

High-precision measurement of the HFS of $^3\text{He}^+$ in a Penning trap

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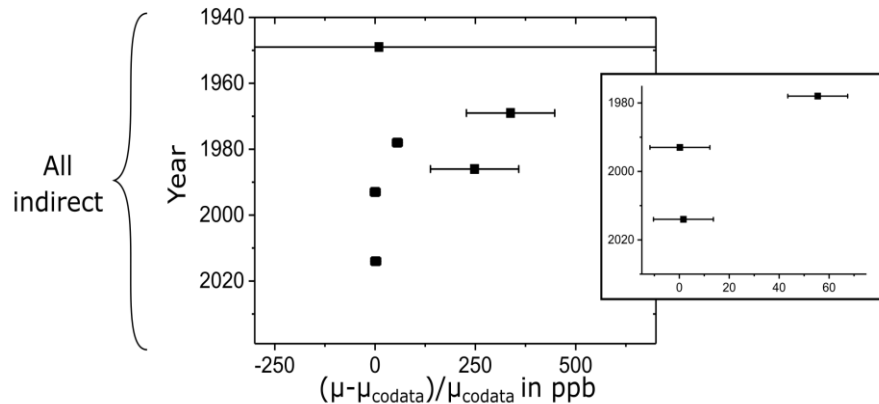


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Motivation

First direct high-precision measurement of ^3He nuclear magnetic moment with ppb precision



Previous measurements:

- Comparisons of ^3He and H_2O or H_2 probe only
- μ_{He} known to $1.2 \cdot 10^{-8}$ only
limited by knowledge of shielded proton magnetic moment

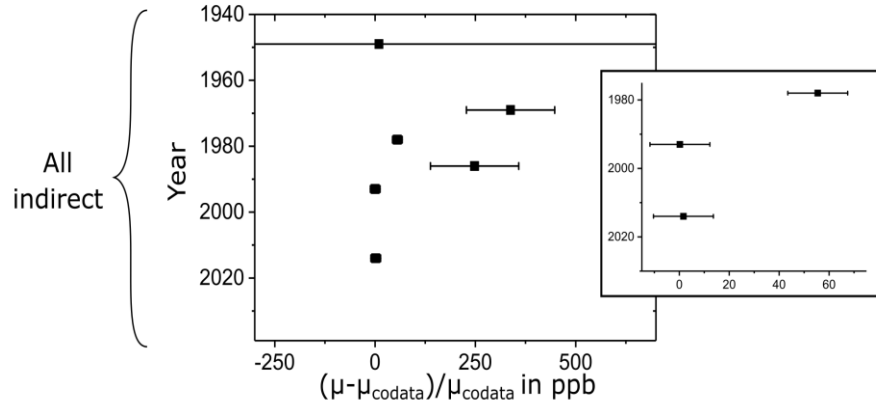
Rudzinski A., et al. *J.Chem. Phys.* **130** 244102 (2009)

Nikiel A., et al. *Eur. Phys. J. D* **68** 330 (2014)



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Establish hyper-polarized ^3He NMR probes as independent standard for precision magnetometry

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| | Water NMR | | ^3He |
|---------------------------|---------------|---|--------------------|
| Dependence on temperature | 1 | ➤ | 1/100 |
| Dependence on probe shape | 1 | ➤ | 1/1000 |
| Diamagnetic shielding | 1 measured | ➤ | 1/10 calculated |

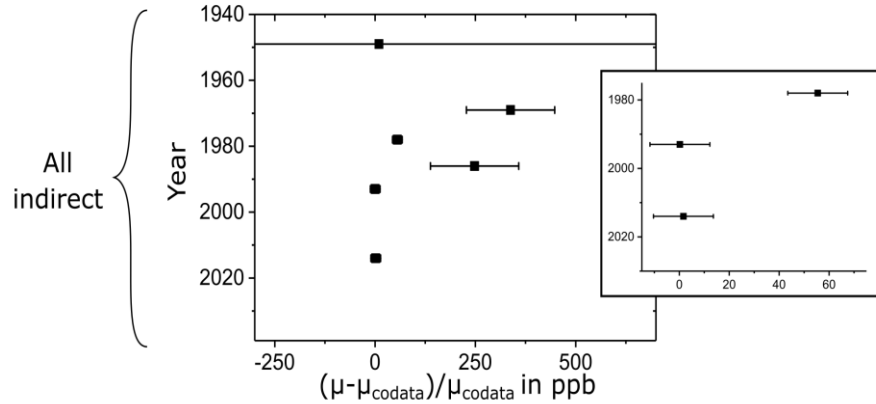
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➡ Application: muon g-2

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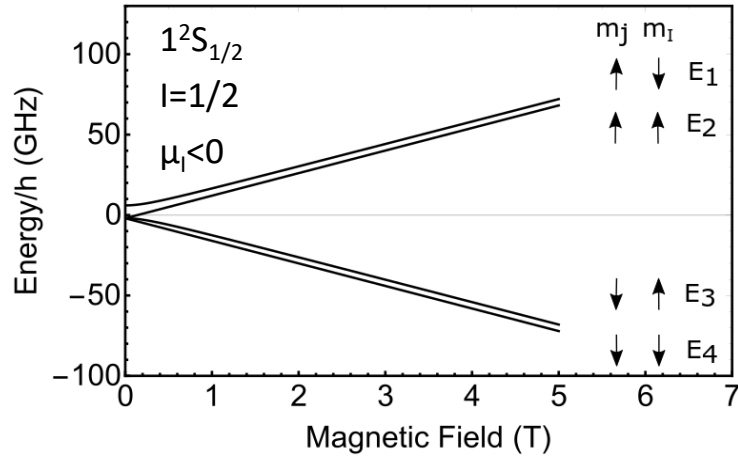
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Motivation



Zero-field splitting:

$$\Delta E^{HFS} = E^F (1 + \delta^{QED} + \delta^{rec} + \delta^{str} + \delta^{nucl})$$

with Fermi contact energy E^F

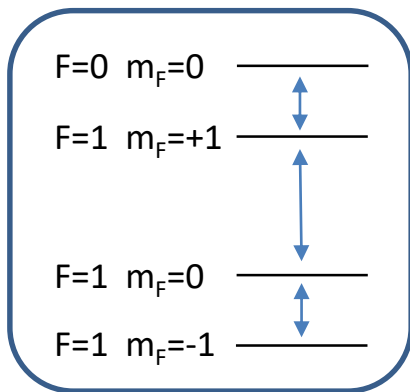
➔ determination of e.g. nuclear structure effect δ^{nucl}

ΔE^{HFS} known to 1.1 ppb (Schuessler et al., Phys. Rev. **187** 5 (1968))

We aim for measurement of order 10ppt

Magnetic Moments in Penning Traps

Determination of energy splitting between spin-states



$$\omega_{F=I\pm\frac{1}{2}}(g_I, g_J, \Delta E^{\text{HFS}}, B)$$

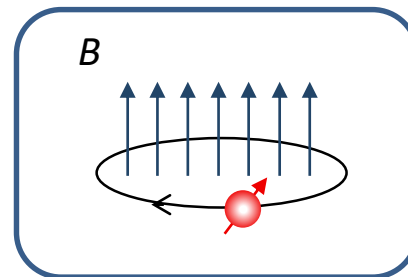


$$1^2S_{1/2}$$

$$l=1/2$$

$$\mu_l < 0$$

Simultaneous cyclotron frequency measurement



$$\omega_c = \frac{e}{m_{\text{He}}} B$$

B-field independent measurement of g_I, g_J and ΔE^{HFS}

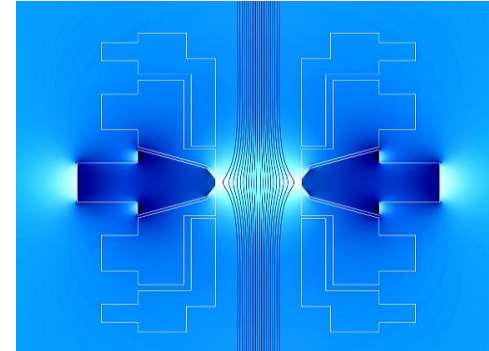
Detection of Spin-State - Continuous Stern-Gerlach Effect

Magnetic field inhomogeneity

$$B_z = B_0 + B_2 \left(z^2 - \frac{\rho^2}{2} \right)$$

➔ axial frequency dependent on magnetic moment

Ring electrode made of CoFe



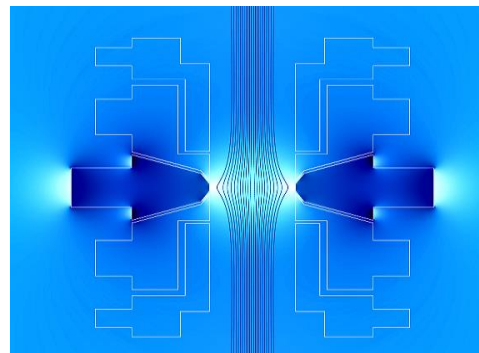
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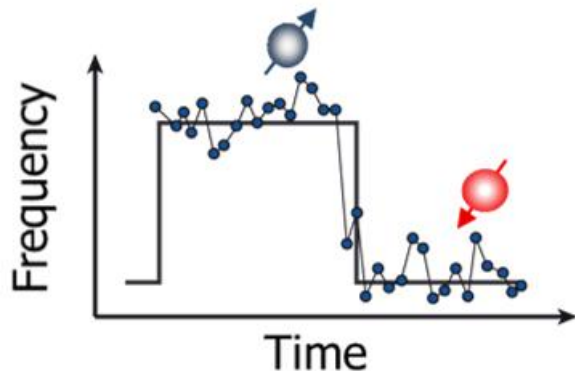
$$B_z = B_0 + B_2 \left(z^2 - \frac{\rho^2}{2} \right)$$

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Spin-transition induces frequency jump



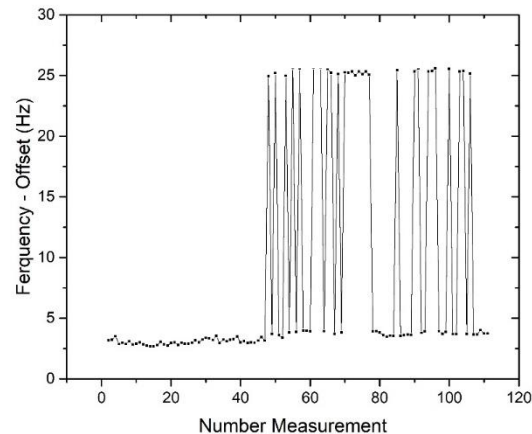
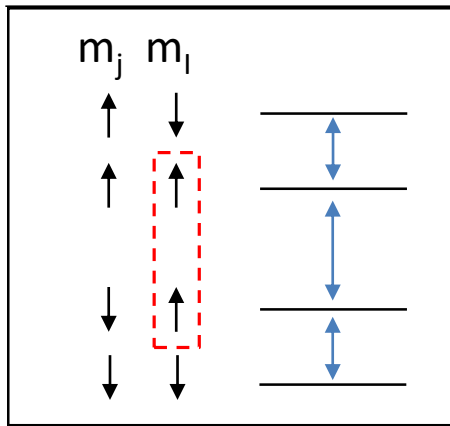
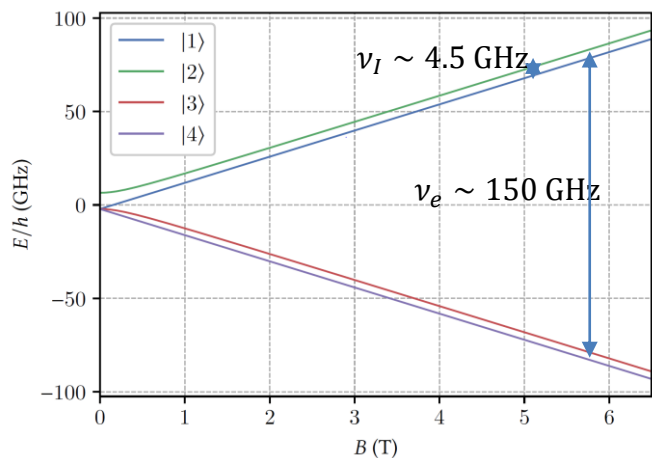
$$\Delta\nu_{z,SF} \sim \mu / (qm)^{1/2}$$

$$\Delta\nu_p / \Delta\nu_e = 10^{-4}$$

$$\Delta\nu_{He} / \Delta\nu_p = 0.3$$

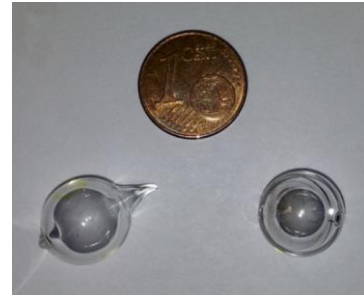
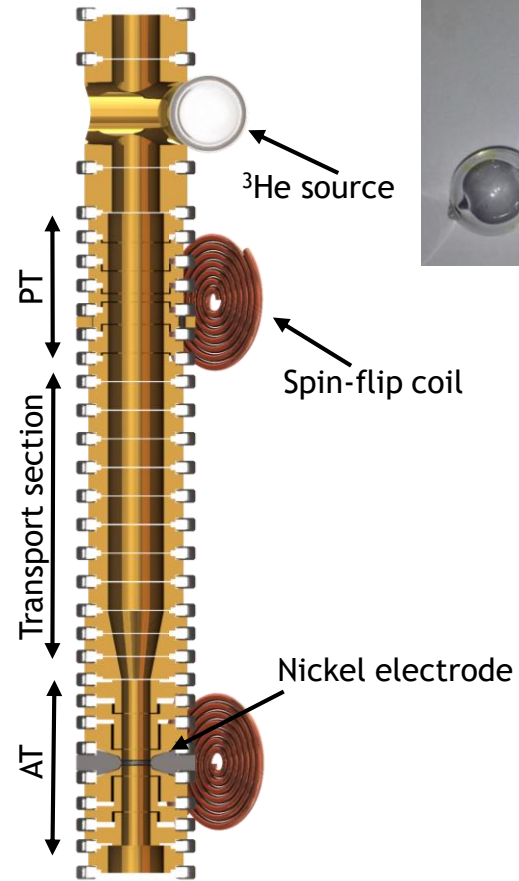
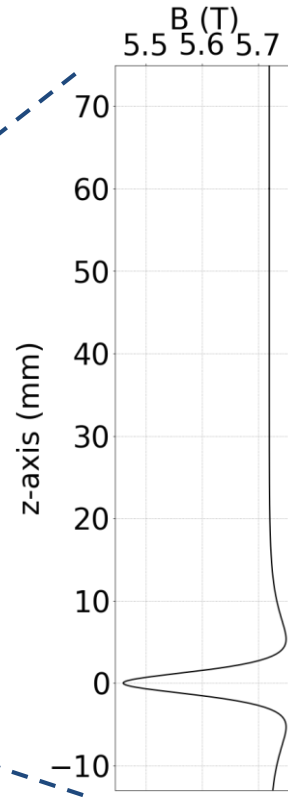
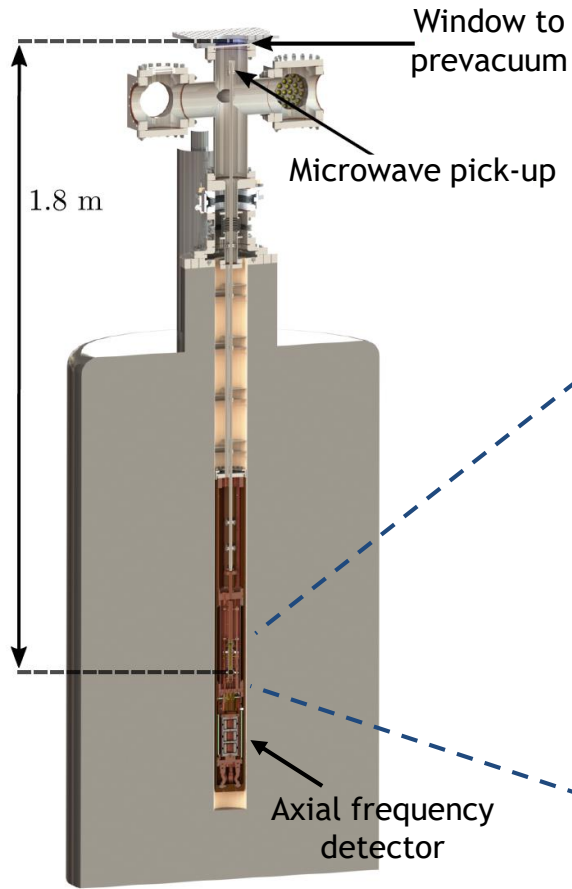
Spin-State Detection ${}^3\text{He}^+$

➔ $\Delta\nu_{z,SF}$ of 20Hz, much easier to detect compared to 90mHz

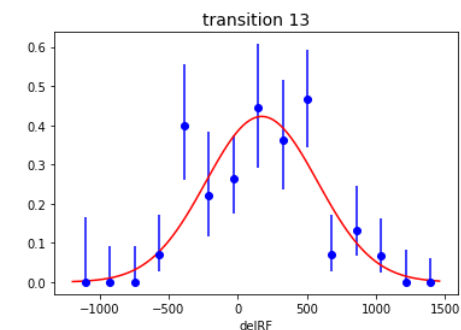
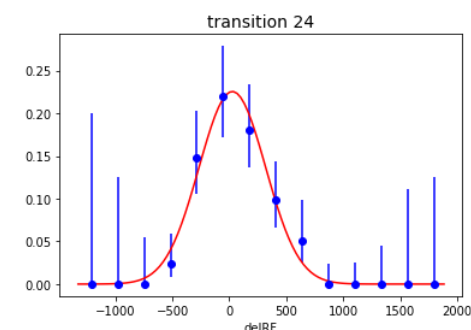
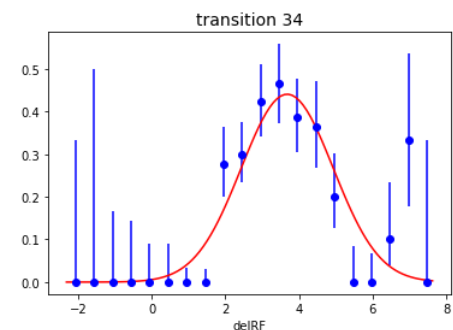
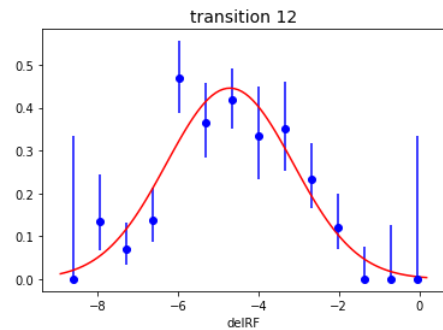


Map readout of nuclear spin-state onto detection of electronic transitions

Setup



Results



| | Relative uncertainties |
|------------------|------------------------|
| g_e | 3e-10 |
| g_l | 8e-10 |
| E_{HFS} | 2e-11 |



Summary

Motivation:

- Calibration for ^3He NMR probes independent of water probes
- Check of theoretical shielding by combining $^3\text{He}^{2+}$ and $^3\text{He}^+$ measurements
- Determination of nuclear structure effects

$^3\text{He}^+$ measurement:

- Avoid direct nucl. SF detection by mapping the nucl. state on the electronic transitions
- Measured four HFS transitions

Next steps:

- Building new setup for $^3\text{He}^{2+}$ g -factor measurement
- requires sympathetic laser cooling to allow nucl. spin-state detection

