Making Neutrino Beams -I

Accelerator Neutrinos

International Neutrino Summer School 2021, Aug 2-13, CERN

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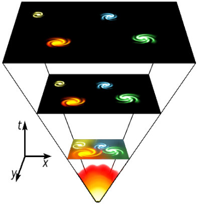
Brookhaven National Laboratory

Aug 2nd, 2021

Introduction

Sources of Neutrinos

Big Bang

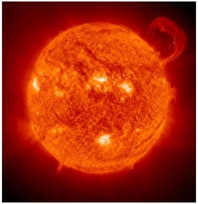


10^{-4} eV
$56/cm^3$

Reactors

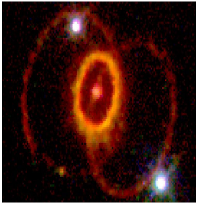
few MeV
$10^{21}/\mathrm{GW_{th}}/s$

Sun



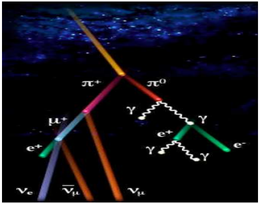
0.1-14 MeV
$10^{10}/cm^2/s$

SuperNova



$\sim$ 10 **MeV**
$10^9/cm^2/s$

Atmosphere

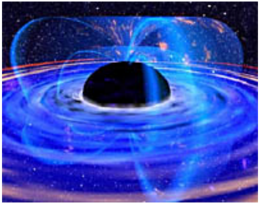


$\sim$ 1 **GeV**
few/cm^2/s

Accelerators

1-20 GeV
$10^6/cm^2/s/MW$ **(at 1km)**

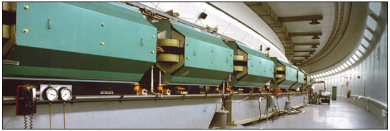
Extragalactic



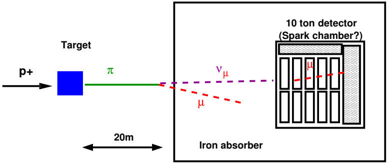
TeV-PeV
varies

Producing Neutrinos from an Accelerator

1962: Leon Lederman, Melvin Schwartz and Jack Steinberger use a proton beam from BNL's Alternating Gradient Synchrotron (AGS) to produce a beam of neutrinos using the decay $\pi \rightarrow \mu\nu_x$

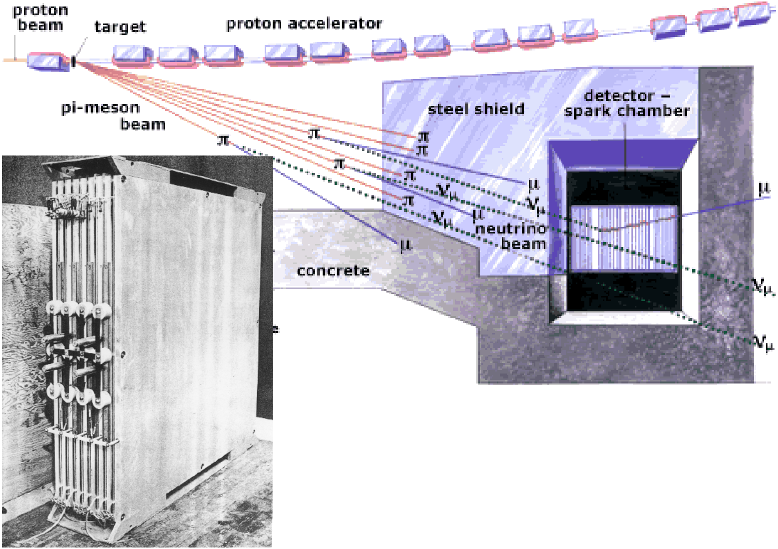


The AGS

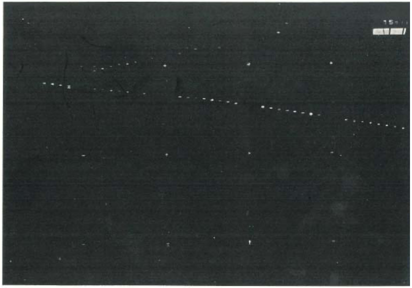


Making ν's

The Two-Neutrino Experiment

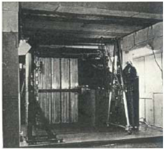


The Two-Neutrino Experiment

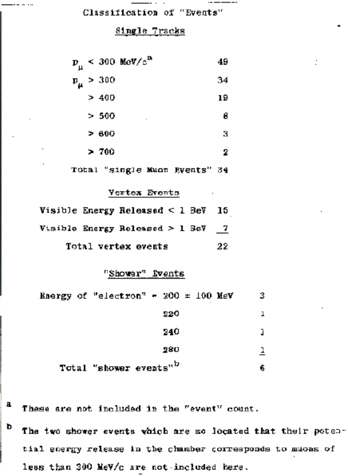


Neutrino Event

Columbia (Nevis)



BNL



Classification of "Events"

Single Tracks

p_μ < 300 MeV/c[a]	49
p_μ > 300	34
> 400	19
> 500	8
> 600	3
> 700	2
Total "single Muon Events"	34

Vertex Events

Visible Energy Released < 1 BeV	15
Visible Energy Released > 1 BeV	7
Total vertex events	22

"Shower" Events

Energy of "electron" ≈ 200 ± 100 MeV	3
220	1
240	1
280	1
Total "shower events"[b]	6

[a] These are not included in the "event" count.

[b] The two shower events which are so located that their potential energy release in the chamber corresponds to muons of less than 300 MeV/c are not included here.

The first event!

The Two-Neutrino Experiment

Result: 40 neutrino interactions recorded in the detector, 6 of the resultant particles where identified as background and 34 identified as $\mu \Rightarrow \nu_x = \nu_\mu$

The first successful accelerator neutrino experiment was at Brookhaven Lab.

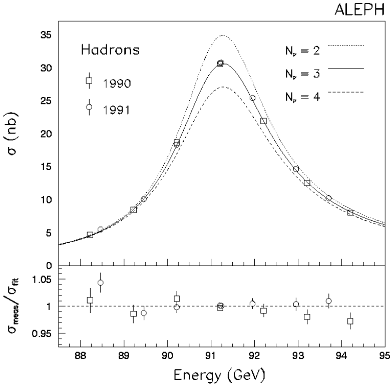
1988 NOBEL PRIZE

Number of Neutrino Flavors: Particle Colliders

1980's - 90's: The number of neutrino types is precisely determined from studies of Z^0 boson properties produced in e^+e^- colliders.

The LEP e^+e^- collider at CERN, Switzerland

The 27km LEP ring was reused to build the Large Hadron Collider



$N_\nu = 2.984 \pm 0.008$

Neutrino Mixing ⇒ Oscillations

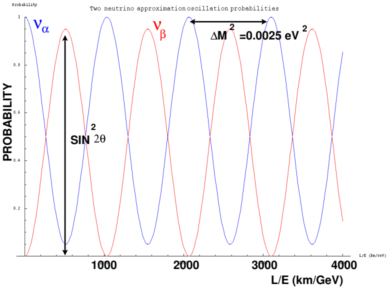
$$\begin{pmatrix} \nu_a \\ \nu_b \end{pmatrix} = \begin{pmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

$$\begin{aligned} \nu_a(t) &= \cos(\theta)\nu_1(t) + \sin(\theta)\nu_2(t) \\ P(\nu_a \to \nu_b) &= |<\nu_b|\nu_a(t)>|^2 \\ &= \sin^2(\theta)\cos^2(\theta)|e^{-iE_2 t} - e^{-iE_1 t}|^2 \end{aligned}$$

$$P(\nu_a \to \nu_b) = \sin^2 2\theta \sin^2 \frac{1.27\Delta m^2_{21} L}{E}$$

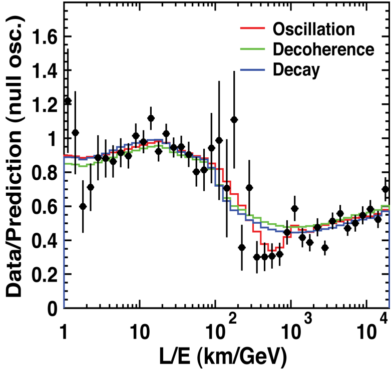
where $\Delta m^2_{21} = (m^2_2 - m^2_1)$ in eV^2, L (km) and E (GeV).

Observation of oscillations implies non-zero mass eigenstates



Two Different Mass Scales!

Super-K, atmospheric ν_μ



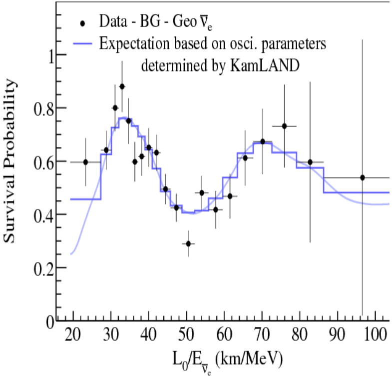
Global fit 2013:

$$\Delta m^2_{\rm atm} = 2.43^{+0.06}_{-0.10} \times 10^{-3}\ \mathbf{eV^2}$$

$$\sin^2\theta_{\rm atm} = 0.386^{+0.24}_{-0.21}$$

Atmospheric L/E ∼ 500 km/GeV

KamLAND, reactor $\bar{\nu}_e$



Global fit 2013:

$$\Delta m^2_{\rm solar} = 7.54^{+0.26}_{-0.22} \times 10^{-5}\ \mathbf{eV^2}$$

$$\sin^2\theta_{\rm solar} = 0.307^{+0.18}_{-0.16}$$

Solar L/E ∼ 15,000 km/GeV

Neutrino Oscillation Scales

The mass-squared differences Δm^2_{21} (solar), Δm^2_{32} (atmospheric) and $\Delta m^2_{\text{sterile}} = 1\text{eV}^2$ (LSND?) drive very different experimental scales. The location of the oscillation maxima occur at

$$\begin{aligned} L/E^{\nu}_n &= (2n-1)\frac{\pi}{2}\frac{1}{(1.267 \times \Delta m^2\ (\mathbf{eV}^2))} \\ &\approx (2n-1) \times 1\ \mathbf{km/GeV(m/MeV)\ for}\ \Delta m^2_{43}\ \mathbf{(LSND)} \\ &\approx (2n-1) \times 500\ \mathbf{km/GeV(m/MeV)\ for}\ \Delta m^2_{32}\ \mathbf{(atmos.)} \\ &\approx (2n-1) \times 15,000\ \mathbf{km/GeV(m/MeV)\ for}\ \Delta m^2_{21}\ \mathbf{(solar)} \end{aligned}$$

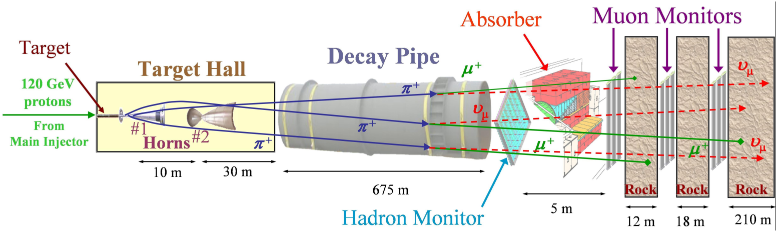
where E^{ν}_n is the neutrino energy at the maximum of oscillation node n.

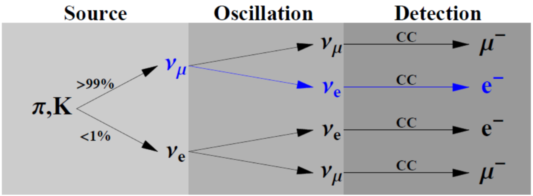
Oscillations of GeV (MeV) scale neutrinos over distances from 1 - 15,000 km (m) probe 3x3 PMNS parameters and beyond. High energy particle accelerators operate at the GeV scale (lecture I) while reactors generate neutrinos at the MeV scale (lecture II).

Neutrinos from Accelerators: Decay-in-flight

Conventional Muon Neutrino Beams

High power conventional neutrino beams (NuMI):





Neutrinos from Accelerators

To produce neutrinos from accelerators

$p^+ + A \rightarrow \pi^\pm + X, \quad \pi^\pm \rightarrow \mu^\pm + \nu_\mu/\bar{\nu}_\mu$

where $A =$ **Carbon (Graphite), Berillyium, Tungsten,** X **is other particles**

ν Exercise: The Main Injector accelerator at Fermilab produces 4.86×10^{13} **120 GeV protons in a 10 microsecond pulse every 1.33 seconds to the NuMI beamline. What is the average power of the proton beam delivered in megawatts?**

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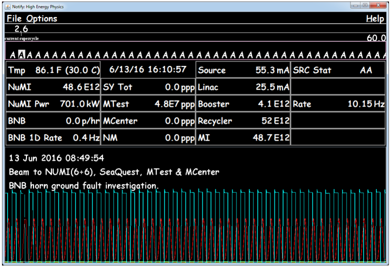
Power = 120 GeV $\times$ **4.86** 10^{13} **protons** $\times$ **1.6** 10^{-10} **Joules/GeV** $\times$ **1/1.33s = 702 kW**

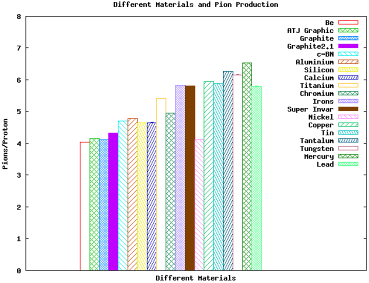


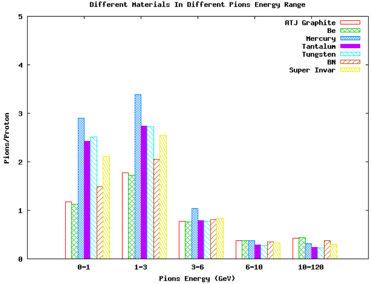
Tmp	86.1 F (30.0 C)	6/13/16 16:10:57		Source	55.3 mA	SRC Stat	AA
NuMI	48.6 E12	SY Tot	0.0 ppp	Linac	25.5 mA		
NuMI Pwr	701.0 kW	MTest	4.8E7 ppp	Booster	4.1 E12	Rate	10.15 Hz
BNB	0.0 p/hr	MCenter	0.0 ppp	Recycler	52 E12		
BNB 1D Rate	0.4 Hz	NM	0.0 ppp	MI	48.7 E12		

13 Jun 2016 08:49:54
Beam to NUMI(6+6), SeaQuest, MTest & MCenter
BNB horn ground fault investigation.

Decay-in-flight beams: Fundamentals

The result of a FLUKA (`http://www.fluka.org/fluka.php`) simulation of pion production from 120 GeV protons is shown below





ν Exercise: **What fraction of 6 GeV pions on average will decay before reaching the end of an evacuated pipe 200m (675m) long? The π^+ rest mass and lifetime are 140 MeV and 26 ns**

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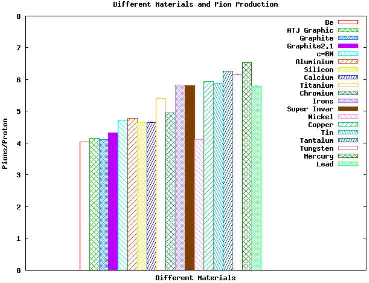

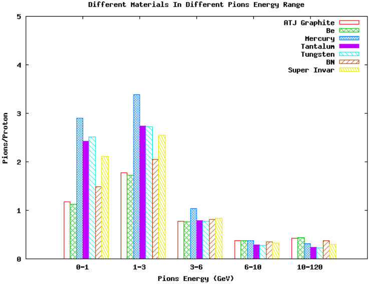

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6 GeV π^+ lifetime: $\tau = \gamma\tau_0 = \frac{E}{m_0c^2} \times 26\text{ns} = \mathbf{1.1ns}$, $c\tau = 334$ **m**

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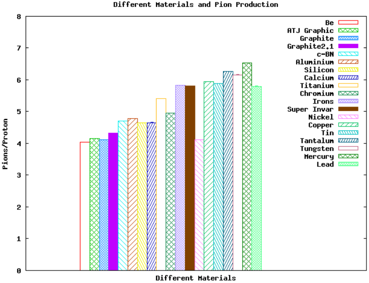

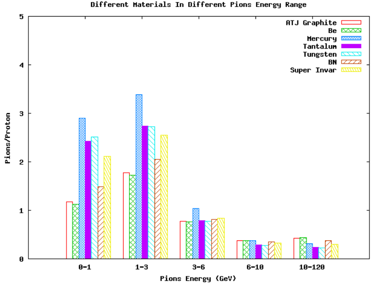

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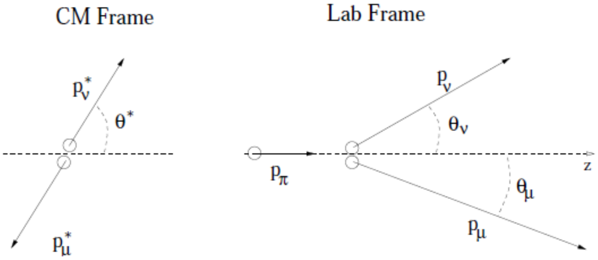
$F_{decays} = (1 - \exp^{-l/c\tau}) = 0.45(0.87)$

Pion Decay-in-Flight (DIF) beams: kinematics



ν Exercise: **Solve the $\pi/K \to \mu\nu$ two body decay for high energy pions and Kaons ($E_{\pi,K} >> m_{\pi,K}$) and show that the energy of the neutrino E_ν and the probability that a neutrino is emited withn a solid angle $dP/d\Omega$ can be approximated as follows:**

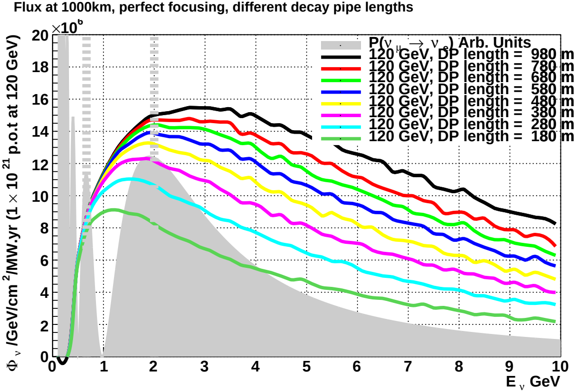
$$E_\nu = \frac{\left(1 - \frac{m_\mu^2}{m_{\pi,K}^2}\right) E_{\pi,K}}{1 + \gamma^2\theta_\nu^2}, \quad \frac{dP}{d\Omega} \sim \frac{1}{4\pi}\left(\frac{2\gamma}{1+\gamma^2\theta_\nu^2}\right)^2$$

Assume $\theta_\nu << 1$

Neutrino fluxes with perfect focusing

ν_μ fluxes from pion decay-in-flight (DIF) beams assuming perfect focusing and charge selection:

120 GeV, decay channel lengths from 200m to 1km

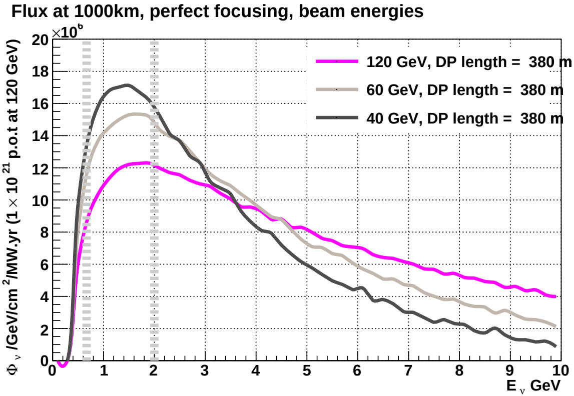


Gain with longer decay channels, BUT excavation is challenging/expensive

Neutrino fluxes with perfect focusing

ν_μ fluxes from pion decay-in-flight (DIF) beams assuming perfect focusing and charge selection:

40 to 120 GeV, decay channel length = 400m

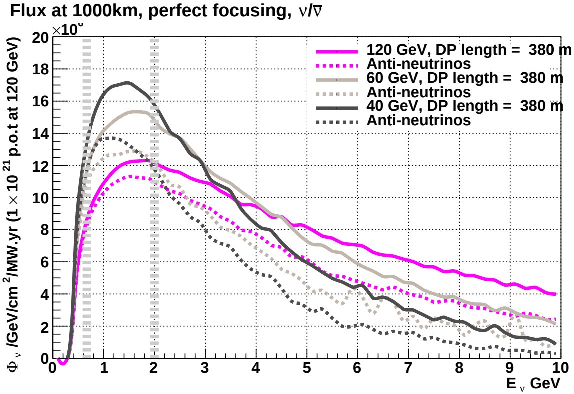


Lower energy flux benefits at lower P beam energy BUT only at constant power = more protons.

Neutrino fluxes with perfect focusing

ν_μ fluxes from pion decay-in-flight (DIF) beams assuming perfect focusing and charge selection:

Neutrino vs anti-neutrino fluxes

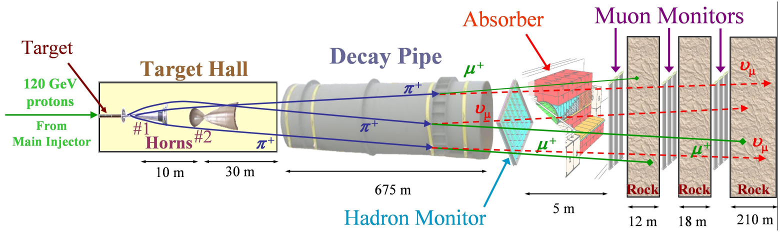


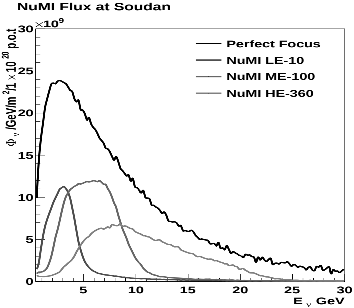
$\bar{\nu}/\nu$ fluxes are more favorable at higher proton beam energies.

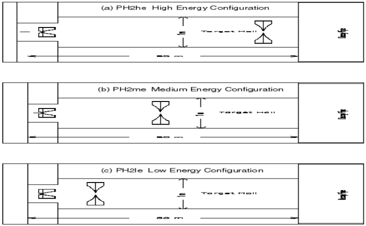
Examples of Neutrino decay-in-flight Beamlines

Examples of Conventional Neutrino Beams

Multi-GeV, on-axis, tunble beams: NuMI





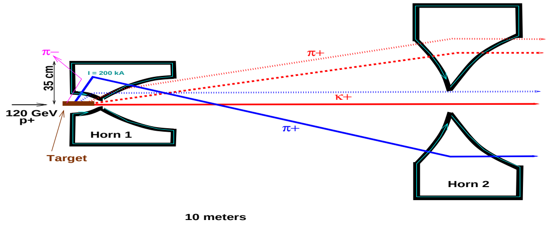


H1-H2: LE=10m, ME=23m, HE=40m

Target z_0 = -35cm from H1

Examples of Conventional Neutrino Beams

NuMI Focusing System Details

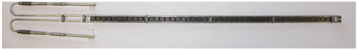


Horn 2

Parabolic magnetic lens.

3T at 200 kA

NuMI Target



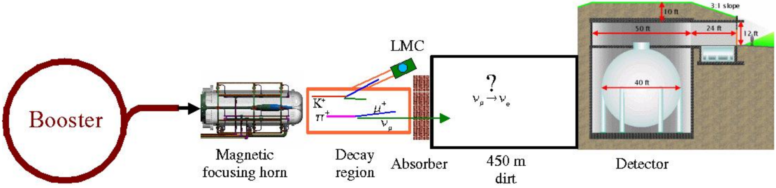
6.4 x 15 mm^2 graphite segments.
1m long = 1.9 interaction lengths.
$\mathcal{O}(10)$ **KW beam power at 1 mm beam width.**
Water cooled.

Horn 1

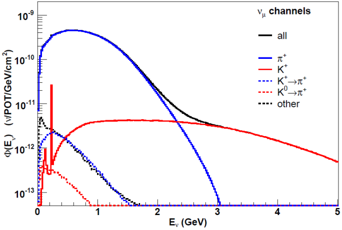
Examples of Conventional Neutrino Beams

sub-GeV on-axis Beams: Booster Neutrino Beam

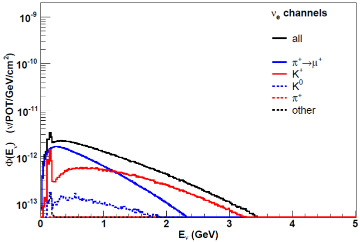
8 GeV proton, Be target l=71cm, 174 kA pulsed horn (1).



ν_μ Flux



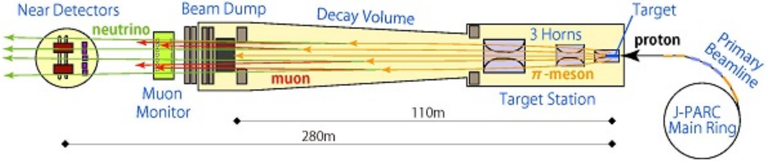
ν_e Flux



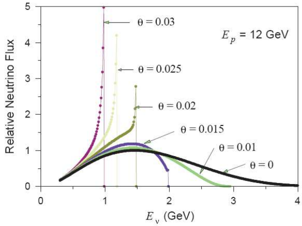
Examples of Conventional Neutrino Beams

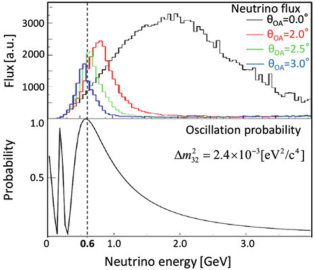
Off-axis beams: JPARC Neutrino Beam

30 GeV proton, C target l=90cm, 250-320 kA pulsed horns (3)

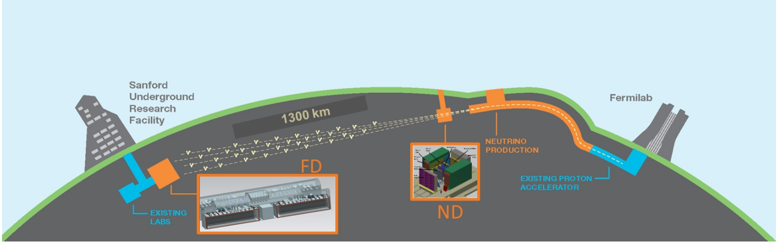


First proposed for BNL E-889 (1995): A narrow beam of ν_μ can be achieved by going off-axis to the π beam. More flux at sub-GeV.



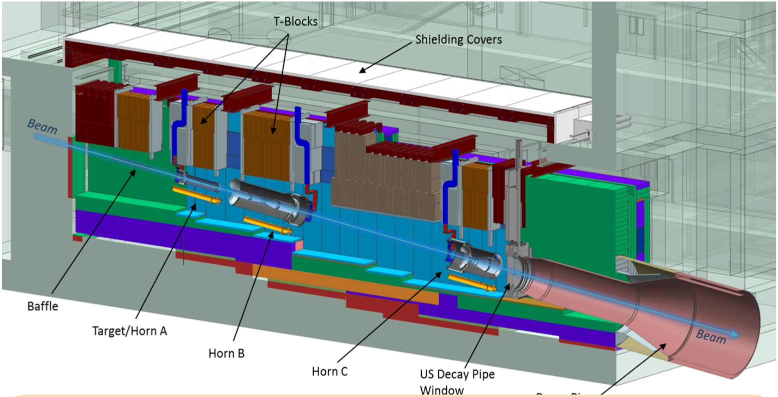


The Deep Underground Neutrino Experiment



- **A very long baseline experiment:** **1300km from Fermilab in Batavia, IL to the Sanford Underground Research Facility (former Homestake Mine) in Lead, SD.**
- **A highly capable near detector at Fermilab.**
- **A very deep (1 mile underground) far detector: massive 40-kton Liquid Argon Time-Projection-Chamber with state-of-the-art instrumentation.**
- **High intensity *tunable* wide-band neutrino beam from LBNF produced from upgraded MW-class proton accelerator at Fermilab.**

LBNF/DUNE Beamline Target Hall Design



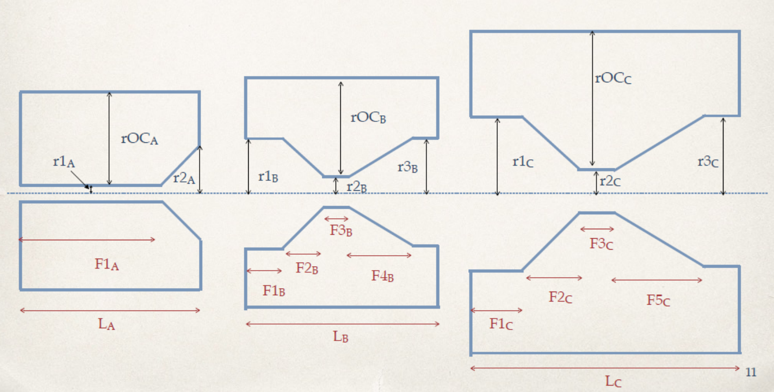
A Genetic Algorithim was used to optimized the target and focusing system design to maximize CP violation sensitivity. The focusing system is 3 horns operated at ~ 300 kA with a 2.3m long graphite target inserted into the first horn. $\approx$ 40% of beam power is deposited in target hall shielding!

Optimization of beamline designs: DUNE/LBNF beam

- **The 2015 reference design for LBNF/DUNE was a NuMI-like movable target (segmented rectangular graphite fins with water cooling $\approx$ 1m long) and 2 modified NuMI horns 6.6m apart**
- **In Sep 2017 LBNF adopted a focusing design with 3 horns optimized using a *genetic algorithim* with the physics parameter to be measured (CPV sensitivity) used to gauge fitness.**
- **Target geometry is optimized at the same time, as well as proton beam energy with realistic Main Injector power profile (1.03 MW at 60 GeV to 1.2 MW at 120 GeV).**
- **Limits on horn current, diameter and length are imposed based on experience with T2K and NuMI horn manufacturing**
- **Limits on horn separation imposed based on size of target chase.**

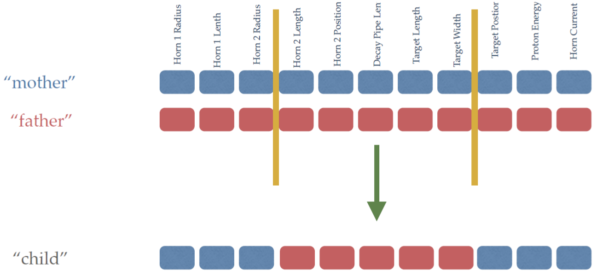
Optimization of beamline designs: DUNE/LBNF beam

Horn parameters used in GEANT4 simulation for GA optimization:



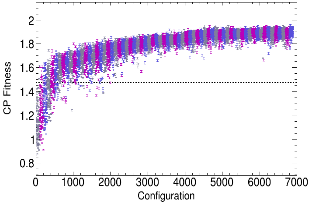
Optimization of beamline designs: DUNE/LBNF beam

Schematic of the Genetic Algorithim:



CP Fitness = minimum significance with which 75% of $\delta_{\rm cp}$ can be determined $\neq 0$ or π for a given exposure

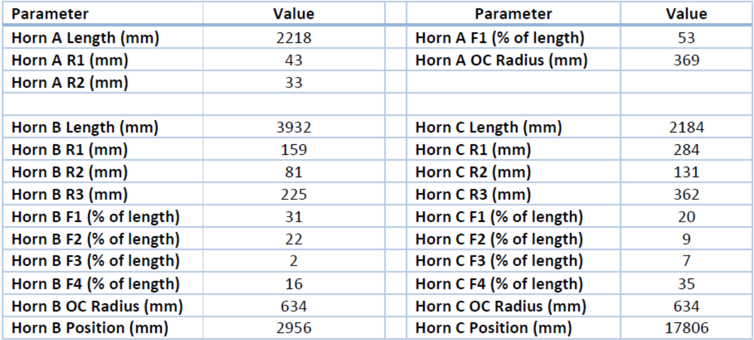
Fast CP Fitness estimator was determined by calculating the change in CP sensitivity given some fixed change in a single energy bin.



CP Fitness vs configuration

Optimization of beamline designs: DUNE/LBNF beam

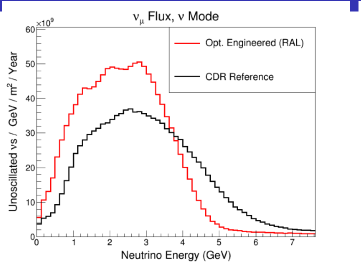
Optimized horn design with 297kA current :

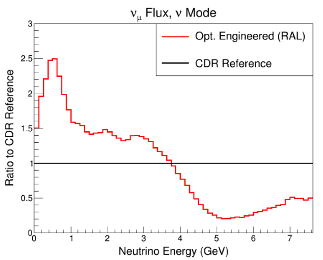


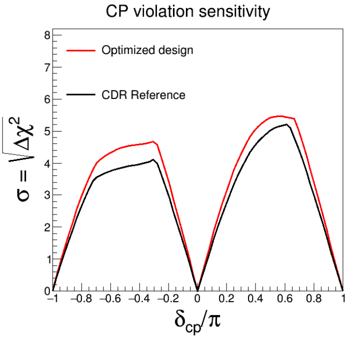
Parameter	Value		Parameter	Value
Horn A Length (mm)	2218		Horn A F1 (% of length)	53
Horn A R1 (mm)	43		Horn A OC Radius (mm)	369
Horn A R2 (mm)	33			
Horn B Length (mm)	3932		Horn C Length (mm)	2184
Horn B R1 (mm)	159		Horn C R1 (mm)	284
Horn B R2 (mm)	81		Horn C R2 (mm)	131
Horn B R3 (mm)	225		Horn C R3 (mm)	362
Horn B F1 (% of length)	31		Horn C F1 (% of length)	20
Horn B F2 (% of length)	22		Horn C F2 (% of length)	9
Horn B F3 (% of length)	2		Horn C F3 (% of length)	7
Horn B F4 (% of length)	16		Horn C F4 (% of length)	35
Horn B OC Radius (mm)	634		Horn C OC Radius (mm)	634
Horn B Position (mm)	2956		Horn C Position (mm)	17806

Optimized target is 4λ (2m C) with $\sigma_{\text{beam}} = 2.7$mm, $E_p \sim 110$ GeV

Optimization of beamline designs: DUNE/LBNF beam





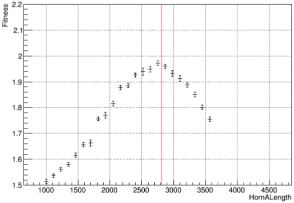


Computationally advanced optimization techniques = significant gain in flux and CPV sensitivity from *many* small changes

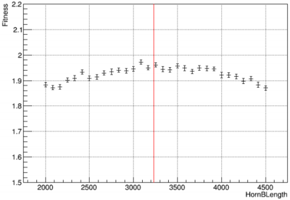
Gain in sensitivity ≡ 70% increase in FD mass

Optimization of beamline designs: DUNE/LBNF beam

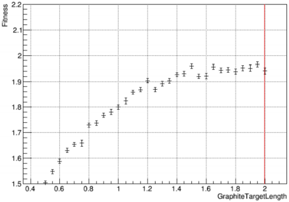
Scan over some sample optimization parameters:



Horn A length



Horn B length

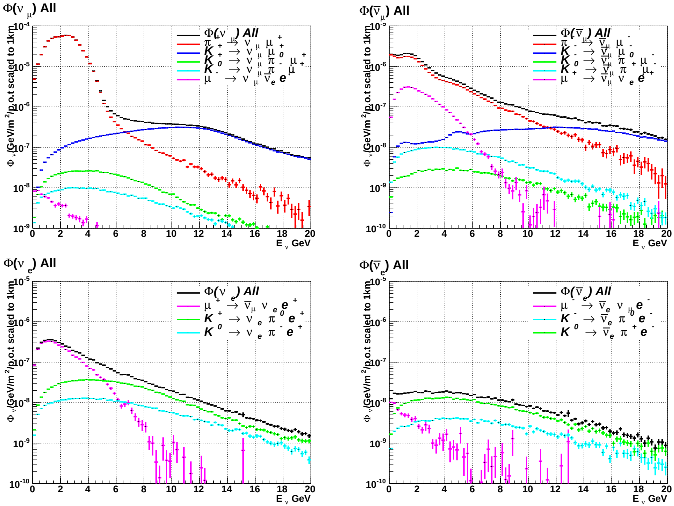


Target length

DIF Flux Estimation and Uncertainties in Long-Baseline Experiments

LBNF/DUNE Flux components at near and far

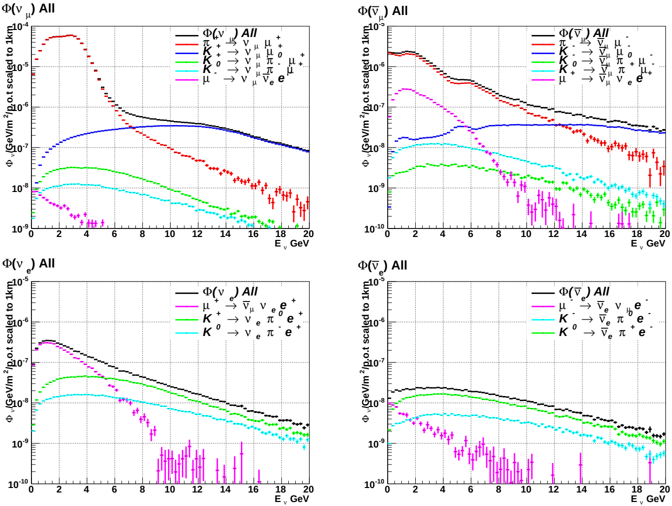
ND 570



Baseline scaled to 1km from middle of decay channel

LBNF/DUNE Flux components at near and far

FD 1300km



Baseline scaled to 1km from middle of decay channel

Flux Modeling Uncertainties at ND

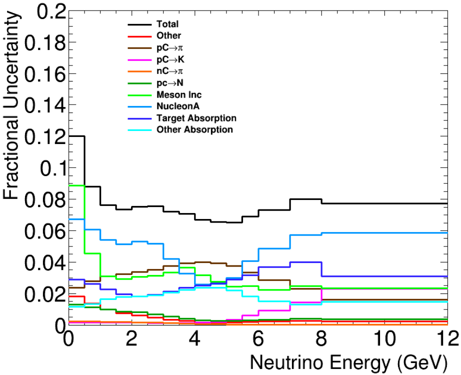
L. Fields and A. Bashyal

The main sources of flux modeling uncertainties are:

- **Hadron production uncertainties: driven by uncertainities in the hadron interaction models used to estimate hadron distributions exiting the target (prior to focusing) as well as secondary and tertiary interactions of hadrons with beamline material. Fully evaluated for LBNF/DUNE using the ppfx package developed for MINERνA.**
- **Focusing uncertainties: Dominated by horn material, geometry and magentic field modeling as well as target geometry and density. Alignment of the neutrino beamline elements can also have large impact on ν flux. Includes proton counting uncertainities. These uncertainties are assessed by simulating individual effects in Geant 4 and combining.**
- **Other beamline uncertainties: Primarily uncertainties on the distribution of passive material in the beamline: for e.g. impact of Nitrogen in the target chase, decay pipe window thickness...etc. Experience with NuMI indicates these are subdominant**

Flux Modeling Uncertainties at ND

L. Fields and A. Bashyal



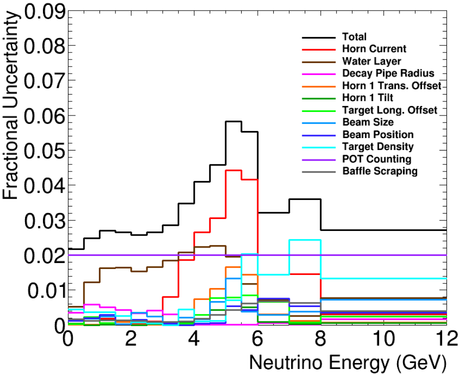
Hadron Prod. Uncertainties

NA49/MIPP/older datasets used to constrain $pC \rightarrow \pi^{\pm}, K^{\pm}, n(p)X$

Pion production by neutrons from data (assuming isospin symmetry)

Nucleon incident interactions not covered by data

Flux Modeling Uncertainties at ND

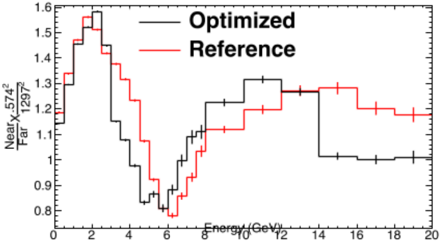


Focusing Uncertainties

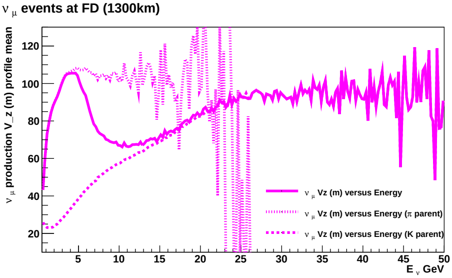
Detailed focusing uncertainties based on the NuMI experience in MINERνA. Detailed estimates for both 2015 NuMI-like design and CPV optimized design with simplified 2 horns.

Near to Far Extrapolation

Simple ratio of near spectrum/far spectrum:



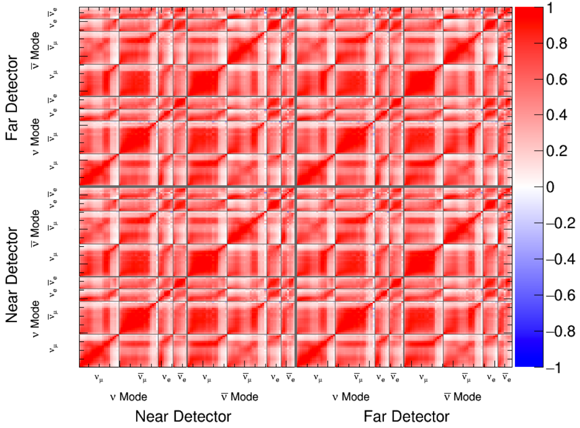
Neutrino parent decay location in decay pipe:



π/K decay kinematics and decay channel geometry are primary reason for strange shape of N/F ratio

Near to Far Extrapolation

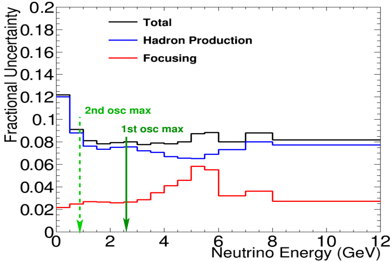
To correctly relate near to far fluxes - need to use a correlation matrix:



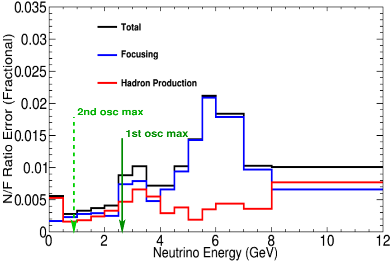
Flux correlation matrix comes from simulation and is highly correlated

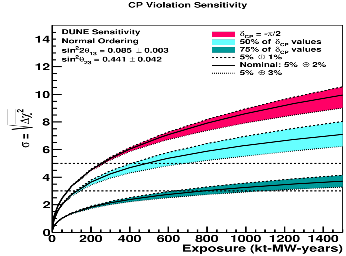
FD Flux Determination Uncertainities

Uncertainty on FD flux prediction



Residual uncertainty on flux at FD



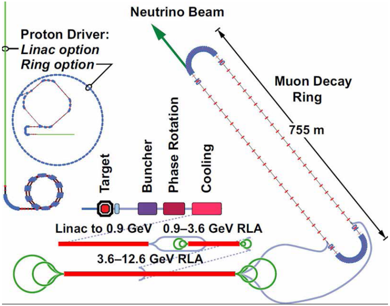


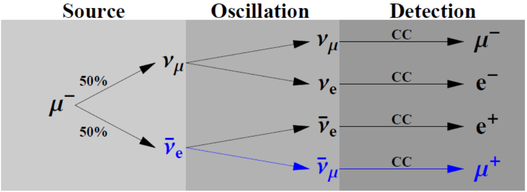
How well do we actually trust the simulation to correctly estimate the uncertainties on near → far extrapolation?

Muon decay-in-flight Beams and Neutrino Factories

Neutrino Factories/Muon Storage Rings

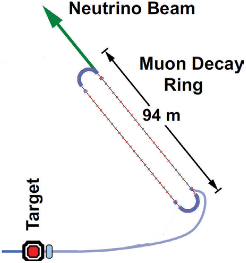
Long baseline experiments



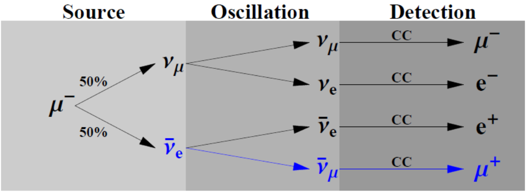


Neutrino Factories/Muon Storage Rings

Short baseline experiments

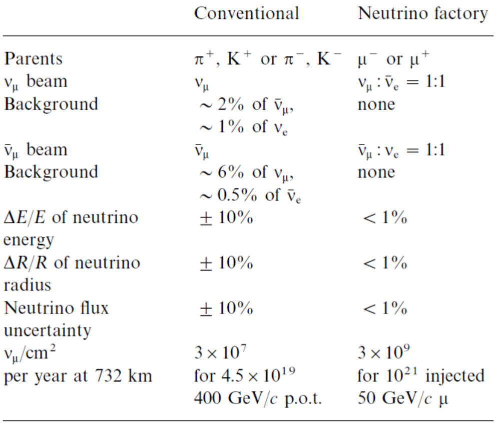


Neutrinos from STOred Muons (NuSTORM) @ CERN proposal:
`https://cds.cern.ch/record/2654649?ln=en`



Conventional Beams vs Neutrino Factories

From A. Blondel et. al. NIM A 451 (2000) 102-122

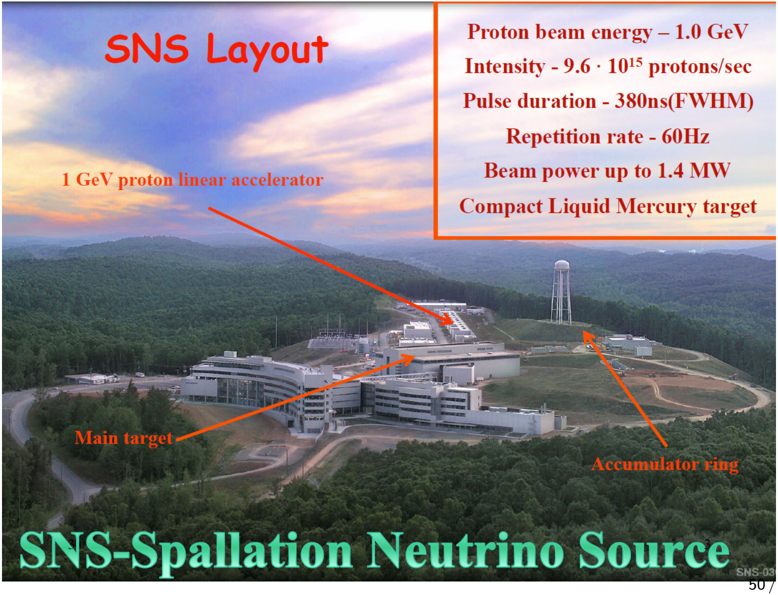


	Conventional	Neutrino factory
Parents	π^+, K^+ or π^-, K^-	μ^- or μ^+
ν_μ beam	ν_μ	$\nu_\mu : \bar{\nu}_e = 1{:}1$
Background	$\sim 2\%$ of $\bar{\nu}_\mu$, $\sim 1\%$ of ν_e	none
$\bar{\nu}_\mu$ beam	$\bar{\nu}_\mu$	$\bar{\nu}_\mu : \nu_e = 1{:}1$
Background	$\sim 6\%$ of ν_μ, $\sim 0.5\%$ of $\bar{\nu}_e$	none
$\Delta E/E$ of neutrino energy	$\pm 10\%$	$< 1\%$
$\Delta R/R$ of neutrino radius	$\pm 10\%$	$< 1\%$
Neutrino flux uncertainty	$\pm 10\%$	$< 1\%$
ν_μ/cm^2 per year at 732 km	3×10^7 for 4.5×10^{19} 400 GeV/c p.o.t.	3×10^9 for 10^{21} injected 50 GeV/c μ

Neutrino factories technologically challenging - but best chance for probing $\nu_e \rightarrow \nu_\mu$ appearance Muon storage rings currently only viable for short baseline.

Neutrinos from Accelerators: Decay-at-rest

Spallation Neutron Source Pion decay-at-rest beams



SNS Layout

Proton beam energy – 1.0 GeV

Intensity - $9.6 \cdot 10^{15}$ protons/sec

Pulse duration - 380ns(FWHM)

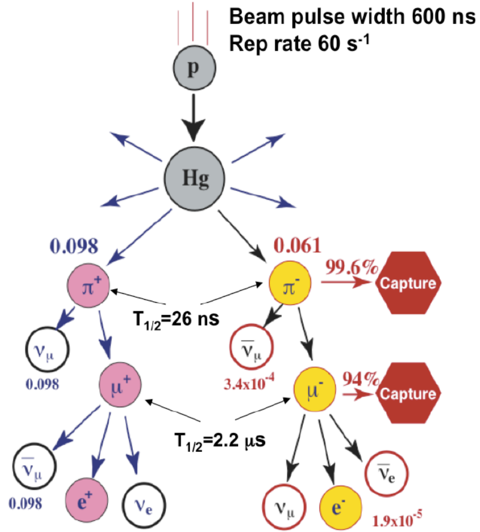
Repetition rate - 60Hz

Beam power up to 1.4 MW

Compact Liquid Mercury target

SNS-Spallation Neutrino Source

Spallation Neutron Source Pion decay-at-rest beams

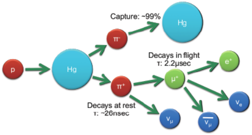


Decay-at-rest Kinematics

ν **Exercise: At the SNS a** pi$^+$ **will decay at rest to a** mu$^+$ **and a** ν_μ**. This is a two body decay which leads to a monochromatic beam of** ν_μ**. What is the energy of the** ν_μ**? Derive the two body formula for mass** M **decaying to** $m_1 + m_2$ **in the rest frame of** M**:**

$$E_2 = \frac{M^2 + m_2^2 - m_1^2}{2M} \tag{1}$$

Decay-at-rest Kinematics



$$\pi^+ \rightarrow \mu^+ + \boxed{\nu_\mu}$$

2-body decay: monochromatic 29.9 MeV ν_μ
PROMPT

$$\downarrow$$

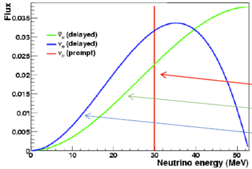
$$\mu^+ \rightarrow e^+ + \boxed{\bar{\nu}_\mu} + \boxed{\nu_e}$$

3-body decay: range of energies
between 0 and $m_\mu/2$
DELAYED (2.2 μs)

1 MW power for high ν flux

60 Hz timing protons on target (POT)

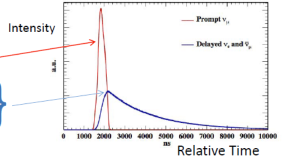
Produces sharply pulsed time structure for background rejection factor ~ 10^{-4}



Prompt ν_μ

delayed ν_μ–bar

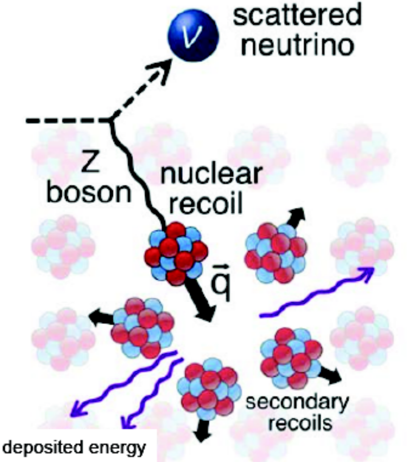
delayed ν_e }



Measurement of Coherent ν-Nucleus Scattering

The only experimental signature:

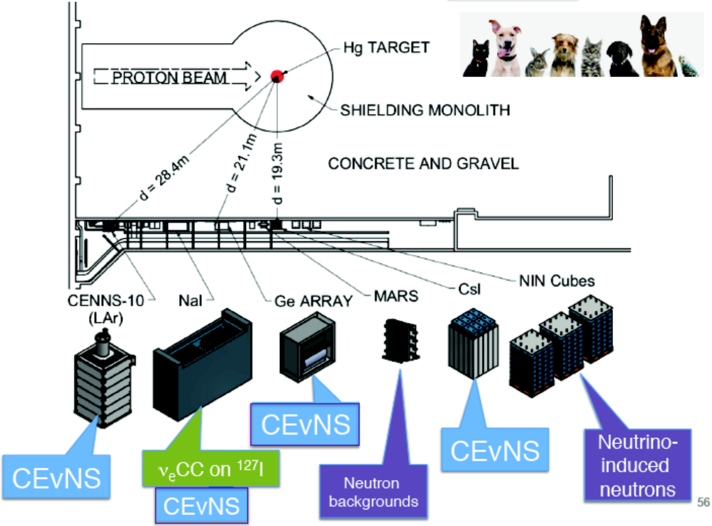
tiny energy deposited by nuclear recoils in the target material



The COHERENT Experiment and Proposed Upgrades

slides from K. Scholberg

Neutrino Alley Deployments: current & near future

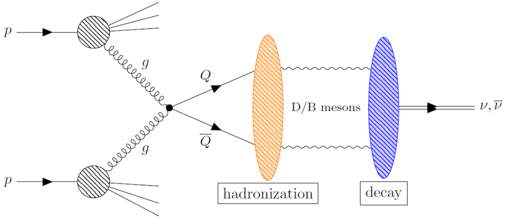


Neutrinos from colliding beams

Prompt neutrinos

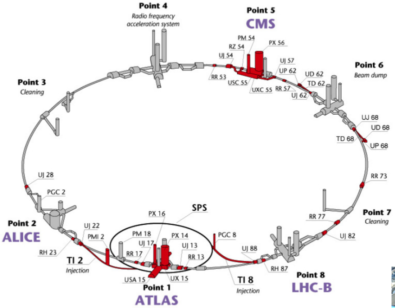
- In pp collision at the LHC, various hadrons are produced.
- A number of neutrinos are produced from subsequent decay of the secondary hadrons.

  e.g.) $\pi, K, D, B \ldots \rightarrow \nu + X$
- Neutrinos generated from the decay of charmed/bottom hadrons are called prompt neutrinos.



LHC ν Beams

Possible sites for detection



- Near CMS interaction point (IP)
  - 25 m from IP (quadruplet region)
  - 90 &120 m from IP (UJ53 & UJ57)
  - 240 m from IP (PR53 and PR57)
- Near ATLAS IP
  - 480 m from IP (TI18 and TI12)

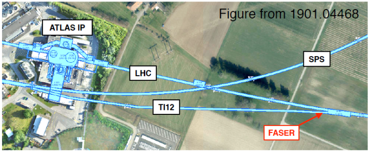
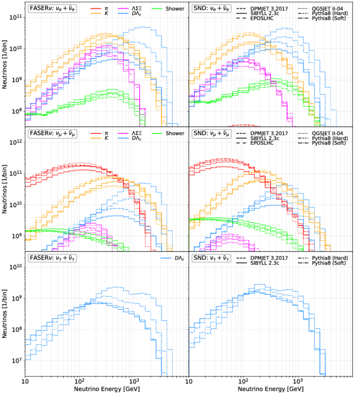


Figure from 1901.04468

Ref:1903.06564 (CMS note)
1901.04468 (FASER)

Forward Neutrinos from the LHC

The ForwArd Search ExpeRiment (FASERν) is an emulsion detector added to FASER an approved experiment dedicated to searching for light, extremely weakly interacting particles at the LHC located 480 m from the ATLAS interaction point. Calculations of forward neutrino fluxes at the LHC from arXiv 2105.08270:



Summary and Conclusions

Summary and Conclusions

- **High energy and high power proton accelerators can be used to generate neutrino beams of all 3 flavors ν_e, ν_μ, ν_τ with energies from 10's of MeV to multi-TeV**
- **High purity ν_μ GeV-scale neutrino beams from pion decay-in-flight are used by short and long-baseline experiments to study $\nu_\mu \rightarrow \nu_e$ oscillations**
- **Neutrino beams from pion decay-at-rest with energies of 10's MeV are used for measurements of coherent neutrino-nucleus scattering as well as searches for non-standard oscillations**
- **Neutirno beams from muon decay-at-rest produce equal numbers of ν_μ and ν_e and can be used to study $\nu_e \rightarrow \nu_\mu$ oscillations**
- **Far forward experiments at the LHC can study multi-TeV neutrino interactions and produce ν_τ beams**