## Dynamic Strong Magnetic Field for Quark Gluon Plasma Equation of State



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# OUTLINE

## INTRODUCTION

# **MOTIVATION**

# RESULTS

# CONCLUSION

## **Two unusual properties of quarks**

### **Asymptotic Freedom:**

Its essence is that: At small ranges (<  $10^{-16}$  m) the quark-quark forces are negligible. In accordance with uncertainty principle this means that quarks behave as free particles at relativistic momenta.

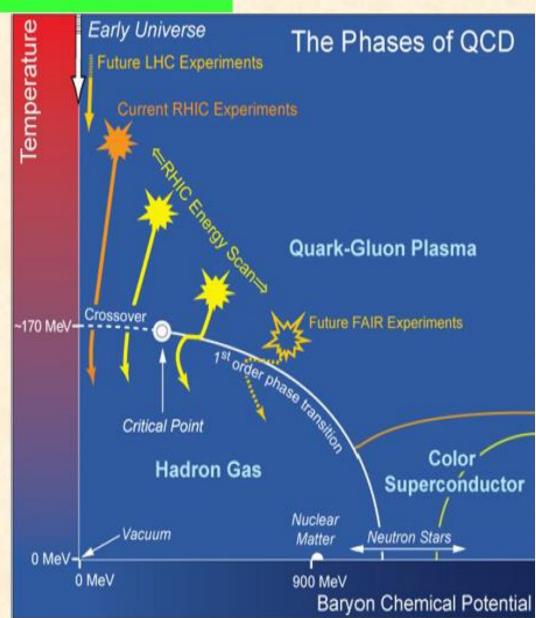
### **Confinement:**

Its essence is that: The potential energy of quark-quark interaction rises infinitely with distance, such an increase being so rapid that two quarks cannot be separated beyond the radius of a hadron.

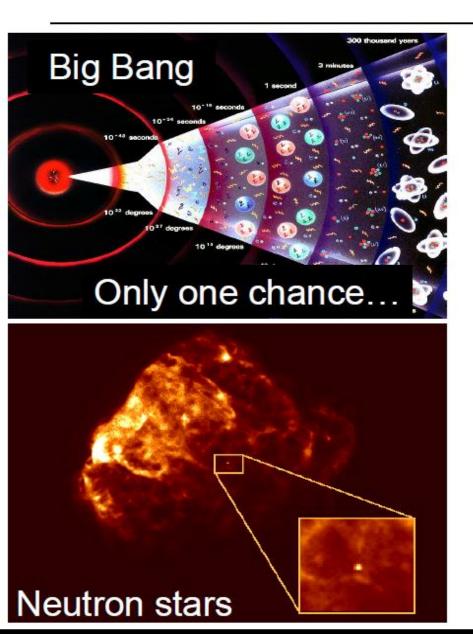
## Phase Diagram of QCD

A new phase of matter called the Quark Gluon Plasma (QGP)

 $QGP \equiv a$  (locally) thermally equilibrated state of matter in which quarks and gluons are deconfined from hadrons, so that color degrees of freedom become manifest over nuclear, rather than merely nucleonic, volumes.



# Where to study the QGP?





#### Heavy lon Colliders

## **MOTIVATION AND WORK**

>At present a rigorous QCD treatment of the QGP is almost impossible, given the complexity of the physical system involved.

>However, the existence of a QGP can be theoretically inferred through lattice gauge simulations of QCD, which provide the only rigorous method to compute the QCD equation of state. These simulations predict a phase transition of confined hadronic matter to a deconfined state of hadrons.

>In the meanwhile, a number of papers using some phenomenological models have appeared over the past decade investigating the phase transition between hadronic and QGP phases. It is fine to use the MIT bag model to describe the hadrons as bags of quarks, anti quarks and gluons, but to extend the idea to represent the phase boundary between the QGP droplet and the bulk hadronic medium makes one a bit uneasy.

It is to remedy this rather unnatural assumption, i.e. the confining bag of the hadrons has the same property as the interface separating the two phases, we propose an alternative model to represent the same physical situation.

Another drawback of the MIT bag model is its disagreement with "numerical experiments" using lattice gauge pure SU(3) simulation. As pointed out by Peshier et al., the simulation "data" is satisfied only by a bag pressure p = ae - 4B/3, with a = 0.297 (not 1/3 as for MIT bag Model), where 'e' is the energy density and  $B^{1/4} = 205MeV$  for the bag constant.

This mismatch with lattice simulations had led earlier authors to abandon the MIT bag model in the context of QGP by introducing "thermal parton masses"  Simple statistical model for analysis of QGP droplet (fireball) formation and EoS of QGP (PRC 70, 027903(2004), PJP 68,757 (2007))

➢ In our present work we use the statistical tools to extract some knowledge about the formation and evolution of the quark gluon plasma. Here we basically used the statistical model developed by Ramanathan and Kumar et al.

-Since the model depends crucially on the nature of the effective semiphenomenological QCD oriented potential (mean field potential) between quarks that we extract from the large momentum approximation to the "thermal mass" introduced by Peshier et al.

> Peshier et al. (PLB 337, 235 (1994)), Ramanathan et al., (PRC 70, 027903(2004))

The model has its merits in its simplicity and robustness to give a qualitative and quantitative idea about QGP. we construct the density of states using methods analogous to the Thomas–Fermi model (ZFP 48, 73 (1928)) for the atoms and the Bethe model (RMP 9, 691937) for the nucleons as

$$\rho_{q,g}(k) = \left(\frac{\upsilon}{\pi^2}\right) \left\{ \left(-V_{eff}(k)\right)^2 \left(\frac{-dV_{eff}}{dk}\right) \right\}_{q,g}$$

where effective potential  $(V_{eff}(k))$  is considered as:

$$V_{eff}(k) = \left(\frac{1}{2k}\right) \gamma_{q,g} g^2(k) T^2$$

Known as mean field effective potential among the quarksgluons.

The above potential is a result of the use of a thermal Hamiltonian for the Quark-Gluon system.

we have used  $\gamma_q = \frac{1}{6}$  and  $\gamma_g = 6\gamma_q$  or  $\gamma_g = 8\gamma_q$ . The choice of these parameters motivates from the fact that they exhibit the formation of most stable QGP droplet.

In the effective thermal potential, g(k) is the first order running coupling constant given as,

$$g^{2}(k) = \left(\frac{4}{3}\right)\left(\frac{12\pi}{27}\right)\left|\frac{1}{\ln\left(1+\frac{k^{2}}{\Lambda^{2}}\right)}\right|$$

So in this statistical model we have an advantage that it has a natural low momentum cut-off leading to finite results hence avoiding any infra-red divergence,

$$k_{\min} = \left(\frac{\gamma N^{1/3} T^2 \Lambda^2}{2}\right)^{\frac{1}{4}} \quad \begin{array}{l} \text{Here } \Lambda = 150 \, \text{MeV} \text{ is the QCD} \\ \text{parameter and N is } \left(\frac{4}{3}\right) \left(\frac{12\pi}{27}\right) \end{array}$$

where  $\gamma$  is introduced to take care the plasma (hydro-dynamical) nature of the droplet and it is chosen as:

$$\gamma = \sqrt{2} \times \sqrt{\left(\frac{1}{\gamma_q}\right)^2 + \left(\frac{1}{\gamma_g}\right)^2}$$

It is the inverse rms value of the flow parameter of the quarks and gluons. <sup>11</sup>

The Weyl density of states is:

$$\rho_{Weyl}(k) = \left(\frac{4\pi R^2}{16\pi}\right) k^2$$

Where R is the radius of the droplet of QGP.

The basic idea here is to treat the QGP as composed of u,d,s quarks and gluons, confined in a volume 'v', outside the volume (which is assumed having spherical symmetry) pions are present. Our aim is to calculate the free energy of this whole system which can be used to calculate various thermodynamic quantities. We compute the free energies in which we used the usual continuum expression for the system of non-interacting Fermions and Bosons: PRD 44, 878 (1991), PRD 60, 054011 (1999))

$$F_i = \mp g_i T \int dk \rho_i(k) \ln \left| 1 \pm e^{\frac{-\sqrt{m_i^2 + k^2}}{T}} \right|$$

where for fermions we used upper sign and for bosons lower sign.

The interface is no longer assumed a MIT bag, and yet it has a contribution to free energy on account of the surface energy which is assumed to be scalar Weyl surface. Hence the interface free energy is taken as:

$$F_{\text{int erface}} = \gamma T \int dk \rho_{weyl}(k) \delta(k-T)$$

$$F_{\text{interface}} = \frac{R^2 T^3 \gamma}{4}$$

**Pion free energy is :** 

$$F_{\pi} = -\left(\frac{3T}{2\pi^{2}}\right) \upsilon_{0}^{\infty} k^{2} dk \ln\left(1 - e^{\frac{-\sqrt{m_{\pi}^{2} + k^{2}}}{T}}\right)$$

The total free energy (F) is given as:

$$F = F_i + F_{interface} + F_{\pi}$$

Here *i* stands for u,d,s (quarks) and gluon.

It explains the creation of the plasma formation with the size of the droplets and also indicate the nature of QGP fireball.

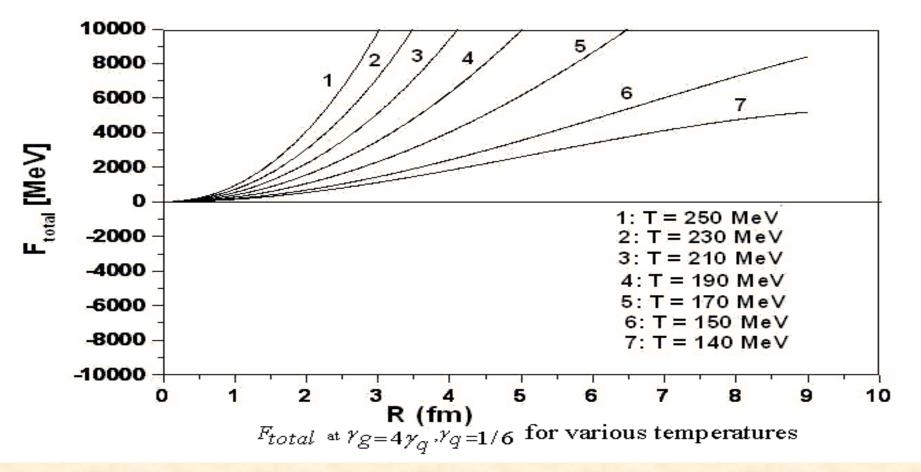
Various thermodynamic quantities can be calculated using total free energy (F) :-

$$P = -\left(\frac{dF_{total}}{d\upsilon}\right) \quad ; \quad \varepsilon = T \frac{dP}{dT} - P \quad ; \quad S = \frac{dP}{dT} \quad ; \quad C_{\nu} = -\left(\frac{\partial^2 F}{\partial T^2}\right)_{\nu} \quad ; \quad C_{s}^2 = \frac{dP}{d\varepsilon}$$

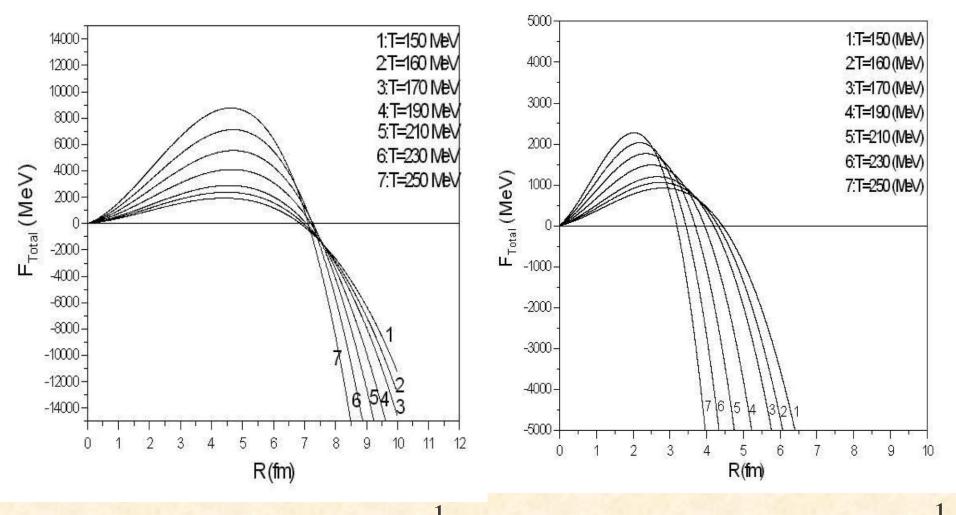
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# RESULTS

### Variation of free energy with size of QGP droplets :



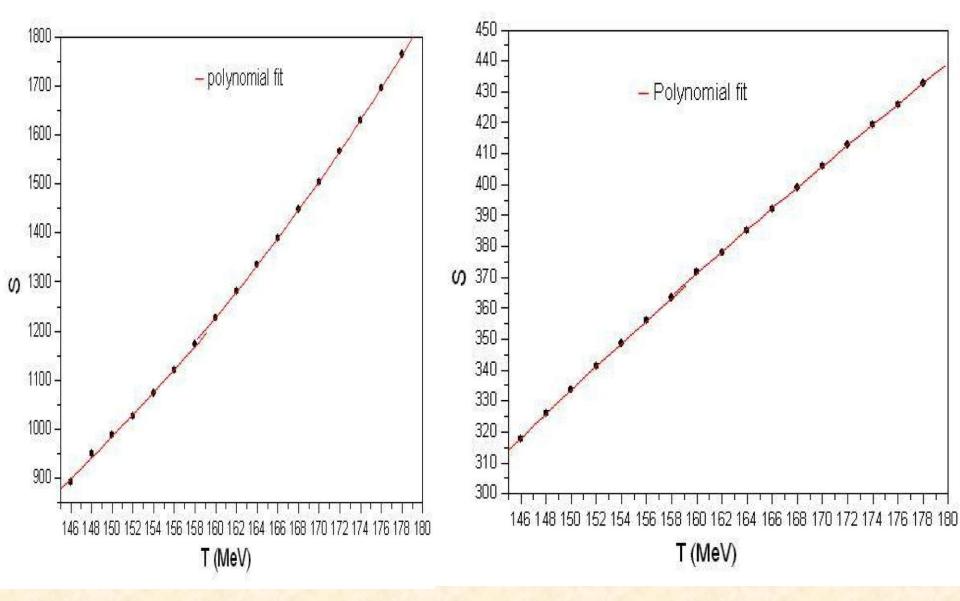
### Variation of free energy with size of QGP droplets :



Modified  $F_{total}$  at  $\gamma_g = 6\gamma_q$ ,  $\gamma_q = \frac{1}{6}$ 

for various temperatures

Modified  $F_{total}$  at  $\gamma_g = 8\gamma_q$ ,  $\gamma_q = \frac{1}{6}$ for various temperatures. 17



Variation of *S* with at Temperature T at  $\gamma_g = 6\gamma_q$ ,  $\gamma_q = \frac{1}{6}$ . Variation of *S* with Temperature T at  $\gamma_g = 8\gamma_q$ ,  $\gamma_q = \frac{1}{6}$ .

#### Effective quark mass in the presence of Magnetic field :

The effective quark mass created in heavy-ion collisions is considered as linear function of square of current mass, coupling of thermal and current mass and square of thermal mass which is again suitably modified with the help of magnetic field : Phys. Rev. D 82, 014023 (2010)

$$M_{eff}^2 = m_c^2 + \sqrt{2} m_c m_q + m_c^2$$

where mc is the current quark mass and mq is the thermal quark mass :

$$m_q^2(T,\mu) = \gamma_q' \left[ \frac{N}{\ln\left(1 + \frac{k^2}{\Lambda^2}\right)} \right] T^2 \quad \text{and} \quad \gamma_q' = \gamma_q \left(1 + \frac{\mu^2}{\pi^2 T^2}\right)$$

Assume the system in the presence of a strong magnetic field background that is constant and homogeneous so the single particle energy eigen value is given by,

$$E = \left[k^{2} + M_{eff}^{2} + eB(2n + s + 1)\right]^{1/2}$$

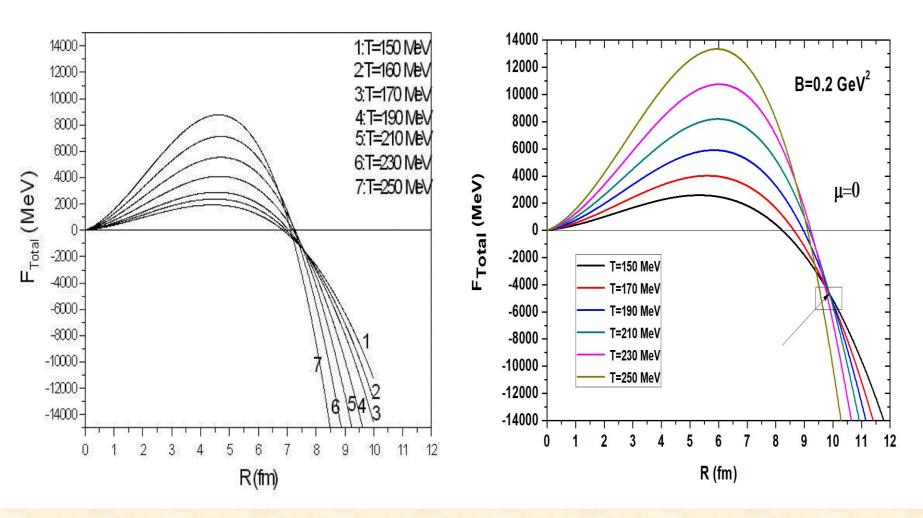
Where, n=0,1,2,.... are the principle quantum numbers for allowed Landau levels, s=plus(minus)1 refers to spin up (+) or down (-) states.

The immense value of C.M.S. available at RHIC and LHC allow us to consider the time varying magnetic field which should be adiabatic in nature. The estimated time dependent magnetic field can be expressed as,

> K. Tuchin et al. Phys. Rev. C 88, 024910 (2013)

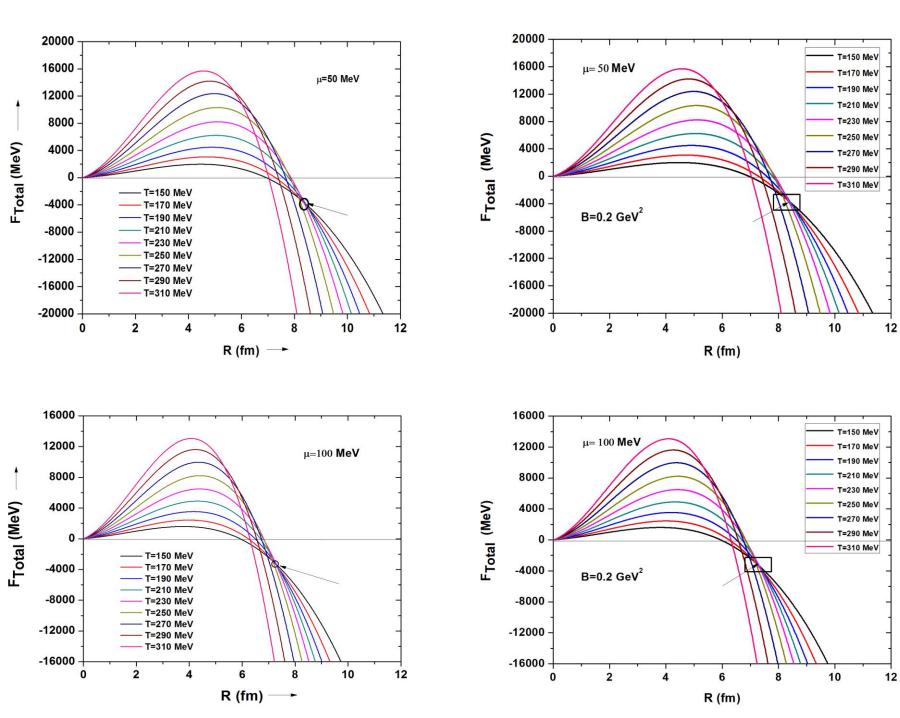
$$eB(t) = \frac{\alpha z R\sigma}{t^2} \exp\left(-\frac{R^2\sigma}{4t}\right)$$

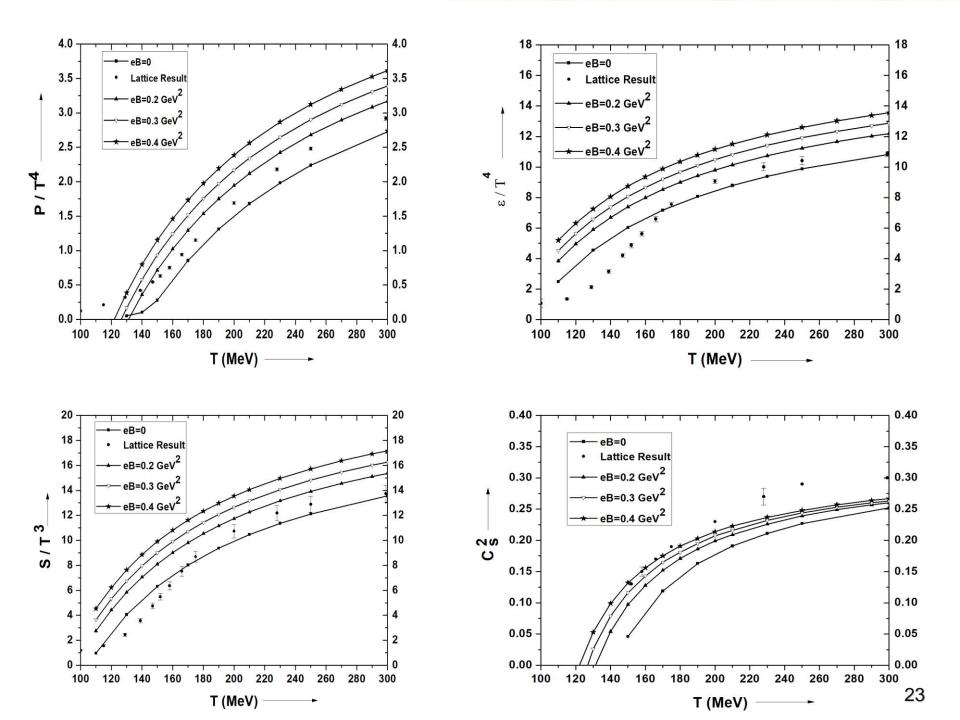
where  $\sigma$  is electrical conductivity of QGP, z is taken as nuclear charge, R is the size of the nucleus and t is time. This time varying magnetic field may be one of the important factor which affect the equation of state of QGP and hence could be responsible to see the dynamics of QGP. It help us to understand that how system evolve with time varying magnetic field.

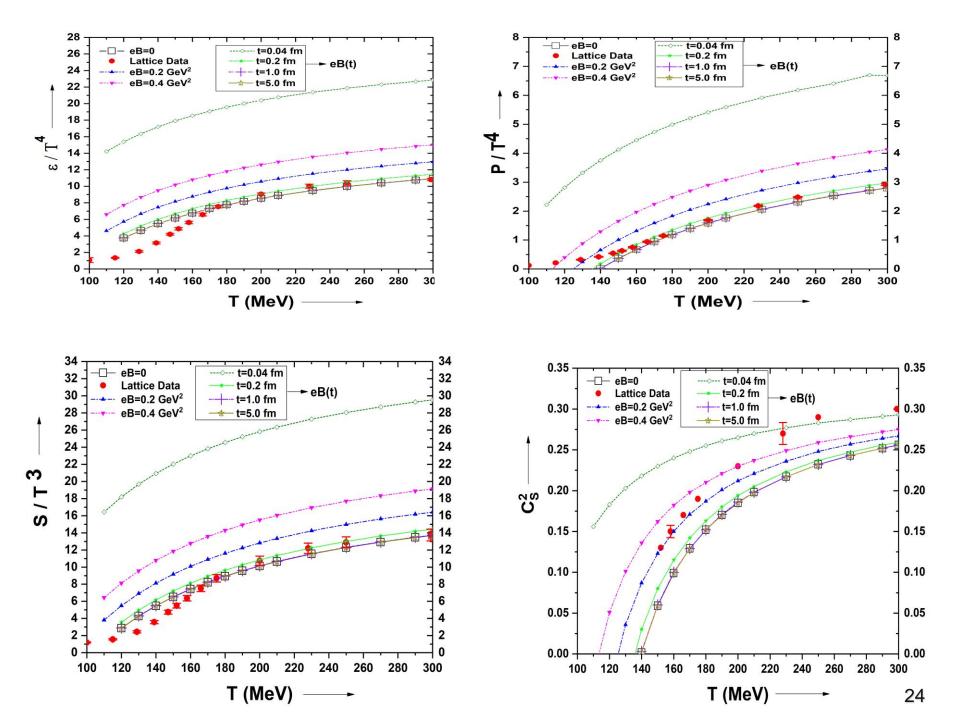


The model result indicate that the use of finite value of quark mass at zero chemical potential in the presence of B enhances the evolution and make more stability in droplet size formation.

The bunching of curves provide more realistic picture for the stability of QGP droplet as shown by arrowhead.







# CONCLUSION

- The model we have discussed here is not only simple but grasp a lot of physics about the formation and evolution of quark gluon plasma.
- The results with effective quark mass in the presence of magnetic field shows significant improvement in order to enhances the droplet size and make more stability in plasma evolution. The observations could have interesting implications on the expansion dynamics of the medium produced at RHIC and LHC, which may influence the outcomes of various signatures.
- In order to explore the structure of quark gluon plasma to deal with the dynamics of quarks and gluons, we investigate the equation of states (EoS) not only in the environment of static magnetic field but also in the presence of time varying magnetic fields.
- Results are presented for a variety of thermodynamic observables, indicating that the EoS is significantly affected by the magnetic field, even at moderate values of B. Our results are in good agreement with the present lattice QCD simulation.

Using phenomenological model, some appealing features are noticed depending upon four different scales; effective mass of quark, temperature and time independent as well as time dependent magnetic field.

These crucial findings with and without time varying magnetic field could have phenomenological implications in various sectors like as cosmology, astrophysics and heavy ion collisions.

Overall all results are folded with a model which explain the evolution through the thermodynamic variables like free energy, entropy, specific heat and also helps us to produce EoS of QGP.



## **Any Question ?**