

# Top and Beauty synergies in SMEFT fits

based on works with Stefan Bissmann, Cornelius Grunwald and Kevin Kröninger, 2012.10456 [hep-ph], to appear in JHEP

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DPG spring meeting March 2021: 6 sessions on flavor physics

NA 62	$s$
Belle, BaBar	$c, b$
BES III	$c$
Belle II	$c, b$
LHCb	$c, b, (s)$
ATLAS, CMS	$b, t (c, s)$
Z-factory (CLIC-like)	$c, b (t)$

Dream time to be in flavor physics

2 anomalies strengthened in past few weeks:  $R_K$ :  $3.1\sigma$  new LHCb result <sup>2103.11769</sup>  $(g - 2)$  of muon  $4.2\sigma$  – new FNAL result

- rates and angular distributions  $b \rightarrow s\mu\mu$ ,  $b \rightarrow s\gamma$  aka "the global fit"
- $R_{K,K^*}$ : ratio of branching fractions  $b \rightarrow s\mu\mu$  vs  $b \rightarrow see$  <sup>hep-ph/0310219</sup>
- $R_{D,D^*}$ :  $b \rightarrow c\tau\nu$  vs  $b \rightarrow c(e, \mu)\nu$
- Cabibbo-angle anomaly  $V_{us}$  from  $s \rightarrow u\mu\nu$  vs  $d \rightarrow ue\nu$
- $(g - 2)$  of muon and electron

common denominator: "something with leptons (in low energy data) "

Flavor continues to be interesting and inspiring; the anomalies require flavor BSM model building and flavorful fits.

# Moving ahead .... getting more global

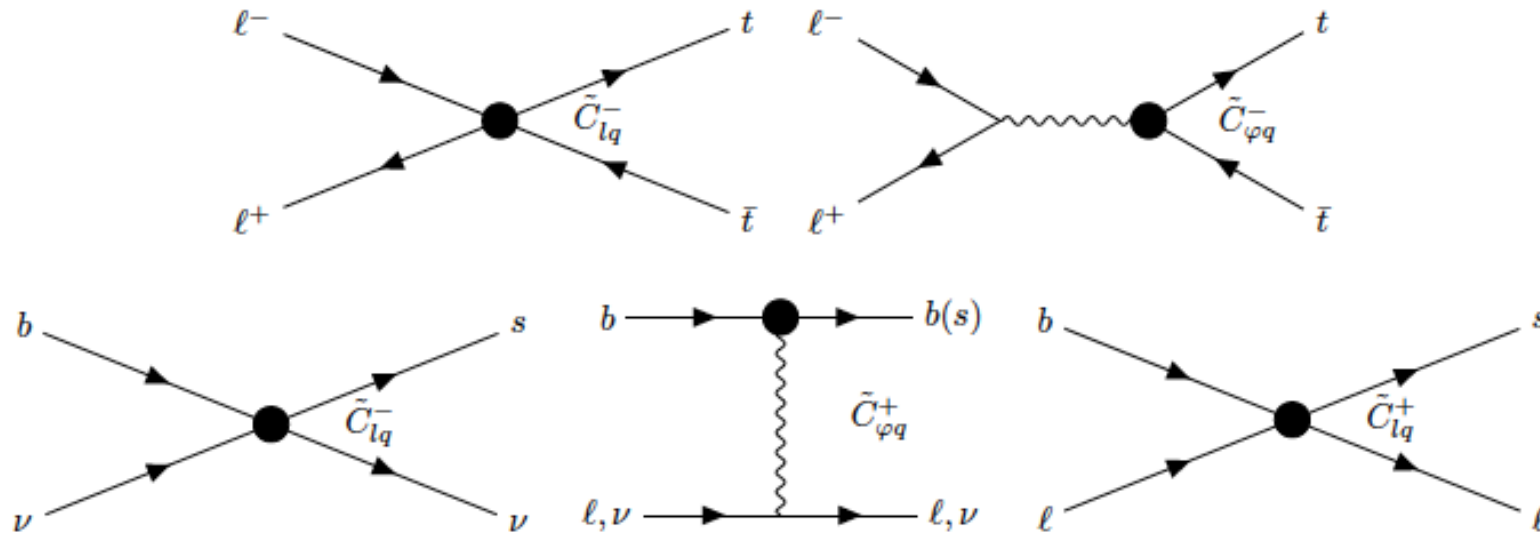
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towards more global approach across the flavors  $s, c, b, t...$

NA 62	$s$
Belle, BaBar	$c, b$
BES III	$c$
Belle II	$c, b$
LHCb	$c, b, (s)$
ATLAS, CMS	$b, t$

The tool to achieve a cross community global analysis are effective field theories: Study correlations among multi-observables from different experiments ( $B \rightarrow K^{(*)} \mu\mu, B_s \rightarrow \mu\mu, B \rightarrow X_s \gamma$ ) in WET (the global  $b \rightarrow s$ -fit aka  $C_7, C_9, C_{10}$ -fits). ongoing precision program

Use SMEFT to include tops, and exploit unbroken SM symmetries  $SU(2)_L \times U(1)_Y$  as a lab for flavor links.



SMEFT coefficients  $C^\pm = C^{(1)} \pm C^{(3)}$  top and beauty, leptons and neutrinos, linked and complementary; **flat directions are removed**

$b \rightarrow s\mu\mu$  (LHC), probes  $C^+$

$b \rightarrow s\nu\nu$  (BelleII), probes  $C^-$

$e^+e^- \rightarrow t\bar{t}$  (CLIC-like), probes  $C^-$  — quark flavor link implied  $C_{23} = V_{tb}V_{ts}^*C_{33}$ , lepton universality,....

11 dim 6 operators in fit [2012.10456](#) . Penguins, dipole operators

$$O_{\varphi q}^{(1)} = \left( \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \right) (\bar{q}_L \gamma^\mu q_L) , \quad O_{\varphi q}^{(3)} = \left( \varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi \right) (\bar{q}_L \tau^I \gamma^\mu q_L) ,$$

$$O_{\varphi u} = \left( \varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \right) (\bar{u}_R \gamma^\mu u_R) , \quad O_{uG} = (\bar{q}_L \sigma^{\mu\nu} T^A u_R) \tilde{\varphi} G_{\mu\nu}^A ,$$

$$O_{uB} = (\bar{q}_L \sigma^{\mu\nu} u_R) \tilde{\varphi} B_{\mu\nu} , \quad O_{uW} = (\bar{q}_L \sigma^{\mu\nu} \tau^I u_R) \tilde{\varphi} W_{\mu\nu}^I ,$$

and semileptonic four-fermion operators

$$O_{lq}^{(1)} = (\bar{l}_L \gamma_\mu l_L) (\bar{q}_L \gamma^\mu q_L) , \quad O_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L) (\bar{q}_L \gamma^\mu \tau^I q_L) , \quad O_{qe} = (\bar{q}_L \gamma_\mu q_L) (\bar{e}_R \gamma^\mu e_R) ,$$

$$O_{eu} = (\bar{e}_R \gamma_\mu e_R) (\bar{u}_R \gamma^\mu u_R) , \quad O_{lu} = (\bar{l}_L \gamma_\mu l_L) (\bar{u}_R \gamma^\mu u_R) .$$

Corresponding Wilson coefficients have up to four **flavor indices**,  
for instance  $C_{lq}^{(1)kl ij} \cdot (\bar{l}_{Lk} \gamma_\mu l_{Ll}) (\bar{q}_{Li} \gamma^\mu q_{Lj})$ ,  $i, j, k, l = 1, 2, 3$ .

Quark flavor patterns in operators:  $\bar{q}_{Li}(\dots)q_{Lj}$ ,  $\bar{q}_{Li}(\dots)u_{Rj}$  and  $\bar{u}_{Ri}(\dots)u_{Rj}$ .

Top-(beauty)-philic flavor pattern: only  $C^{i=3,j=3}$  switched on.

Consider second-third generation only

Top-(beauty)-philic:  $C_x^{ij} = C_x^{33} \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$  for all 11 ops  $O_x$ .

Flavor mixing for doublets  $q_L$ :  $V_{\text{CKM}} = V_u V_d^\dagger$ . In up-mass basis  $V_u = 1$ .  $d_L^{\text{mass}} = V_{\text{CKM}} d_L^{\text{flavor}}$

all  $\bar{q}_{Li}(\dots)q_{Lj}$  ops:

$$C_{lq}^{(1,3)}, C_{\varphi q}^{(1,3)}, C_{qe} \propto \begin{pmatrix} |V_{ts}|^2 & V_{tb} V_{ts}^* \\ h.c. & |V_{tb}|^2 \end{pmatrix} \sim \begin{pmatrix} 0 & -0.04 \\ -0.04 & 1 \end{pmatrix}$$

tree level FCNCs; synergies between **top** and  **$b \rightarrow s$**  anomalies

1. most of today's data, e.g.,  $b \rightarrow s\ell^+\ell^-$ , is for  $\ell = \mu$ . Therefore, most of the results are "lepton-specific"  $k = l = 2$ .

2. notable exceptions are bounds on dineutrino modes

$B(B \rightarrow K^{(*)}\nu\bar{\nu}) = \sum_{k,l} B(B \rightarrow K^{(*)}\nu_k\bar{\nu}_l)$ , which are flavor-summed.

3. To include 2., we assume lepton universality. So, in the semileptonic 4-fermion operators, we assume for the lepton flavor  $C^{kl} \propto \delta_{kl}$ .

(in view of 1., this is only a mild assumption, however, turns out that  $B(B \rightarrow K^{(*)}\nu\bar{\nu})$  in particular when observed, is an important constraint)

4. In view of current tensions with  $R_K$  etc, it is desirable to perform lepton-specific fits for  $ee, \mu\mu (\tau\tau)$  operators as well as LFV ones.

choose your initial state:  $e^+e^-$ -collider, muon collider are complementary

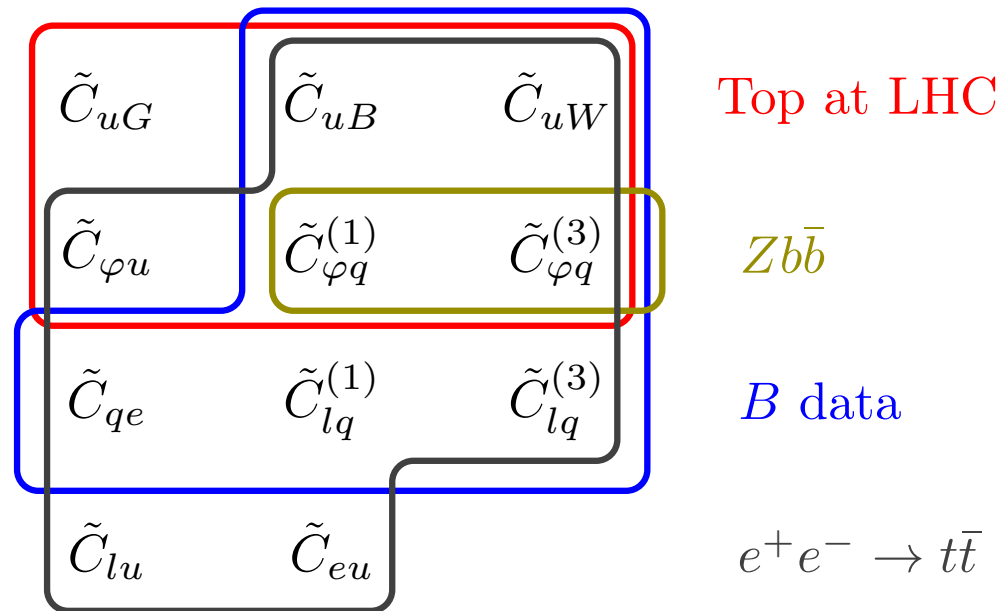


# top and beauty synergies – a global fit

procedure:

scan 11  $C_i$  at  $\Lambda = 1$  TeV. 1-loop RGE to  $m_t$ ,  $m_W$ . Matching onto WET, computation of  $b$ -observables, flavio, wilson tools

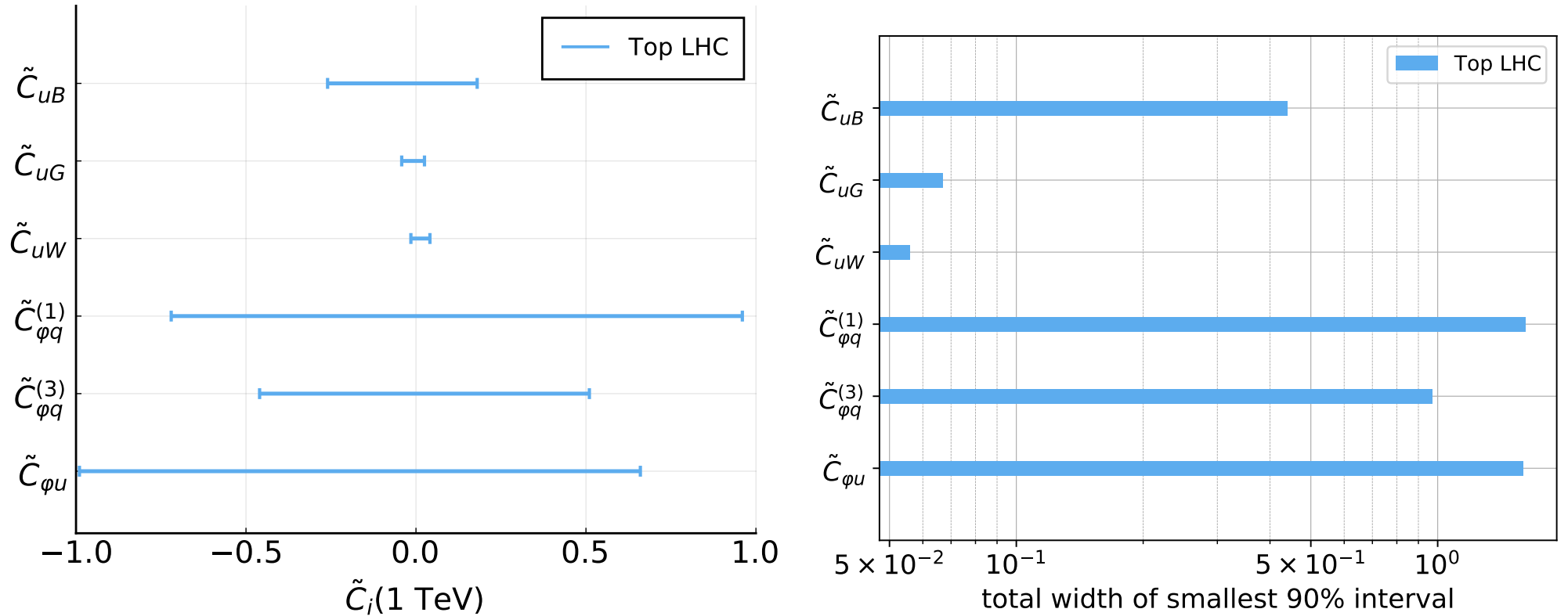
confronting to data; EFT-fitter



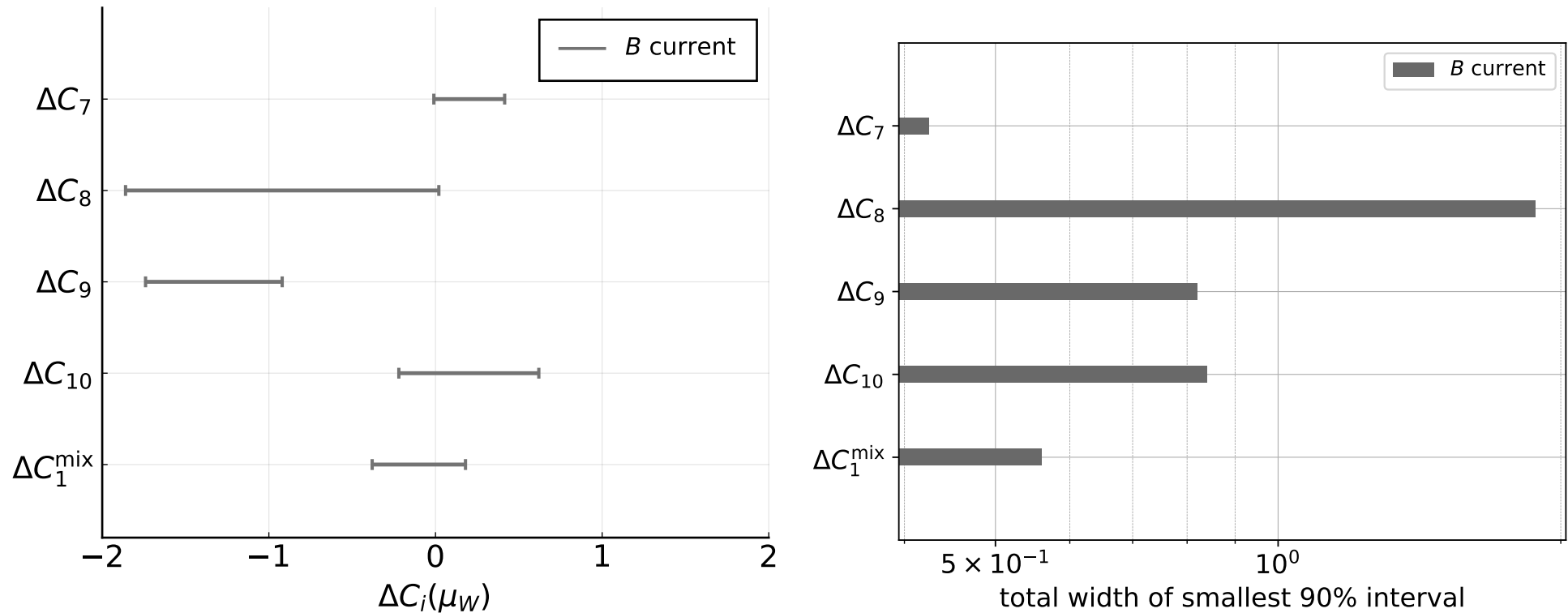
Process	Observable	Two-fermion operators	sl. four-fermion operators
$pp \rightarrow t\bar{t}$	$\sigma^{\text{inc}}$	$\tilde{C}_{uG}$	-
$pp \rightarrow t\bar{t}\gamma$	$\sigma^{\text{fid}}$	$\tilde{C}_{uB}, \tilde{C}_{uW}, \tilde{C}_{uG}$	-
$pp \rightarrow t\bar{t}Z$	$\sigma^{\text{inc}}$	$\tilde{C}_{uB}, \tilde{C}_{uW}, \tilde{C}_{uG}, \tilde{C}_{\varphi q}^-, \tilde{C}_{\varphi u}$	-
$t \rightarrow bW$	$F_{0,L}$	$\tilde{C}_{uW}$	-
Top decay	$\Gamma_t$	$\tilde{C}_{\varphi q}^{(3)}, \tilde{C}_{uW}$	-
$Z \rightarrow b\bar{b}$	$A_{FB}^b, R_b, \sigma_{\text{had}}$	$\tilde{C}_{\varphi q}^+$	-
$b \rightarrow s\gamma$	BR	$[\tilde{C}_{uB}], [\tilde{C}_{uW}], \{\tilde{C}_{uG}\}, [\tilde{C}_{\varphi q}^{(3)}]$	-
$b \rightarrow s\ell^+\ell^-$	BR, $A_{FB}, P_i^{(\prime)}, \dots$	$[\tilde{C}_{uB}], [\tilde{C}_{uW}], \{\tilde{C}_{uG}\}, \tilde{C}_{\varphi q}^{+(*)}, [\tilde{C}_{\varphi q}^{(3)}]$	$\tilde{C}_{lq}^{+(*)}, \tilde{C}_{qe}^{(*)}$
$b \rightarrow s\nu\bar{\nu}$	BR	$\tilde{C}_{\varphi q}^{+(**)}$	$\tilde{C}_{lq}^{-(*)}$
Mixing	$\Delta M_s$	$[\tilde{C}_{uW}], \{\tilde{C}_{uG}\}, [\tilde{C}_{\varphi q}^{(1,3)}]$	-
$e^+e^- \rightarrow t\bar{t}$	$\sigma, A_{FB}$	$\tilde{C}_{uB}, \tilde{C}_{uW}, \{\tilde{C}_{uG}\}, \tilde{C}_{\varphi q}^-, \tilde{C}_{\varphi u}$	$\tilde{C}_{eu}, \tilde{C}_{qe}, \tilde{C}_{lu}, \tilde{C}_{lq}^-$

Process	Observable	$\sqrt{s}$	Int. luminosity	Experiment
$t\bar{t}\gamma$	$\sigma^{\text{fid}}(t\bar{t}\gamma, 1\ell), \sigma^{\text{fid}}(t\bar{t}\gamma, 2\ell)$	13 TeV	36.1 fb <sup>-1</sup>	ATLAS
$t\bar{t}Z$	$\sigma^{\text{inc}}(t\bar{t}Z)$	13 TeV	77.5 fb <sup>-1</sup>	CMS
$t\bar{t}$	$\sigma^{\text{inc}}(t\bar{t})$	13 TeV	36.1 fb <sup>-1</sup>	ATLAS
	$F_0, F_L$	8 TeV	20.2 fb <sup>-1</sup>	ATLAS
	$\Gamma_t$	8 TeV	20.2 fb <sup>-1</sup>	ATLAS

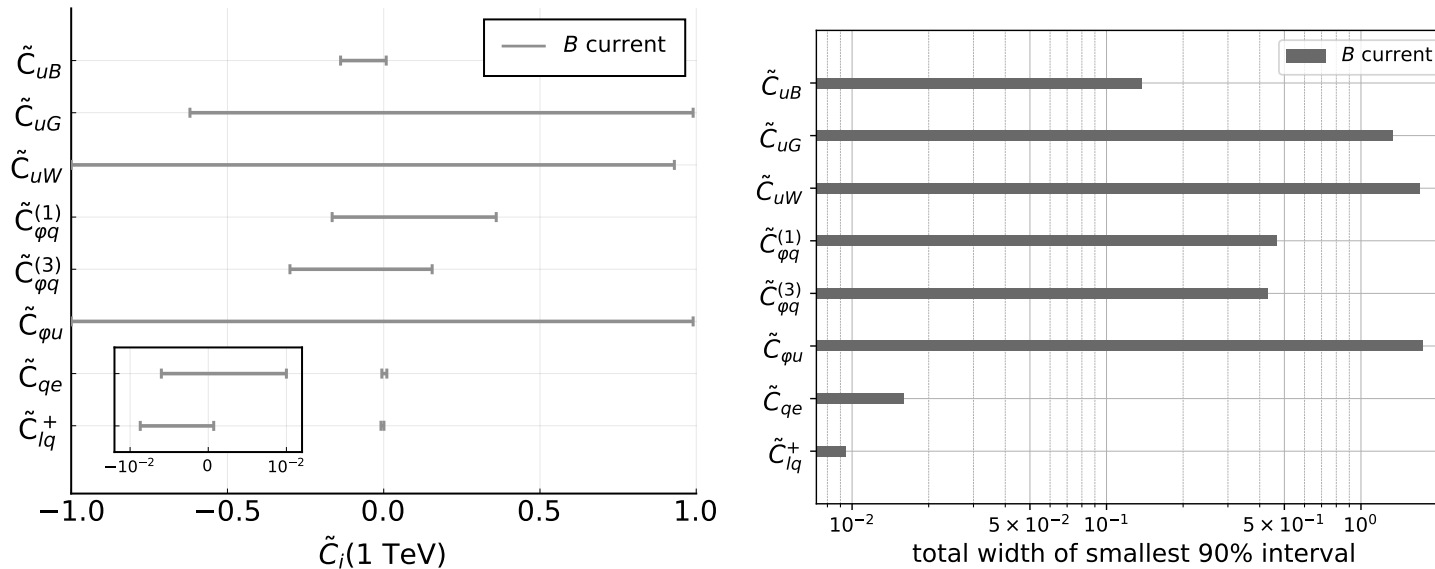
Table 1: Considered bservables for top- quark processes at the LHC 2012.10456 [hep-ph] .



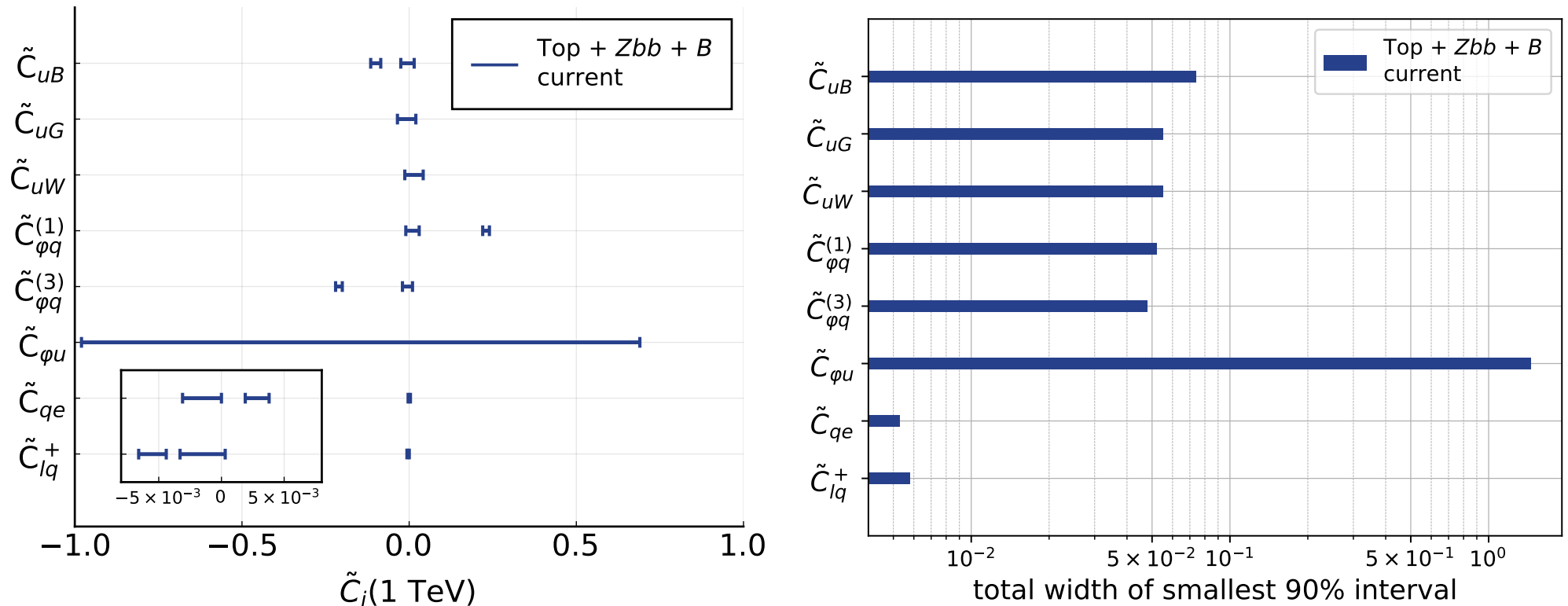
**Figure 1:** Constraints on SMEFT  $\tilde{C}_i$  at  $\Lambda = 1$  TeV from top measurements in Tab. 1; marginalized smallest intervals containing 90 % posterior probability (left) and the total width of these intervals (right). For all coefficients we choose a uniform distribution in  $-1 \leq \tilde{C}_i \leq 1$  as the prior. **6 WCs constrained, all penguins  $C_{\varphi x}$  poorly**



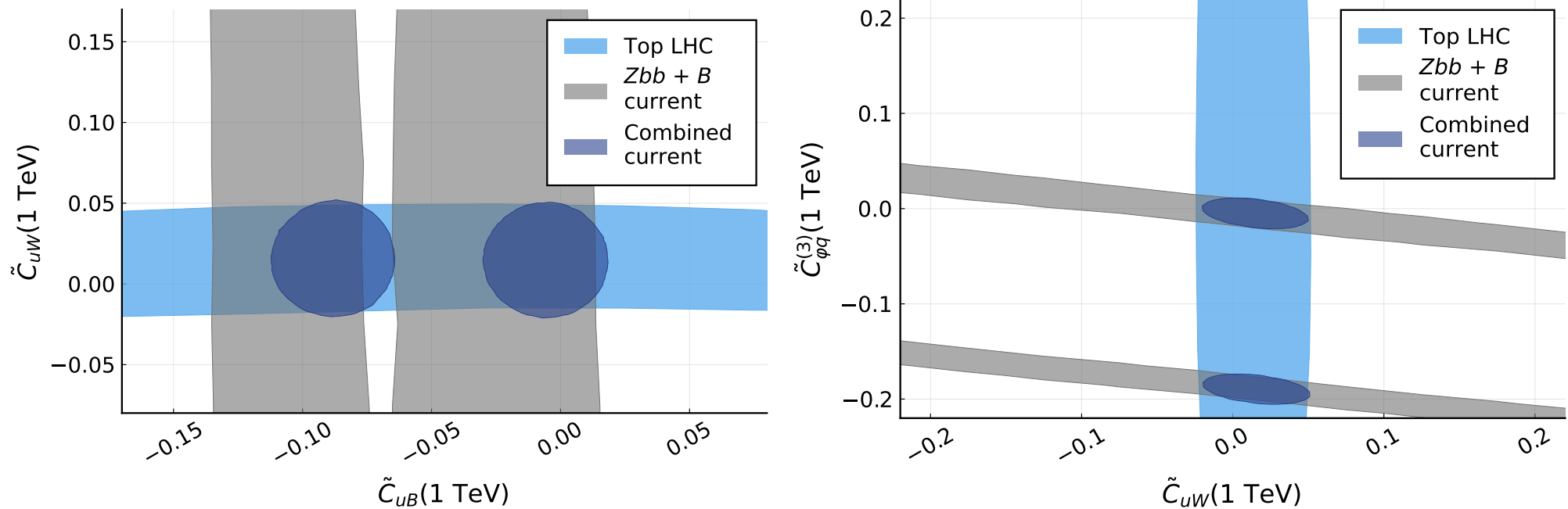
**Figure 2:** Constraints on WET coefficients  $\Delta C_i$  at the scale  $\mu = \mu_W$ . 5 WET-WCs constrained, new physics hint in  $C_9$



**Figure 3:** Constraints on SMEFT coefficients (lower plots) from measurements of  $B$  observables in Tab. ???. Shown are the marginalized smallest intervals containing 90 % of the posterior probability (left) and the total width of these intervals (right) obtained in a fit of five WET (upper plots) and eight SMEFT coefficients (lower plots) to the data. **8 SMEFT WCs constrained, incl 2 sl 4-fermis with tight constraints, others (penguins, dipoles) except  $C_{uB}$  not too great**

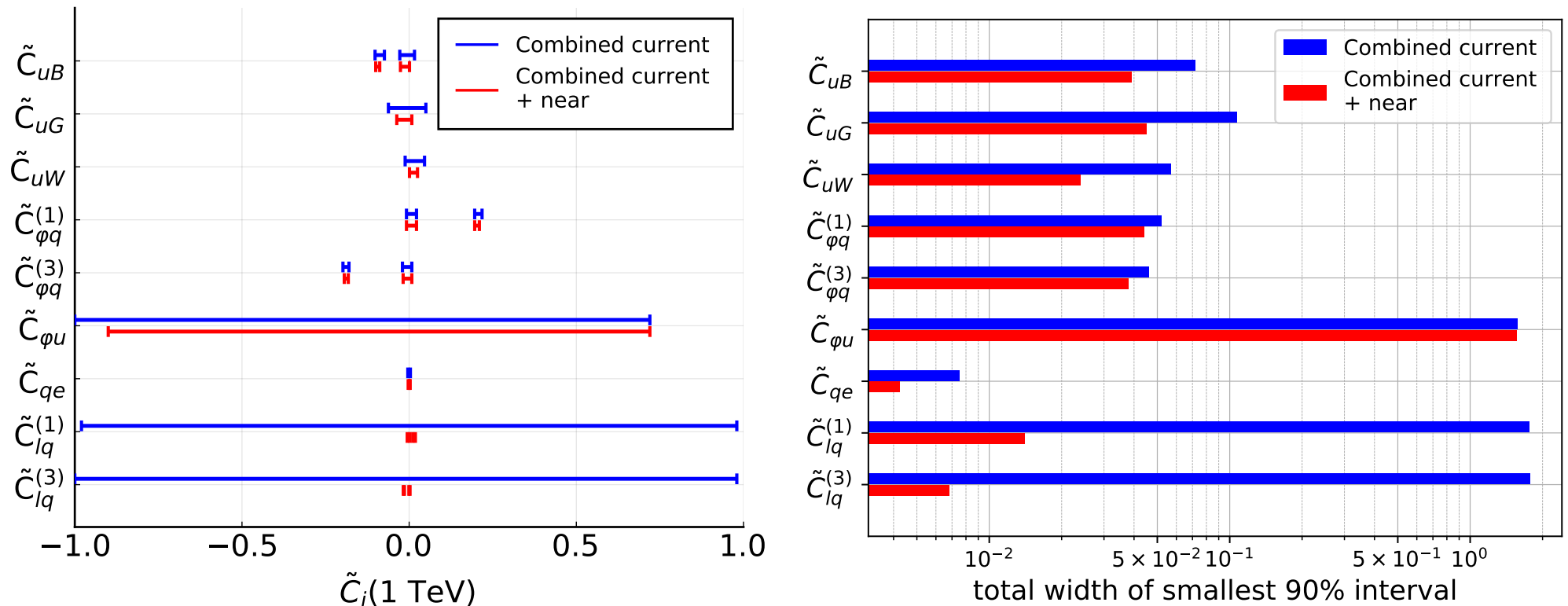


**Figure 4:** Constraints on SMEFT coefficients  $\tilde{C}_i$  in Eq. (??) obtained in a fit to top-quark data in Tab. 1,  $Zbb$  data, and  $B$  physics data in Tab. ?? . Shown are smallest intervals containing 90 % posterior probability (left) and total width of these intervals (right). For the prior we assume a uniform distribution over the interval  $-1 \leq \tilde{C}_i \leq 1$ . **8 WCs constrained, including 2 sl 4-fermis,  $C_{lq}^+ \lesssim 10^{-2}$ ,  $C_{uB}$  and penguins improved,  $C_{\phi u}$  still a mess**



**Figure 5:** Examples for two-dimensional posterior distributions of SMEFT coefficients  $\tilde{C}_i$  in Eq. (??) obtained in a fit to top-quark data (light blue),  $B$  physics data (grey) and the combined dataset including  $Zbb$  data (blue). Shown are the smallest intervals containing 90 % of the posterior distribution. For the prior we assume a uniform distribution over the interval  $-1 \leq \tilde{C}_i \leq 1$ . synergies at work, see also 1909.13632 for  $C_{uB}$

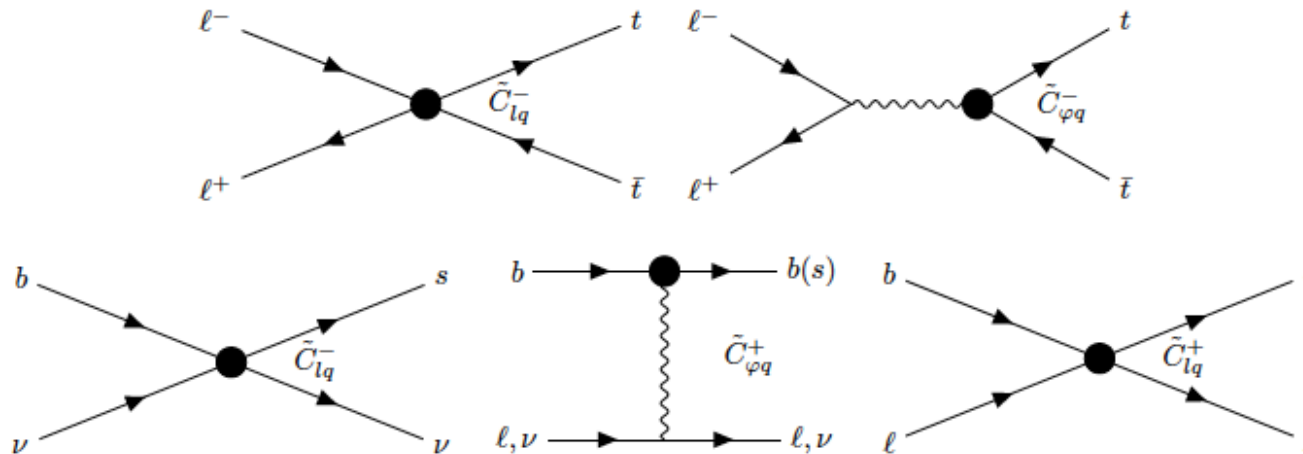


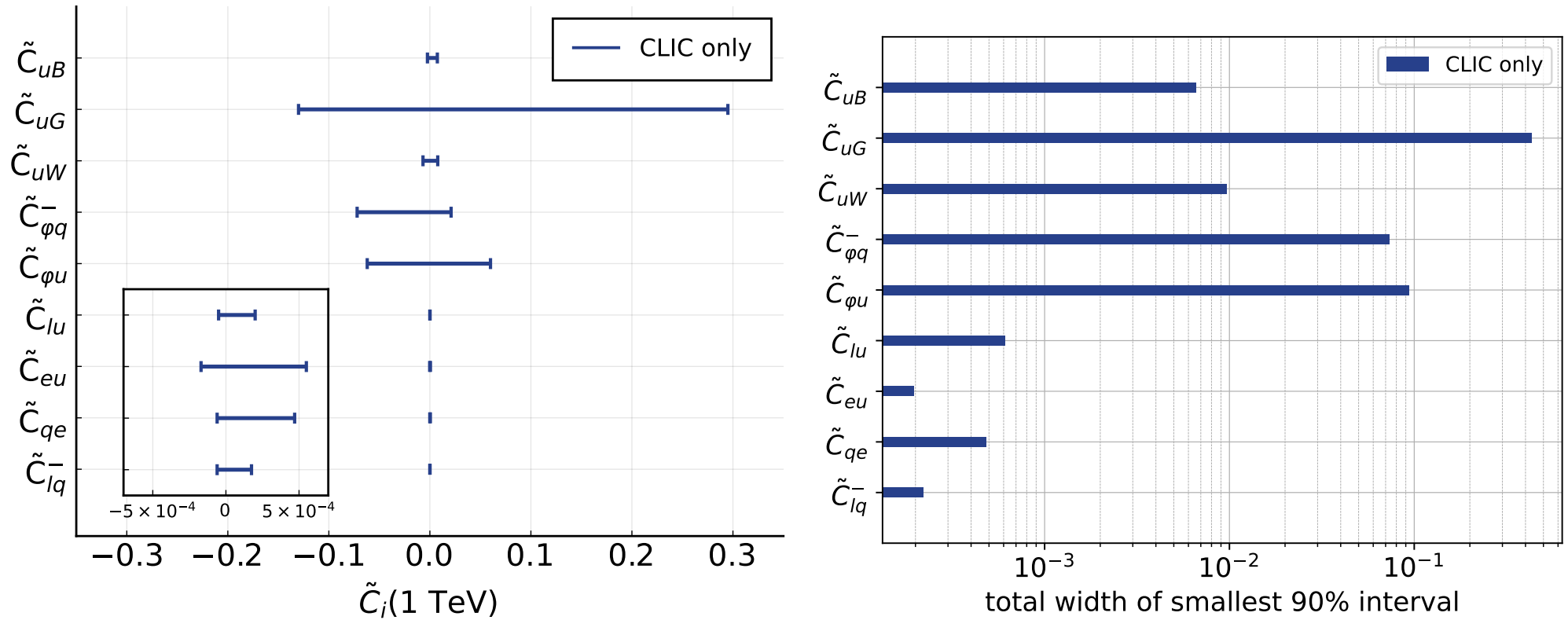


**Figure 6:** Constraints on coefficients  $\tilde{C}_i$  from fits to current top-quark and  $B$  measurements in Tabs. 1 and ?? (blue) and to current measurements and projections of top-quark and  $B$  observables in Tabs. 1-?? (red). Shown are the marginalized smallest intervals containing 90 % posterior probability (left) and the total widths of these intervals (right). **9 WCs constrained; both  $C_{lq}^{\pm}$  resolved; BSM solution due to  $b$ -anomalies visible in  $C_{lq}^{(1)}$  and  $C_{lq}^{(3)}$ .**

Observable	$\sqrt{s}$	Polarization ( $e^-, e^+$ )	Ref. experiment
$\sigma_{t\bar{t}}, A_{\text{FB}}$	380 GeV	(80%, 0)	Abramowicz:2018
$\sigma_{t\bar{t}}, A_{\text{FB}}$	1.4 TeV	(80%, 0)	Abramowicz:2018
$\sigma_{t\bar{t}}, A_{\text{FB}}$	3 TeV	(80%, 0)	Abramowicz:2018

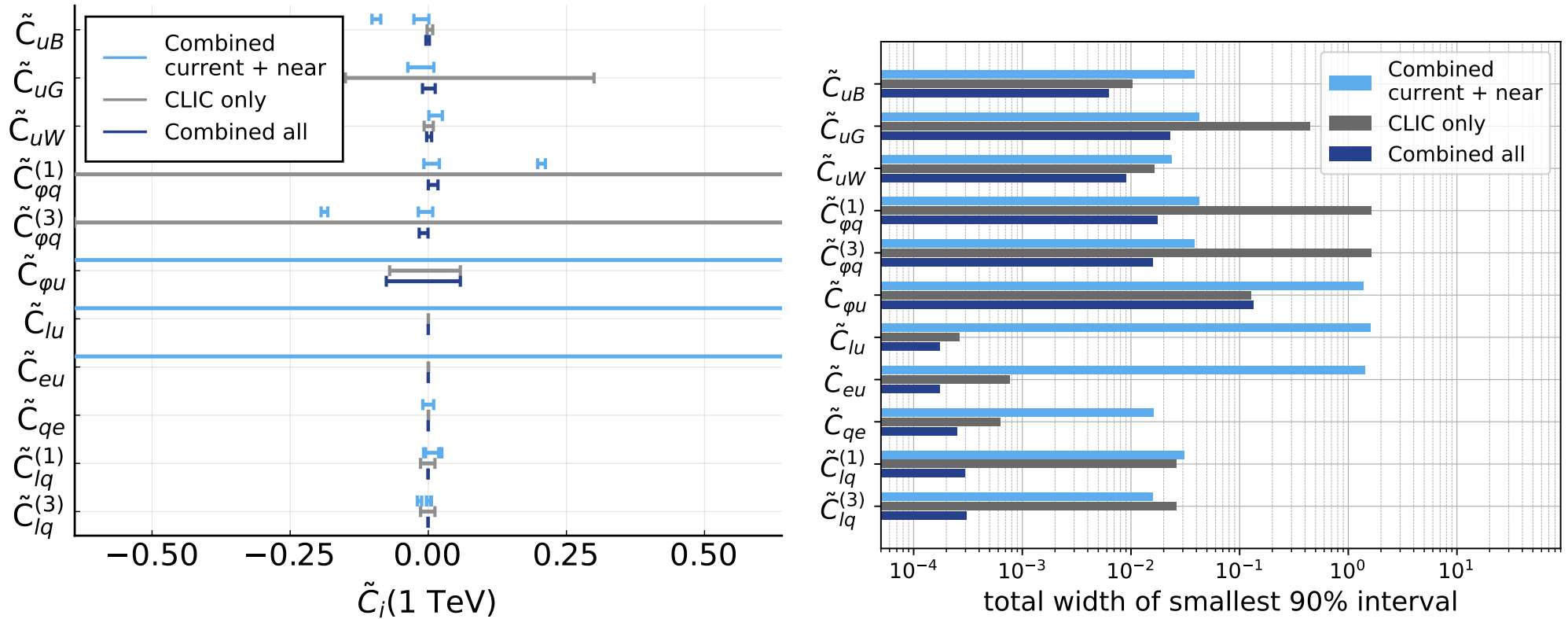
**Table 2:** Observables at different energies and polarizations for  $t\bar{t}$  production at CLIC Abramowicz:2018. SM predictions are taken from Durieux:2018tev.





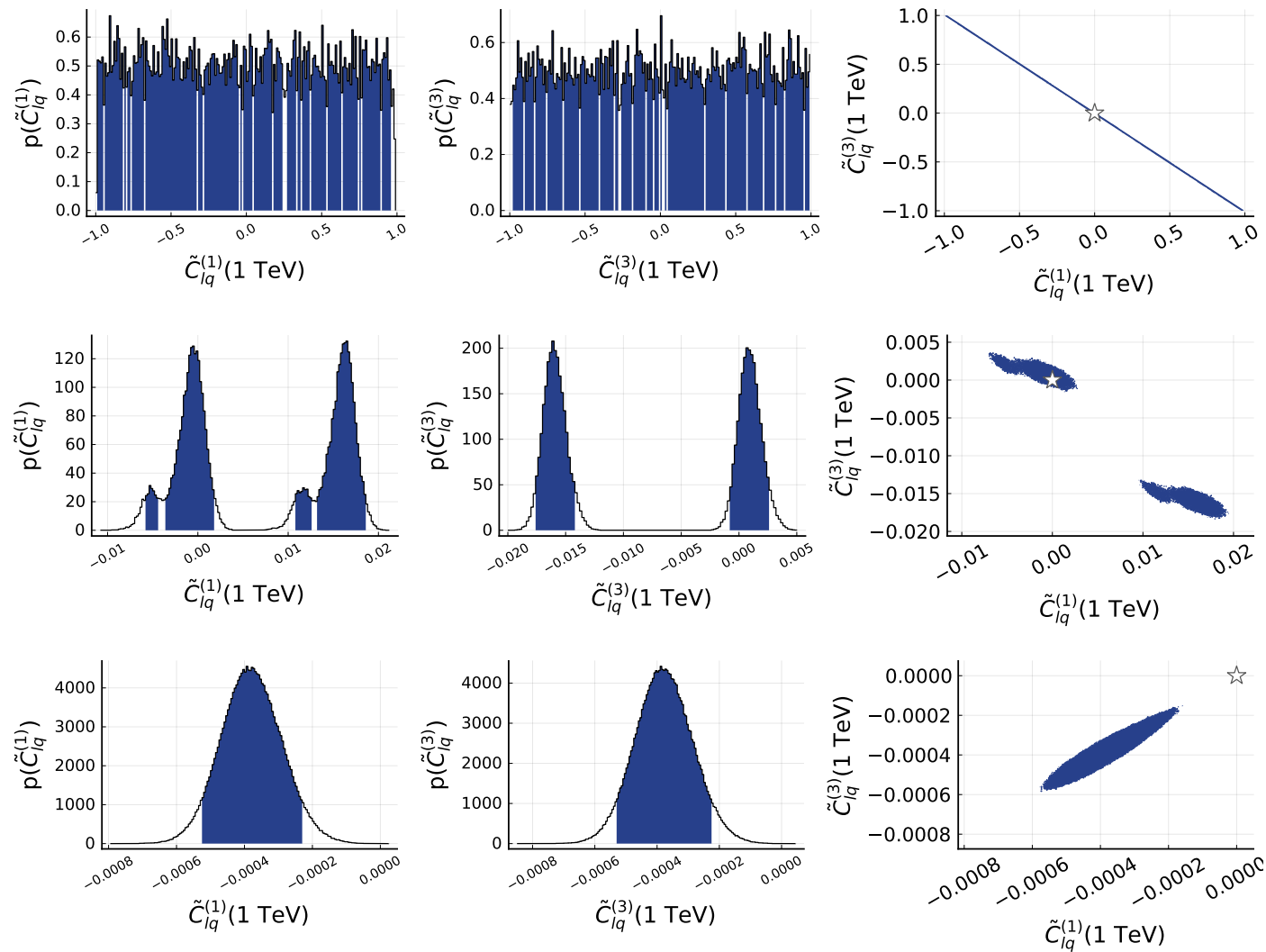
**Figure 7:** Constraints on coefficients  $\tilde{C}_i$  from fits to CLIC observables in Tab. 2. Shown are the marginalized smallest intervals containing 90 % posterior probability (left) and the total widths of these intervals (right). **4 sl 4-fermis; electron-specific; only  $C_{lq}^-$  and  $C_{\varphi q}^-$**

# top- $b$ synergies future (Belle II+HL-LHC+CLIC)



**Figure 8:** Constraints on coefficients  $\tilde{C}_i$  from fits to top-quark and  $B$  data and near-future projections at HL-LHC and Belle II in Tabs. 1-?? and CLIC future projections in Tab. 2. Shown are the marginalized smallest intervals containing 90 % posterior probability (left) and the total widths of these intervals (right). synergies for semileptonic 4-fermi operators

# b-anomalies today, near, far (Belle II+HL-LHC+CLIC)



1D and 2D (right) projections of the posterior distribution for  $\tilde{C}_{lq}^{(1)}$  and  $\tilde{C}_{lq}^{(3)}$ ; star denotes SM. **b-anomalies become visible in future fit**

- Synergies between beauty and top are reality [Fox et al 2007](#), [Bissmann '21](#), [Brugisser '21](#) and do work!
- Semileptonic 4-fermion operators connect top to  $b$ -anomalies  
CMS reports constraints on semileptonic four-fermion operators from tops with leptons [2012.04120](#); weaker than our bounds for  $C_{qe}, C_{lq}^-$ , but CMS also probes  $C_{eu}, C_{lu}$  which are NOW unconstrained.
- In view of  $b$ -anomalies hinting at universality violation lepton specific fits become desirable
- Global fits have sensitivity to flavor — exploit more flavor links
- Merge with other sectors (EWK, Higgs,...)