

Beauty 2011, Amsterdam 4th-8th April

First measurement of $\sin 2\beta$
at LHCb with $B^0 \rightarrow J/\psi K_s$



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On behalf of the LHCb
collaboration



CP Violation

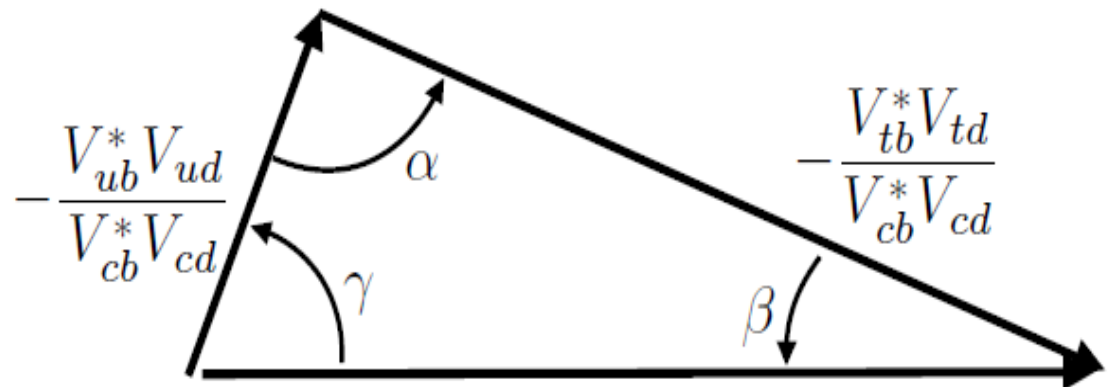
In the standard model **one complex phase** is enough to explain all CPV effects

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

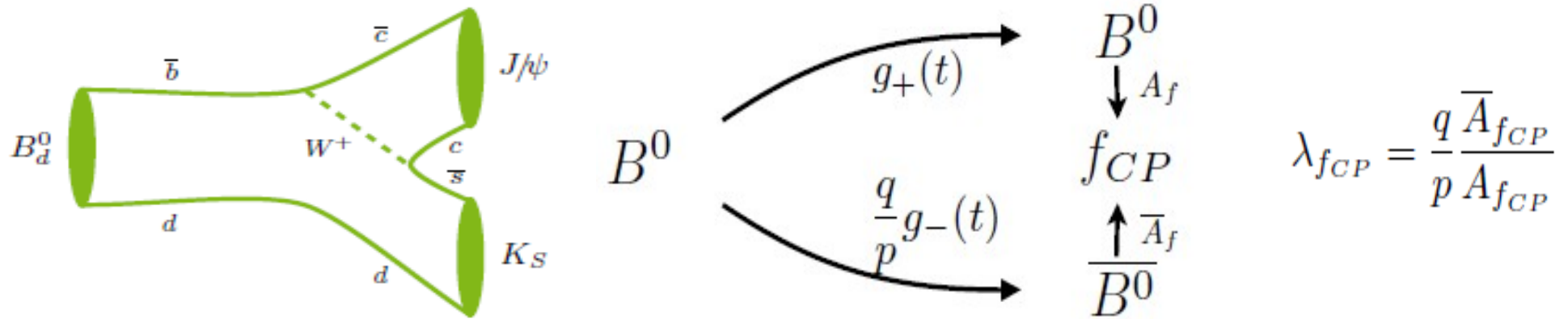
Unitarity conditions of the mixing matrix can be written as 6 **Unitary Triangles**

$$V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$

$$\bar{\rho} + i\bar{\eta} \equiv (\rho + i\eta) \left(1 - \frac{\lambda^2}{2}\right)$$



$\sin 2\beta$ in $B^0 \rightarrow J/\psi K_s$



$$\begin{aligned}
 A_{J/\psi K_S^0} &\equiv \frac{\Gamma(\bar{B}^0(t) \rightarrow J/\psi K_S^0) - \Gamma(B^0(t) \rightarrow J/\psi K_S^0)}{\Gamma(\bar{B}^0(t) \rightarrow J/\psi K_S^0) + \Gamma(B^0(t) \rightarrow J/\psi K_S^0)} \\
 &= S_{J/\psi K_S^0} \sin(\Delta m_d t) - C_{J/\psi K_S^0} \cos(\Delta m_d t).
 \end{aligned}$$

Interference between
mixing & decay

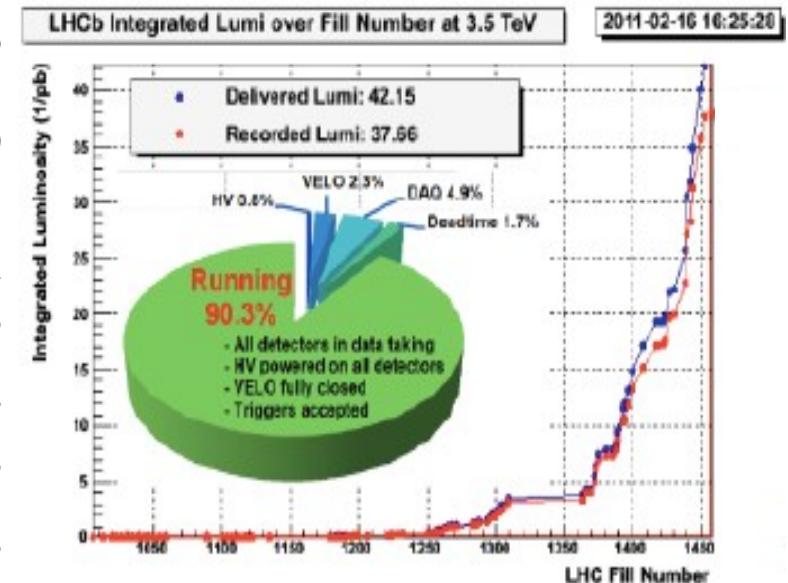
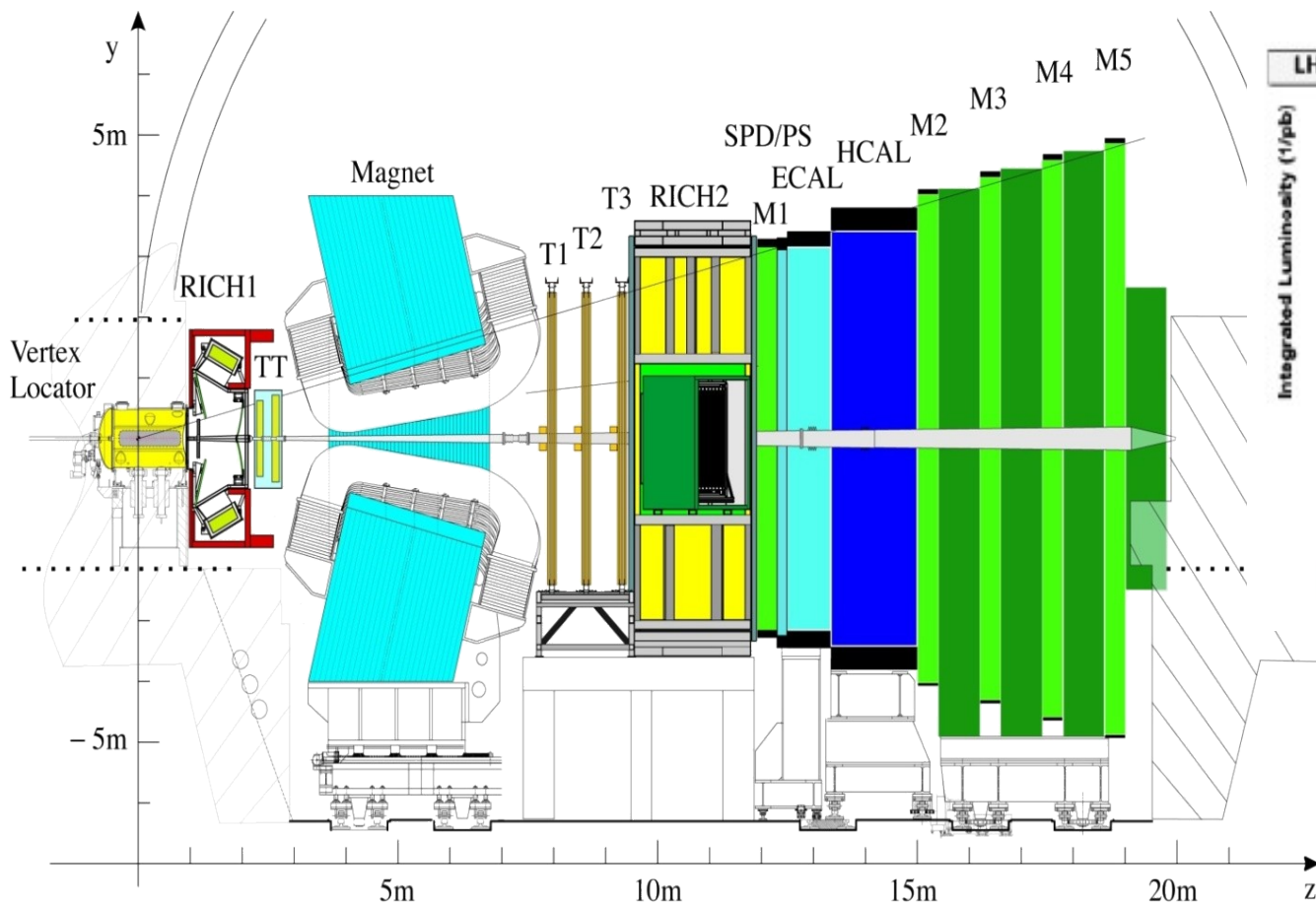
mixing & decay CP
violation (negligible in SM)

$$S_{J/\psi K_S^0} = \sin 2\beta$$

The LHCb experiment

LHCb is dedicated to study CP violation and rare decays in the beauty sector.

Forward spectrometer ($2 < \eta < 5$) characterized by excellent tracking, vertexing, and particle identification system



~37pb⁻¹ collected at 7TeV in 2010 run

Analysis $\sin 2\beta$ with $B^0 \rightarrow J/\psi K_s$

- Selection of signal and trigger
- Flavour Tagging

Calibration of flavour tagging

- Fit

$$A_{J/\psi K_s^0}^{\text{meas}} = (1 - 2\omega) A_{J/\psi K_s^0} \otimes \mathcal{R}(t)$$

- Systematic uncertainties
- Results

World average
 $\sin 2\beta = 0.673 \pm 0.023$

Show first results at LHCb of CP violation in

$B^0 \rightarrow J/\psi K_s$

Trigger and selection

- 35 pb⁻¹ at $\sqrt{s} = 7$ TeV in 2010
- Trigger

Contains components which biases the proper time distribution of the selected events (impact parameter cut)

To increase statistics time biased trigger lines ($\sim 20\%$) are also used

Added acceptance for biased events $\epsilon_S(t) = \frac{(a_a t)^{c_a}}{1 + (a_a t)^{c_a}}$

- Common selection for $b \rightarrow J/\psi X$
- Only tagged events are sensitive to $\sin 2\beta$
- Selection of ~ 280 tagged events for $B^0 \rightarrow J/\psi K_s$

Flavour Tagging

- Flavour Tagging is the procedure to determine the flavour of the reconstructed B meson at production time

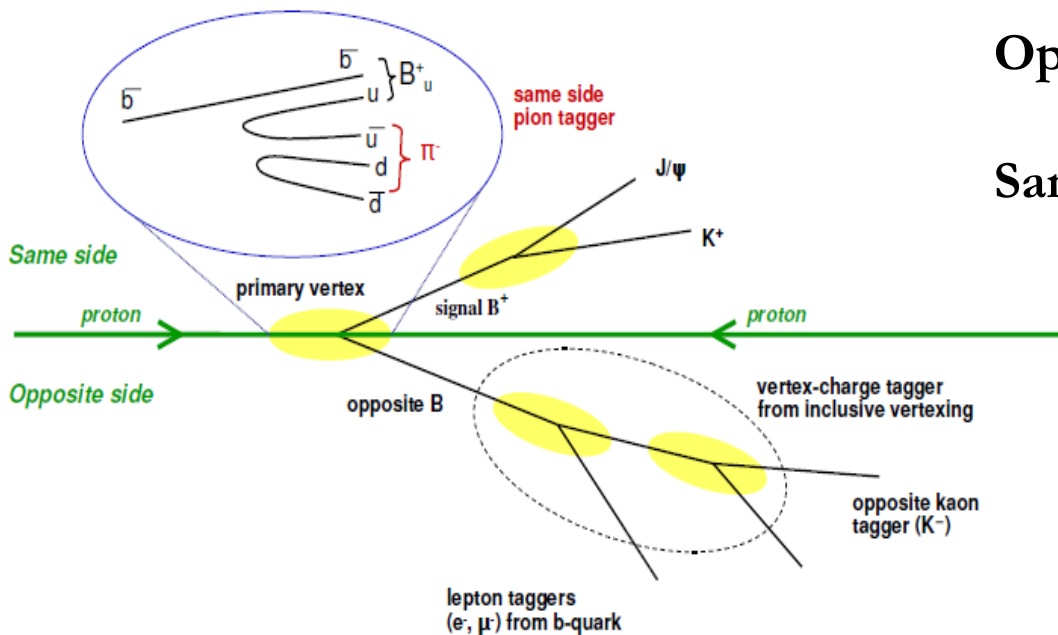
Taggers

Opposite Side:

muons, electrons, kaons, vertex charge

Same Side:

kaons (B_s) or pions ($B_{d,u}$)



$$\varepsilon_{tag} = \frac{N_R + N_W}{N_R + N_W + N_U} \quad \omega = \frac{N_W}{N_R + N_W}$$

$$\varepsilon_{eff} = \varepsilon_{tag} (1 - 2\omega)^2$$

- When measuring $\sin 2\beta$ it is crucial to know the initial flavour of the decaying B.

The measurement is influenced directly by the tagging dilution.

Calibration of Flavour Tagging

- For each event an estimated probability of the tagging decision to be correct (η) is given by a neural net.

Calibration of η is needed to obtain an ω event per event

- Use per event mistag as observable $\omega = p_0 + p_1 \cdot (\eta - \bar{\eta})$
- $B^+ \rightarrow J/\psi K^+$ used for calibration, and the kinematically similar $B^0 \rightarrow J/\psi K^*$ is used as crosscheck

MC ω distribution/calibration totally compatible with $B^0 \rightarrow J/\psi K_s$

Study correction function between actual mistag and calibrated mistag

Expected	Obtained
$p_0 = \bar{\eta} = 0.35$	$p_0 = 0.333 \pm 0.025$
$p_1 = 1$	$p_1 = 0.71 \pm 0.36$

Likelihood Fit

- The CP violation parameters are extracted through a simultaneous multidimensional unbinned extended maximum likelihood fit.

$$\mathcal{L}(\vec{\lambda}) = \frac{e^{-N} N^n}{n!} \prod_s \prod_{i=1}^{N^s} \mathcal{P}^s(\vec{x}_i; \vec{\lambda}_s)$$

- The fit is done simultaneous in 4 subsamples:

triggered by lifetime **biased/unbiased** (B/U) lines, and **tagged/untagged** (t,u) events

- We consider 4 observables:

the reconstructed **mass** of the **B** candidate, its **proper time** t , the flavour **tagging decision**, and the combined per-event mistag ω

- The pdf consists of three components:

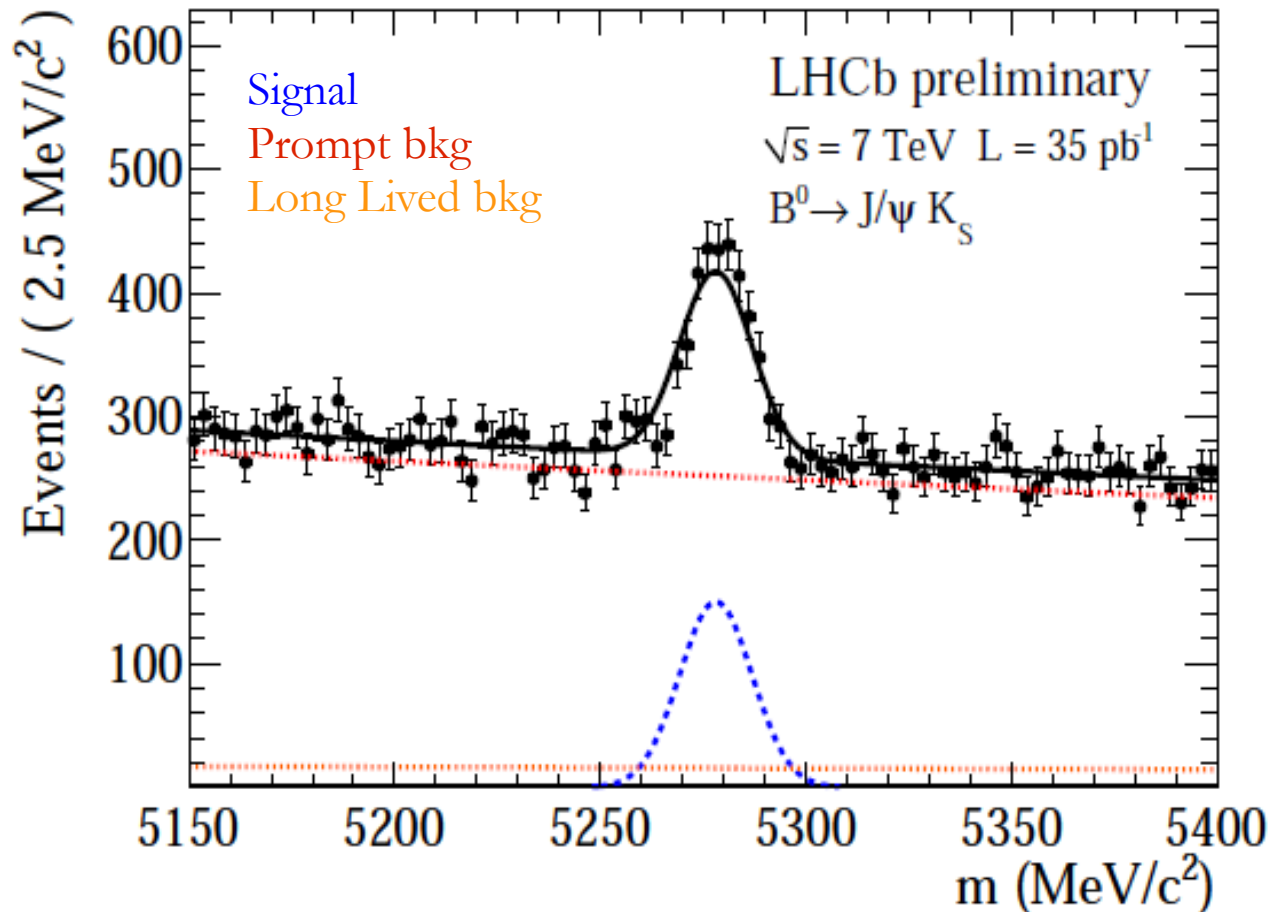
Signal (S), **prompt bkg** (P) and **long lived bkg** (L)

Parametrization (I)

- **Mass p.d.f**

Signal: Single Gaussian
(parameters shared)

Bkg: Exponential
(P, L bkg have similar
mass distribuion, use the
same parametrization for
both)



Parametrization (II)

- Proper time p.d.f

$$\mathcal{P}_S(t, d, \omega) = \mathcal{P}_S(t, d|\omega) \cdot \mathcal{P}_S(\omega)$$

$$\mathcal{P}_B(t, d, \omega) = \mathcal{P}_B(t, d) \cdot \mathcal{P}_B(\omega)$$

Describes decay, mixing and CP violation

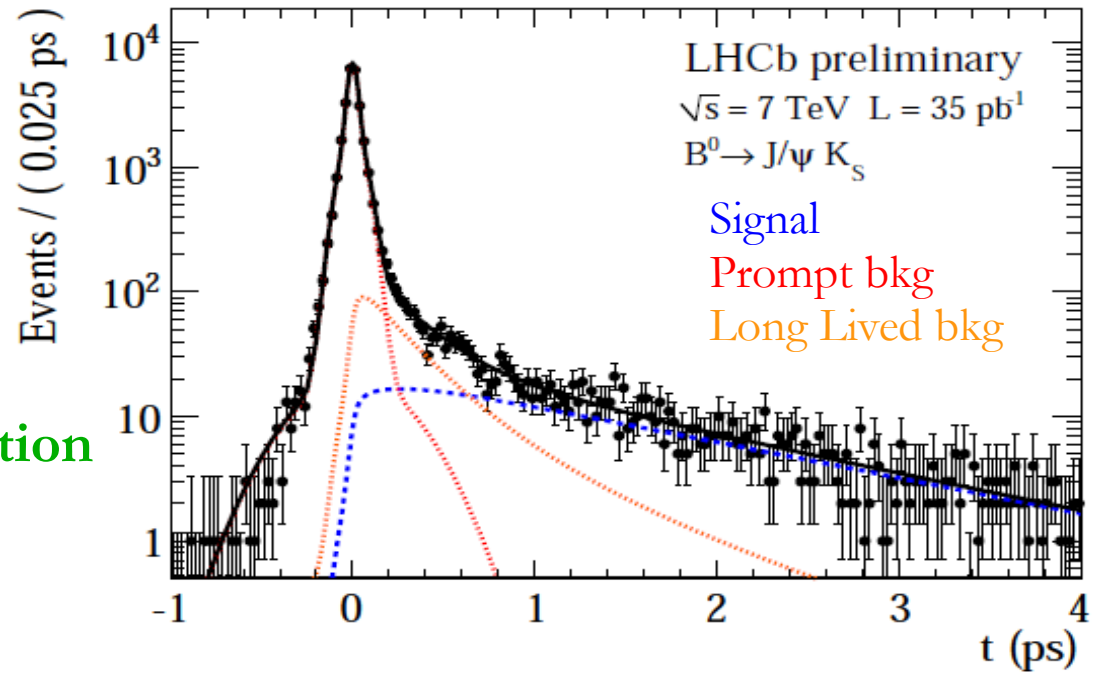
Acceptance effects

$$\mathcal{P}_S(t, d|\omega) = \epsilon_S(t) \cdot \left(\mathcal{P}_{S,CP}(t, d|\omega) \otimes \mathcal{R}(t) \right)$$

$$\mathcal{P}_P(t) \propto \delta(t) \otimes \mathcal{R}(t; \lambda_{R,t})$$

$$\mathcal{P}_L^U(t; \lambda_{L,t}^U) = \left(f_{L,t}^U \cdot \frac{1}{N_{L,1}^U} e^{-t/\tau_{L,1}^U} + (1 - f_{L,t}^U) \cdot \frac{1}{N_{L,2}^U} e^{-t/\tau_{L,2}^U} \right) \otimes \mathcal{R}(t; \lambda_{R,t})$$

$$\mathcal{P}_{L,t}^B(t; \lambda_{L,t}^B) \propto e^{-t/\tau_L^B} \otimes \mathcal{R}(t; \lambda_{R,t})$$



Resolution (triple gaussian)
Constrain due to prompt component

Systematic uncertainties

- Tagging (main effect),
 - Calibration: Propagate uncertainties on calibration (multiply gaussian priors to full pdf). Fit with the parameters obtained with the control channel
 - Per event mistag
- Production asymmetry (asymmetry in $B^0, \bar{B}^0 \epsilon_{\text{tag}}$)
- Proper time resolution (variation to statistic accuracy)
- Acceptance
 - Biased events (propagate the errors of acceptance function)
 - High proper time (omited correction for high t in test fit)
- Δm_d fixed to pdg value, refit with $\pm\sigma$

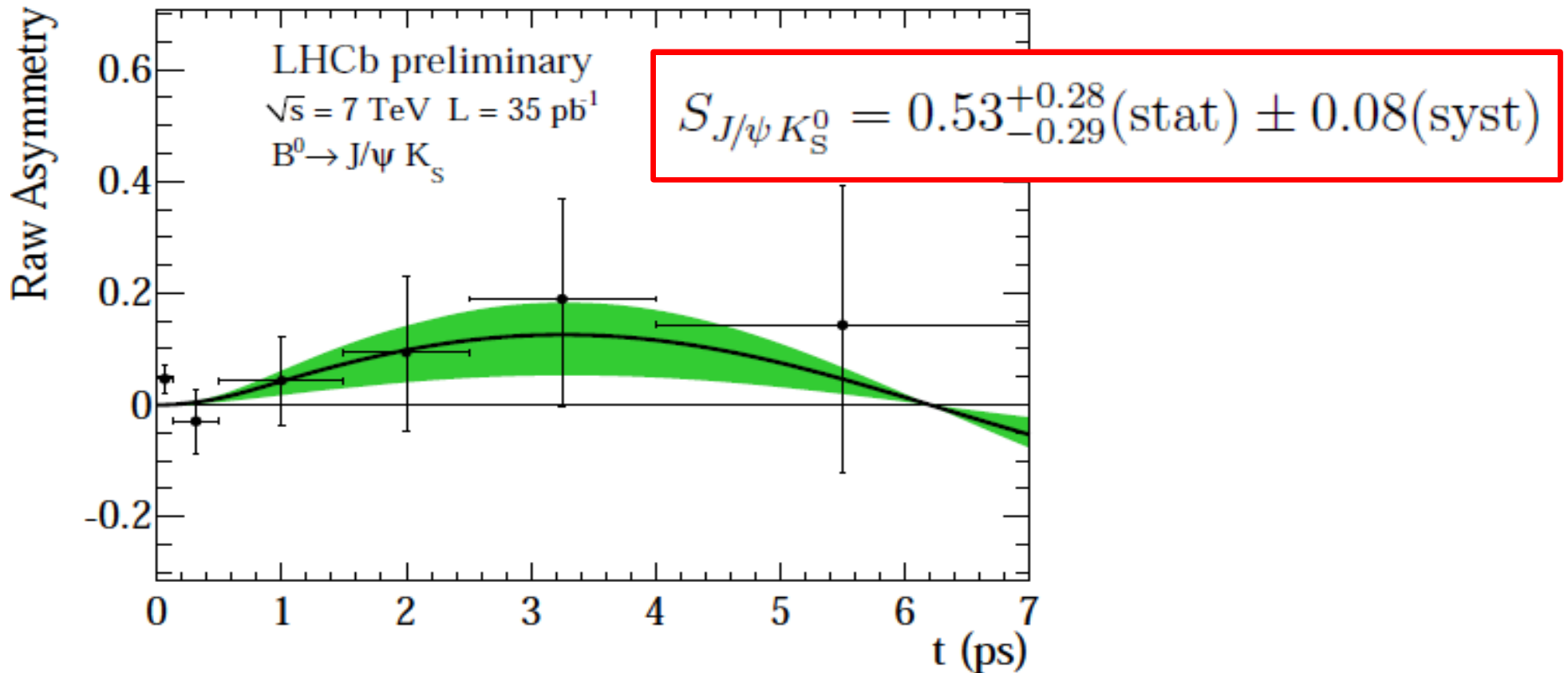
Systematic uncertainties

List of systematic uncertainties

Source	uncertainty
tagger calibration	0.067
per-event mistags p.d.f.	0.012
Δm_d uncertainty, z-scale	0.0017
proper time resolution	0.0085
high proprietime acceptance	0.00065
biased events acceptance	0.0042
production asymmetry	0.041
total (sum in squares)	0.080

Results: $\sin 2\beta$

LHCb measurement of CP violation in $\sin 2\beta$



Statistically compatible with world average

$$\sin 2\beta = 0.673 \pm 0.023$$

Floating $C_{J/\psi K_S}$

- Refit without assuming null direct CP violation in SM
- When floating $C_{J/\psi K_S}$ a correlation appears

$$\rho(S_{J/\psi K_S}, C_{J/\psi K_S}) = 0.53$$

will not decrease with more statistics (sensitivity comes from proper time)

- Results are compatible with world average measurements

$$C_{J/\psi K_S^0} = 0.28_{-0.32}^{+0.32}$$

$$S_{J/\psi K_S^0} = 0.38_{-0.35}^{+0.34}$$

Conclusion

- Performed time dependent tagged CP analysis
- Flavour tagging is already performing in LHCb
- First measurement of $\sin 2\beta$ in LHCb

Measurement of $\sin 2\beta$

$$S_{J/\psi K_s^0} = 0.53_{-0.29}^{+0.28}(\text{stat}) \pm 0.08(\text{syst})$$

Results consistent with world average

- Waiting for more data

LHCb coll. “Measurement of CP violation in the time-dependent analysis of $B^0 \rightarrow J/\psi K_s$ decays with the 2010 data”,

LHCb-CONF-2011-004

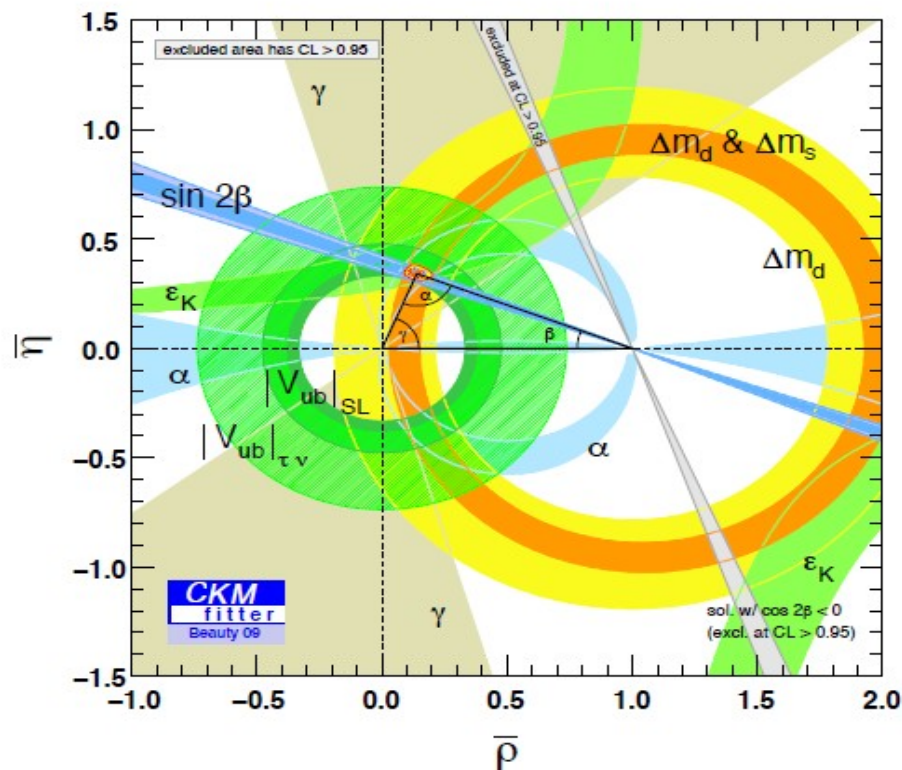
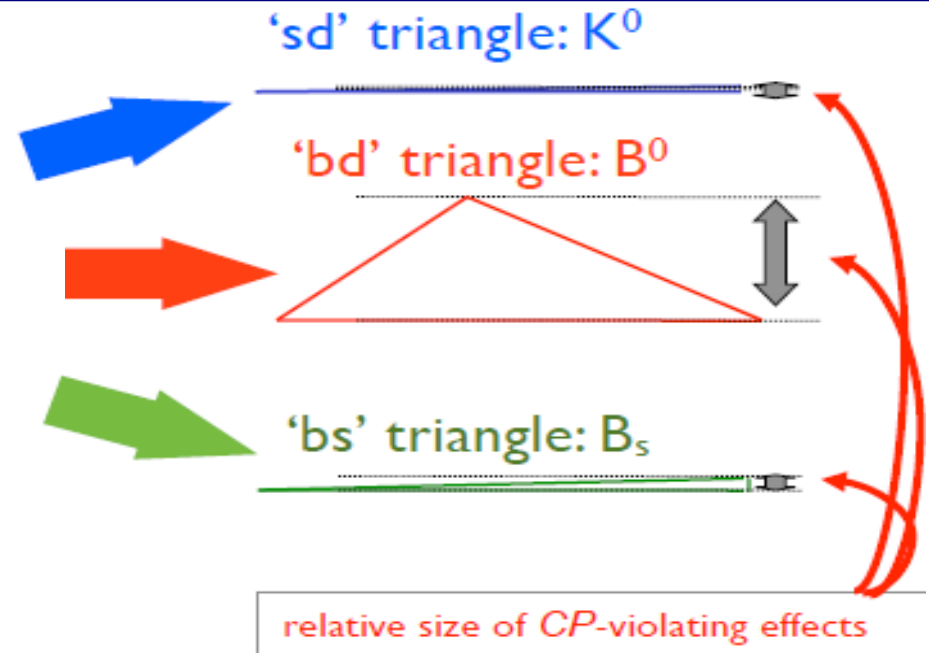
Back-Up

More on CP violation

$$V_{us}^* V_{ud} + V_{cs}^* V_{cd} + V_{ts}^* V_{td} = 0$$

$$V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$

$$V_{ub}^* V_{us} + V_{cb}^* V_{cs} + V_{tb}^* V_{ts} = 0$$

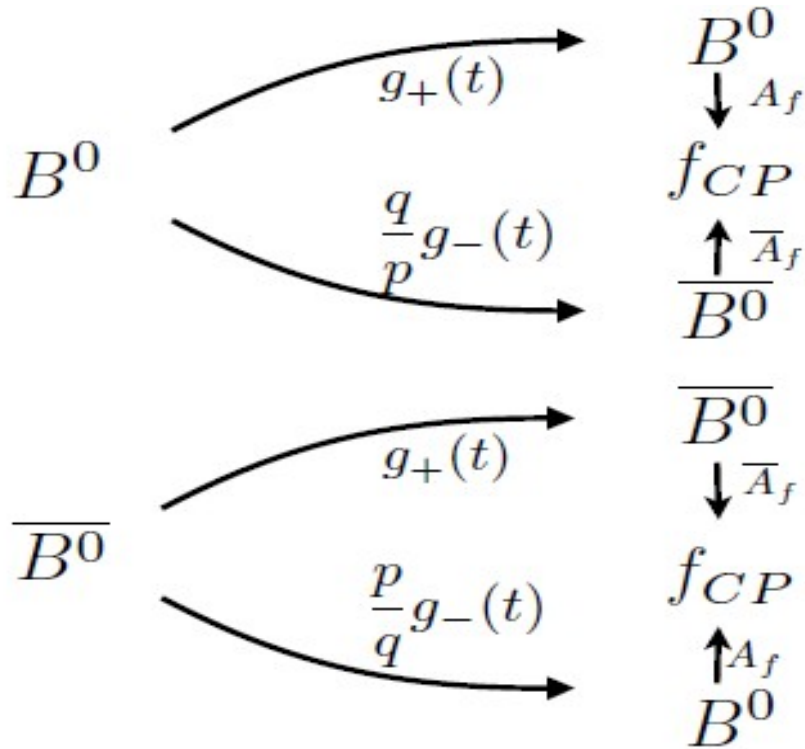


$$\alpha = \arg \left(-\frac{V_{tb}^* V_{td}}{V_{ub}^* V_{ud}} \right)$$

$$\gamma = \arg \left(-\frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}} \right)$$

$$\beta = \arg \left(-\frac{V_{cb}^* V_{cd}}{V_{tb}^* V_{td}} \right)$$

CP violation in B mesons



Amplitude

$$A_{f_{CP}} e^{-imt} e^{-\Gamma t/2} \left(\cos \frac{\Delta mt}{2} + \lambda_{f_{CP}} i \sin \frac{\Delta mt}{2} \right)$$

$$g_+(t) = e^{-imt} e^{-\Gamma t/2} \cos \frac{\Delta mt}{2}$$

$$g_-(t) = e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta mt}{2}$$

$$\lambda_{f_{CP}} = \frac{q \overline{A}_{f_{CP}}}{p A_{f_{CP}}}$$

$$\overline{A}_{f_{CP}} e^{-imt} e^{-\Gamma t/2} \left(\cos \frac{\Delta mt}{2} + \frac{1}{\lambda_{f_{CP}}} i \sin \frac{\Delta mt}{2} \right)$$

$$B^0 \rightarrow f_{CP}$$

$$\overline{B^0} \rightarrow f_{CP}$$

Rate

$$\frac{1}{2} e^{-\Gamma t} \left[1 + \left(\frac{1 - |\lambda|^2}{1 + |\lambda|^2} \right) \cos(\Delta mt) - \left(\frac{2\mathcal{I}(\lambda)}{1 + |\lambda|^2} \right) \sin(\Delta mt) \right]$$

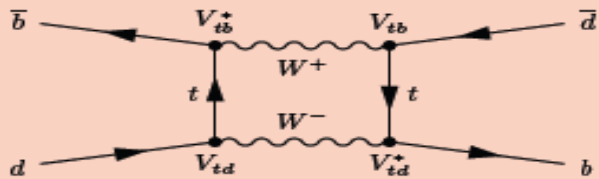
$$\frac{1}{2} e^{-\Gamma t} \left[1 - \left(\frac{1 - |\lambda|^2}{1 + |\lambda|^2} \right) \cos(\Delta mt) + \left(\frac{2\mathcal{I}(\lambda)}{1 + |\lambda|^2} \right) \sin(\Delta mt) \right]$$

CP violation in $B^0 \rightarrow J/\psi K_s$

$$\lambda_{J/\psi K_s} \equiv \frac{q \bar{A}_{J/\psi K_s}}{p A_{J/\psi K_s}}$$

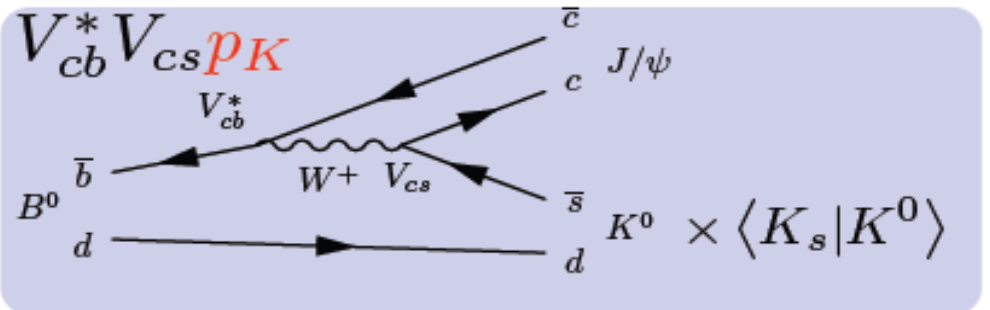
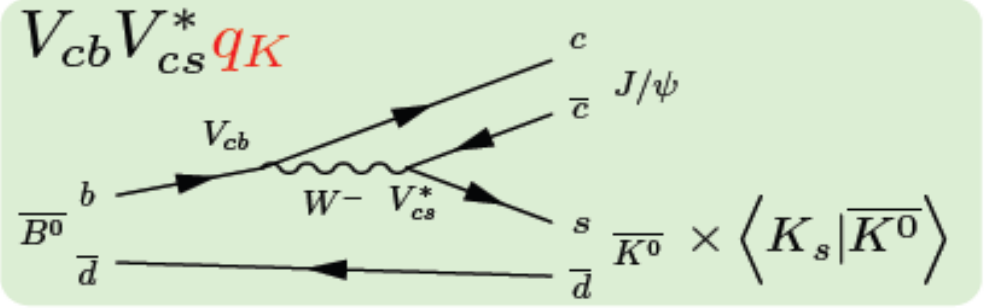
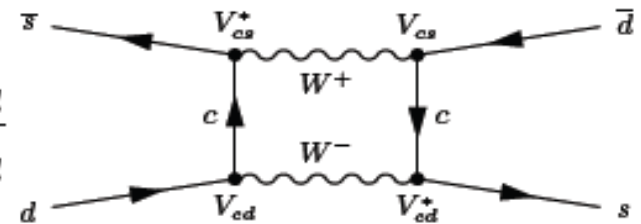
$$= - \frac{q \bar{A}_{J/\psi \bar{K}^0, \bar{K}^0 \rightarrow K_s}}{p A_{J/\psi K^0, K^0 \rightarrow K_s}}$$

$$\frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*}$$



$$\lambda_{J/\psi K_s} = -e^{-2i\beta}$$

$$\frac{qK}{pK} \approx \frac{V_{cs}^* V_{cd}}{V_{cs} V_{cd}^*}$$



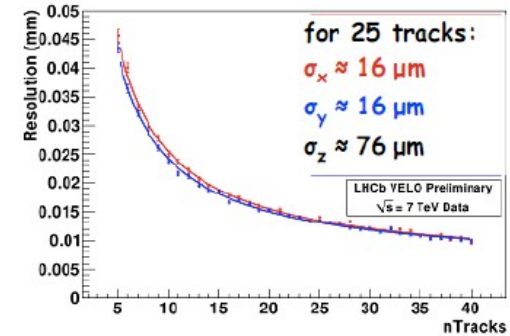
$$|K_s\rangle = pK |K^0\rangle + qK |\bar{K}^0\rangle$$

$$A_{CP} = \frac{\Gamma(\bar{B}^0 \rightarrow J/\psi K_s) - \Gamma(B^0 \rightarrow J/\psi K_s)}{\Gamma(\bar{B}^0 \rightarrow J/\psi K_s) + \Gamma(B^0 \rightarrow J/\psi K_s)} = \sin(2\beta) \sin(\Delta m t)$$

The LHCb experiment

PV resolution:

Data: 16 μm for X & Y and 76 μm for Z
MC: 11 μm for X & Y and 60 μm for Z

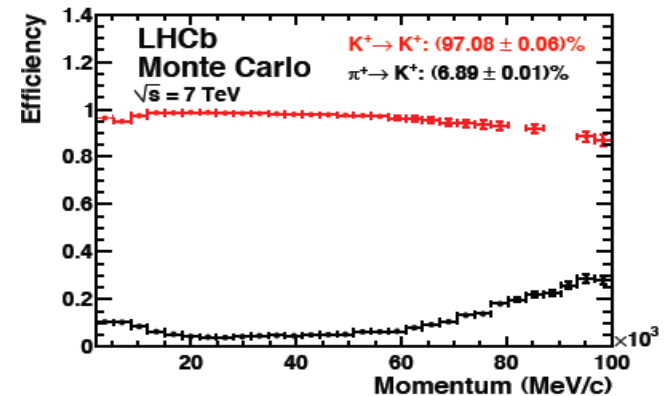


IP resolution:

$\sim 15 \mu\text{m}$ for highest pt bins

PID: RICH

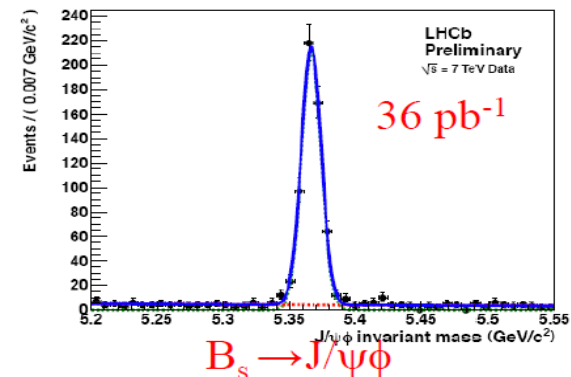
Enables clean reconstruction of various hadronic decay channels of $D(s)$ and $B(s)$ mesons



$\sigma_m = 7 \text{ MeV}$

Tracking:

Excellent mass resolution



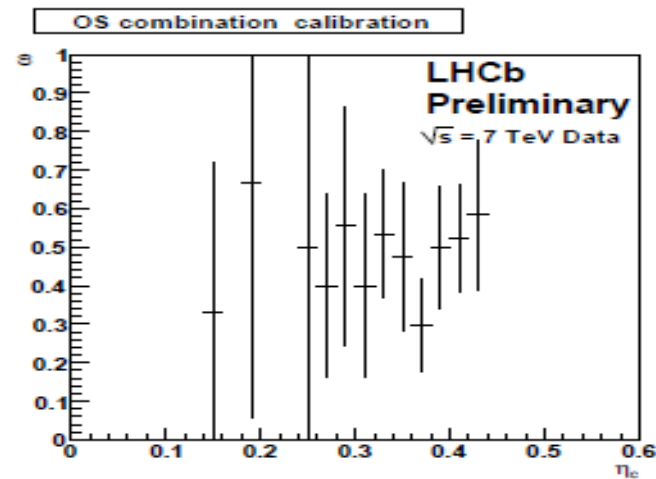
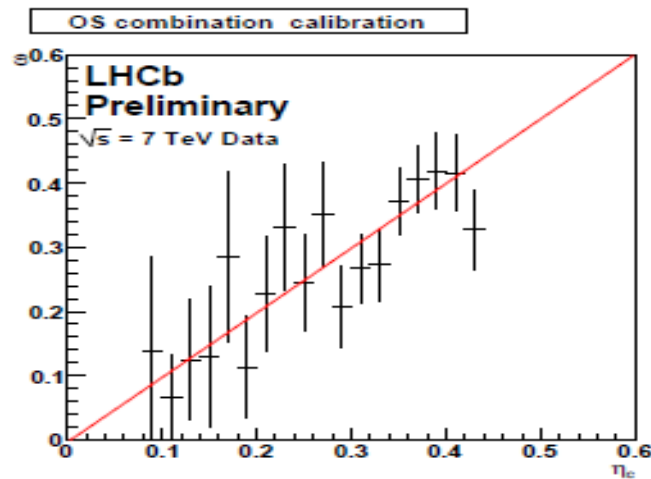
$B_s \rightarrow J/\psi\phi$

Calibration of Flavour Tagging

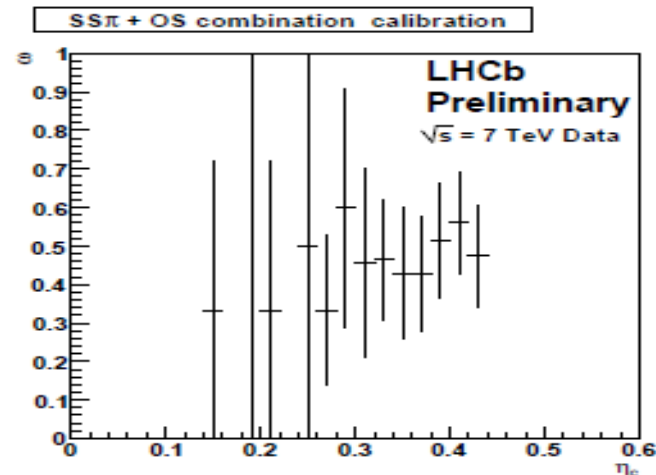
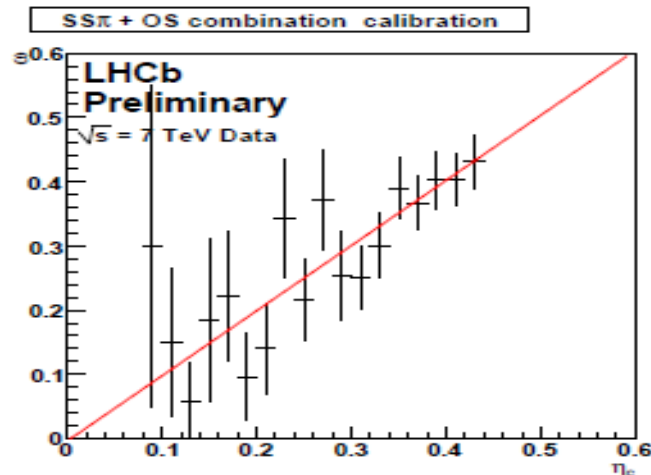
- Calibration of $B^+ \rightarrow J/\psi K^+$

Signal

Bkg



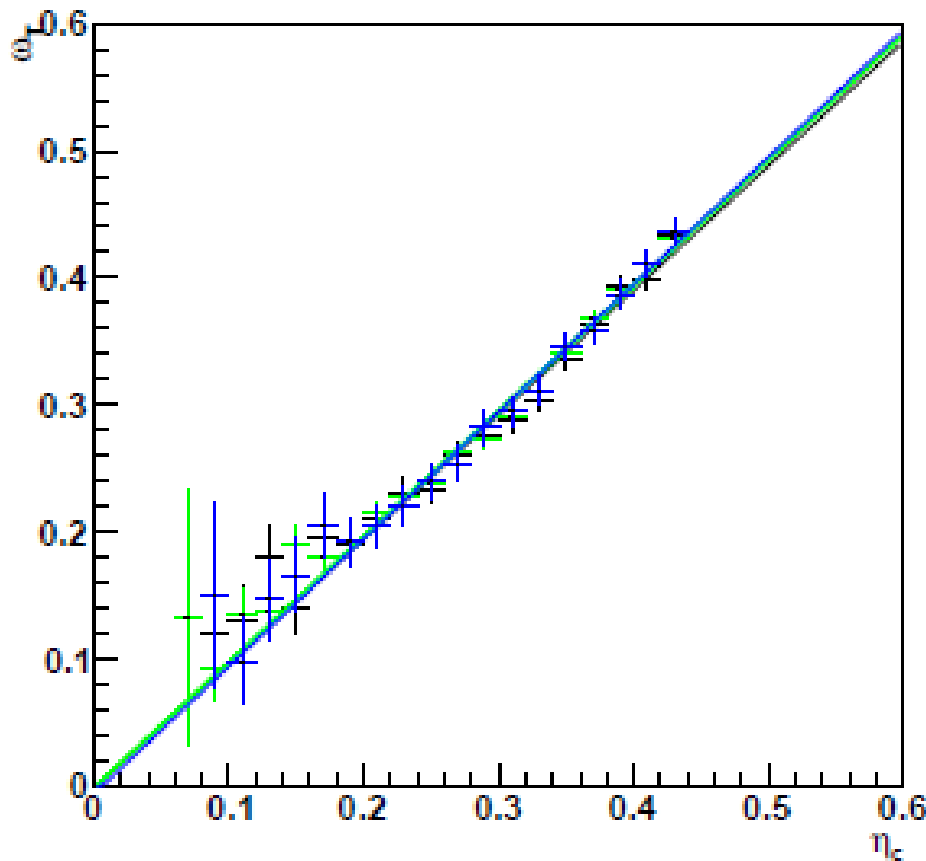
OS
combination



OS + SS
combination

Calibration of Flavour Tagging

- MC validation of tagging with other channels



$B^+ \rightarrow J/\psi K^+$
 $B^0 \rightarrow J/\psi K^*$
 $B^0 \rightarrow J/\psi \phi$

LHCb coll. “Optimization and calibration of the LHCb flavour tagging performance using 2010 data”,
LHCb-CONF-2011-003

Lifetime

- The fitted value is:

$$\tau(B^0 \rightarrow J/\psi K_S^0) = 1.558 \pm 0.056 \text{ (stat.)} \pm 0.022 \text{ (syst.) ps}$$

$$\text{PDG evaluation (ps)} \quad 1.525 \pm 0.009$$

- The proper time has a high precision in the fit
- We include acceptance correction in agreement with:

LHCb coll. “b-hadron lifetime measurements with exclusive $b \rightarrow J/\psi X$ decays reconstructed in the 2010 data”, LHCb-CONF-2011-001

Parametrization (III)

- The efficiency function describes acceptance effects observed in the biased sample at low proper times..

$$\epsilon_S(t) = \frac{(a_a t)^{c_a}}{1 + (a_a t)^{c_a}}$$

- CP p.d.f

Correction for acceptance
at high lifetimes

$$\mathcal{P}_{S,CP}^t(t, d|\omega) \propto e^{-t/\tau'} (1 - d(1 - 2\omega) S_{J/\psi K_S^0} \sin \Delta m_d t + d(1 - 2\omega) C_{J/\psi K_S^0} \cos \Delta m_d t)$$

$$\mathcal{P}_{S,CP}^u(t) \propto e^{-t/\tau'}$$

Describes decay, mixing and CP violation in the B^0 system.

Parametrization (IV)

- Per event mistag probability (included in full pdf)

Use sPlot technique to extract histo pdf for sig/bkg η_c distribution

- The B^0 lifetime is shared in all four sample
- Δm_d , $S_{J/\psi K}$, $C_{J/\psi K}$ shared between the tagged sample

Fit details

- Fit results and fitted event yields on the full $B^0 \rightarrow J/\psi K_s$

Parameter	Unit	Fitted Value	Sample	Parameter	Fitted Value
$S_{J/\psi K_s^0}$		$0.53_{-0.29}^{+0.28}$	U,t	$N_S^{U,t}$	221_{-17}^{+17}
m_S	MeV/ c^2	$5278.13_{-0.29}^{+0.29}$		$N_P^{U,t}$	3218_{-62}^{+62}
$\sigma_{S,m}$	MeV/ c^2	$8.82_{-0.24}^{+0.24}$		$N_L^{U,t}$	309_{-30}^{+33}
τ	ps	$1.517_{-0.045}^{+0.046}$		$N_S^{B,t}$	$59.8_{-8.0}^{+8.7}$
α_m^B	(MeV/ c^2) $^{-1}$	$-8.71_{-3.8}^{+3.8} \cdot 10^{-4}$	B,t	$N_P^{B,t}$	164_{-14}^{+14}
α_m^U	(MeV/ c^2) $^{-1}$	$-5.864_{-0.87}^{+0.87} \cdot 10^{-4}$		$N_L^{B,t}$	102_{-12}^{+12}
$f_{L,t}^U$		$0.836_{-0.054}^{+0.049}$	U,u	$N_S^{U,u}$	767_{-31}^{+32}
$\tau_{L,1}^U$	ps	$0.221_{-0.032}^{+0.036}$		$N_P^{U,u}$	21134_{-161}^{+161}
$\tau_{L,2}^U$	ps	$1.04_{-0.16}^{+0.24}$		$N_L^{U,u}$	807_{-74}^{+79}
τ_L^B	ps	$0.482_{-0.027}^{+0.029}$		$N_S^{B,u}$	279_{-18}^{+18}
$f_{\mathcal{R},1}$		$0.500_{-0.019}^{+0.019}$	B,u	$N_P^{B,u}$	747_{-29}^{+30}
$f_{\mathcal{R},2}$		$0.477_{-0.017}^{+0.017}$		$N_L^{B,u}$	339_{-22}^{+23}
$\sigma_{\mathcal{R},1}$	ps	$0.02522_{-0.00066}^{+0.00066}$			
$\sigma_{\mathcal{R},2}$	ps	$0.0685_{-0.0015}^{+0.0016}$			
$\sigma_{\mathcal{R},3}$	ps	$0.293_{-0.017}^{+0.019}$			