Anomalous *tWb* couplings Interplay of top and bottom physics



9. 6. 2011, Perugia, Italy PLHC 2011

Anomalous tWb couplings – p. 1/11

Outline of the talk

- Anomalous tWb couplings and top quark decays.
 - Effects on helicity fractions of *W* boson.
 - Analysis at NLO in QCD.
 - Direct constraints.
- ► Anomalous tWb couplings and $B_{d,s} \overline{B}_{d,s}$ mixing.
 - Effects on the the mixing amplitude M_{12} .
 - Can these effects comply with the favored non-SM M_{12} values from recent fits?
 - If so, what kind of helicity fractions do they predict? ← interplay
- ► Conclusions.

Helicity fractions of W boson in

 $t \to bW$



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Most general parameterization of tWb vertex. J. A. Aguilar-Saavedra 0811.3842



- Helicity surpression in *F*₊ present also in anomalous contributions.
- This mandates analysis at NLO in QCD. J. Drobnak, J. F. Kamenik, S. Fajfer

1010.2402



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Indirect $b \to s\gamma$ constrains on $a_{L,R}$, b_{RL} are sever! Bound on b_{LR} is looser.

B. Grzadkowski, M. Misiak 0802.1413

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Highest allowed effects on \mathcal{F}_+ given in the table and in the graph.

$$\frac{\mathsf{SM}(\delta a_L)}{\mathcal{F}_+^{\rm NLO}/10^{-3}} \frac{\mathsf{M}(\delta a_L)}{1.32} \frac{a_R}{1.34} \frac{b_{RL}}{1.34}$$

Presence of anomalous tWb can not significantly change $\mathcal{F}_+!$



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 b_{LR} < 0.09, 95% C.L. from \mathcal{F}_L b_{LR} < 0.16, 95% C.L. from $b \rightarrow s\gamma$

CDF measurement of \mathcal{F}_L puts a bound on b_{LR} that is *competitive* with indirect $b \rightarrow s\gamma$ constraints.



Tevatron experiments quantifying B_s sector.

Some indications of NP

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 $\blacktriangleright \ \Delta \Gamma_s \text{ vs. } \phi_s^{J/\psi\phi}.$

D0 Note 6093-CONF CDF Public Note 10206



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D0 Note 6093-CONF CDF Public Note 10206



. SM

 $\mathbf{a}_{\mathrm{sl}}^{\mathrm{d}}$

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-0.04-0.03-0.02-0.01 0 0.01





Some indications of NP

 $\blacktriangleright \ \Delta \Gamma_s \text{ vs. } \phi_s^{J/\psi\phi}.$ **D0** Note 6093-CONF

Dimuon charge asymmetry.





► Could NP be hiding in $B_{d,s} - \overline{B}_{d,s}$ mixing?

$$M_{12}^{(d,s)} = M_{12}^{(d,s)SM} \Delta_{d,s}$$

► Analyzed and found consistency with present data with $\Delta_{d,s} = 1$ disfavored!

Z. Ligeti, M. Papucci, G. Perez, J. Zupan 1006.0432 A. Lenz, U. Nierste and CKMfitter group 1008.1593

NP in tWb: $B_{d,s} - \bar{B}_{d,s}$ mixing

- Anomalous tWb can cause $\Delta_{d,s} \neq 1!$
- Effective vertex notation sufficient for setting direct constraints from $t \to Wb$ decays.
- ► For indirect constraints we take a step further: effective theory, described by the Lagrangian

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum_i C_i \mathcal{Q}_i + \text{h.c.} + \mathcal{O}(1/\Lambda^3).$$

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- Restrictions:
 - Dim. 6 operators, invariant under SM gauge group, involving charged quark currents with W.
 - Minimal Flavor Violation.
 - Rid tree level FCNCs in down sector and flavor universal interactions affecting G_F.

NP in tWb: $B_{d,s} - \bar{B}_{d,s}$ mixing

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Lowest order in down Yukawa

$$\begin{aligned} \mathcal{Q}_{RR} &= V_{tb}[\bar{t}_R\gamma^{\mu}b_R] \left(\phi^{\dagger}_u \mathrm{i} D_{\mu}\phi_d\right), \\ \mathcal{Q}_{LL} &= [\bar{Q}'_3\tau^a\gamma^{\mu}Q'_3] \left(\phi^{\dagger}_d\tau^a \mathrm{i} D_{\mu}\phi_d\right) \\ &- [\bar{Q}'_3\gamma^{\mu}Q'_3] \left(\phi^{\dagger}_d \mathrm{i} D_{\mu}\phi_d\right), \\ \mathcal{Q}_{LRt} &= [\bar{Q}'_3\sigma^{\mu\nu}\tau^a t_R]\phi_u W^a_{\mu\nu}, \\ \mathcal{Q}_{LRb} &= [\bar{Q}_3\sigma^{\mu\nu}\tau^a b_R]\phi_d W^a_{\mu\nu}. \end{aligned}$$

Same operator bases used in $b \to s \gamma$ decays B. Grzadkowski, M. Misiak 0802.1413

Higher order in down Yukawa

A. L. Kagan, G. Perez, T. Volansky, J. Zupan 0903.1794

$$\mathcal{Q}_{LL}' = [\bar{Q}_3 \tau^a \gamma^\mu Q_3] (\phi_d^{\dagger} \tau^a i D_\mu \phi_d) - [\bar{Q}_3 \gamma^\mu Q_3] (\phi_d^{\dagger} i D_\mu \phi_d), \mathcal{Q}_{LL}'' = [\bar{Q}_3' \tau^a \gamma^\mu Q_3] (\phi_d^{\dagger} \tau^a i D_\mu \phi_d),$$

$$Q_{LL} = [Q_3 \tau \gamma' Q_3] (\phi_d^{\dagger} \tau D_\mu \phi_d) - [\bar{Q}'_3 \gamma^\mu Q_3] (\phi_d^{\dagger} D_\mu \phi_d),$$

$$\mathcal{Q}'_{LRt} = [\bar{Q}_3 \sigma^{\mu\nu} \tau^a t_R] \phi_u W^a_{\mu\nu}$$

▶ Rotation to mass eigen-basis: $Q_i = (V_{ki}^* u_{Lk}, b_{Li}), \bar{Q}'_3 = \bar{Q}_i V_{ti}^*$.

NP in tWb: $B_{d,s} - \bar{B}_{d,s}$ mixing

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 $\triangleright Q_{LL}$ and Q_{LRt} modify also tWd and tWs couplings

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum_i C_i \mathcal{Q}_i + \text{h.c.} + \mathcal{O}(1/\Lambda^3)$$

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0802.1413
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- \triangleright Q_{LL} and Q_{LRt} modify also tWd and tWs couplings
- ▶ Q'_{LL} and Q_{LRb} modify also uWb and cWb couplings



The set of our seven dim-six operators contribute to $\Delta_{d,s}$ J. Drobnak, J. F. Kamenik, S. Fajfer

$$\Delta_{d,s} = 1 - 2.57 \operatorname{Re}\{\kappa_{LL}\} + 2.00 \kappa'_{LL} - 1.29 \kappa''_{LL} - 1.54 \operatorname{Re}\{\kappa_{LRt}\} - 0.77 \kappa'_{LRt} + \{4.48_d, 4.46_s\} \kappa^2_{RR} + \{4.15_d, 4.13_s\} \kappa^2_{LRb},$$

Analyze one operator at the time, use fitted values of $\Delta_{d,s}$ from A. Lenz, U. Nierste and CKMfitter group 1008.1593



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1) $\kappa_{LL} = \frac{C_{LL}}{\Lambda^2 \sqrt{2}G_F}$ and $\kappa_{LRt} = \frac{C_{LRt}}{\Lambda^2 G_F}$ can not contribute new CPV phases. New bounds obtained

$$\begin{split} -0.082 < &\kappa_{LL} < 0.078 \,, \quad \text{at 95\% C.L.} \,, \\ -0.14 < &\kappa_{LRt} < 0.13 \,, \quad \text{at 95\% C.L.} \,. \end{split}$$



Anomalous tWb couplings – p. 8/11



The set of our seven dim-six operators contribute to $\Delta_{d,s}$ J. Drobnak, J. F. Kamenik, S. Fajfer 1102.4347

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2) $\kappa_{RR} = \frac{C_{RR}}{\Lambda^2 2\sqrt{2}G_F}$ and $\kappa_{LRb} = \frac{C_{LRb}}{\Lambda^2 G_F}$ severely constrained by $b \to s\gamma$. Contribute to mixing only upon two insertions. No considerable effect on $\Delta_{d,s}$.



3) $\kappa_{LL}^{\prime(\prime\prime)} = \frac{C_{LL}^{\prime(\prime\prime)}}{\Lambda^2 \sqrt{2} G_F}$ and $\kappa_{LRt}^{\prime} = \frac{C_{LRt}^{\prime}}{\Lambda^2 G_F}$ not overly constrained by $b \to s\gamma$.

	Re	Im
κ'_{LL}	$-0.062\substack{+0.063\\-0.030}$	$-0.110\substack{+0.029\\-0.024}$
$\kappa^{\prime\prime}_{LL}$	$0.097\substack{+0.048 \\ -0.098}$	$0.180\substack{+0.037 \\ -0.044}$
κ'_{LRt}	$0.160\substack{+0.079 \\ -0.160}$	$0.290\substack{+0.062\\-0.074}$

Central fitted values and 1 σ intervals

- Up to 30% change in \mathcal{F}_+
- Up to 15% change in \mathcal{F}_L



 $\text{Re}[\kappa'_{\text{LRt}}]$ Anomalous tWb couplings – p. 8/11

Conclusions

Helicity fractions can give information about tWb coupling

- Possible measured $\mathcal{F}_+ \gg 0.1\%$ can not be explained by a simple effective vertex.
- Latest measurements of \mathcal{F}_L give direct bounds on anomalous dipole couplings competitive with indirect bounds from $b \to s\gamma$ (MFV).

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- Anomalous top coupling affect $B \overline{B}$ mixing.
 - For MFV models with small bottom Yukawa effects, the bounds are competitive, in some cases improved, compared to bounds from $b \rightarrow s\gamma$.
 - MVF models with large bottom Yukawa effects could accommodate the latest global fits (complex Wilson coefficients).

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- Anomalous top coupling affect $B \overline{B}$ mixing.
 - For MFV models with small bottom Yukawa effects, the bounds are competitive, in some cases improved, compared to bounds from $b \rightarrow s\gamma$.
 - MVF models with large bottom Yukawa effects could accommodate the latest global fits (complex Wilson coefficients).
 - Favored non-zero dipole Wilson coefficient affects the helicity fractions!

- Lagrangian formally invariant under the SM flavor group $\mathcal{G}^{SM} = U(3)_Q \times U(3)_u \times U(3)_d$
- Only \mathcal{G}^{SM} symmetry breaking spurionic fields in the theory are the up and down quark Yukawa matrices $Y_{u,d}$, formally transforming as $(3, \overline{3}, 1)$ and $(3, 1, \overline{3})$ respectively.
- ▶ Most general \mathcal{G}^{SM} invariant quark bilinear flavor structures

 $\bar{u}Y_u^{\dagger}\mathcal{A}_{ud}Y_dd$, $\bar{Q}\mathcal{A}_{QQ}Q$, $\bar{Q}\mathcal{A}_{Qu}Y_uu$, $\bar{Q}\mathcal{A}_{Qd}Y_dd$,

where \mathcal{A}_{xy} are arbitrary polynomials of $Y_u Y_u^{\dagger}$ and/or $Y_d Y_d^{\dagger}$,

•
$$\langle Y_d \rangle = \operatorname{diag}(m_d, m_s, m_b) / v_d$$
 and $\langle Y_u \rangle = V^{\dagger} \operatorname{diag}(m_u, m_c, m_t) / v_u$

Linear MFV

Simplest case of linear MFV where within $\langle A_{xy} \rangle$ higher powers of $\langle Y_d Y_d^{\dagger} \rangle \simeq \operatorname{diag}(0, 0, m_b^2/v_d^2)$ can be neglected. Neglecting also contributions suppressed by first and second generation quark masses, the only relevant flavor contributions of the arbitrary A_{xy} structures

$$ar{t}_R V_{tb} b_R \,, \qquad ar{Q}_i Q_i \,, \qquad ar{Q}_i V_{ti}^* V_{tj} Q_j \,, \ ar{Q}_i V_{ti}^* t_R \,, \qquad ar{Q}_3 b_R \,, \qquad ar{Q}_i V_{ti}^* V_{tb} b_R \,.$$

Non-Linear MFV

- Generalization to MFV scenarios where large bottom Yukawa effects can be important.
- ► Higher powers of $\langle Y_d Y_d^{\dagger} \rangle$ within \mathcal{A}_{xy} effectively project to the third generation in the down sector yielding the following additional flavor structures

$$\bar{Q}_3 Q_3 , \qquad \bar{Q}_3 V_{tb}^* V_{tj} Q_j , \qquad \bar{Q}_3 V_{tb}^* t_R .$$

Basis independence

Example: $\bar{Q}A_{QQ}Q \rightarrow \bar{Q}_i \langle Y_u Y_u^{\dagger} \rangle_{ij} Q_j$

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Up-Yukawa diagonal
 $\langle Y_u Y_u^{\dagger} \rangle_{ij} = \delta_{3i}\delta_{3j} \frac{m_t^2}{v^2}, \qquad Q_i = \begin{pmatrix} u_i \\ V_{ik}d_k \end{pmatrix}$
 $\bar{Q}_i \langle Y_u Y_u^{\dagger} \rangle_{ij} Q_j = \frac{m_t^2}{v^2} \bar{Q}_3 Q_3 = \frac{m_t^2}{v^2} (\bar{t}, V_{3k}^* \bar{d}_k) \begin{pmatrix} t \\ V_{3k}d_k \end{pmatrix}$

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Down-Yukawa diagonal
 $\langle Y_u Y_u^{\dagger} \rangle_{ij} = V_{3i}^* V_{3j} \frac{m_t^2}{v^2}, \qquad Q_i = \begin{pmatrix} V_{ki}^* u_k \\ d_i \end{pmatrix}$
 $\bar{Q}_i \langle Y_u Y_u^{\dagger} \rangle_{ij} Q_j = \bar{Q}_i \frac{m_t^2}{v^2} V_{3i}^* V_{3j} Q_j = \frac{m_t^2}{v^2} (V_{mi} \bar{u}_m, \bar{d}_i) V_{3i}^* V_{3j} \begin{pmatrix} V_{nj}^* u_n \\ d_j \end{pmatrix}$

$$= \frac{m_t^2}{v^2} (\bar{t}, V_{3i}^* \bar{d}_i) \begin{pmatrix} t \\ V_{3j} d_j \end{pmatrix}$$

Anomalous tWb couplings – p. 11/11

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