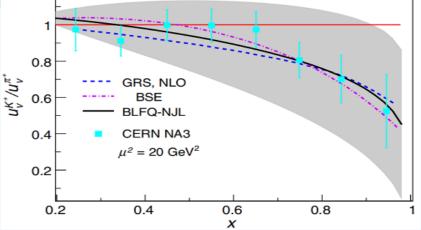


# Conserved charge number fluctuations and their correlations at nonzero n



#### Sheng-Tai Li

(./kyjz2017/201905/t20190508\_5289896.html) Institute of Modern Physics, Chinese Academy of Sciences

> 前,研究人员利用基矢光前量子化(BLFQ)方法,获得其中价夸克的波函数,用以理解π介子和K介子的结构。研究人员在 后,通过考虑夸克与胶子的辐射与湮灭,就可以理解与描述实验上通过高分辨率探针所观测到的介子内部结构。

In collaboration with Heng-Tong Ding, Qi Shi, Xiao-Dan Wang, at

based on EPJA 57(2021) 6,202 (arxiv: 2104.06843)





### **\*** Motivation

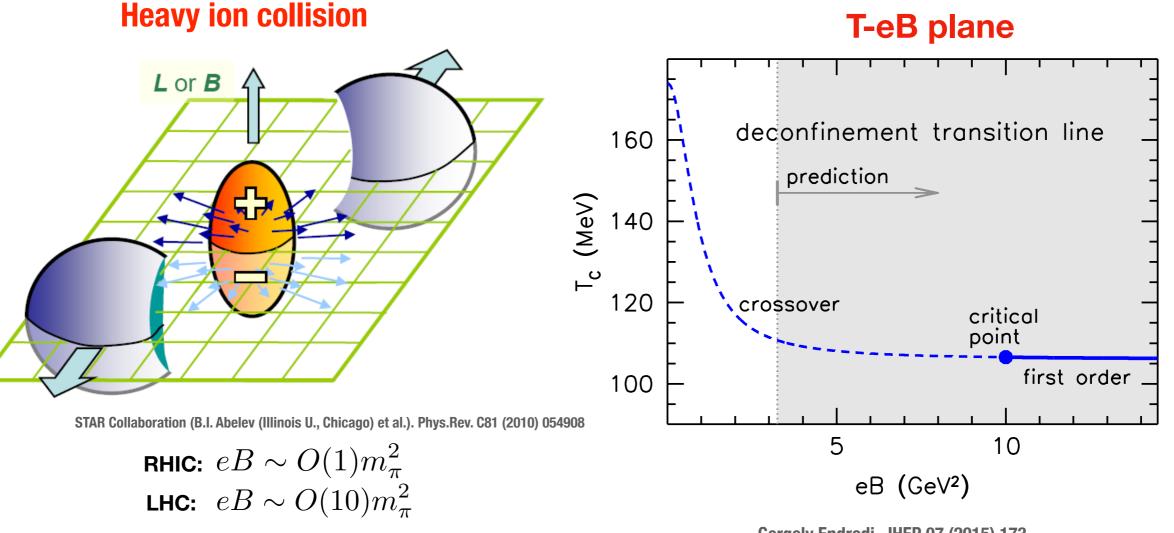
#### \* Conserved number fluctuations and their correlations at finite eB

- **\*** Lattice QCD calculation
- **\*** Ideal gas limit
- **\*** HRG model

### **\*** Lattice results

**\*** Summary and outlook





V. Skokov, etc., Int.J.Mod.Phys.A 24 (2009) 5925-5932 A. Bzdak, etc., Phys. Rev. Lett. 110, 192301 (2013). J. Bloczynski, etc., Phys. Lett. B 718, 1529-1535 (2013). Gergely Endrodi, JHEP 07 (2015) 173

Quantities to detect magnetic fields in Heavy-lon collision
 Possible signatures for a critical end point in T-eB plane

### **Conserved charge number fluctuations**

$$Z(T,V) = \int [DU] \left(\det M_s[U]\right)^{1/4} \left(\det M_u[U]\right)^{1/4} \left(\det M_d[U]\right)^{1/4} e^{-S_G[U]}$$

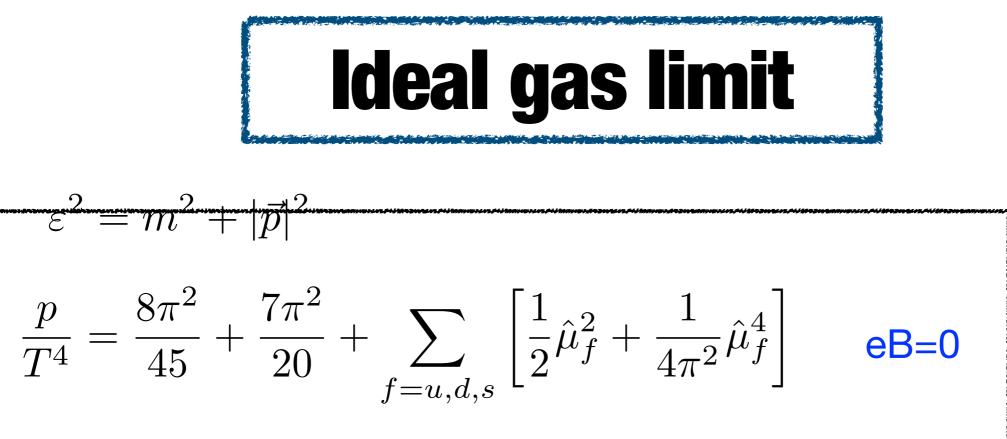
$$\frac{p}{T^4} = \frac{1}{VT^3} \ln Z\left(T, \mu_u, \mu_d, \mu_s\right)$$

$$\hat{\chi}_{ijk}^{uds} = \frac{\partial^{i+j+k} p/T^4}{\partial \left(\mu_u/T\right)^i \partial \left(\mu_d/T\right)^j \partial \left(\mu_s/T\right)^k} \Big| \mu_{u,d,s} = 0$$

$$\hat{\chi}_{ijk}^{BQS} = \frac{\partial^{i+j+k} p/T^4}{\partial \left(\mu_B/T\right)^i \partial \left(\mu_Q/T\right)^j \partial \left(\mu_S/T\right)^k} \Big| \mu_{B,Q,S} = 0$$

Accessible from lattice calculation

HotQCD Collaboration Phys. Rev. D 86 (2012) 034509



Kapusta & Gale, Finite-temperature field theory: Principles and applications

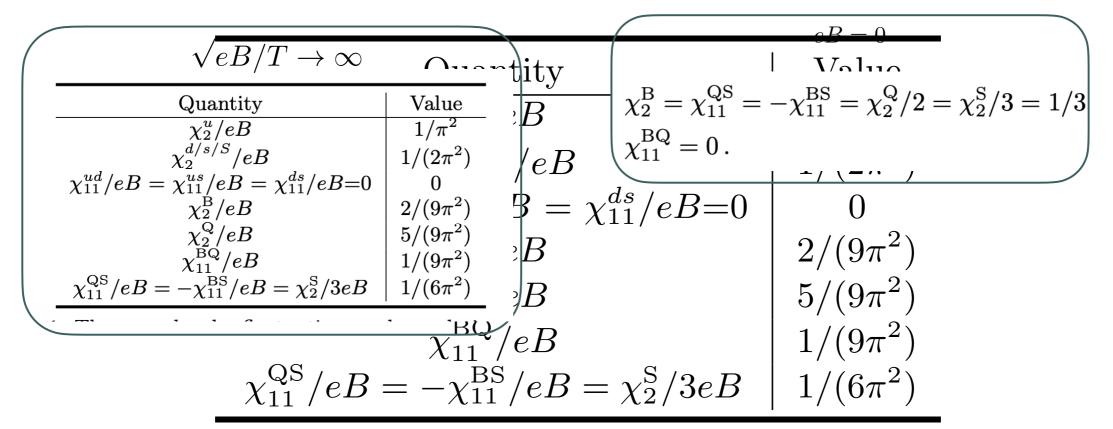
$$=\frac{8\pi^{2p}_{45}}{45}\frac{8\pi^{2}}{T^{4}} = \sum_{f=u,d,s}^{8\pi^{2}} \frac{3|q_{f}| \sum_{\pi^{2}} \pi^{2} \frac{3|q_{f}| B}{\pi^{2} T_{4}^{\frac{1}{2}}}}{\pi^{2} T_{4}^{\frac{1}{2}}} + \left[\frac{\pi^{2} \frac{\hat{\mu}_{f}^{2}}{T^{4}}}{T^{4}} \sum_{l=1}^{\infty} p_{f} \sqrt{l} \sum_{k=1}^{\infty} \frac{(-1)^{k+1}}{k} \cosh(k \hat{\mu}_{f}) \times K_{1}\left(\frac{k\sqrt{2|q_{f}|Bl}}{T}\right)\right]$$

$$p_{f}(B) = 2\frac{\sqrt{2|q_{f}|B}}{T} \sum_{l=1}^{\infty} \sqrt{l} \sum_{k=1}^{\infty} \frac{(-1)^{k+1}}{k} \cosh(k \hat{\mu}_{f}) \times K_{1}\left(\frac{k\sqrt{2|q_{f}|Bl}}{T}\right)$$

$$\text{H.T. Ding, S.-T. Li, Q. Shi and X.-D. Wang, EPJA 57(2021) 6,202}$$

# **Ideal gas limit**

$$\begin{aligned} \frac{\chi_2^{\rm B}}{eB} &= \frac{4}{9\pi^2} \left( \frac{1}{2} + \hat{b} \sum_{l=1}^{\infty} \sqrt{l} \sum_{k=1}^{\infty} (-1)^{k+1} k \times \left[ \sqrt{2} \,\mathrm{K}_1 \left( k \, \hat{b} \, \sqrt{2l} \right) + \mathrm{K}_1 \left( k \, \hat{b} \, \sqrt{l} \right) \right] \right) \\ \frac{\chi_{11}^{\rm BQ}}{eB} &= \frac{4}{9\pi^2} \left( \frac{1}{4} + \hat{b} \sum_{l=1}^{\infty} \sqrt{l} \sum_{k=1}^{\infty} (-1)^{k+1} k \times \left[ 2\sqrt{2} \,\mathrm{K}_1 \left( k \, \hat{b} \, \sqrt{2l} \right) - \mathrm{K}_1 \left( k \, \hat{b} \, \sqrt{l} \right) \right] \right) \\ \end{aligned}$$



Taking derivatives with respect to chemical potentials, and set chemical potentials to zero, then take √eB/T to infinity limit

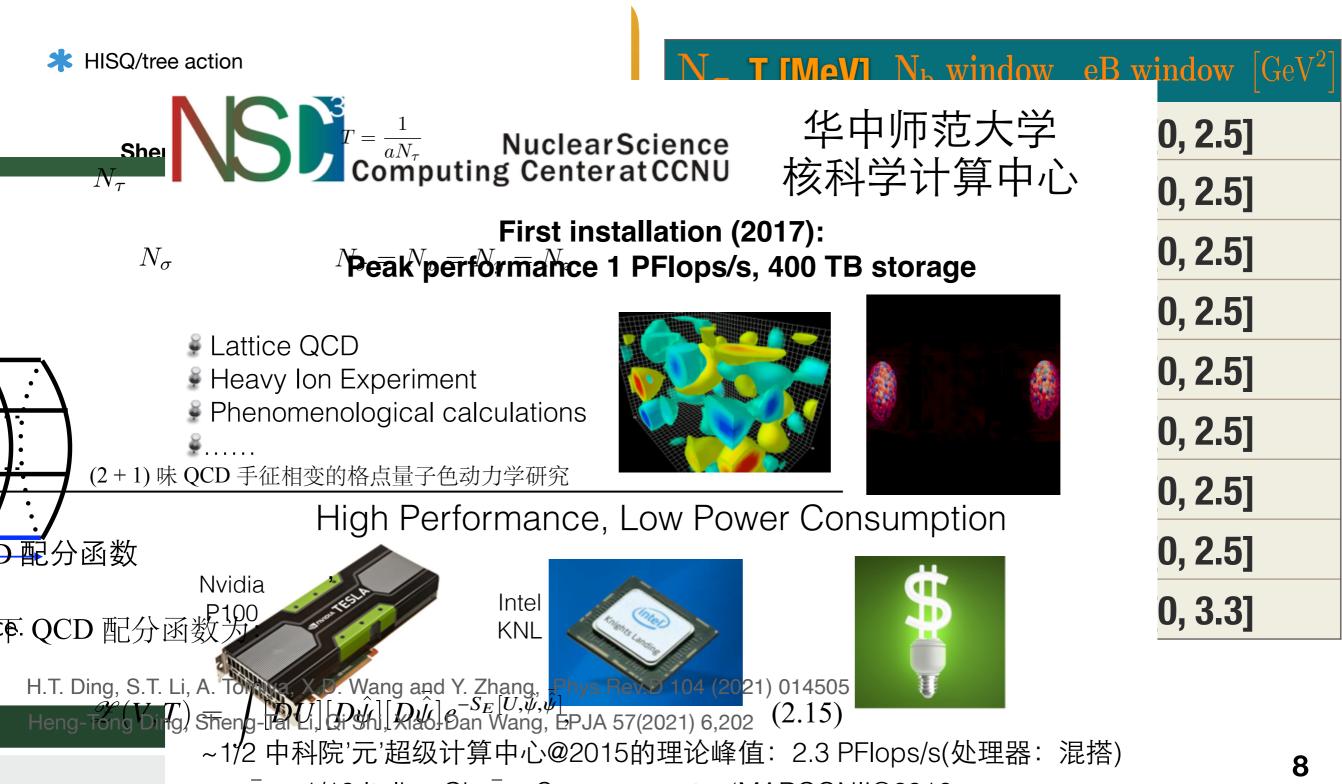
Hadron resonance gas model  

$$\begin{aligned}
y_{n}^{M/B} &= \pm \frac{d_{i}T}{2\pi^{2}} \int_{0}^{\infty} dp |\vec{p}|^{2} \ln \left[ 1 \pm e^{-(E_{n} - \mu_{i})/T} \right] \\
e_{n} &= \sqrt{m_{i}^{2} + |\vec{p}|^{2}} e^{-(E_{n} - \mu_{i})/T} \end{aligned}
e= 0$$
Starting point
$$\begin{aligned}
y_{c}^{M/B} &= \pm \frac{|q_{i}|BT}{2\pi^{2}} \sum_{s_{z} = -s_{i}}^{s_{i}} \sum_{l=0}^{\infty} \int_{0}^{\infty} dp_{z} \ln \left[ 1 \pm e^{-(E_{c} - \mu_{i})/T} \right] \\
e_{z} &= \sqrt{p_{z}^{2} + m_{i}^{2} + 2|q_{i}|B(l + 1/2 - s_{z})} e^{B \neq 0} \end{aligned}$$
Take derivatives with respect to  $\mu$ 

$$\begin{aligned}
x_{2}^{X} &= \frac{B}{2\pi^{2}T} \sum_{i} |q_{i}|X_{i}^{2} \sum_{s_{z} = -s_{i}}^{s_{i}} \sum_{l=0}^{\infty} f(\varepsilon_{0}), \\
&\chi_{1}^{X} &= \frac{B}{2\pi^{2}T} \sum_{i} |q_{i}|X_{i}Y_{i} \sum_{s_{z} = -s_{i}}^{s_{i}} \sum_{l=0}^{\infty} f(\varepsilon_{0}), \quad f(\varepsilon_{0}) = \varepsilon_{0} \sum_{k=1}^{\infty} (\pm 1)^{k+1} kK_{1}(\frac{k\varepsilon_{0}}{T})
\end{aligned}$$

**In our case, we incorporated all the hadrons listed in the PDG up to the mass of 2.5 GeV** Particle Data Group collaboration, Review of Particle Physics, Phys. Rev. D 98 (2018) 030001 Sheng-Tai Li for HotQCD collaboration

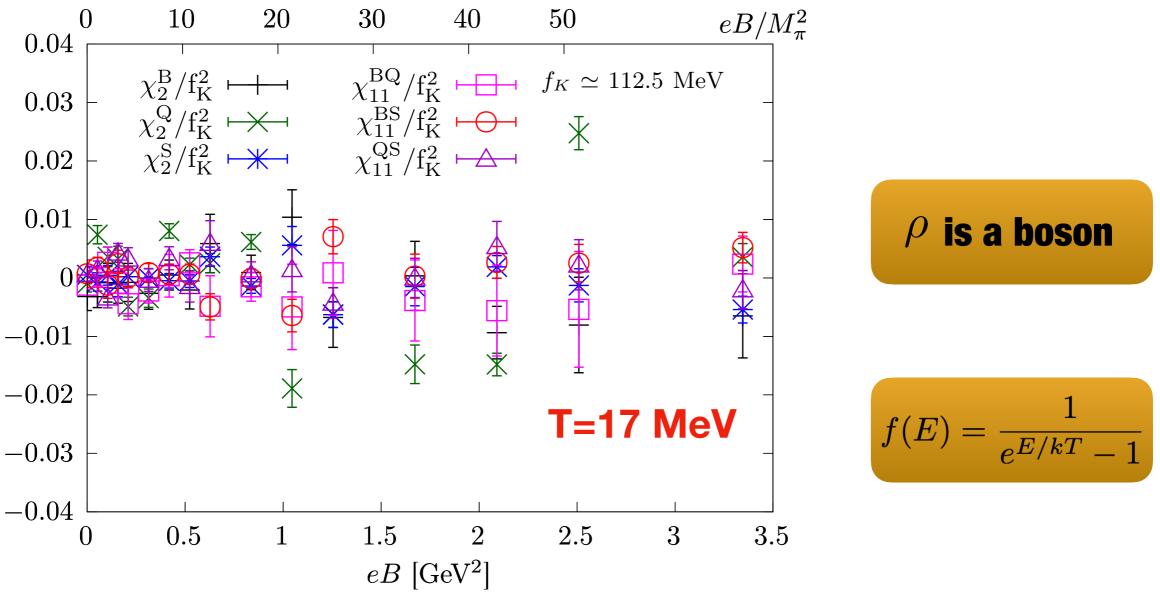




**attice Setup** 

 $c = \frac{1}{2} \frac{1}{2}$ 

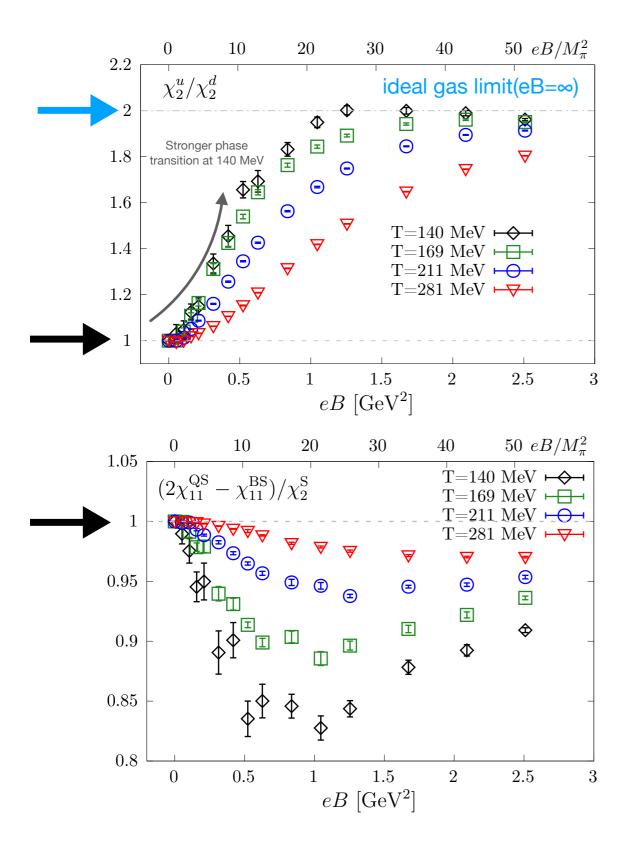
### **Conserved charge fluctuations and correlations at T=0**

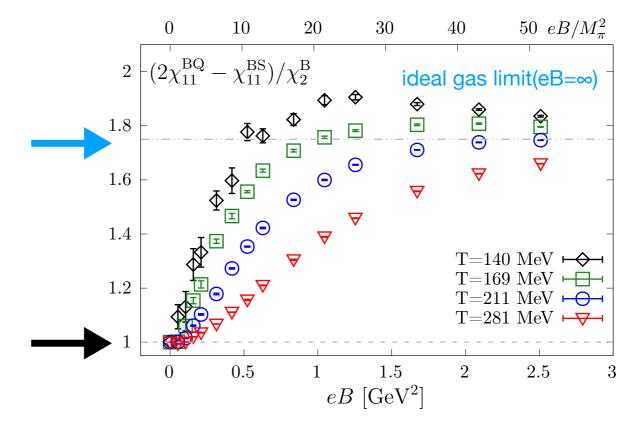


Heng-Tong Ding, Sheng-Tai Li, Qi Shi, Xiao-Dan Wang, EPJA 57(2021) 6,202

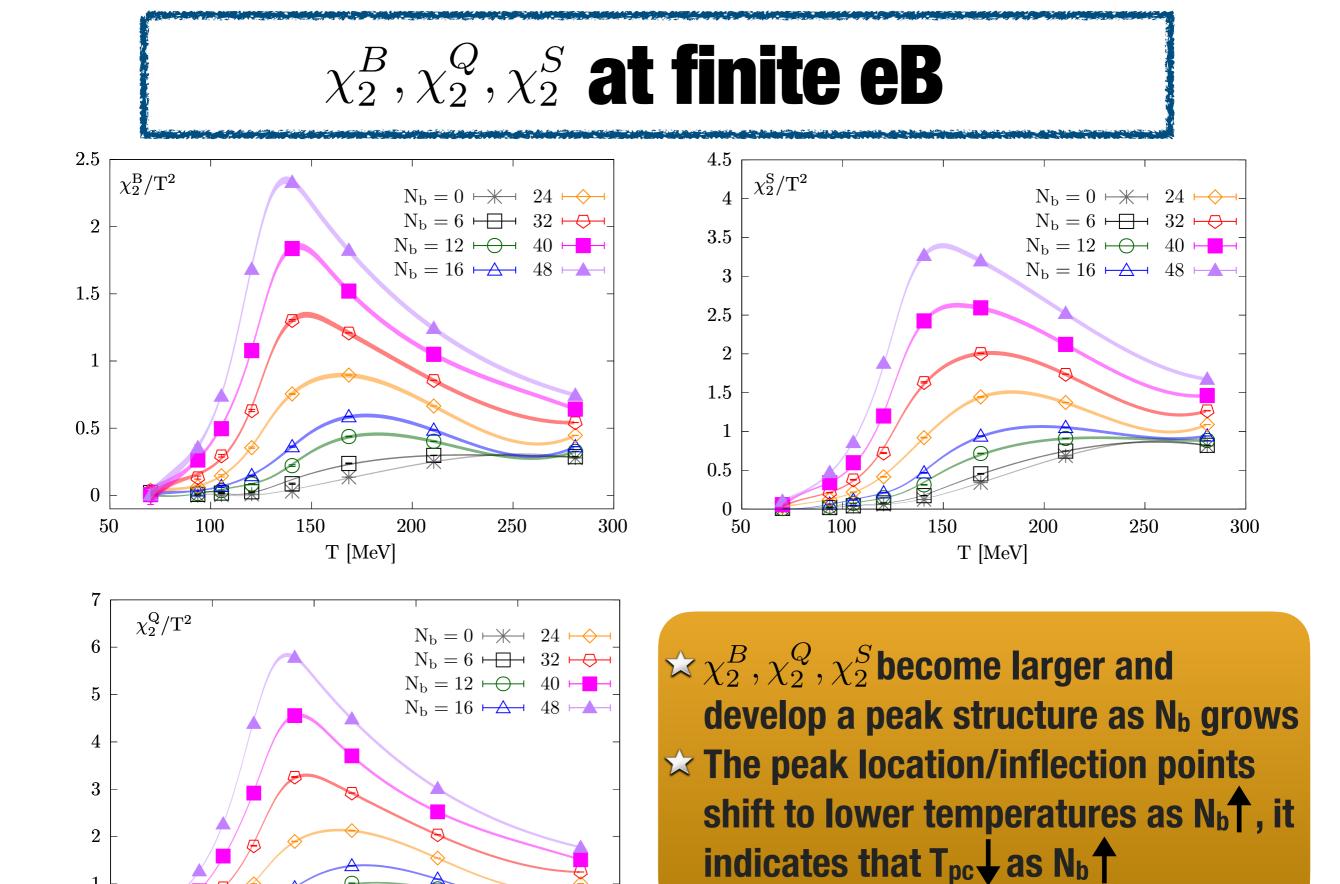
No evidence ( $\chi_2^Q$  is not divergent) for a superconducting phase at T=0 is found

# **Isospin symmetry breaking**

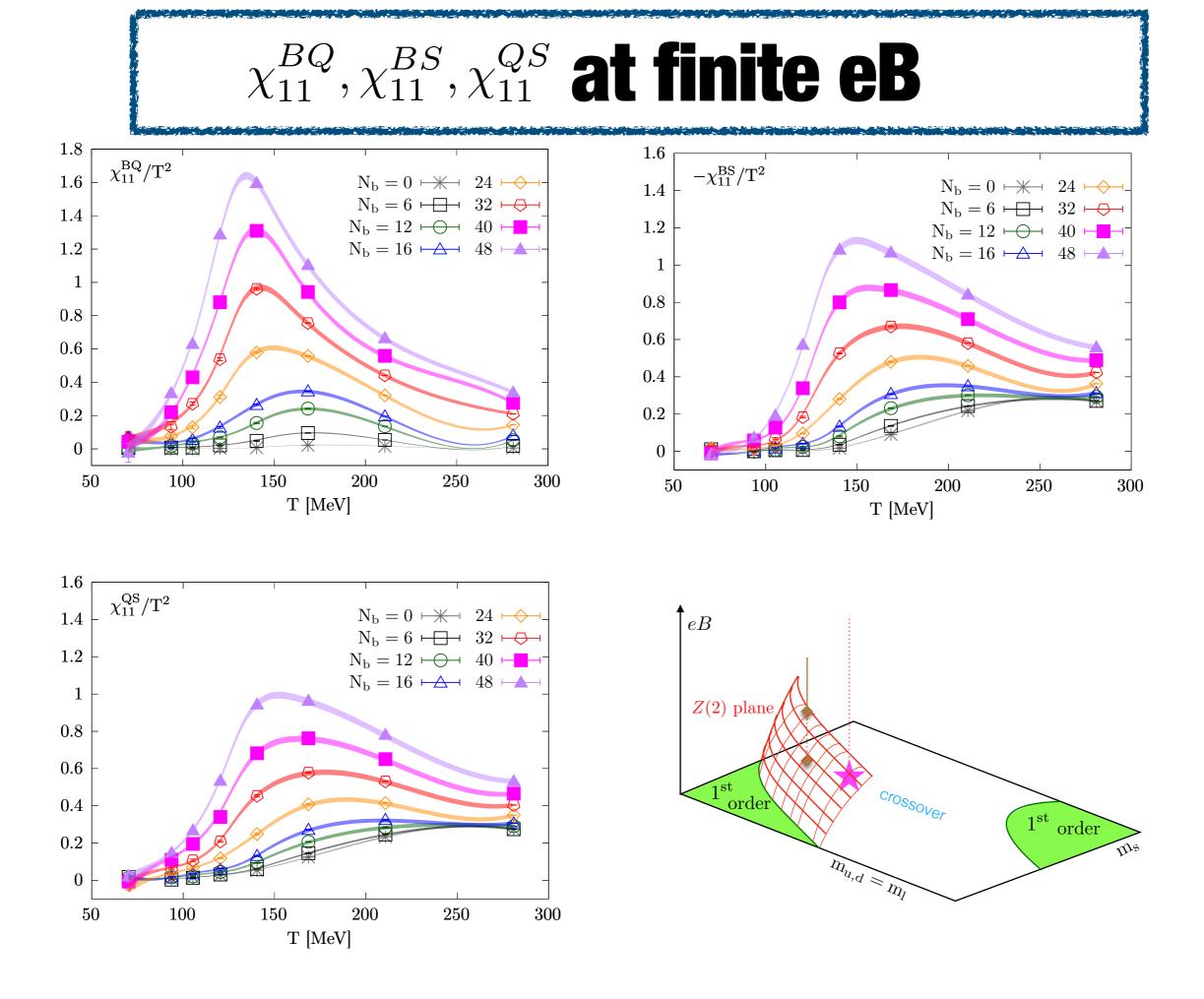




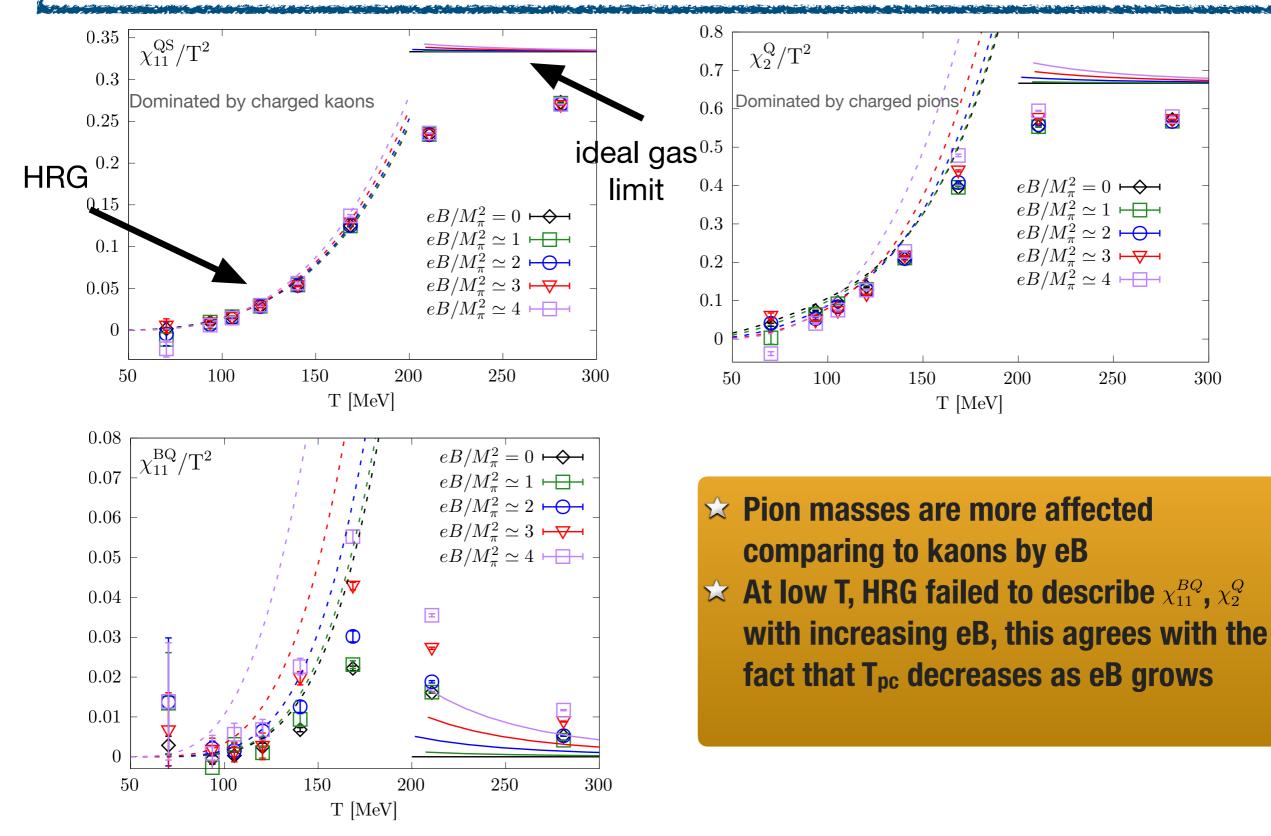
★ → Denotes the isospin symmetric phase
 ★ Denotes the ideal gas limits
 ★ Stronger isospin symmetry breaking at lower T
 ★ (2\chi\_{11}^{BQ} - \chi\_{11}^{BS})/\chi\_{2}^{B} and (2\chi\_{11}^{QS} - \chi\_{11}^{BS})/\chi\_{2}^{S} could be useful in experiment to observe the isospin symmetry breaking



T [MeV]

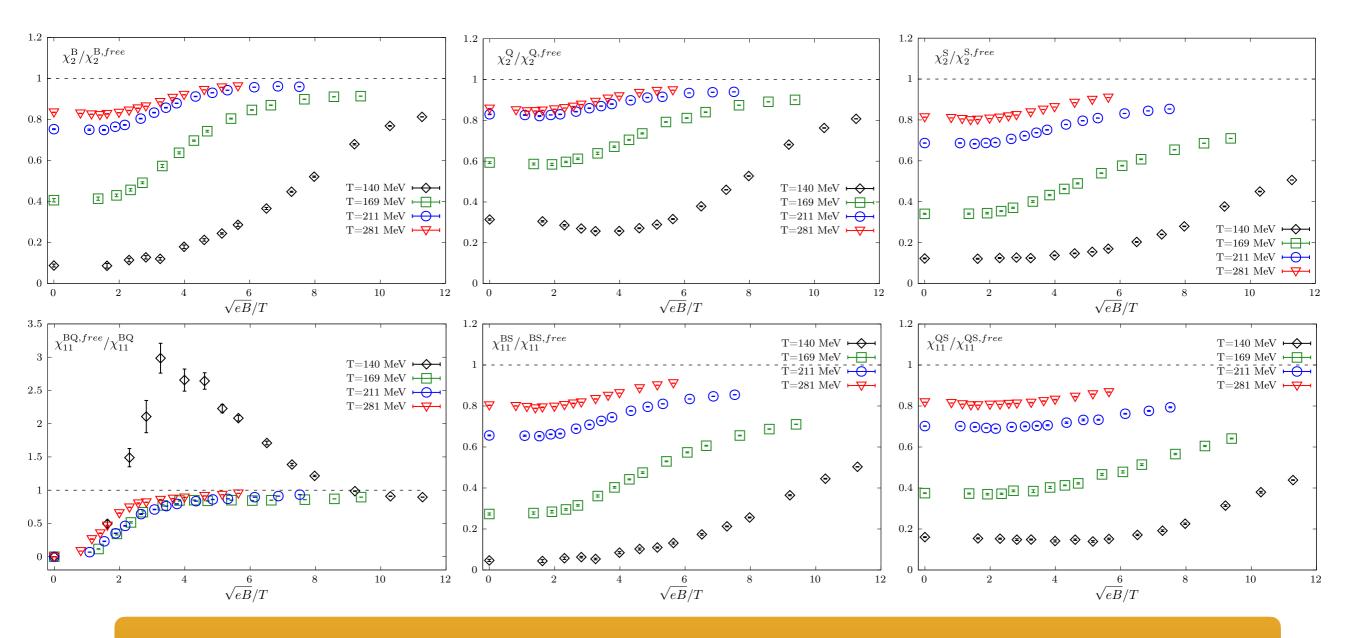


## **Comparisons to HRG & free limit**



Complex eB dependence of charged baryons

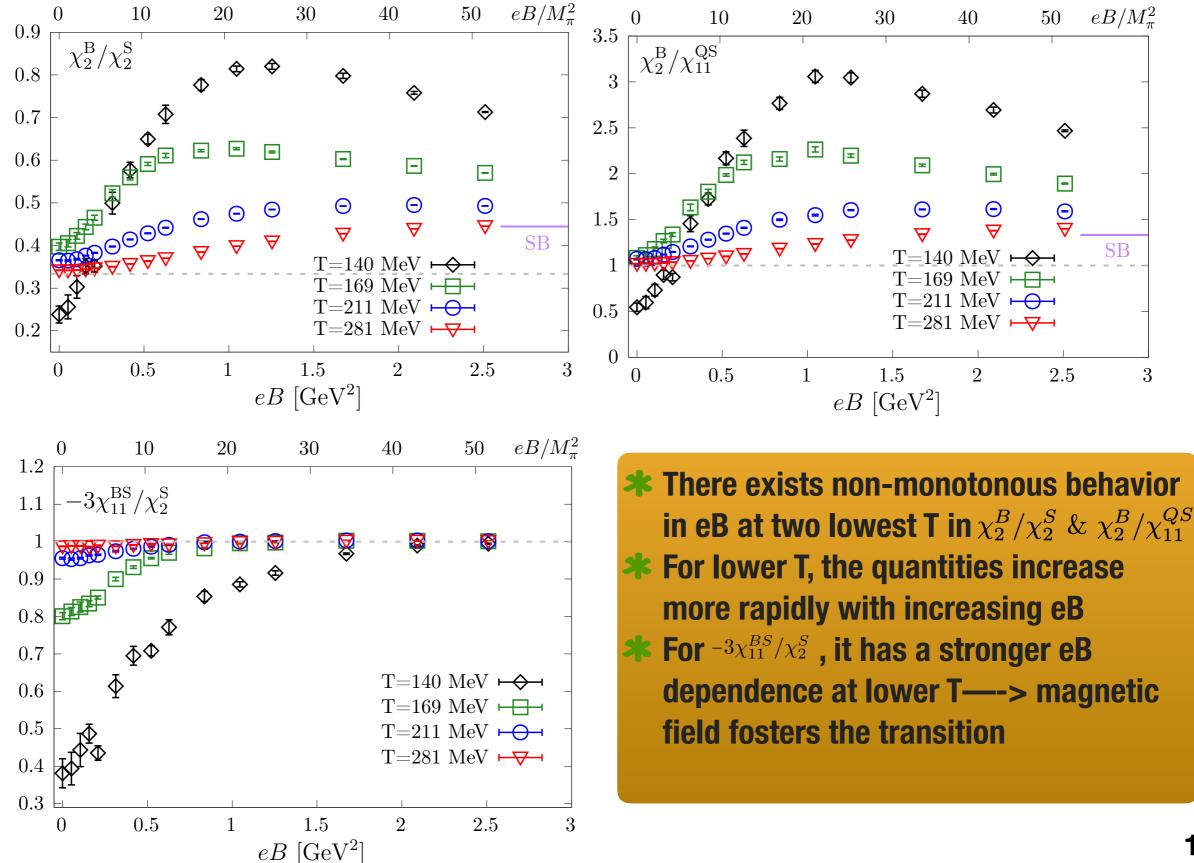
## **Comparisons to HRG & free limit**



T<sub>pc</sub> becomes lower at larger eB, indicating that free theory works at larger eB for fixed T

\* At lower T, degree of freedom in the system changes dramatically from confined hadron phase to deconfined QGP phase

The ratios:  $\chi_2^{\rm B}/\chi_2^{\rm S}$  ,  $\chi_2^{\rm B}/\chi_{11}^{\rm QS}$  and  $-3\chi_{11}^{BS}/\chi_2^{\rm S}$ 



# Summary and outlook

- ☑ No superconducting phase is found in our eB window
- ☑ At lower T, as eB grows, the degree of freedom changes faster
- Several quantities might be useful to probe eB in Heavy ion collision experiments
- A possible Z(2) second order phase transition at sufficiently high eB
- The study at finite eB with physical pion mass is in progress