

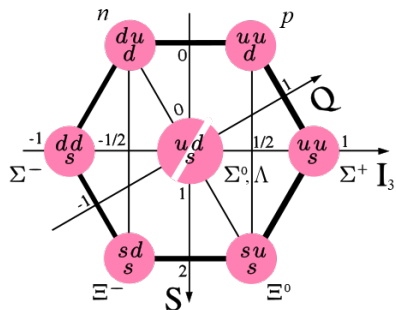
Hyperon Physics at BESIII

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on behalf of the BESIII collaboration

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Pitlochry, Scotland
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Hyperons



+ $\Omega^- (sss)$ Spin $3/2$

Hyperon	Mass [GeV/c ²]	Decay (BF)
Λ	1.116	$p\pi^-$ (63.9%) $n\pi^0$ (35.8%)
Σ^-	1.197	$n\pi^-$ (99.8%)
Σ^+	1.189	$p\pi^0$ (51.6%) $n\pi^+$ (48.3%)
Ξ^0	1.315	$\Lambda\pi^0$ (99.5%)
Ξ^-	1.321	$\Lambda\pi^-$ (99.8%)
Ω	1.672	ΛK^- (67.8%) $\Xi^0\pi^-$ (23.6%) $\Xi^-\pi^0$ (8.6%)

Direct CP-Violation: Hyperon vs. Kaon Decays

To see CPV, need ≥ 2 amplitudes

Kaons:

Isospin amplitudes $\mathcal{A}_{\Delta I=1/2}$ and $\mathcal{A}_{\Delta I=3/2}$

Test direct CPV via $\frac{\mathcal{A}(K_L \rightarrow \pi^0 \pi^0)}{\mathcal{A}(K_S \rightarrow \pi^0 \pi^0)} \equiv \epsilon - 2\epsilon'$, $\frac{\mathcal{A}(K_L \rightarrow \pi^+ \pi^-)}{\mathcal{A}(K_S \rightarrow \pi^+ \pi^-)} \equiv \epsilon + \epsilon'$

Hyperons:

Two amplitudes S , P even for $\Delta I = 1/2$:

$$\mathcal{A} = S + P \sigma \cdot \hat{n}$$

Strong phases

$$S = |S| \exp(i\xi_S) \exp(i\delta_S)$$

$$P = |P| \exp(i\xi_P) \exp(i\delta_P)$$

Weak CP-odd phases

Two Measurable Parameters

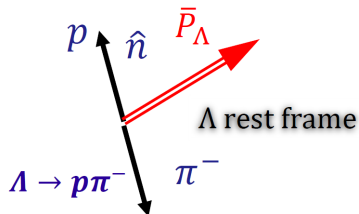
$$\alpha = \frac{2\text{Re}(S^* P)}{|S|^2 + |P|^2}$$

$$\beta = \frac{2\text{Im}(S^* P)}{|S|^2 + |P|^2}$$

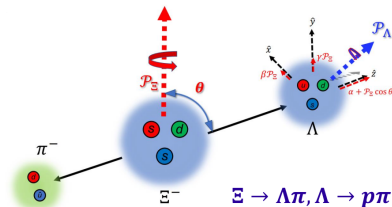
$$= \sqrt{1 - \alpha^2} \sin \phi$$

Methods in Hyperon Decays

$$\frac{d\Gamma}{d\Omega} = \frac{1}{4\pi}(1 + \alpha_\Lambda \hat{n} \bar{P}_\Lambda)$$



Experimentally, ϕ accessible when polarization of mother and daughter hyperon measured.



$$\beta = \sqrt{1 - \alpha^2} \sin \phi$$

CP Tests in Hyperon Decays

If CP conserved: $\bar{\alpha} = -\alpha$, $\bar{\beta} = -\beta$ (Experimentally $\bar{\phi} = -\phi$)

CP-tests: $A_{CP} = \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}}$, $B_{CP} = \frac{\beta + \bar{\beta}}{\alpha - \bar{\alpha}} = (\xi_P - \xi_S)$

SM prediction¹:

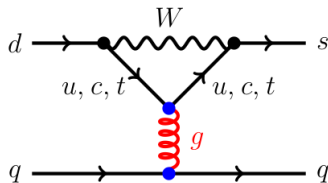
$$-3 \times 10^{-5} \leq A_{\Lambda} \leq 4 \times 10^{-5}$$

$$-2 \times 10^{-5} \leq A_{\Xi} \leq 1 \times 10^{-5}$$

Decay mode	$\xi_S - \xi_P$ (10^{-4} rad.)
$\Lambda \rightarrow p\pi^-$	0.3 ± 2.2
$\Xi \rightarrow \Lambda\pi^-$	-1.9 ± 1.6

HyperCP measurement²:

$$A_{CP}^{\Xi} + A_{CP}^{\Lambda} = 0(5)(4) \times 10^{-4}$$



$$(\xi_P - \xi_S)_{BSM} = \frac{C'_B}{B_G} \left(\frac{\epsilon'}{\epsilon} \right)_{BSM} + \frac{C_B}{\kappa} \epsilon_{BSM}$$

$0.5 < B_G < 2$ and $0.2 < |\kappa| < 1^3$

Decay	C_B	C'_B
$\Lambda \rightarrow p\pi^-$	1.1 ± 2.2	0.4 ± 0.8
$\Xi \rightarrow \Lambda\pi^-$	-0.5 ± 1.0	0.4 ± 0.7

¹Tandean, Valencia PRD67 (2003) 056001

²PRL 93 (2004) 262001

³Tandean, PRD69 (2004) 076008

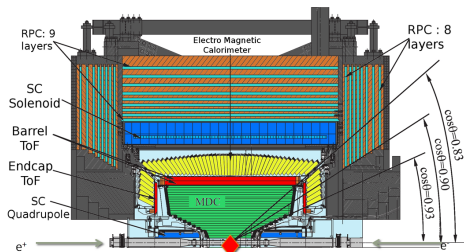
BESIII at BEPCII

Beijing Electron-Positron Collider (BEPCII)

- CMS Energy from 2 to 4.95 GeV/c²
- Design luminosity 10³³ cm⁻²s⁻¹

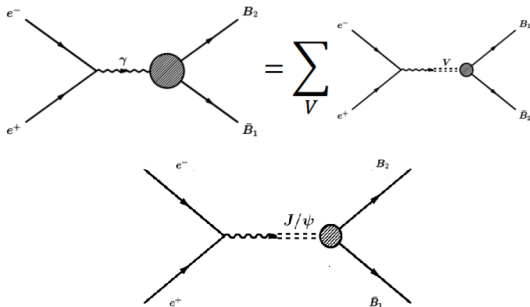
Beijing Spectrometer (BESIII)

- Near 4 π coverage
- Helium-gas drift chamber
- CsI(Tl) crystal calorimeter
- Plastic scintillator TOF-system (endcaps upgraded to MRPC in 2015)
- 1 T super-conducting solenoid
- RPC-based muon chamber
- World's largest datasets at:
 - J/ψ : 10B events
 - $\psi(2S)$: 3B events(here results from 0.4B)



Decay	\mathcal{B} (10^{-5})	Events at BESIII
$J/\psi \rightarrow \Lambda\bar{\Lambda}$	189 ± 9	18.9×10^6
$J/\psi \rightarrow \Sigma^+\bar{\Sigma}^-$	150 ± 24	15.0×10^6
$J/\psi \rightarrow \Xi\bar{\Xi}$	97 ± 8	9.7×10^6
$\psi(2S) \rightarrow \Sigma\bar{\Sigma}$	23.2 ± 1.2	696×10^3
$\psi(2S) \rightarrow \Omega\bar{\Omega}$	5.66 ± 0.30	170×10^3

$$e^+e^- \rightarrow \gamma^* \rightarrow B\bar{B}$$



Both processes described by two complex form factors.
 Ratio of FFs: α_ψ
 Relative phase: $\Delta\Phi$

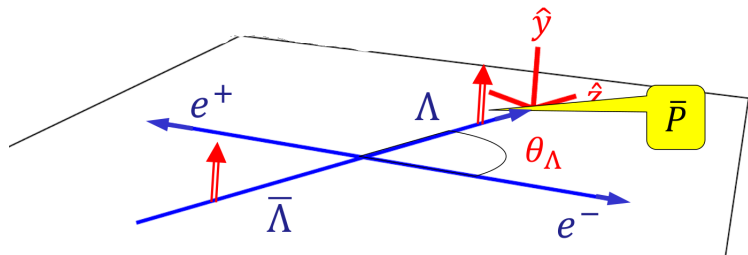
Timelike spin-1/2 EM FFs

Dubnickova, Dubnicka, Rekalov Nuovo Cim. A109 (1996) 241
 Gakh, Tomasi-Gustafsson Nucl.Phys. A771 (2006) 169
 Czyz, Grzelinska, Kuhn PRD75 (2007) 074026
 Fäldt EPJ A51 (2015) 74; EPJ A52 (2016)141

Charmonium decays:

Fäldt, Kupsc, PLB 772 (2017) 16

$B\bar{B}$ Production in e^+e^- -Annihilation



Unpolarized e^+e^- beams \rightarrow Transverse polarization:

$$P_y(\cos \theta_\Lambda) = \frac{\sqrt{1-\alpha_\psi^2} \cos \theta_\Lambda \sin \theta_\Lambda}{1+\alpha_\psi \cos^2 \theta_\Lambda} \sin(\Delta\Phi)$$

Angular distribution: $\frac{d\Gamma}{d\Omega} \propto 1 + \alpha_\psi \cos^2 \theta_\Lambda$, $-1 \leq \alpha_\psi \leq 1$

$B\bar{B}$ Production in e^+e^- -Annihilation: Modular Description

Two spin 1/2 particle state:

$$\rho_{1/2,1/2} = \frac{1}{4} \sum_{\mu\bar{\nu}} C_{\mu\bar{\nu}} \sigma_{\mu}^{\Lambda} \otimes \sigma_{\bar{\nu}}^{\bar{\Lambda}}$$

$$C_{\mu\bar{\nu}} = \begin{pmatrix} 1 + \alpha_{\psi} \cos^2 \theta & 0 & \beta_{\psi} \sin \theta \cos \theta & 0 \\ 0 & \sin^2 \theta & 0 & \gamma_{\psi} \sin \theta \cos \theta \\ -\beta_{\psi} \sin \theta \cos \theta & 0 & \alpha_{\psi} \sin^2 \theta & 0 \\ 0 & -\gamma_{\psi} \sin \theta \cos \theta & 0 & -\alpha_{\psi} - \cos^2 \theta \end{pmatrix}$$

Spin correlations

$$\beta_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \sin(\Delta\Phi) \quad \gamma_{\psi} = \sqrt{1 - \alpha_{\psi}^2} \cos(\Delta\Phi)$$

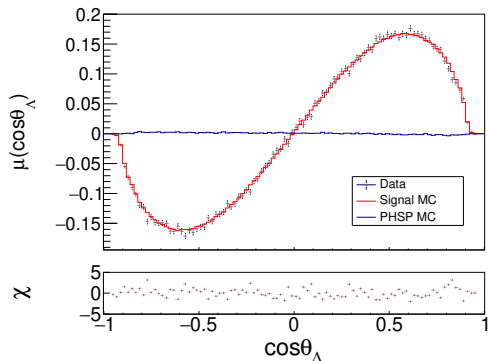
Include decay via decay matrices:

$$\sigma_{\mu}^{\Lambda} \rightarrow \sum_{\mu'=0}^3 a_{\mu,\mu'}^{\Lambda} \sigma_{\mu'}^p$$

Full angular distribution:

$$W = \text{Tr} \rho_{p,\bar{p}} = \sum_{\mu,\bar{\nu}=0}^3 C_{\mu\bar{\nu}} a_{\mu,0}^{\Lambda} a_{\bar{\nu},0}^{\bar{\Lambda}}$$

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}, \Lambda \rightarrow p\pi^- + c.c.$$



(Based on 10^{10} J/ψ events)

Exclusive analysis. 3.2M events (3801 background)

BESIII

BESIII, *arxiv:2204.11058,
BESIII, **Nature Phys. 15 (2019) 631

Par.	This Work*	Previous results **	PDG 2018 ***
$\alpha_{J/\psi}$	$0.4748 \pm 0.0022 \pm 0.0024$	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027
$\Delta\Phi$	$0.7521 \pm 0.0042 \pm 0.0080$	$0.740 \pm 0.010 \pm 0.009$	-
α_-	$0.7519 \pm 0.0036 \pm 0.0019$	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013
α_+	$-0.7559 \pm 0.0036 \pm 0.0029$	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08
A_{CP}	$-0.0025 \pm 0.0046 \pm 0.0011$	$0.006 \pm 0.012 \pm 0.007$	-
$\alpha_{\pm, avg.}$	$0.7542 \pm 0.0010 \pm 0.0020$	$0.754 \pm 0.003 \pm 0.002$	-

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}, \Lambda \rightarrow p\pi^- + c.c.$$

$$A_{CP} = \frac{\alpha_\Lambda + \alpha_{\bar{\Lambda}}}{\alpha_\Lambda - \alpha_{\bar{\Lambda}}} = -0.0025 \pm 0.0046 \pm 0.0011$$

$$\text{PS185: } A_\Lambda = 0.013 \pm 0.021$$

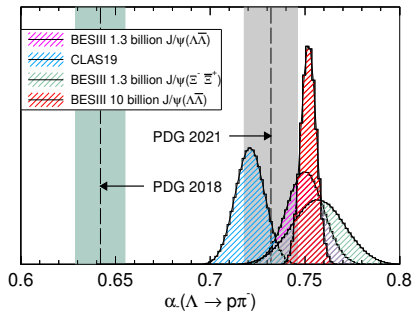
PRC54(96)1877

$$\langle \alpha \rangle = \frac{\alpha_\Lambda - \alpha_{\bar{\Lambda}}}{2} = 0.7542 \pm 0.0010 \pm 0.0020$$

$$\text{CLAS: } \alpha_\Lambda = 0.721 \pm 0.006 \pm 0.005$$

PRL 123 (2019) 182301

Data on $\Lambda_b \rightarrow J/\psi\Lambda$ favor new value
LHCb, JHEP 06 (2020) 110

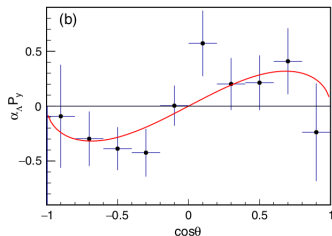


$e^+e^- \rightarrow \Lambda\bar{\Lambda}, \Lambda \rightarrow p\pi^- + c.c.$

2.396 GeV

Exclusive analysis.

$\alpha_\Lambda = -\alpha_{\bar{\Lambda}} = 0.750$ fixed



555 events (2.5% bkg)

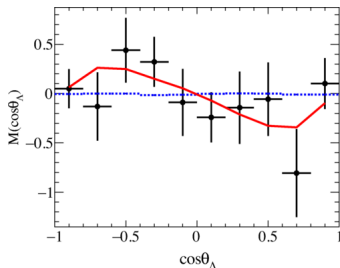
$R = |G_E/G_M| = 0.96 \pm 0.14 \pm 0.02$

$\Delta\Phi = 37 \pm 12 \pm 6^\circ$

3.773 GeV

Exclusive analysis.

$\alpha_\Lambda = -\alpha_{\bar{\Lambda}} = 0.754$ fixed



262 events (0.5% bkg)

$\alpha_\Psi = 0.85^{+0.12}_{-0.20} \pm 0.02$

$R_\Psi = 0.48^{+0.21}_{-0.35} \pm 0.03$

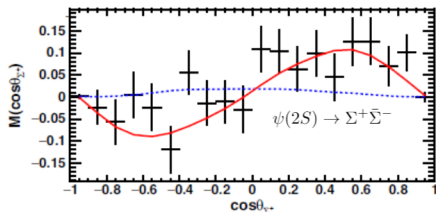
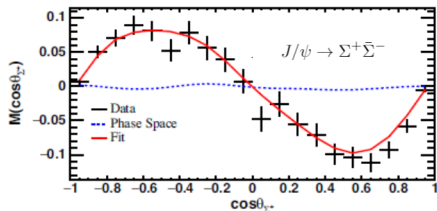
$\Delta\Phi = 71^{+66}_{-46} \pm 5^\circ$

BESIII

$e^+e^- \rightarrow J/\psi, \psi(2S) \rightarrow \Sigma^+\bar{\Sigma}^-, \Sigma^+ \rightarrow p\pi^0 + c.c.$

Based on 1.31×10^9 J/ψ events, and 0.5×10^9 $\psi(2S)$ events.

Plots acceptance uncorrected



87k events (5% bkg)

$$\alpha_{J/\psi} = -0.507 \pm 0.006 \pm 0.002$$

$$\Delta\Phi(J/\psi) = (-15.4 \pm 0.7 \pm 0.3)^\circ$$

$$\langle \alpha \rangle = (\alpha - \bar{\alpha})/2 = -0.994 \pm 0.004 \pm 0.002$$

$$A_{CP} = -0.004 \pm 0.037 \pm 0.010$$

$$\text{c.f. SM prediction } A_{CP} \sim 3.6 \times 10^{-6}$$

5k events (1% bkg)

$$\alpha_\psi = 0.676 \pm 0.030 \pm 0.006$$

$$\Delta\Phi(\psi) = (21.5 \pm 0.4 \pm 0.5)^\circ$$

BESIII

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^- \bar{\Xi}^+ \rightarrow \Lambda \pi^- \bar{\Lambda} \pi^+ \rightarrow p \pi^- \pi^- \bar{p} \pi^+ \pi^+$$

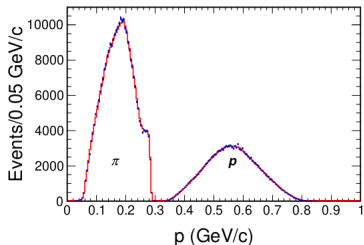
$$W = \sum_{\mu, \bar{\nu}=0}^3 C_{\mu\bar{\nu}} \sum_{\mu', \bar{\nu}'=0}^3 a_{\mu, \mu'}^{\Xi} a_{\bar{\nu}, \bar{\nu}'}^{\bar{\Xi}} a_{\mu', 0}^{\Lambda} a_{\bar{\nu}', 0}^{\bar{\Lambda}}$$

$d\Gamma \propto W(\xi, \omega)$, ξ : 9 kin. variables

8 parameters:

$$\omega = (\underbrace{\alpha_{\Psi}, \Delta\Phi}_{\text{Production}}, \underbrace{\alpha_{\Xi}, \phi_{\Xi}, \alpha_{\Lambda}, \bar{\alpha}_{\Xi}, \bar{\phi}_{\Xi}, \bar{\alpha}_{\Lambda}}_{\text{Decay}})$$

BESIII



- Exclusive analysis. 73k events (190 bkg)
- Parameters estimated using unbinned MLL fit

E.Perotti, G.Faltdt, A. Kupsc, S.Leupold, J.J.Song PRD99 (2019)056008

BESIII, Nature 606, 64–69 (2022)

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^-\bar{\Xi}^+ \rightarrow \Lambda\pi^-\bar{\Lambda}\pi^+ \rightarrow p\pi^-\pi^-\bar{p}\pi^+\pi^+$$

Parameter	This work	Previous result	Reference
α_ψ	$0.586 \pm 0.012 \pm 0.010$	$0.58 \pm 0.04 \pm 0.08$	*
$\Delta\Phi$	$1.213 \pm 0.046 \pm 0.016 \text{ rad}$	-	
α_Ξ	$-0.376 \pm 0.007 \pm 0.003$	-0.401 ± 0.010	**
ϕ_Ξ	$0.011 \pm 0.019 \pm 0.009 \text{ rad}$	$-0.037 \pm 0.014 \text{ rad}$	**
$\bar{\alpha}_\Xi$	$0.371 \pm 0.007 \pm 0.002$	-	
$\bar{\phi}_\Xi$	$-0.021 \pm 0.019 \pm 0.007 \text{ rad}$	-	
α_Λ	$0.757 \pm 0.011 \pm 0.008$	$0.750 \pm 0.009 \pm 0.004$	***
$\bar{\alpha}_\Lambda$	$-0.763 \pm 0.011 \pm 0.007$	$-0.758 \pm 0.010 \pm 0.007$	***
$\xi_P - \xi_S$	$(1.2 \pm 3.4 \pm 0.8) \times 10^{-2} \text{ rad}$	-	
$\bar{\delta}_P - \bar{\delta}_S$	$(-4.0 \pm 3.3 \pm 1.7) \times 10^{-2} \text{ rad}$	$(10.2 \pm 3.9) \times 10^{-2} \text{ rad}$	****
A_{CP}^{Ξ}	$(6 \pm 13 \pm 6) \times 10^{-3}$	-	
$\Delta\phi_{\text{CP}}^{\Xi}$	$(-5 \pm 14 \pm 3) \times 10^{-3} \text{ rad}$	-	
A_{CP}^Λ	$(-4 \pm 12 \pm 9) \times 10^{-3}$	$(-6 \pm 12 \pm 7) \times 10^{-3}$	***
$\langle\phi_\Xi\rangle$	$0.016 \pm 0.014 \pm 0.007 \text{ rad}$		

8 fit parameters

3 CP-tests

BESIII

* PRD 93, 072003 (2016)

** PDG 2020

*** Nat. Ph. 15, 631 (2019)

**** PRL 93, 011802 (2004)

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^-\bar{\Xi}^+ \rightarrow \Lambda\pi^-\bar{\Lambda}\pi^+ \rightarrow p\pi^-\pi^-\bar{p}\pi^+\pi^+$$

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First measurement of weak phase difference



* PRD 93, 072003 (2016)
 ** PDG 2020
 *** Nat. Ph. 15, 631 (2019)
 **** PRL 93, 011802 (2004)

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi^-\bar{\Xi}^+ \rightarrow \Lambda\pi^-\bar{\Lambda}\pi^+ \rightarrow p\pi^-\pi^-\bar{p}\pi^+\pi^+$$

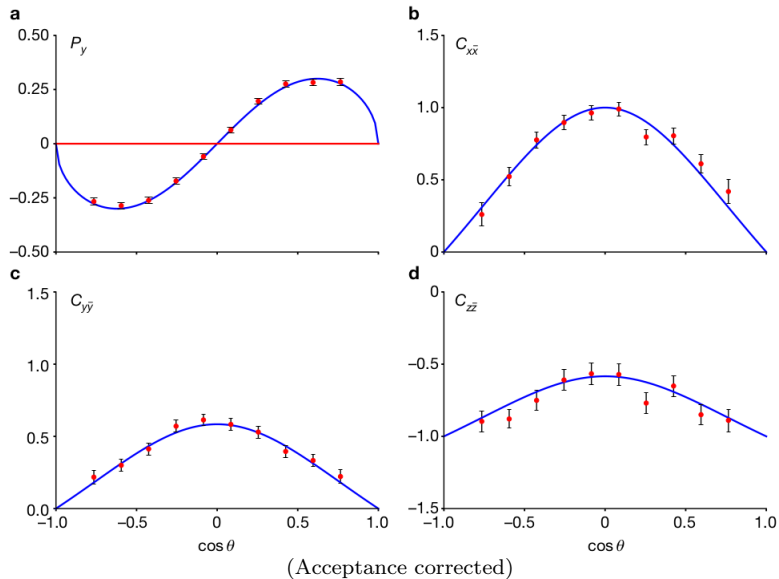
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**Independent
measurement of
 α_Λ
Consistent with
previous BESIII
measurement**



* PRD 93, 072003 (2016)
** PDG 2020
*** Nat. Ph. 15, 631 (2019)
**** PRL 93, 011802 (2004)

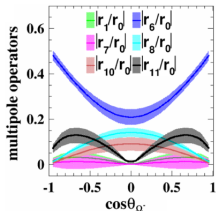
Polarization and C_{ii} for $e^+e^- \rightarrow J/\psi, \rightarrow \Xi\bar{\Xi}$



$$e^+e^- \rightarrow \psi(2S) \rightarrow \Omega\bar{\Omega}, \Omega \rightarrow \Lambda\pi^-, \Lambda \rightarrow p\pi^- + c.c.$$

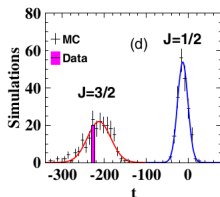
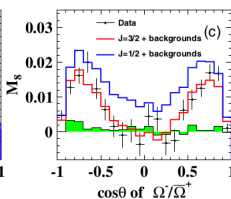
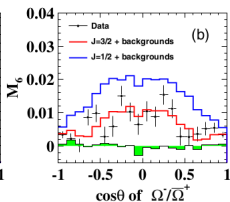
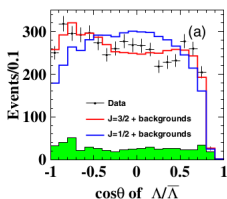
$$W = \sum_{\mu=0}^{15} C_{\mu,0} \sum_{\nu=0}^3 b_{\mu,\nu}^{\Omega} a_{\mu,0}^{\Lambda}$$

decay $1/2 \rightarrow 1/2 + 0$
 decay $3/2 \rightarrow 1/2 + 0$ ($\Lambda \rightarrow p\pi^-$)
 ($\Omega^- \rightarrow \Lambda\pi^-$)



- Single-tag analysis of 4.48×10^8 $\psi(2S)$ events
 \rightarrow 2507 Ω^- (298 bkg) and 2238 $\bar{\Omega}^+$ (189 bkg)
- Spin 3/2 confirmed model-independently for the first time.
- Multipolar polarization measured

BESIII



E.Perotti, G.Faltdt, A. Kupsc, S.Leupold, J.J. Song PRD99 (2019)056008

BESIII, Phys. Rev. Lett. 126, 092002 (2021)

Conclusion

Summary

- Polarization/spin correlations measured in $J/\psi(\psi(2S)) \rightarrow \Lambda\bar{\Lambda}, \Sigma\bar{\Sigma}, \Xi\bar{\Xi}, \Omega\bar{\Omega}$
- Hyperon and anti-hyperon decay parameters determined
- CP-tests in decays of Λ, Σ^+, Ξ^-
- Model independent determination of Ω^- spin
- Timelike electromagnetic form factors of Λ at 2.396 GeV

Outlook

- At BESIII
 - 10B J/ψ
 - 3B $\psi(2S)$
- Future super charm-tau factory?
 - 2×10^{12} J/ψ
 - Polarized electron beam?

Backup: Exclusive Analysis

$$e^+e^- \rightarrow Y\bar{Y}, Y \rightarrow BM + c.c.$$

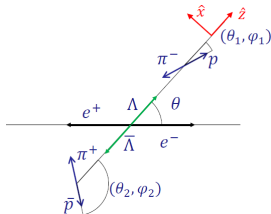
Production parameters: $\alpha_\psi, \Delta\Phi$

Decay parameters:

$$\alpha_\Lambda (\Lambda \rightarrow p\pi^-)$$

$$\bar{\alpha}_\Lambda (\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

5D phase space $\xi = (\theta, \theta_1, \phi_1, \theta_2, \phi_2)$



$$\begin{aligned} d\Gamma \propto \mathcal{W}(\xi) &= \mathcal{F}_0(\xi) + \alpha_\psi \mathcal{F}_5(\xi) && \text{spin correlations} \\ &+ \alpha_\Lambda \bar{\alpha}_\Lambda \left(\mathcal{F}_1(\xi) + \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \mathcal{F}_2(\xi) + \alpha_\psi \mathcal{F}_6(\xi) \right) \\ &+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) (\alpha_\Lambda \mathcal{F}_3(\xi) + \bar{\alpha}_\Lambda \mathcal{F}_4(\xi)) && \text{polarization} \end{aligned}$$

Non-zero $\Delta\Phi \implies$ independent measurement of $\alpha_\Lambda, \bar{\alpha}_\Lambda$