

Nonperturbative QCD Calculations: *Status and Prospects*

MATTHEW WINGATE
DAMTP, UNIVERSITY OF CAMBRIDGE



BEAUTY 2011
AMSTERDAM

An Idiosyncratic Overview

rather than an encyclopedic review

- ❖ Focus on hadronic matrix elements from Lattice QCD
- ❖ CKM unitarity
- ❖ B_s mixing
- ❖ Rare B decays
- ❖ Beautiful baryons

Lattice QCD

- ❖ Nonperturbative regulator of quantum field theories
- ❖ Quantifiable and improvable uncertainties
- ❖ No time for a pedagogic introduction, but
- ❖ Reminder of sources of lattice uncertainties . . .

Lattice QCD

Lattice QCD

in 1 minute

Lattice QCD

in 1 minute

a silent film
by Matthew Wingate





finite box
 L^3

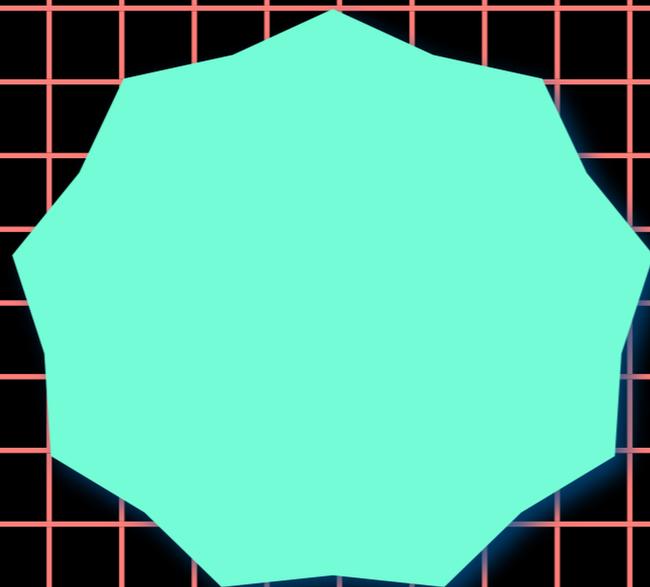
finite imaginary time

L_τ

∴ evolution operator: $\exp(-\hat{H}\tau)$

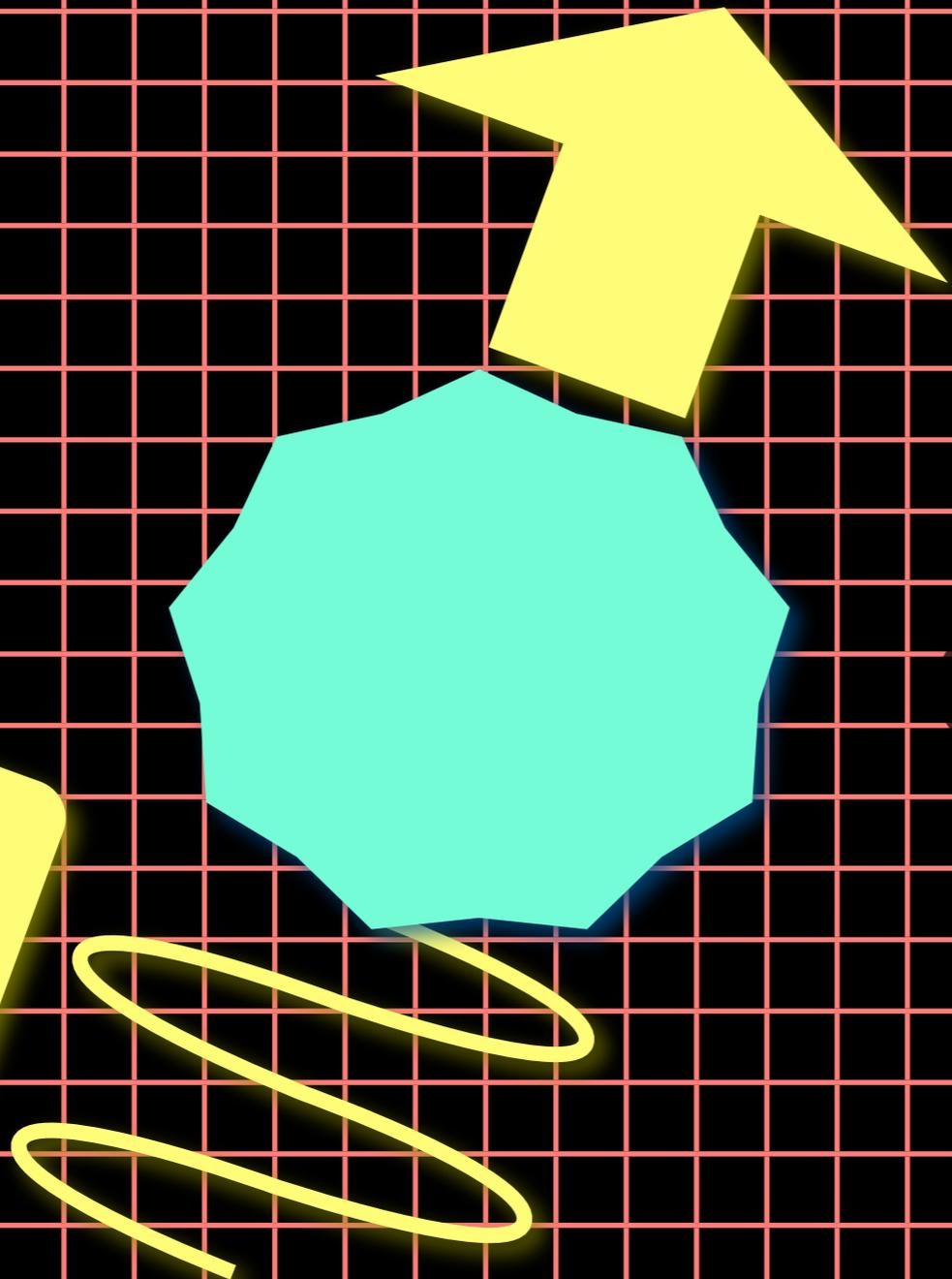
$\hbar c / \Lambda_{\text{QCD}}$
or
 $\hbar / m_{\pi} c$

hadron
should be smaller than box



hadron
should not notice grid





fast hadron
notices grid

$$\hbar/m_b c$$



b quark

$$\hbar/m_b c$$



b quark



$$\hbar/m_b c$$



b quark



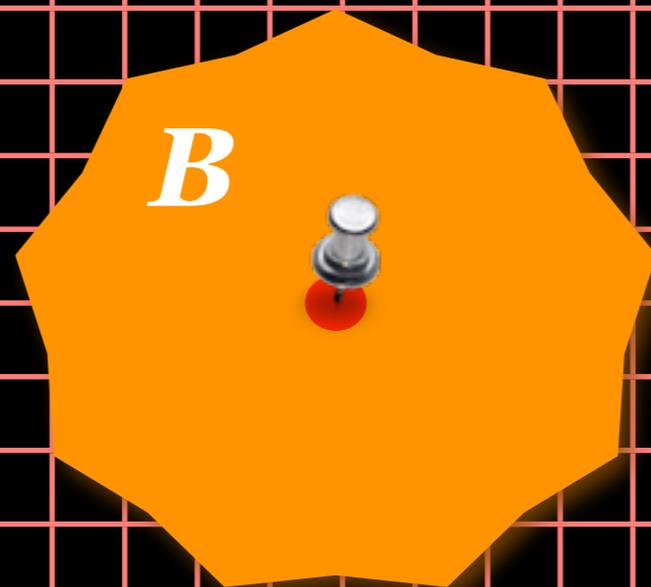
$$\hbar/m_b c$$

→ || ←

b quark

...too
small

HQET (NRQCD) *to the rescue!*



*b as static
color source*

**hadronic physics
as “brown muck”**

einde

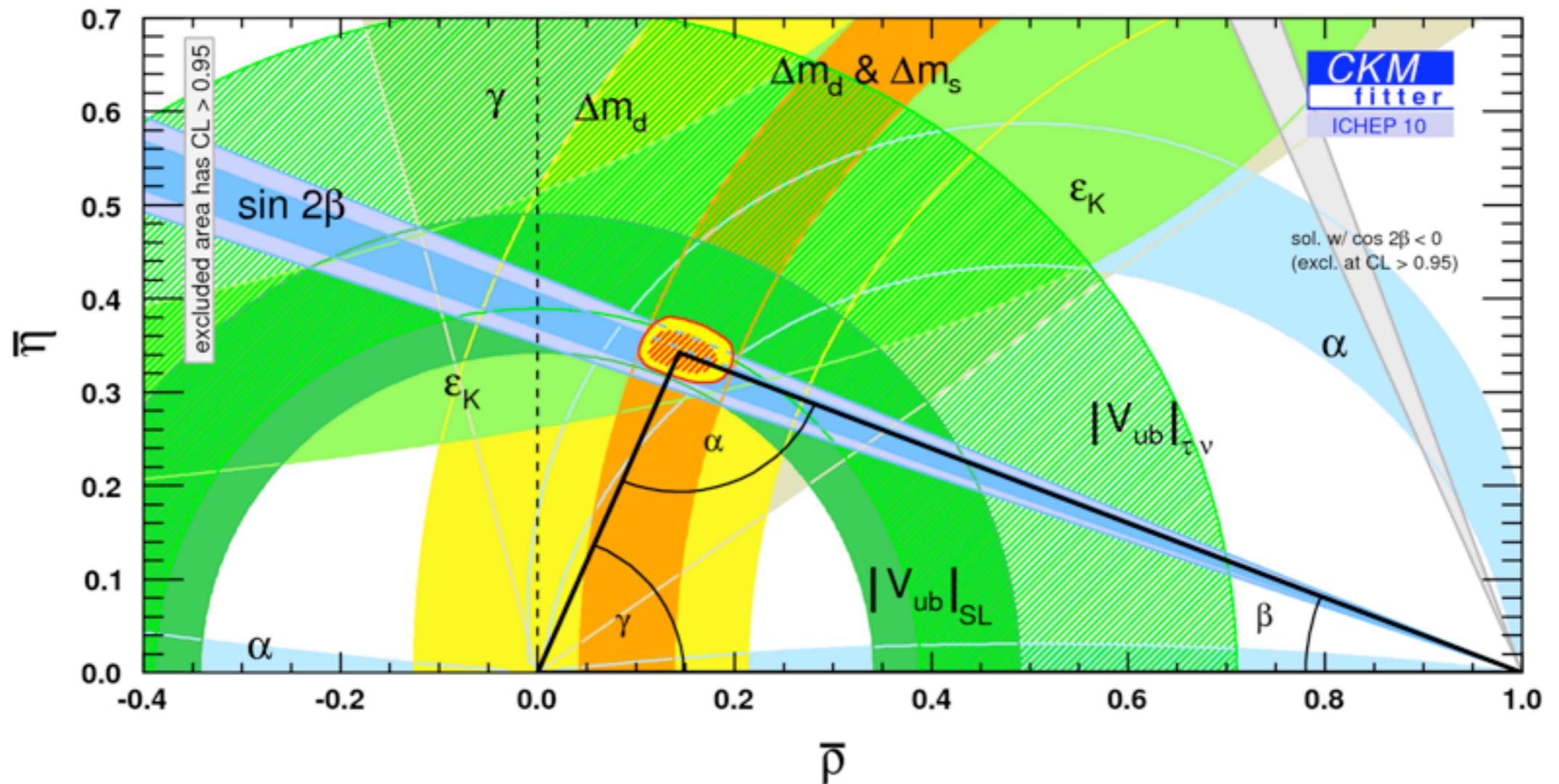
Salient points

- ❖ Need clean separation of scales
- ❖ Physical point still too expensive

$$a \ll m_b^{-1} \sim m_\pi^{-1} \ll L$$

- ❖ Effective theories (HQET, chiral PT) used to treat heavy quark effects, extrapolate in light quark mass
- ❖ Both lattice spacing and use of HQET restrict kinematics
- ❖ Imaginary time \Rightarrow at most 1 hadron init/final state
- ❖ Statistical errors (physical reasons why some quantities have larger errors than others), another 5-minute film...

Global fits to CKM parameters



CKMfitter: Bona *et al.*, ICHEP 2010
Talk by Heiko Lacker, Friday

Global fits to CKM parameters

Results of the SM analysis

preliminary Summer '10
SM determination of
the Unitarity Triangle

$$R_u e^{i\gamma} + R_d e^{-i\beta} = 1$$

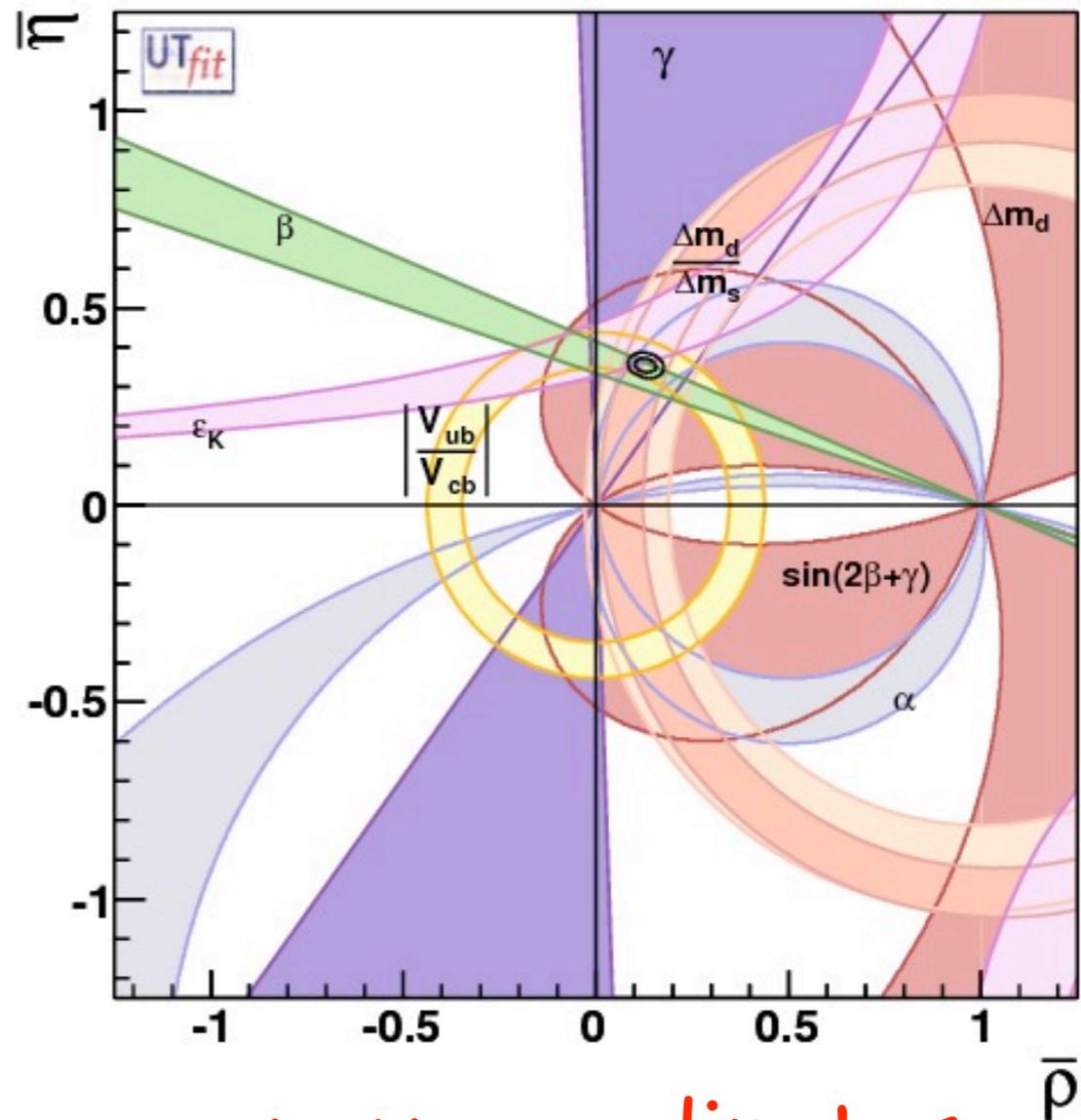
$$R_u = 0.379 \pm 0.013$$

$$R_d = 0.939 \pm 0.021$$

$$\gamma = (69.8 \pm 3.1)^\circ$$

$$\beta = (22.15 \pm 0.75)^\circ$$

$$\alpha = (87.8 \pm 3.0)^\circ$$

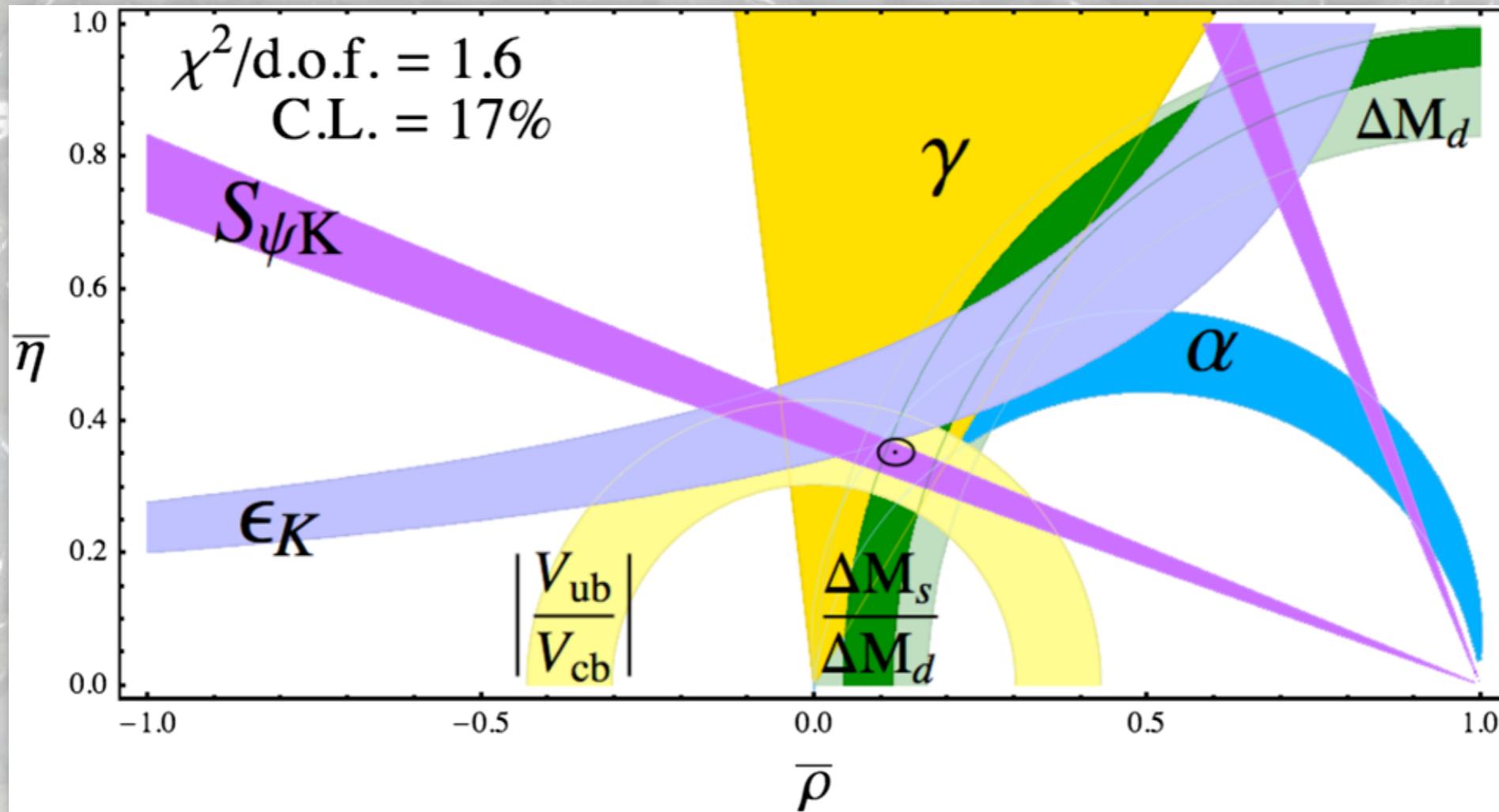


apex coordinates

$$\bar{\rho} = 0.130 \pm 0.021$$

$$\bar{\eta} = 0.355 \pm 0.013$$

Global fits to CKM parameters



$$\langle \bar{K}^0 | Q_{\Delta S=2} | K^0 \rangle \quad \langle \pi | \bar{u} \gamma^\mu b | B \rangle \quad \langle \bar{B}_q | Q_{\Delta B=2} | B_q \rangle \quad \langle 0 | \bar{u} \gamma^\mu \gamma^5 b | B \rangle$$

$$B_K \quad f_+(q^2) \quad f_{B_q}^2 B_{B_q} \quad f_B$$

$$\langle D | \bar{c} \gamma^\mu b | B \rangle \quad \langle D^* | \bar{c} \gamma^\mu b | B \rangle$$

$$\mathcal{F}_{B \rightarrow D}(1) \quad \mathcal{F}^{B \rightarrow D^*}(1) \quad f_\pi, f_K, \langle \pi | \bar{u} \gamma^\mu s | K \rangle$$

Fitters: LQCD averages and errors

♣ **CKMfitter (Charles, et al.)** (arXiv:0905.1572)

- ◆ 2 and 2+1 flavor LQCD results
- ◆ Rfit (Gaussian + flat components to syst. errors)
- ◆ Systematic errors added linearly

♣ **UTfit (Bona, et al.)** (arXiv:0807.4605)

- ◆ 0 (??), 2 and 2+1 flavor LQCD results
- ◆ Bayesian

♣ **Laiho, Lunghi, Van de Water** (PRD 81, 034503, 2010)

- ◆ 2+1 flavor LQCD results
- ◆ Frequentist, systematic errors as Gaussian
- ◆ Systematic errors added quadratically

Fitters: LQCD averages

e.g. \hat{B}_K

❖ CKMfitter (Charles, et al.) (arXiv:1508.01903)

0.721(5)_{stat}(40)_{sys}

- ◆ 2 and 2+1 flavor LQCD results
- ◆ Rfit (Gaussian + flat components to priors)
- ◆ Systematic errors added linearly

❖ UTfit (Bona, et al.) (L & T, arXiv:0803033)

0.750(70)

- ◆ 0 (??), 2 and 2+1 flavor LQCD results
- ◆ Bayesian

❖ Laiho, Lunghi, Van de Water (arXiv:1508.01903)

0.725(27)

- ◆ 2+1 flavor LQCD results
- ◆ Frequentist, systematic errors as Gaussian
- ◆ Systematic errors added quadratically

Snapshot of recent work

$$f_B, f_{B_s}$$

ETM, PoS(LAT2009);
 HPQCD, PRL 92 (2004);
 FNAL/MILC, PoS(LAT2008);
 HPQCD, PRD 80 (2009)

$$B_{B_d}, B_{B_s}$$

HPQCD, PRD 76 (2007);
 RBC-UKQCD, PoS(LAT2007);
 HPQCD, PRD 80 (2009);
 RBC-UKQCD, PRD 82 (2010)

$$f_+^{B \rightarrow \pi}(q^2)$$

HPQCD, PRD 73 (2006);
 FNAL/MILC, PRD 79 (2009) 054507;
 FNAL/MILC, PRD 80 (2010)

$$\mathcal{F}^{B \rightarrow D}(1)$$

FNAL/MILC, NPB Proc Suppl (2005)

$$\mathcal{F}^{B \rightarrow D^*}(1)$$

FNAL/MILC, PRD 79 (2009) 014506

$$\hat{B}_K$$

JLQCD, PRD 77 (2008);
 HPQCD, PRD 73 (2006);
 RBC-UKQCD, PRL 100 (2008);
 Aubin et al., PRD 81 (2010)

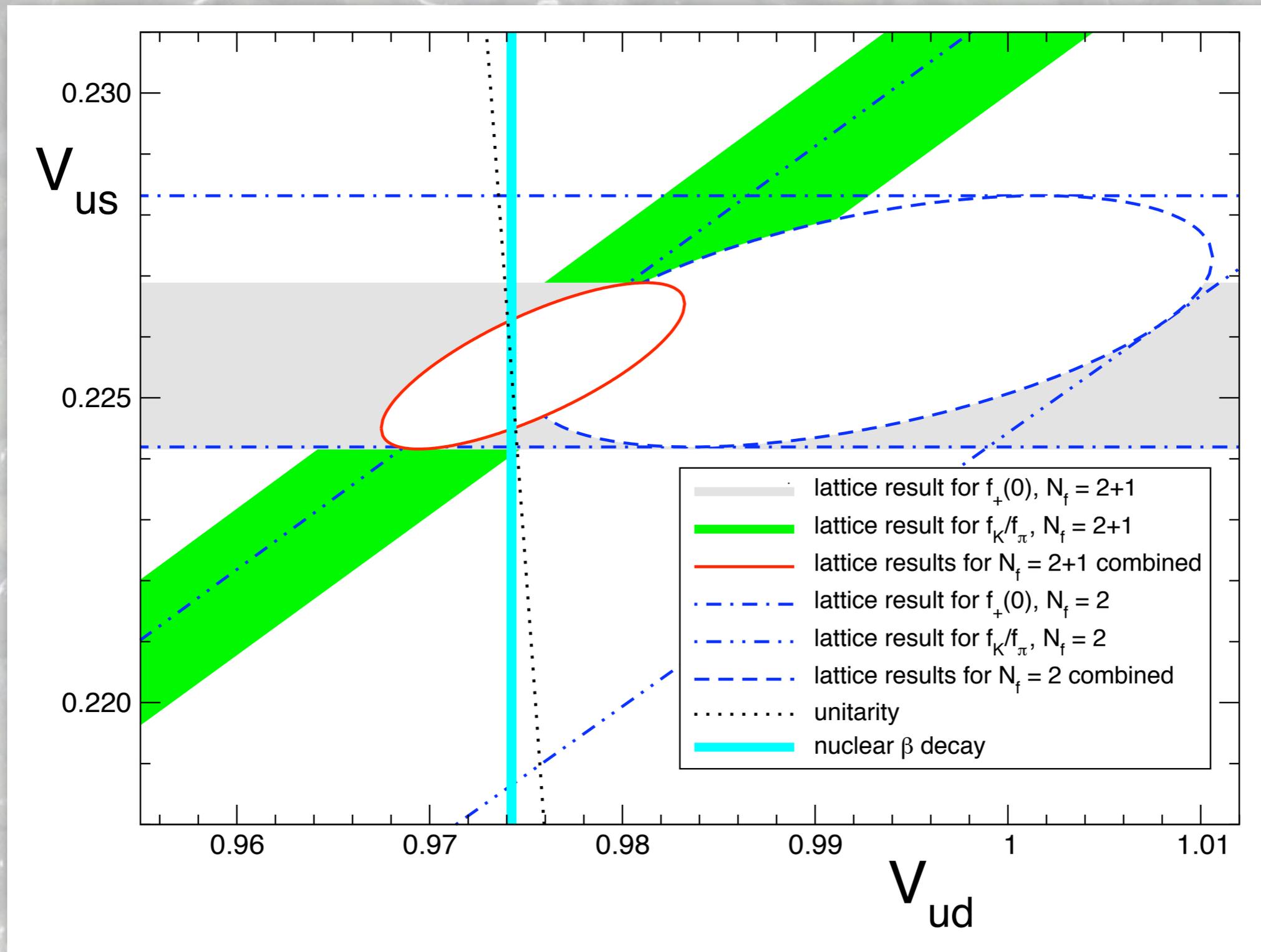
$$f_+^{K \rightarrow \pi}(0)$$

RBC-UKQCD, PRL 100 (2008);
 ETM, PRD 80 (2009);
 RBC-UKQCD, EPJ C69 (2010)

$$f_\pi, f_K$$

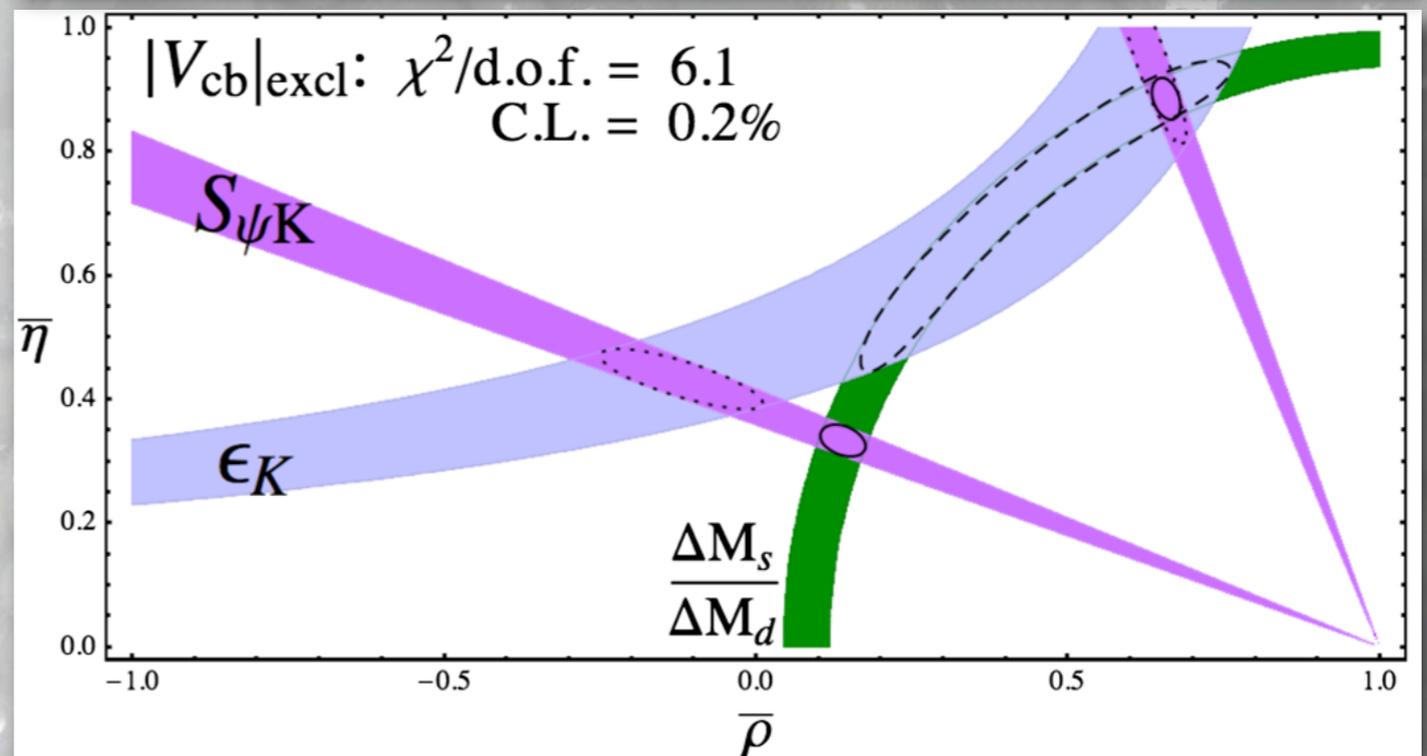
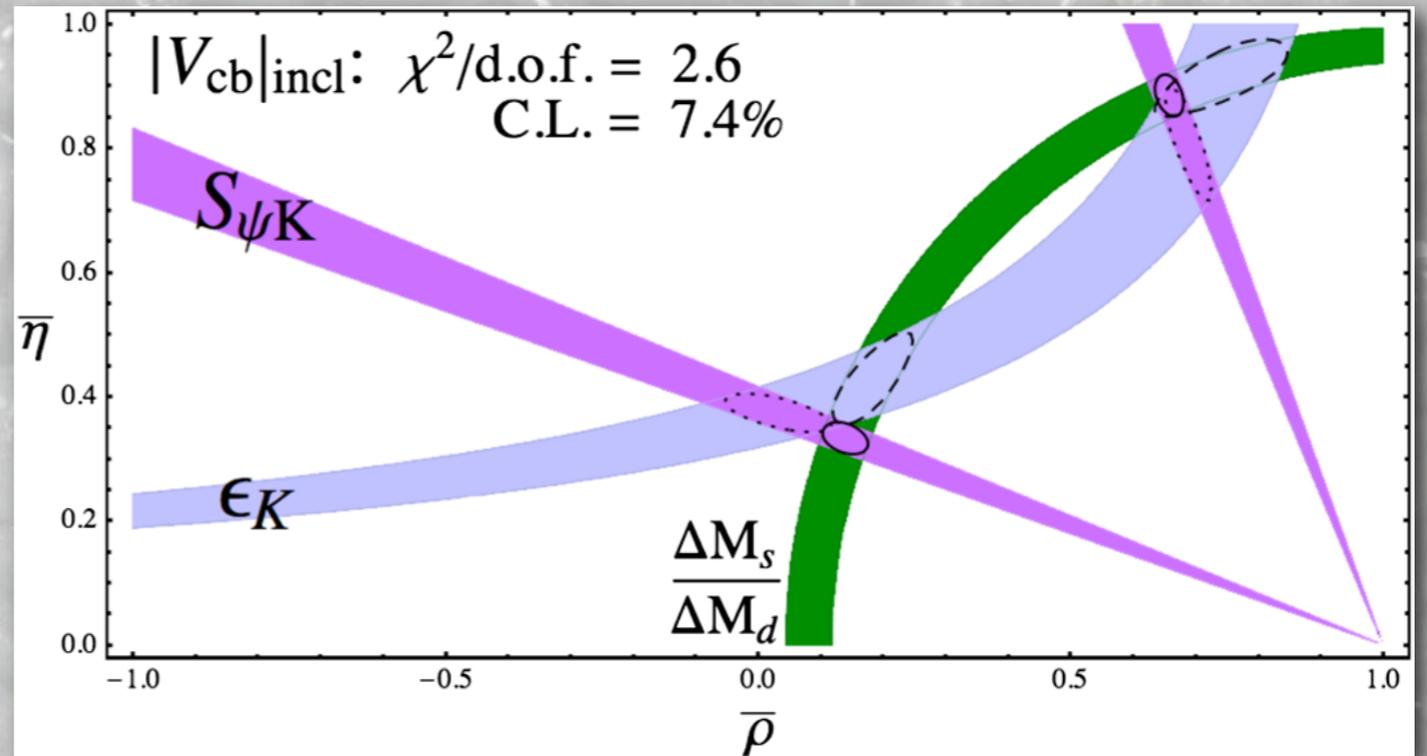
NPLQCD, PRD 75 (2007);
 HPQCD, PRL 100 (2008);
 QCDSF, PoS(LAT2007);
 PACS-CS, PoS(LAT2008);
 PACS-CS, PRD 79 (2009);
 RBC-UKQCD, PRD 78 (2008);
 Aubin et al., PoS(LAT2008);
 MILC, PoS(CD09);
 MILC, RMP 82 (2010);
 JLQCD/TWQCD, PoS(LAT2009);
 ETM, JHEP 07 (2009);
 BMW, PRD 82 (2010)

Cabibbo angle



Tensions

- ❖ Uncertainty in V_{cb} affects ϵ_K
- ❖ Inclusive/exclusive tension in V_{cb}
- ❖ As with V_{ub} , exclusive “check” of inclusive result has exposed interesting “features”



B_s mixing

Anomalous like-sign di-muon asymmetry

$$A_{SL}^{D^0} = (-9.6 \pm 2.5 \pm 1.5) \times 10^{-3}$$
$$A_{SL}^{LN} = (-0.20 \pm 0.03) \times 10^{-3}$$

A discrepancy of $\sim 3\sigma$

$$A_{SL} = (0.506 \pm 0.043) a_{fs}^d + (0.494 \pm 0.043) a_{fs}^s$$
$$a_{fs}^d = (-4.1 \pm 0.6) \times 10^{-4}$$

$a_{fs}^{s,SM}$	L&N, '11	L&N, '07
Central Value	$2.11 \cdot 10^{-5}$	$2.06 \cdot 10^{-5}$
$\delta(V_{ub}/V_{cb})$	11.6%	19.5%
$\delta(\mu)$	8.9%	12.7%

Tables from Lenz & Nierste, arXiv:1102.4274 (cf. L&N, JHEP **0706** (2007))

B_s mixing

- ❖ LQCD progress reducing f_{B_s} error by more than half
- ❖ Still dominant uncertainty in ΔM_s
- ❖ Full NLO calculation requires dedicated effort

ΔM_s^{SM}	L&N, '11	L&N, '07
Central Value	17.3 ps ⁻¹	19.3 ps ⁻¹
$\delta(f_{B_s})$	13.2%	33.4%
$\delta(V_{cb})$	3.4%	4.9%
$\delta(\mathcal{B}_{B_s})$	2.9%	7.1%

$\Delta\Gamma_s^{\text{SM}}$	L&N, '11	L&N, '07
Central Value	0.087 ps ⁻¹	0.096 ps ⁻¹
$\delta(\mathcal{B}_{\tilde{R}_2})$	17.2%	15.7%
$\delta(f_{B_s})$	13.2%	33.4%
$\delta(\mu)$	7.8%	13.7%

$$R_{2/\tilde{2}} = \frac{1}{m_b^2} [\bar{s}_\alpha \overleftarrow{D}_\rho \gamma^\mu (1 - \gamma_5) D^\rho b_{\alpha/\beta}] [\bar{s}_{\beta/\alpha} \gamma_\mu (1 - \gamma_5) b_\beta]$$

From Status to Prospects

- ♣ Checks w/ alt. LQCD formulations (actions, etc.)
- ♣ Reduction of errors will occur via
 - ◆ Further-improved actions (*e.g.* NRQCD/HISQ for $B \rightarrow D$)
 - ◆ Nonperturbative operator matching
 - ◆ Fine enough lattices for relativistic b

Rare B decays

- ❖ Talk by David Straub yesterday
- ❖ At large q^2 hadronic physics is determined by $B \rightarrow K^{(*)}$ form factors (Buchalla & Isidori; Grinstein & Pirjol; Beylich, Buchalla, Feldmann)
- ❖ LQCD calculations of the relevant 10 form factors are being completed (Meinel, Liu, *et al*)
- ❖ Permits SM tests with more observables, those where form factors do *not* cancel (Bobeth, Hiller, van Dyk)

Beautiful baryon spectrum

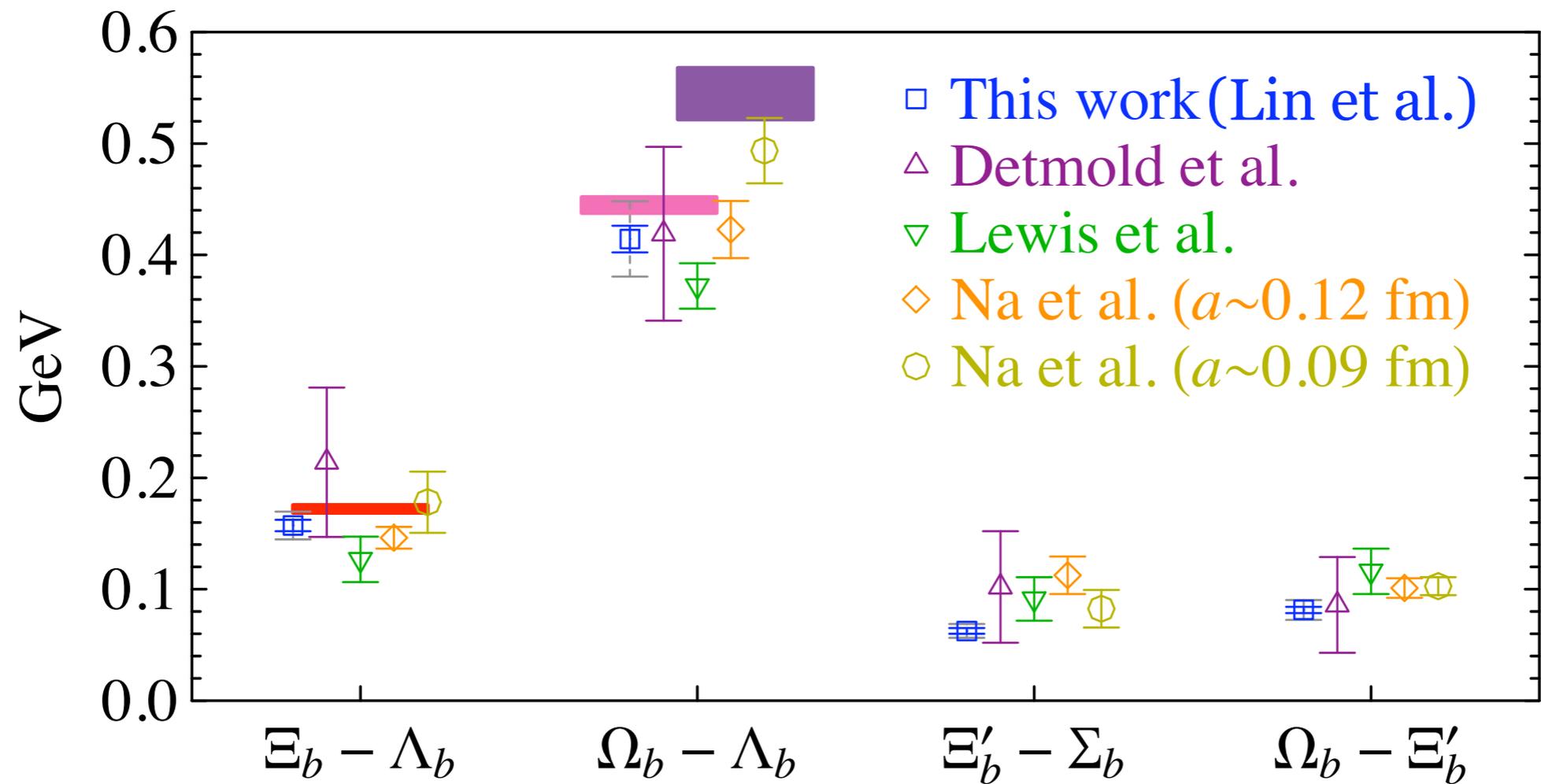


Figure from Lin, Cohen, Mathur, Orginos (2009)
LQCD data also from: Lewis & Woloshyn, PRD **79** (2009);
Detmold, Lin, Wingate, NPB (2009); Na & Gottlieb, PoS
(2008)
Experimental bands: PDG (red), CDF (pink), D0 (purple)

Rare Λ_b decay

$$\Lambda_b \rightarrow \Lambda \ell^+ \ell^-$$

In the static limit, the 12 form factors reduce to only 2 form factors

$$\langle \Lambda(p) | \bar{s} \Gamma b | \Lambda_b(p+q) \rangle = \bar{u}_\Lambda(p) \left[F_1(q^2) + \psi F_2(q^2) \right] \Gamma u_{\Lambda_b}(p+q)$$

Mannel, Roberts, Ryzak, Nucl. Phys. B **355**, 38 (1991)

- ❖ Future LQCD calculation of f.f. at large Q^2
- ❖ Baryons noisier than mesons, esp. pseudoscalars
- ❖ Hard to imagine ever calculating $1/m$ corrections

Conclusions

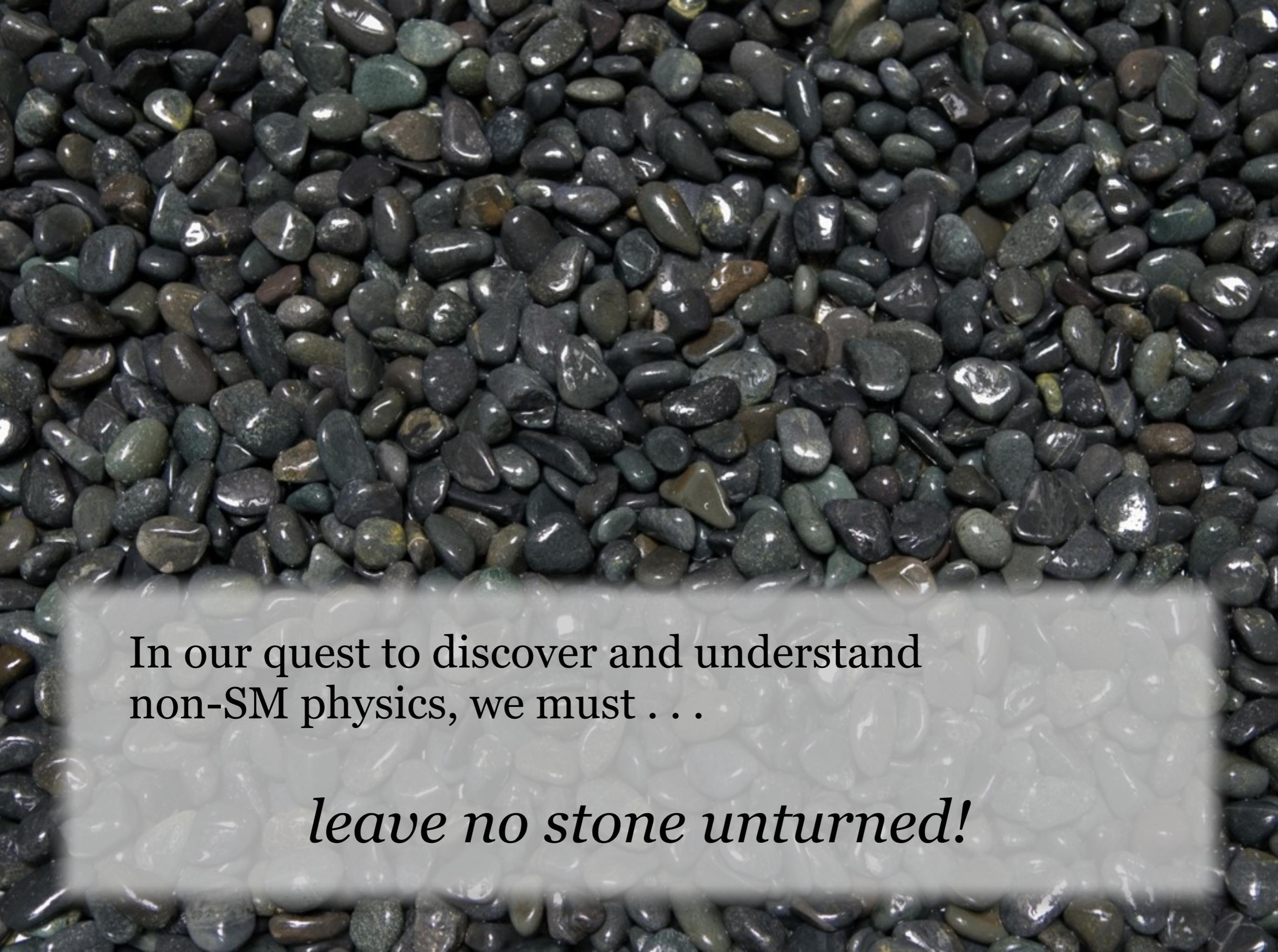
CKM unitarity

- ✦ Recent progress due to light quarks, use of EFT
- ✦ Further reduction of errors, relativistic b
- ✦ Meantime: other choices to confirm or expose hidden systematics

FCNC

- ✦ B_s mixing
- ✦ Rare decays
- ✦ b baryons





In our quest to discover and understand
non-SM physics, we must . . .

leave no stone unturned!