

# Chromo-electric and chromo-magnetic correlators at high temperature from gradient flow

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**Julian Frederic Mayer-Steudte**

**In collaboration with**

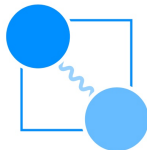
Nora Brambilla (TUM)

Viljami Leino (TUM)

Péter Petreczky (BNL)

Antonio Vairo (TUM)

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- 1 Physical Background
- 2 Discretization of  $G_E$  and  $G_B$
- 3 Analysis and results

# Background: Heavy Quark Diffusion

- Quark Gluon Plasmas can be probed in heavy ion collisions
- HQ momentum is changed by random kicks from the medium  
→ Brownian motion: Follows Langevin dynamics

$$\dot{\mathbf{p}} - \eta \mathbf{p} = \mathbf{f}(t)$$

$$\langle f_i(t) \rangle = 0, \quad \langle f_i(t') f_j(t) \rangle = \kappa \delta_{ij} \delta(t - t') \quad \eta \approx \frac{\kappa}{2MT} \left( 1 - \frac{5T}{2M} \right)$$

- Deriving from the force-force correlator in a Heavy Quark expansion:  
(Bouttefeux and Laine JHEP12(2020))

$$G_E = - \frac{\sum_i \text{Tr} \langle U(\beta; \tau) g E_i(\tau) U(\tau; 0) g E_i(0) \rangle}{3 \text{Tr} \langle U(\beta; 0) \rangle}$$

$$G_B = \frac{\sum_i \text{Tr} \langle U(\beta; \tau) g B_i(\tau) U(\tau; 0) g B_i(0) \rangle}{3 \text{Tr} \langle U(\beta; 0) \rangle}$$

# Background: Heavy Quark Diffusion

- Spectral analysis:

$$G_{E/B}(\tau) = \int_0^\infty \frac{d\omega}{\pi} \rho_{E/B}(\omega) \frac{\cosh\left(\frac{\beta}{2} - \tau\right) \omega}{\sinh \frac{\beta\omega}{2}}$$

$$\kappa_{E/B} = \lim_{\omega \rightarrow 0} \frac{2T \rho_{E/B}(\omega)}{\omega}$$

- Total heavy quark momentum coefficient:

$$\kappa_{\text{tot}} \approx \kappa_E + \frac{2}{3} \langle \mathbf{v}^2 \rangle \kappa_B, \quad \langle \mathbf{v}^2 \rangle \sim T/M$$

- Determination of  $G_E$  and  $G_B$  requires non-perturbative calculations

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## Discretization of $G_E$ and $G_B$

- The chromo electric and magnetic correlators:

$$G_E(\tau) = -\frac{1}{3} \sum_{i=1}^3 \frac{\langle \text{ReTr}[U(\beta, \tau) E_i(\tau) U(\tau, 0) E_i(0)] \rangle}{\langle \text{ReTr}[U(\beta, 0)] \rangle}$$

$$G_B(\tau) = \frac{1}{3} \sum_{i=1}^3 \frac{\langle \text{ReTr}[U(\beta, \tau) B_i(\tau) U(\tau, 0) B_i(0)] \rangle}{\langle \text{ReTr}[U(\beta, 0)] \rangle}$$

- Discretising the  $E$ -field insertion:

(Caron-Huot and Laine JHEP(2009))

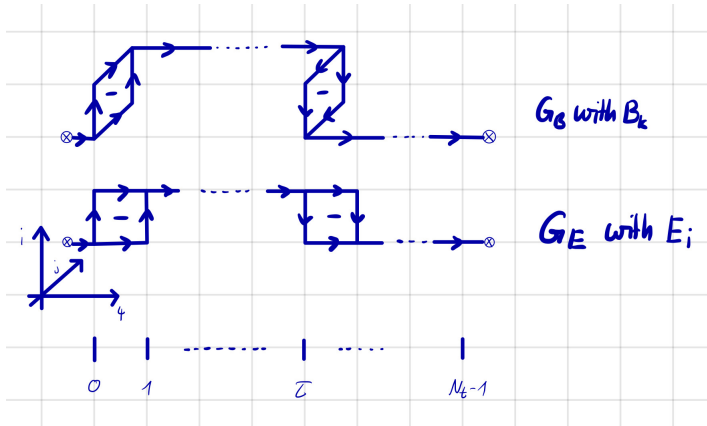
$$E_i(\tau, \mathbf{x}) = U_i(\tau, \mathbf{x}) U_4(\tau, \mathbf{x} + a\hat{\mathbf{e}}_i) - U_4(\tau, \mathbf{x}) U_i(\tau, \mathbf{x} + a\hat{\mathbf{e}}_4)$$

- Discretising the  $B$ -field insertion:

$$B_i(\tau, \mathbf{x}) = \epsilon_{ijk} U_j(\tau, \mathbf{x}) U_k(\tau, \mathbf{x} + a\hat{\mathbf{e}}_j)$$

- Finite extent of  $E$  and  $B$  field requires "renormalization"

# Discretization of $G_E$ and $G_B$



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## Analysis: Lattice setup

- Using quenched lattices
- Lattice parameters:

$N_s$	$N_t$	$\beta$	$N_{\text{conf}}$
48	16	6.872	990
48	20	7.044	990
48	24	7.192	1500
56	28	7.321	1320

(a)  $T = 1.5T_c$

$N_s$	$N_t$	$\beta$	$N_{\text{conf}}$
48	16	14.443	990
48	20	14.635	990
48	24	14.792	1500
56	28	14.925	1950
68	34	15.093	1170

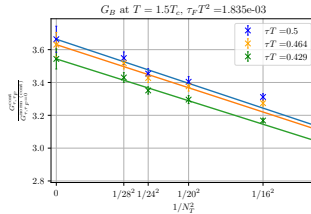
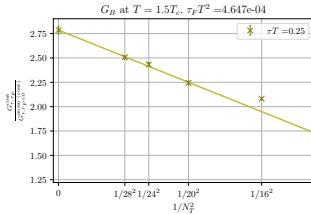
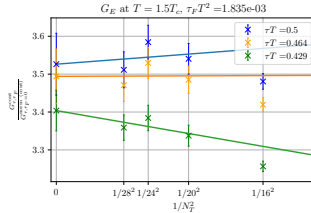
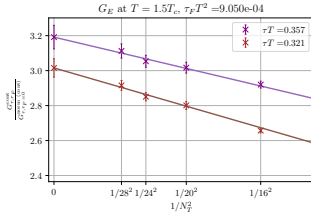
(b)  $T = 10^4 T_c$

- Lattice configurations produced with heat bath and overrelaxation algorithm
- flowtime evolving with Symanzik flow, flow-time range:

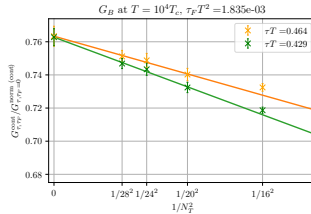
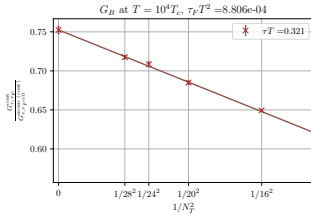
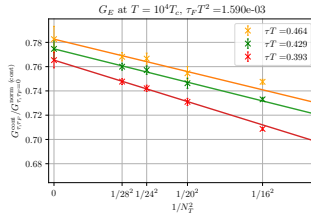
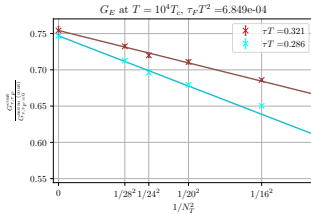
$$a \leq \sqrt{8\tau_F} \leq \frac{\tau - a}{3}$$

- Normalize the correlators with  $G^{\text{norm}} = \frac{G^{\text{latt}}(\tau, \tau_F)}{g^2 C_F} \rightarrow G^{\text{latt}} / G^{\text{norm}}$

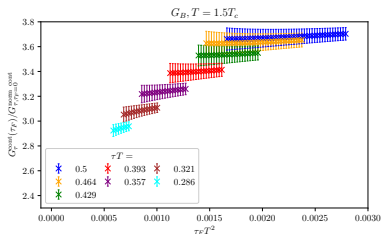
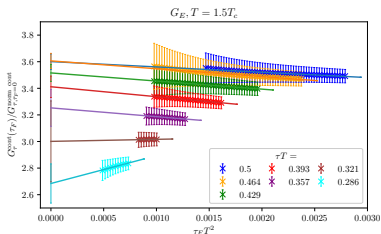
# Analysis: Continuum limit



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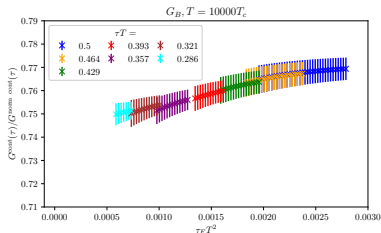
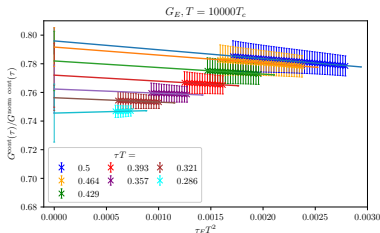


# Analysis: Zero-flowtime limit $T = 1.5T_c$

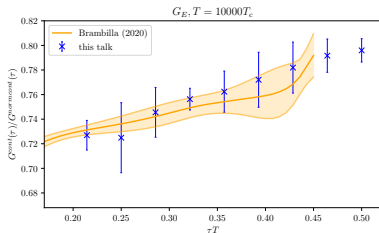
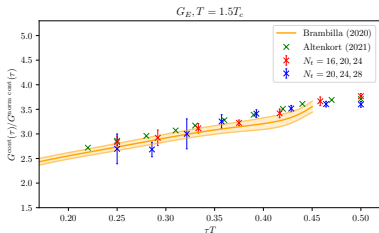


- $G_E$ : perform  $\tau_F \rightarrow 0$  limit extrapolation
- $G_B$ : no  $\tau_F \rightarrow 0$  limit due to non-trivial anomalous dimension of  $G_B$  (Laine JHEP (2021))
- different behavior for  $G_E$  and  $G_B$ :
  - $G_E$  increases for  $\tau_F \rightarrow 0$
  - $G_B$  decreases for  $\tau_F \rightarrow 0$

# Analysis: Zero-flowtime limit $T = 10^4 T_c$

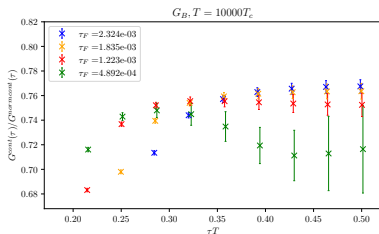
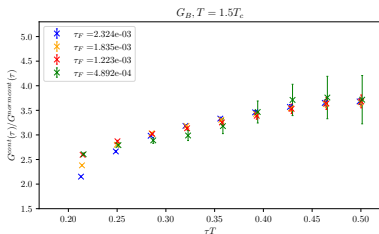


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  - $G_E$  increases for  $\tau_F \rightarrow 0$
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(Altenkort et al. Physical Review D(2021)) (Brambilla et al. Physical Review D(2020))

- $\tau_F \rightarrow 0$  reproduces previous results for both,  $T = 1.5T_c$  and  $T = 10^4T_c$



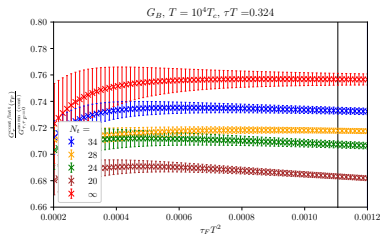
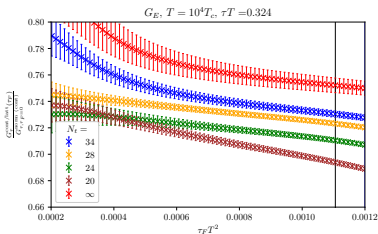
- complete new results for the Chromo-magnetic correlator
- $G_B$  almost  $\tau_F$ -independent for  $\tau T \geq 0.25$  at  $T = 1.5T_c$  and for  $\tau \geq 0.3$  at  $T = 10^4T_c$

Thank you for your attention!



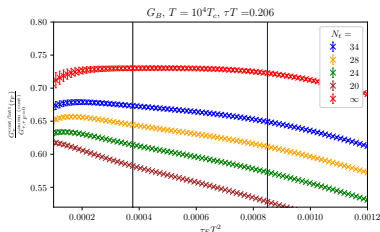
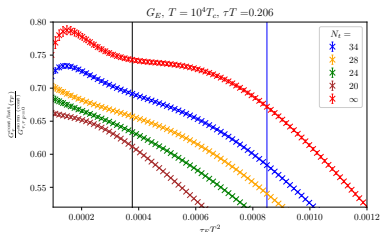
# Analysis: Chromo magnetic correlator

- How does the Chromo magnetic correlator behave under gradient flow?



- Linear behaviour of the correlators up to the maximum flowtime limit
- $G_B$  exhibits a wider flow-independent range

- How does the Chromo magnetic correlator behave under gradient flow?



- $G_E$  breaks down beyond the maximum flowtime limit
- $G_B$  still exhibits a flow-independent range beyond the limit
- Different behaviour might be caused by the anomalous dimension of  $G_B$  (Mikko Laine JHEP (2021))