



РОСАТОМ



ГОСУДАРСТВЕННАЯ КОРПОРАЦИЯ ПО АТОМНОЙ ЭНЕРГИИ «РОСАТОМ»

${}^6\text{Li}(d,p_0){}^7\text{Li}$, ${}^6\text{Li}(d,p_1){}^7\text{Li}^*(0.478 \text{ МэВ})$,
 ${}^6\text{Li}(d,p_2){}^7\text{Li}^*(4.63 \text{ МэВ})$, ${}^6\text{Li}(d,p_4){}^7\text{Li}^*(7.46 \text{ МэВ})$,
 ${}^6\text{Li}(d,n_0){}^7\text{Be}$, ${}^6\text{Li}(d,n_1){}^7\text{Be}^*(0.429 \text{ МэВ})$,
 ${}^6\text{Li}(d,n_2){}^7\text{Be}^*(4.57 \text{ МэВ})$, ${}^6\text{Li}(d,n_4){}^7\text{Be}^*(7.21 \text{ МэВ})$,
 ${}^6\text{Li}(d,x){}^7\text{Be}$ REACTION CROSS SECTION

Generalov L.N., Zherebtsov V.A., Selyankina S.M.

**71st meeting on nuclear spectroscopy and atomic nucleus
structure «Nucleus-2021»**

Online-conference, 20-25 September

MOTIVATION

- Appearance of our ${}^6\text{Li}(\text{d},\text{p}_{0,1,2,4})$ and ${}^6\text{Li}(\text{d},\text{x}){}^7\text{Be}$ reaction experimental data.
- Conflicting and unmatched integral cross section data in world literature.
- Appearance of the publication by Austin S.M. et al. (Phys. Rev. C. 2019. V. 99. Art. No 024320) with new evaluation of ${}^6\text{Li}(\text{d},\text{p}_1)$ and ${}^6\text{Li}(\text{d},\text{n}_1)$ reaction cross section.

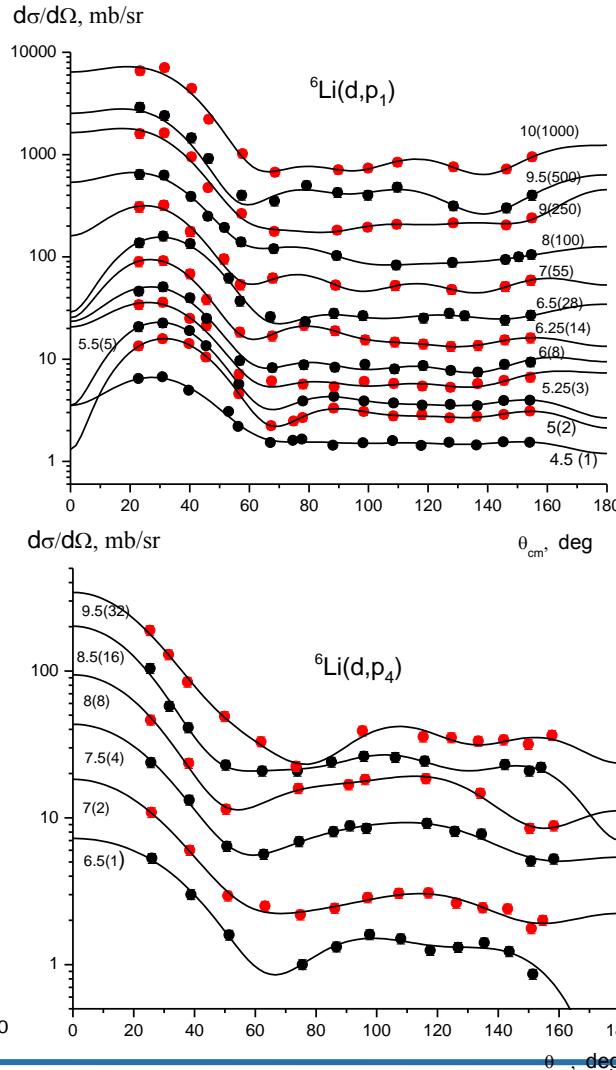
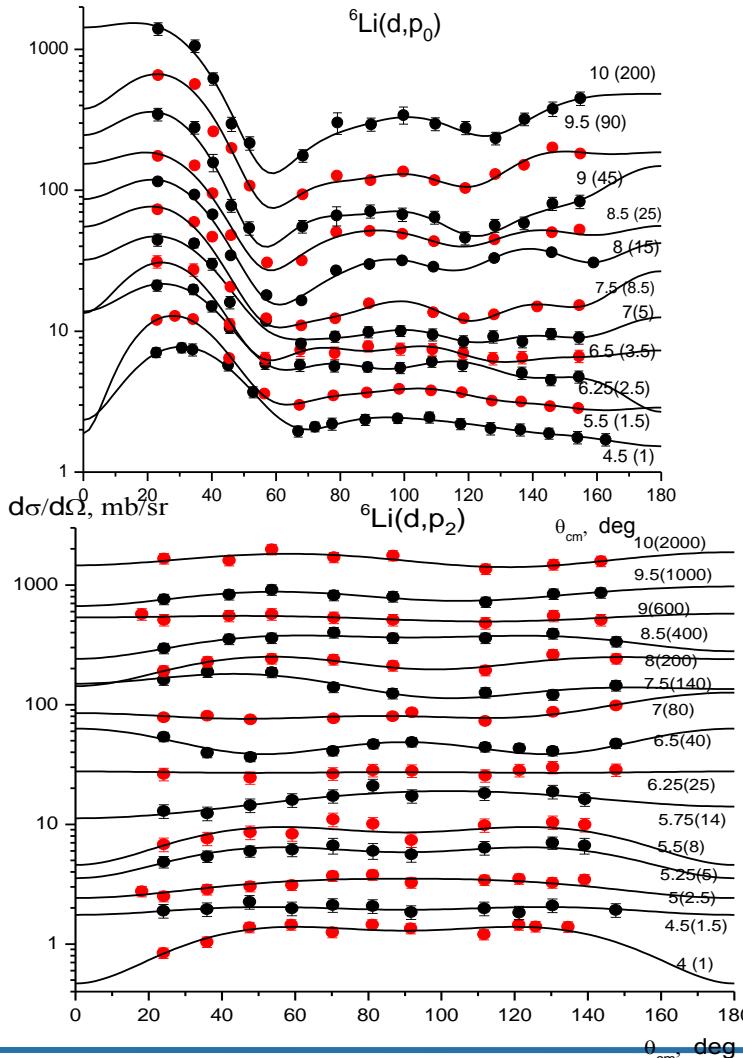
Goal

- Obtaining of the ${}^6\text{Li}(\text{d},\text{p}_0){}^7\text{Li}$, ${}^6\text{Li}(\text{d},\text{p}_{1,2,4}){}^7\text{Li}^*$,
 ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$, ${}^6\text{Li}(\text{d},\text{n}_{1,2,4}){}^7\text{Be}^*$ and ${}^6\text{Li}(\text{d},\text{x}){}^7\text{Be}$ reactions evaluated integral cross section data.

Data used in analysis (1/2)

Our data: scattering angle 20-160 degr, deuteron energy 4-10 MeV,
random error 7-10%, systematic error 4%.

$d\sigma/d\Omega$, mb/sr



Circles -
experimental
points (multiplied
by the relevant
values in
brackets), lines -
Legendre
polynomial fitting

(Experiment:
Generalov L.N. et al.
// Izv. RAS. 2020. V.
84. P. 1774.)

Data used in analysis (2/2)

- Literature data

Type	Scattering Angle, degr	E_d , MeV
$d\sigma/d\Omega$ (production of p or n or γ) (Legendre polynomial fitting for σ obtaining)	0-180	0.005-15
σ from the article	-	

- Data sets for (d,n_2) and (d,n_4) reactions are poor. So **data from (d,p_2) and (d,p_4) reactions** were used as cross section data **for the relevant mirror reactions (d,n_2) and (d,n_4)** .

- The library of evaluated and experimental data on charged particles interactions with light nuclei developed at VNIIEF.
 - 134 reaction channels; data types: integral and differential cross sections and nuclear reaction rates.
 - No-model approach is used for obtaining of evaluated data.
 - Evaluated function

$$f = S(E) + R(E)$$

Smooth part - spline

$$S(E) = \sum_{j=0}^p a_j (E - x_0)_+^j$$

Breit-Wigner resonances

$$R_l(E) = \sum_{i=0}^{n_l-1} \frac{H_i (\Gamma_i / 2)^2}{(E - E_i)^2 + (\Gamma_i / 2)^2} + \delta_l \sum_{j=0}^{p_l} a_j (E - x_0)_+^j$$

resonance **background**

- **Astrophysical S-factor is used for evaluation**

$$S(E_{cm}) = \sigma(E_{cm}) E_{cm} \exp\left(\sqrt{\frac{E_G}{E_{cm}}}\right) \sqrt{E_G} = 0.98948 z_1 z_2 \sqrt{\frac{m_1 m_2}{m_1 + m_2}}$$

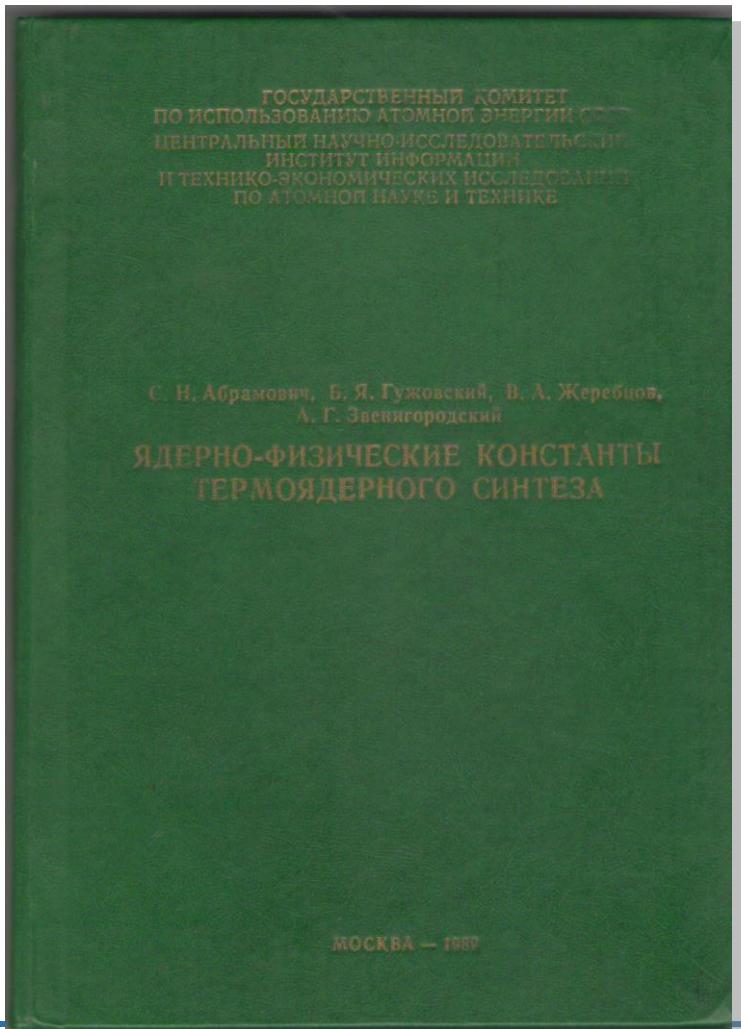
- **X² minimization for quality control of the evaluated curve**

$$\chi^2 = \frac{\sum_{i=1}^{N_d} \left(\frac{S_i - f(E_i)}{\sigma_i} \right)^2}{N_d - N_p}$$

SaBa Data Base (3/5)

РФЯЦ
ВНИИЭФ

- First version, 1989
- IAEA report, 1999



The image shows the cover of an IAEA report. It features the IAEA logo at the top, which consists of a stylized atom symbol inside a laurel wreath. Below the logo, the text "IAEA-NDS-191" and "December 1999" is printed. The main title of the report is "THE LIBRARY OF EVALUATED AND EXPERIMENTAL DATA ON CHARGED PARTICLES FOR FUSION APPLICATION". Below the title, the names of the authors are listed: A.G. Zvenigorodskij, V.A. Zhrebsov, L.M. Lazarev, S.A. Dunaeva, L.N. Generalov, S.M. Taova, E.V. Kamskaya, and R.I. Marshalkina. The report is published by the Russian Federal Nuclear Center, All-Russia Scientific Research Institute of Experimental Physics (VNIIEF), 607190, Russia, Nizhni Novgorod reg., Sarov, Mira, 37. An abstract is provided, stating that the report contains evaluated and experimental data on charged particles for thermonuclear applications, based on the handbook "Nuclear Physics Constants for Thermonuclear Fusion" (INDC(CCP)-326/L+F, VIENNA, 1991). The data is presented in a library with 100 channels and 52 reactions, using Borland C++ Builder for Windows 95 and NT operating systems. The report also mentions an optimal set of data processing procedures and a friendly interface. Summary documentation is prepared by S.A. Dunaeva and S.M. Taova. Contact information for the Nuclear Data Section, International Atomic Energy Agency, P.O. Box 100, A-1400 Vienna, Austria, is provided, along with e-mail, fax, cable, and telephone numbers. Online access details are also given.

Summary Documentation (prepared by S.A.Dunaeva, S.M.Taova)

Nuclear Data Section
International Atomic Energy Agency
P.O. Box 100
A-1400 Vienna
Austria

e-mail: services@iaeaand.iaeа.or.at
fax: (43-1) 26007
cable: INATOM VIENNA
tellex: 1-12645
telephone: (43-1) 2600-21710

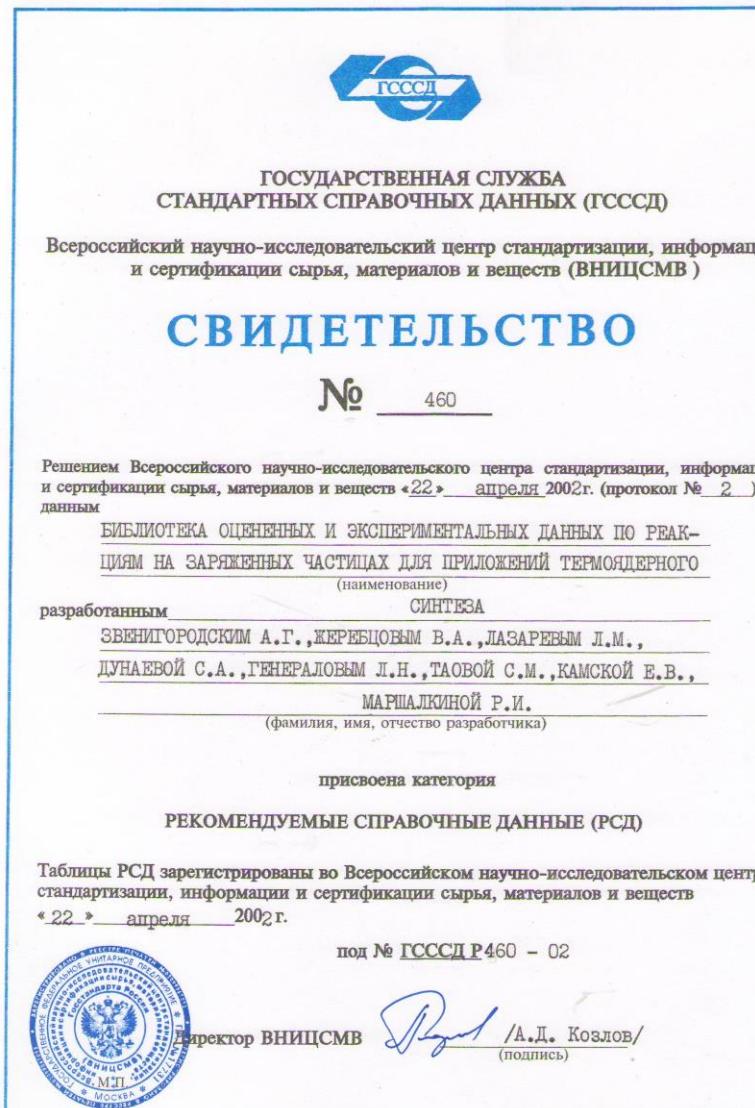
Online: TELNET or FTP: iaeaand.iaeа.or.at
username: IAEANDS for interactive Nuclear Data Information System
usernames: ANONYMOUS for FTP file transfer;

SaBa Data Base (4/5)

• Electron version, 2002

The screenshot shows the SaBa Data Base software interface. On the left, a tree view displays various nuclear reactions involving Lithium isotopes. The main window is divided into three vertical sections: LIBRARY, PROCESSING, and EDITING. The LIBRARY section contains buttons for Reaction list, Information, and Review. The PROCESSING section contains buttons for Evaluation, Calculation of SIG-V, and ENDF files. The EDITING section contains buttons for Experimental data and New reaction. At the bottom right, there is a graph titled 'Графики' (Graphs) showing experimental data points with error bars and several theoretical curves (solid and dashed lines) representing different models or calculations. The x-axis is labeled 'Елаб, МэВ' (Energy, MeV) and ranges from approximately 0.5 to 12. The y-axis is labeled 'Число, мб' (Number, mb) and ranges from 0 to 70.

SaBa Data Base (5/5)



- State registration, recommended data, 2002
- #460

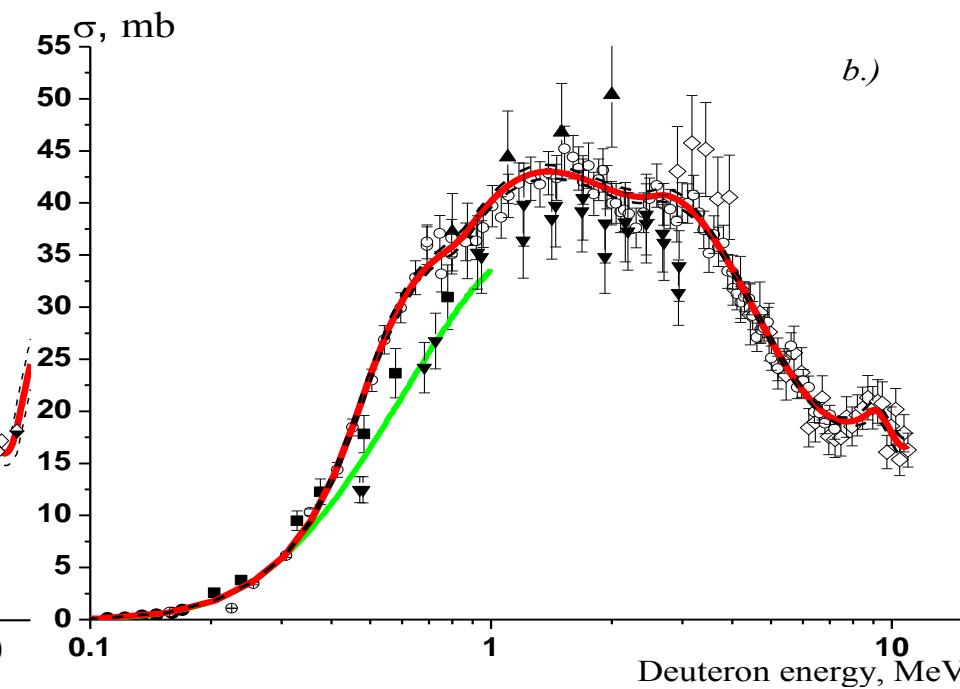
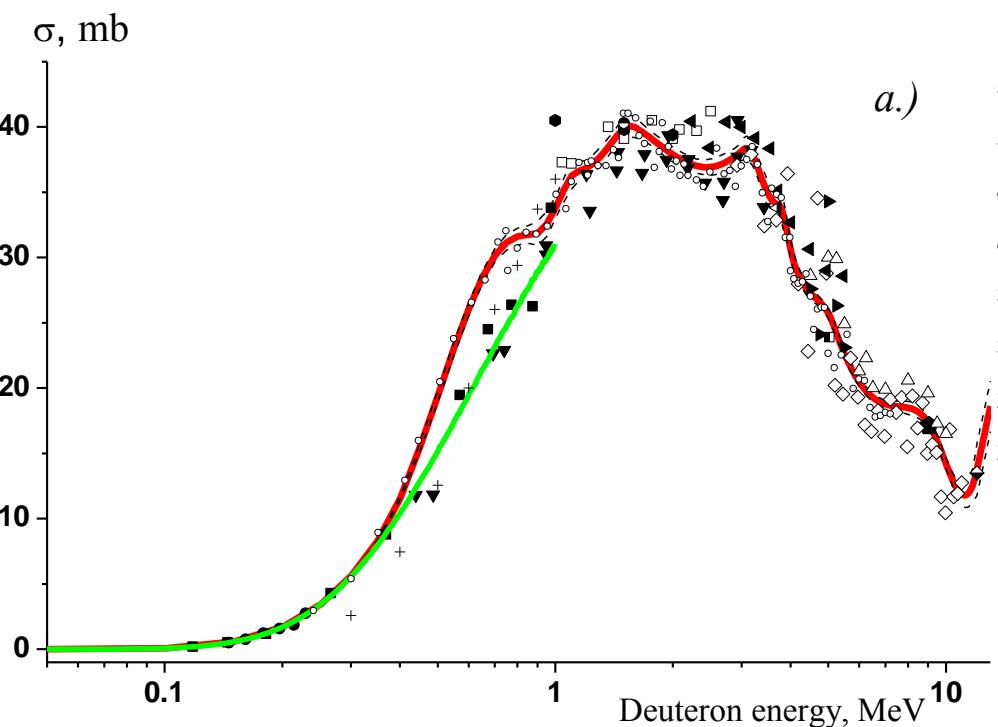
Mirror reactions

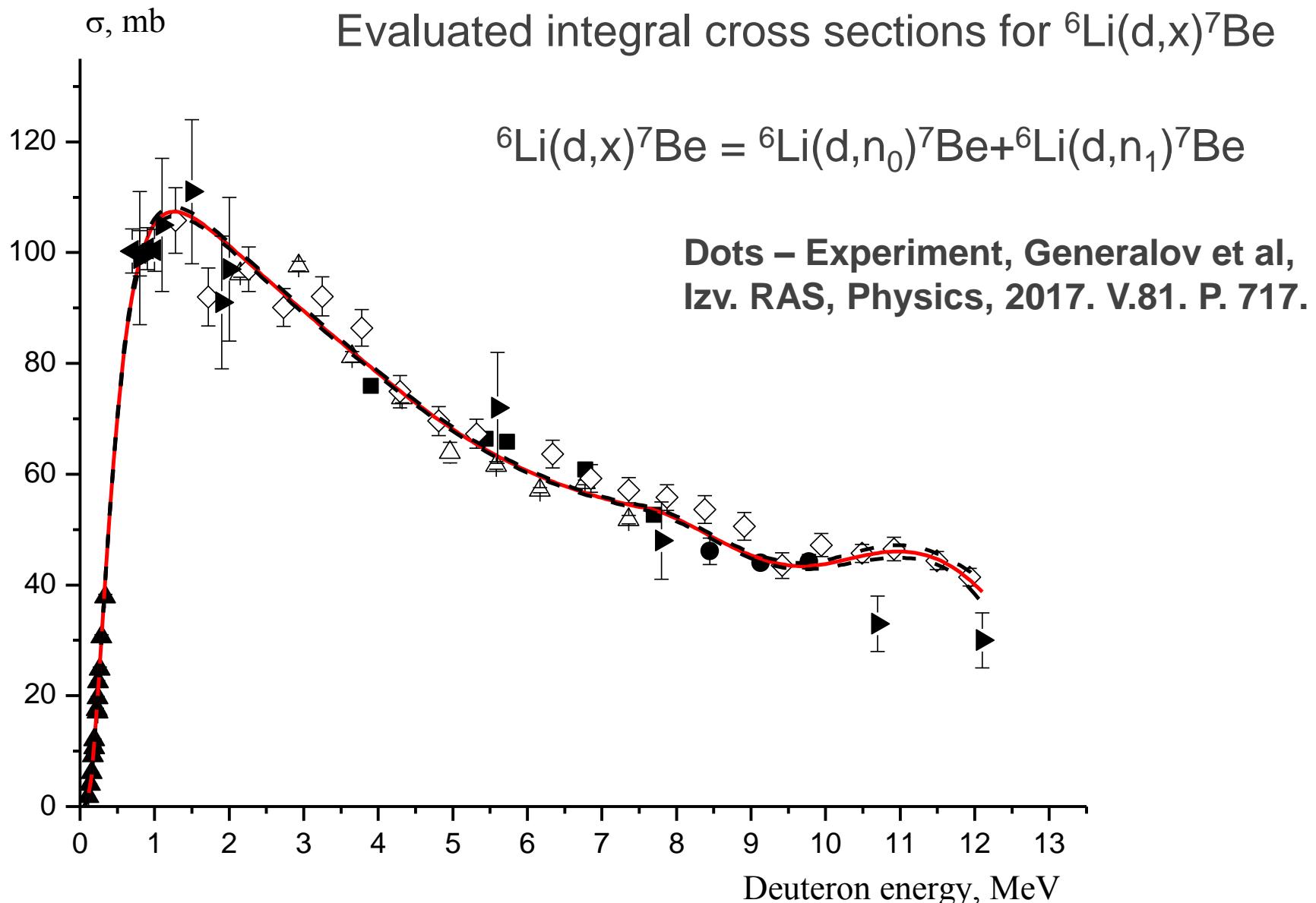
<i>dp</i> -реакции	<i>Q</i> , МэВ	<i>E_{thr}</i> , МэВ	<i>dn</i> -реакции	<i>Q</i> , МэВ	<i>E_{thr}</i> , МэВ
${}^6\text{Li} + d \rightarrow {}^7\text{Li}_{\text{g.s.}} + p_0$	5.026		${}^6\text{Li} + d \rightarrow {}^7\text{Be}_{\text{g.s.}} + n_0$	3.382	
${}^6\text{Li} + d \rightarrow {}^7\text{Li}^*(0.478) + p_1$	4.548		${}^6\text{Li} + d \rightarrow {}^7\text{Be}^*(0.429) + n_1$	2.953	
${}^6\text{Li} + d \rightarrow {}^7\text{Li}^*(4.63) + p_2 \rightarrow$ ${}^4\text{He} + t + p_2$	0.396		${}^6\text{Li} + d \rightarrow {}^7\text{Be}^*(4.57) + n_2 \rightarrow$ ${}^4\text{He} + \text{he} + n_2$	-1.188	1.584
${}^6\text{Li} + d \rightarrow {}^7\text{Li}^*(6.68) + p_3 \rightarrow$ ${}^4\text{He} + t + p_3$	-1.35	1.8	${}^6\text{Li} + d \rightarrow {}^7\text{Be}^*(6.73) + n_3 \rightarrow$ ${}^4\text{He} + \text{he} + n_3$	-3.35	4.47
${}^6\text{Li} + d \rightarrow {}^7\text{Li}^*(7.46) + p_4 \rightarrow$ ${}^4\text{He} + t + p_4$ → ${}^6\text{Li} + n + p_4$	-1.564	2.085	${}^6\text{Li} + d \rightarrow {}^7\text{Be}^*(7.21) + n_4 \rightarrow$ ${}^4\text{He} + \text{he} + n_4$ → ${}^6\text{Li} + p + n_4$	-3.83	5.11

- Our experimental results were used as reference ones.
- Each pair of mirror reactions was analyzed simultaneously: (d,p_0) and (d,n_0) , (d,p_1) and (d,n_1) , (d,p_2) and (d,n_2) , (d,p_4) and (d,n_4) . Evaluation of the data consisted of evaluation of the mirror reactions integral cross sections and its experimental ratios. Evaluation procedure was performed at iterative way.

Results 1/6

Evaluated integral cross sections of mirror reactions, red lines – present,
green – K.Czerski, 1997, direct+resonance



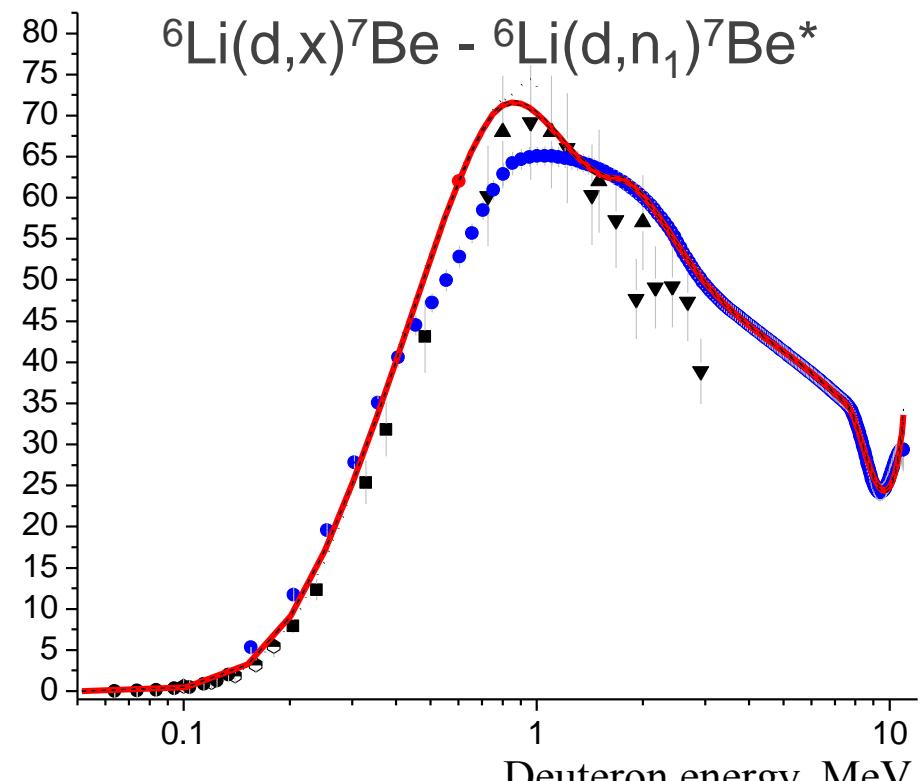


Results 3/6

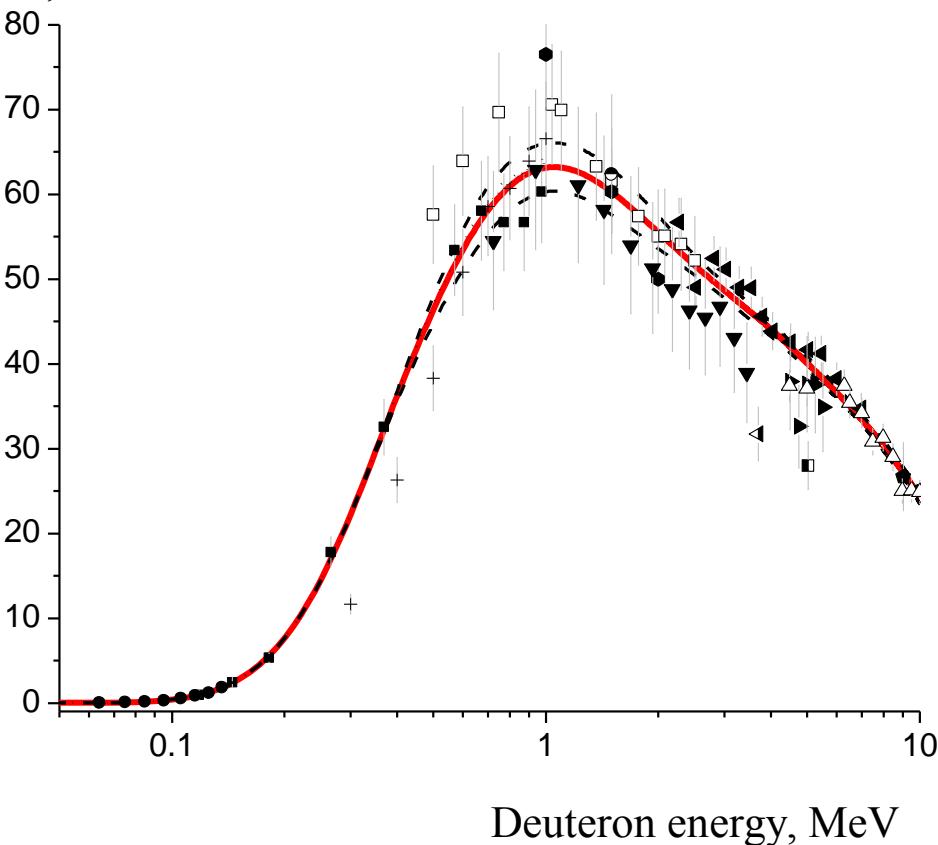
Evaluated integral cross sections of mirror reactions, red lines - present

σ , mb

Blue dots: our subtraction

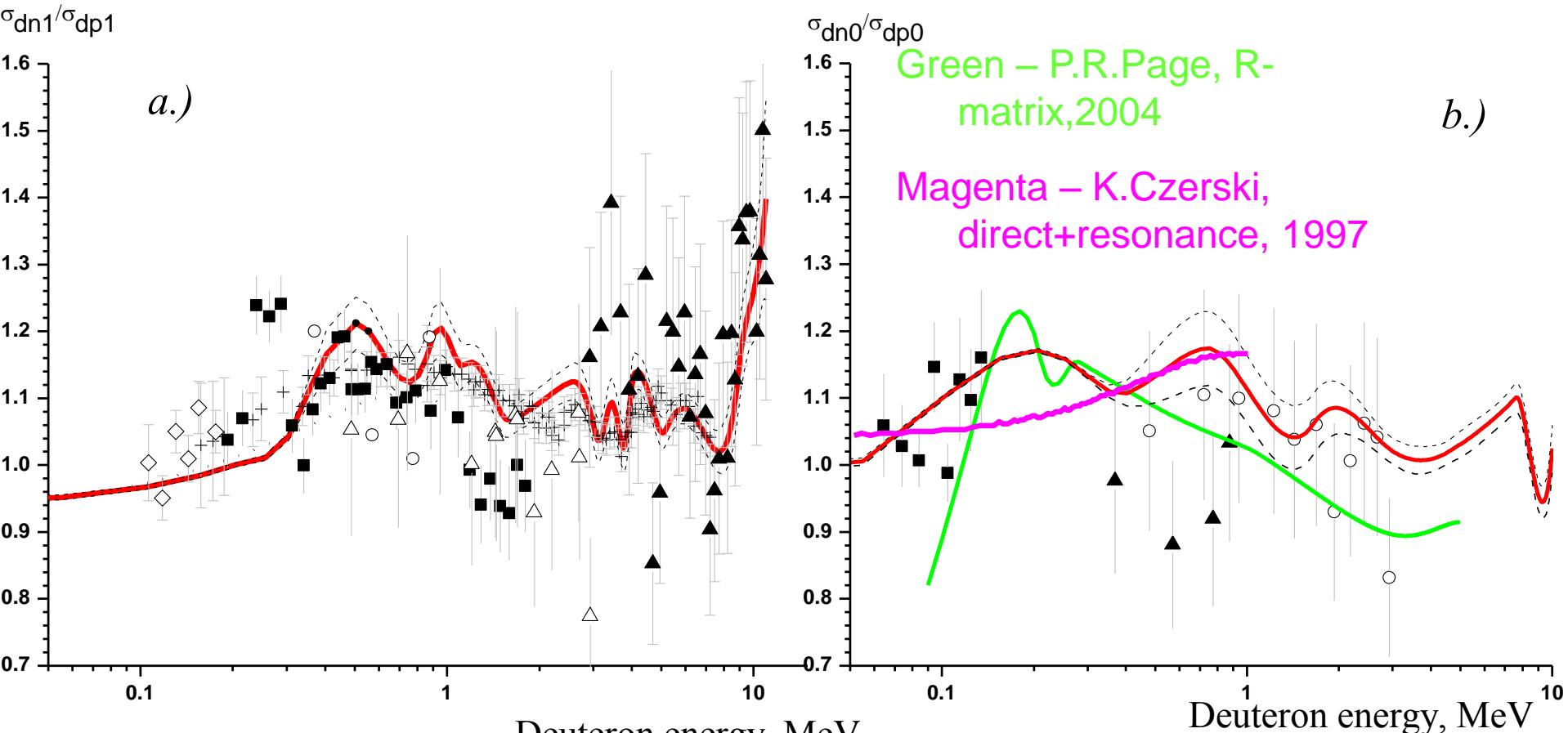


σ , mb



Results 4/6

Ratio of the mirror reactions integral cross sections, red lines - present



dn_1/dp_1

dn_0/dp_0

Data used in analysis (2/2)

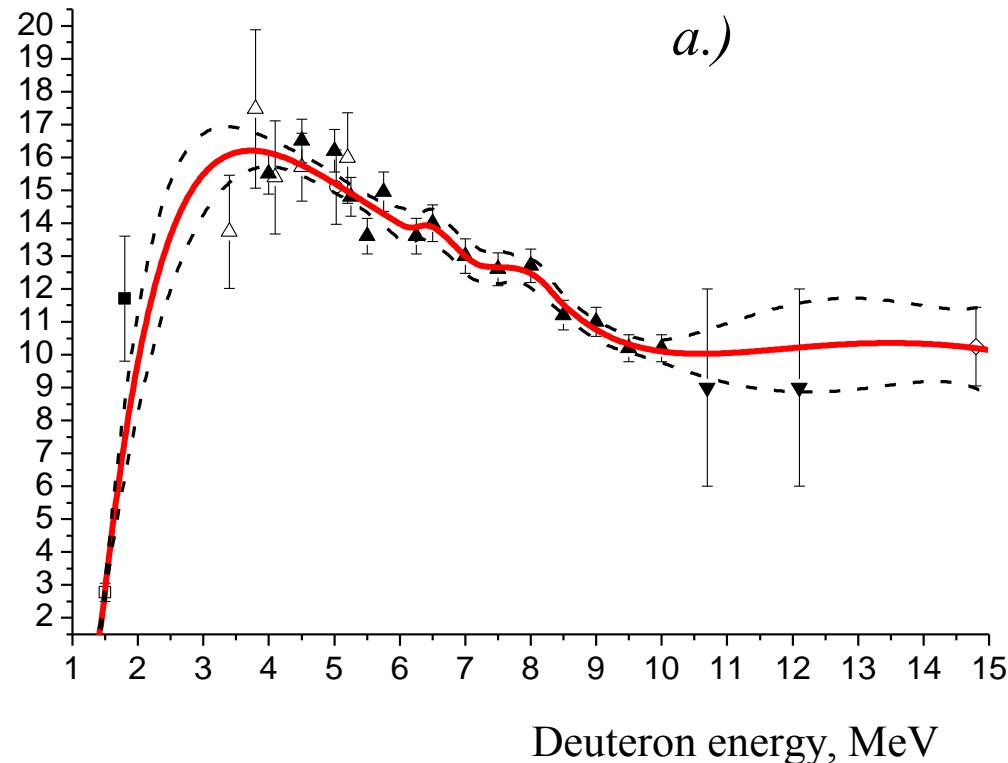
- Literature data

Type	Scattering Angle, degr	E_d , MeV
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σ from the article	-	

- Data sets for (d,n_2) and (d,n_4) reactions are poor. So **data from (d,p_2) and (d,p_4) reactions** were used as cross section data **for the relevant mirror (d,n_2) and (d,n_4) reactions.**

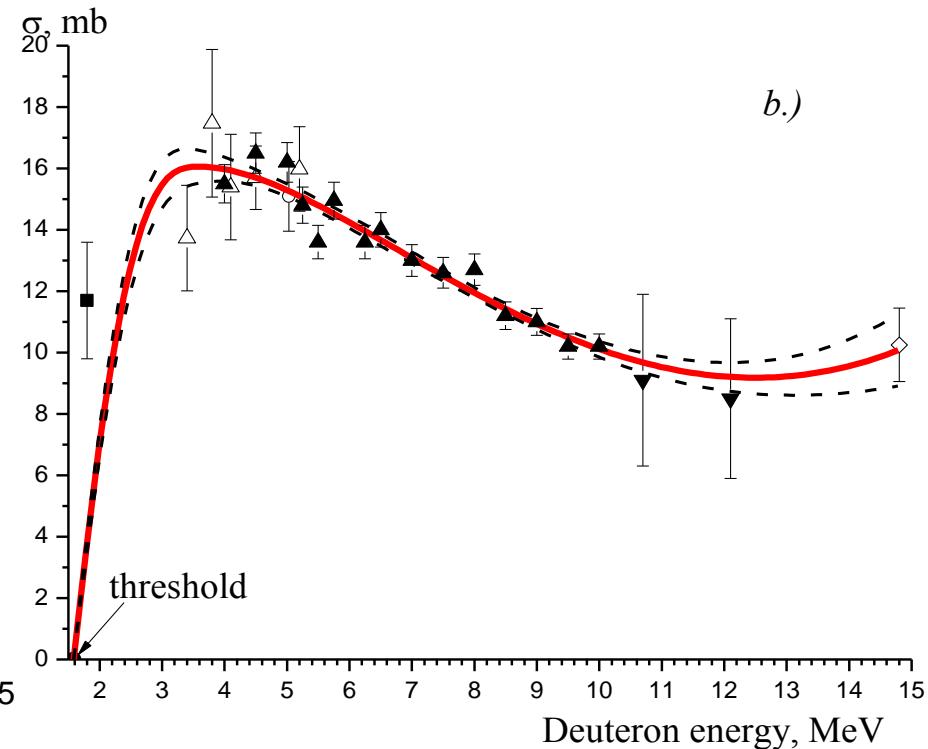
Evaluated integral cross sections of mirror reactions

σ , mb



a.)

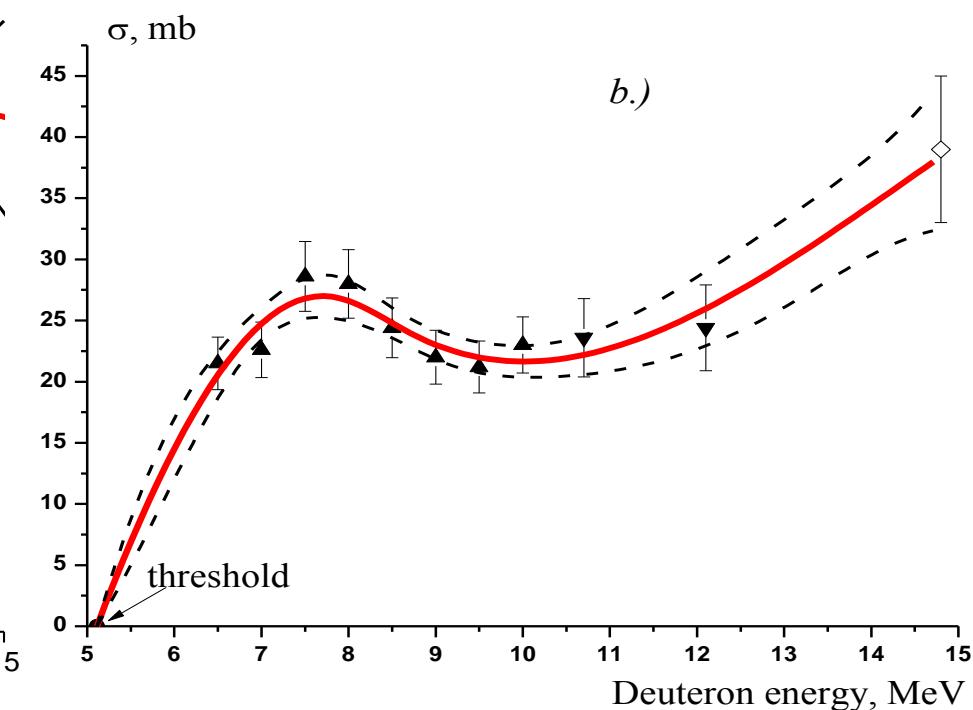
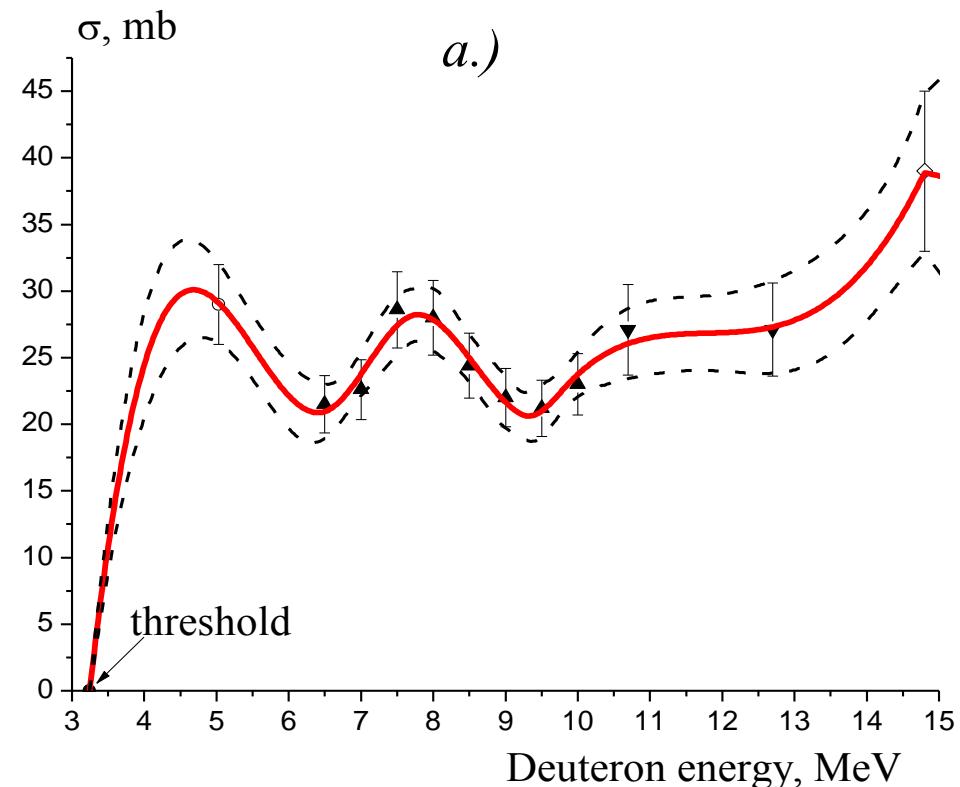
σ , mb



b.)



Evaluated integral cross sections of mirror reactions

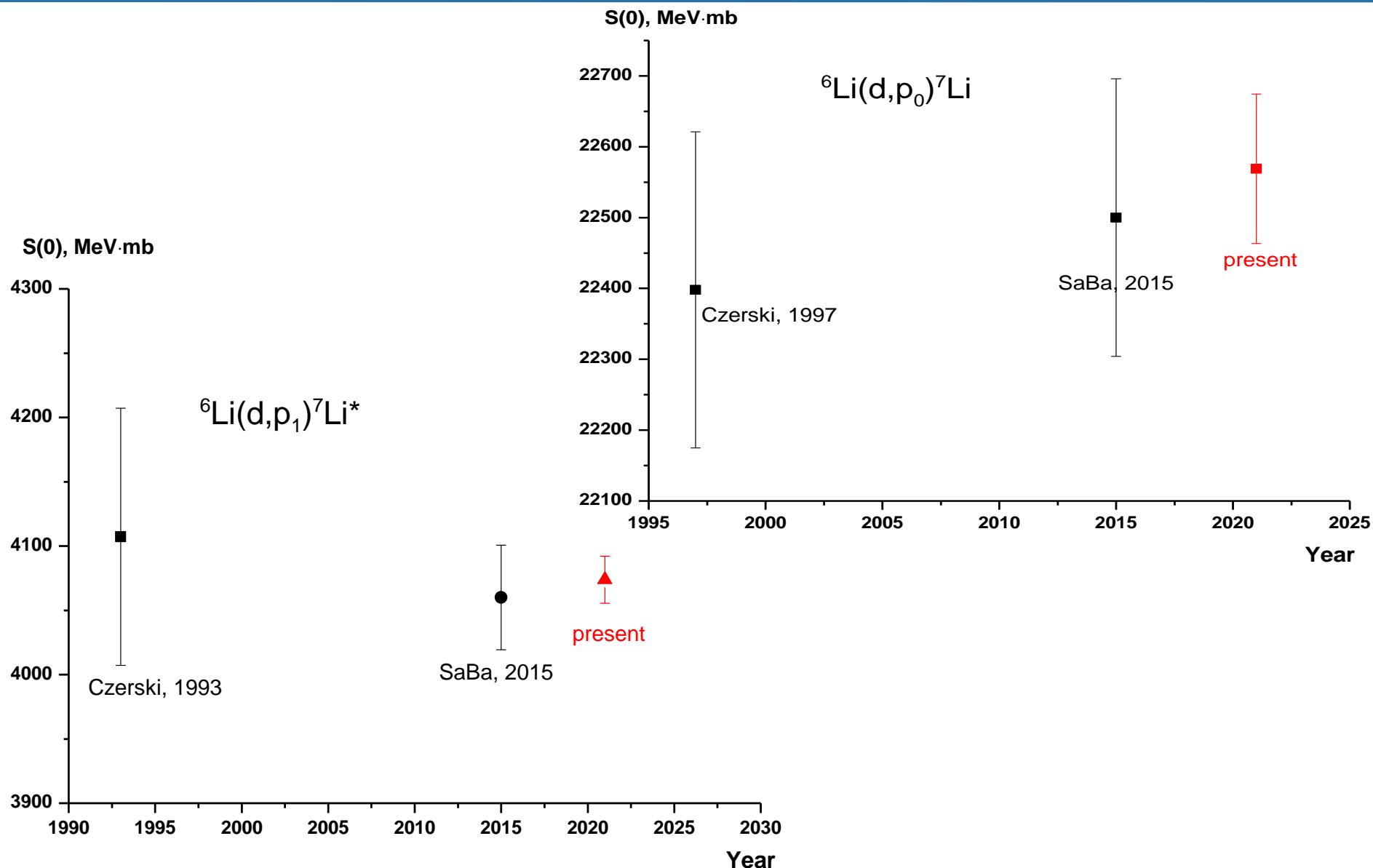


Spline coefficients (${}^6\text{Li}(\text{d},\text{p}_1){}^7\text{Li}^*$)

$$S(E) = C_0 + C_1(E - x_0) + C_2(E - x_0)^2 + C_3(E - x_0)^3$$

Энергия узла сплайна x_0 , МэВ	Значения коэффициентов			
	C_0	C_1	C_2	C_3
$5.996 \cdot 10^{-3}$	$4.042 \cdot 10^3$	$-5.319 \cdot 10^3$	$-1.754 \cdot 10^4$	$6.781 \cdot 10^4$
$3.132 \cdot 10^{-1}$	$2.718 \cdot 10^3$	$3.098 \cdot 10^3$	$-2.916 \cdot 10^4$	$3.786 \cdot 10^4$
$6.568 \cdot 10^{-1}$	$1.875 \cdot 10^3$	$-3.535 \cdot 10^3$	$2.498 \cdot 10^4$	$-6.955 \cdot 10^4$
$8.532 \cdot 10^{-1}$	$1.618 \cdot 10^3$	$-1.768 \cdot 10^3$	$6.108 \cdot 10^3$	$-9.618 \cdot 10^3$
.....				
3.050	$7.310 \cdot 10^2$	$-3.179 \cdot 10^2$	$5.192 \cdot 10^2$	$-3.773 \cdot 10^2$
3.873	$6.109 \cdot 10^2$	$-2.293 \cdot 10^2$	$1.322 \cdot 10^2$	$-2.389 \cdot 10^1$
6.867	$4.684 \cdot 10^2$	$-8.009 \cdot 10^1$	$-6.362 \cdot 10^1$	$4.234 \cdot 10^1$
8.990	$4.168 \cdot 10^2$	$2.224 \cdot 10^2$	—	—

Astrophysical S-factor $S(E=0)$, ${}^6\text{Li}(d,p_{0,1}){}^7\text{Li}$



- **Evaluated integral cross sections of the ${}^6\text{Li}(\text{d},\text{p}_0){}^7\text{Li}$, ${}^6\text{Li}(\text{d},\text{p}_{1,2,4}){}^7\text{Li}^*$, ${}^6\text{Li}(\text{d},\text{n}_0){}^7\text{Be}$, ${}^6\text{Li}(\text{d},\text{n}_{1,2,4}){}^7\text{Be}^*$ and ${}^6\text{Li}(\text{d},\text{x}){}^7\text{Be}$ reactions were obtained.**
- **The ratio of the mirror reaction integral cross sections was obtained.**

Thank you
for your
attention!