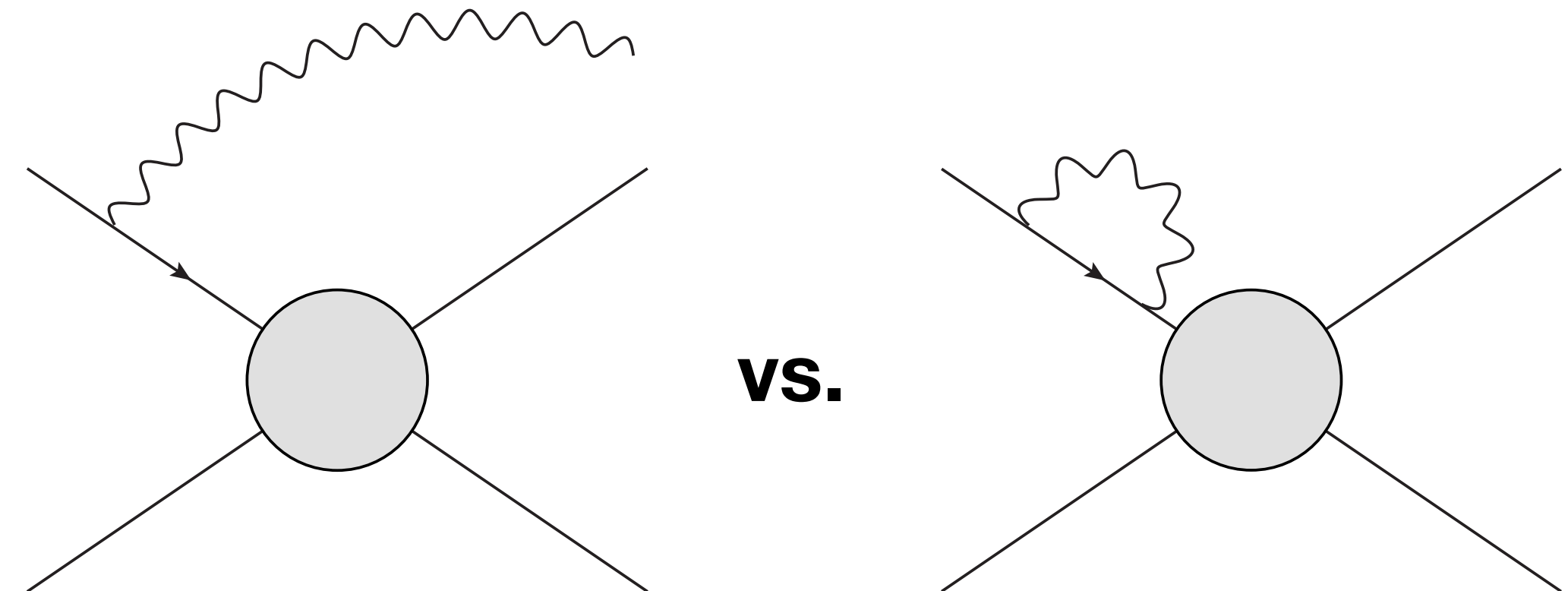
# Backup

# Bloch-Nordsieck Violations

**BN / KLN Theorems: Real and virtual IR singularities cancel**

Requirement: Summing over gauge indices

W radiation in the initial state:  
PDFs are not isospin symmetric  
→ Incomplete cancellation



Effects not large at LHC, but will be significant at higher energies

No straightforward solution in shower language

# Spinor-Helicity formalism

## Fermion

$$u_{\pm}(p) = \frac{1}{\sqrt{2p \cdot k}} (\not{p} + m) u_{\mp}(k)$$

$$v_{\pm}(p) = \frac{1}{\sqrt{2p \cdot k}} (\not{p} - m) u_{\mp}(k)$$

$k \rightarrow$  helicity for massive fermions

Spin points in direction of motion

## Gauge boson

$$\epsilon_{\pm}^{\mu}(p) = \pm \frac{1}{\sqrt{2}} \frac{1}{2p \cdot k} \bar{u}_{\mp}(k) \not{p} \gamma^{\mu} u_{\pm}(k)$$

$$\epsilon_0^{\mu}(p) = \frac{1}{m} \left( p^{\mu} - \frac{m^2}{p \cdot k} k^{\mu} \right)$$

$k \rightarrow$  gauge choice

Purely transverse & longitudinal

$$k = (1, -\vec{e}_p)$$



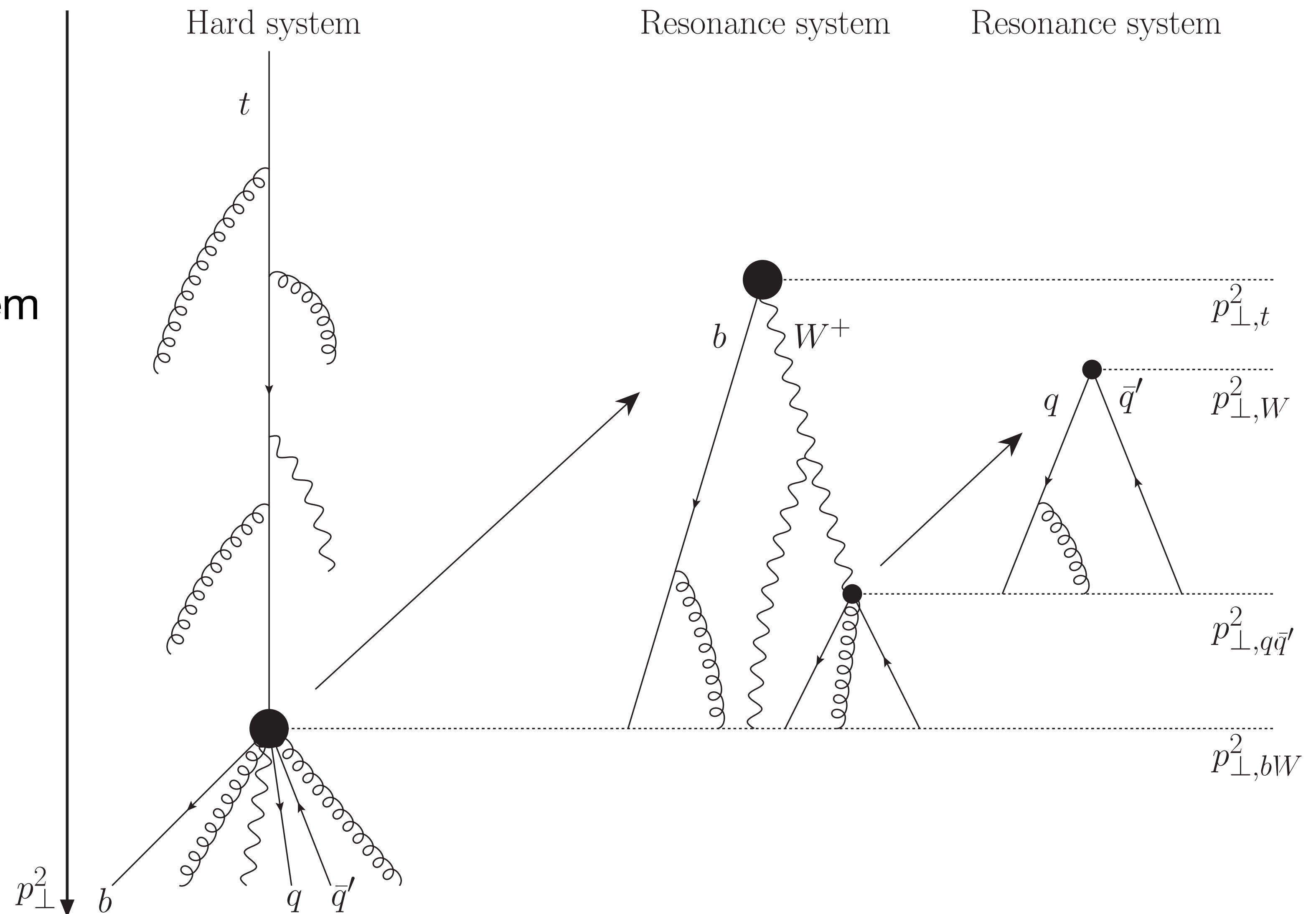
# Resonance Matching

## Pythia

- Narrow width approximation
- Decay showers after hard system

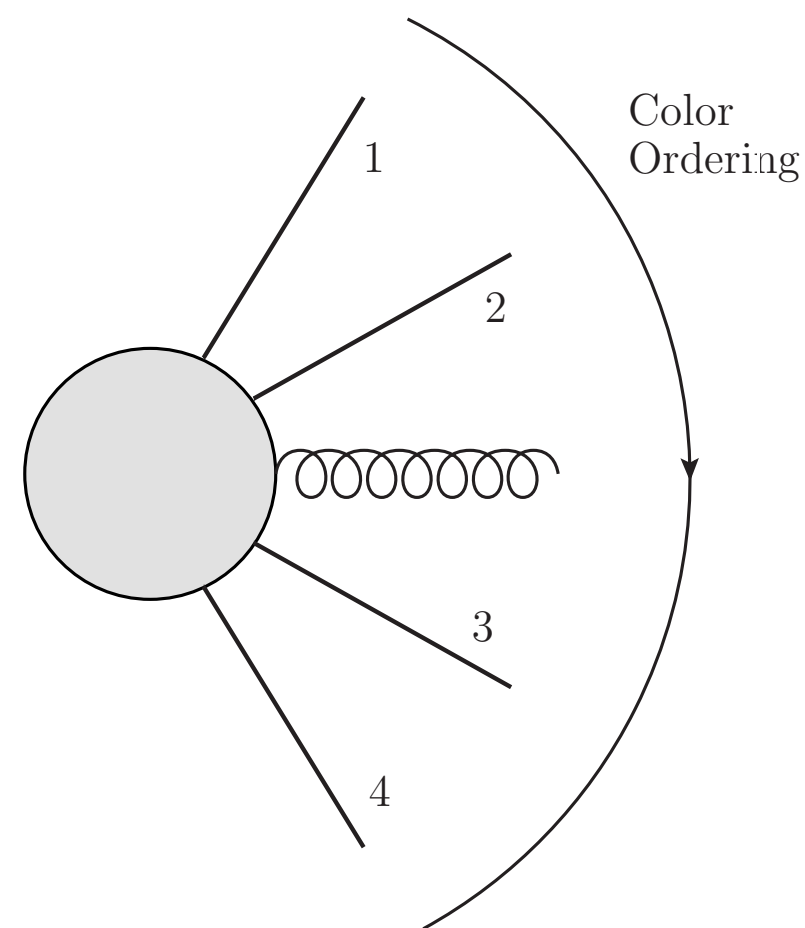
## Vincia

- Decays part of hard system
- Natural treatment of finite width effects



# Recoiler Selection

In QCD recoiler determined by colour structure



Gluon splitting: recoiler ambiguous

In EW no such guidance exists

$$\begin{aligned}
 \left| \text{Vertex} \right|^2 &= \frac{\left| \text{Diagram 1} \right|^2}{\left| \text{Diagram 1} \right|^2 + \left| \text{Diagram 2} \right|^2} \left| \text{Recoiler} \right|^2 \\
 &+ \frac{\left| \text{Diagram 3} \right|^2}{\left| \text{Diagram 3} \right|^2 + \left| \text{Diagram 4} \right|^2} \left| \text{Recoiler} \right|^2
 \end{aligned}$$

Probabilistic choice to avoid back reaction effects