

Impact of Jet data on PDFs

Lucian Harland-Lang, University of Oxford

Jets and their Substructure from LHC data, 31
May 2021

*In collaboration with Shaun Bailey, Tom
Cridge, Alan Martin and Robert Thorne*

With special thanks to Emanuele Nocera and Alex Huss

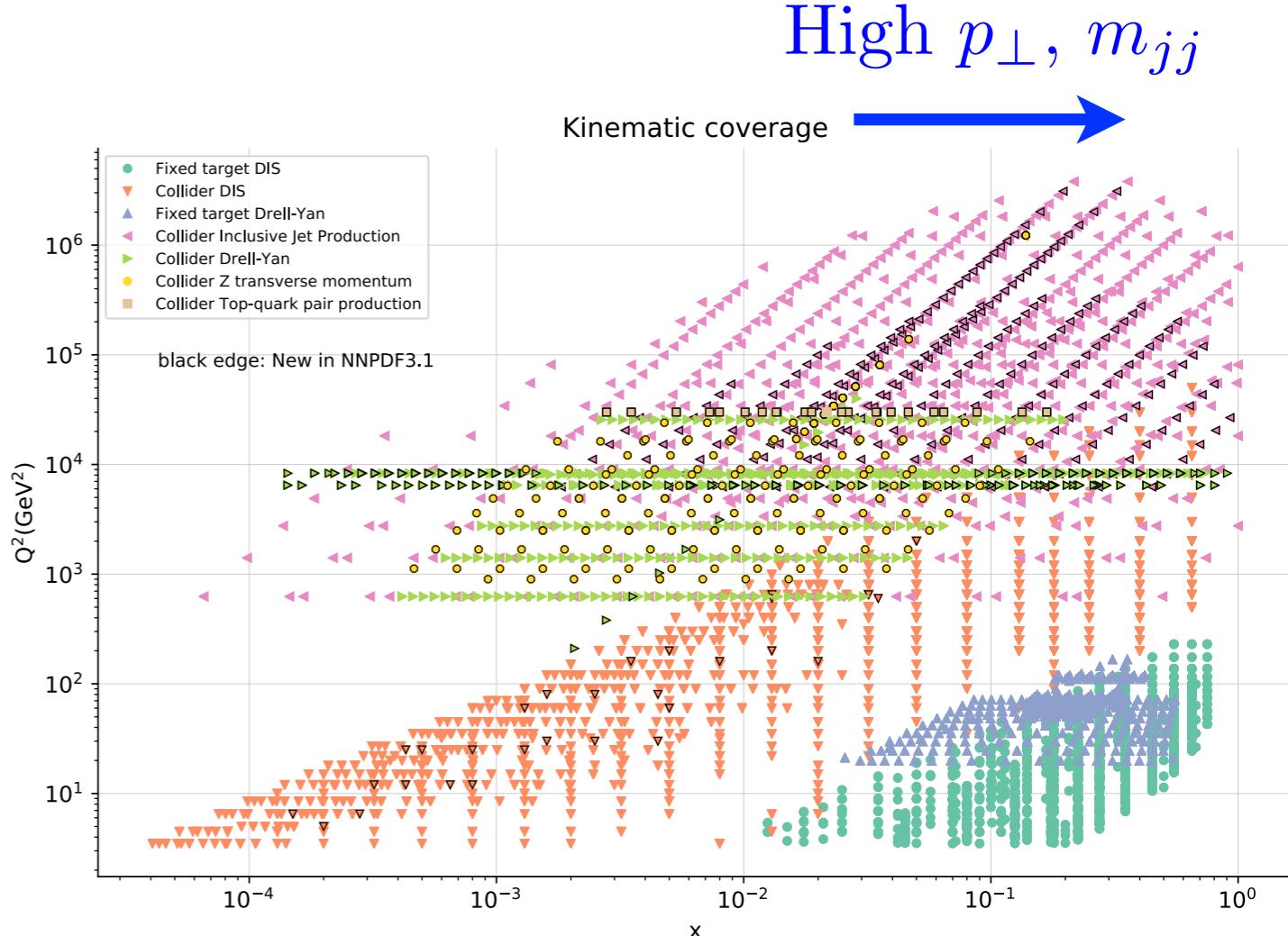


Jets for PDF fits

- Jet production a **key ingredient** in modern PDF fits.
- Sensitive to gluon and quark initial states:

$$gg \rightarrow gg, gg \rightarrow q\bar{q}, gq \rightarrow gq, q\bar{q} \rightarrow gg, \\ q\bar{q} \rightarrow q\bar{q}, q\bar{q} \rightarrow q'\bar{q}', q\bar{q}' \rightarrow q\bar{q}', qq \rightarrow qq, qq' \rightarrow qq',$$

- By pushing to larger jet p_\perp (dijet m_{jj}) go to larger x .
- Though quark-initiated contribution can be large, these are rather well constrained (DIS).
- Hence, jet data particularly relevant for **gluon** at high x (less well constrained).



- NNLO QCD (and NLO EW) theory available for both inclusive and dijet data.

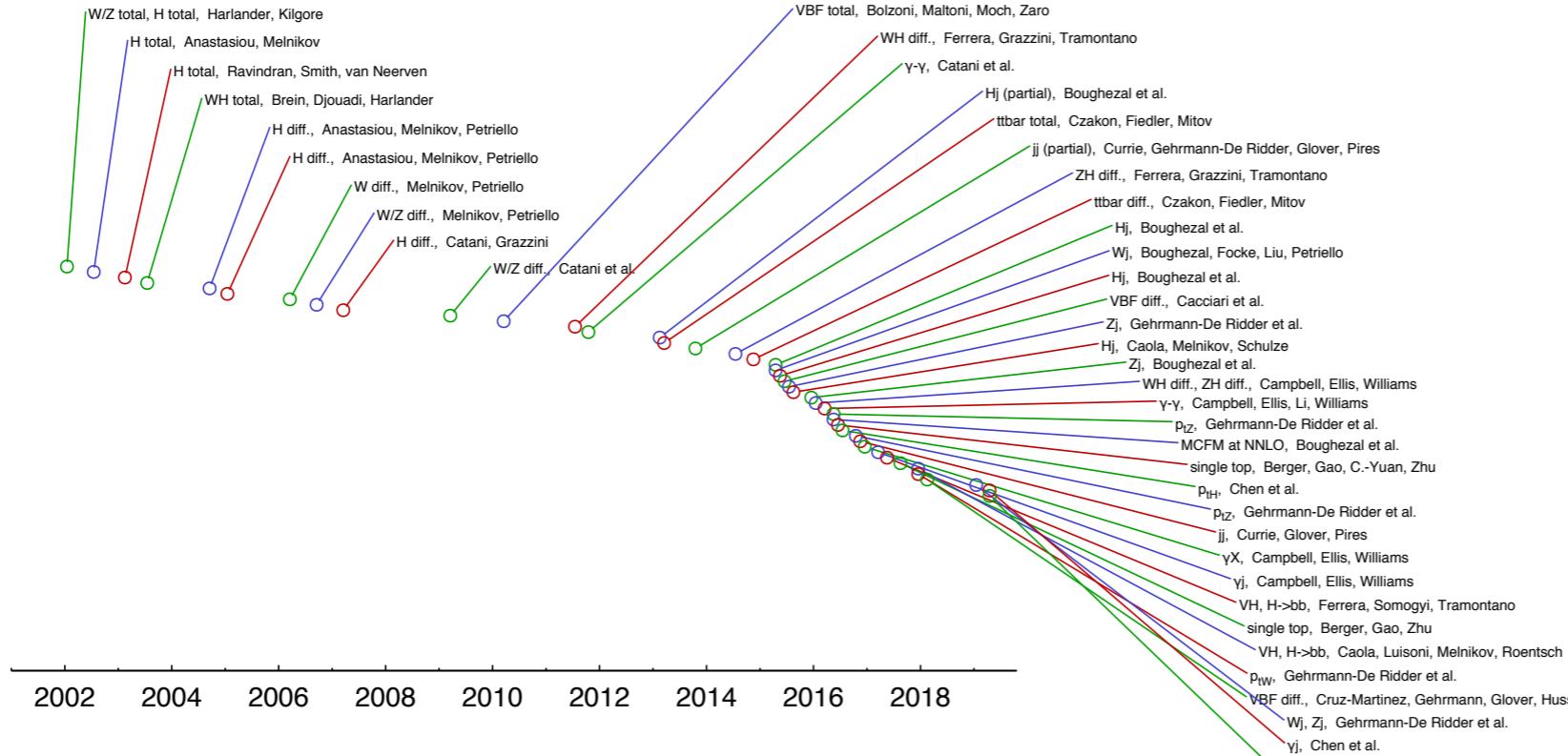


Image Credit: Gavin Salam

See T.
Gehrmann's Talk

- As we will see a key ingredient in fitting these data (particularly dijets).
- In addition, significant amount of inclusive jet and dijet **data** from LHC. High **precision** and spanning large range of kinematic space.

See B. Bilin and P.
Starovoitov talks

Jet Kinematics: Inclusive

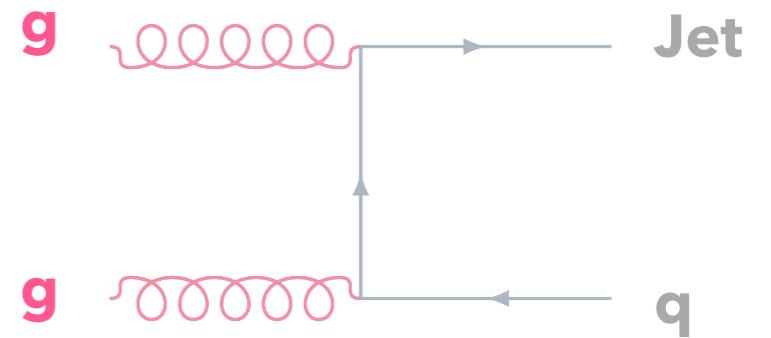
- Inclusive jets measured in terms of jet p_\perp and y_j .
- Schematically, **LO** relationship to high x parton:

$$x = \frac{p_\perp}{\sqrt{s}} (e^{y_j} + e^{y_{j'}})$$

Observed Jet j ($y_j > 0$)
‘Unobserved’ Jet j'

→ Need 3 kinematic inputs to uniquely determine x .

- Inclusive jets: effectively integrate over $x \gtrsim \frac{p_\perp}{\sqrt{s}} e^{y_j}$.
- So certainly sensitive to high x region, but washed out somewhat.



Jet Kinematics: Dijets

- For dijets, both jets measured. Same schematic **LO** relationship:

$$x_{1,2} = \frac{p_\perp}{\sqrt{s}} (e^{\pm y_j} + e^{\pm y_{j'}})$$

- Double differential measurements in terms of m_{jj} and y^*/y_{\max} : not sufficient to uniquely pin down LO x .
- That is, some washing out (though precise effect depends on choice of variable).
- However, also possible to measure triple differentially - expect to provide stronger, more direct constraints.

$$d^3\sigma/dp_{\perp,avg} dy_b dy^*$$

See J.Stark's/K.
Rabbertz's talks

Jets in MSHT20

S. Bailey et al., *Eur.Phys.J.C* 81 (2021) 4, 341

Parton distributions from LHC, HERA,
Tevatron and fixed target data:

MSHT20 PDFs

- The ‘Post-Run I’ set from the MSTW, MMHT... group:
MSHT20.

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[h] 20 Dec 2020

Abstract

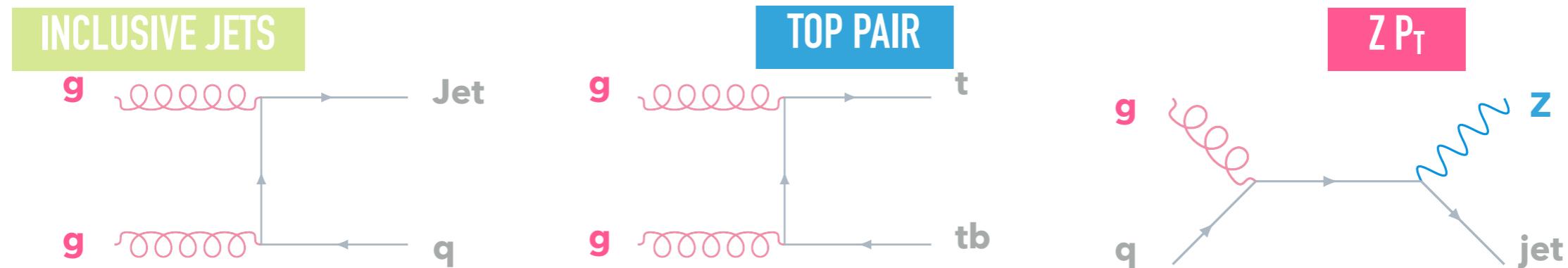
We present the new MSHT20 set of parton distribution functions (PDFs) of the proton, determined from global analyses of the available hard scattering data. The PDFs are

- Focus on including significant amount of **new data**, higher **precision theory** and on **methodological improvements**.
NNLO, χ^2/N_{pt}
- Range of inclusive LHC jet dat fit:

ATLAS 7 TeV jets [18]	221.6/140
CMS 2.76 TeV jet [107]	102.9/81
CMS 7 TeV jets [100]	175.8/158
CMS 8 TeV jets [101]	261.3/174
- Fit quality acceptable. Impact tied up with other high x gluon sensitive data....

High x gluon: global sensitivity

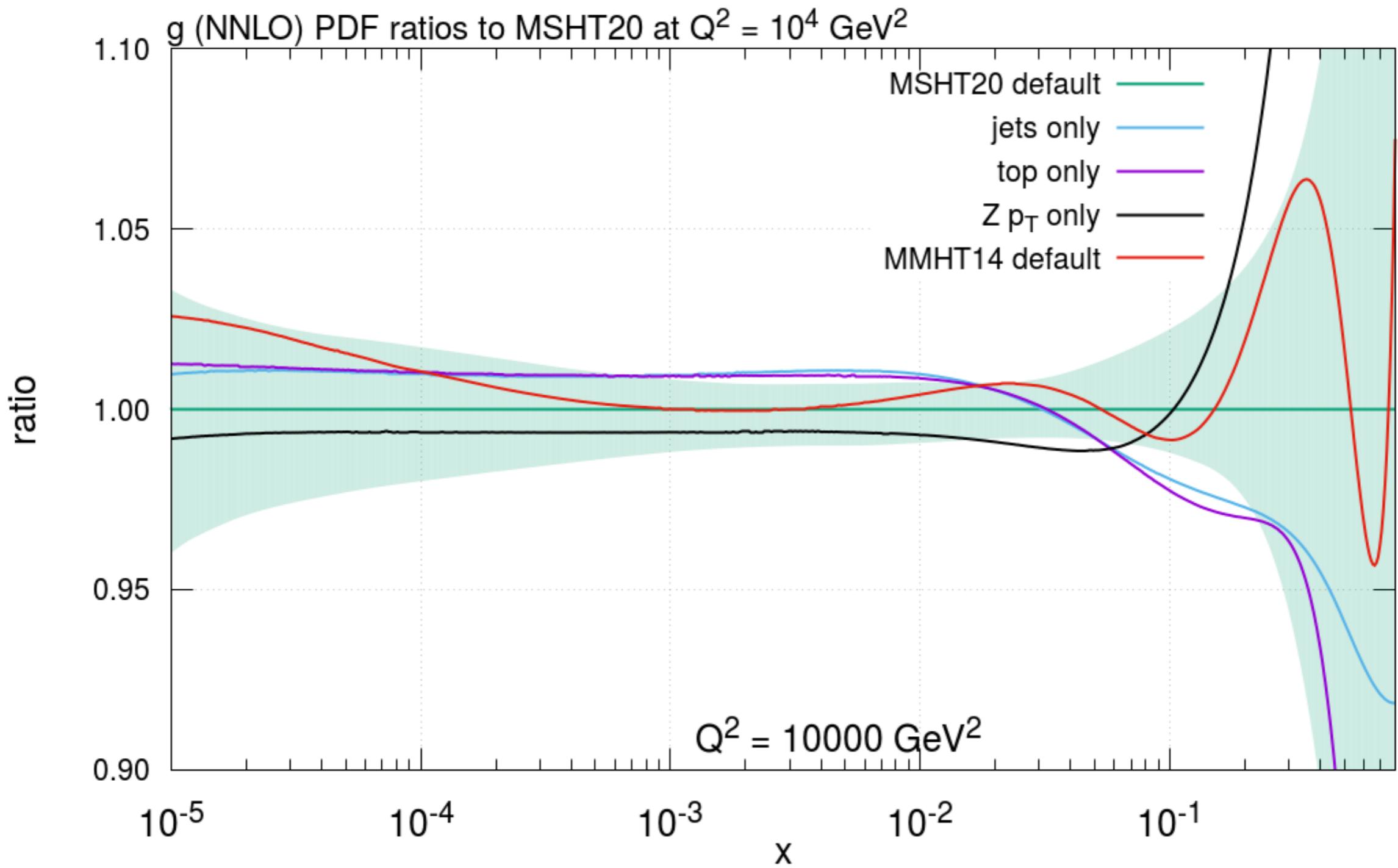
- Jet data one of three major LHC datasets with potential significant impact on high x gluon.



M. Ubiali, Higgs Coupling 2019

- NNLO QCD + high precision multi-differential data available.
 - **High precision** PDF determination.
- Caveats: various issues in fit quality in all three cases.
- In terms of gluon impact, these do not pull in same direction (for MSHT).

S. Bailey et al., *Eur.Phys.J.C* 81 (2021) 4, 341
S. Bailey and LHL., *Eur.Phys.J.C* 80 (2020) 1, 60
LHL, R.S. Thorne and A.D. Martin., *Eur.Phys.J.C* 78 (2018) 3, 248



- **MSHT20**: top and jet data pull in (roughly) same direction, i.e. lower high x gluon. $Z p_\perp$ prefers the opposite.
- Final result a **balance** between these. Important to bear in mind: impact on PDFs in global fit and not in isolation!

Fitting Jets

- Is fit quality good? For jets well beyond simple:

$$\chi^2 = \sum_{k=1}^{N_{\text{pt}}} \frac{(D_k - T_k)^2}{s_k^2}$$

- In particular, measurements often dominated by systematic errors and their **correlations**:

- Fit quality accounts for these, and can be dominated by them:

$$\chi^2(\{a\}, \{\lambda\}) = \sum_{k=1}^{N_{pt}} \frac{1}{s_k^2} \left(D_k - T_k - \sum_{\alpha=1}^{N_\lambda} \beta_{k,\alpha} \lambda_\alpha \right)^2 + \sum_{\alpha=1}^{N_\lambda} \lambda_\alpha^2 ,$$

$$D_k \rightarrow D_k - \sum_{\alpha=1}^{N_\lambda} \beta_{k,\alpha} \hat{\lambda}_\alpha$$

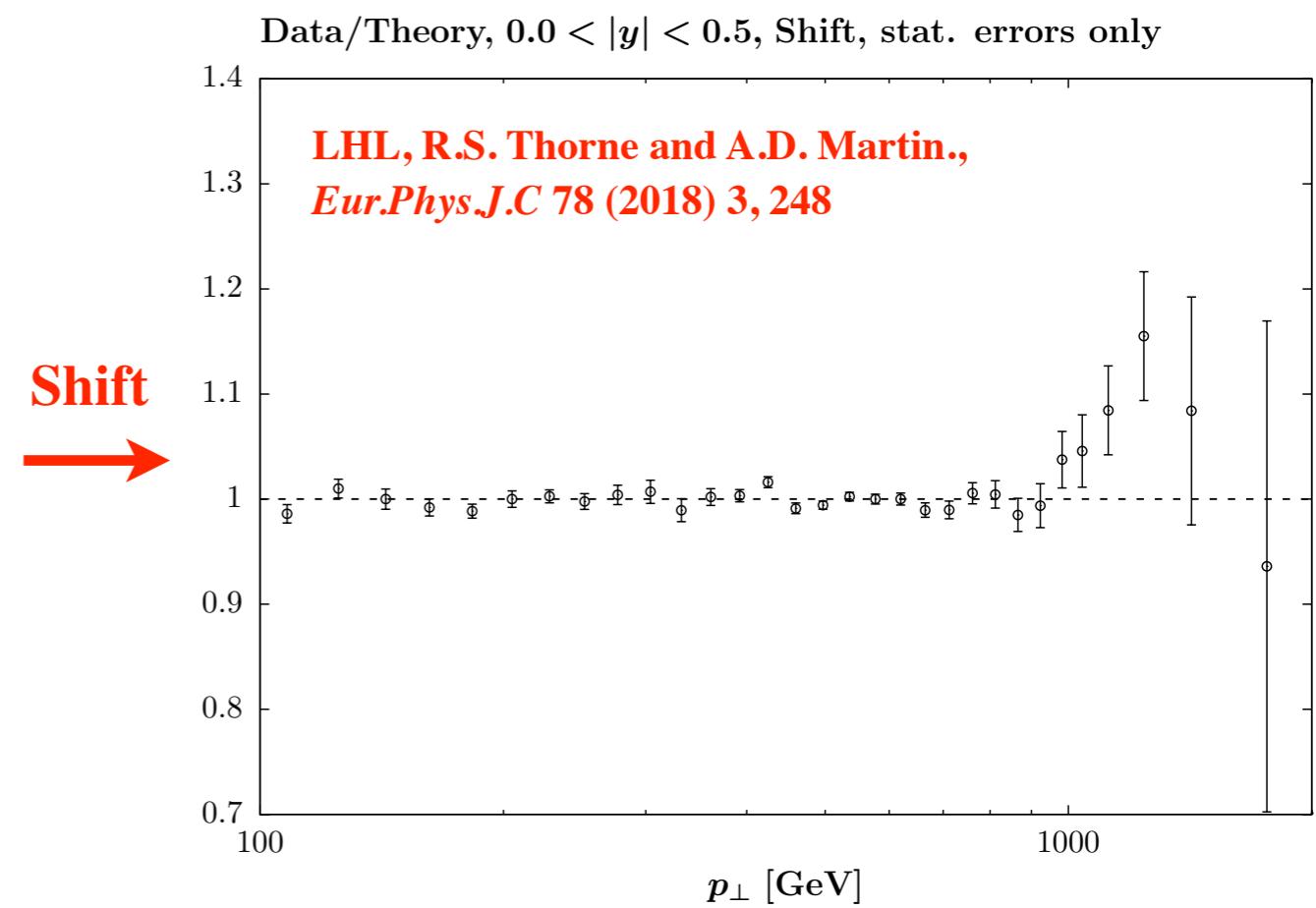
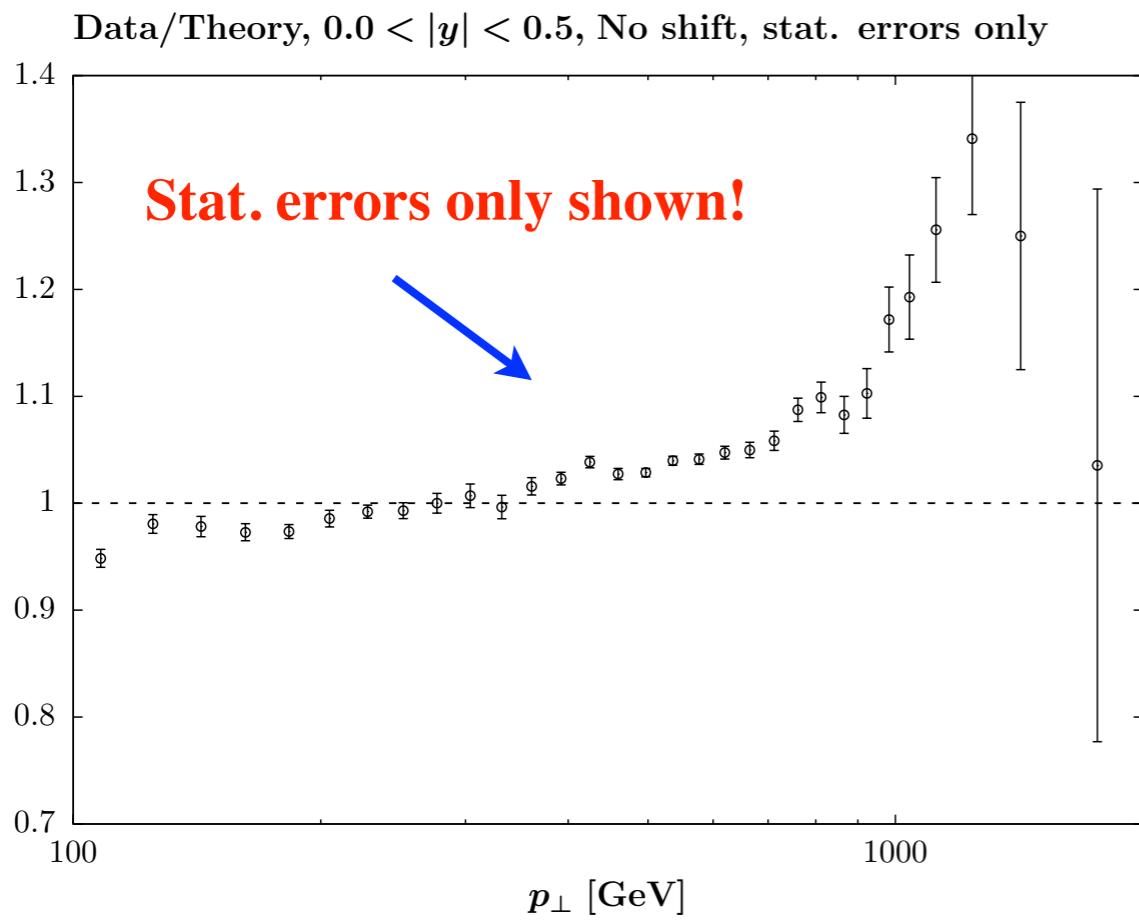
Uncorrelated errors

$$-\left(\sum_{\alpha=1}^{N_\lambda} \beta_{k,\alpha} \lambda_\alpha\right)^2 + \sum_{\alpha=1}^{N_\lambda} \lambda_\alpha^2,$$

↑ ↑
Correlated errors **Penalty for shifts**

Fitting Jets

- This issue/question arises in e.g. description of ATLAS 7, 8 TeV jet data. Provided differentially in p_\perp for various jet rapidity bins.
- Studied in [arXiv:1711.05757](#). 7 TeV data can be v. well fit for single rapidity bin, but not all in combination.
- Can also get good fit with systematics correlated only within rapidity bins.
- This is clearly too strong a choice, but indicates sensitivity.



- Fitting to e.g. just one rapidity bin throws away information and does not resolve underlying issue.
- In some cases due to two-point model variations - can certainly loosen.
Dedicated ATLAS study on this.
- We follow this in MSHT fits:

ATLAS 7 TeV χ^2/N_{pt}

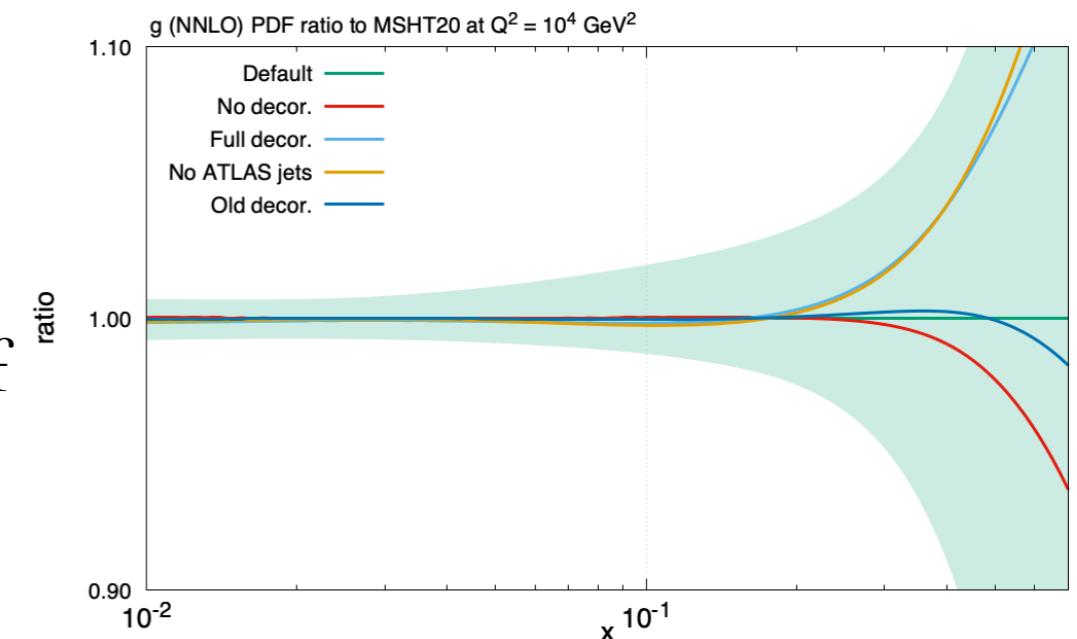
ATLAS Collab., JHEP 09 (2017) 020

Splitting options for $R = 0.4$	CT14	NNPDF3.0
JES Flavour Response Opt 7		
JES MJB Fragmentation Opt 17		
JES Pile-up Rho topology Opt 18		
Scale variations Opt 17		
Alternative scale choice Opt 7		
Non-perturbative corrections Opt 7	268/159	257/159

S. Bailey et al., Eur.Phys.J.C 81 (2021) 4, 341

	No decor.	Ref. [15] decor.	Smooth decor.	Full decor.
LO _{EW}	2.00	1.09	1.48	0.81
NLO _{EW}	1.80	1.15	1.57	0.92

- Permissible decorrelation improves fit.
Impact on gluon limited (though not zero).
- **However:** level of improvement sensitive to theory input. More complete theory/inclusion of MHO uncertainties may reduce this sensitivity further. Delicate interplay here...



Fitting Jets/Dijets: Recent Studies

Jet Data at the LHC

- Focussing on Run-I data (i.e. current PDF fits):
• Inclusive jets:
 $d^2\sigma/dp_\perp dy$
 $0.0 < |y| < 2.5 - 3.0$
 - ★ CMS 2.76 TeV: 81 points – 5.43 pb^{-1} – $74 < p_\perp < 592 \text{ GeV}$
 - ★ CMS 7 TeV: 158 points – 5.0 fb^{-1} – $74 < p_\perp < 2500 \text{ GeV}$
 - ★ CMS 8 TeV: 174 points – 19.7 fb^{-1} – $60 < p_\perp < 1300 \text{ GeV}$
 - ★ ATLAS 7 TeV: 140 points – 4.5 fb^{-1} – $100 < p_\perp < 2000 \text{ GeV}$
 - ★ ATLAS 8 TeV: 171 points – 20.2 fb^{-1} – $70 < p_\perp < 2500 \text{ GeV}$

→ 724 points in total, v.s. ~ 4500 in global MSHT fit (inc.).

- We take the larger of the jet radii available in both cases,
i.e. R=0.6/0.7.

See B. Bilin and P.
Starovoitov talks

- Dijets:

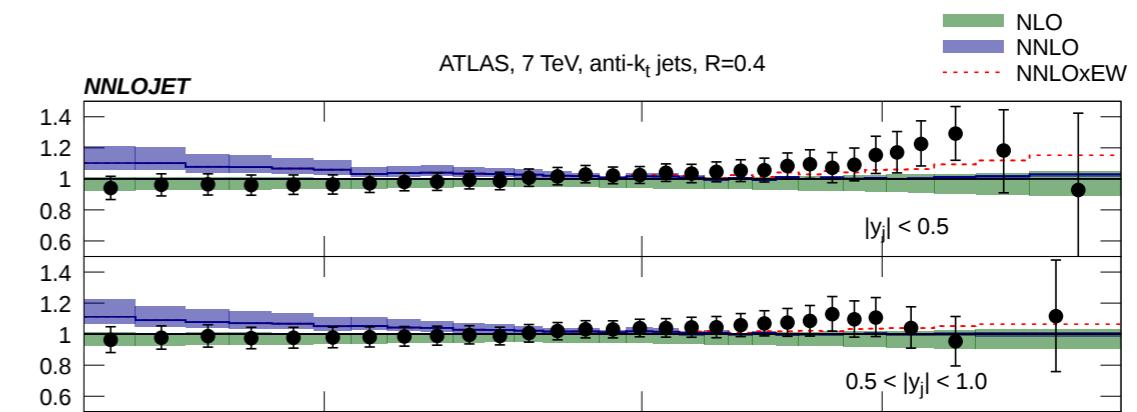
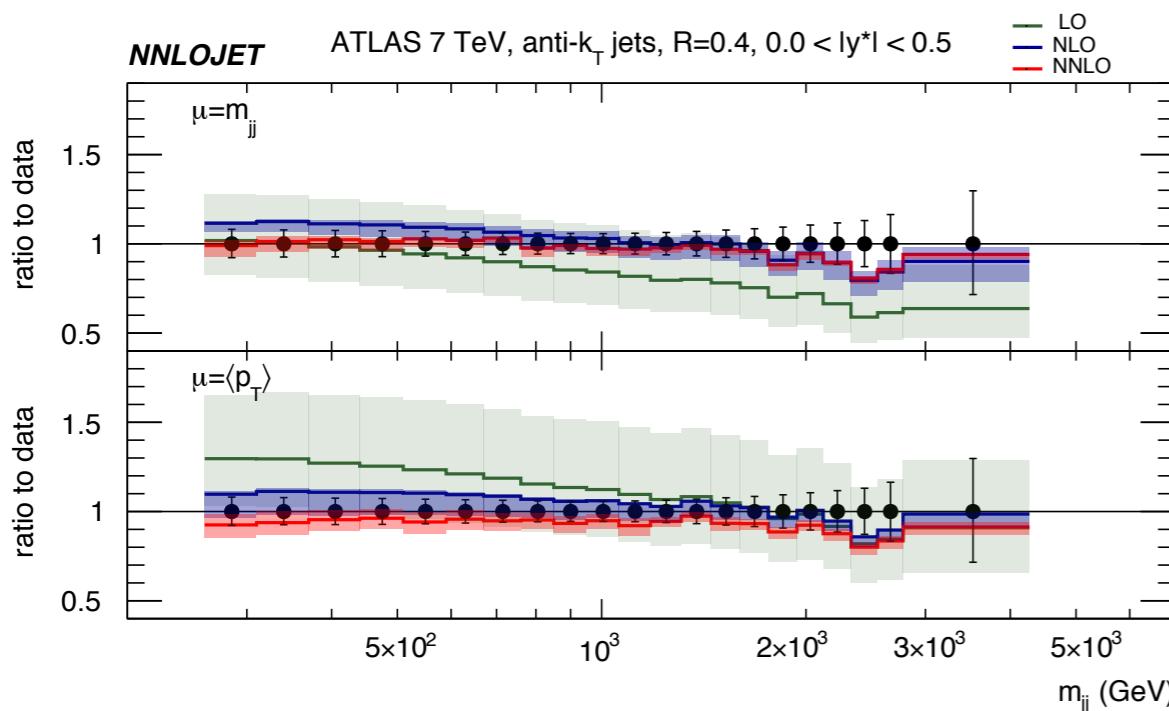
- ★ ATLAS 7 TeV: 90 points – 4.5 fb^{-1} – $\frac{d^2\sigma/dm_{jj}dy_{\max}}{0.26 < m_{jj} < 5.04 \text{ TeV}}$
- ★ CMS 7 TeV: 54 points – 5.0 fb^{-1} – $\frac{d^2\sigma/dm_{jj}dy^*}{0.25 < m_{jj} < 4.48 \text{ TeV}}$
- ★ CMS 8 TeV: 122 points – 19.7 fb^{-1} – $\frac{d^3\sigma/dp_{\perp,avg}dy_b dy^*}{143 < p_{\perp,avg} < 1638 \text{ GeV}}$

→ 266 points in total, v.s. ~ 4000 in global MSHT fit (inc.).

- Again take the larger of the jet radii available in both cases, i.e. R=0.6/0.7.

Fit Quality

- Will consider fits either to 7 + 8 TeV inclusive jets, or to 7 + 8 TeV dijets.
 - MSHT20 baseline, and NNLO QCD + NLO EW, unless otherwise stated.
- Theory from [arXiv:2005.11327](#) + NNLOJET.
- For inclusive jets take $\mu = p_{\perp}^j$, for dijets $\mu = m_{jj}$.
 - Various benchmarks/checks performed, but results presented here **preliminary**.



J. Currie, E.W.N. Glover, J. Pires, Phys.Rev.Lett. 118 (2017) 7, 072002

J. Currie et al., Phys.Rev.Lett. 119 (2017) 15, 152001

- We find:

Dijet fit:

	N_{pts}	χ^2/N_{pt}
ATLAS 7 TeV dijets	90	1.05
CMS 7 TeV dijets	54	1.43
CMS 8 TeV dijets	122	1.04
Total Dijets	266	1.12

Jet fit:

	N_{pts}	χ^2/N_{pt}
ATLAS 7 TeV jets	140	1.53
ATLAS 8 TeV jets	171	1.45
CMS 7 TeV jets	158	1.22
CMS 8 TeV jets *	174	1.80
Total Jets	643	1.50

	N_{pts}	χ^2/N_{pt}
ATLAS $Z p_{\perp}$	104	1.65
Diff. top	54	1.24
7 + 8 TeV Jets	643	[1.62]

Prediction

	N_{pts}	χ^2/N_{pt}
ATLAS $Z p_{\perp}$	104	1.85
Diff. top	54	1.12
7 + 8 TeV Dijets	643	[1.32]

- ★ Fit quality to dijet data very good (1.12), clearly worse for jets (1.50).
- ★ No signs of significant inconsistency in fit vs. predicted χ^2 , though some difference in pull implied.
- ★ Fit quality to top ($Z p_{\perp}$) data better in jet (dijet) fit. Latter particularly notable.
- ★ (Not shown) - fit quality to other data in global fit v. similar.

*NB we use stat. correlations here. Not included by other groups, and leads to deterioration in fit quality.

Impact of HO corrections

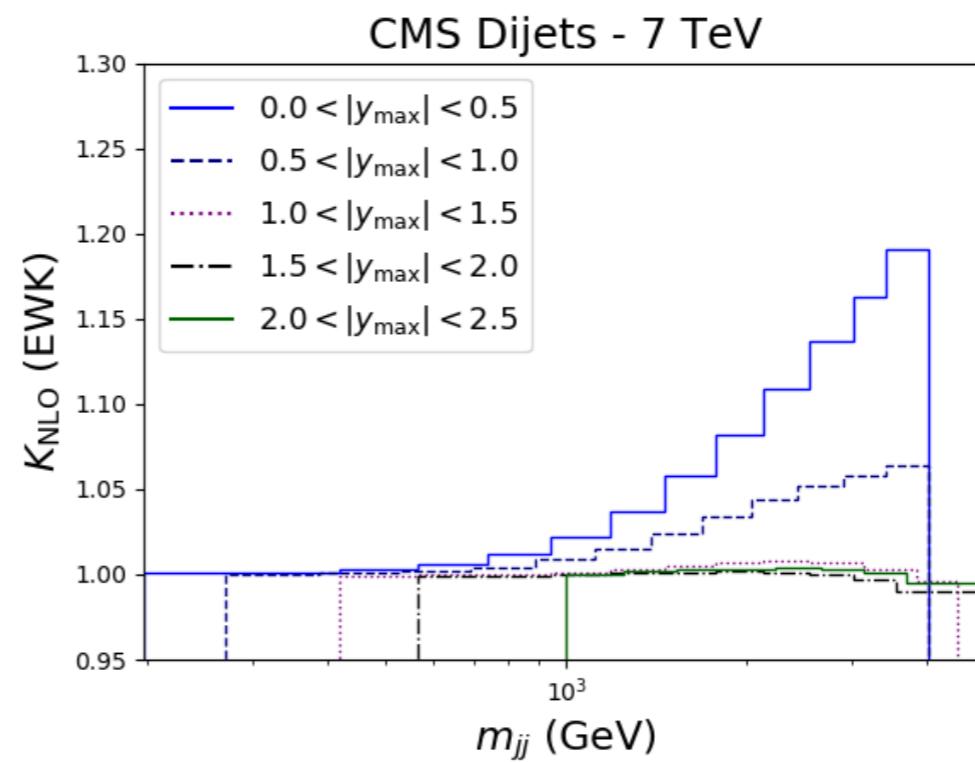
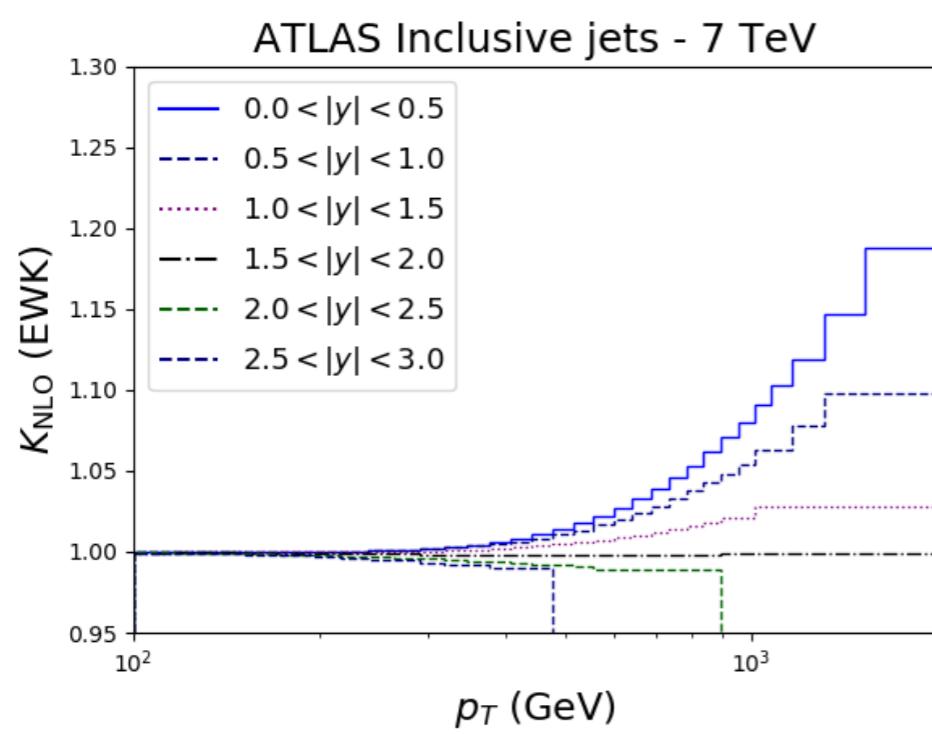
- ★ EW corrections:

Dijet fit: $\chi^2(\text{no EW}) \rightarrow \chi^2(\text{EW}) : 1.34 \rightarrow 1.12$

(NNLO
QCD)

Jet fit: $\chi^2(\text{no EW}) \rightarrow \chi^2(\text{EW}) : 1.39 \rightarrow 1.50$

i.e. we find dijet fit quality improved (driven by CMS 8 TeV), but inclusive (uniformly) deteriorates! Unclear why, but clearly impacts on discussion of relative fit quality.



★ NNLO QCD

corrections.

Jets fit:

	N_{pts}	NLO	NNLO
ATLAS 7 TeV jets	140	1.69	1.53
ATLAS 8 TeV jets	171	2.37	1.45
CMS 7 TeV jets	158	1.38	1.22
CMS 8 TeV jets	174	1.65	1.80
Total Jets	643	<u>1.78</u>	<u>1.50</u>

Dijet fit:

	N_{pts}	NLO	NNLO
ATLAS 7 TeV dijets	90	1.10	1.05
CMS 7 TeV dijets	54	1.71	1.43
CMS 8 TeV dijets	122	5.30	1.04 ←
Total Dijets	266	<u>3.15</u>	<u>1.12</u>

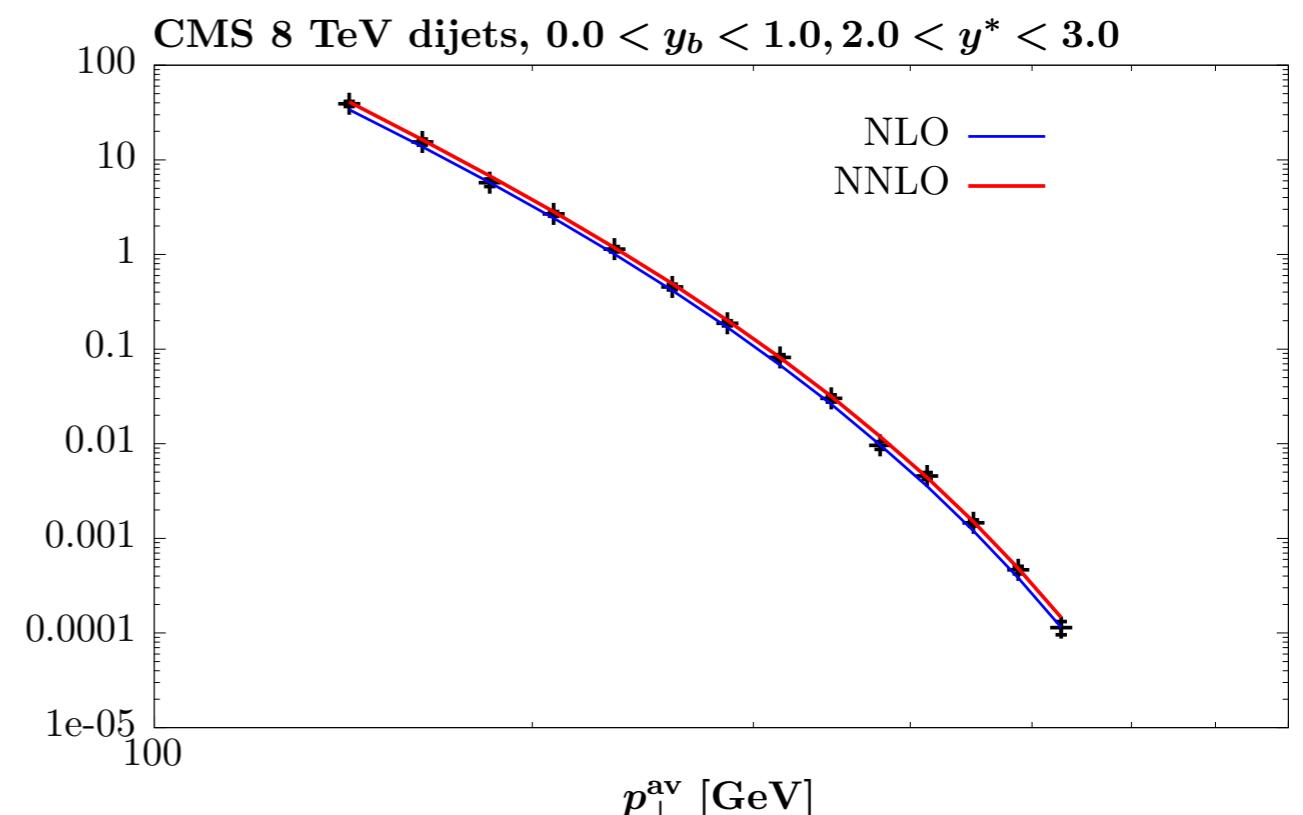
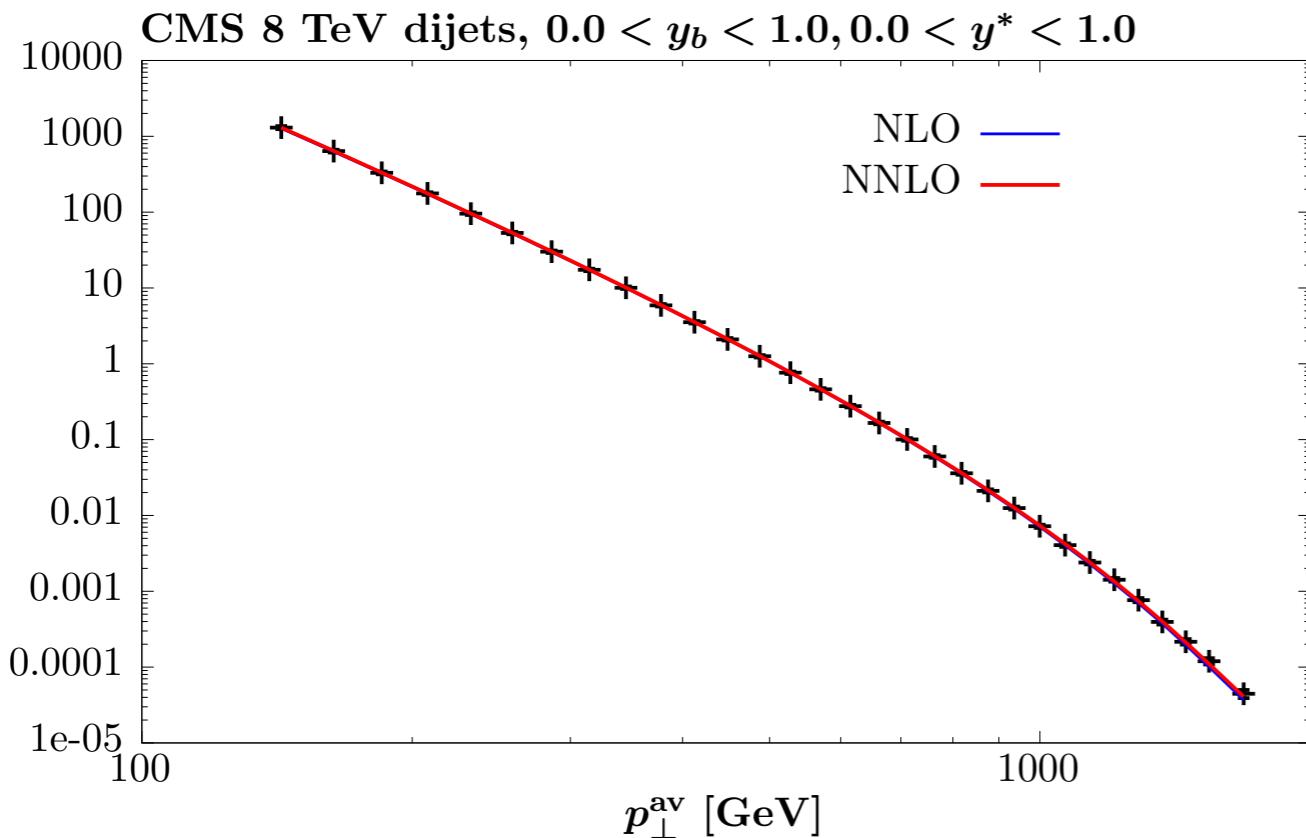
Not a typo!

- ★ Clear trend in both cases for QCD corrections to improve fit quality. pQCD working as it should!
- ★ For jets, this is different to [arXiv:2005.11327](#) trend (though same as in [MSHT20](#)), but note scale different (p_T^j rather than H_T).
- ★ Improvement in CMS 8 TeV dijets particularly remarkable. Clear need for NNLO QCD at high precision LHC (c.f. e.g. ATLAS 7 TeV, W,Z, which gives $5.0 \rightarrow 1.9$). In more detail...

CMS 8 TeV Dijets

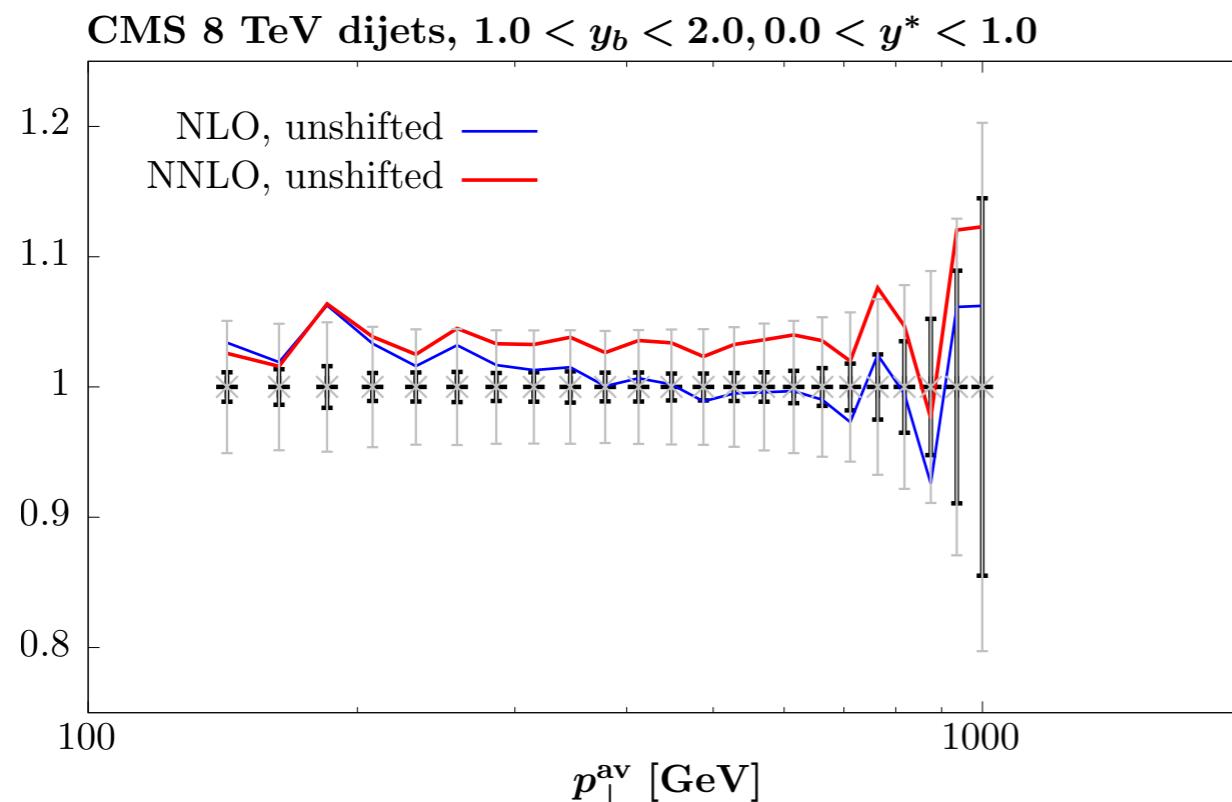
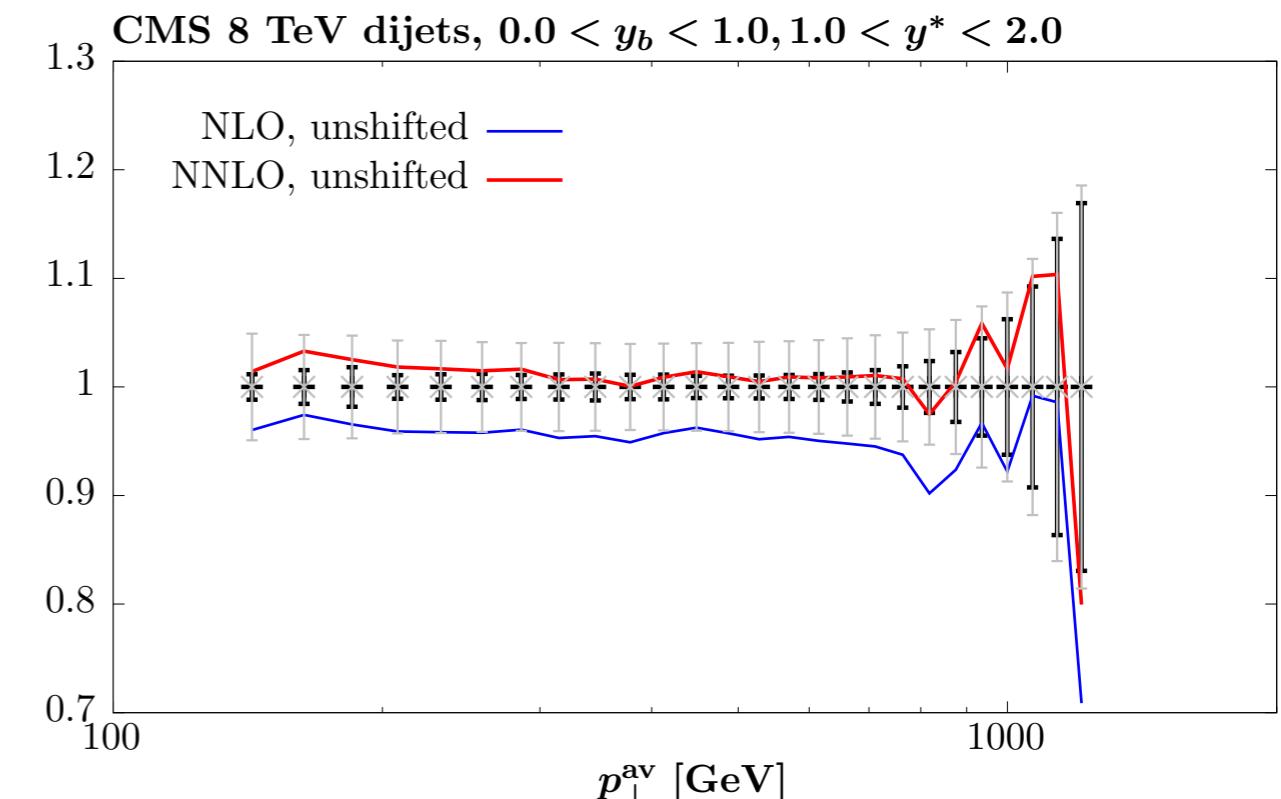
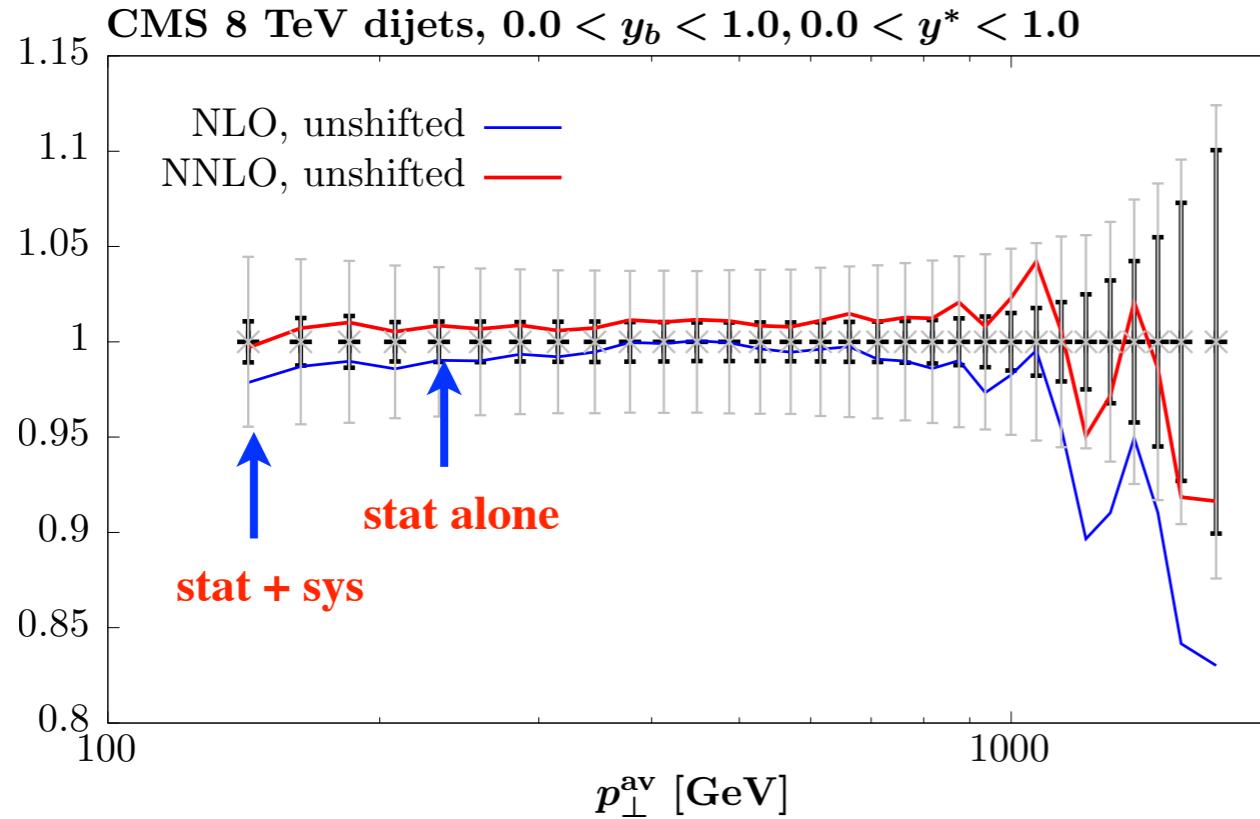
- What is driving this improvement?

$$\frac{d\sigma}{dp_{\perp,avg}} [\text{pb}/\text{GeV}]$$



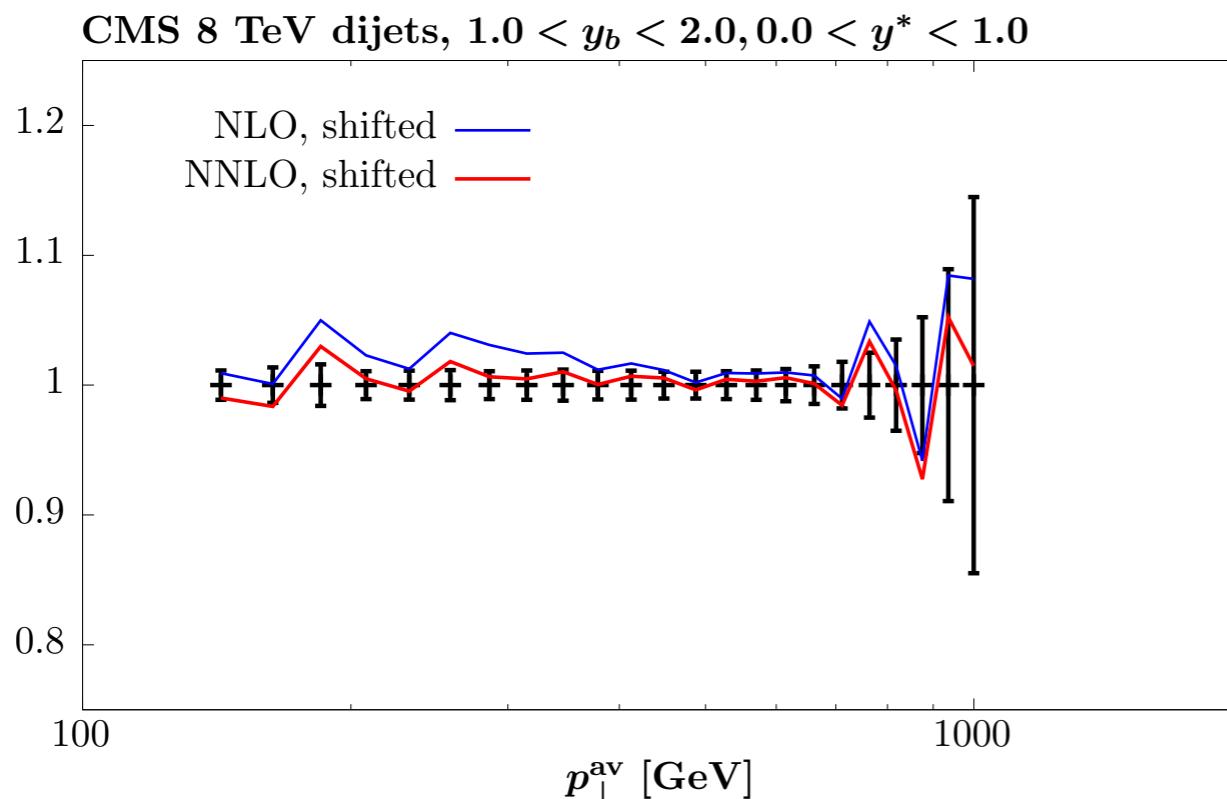
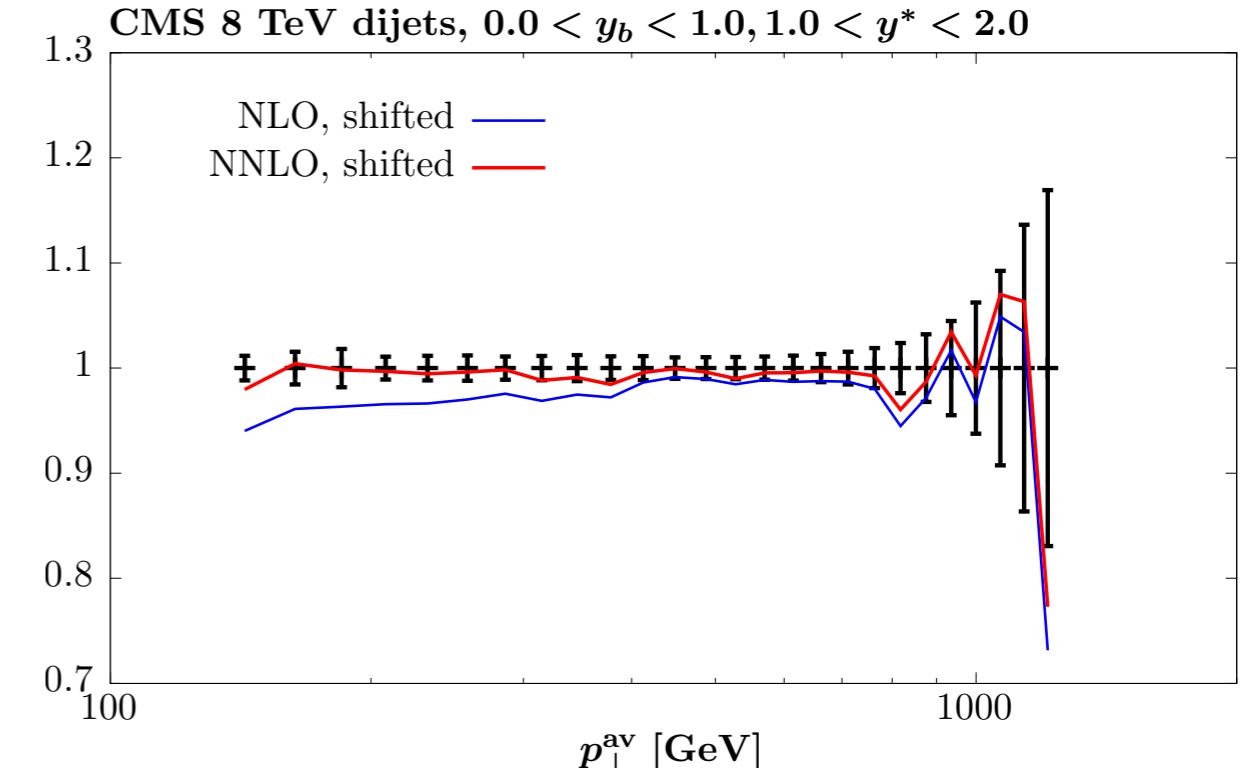
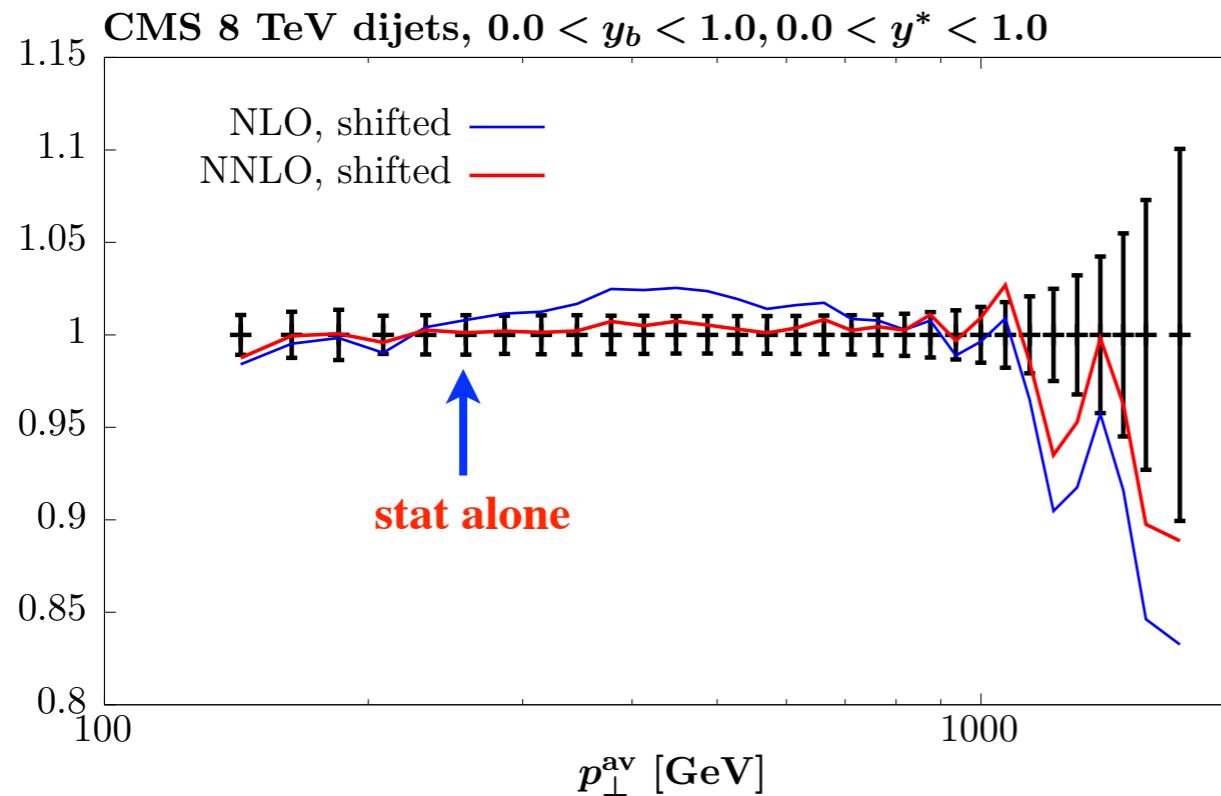
- Focus in on data/theory comparison...

- Overlaying data/theory no clear, by eye, trend for better description at NNLO.



- However this is **before** shifting by correlated systematics.

- After including shifts from correlated systematics:

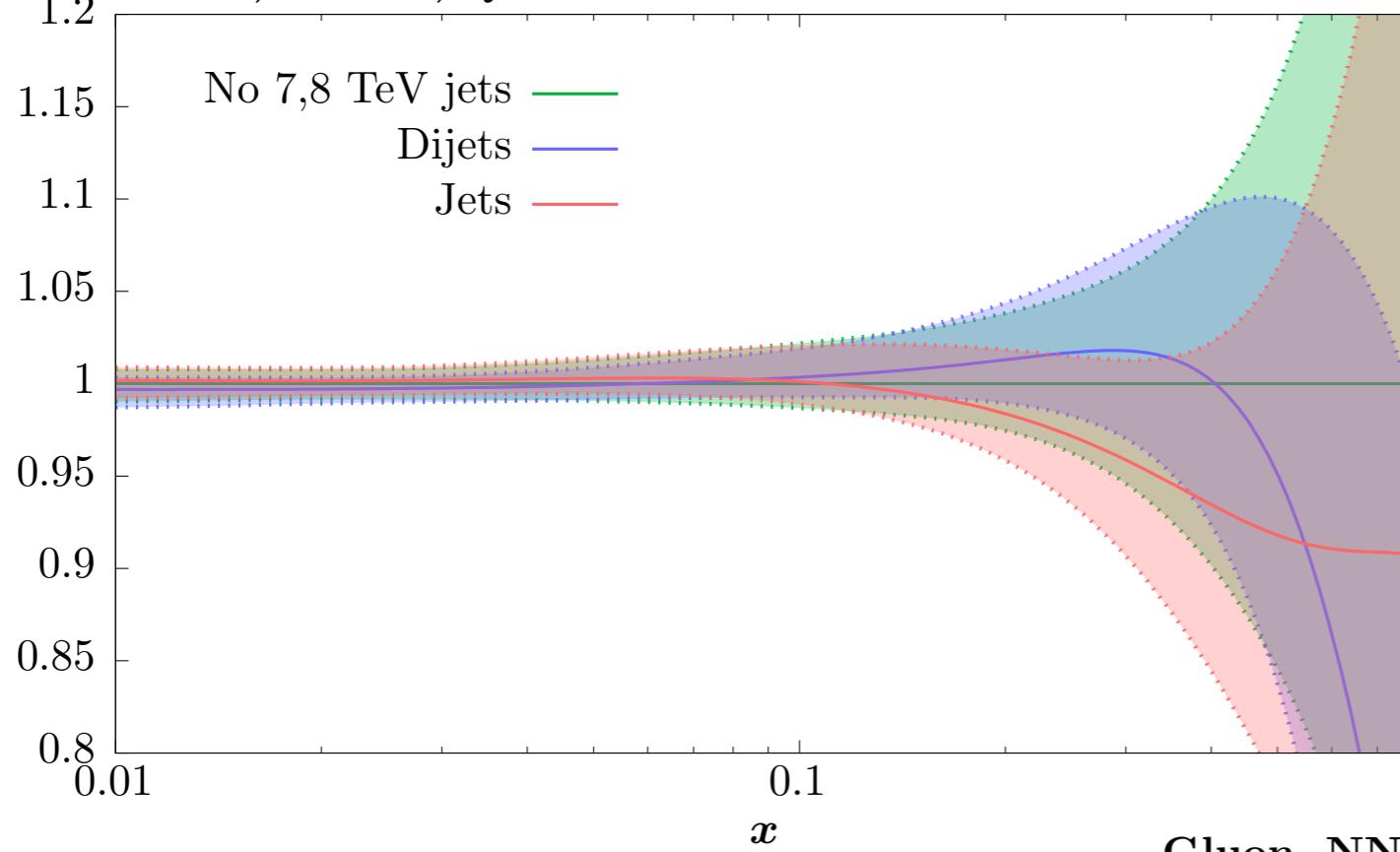


- Now improvement of NNLO is clear.
- Impact on shape of distributions in 3D kinematic space and interplay with correlated systematics drives this.

Impact on PDFs

Dijets vs. Jets

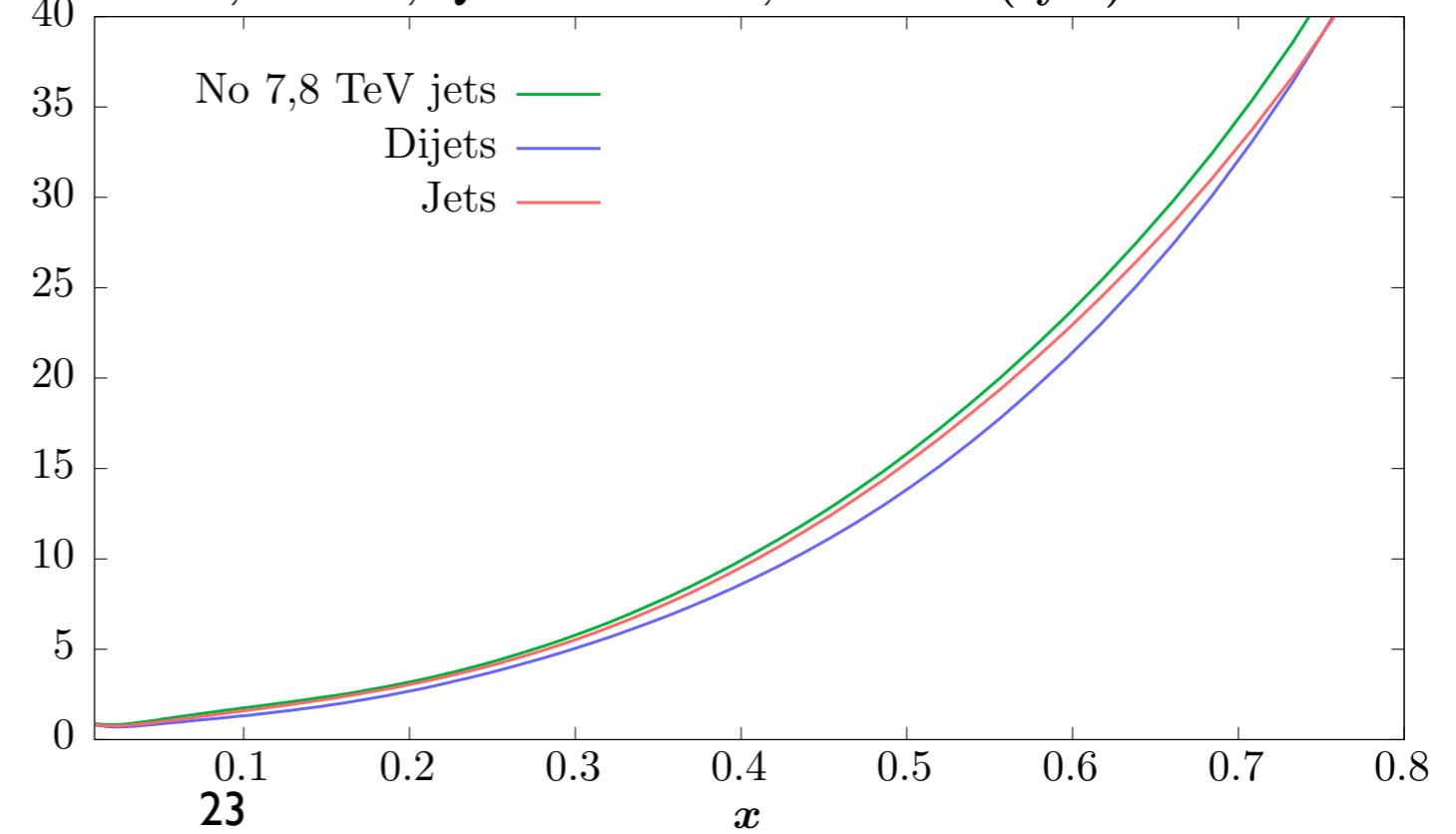
Gluon, NNLO, $Q^2 = 10^4 \text{ GeV}^2$



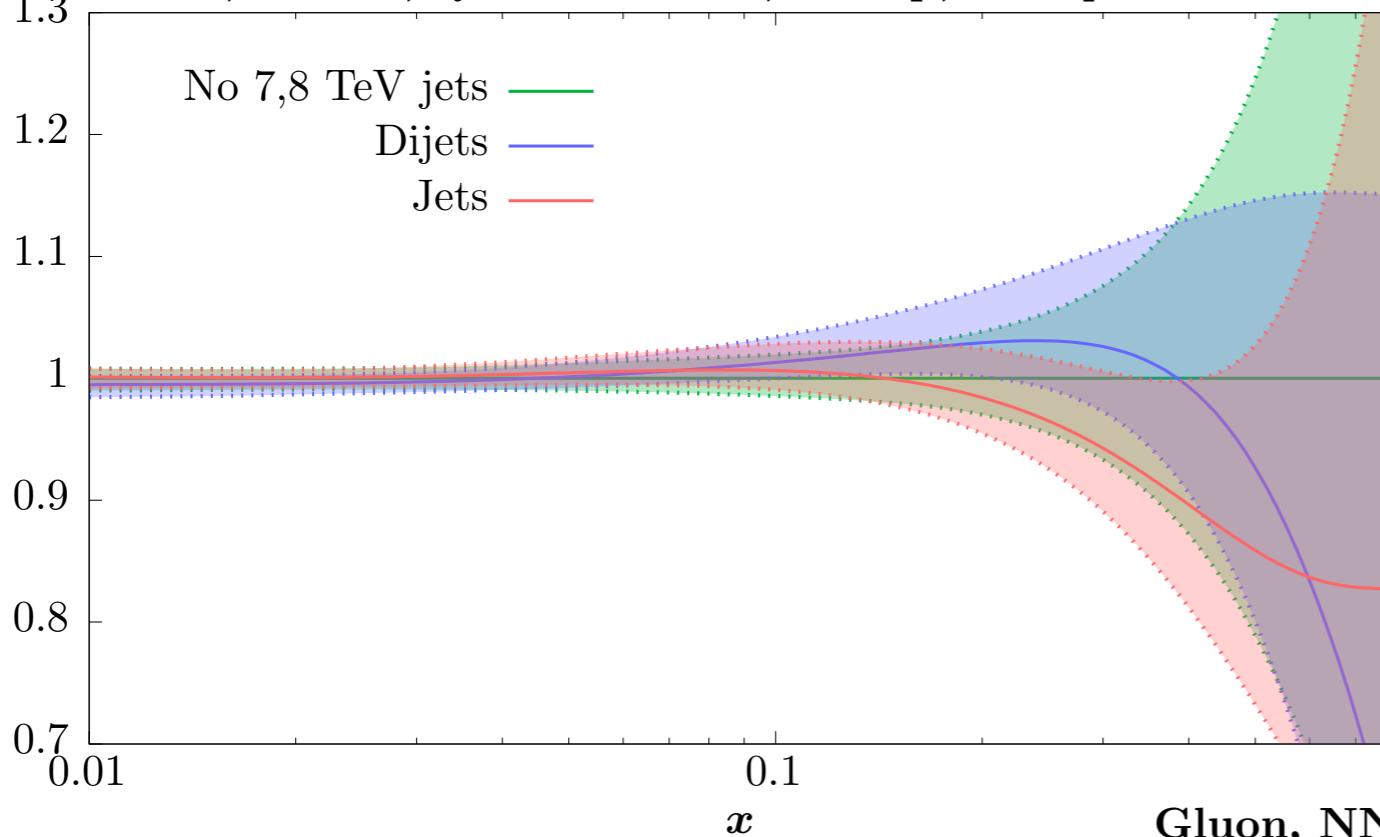
- Impact of jets data on gluon uncertainty very mild. Larger for dijets.

- Add dijets or jets to MSHT20 (no jets) baseline. Focus on gluon here.
- Overall **consistency** between two cases.
- But pull **rather different**.

Gluon, NNLO, $Q^2 = 10^4 \text{ GeV}^2$, % errors (sym)

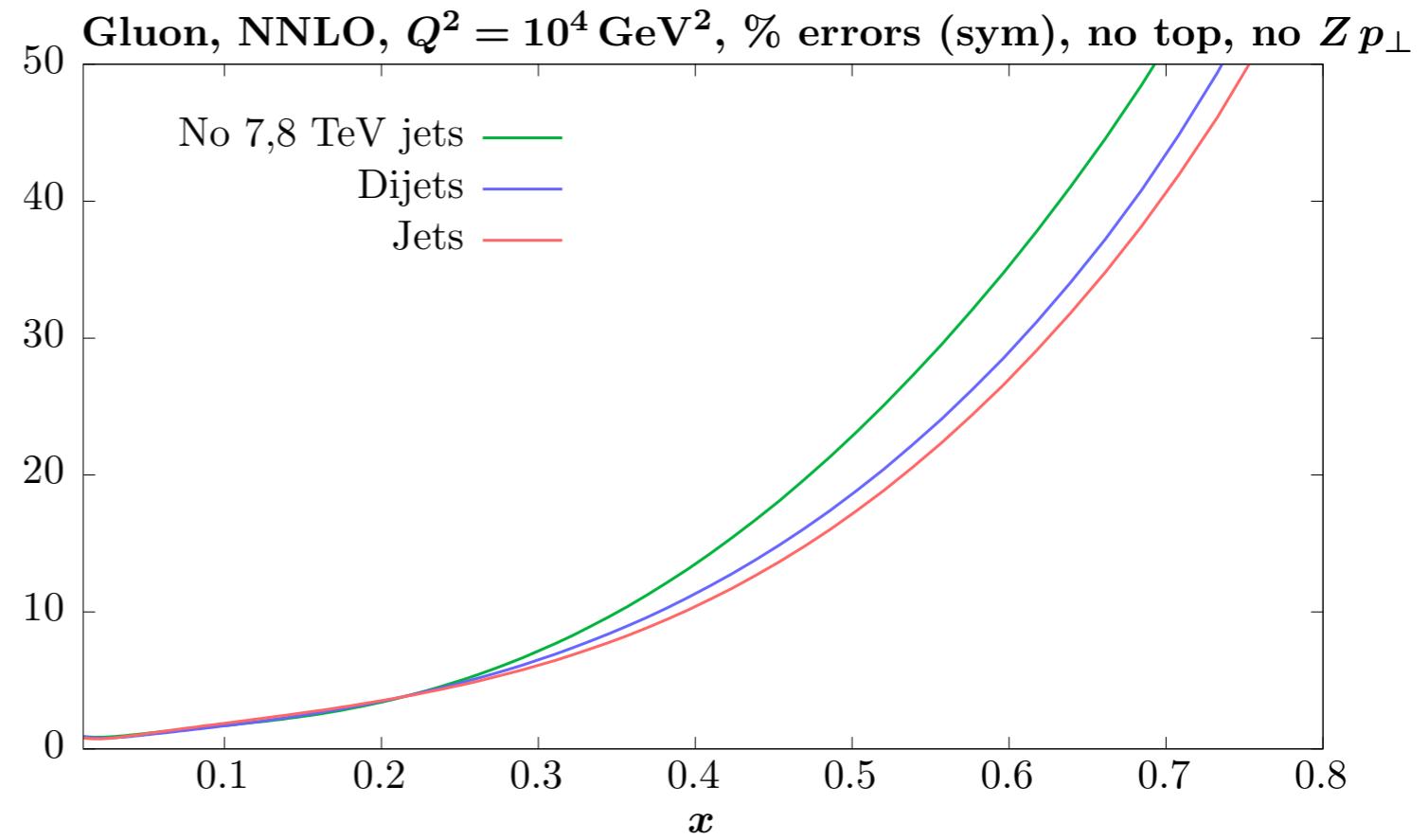


Gluon, NNLO, $Q^2 = 10^4 \text{ GeV}^2$, no top, no $Z p_\perp$



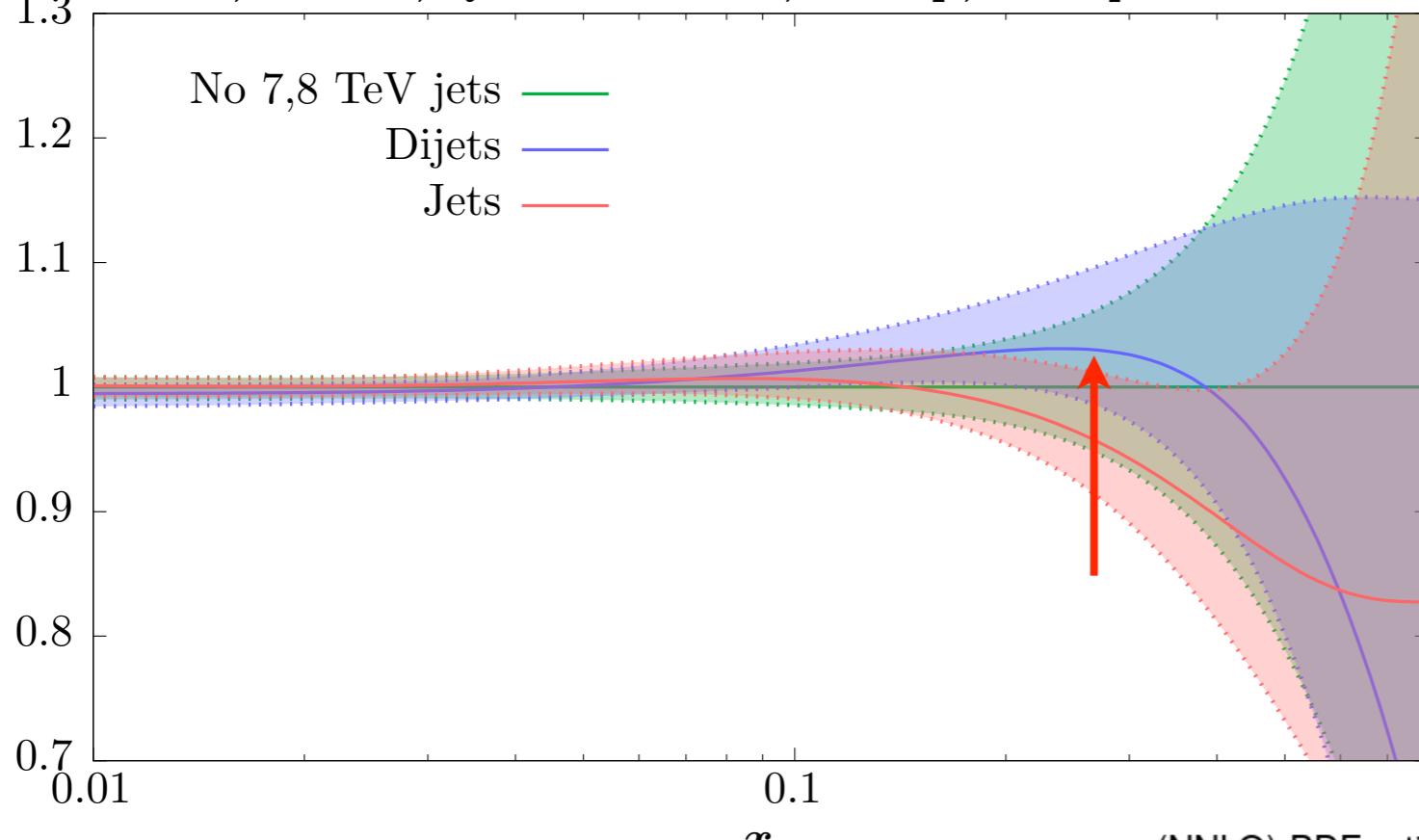
- Now consider fits but added to MSHT20 baseline with no diff. top or $Z p_\perp$.
- Basic pulls as before.

- However relative impact on uncertainty different. Now jets more significant at high x .

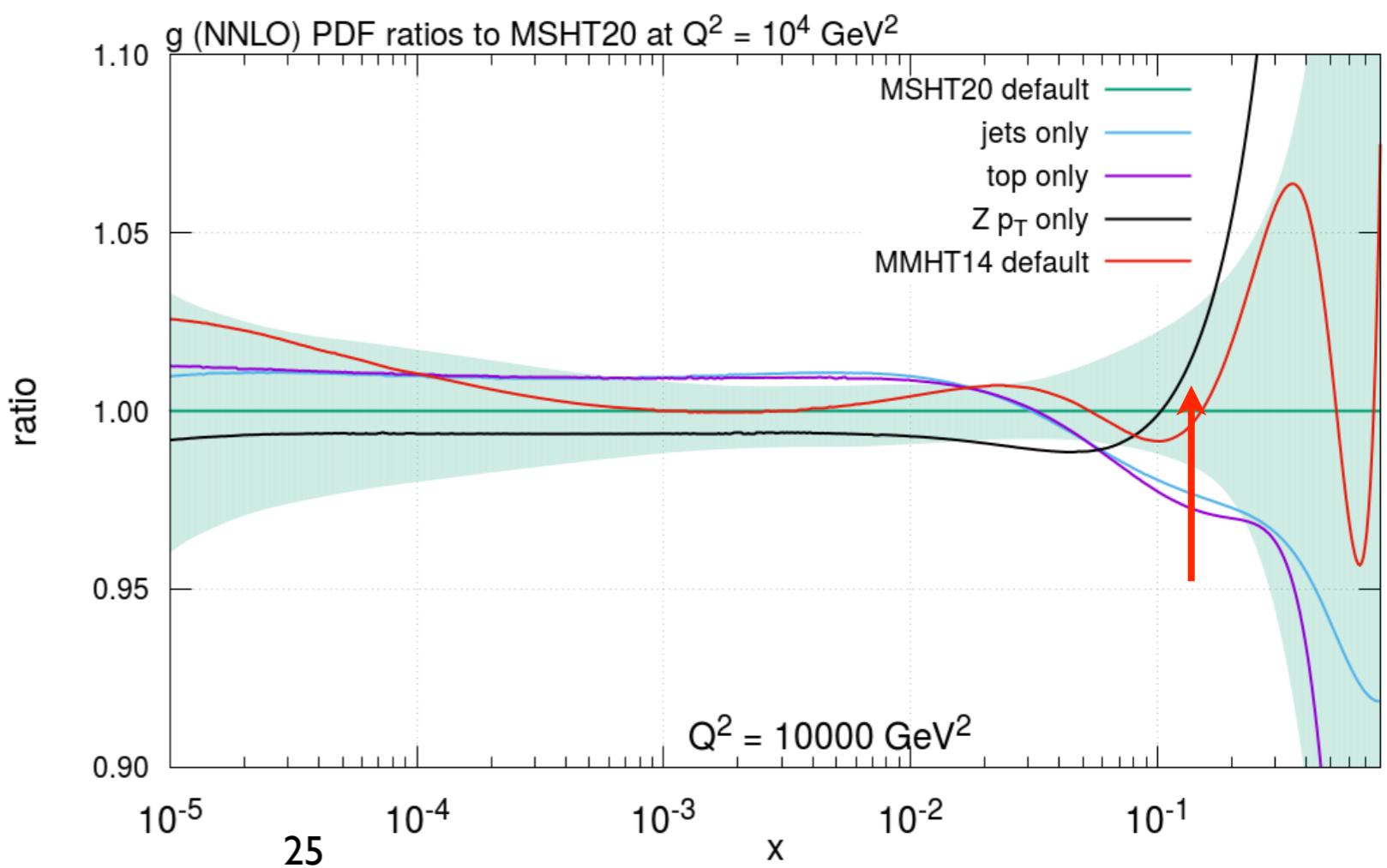


→ Clear that interplay with other data in fit drives impact. In particular greater consistency between dijets and $Z p_\perp$.

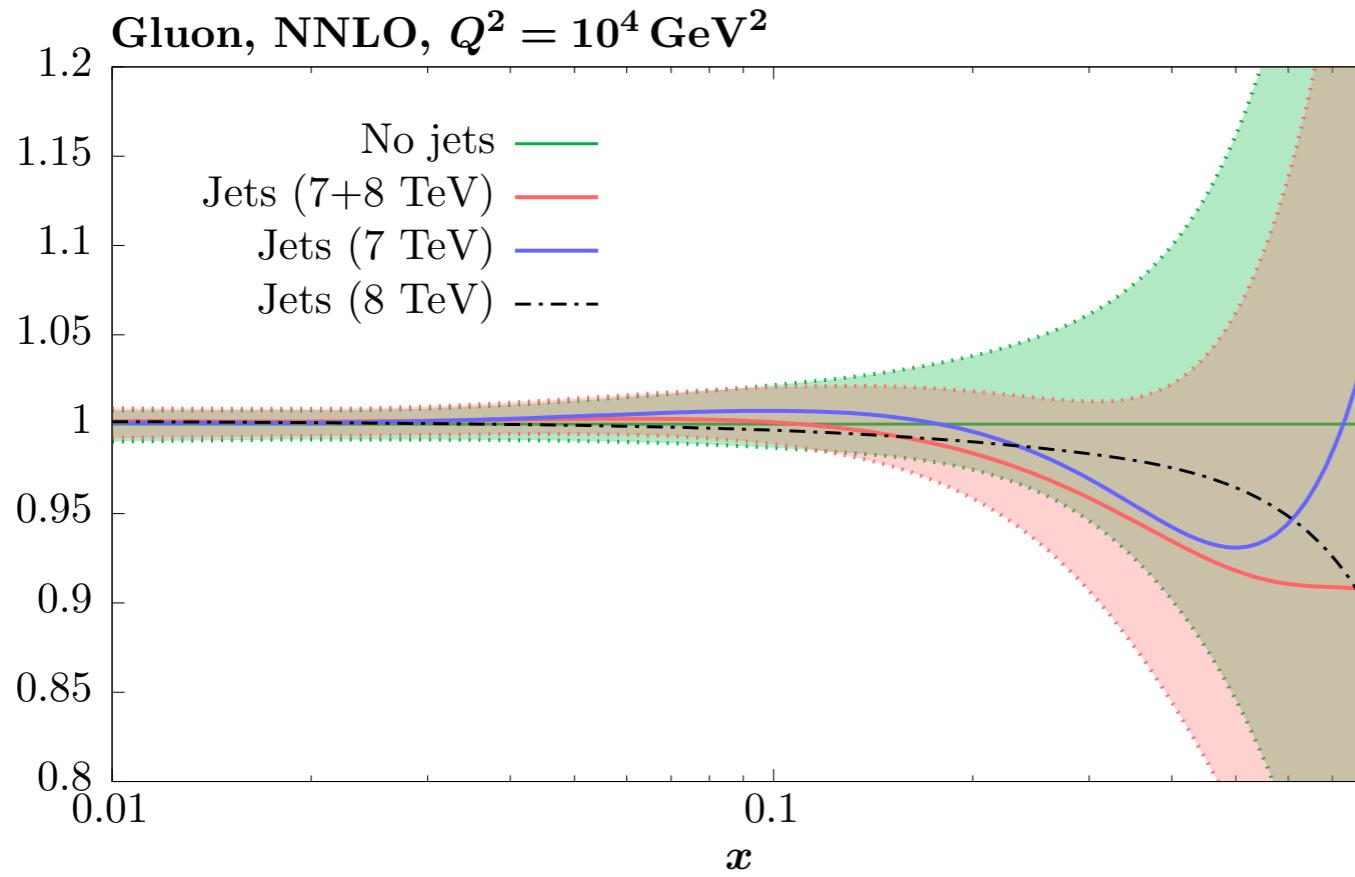
Gluon, NNLO, $Q^2 = 10^4 \text{ GeV}^2$, no top, no $Z p_\perp$



- In more detail, Dijets and both prefer rather higher $Z p_\perp$ gluon in $0.1 \lesssim x \lesssim 0.4$ region ($Z p_\perp$ out to higher x).

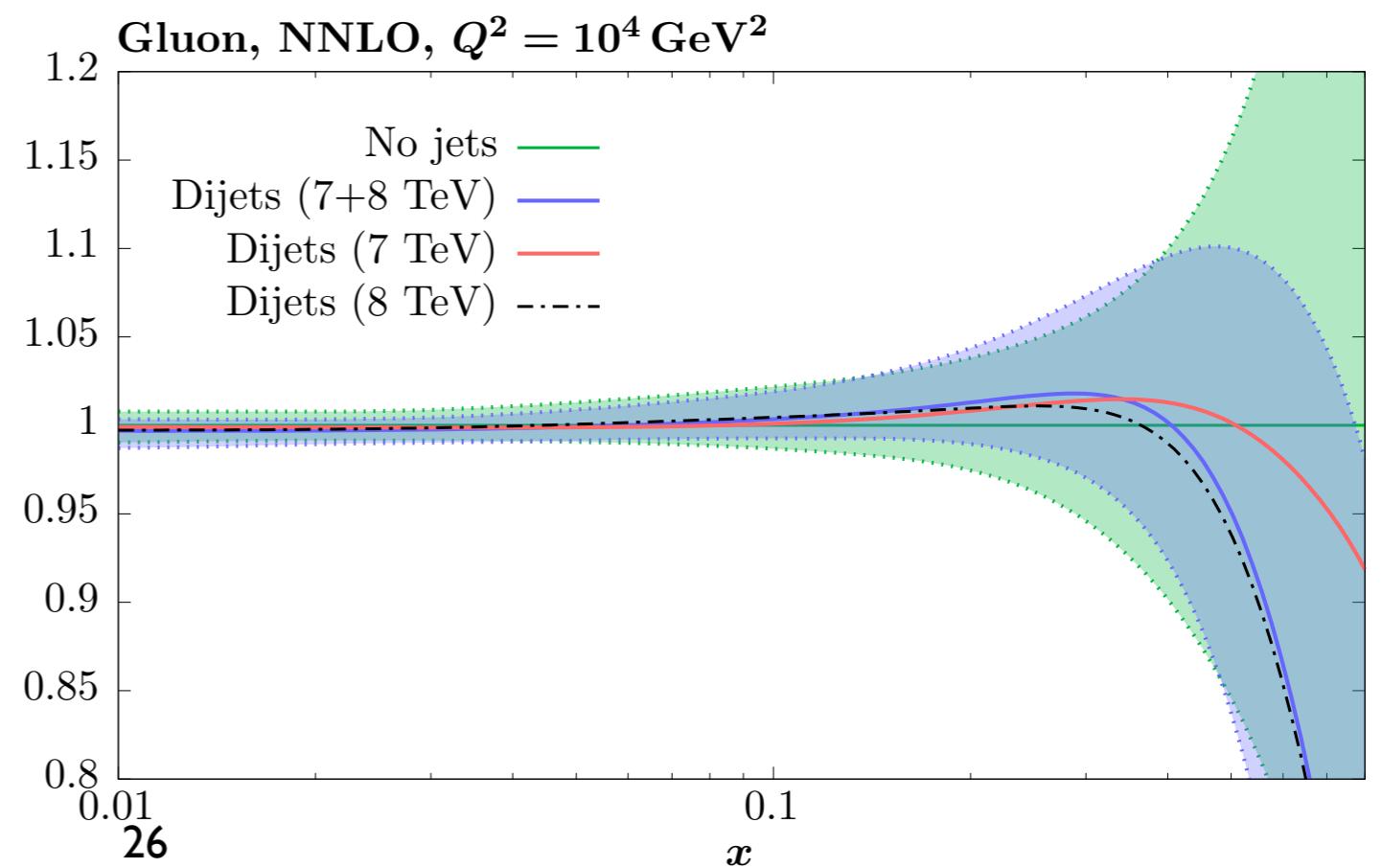


Consistency within datasets

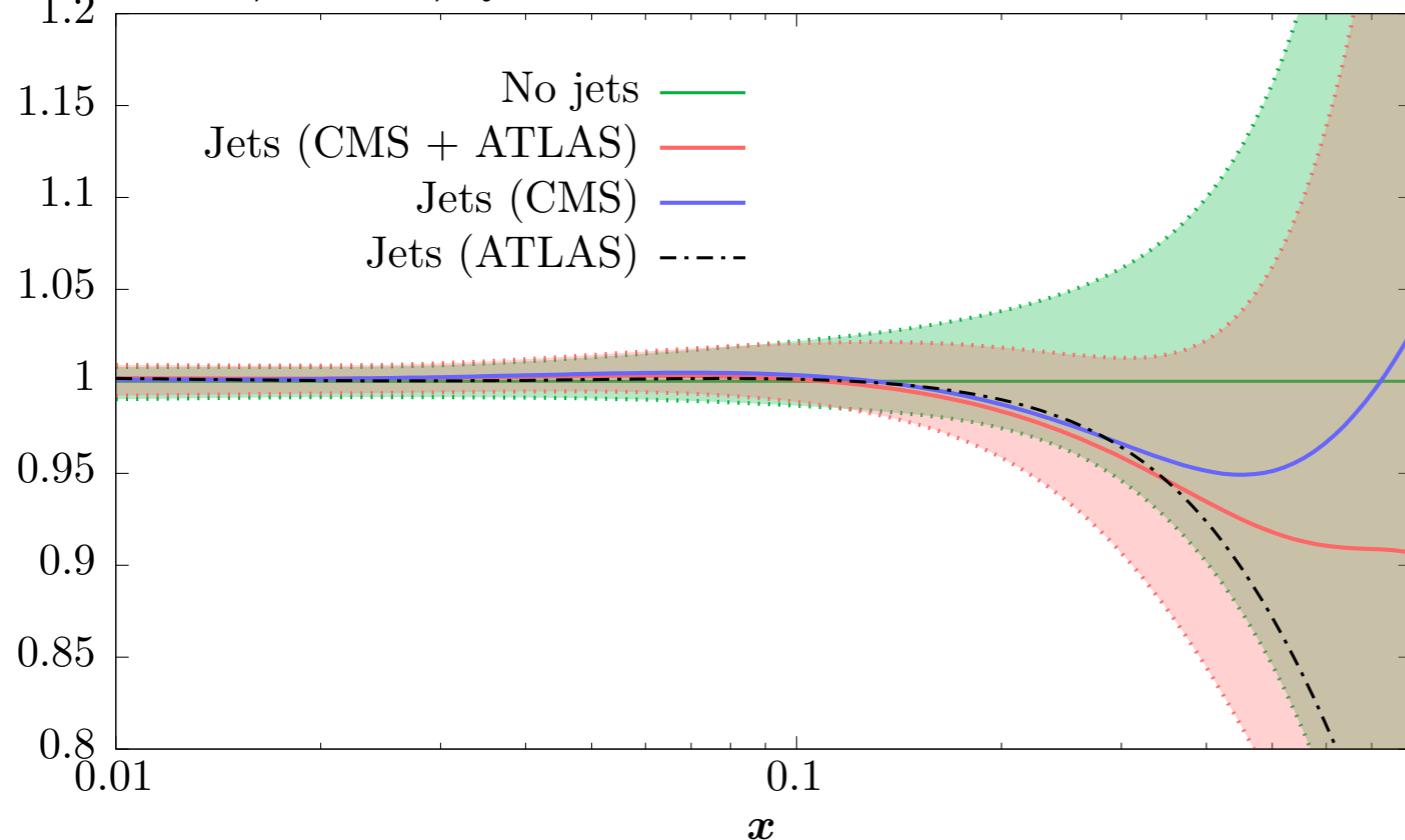


- 7 & 8 TeV data ~ consistent for inclusive jets.

- 7 & 8 TeV data consistent for dijets, but this is due to broader result.
- That is: all dijet fits completely driven by CMS 8 TeV data.



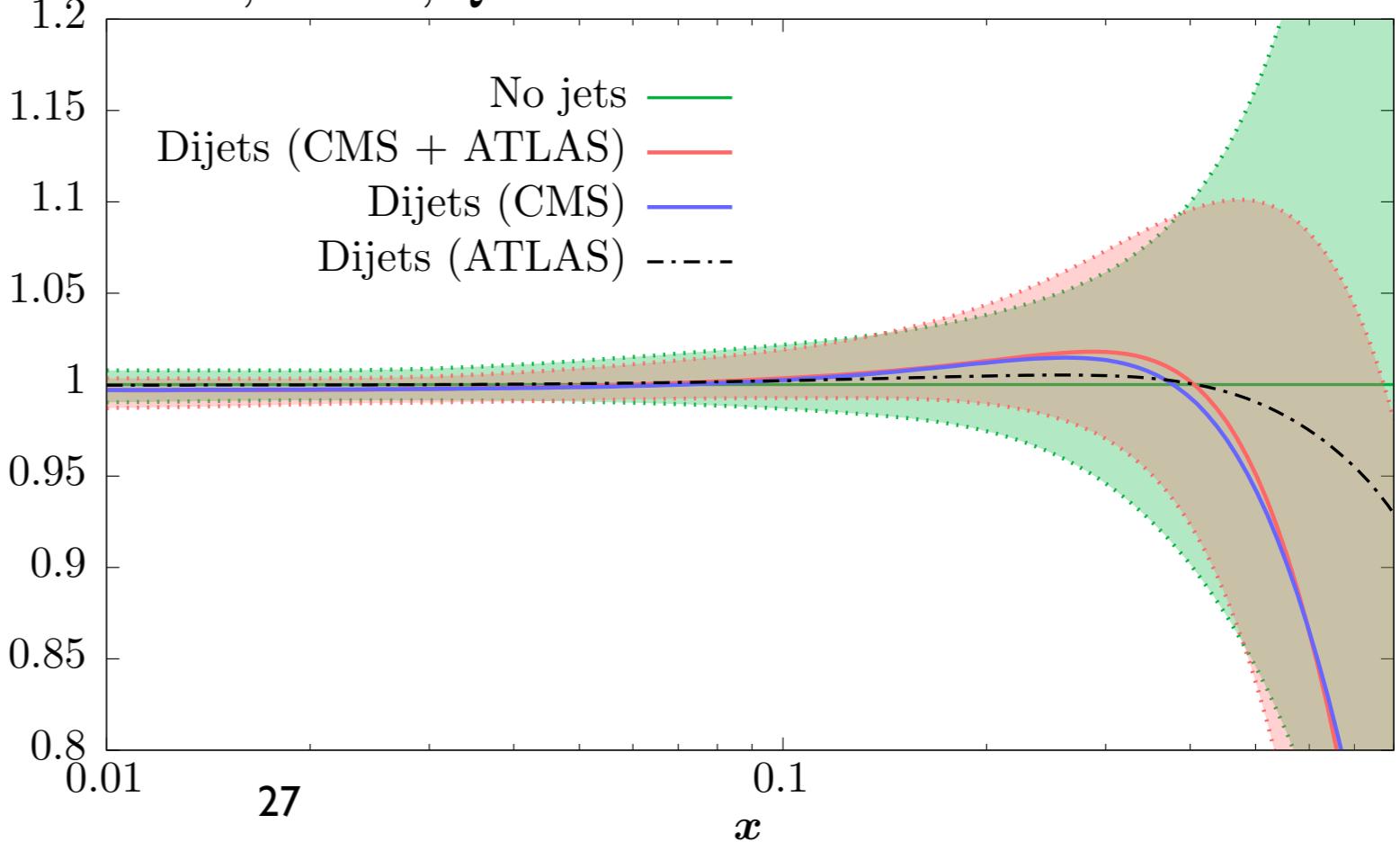
Gluon, NNLO, $Q^2 = 10^4 \text{ GeV}^2$



- At higher x clear difference between pulls of ATLAS and CMS (also seen in MSHT20).
- Final result compromise between these.

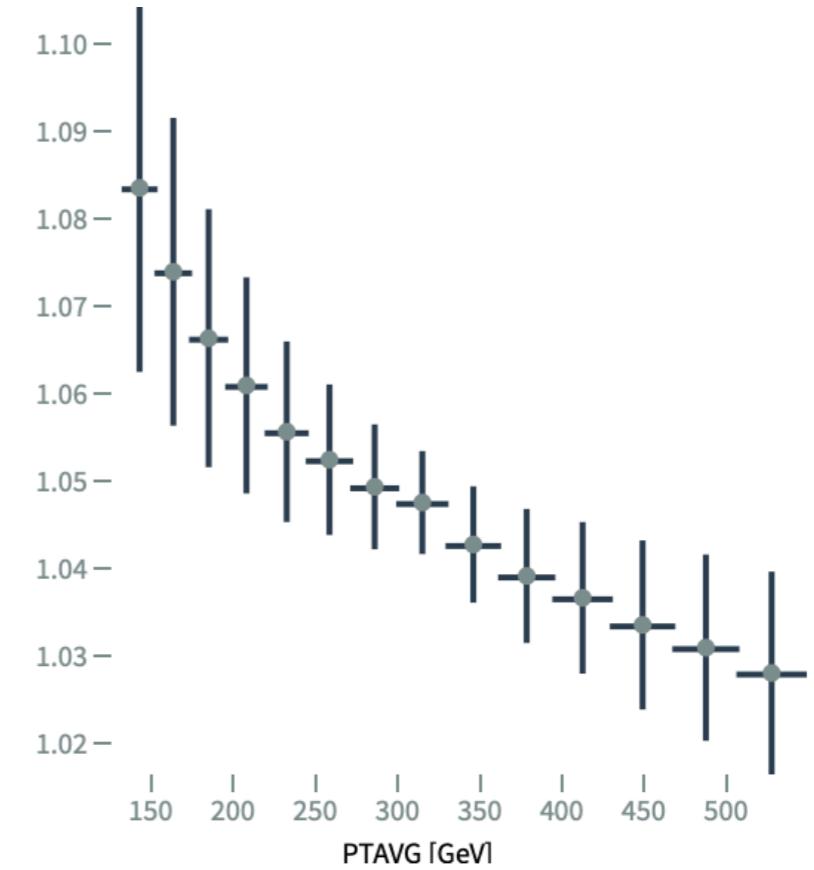
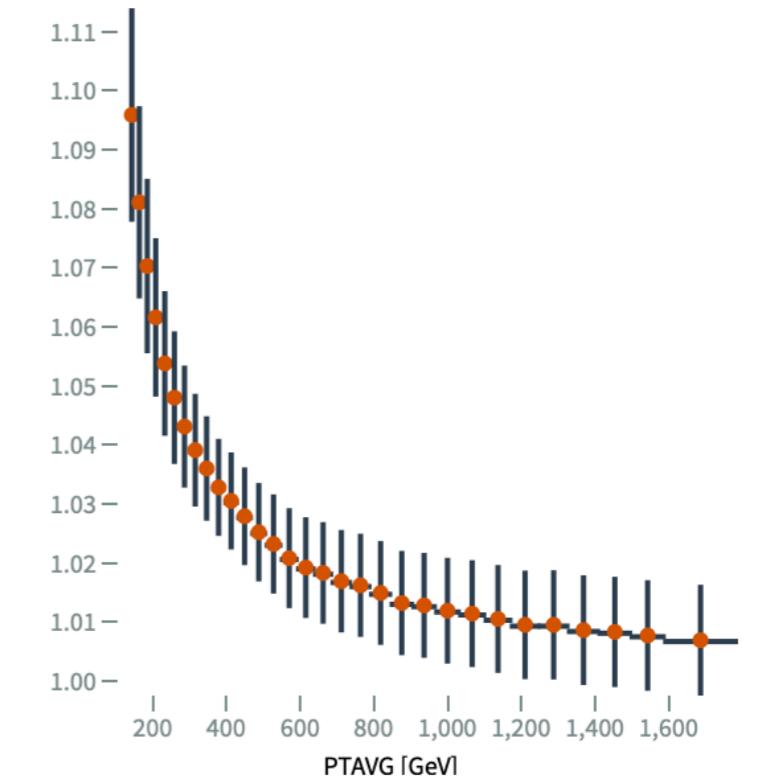
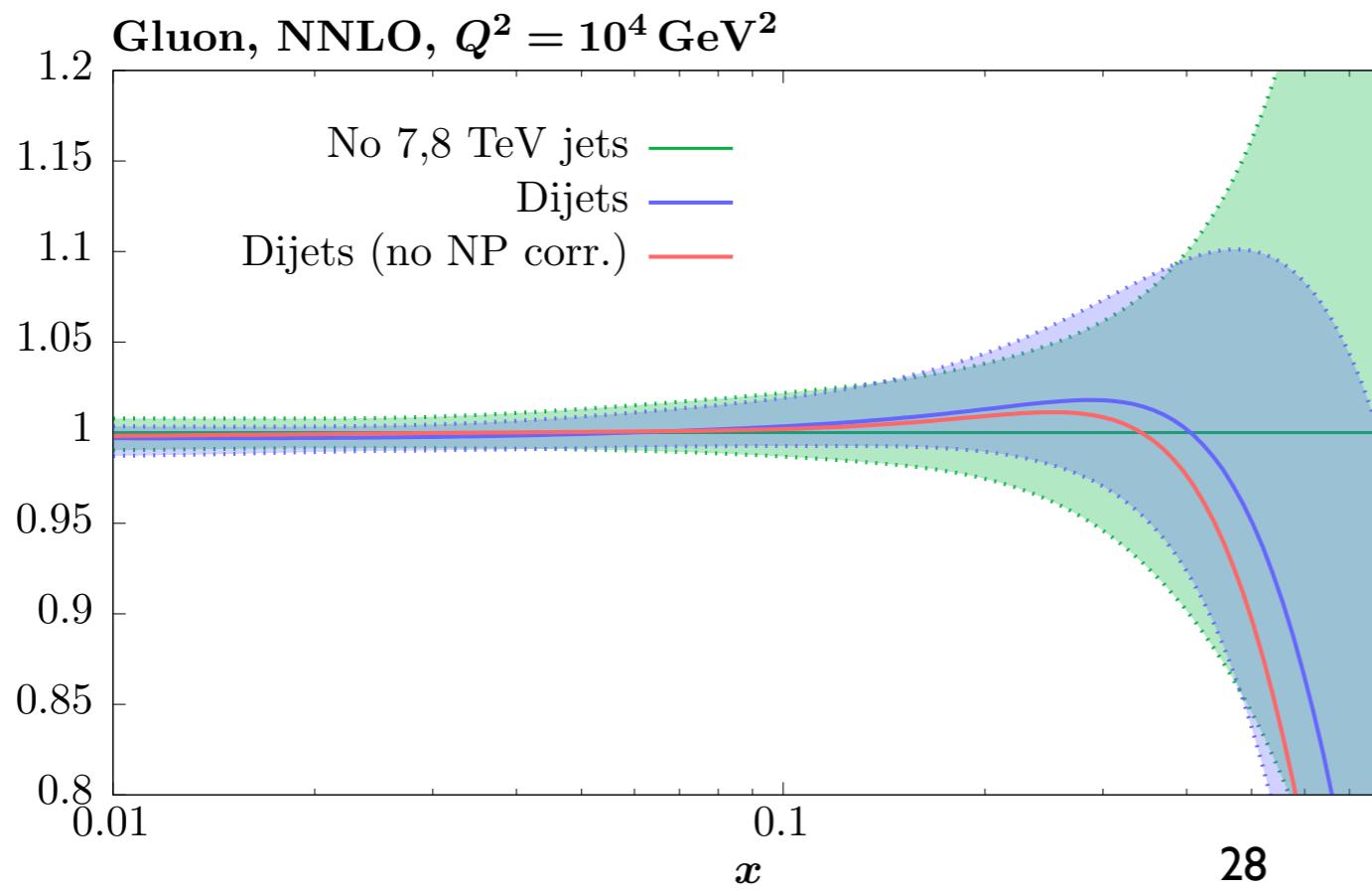
- Consistency between CMS and ATLAS, but latter has very little impact alone.
- Again CMS 8 TeV driving fit.

Gluon, NNLO, $Q^2 = 10^4 \text{ GeV}^2$



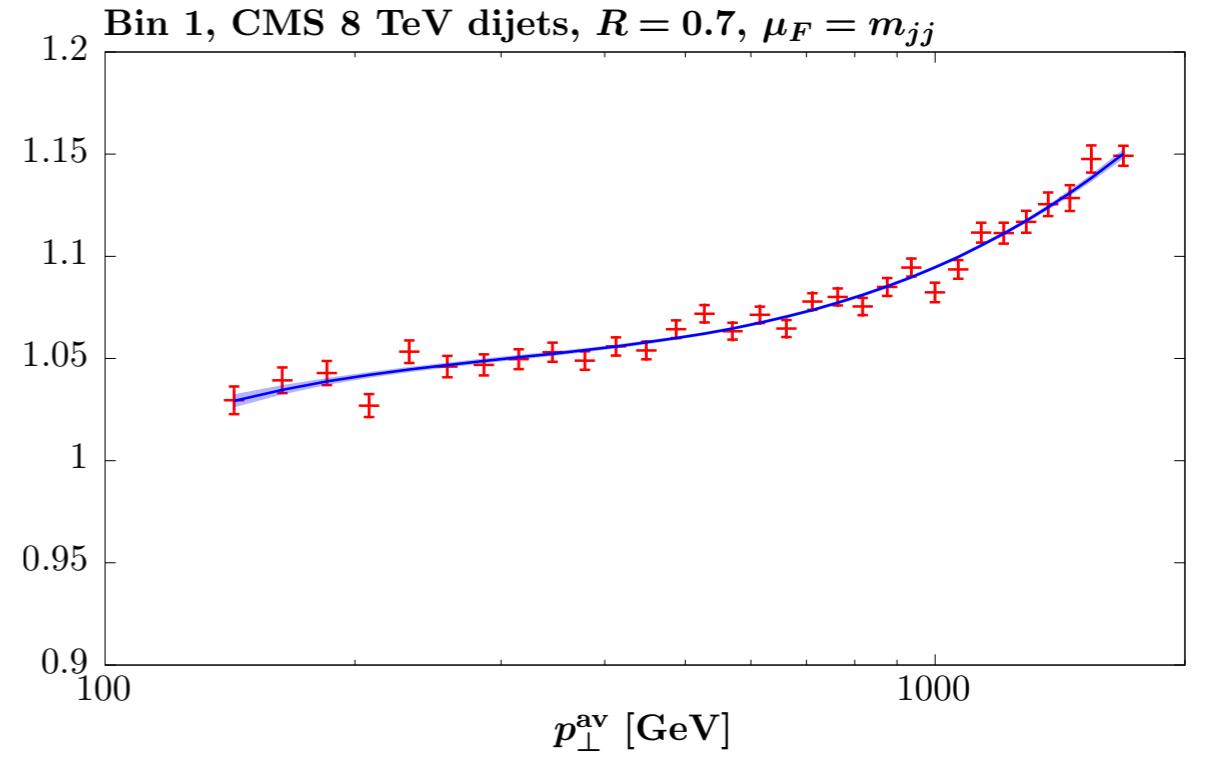
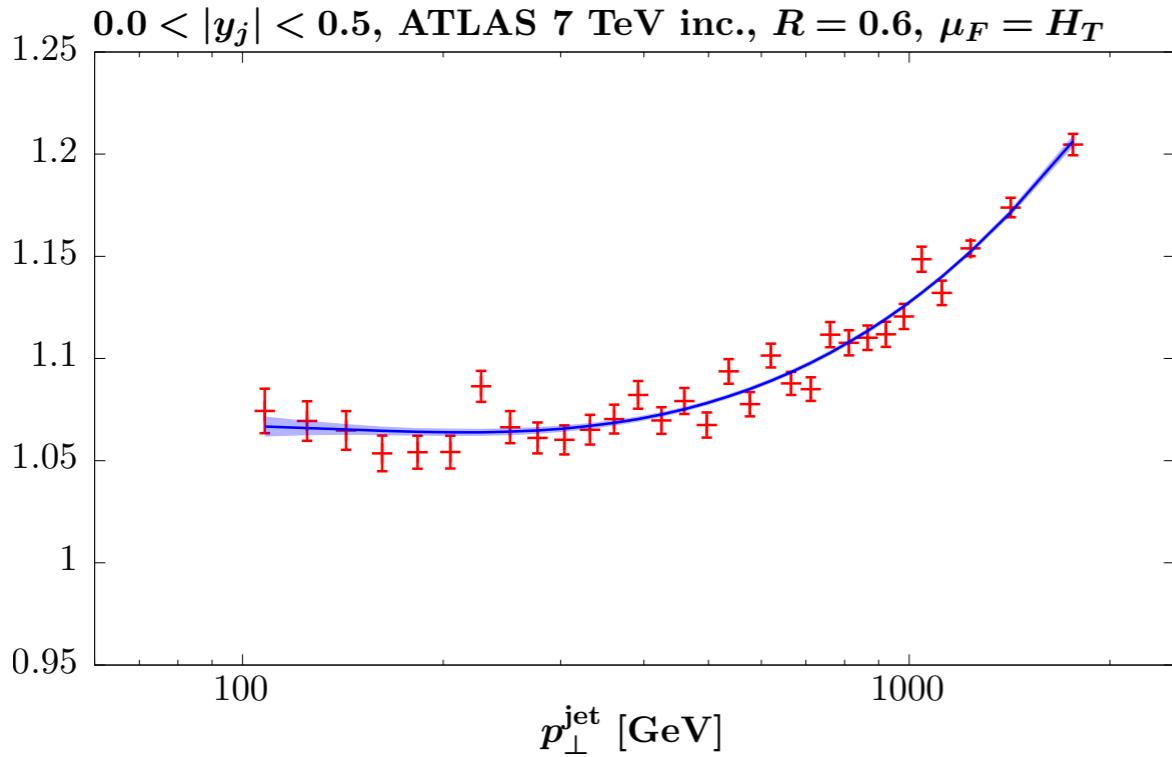
Technical aside (1) - NP corrections

- Not just high precision QCD/EW needed.
- Nonperturbative corrections enter at same level \sim NNLO QCD corrections. Percent level (two-point) uncertainties.
- Turning off in dijet fit, χ^2 deteriorates from 1.12 to 1.40. Some impact on gluon.



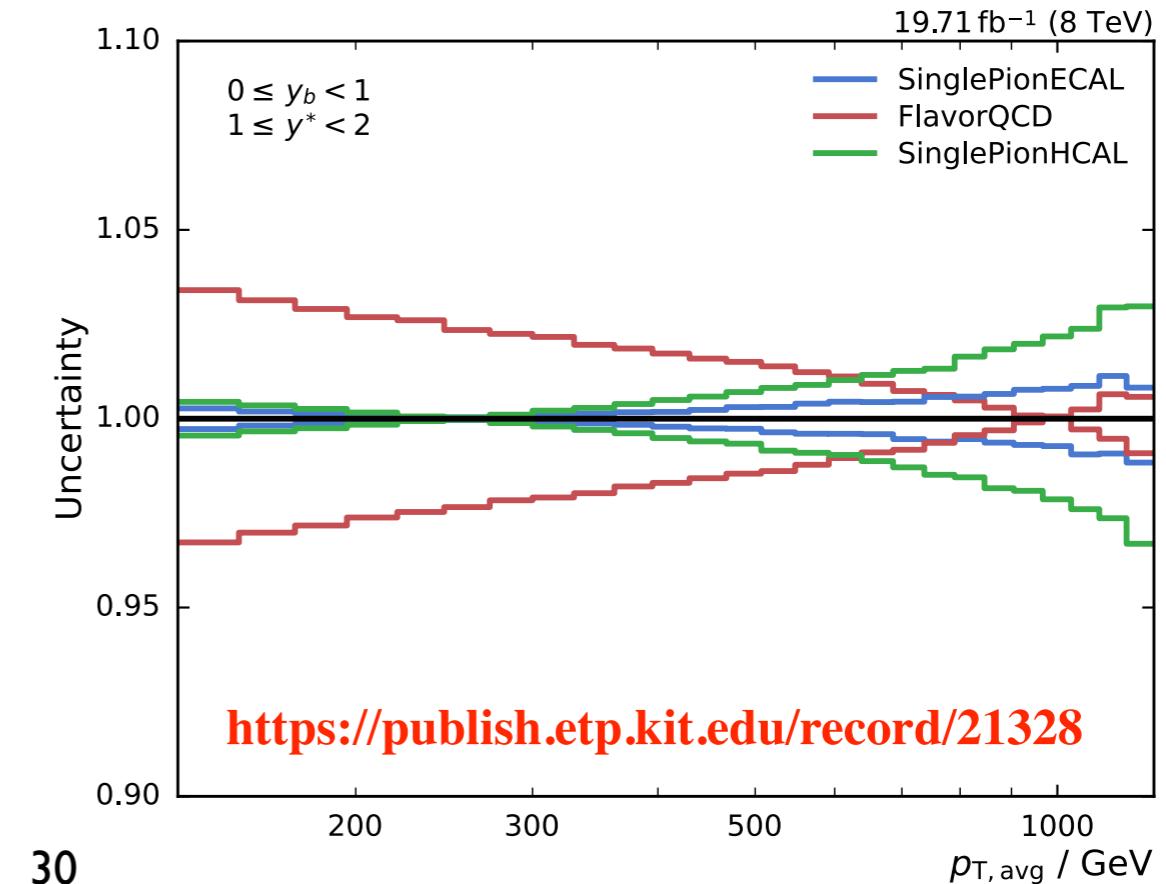
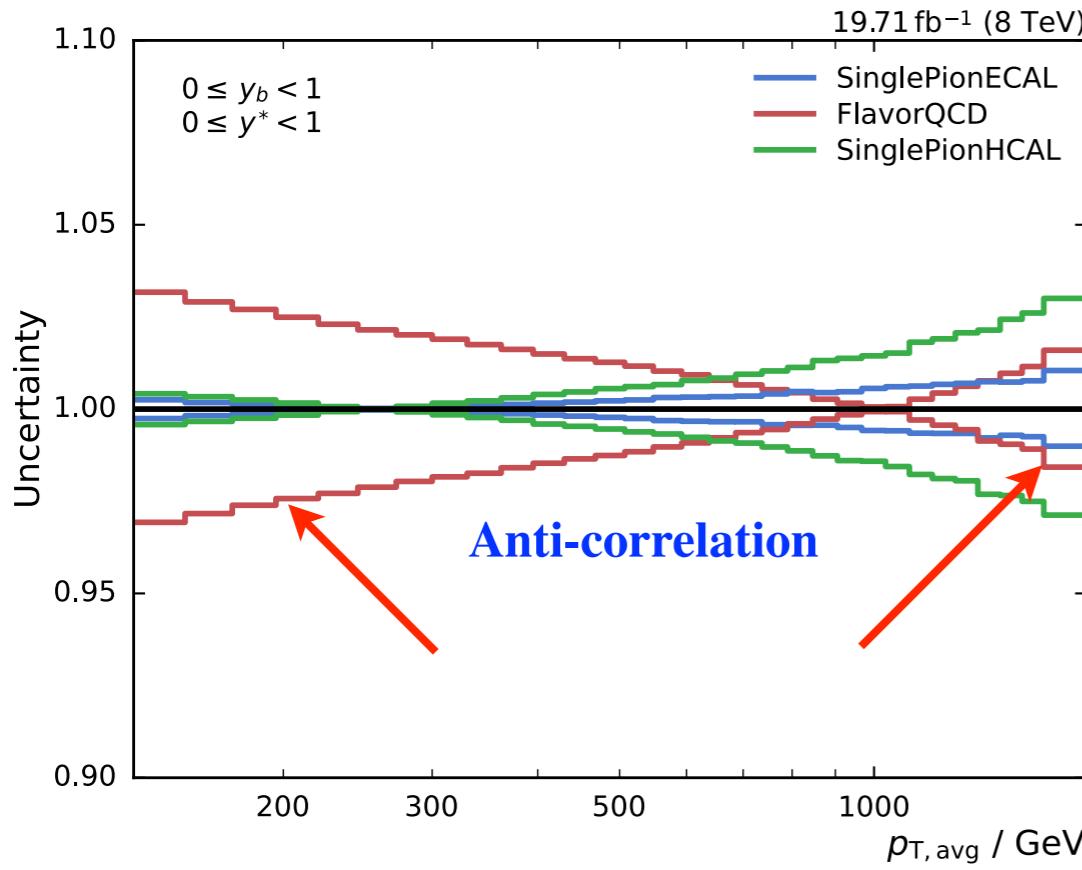
Technical aside (2) - K-factors

- NNLO QCD corrections included via K-factors. MC uncertainties on these not negligible.
- We argue better to fit these to smooth functions. Can impact on fit quality at the $\sim 0.1\text{-}0.2$ per point level, though PDFs very stable.
- Provides cleaner idea of improvements from NLO to NNLO etc.



Technical aside (3) - CMS 8 dijets

- Systematic uncertainties related to jet calibration correlated across kinematic (rapidity/ p_T) space. Shape of these indicates anti-correlation between certain regions. However `hepdata` entries [entirely positive](#).
- Through discussion with CMS colleagues have changed sign to more ‘natural’ (anti)-correlation.
- In the end this makes very little difference: improves χ^2 by $\sim 1\text{-}2$ points and gluon very stable. But more by chance than design.
- Detailed understanding/bookkeeping of systematic correlations key.



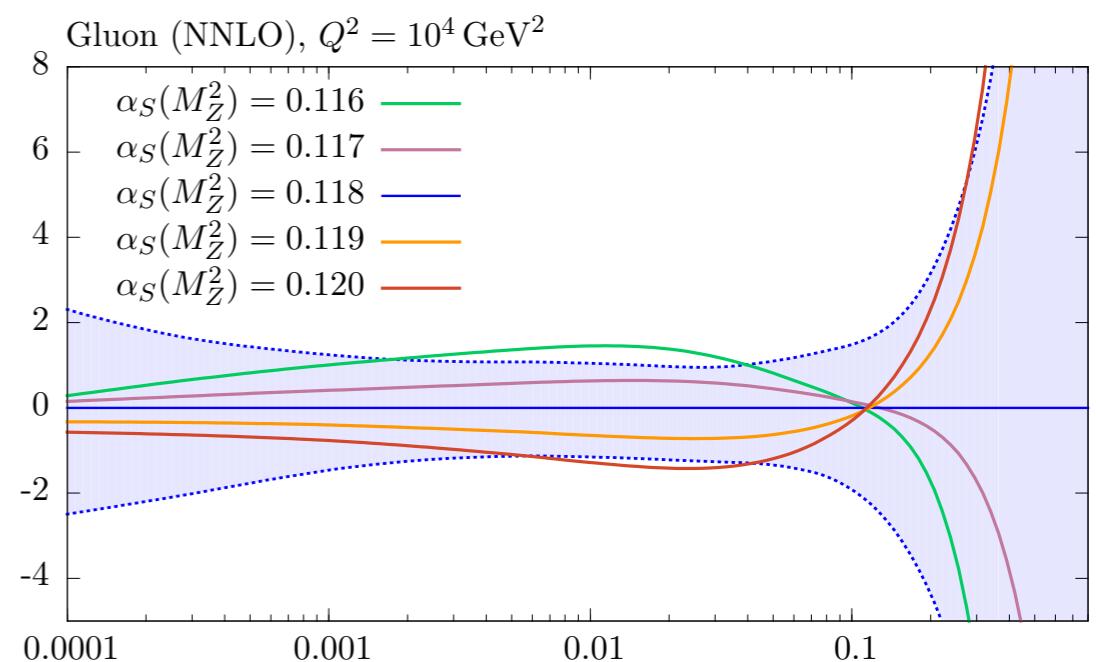
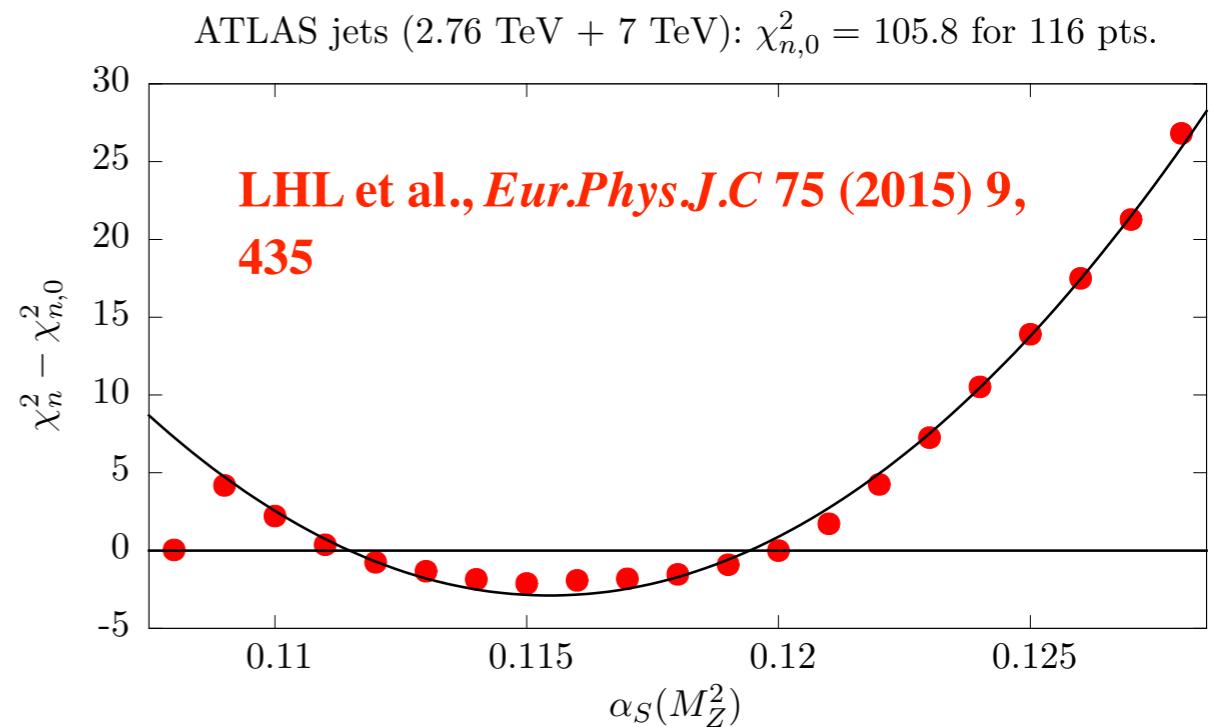
The strong coupling

- All results so far performed with fixed value of $\alpha_S(M_Z^2) = 0.118$

- Jet data can clearly be sensitive to value of strong coupling.
- However this is strongly correlated to extracted gluon.
- Work in preparation.

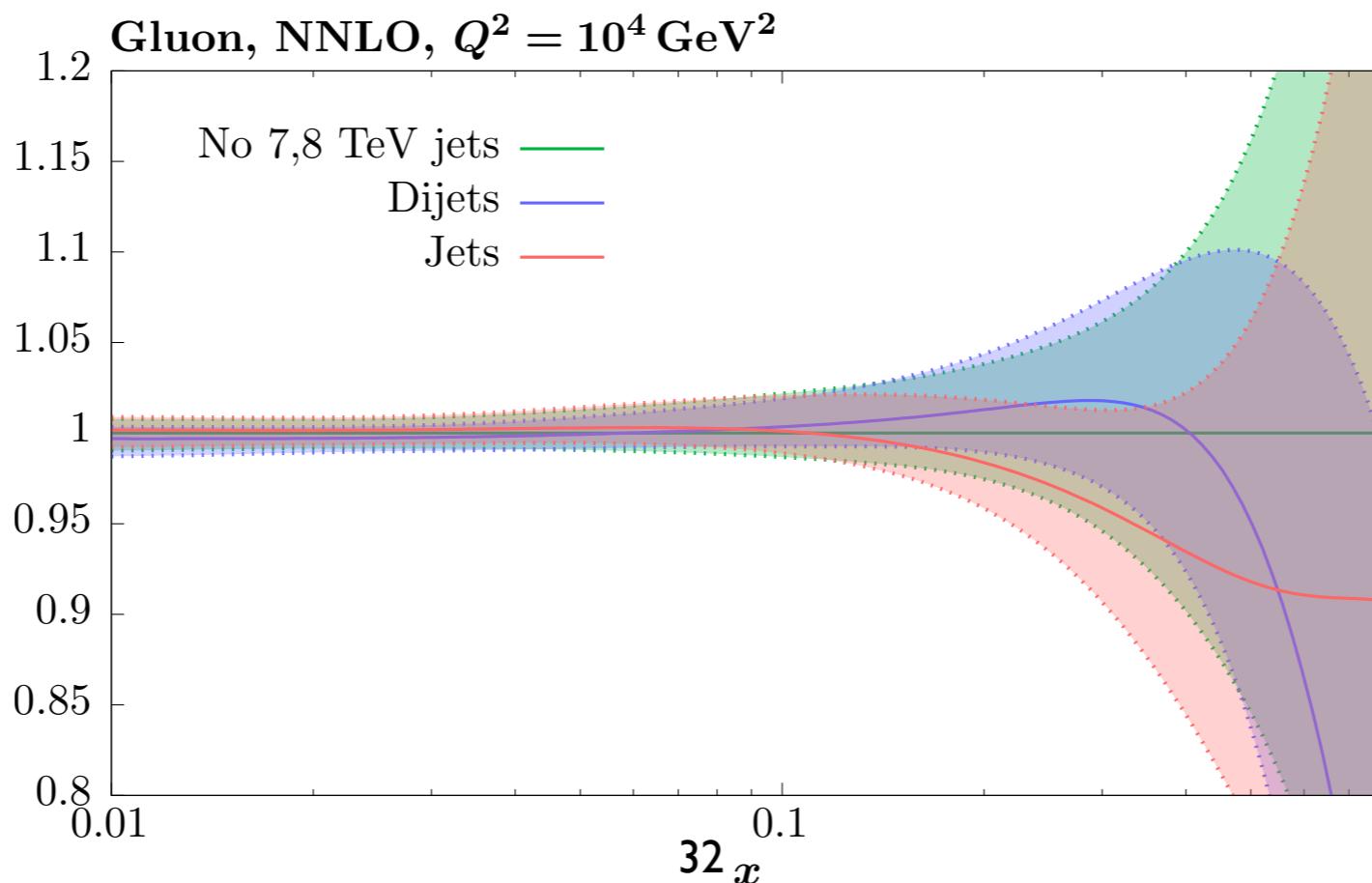
- Care needed in interpretation of preferred value of α_S in PDF sensitive observables outside of global fit.

S. Forte and Z. Kassabov,
Eur.Phys.J.C 80 (2020) 3, 182

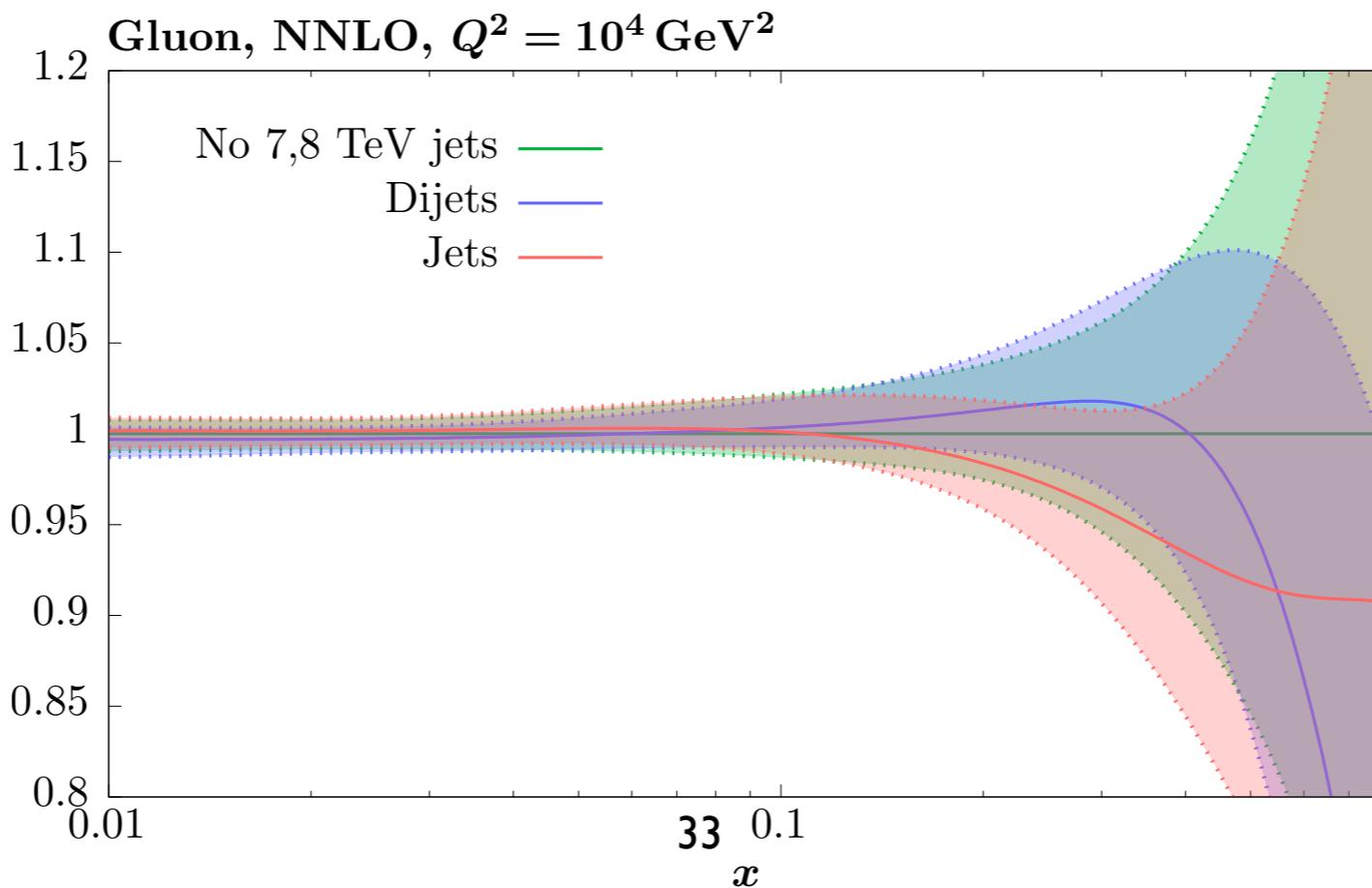


Summary/Outlook

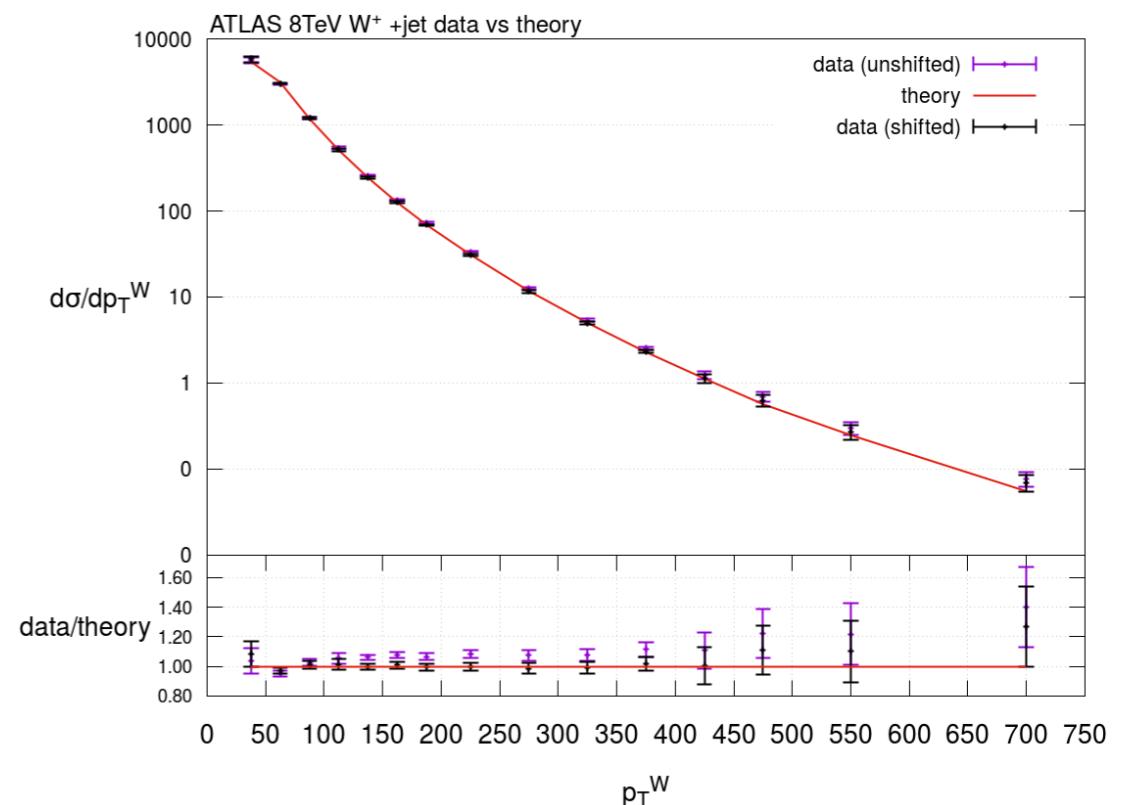
- We find:
 - ★ Impact of 7 + 8 TeV inclusive jets and dijets **consistent** (within uncertainties). However precise pulls not identical.
 - ★ **Fit quality** better for dijets and impact on gluon uncertainty larger in MSHT baseline fit.
 - ★ Great **impact** driven by 3D nature of CMS 8 TeV data, but also interplay with other data in fit. Global view needed.



- ★ NNLO QCD corrections improve fit quality for inclusive jets and absolutely essential for dijets.
- ★ Some difference in pulls between ATLAS/CMS for inclusive jets. Not seen in dijet data.
- ★ However, for dijets this is essentially a trivial statement, as here completely driven by single CMS 8 TeV dataset.
- ★ Our results qualitatively similar, though not identical in all cases, with original NNPDF study. See Tommaso's talk (now).



- Not discussed here:
 - ★ Impact of **missing higher order** corrections. Essential to include these in fit before making firm conclusion about jets vs. dijets and interplay with other data in fit. Work ongoing.
 - ★ Other jet related data. For example, ATLAS 8 TeV **W + jets** included in MSHT20 fit. Sensitive to high x gluon/quarks. Well fit, with moderate impact.
 - ★ Jets in DIS. No included so far in MSHT20, but to be looked at.



Thank you for listening!
 (and over to Tommaso)