

Constraints on the CKM matrix and on New Physics in Mixing

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Beauty 2011, 4.4.-8.4.2011, Amsterdam

Focus here on recent work:

Lenz, Nierste &

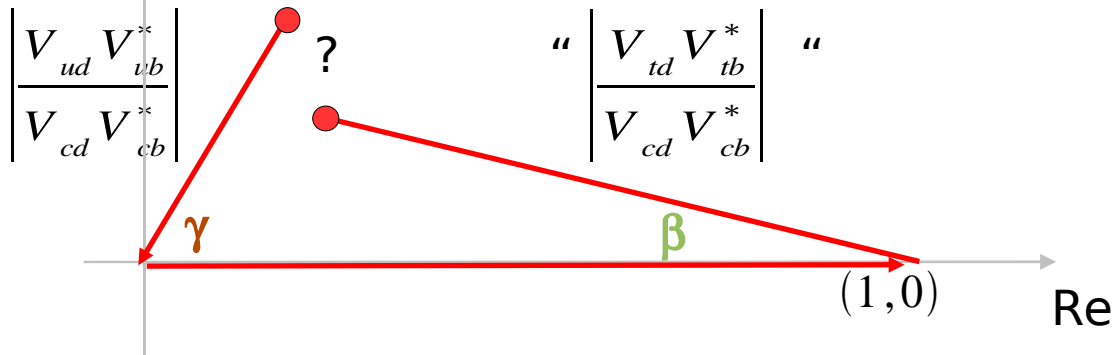
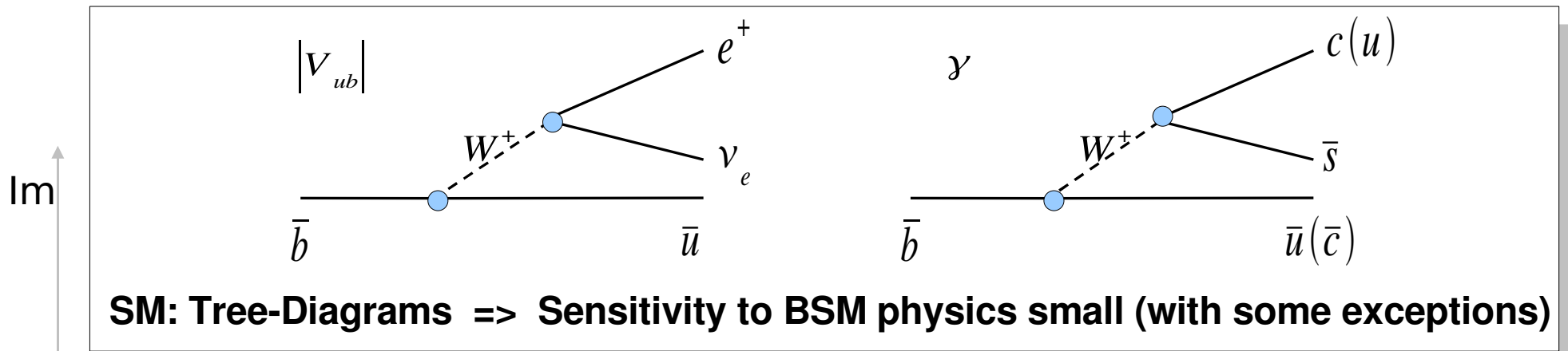
**Charles, Descotes-Genon, Jantsch, Kaufhold, L., Monteil, Niess,
T'Jampens (CKMfitter), «Anatomy of New Physics in $B\text{-}\bar{B}$ mixing»,
PRD 83, 036004 (2011)**

See also:

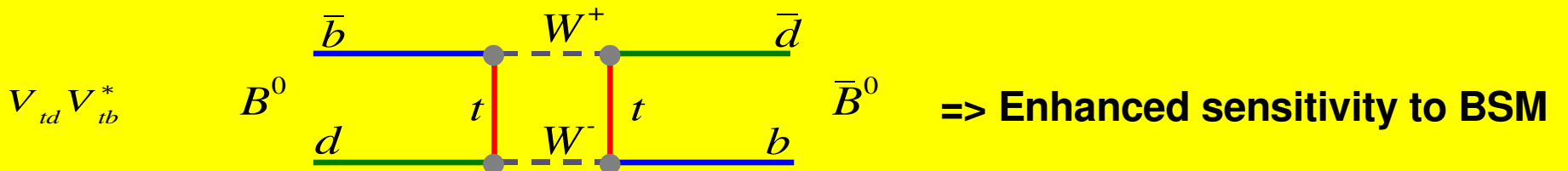
Lunghi, Laiho, van de Water, 1102.3917 [hep-ph]

**Lunghi and Soni, PLB 697, 323 (2011) for UT analysis quantifying
possible New Physics contributions and scale of New Physics**

Hunting for New Physics in FCNC (in particular $\Delta F=2$) processes



SM: $\Delta F=2$ process loop and CKM suppressed



Inputs to the numerical analysis

Tree-level	$ V_{ud} $	0.97425 ± 0.00022
	$ V_{us} $	0.2254 ± 0.0013
	$ V_{cb} $	$(40.89 \pm 0.38 \pm 0.58) \times 10^{-3}$
	$ V_{ub} $	$(3.92 \pm 0.09 \pm 0.45) \times 10^{-3}$
	$B(B^+ \rightarrow \tau^+ \nu)$	$(1.68 \pm 0.31) \times 10^{-4}$
	γ	$(71^{+21}_{-25})^\circ$

B ₀ Mixing	Δm_d	$(0.507 \pm 0.005) ps^{-1}$
	$a_{SL}(B_d)$	$(-47 \pm 46) \times 10^{-4}$
	$\sin 2\beta$	0.673 ± 0.023
	$\cos 2\beta$	> 0
	α	$(89.0^{+4.4}_{-4.2})^\circ$

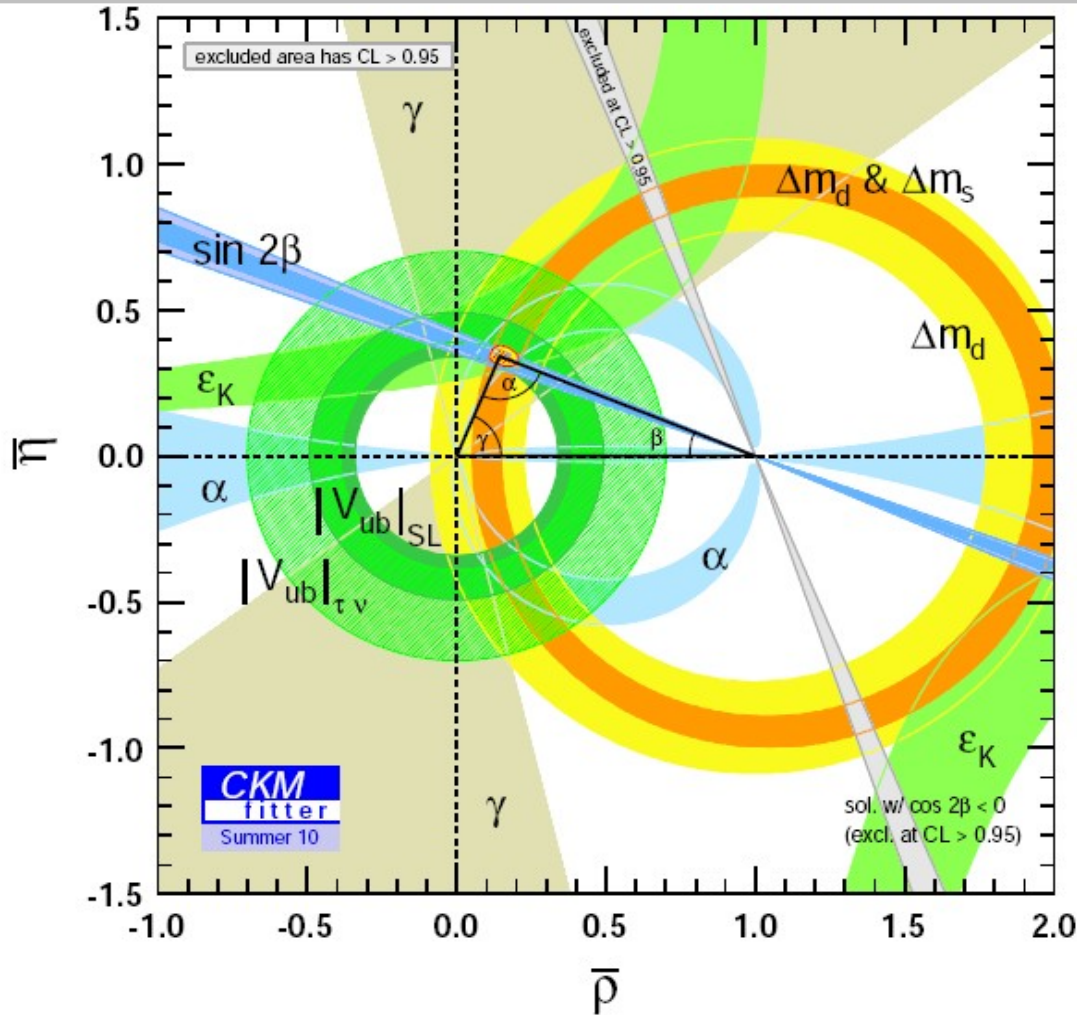
B _s Mixing	Δm_s	$(17.77 \pm 0.12) ps^{-1}$
	$a_{SL}(B_s)$	$(-17 \pm 93) \times 10^{-4}$
	A_{SL}	$(-85 \pm 28) \times 10^{-4}$
	$(\phi_s^\Delta - 2\beta_s) - \Delta\Gamma_s(B_s \rightarrow \psi\phi)$ (CDF-D0 av. (2.8 fb ⁻¹))	

Kaons	ϵ_K	$(2.229 \pm 0.010) \times 10^{-3}$
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Theory parameter $\pm \sigma(\text{stat}) \pm \sigma(\text{theo, Rfit})$

B Mixing	f_{B_s}	$(231 \pm 9 \pm 15) \text{ MeV}$
	$B_{B_s}(m_b)$	$0.841 \pm 0.013 \pm 0.020$
	f_{B_s}/f_{B_d}	$1.209 \pm 0.007 \pm 0.023$
	B_{B_s}/B_{B_d}	$1.01 \pm 0.01 \pm 0.03$
	$\hat{\eta}_B$	0.8393 ± 0.0034
Kaon Sector	$m_t(m_t)$	$(165.017 \pm 1.156 \pm 0.11) \text{ GeV}$
	\hat{B}_K	$0.724 \pm 0.004 \pm 0.067$
	κ_ϵ	$0.940 \pm 0.013 \pm 0.023$
	η_{tt}	0.5765 ± 0.0065
	η_{ct}	0.47 ± 0.04
	η_{cc}	$(1.30 \pm 0.35)(1.29 \text{ GeV}/m_c)^{1.1}$
	$m_c(m_c)$	$(1.286 \pm 0.013 \pm 0.040) \text{ GeV}$
	$\tilde{B}_{S,B_s}/\tilde{B}_{S,B_d}$	$1.01 \pm 0 \pm 0.03$
	$\tilde{B}_{S,B_s}(m_b)$	$0.91 \pm 0.03 \pm 0.12$
	B_{R_0}	1.0 ± 0.5
$\Gamma_{-12}/(M_{-12})$	$B_{\tilde{R}_1}$	1.0 ± 0.5
	B_{R_1}	1.0 ± 0.5
	$B_{\tilde{R}_2}$	$1.0 \pm 0 \pm 0.5$
	$B_{\tilde{R}_3}$	$1.0 \pm 0 \pm 0.5$

CKM fit within the SM



- Qualitative picture:
b→u & b→d transitions fit into CKM mechanism and are in agreement with s→d transitions

Quantity	Central \pm C.L. $\equiv 1\sigma$	\pm C.L. $\equiv 2\sigma$	\pm C.L. $\equiv 3\sigma$
A	$0.815^{+0.011}_{-0.029}$	$0.815^{+0.020}_{-0.038}$	$0.815^{+0.029}_{-0.046}$
λ	$0.22543^{+0.00077}_{-0.00077}$	$0.2254^{+0.0015}_{-0.0015}$	$0.2254^{+0.0023}_{-0.0023}$
$\bar{\rho}$	$0.144^{+0.029}_{-0.018}$	$0.144^{+0.054}_{-0.028}$	$0.144^{+0.068}_{-0.037}$
$\bar{\eta}$	$0.342^{+0.016}_{-0.016}$	$0.342^{+0.030}_{-0.028}$	$0.342^{+0.045}_{-0.037}$

- NP (TeV scale?) suppressed wrt SM
- By how much? Focus on NP in mixing including Minimal Flavour Violation

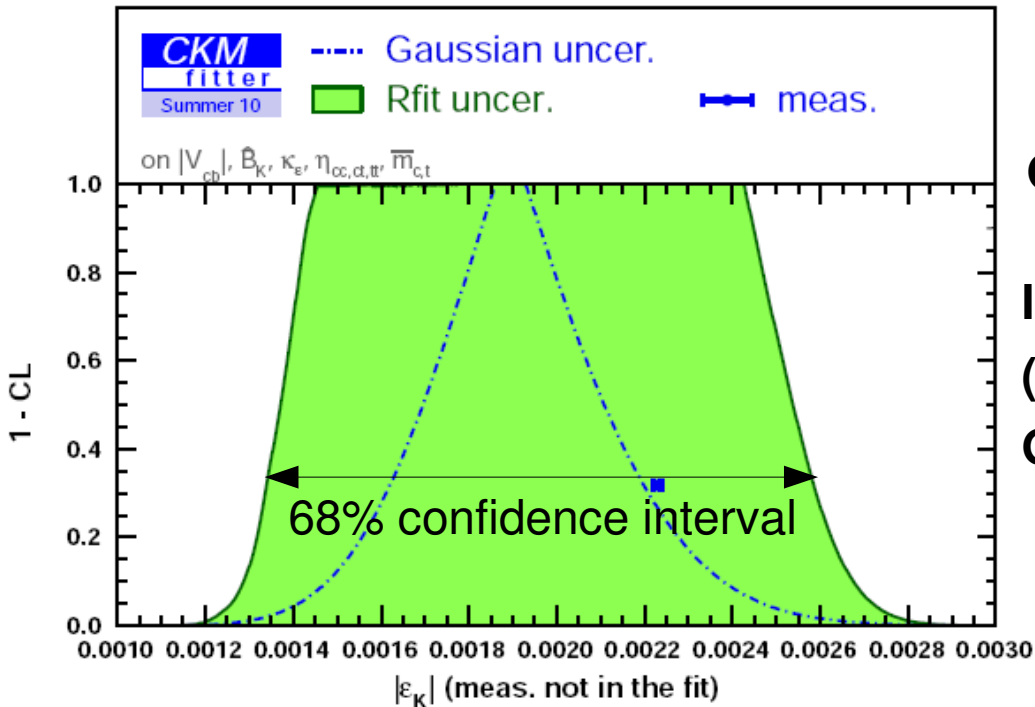
However: quantitatively interesting “Anomalies”/”deviations”

Kaon sector: ϵ_K

B_d sector: $\sin 2\beta$ & $B \rightarrow \tau \nu$

B_s sector: $A_{SL}(D0)$ & $\phi_s^\Delta - 2\beta_s$

ϵ_K anomaly ?



Theory Prediction

Gaussian errors: $10^3 |\epsilon_K| = 1.89^{+0.26}_{-0.23} \quad (1.2 \sigma)$

Inputs from Lunghi
(FPCP2010) and

Gaussian errors: $10^3 |\epsilon_K| = 1.77^{+0.18}_{-0.16} \quad (2.4 \sigma)$

Deviation sensitive to B_K input (Laiho, Lunghi, van de Water @ CKM2010: 0.724 ± 0.020)

+ other inputs/CKM params, in particular: $|\epsilon_K| \sim |V_{cb}|^4$

$$|V_{cb}|(\text{Lunghi, FPCP10}) = 40.43 \cdot 10^{-3}$$

$$|V_{cb}|(\text{CKMfitter}) = 40.89 \cdot 10^{-3} \quad \Rightarrow \quad 10^3 \cdot |\epsilon_K|: 1.77 \rightarrow 1.85$$

$\sin 2\beta$ - $B \rightarrow \tau \nu$ anomaly

$$\mathcal{B}(B \rightarrow \tau \nu) = \frac{G_F^2 m_{B^+} m_\tau^2}{8\pi} \left(1 - \frac{m_\tau^2}{m_{B^+}^2}\right)^2 |V_{ub}|^2 f_B^2 \tau_{B^+}$$

* **Predicted:** $(0.764^{+0.087}_{-0.072}) \times 10^{-4}$

$\updownarrow 2.9\sigma$

* **Measured:** $(1.68 \pm 0.31) \times 10^{-4}$

Recoil	Belle (10^{-4})	BABAR (10^{-4})
Hadronic	$1.79^{+0.56+0.46}_{-0.49-0.51}$	$1.80^{+0.57}_{-0.54} \pm 0.26$
DlvX	$1.54^{+0.38+0.29}_{-0.37-0.31}$	$1.7 \pm 0.8 \pm 0.2$

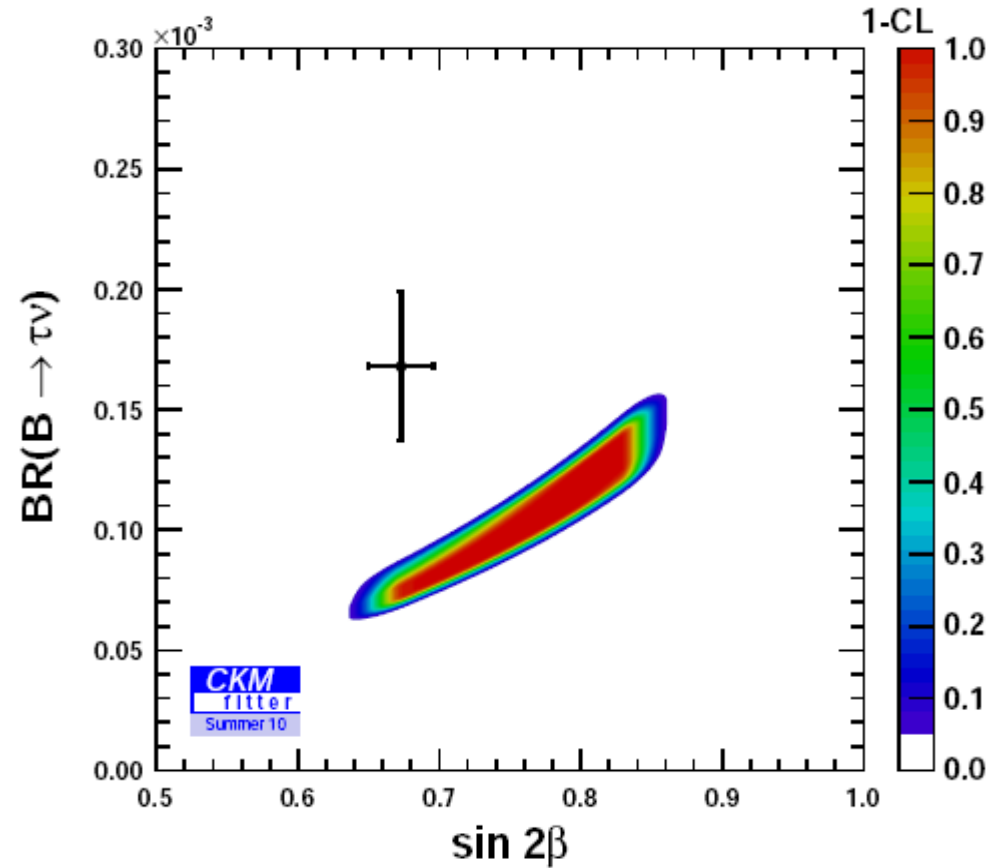
* **Not driven by $|V_{ub}|$ from $B \rightarrow \pi \ell \nu / X_u \ell \nu$ as**

$|V_{ub}|$ well constrained from α and β :

$$|V_{ub}|_{pred} = (3.56^{+0.15}_{-0.20}) \times 10^{-3}$$

Average for $B \rightarrow \pi \ell \nu$ & $X_u \ell \nu$ used:

$$|V_{ub}| = (3.92 \pm 0.09 \pm 0.45) \times 10^{-3}$$

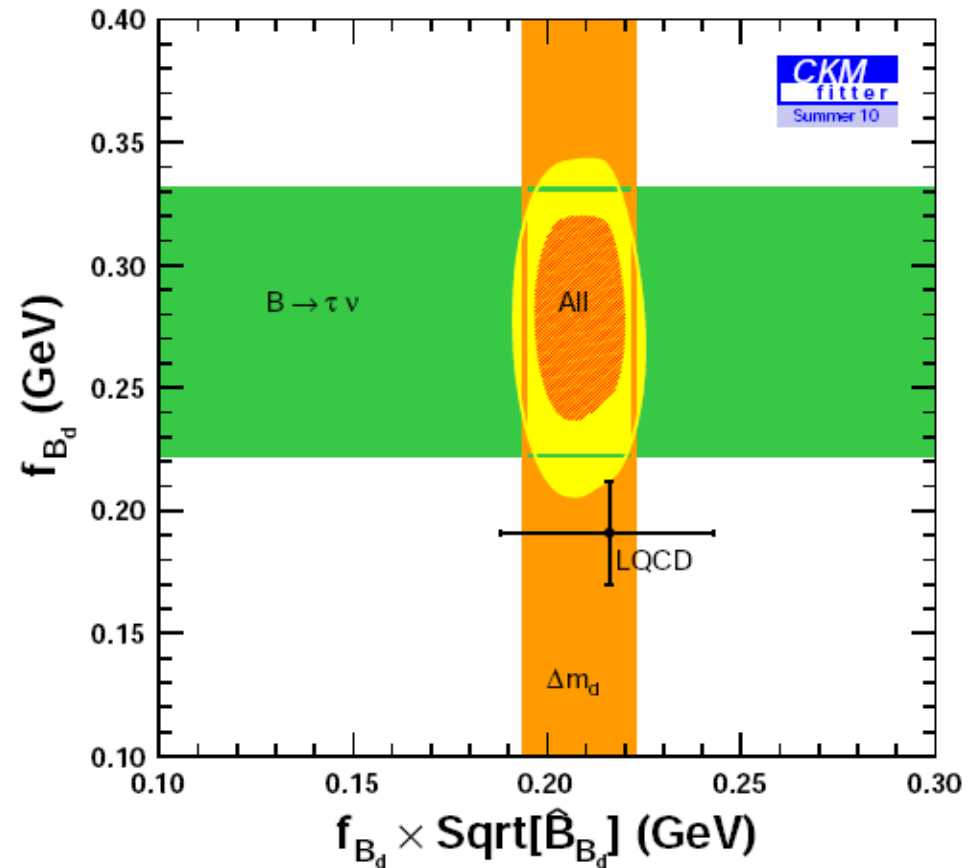
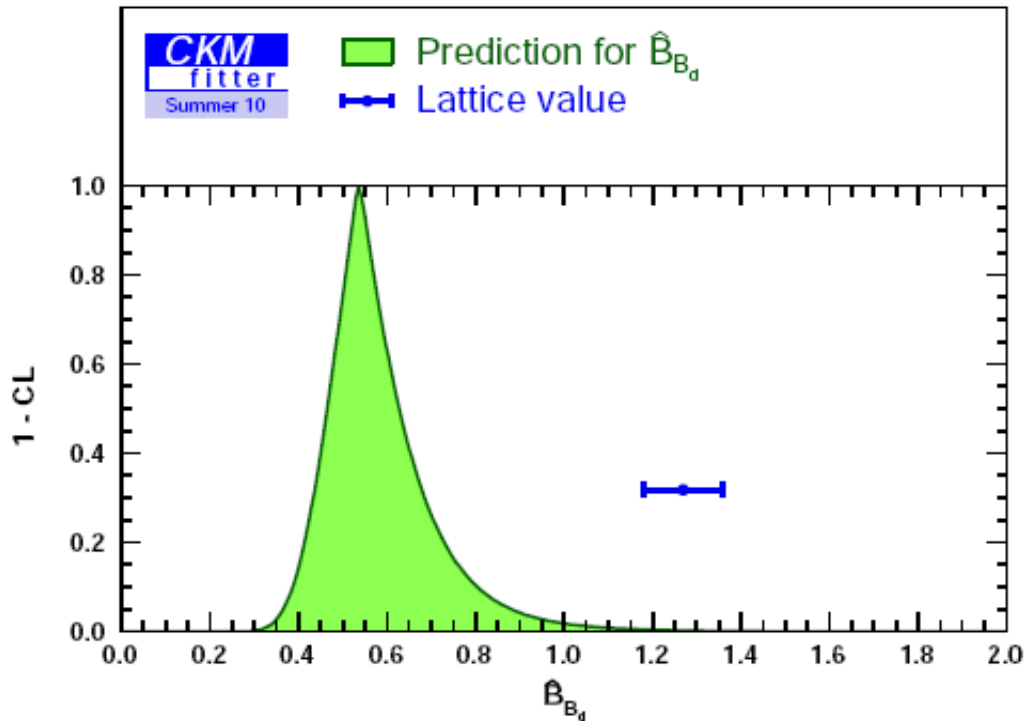


$\sin 2\beta$ - $B \rightarrow \tau \nu$ anomaly

- * Experimental effect: fluctuation, background, ...?
- * Bias in LQCD calculation of f_{B_d} ?
- * NP in $B \rightarrow \tau \nu$ (difficult) and/or $\sin 2\beta$ (easier) ?

* In this ratio f_{B_d} cancels:

$$\frac{\mathcal{B}(B \rightarrow \tau \nu)}{\Delta m_d} = \frac{3\pi}{4} \frac{m_\tau^2}{m_W^2 S(x_t)} \left(1 - \frac{m_\tau^2}{m_{B^+}^2}\right)^2 \tau_{B^+} \times \frac{1}{\hat{\mathcal{B}}_{B_d} \eta_B} \frac{1}{|V_{ud}|^2} \left(\frac{\sin \beta}{\sin \gamma}\right)^2$$



* If f_{B_d} is the culprit: B_{B_d} is also off in such a way that $\Delta m_d(\text{meas})$ & $\Delta m_d(\text{pred})$ fit

New Physics in Mixing: Assumptions

1. 3x3 CKM-unitarity
2. SM4FC: $b \rightarrow q_1 \bar{q}_2 q_3$ ($q_1 \neq q_2 \neq q_3$) SM only
3. Neglect NP in decay in $B_d \rightarrow J/\Psi K$, $B_s \rightarrow J/\Psi \phi$
4. Leptonic meson decays are SM-like (e.g. no charged Higgs)
5. Γ_{12} not affected by NP
6. NP shows only up in M_{12}

B Mixing:

$$M_{12}^q \equiv M_{12}^{\text{SM},q} \cdot \Delta_q, \quad \Delta_q \equiv |\Delta_q| e^{i\phi_q^\Delta}$$

K Mixing:

$$M_{12}^K \equiv \frac{\langle K | H^{|\Delta S|=2} | \bar{K} \rangle}{2M_K} = (V_{ts} V_{td}^*)^2 M_{12}^{tt} + 2V_{ts} V_{td}^* V_{cs} V_{cd}^* M_{12}^{ct} + (V_{cs} V_{cd}^*)^2 M_{12}^{cc}$$

$$M_{12}^{ij} = M_{12}^{\text{SM},ij} \Delta_K^{ij} \equiv M_{12}^{\text{SM},ij} |\Delta_K^{ij}| e^{i\phi_K^{\Delta ij}}$$

B sector simpler than K sector: charm contributions suppressed in M_{12}^q

New Physics in Mixing

Scenario I:

No assumption about flavour structure of NP contributions to mixing

(E.g.: MSSM with general flavour structure of soft breaking terms and small $\tan\beta$)

$$\begin{aligned} \Rightarrow \epsilon_K &= \frac{\kappa_\epsilon}{\sqrt{2}} e^{i\phi_\epsilon} \left[\frac{\text{Im}M_{12}^{(6)}}{\Delta M} \right] = C_\epsilon \kappa_\epsilon e^{i\phi_\epsilon} \hat{\mathcal{B}}_K \left[\text{Im}[(V_{cs} V_{cd}^*)^2 \Delta_K^{cc}] \eta_{cc} S\left(\frac{\bar{m}_c^2}{M_W^2}\right) \right. \\ &\quad \left. + \text{Im}[(V_{ts} V_{td}^*)^2 \Delta_K^{tt}] \eta_{tt} S\left(\frac{\bar{m}_t^2}{M_W^2}\right) \right. \\ &\quad \left. + 2 \text{Im}(V_{ts} V_{td}^* V_{cs} V_{cd}^* \Delta_K^{ct}) \eta_{ct} S\left(\frac{\bar{m}_c^2}{M_W^2}, \frac{\bar{m}_t^2}{M_W^2}\right) \right] \end{aligned}$$

=> Kaon sector: 3 independent parameters but only one observable

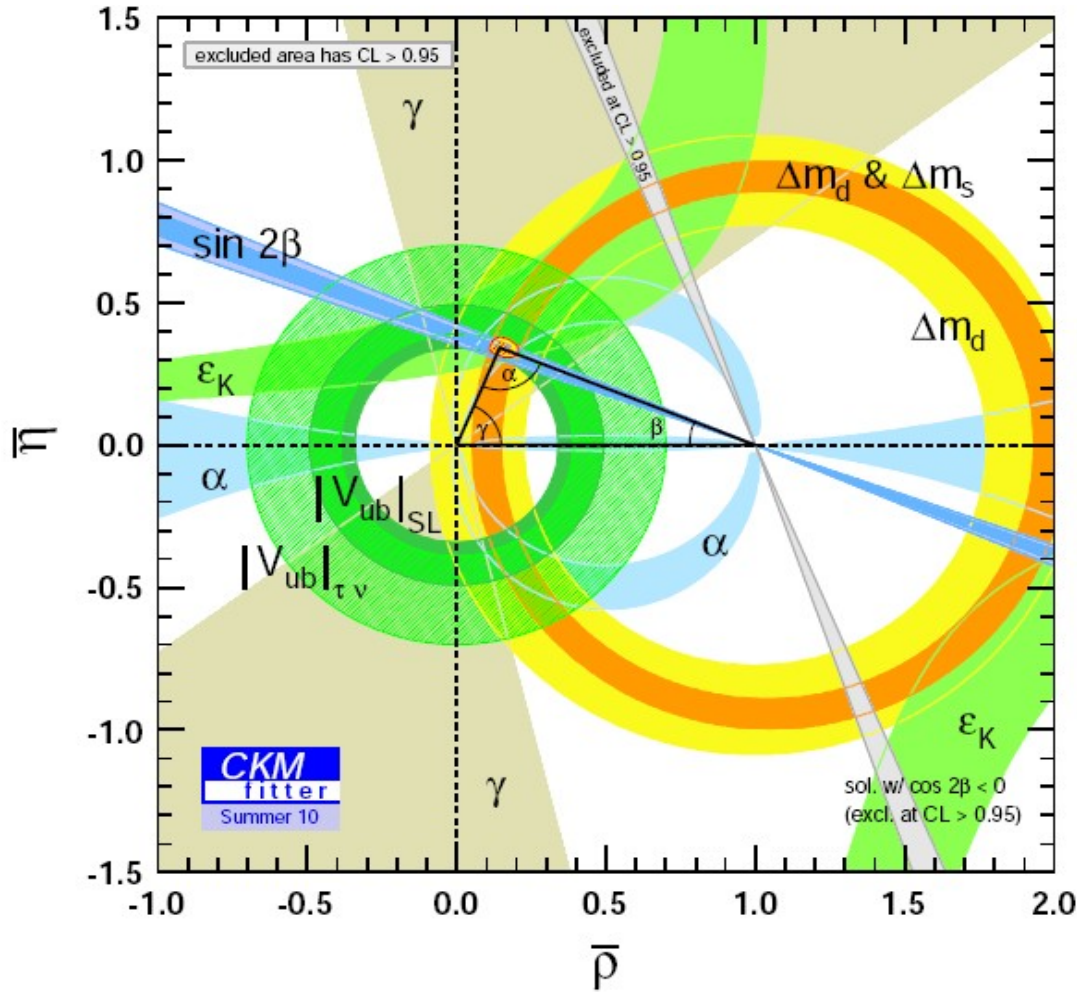
=> Consider only B_d and B_s sector: 2 new complex parameters Δ_s, Δ_d

New Physics in Mixing: Scenario I (no relation btw sectors)

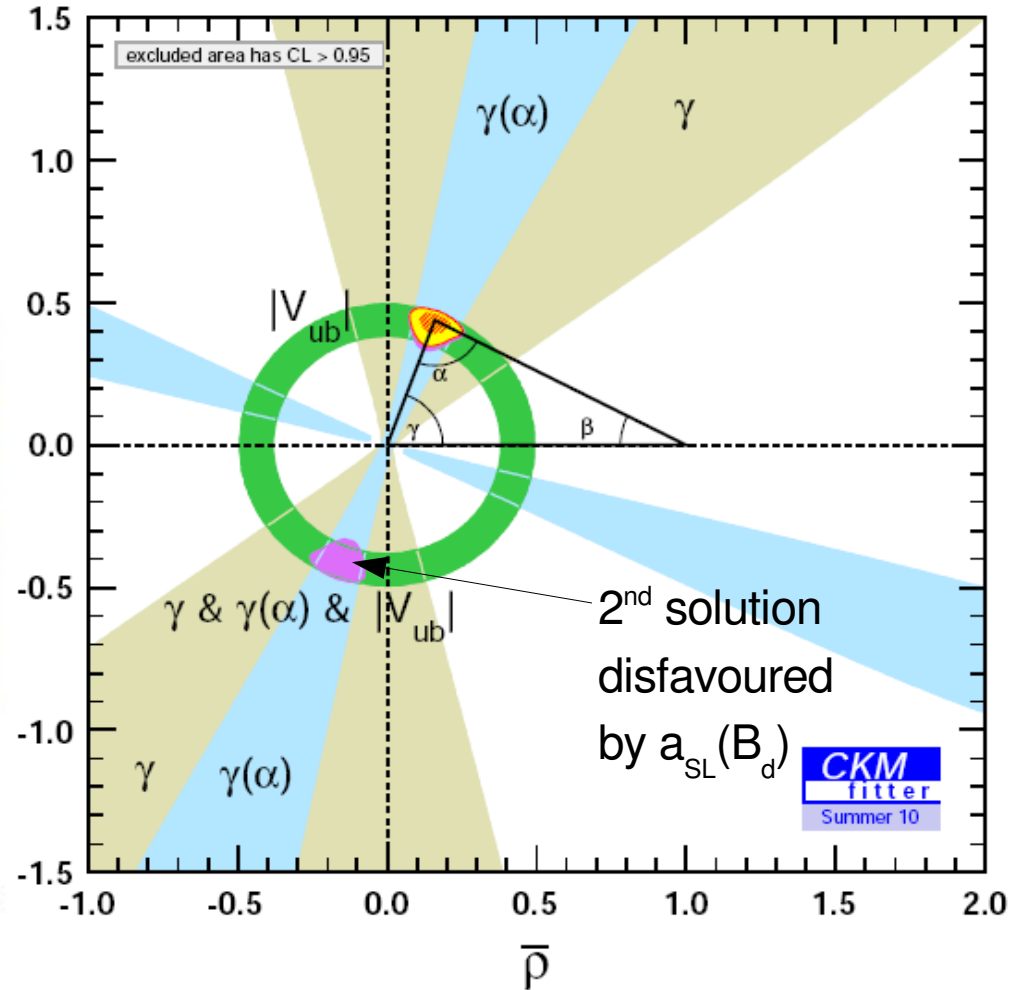
Even in the presence of NP in B-mixing:

γ can be obtained from “ α ” ($\pi - \gamma - \beta - \phi_d^\Delta / 2$) and “ β ” ($2\beta + \phi_d^\Delta$) as ϕ_d^Δ drops out

UT in SM fit

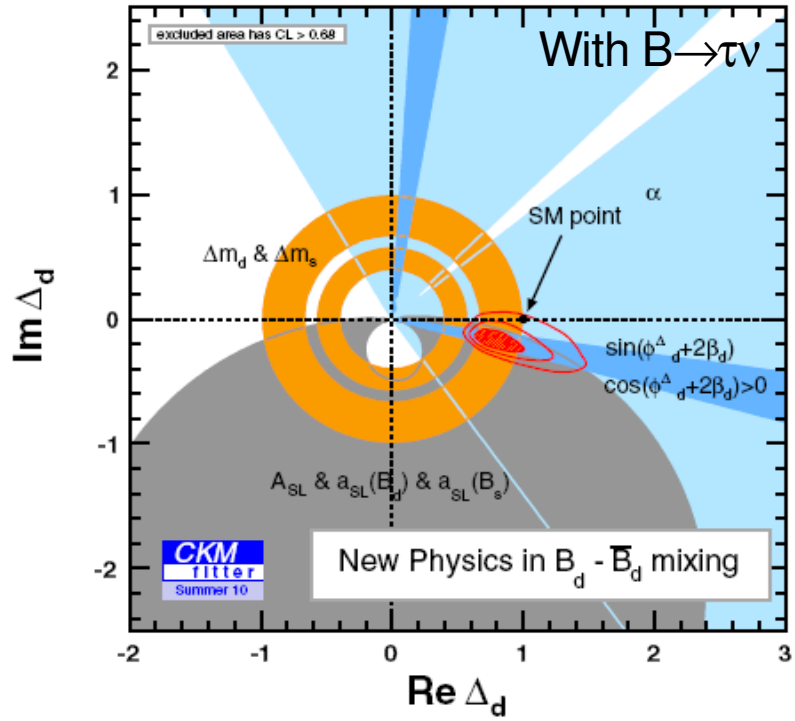


UT in Scenario I: “Reference UT”

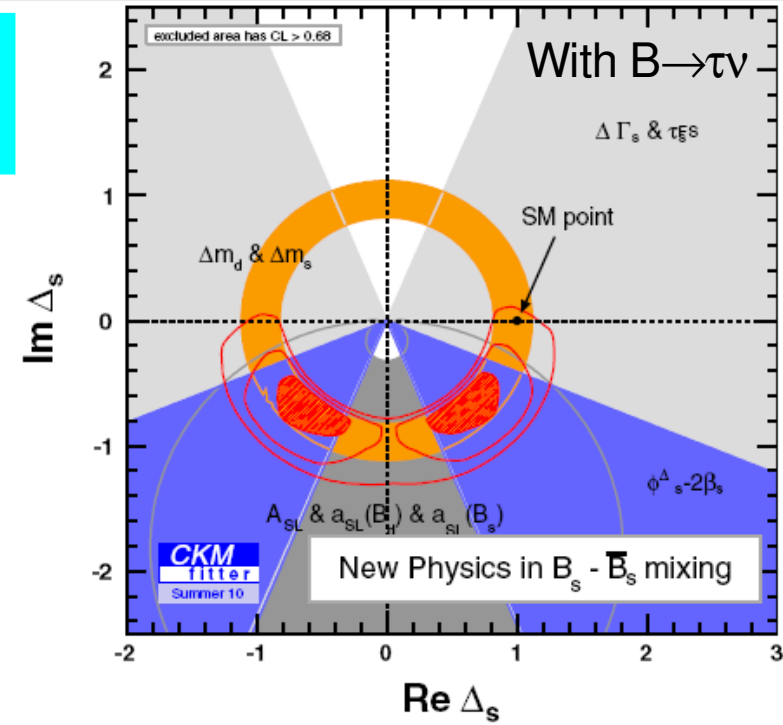


\Rightarrow ρ - η constraint significantly weaker when allowing for NP in B mixing!

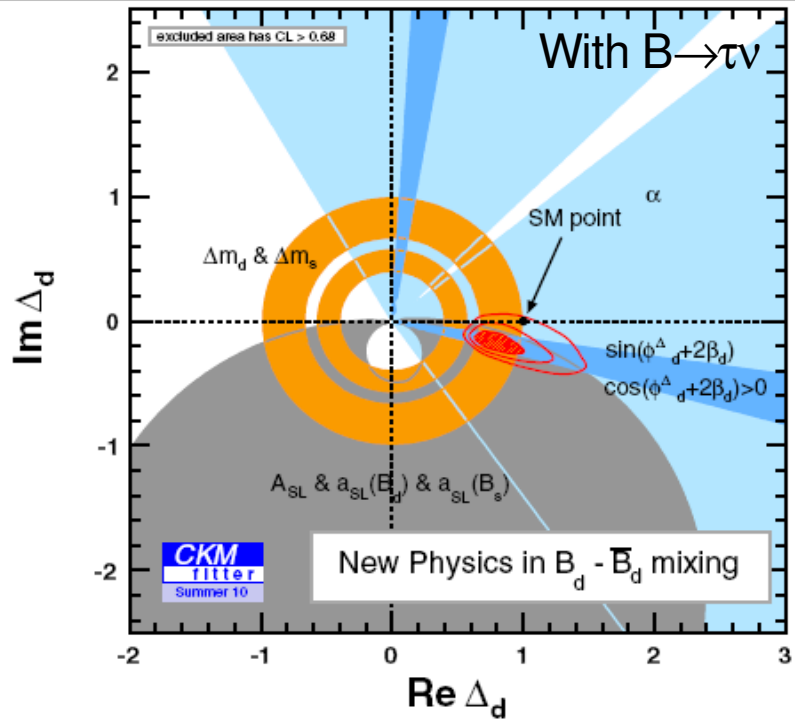
New Physics in B-mixing: Scenario I



2 rings \leftrightarrow 2 ρ - η -sols.
($a_{SL}(B_d)$ disf. 2nd sol.)



New Physics in B-mixing: Scenario I



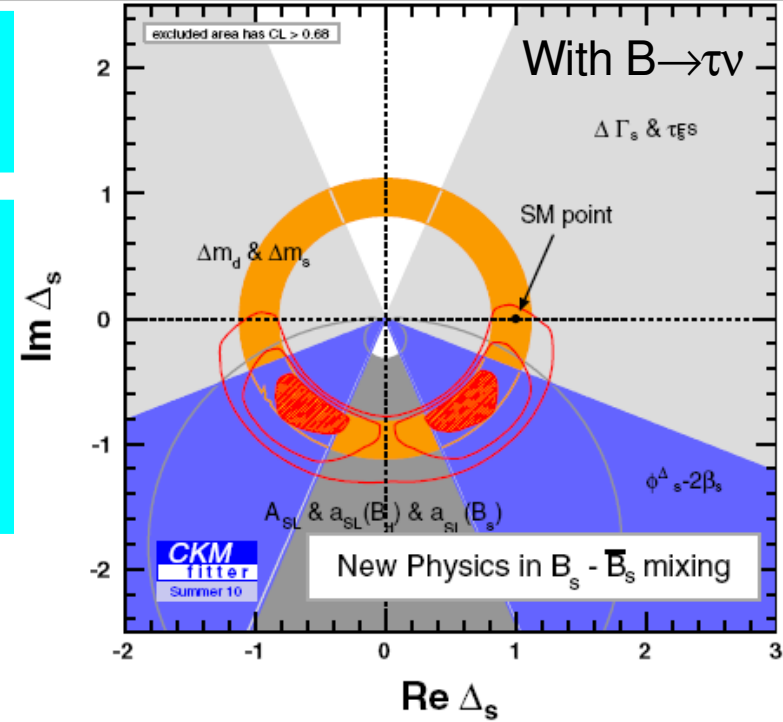
2 rings \leftrightarrow 2 ρ - η -sols.
($a_{SL}(B_d)$ disf. 2nd sol.)

$\sigma(|\Delta_s|) < \sigma(|\Delta_d|)$:

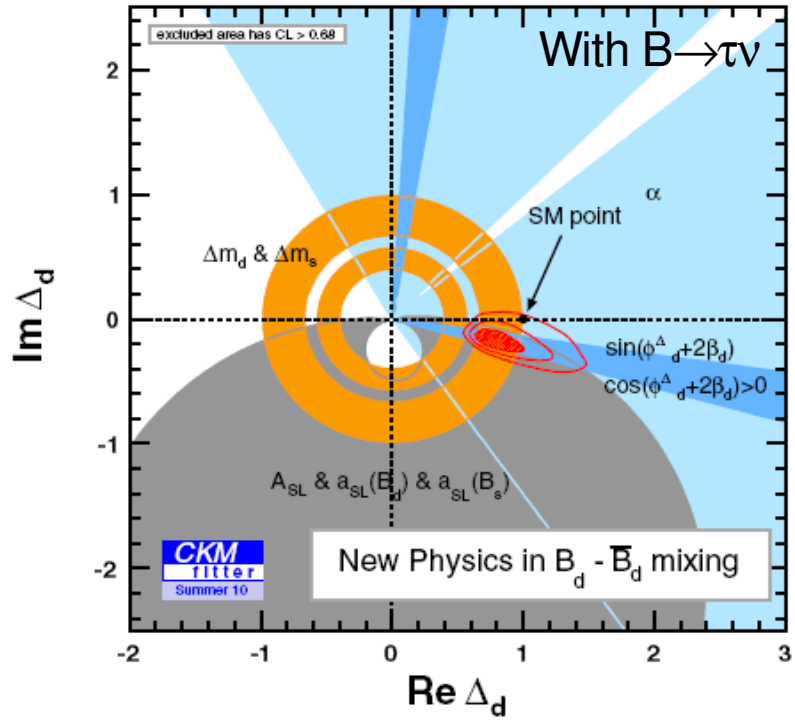
* $\sigma(f_{B_s}^2 B_{B_s}) < \sigma(f_{B_d}^2 B_{B_d})$

* $|\Delta_d|$: ρ - η dependent

($\rightarrow |V_{ub}|$ & $\gamma(\alpha)$)



New Physics in B-mixing: Scenario I



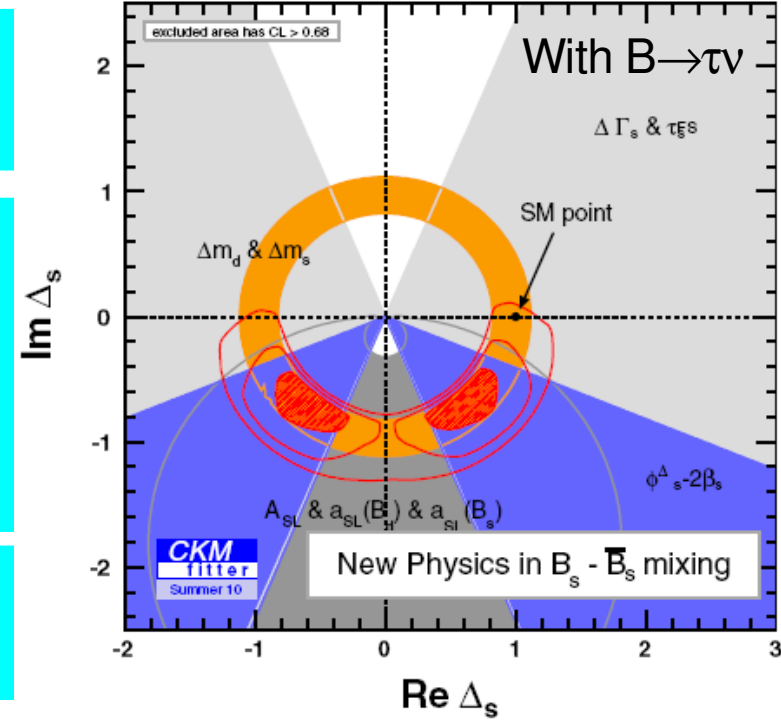
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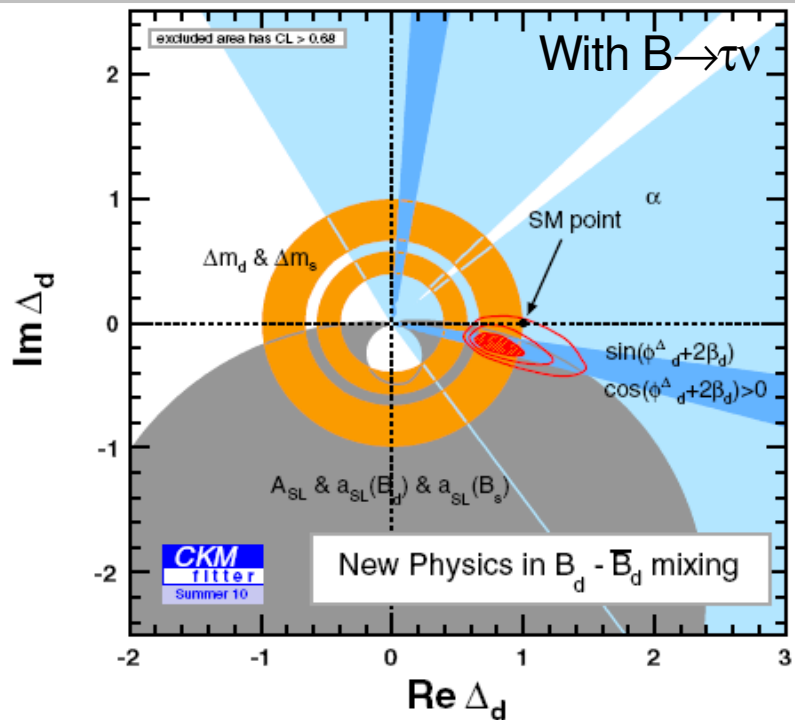
* $\sigma(f_{B_s}^2 B_{B_s}) < \sigma(f_{B_d}^2 B_{B_d})$

* $|\Delta_d|$: ρ - η dependent
($\rightarrow |V_{ub}|$ & $\gamma(\alpha)$)

NP contributions can
be as large as 40%



New Physics in B-mixing: Scenario I



2 rings \leftrightarrow 2 ρ - η -sols.
($a_{SL}(B_d)$ disf. 2nd sol.)

$\sigma(|\Delta_s|) < \sigma(|\Delta_d|)$:

* $\sigma(f_{Bs}^2 B_{Bs}) < \sigma(f_{Bd}^2 B_{Bd})$

* $|\Delta_d|$: ρ - η dependent

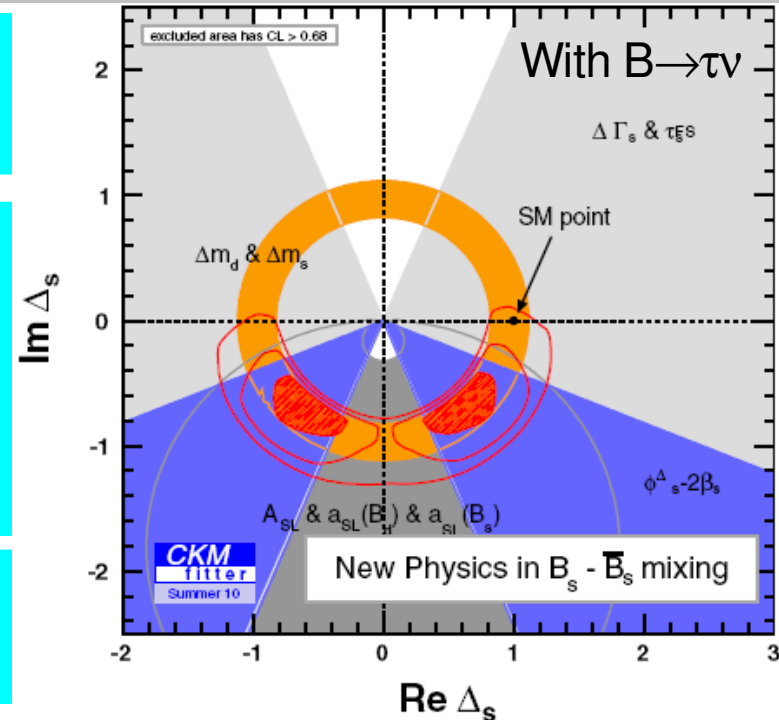
($\rightarrow |V_{ub}|$ & $\gamma(\alpha)$)

NP contributions can
be as large as 40%

$\phi_s^\Delta (3.3\sigma)$: A_{SL} & $B_s \rightarrow \psi\phi$
(Tevatron)

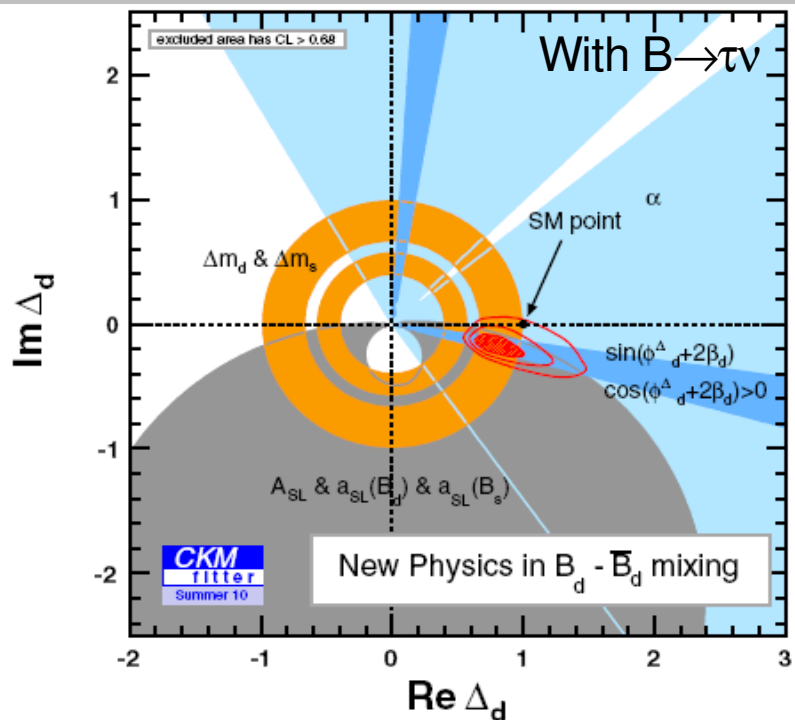
$\phi_d^\Delta (2.8\sigma)$: $\sin 2\beta - B \rightarrow \tau\nu$
(B-factories)

$$\phi_d^\Delta = (-12.9^{+8.9}_{-4.9})^\circ \quad (2\sigma)$$



$$\phi_s^\Delta - 2\beta_s = (-55^{+33}_{-25})^\circ \quad (2\sigma)$$

New Physics in B-mixing: Scenario I



2 rings \leftrightarrow 2 ρ - η -sols.
($a_{SL}(B_d)$ disf. 2nd sol.)

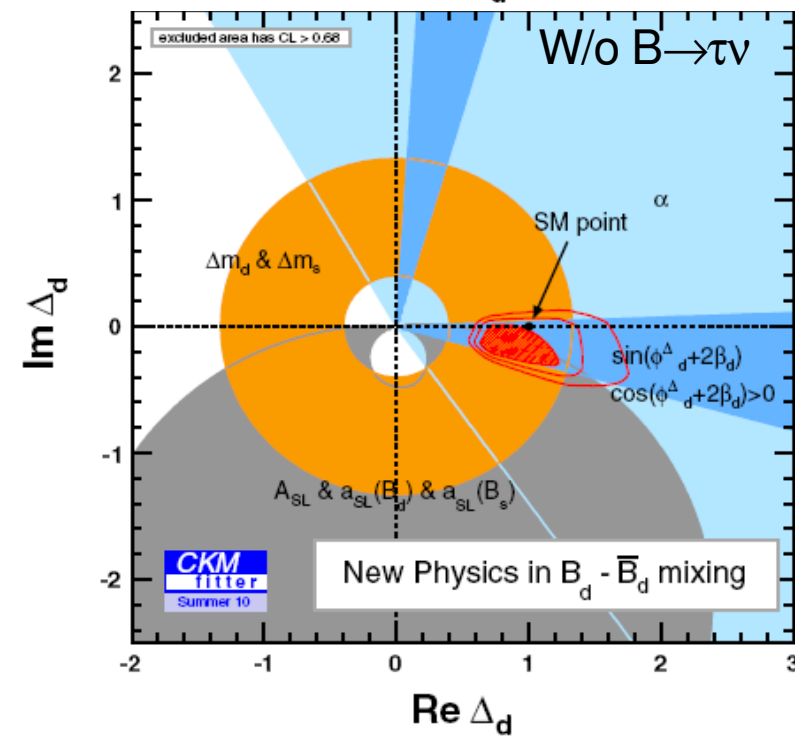
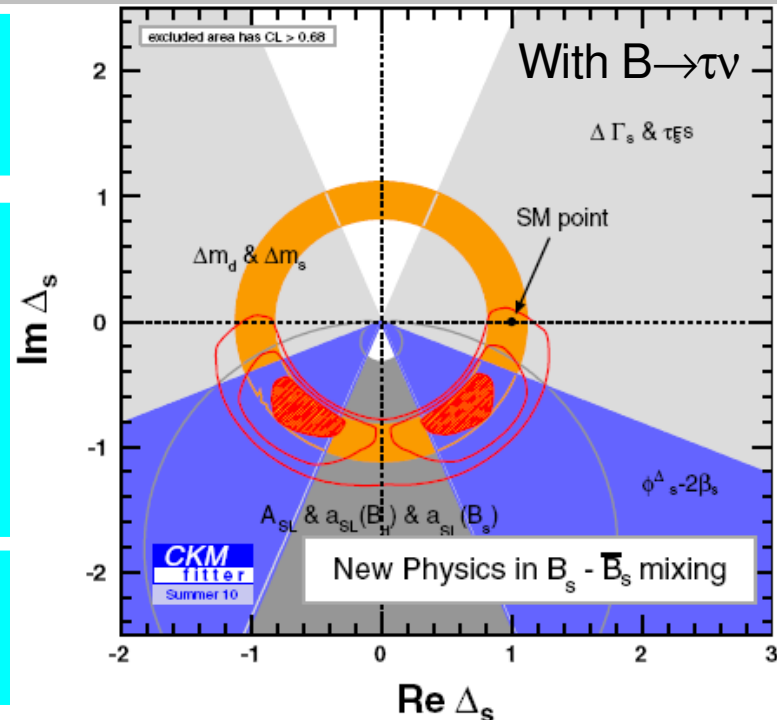
$\sigma(|\Delta_s|) < \sigma(|\Delta_d|)$:

* $\sigma(f_{B_s}^2 B_{B_s}) < \sigma(f_{B_d}^2 B_{B_d})$

* $|\Delta_d|$: ρ - η dependent

($\rightarrow |V_{ub}|$ & $\gamma(\alpha)$)

NP contributions can be as large as 40%



$\phi_s^\Delta (3.3\sigma)$: $A_{SL} & B_s \rightarrow \psi\phi$
(Tevatron)

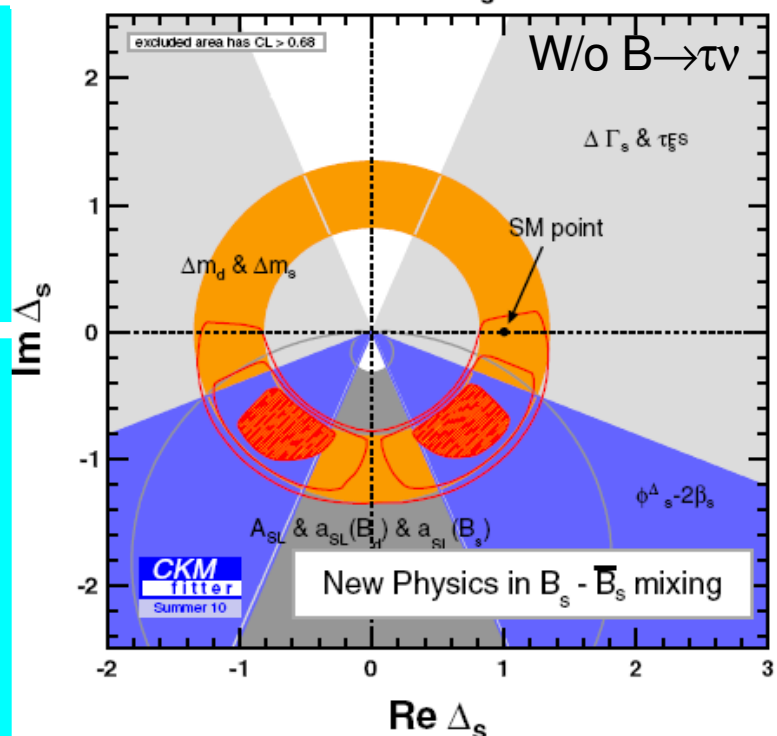
$\phi_d^\Delta (2.8\sigma)$: $\sin 2\beta - B \rightarrow \tau\nu$
(B-factories)

$B \rightarrow \tau\nu$:

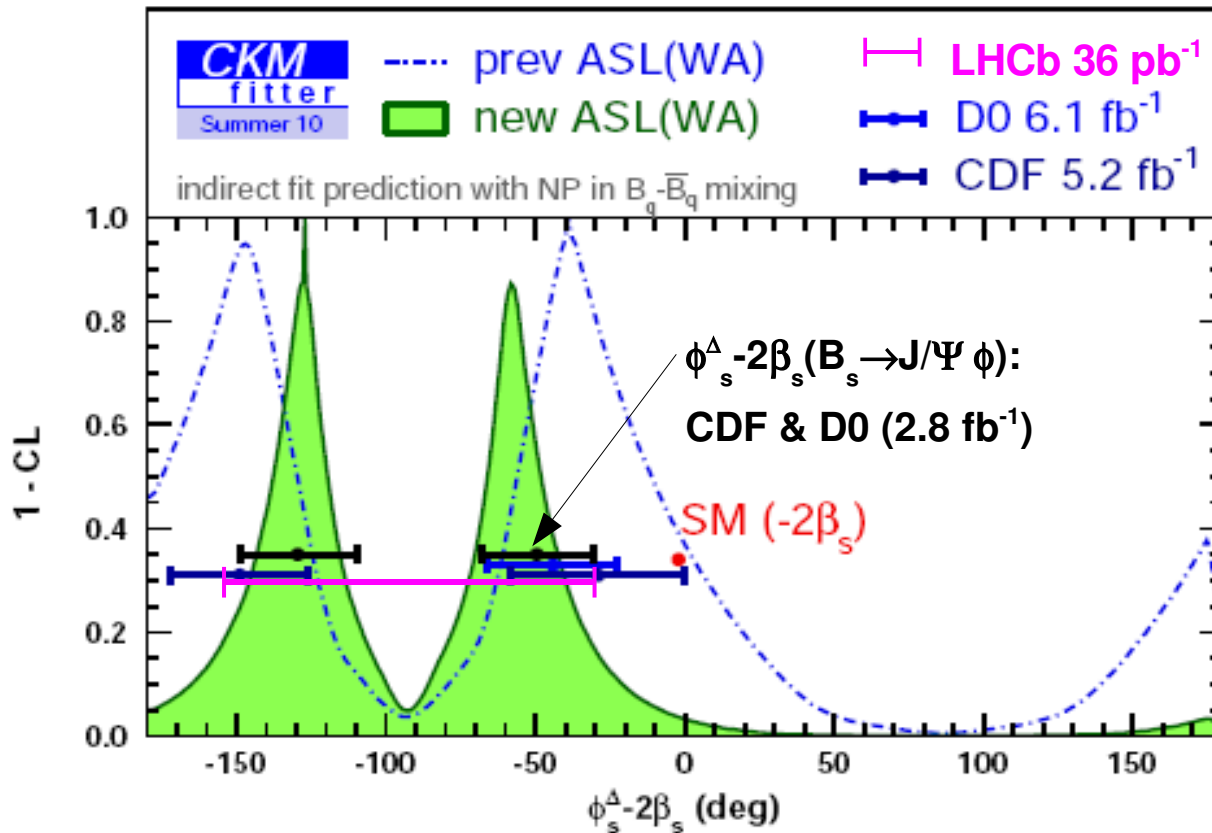
* $\sigma(|\Delta_d|) \downarrow$ by removing f_{B_d}

* $\sigma(|\Delta_s|) \downarrow$ thanks to ξ :

$$\frac{f_{B_s}^2 B_{B_s}}{f_{B_d}^2 B_{B_d}} f_{B_d}^2 B_{B_d} = \xi^2 f_{B_d}^2 B_{B_d}$$



New Physics in B mixing: Scenario I



- $A_{SL}(\underline{D0\&CDF})$: (very) good agreement with
 - $\phi_s^\Delta - 2\beta_{s(B_s \rightarrow \psi \phi)}$ CDF-D0 average (2.8 fb^{-1})
 - $\phi_s^\Delta - 2\beta_s (B_s \rightarrow \psi \phi)$ from CDF(5.2 fb^{-1}) & D0(6.1 fb^{-1}) (no average yet)
- If A_{SL} driven by NP in mixing & stays large: more driven by NP in B_s mixing since $a_{sl}(B_d)$ well constrained by “ $\sin 2\beta$ ”
- First tagged LHCb result for $B_s \rightarrow \psi \phi$ prefers $\phi_s^\Delta - 2\beta_s < 0$

New Physics in B mixing: Scenario I

Test specific combinations of Δ 's taking their SM values (SM null hypothesis composite!)

Most natural choice (?): $\Delta_s = \Delta_d = 1$ (3.6 σ)

Might dilute the anomalies (CP violation)

=> Test: $\text{Im}(\Delta_s) = \text{Im}(\Delta_d) = 0$ (3.8 σ)

Hypothesis	p-value
$\text{Im}(\Delta_d) = 0$ (1D)	2.7 σ
$\text{Im}(\Delta_s) = 0$ (1D)	3.1 σ
$\Delta_d = 1$ (2D)	2.7 σ
$\Delta_s = 1$ (2D)	2.7 σ
$\text{Im}(\Delta_d) = \text{Im}(\Delta_s) = 0$ (2D)	3.8 σ
$\Delta_d = \Delta_s$ (2D)	2.1 σ
$\Delta_d = \Delta_s = 1$ (4D)	3.6 σ

New Physics in Mixing: Minimal Flavour Violation (MFV)

$$H_q^{|\Delta B|=2} = (V_{tq}^* V_{tb})^2 [CQ + C_S Q_S + \tilde{C}_S \tilde{Q}_S] + \text{H.c.}$$

$$Q = \bar{q}_L \gamma_\mu b_L \bar{q}_L \gamma^\mu b_L \quad Q_S = \bar{q}_L b_R \bar{q}_L b_R \quad \tilde{Q}_S = \bar{q}_L^\alpha b_R^\beta \bar{q}_L^\beta b_R^\alpha$$

Chivukala & Georgi (1987), Hall & Randall (1990),
 Gabrielli & Giudice (1995/97), Ali & London (1999)
 Buras et al. (2001), D'Ambrosio et al. (2002)

Lenz, Nierste, Charles et al., PRD83, 036004 (2011)

See also: Kagan et al., PRD80, 076002 (2009)

Scenario II: Small b-Yukawa couplings

$$C_S, \tilde{C}_S \approx 0, \quad C \text{ real}$$

(E.g.: MSSM with MFV and small $\tan\beta$)

$$\Delta_d = \Delta_s = \Delta_K^{tt} = \Delta$$

$$\phi_s^\Delta = \phi_d^\Delta = \phi_K^{ij\Delta} = 0$$

Scenario III: Large b-Yukawa couplings

$$C_S, \tilde{C}_S, C \text{ complex}$$

(E.g.: certain 2HDMs)

$$\Delta_d = \Delta_s \equiv \Delta \quad \Delta_K^{tt}$$

$$\phi_s^\Delta = \phi_d^\Delta$$

$$\Delta_K^{cc} = 1$$

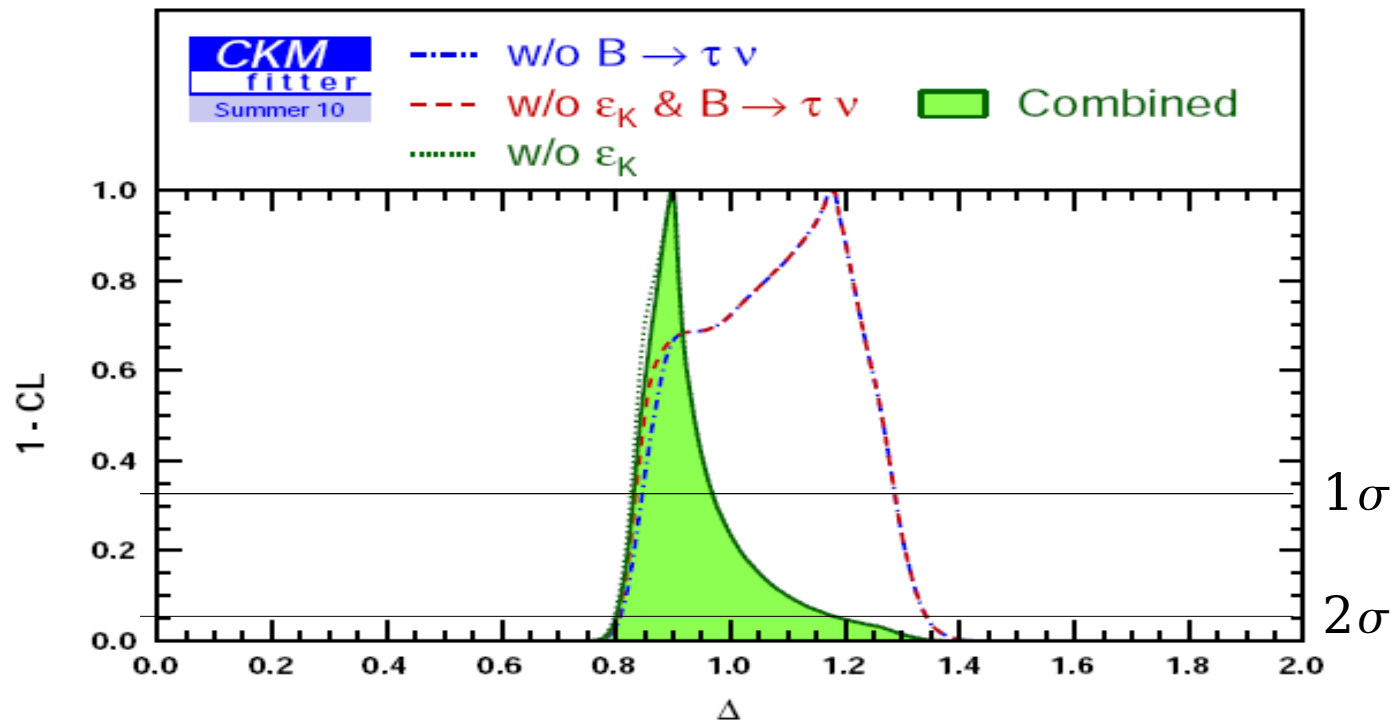
$$\Delta_K^{ct} = 1 + \lambda_K \frac{\bar{m}_c^2(\bar{m}_t)}{\bar{m}_t^2(\bar{m}_t)} \frac{S(\bar{m}_t^2/M_W^2)\eta_{tt}}{S(\bar{m}_c^2/M_W^2, \bar{m}_t^2/M_W^2)\eta_{ct}} (\Delta_K^{tt} - 1)$$

$$0.5 \leq \lambda_K \leq 2$$

Scenario II: MFV with small b-Yukawa couplings

$$\Delta_s = \Delta_d = \Delta_K^{tt} \quad \text{with} \quad \phi_s^\Delta = \phi_d^\Delta = \phi_K^{ij\Delta} = 0$$

$$\Delta_K^{ct} = 1 + \lambda_K \frac{\bar{m}_c^2(\bar{m}_t)}{\bar{m}_t^2(\bar{m}_t)} \frac{S(\bar{m}_t^2/M_W^2)\eta_{tt}}{S(\bar{m}_c^2/M_W^2, \bar{m}_t^2/M_W^2)\eta_{ct}} (\Delta_K^{tt} - 1) \quad \Delta_K^{cc} = 1$$



• $B \rightarrow \tau \nu$: significant impact; ϵ_K : only minor impact (with our inputs)

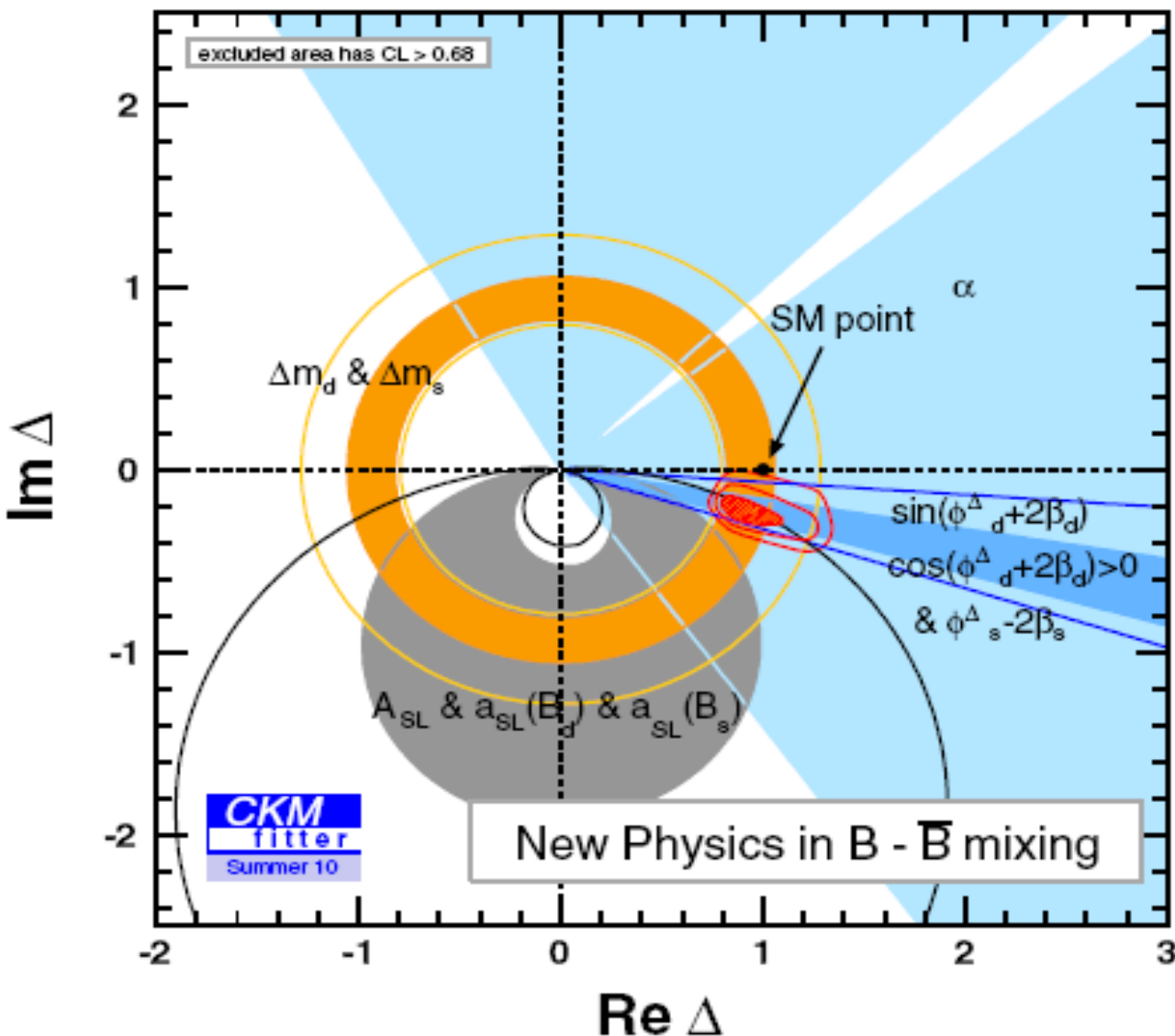
• No new NP phases \Rightarrow Similar data-theory discrepancy as for SM

Hypothesis test within Scenario I: $\Delta_d = \Delta_s = \Delta$ with $\Im(\Delta) = 0$: 3.7σ

• mSUGRA/CMSSM: special cases of scenario II \Rightarrow Disfavoured

Scenario III: MFV with large b-Yukawa couplings

$$\Delta_d = \Delta_s \equiv \Delta \quad \phi_s^\Delta = \phi_d^\Delta \quad \Delta_K^{tt}$$



Test of SM hypothesis:

Hypothesis	p-value
$\text{Im}(\Delta) = 0$ (1D)	3.5σ
$\Delta = 1$ (2D)	3.3σ

Test of Scenario III within I:

$\Delta_d = \Delta_s = \Delta$	2.1σ
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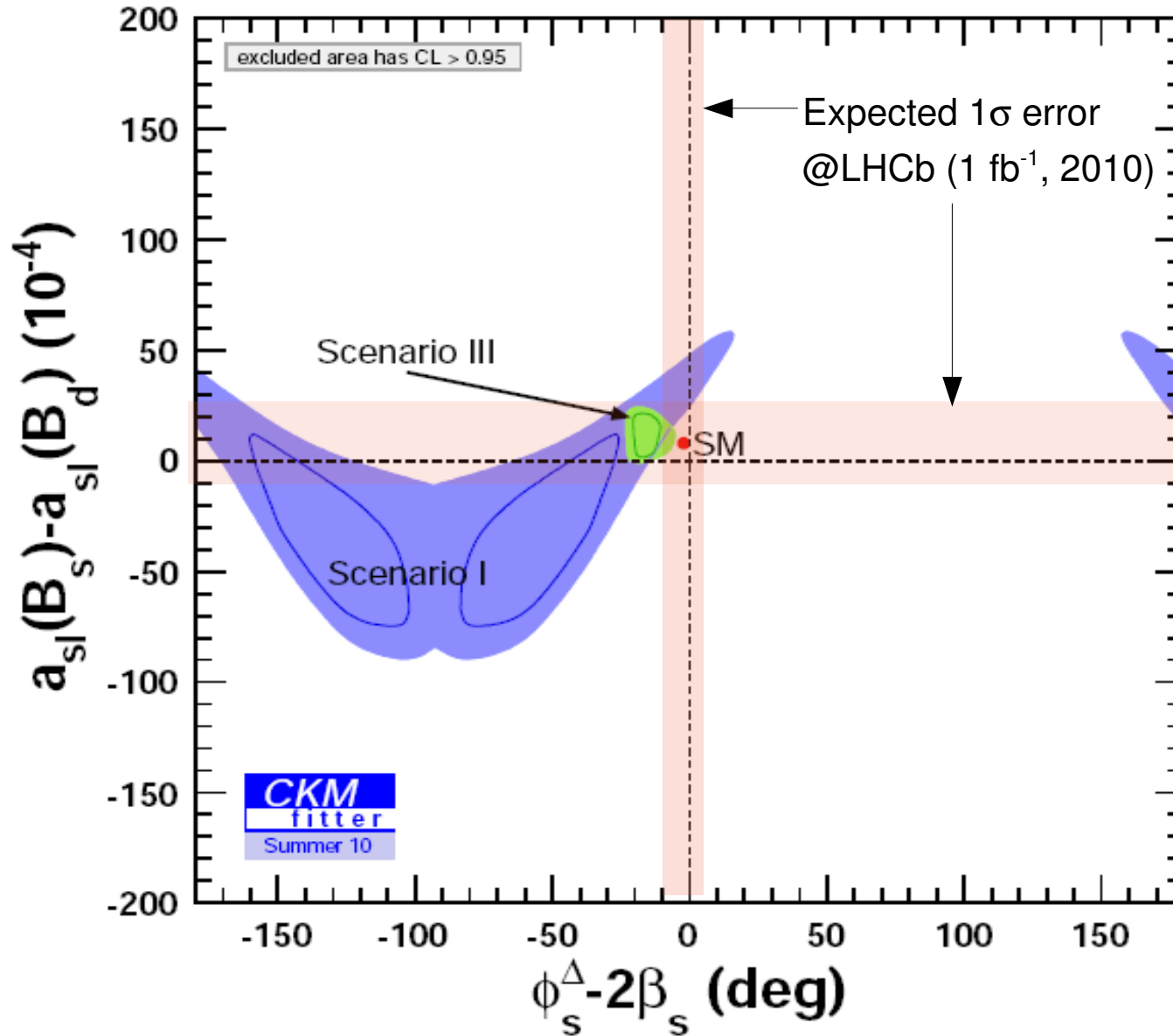
$$\Delta_K^{tt} = 1.01^{+0.53}_{-0.43} \quad (2\sigma \text{ range})$$

Summary

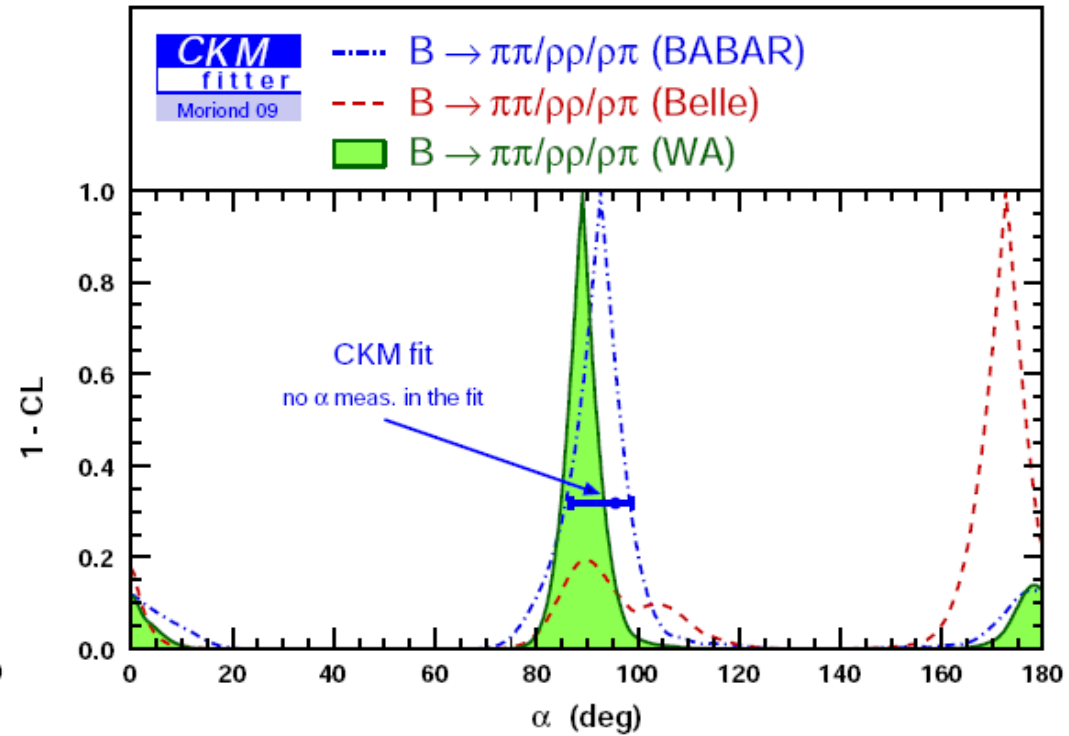
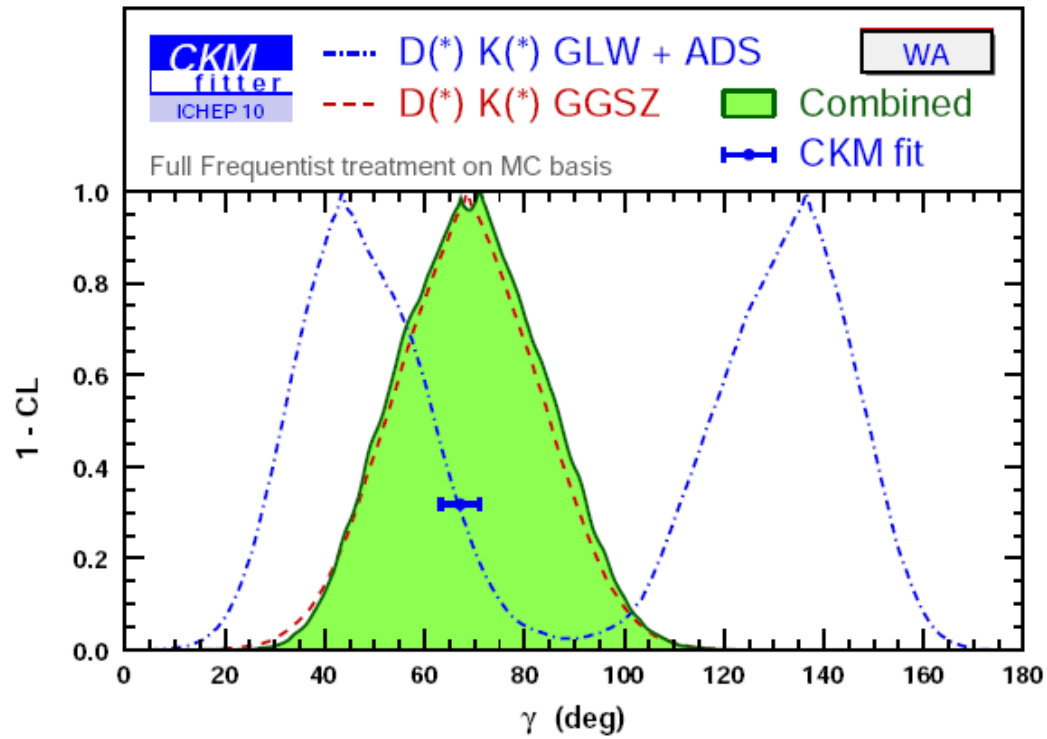
- CKM mechanism well-established but NP in Mixing of up to O(40%) allowed
- ε_K anomaly: B_K and $|V_{cb}|$ crucial
- $B \rightarrow \tau \nu$:
 - * 2.9σ wrt SM (have to wait for Belle II/SuperB)
 - * If not an experimental effect: NP in B_d mixing?
 - * If f_{B_d} underestimated by a factor of 0.7 on the Lattice then B_{B_d} overestimated by > 2 on the Lattice to meet Δm_d
- A_{SL} & $\phi^\Delta - 2\beta_s$: 3.3σ wrt SM
 - $\phi^\Delta - 2\beta_s$ ($B_s \rightarrow \psi\phi$): average for new CDF-D0 results?, LHCb!
- NP phase < 0 preferred in B_d & $B_s \Rightarrow$ MFV with large b-Yukawa's? (p-value: 2.1σ)
- Scenario I fits best
 - p-values for SM hypothesis: 3.6σ ($\Delta_s = \Delta_d = 1$), 3.8σ ($\text{Im}(\Delta_s) = \text{Im}(\Delta_d) = 0$)
- Scenario II: p-value: $3.7\sigma \Rightarrow$ Troublesome for mSUGRA/CMSSM

Outlook

- LHCb can further test these different scenarios



α and γ



Averages of Lattice QCD parameters

- Algorithmic procedure for averaging (using unquenched 2 and 2+1 calculations):
 - stat. & well-contr. syst. (Gaussian); Remaining part: Rfit, several sources added linearly
 - Combine using only Gaussian error & assign smallest Rfit error
- Alternative attempts: Lubicz & Tarantino, NCSIF B123, 674 (2008) (Not algorithmic)
Laiho, Lunghi, Van de Water, PRD81, 034503 (2010) (algorithmic)

Collaboration	N_f	$f_{B_s} \pm \sigma_{\text{stat}} \pm \sigma_{R\text{fit}}$
CP-PACS01	2	$242 \pm 9^{+53}_{-34}$
MILC02	2	$217 \pm 6^{+58}_{-31}$
JLQCD03	2	$215 \pm 9^{+19}_{-15}$
ETMC09	2	$243 \pm 6 \pm 15$
HPQCD03	2 + 1	$260 \pm 7 \pm 39$
FNAL-MILC09	2 + 1	$243 \pm 6 \pm 22$
HPQCD09	2 + 1	$231 \pm 5 \pm 30$
Our average		$231 \pm 3 \pm 15$

Collaboration	N_f	$f_{B_s}/f_{B_d} \pm \sigma_{\text{stat}} \pm \sigma_{R\text{fit}}$
CP-PACS01	2	$1.179 \pm 0.018 \pm 0.023$
MILC02	2	$1.16 \pm 0.01^{+0.08}_{-0.04}$
JLQCD03	2	$1.13 \pm 0.03^{+0.17}_{-0.02}$
ETMC09	2	$1.27 \pm 0.03 \pm 0.04$
FNAL-MILC09	2 + 1	$1.245 \pm 0.028 \pm 0.049$
HPQCD09	2 + 1	$1.226 \pm 0.020 \pm 0.033$
RBC/UKQCD10	2 + 1	$1.15 \pm 0.05 \pm 0.20$
Our average		$1.209 \pm 0.007 \pm 0.023$

Collaboration	N_f	$\hat{\mathcal{B}}_{B_s} \pm \sigma_{\text{stat}} \pm \sigma_{R\text{fit}}$
JLQCD03	2	$1.299 \pm 0.034^{+0.122}_{-0.095}$
HPQCD06	2 + 1	$1.168 \pm 0.105 \pm 0.140$
RBC/UKQCD07	2 + 1	$1.21 \pm 0.05 \pm 0.05$
HPQCD09	2 + 1	$1.326 \pm 0.04 \pm 0.03$
Our average		$1.28 \pm 0.02 \pm 0.03$

Collaboration	N_f	$\mathcal{B}_{B_s}/\mathcal{B}_{B_d} \pm \sigma_{\text{stat}} \pm \sigma_{R\text{fit}}$
JLQCD03	2	$1.017 \pm 0.016^{+0.076}_{-0.017}$
HPQCD09	2 + 1	$1.053 \pm 0.020 \pm 0.030$
RBC/UKQCD10	2 + 1	$0.96 \pm 0.02 \pm 0.03$
Our average		$1.006 \pm 0.010 \pm 0.030$

Collaboration	N_f	$\mathcal{B}_K(2 \text{ GeV}) \pm \sigma_{\text{stat}} \pm \sigma_{R\text{fit}}$
JLQCD08	2	$0.537 \pm 0.004 \pm 0.072$
HPQCD/UKQCD06	2 + 1	$0.618 \pm 0.018 \pm 0.179$
RBC/UKQCD07	2 + 1	$0.524 \pm 0.010 \pm 0.052$
ALVdW09	2 + 1	$0.527 \pm 0.006 \pm 0.049$
Our average		$0.527 \pm 0.0031 \pm 0.049$

$|V_{ub}|$ input

$|V_{ub}|$ (incl.): BLNP

$$(4.32^{+0.21}_{-0.24} \pm 0.45) \times 10^{-3}$$

Start from HFAG average

Add linearly uncertainties from SF, SSF, WA,
scale matching & additional m_b unc. of 50 MeV
(neglect of higher orders)

$|V_{ub}|$ (excl.)

$$(3.51 \pm 0.10 \pm 0.46) \times 10^{-3}$$

$|V_{ub}|$ average

$$(3.92 \pm 0.09 \pm 0.45) \times 10^{-3}$$

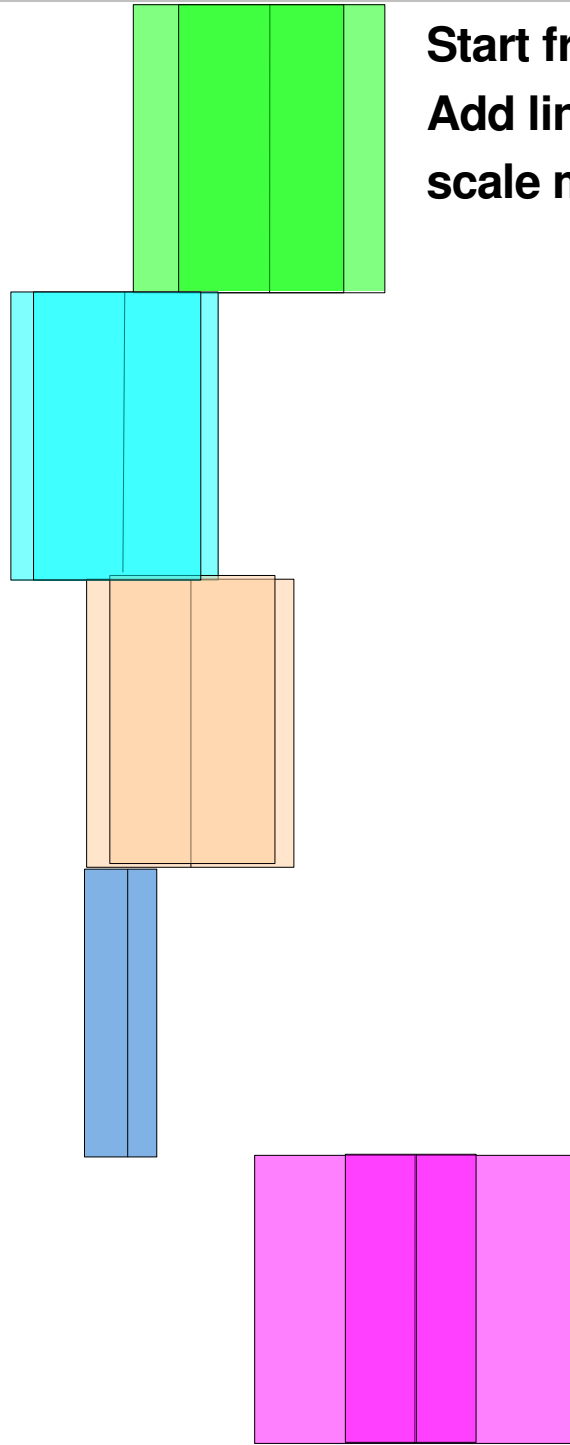
$|V_{ub}|$ fit prediction

$$(3.56^{+0.15}_{-0.20}) \times 10^{-3}$$

$|V_{ub}|$ from $B \rightarrow \tau \nu$

(using $f_{B_d} = 191 \pm 13$ MeV)

$$(5.10 \pm 0.47 \pm 0.35) \times 10^{-3}$$



Recent developments

1. $|V_{cb}|$ (excl.): $(38.85 \pm 0.77 \pm 0.84) \times 10^{-3}$ $\xrightarrow{F(1)_{old}=0.921 \pm 0.013 \pm 0.020}$ $(39.42 \pm 0.61 \pm 0.69) \times 10^{-3}$
 $F(1)_{new}=0.9077 \pm 0.0051 \pm 0.0088$

\Rightarrow Discrepancy wrt inclusive $((41.85 \pm 0.43 \pm 0.59) \times 10^{-3})$ reduced

However, no significant change in our average value: $(40.88 \pm 0.35 \pm 0.59) \times 10^{-3}$

2. $\sin 2\beta$ from Belle: $0.668 \pm 0.023 \pm 0.013$ (711 M BBbar)
 $(0.642 \pm 0.031 \pm 0.017$ (553 M Bbbar))
 $(0.687 \pm 0.028 \pm 0.012$ (BABAR))

My personal average: 0.676 ± 0.020
(HFAG average was: 0.673 ± 0.023)

$\Rightarrow \epsilon_K$ “anomaly” slightly reduced

$\Rightarrow \sin 2\beta$ & $B \rightarrow \tau \nu$ “anomaly” slightly reduced

3. First Δm_s measurement from LHCb in perfect agreement with CDF

4. New analysis results on $\gamma \Rightarrow$ New global analysis necessary

ϵ_K anomaly ?

$$\epsilon_K = \sin\phi_\epsilon e^{i\phi_\epsilon} \left[\frac{\text{Im}M_{12}^K}{\Delta M_K} + \xi \right] = \frac{\kappa_\epsilon}{\sqrt{2}} e^{i\phi_\epsilon} \left[\frac{\text{Im}M_{12}^{(6)}}{\Delta M} \right] \quad \xi = \frac{\text{Im}A_0}{\text{Re}A_0} \quad \tan\phi_\epsilon = \frac{2\Delta M_K}{\Delta\Gamma_K}$$

For a long time: $\kappa_\epsilon = 1$

1. **Measurement:** $\sin\phi_\epsilon = (43.5 \pm 0.7)^\circ$
2. ξ from measured ϵ'/ϵ , $\omega = \text{Re}A_2/\text{Re}A_0$ + estimate of R_8 (assumes no NP in ϵ'/ϵ)
3. Higher dimension contributions (d=8) to $\text{Im} M_{12}$

$$\Rightarrow \kappa_\epsilon = 0.940 \pm 0.013 \pm 0.023$$

In agreement with first estimate: $\kappa_\epsilon = 0.94 \pm 0.02$

(Buras, Guadagnoli, Isidori PLB 688, 309 (2010))

(See also: Buras & Guadagnoli, PRD78, 033005 (2008); PRD79, 053010 (2009)
Andriyash, Ovanesyan, Vysotzky, PLB599, 253 (2004))

Deviation of measured observables wrt Theory predictions

Quantity	Deviation			
	wrt SM fit	wrt Sc. I	wrt Sc. II	wrt Sc. III
α	1.1σ	0.2σ	0.7σ	1.0σ
$\phi_d^\Delta + 2\beta$	2.8σ	0.8σ	2.6σ	1.3σ
γ	0.0σ	0.0σ	0.0σ	0.0σ
$\phi_s^\Delta - 2\beta_s$	2.3σ	0.5σ	2.4σ	1.6σ
$ \epsilon_K $	0.0σ		0.0σ	
Δm_d	1.0σ	0.9σ	1.0σ	0.8σ
Δm_s	0.3σ	0.7σ	0.9σ	1.2σ
A_{SL}	2.9σ	1.2σ	2.9σ	2.2σ
a_{SL}^d	0.9σ	0.2σ	0.8σ	0.3σ
a_{SL}^s	0.2σ	0.7σ	0.2σ	0.0σ
$\Delta\Gamma_s$	1.0σ	0.2σ	1.1σ	0.9σ
$\mathcal{B}(B \rightarrow \tau\nu)$	2.9σ	0.7σ	2.6σ	1.0σ
$\mathcal{B}(B \rightarrow \tau\nu)$ and A_{SL}	3.7σ	0.9σ	3.5σ	2.0σ
$\phi_s^\Delta - 2\beta_s$ and A_{SL}	3.3σ	0.8σ	3.3σ	2.3σ
$\mathcal{B}(B \rightarrow \tau\nu)$, $\phi_s^\Delta - 2\beta_s$ and A_{SL}	4.0σ	0.6σ	3.8σ	2.1σ

A_{sl}

$$A_{sl}^{meas} = (-85 \pm 28) \times 10^{-4} \quad A_{SL} = (0.506 \pm 0.043) a_{sl}(B_s) + (0.494 \pm 0.043) a_{sl}(B_d)$$

If A_{SL} driven by NP in mixing & stays large: mainly NP in B_s mixing since

$$a_{sl}(B_d) \text{ constrained by "sin}2\beta\text{"}: a_{sl}^{meas}(B_d) = (-47 \pm 46) \times 10^{-4} \quad a_{sl}^{pred}(B_d) = (-36_{-11}^{+23}) \times 10^{-4}$$

