

Status of W-boson mass combinations

Working group involving members of the ATLAS, CDF, D0 & CMS collaborations

<https://indico.cern.ch/category/3290/>

lhc-tevatron-wmass-combinations@cern.ch

- Reminders
- Recent discussions : measurement emulation ; PDF extrapolation studies; generator comparisons
- Plan to completion

Status of W-boson mass combinations

Working group involving members of the ATLAS, CDF, D0 & CMS collaborations

<https://indico.cern.ch/category/3290/>

lhc-tevatron-wmass-combinations@cern.ch

- Contributions

- N.Andari (overall emulation infrastructure), J.Kretzschmar, S.Amoroso (Generators and Predictions)
- B.Tuchming, Chen Wang (D0 emulation, generator predictions)
- C.Hays (CDF emulation and event generation)
- Coordination C.Hays (CDF), B.Tuchming (D0), M.Boonekamp (ATLAS), J.Bendavid (CMS)

Objectives

- Experiment-endorsed world averages for published measurements of m_W , and corrections of existing measurements to newer PDFs
- Specific issues :
 - Measurements performed at detector level; no unfolded data
 - Strong role of PDFs in measurement uncertainties, and central values →
Correlations, PDF model dependence
- Areas of development:
 - Existing / coming Tevatron / ATLAS measurements :
 - χ^2 -based measurements with forward error propagation; no explicit profiling of uncertainties
 - Extrapolation from legacy to modern PDF sets using measurement emulation
 - “future” :
 - Harmonization of theory inputs
 - extension to measurements based on profile-likelihood fits [deferred], in view of LHC measurement combinations. Uncertainty decomposition – how to properly correlate measurement results?

Methods

- Measurement emulation
 - Physics modelling with the PDF sets and pTW models used for the publications
 - Main generator : Powheg + PHOTOS
 - Simplified parameterisation of the detector responses:
 - Lepton energy resolution and efficiencies → $p_{T}^{e,\mu}$
 - Recoil resolution → u_T, m_T, MET
 - Correlations between leptons and the recoil, when relevant:
 - ”lepton removal” effects
 - recoil-dependent lepton efficiencies
 - Analysis cuts
- by no means a way to reproduce measurements in full detail, but sufficient to calculate the relative effect of PDF variations with sub-MeV accuracy

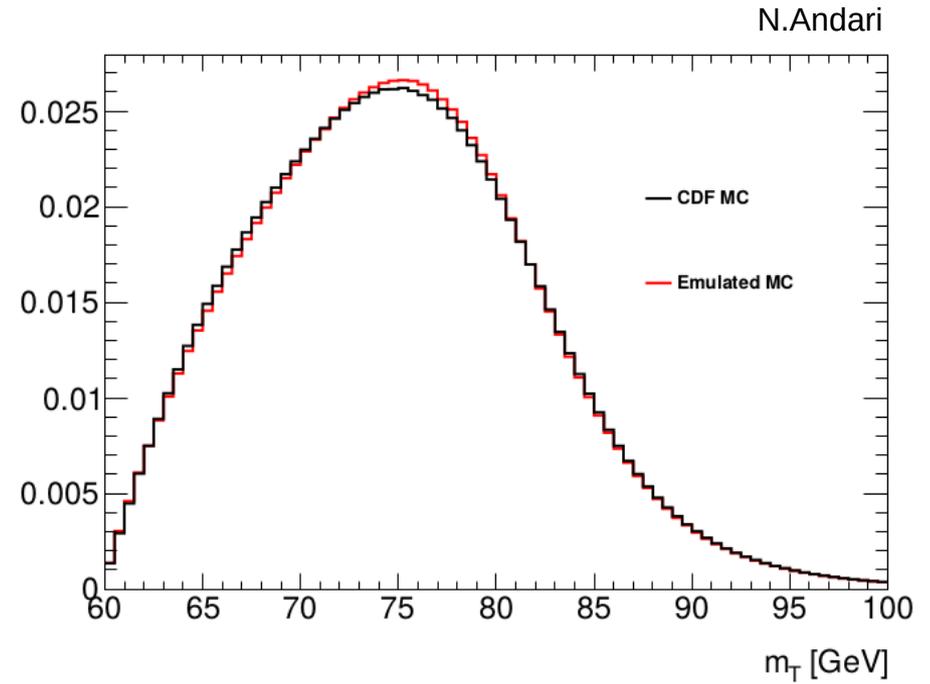
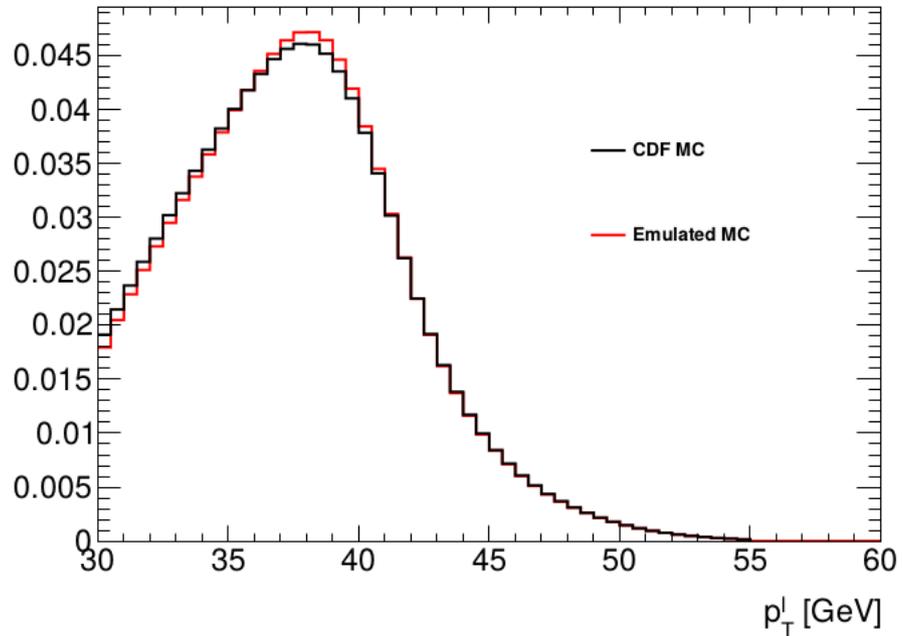
Methods

- Measurement emulation

Experiment	Event selections	Fit ranges
CDF	$30 < p_T^\ell < 55 \text{ GeV}, \eta_\ell < 1$ $30 < E_T^{\text{miss}} < 55 \text{ GeV}, 60 < m_T < 100 \text{ GeV}$ $u_T < 15 \text{ GeV}$	$32 < p_T^\ell < 48 \text{ GeV}$ $32 < E_T^{\text{miss}} < 48 \text{ GeV}$ $65 < m_T < 90 \text{ GeV}$
D0	$p_T^\ell > 25 \text{ GeV}, \eta_\ell < 1.05$ $E_T^{\text{miss}} > 25 \text{ GeV}, m_T > 50 \text{ GeV}$ $u_T < 15 \text{ GeV}$	$32 < p_T^\ell < 48 \text{ GeV}$ $65 < m_T < 90 \text{ GeV}$
ATLAS	$p_T^\ell > 30 \text{ GeV}, \eta_\ell < 2.4$ $E_T^{\text{miss}} > 30 \text{ GeV}, m_T > 60 \text{ GeV}$ $u_T < 30 \text{ GeV}$	$32 < p_T^\ell < 45 \text{ GeV}$ $66 < m_T < 99 \text{ GeV}$

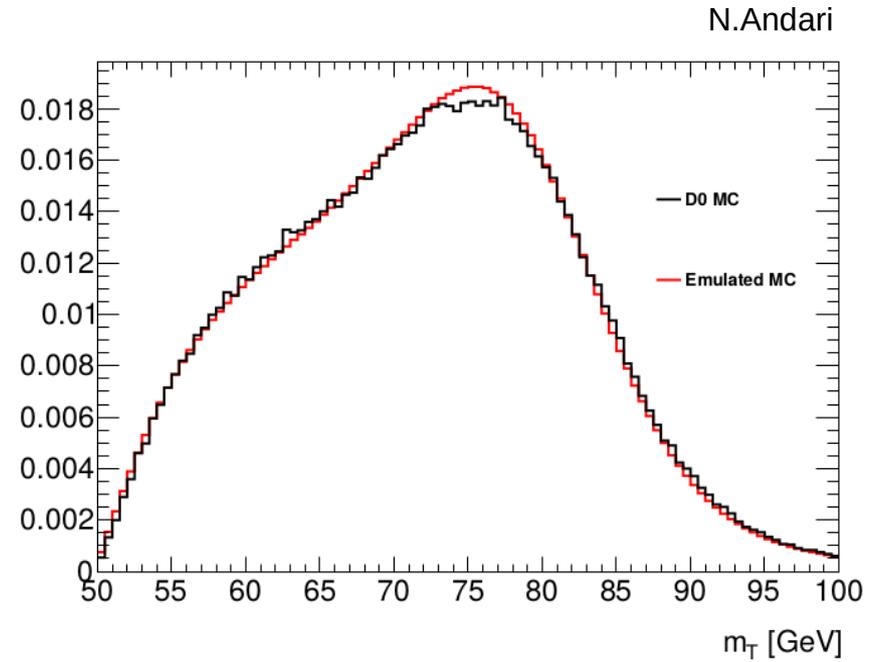
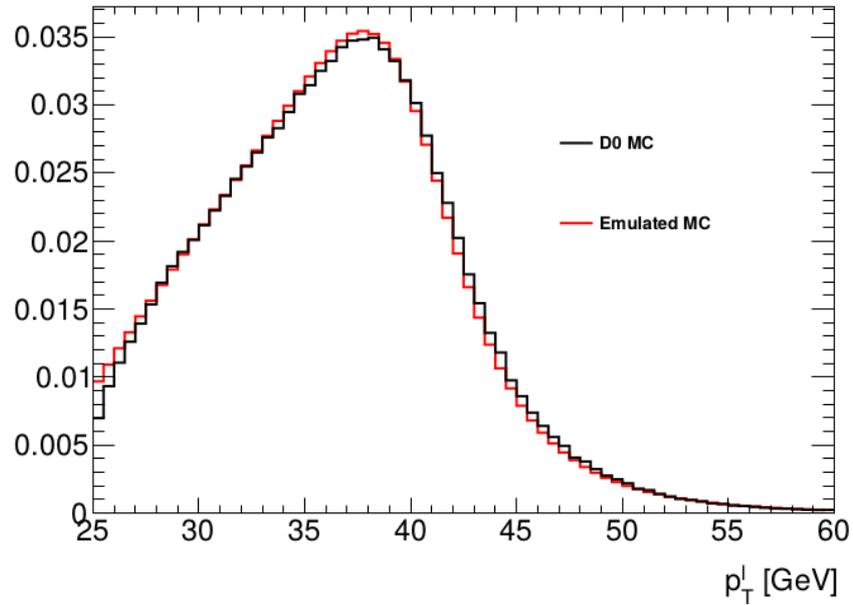
Methods

- Measurement emulation
 - CDF distributions



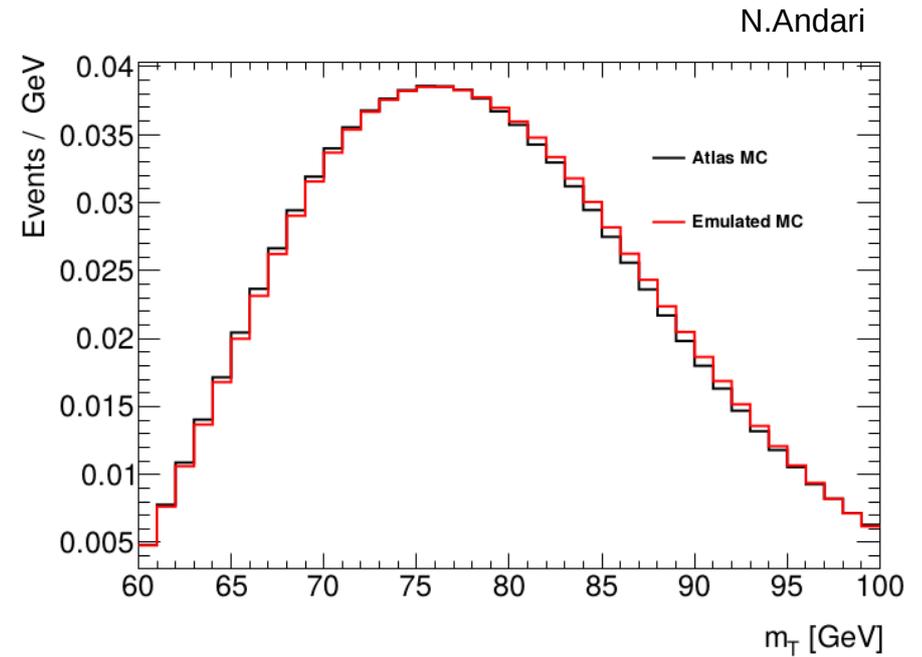
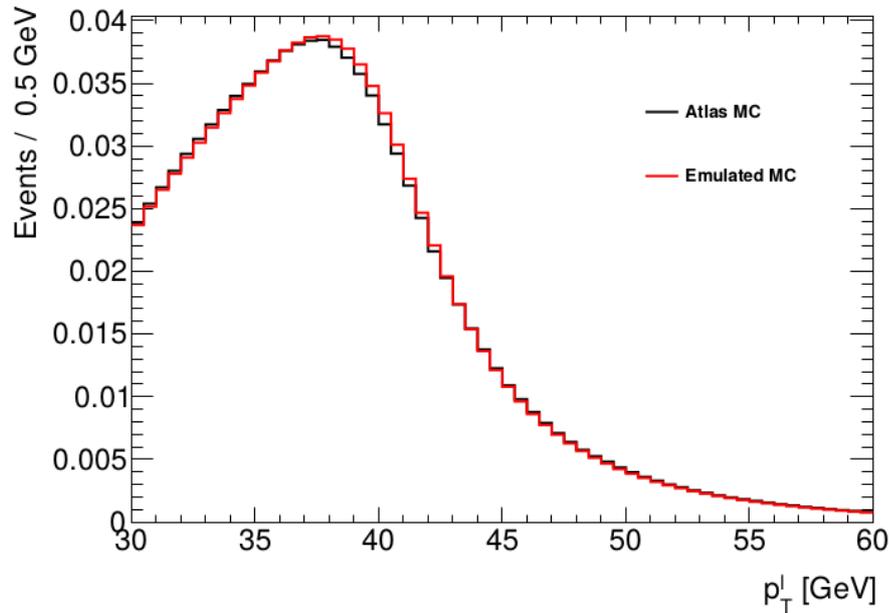
Methods

- Measurement emulation
 - D0 distributions



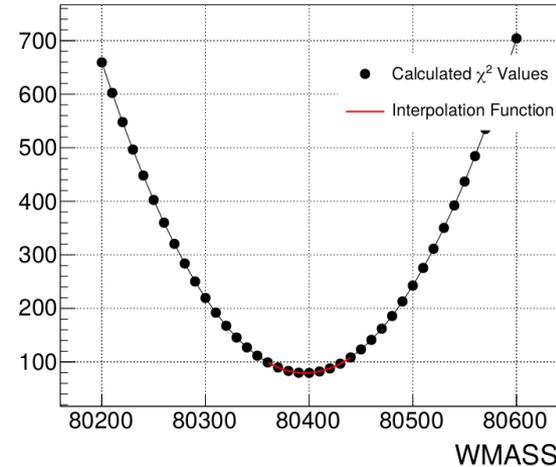
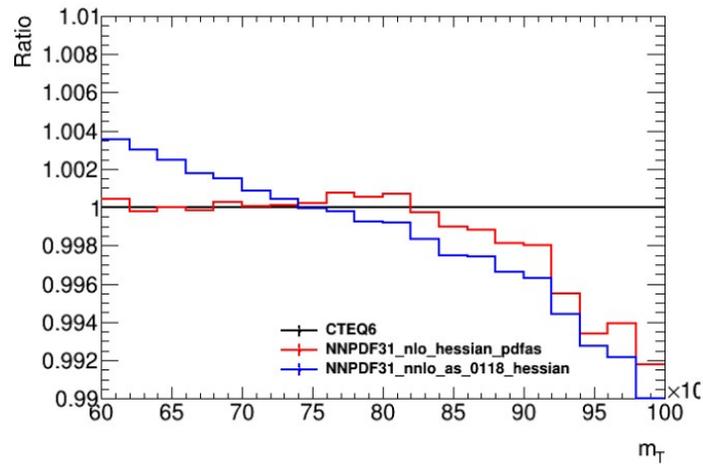
Methods

- Measurement emulation
 - ATLAS distributions



Methods

- PDF shifts and uncertainties
 - Shift in m_W when going from PDF_A to PDF_B
 - Templates with PDF_A and varying values of m_W ,
 - Pseudo-data with reference value of m_W and PDF_B ; χ^2 fit
 - $\delta m_W^{A \rightarrow B} = - (m_W^{\text{fit}} - m_W^{\text{ref}})$



- Used to calculate PDF uncertainties, and update measurement central values

Validation

	Published	Emulated			
	CTEQ6M [†] MSTW2008 [§]	CTEQ6M [†]	CTEQ6.6	CT10nlo	MSTW2008 [§]
CDF	80 387	80 389	80 402	80 402	80 400
PDF	10	15	14	11	10
Total	19	22	22	20	19
χ^2/ndof	7/5	7/5	7/5	8/5	7/5

	Published	Emulated			
	CT10nlo ^{†§}	CTEQ6M	CTEQ6.6	CT10nlo ^{†§}	MSTW2008
ATLAS	80 370	80 343	80 357	80 371	80 351
PDF	9	8	8	10	5
Total	19	17	18	19	16
χ^2/ndof	29/27	29/27	31/27	29/27	40/27

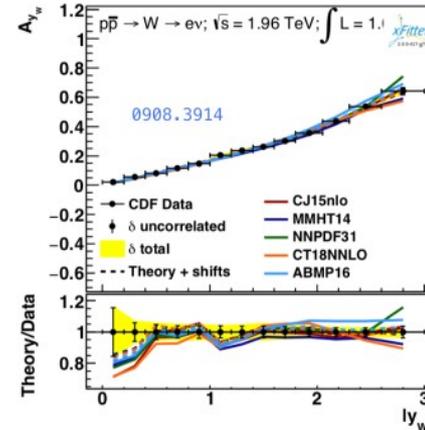
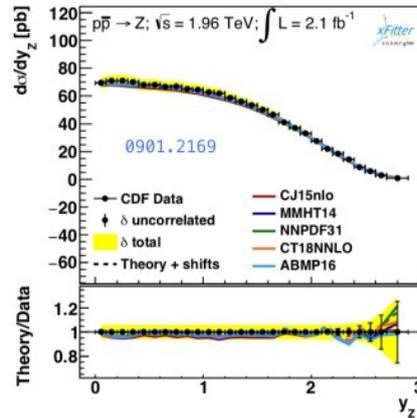
Validation

- Past combinations : Tevatron, Tevatron + LEP

	Tevatron	Tevatron+LEP
Published	80387 + 16	80385 + 15
Validation	80388 + 16	80385 + 15 (actually 14.47)

Choice of modern “target” PDFs

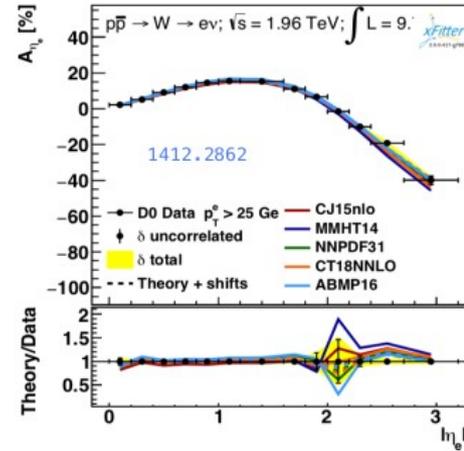
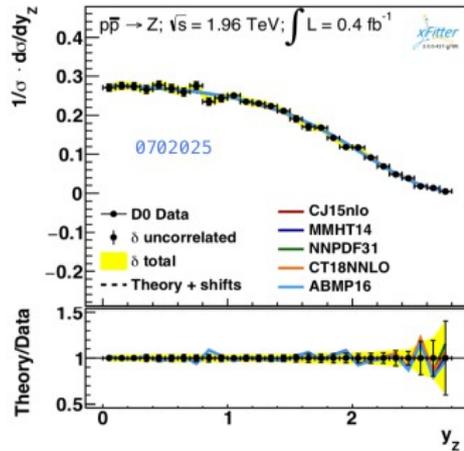
- Comparisons between existing Drell-Yan data and “recent” NNLO PDFs
 - CDF



Dataset	CJ15nlo	MMHT14	NNPDF31	CT18NNLO	ABMP16
CDF W asymmetry 2009	18 / 13	12 / 13	11 / 13	13 / 13	17 / 13
Correlated χ^2	1.6	1.7	2.6	2.9	6.5
Log penalty χ^2	-0.00	-0.00	-0.00	-0.00	-0.00
Total χ^2 / dof	19 / 13	14 / 13	13 / 13	16 / 13	23 / 13
χ^2 p-value	0.11	0.37	0.43	0.25	0.04
Dataset	CJ15nlo	MMHT14	NNPDF31	CT18NNLO	ABMP16
CDF Z rapidity 2010	29 / 28	30 / 28	25 / 28	27 / 28	30 / 28
Correlated χ^2	1.5	0.99	1.7	0.49	0.69
Log penalty χ^2	-1.16	-0.63	-0.44	-0.60	-0.90
Total χ^2 / dof	30 / 28	30 / 28	26 / 28	27 / 28	30 / 28
χ^2 p-value	0.37	0.36	0.55	0.53	0.36

Choice of modern “target” PDFs

- Comparisons between existing Drell-Yan data and “recent” NNLO PDFs
 - D0

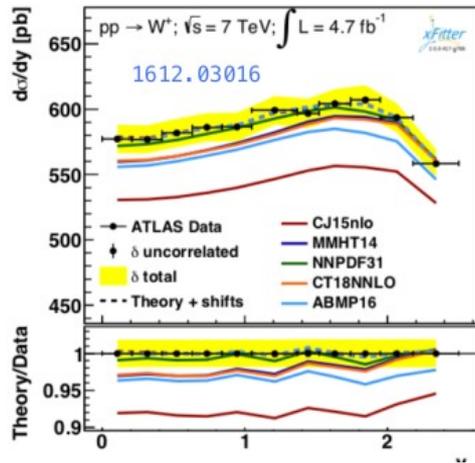


Dataset	CJ15nlo	MMHT14	NNPDF31	CT18NNLO	ABMP16
D0 W el nu lepton asymmetry pT > 25 GeV	32 / 13	24 / 13	19 / 13	17 / 13	23 / 13
Correlated χ^2	8.7	11	7.4	4.6	4.1
Log penalty χ^2	+0.00	+0.00	+0.00	+0.00	+0.00
Total χ^2 / dof	41 / 13	35 / 13	27 / 13	22 / 13	27 / 13
χ^2 p-value	0.00	0.00	0.01	0.05	0.01

Dataset	CJ15nlo	MMHT14	NNPDF31	CT18NNLO	ABMP16
D0 Z rapidity 2007	22 / 28	23 / 28	22 / 28	22 / 28	23 / 28
Correlated χ^2	0.0097	0.14	0.10	0.041	0.061
Log penalty χ^2	+0.01	-0.07	+0.10	+0.09	-0.17
Total χ^2 / dof	22 / 28	23 / 28	22 / 28	22 / 28	23 / 28
χ^2 p-value	0.76	0.74	0.76	0.79	0.75

Choice of modern “target” PDFs

- Comparisons between existing Drell-Yan data and “recent” NNLO PDFs
 - ATLAS



S.Amoroso

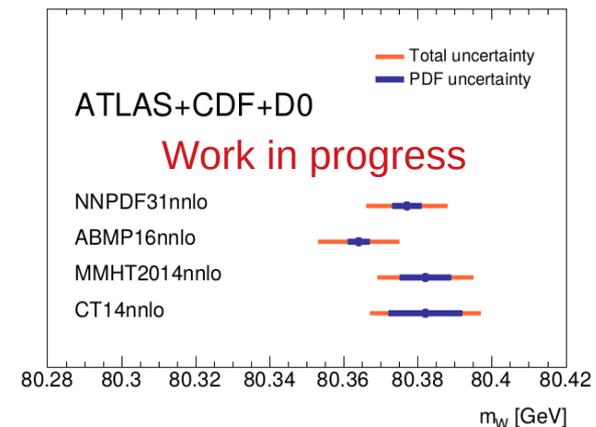
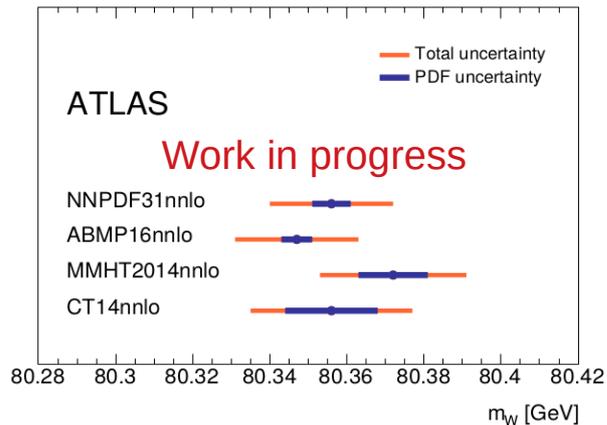
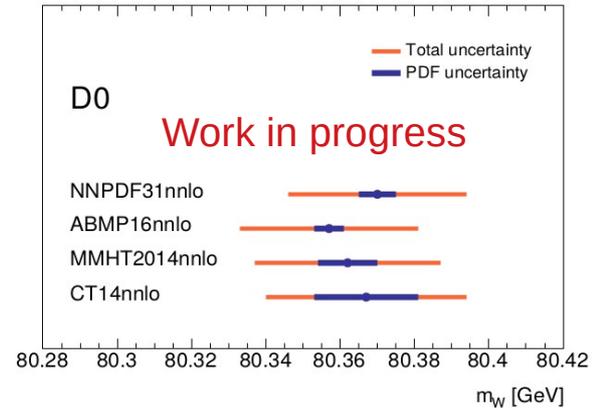
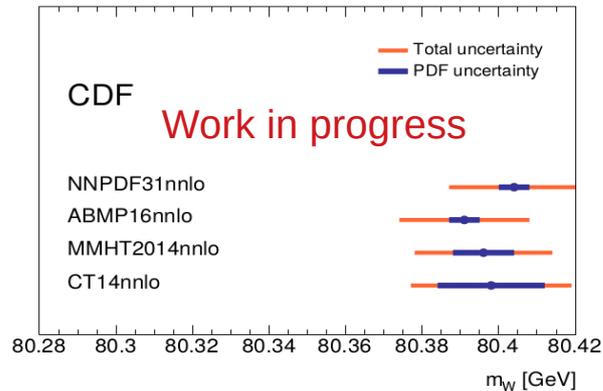
Dataset	CJ15nlo	MMHT14	NNPDF31	CT18NNLO	ABMP16
ATLAS low mass Z rapidity 2011	26 / 6	18 / 6	14 / 6	12 / 6	21 / 6
ATLAS peak CC Z rapidity 2011	52 / 12	21 / 12	12 / 12	16 / 12	24 / 12
ATLAS peak CF Z rapidity 2011	16 / 9	11 / 9	11 / 9	10 / 9	9.2 / 9
ATLAS high mass CC Z rapidity 2011	7.7 / 6	6.1 / 6	5.8 / 6	5.9 / 6	6.1 / 6
ATLAS high mass CF Z rapidity 2011	4.6 / 6	5.5 / 6	4.7 / 6	4.8 / 6	4.5 / 6
ATLAS W ⁻ lepton rapidity 2011	17 / 11	8.4 / 11	8.7 / 11	9.1 / 11	10 / 11
ATLAS W ⁺ lepton rapidity 2011	16 / 11	11 / 11	11 / 11	10 / 11	13 / 11
Correlated χ^2	118	50	31	40	50
Log penalty χ^2	-9.09	-3.32	-2.45	-3.66	-4.22
Total χ^2 / dof	247 / 61	127 / 61	95 / 61	104 / 61	134 / 61
χ^2 p-value	0.00	0.00	0.00	0.00	0.00

- consider MMHT14, NNPDF3.1, CT18NNLO, ABMP16
- best overall description of the data by NNPDF3.1, CT18NNLO

Preliminary results

- Just an example – discussions ongoing [see later]

N.Andari



Correlation of PDF uncertainties

- CTEQ6

CDF/D0

```

-> Joint Total correlation

```

	mw_run2cdf	mw_run2d0	mw_run1cdf	mw_run1d0
mw_run2cdf	1	0.459247	0	0
mw_run2d0	0.459247	1	0	0
mw_run1cdf	0	0	1	0
mw_run1d0	0	0	0	1

```

-> Joint PDF correlation

```

	mw_run2cdf	mw_run2d0	mw_run1cdf	mw_run1d0
mw_run2cdf	1	0.998813	--	--
mw_run2d0	0.998813	1	--	--
mw_run1cdf	--	--	1	--
mw_run1d0	--	--	--	1

Tevatron/LHC

```

-> Joint Total correlation

```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.269722	0
mw_tevatron	0.269722	1	0
mw_lep	0	0	1

```

-> Joint PDF correlation

```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.71625	--
mw_tevatron	0.71625	1	--
mw_lep	--	--	1

- CTEQ6.1

CDF/D0

```

-> Joint Total correlation

```

	mw_run2cdf	mw_run2d0	mw_run1cdf	mw_run1d0
mw_run2cdf	1	0.457046	0	0
mw_run2d0	0.457046	1	0	0
mw_run1cdf	0	0	1	0
mw_run1d0	0	0	0	1

```

-> Joint PDF correlation

```

	mw_run2cdf	mw_run2d0	mw_run1cdf	mw_run1d0
mw_run2cdf	1	0.998901	--	--
mw_run2d0	0.998901	1	--	--
mw_run1cdf	--	--	1	--
mw_run1d0	--	--	--	1

Tevatron/LHC

```

-> Joint Total correlation

```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.253547	0
mw_tevatron	0.253547	1	0
mw_lep	0	0	1

```

-> Joint PDF correlation

```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.700236	--
mw_tevatron	0.700236	1	--
mw_lep	--	--	1

Correlation of PDF uncertainties

- Correlations
 - CTEQ6.6

Tevatron/LHC

```
5
  mw_atlas      mw_tevatron      mw_lep
  mw_atlas      1      0.281416      0
  mw_tevatron   0.281416      1      0
  mw_lep        0      0      1
-> Joint PDF correlation
7
  mw_atlas      mw_tevatron      mw_lep
  mw_atlas      1      0.741186      --
  mw_tevatron   0.741186      1      --
  mw_lep        --      --      --
8
```

- CT10

```
-> Joint Total correlation
cout << setw(15) << m_jointCovPDF(i,j)/sqrt(m_jointCovPDF(i,i)*m
cout << setw(15) << "--";
cout << endl;
  mw_atlas      mw_tevatron      mw_lep
  mw_atlas      1      0.409274      0
  mw_tevatron   0.409274      1      0
  mw_lep        0      0      1
-> Joint PDF correlations to 0
m_lsqChiSquare = 0;
  mw_atlas      mw_tevatron      mw_lep
  mw_atlas      1      0.751231      --
  mw_tevatron   0.751231      1      --
  mw_lep        --      --      --
return true;
```

Correlation of PDF uncertainties

- Correlations
 - CT10nnlo
 - CJ15

Tevatron/LHC

```
-> Joint Total correlation
cout << endl << " -> Joint PDF correlation " << endl << endl;
cout << setw(15) << "mw_atlas      mw_tevatron      mw_lep
mw_atlas << m_rank-m_nsys; i++)      0.300246      0
mw_tevatron << setw(15) << m_channels[i];      0.300246      1      0
mw_lep      0      0      1
for(int i=0; i<m_rank-m_nsys; i++) {
cout << setw(15) << m_channels[i];
for(int j=0; j<m_rank-m_nsys; j++)
if(sqrt(m_jointCovPDF(i,j))>0)
cout << setw(15) << m_jointCovPDF(i,j) << "
mw_atlas      mw_tevatron      mw_lep
mw_atlas      1      0.755786      --
mw_tevatron   0.755786      1      --
mw_lep        --      --      --
cout << endl;
}
```

```
-> Joint Total correlation
cout << endl << " -> Joint PDF correlation " << endl << endl;
cout << setw(15) << "mw_atlas      mw_tevatron      mw_lep
mw_atlas << m_rank-m_nsys; i++)      1      0.107284      0
mw_tevatron << setw(15) << m_channels[i];      0.107284      1      0
mw_lep      0      0      1
for(int i=0; i<m_rank-m_nsys; i++) {
cout << setw(15) << m_channels[i];
for(int j=0; j<m_rank-m_nsys; j++)
if(sqrt(m_jointCovPDF(i,j))>0)
cout << setw(15) << m_jointCovPDF(i,j) << "
mw_atlas      mw_tevatron      mw_lep
mw_atlas      1      0.712279      --
mw_tevatron   0.712279      1      --
mw_lep        --      --      --
cout << endl;
}
```

Correlation of PDF uncertainties

- Correlations
 - CT14nnlo
 - CT14nlo

Tevatron/LHC

```
cout << setw(15) << "#";
for(int i=0; i<m_rank-m_nsys; i++)
    cout << setw(15) << m_channels[i];
cout << endl;
mw_atlas << m_rank-m_nsys; 1 { 0.334286 mw_tevatron mw_lep
mw_atlas << m_rank-m_nsys; 1 { 0.334286 mw_tevatron mw_lep
mw_tevatron (15) << 0.334286 (15) << m_channel[i]; mw_tevatron mw_lep
for(mw_lep j<m_rank-m_nsys; 0) mw_lep mw_lep
if(sqrt(m_jointCovPDF(i,i)*m_jointCovPDF(j,j))>0)
else
cout << setw(15) mw_atlas mw_tevatron mw_lep
mw_atlas; mw_atlas 1 mw_tevatron mw_lep
mw_tevatron 0.710479 mw_tevatron 1 mw_lep
mw_lep -- mw_lep -- mw_lep --
// }
```

```
// cout << endl;
-> Joint Total correlation
cout << endl << " -> mw_atlas mw_tevatron mw_lep
cout << setw(15) << " mw_atlas 1 mw_tevatron mw_lep
mw_atlas << m_rank-m_nsys; 1 { 0.32786 mw_tevatron mw_lep
mw_tevatron << m_rank-m_nsys; 1 { 0.32786 mw_tevatron mw_lep
mw_lep (15) << m_channel[i]; mw_tevatron mw_lep
cout << endl;
for(int i=0; i<m_rank-m_nsys; i++) {
cout << setw(15) m_channels[i];
for(int j=0; j<m_rank-m_nsys; j++)
if(sqrt(m_jointCovPDF(i,i)*m_jointCovPDF(j,j))>0)
cout << setw(15) << m_jointCovPDF(i,j)/sqrt(m_jointCovPDF(i,i)*m
mw_atlas mw_tevatron mw_lep
mw_atlas 1 mw_tevatron mw_lep
mw_tevatron 0.807696 mw_tevatron 1 mw_lep
mw_lep -- mw_lep -- mw_lep --
cout << endl;
```

Correlation of PDF uncertainties

- Correlations

- MMHT2014nlo 68%CL

Tevatron/LHC

```
-> Joint Total correlation
```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.195674	0
mw_tevatron	0.195674	1	0
mw_lep	0	0	1

```
-> Joint PDF correlation
```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.626974	--
mw_tevatron	0.626974	1	--
mw_lep	--	--	--

- MMHT2014nnlo 68%CL

```
-> Joint Total correlation
```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.226108	0
mw_tevatron	0.226108	1	0
mw_lep	0	0	1

```
-> Joint PDF correlation
```

	mw_atlas	mw_tevatron	mw_lep
mw_atlas	1	0.656986	--
mw_tevatron	0.656986	1	--
mw_lep	--	--	--

Remaining issue : central value extrapolations

- The present analysis, using Powheg, observes shifts between PDFs that can typically reach ~ 10 MeV at the Tevatron, up to 20 MeV at the LHC

CDF, D0

PDF	Shift wrt. CTEQ6M
CTEQ6.6	+11 MeV
CT18NNLO	+9 MeV
MMHT2014	+7 MeV
ABMP16	+2 MeV
NNPDF3.1	+12 MeV

ATLAS

PDF	Shift wrt. CT10nnlo
CTEQ6.6	-13 MeV
CT18NNLO	-8 MeV
MMHT2014	+1 MeV
ABMP16	-23 MeV
NNPDF3.1	-12 MeV

- Questions raised on generator dependence of these shifts. Studies performed using aMC@NLO+Pythia (shown here) and Resbos (TODO)

Remaining issue : central value extrapolations

- How much do the shifts in mW depend on the generator used to evaluate them?
 - Benchmark: CTEQ6M (CDF legacy) → NNPDF3.1 (NNLO, smallest unc.)
 - Generators at hand : Powheg, MiNNLO, aMC@NLO+Pythia

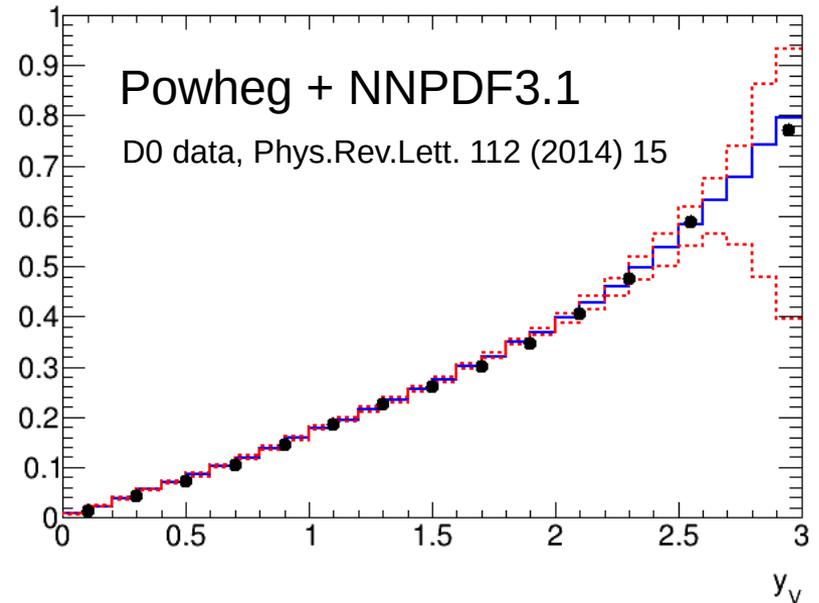
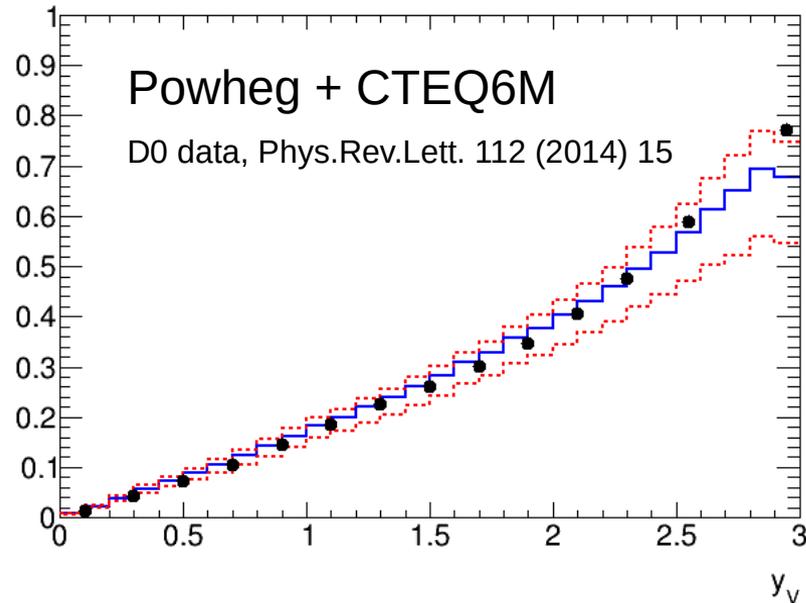
N.Andari

NNPDF/ CTEQ	Powheg Reweighted	Powheg Explicit generation	aMC@NLO+Pythia	MiNNLO
mT	<i>no ptw constraint:</i> -13.19 MeV <i>ptw constraint:</i> -12.19 MeV	<i>no ptw constraint:</i> -31.27 MeV <i>ptw constraint:</i> -12.07 MeV	<i>no ptw constraint:</i> -8.63 MeV <i>ptw constraint:</i> -6.56 MeV	<i>no ptw constraint:</i> -22.33 MeV <i>ptw constraint:</i> -12.73 MeV
pTl	<i>no ptw constraint:</i> -16.42 MeV <i>ptw constraint:</i> -13.61 MeV	<i>no ptw constraint:</i> -70.24 MeV <i>ptw constraint:</i> -12.85 MeV	<i>no ptw constraint:</i> -11.7 MeV <i>ptw constraint:</i> -7.26 MeV	<i>no ptw constraint:</i> -44.89 MeV <i>ptw constraint:</i> -14.96 MeV

Agreement between pTW-constrained Powheg (explicit generation and reweighting) and MiNNLO; smaller effect for aMC@NLO+Pythia.

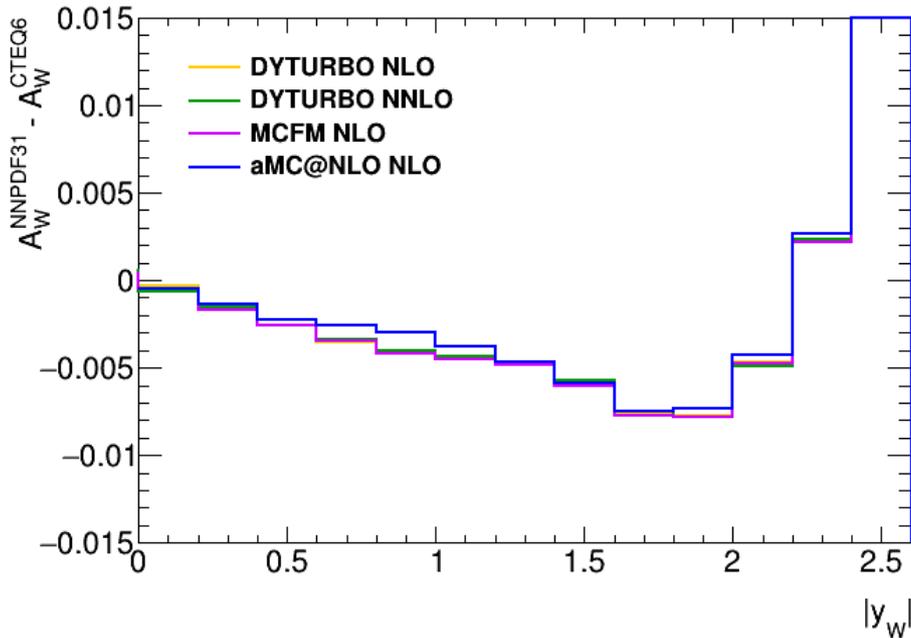
Remaining issue : central value extrapolations

- The role of the W charge asymmetry at the Tevatron
 - Main driver of small residual PDF uncertainty ($\sim 3\text{-}4$ MeV with NNPDF 3.1)
 - Important to verify that generator predictions with NNPDF3.1 reproduce the measurement data, since the latter are used in the NNPDF fit (closure!)

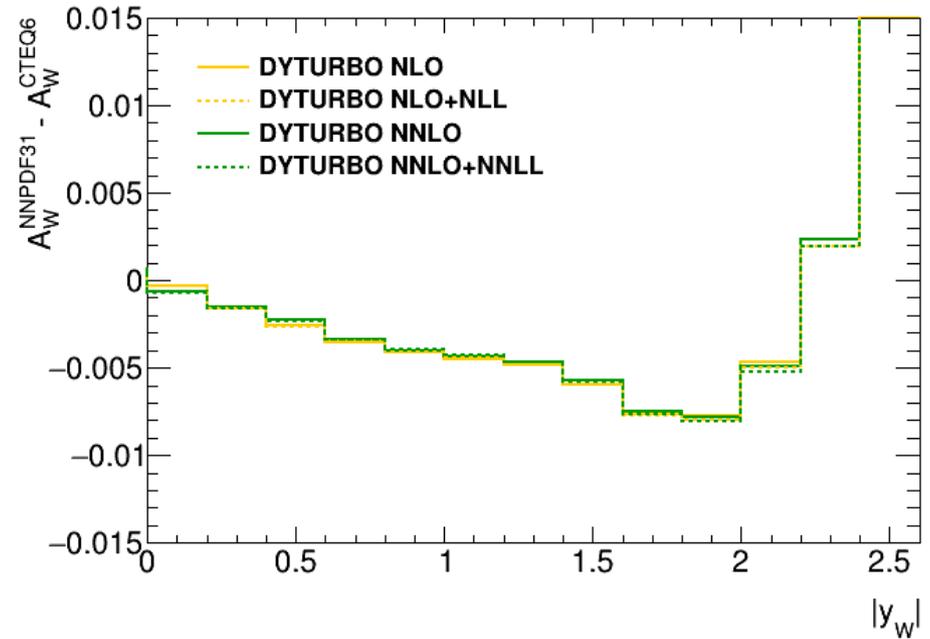


W charge asymmetry : CTEQ6M \rightarrow NNPDF3.1

How well do various calculations agree, for the prediction of the PDF-dependence of this observable?



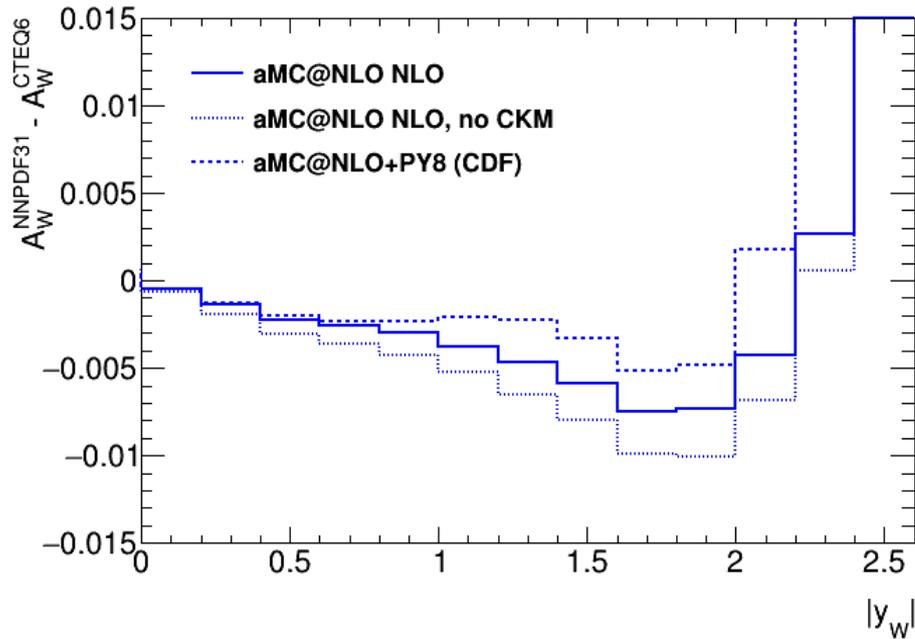
Fixed-order calculations



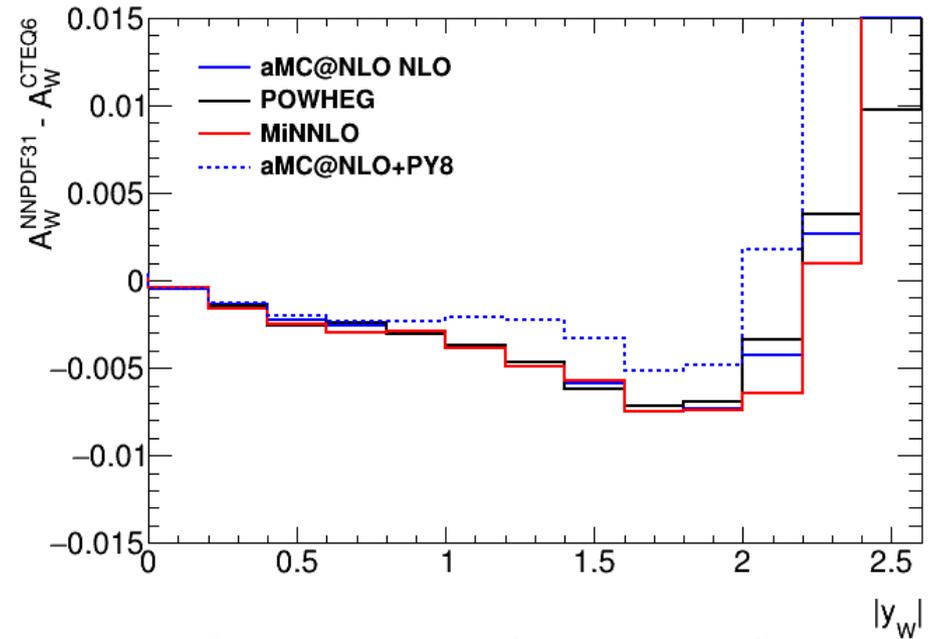
Dyturbo variations

W charge asymmetry : CTEQ6M \rightarrow NNPDF3.1

How well do various calculations agree, for the prediction of the PDF-dependence of this observable?



aMC@NLO+Pythia variations



Shower MC's and F.O – overall consensus, except aMC@NLO+Py

Discussion and plan to completion

- Differences in m_W extrapolations, between Powheg/MiNNLO and aMC@NLO+Pythia, relate to discrepancies in the predictions of W charge asymmetry. To be repeated with Resbos, for a complete picture.
- Predictions required for a complete set of comparisons :
 - theory/theory and theory/data comparisons for W charge asymmetry, as main probe of PDF accuracy (most constraining distribution)
 - Predictions :
 - Powheg with PDF reweighting, Powheg generated with diff. PDFs, MiNNLO
 - aMC@NLO+Pythia
 - Dyturbo, Resbos
 - aMC@NLO fixed-order, MCFM

Discussion and plan to completion

- Resbos is missing in all previous comparisons. Needed to compare shifts and uncertainties in m_W , and predictions of basic W distributions
 - Available :
 - from Resbos authors : CT14, CT18, CTEQ6.6 all NLO
 - from D0 : CTEQ6.6
 - from CDF : CTEQ6M
 - Still needed
 - Correct NNLO grids for CT14, CT18, CTEQ6.6
 - CTEQ6M, NNPDF3.1, MMHT2014 from authors

Resbos predictions are the single missing piece in the present analysis, and required to “solve” the ongoing discussions and consolidate the theoretical description of this measurement

Summary

- Analysis almost complete
 - Numbers didn't significantly change since >6 months.
 - Refined emulations, with 1-2%-level agreement between emulated and published distributions
 - Predictions for all relevant PDFs (legacy, modern)
 - Collection of fixed-order and resummed/showered predictions for comparisons of Drell-Yan production at the Tevatron and LHC
 - Powheg, MiNNLO for PDF uncertainties and correlations in the mW analysis.
Resbos is needed for the mW shift for CDF, per request from CDF.
 - **Resbos critically needed to complete the analysis!**
- Discrepancies in central value extrapolations : conclusions expected as soon as Resbos available.
- Synchronization between this study and the forthcoming CDF measurement under discussion.