

Improving theory predictions for SM processes

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Science & Technology
Facilities Council

UK Research
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PITT PACC Workshop: LHC physics for Run 3
7th April 21



Improving theory predictions for SM processes

...to help to discover new physics in Run 3

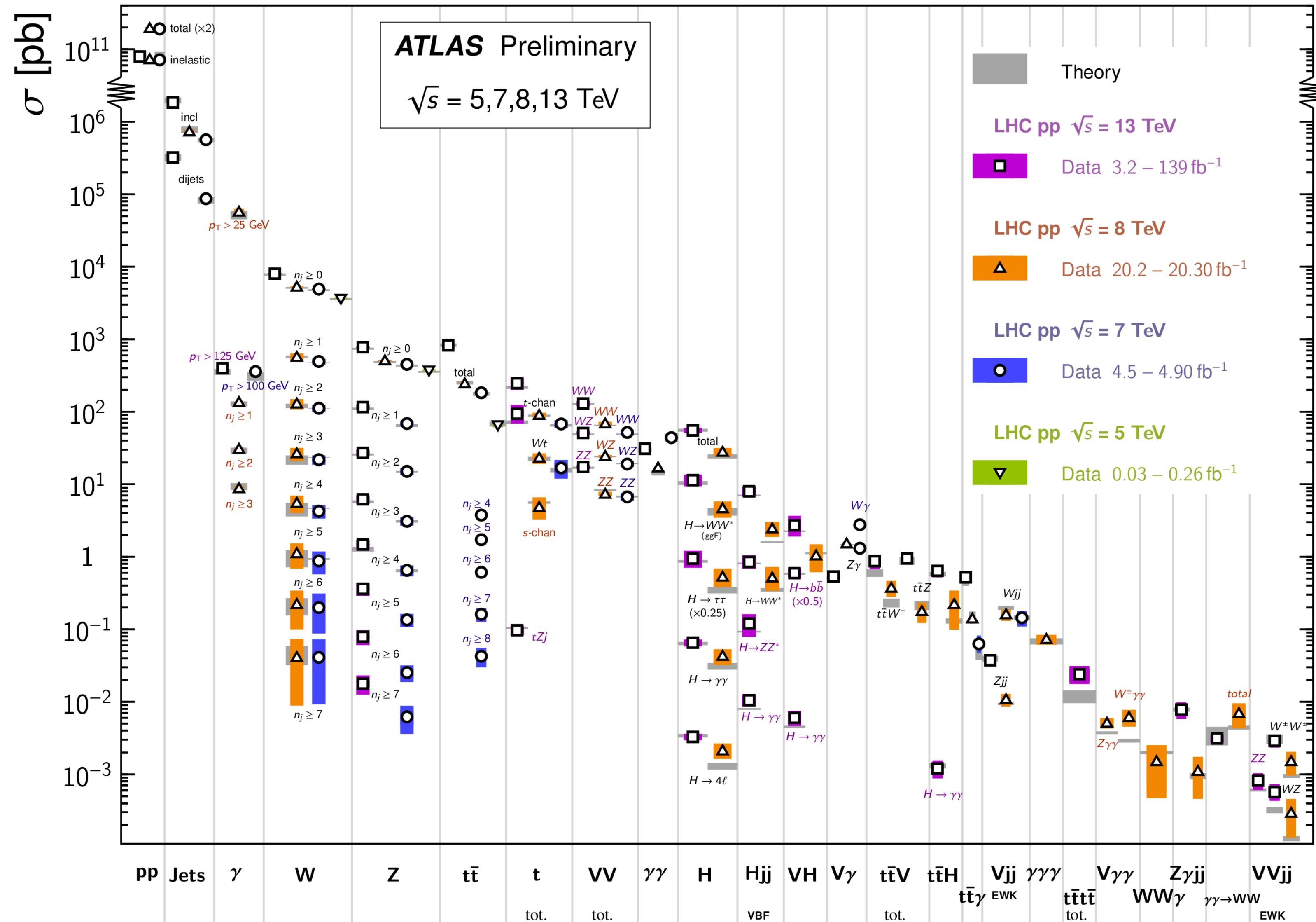
What lessons have been learned from Run 2 analyses?

How to apply these lessons to Run 3?

The success of the SM

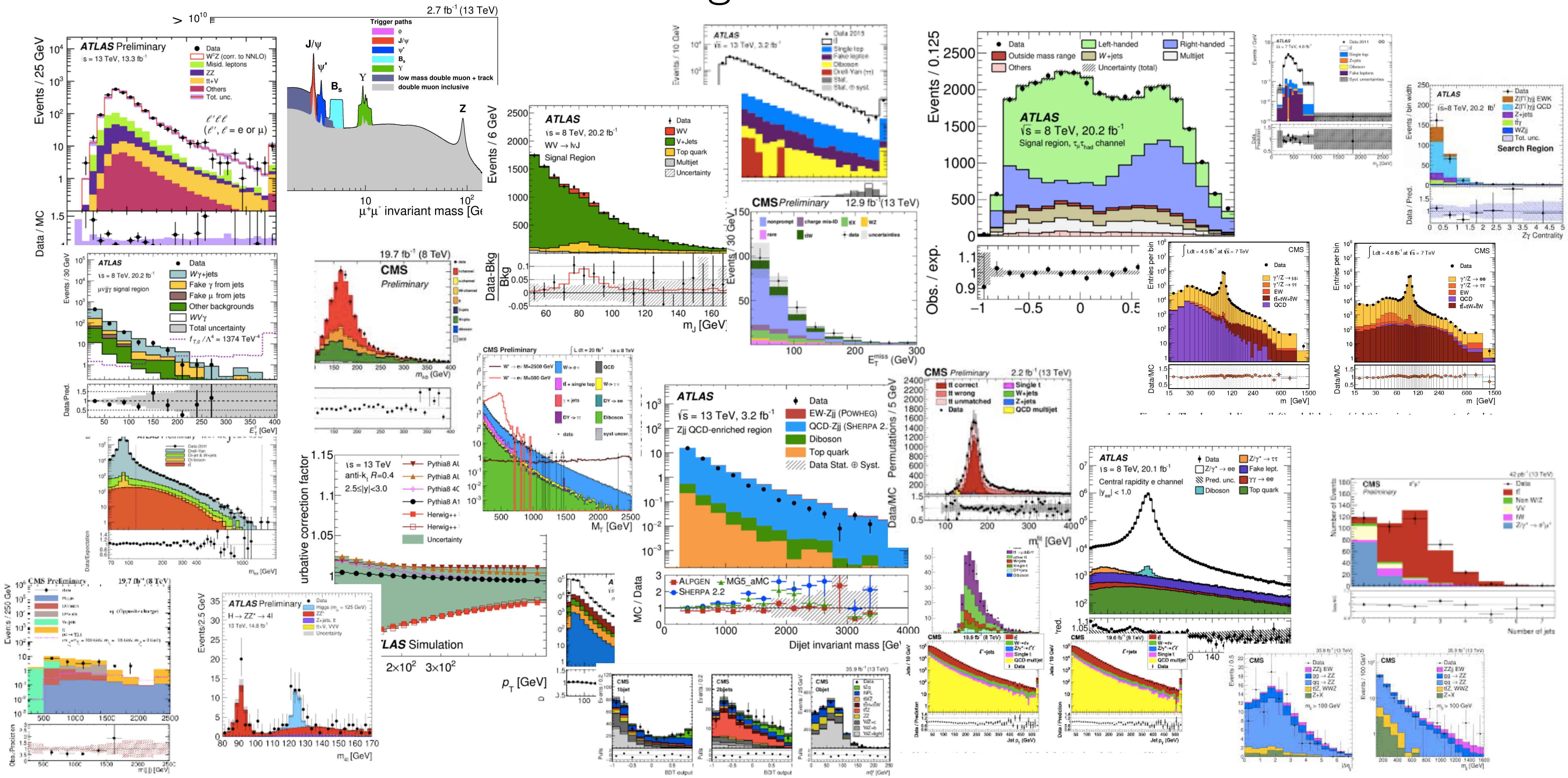
Standard Model Production Cross Section Measurements

Status: March 2021



Overall extremely good experiment-theory agreement

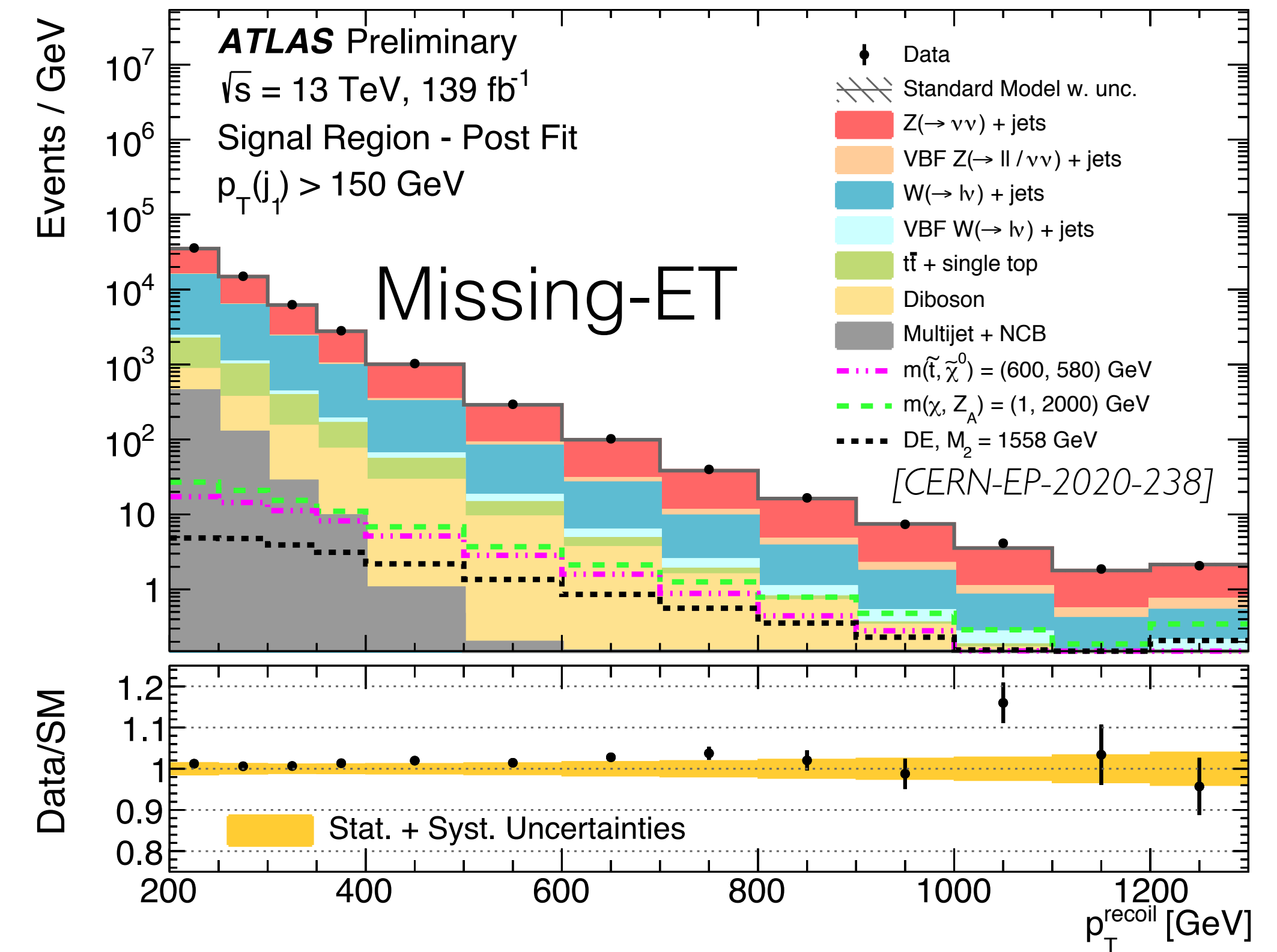
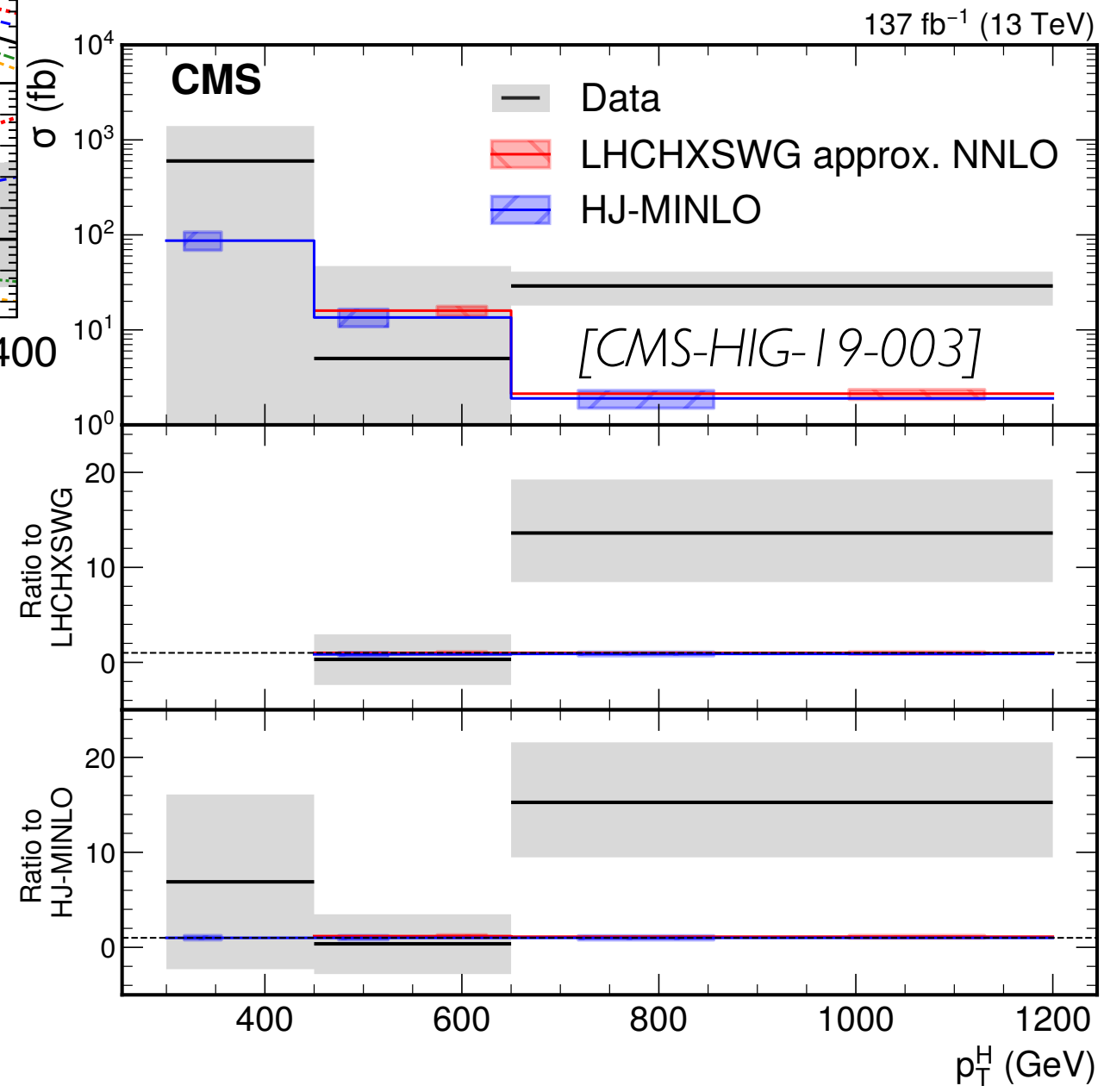
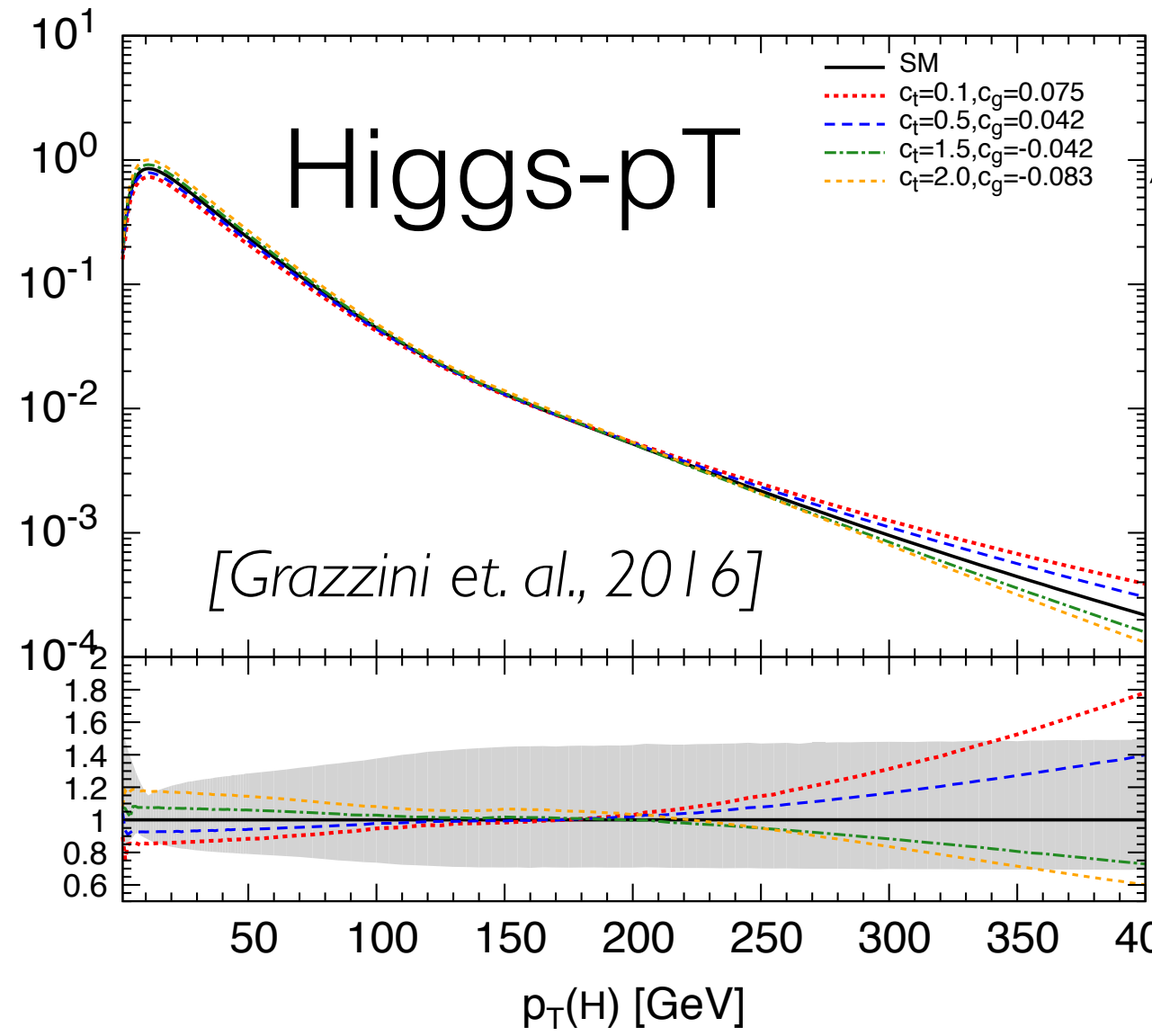
Goal: go differential



The need for precision in tails

Indirect searches

Direct searches



- In case new physics is heavy: expect small deviations in tails of distributions
- good control on theory necessary!

- Dark Matter particles produced at the LHC leave the detectors unobserved: signature missing transverse energy
- large irreducible SM backgrounds
- good control on theory necessary!

Theoretical Predictions for the LHC

Hard (perturbative) scattering process:

$$d\sigma = d\sigma_{\text{LO}} + \alpha_S d\sigma_{\text{NLO}} + \alpha_{\text{EW}} d\sigma_{\text{NLO EW}} + \alpha_S^2 d\sigma_{\text{NNLO}} + \alpha_{\text{EW}}^2 d\sigma_{\text{NNLO EW}} + \alpha_S \alpha_{\text{EW}} d\sigma_{\text{NNLO QCD} \times \text{EW}}$$

NLO **QCD** (standard in NLOPS MC's):

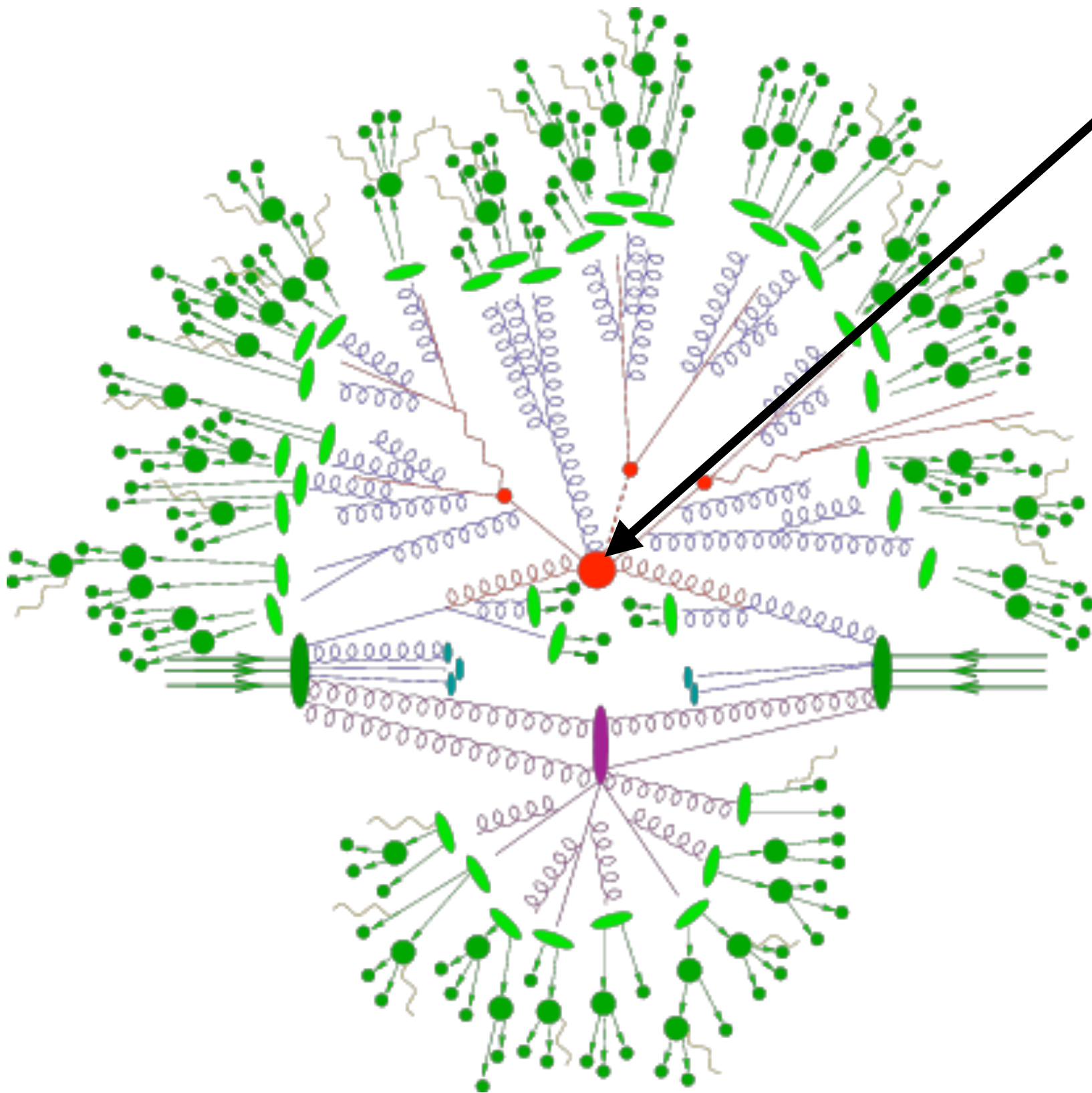
- O(10-100%) corrections with respect to LO
- often not covered by LO scale variations
- opening up of new channels / phase space

NNLO **QCD** (known for pretty much all $2 \rightarrow 2$ SM processes)

- O(1-10%) corrections with respect to NLO **QCD**
- remaining uncertainty: O(1%)

NLO **EW** (available at fixed-order for any SM process):

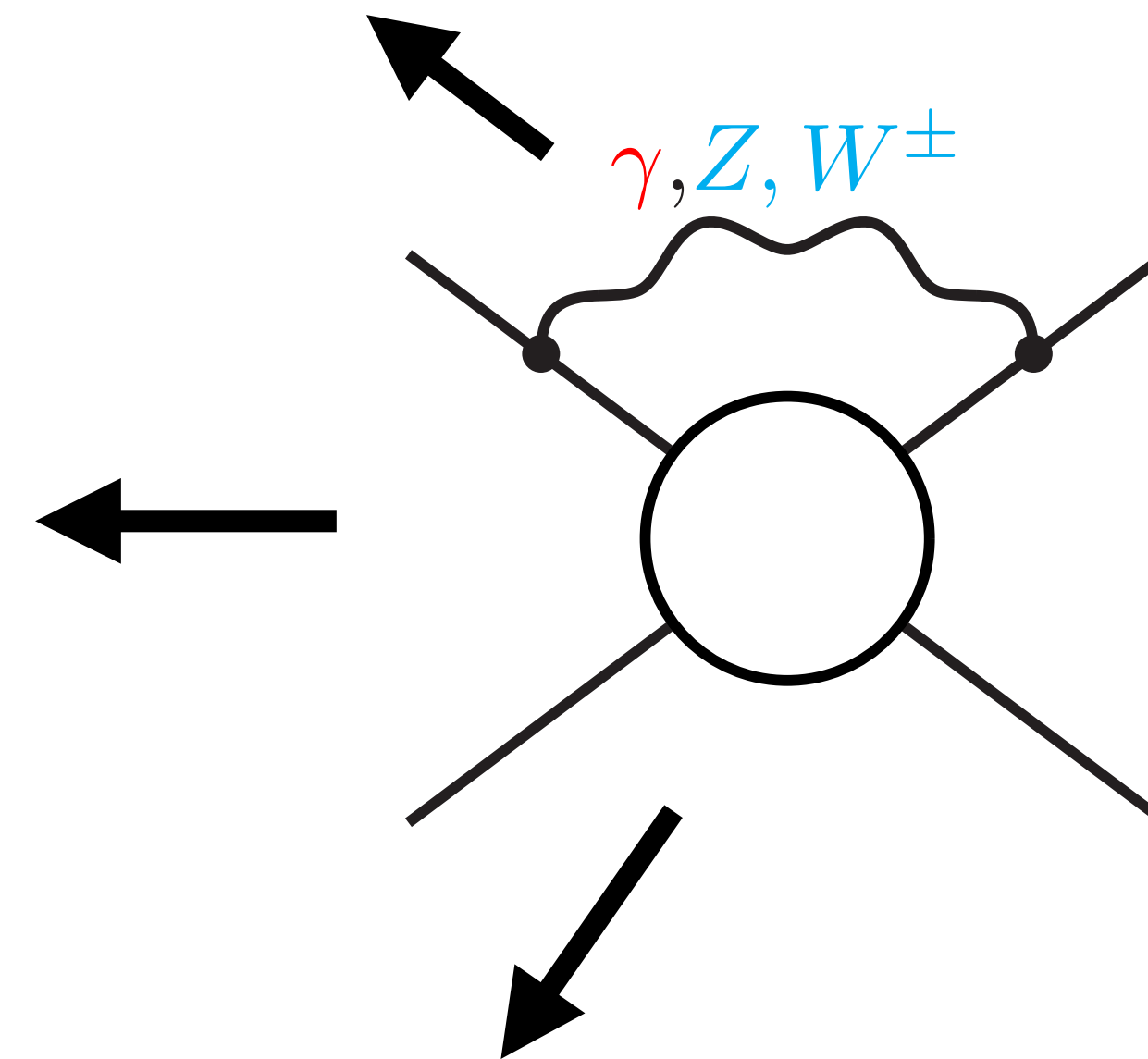
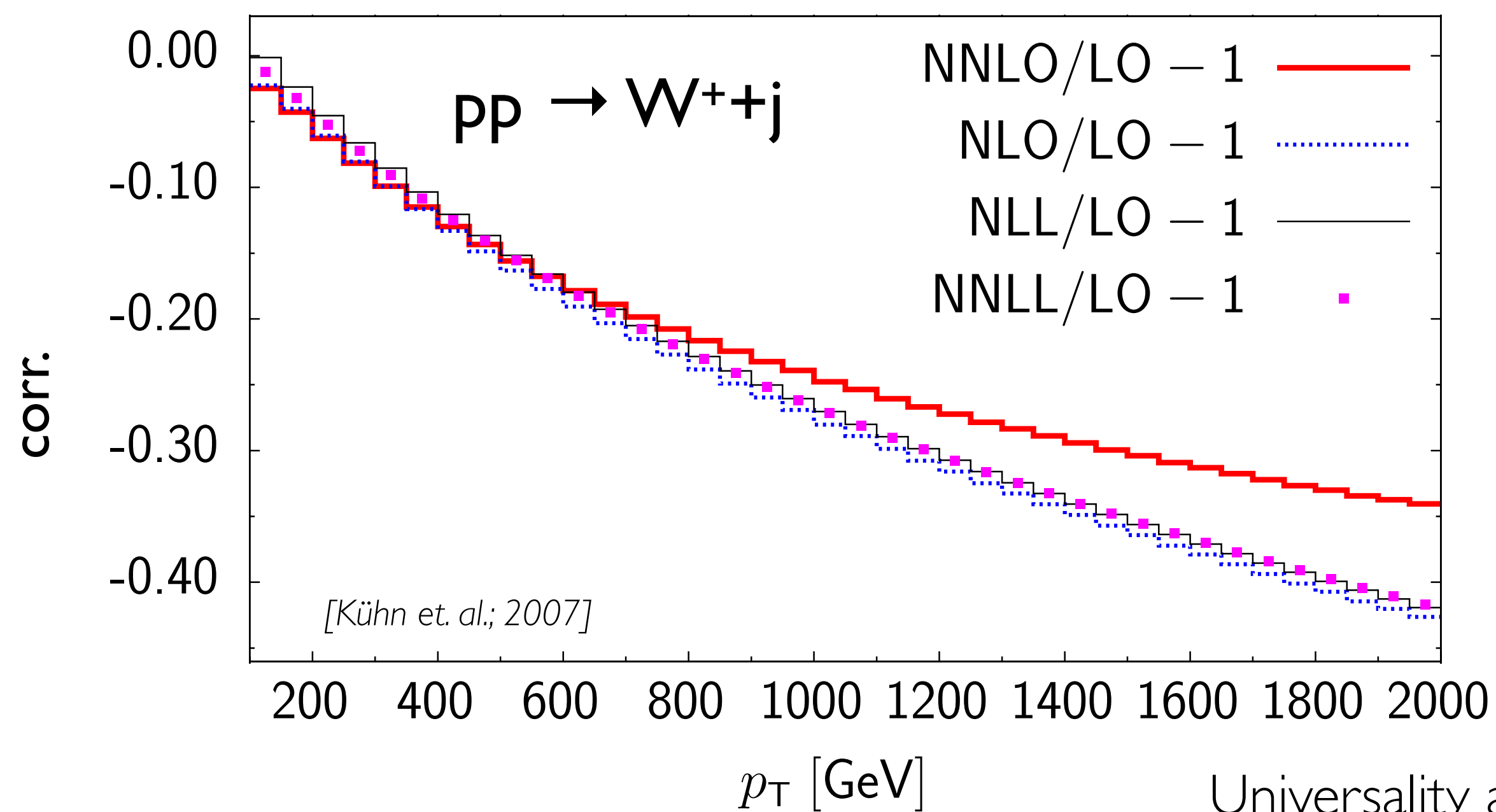
- O(1%) inclusive corrections
- O(10%) negative corrections at large energies due to Sudakov logs



Relevance of EW higher-order corrections

Numerically $\mathcal{O}(\alpha) \sim \mathcal{O}(\alpha_s^2) \Rightarrow$ **NLO EW ~ NNLO QCD**

Possible large (negative) enhancement due to soft/collinear **logs** from virtual EW gauge bosons:



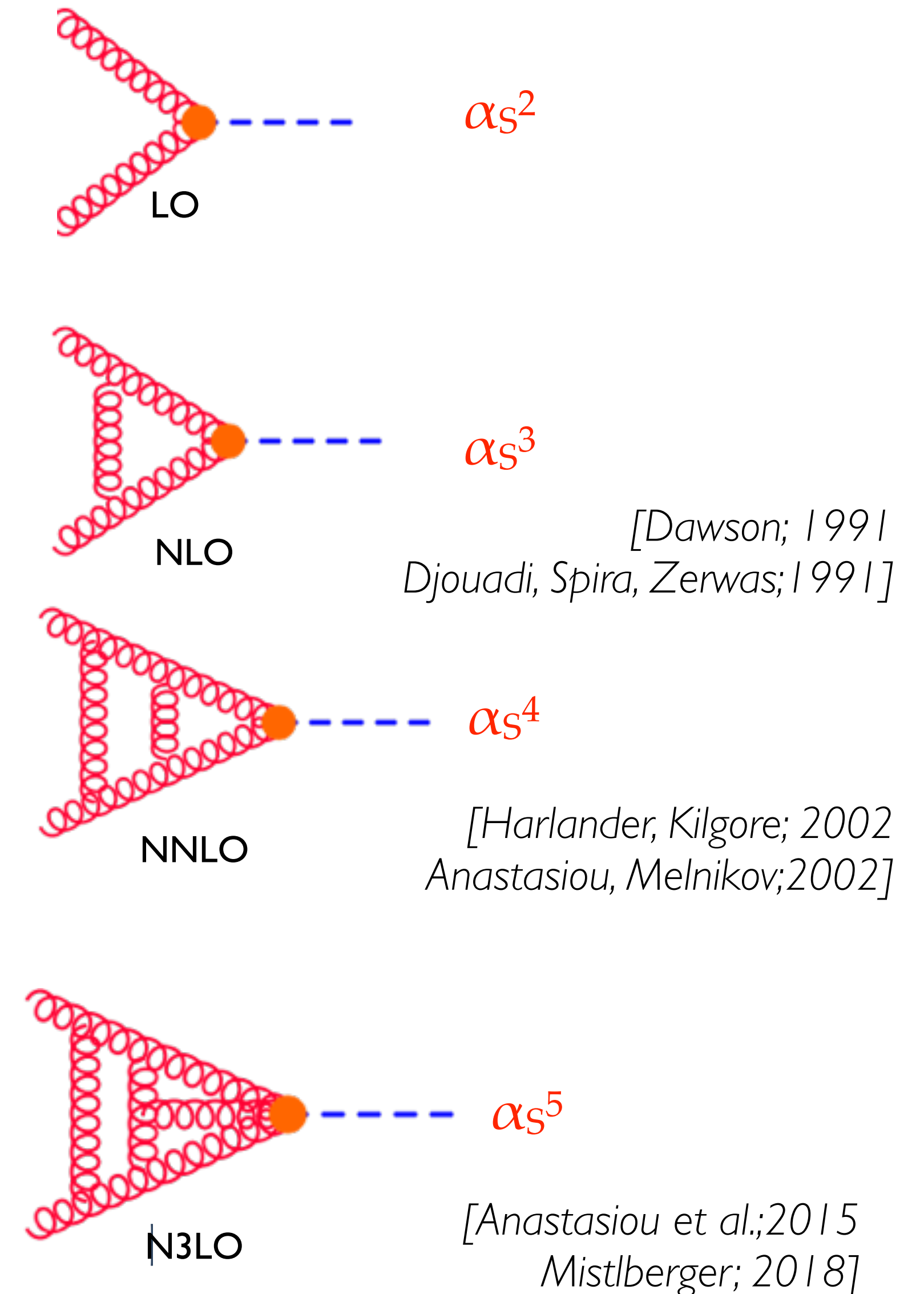
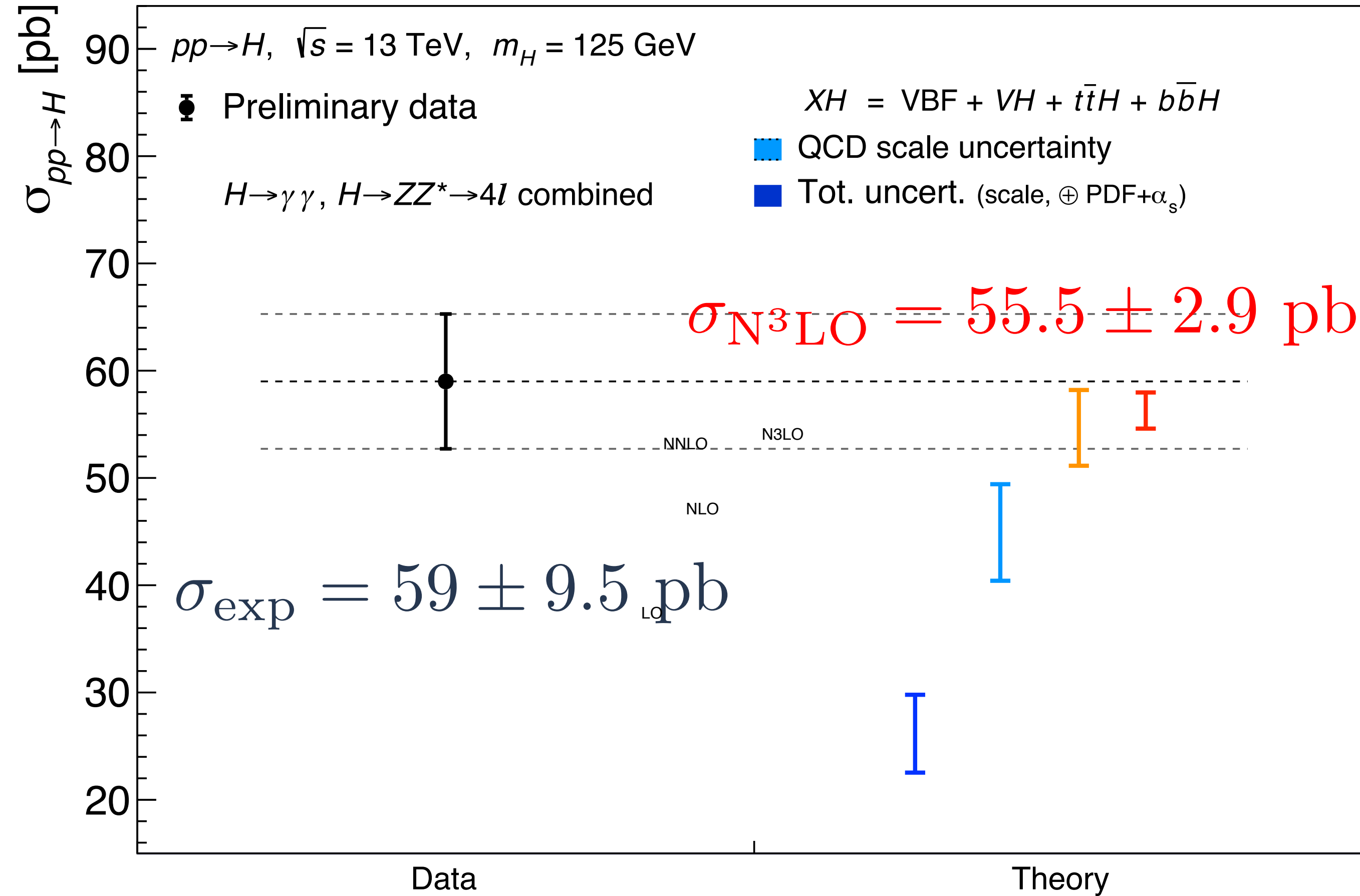
[Ciafaloni, Comelli, '98;
Lipatov, Fadin, Martin, Melles, '99;
Kuehen, Penin, Smirnov, '99;
Denner, Pozzorini, '00]

Universality and factorisation: [Denner, Pozzorini; '01]

$$\delta\mathcal{M}_{\text{LL+NLL}}^{1\text{-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^n \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^\pm} I^a(k) I^{\bar{a}}(l) \ln^2 \frac{\hat{s}_{kl}}{M^2} + \gamma^{\text{ew}}(k) \ln \frac{\hat{s}}{M^2} \right\} \mathcal{M}_0$$

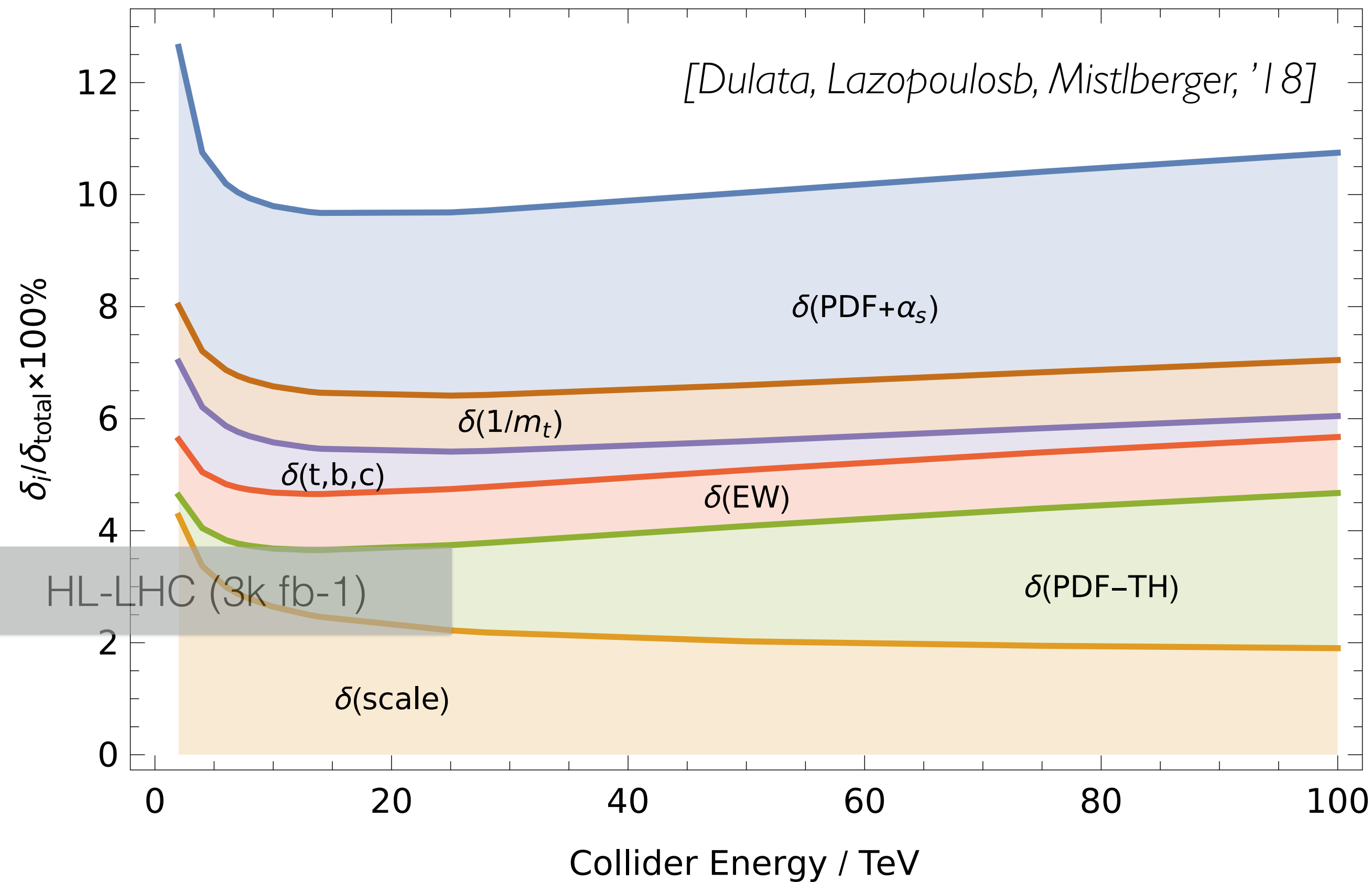
→ overall large effect in the tails of distributions: $p_T, m_{\text{inv}}, H_T, \dots$ (relevant for BSM searches!)

Convergence of the perturbative expansion: inclusive Higgs

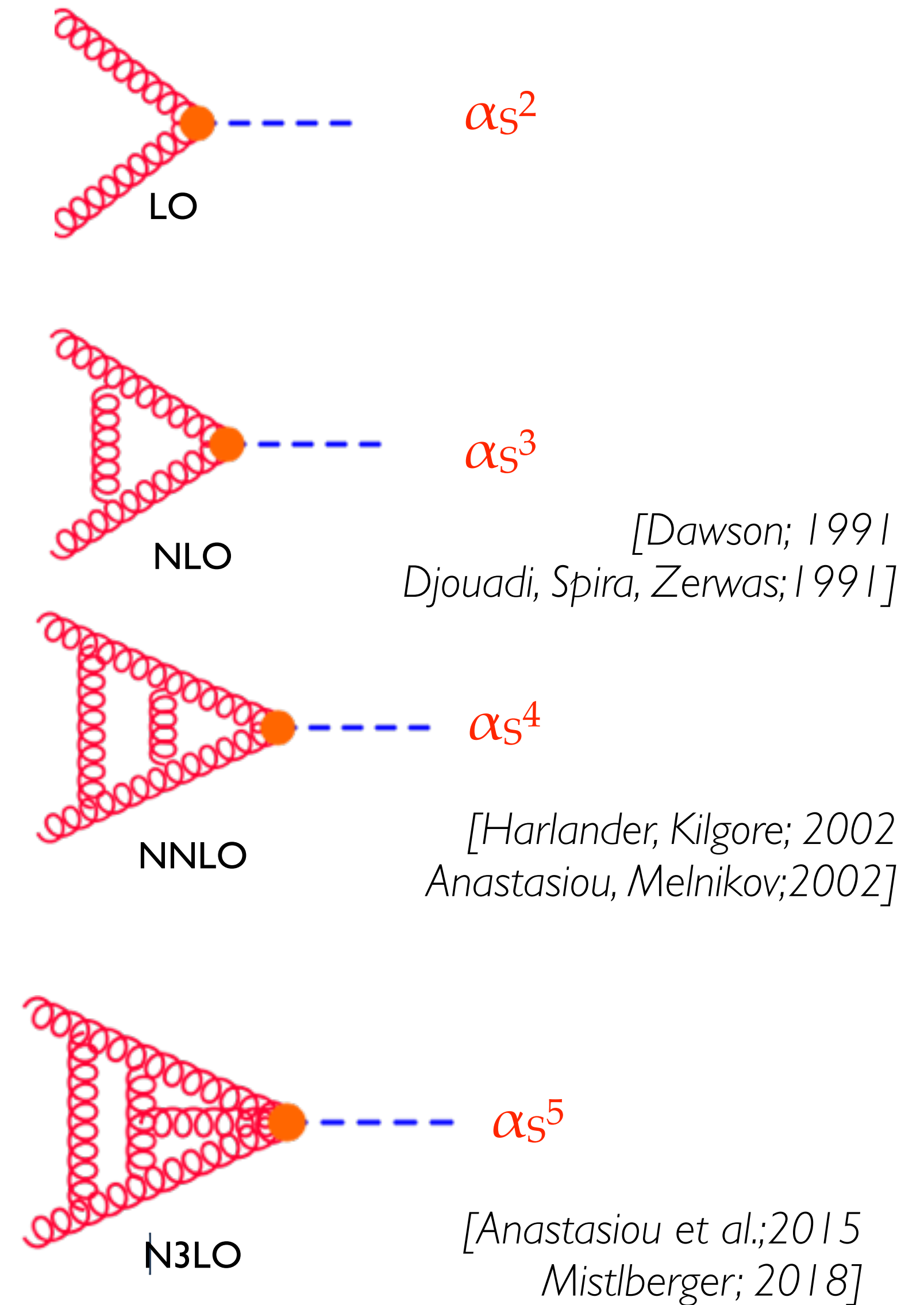


- ➔ Error estimate at LO largely underestimated!
- ➔ N3LO ~ 2 LO
- ➔ Higher-orders are crucial for reliable predictions and precision tests of Higgs properties

Convergence of the perturbative expansion: inclusive Higgs up to N3LO

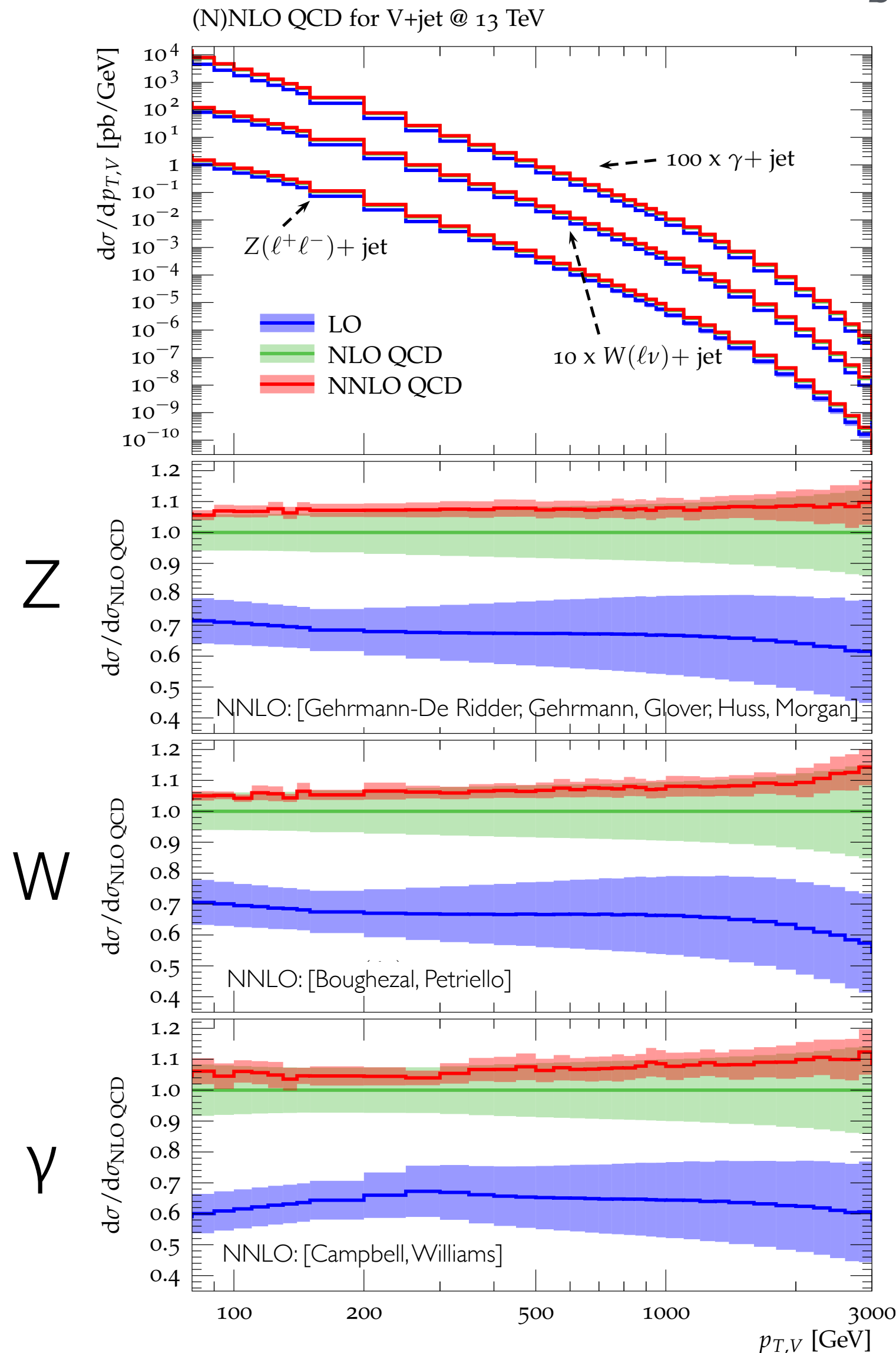


➔ At this level: crucial to investigate any possible uncertainty beyond naive scale variations



Convergence of the perturbative expansion: V+jets @ NNLO

[JML et. al.: 1705.04664]



$$\frac{d}{dx}\sigma_{\text{QCD}}^{(V)} = \frac{d}{dx}\sigma_{\text{LO QCD}}^{(V)} + \frac{d}{dx}\sigma_{\text{NLO QCD}}^{(V)} + \frac{d}{dx}\sigma_{\text{NNLO QCD}}^{(V)}$$

$$\mu_0 = \frac{1}{2} \left(\sqrt{p_{T,\ell+\ell^-}^2 + m_{\ell+\ell^-}^2} + \sum_{i \in \{q,g,\gamma\}} |p_{T,i}| \right)$$

this is a 'good' scale for V+jets

- at large p_{TV} : $HT'/2 \approx p_{TV}$
- modest higher-order corrections
- sufficient convergence

scale uncertainties due to 7-pt variations:

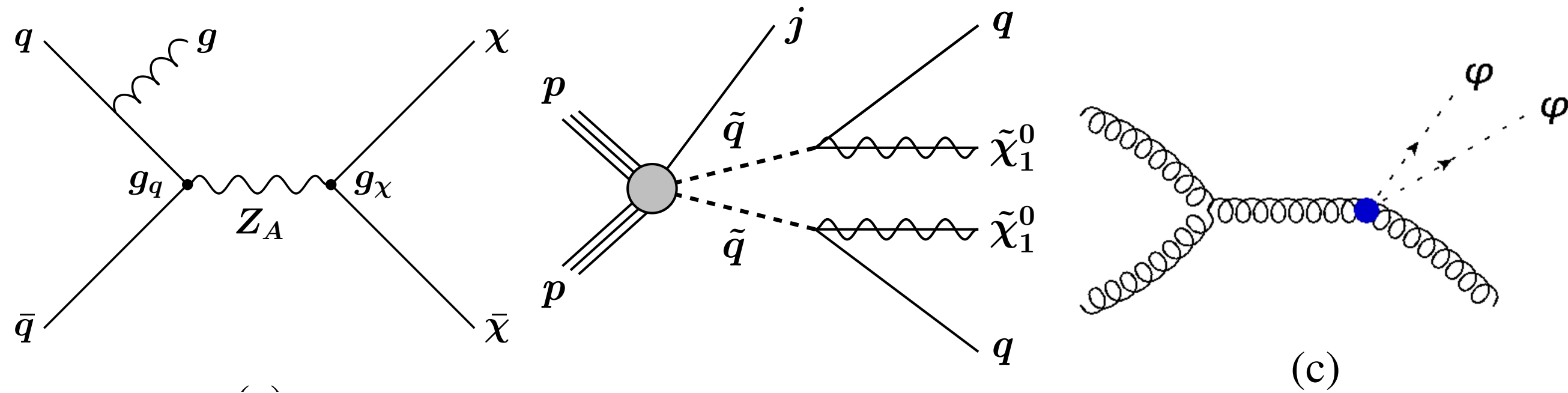
- (20%) uncertainties at LO
- (10%) uncertainties at NLO
- (5%) uncertainties at NNLO

with minor shape variations.

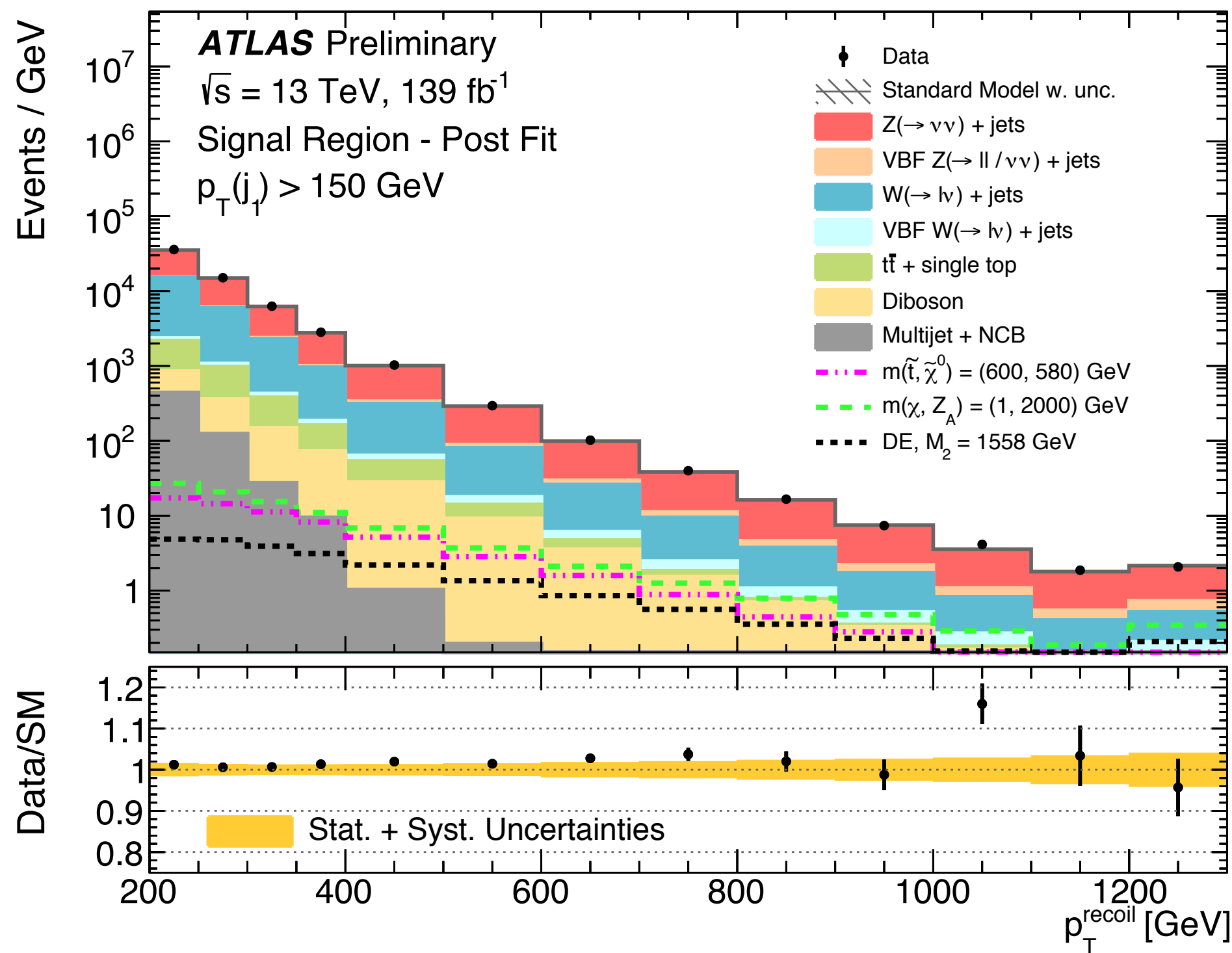
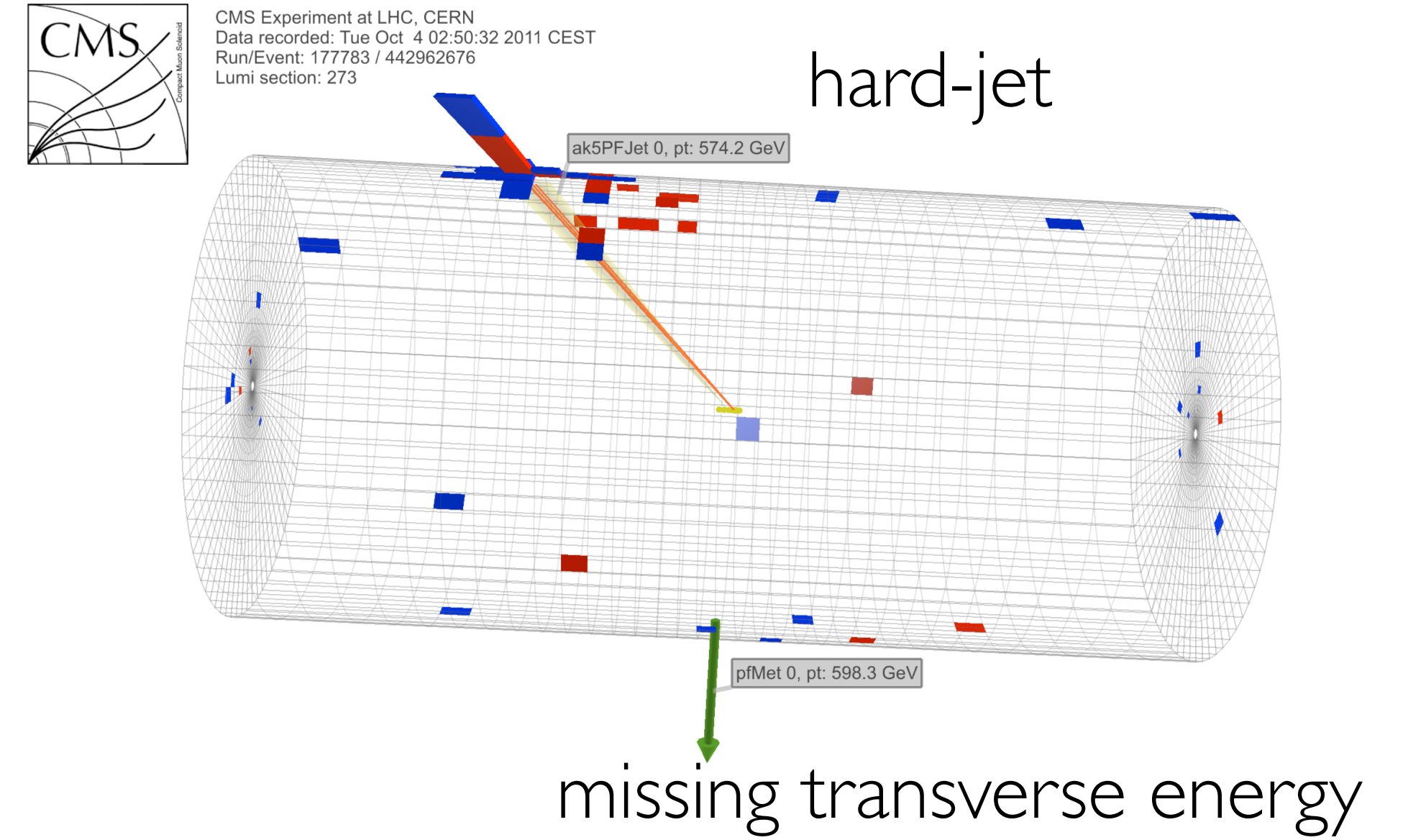
This level of precision for V+jets allows to boost the sensitivity of MET+X searches.

MET+X searches

- Allows to access a broad range of BSM hypotheses



experimental signal:



irreducible SM backgrounds:

$$pp \rightarrow Z(\rightarrow \nu\bar{\nu}) + \text{jets} \Rightarrow \text{MET} + \text{jets}$$

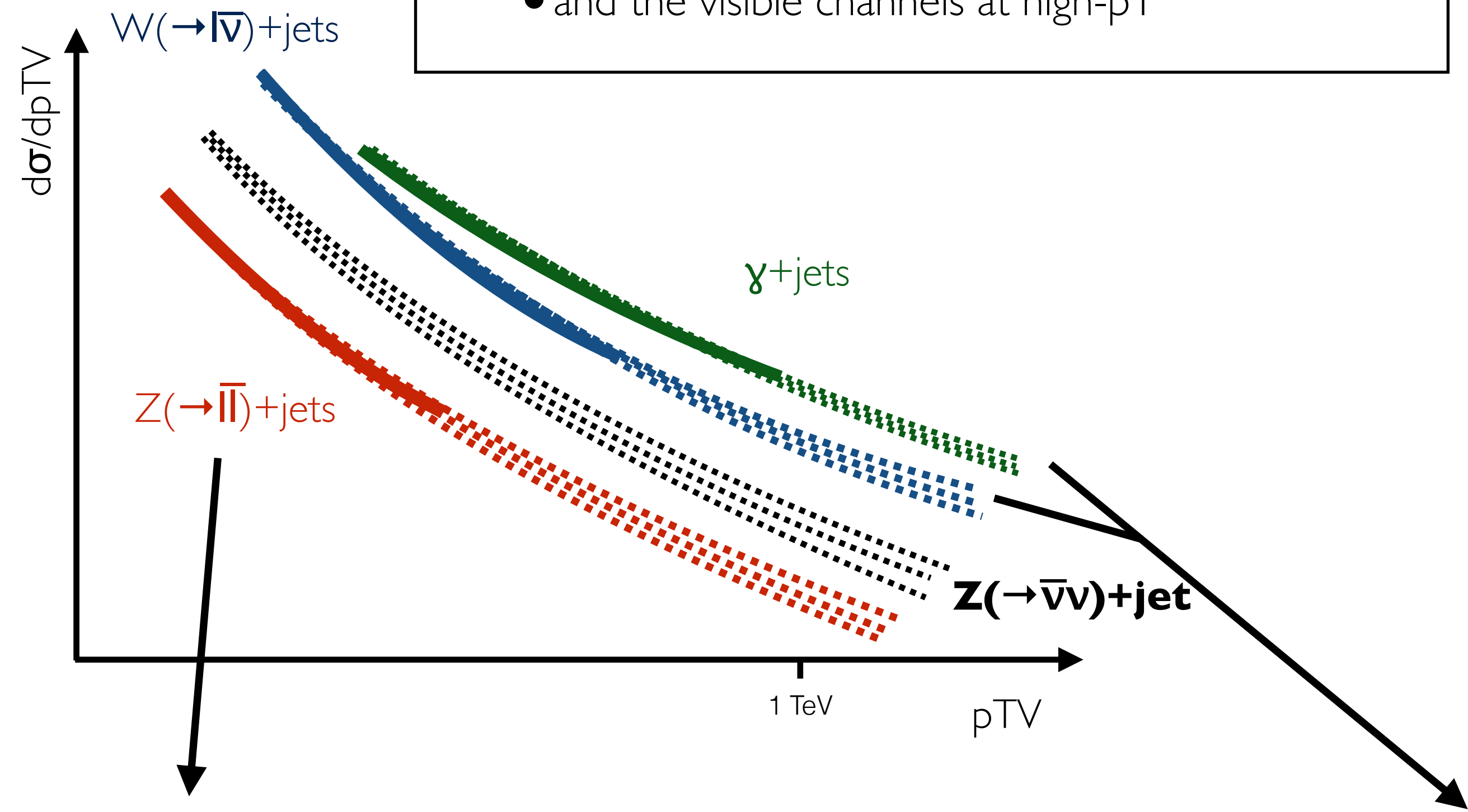
$$pp \rightarrow W(\rightarrow lv) + \text{jets} \Rightarrow \text{MET} + \text{jets} \text{ (lepton lost)}$$

} V + jets

Determine V+jets DM backgrounds

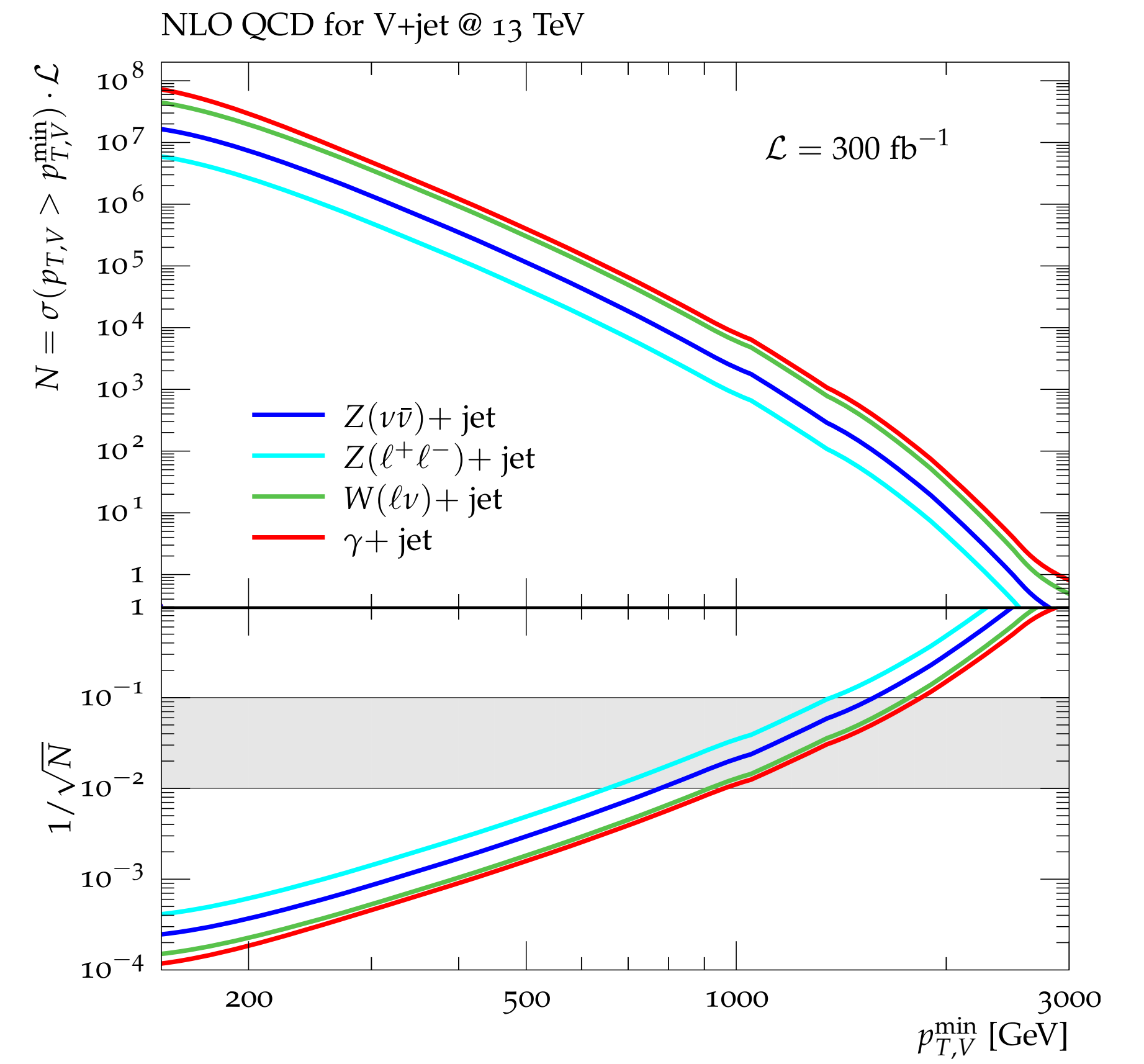
global fit of $Z(\rightarrow \bar{l}l)+jets$, $W(\rightarrow \bar{l}V)+jets$ and $\gamma+jets$ measurements

- to determine $Z(\rightarrow \bar{\nu}\nu)+jet$
- and the visible channels at high- p_T



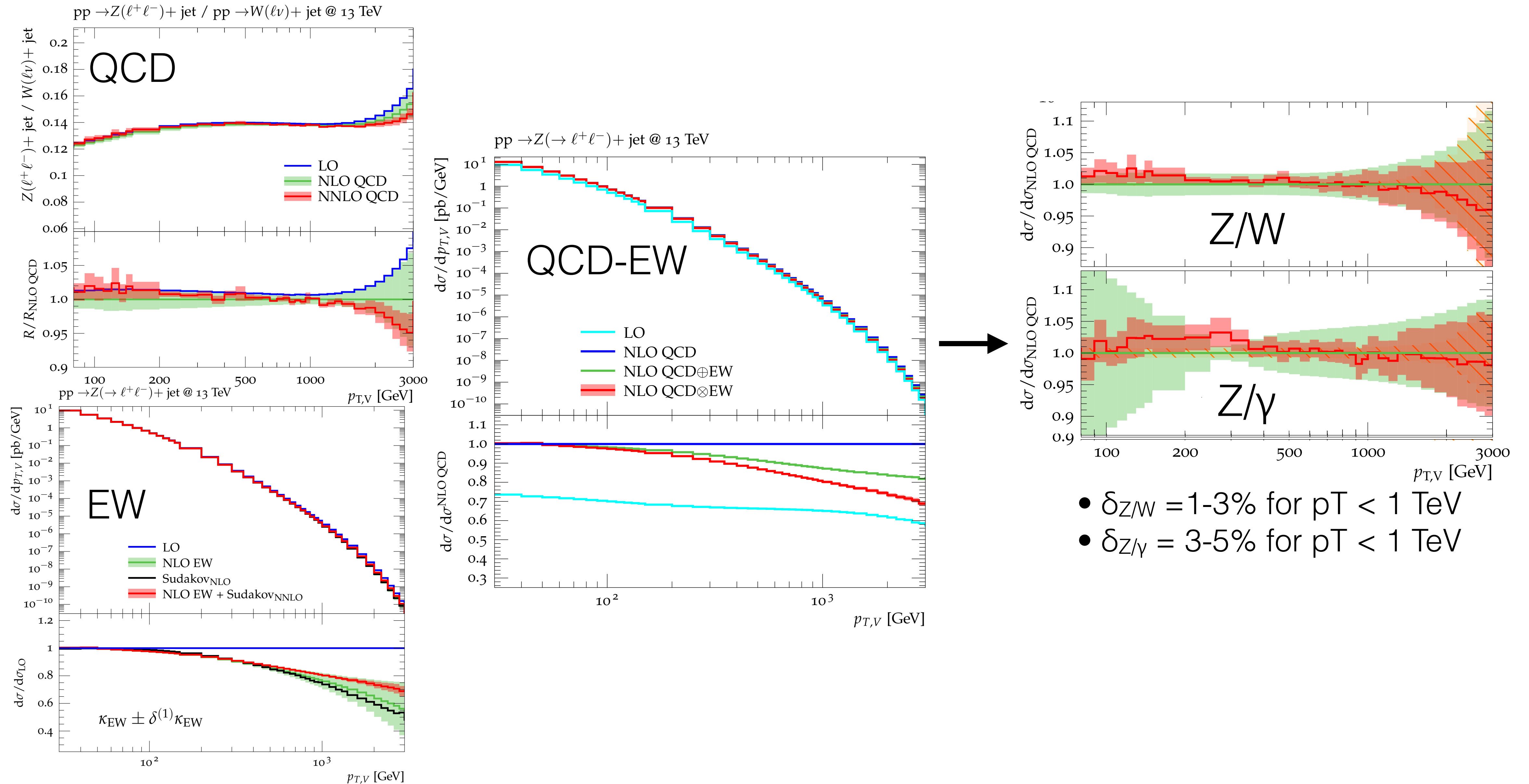
- hardly any systematics (just QED dressing)
- very precise at low p_T
- but: limited statistics at large p_T

- fairly large data samples at large p_T
- systematics from transfer factors

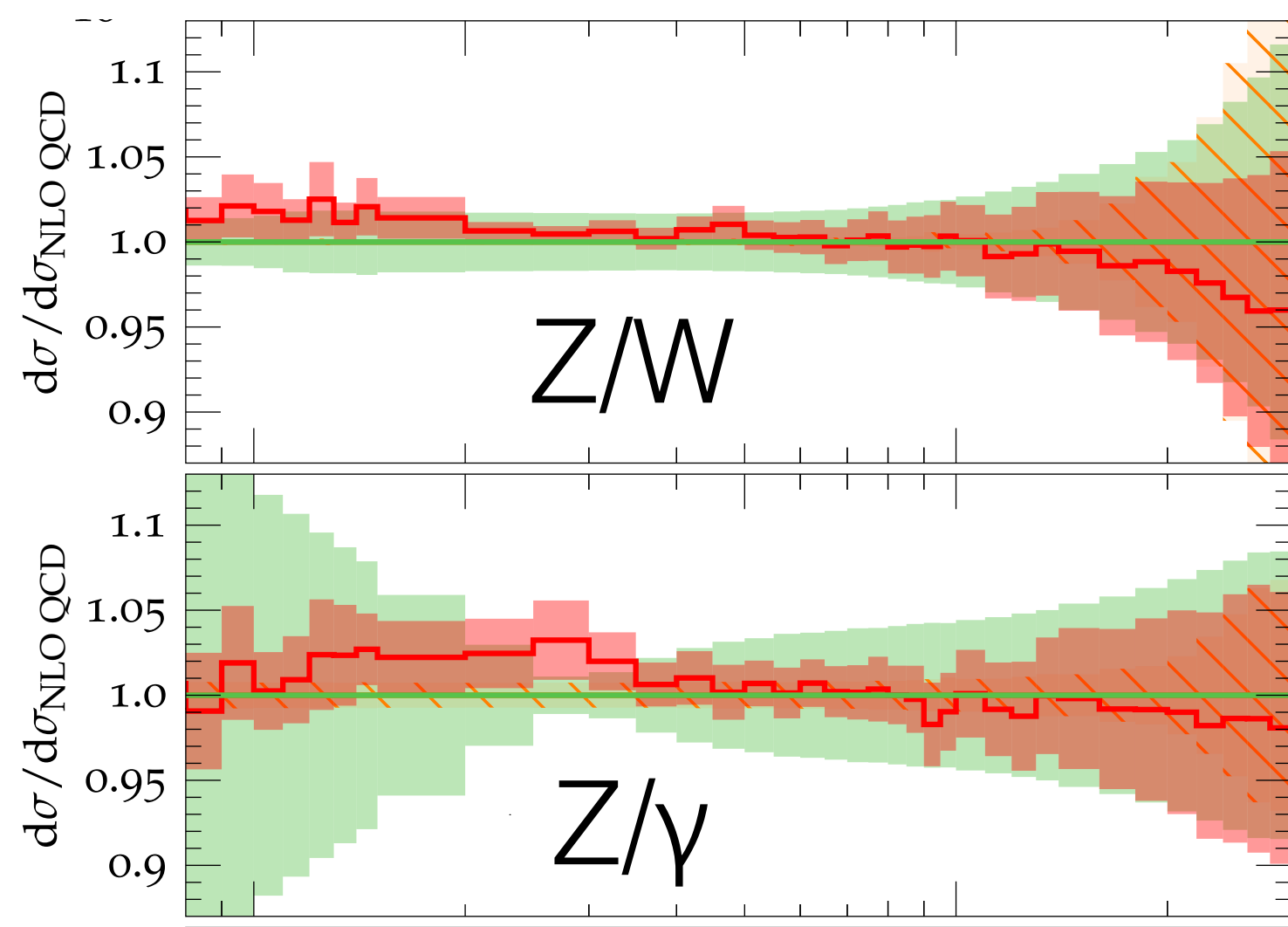


- for $500 \text{ GeV} < p_{TV} < 1000 \text{ GeV}$: background statistics will be at **1% level**
- this level of precision is theoretically possible @ **NNLO QCD + NNLO EW**

Improving MET+X searches with precision



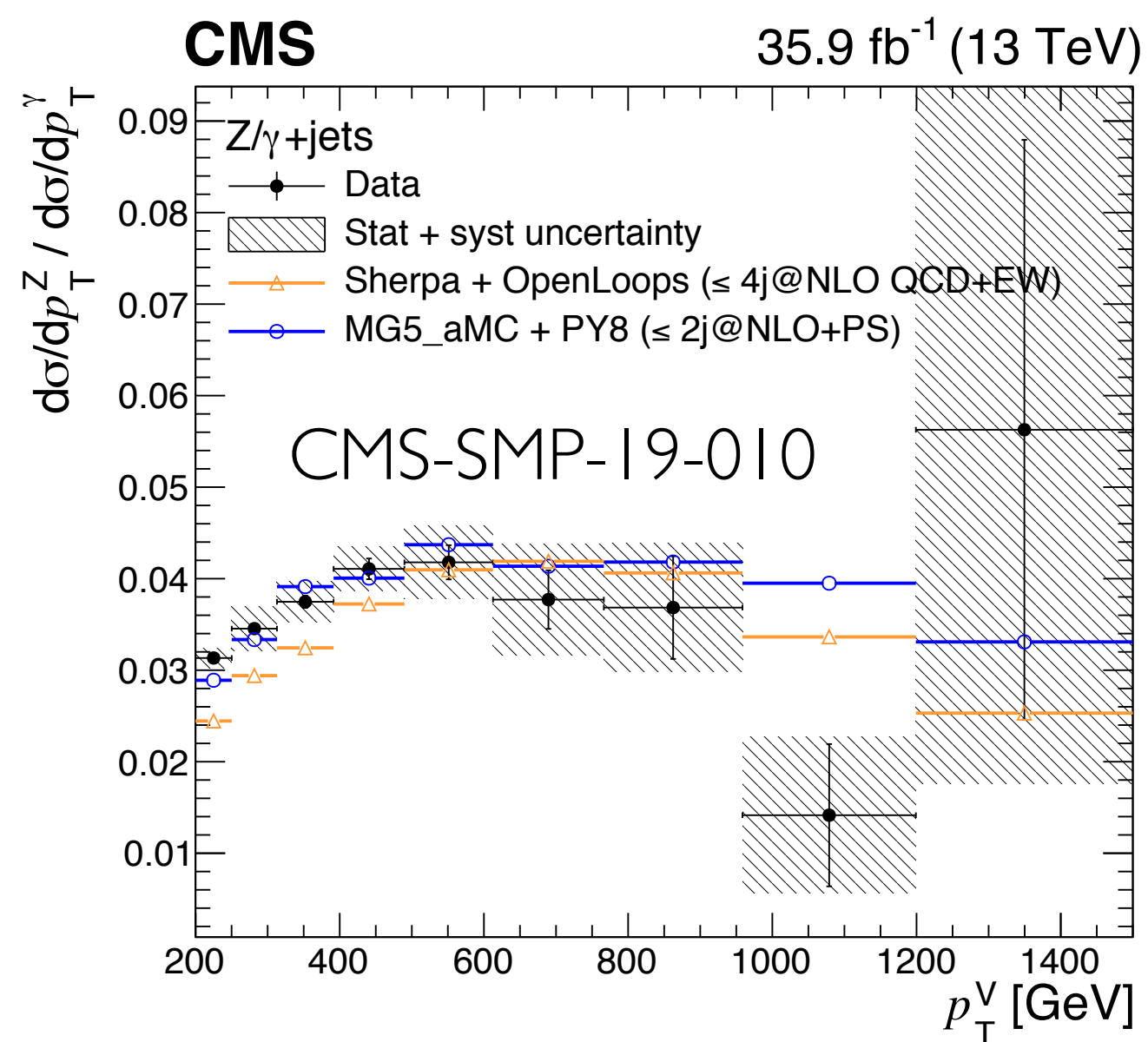
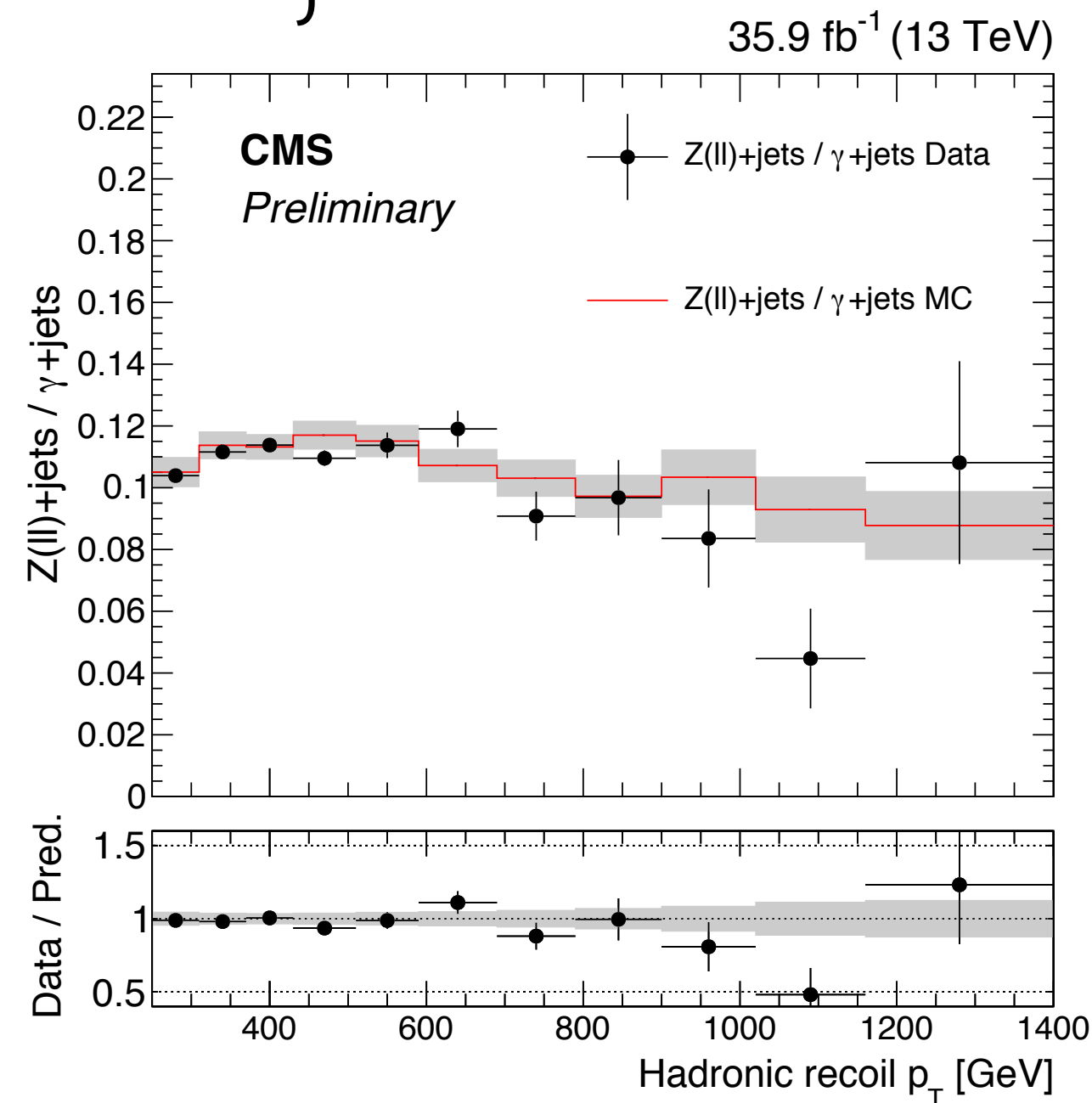
Combined uncertainties on V+jets ratios



- $\delta_{Z/W} = 1-3\%$ for $p_T < 1$ TeV
- $\delta_{Z/\gamma} = 3-5\%$ for $p_T < 1$ TeV

CR

dedicated
SM measurements



The Zoo of MET+X searches

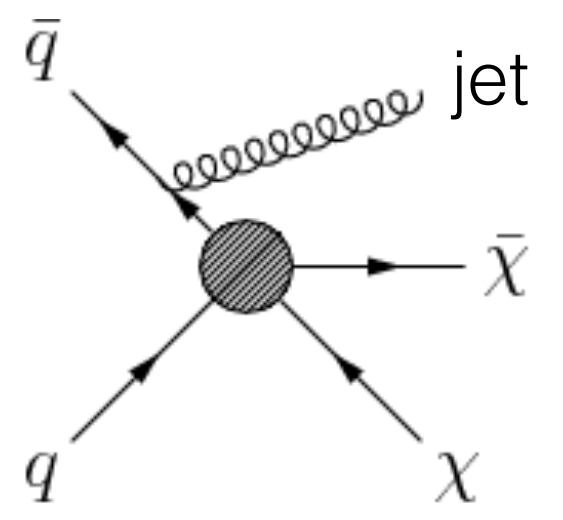
ISR

Higgs-Strahlung

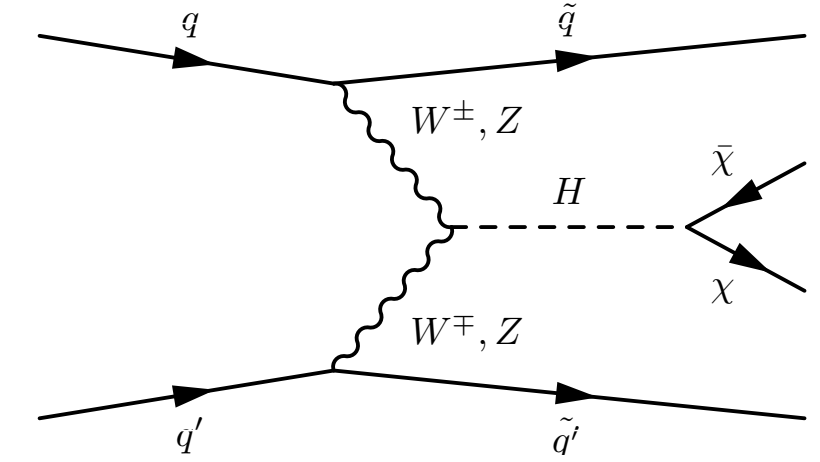
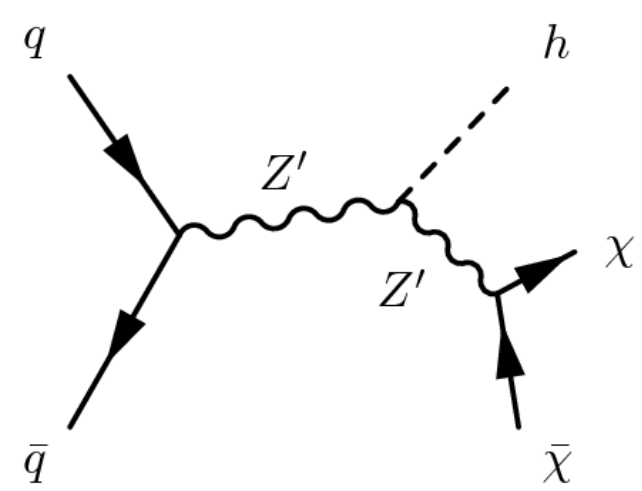
VBF

HF-associated

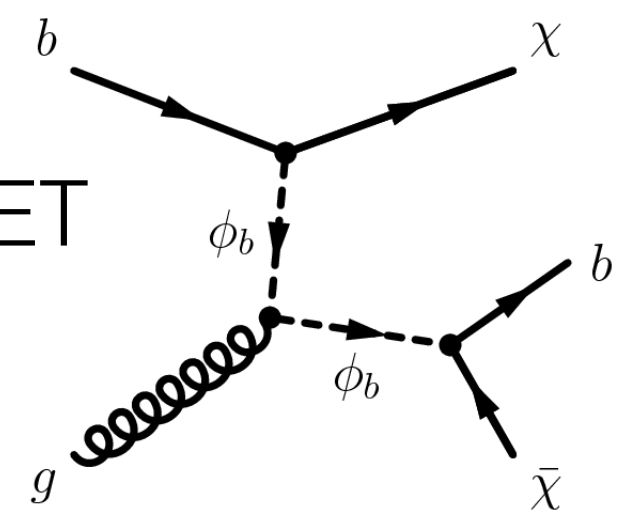
Mono-jet



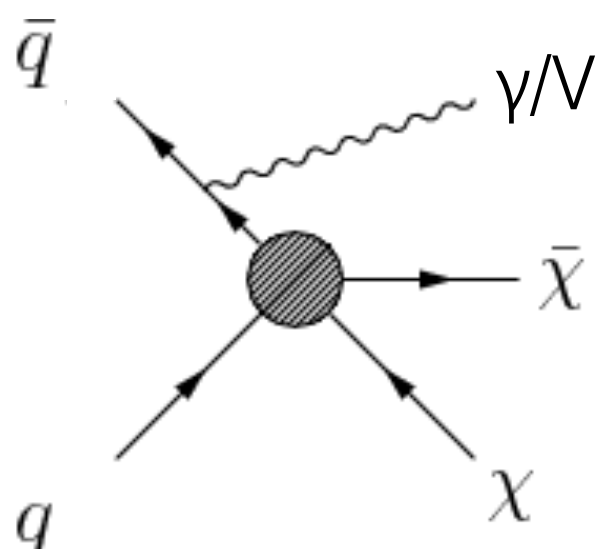
Mono-H



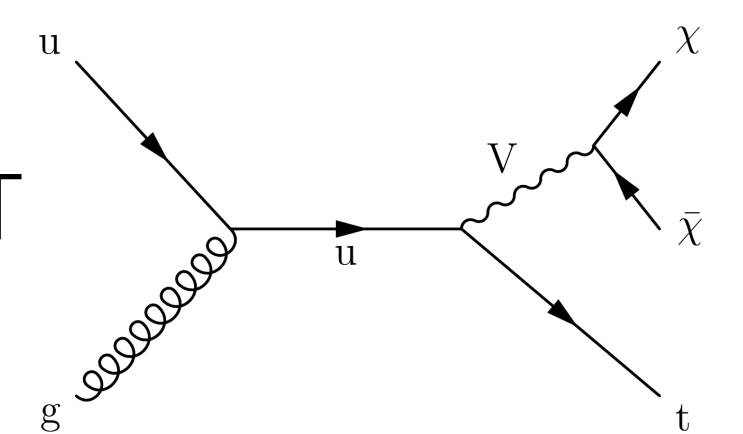
b+MET



Mono- γ/V

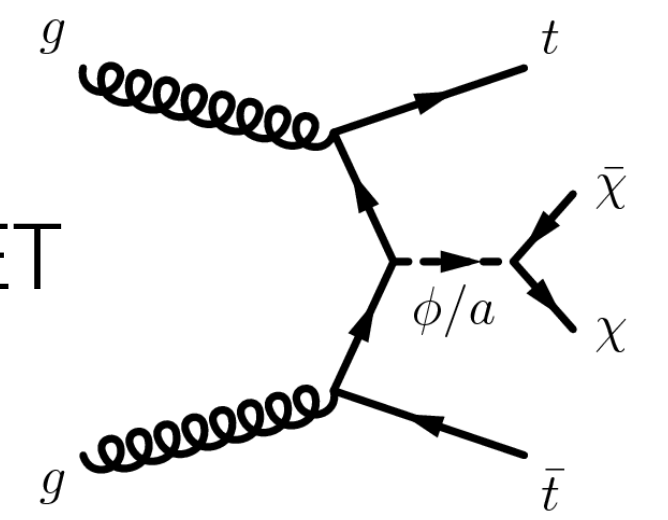


t+MET

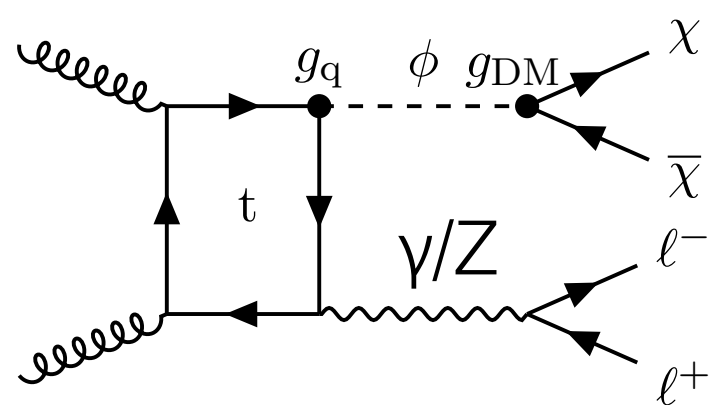


and many more....

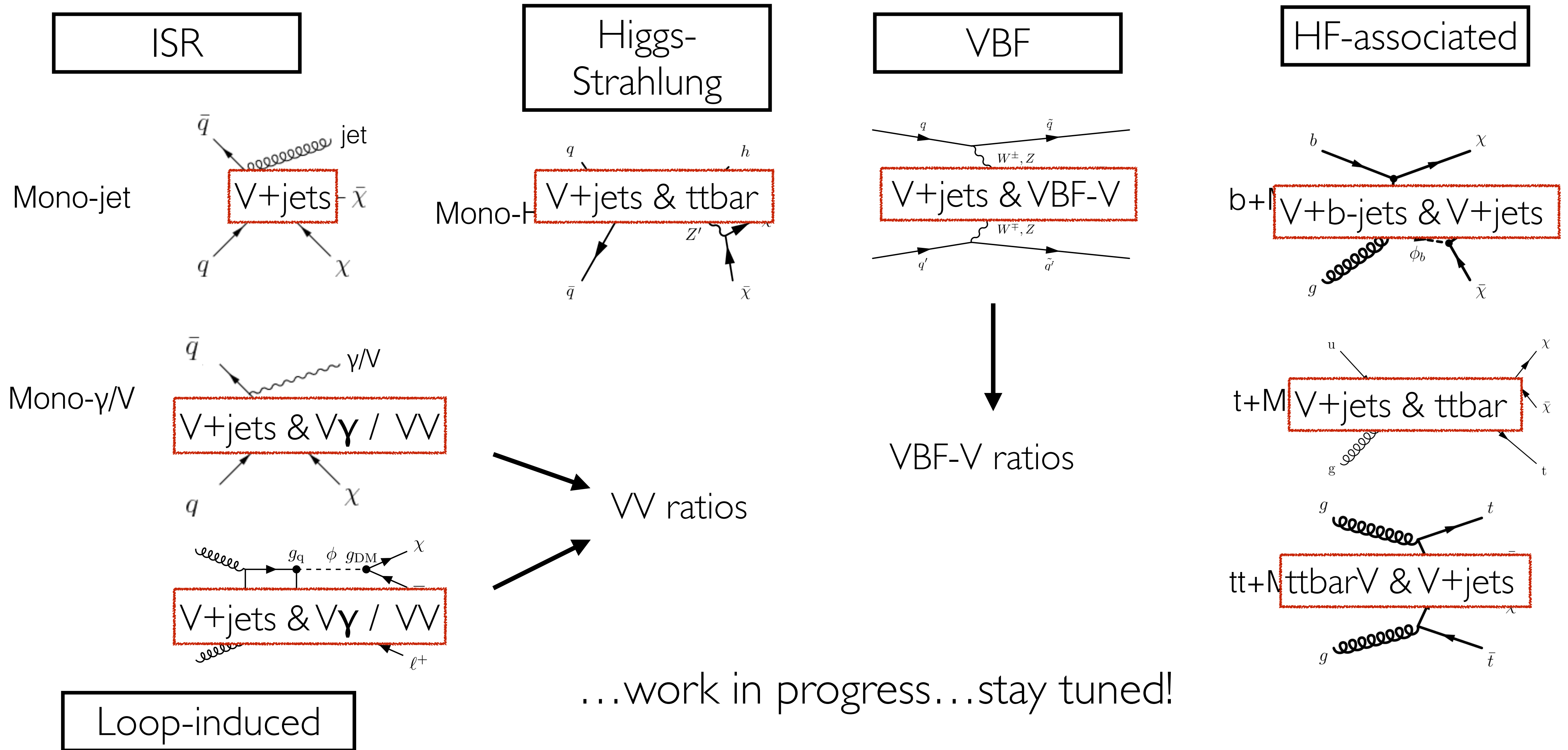
tt+MET



Loop-induced

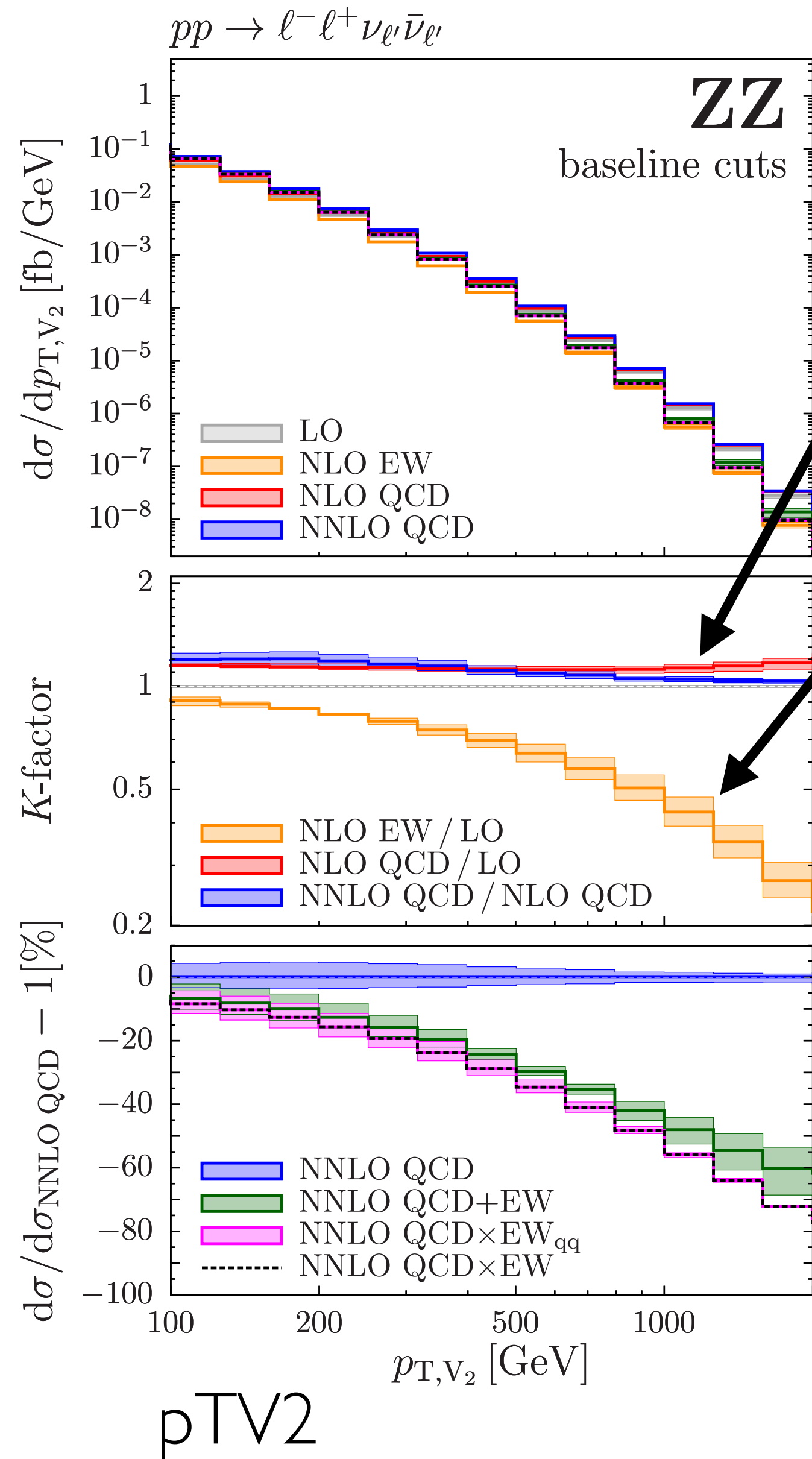


The Zoo of MET+X searches: backgrounds



NNLO QCD + NLO EW for VV: pTV2

[M. Grazzini, S. Kallweit, JML, S. Pozzorini, M. Wiesemann; 1912.00068]



- moderate QCD corrections

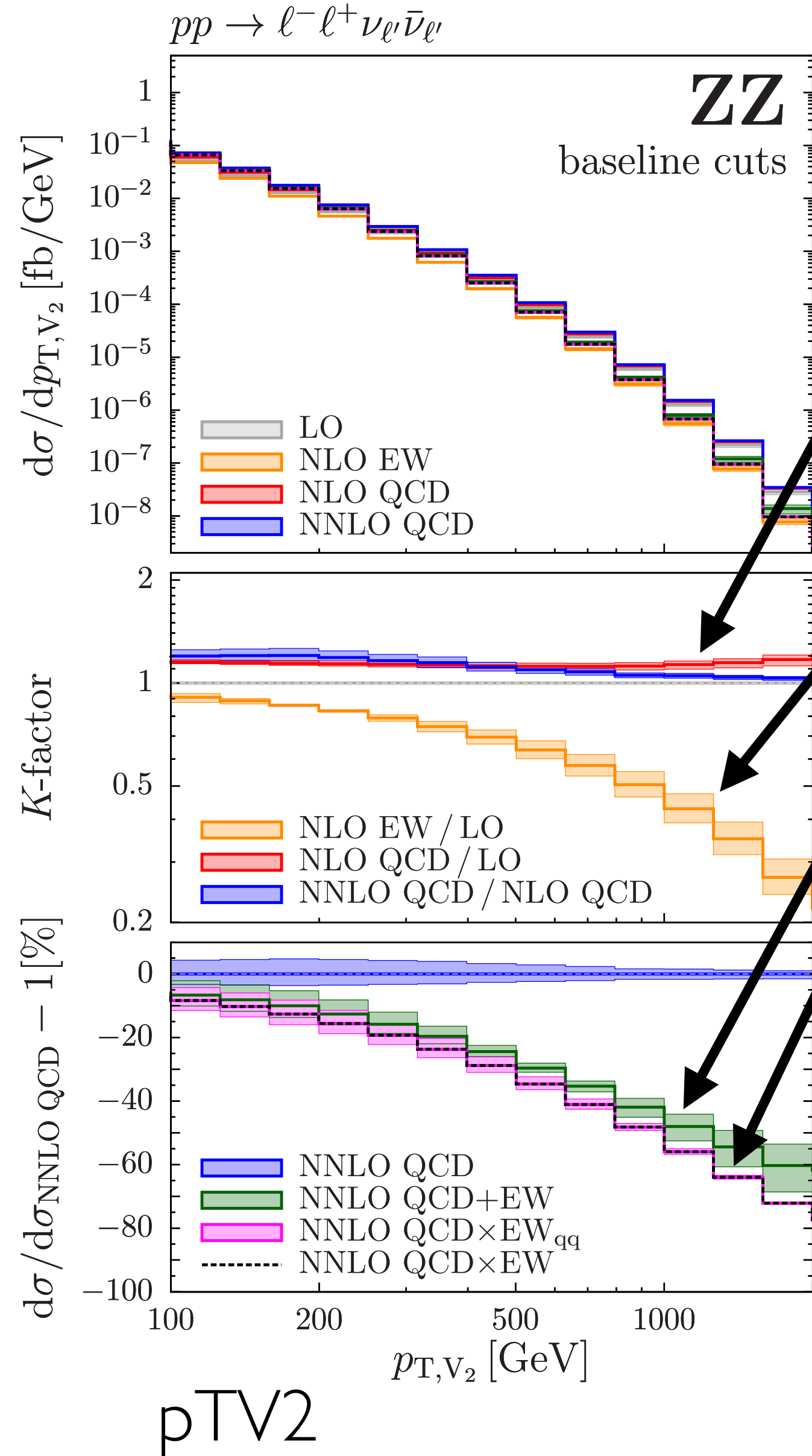
- ▶ NNLO/NLO QCD very small at large pTV2

- ▶ NNLO QCD uncertainty: few percent

- NLO EW/LO = -(50-60)% @ 1 TeV

NNLO QCD + NLO EW for VV: pTV2

[M. Grazzini, S. Kallweit, JML, S. Pozzorini, M. Wiesemann; 1912.00068]



- moderate QCD corrections

- ▶ NNLO/NLO QCD very small at large pTV2

- ▶ NNLO QCD uncertainty: few percent

- NLO EW/LO = -(50-60)% @ 1 TeV

$$d\sigma_{\text{NNLO QCD+EW}} = d\sigma_{\text{LO}} (1 + \delta_{\text{QCD}} + \delta_{\text{EW}}) + d\sigma_{\text{LO}}^{gg}$$

$$d\sigma_{\text{NNLO QCD}\times\text{EW}} = d\sigma_{\text{LO}} (1 + \delta_{\text{QCD}}) (1 + \delta_{\text{EW}}) + d\sigma_{\text{LO}}^{gg}$$

$$= d\sigma_{\text{NNLO QCD+EW}} + d\sigma_{\text{LO}} \delta_{\text{QCD}} \delta_{\text{EW}}$$

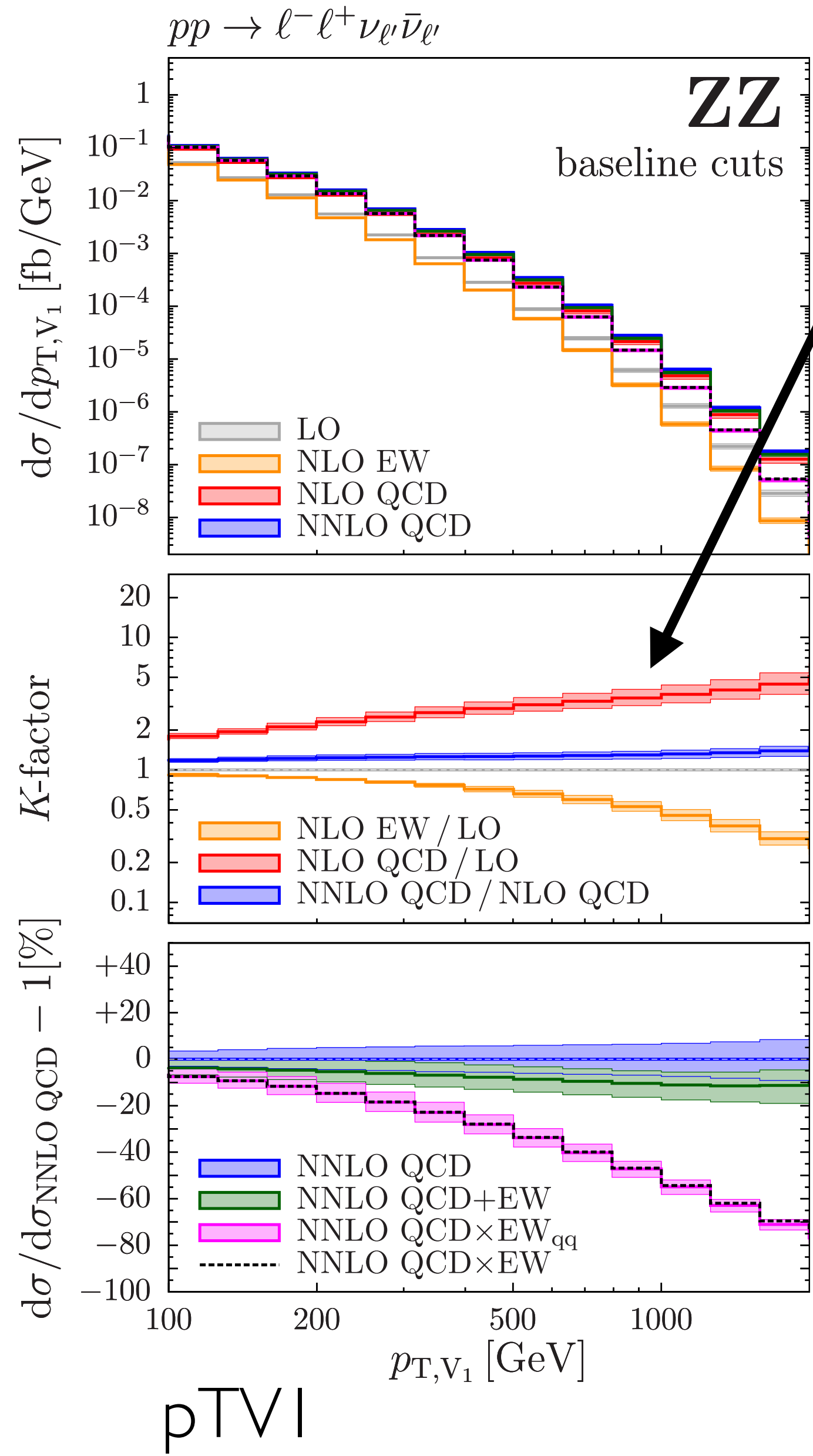
- difference very conservative upper bound on $\mathcal{O}(\alpha_s \alpha)$

- multiplicative/factorised combination clearly superior (EW Sudakov logs x soft QCD)

- dominant uncertainty at large pTV2: $\mathcal{O}(\alpha^2) \sim \alpha_w^2 \log^4(Q^2/M_W^2)$

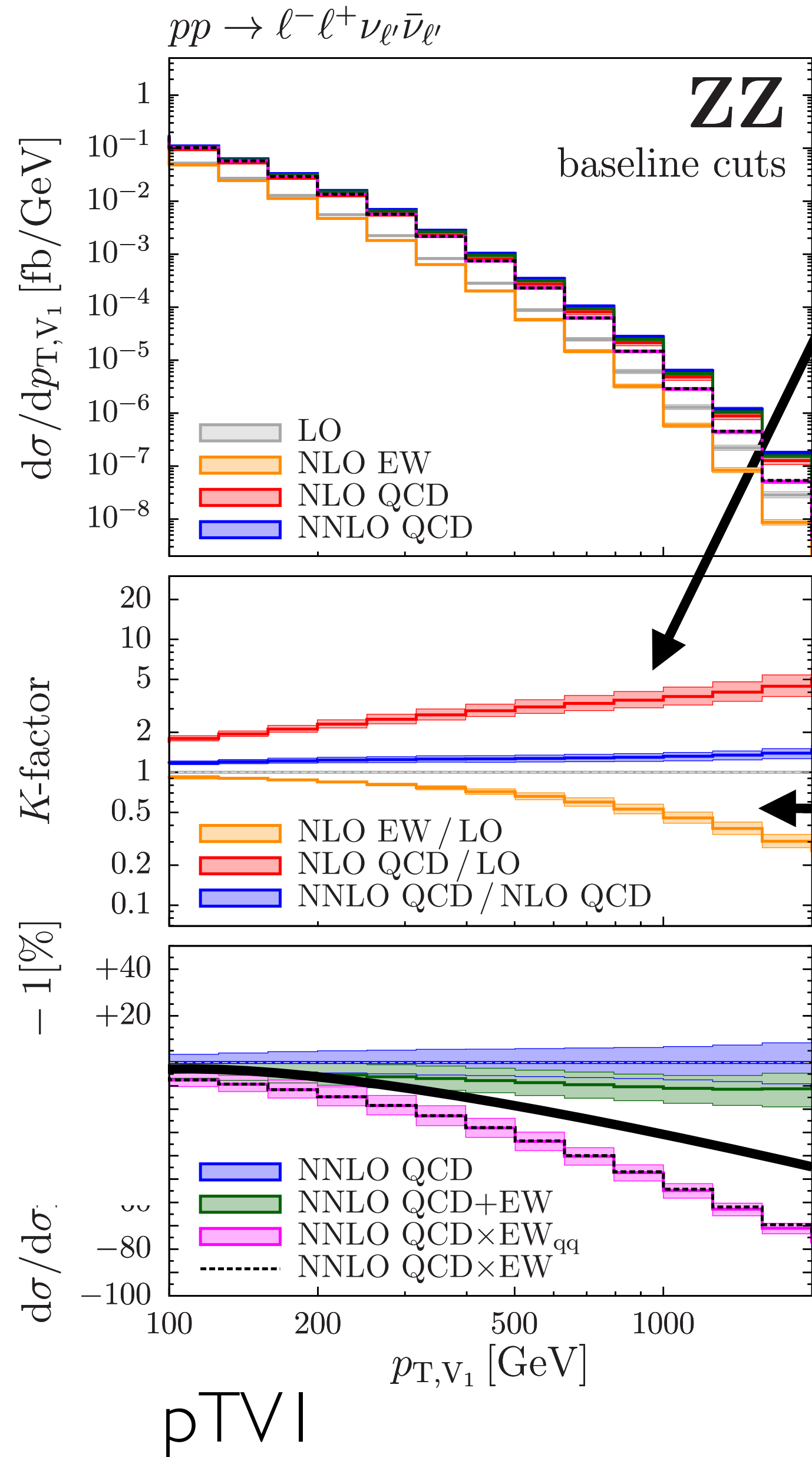
Estimate: $\frac{1}{2} \delta_{\text{EW}}^2$

Giant QCD K-factors and EW corrections: pTVI

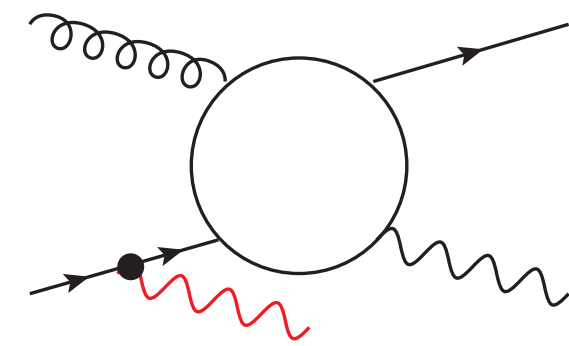


- NLO QCD/LO=2-5! (“giant K-factor” [Rubin, Salam, Sapeta, ‘10])

Giant QCD K-factors and EW corrections: pTVI



- NLO QCD/LO=2-5! (“giant K-factor” [Rubin, Salam, Sapeta, '10])
- at large pTVI: VV phase-space is dominated by V+jet (w/ soft V radiation)



$$\frac{d\sigma^{V(V)j}}{d\sigma_{VV}^{\text{LO}}} \propto \alpha_S \log^2 \left(\frac{Q^2}{M_W^2} \right) \simeq 3 \quad \text{at } Q = 1 \text{ TeV}$$

- NNLO / NLO QCD moderate and NNLO uncert. 5-10%
- NLO EW/LO=-(40-50)%
- Very large difference $d\sigma_{\text{NNLO QCD}+EW}$ vs. $d\sigma_{\text{NNLO QCD} \times EW}$

• Problems:

1. In additive combination dominant Vj topology does not receive any EW corrections
2. In multiplicative combination EW correction for VV is applied to Vj hard process

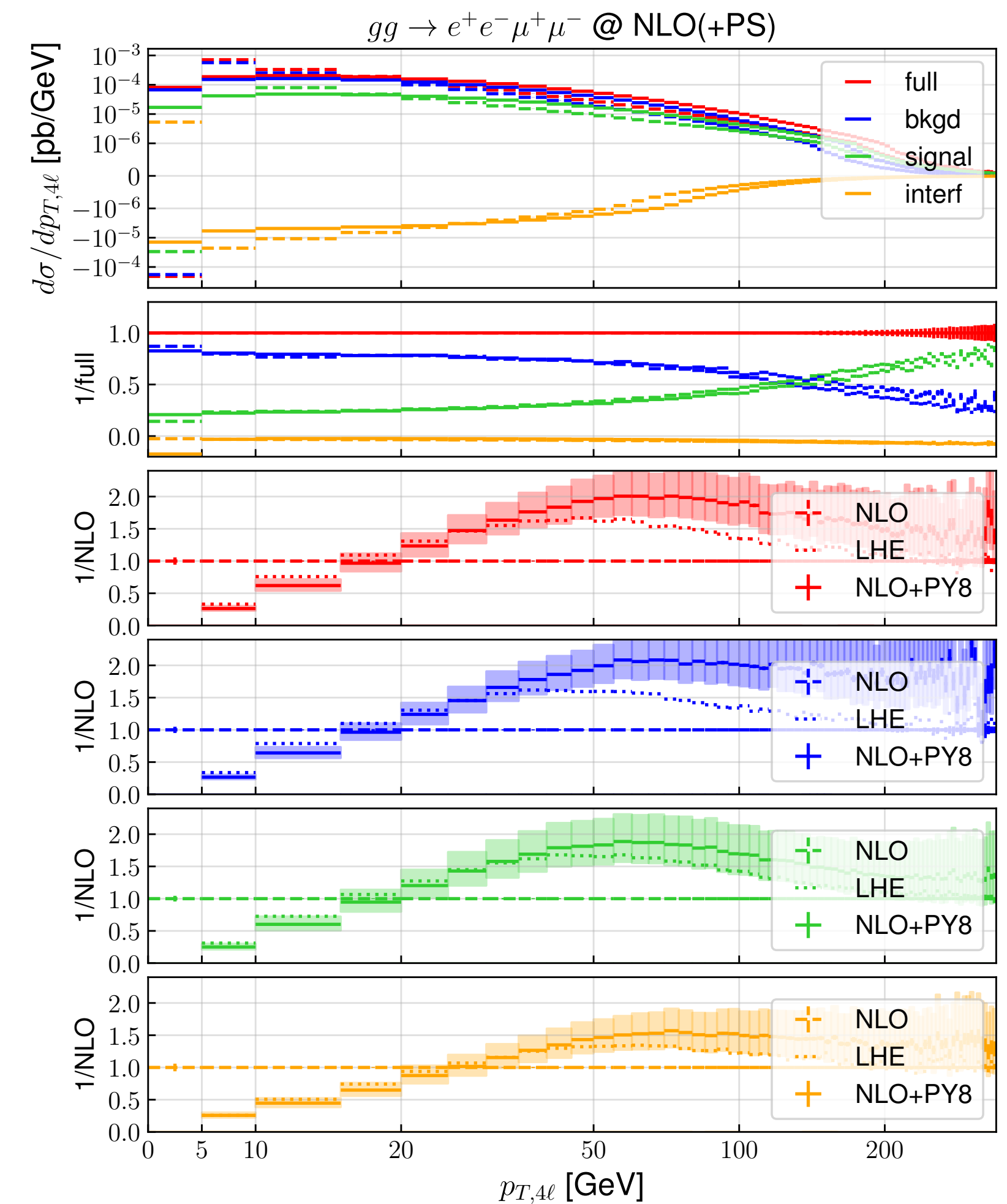
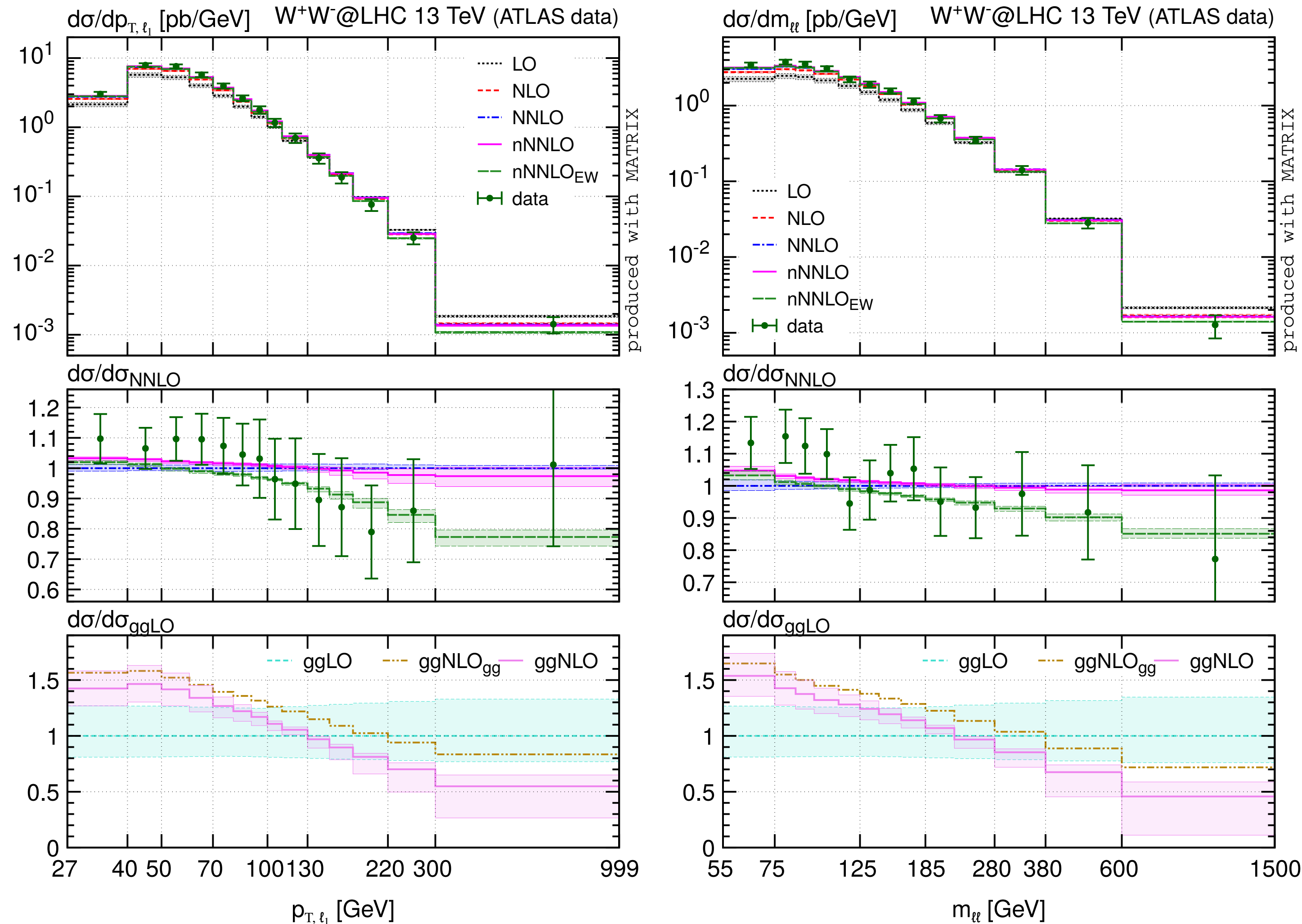
- Pragmatic solution: take average as nominal and spread as uncertainty
- Rigorous solution: merge VVj incl. EW corrections with VV retaining NNLO QCD + EW

First steps in this direction: NLO QCD + EW_{virt} in Sherpa's MEPS@NLO

NNLO QCD + NLO QCD_{gg} + NLO EW vs. data

[M. Grazzini, S. Kallweit, J.Y. Yook, M. Wiesemann; 2002.01877]

[Alioli, Ferrario Ravasio, JML, Röntschi, '21]

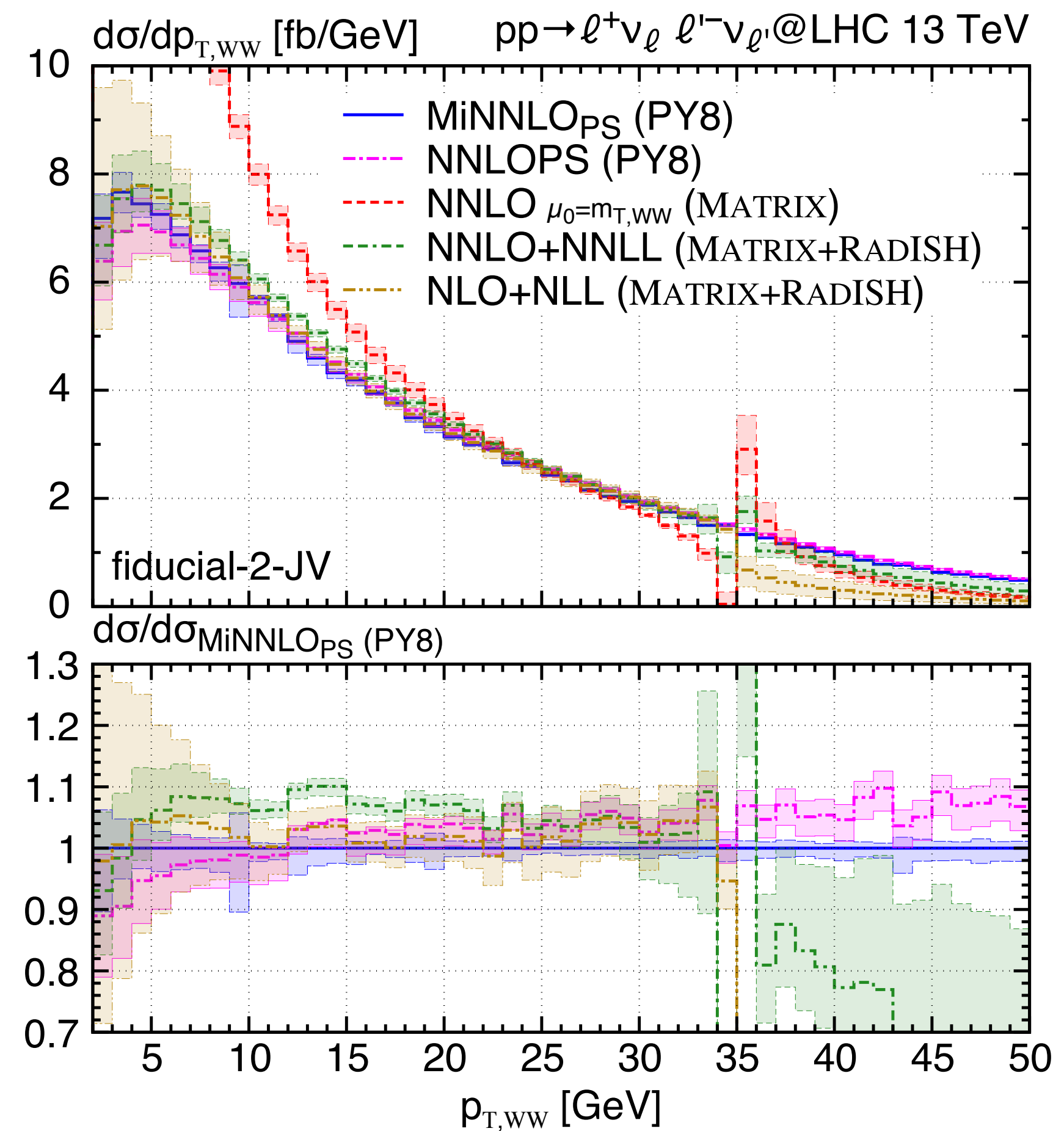
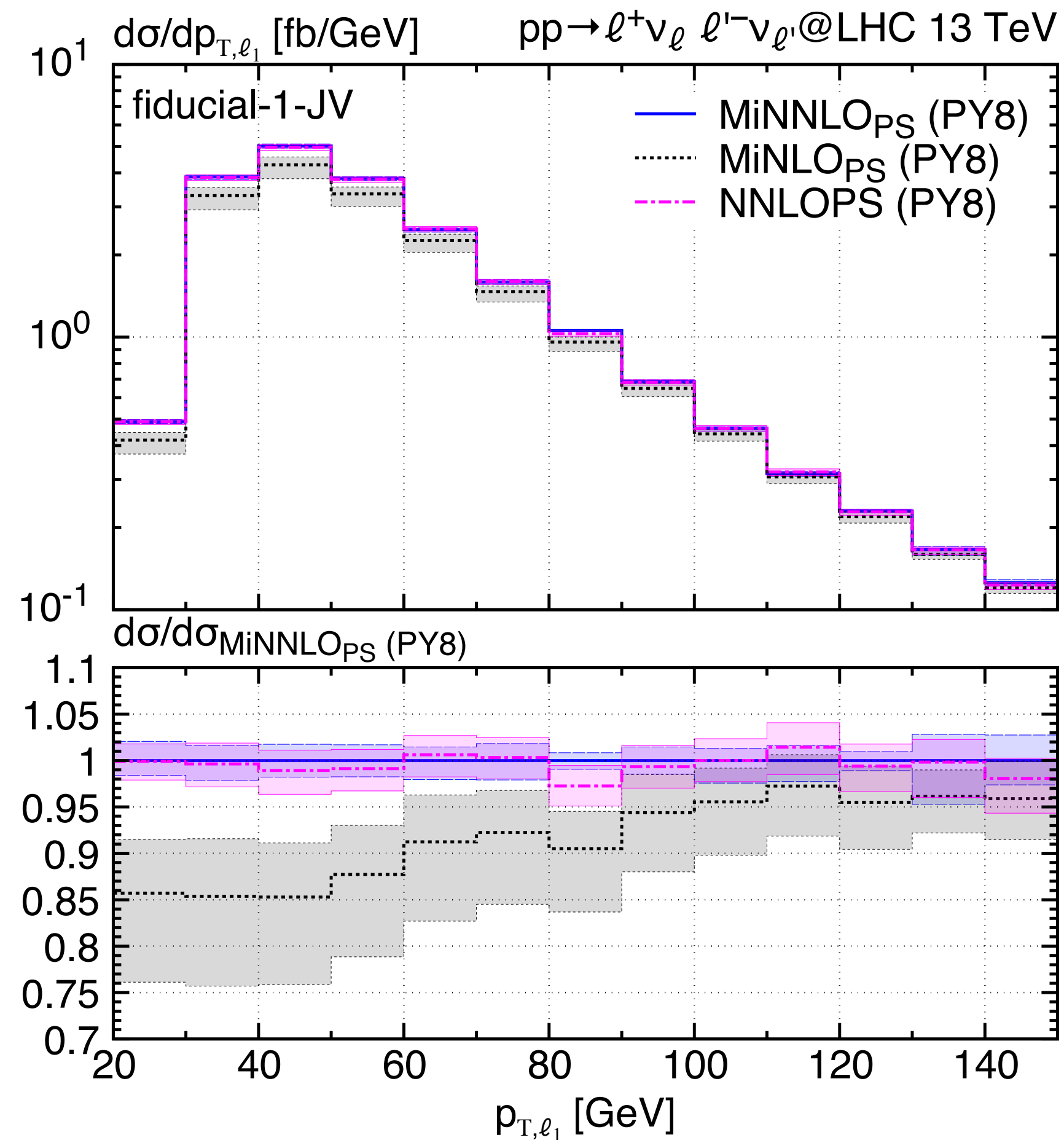


• Very good data vs. theory agreement

• gg @ NLO QCD + PS now available!

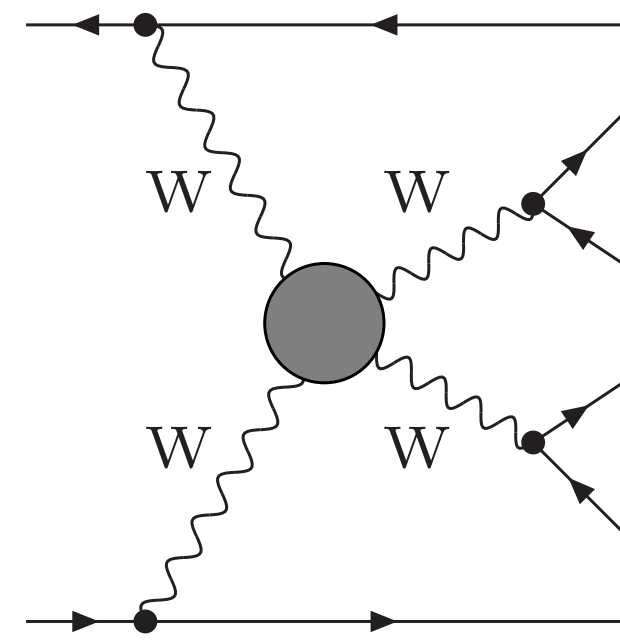
NNLO QCD + PS

[D. Lombardi, M. Wiesemann, G. Zanderighi; 2103.12077]

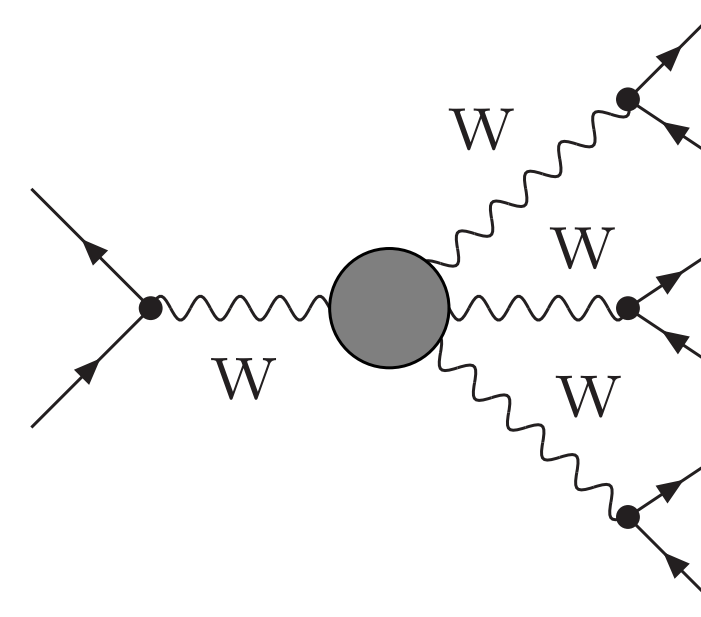


- Very small PS corrections for inclusive observables.
- Inclusion mandatory for (jet) exclusive observables

Rare EW processes

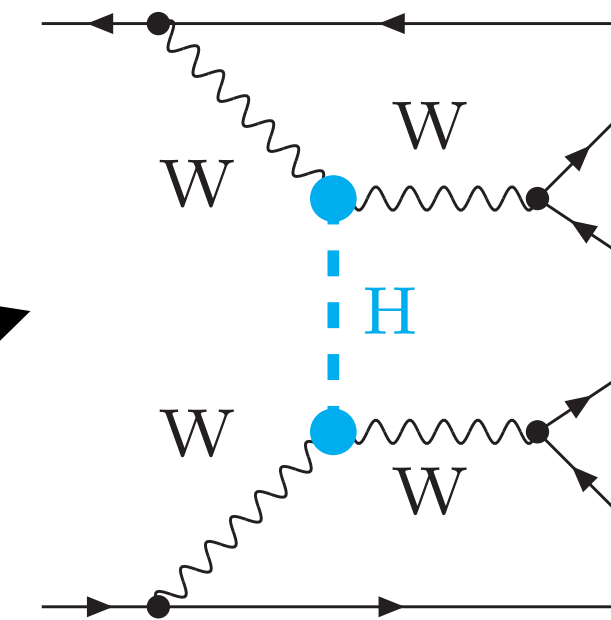


VBS



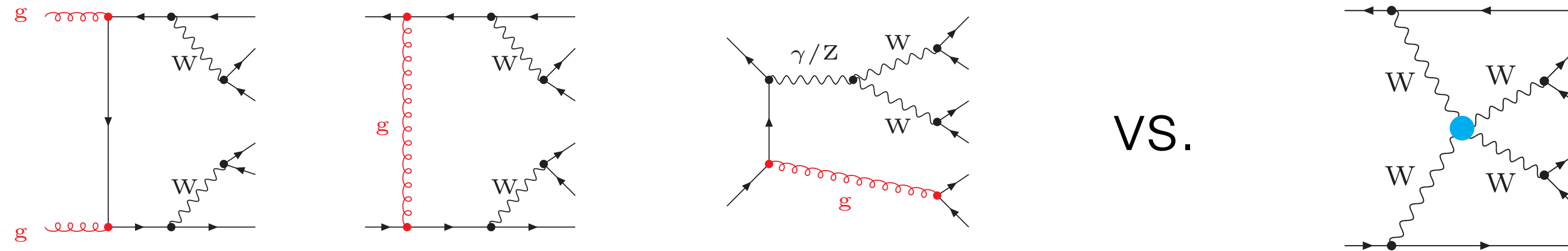
Triboson

- direct access to quartic EW gauge couplings
- VBS: longitudinal gauge bosons at high energies
- window to electroweak symmetry breaking via off-shell Higgs exchange



VBS

Note: severe QCD background to VBS signatures + interference:



VS.

$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$$

LO

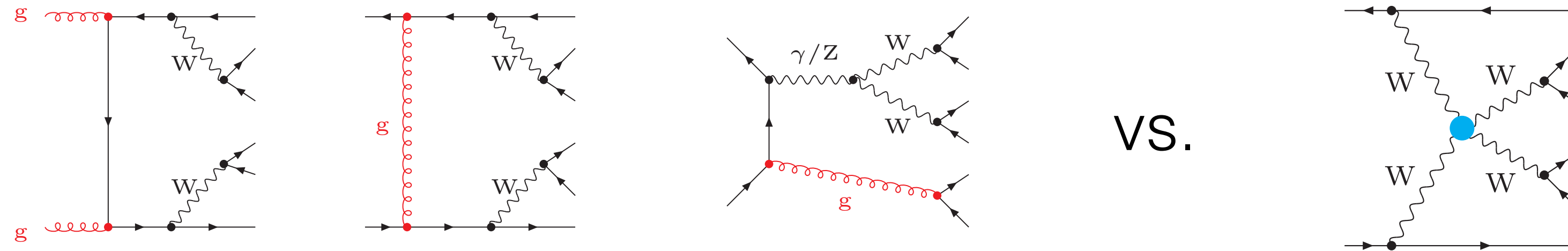
QCD-background

interference

VBS-signal

VBS

Note: severe QCD background to VBS signatures + interference:



$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$$

LO

QCD-background

interference

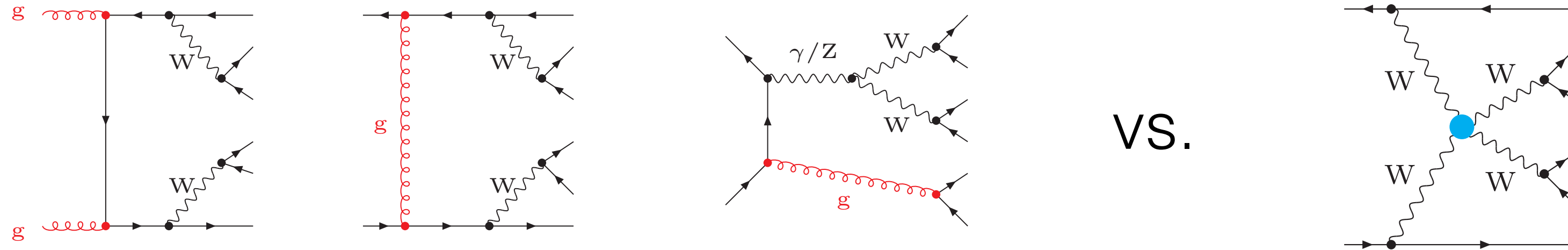
VBS-signal

$$\dots + d\sigma(\alpha_S^3 \alpha^4) + d\sigma(\alpha_S^2 \alpha^5) + d\sigma(\alpha_S \alpha^6) + \sigma(\alpha^7)$$

NLO

VBS

Note: severe QCD background to VBS signatures + interference:



VS.

$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$$

LO



$$\dots + d\sigma(\alpha_S^3 \alpha^4) + d\sigma(\alpha_S^2 \alpha^5) + d\sigma(\alpha_S \alpha^6) + \sigma(\alpha^7)$$

NLO

“NLO QCD”

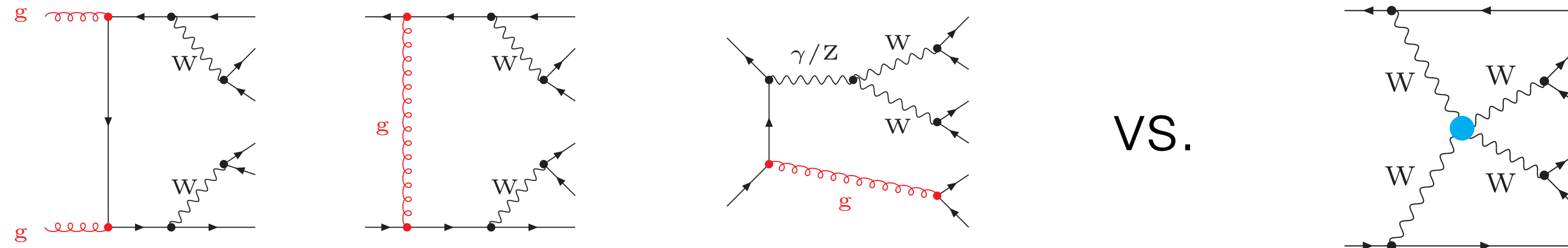
“NLO EW”

“NLO QCD”

“NLO EW”

VBS

Note: severe QCD background to VBS signatures + interference:



$$d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots \quad \text{LO}$$



$$\dots + d\sigma(\alpha_S^3 \alpha^4) + d\sigma(\alpha_S^2 \alpha^5) + d\sigma(\alpha_S \alpha^6) + \sigma(\alpha^7) \quad \text{NLO}$$

“NLO QCD”

“NLO EW”

“NLO QCD”

“NLO EW”

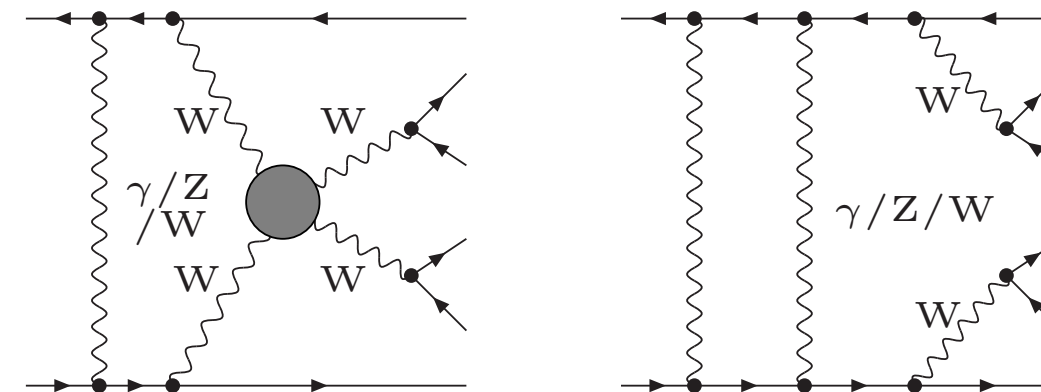
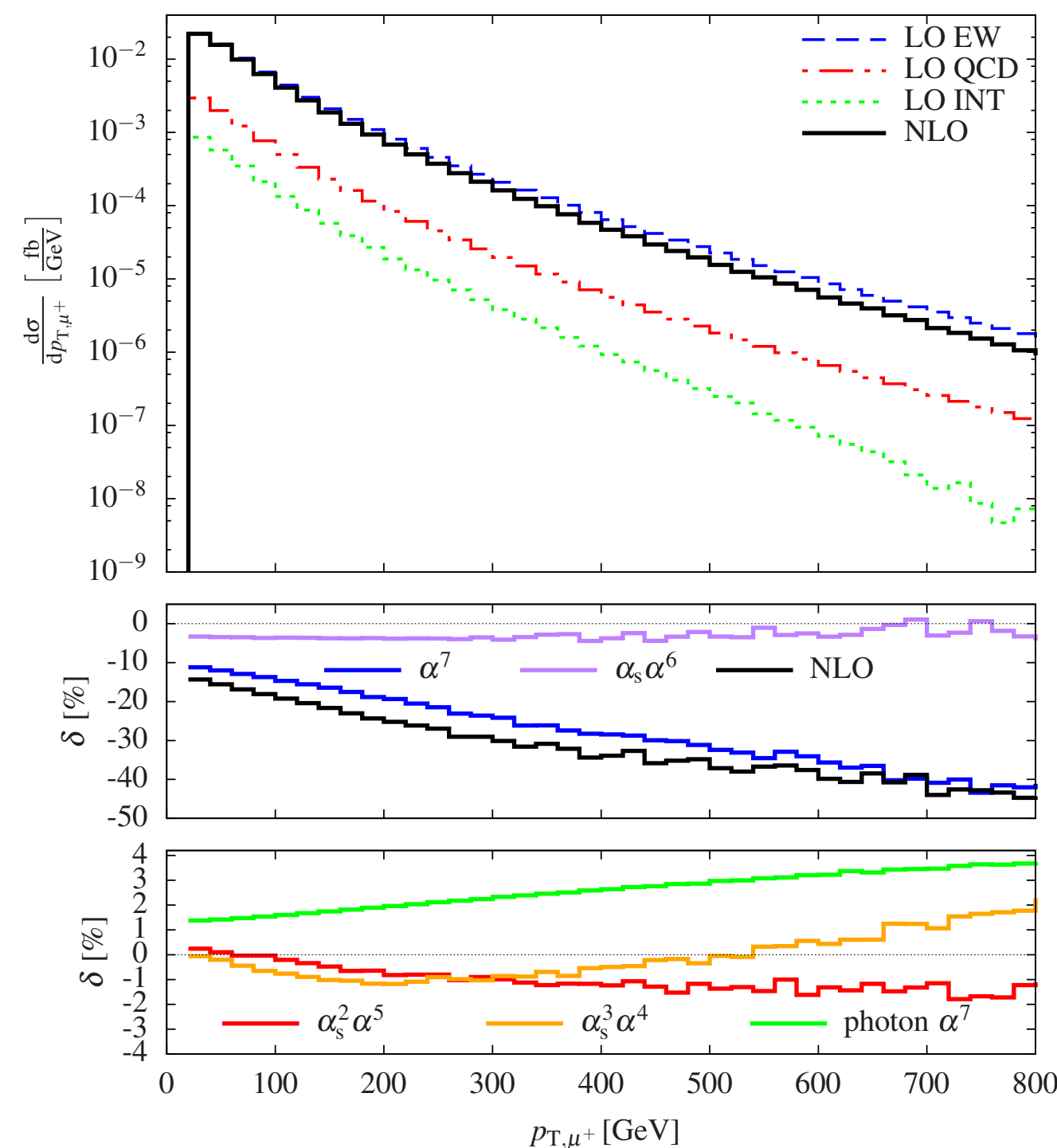
➡ separation meaningless at NLO

VBS-@ full NLO

WW full NLO: [Biedermann, Denner, Pellen '16+'17]

WZ-EW NLO QCD+EW: [Denner, Dittmaier, Maierhöfer, Pellen, Schwan, 19]

ZZ-EW NLO QCD+EW: [Denner, Franken, Pellen, Schmidt, '20]



- 2 → 6 particles at NLO EW !
- highly challenging computation!

- NLO corrections dominated by α^7 :

Order	$\mathcal{O}(\alpha^7)$	$\mathcal{O}(\alpha_s \alpha^6)$	$\mathcal{O}(\alpha_s^2 \alpha^5)$	$\mathcal{O}(\alpha_s^3 \alpha^4)$	Sum
$\delta\sigma_{\text{NLO}}$ [fb]	-0.2169(3)	-0.0568(5)	-0.00032(13)	-0.0063(4)	-0.2804(7)
$\delta\sigma_{\text{NLO}}/\sigma_{\text{LO}}$ [%]	-13.2	-3.5	0.0	-0.4	-17.1

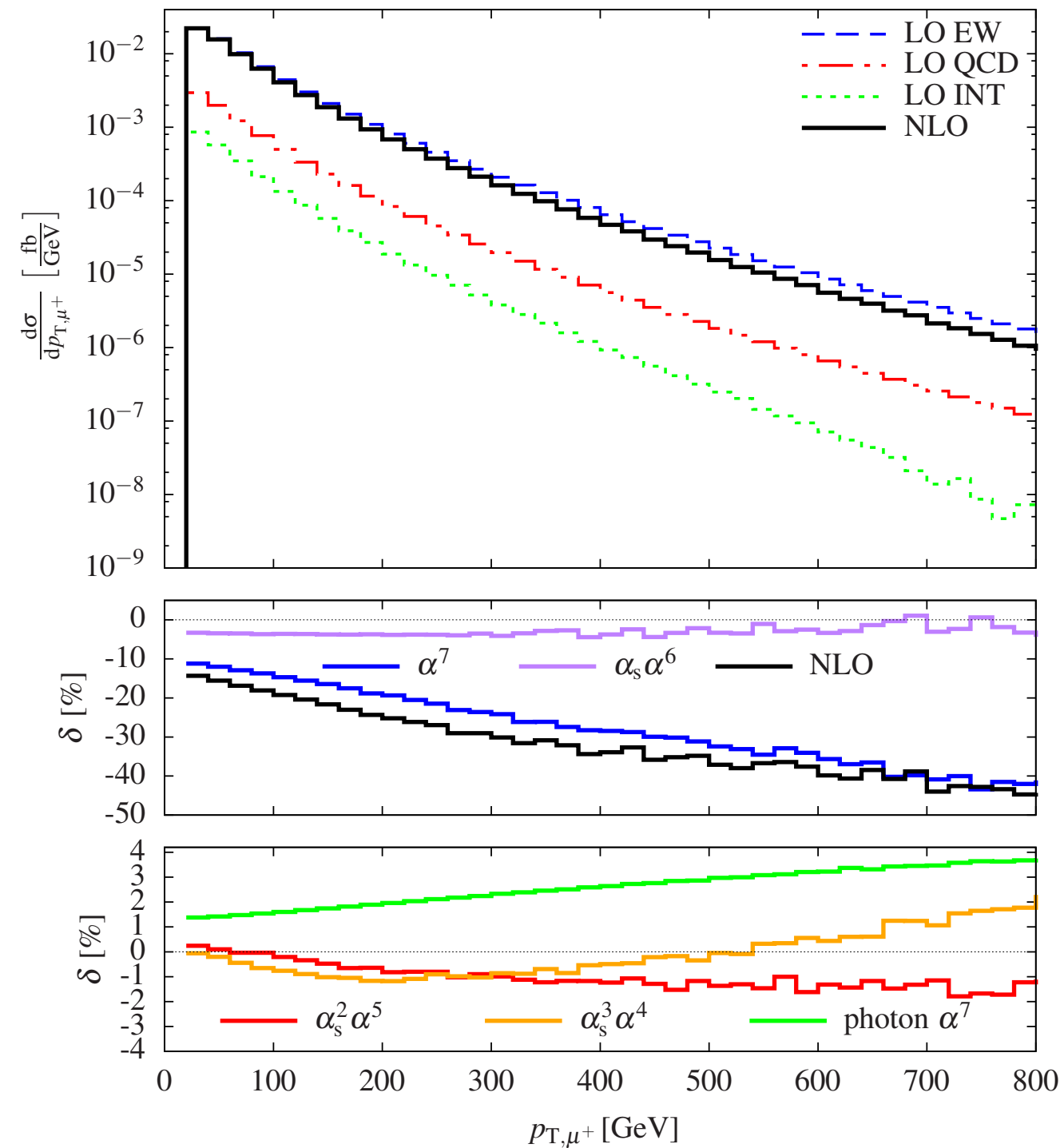
with $M_{jj} > 500 \text{ GeV}$, $p_{T,j} > 30 \text{ GeV}$, $p_{T,\ell} > 20 \text{ GeV}$,

LO: $\mathcal{O}(\alpha^6)$	σ^{LO} [fb]	$\sigma_{\text{EW}}^{\text{NLO}}$ [fb]	δ_{EW} [%]
NLO: $\mathcal{O}(\alpha^7)$	1.5348(2)	1.2895(6)	-16.0

- VERY large inclusive EW corrections (dominated by Sudakov logs)

VBS- W^+W^+ @ full NLO

[Biedermann, Denner, Pellen '16+'17]



- VERY large EW corrections (dominated by Sudakov logs)

LO: $\mathcal{O}(\alpha^6)$	σ^{LO} [fb]	$\sigma_{\text{EW}}^{\text{NLO}}$ [fb]	δ_{EW} [%]
NLO: $\mathcal{O}(\alpha^7)$	1.5348(2)	1.2895(6)	-16.0

Leading logarithm approximation [Denner, Pozzorini; hep-ph/0010201]

$$\sigma_{\text{LL}} = \sigma_{\text{LO}} \left[1 - \frac{\alpha}{4\pi} 4C_W^{\text{ew}} \log^2 \left(\frac{Q^2}{M_W^2} \right) + \frac{\alpha}{4\pi} 2b_W^{\text{ew}} \log \left(\frac{Q^2}{M_W^2} \right) \right]$$

$$= -16\% (!)$$

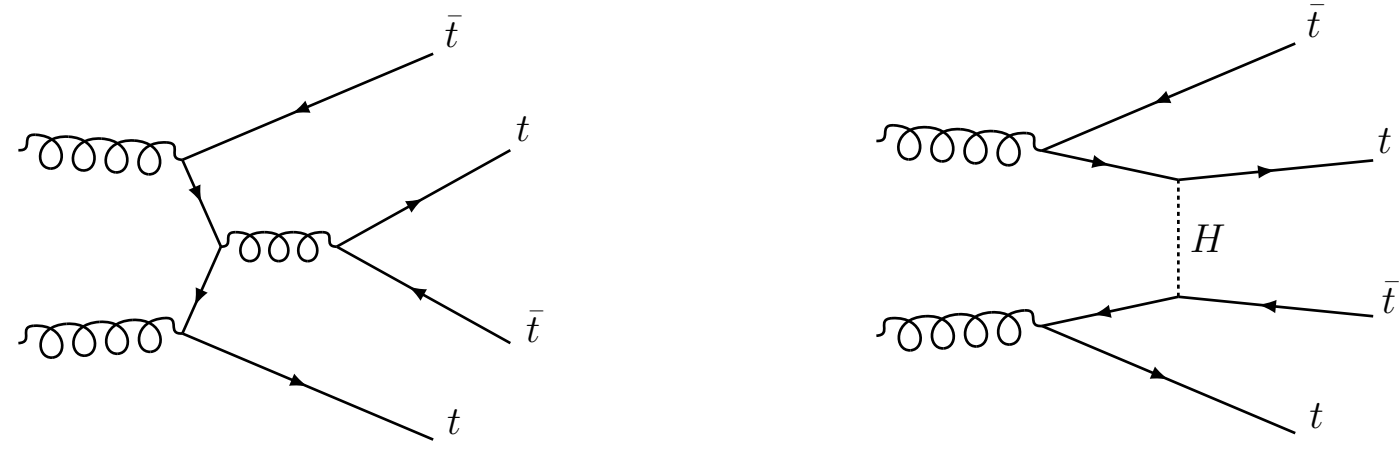
$$\text{For } Q = \langle m_{4\ell} \rangle \sim 390 \text{ GeV}$$

$\langle m_{4\ell} \rangle$ larger for VBS (massive t -channel)

NB: $\langle m_{4\ell} \rangle \sim 250 \text{ GeV}$ for $q\bar{q} \rightarrow W^+W^+$

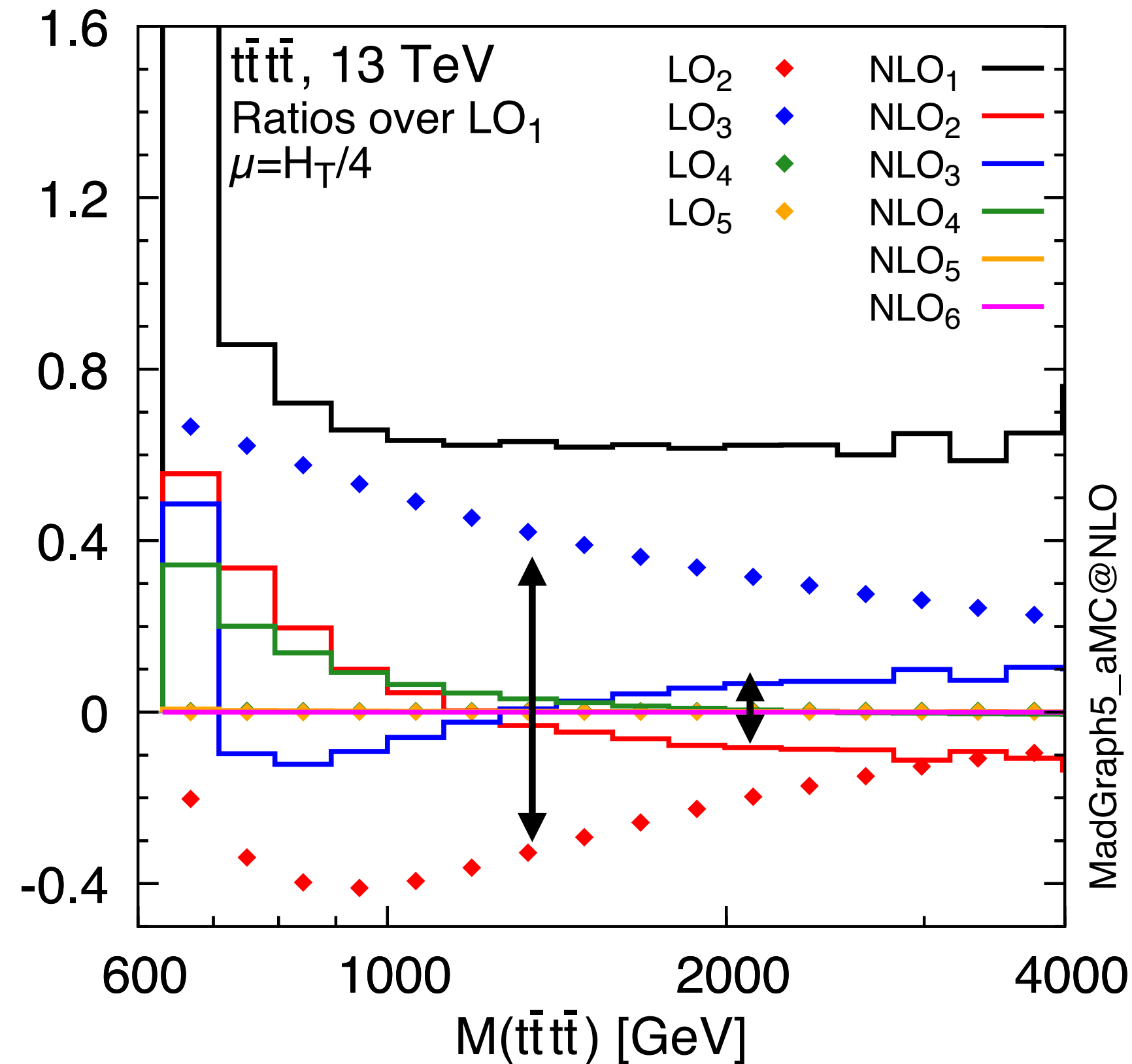
- ➔ Large NLO EW corrections: intrinsic feature of VBS at the LHC

Rare top processes



Motivation:

- Constraining top-quark flavour violation [1804.05598]
- Constraining qqtt operators [1708.05928]
- Higgs width and top quark Yukawa coupling [1602.01934]



[Frederix, Pagani, Zaro; '17]

$$\begin{aligned} \Sigma_{\text{LO}}^{t\bar{t}t\bar{t}}(\alpha_s, \alpha) &= \alpha_s^4 \Sigma_{4,0}^{t\bar{t}t\bar{t}} + \alpha_s^3 \alpha \Sigma_{4,1}^{t\bar{t}t\bar{t}} + \alpha_s^2 \alpha^2 \Sigma_{4,2}^{t\bar{t}t\bar{t}} + \alpha_s \alpha^3 \Sigma_{4,3}^{t\bar{t}t\bar{t}} + \alpha^4 \Sigma_{4,4}^{t\bar{t}t\bar{t}} \\ &\equiv \Sigma_{\text{LO}_1} + \Sigma_{\text{LO}_2} + \Sigma_{\text{LO}_3} + \Sigma_{\text{LO}_4} + \Sigma_{\text{LO}_5} . \end{aligned}$$

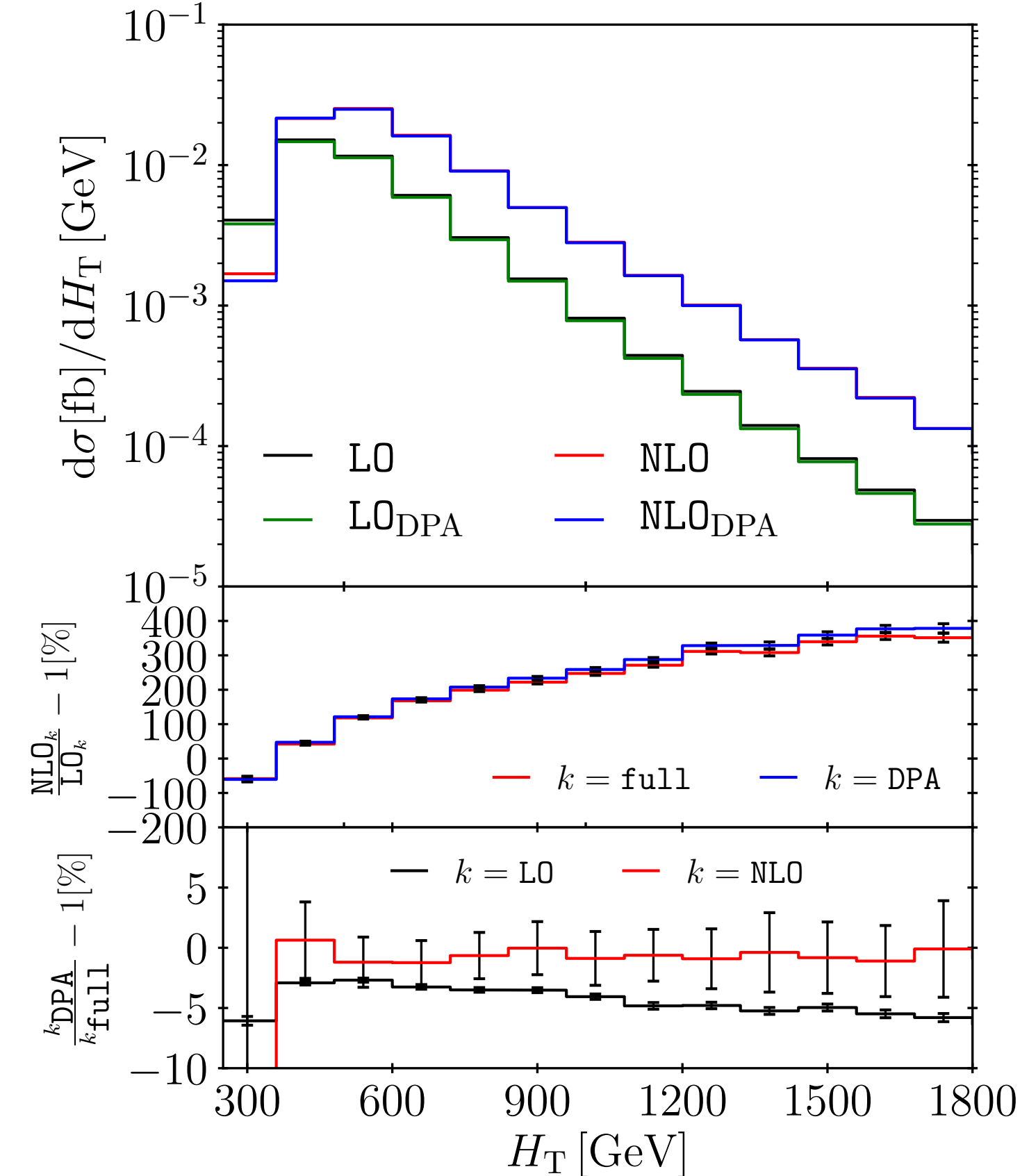
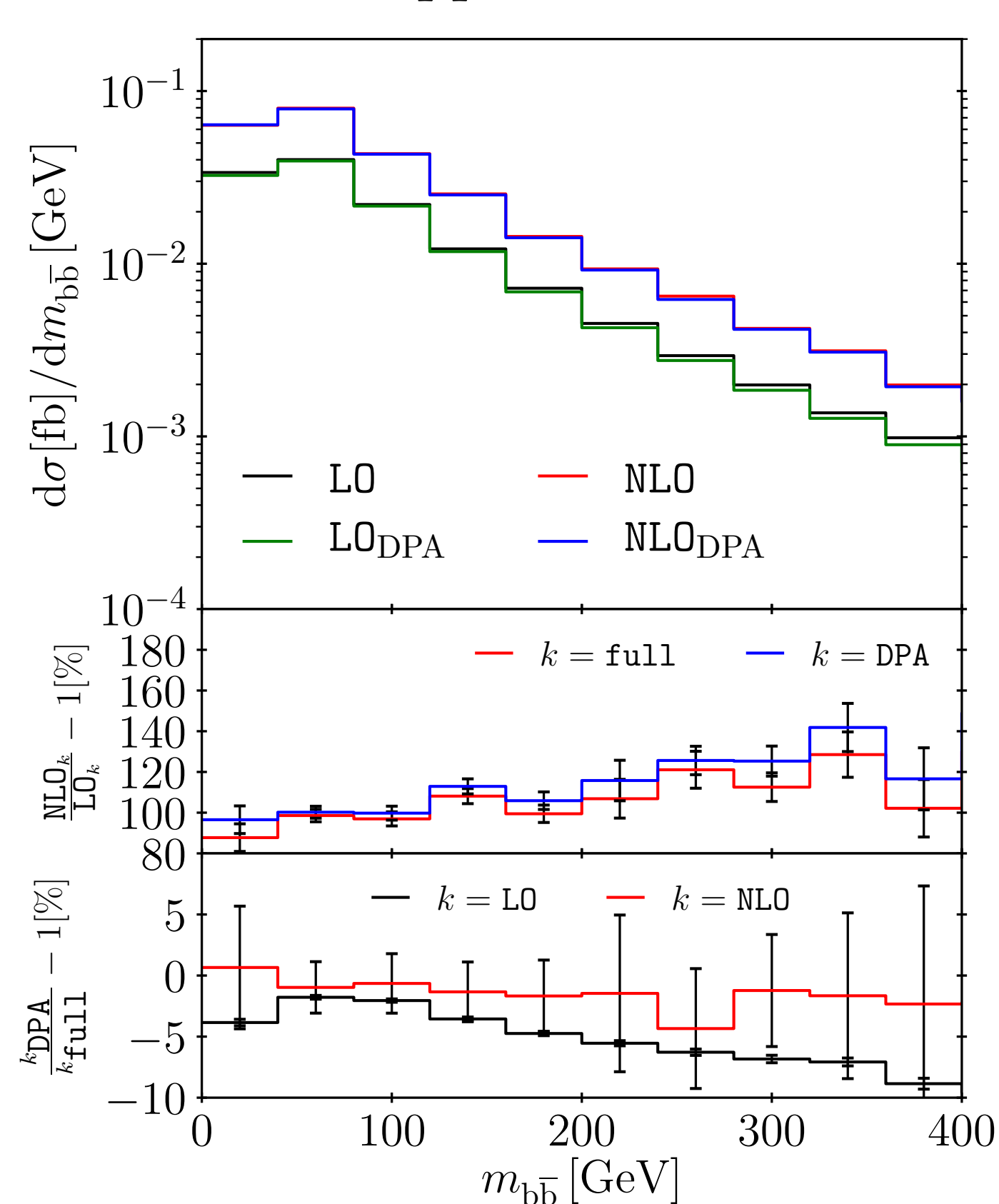
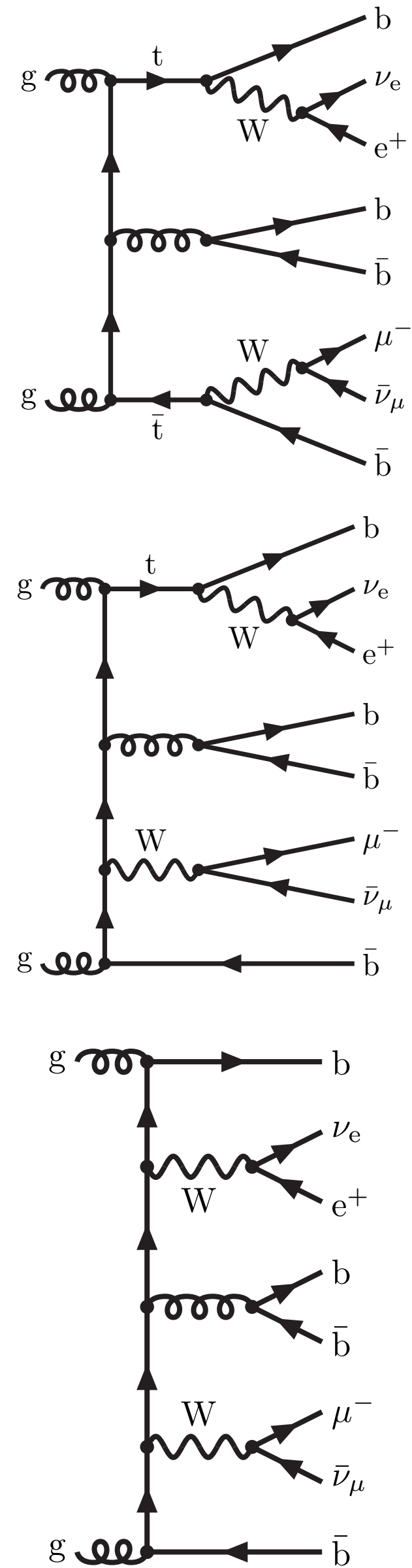
$$\begin{aligned} \Sigma_{\text{NLO}}^{t\bar{t}t\bar{t}}(\alpha_s, \alpha) &= \alpha_s^5 \Sigma_{5,0}^{t\bar{t}t\bar{t}} + \alpha_s^4 \alpha \Sigma_{5,1}^{t\bar{t}t\bar{t}} + \alpha_s^3 \alpha^2 \Sigma_{5,2}^{t\bar{t}t\bar{t}} + \alpha_s^2 \alpha^3 \Sigma_{5,3}^{t\bar{t}t\bar{t}} + \alpha_s \alpha^4 \Sigma_{5,4}^{t\bar{t}t\bar{t}} + \alpha^5 \Sigma_{5,5}^{t\bar{t}t\bar{t}} \\ &\equiv \Sigma_{\text{NLO}_1} + \Sigma_{\text{NLO}_2} + \Sigma_{\text{NLO}_3} + \Sigma_{\text{NLO}_4} + \Sigma_{\text{NLO}_5} + \Sigma_{\text{NLO}_6} . \end{aligned}$$

- Sizeable (accidental) cancellation between different LO and NLO orders
- calculation of only part of the complete-NLO results would be misleading
- cancellation could be spiked by BSM effects

Precision for the highest multiplicities

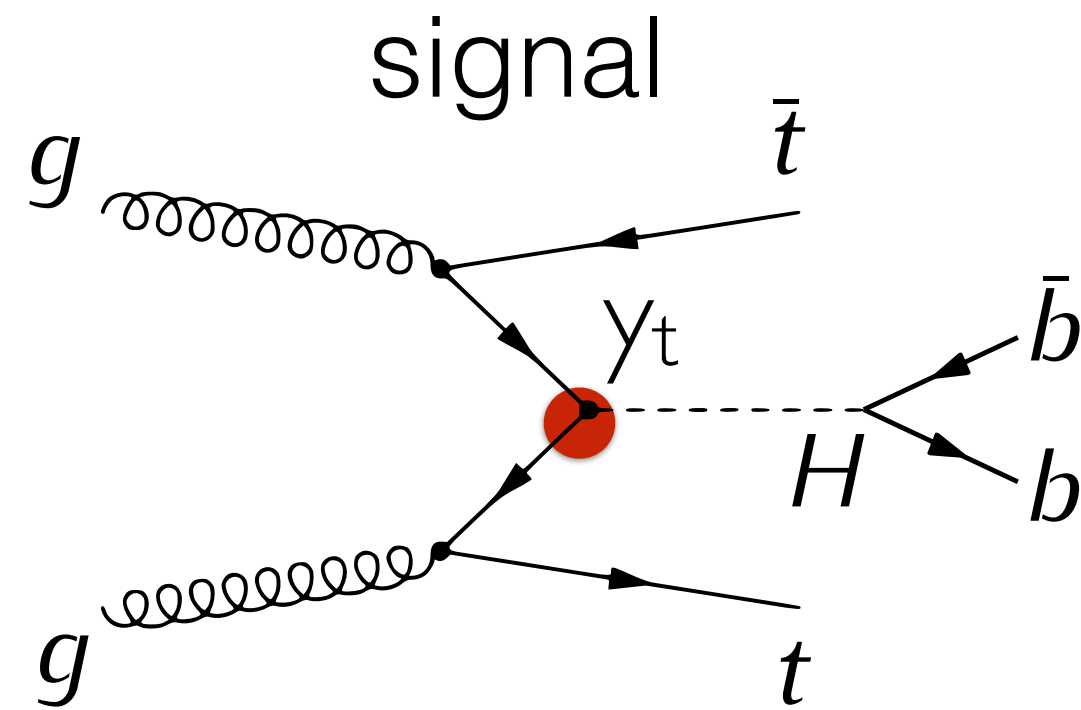
[Denner, Lang, Pellen '20]

$pp \rightarrow 2\ell 2\nu b\bar{b}b\bar{b}$ @ NLO QCD

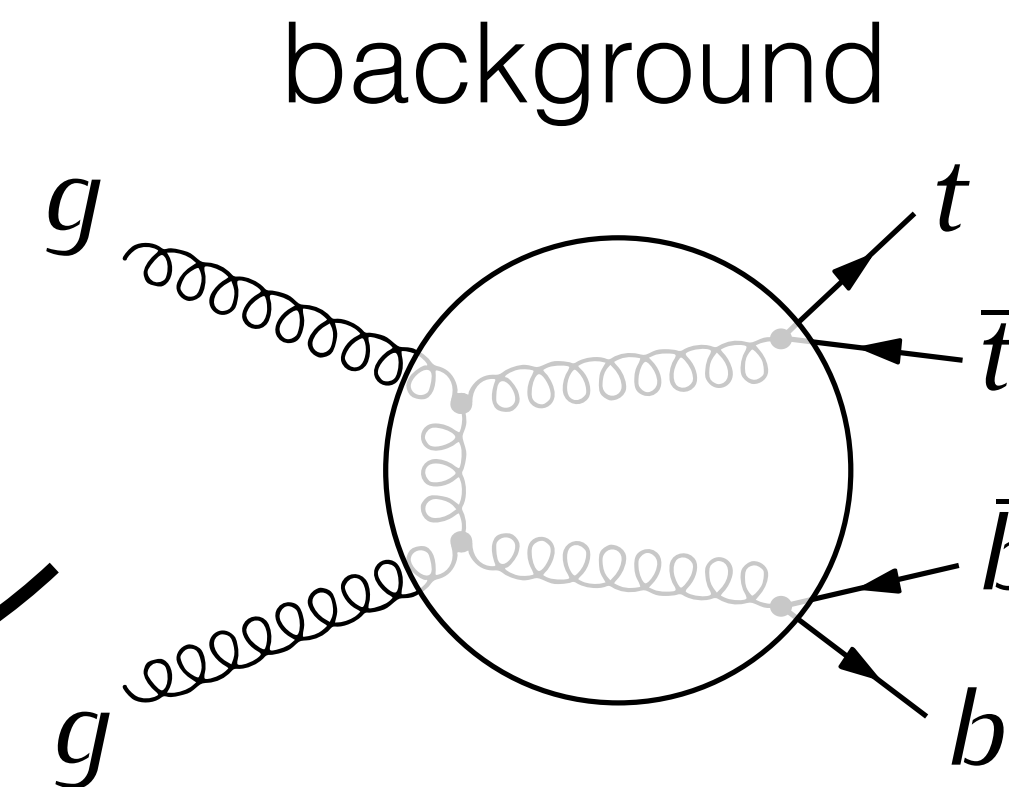
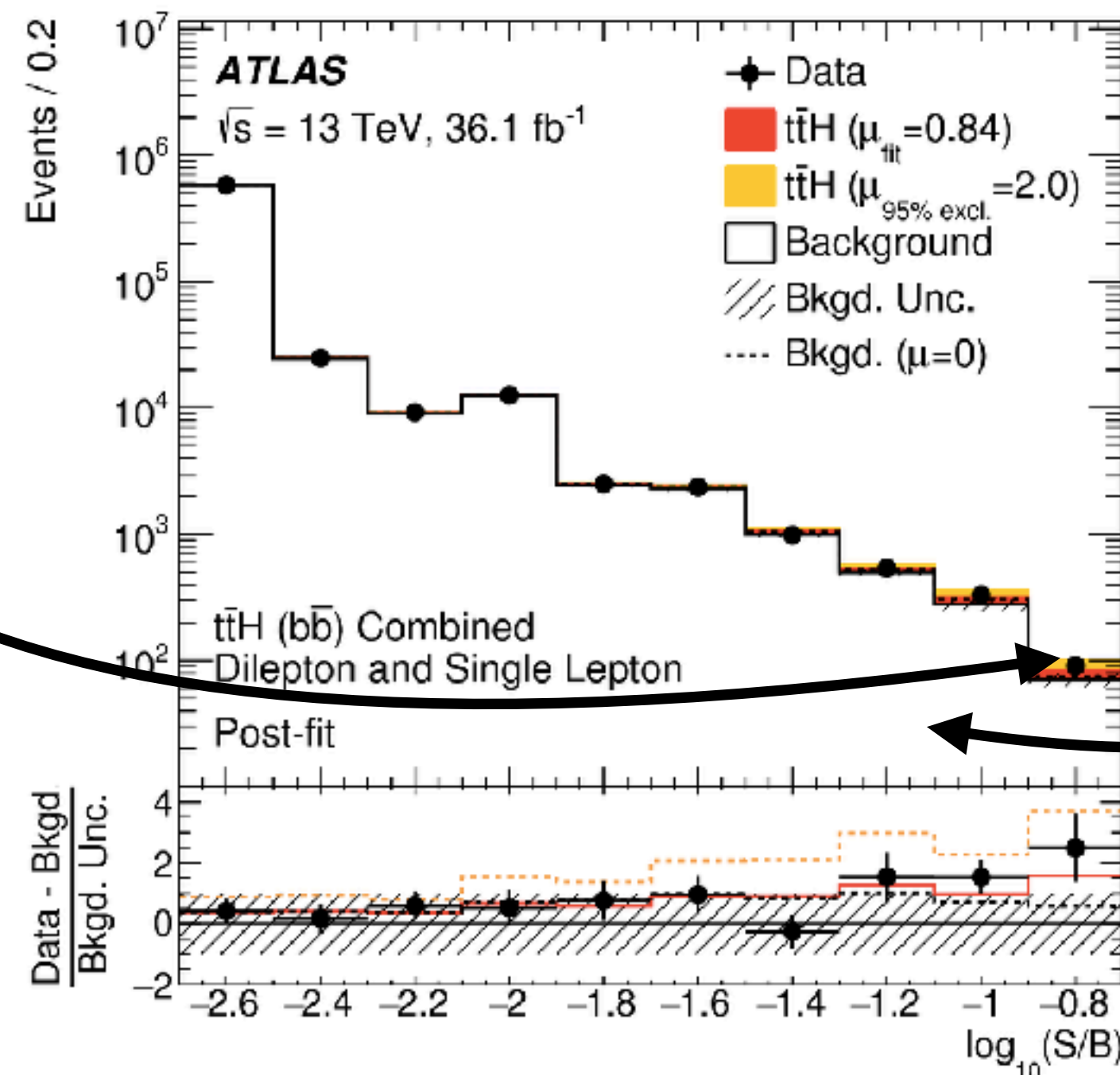


- Thorough understanding of theory systematics in this channel crucial for ttH measurements where $H \rightarrow b\bar{b}$
- ttbb receives sizeable QCD corrections
- Very important confirmation of (ttbb) double pole approximation

Taming $t\bar{t}H$ backgrounds



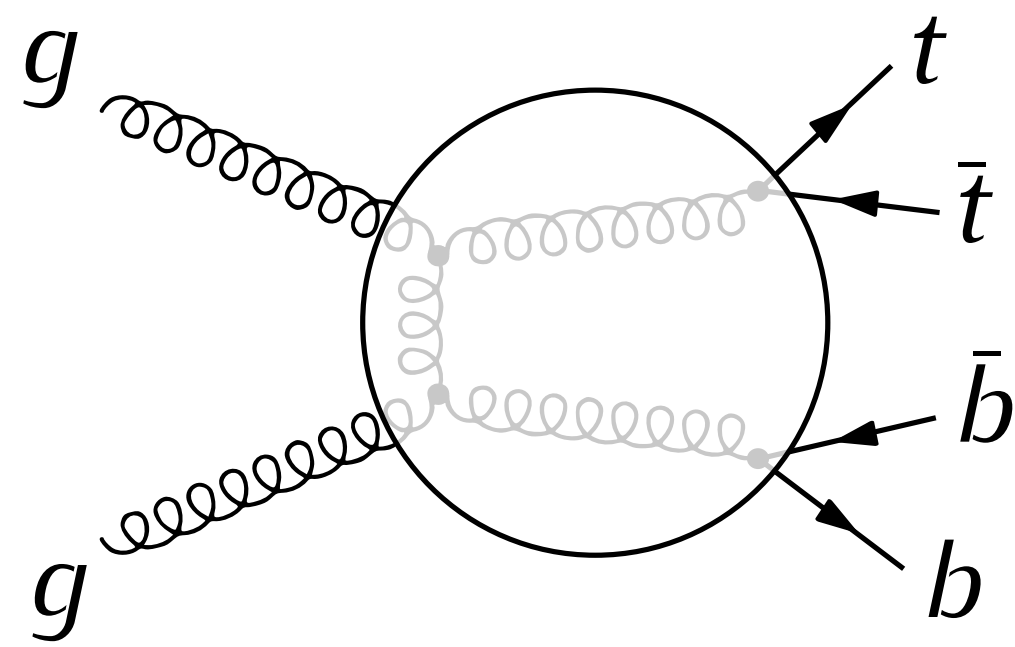
- ➔ direct probe of the top Yukawa coupling
- ➔ unfortunately very small cross section
- ➔ have to consider $H \rightarrow b\bar{b}$ decay with large BR
- ➔ large QCD background: $t\bar{t}+b$ -jets with sizeable uncertainties



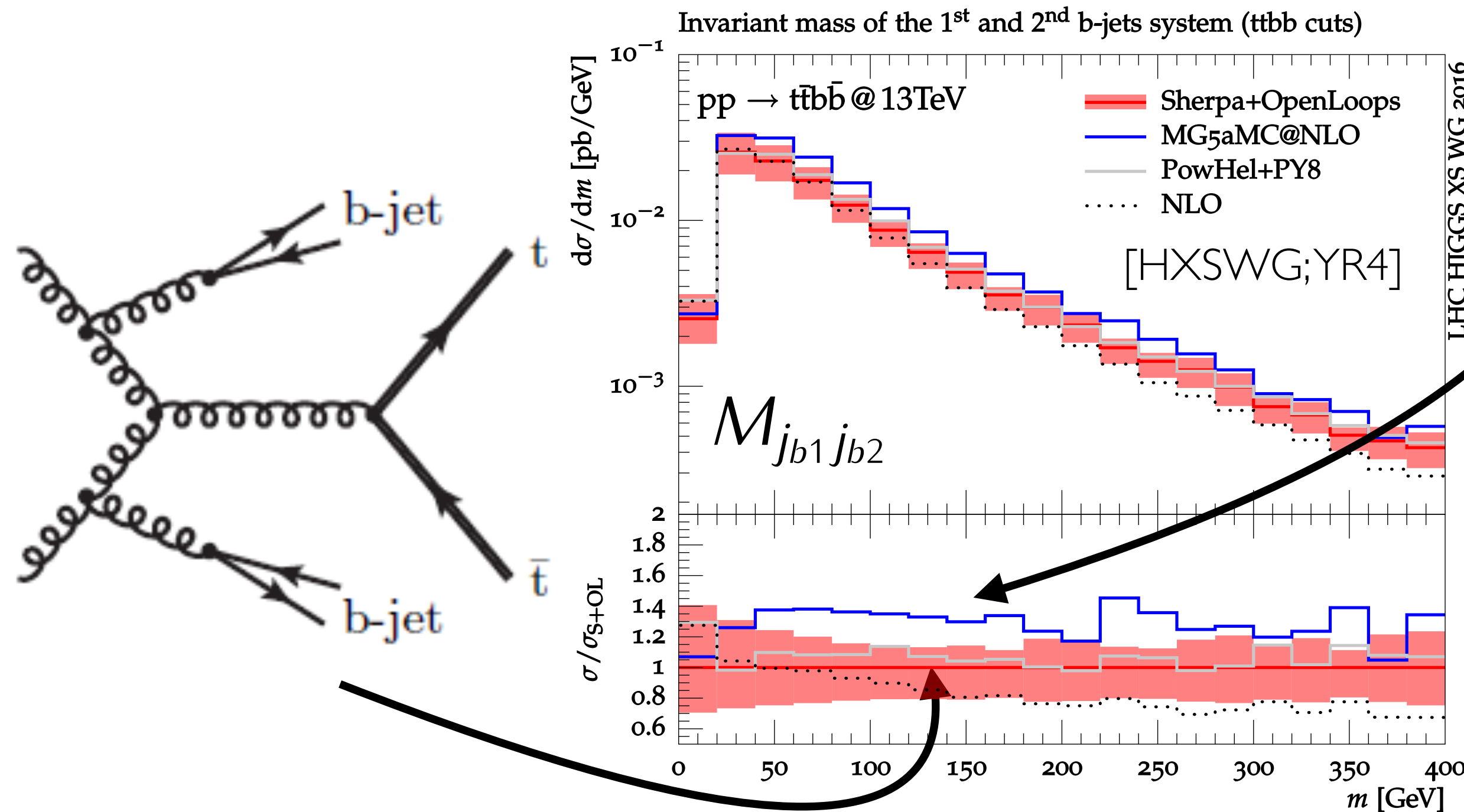
Taming $t\bar{t}H$ backgrounds

[Bevilacqua, Czakon, Papadopoulos, Pittau, Worek '09]
 [Bredenstein, Denner, Dittmaier, Pozzorini '10]

background

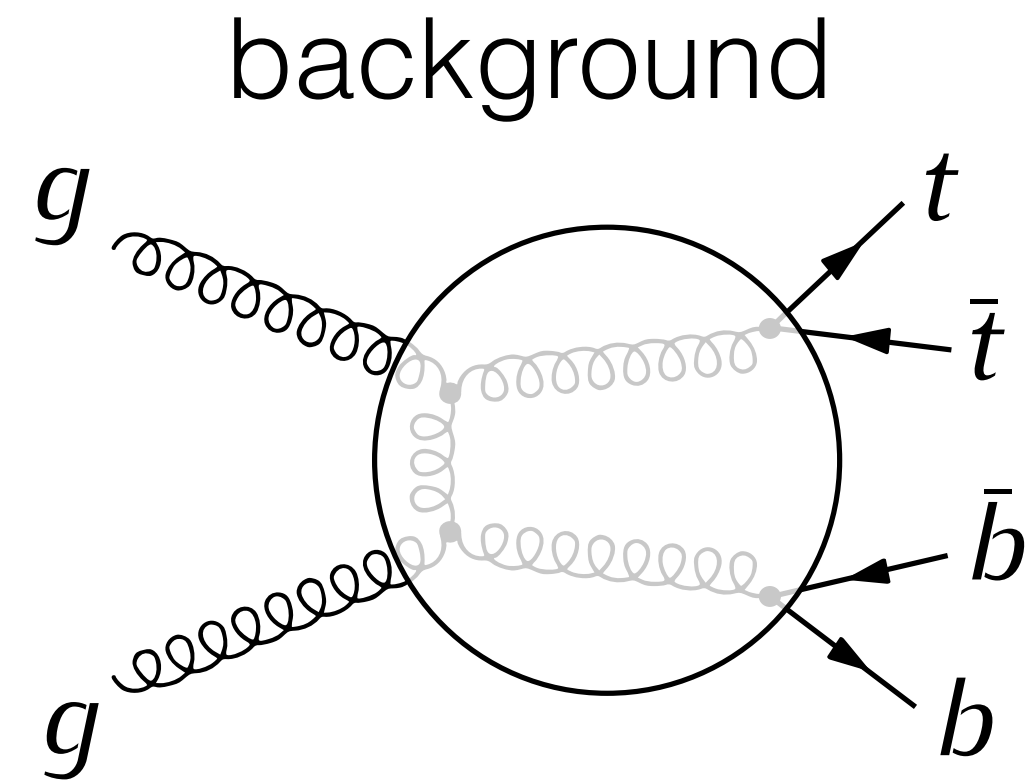


- ➔ in principle this process can be calculated out of the box at NLO+PS: NLO reduces scale uncertainties from 80% to 20-30%
- ➔ However: notoriously difficult multi-scale problem: $ET_t, ET_{\bar{t}}, ET_b, ET_{\bar{b}}$
- ➔ Large shower effects, in particular from double $g \rightarrow b\bar{b}$ splittings
- ➔ Large systematic uncertainties from parton shower matching

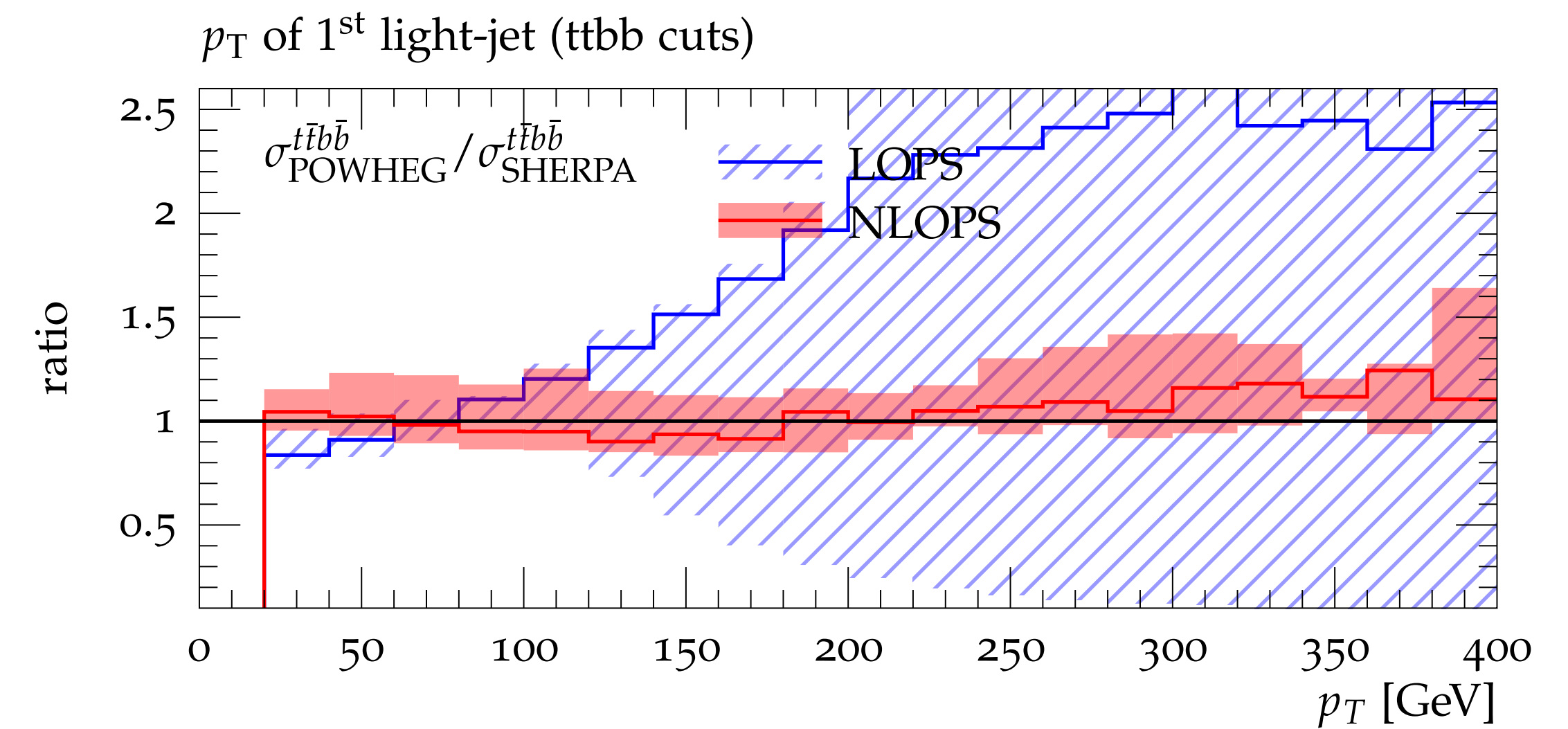
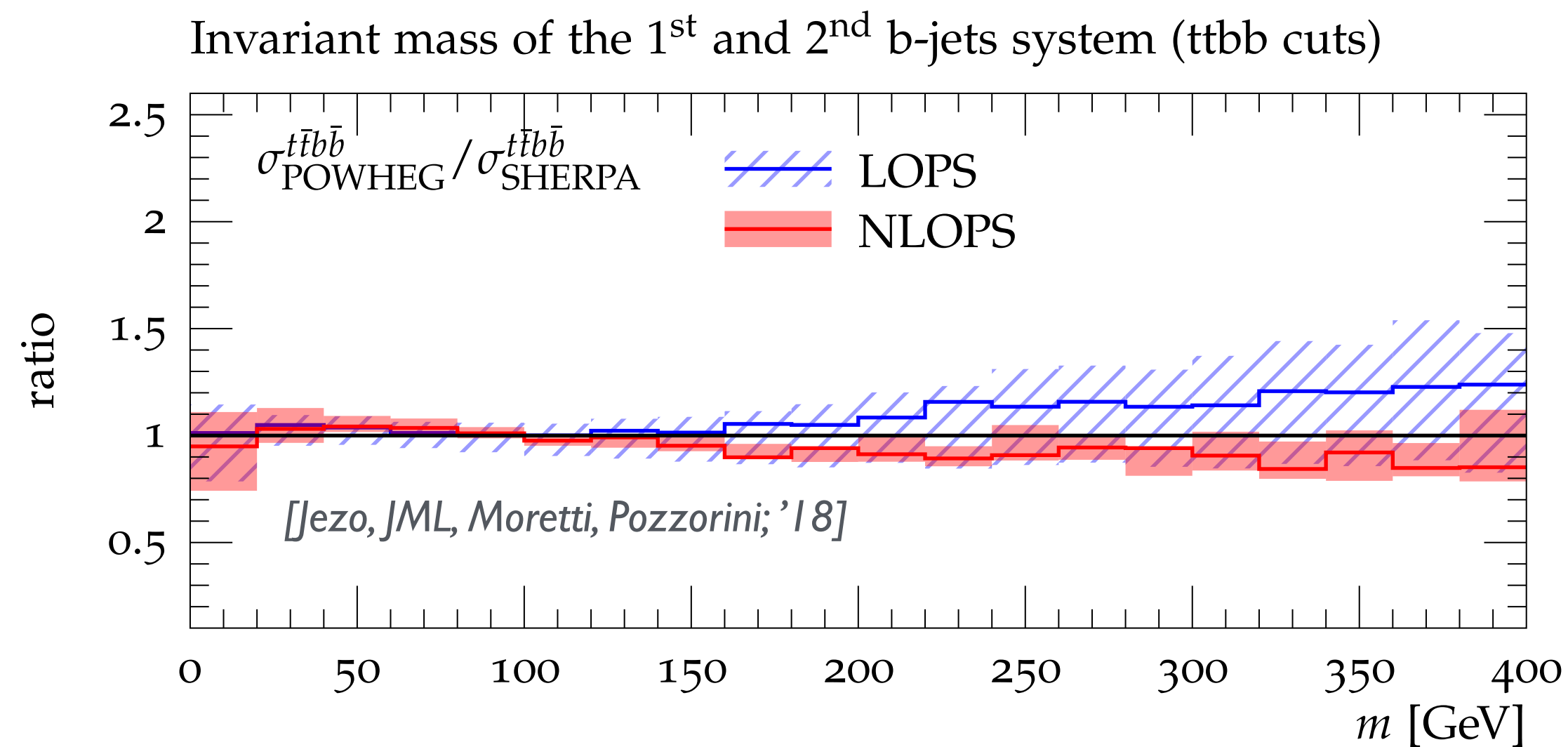


~20% in the signal region

Taming $t\bar{t}H$ backgrounds



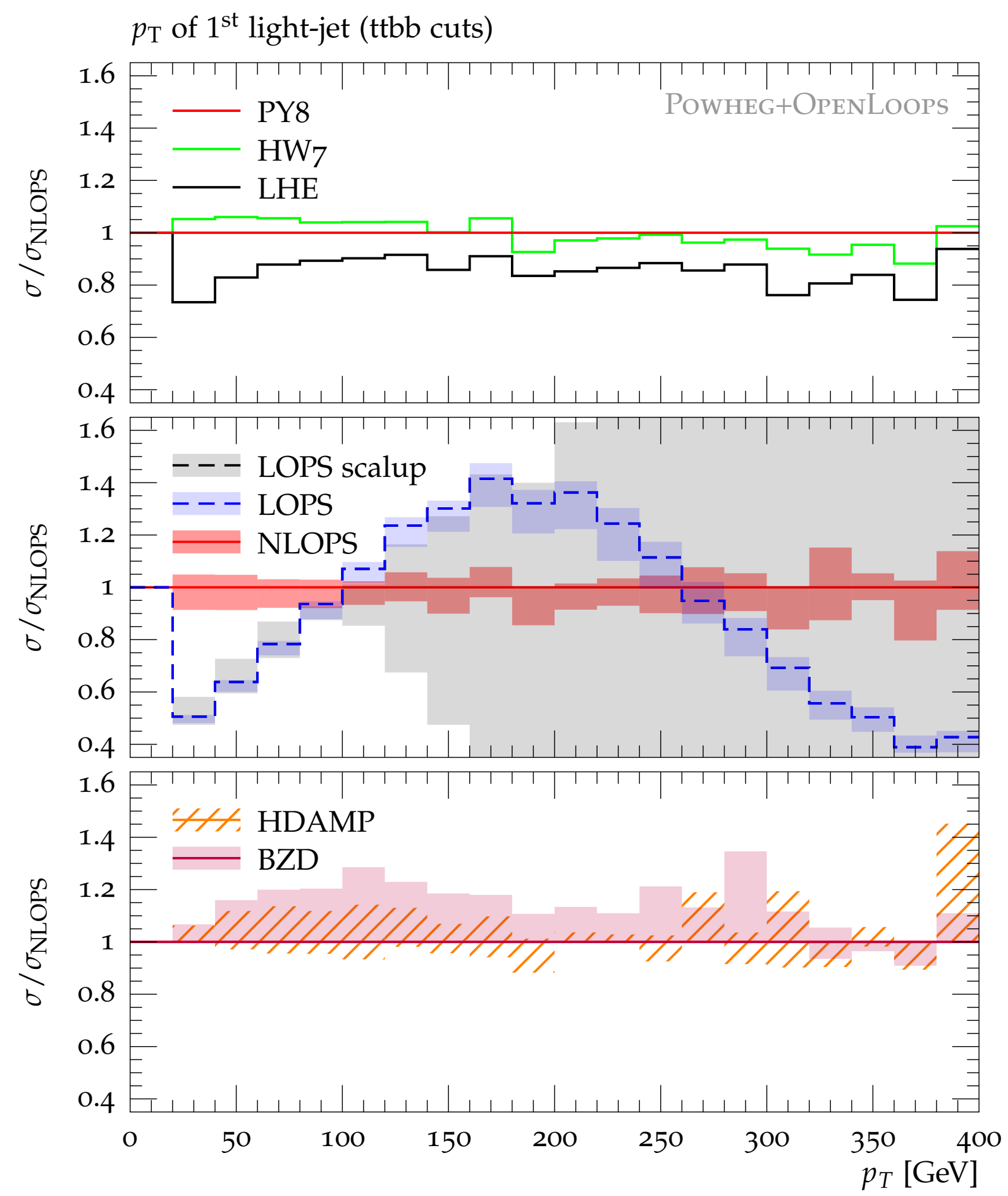
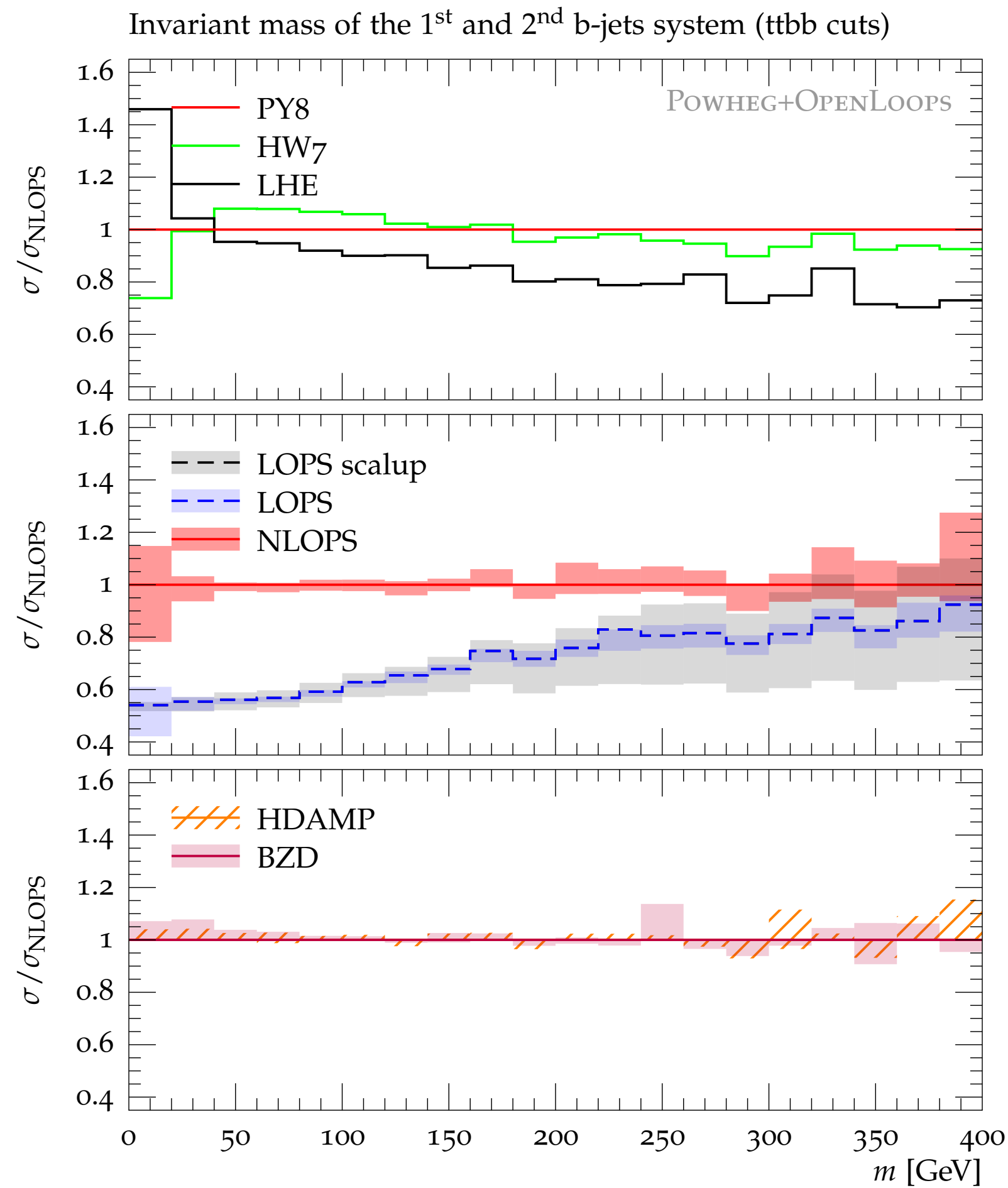
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- ➔ Large shower effects, in particular from double $g \rightarrow b\bar{b}$ splittings
- ➔ Large systematic uncertainties from parton shower matching
- ➔ Careful study required to understand these systematics



➔ Sherpa vs. POWHEG+PY8 (both in 4-FS) in very good agreement

Taming $t\bar{t}H$ backgrounds

[Jezo, JML, Moretti, Pozzorini; '18]



► Shower variations

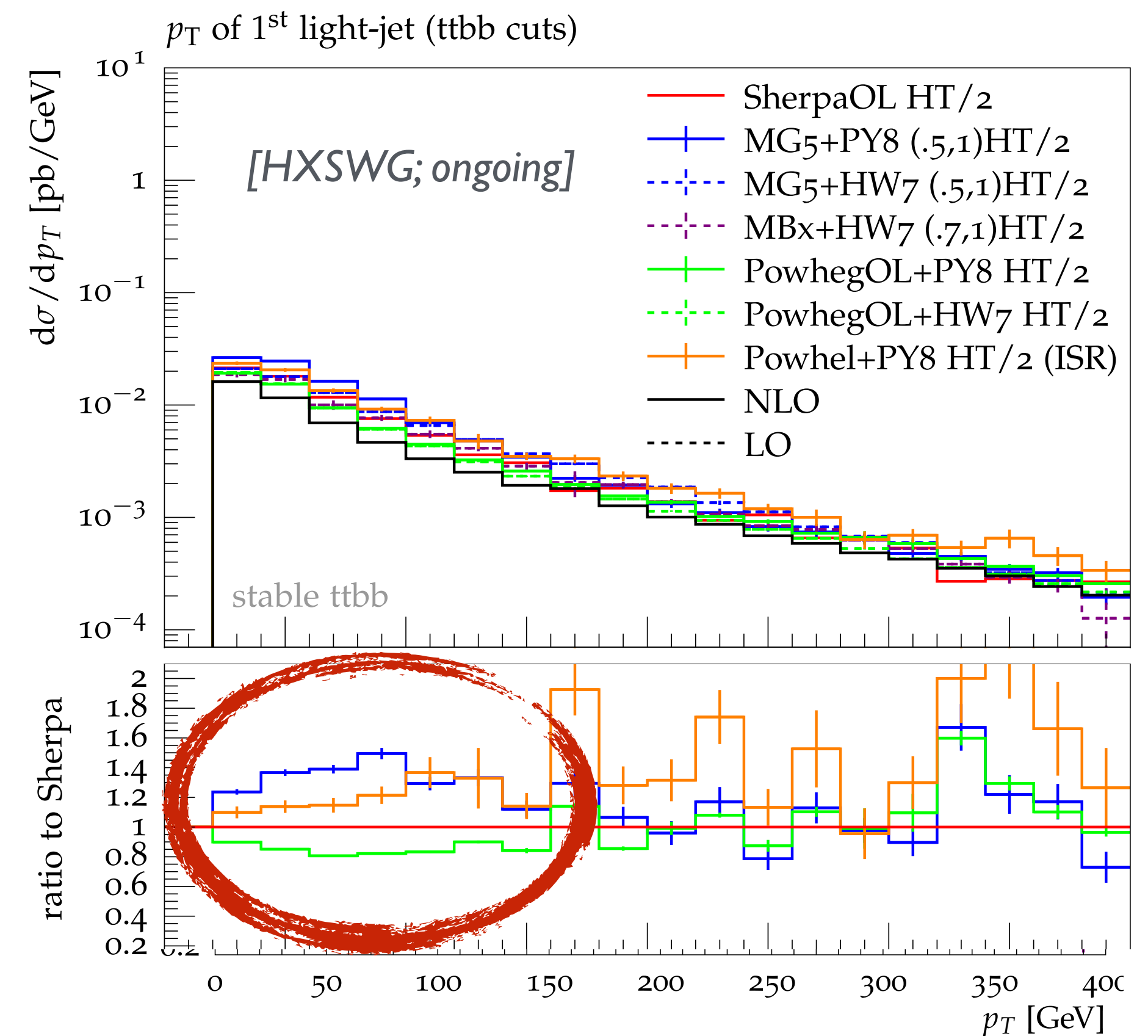
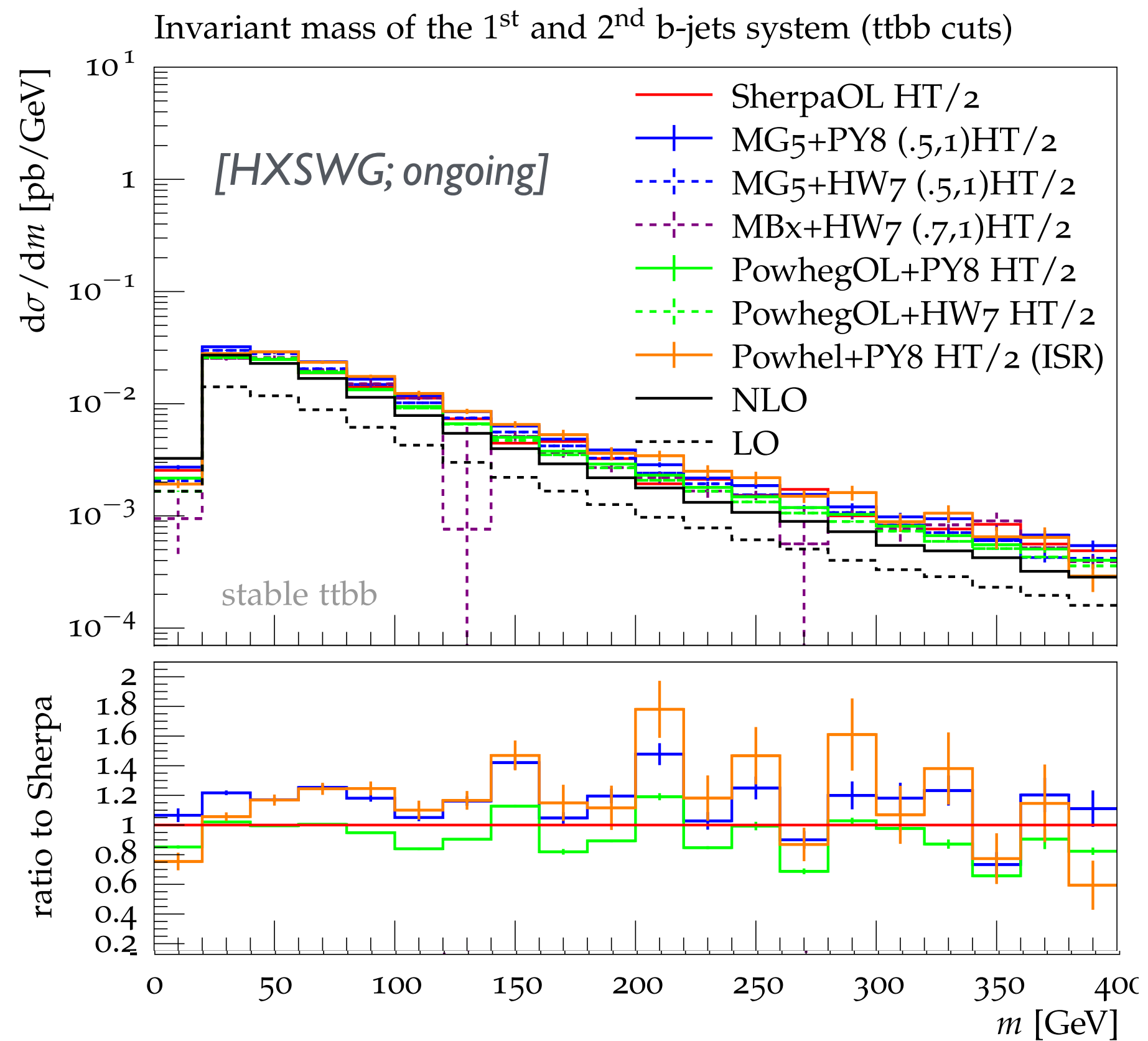
► α_s & $g \rightarrow b\bar{b}$ variations

► hdamp & bzd variations

$$g_{\text{soft}}(\Phi_{\text{rad}}, h_{\text{damp}}, h_{\text{bzd}}) = \frac{h_{\text{damp}}^2}{h_{\text{damp}}^2 + k_T^2} \theta\left(h_{\text{bzd}} B(\Phi_B) \otimes K_{\text{soft/coll}}(\Phi_{\text{rad}}) - R(\Phi_R)\right)$$

► Intrinsic shower systematics in POWHEG+PY8/HW7 under very good control

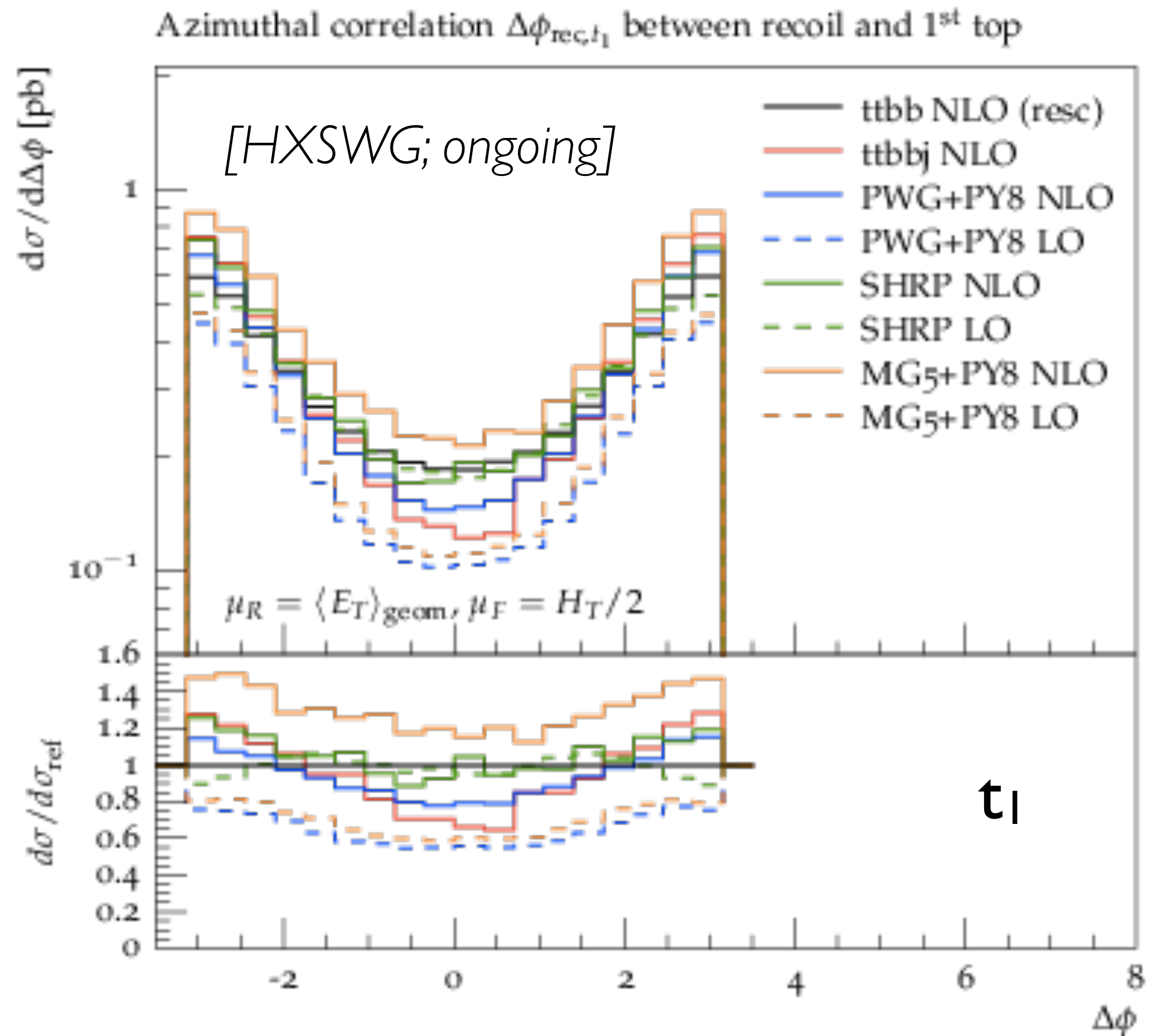
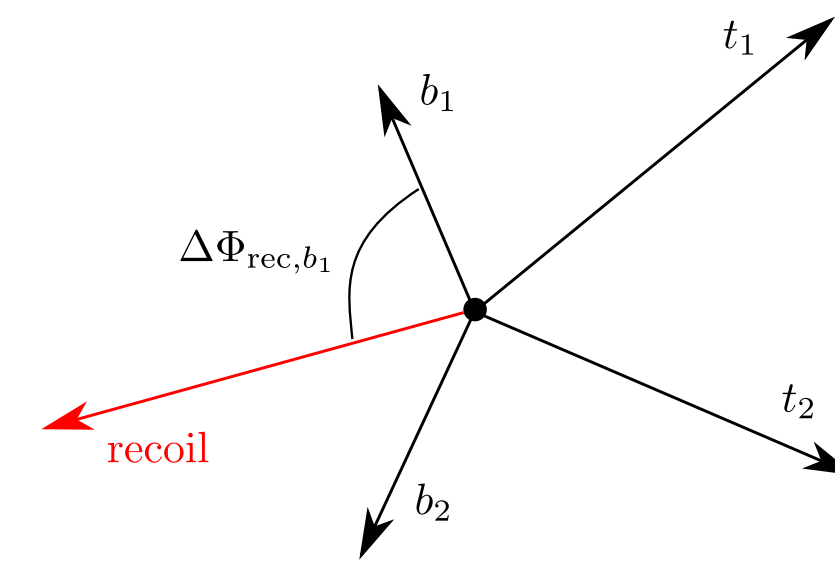
Taming $t\bar{t}H$ backgrounds



- ➔ Sizable differences between different generators: in particular in radiation/recoil spectrum
- ➔ Without understanding their origin (physical or not?) we should not use MC differences as theory uncertainty!
- ➔ **Careful look inside the NLO+PS black-boxes necessary:** ongoing within HXSWG!

The smoking gun

Study recoil observables: $\Delta\phi_{\text{rec},X} = \Delta\phi(\vec{p}_{\text{rec}}, \vec{p}_X)$, $\vec{p}_{\text{rec}} = -\sum_{t,\bar{t},b_1,b_2} \vec{p}_i$

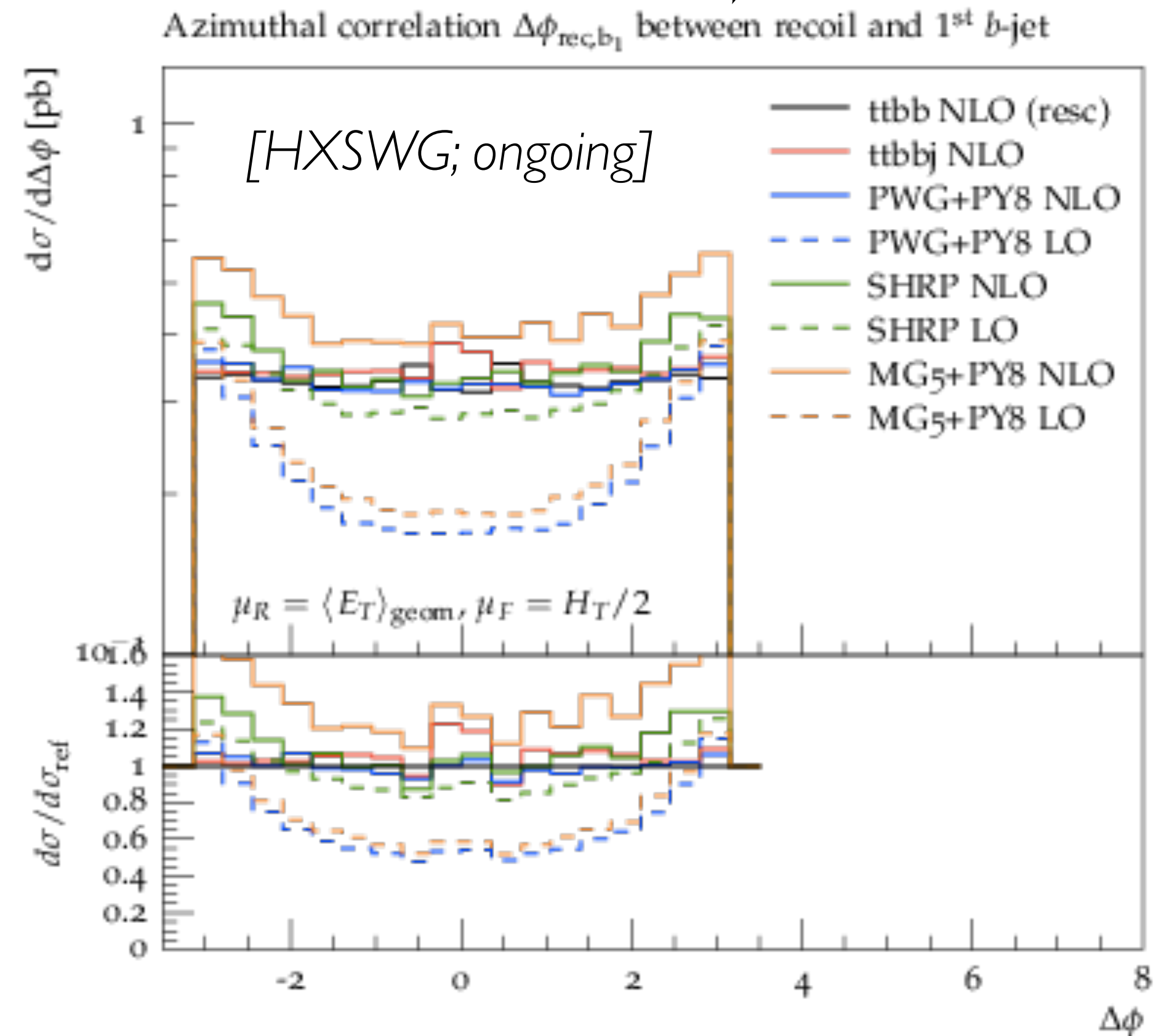
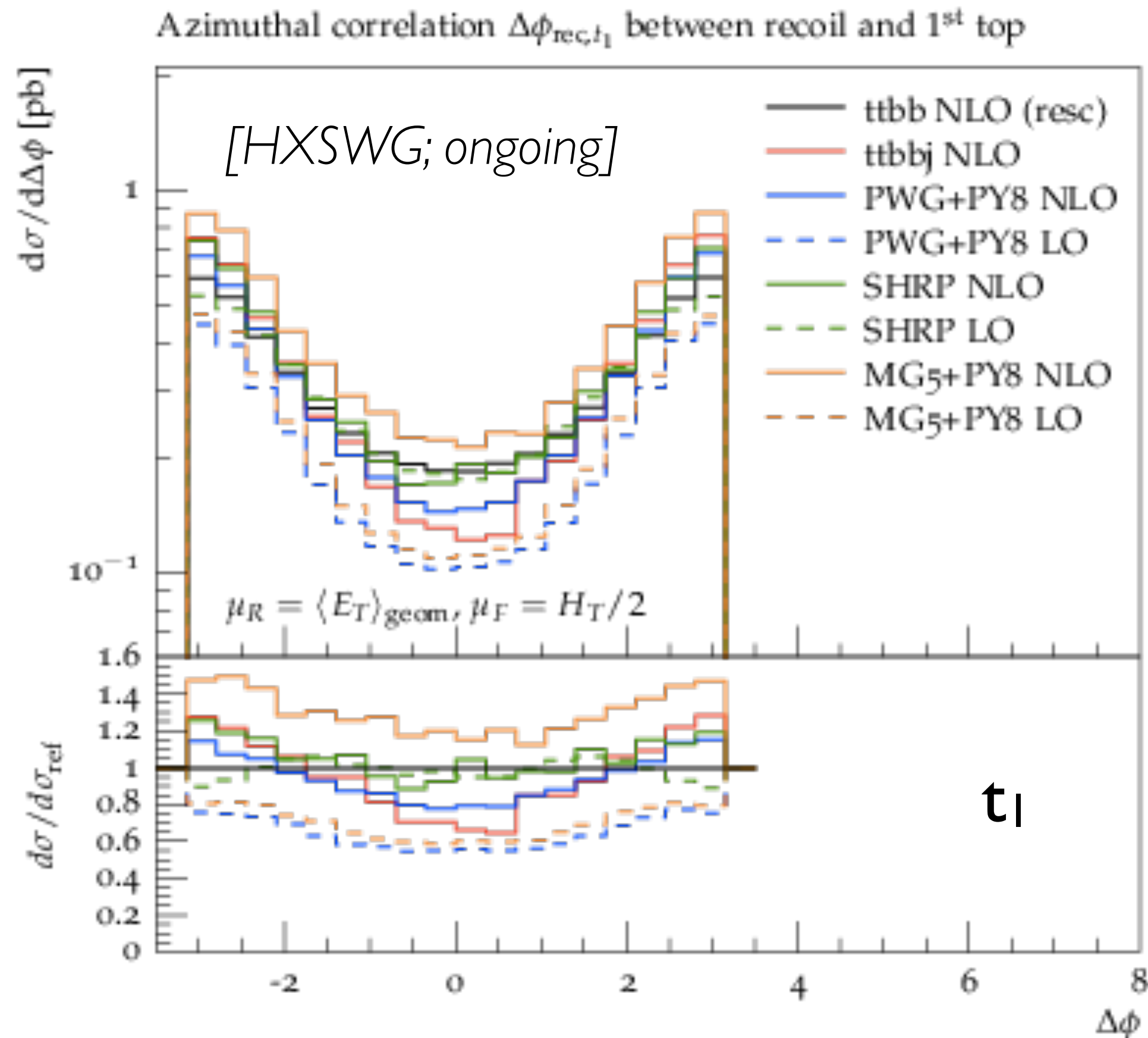
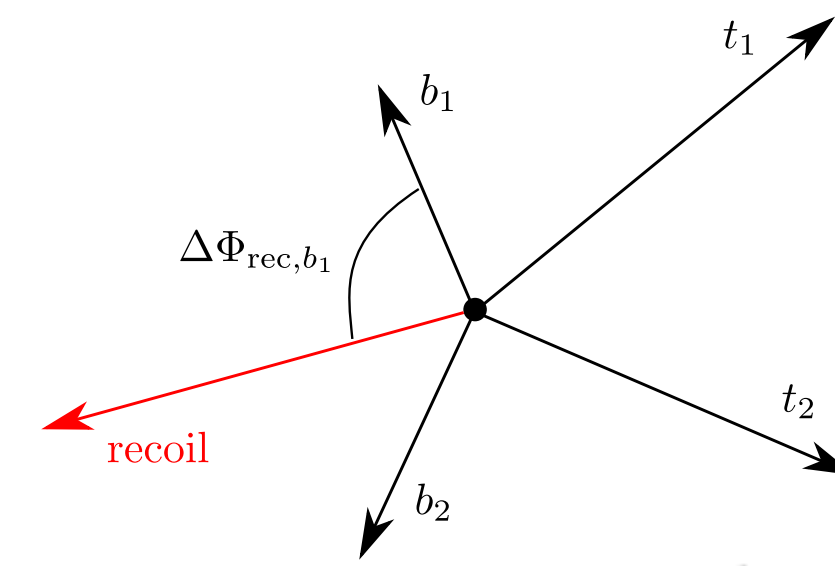


- leading top absorbs **strong recoil** from QCD radiation
- NLOPS enhancement of recoil well consistent with **ttbbj at NLO** (nontrivial!)

[Buccioni, Pozzorini, Zoller, 1907.13624]

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- leading top absorbs **strong recoil** from QCD radiation
- NLOPS enhancement of recoil well consistent with **ttbbj at NLO** (nontrivial!)

[Buccioni, Pozzorini, Zoller, 1907.13624]

- leading bottom gets strong **UNPHYSICAL** recoil in LO+PY8
- unphysical since no evidence of recoil in ttbb, ttbbj, or PWG+PY8 at NLO
- unphysical recoil strongly suppressed only by Powheg / attenuated by MC@NLO matching (MG and Sherpa)

Conclusions

- SM is in excellent shape
- High-precision (Theo + Exp) allows to push limits to unprecedented levels
- NNLO QCD + NLO EW is the new standard: VV, V+jets, dijets, tt, HV, VBF
- Use ratios for theory X exp background improvements
- Explore the unknown: **tail, tails, tails!!**



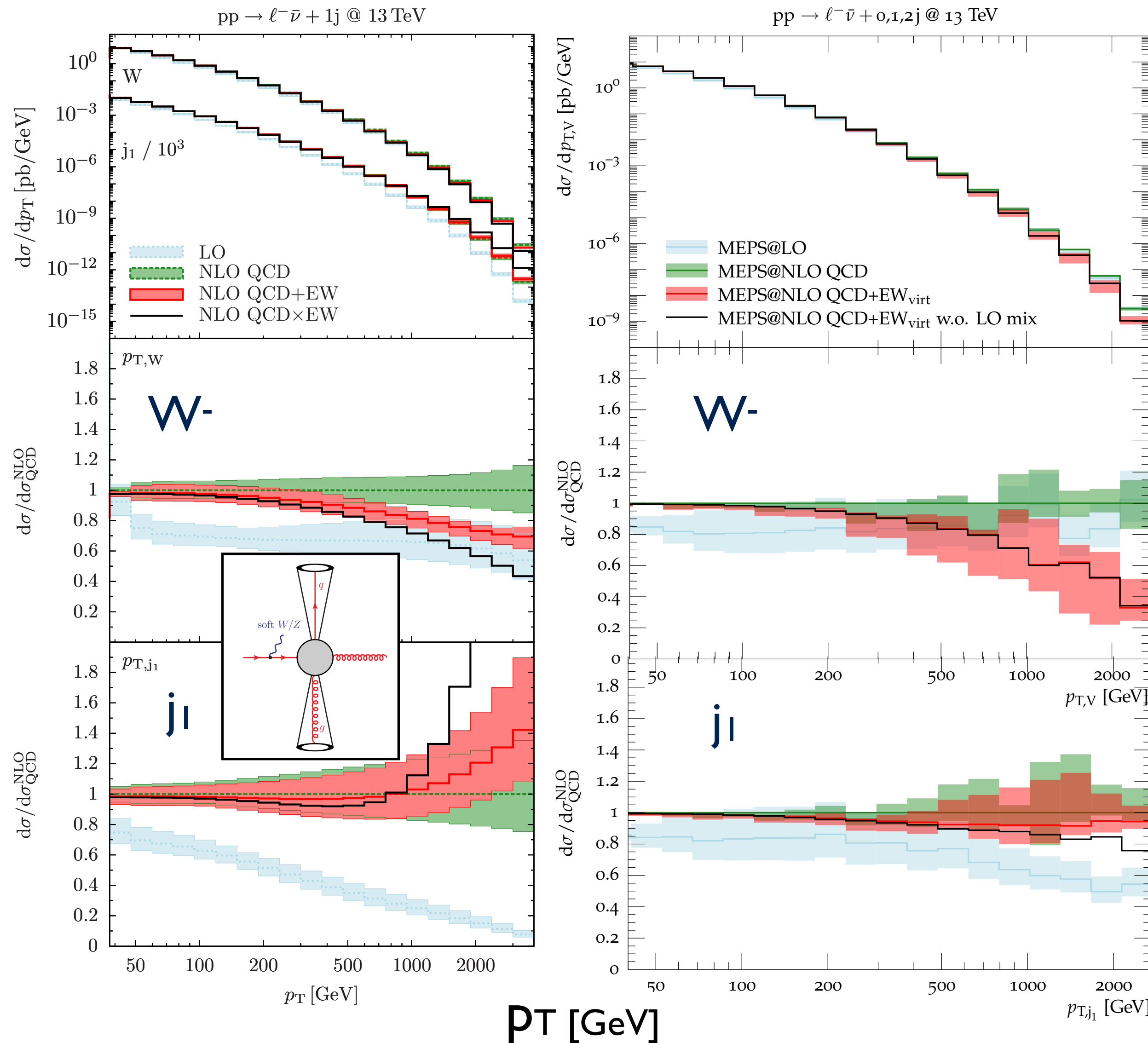
Developments relevant for Run-3 analyses

- NNLO QCD + PS
- PS matching and multi-jet merging @ NLO QCD+EW
- open the NLO PS black boxes
(benchmark against NNLO or NLO multijet computations)
- NNLO QCDxEW & NNLO EW uncertainty estimates

precision for Run-3

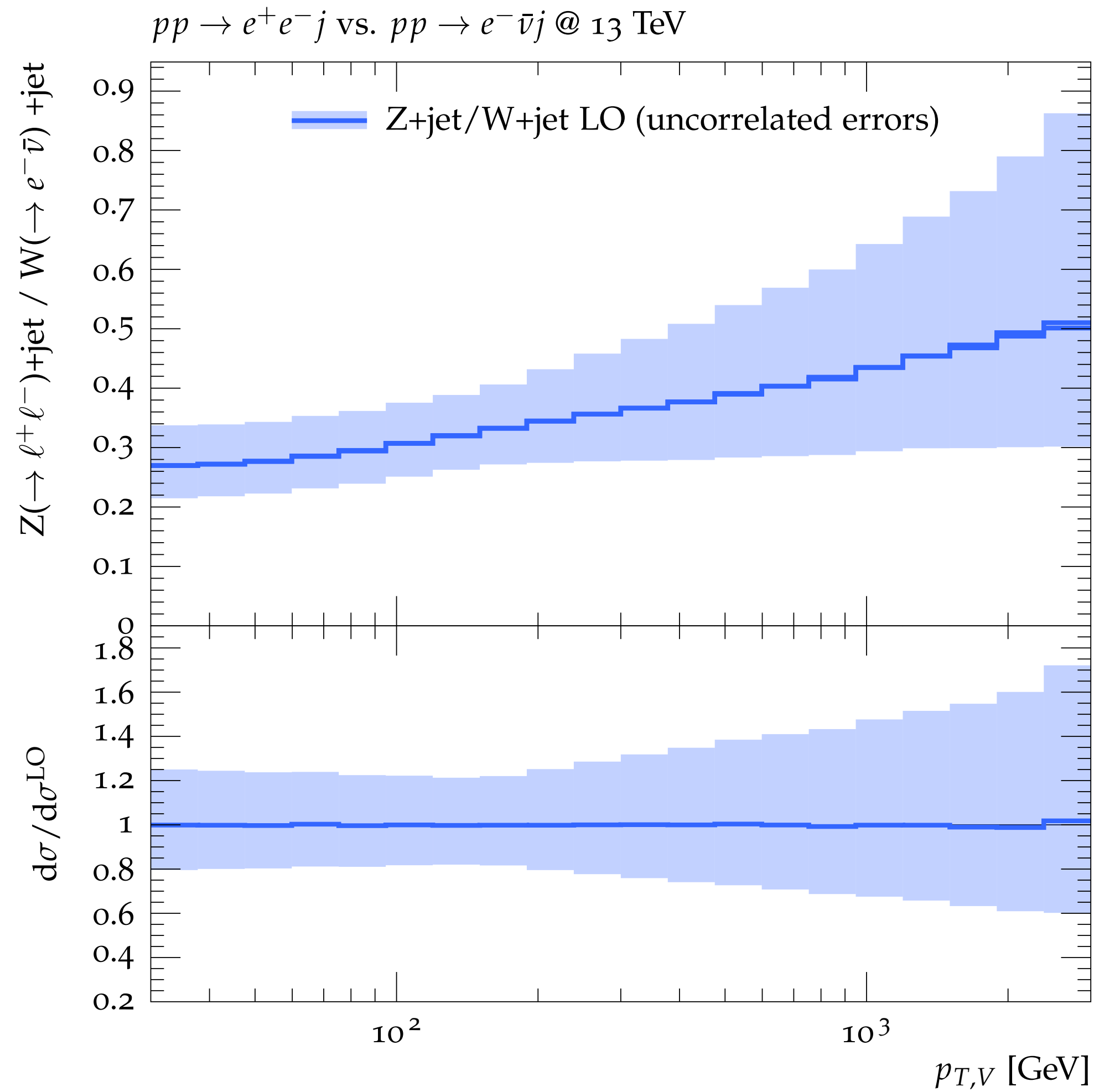
Backup

inclusive V: MEPS@NLO QCD+EW_{virt}



- ▶ Bases on Sherpa's standard MEPS@NLO
- ▶ Stable NLO QCD+EW predictions in all of the phase-space...
- ▶ ...including Parton-Shower effects.
- ▶ Can directly be used by the experimental collaborations
- ▶ $p_{T,V}$: MEPS@NLO QCD+EW in agreement with QCD \times EW (fixed-order)
- ▶ p_{T,j_1} :
 - merging ensures stable results (dijet topology at LO)
 - compensation between negative Sudakov and LO mix

How to correlate QCD uncertainties across processes?



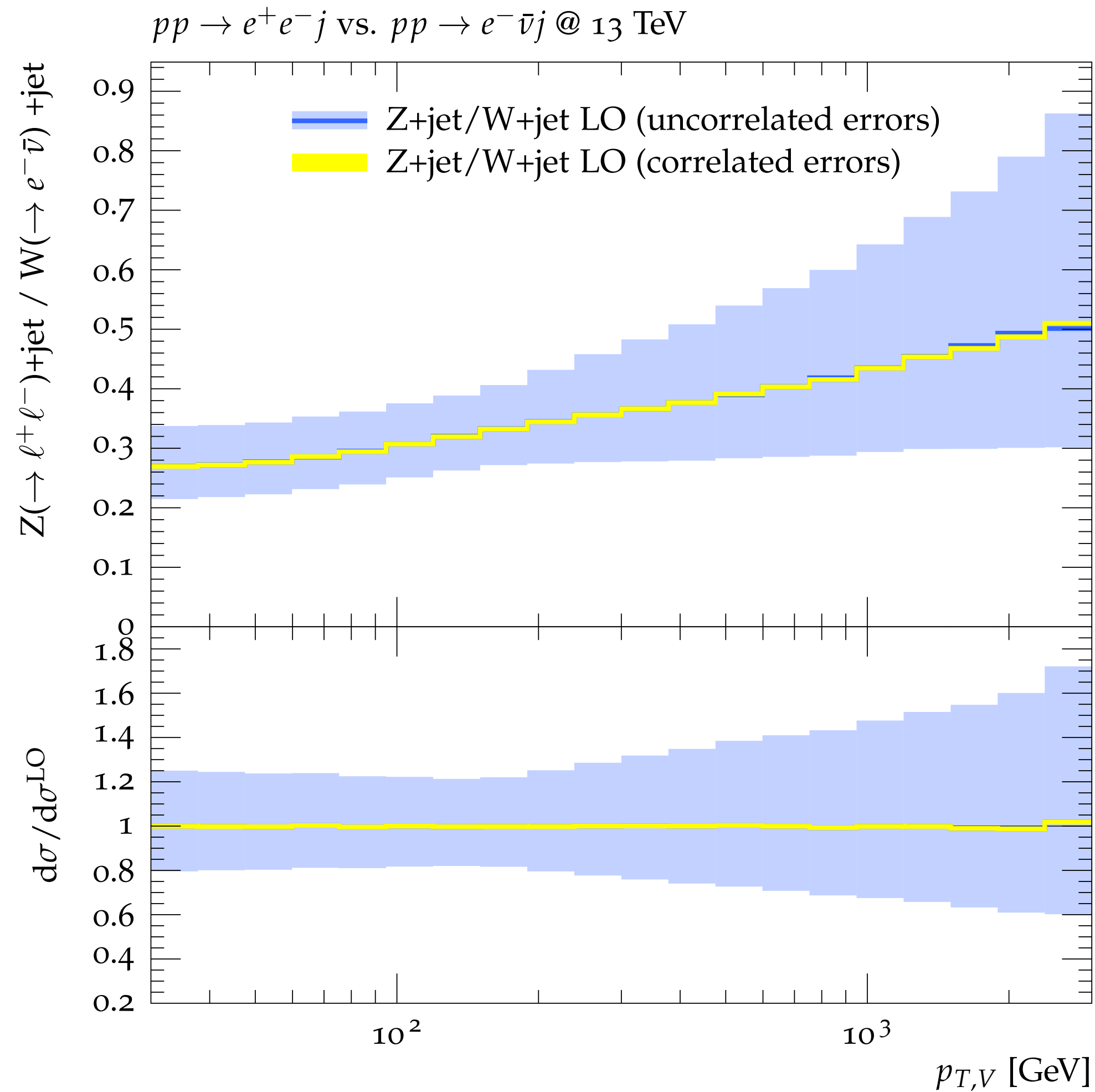
consider Z+jet / W+jet $p_{T,V}$ -ratio @ LO

uncorrelated treatment yields

O(40%) uncertainties

How to correlate QCD uncertainties across processes?

[1705.04664]



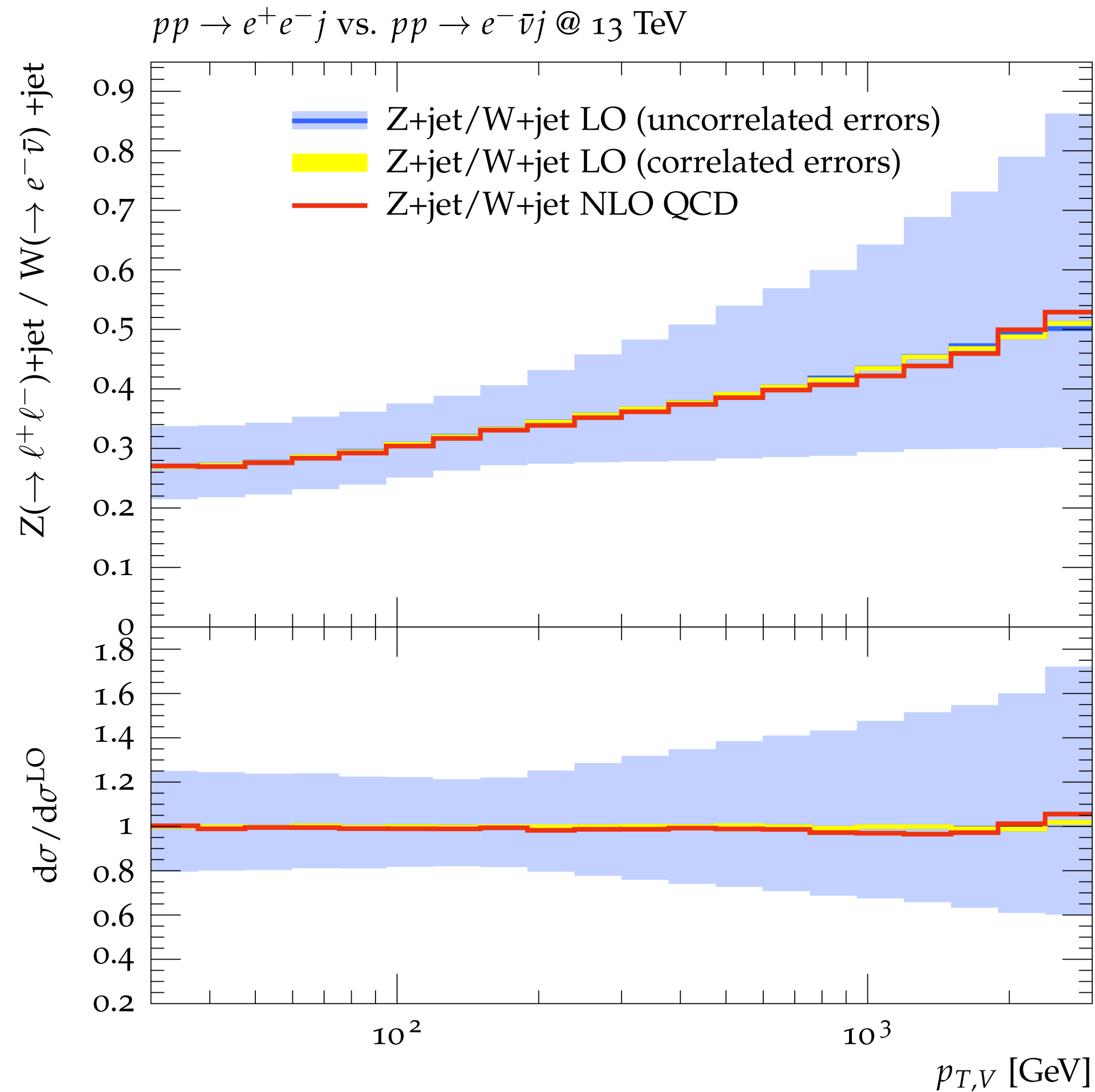
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uncorrelated treatment yields
 $O(40\%)$ uncertainties

correlated treatment yields tiny
 $O(<\sim 1\%)$ uncertainties

How to correlate QCD uncertainties across processes?

[1705.04664]



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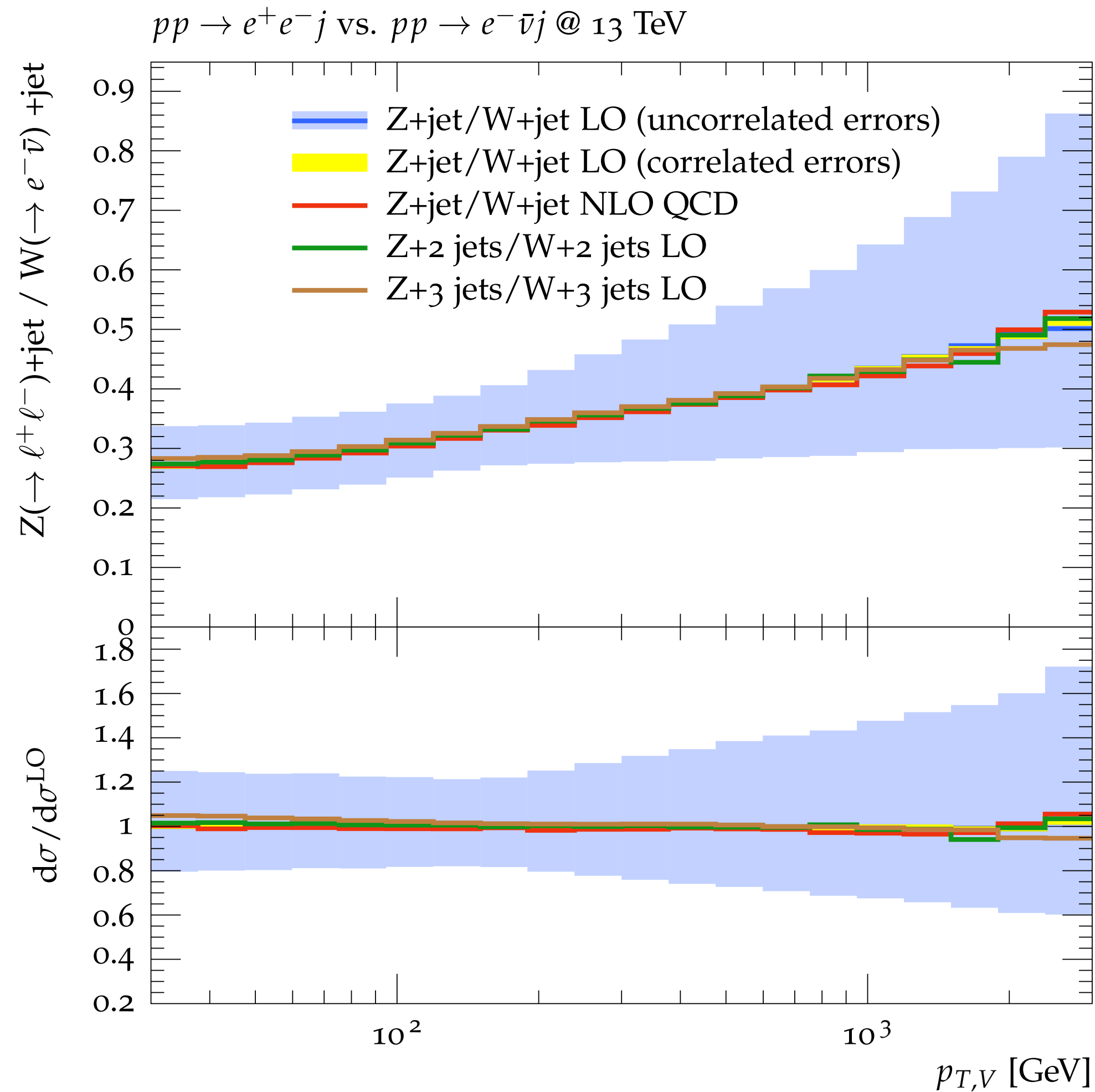
check against NLO QCD!

NLO QCD corrections remarkably flat
in Z+jet / W+jet ratio!

→ supports correlated treatment of
uncertainties!

How to correlate QCD uncertainties across processes?

[1705.04664]



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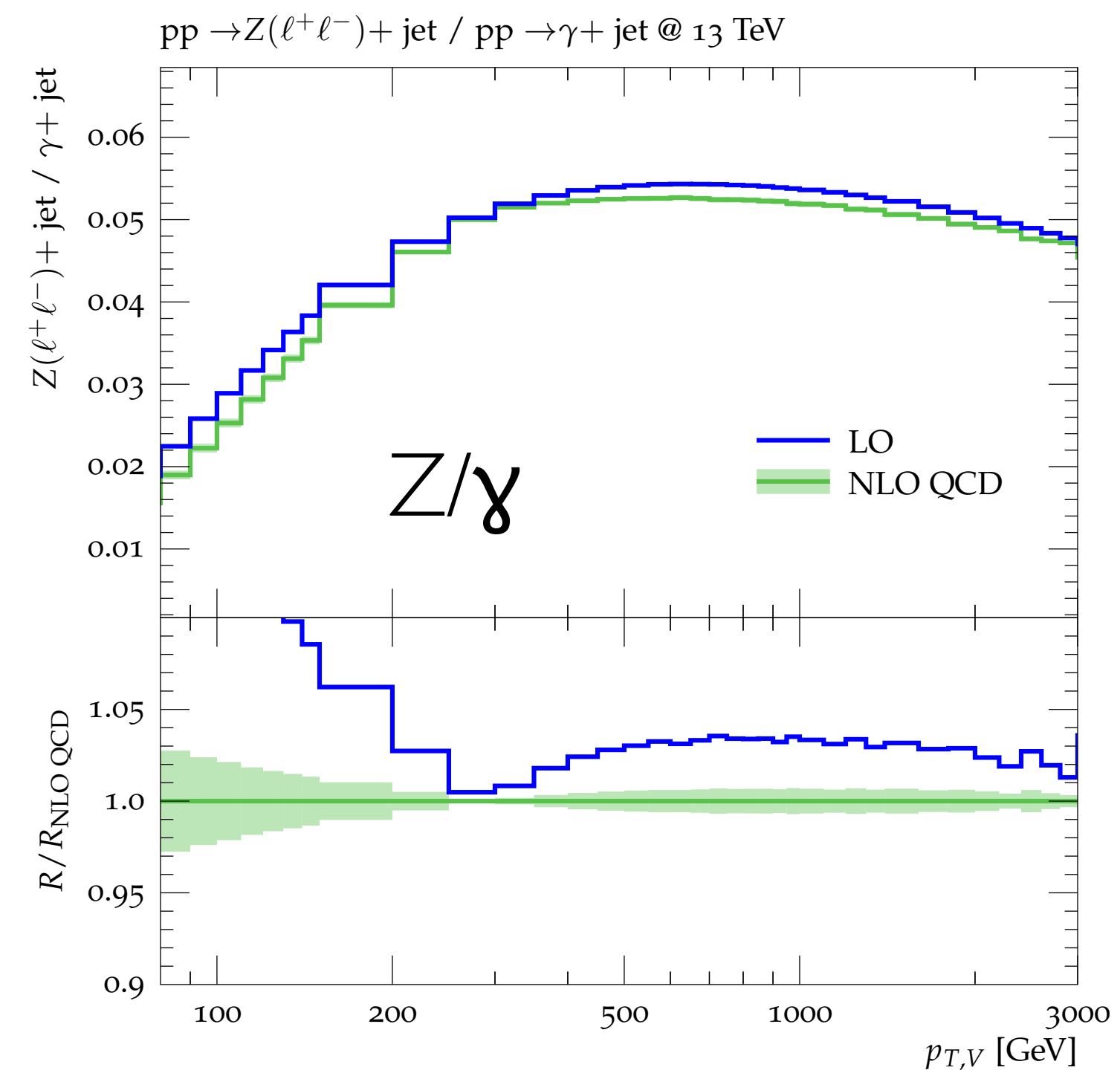
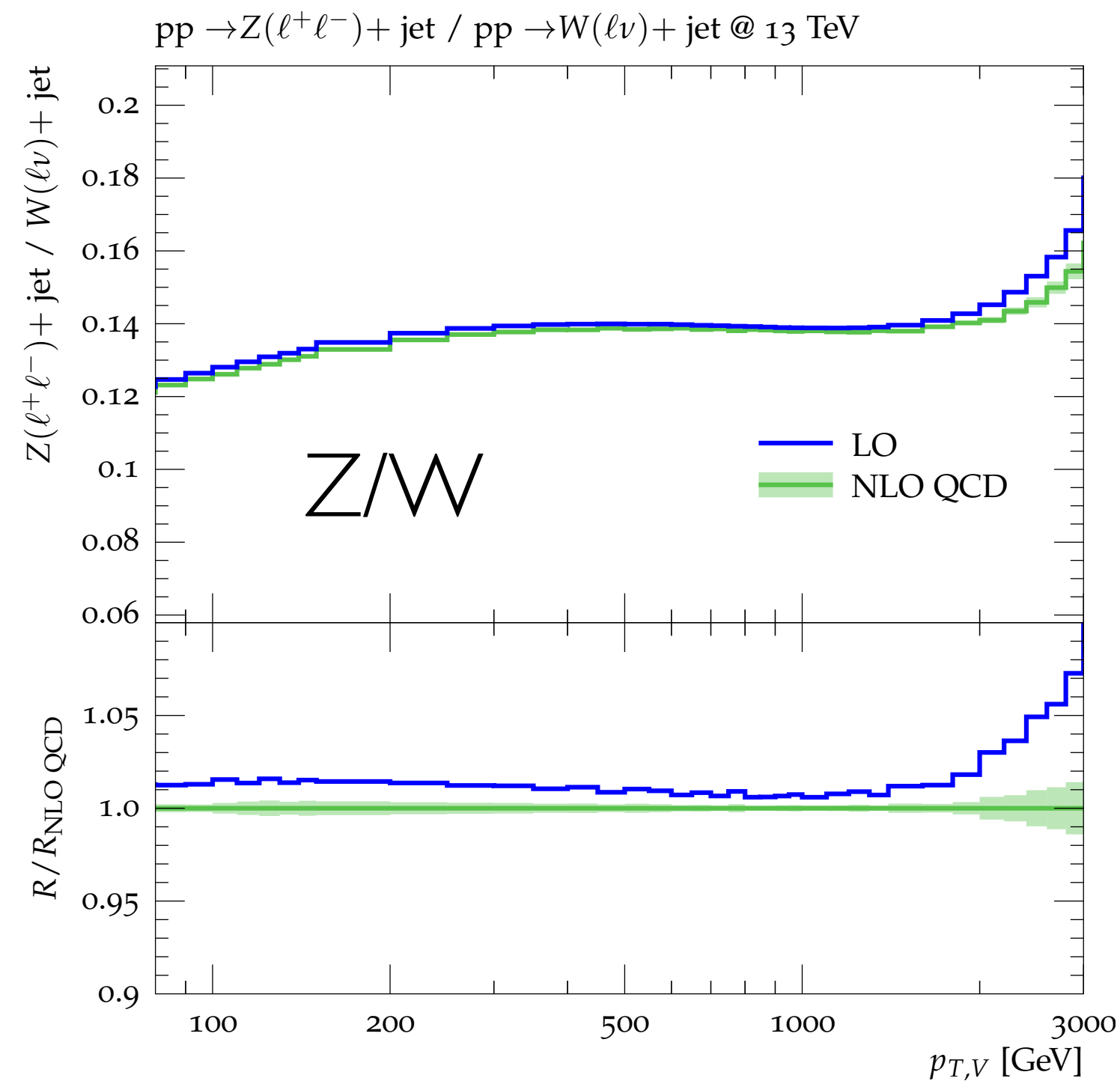
Also holds for higher jet-multiplicities

→ indication of correlation also in higher-order corrections beyond NLO!

QCD uncertainties: ratios

How to correlate these uncertainties across processes?

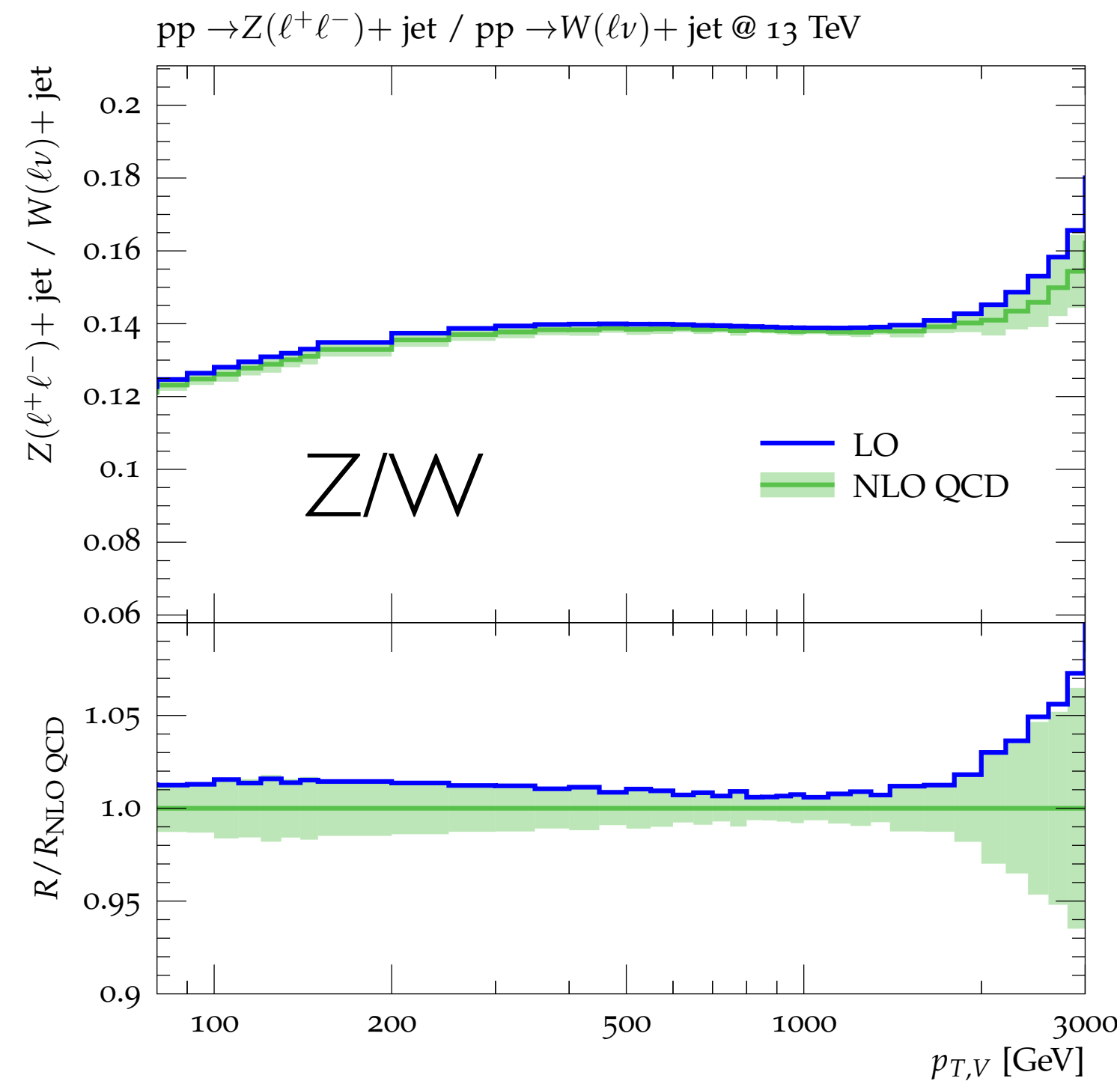
- take scale uncertainties as fully correlated:
NLO QCD uncertainties cancel at the $< \sim 1\%$ level



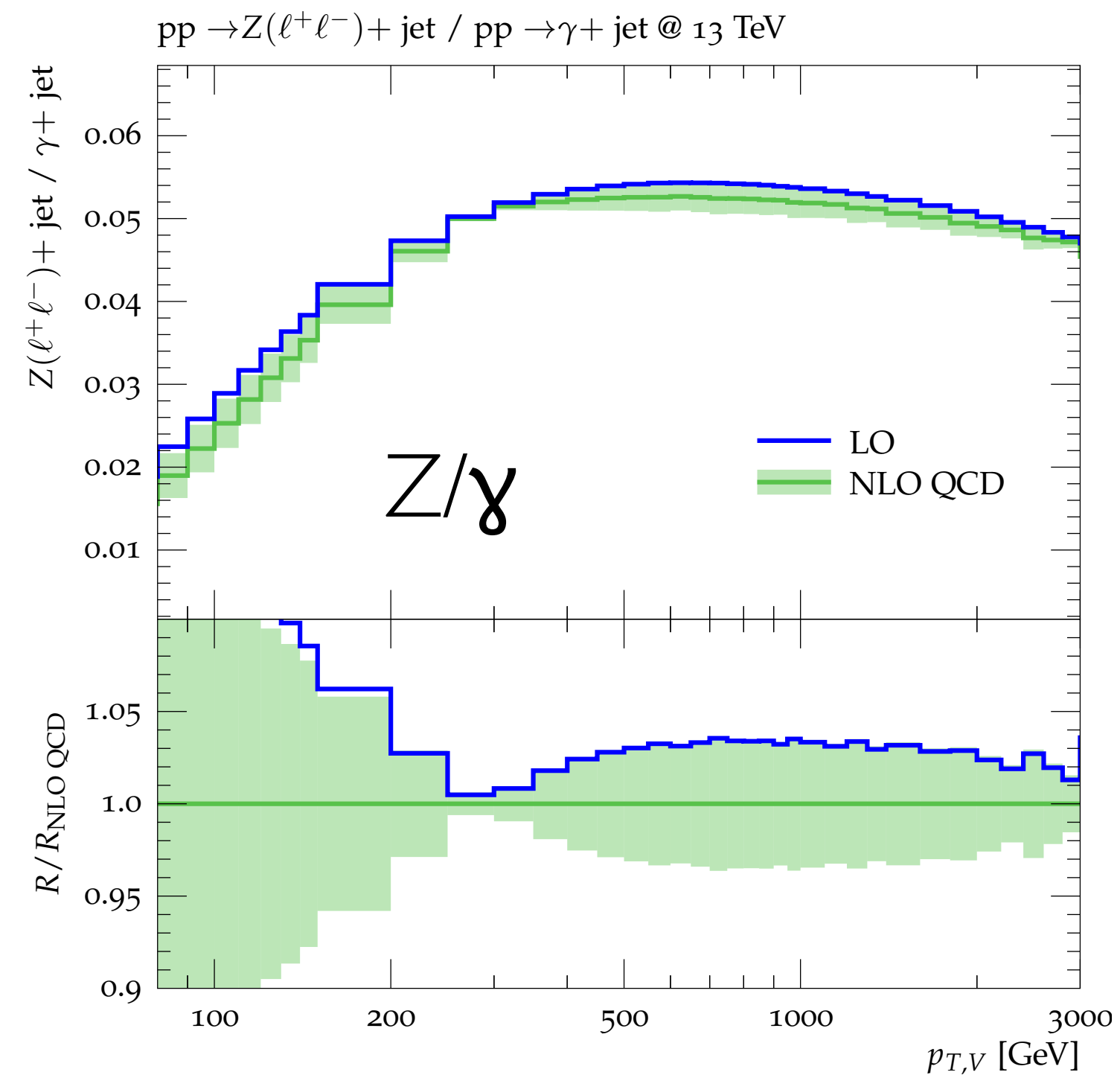
QCD uncertainties: ratios

How to correlate these uncertainties across processes?

- take scale uncertainties as fully correlated:
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- introduce **process correlation uncertainty** based on K-factor difference: $\delta K_{\text{NLO}} = K_{\text{NLO}}^V - K_{\text{NLO}}^Z$
→ effectively degrades precision of last calculated order



$\delta < 2\%$

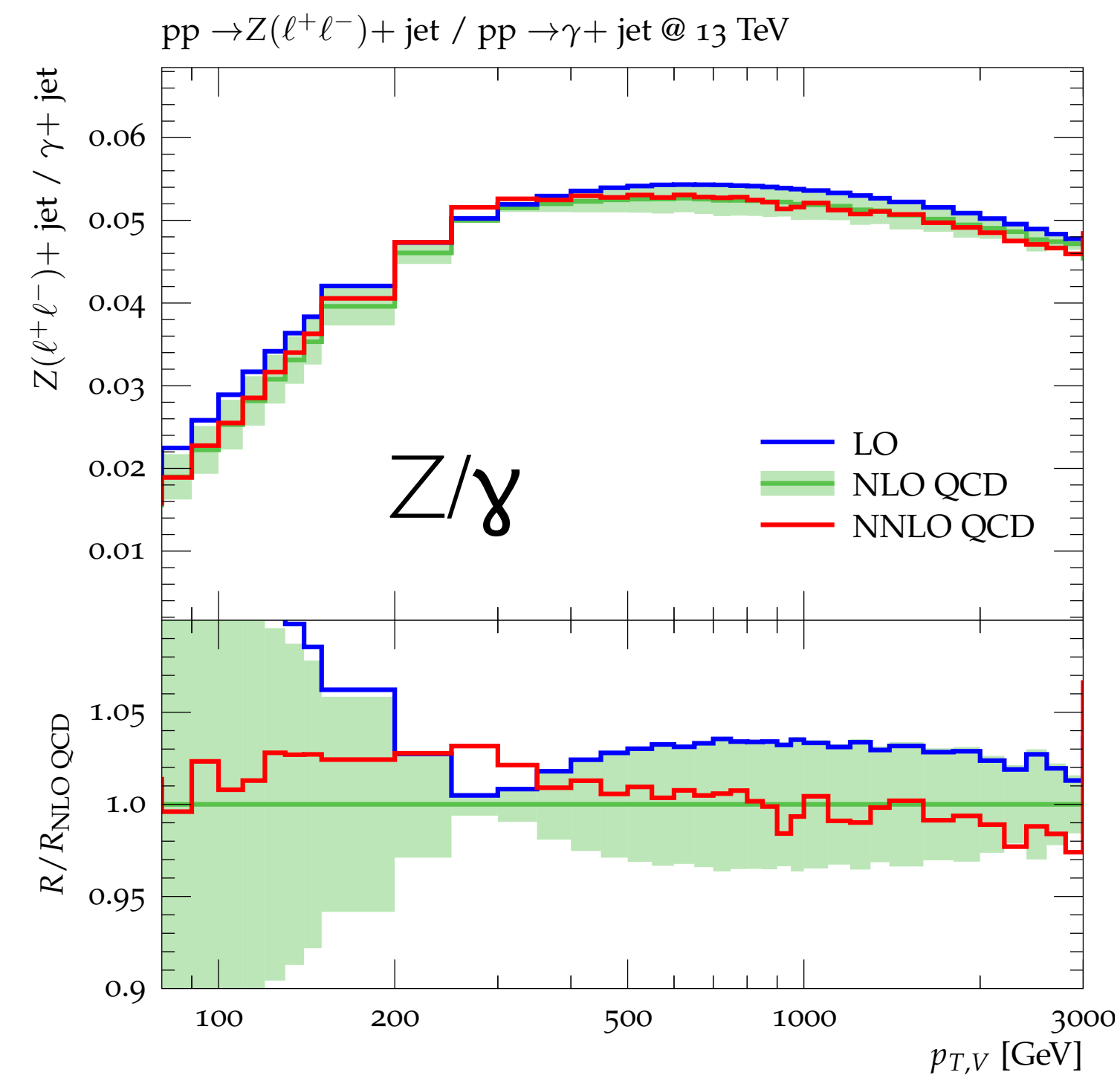
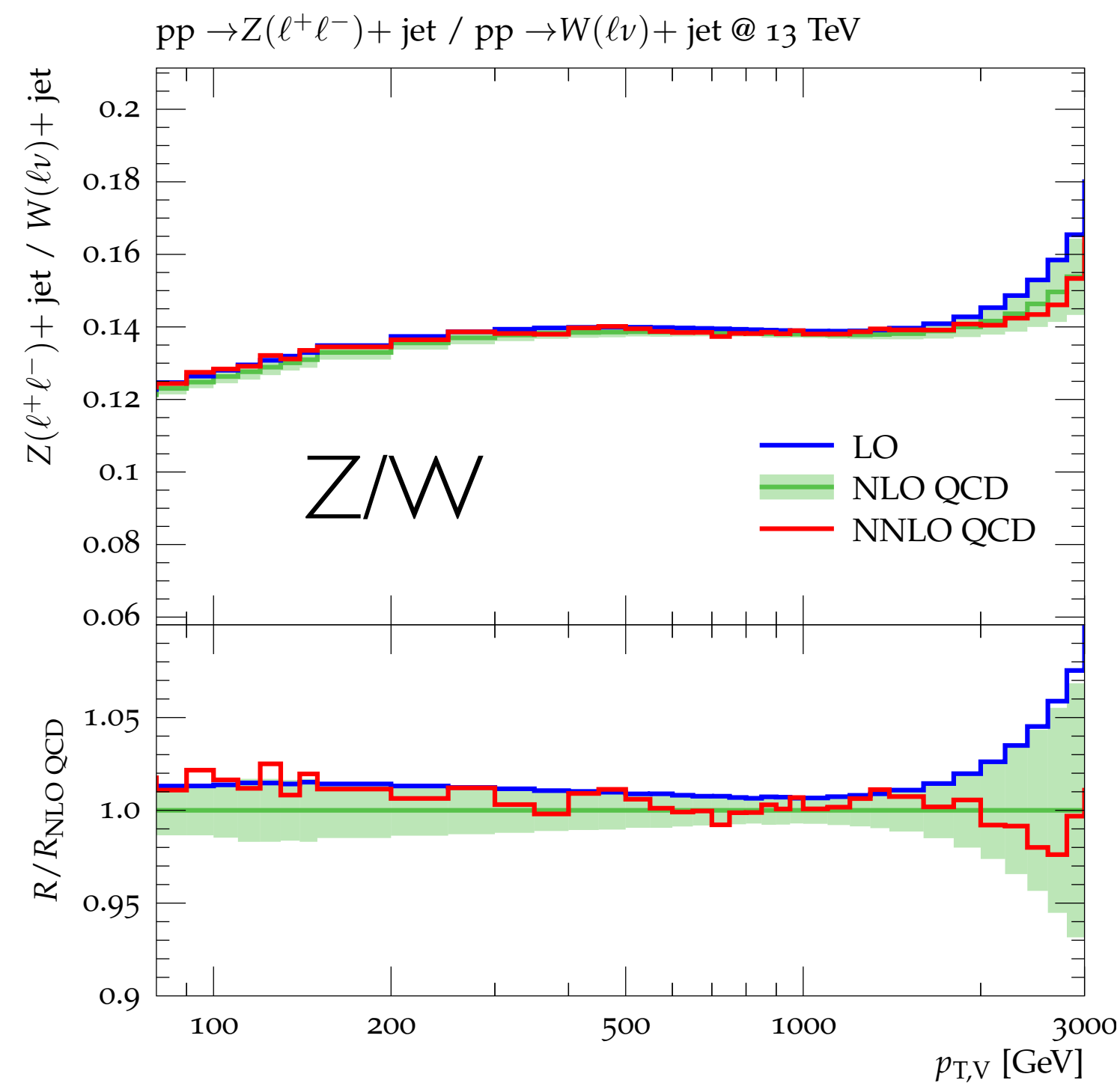


$\delta < 3-4\%$

QCD uncertainties: ratios

How to correlate these uncertainties across processes?

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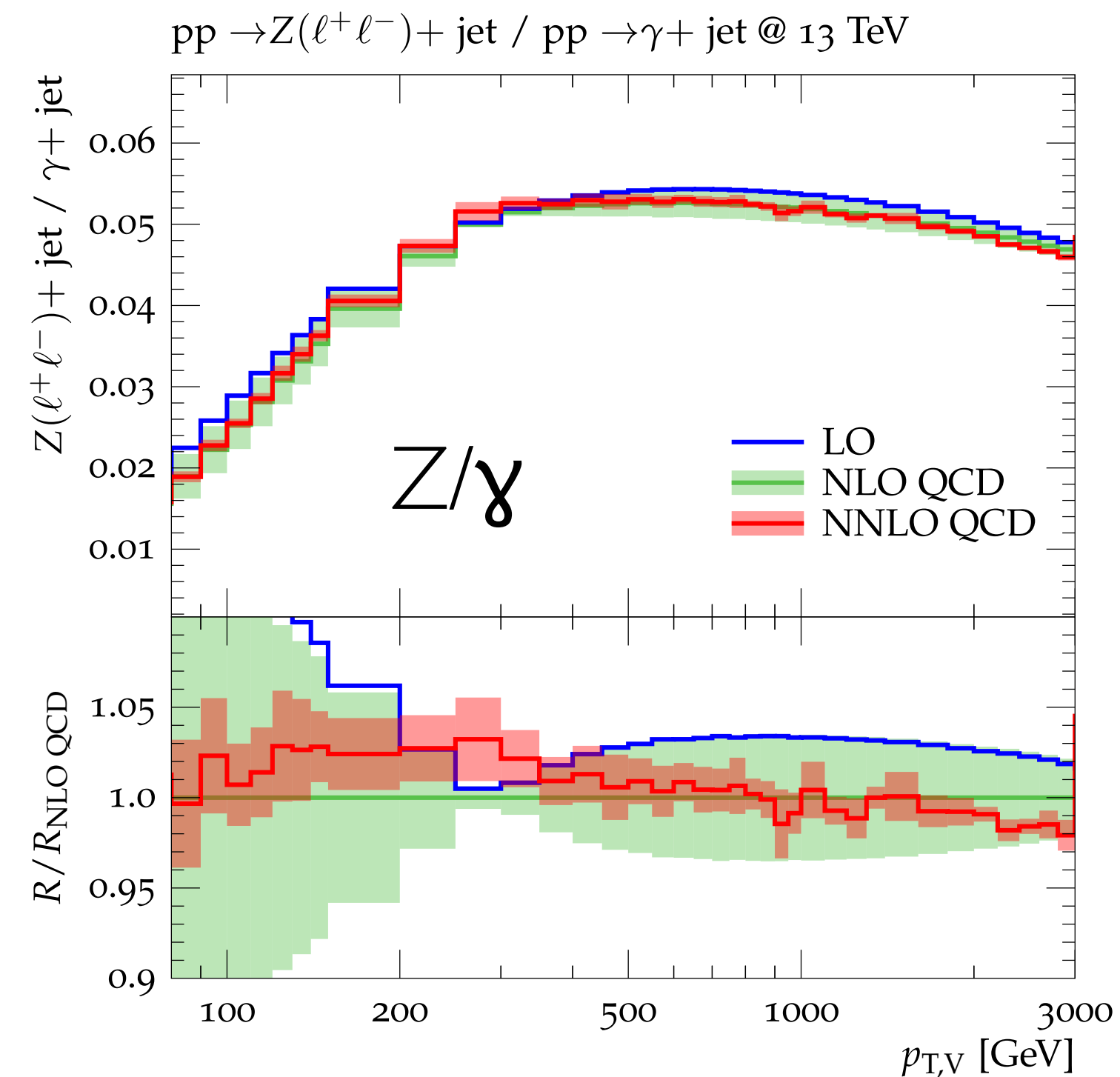
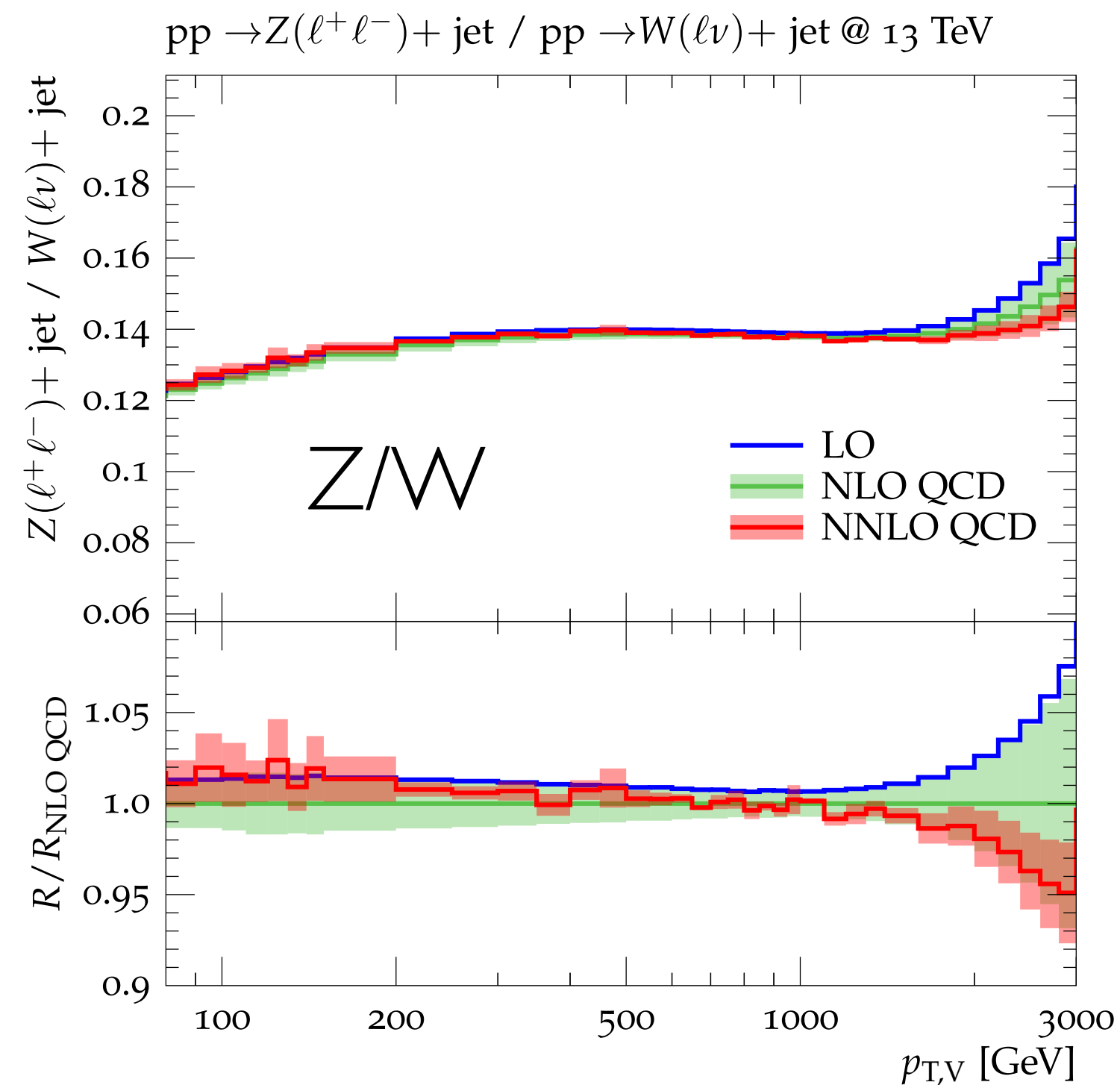


check against NNLO QCD!

QCD uncertainties: ratios

How to correlate these uncertainties across processes?

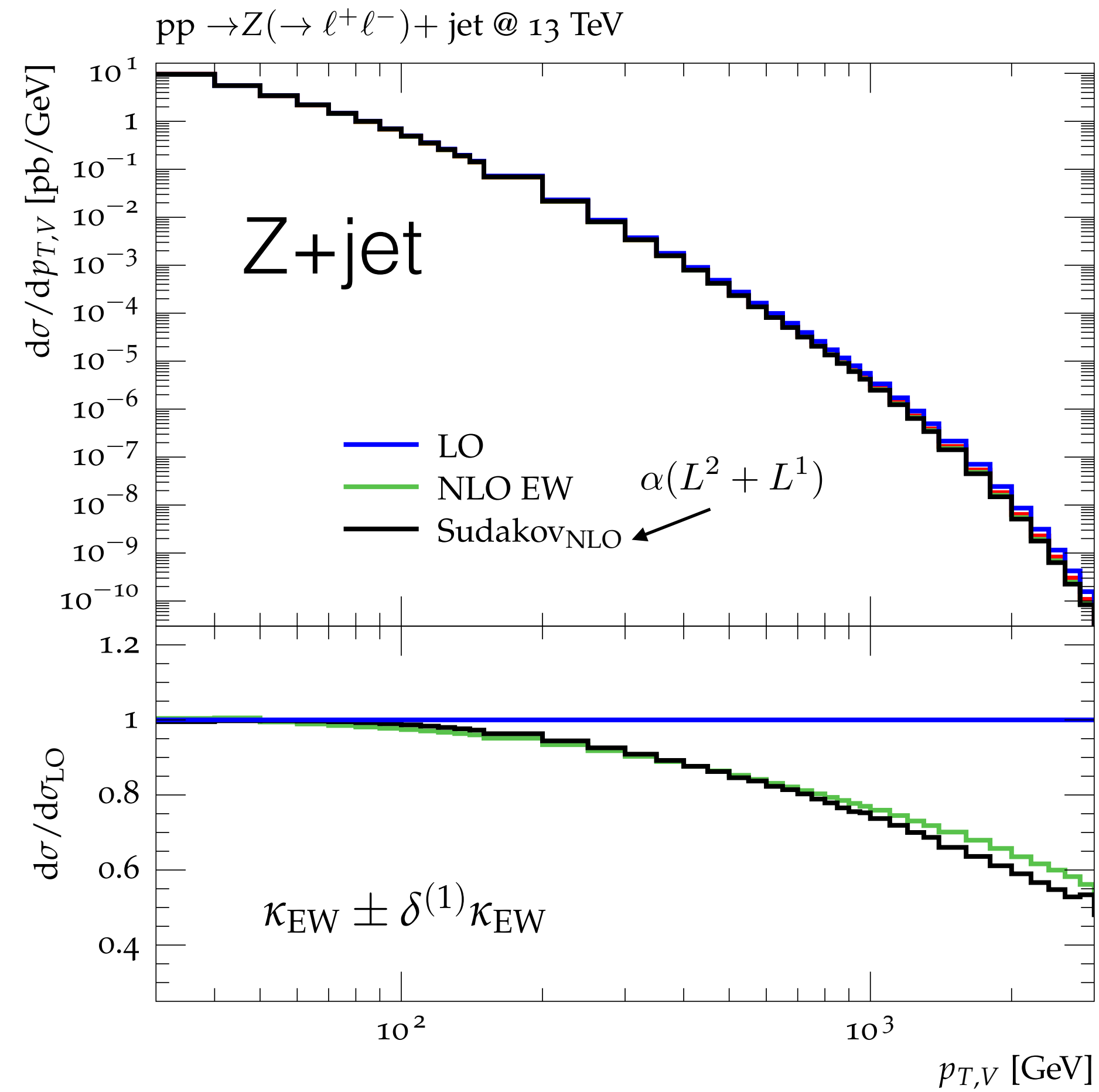
- take scale uncertainties as fully correlated:
NLO QCD uncertainties cancel at the $< \sim 1\%$ level
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→ effectively degrades precision of last calculated order



Uncertainty estimates at NNLO QCD

Pure EW uncertainties

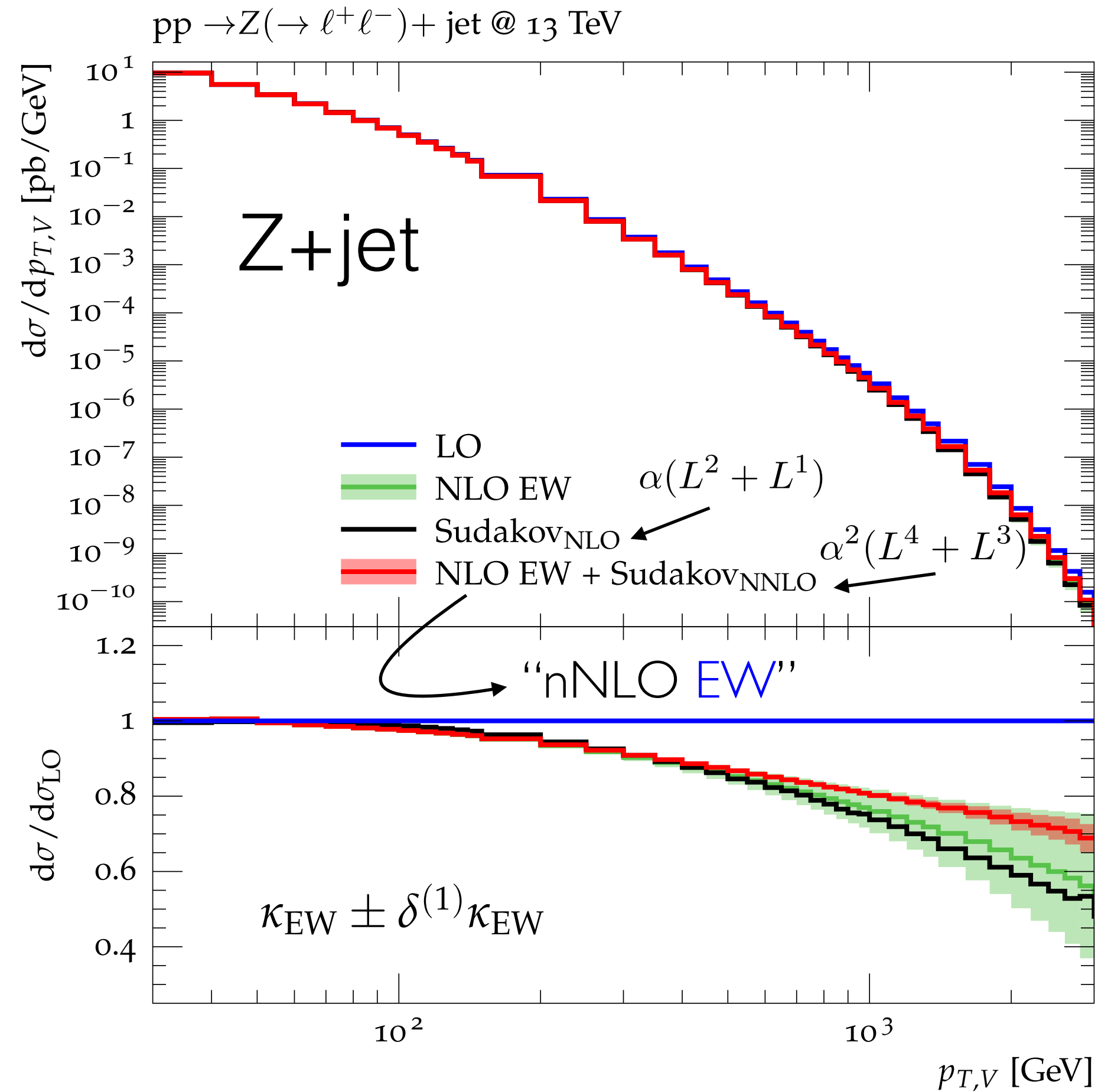
[JML et. al.: 1705.04664]



Large EW corrections dominated by Sudakov logs

Pure EW uncertainties

[JML et. al.: 1705.04664]



Large EW corrections dominated by Sudakov logs



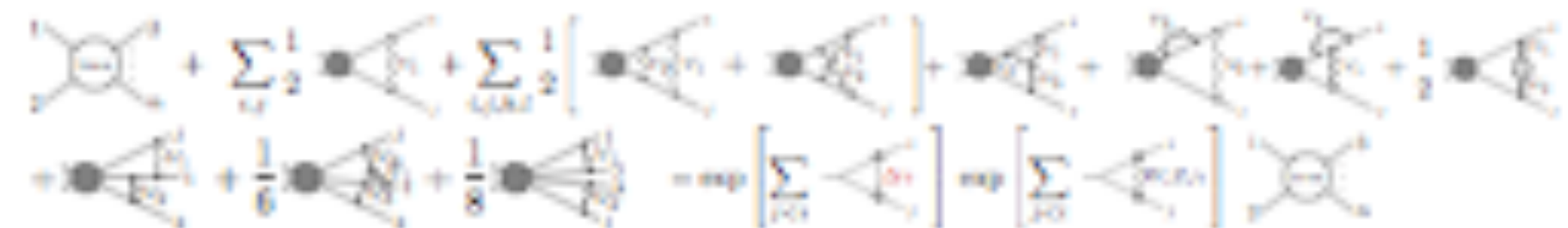
Uncertainty estimate of (N)NLO EW from naive exponentiation × 2:

$$\delta^{(1)} \kappa_{EW} \simeq \frac{2}{k!} \left(\kappa_{NLO,EW} \right)^k \quad (\text{correlated})$$



check against two-loop Sudakov logs

[Kühn, Kulesza, Pozzorini, Schulze; 05-07]

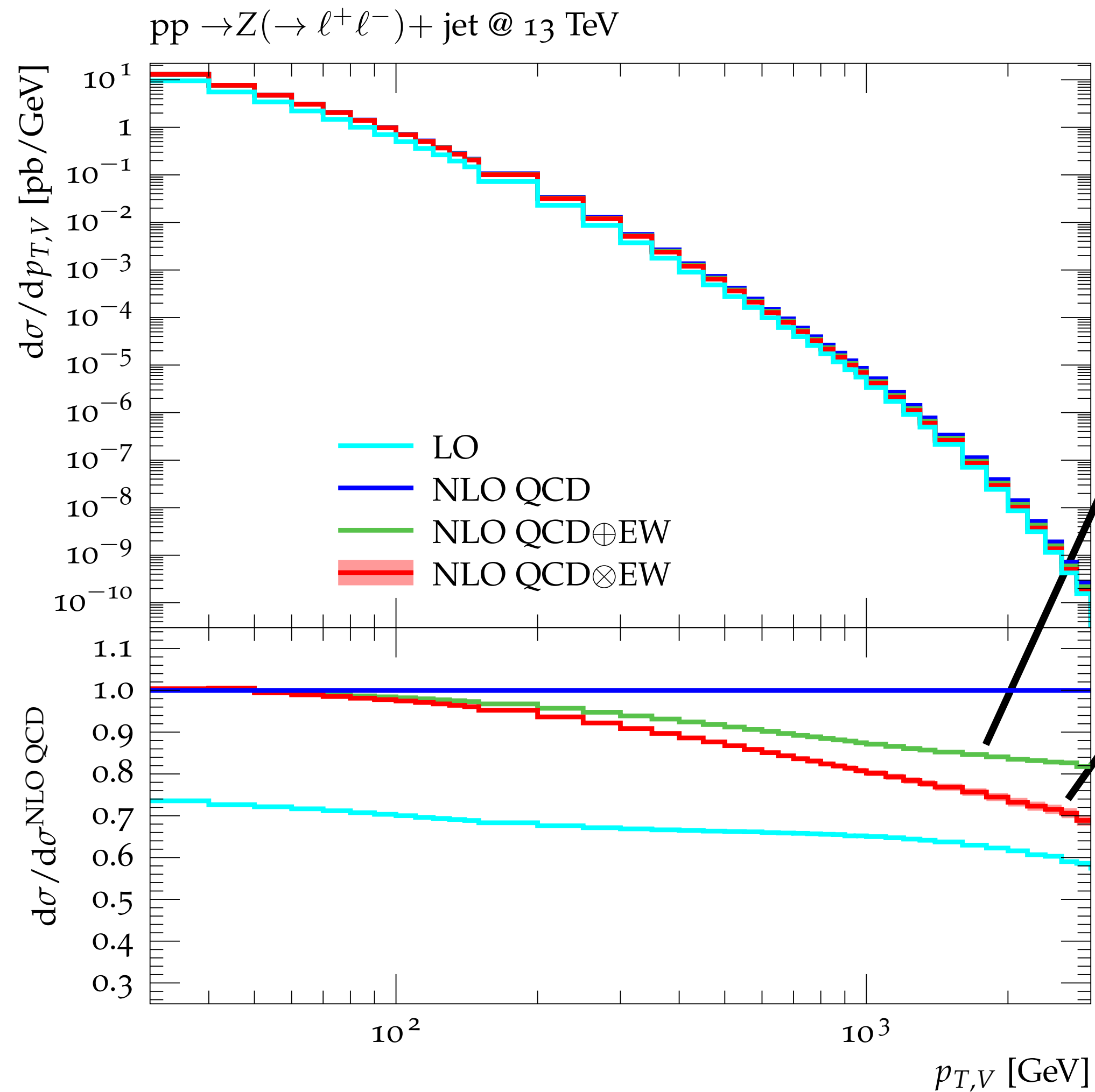


$$\kappa_{NLO\ EW}(\hat{s}, \hat{t}) = \frac{\alpha}{\pi} \left[\delta_{\text{hard}}^{(1)} + \delta_{\text{Sud}}^{(1)} \right]$$

$$\kappa_{NNLO\ Sud}(\hat{s}, \hat{t}) = \left(\frac{\alpha}{\pi} \right)^2 \delta_{\text{Sud}}^{(2)}$$

+ additional uncertainties for hard non-log NNLO EW effects (uncorrelated)

Mixed QCD-EW uncertainties



Given QCD and EW corrections are sizeable, also mixed QCD-EW uncertainties of relative $\mathcal{O}(\alpha\alpha_s)$ have to be considered.

Additive combination

$$\sigma_{\text{QCD+EW}}^{\text{NLO}} = \sigma^{\text{LO}} + \delta\sigma_{\text{QCD}}^{\text{NLO}} + \delta\sigma_{\text{EW}}^{\text{NLO}}$$

(no $\mathcal{O}(\alpha\alpha_s)$ contributions)

Multiplicative combination

$$\sigma_{\text{QCD}\times\text{EW}}^{\text{NLO}} = \sigma_{\text{QCD}}^{\text{NLO}} \left(1 + \frac{\delta\sigma_{\text{EW}}^{\text{NLO}}}{\sigma^{\text{LO}}} \right)$$

(try to capture some $\mathcal{O}(\alpha\alpha_s)$ contributions, e.g. EW Sudakov logs \times soft QCD)

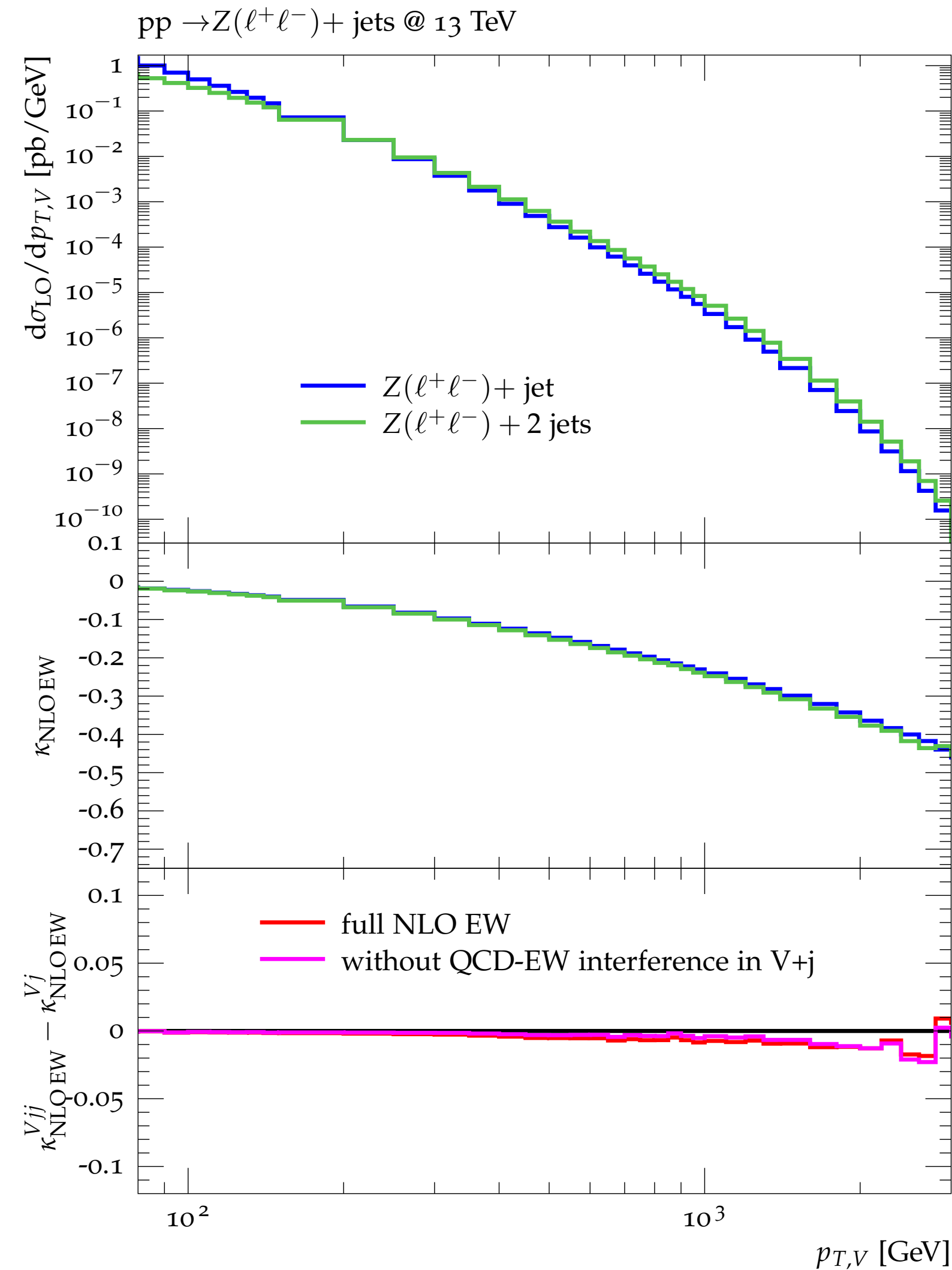
Difference between these two approaches indicates size of missing mixed EW-QCD corrections.

$$K_{\text{QCD}\otimes\text{EW}} - K_{\text{QCD}\oplus\text{EW}} \sim 10\% \quad \text{at 1 TeV}$$

Too conservative!?

For dominant Sudakov EW logarithms factorization should be exact!

Mixed QCD-EW uncertainties



Bold estimate:

Consider real $\mathcal{O}(\alpha\alpha_s)$ correction to V+jet

\simeq NLO EW to V+2jets

and we observe

$$\left. \frac{d\sigma_{\text{NLOEW}}}{d\sigma_{\text{LO}}} \right|_{V+2\text{jet}} - \left. \frac{d\sigma_{\text{NLOEW}}}{d\sigma_{\text{LO}}} \right|_{V+1\text{jet}} \lesssim 1\%$$

strong support for

- factorization
- multiplicative QCD \times EW combination

Estimate of non-factorising contributions

(correlated)

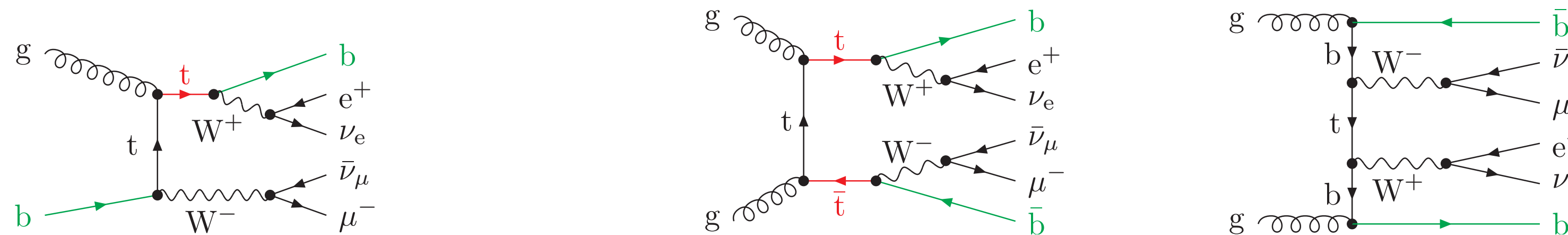
$$\delta K_{\text{mix}}^{(V)}(x) = 0.1 \left[K_{\text{TH},\oplus}^{(V)}(x, \vec{\mu}_0) - K_{\text{TH},\otimes}^{(V)}(x, \vec{\mu}_0) \right]$$

(tuned to cover above difference of EW K-factors)

Top-free W^+W^- definitions

Huge Wt and $t\bar{t}$ contamination from $\overbrace{W^+W^-b}^{+40\% \text{ NLO}}$ and $\overbrace{W^+W^-b\bar{b}}^{+400\% \text{ NNLO}}$

- intimately connected with W^+W^- through $g \rightarrow b\bar{b}$ singularities
- **top subtraction** tricky and not unique \Rightarrow **theoretical ambiguity in $\sigma_{WW}^{(N)\text{NLO}}$!**



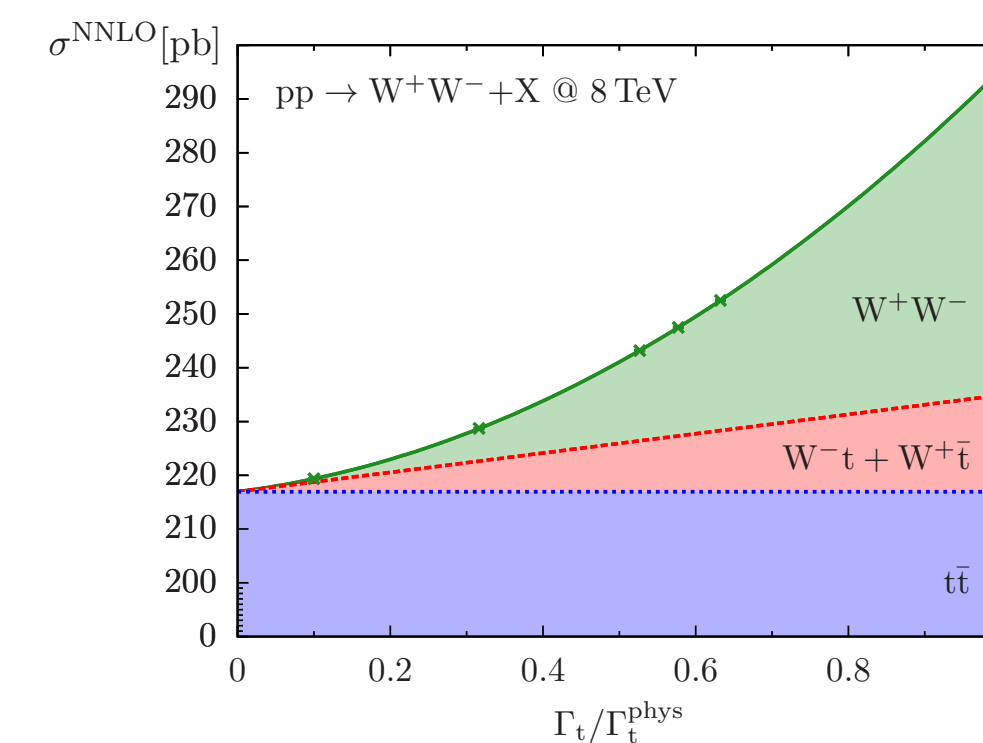
Definition A: veto b -quark emissions in 4F scheme ($m_b > 0$)

- $\Rightarrow \ln(m_b/M_W)$ terms **might jeopardize NNLO accuracy!**

Definition B: top-resonance fit in 5F-scheme ($m_b = 0$)

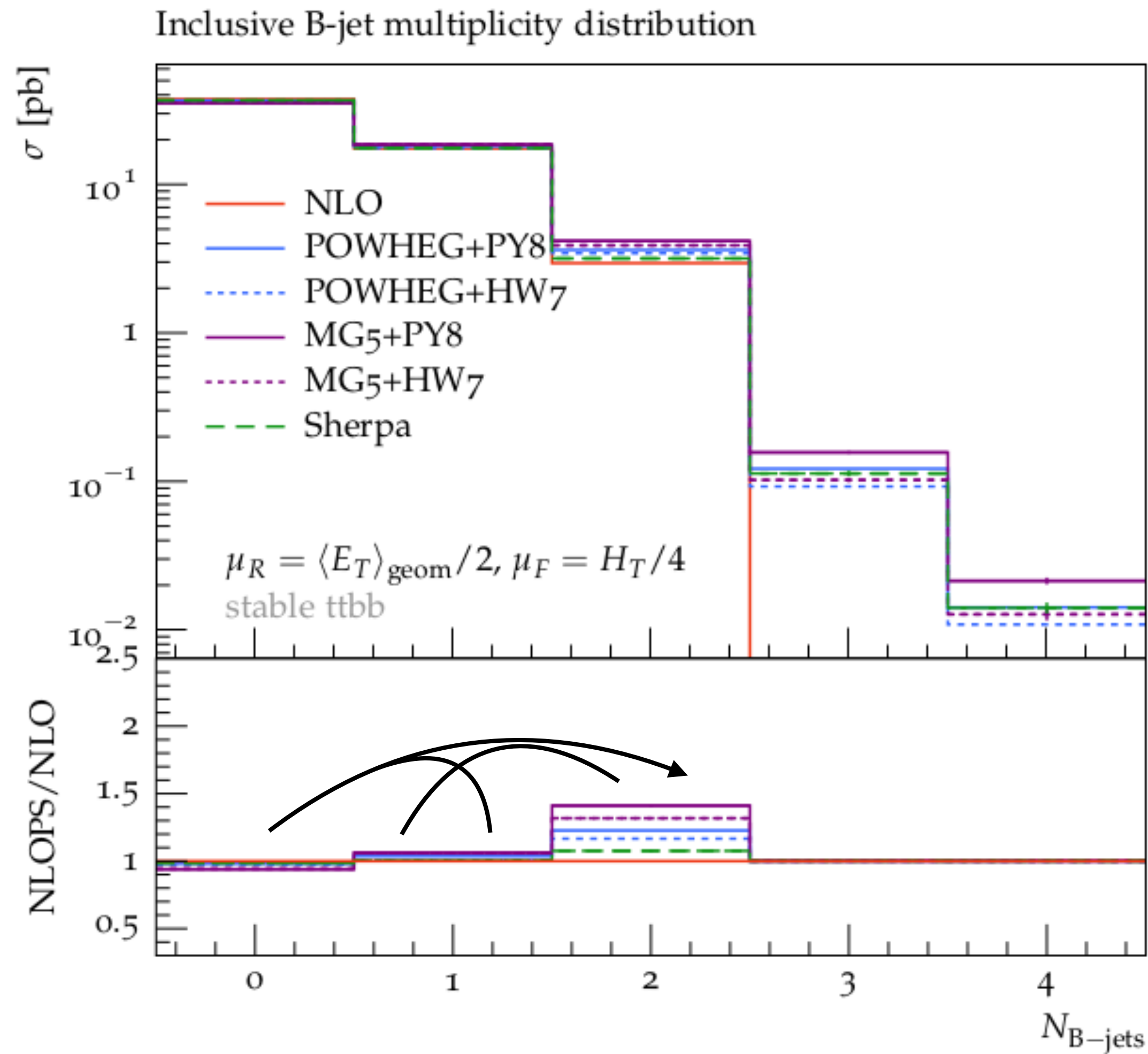
$$\lim_{\xi_t \rightarrow 0} \sigma_{\text{full}}^{5\text{F}}(\xi_t \Gamma_t) = \xi_t^{-2} \left[\sigma_{t\bar{t}}^{5\text{F}} + \xi_t \sigma_{Wt}^{5\text{F}} + \xi_t^2 \sigma_{W^+W^-}^{5\text{F}} \right]$$

\Rightarrow **for inclusive $\sigma_{WW}^{\text{NNLO}}$ only 1–2% ambiguity (A vs B)**



Relevant issue for percent-precision tests of W^+W^- physics! ... Relation to σ_{WW}^{EXP} ?

Origin of these differences



- origin: different shower-induced bins migrations across b-jets cuts

anti- k_t , $R = 0.4$

cuts: $p_T > 25$ GeV, $\eta < 2.5$