

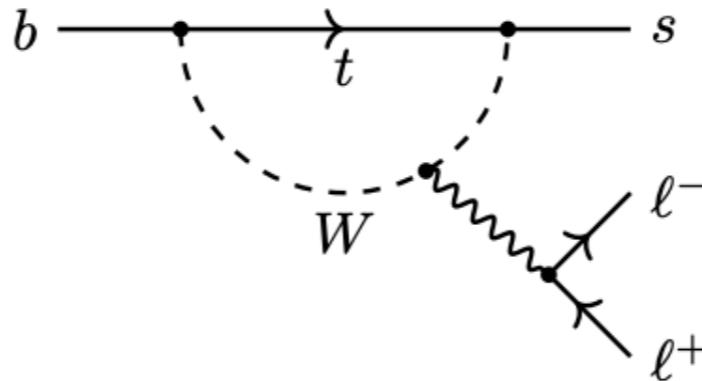


# The first angular analysis of the $B^+ \rightarrow \pi^+ \mu^- \mu^+$ decay using Run I and Run II data at the LHCb experiment

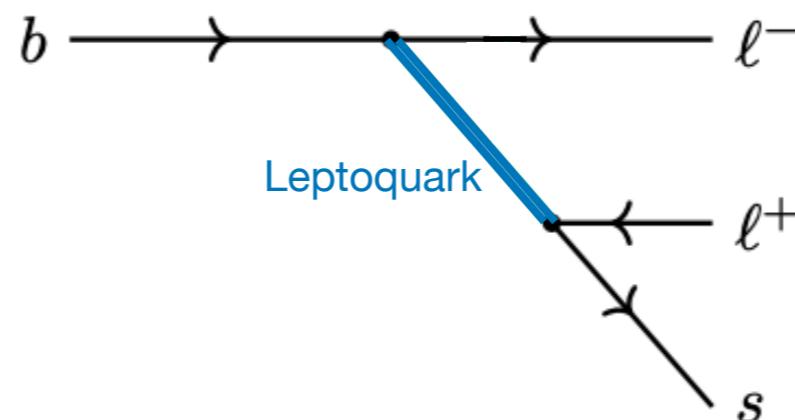
**Maria Flavia Cicala**  
University of Warwick  
On behalf of the LHCb Collaboration

# Rare B decays

- Flavour-Changing Neutral Current B decays are suppressed in the SM as they can only occur at loop level



- Because of their suppression in the SM, rare B decays are a good probe for New Physics
- A deviation from SM predictions in rare B decays could be evidence of New Physics



# Rare B decays

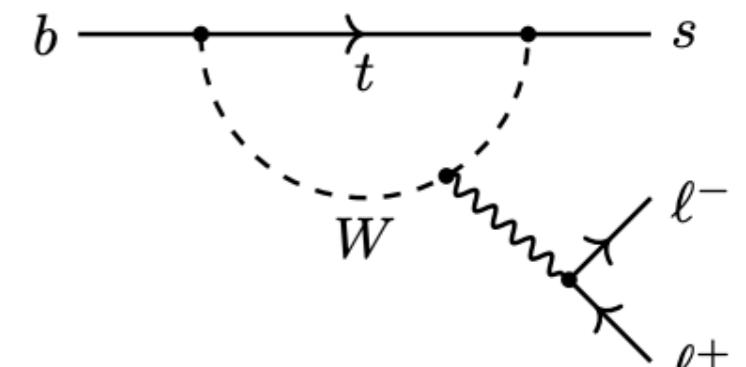
- Processes are described using an Effective field theory ( $M_b \ll M_W$ ):

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} \sum_i V_{CKM}^i C_i \mathcal{O}_i$$

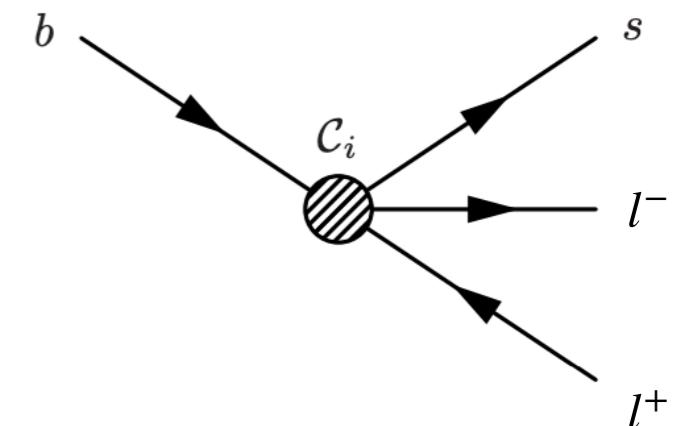
$C_i$  = Wilson coefficients

related to

$\mathcal{O}_i$  = Local operators



Point - like interaction



# Rare B decays

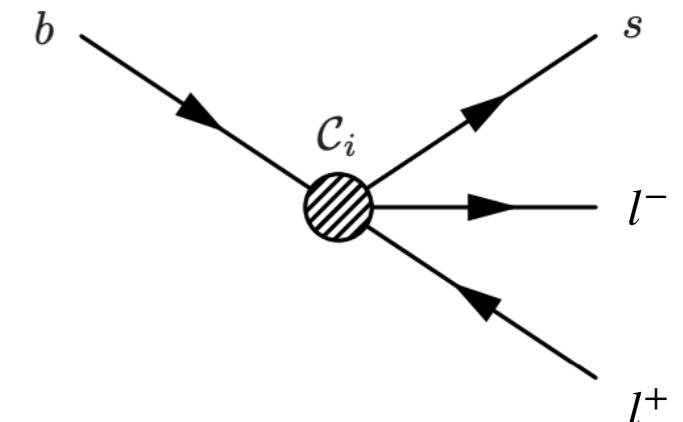
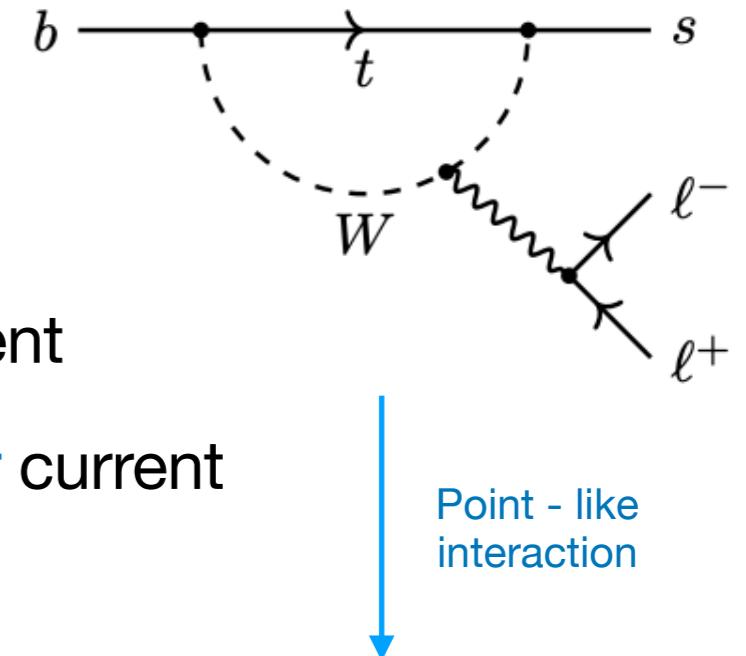
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$\begin{cases} C_9 & \rightarrow \text{vector current} \\ C_{10} & \rightarrow \text{axial vector current} \end{cases}$



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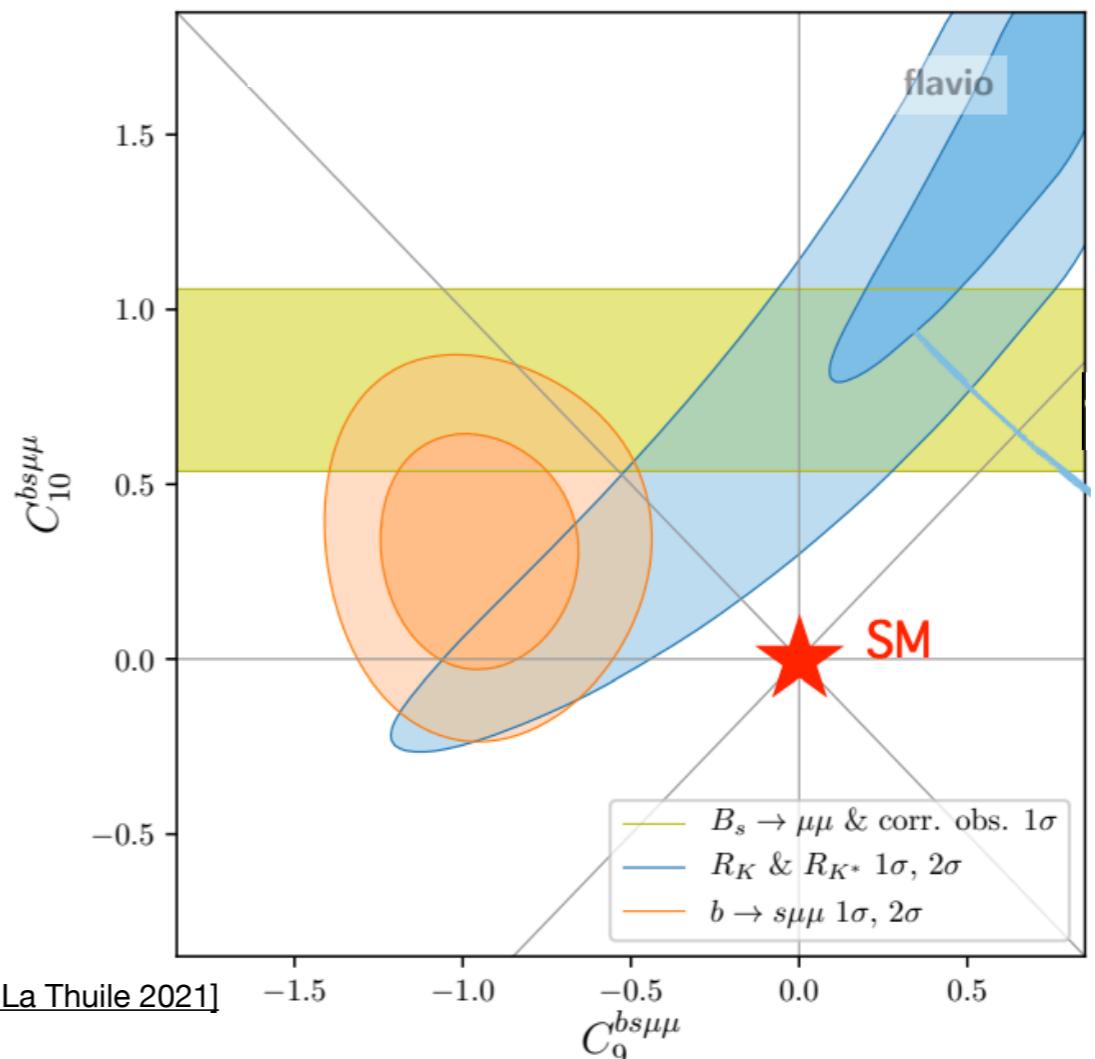
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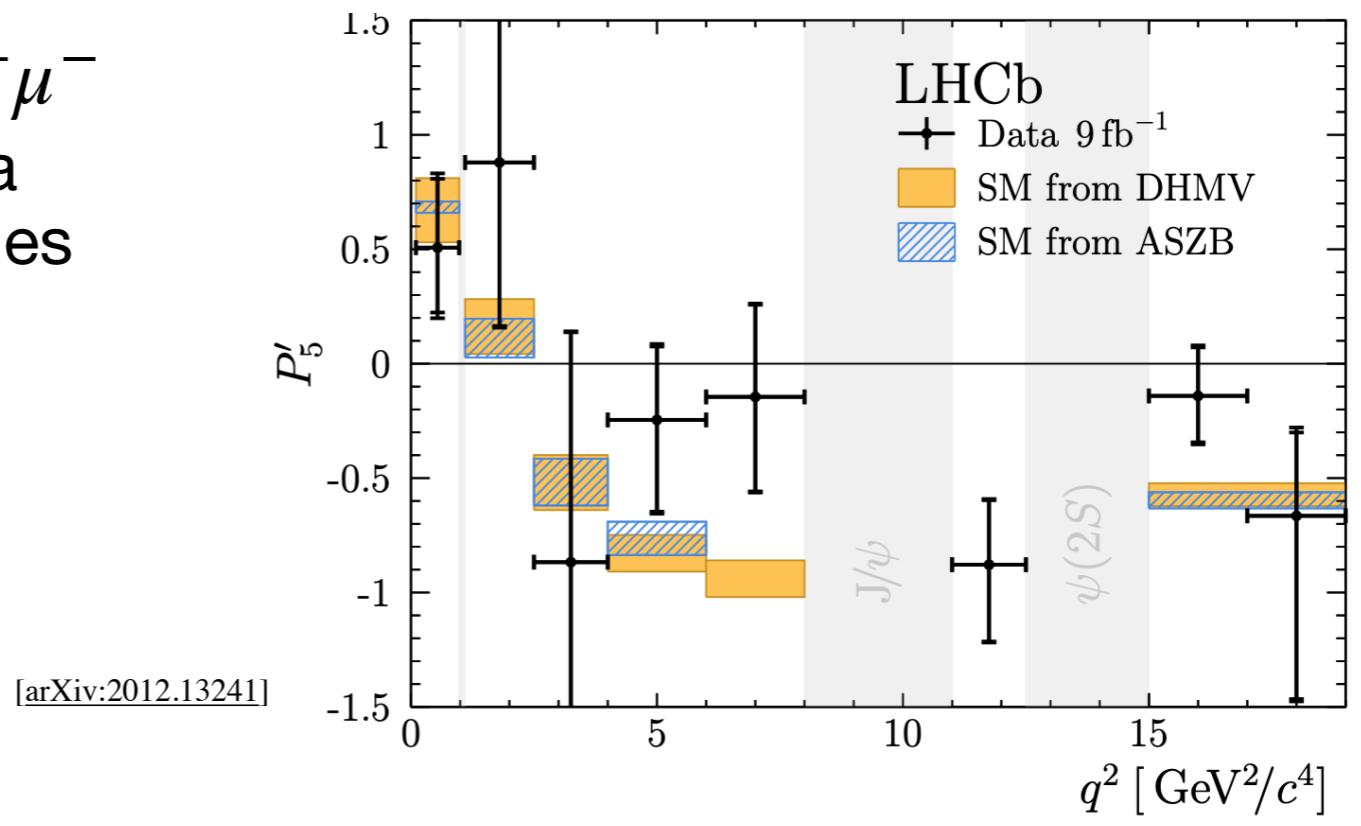
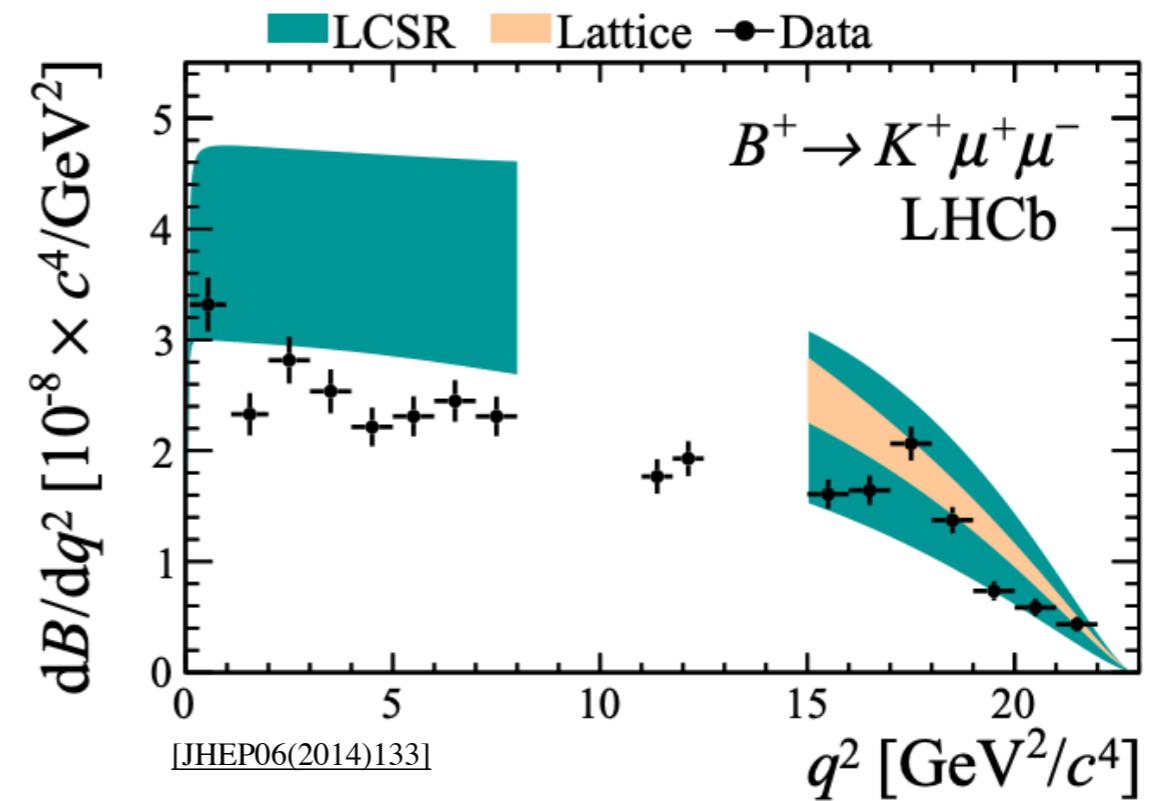
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[Stangl @ La Thuile 2021]

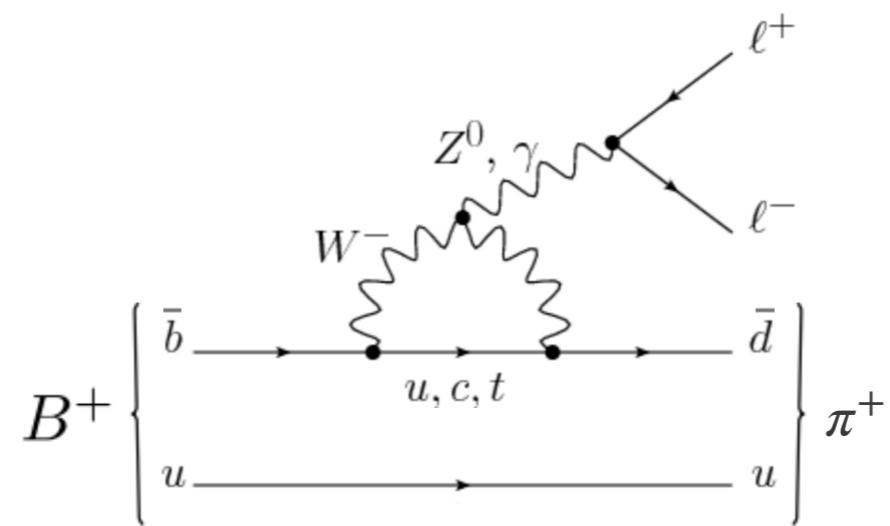
# Flavour anomalies in $b \rightarrow sl^+l^-$ processes

- Flavour anomalies observed consistently in  $b \rightarrow sl^+l^-$  transitions
- Decay rate measurements lower than theory predictions at low  $q^2 (= m_{ll}^2)$ .
- Angular analyses of  $B^0 \rightarrow K^{*0}\mu^+\mu^-$  and  $B^+ \rightarrow K^{*+}\mu^+\mu^-$  measured a combination of angular observables finding a  $\sim 3\sigma$  tension with SM predictions.



# $B^+ \rightarrow \pi^+ \mu^- \mu^+$ decay

$B^+ \rightarrow \pi^+ \mu^- \mu^+$  is a FCNC process not allowed at tree-level in SM

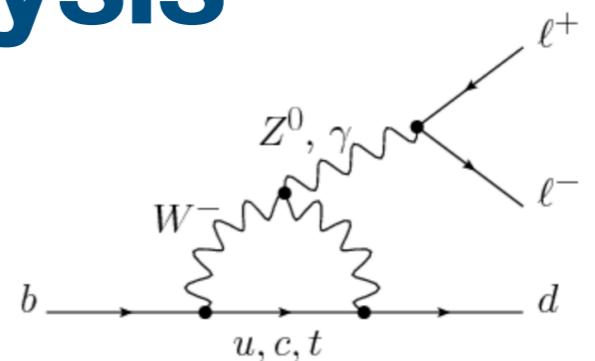


$b \rightarrow d l^+ l^-$  transitions are further CKM-suppressed by  $|V_{tb}/V_{td}|^2$  in the SM

$$\frac{\Gamma(b \rightarrow d l^+ l^-)}{\Gamma(b \rightarrow s l^+ l^-)} \sim \frac{1}{25} \quad [\text{JHEP10(2015)034}]$$

# $B^+ \rightarrow \pi^+ \mu^- \mu^+$ angular analysis

Angular distribution of  $B^+ \rightarrow \pi^+ \mu^- \mu^+$  is:



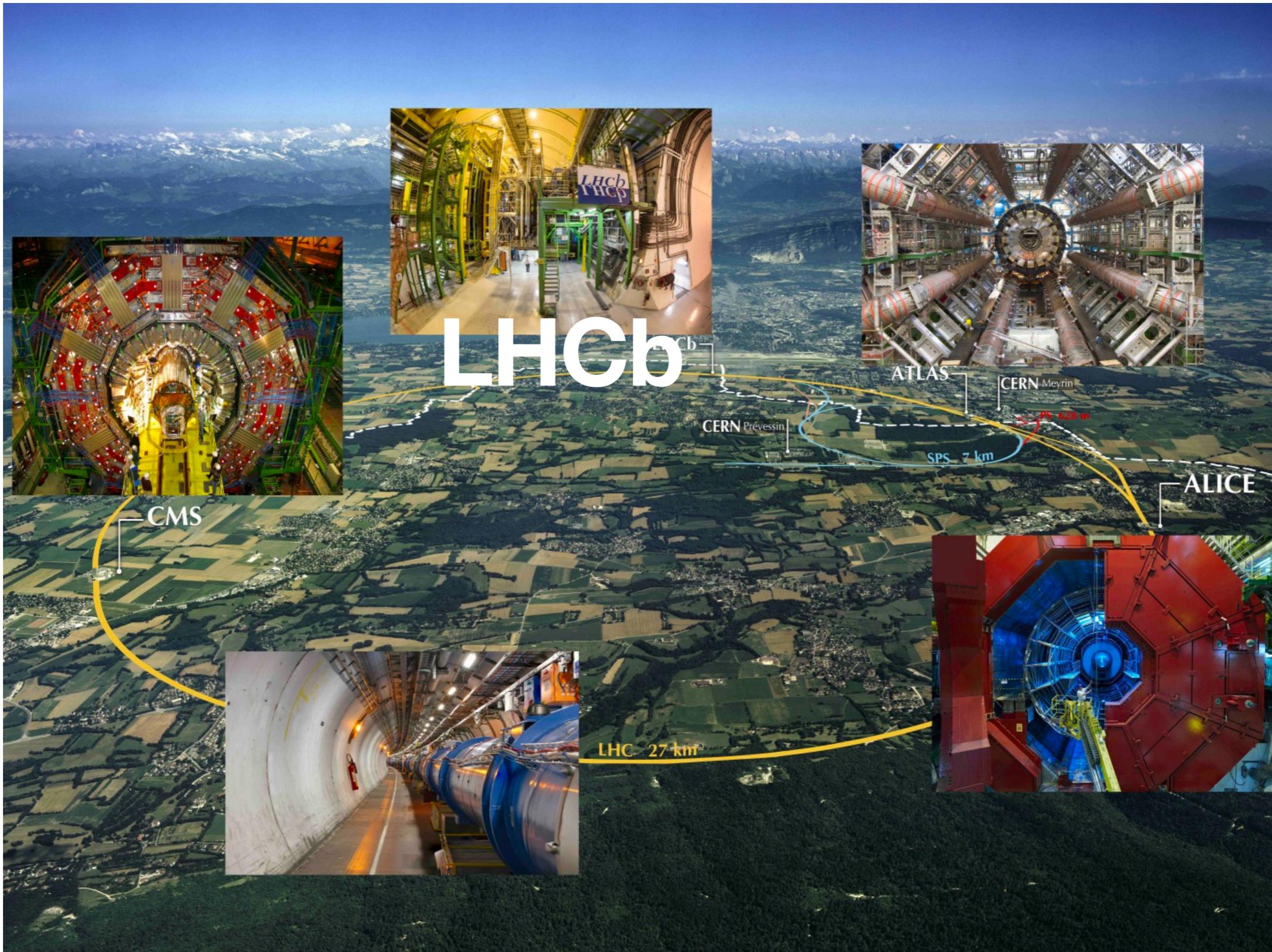
$$\frac{1}{\Gamma} \frac{d\Gamma(B \rightarrow Kl^+l^-)}{d \cos \theta_l} = \frac{3}{4}(1 - F_H)(1 - \cos^2 \theta_l) + \frac{1}{2}F_H + A_{FB} \cos \theta_l$$

- $\theta_l$  = angle between the direction of  $l^+$  and that of  $\pi$  in the  $l^+l^-$  rest-frame
- $F_H$  = the fractional contribution of scalar, pseudo-scalar and tensor amplitudes
- $A_{FB}$  = the forward-backward asymmetry of the dilepton system.

In the SM:  $F_H = 0$  and  $A_{FB} \sim 0$ . [JHEP05(2014)082]

# LHCb Detector

- The detector is a single - arm forward spectrometer at CERN

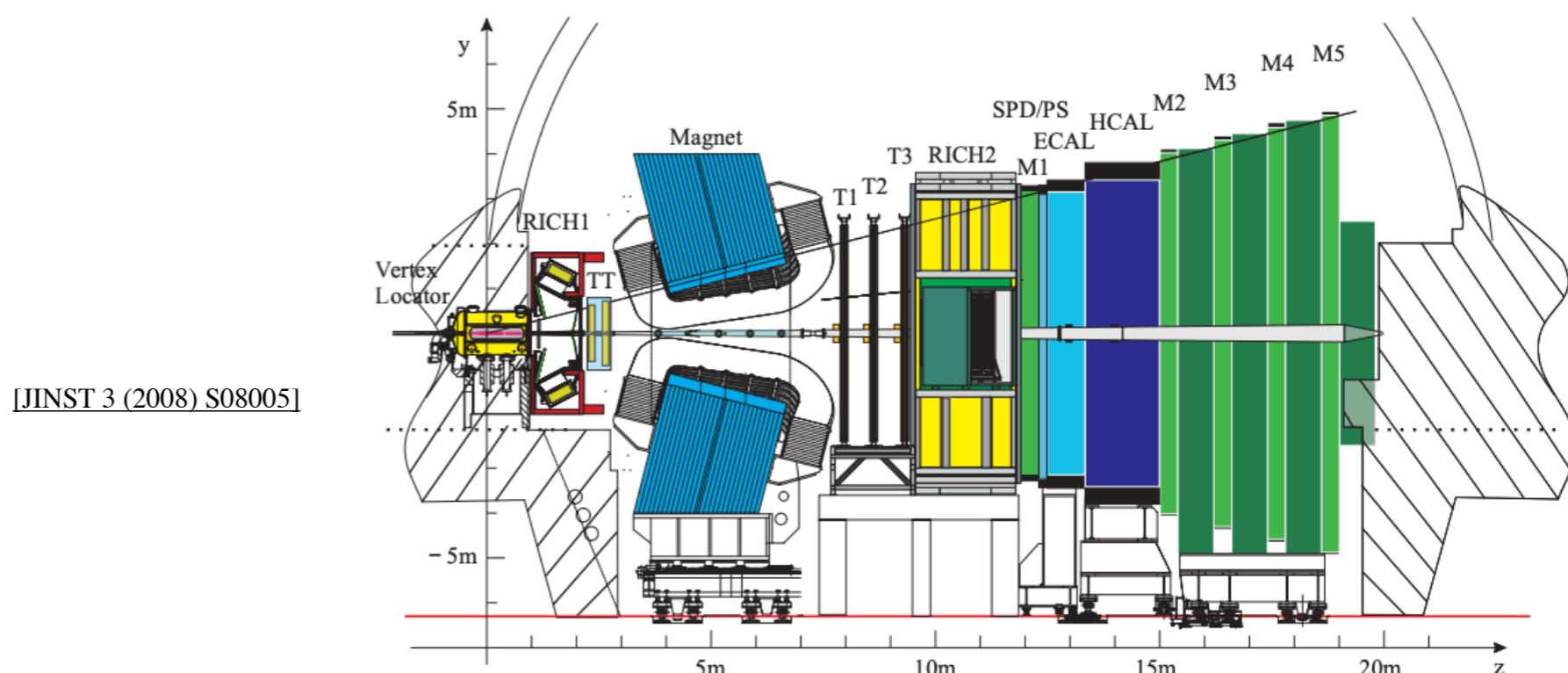
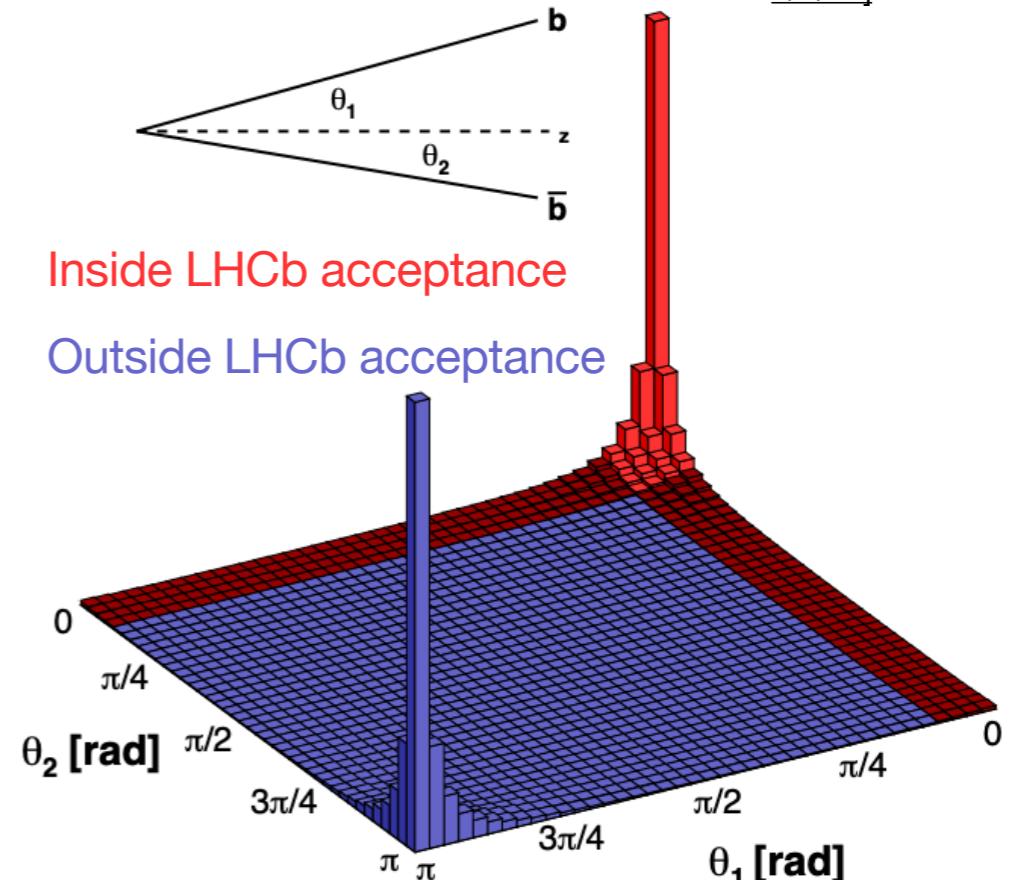


[Image provided by  
CERN]

# LHCb Detector

[ $b\bar{b}$  production plots,  
Elsasser, LHCb Collaboration,  
1/4/21]

- The detector is a single - arm forward spectrometer at CERN
- CoM energy at the LHC of 7, 8 and 13 TeV
- At 13 TeV LHCb provides a  $b\bar{b}$  cross-section production of  $500 \mu b$ , 24 % of pairs inside the detector acceptance



[JINST 3 (2008) S08005]

# LHCb Detector

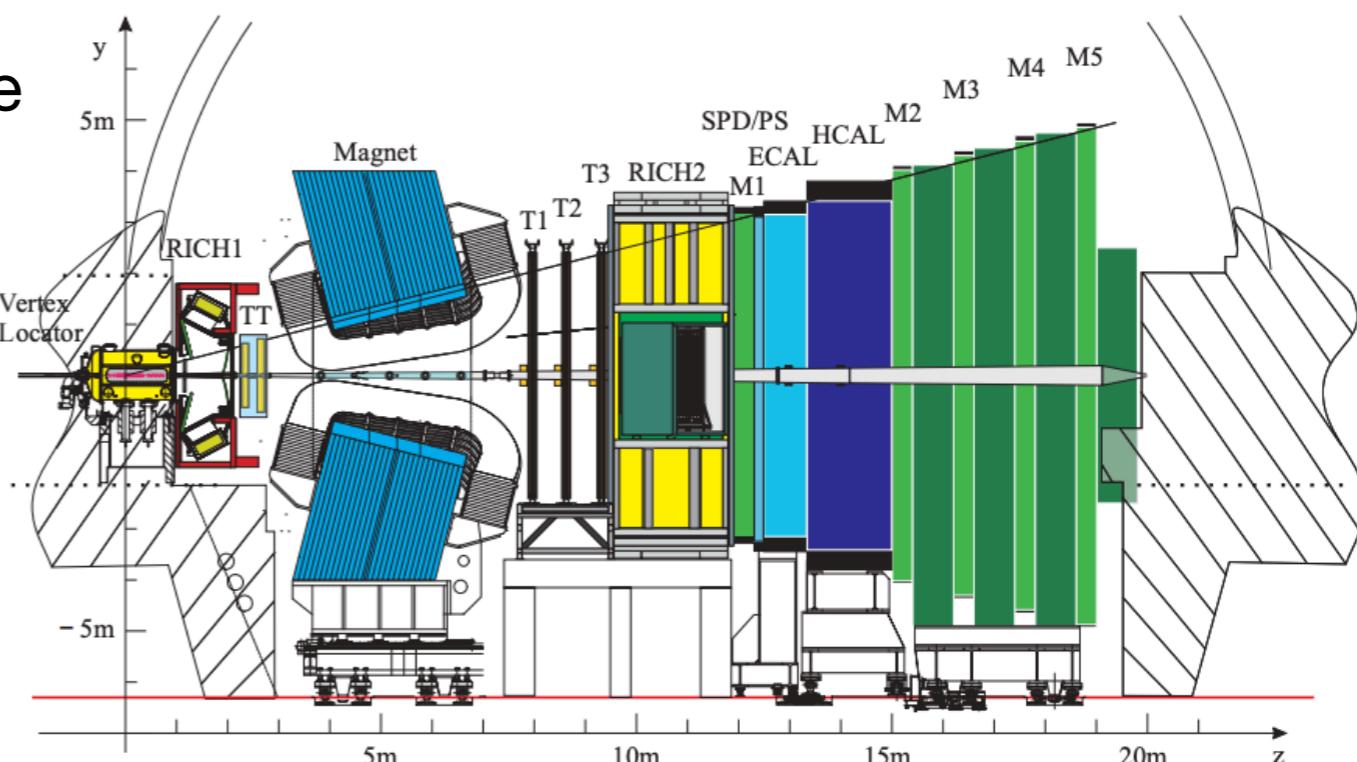
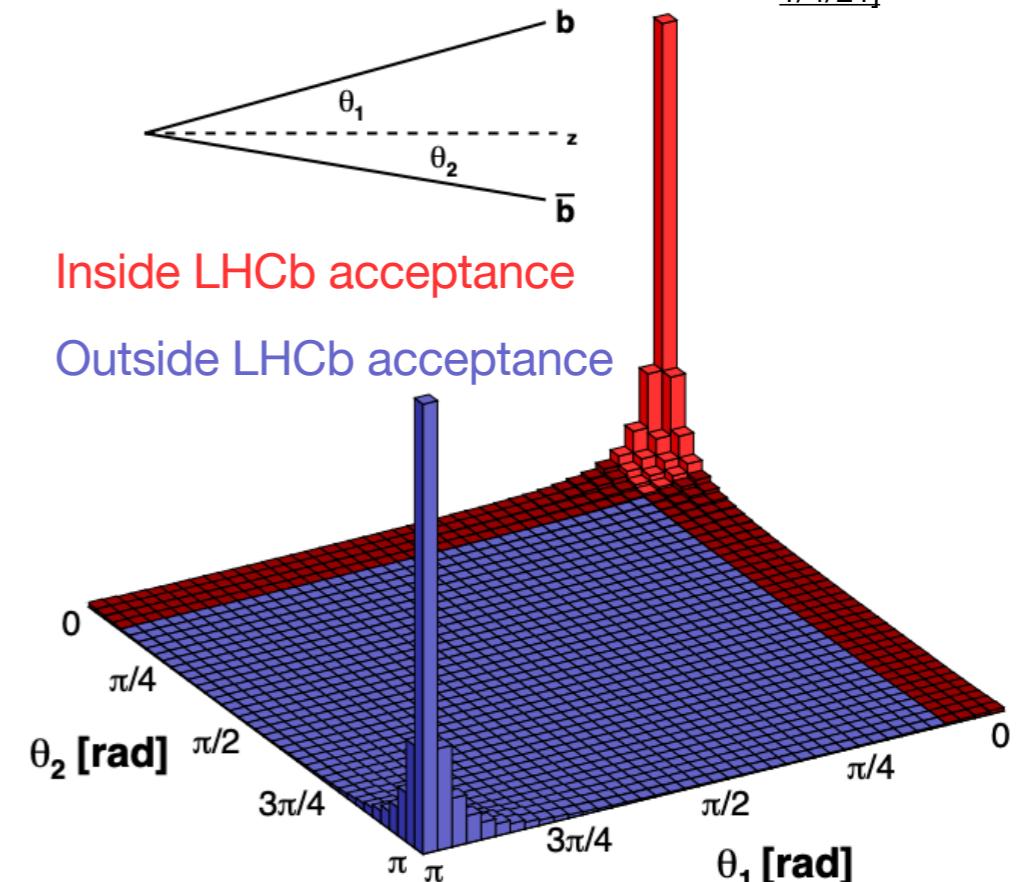
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- CoM energy at the LHC of 7, 8 and 13 TeV
- At 13 TeV LHCb provides a  $b\bar{b}$  cross-section production of  $500 \mu b$ , 24 % of pairs inside the detector acceptance
- Excellent invariant mass  $\sim 22 \text{ MeV}/c^2$  for 2body B decays and vertex  $(15 + 29/\text{pT}[\text{GeV}]) \mu\text{m}$  resolution
- RICH system PID typical performance between 2 and 100  $\text{GeV}/c$ :

$$\epsilon(K \rightarrow K) \sim 95 \%$$

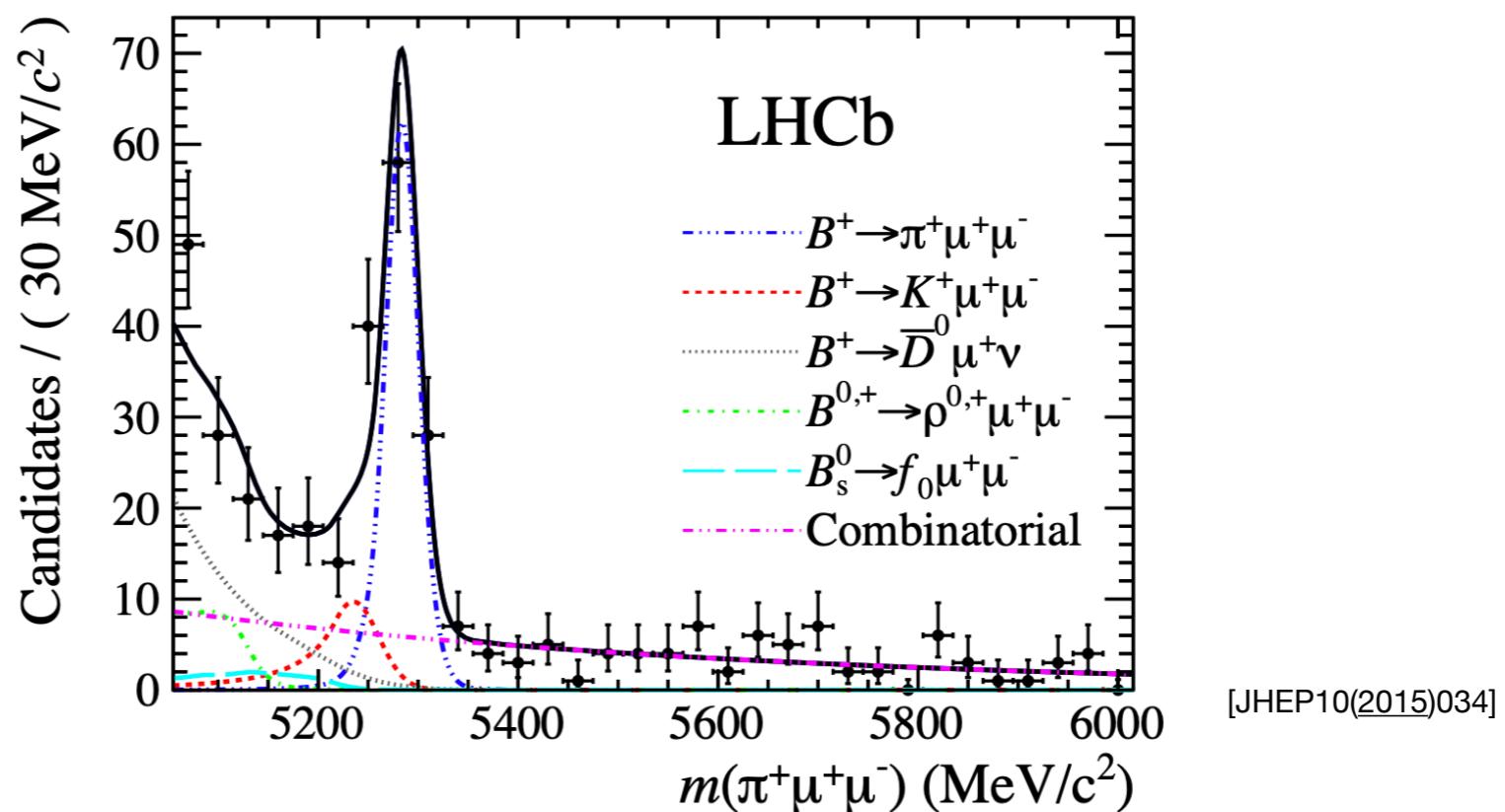
[JINST 3 (2008) S08005]

$$\epsilon(\pi \rightarrow K) \sim 5 \%$$



# $B^+ \rightarrow \pi^+\mu^-\mu^+$ at LHCb

- First measurement: differential branching fraction and CP asymmetry, using LHCb Run I data
- Found 28.8 and 24.1 signal decays for the  $(1.1, 6.0) \text{ GeV}/c^4$  and  $(15.0, 22.0) \text{ GeV}/c^4$   $q^2$  regions



- Differential BF analysis using Run I+II datasets is on the way
  - Expecting 95 and 80 signal decays for the low and high  $q^2$  regions from Run I+II datasets

# Backgrounds

- Combinatorial

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- Partially reconstructed:

$$\bullet \quad B^0 \rightarrow K^{*0} \mu^- \mu^+$$

$$K^{*0} \rightarrow K\pi$$

$$\bullet \quad B^0 \rightarrow \rho \mu^- \mu^+$$

$$\rho \rightarrow \pi\pi$$

$$\bullet \quad B_s^0 \rightarrow f_0 \mu^- \mu^+$$

where:

$$f_0 \rightarrow \pi\pi$$

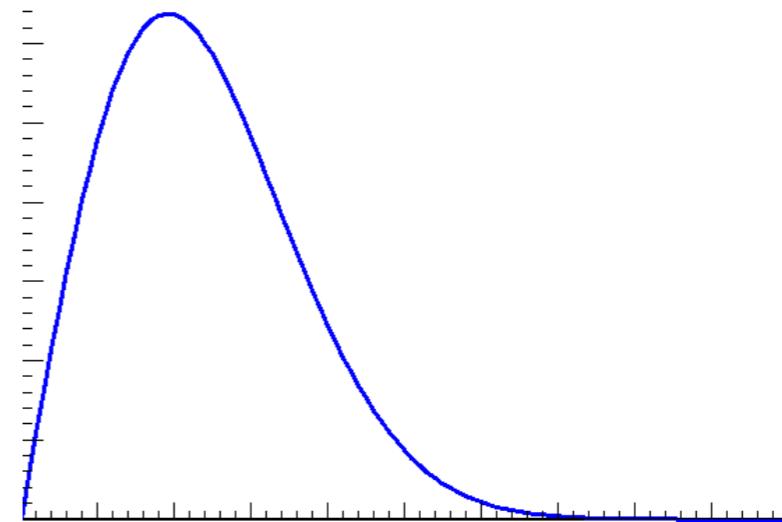
$$\bullet \quad B^+ \rightarrow \rho^+ \mu^- \mu^+$$

$$\rho^+ \rightarrow \pi\pi$$

and a hadron is not reconstructed

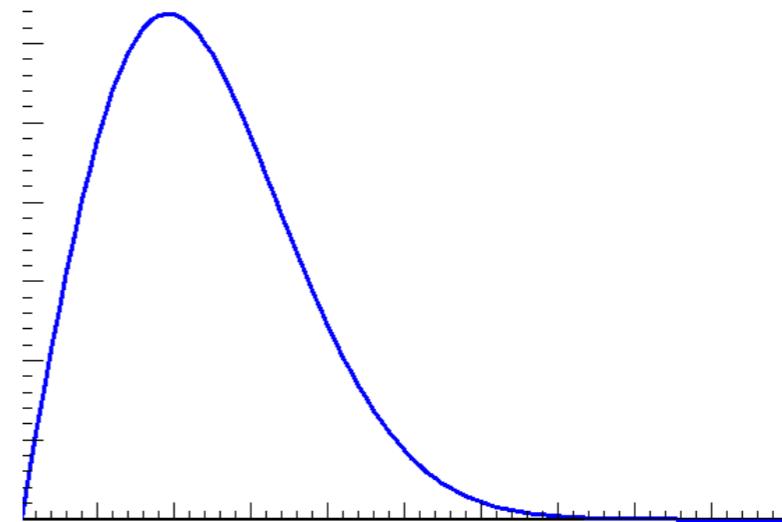
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  - $B_s^0 \rightarrow f_0 \mu^- \mu^+$
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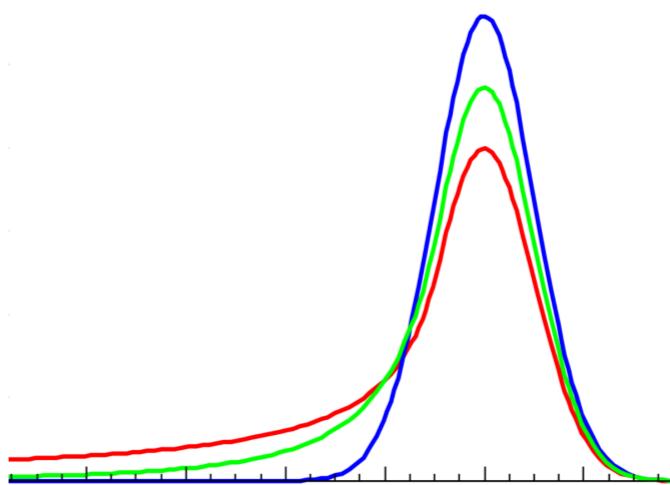
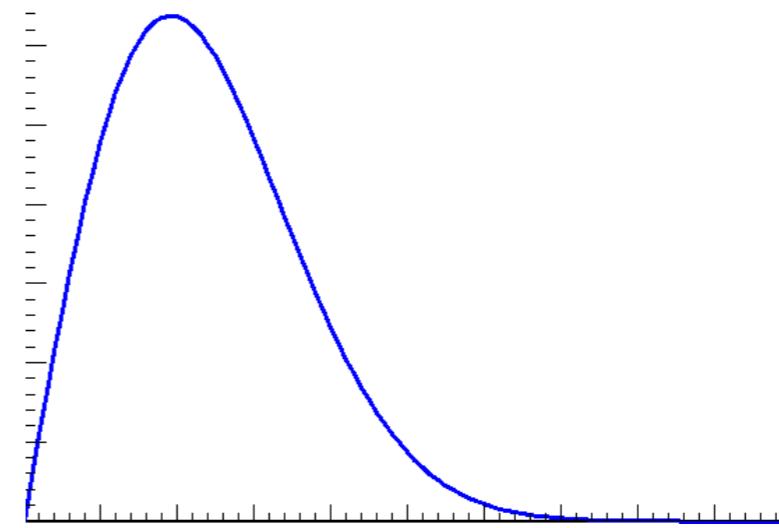
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  - $B^+ \rightarrow \rho^+ \mu^- \mu^+$
- Mis-reconstructed:
  - $B^+ \rightarrow K^+ \mu^- \mu^+$  where  $K^+ \rightarrow \pi^+$  mis-ID takes place



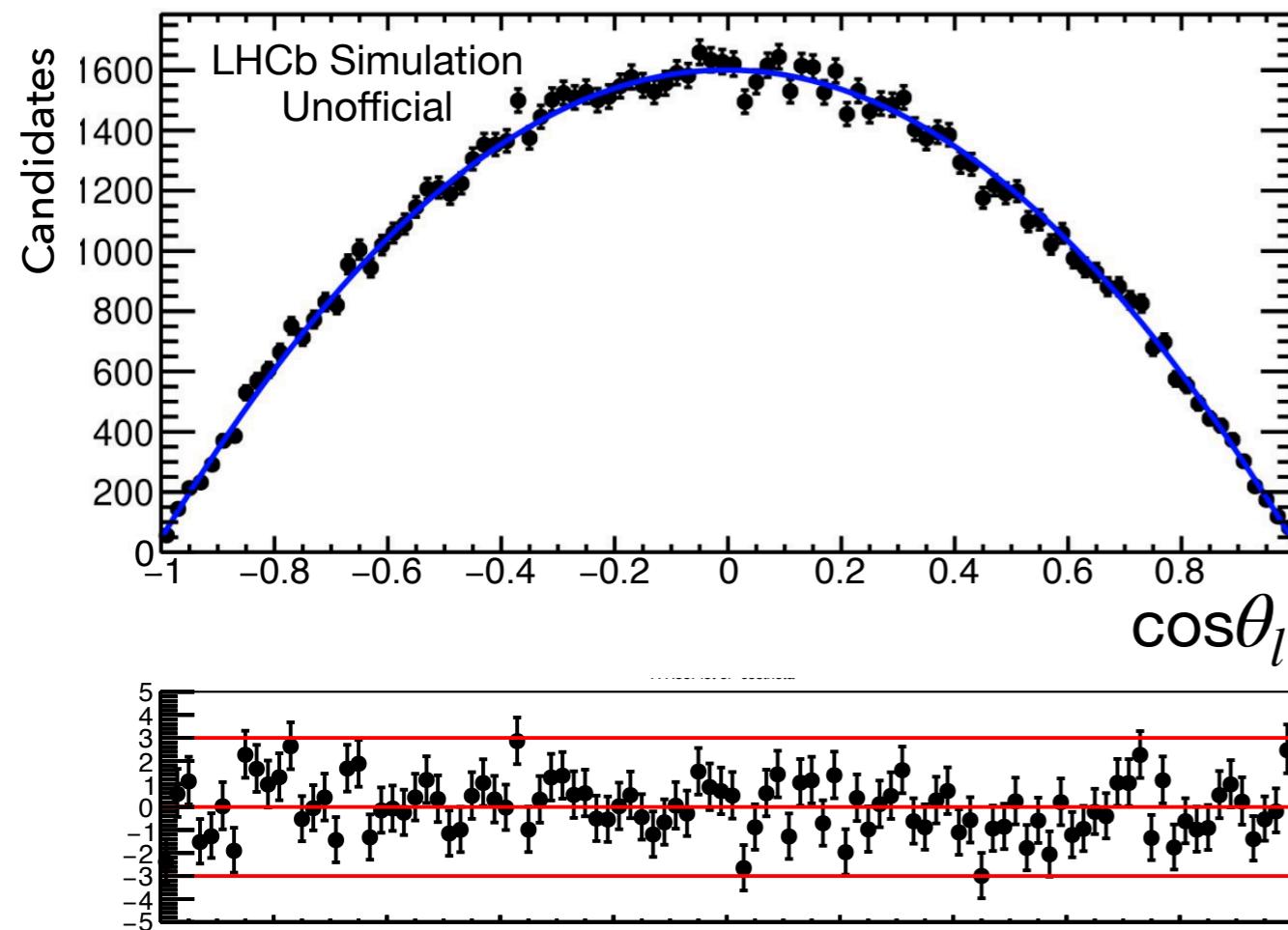
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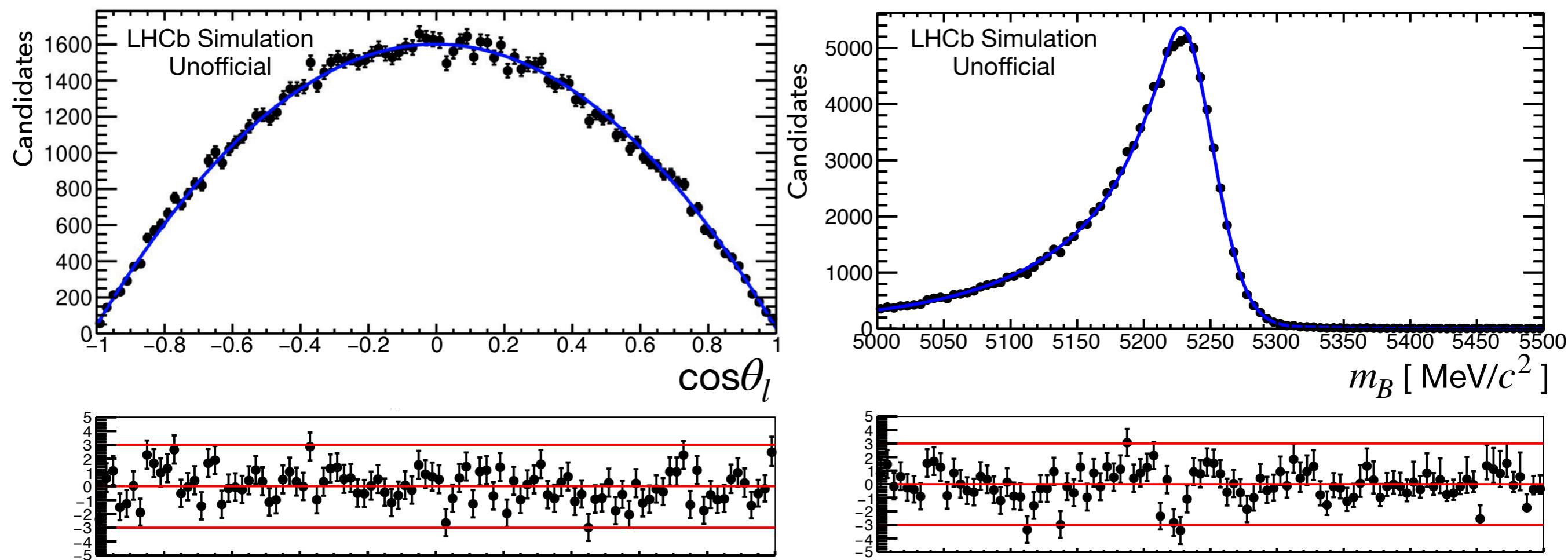
# Mis - reconstructed background

- $B^+ \rightarrow K^+\mu^-\mu^+$  decay where the K is reconstructed as a  $\pi^+$
- Used LHCb simulation data to plot:  $\left\{ \cos\theta_l \text{ in bins of } q^2 \right\} \xrightarrow{\text{Fit}} \text{Chebychev Polynomial}$



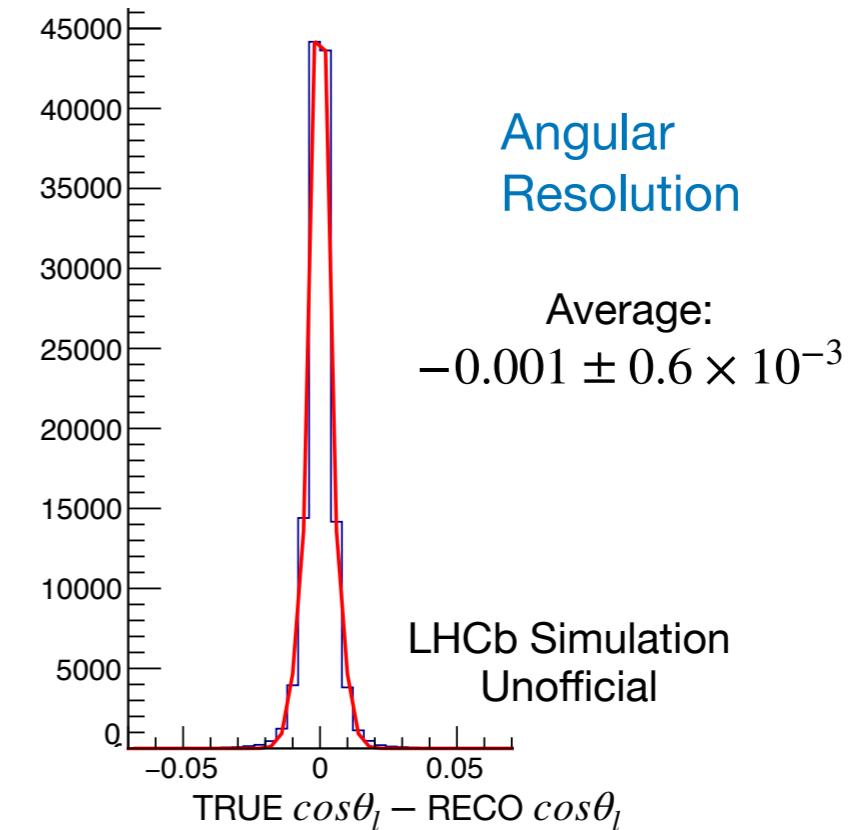
# Mis - reconstructed background

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- Used LHCb simulation data to plot:  
 $\left\{ \begin{array}{l} \cos\theta_l \text{ in bins of } q^2 \\ B_{mass} \end{array} \right. \begin{array}{l} \xrightarrow{\text{Chebychev Polynomial}} \\ \xrightarrow{\text{Fit}} \\ \xrightarrow{\text{Double Crystal Ball}} \end{array}$



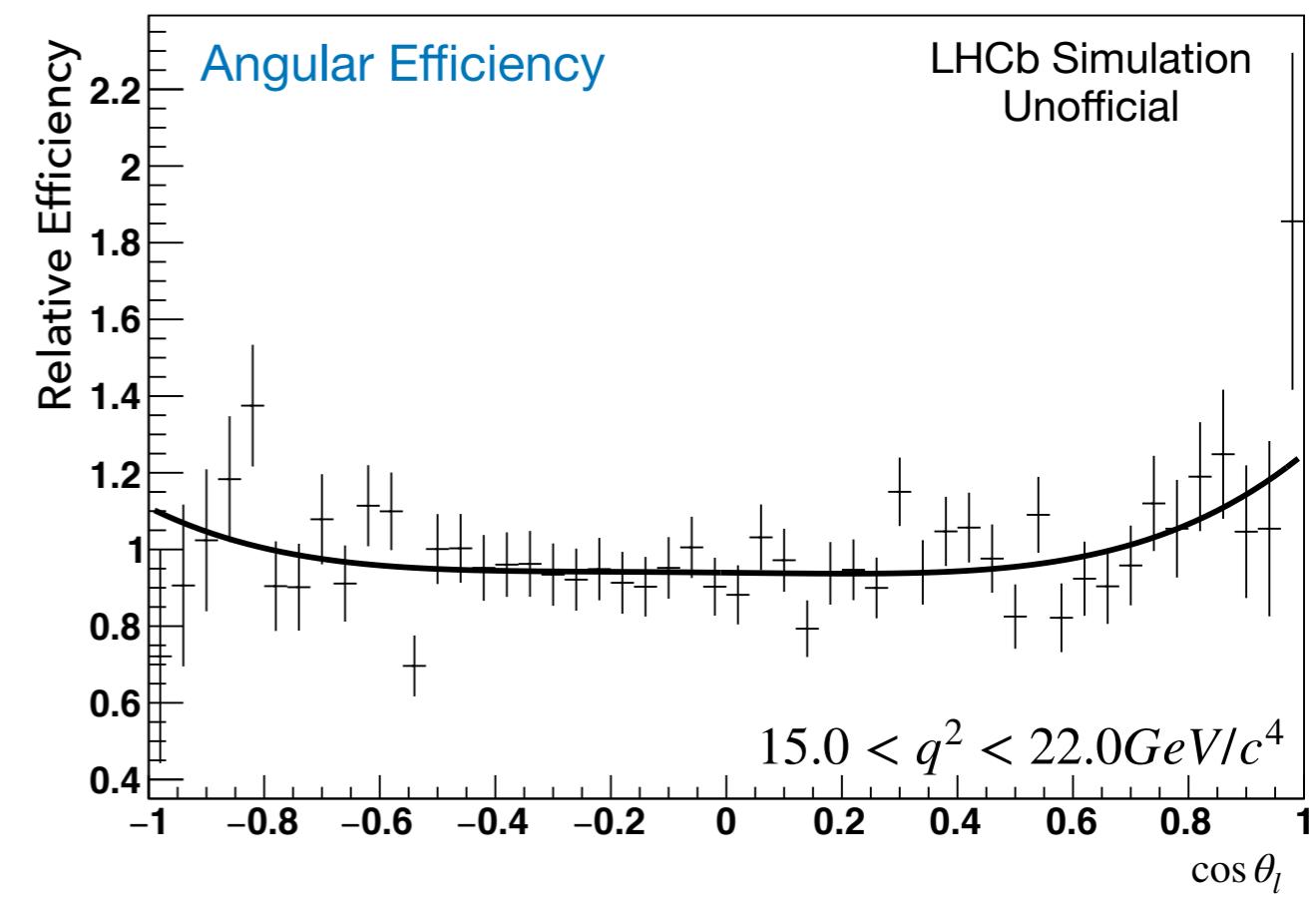
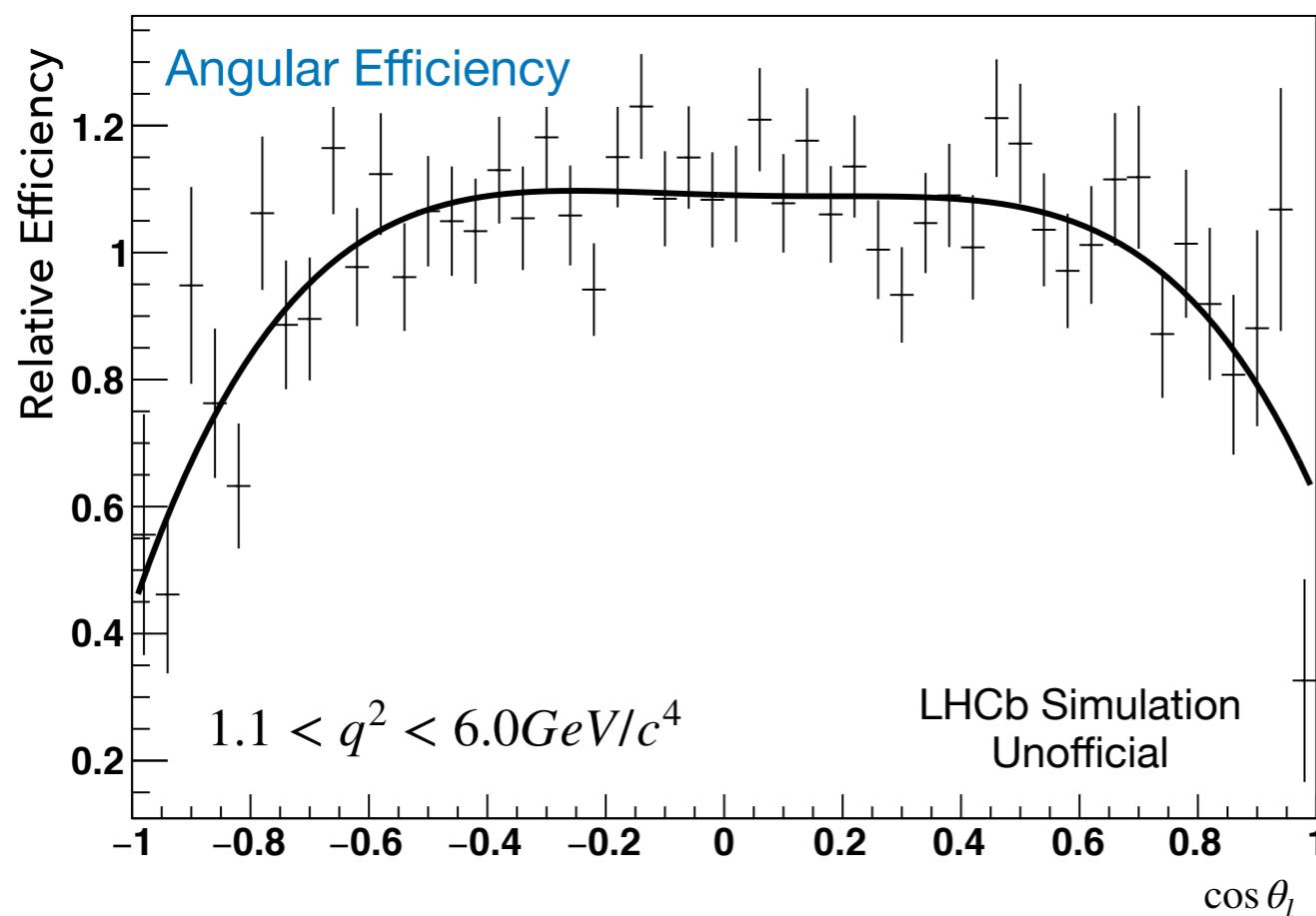
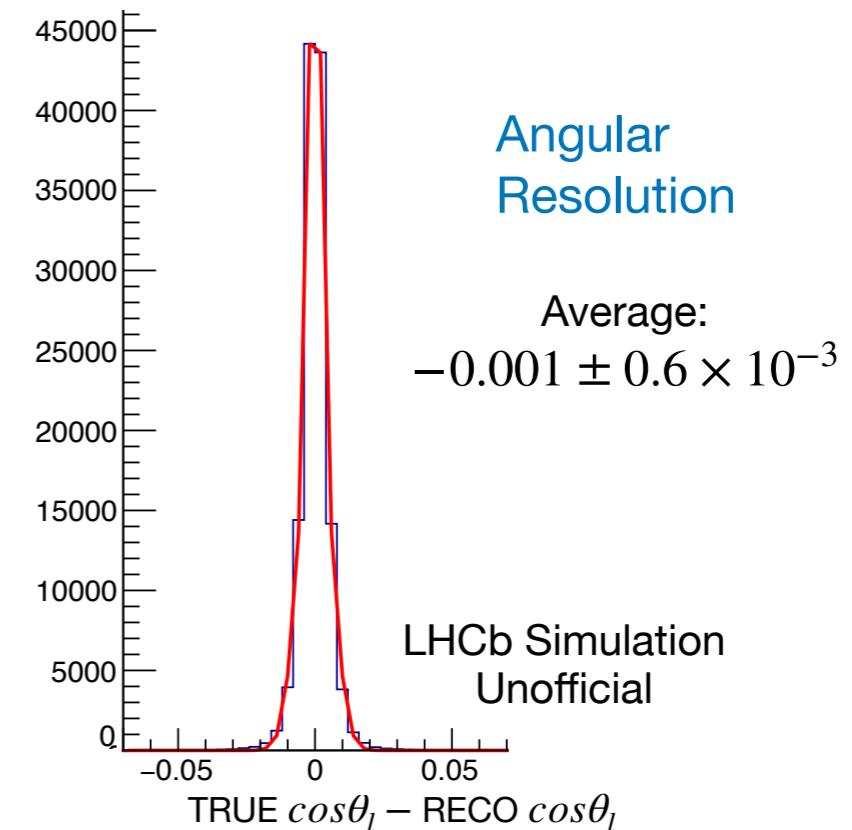
# Angular resolution and efficiency

- Angular resolution and efficiency are measured using LHCb simulation data
- Difference in  $\cos\theta_l$  between true and reconstructed events is small enough for the resolution to be neglected



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# Toy experiments: Profiling log-likelihood

Goal:

Reliably determine  $A_{\text{FB}}$  and  $F_H$

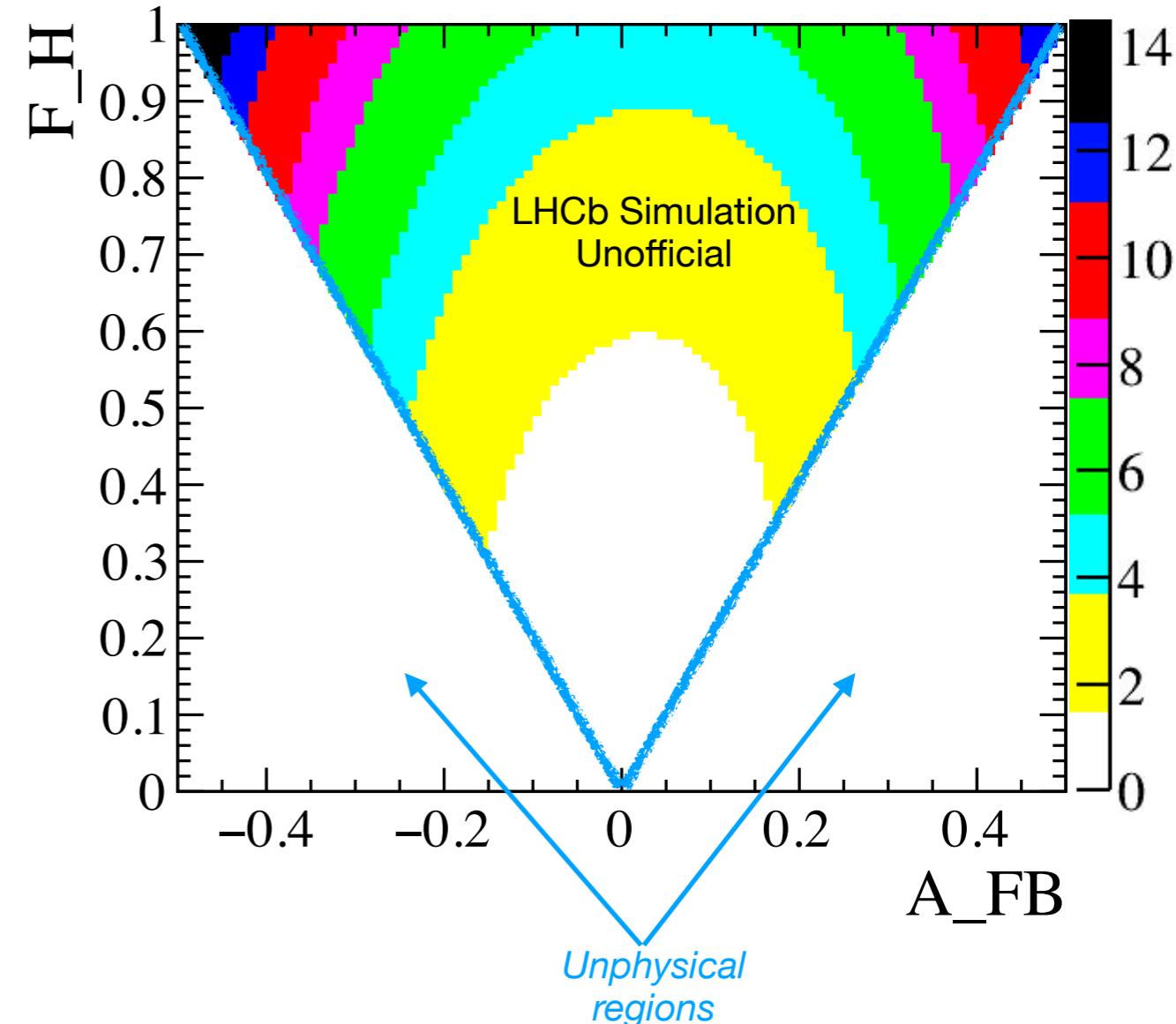
- Toy experiment simulating
  - $B^+ \rightarrow \pi^+ \mu^- \mu^+$  decay signal
  - Angular efficiency
  - Background from mis-reconstructed  $B^+ \rightarrow K^+ \mu^- \mu^+$  decay
- Set the initial values:  
 $A_{\text{FB}} = 0.0, F_H = 0.1$
- 2D Profile of the Negative LogLikelihood function

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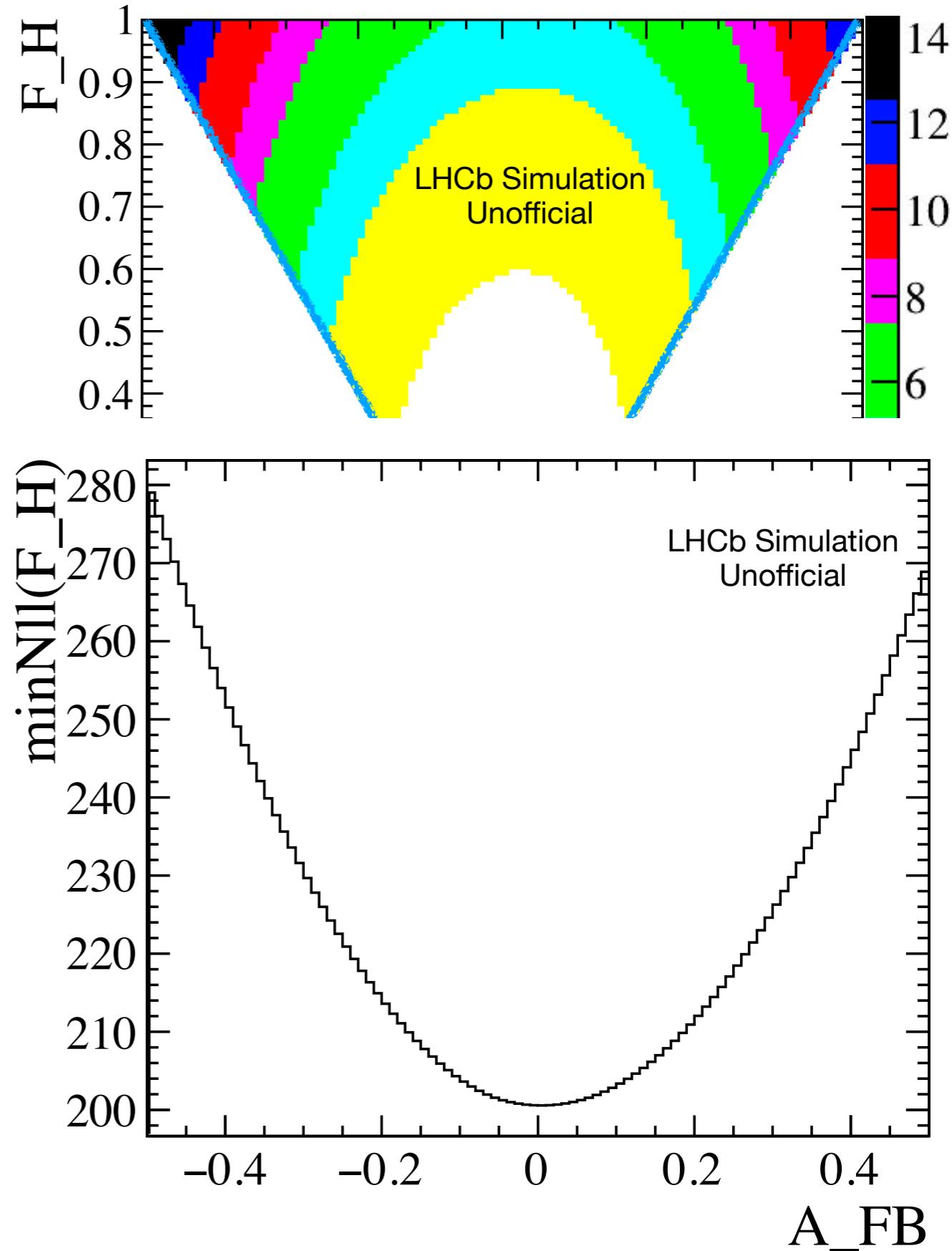


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  - Angular efficiency
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- Set the initial values:  
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- 2D Profile of the Negative LogLikelihood function
- Minimise the  $NLL(F_H)$  for every  $A_{\text{FB}}$

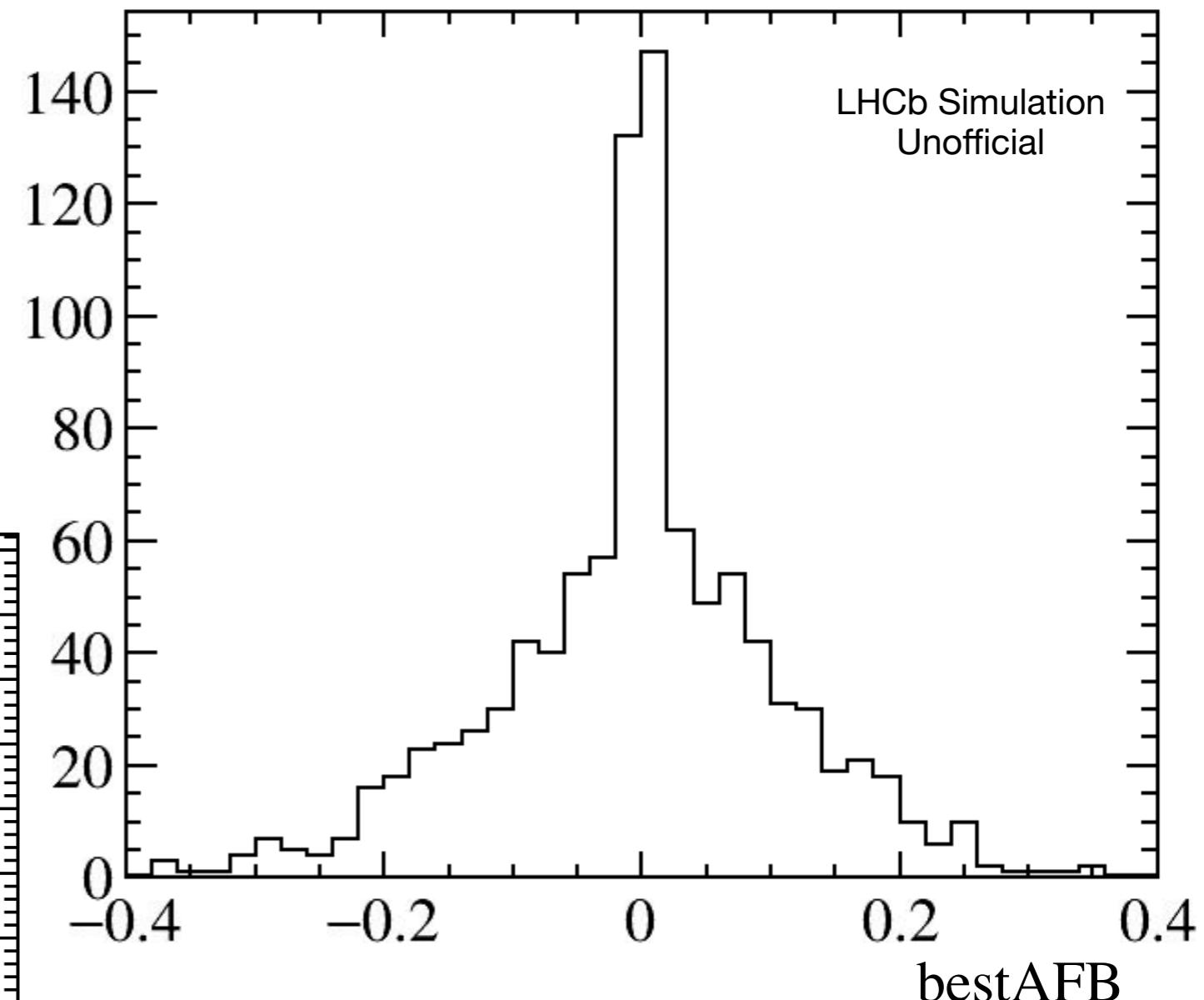
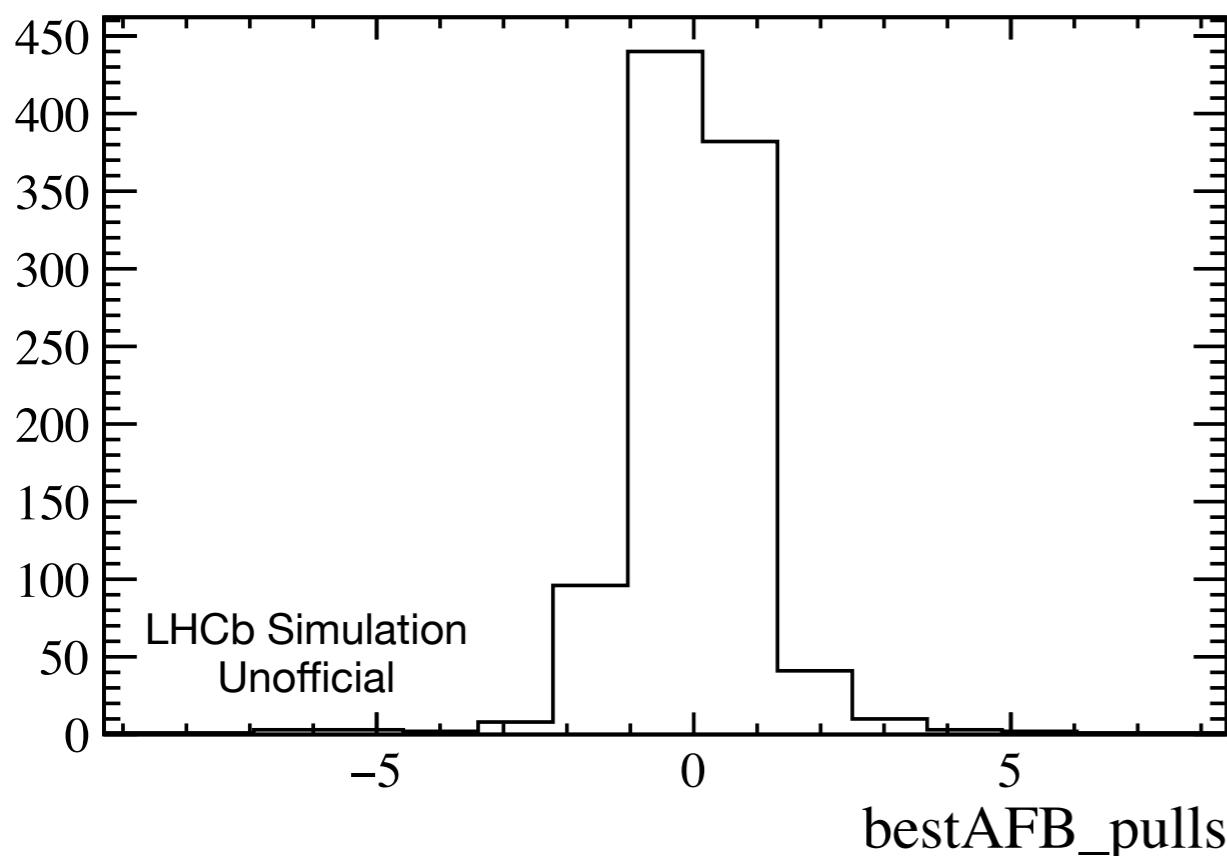


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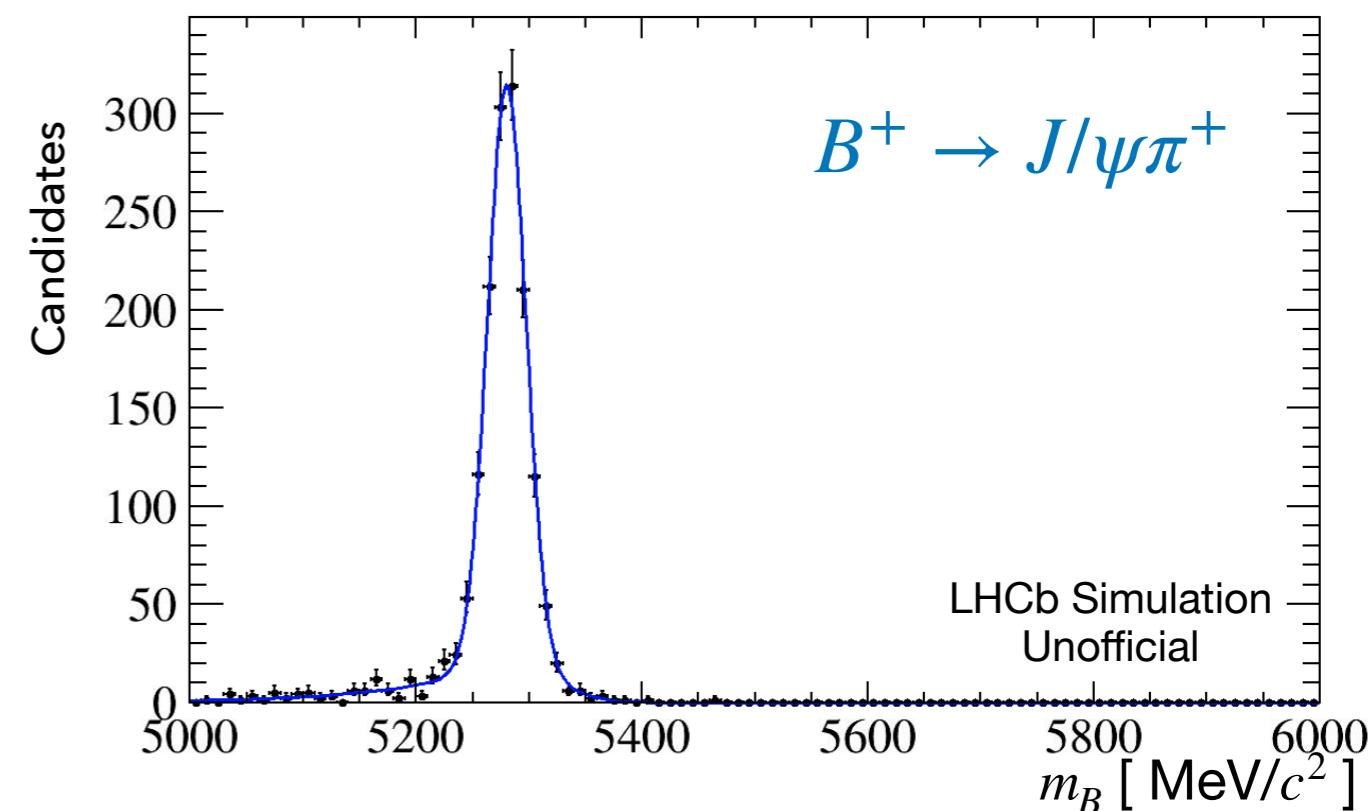
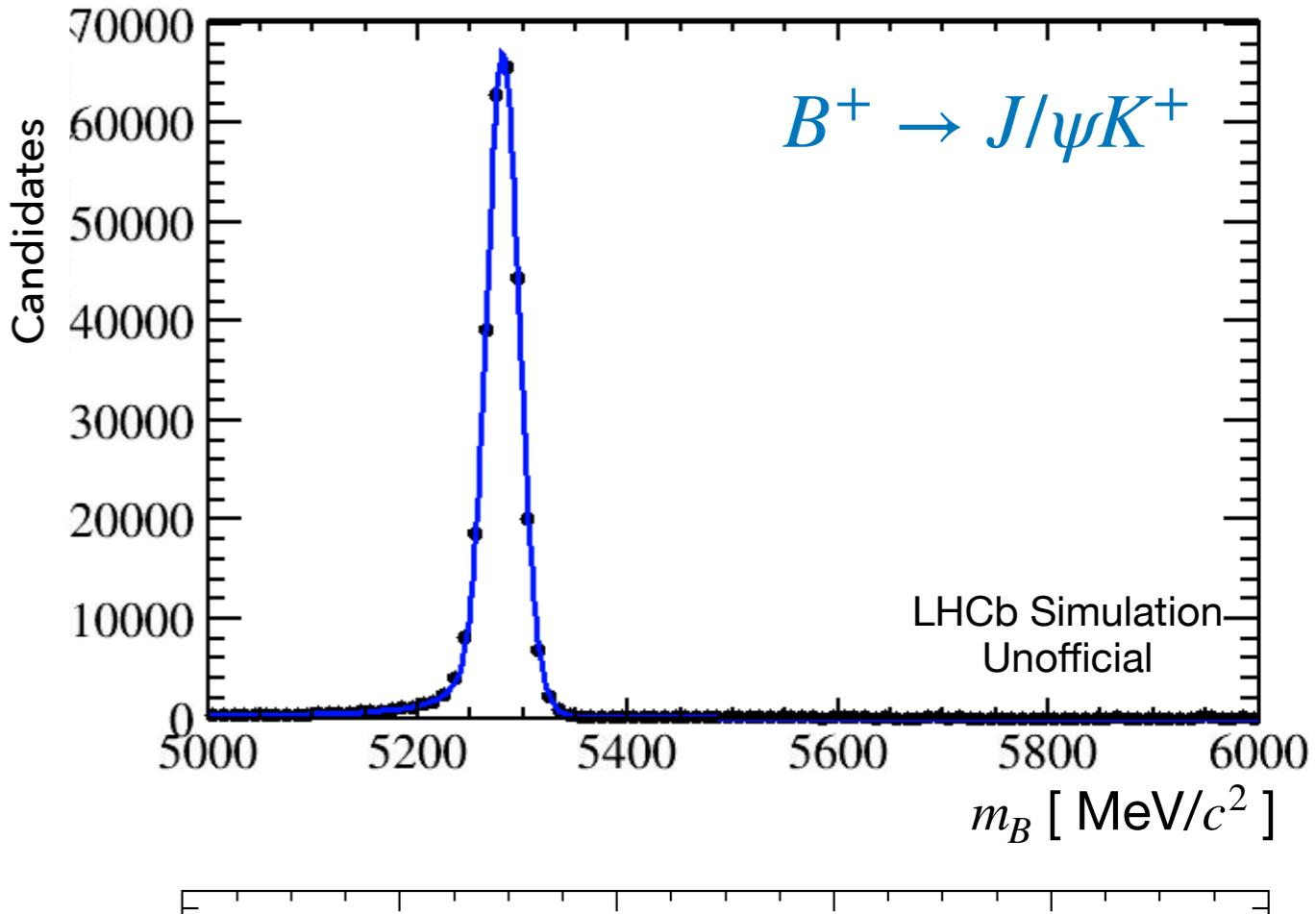
Reliably determine  $A_{\text{FB}}$  and  $F_H$

- Ensemble of 1000 toys,  
initial values:  
 $A_{\text{FB}} = 0.0, F_H = 0.1$
- Results from the toys ensemble:



# Control mode mass fits

- Well measured control modes:  
 $B^+ \rightarrow J/\psi K^+$   
 $B^+ \rightarrow J/\psi \pi^+$
- Mass fit to LHCb simulation data,  
selecting control mode events,  
fitting with a Double Crystal Ball function



# Next steps and Summary

- Conduct a 2D mass and angular fit on the control modes to validate the fit.
- Perform the angular analysis on the rare mode using the Feldman-Cousins method on data from Run I and Run II.
  - This method is preferred for better statistical properties.
- Excellent sensitivity to the SM in  $B^+ \rightarrow \pi^+\mu^-\mu^+$  decay.
- Aim to test the SM with  $b \rightarrow dl^+l^-$  processes as has already been done with  $b \rightarrow sl^+l^-$ .

# Backup slides

# Control mode mass fits

- Well measured control modes are  $B \rightarrow J/\psi K$  and  $B \rightarrow J/\psi \pi$
- Performed a mass fit to LHCb simulation data, selecting  $B \rightarrow J/\psi K$  events and fitting with a Double Crystal Ball function
  - Pass preselection cuts:
    - $B_{\text{PT}}$ ,  $\text{hadron}_{\text{PT}}$ ,  $\mu^-_{\text{PT}}$ ,  
 $\mu^+_{\text{PT}} > 300 \text{ GeV}$
    - $\text{hadron\_isMuonLoose} == 0$
    - $\text{hadron\_InAccMuon} != 0$
  - Pass trigger selection cut
  - Apply mva\_mcweights from MVA conducted by the BF group
  - Apply PIDresampling cuts  
( $\text{ProbNNpi\_resampled} < 0.25 \&& \text{ProbNNK\_resampled} > 0.2$ )
  - Apply BDT to  $> 0.4$  from BF analysis
  - Simulation correction weights applied

