

## Energy and mass dependencies for the characteristics of $p_T$ regions observed at LHC energies

Presenter : *Professor Mais Suleymanov*

*Baku State University , Azerbaijan*

**Time: 17:30 - 17:55 (Online)**

# Introduction

In fact, this talk is a continuation of my previous talk given at NUCLEUS-2020 : “The meaning behind observed  $p_T$  regions at the LHC energies, some properties of the regions” .

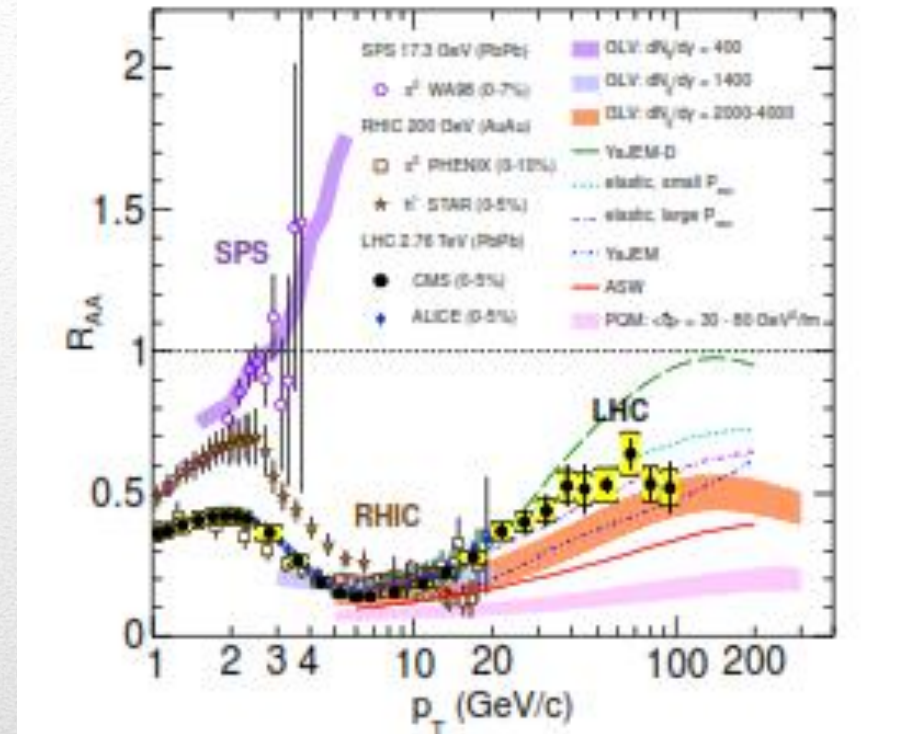
I want to remind you about some points of that talk.

The motivation of the research was connected with that : the evolution picture of the Nuclear Modification Factor [CMS Collaboration. *Eur. Phys. J. C* (2012) 72:1945] –

$$R_{AA} = \frac{d^2N/dp_T d\eta}{\langle T_{AA} \rangle d^2\sigma^{pp}/dp_T d\eta}$$

as a function of  $p_T$  shows that in the range of  $p_T = 5-10$  GeV/c, the suppression is stronger than before observed at the RHIC. Beyond  $p_T = 10$  GeV/c up to 20 GeV/c  $R_{AA}$  shows a rising trend, this rise continues at higher  $p_T$ , approaching a suppression factor 0.5-0.6 in the range of 40 – 100 GeV/c.

The behavior of the  $R_{AA}$  is very complex and today we are far from understanding completely this. So we tried to understand the behavior of the  $R_{AA}$  from the initial  $p_T$  distributions.



# Method

For this goal the invariant differential yield of the charged particles,  $\pi^0$ -,  $\eta$ -,  $K^0$ - and  $\phi$ -mesons as a function of  $p_T$  in  $pp$  and  $Pb$ - $Pb$  collisions at the LHC energies were analyzed

/Mais Suleymanov, *Int.J.Mod.Phys. E* 27 (2018) no. 1, 1850008 ;*Int.J.Mod.Phys. E*28 (2019) no.10, 1950084; *arXiv:nucl-ex/1710.09296*; The [ALICE Collaboration](#). *Phys. Rev. C* 95, 064606(2017); DOI: [10.1103/PhysRevC.95.064606](#)

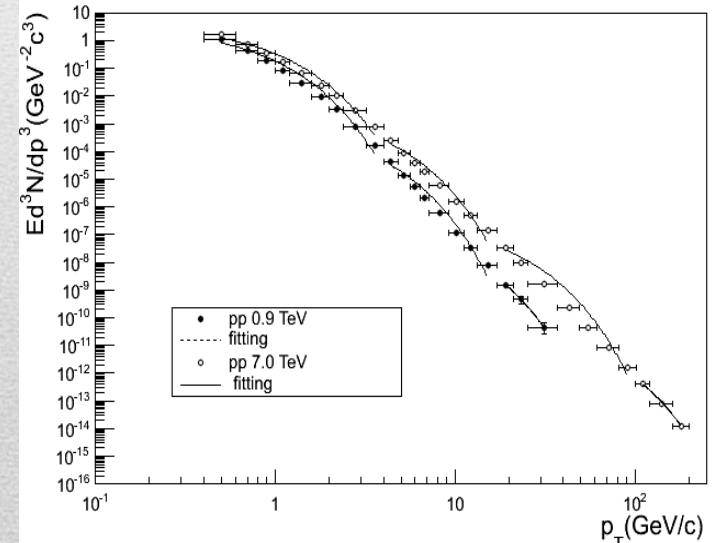
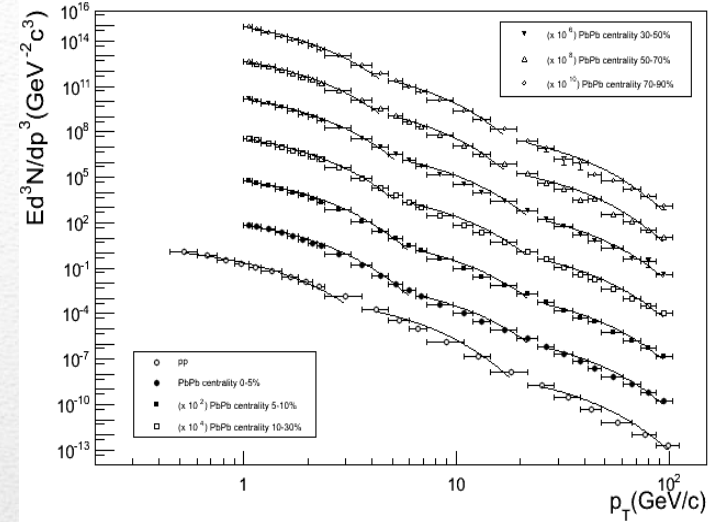
/. The published experimental data by CMS, ALICE and ATLAS collaborations were used.

First, we fit the  $p_T$  distributions in the whole experimentally measured ranges (from the minimum measured value of  $p_T$  ( $p_T^{min}$ ) to maximum one ( $p_T^{max}$ )) with a simple fitting function :

$$y = a_K^c e^{-p_T b_K^c}$$

the  $a_K^c$  and  $b_K^c$  are the free fitting parameters. The index  $c$  is used to designate the type of the events (see table) and the index  $K$  represents the number of the  $p_T$  regions.

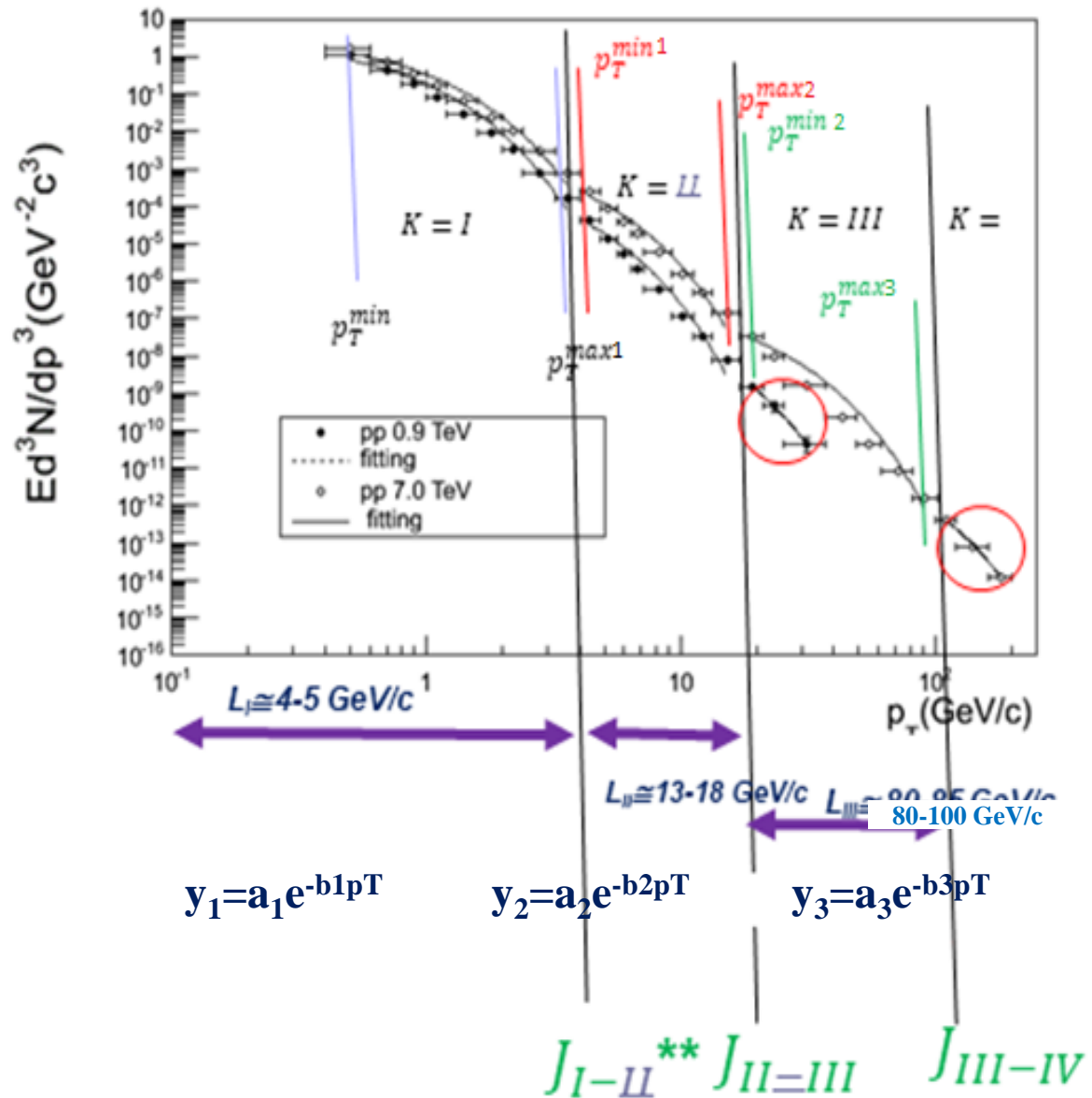
particles	energy (TeV)	0.9	2.76	7	8
	pp	pp	PbPb		
charged particles		3	1 2	4	5
$\pi^0$ -meson		31	11 -	41	51
$\eta$ -meson		32	12 -	42	52
$K^0$ -meson		-	13 -	-	-
$\phi$ -meson		-	14 -	-	-



# Method

This fitting attempt did not produce good fitting results and we decided to decrease the values of the  $p_T^{max}$  till getting a value of  $p_T^{max1}$  at which the best fitting results are reached. So we defined the boundary values of the  $p_T$  (from  $p_T^{min}$  to  $p_T^{max1}$ ), for the first  $p_T$  region ( $K=I$ ).

The rest of the distributions (from the first point after the  $p_T^{max1}$  ( $p_T^{min1}$ ) till  $p_T^{max}$ ) were fitted again by the same function and again to get the optimized fitting results the values of the  $p_T^{max}$  was limited to find the  $p_T^{max2}$  at which the best fitting results reached. After getting the values of the  $p_T^{max2}$  we defined the boundary values of the  $p_T$  (from  $p_T^{min1}$  to  $p_T^{max2}$ ), for the second  $p_T$  region ( $K=II$ ) and so on. The figure, as an example, visualizes the procedure of the getting the best fitting results. Then using the obtained values of the maximum and minimum  $p_T$  for the best fittings in the different regions, the boundary values of  $p_T$  for the regions ( $J_K^c$ ), and the lengths ( $L_K^c$ ) of the regions have been defined



<sup>c</sup>The values of  $J_K^c$  were calculated using experimentally measured values of  $p_T^{min}$  (the value of  $p_T^{min}(I)$  for the regions  $I$  was taken as  $p_T^{min}(I) = 0$ ) and  $p_T^{max}$  as  $J_{I-II}^c = (p_T^{max}(I) + p_T^{min}(II))/2$  for the region  $I$  and  $II$ ,  $J_{II-III}^c = (p_T^{max}(II) + p_T^{min}(III))/2$  for the region  $II$  and  $III$  and so on. The values of  $L_K^c$  were calculated as  $L_I^c = J_{I-II}^c$ ;  $L_{II}^c = J_{II-III}^c - J_{I-II}^c$  and  $L_{III}^c = J_{III-IV}^c - J_{II-III}^c$  and so on.

# Results

The applied method has shown that the  $p_T$  distributions contain several  $p_T$  regions (the number of regions increase with  $p_T$ ).

The regions could be characterized by the lengths  $L_K^c$  and two free fitting parameters  $a_K^c$  and  $b_K^c$ .

The values of the  $L_K^c$  increase with  $p_T$  (and with  $K$ ) and for example for the charged particles at 2.76 TeV there equations :

$$L_{III}^1 : L_{II}^1 \cong 5 ; L_{II}^1 : L_I^1 \cong 3 \text{ (Pb-Pb);}$$

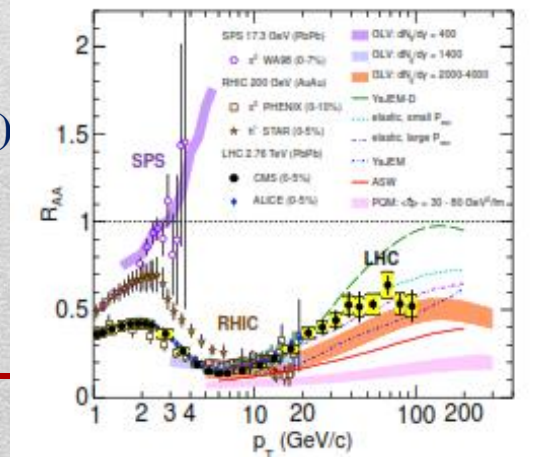
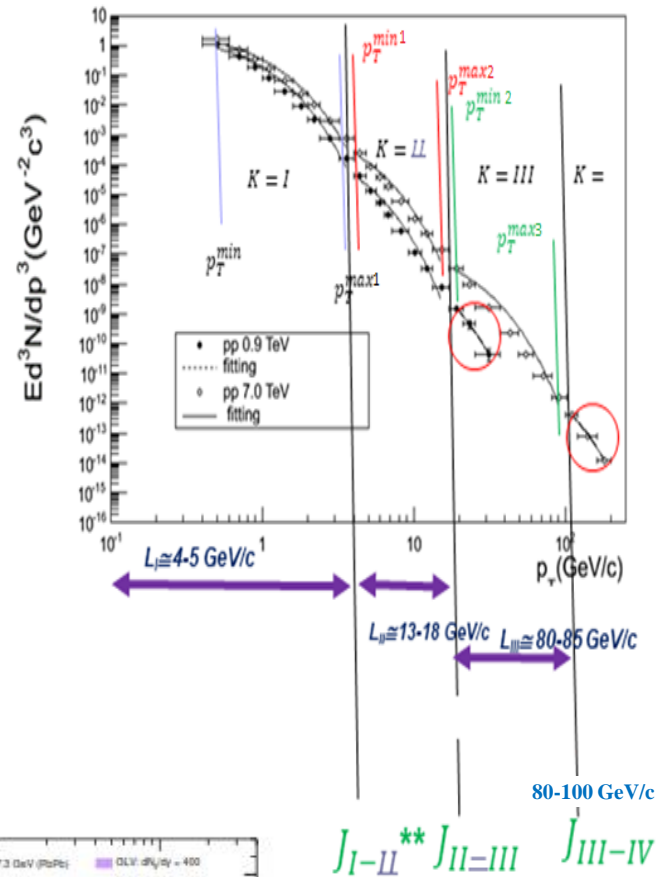
$$L_{III}^1 : L_{II}^1 \cong 5 ; L_{II}^1 : L_I^1 \cong 5 \text{ (pp)}$$

It may be due to that the observed  $p_T$  regions reflect features of fragmentation and hadronization of partons through the string dynamics.

Again one can say that for the charged particles at 2.76 TeV the regions are limited by the values of  $p_T$  :

- $< 4 - 6 \text{ GeV}/c$  (I region);
- $4 - 6 \text{ GeV}/c < p_T < 17 - 20 \text{ GeV}/c$  (II region)
- $> 17 - 20 \text{ GeV}/c$  (III region).

Let us note that the II region is the area where Nuclear Modification Factor has minimum for the most central heavy ion collisions- jet suppression.



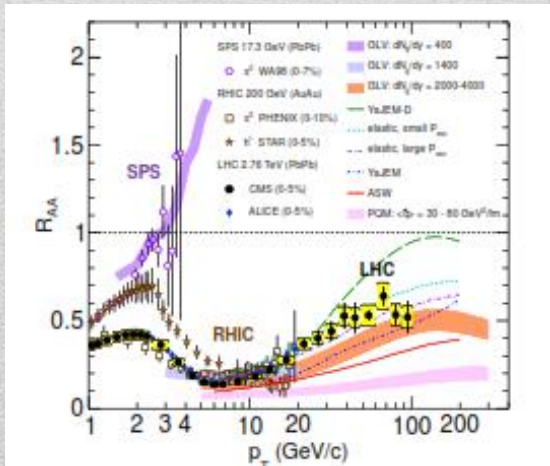
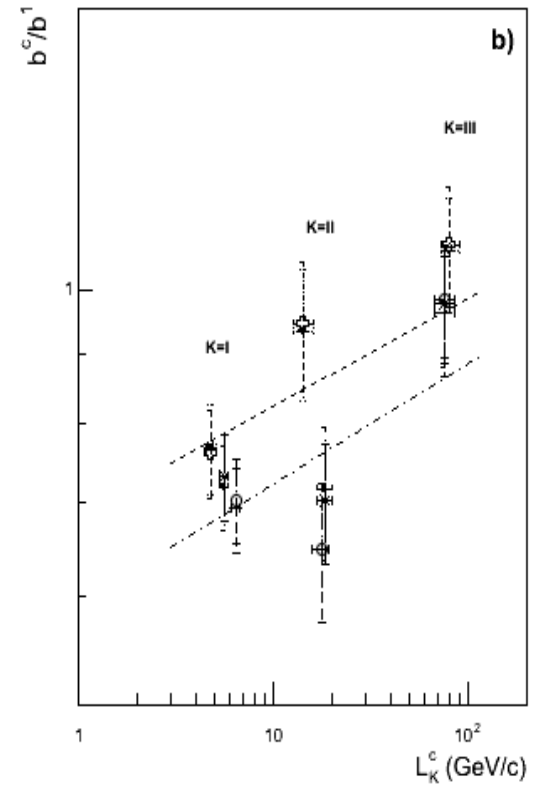
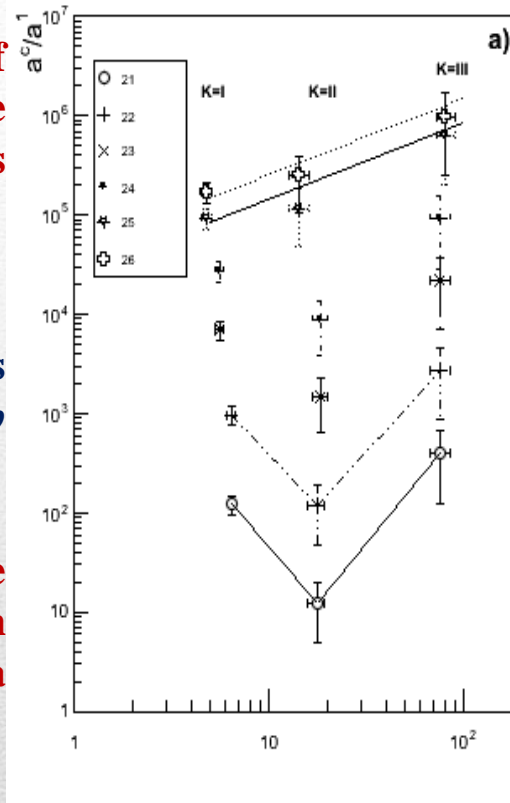
# Results

We have constructed the ratios of :

–  $a^c/a^1$ , here  $a^c$  and  $a^1$  is the values of the free fitting parameters  $a_K^c$  for the most central  $PbPb$  and  $pp$  collisions respectively

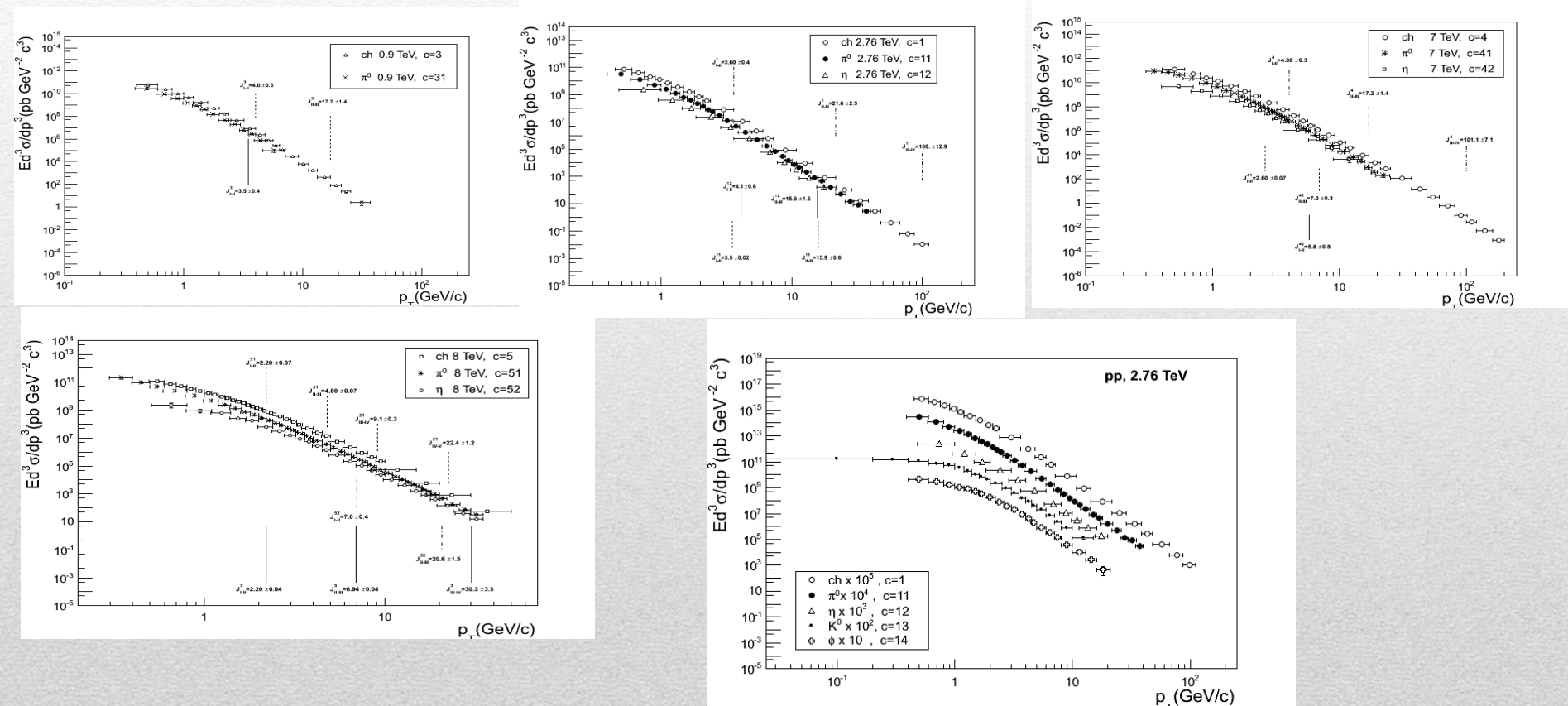
-  $b^c/b^1$ , here  $b^c$  and  $b^1$  is the values of the free fitting parameters  $b_K^c$  for the most central  $PbPb$  and  $pp$  collisions respectively .

One can see that the ratios for the parameter  $a_K^c$  have the minimum values for the second  $p_T$  region - a suppression.



# Results

The including of the spectra of  $\pi^0$ -,  $\eta$ -,  $K^0$ - and  $\phi$ - mesons to the consideration and increasing the energy of colliding particles has given new results to study some properties of the  $p_T$  regions and to get an additional information on the energy and mass dependences of the characteristics of the  $p_T$  regions:  $L_K^C$ ,  $a_K^C$  and  $b_K^C$ .



The distributions were processed using same method which was applied to process the charged particles spectra.

One can say that again as in the case of the charged particles the  $p_T$  distribution data on invariant differential yield of the  $\pi^0$ -,  $\eta$ -,  $K^0$ - and  $\phi$ - mesons produced in the pp collisions contained several  $p_T$  regions which could be characterized by the values of the regions' lengths and the values of the free fitting parameters  $a_K^c$  and  $b_K^c$ .

Taking into account the results coming from the papers [*Mais Suleymanov, Int.J.Mod.Phys. E 27 (2018) no. 1, 1850008 ;Int.J.Mod.Phys. E28 (2019) no.10, 1950084; arXiv:nucl-ex/1710.09296*] on the  $p_T$  distributions of the charged particles, the  $\pi^0$ - and  $\eta$ - mesons and the new data for the  $K^0$ - and  $\phi$ - mesons we have analyzed the energy and mass dependences of the  $p_T$  regions' parameters to reach the aim of paper: to get an additional information on the energy and mass dependences of the characteristics of the  $p_T$  regions.

---

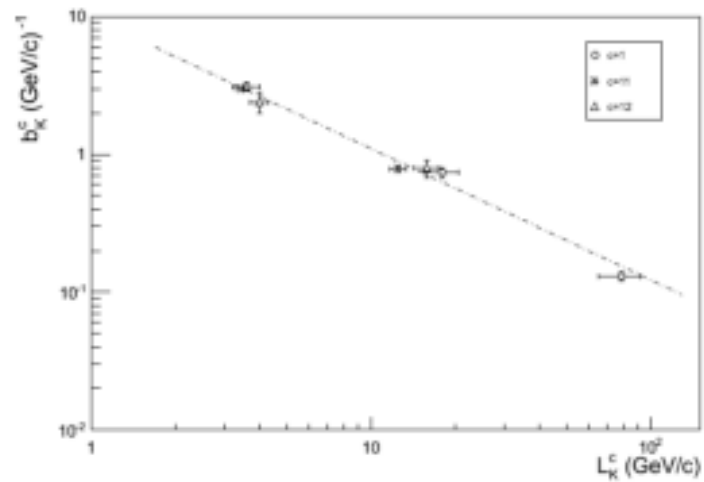
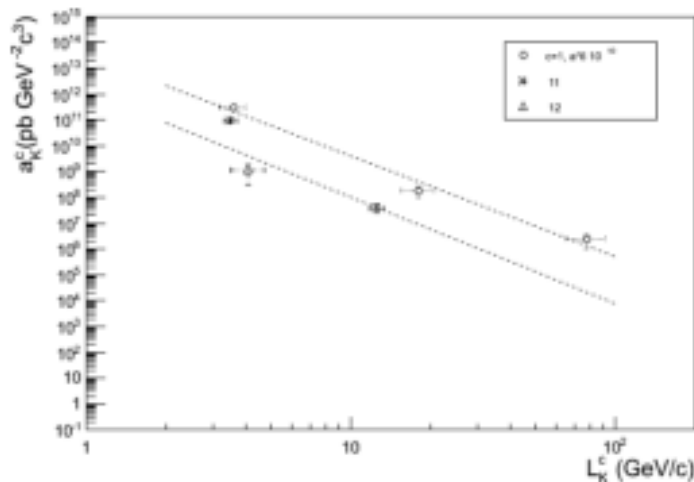


# Results

The study of the  $L_K^c$  dependencies of the parameters  $a_K^c$  and  $b_K^c$  have showed that the regions can be classified into two groups depending on the values of the  $L_K^c$ ,  $a_K^c$  and  $b_K^c$ ; the characteristics for the first group regions don't depend on colliding energy and the type of the events ( $c$ ) (though the values of  $a_K^c$  increase linearly with energy) whereas the characteristics for the second group ones show strong dependencies on the type of the events  $c$  and colliding energies. It was found that for:

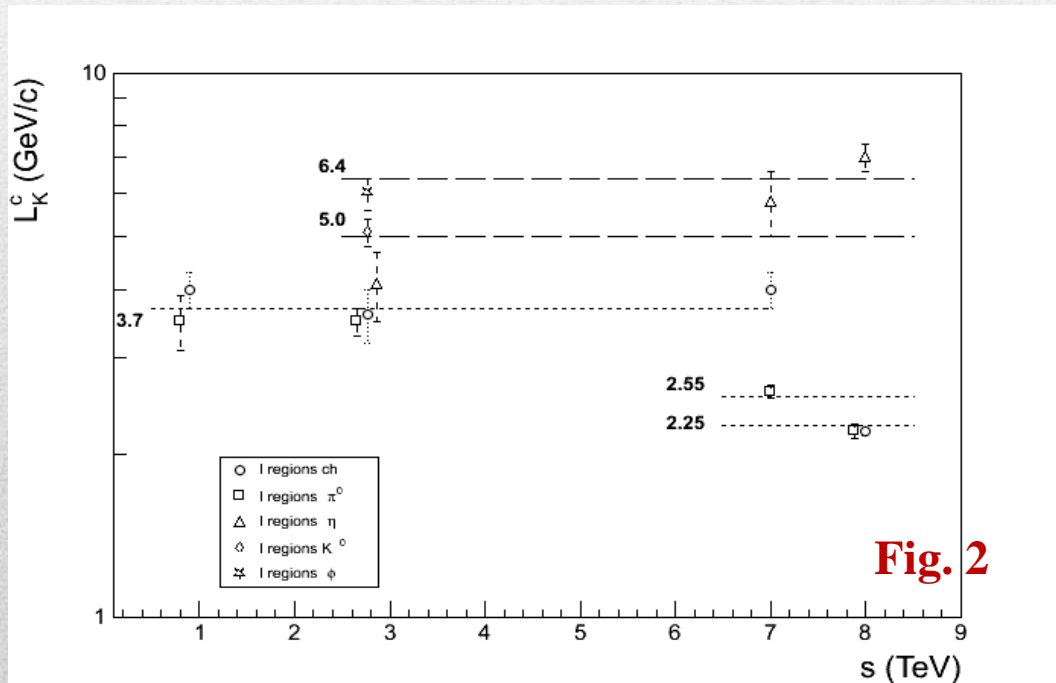
- the first group of regions the lengths are 3-5 times greater than the lengths of neighboring, lower  $p_T$  regions.
- the second group of regions the lengths are 1-2 times greater than the lengths of neighboring lower  $p_T$  region.

In the framework of the string fragmentation and hadronization dynamics, this could mean that the particles in the group I of regions are produced through previous-generation strings decays into 3-5 strings while those in group II originate from previous-generation strings decays into 2 strings.



# Results

The Fig. 2 shows the energy dependences of the values of  $L_I^c$  ( I  $p_T$  regions' length) for the charged particles,  $\pi^0$ -,  $\eta$ -,  $K$ - and  $\phi$ -mesons produced in the pp collisions. The lines in the figure have been drawn by hand. One can see that all points relevant to values of the  $L_I^c$  lie down on 5 lines at  $L_I^c \cong 2.25; 2.55; 3.7; 5.0; 6.4$  GeV/c. The figure say us that for the considered charged particles, the energy dependence appear jump-like.



# Results

The energy dependences of the II  $p_T$  regions' lengths for the charged particles,  $\pi^0$ -,  $\eta$ -mesons produced in the  $pp$  collisions are shown in the Fig. 3.

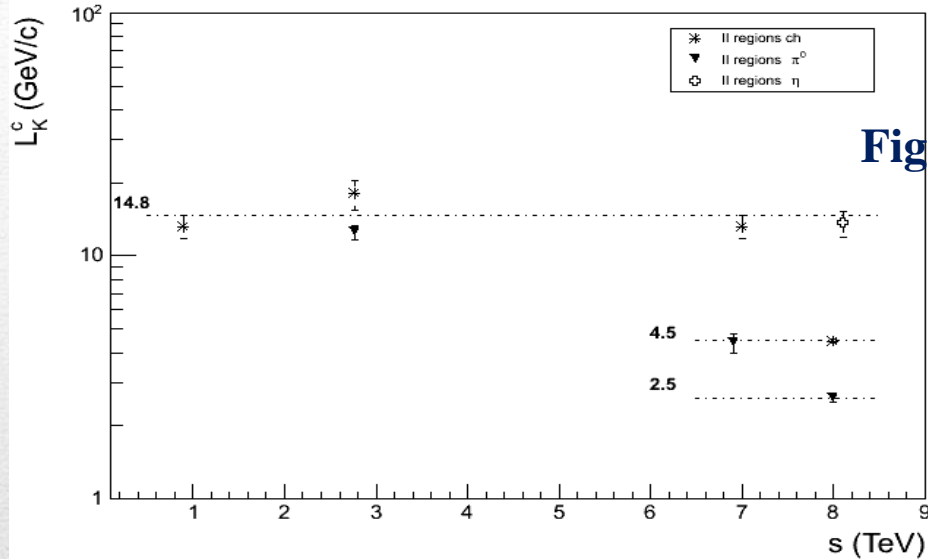


Fig. 3

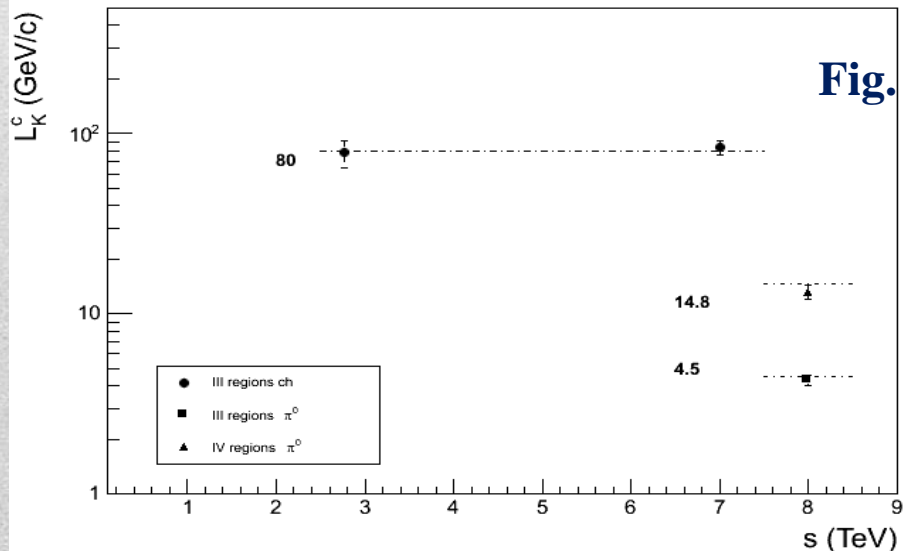


Fig. 4

The Fig. 4 shows the energy dependences of the values of the lengths for the III and IV  $p_T$  regions for the charged particles and  $\pi^0$ -mesons produced in the  $pp$  collisions.

One can say that all points relevant to values of the lengths for: the I  $p_T$  regions as a function of energy lie down on 5 lines at  $L_I^c \approx 2.25; 2.55; 3.7; 5.0; 6.4$  GeV/c; the II  $p_T$  regions are approximately on 3 lines at level  $L_{II}^c \approx 14.8; 4.5; 2.5$  GeV/c; the III and IV ones roughly lie down on 3 lines at  $L_{III}^c \approx 80; 14.8$  and  $4.5$  GeV/c. The energy dependence shows jump-like changes and give clue on discrete changes with energy.

One can see that wherein the lengths for the light mesons decrease and they increase for the heavy mesons.

# Results

The last result is seen more cleanly from the Fig. 5 which shows the mass dependence for the values of  $L_K^c$  (in cases 2 or more points in the distributions). The lines have been drawn by hand. One can see that with mass (in the I  $p_T$  region at  $s = 2.76$  TeV) the values of the lengths increase slowly and in the II  $p_T$  regions at  $s=2.76$  TeV (we have had only 2 points) the values of the lengths show an independence on mass. At  $s = 7$  TeV the values of  $L_K^c$  increase sharper than at 2.76 TeV, gets more strong at energy 8 TeV and the relation holds:  $\langle L_\eta \rangle : \langle L_{\pi^0} \rangle \cong m_\eta : m_{\pi^0}$  (which was observed in the paper [*Int.J.Mod.Phys. E28 (2019) no.10, 1950084*]). The dependences of the lengths of  $p_T$  regions on the mass of particles and the strengthening of this dependence with increasing energy of colliding protons and the result on  $\langle L_\eta \rangle : \langle L_{\pi^0} \rangle \cong m_\eta : m_{\pi^0}$  together with jump-like energy dependences can be arguments in favor of string theory.

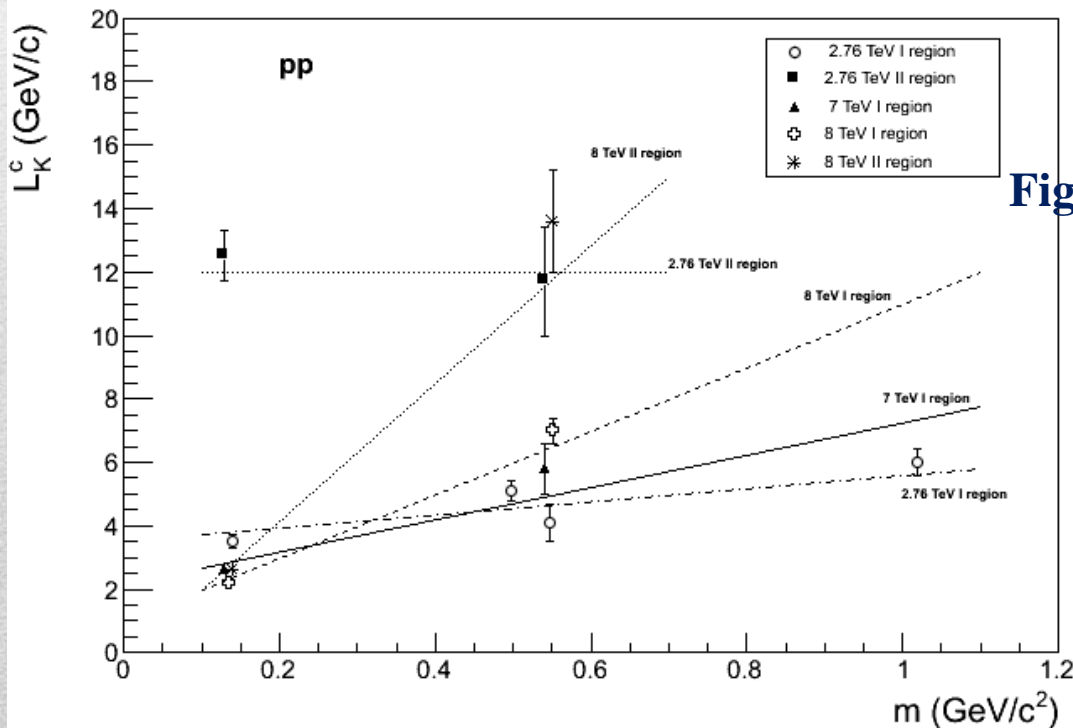
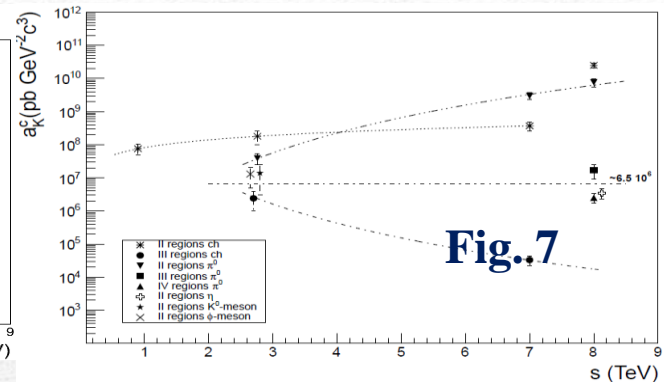
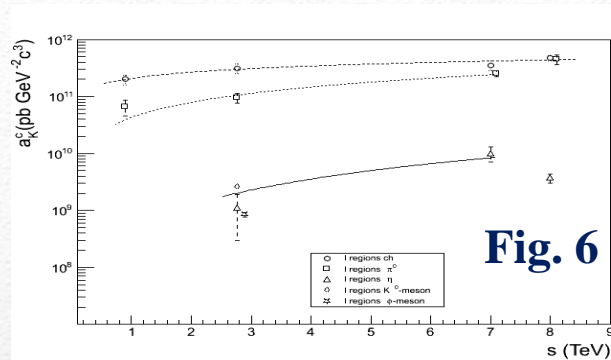


Fig. 5

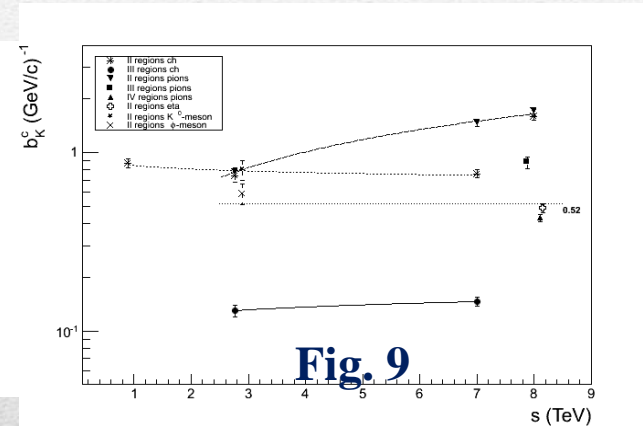
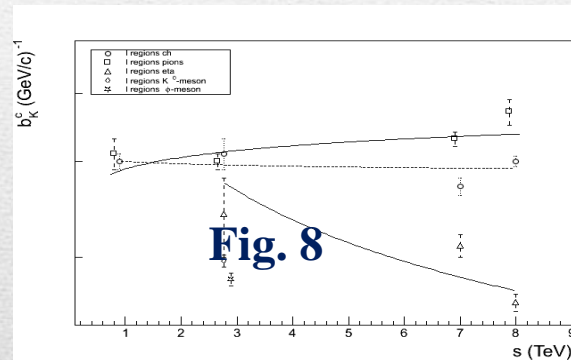
Assuming that the values of the  $L_K^c$  are directly proportional to the string tension the result could be considered as evidence in favor of parton string fragmentation dynamics. Because in string theory the masses of elementary particles and their energy are defined by the intensity of string vibration and strangeness of the string stretch.

# Results

The energy dependences for the parameters  $a_K^c$  (I-IV  $p_T$  regions) are shown in the Fig. 6-7.



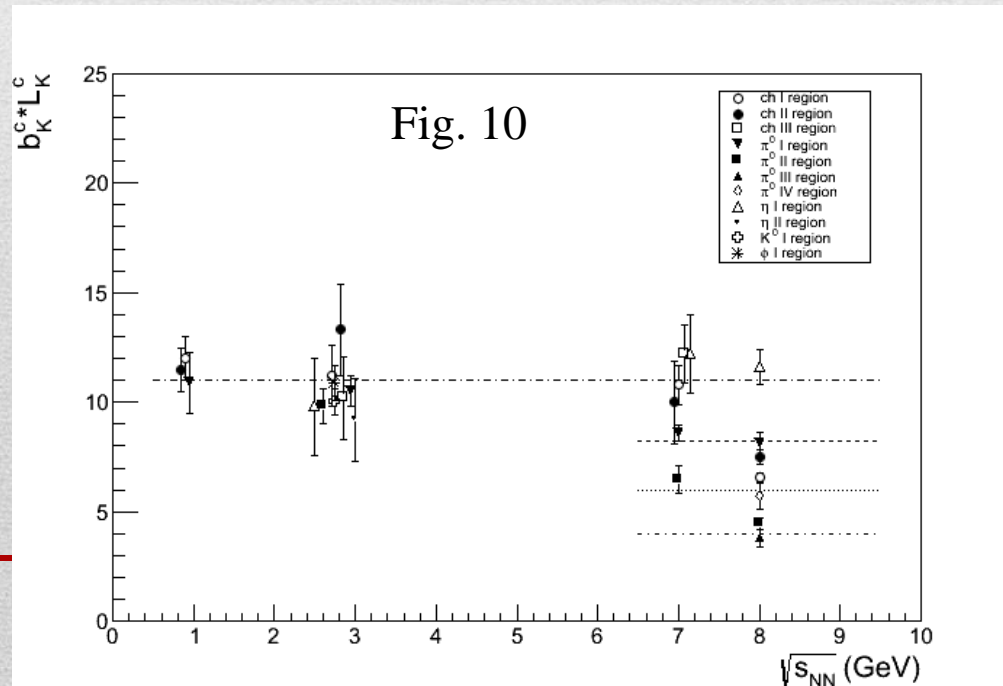
The energy dependences for the parameters  $b_K^c$  are shown in the Fig. 8-9 for the  $p_T$  regions' data.



One can see again that the values of  $a_K^c$  and  $b_K^c$  as a function of energy grouped around several lines and show jump-like changing with energy and again parameters  $a_K^c$  and  $b_K^c$  have showed that the regions can be classified into two groups depending on the values of the  $L_K^c$ ,  $a_K^c$  and  $b_K^c$ ; the characteristics for the first group regions don't depend on colliding energy and the type of the events ( $c$ ) (though the values of  $a_K^c$  increase linearly with energy) whereas the characteristics for the second group ones show strong dependencies on the type of the events  $c$  and colliding energies.

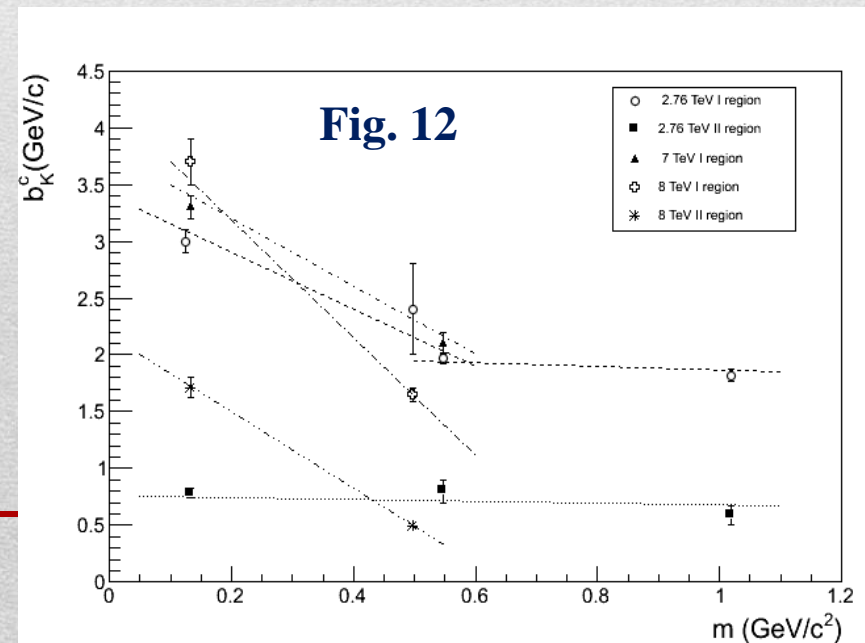
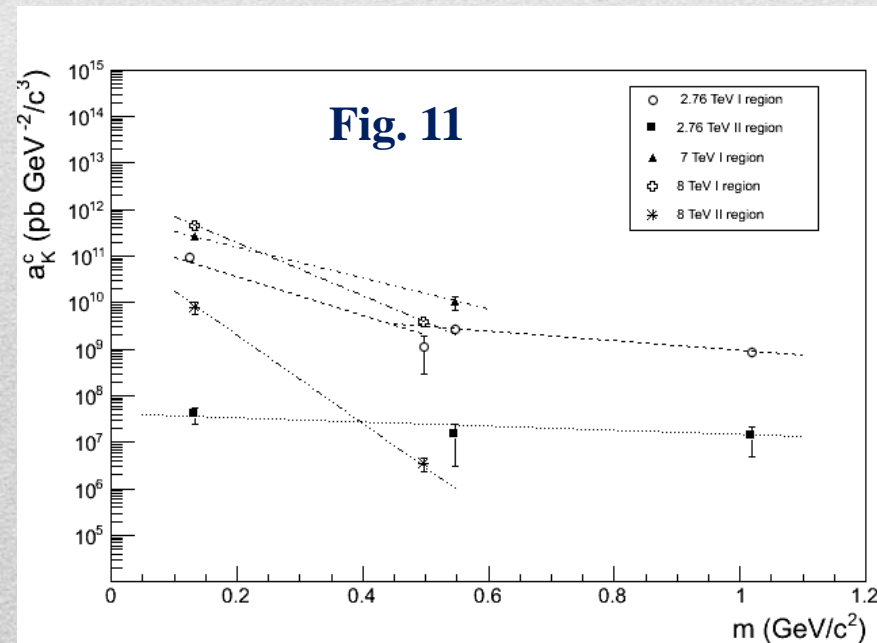
# Results

Fig. 10 shows the energy dependences, of the lengths  $L_K^c$  multiplied by the values of the free fitting parameter  $b_K^c$  in the same regions ( $L_K^c * b_K^c$ ) for the charged particles,  $\pi^0$ -,  $\eta$ -,  $K^0$ - and  $\phi$ - mesons produced in  $pp$  collisions at LHC energies. It can be seen that with energy, the values of  $L_K^c * b_K^c$  for most of cases with remain unchanged at the level of  $L_K^c * b_K^c \cong 11$ . The deviations from this value begin to appear at energy of 7 TeV for charged particles and neutral pions from II  $p_T$  region. For these events the values of  $L_K^c * b_K^c \cong 8$  or 6. At energy 8 TeV, deviations get stronger and have been observed for almost all cases (with except for one case with  $c=52$  - for the eta mesons at 8 TeV). Now the corresponding points are on the lines at 8,6 and 4. Again one can say that with energy the values of the  $L_K^c * b_K^c$  change jump-like as a signal on discrete change the values of  $L_K^c * b_K^c$ .



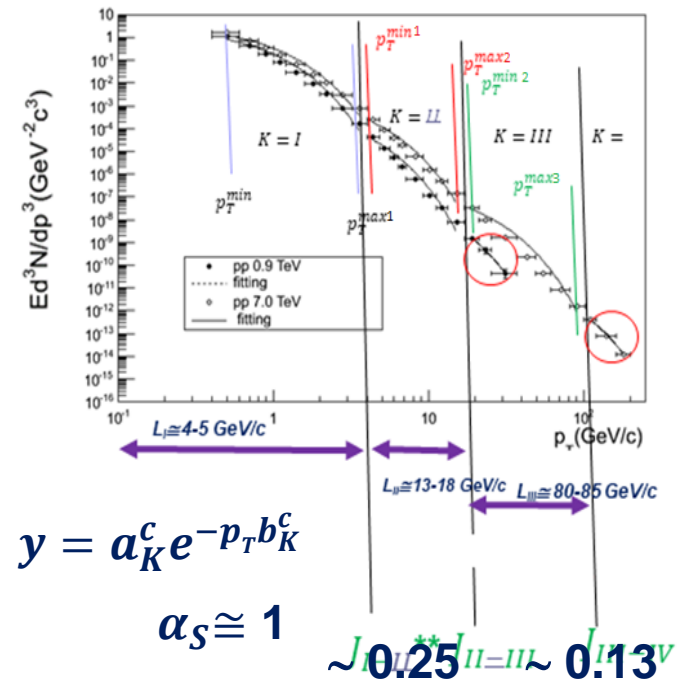
# Results

Fig. 11-12 show the mass dependence of the values of  $a_K^c$  and  $b_K^c$  for the cases when there are at least 2 defined points for the values of  $a_K^c$  and  $b_K^c$ . One can see that with mass in the I  $p_T$  region at  $s = 2.76$  TeV the values of the parameters  $a_K^c$  and  $b_K^c$  first decrease in the interval of mass  $m < 500$  MeV/c<sup>2</sup> and then almost doesn't depend on mass in the interval of  $m > 500$  MeV/c<sup>2</sup>. But for the II  $p_T$  regions at  $s=2.76$  the values of the parameters  $a_K^c$  and  $b_K^c$  don't depend on mass. At  $s=7$  TeV the values the parameters  $a_K^c$  and  $b_K^c$  decrease. At a further increase the energy at 8 TeV the values of the  $a_K^c$  and  $b_K^c$  decrease sharply. So one can note that unlike parameter  $L_K^c$  the mass dependences of the parameters  $a_K^c$  and  $b_K^c$  show regime change at mass  $m \cong 500$  MeV/c<sup>2</sup>.



# Discussion

Observation of the  $p_T$  regions for both  $pp$  and for Pb–Pb collisions suggests that these regions could reflect the fragmentation and hadronization properties of partons. The parameter  $b_K^c$  could be represented as:  $b_K^c \cong \frac{1}{\tilde{p}_T}$  (here  $\tilde{p}_T$  is some average  $p_T$  for parton system) and with considering  $-\tilde{p}_T \cong t \cong -q^2$  ( $t$  is Mandelstam variable) we can write that  $b_K^c \cong \frac{1}{\sqrt{q^2}}$ .



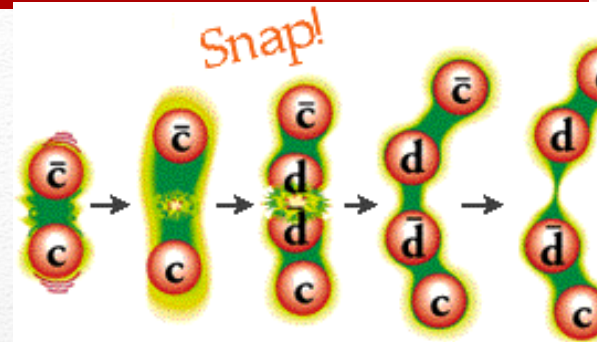
Using the expression  $\alpha_s \cong \left[ \ln \left( \frac{q^2}{\Lambda^2} \right) \right]^{-1}$  (at  $\Lambda=0.2$  GeV/c) one can get that :  $\alpha_s \cong 1$  for the I region;  $\sim 0.25$  for the II region and  $\sim 0.13$  for the III region. The increasing of the  $\alpha_s$  with decreasing of the  $p_T$  is similar to the dependence of the  $\alpha_s$  on  $p_T$  which is characteristics of the QCD quark string :  $\frac{1}{r^2} \sim Q^2 = -q^2$ , in which  $r$  is a distance between quarks in the string

This result together with the above results on the ratios of lengths ( $\langle L_\eta \rangle : \langle L_{\pi^0} \rangle \cong m_\eta : m_{\pi^0}$ ) can be clue that the fragmentation and hadronization of the partons occurs through the string dynamics, and the values of the  $L_K^c$  can be related to the string tension. So one can conclude that the meaning behind observed  $p_T$  regions at LHC energies could be the parton fragmentation and hadronization through parton strings.



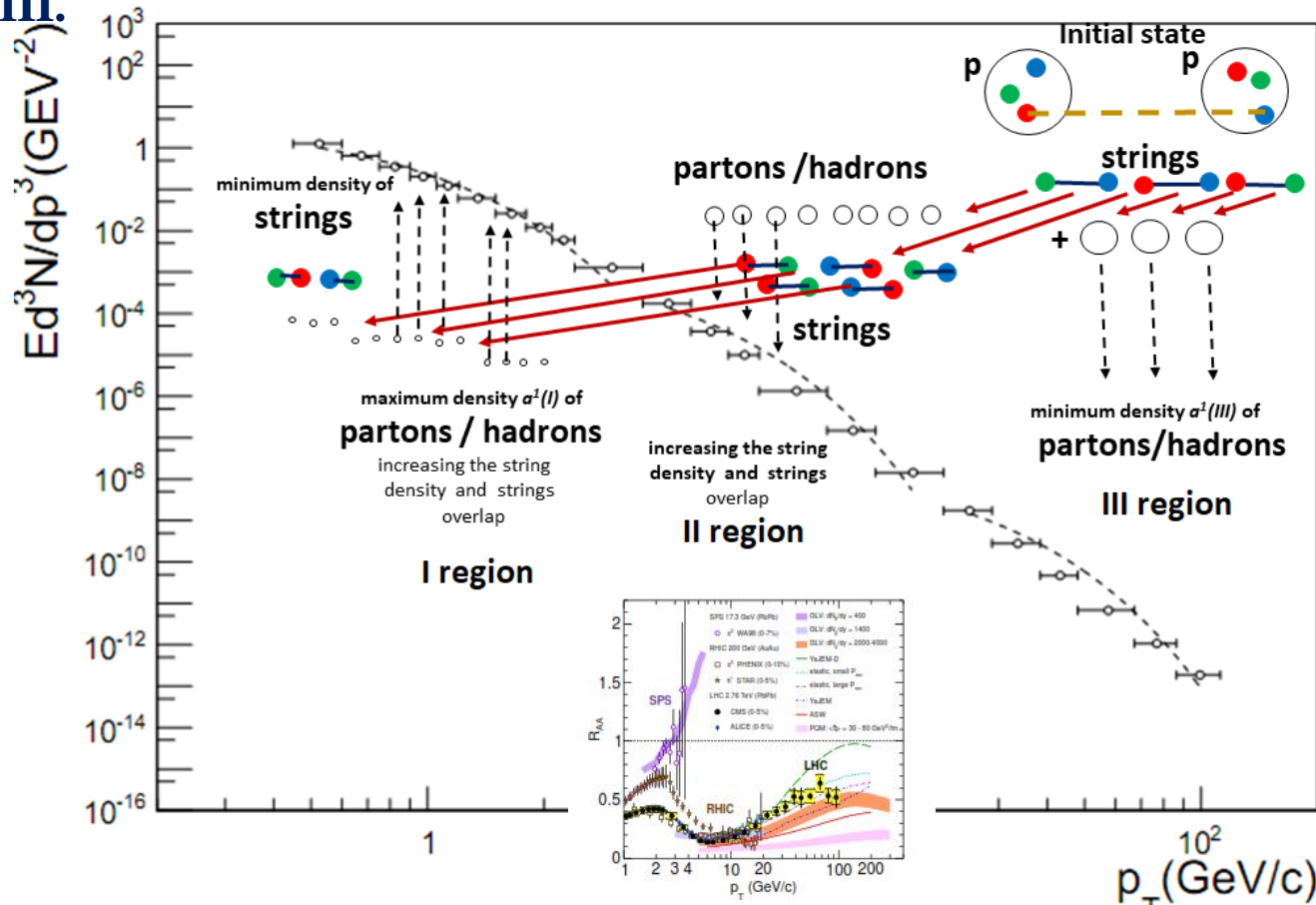
# Discussion

In this picture the region III is the domain of creation of first generation partons/strings (in our measurements) during collisions, where the most energetic hadrons / partons / strings (with highest tension) are produced and weakly modified by the medium. The region II is the one with highest density of the strings decayed from ones in region



In this pictures the region I is the one with the maximum number of hadrons and minimum number of strings.

III.

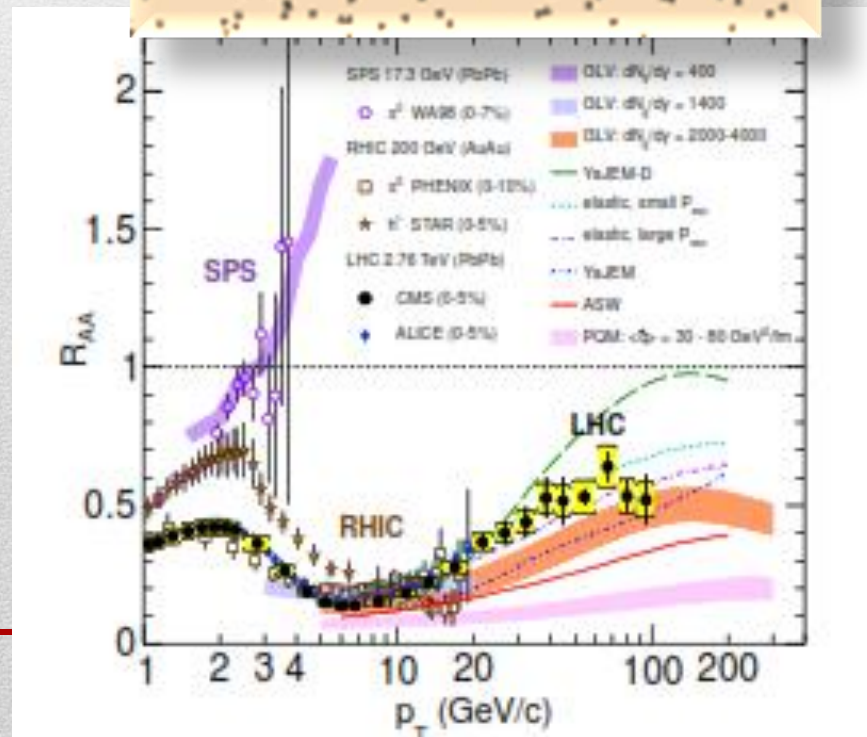
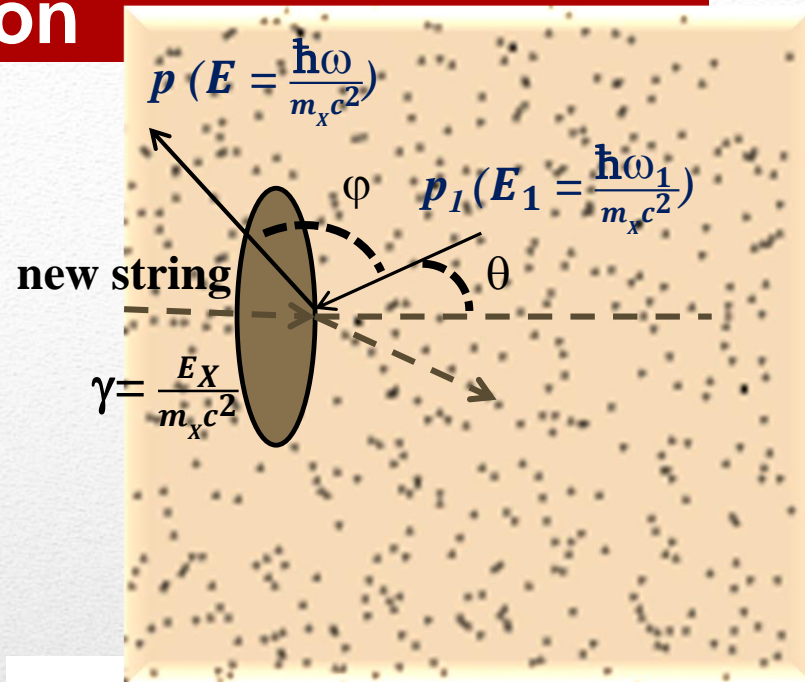


The high density causes string fusion (II region) and a collective phenomenon, which is as a result of the new string formation in the most central pp interactions. It can explain the anomalous behavior of the Nuclear Modification Factor in this region.

# Discussion

In the paper [Mais Suleymanov *arXiv: nucl-ex/1710.09296* ] we have discussed that the phenomena string fusion\* can explain anomalous behaviour of the Nuclear Modification Factor in II region as a result of the inverse Compton effect for partons.

We support that in the case of a coherent collision of the new string with a parton which has a lower energy than the string, the parton can gain energy, resulting in its acceleration and shifting to the higher  $p_T$  region. After losing a significant part of its energy new string can decay into partons with lower energies - slowed partons in the interval of lower  $p_T$ .



# CONCLUSION

- $p_T$  distribution data from the LHC of the particles produced in  $pp$  and  $Pb-Pb$  collisions contain several  $p_T$  regions with special properties, which could be characterized by the length of the regions  $L_K^c$  and two free fitting parameters  $a_K^c$  and  $b_K^c$ ;
- the study of the  $L_K^c$  dependencies of the parameters  $a_K^c$  and  $b_K^c$  and of the energy dependencies of these parameters have showed that the regions can be classified into two groups;
- the values of  $L_K^c$ ,  $a_K^c$  and  $b_K^c$  as a function of energy grouped around several lines and show jump-like changing with energy;
- the lengths of the regions increase with mass of the particles and the increasing gets stronger with energy, at maximum available energy (8TeV) the ratio of lengths for  $\eta$  - mesons to ones for  $\pi^0$ —mesons become approximately equal to ratio of their mass -  $\langle L_\eta \rangle : \langle L_{\pi^0} \rangle \cong m_\eta : m_{\pi^0}$ ;
- the mass dependences of the parameters  $a_K^c$  and  $b_K^c$  show regime change at mass  $\cong 500 \text{ MeV}/c^2$ .

## CONCLUSION

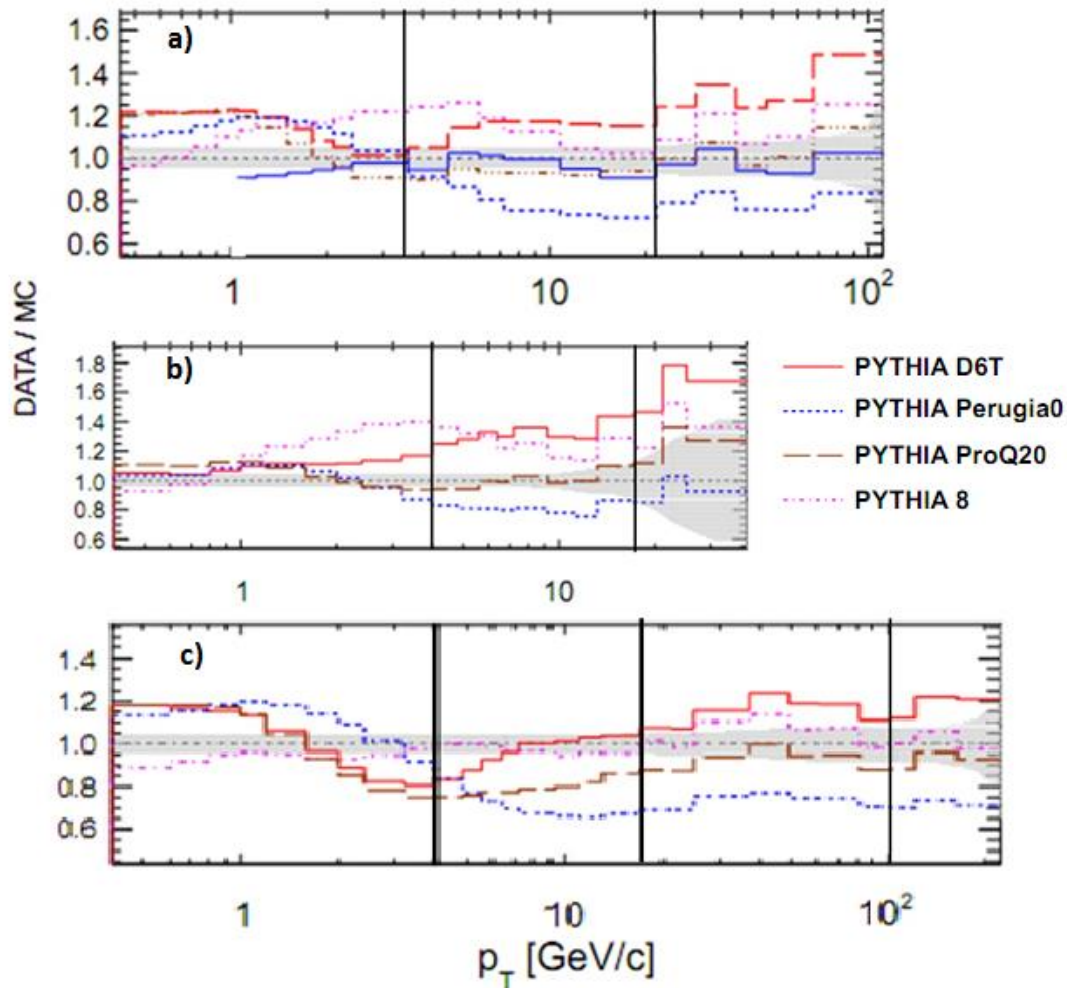
The existing of several  $p_T$  regions, the jump-like changing of the characteristics of the regions and grouping the values of the characteristics around certain lines with energy can say on discrete energy dependences for the characteristics of the regions which is characteristics of the QCD quark string .

So we could conclude that the observed  $p_T$  regions and their characteristics reflect features of fragmentation and hadronization of partons through the string dynamics. According to the logic of string theory, the results could mean that parton strings of the very first generation (with maximum tensions  $T_{\max}$  formed immediately after the collision) either hadronize or decay forming the next generation of strings with tensions  $T' < T_{\max}$  . Some of the newly formed strings can also either hadronize other ones can decay and create strings of the next generation with tensions  $T'' < T'$ , etc., up to the minimum tensions  $T_{\min}$  after which the string decay stops. That is, two processes occur simultaneously: string hadronization; string breaking. In an experiment, we measure the spectrum of hadrons ,we cannot have a spectrum of the strings themselves. We think the the string breaking effect might be the reason of observing several  $p_T$  regions which has a discrete nature.

Finally we want to note that in the experiment, we can see only signature of the last generations of strings, which are in the area of our  $p_T$  measurements. It is very difficult to have signature for the very first generation of strings, since for this it is necessary to have measurements for  $p_T$  in the interval up to several TeV / c.

**Thank you very much**

---



**Fig.3a-c.** The ratio of the measured spectrum for the  $pp$  collisions at: a)  $\sqrt{s} = 2.76 \text{ TeV}$  (lower panel of the Fig.3a from paper [1]) ; b)  $\sqrt{s} = 0.9 \text{ TeV}$  (lower panel in Fig.5a from the paper [5]); c)  $\sqrt{s} = 7 \text{ TeV}$  (lower panel in Fig.5a from the paper [5]) to the predictions of the four PYTHIA tunes and to the interpolated spectrum (in Fig.3a). The grey band corresponds to the statistical and systematic uncertainties of the measurement added in quadrature.