

Top and Beauty synergies in SMEFT fits

based on works with Stefan Bissmann, Cornelius Grunwald and Kevin Kröniger, 2012.10456 [hep-ph]

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Supported by the Federal Ministry for Education and Research (BMBF)

DPG spring meeting March 2021: 6 sessions on flavor physics

NA 62	s
Belle, BaBar	c, b
BES III	c
Belle II	c, b
LHCb	$c, b, (s)$
ATLAS, CMS	$b, t (c, s)$
Z-factory (CLIC-like)	$c, b (t)$

Dream time to be in flavor physics

2 anomalies strengthened in past 3 weeks: R_K : 3.1σ new LHCb, $(g - 2)$ of muon 4.2σ — new FNAL result

- rates and angular distributions $b \rightarrow s\mu\mu$, $b \rightarrow s\gamma$ aka "the global fit"
- R_{K,K^*} branching ratios $b \rightarrow s\mu\mu$ vs $b \rightarrow see$
- R_{D,D^*} $b \rightarrow c\tau\nu$ vs $b \rightarrow c(e, \mu)\nu$
- Cabibbo-angle anomaly V_{us} from $s \rightarrow u\mu\nu$ vs $d \rightarrow ue\nu$
- $(g - 2)$ of muon and electron

common denominator: "something with leptons (in low energy data) "

Flavor continues to be interesting and inspiring; the anomalies require flavor BSM model building and flavorful fits.

Moving ahead ... getting more global

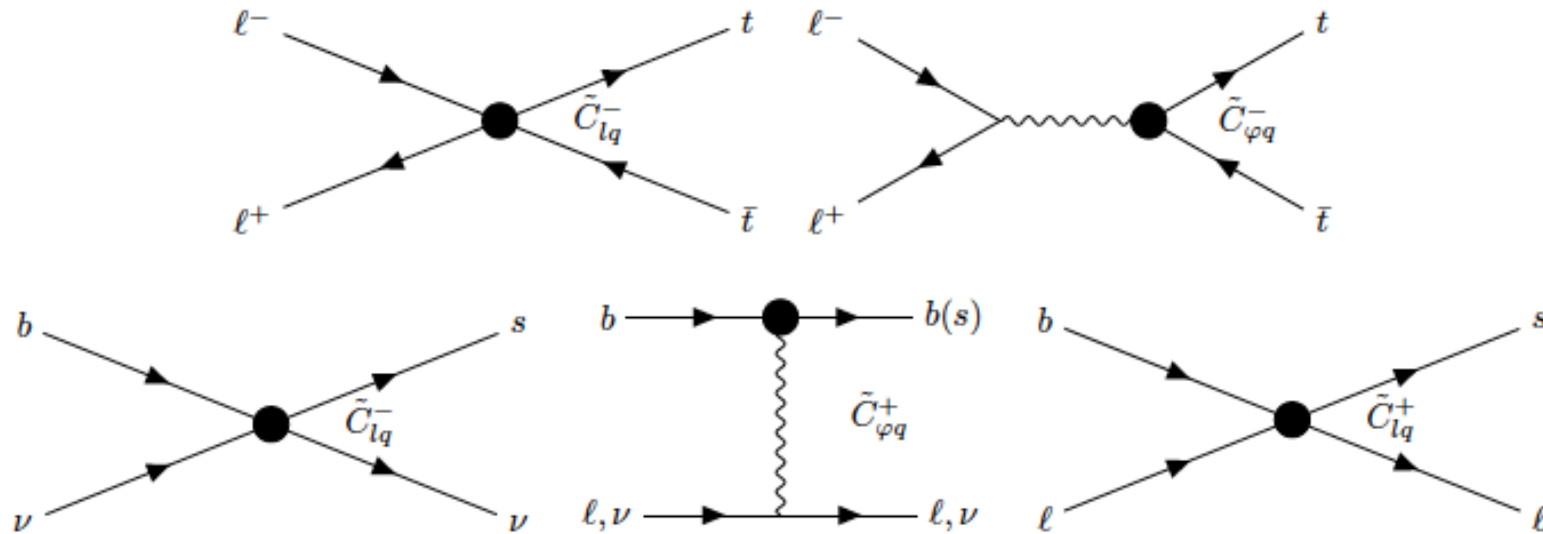
towards more global approach across the flavors $s, c, b, t...$

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The tool to achieve a cross community global analysis are effective field theories: Study correlations among multi-observables from different experiments ($B \rightarrow K^{(*)} \mu\mu, B_s \rightarrow \mu\mu, B \rightarrow X_s \gamma$) in WET (aka C_7, C_9, C_{10} -fits). [ongoing precision program](#)

Use SMEFT to include tops, and exploit unbroken SM symmetries $SU(2)_L \times U(1)_Y$ as a lab for flavor links.

top and beauty synergies



SMEFT coefficients $C^\pm = C^{(1)} \pm C^{(3)}$ top and beauty, leptons and neutrinos, linked and complementary; **flat directions are removed**

$b \rightarrow s\mu\mu$ (LHC), probes C^+

$b \rightarrow s\nu\nu$ (BelleII), probes C^-

$e^+e^- \rightarrow t\bar{t}$ (CLIC-like), probes C^- — quark flavor link implied $C_{23} = V_{tb}V_{ts}^*C_{33}$, lepton universality,....

11 dim 6 operators in fit [2012.10456](#) . Penguins, dipole operators

$$O_{\varphi q}^{(1)} = \left(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \right) (\bar{q}_L \gamma^\mu q_L) , \quad O_{\varphi q}^{(3)} = \left(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi \right) (\bar{q}_L \tau^I \gamma^\mu q_L) ,$$

$$O_{\varphi u} = \left(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi \right) (\bar{u}_R \gamma^\mu u_R) , \quad O_{uG} = (\bar{q}_L \sigma^{\mu\nu} T^A u_R) \tilde{\varphi} G_{\mu\nu}^A ,$$

$$O_{uB} = (\bar{q}_L \sigma^{\mu\nu} u_R) \tilde{\varphi} B_{\mu\nu} , \quad O_{uW} = (\bar{q}_L \sigma^{\mu\nu} \tau^I u_R) \tilde{\varphi} W_{\mu\nu}^I ,$$

and semileptonic four-fermion operators

$$O_{lq}^{(1)} = (\bar{l}_L \gamma_\mu l_L) (\bar{q}_L \gamma^\mu q_L) , \quad O_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L) (\bar{q}_L \gamma^\mu \tau^I q_L) , \quad O_{qe} = (\bar{q}_L \gamma_\mu q_L) (\bar{e}_R \gamma^\mu e_R) ,$$

$$O_{eu} = (\bar{e}_R \gamma_\mu e_R) (\bar{u}_R \gamma^\mu u_R) , \quad O_{lu} = (\bar{l}_L \gamma_\mu l_L) (\bar{u}_R \gamma^\mu u_R) .$$

Corresponding Wilson coefficients have up to four **flavor indices**,

for instance $C_{lq}^{(1)kl ij} \cdot (\bar{l}_{Lk} \gamma_\mu l_{Ll}) (\bar{q}_{Li} \gamma^\mu q_{Lj})$, $i, j, k, l = 1, 2, 3$.

quark flavor considerations

Quark flavor patterns in operators: $\bar{q}_{Li}(\dots)q_{Lj}$, $\bar{q}_{Li}(\dots)u_{Rj}$ and $\bar{u}_{Ri}(\dots)u_{Rj}$.

Top-(beauty)-philic flavor pattern: only $C^{i=3,j=3}$ switched on.

Consider second-third generation only

Top-(beauty)-philic: $C_x^{ij} = C_x^{33} \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$ for all 11 ops O_x .

Flavor mixing for doublets q_L : $V_{CKM} = V_u V_d^\dagger$. In up-mass basis $V_u = 1$. $d_L^{\text{mass}} = V_{CKM} d_L^{\text{flavor}}$

all $\bar{q}_{Li}(\dots)q_{Lj}$ ops:

$$C_{lq}^{(1,3)}, C_{\varphi q}^{(1,3)} \propto \begin{pmatrix} |V_{ts}|^2 & V_{tb}V_{ts}^* \\ h.c. & |V_{tb}|^2 \end{pmatrix} \sim \begin{pmatrix} 0 & -0.04 \\ -0.04 & 1 \end{pmatrix}$$

tree level FCNCs; synergies between top and $b \rightarrow s$ anomalies

lepton flavor considerations

1. most of today's data, e.g., $b \rightarrow s\ell^+\ell^-$, is for $\ell = \mu$. Therefore, most of the results are "lepton-specific" $k = l = 2$.

2. notable exceptions are bounds on dineutrino modes

$$B(B \rightarrow K^{(*)}\nu\bar{\nu}) = \sum_{k,l} B(B \rightarrow K^{(*)}\nu_k\bar{\nu}_l), \text{ which are flavor-summed.}$$

3. To include 2., we assume lepton universality. So, in the semileptonic 4-fermion operators, we assume for the lepton flavor $C^{kl} \propto \delta_{kl}$.

(in view of 1., this is only a mild assumption, however, turns out that $B(B \rightarrow K^{(*)}\nu\bar{\nu})$ in particular when observed, is an important constraint)

4. In view of current tensions with R_K etc, it is desirable to perform lepton-specific fits for $ee, \mu\mu (\tau\tau)$ operators as well as LFV ones.

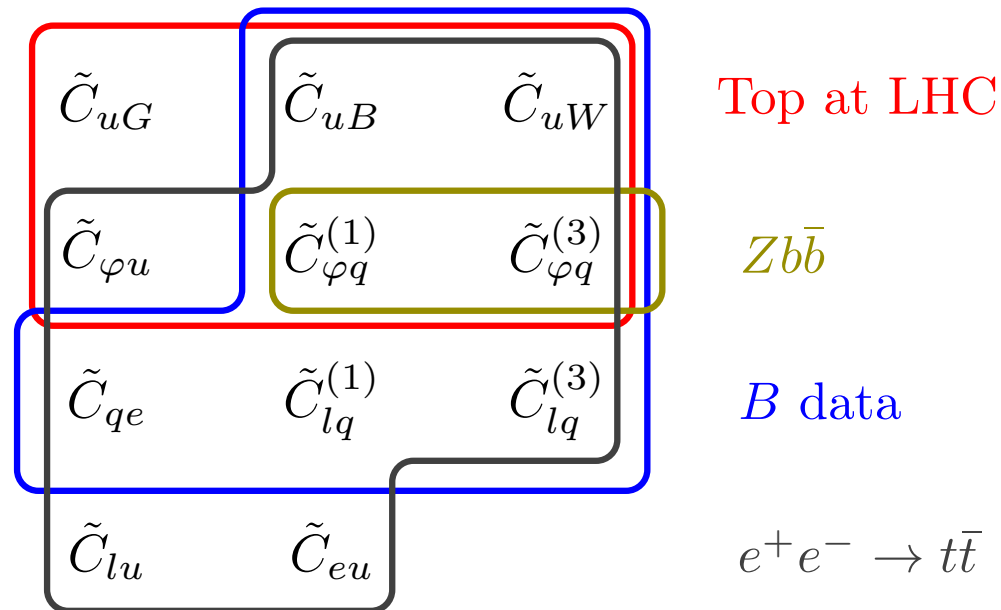
choose your initial state: e^+e^- -collider, muon collider are complementary

top and beauty synergies – a global fit

procedure:

scan 11 C_i at $\Lambda = 1$ TeV. 1-loop RGE to m_t, m_W . Matching onto WET, computation of b -observables, flavio, wilson tools

confronting to data; EFT-fitter



Process	Observable	Two-fermion operators	sl. four-fermion operators
$pp \rightarrow t\bar{t}$	σ^{inc}	\tilde{C}_{uG}	-
$pp \rightarrow t\bar{t}\gamma$	σ^{fid}	$\tilde{C}_{uB}, \tilde{C}_{uW}, \tilde{C}_{uG}$	-
$pp \rightarrow t\bar{t}Z$	σ^{inc}	$\tilde{C}_{uB}, \tilde{C}_{uW}, \tilde{C}_{uG}, \tilde{C}_{\varphi q}^-, \tilde{C}_{\varphi u}$	-
$t \rightarrow bW$	$F_{0,L}$	\tilde{C}_{uW}	-
Top decay	Γ_t	$\tilde{C}_{\varphi q}^{(3)}, \tilde{C}_{uW}$	-
$Z \rightarrow b\bar{b}$	$A_{FB}^b, R_b, \sigma_{\text{had}}$	$\tilde{C}_{\varphi q}^+$	-
$b \rightarrow s\gamma$	BR	$[\tilde{C}_{uB}], [\tilde{C}_{uW}], \{\tilde{C}_{uG}\}, [\tilde{C}_{\varphi q}^{(3)}]$	-
$b \rightarrow sl^+l^-$	BR, $A_{FB}, P_i^{(l)}, \dots$	$[\tilde{C}_{uB}], [\tilde{C}_{uW}], \{\tilde{C}_{uG}\}, \tilde{C}_{\varphi q}^{+(*)}, [\tilde{C}_{\varphi q}^{(3)}]$	$\tilde{C}_{lq}^{+(*)}, \tilde{C}_{qe}^{(*)}$
$b \rightarrow s\nu\bar{\nu}$	BR	$\tilde{C}_{\varphi q}^{+(**)}$	$\tilde{C}_{lq}^{-(*)}$
Mixing	ΔM_s	$[\tilde{C}_{uW}], \{\tilde{C}_{uG}\}, [\tilde{C}_{\varphi q}^{(1,3)}]$	-
$e^+e^- \rightarrow t\bar{t}$	σ, A_{FB}	$\tilde{C}_{uB}, \tilde{C}_{uW}, \{\tilde{C}_{uG}\}, \tilde{C}_{\varphi q}^-, \tilde{C}_{\varphi u}$	$\tilde{C}_{eu}, \tilde{C}_{qe}, \tilde{C}_{lu}, \tilde{C}_{lq}^-$

Process	Observable	\sqrt{s}	Int. luminosity	Experiment
$t\bar{t}\gamma$	$\sigma^{\text{fid}}(t\bar{t}\gamma, 1\ell), \sigma^{\text{fid}}(t\bar{t}\gamma, 2\ell)$	13 TeV	36.1 fb ⁻¹	ATLAS
$t\bar{t}Z$	$\sigma^{\text{inc}}(t\bar{t}Z)$	13 TeV	77.5 fb ⁻¹	CMS
$t\bar{t}$	$\sigma^{\text{inc}}(t\bar{t})$	13 TeV	36.1 fb ⁻¹	ATLAS
	F_0, F_L	8 TeV	20.2 fb ⁻¹	ATLAS
	Γ_t	8 TeV	20.2 fb ⁻¹	ATLAS

Table 1: Considered observables for top- quark processes at the LHC 2012.10456 [hep-ph] .

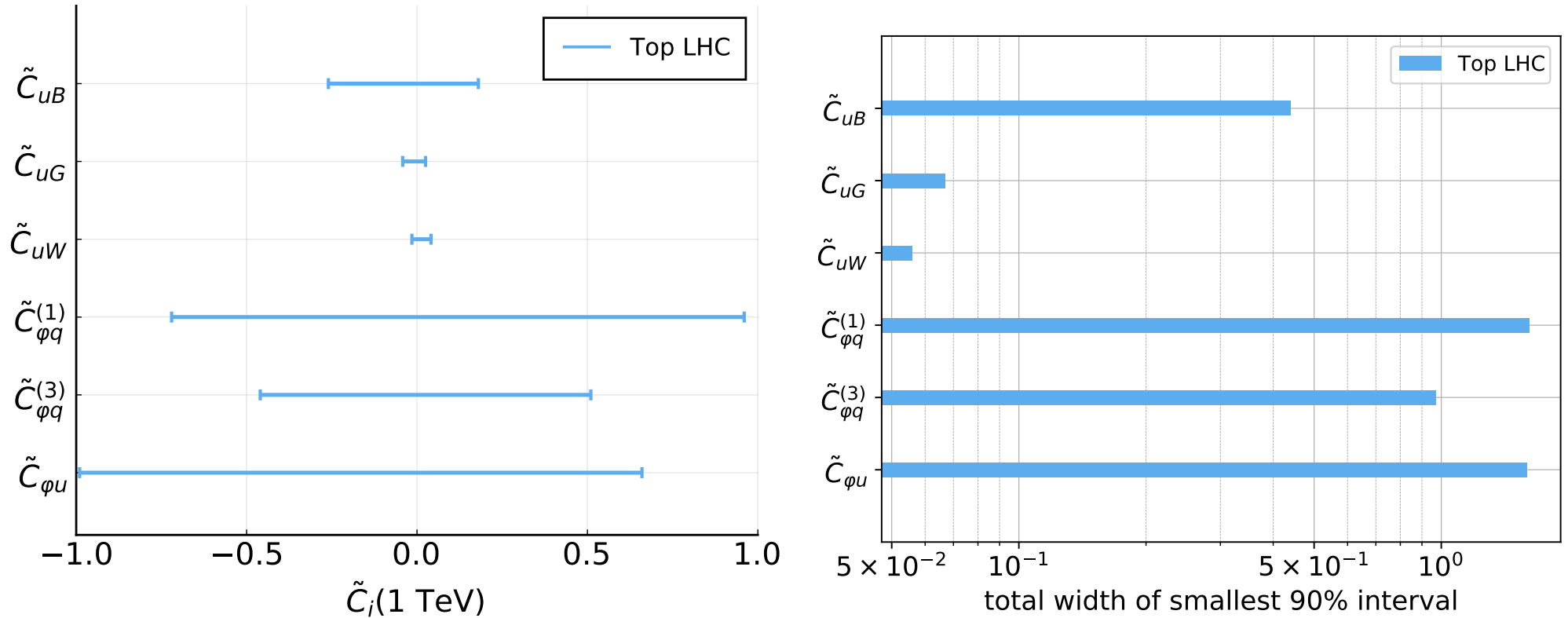


Figure 1: Constraints on SMEFT \tilde{C}_i at $\Lambda = 1$ TeV from top measurements in Tab. 1; marginalized smallest intervals containing 90 % posterior probability (left) and the total width of these intervals (right). For all coefficients we choose a uniform distribution in $-1 \leq \tilde{C}_i \leq 1$ as the prior. **6 WCs constrained**

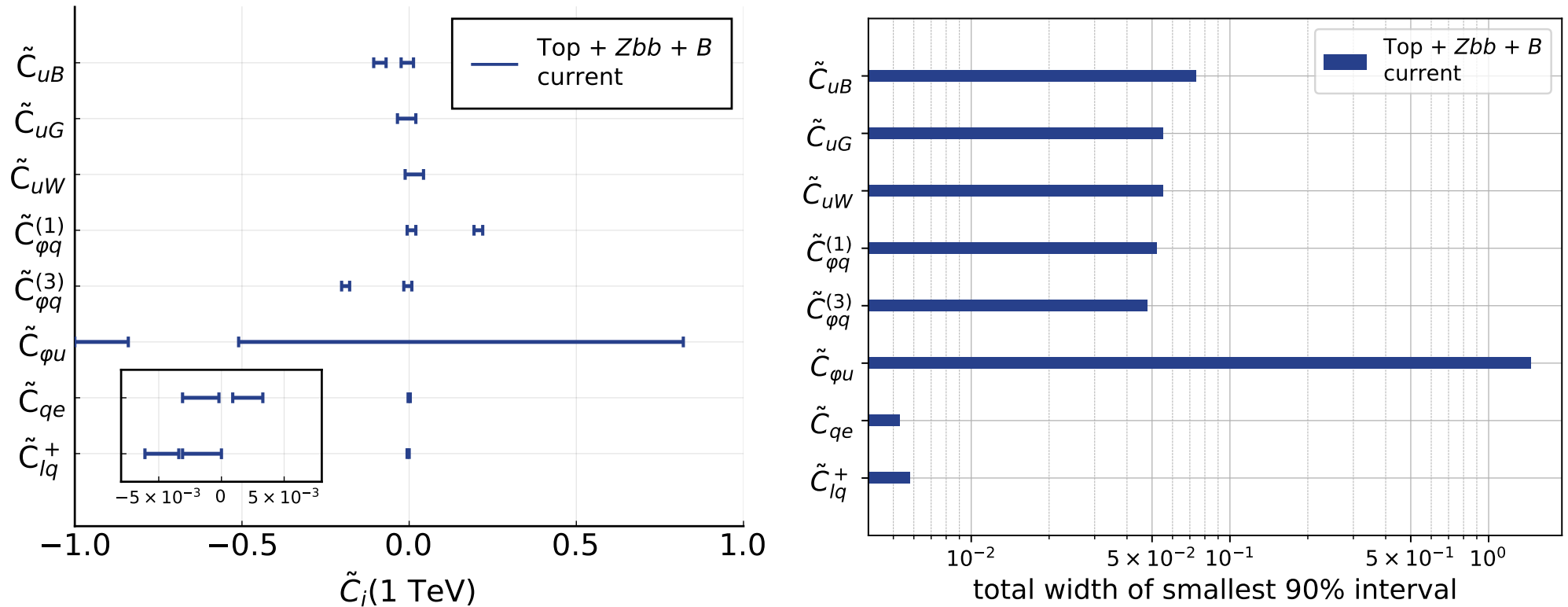


Figure 2: Constraints on SMEFT coefficients \tilde{C}_i in Eq. (??) obtained in a fit to top-quark data in Tab. 1, Zbb data, and B physics data in Tab. ?? . Shown are smallest intervals containing 90 % posterior probability (left) and total width of these intervals (right). For the prior we assume a uniform distribution over the interval $-1 \leq \tilde{C}_i \leq 1$. **8 WCs constrained, including 2 sl 4-fermis, $C_{\phi u}$ still a mess**

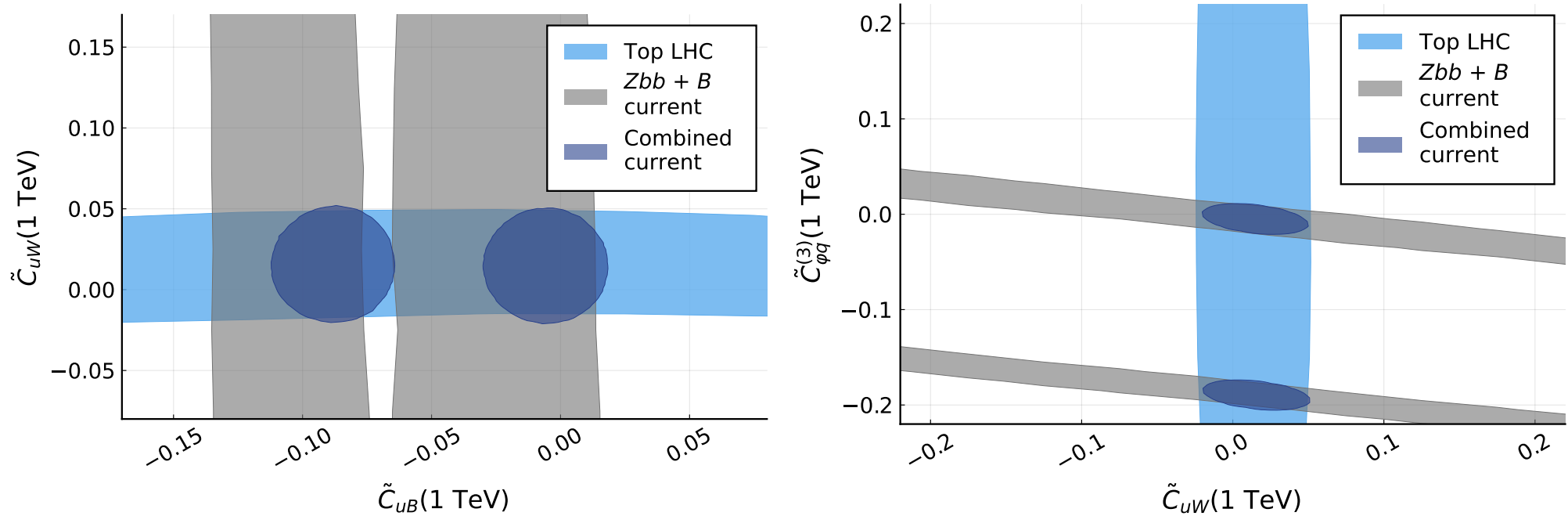


Figure 3: Examples for two-dimensional posterior distributions of SMEFT coefficients \tilde{C}_i in Eq. (??) obtained in a fit to top-quark data (light blue), B physics data (grey) and the combined dataset including Zbb data (blue). Shown are the smallest intervals containing 90 % of the posterior distribution. For the prior we assume a uniform distribution over the interval $-1 \leq \tilde{C}_i \leq 1$. **synergies at work**

top- b synergies near: w Belle II+HL-LHC

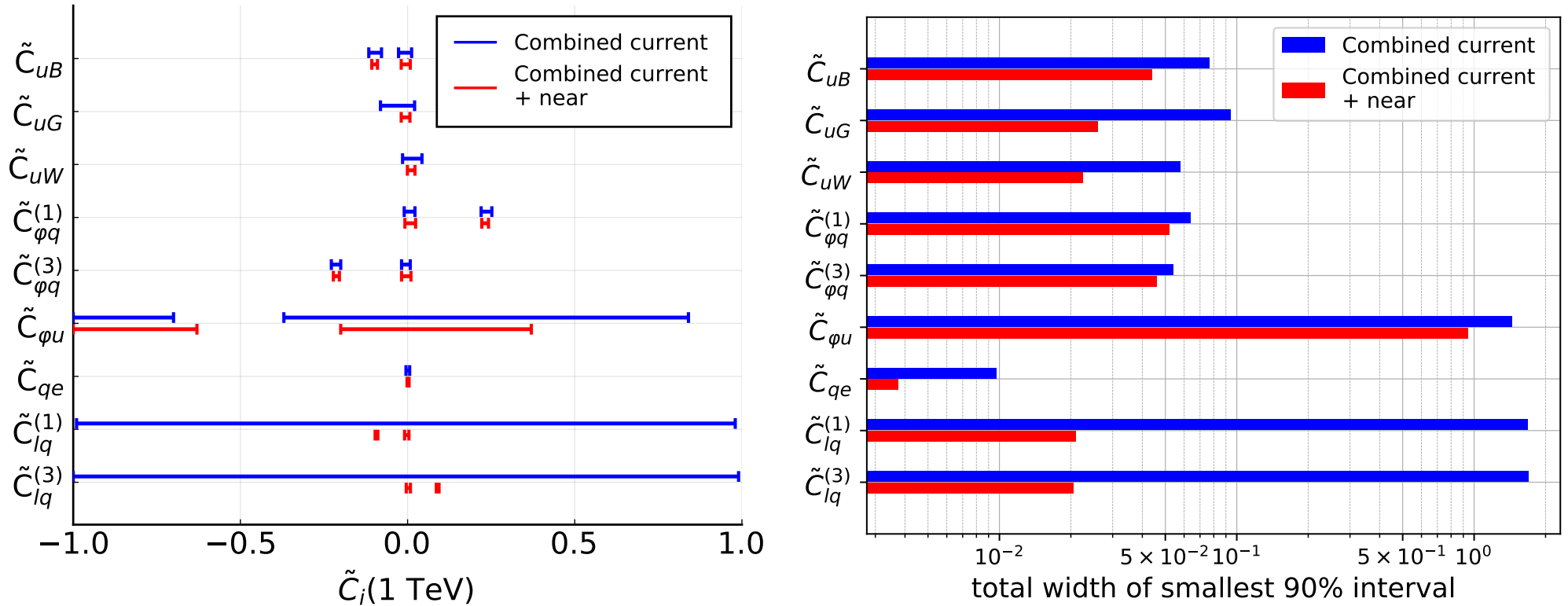


Figure 4: Constraints on coefficients \tilde{C}_i from fits to current top-quark and B measurements in Tabs. 1 and ?? (blue) and to current measurements and projections of top-quark and B observables in Tabs. 1-?? (red). Shown are the marginalized smallest intervals containing 90 % posterior probability (left) and the total widths of these intervals (right). **both C_{lq}^{\pm} resolved**

top- b synergies tomorrow (w CLIC)

Observable	\sqrt{s}	Polarization (e^-, e^+)	Ref. experiment	SM Re
$\sigma_{t\bar{t}}, A_{\text{FB}}$	380 GeV	(80%, 0)	[?]	[?]
$\sigma_{t\bar{t}}, A_{\text{FB}}$	1.4 TeV	(80%, 0)	[?]	[?]
$\sigma_{t\bar{t}}, A_{\text{FB}}$	3 TeV	(80%, 0)	[?]	[?]

Table 2: Observables at different energies and polarizations for $t\bar{t}$ production at CLIC Abramowicz:2018. SM predictions are taken from [?].

top- b synergies tomorrow CLIC only)

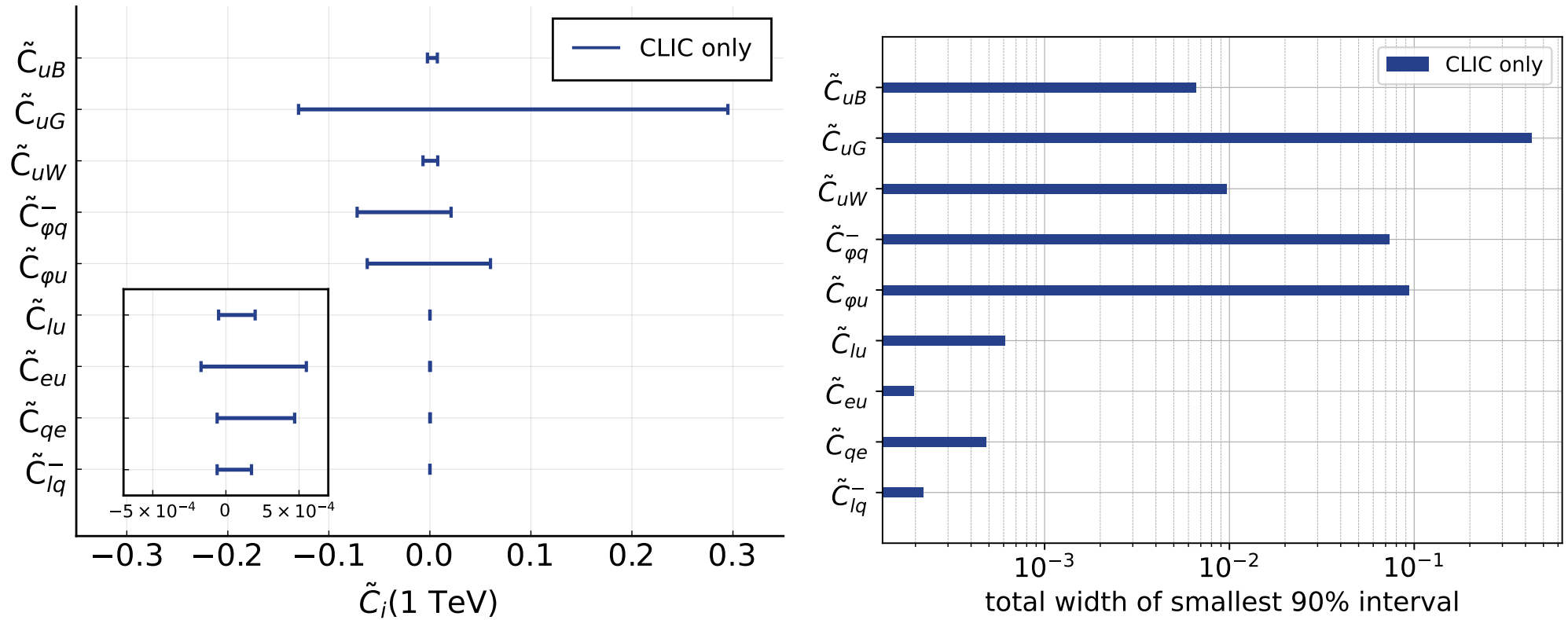


Figure 5: Constraints on coefficients \tilde{C}_i from fits to CLIC observables in Tab. 2. Shown are the marginalized smallest intervals containing 90 % posterior probability (left) and the total widths of these intervals (right). **4 sl 4-fermis; electron-specific; only C_{lq}^- and $C_{\varphi q}^-$**

top- b synergies tomorrow (BelleII+HL-LHC+CLIC)

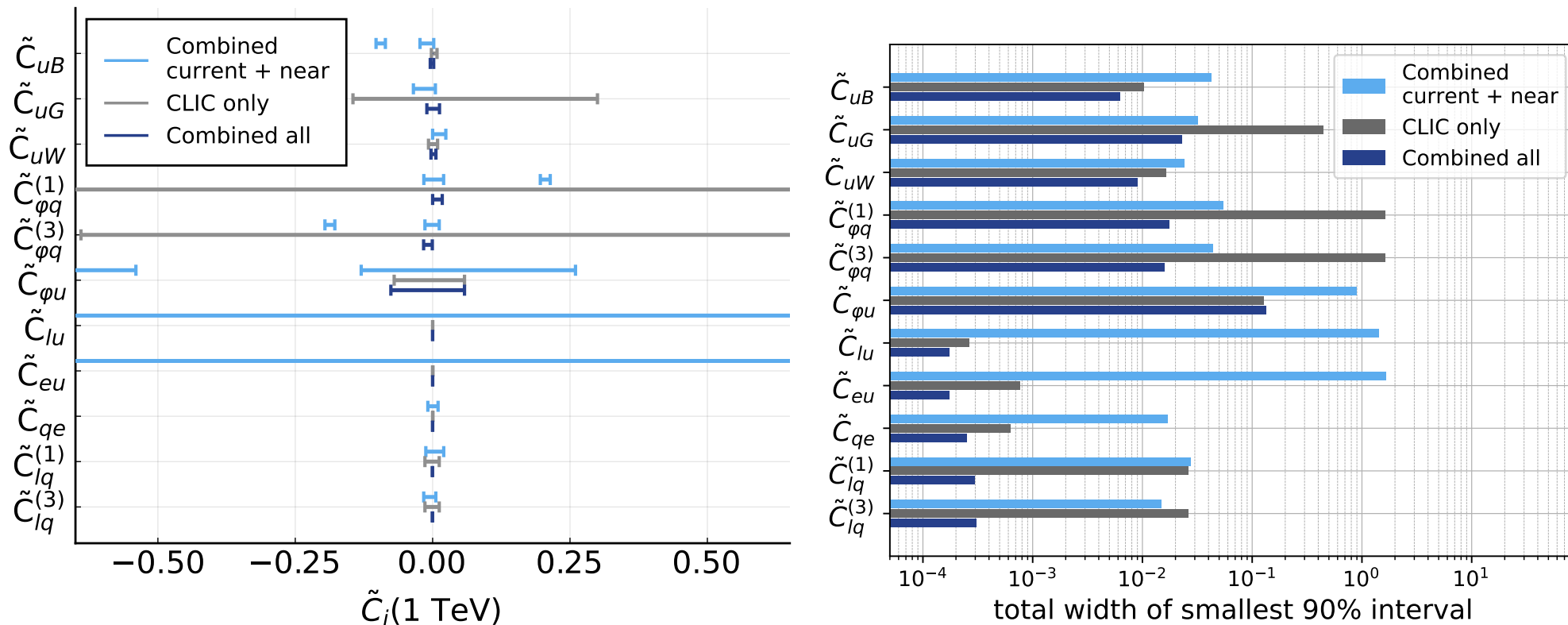


Figure 6: Constraints on coefficients \tilde{C}_i from fits to top-quark and B data and near-future projections at HL-LHC and Belle II in Tabs. 1-?? and CLIC future projections in Tab. 2. Shown are the marginalized smallest intervals containing 90 % posterior probability (left) and the total widths of these intervals (right).

- Synergies between beauty and top are reality [Fox et al 2007](#), [Bissmann '21](#), [Brugisser '21](#) and do work!
- semileptonic 4 fermion operators connect top to b -anomalies
CMS reports constraints on semileptonic four-fermion operators from tops with leptons [2012.04120](#); weaker than our bounds for C_{qe}, C_{lq}^- , but CMS also probes C_{eu}, C_{lu} which is NOW unconstrained.
- lepton specific fits desirable
- sensitivity to flavor — exploit more flavor links