

# Stability of Light Exotic $\Lambda$ -hypernuclei with Unstable Cores

---

S.V. SIDOROV<sup>1,2,3</sup>, D.E. LANSKOY<sup>1</sup>, T.YU. TRETAKOVA<sup>1,2,3</sup>

<sup>1</sup> *Faculty of Physics, Moscow State University, Moscow, Russia*

<sup>2</sup> *Skobel'tsyn Institute of Nuclear Physics, Moscow State University, Moscow, Russia*

<sup>3</sup> *Joint Institute for Nuclear Research, Dubna, Russia*





# Skyrme-Hartree-Fock approach for hypernuclei

- Nucleon-nucleon Skyrme potential (Vautherin and Brink, 1972):

$$V_{NN}(\mathbf{r}_1, \mathbf{r}_2) = t_0(1 + x_0 P_\sigma)\delta(\mathbf{r}_{12}) + \frac{1}{2}t_1(1 + x_1 P_\sigma)(\mathbf{k}'^2\delta(\mathbf{r}_{12}) + \delta(\mathbf{r}_{12})\mathbf{k}^2) \\ + t_2(1 + x_2 P_\sigma)\mathbf{k}'\delta(\mathbf{r}_{12})\mathbf{k} + \frac{1}{6}t_3\rho^\alpha(\mathbf{R})(1 + x_3 P_\sigma)\delta(\mathbf{r}_{12}) + iW(\sigma_1 + \sigma_2)[\mathbf{k}' \times \delta(\mathbf{r})\mathbf{k}]$$

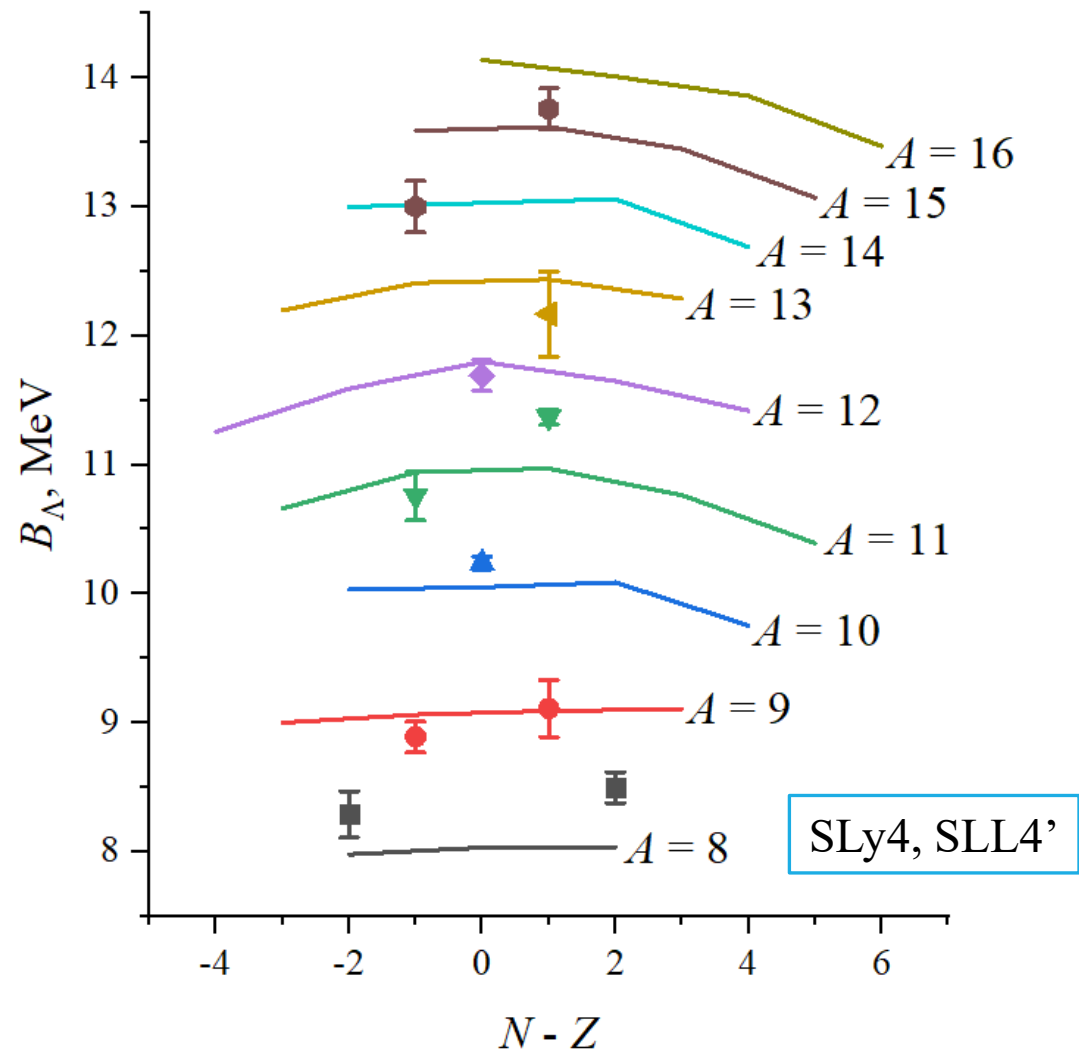
NN: SLy4, SkM\*, SkIII

- Hyperon-nucleon Skyrme potential (Rayet, 1981):

$$V_{\Lambda N}(\mathbf{r}_\Lambda, \mathbf{r}_q) = t_0^\Lambda(1 + x_0^\Lambda P_\sigma)\delta(\mathbf{r}_{\Lambda q}) + \frac{1}{2}t_1^\Lambda(\mathbf{k}^2\delta(\mathbf{r}_{\Lambda q}) + \delta(\mathbf{r}_{\Lambda q})\mathbf{k}'^2) \\ + t_2^\Lambda\mathbf{k}'\delta(\mathbf{r}_{\Lambda q})\mathbf{k} + \frac{1}{6}t_3^\Lambda\rho^\alpha(\mathbf{R})\delta(\mathbf{r}_{\Lambda q})$$

$\Lambda$ N: [SLL4](#), [SLL4'](#) (Schulze and Hiyama, 2014), [YBZ5](#) (Yamamoto et al, 1988),  
[LY1](#) (Lanskoy and Yamamoto, 1997), [LY5r](#) (Zhang et al, 2021), [SkSH1](#)  
(Fernandez et al, 1989)

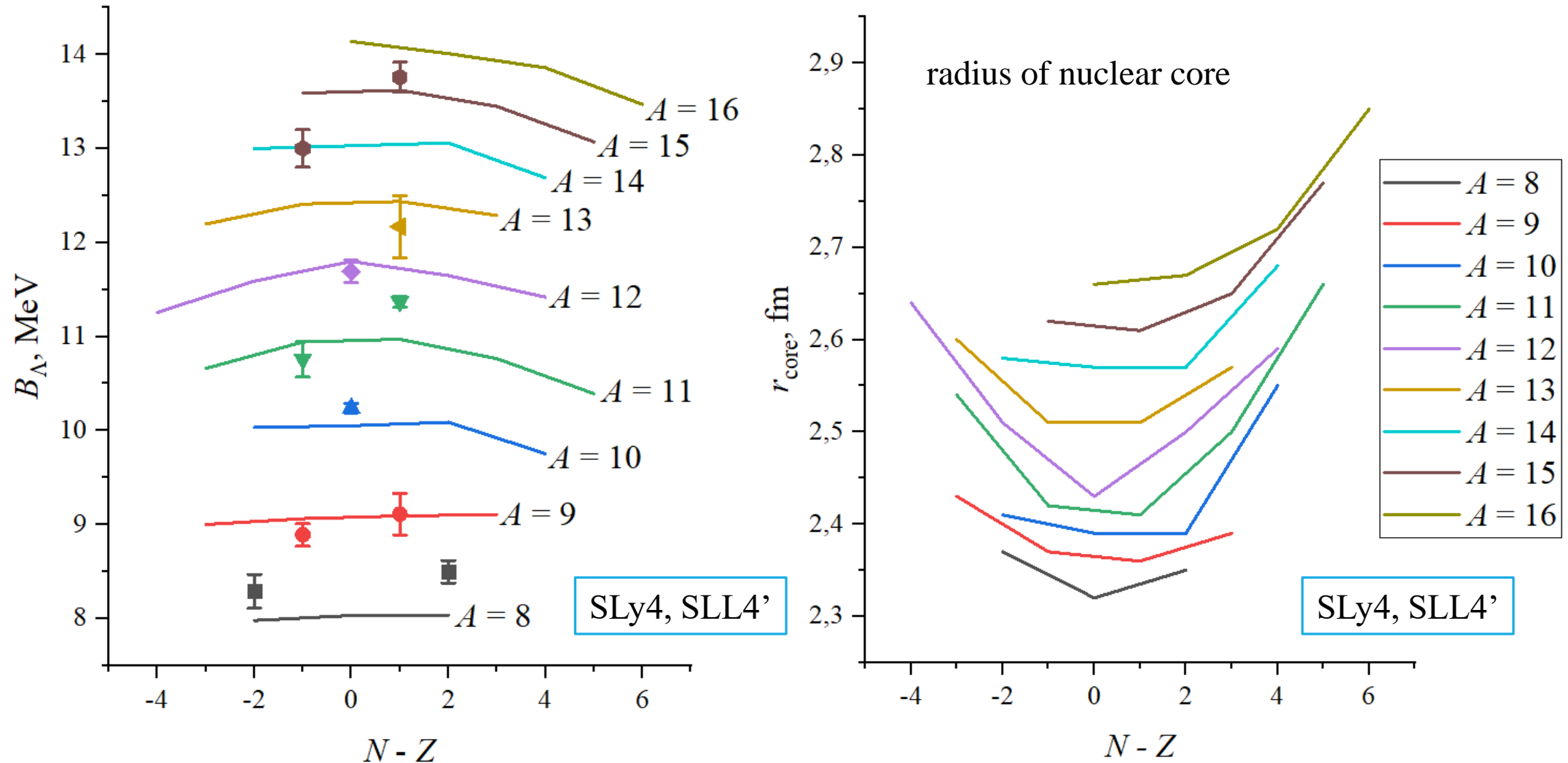
# Hyperon binding energies in $A+1_{\Lambda}Z$ hypernuclei



$$B_{\Lambda}(^{A+1}_{\Lambda}Z) = B_{tot}(^{A+1}_{\Lambda}Z) - B_{tot}(^AZ)$$

- The difference in neighboring isobar chains is around 1 MeV for lighter hypernuclei, smaller as  $A$  increases
- Symmetric character of  $B_{\Lambda}$  with respect to isospin  $N - Z$

# Hyperon binding energies and radii of nuclear cores in $^{A+1}_{\Lambda}Z$ hypernuclei



# Hypernuclei near the proton dripline

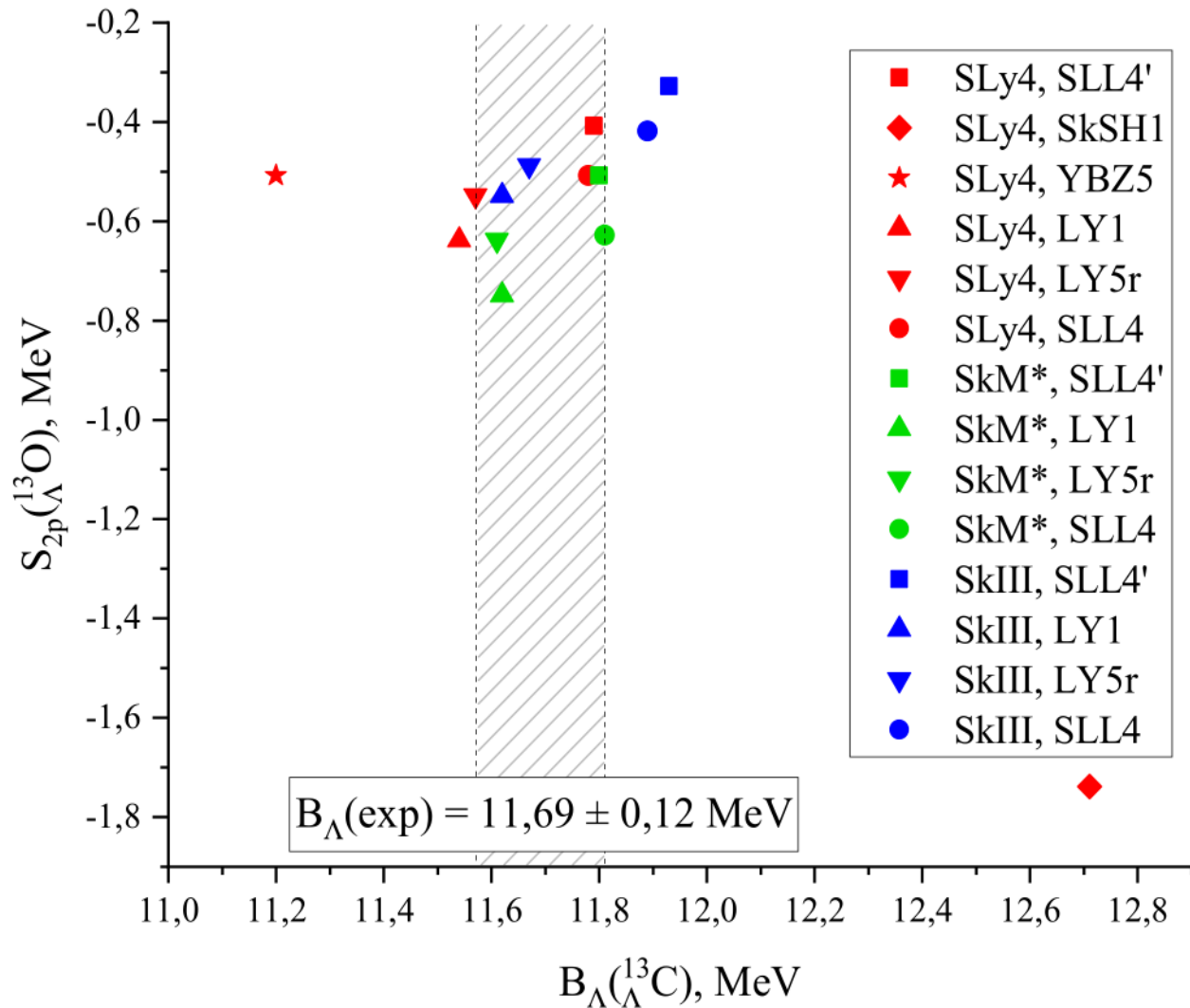
While we do not claim outright that hypernuclear HF approach gives precise predictions for proton (or two-proton) separation energies of hypernuclei, we set the following idea as the cornerstone of our method: hypernuclear HF allows to reproduce the hyperon binding energy  $B_\Lambda$  in light  $\Lambda$ -hypernuclei. Proton (two proton) separation energy  $S_p$  ( $S_{2p}$ ) can then be found using the relation:

$$\begin{aligned} S_p({}^A_\Lambda Z) &= S_p({}^{A-1}Z) + B_\Lambda({}^A_\Lambda Z) - B_\Lambda({}^{A-1}_\Lambda(Z-1)), \\ S_{2p}({}^A_\Lambda Z) &= S_{2p}({}^{A-1}Z) + B_\Lambda({}^A_\Lambda Z) - B_\Lambda({}^{A-2}_\Lambda(Z-2)). \end{aligned}$$

and experimental data for  $S_p({}^AZ)$  and  $S_{2p}({}^AZ)$ .

Here,  $S_p({}^{A-1}Z)$  or  $S_{2p}({}^{A-1}Z)$  is always taken from experiment, while  $B_\Lambda$  is calculated within HF approach when there are no experimental data available. Comparison between calculated values and experimental data on  $B_\Lambda$  in neighbouring nuclei can be used to verify the accuracy of our estimates for  $S_p$  (or  $S_{2p}$ ) in proton-rich hypernuclei.

# 2p separation energy in $^{13}_{\Lambda}\text{O}$



$^{12}\text{O}$  is unstable with respect to 2 proton decay ( $S_{2p}(^{12}\text{O}) = -1,638 \text{ MeV}$ ), and  $^{13}_{\Lambda}\text{O}$  is expected to decay similarly. On the left hand side we show

$$S_{2p}(^{13}_{\Lambda}\text{O}) = S_{2p}(^{12}\text{O}) + B_{\Lambda}(^{13}_{\Lambda}\text{O}) - B_{\Lambda}(^{11}_{\Lambda}\text{C})$$

exp  $\curvearrowright$ 
calc  $\curvearrowright$

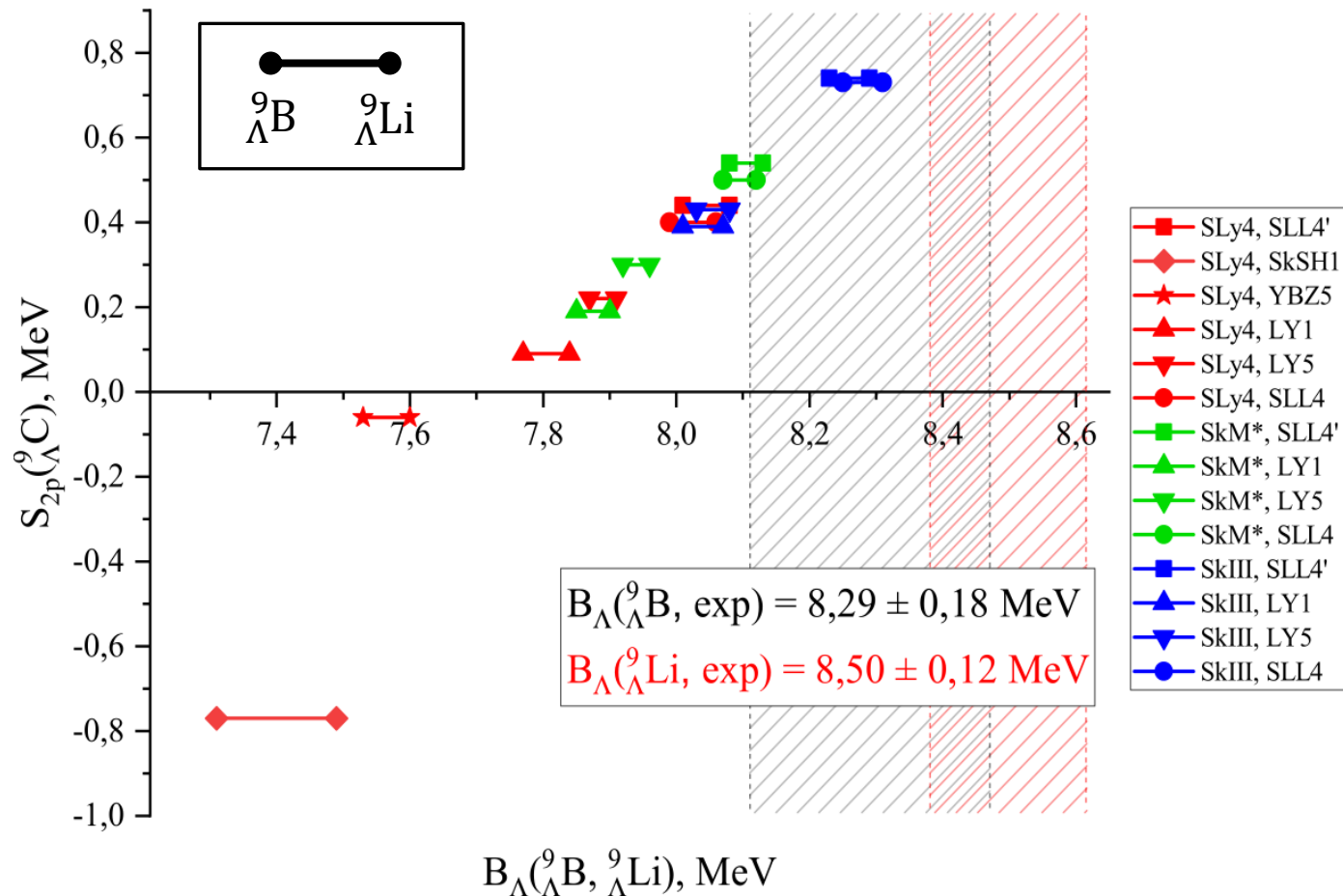
as a function of  $B_{\Lambda}(^{13}_{\Lambda}\text{C})$  for different NN and  $\Lambda\text{N}$  Skyrme interactions. Most of the results are in good agreement with the experimental hyperon binding energy in  $^{13}_{\Lambda}\text{C}$ .

**$^{13}_{\Lambda}\text{O}$  is unbound**

$^8_{\Lambda}\text{B}$ ,  $^{12}_{\Lambda}\text{N}$  are also unbound



# 2p separation energy in ${}^9_{\Lambda}\text{C}$



While  ${}^8\text{C}$  decays primarily by emitting 4 protons,  ${}^9_{\Lambda}\text{C}$  has 2 proton decay as critical decay mode, with bound  ${}^7_{\Lambda}\text{Be}$  as a daughter hypernucleus. On the left hand side we show

$$S_{2p}({}^9_{\Lambda}\text{C}) = S_{2p}({}^8\text{C}) + B_{\Lambda}({}^9_{\Lambda}\text{C}) - B_{\Lambda}({}^7_{\Lambda}\text{Be})$$

calc  $\rightarrow$   
 exp (-2.14 MeV)  $\uparrow$       exp (5.16 MeV)  $\uparrow$

as a function of  $B_{\Lambda}$  in  ${}^9_{\Lambda}\text{B}$  and  ${}^9_{\Lambda}\text{Li}$  for different NN and  $\Lambda\text{N}$  Skyrme interactions. The better  $B_{\Lambda}({}^9_{\Lambda}\text{B})$  and  $B_{\Lambda}({}^9_{\Lambda}\text{Li})$  are described, the stronger is the two-proton binding in  ${}^9_{\Lambda}\text{C}$ , indicating that  $S_{2p}({}^9_{\Lambda}\text{C}) > 0$ .

**${}^9_{\Lambda}\text{C}$  is bound!**

# Skyrme $\Lambda\Lambda$ -interaction for double- $\Lambda$ hypernuclei

Due to glue-like role of  $\Lambda$ -hyperon, there is a chance to stabilize the hypernuclei  ${}^8_{\Lambda}\text{B}$ ,  ${}^{12}_{\Lambda}\text{N}$  and  ${}^{13}_{\Lambda}\text{O}$  by adding yet another  $\Lambda$ -hyperon.  $\Lambda\Lambda$ -interaction then needs to be taken into account

- Hyperon-hyperon Skyrme potential:

$$V_{\Lambda\Lambda}(\mathbf{r}_1, \mathbf{r}_2) = \lambda_0 \delta(\mathbf{r}_{12}) + \frac{1}{2} \lambda_1 (\mathbf{k}'^2 \delta(\mathbf{r}_{12}) + \delta(\mathbf{r}_{12}) \mathbf{k}^2) + \lambda_2 \mathbf{k}' \delta(\mathbf{r}_{12}) \mathbf{k}$$

$\Lambda\Lambda$ : S $\Lambda\Lambda$ 1', S $\Lambda\Lambda$ 3' (Lanskoy, 1998, Minato and Hagino, 2011)

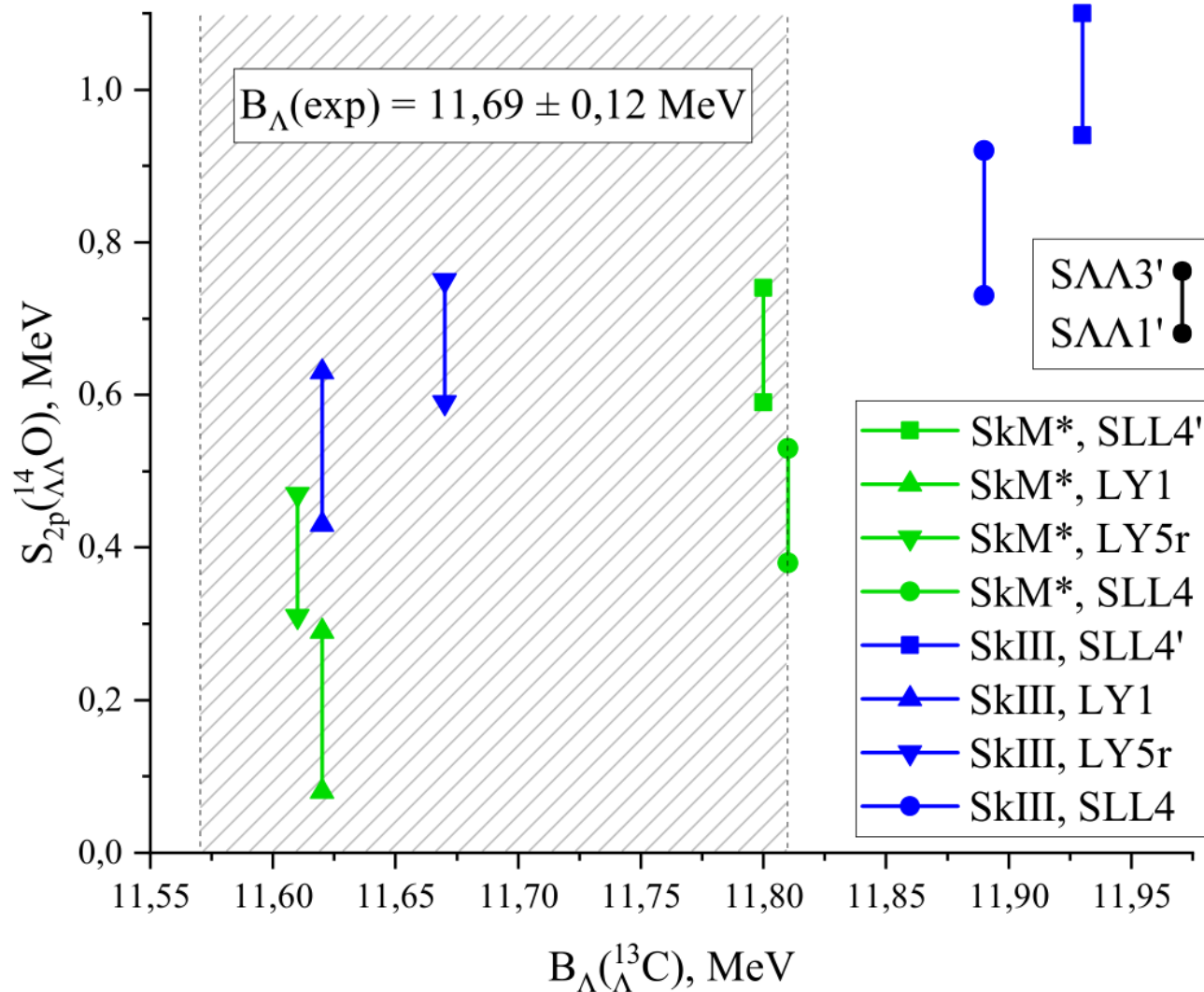
Proton (two proton) separation energy  $S_p$  ( $S_{2p}$ ) can then be found using the relation:

$$\begin{aligned} S_p({}_{\Lambda\Lambda}^AZ) &= S_p({}^{A-2}Z) + B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) - B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^{A-1}(Z-1)), \\ S_{2p}({}_{\Lambda\Lambda}^AZ) &= S_{2p}({}^{A-2}Z) + B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) - B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^{A-2}(Z-2)); \end{aligned}$$

Here, 2 hyperon binding energy is:

$$B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^AZ) = B_{tot}({}_{\Lambda\Lambda}^AZ) - B_{tot}({}^{A-2}Z)$$

# 2p separation energy in ${}_{\Lambda\Lambda}^{14}\text{O}$



$$S_{2p}({}_{\Lambda\Lambda}^{14}\text{O}) = S_{2p}({}^{12}\text{O}) + B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^{14}\text{O}) - B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^{12}\text{C})$$

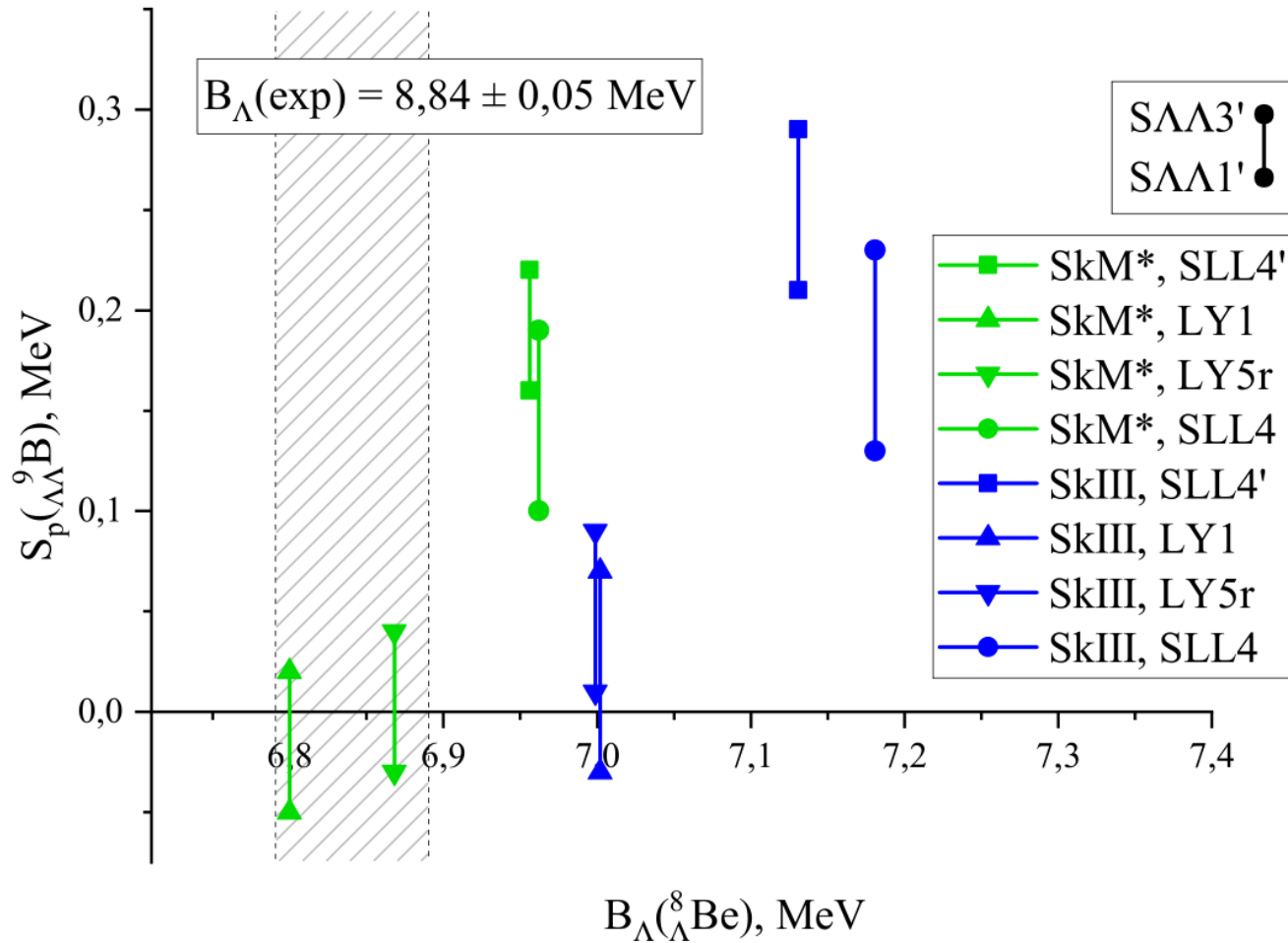
exp

calc

as a function of  $B_{\Lambda}({}_{\Lambda}^{13}\text{C})$  for different NN and  $\Lambda\text{N}$  Skyrme interactions. Earlier we concluded  ${}_{\Lambda}^{13}\text{O}$  is unbound; addition of another hyperon stabilizes the hypernucleus.

**${}_{\Lambda\Lambda}^{14}\text{O}$  is bound!**

# Proton separation energy in ${}_{\Lambda\Lambda}{}^9\text{B}$



$$S_p({}_{\Lambda\Lambda}{}^9\text{B}) = S_p({}^7\text{B}) + B_{\Lambda\Lambda}({}_{\Lambda\Lambda}{}^9\text{B}) - B_{\Lambda\Lambda}({}_{\Lambda\Lambda}{}^8\text{Be})$$

↙ exp (-2.01 MeV)

↖ calc ↗

as a function of  $B_{\Lambda}({}_{\Lambda}{}^8\text{Be})$  for different NN and  $\Lambda\text{N}$  Skyrme interactions. While we concluded  ${}_{\Lambda}{}^8\text{B}$  is unbound,

${}_{\Lambda\Lambda}{}^9\text{B}$  is possibly bound.

Hypernucleus  ${}_{\Lambda\Lambda}{}^{13}\text{N}$  is found to be unbound.

# Conclusions

Hypernuclear Hartree-Fock approach was utilized to study the properties of light proton-rich  $\Lambda$ -hypernuclei.

➤ Hyperon binding energy vs isospin dependence is more pronounced for the cases with more dramatic density changes, and the corresponding nuclei should be chosen as sources of information on  $\Lambda N$  interaction

➤ Among the studied hypernuclei:

- $Z = 5$ :  ${}^8_{\Lambda}B$  is unbound,  ${}^9_{\Lambda\Lambda}B$  could possibly be bound,
- $Z = 6$ :  ${}^9_{\Lambda}C$  is bound, therefore  ${}^{10}_{\Lambda\Lambda}C$  is also evidently bound,
- $Z = 7$ :  ${}^{12}_{\Lambda}N$  and  ${}^{13}_{\Lambda\Lambda}N$  are unbound,
- $Z = 8$ :  ${}^{13}_{\Lambda}O$  is unbound, while  ${}^{14}_{\Lambda\Lambda}O$  is bound.

Thank you for your attention