

# The Chiral Magnetic Effect and its Search in Heavy Ion Collisions



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# PLAN

- Physics motivation of the Chiral Magnetic Effect (CME)
- How do we search for the CME in heavy-ion collisions?
- What have we found?
- What are we going to do next?

ALL ARE MATTER; ALMOST NO VISIBLE ANTIMATTER



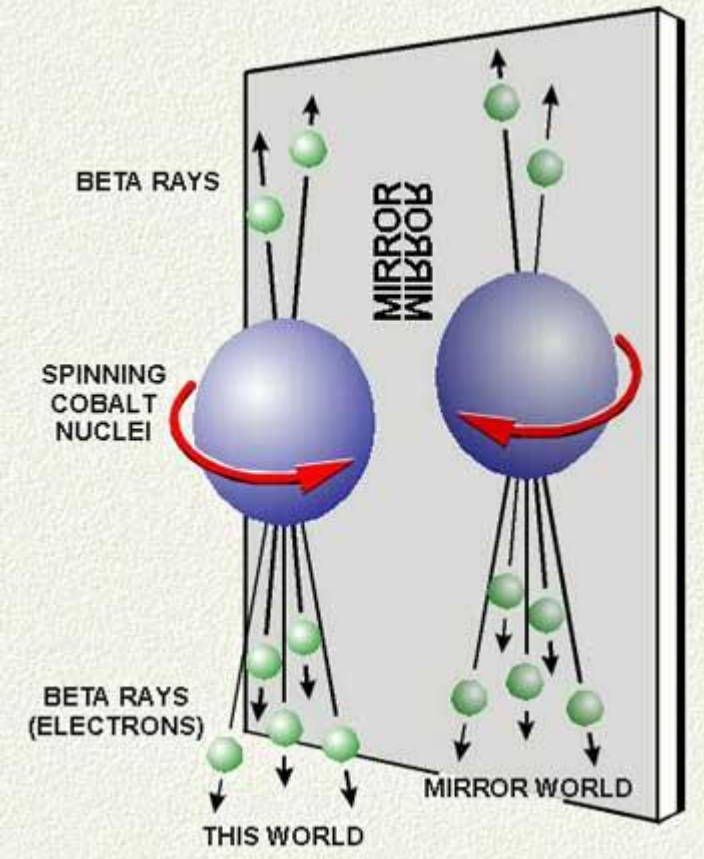
# CP VIOLATION

CP is violated in weak interaction,  $\sim 10^{-3}$ , e.g.  $K_L \rightarrow 2\pi$ ,  
 $BR \approx 2 \times 10^{-3}$

CKM CP violation is too small to explain the matter-  
antimatter asymmetry  $B/\gamma \sim 10^{-10}$   
by some  $\sim 10$  order orders of magnitude

Need CP violation in the strong interaction

In the standard model  
one expects the same level of CP violation in  
electroweak and strong interaction





# THE $\theta$ -VACUUM TERM

't Hooft PRD 1976

$$\mathcal{L}_{QCD} = \sum_q \left( \bar{\psi}_{qi} i\gamma^\mu \left[ \delta_{ij} \partial_\mu + ig \left( G_\mu^\alpha t_\alpha \right)_{ij} \right] \psi_{qj} - m_q \bar{\psi}_{qi} \psi_{qi} \right) - \frac{1}{4} G_{\mu\nu}^\alpha G_\alpha^{\mu\nu}$$

quarks
quark-gluon interactions
quarks
gluons

't Hooft vacuum

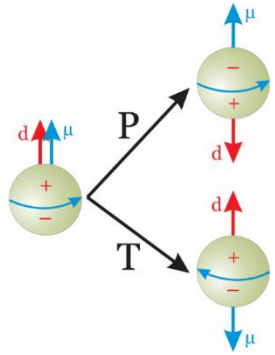
$$+ \theta \frac{\alpha_s}{8\pi} G_{\mu\nu}^\alpha \tilde{G}_\alpha^{\mu\nu}$$

$$= -\theta \frac{\alpha_s}{2\pi} \vec{E}_\alpha \cdot \vec{B}_\alpha$$

Gluon pseudoscalar density

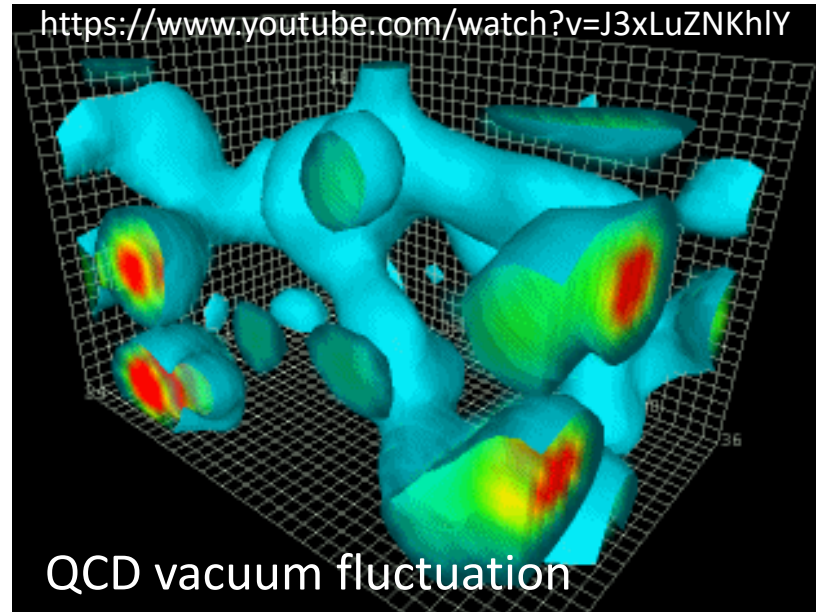
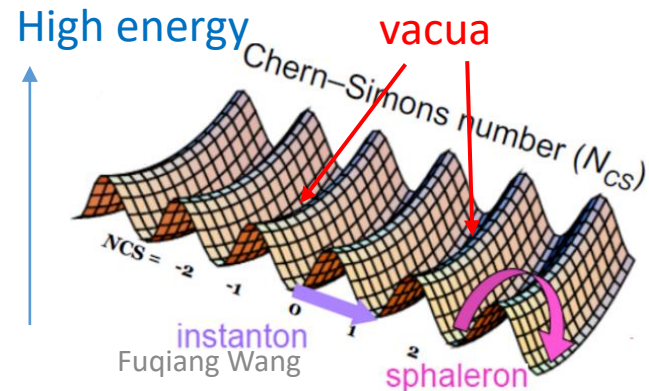
Explicitly breaks CP

Low energy:  $\theta \sim 0$



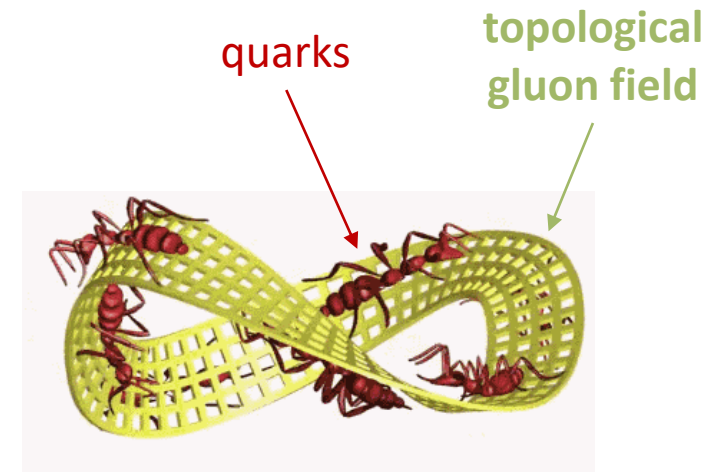
The neutron EDM should be finite, but not observed.

Peccei&Quinn,1977:  
Axion field



Topological charge:  $Q_W = \frac{\alpha_s}{8\pi} \int G_{\mu\nu}^\alpha \tilde{G}_\alpha^{\mu\nu} drdt$

CS winding number:  $N_{CS} = \nu = N_R - N_L = 2Q_W$

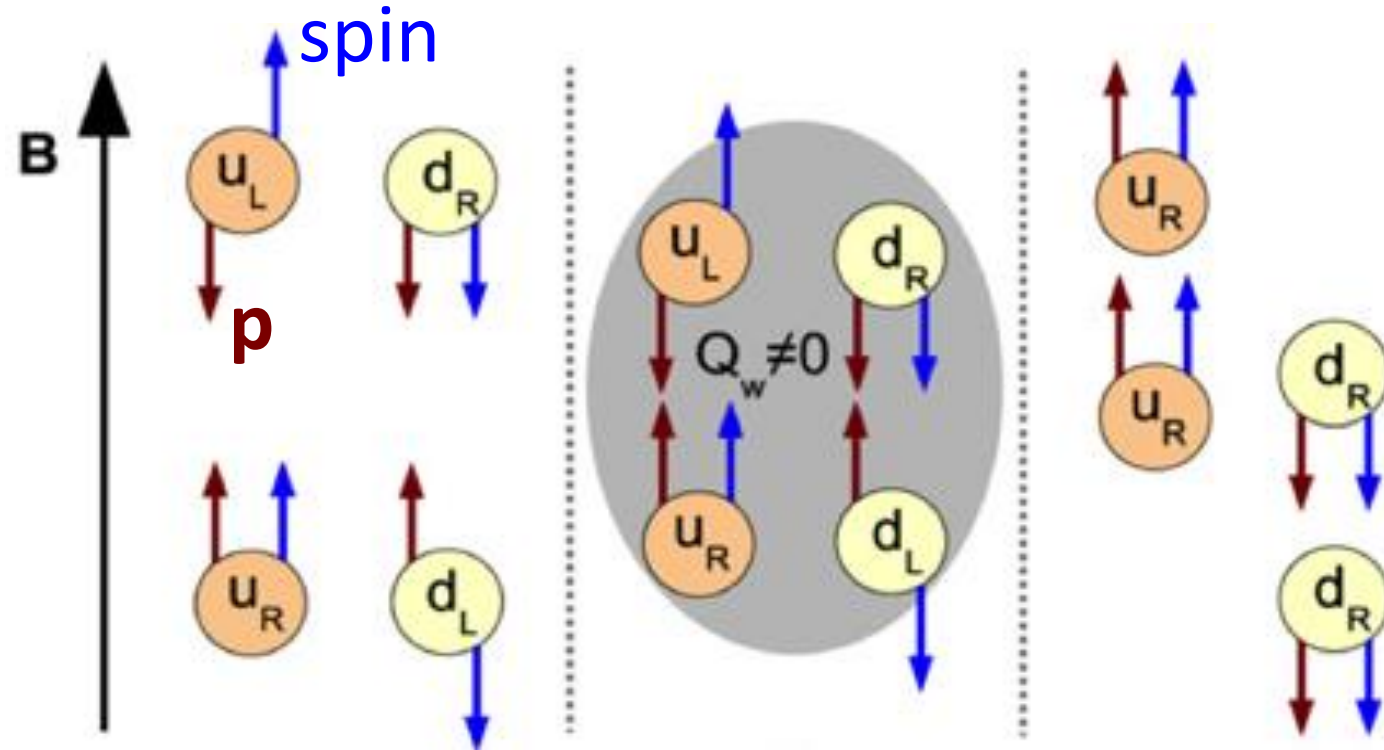
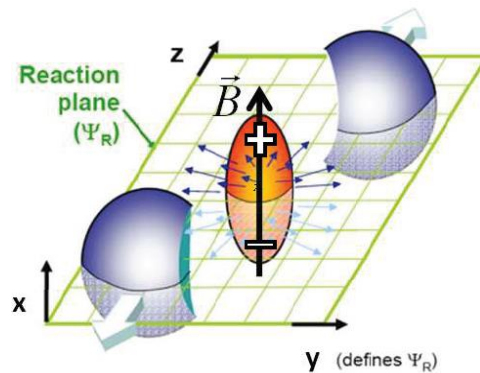


# CAN WE OBSERVE THE TOPOLOGICAL QCD VACUUM?

(and quark handedness, P and CP violations)

QCD anomaly  $\rightarrow$  chirality is not conserved

Need a strong magnetic field!



Kharzeev, et al. Nucl. Phys. A 803 (2008) 227

# How strong is the magnetic field?

Magnetar

$B \sim 10^{11} \text{ T}$



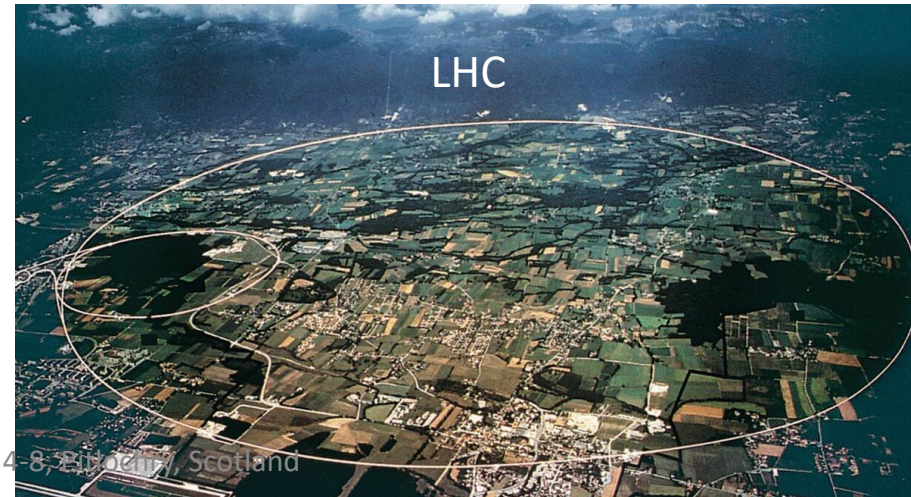
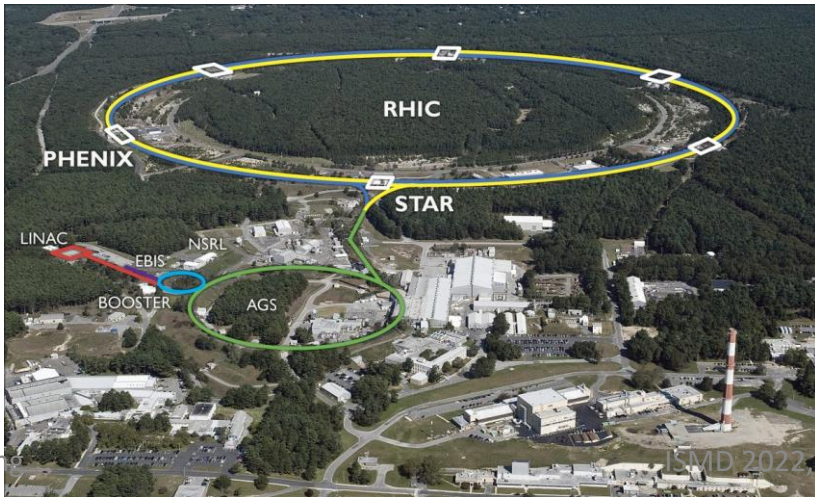
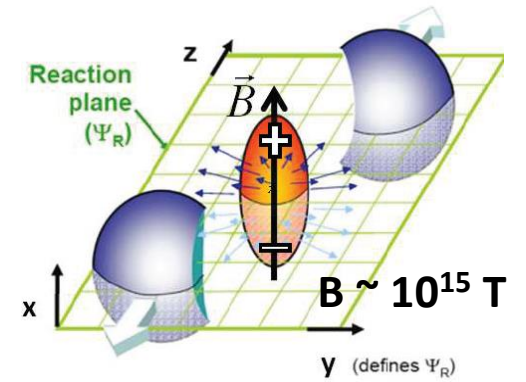
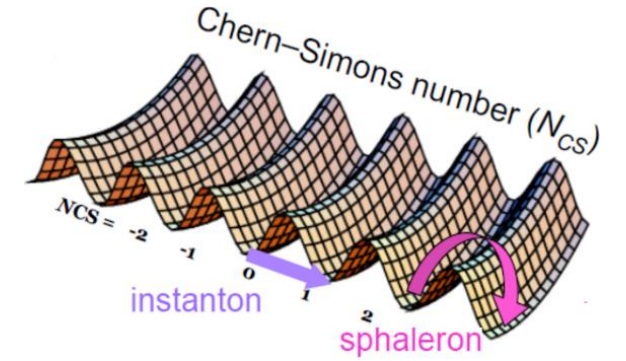
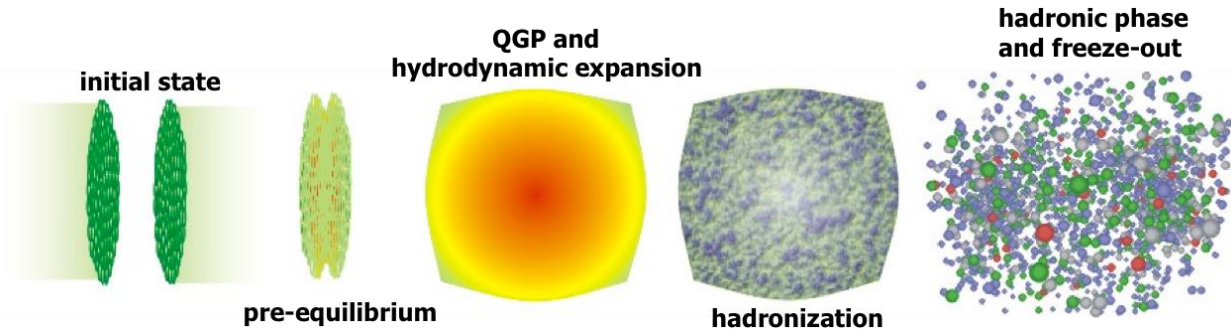
$$B = \frac{\mu_0}{4\pi} \cdot \frac{qv}{r^2} \cdot \gamma \cdot 2 = 10^{-7} \frac{50 \cdot 1.6 \times 10^{-19} \cdot 3 \times 10^8}{(7 \times 10^{-15})^2} \cdot 100 \cdot 2 = 10^{15} \text{ T}$$



# TO SEARCH FOR THE CME IN QCD

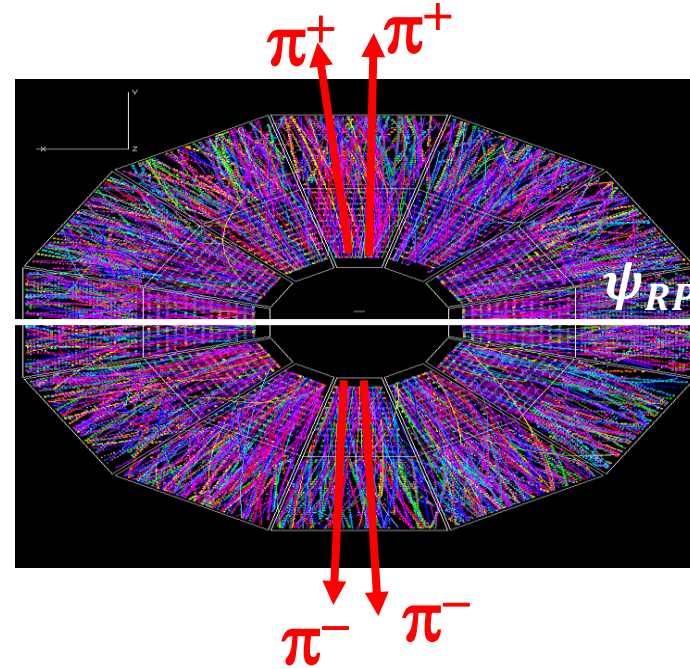
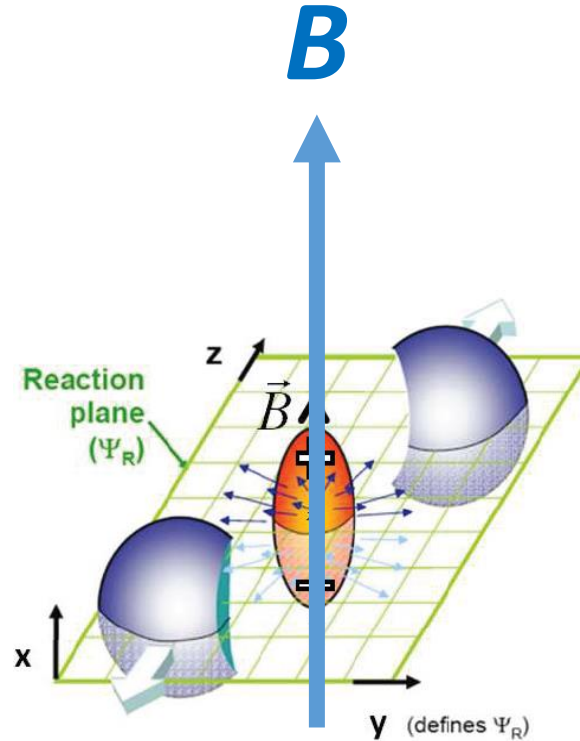
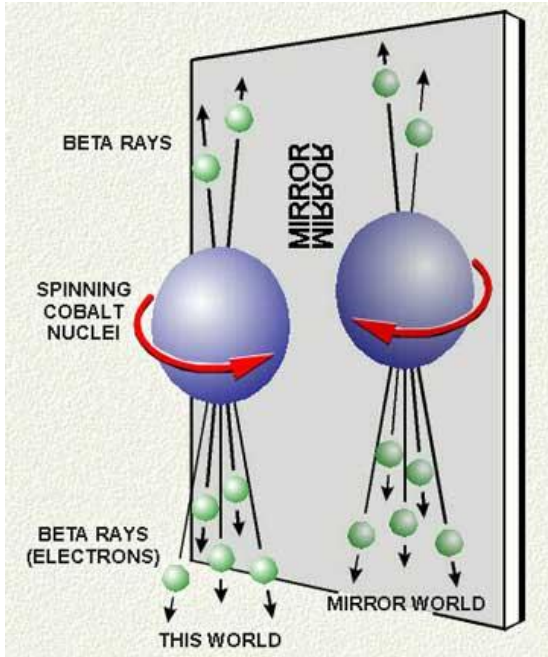
- Need a QCD machine to **recreate the early universe**
- Need **strong magnetic field**

Use  
heavy-ion  
collisions





# HOW TO MEASURE CHARGE SEPARATION



Voloshin, PRC 70  
(2004) 057901

- **parity-odd** observables will average to zero
- have to measure charge correlations, or variance/covariance
- will be proportional to **Parity<sup>2</sup>**, so subject to **P-even backgrounds**
- How big is the signal? hard to predict from first principle  
Guesstimate 1%, or  $10^{-4}$  in correlation measurement

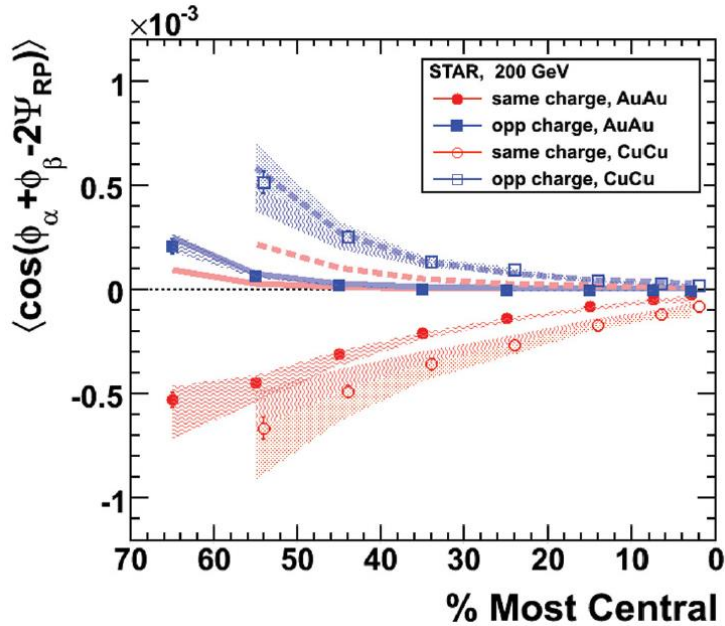
$$\gamma_{\alpha\beta} = \langle \cos(\varphi_\alpha + \varphi_\beta - 2\psi_{RP}) \rangle$$

$$\gamma_{+-,-+} > 0, \quad \gamma_{++,--} < 0$$

$$\Delta\gamma = \gamma_{OS} - \gamma_{SS}$$

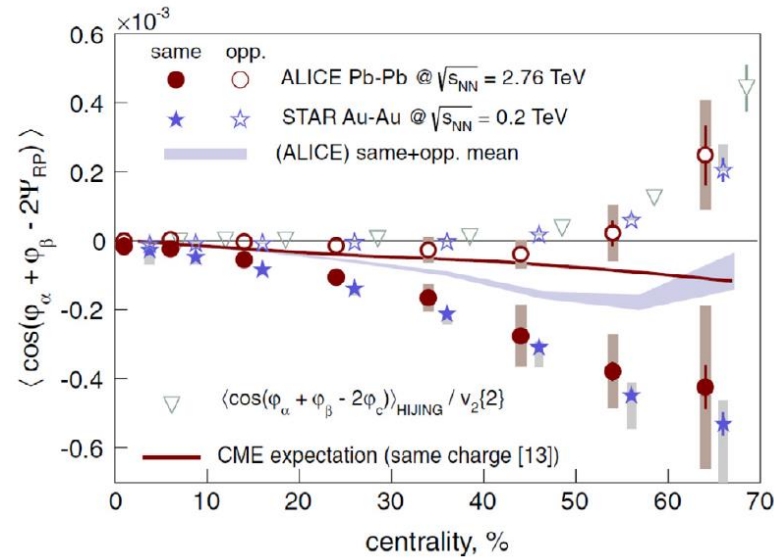
$$\Delta\gamma > 0$$

# INDEED STRONG SIGNALS WERE OBSERVED



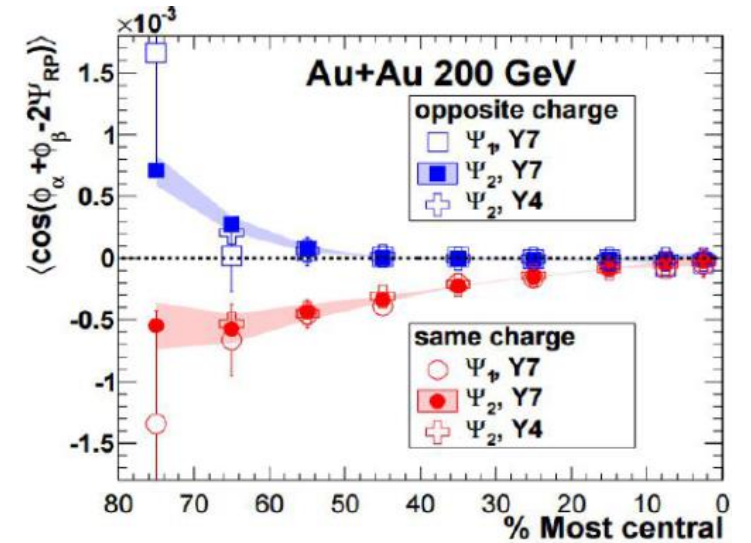
STAR, PRL 103 (2009) 251601  
 PRC 81 (2010) 054908.

STAR, 2009



ALICE, PRL 110 (2013) 012301

ALICE, 2013

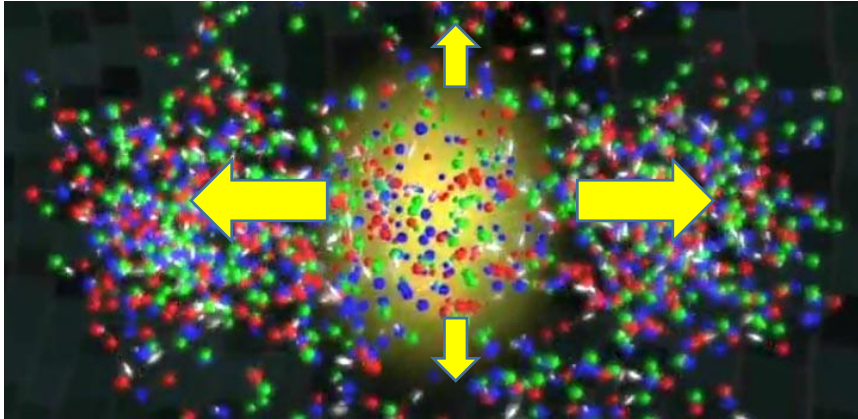


STAR, PRC 88 (2013) 064911

STAR, 2013



# CORRELATION BACKGROUND

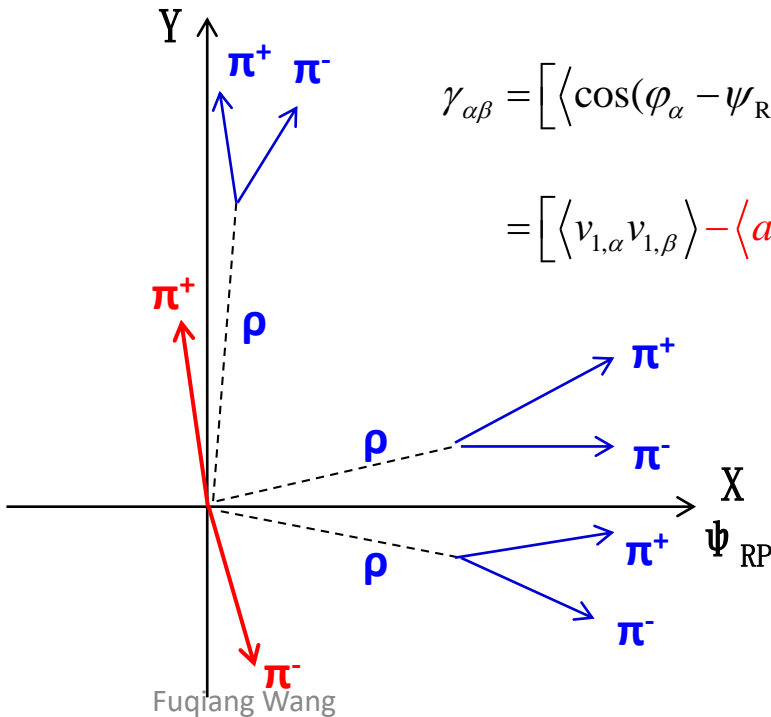


FW 2009; Bzdak, Koch, Liao 2010; Pratt, Schlichting 2010; ...

$$\gamma = \langle \cos(\varphi_\alpha + \varphi_\beta - 2\psi_{RP}) \rangle$$

$$\frac{dN_\pm}{d\varphi} \propto 1 + 2v_1 \cos \varphi^\pm + 2a_\pm \cdot \sin \varphi^\pm + 2v_2 \cos 2\varphi^\pm + \dots$$

$$\begin{aligned} \gamma_{\alpha\beta} &= \left[ \langle \cos(\varphi_\alpha - \psi_{RP}) \cos(\varphi_\beta - \psi_{RP}) \rangle - \langle \sin(\varphi_\alpha - \psi_{RP}) \sin(\varphi_\beta - \psi_{RP}) \rangle \right] + \left[ \frac{N_{\text{cluster}}}{N_\alpha N_\beta} \langle \cos(\varphi_\alpha + \varphi_\beta - 2\varphi_{\text{cluster}}) \cos(2\varphi_{\text{cluster}} - 2\psi_{RP}) \rangle \right] \\ &= \left[ \langle v_{1,\alpha} v_{1,\beta} \rangle - \langle a_\alpha a_\beta \rangle \right] + [\text{charge-independent Bkg (e.g. mom. conservation)}] + \frac{N_{\text{cluster}}}{N_\alpha N_\beta} \langle \cos(\varphi_\alpha + \varphi_\beta - 2\varphi_{\text{cluster}}) \rangle v_{2,\text{cluster}} \end{aligned}$$



$$\Delta\gamma_{\text{bkg}} = 2\langle a_1^2 \rangle + \frac{N_{\text{cluster}}}{N_\alpha N_\beta} \langle \cos(\varphi_\alpha + \varphi_\beta - 2\varphi_{\text{cluster}}) \rangle v_{2,\text{cluster}} \propto v_{2,\rho} / N$$

NONFLOW x FLOW

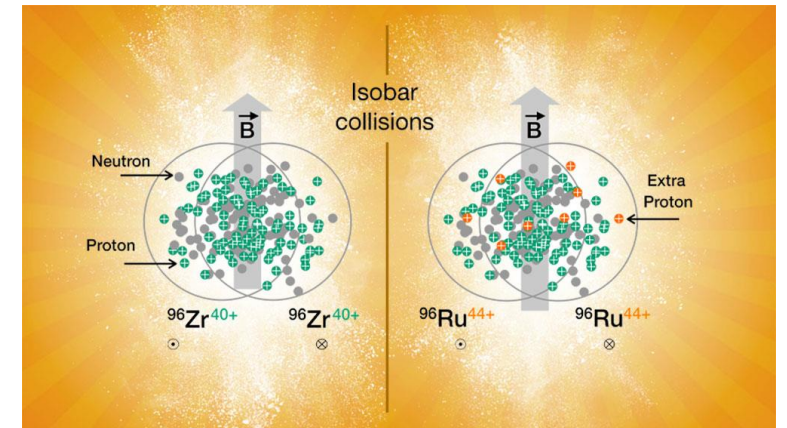
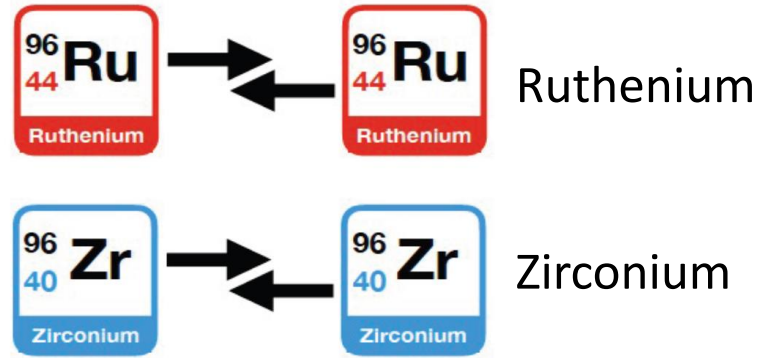
# STRATEGY

- **Isobar collisions**

- Same mass number ( $A=Z+N$ )  
Strong interaction physics is blind to proton vs. neutron  
→ **same QCD background**
- Different atomic number ( $Z$ )  
Magnetic field is produced by the passing protons  
→ different magnetic field → **different CME signal**

- **Isobar blind analysis**

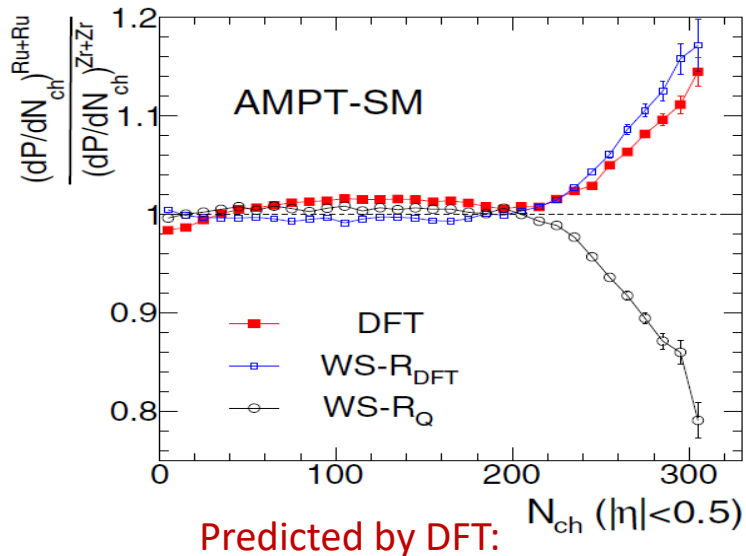
- ✓ Recommended by BNL Physics Advisory Committee
- ✓ First time in heavy ion collisions
- ✓ Design even before data taking: *Methods for a blind analysis of isobar data collected by the STAR Collaboration*, Nucl. Sci. Tech. 32 (2021) 48



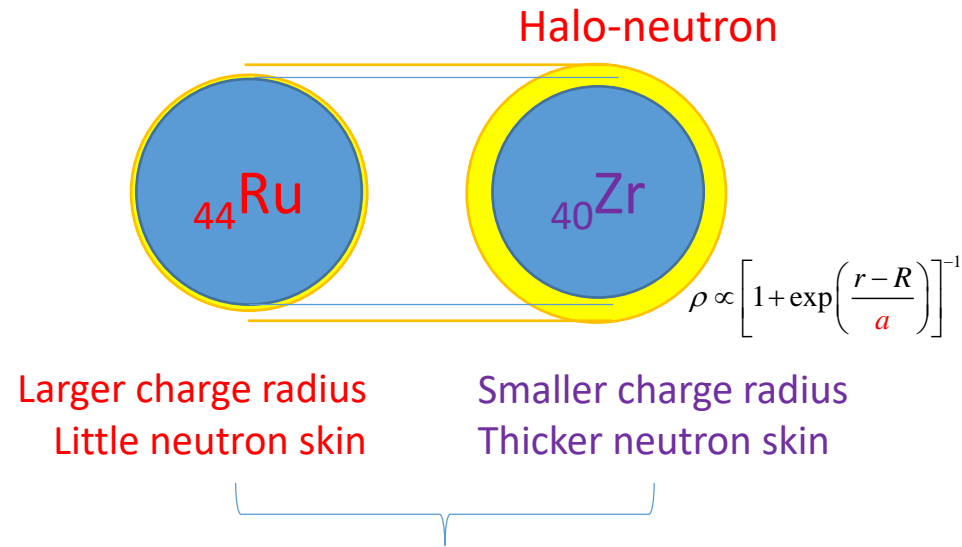
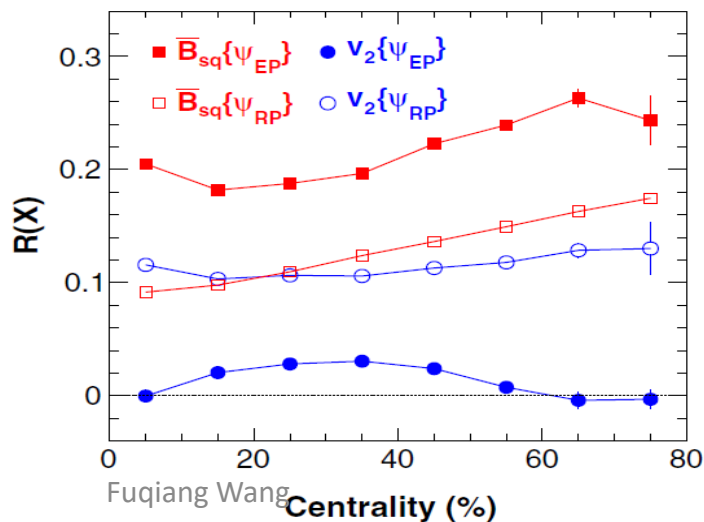
- 2B events are taken for each system
- $3\sigma$  significance if signal is 10% of the measured  $\Delta\gamma$



# ISOBAR SYSTEMS ARE NOT IDENTICAL



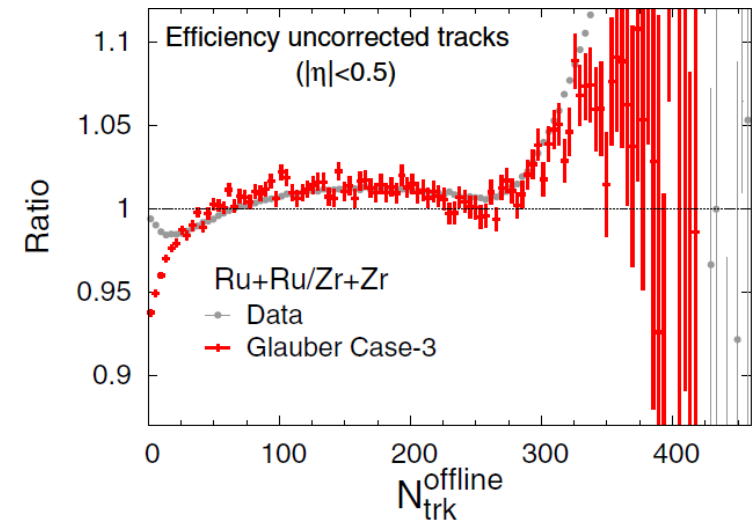
Hanlin Li et al. PRC **98** (2018) 054907  
 Haojie Xu et al. PRL **121** (2018) 022301



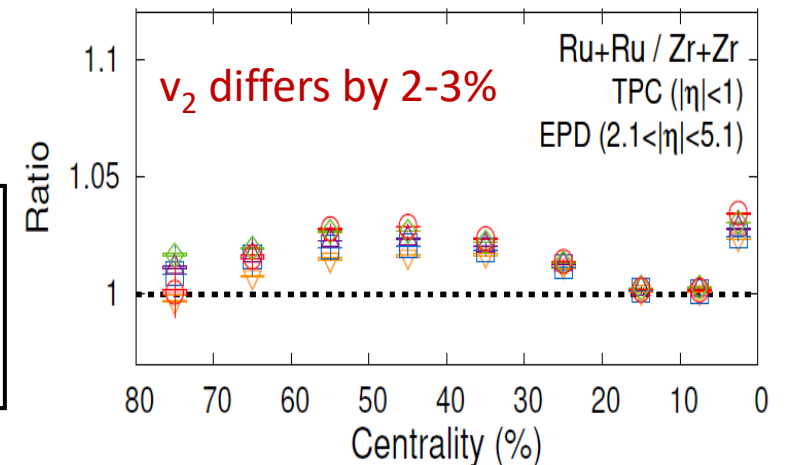
Overall size: Ru < Zr  
 → Larger energy density in Ru > Zr  
 → Larger multiplicity in Ru > Zr

$$\Delta\gamma_{\text{bkg}} = \frac{4N_{2p}}{N^2} \langle \cos(\phi_\alpha + \phi_\beta - 2\phi_{2p}) \rangle v_{2,2p}$$

Normalize by  $v_2$  and  $N \rightarrow N\Delta\gamma/v_2$



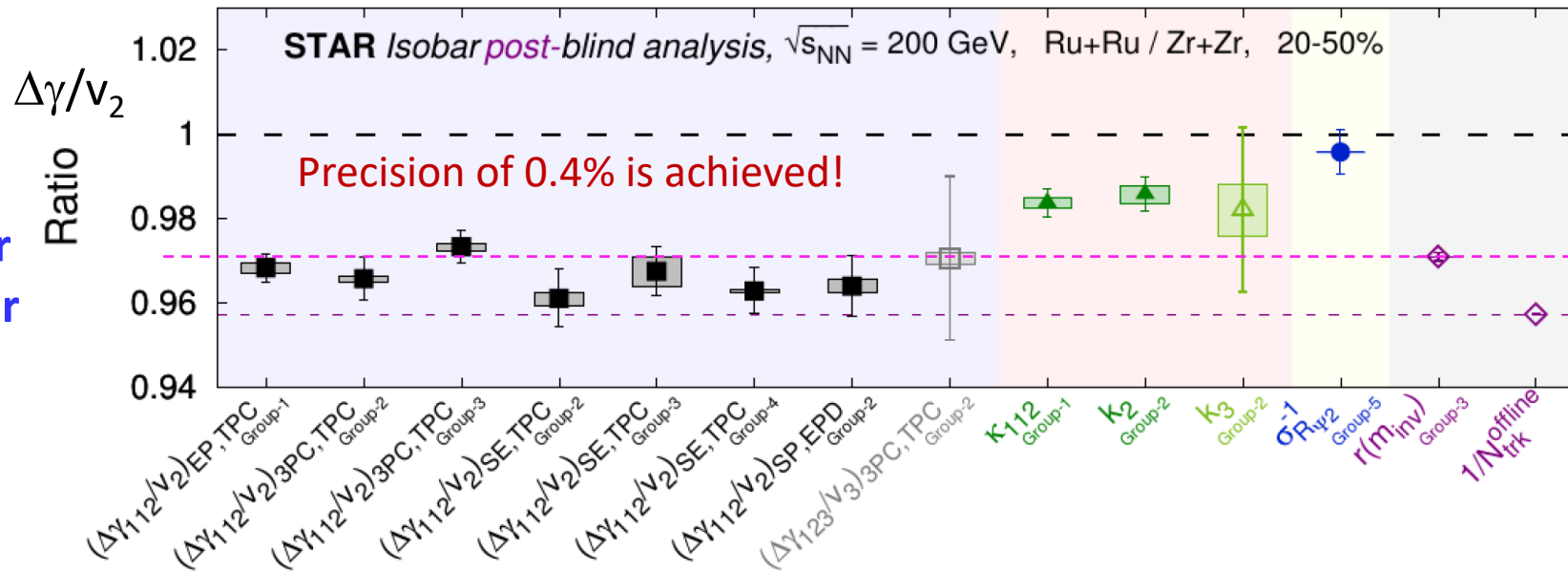
Verified by isobar data:  
 STAR, PRC **105** (2022), 2109.00131



# ISOBAR COLLISION RESULTS

STAR, PRC 105 (2022), 2109.00131

$\Delta\gamma/v_2$  isobar ratio smaller than unity



Primary reason:  
Mult. difference

$$\Delta\gamma_{bkg} \propto N_{cluster} / N^2$$



# REMAINING NONFLOW EFFECTS

Feng, FW, et al., PRC 105 (2022) 024913, arXiv:2106.15595

$$C_3 = \frac{C_{2p} N_{2p}}{N^2} v_{2,2p} v_2 + \frac{C_{3p} N_{3p}}{2N^3}; \quad C_{2p} \equiv \langle \cos(\alpha + \beta - 2\phi_{2p}) \rangle$$

$$C_{3p} \equiv \langle \cos(\alpha + \beta - 2c) \rangle_{3p}$$

$$\varepsilon_2 \equiv \frac{C_{2p} N_{2p}}{N} \cdot \frac{v_{2,2p}}{v_2}$$

$$\varepsilon_3 \equiv \frac{C_{3p} N_{3p}}{2N}$$

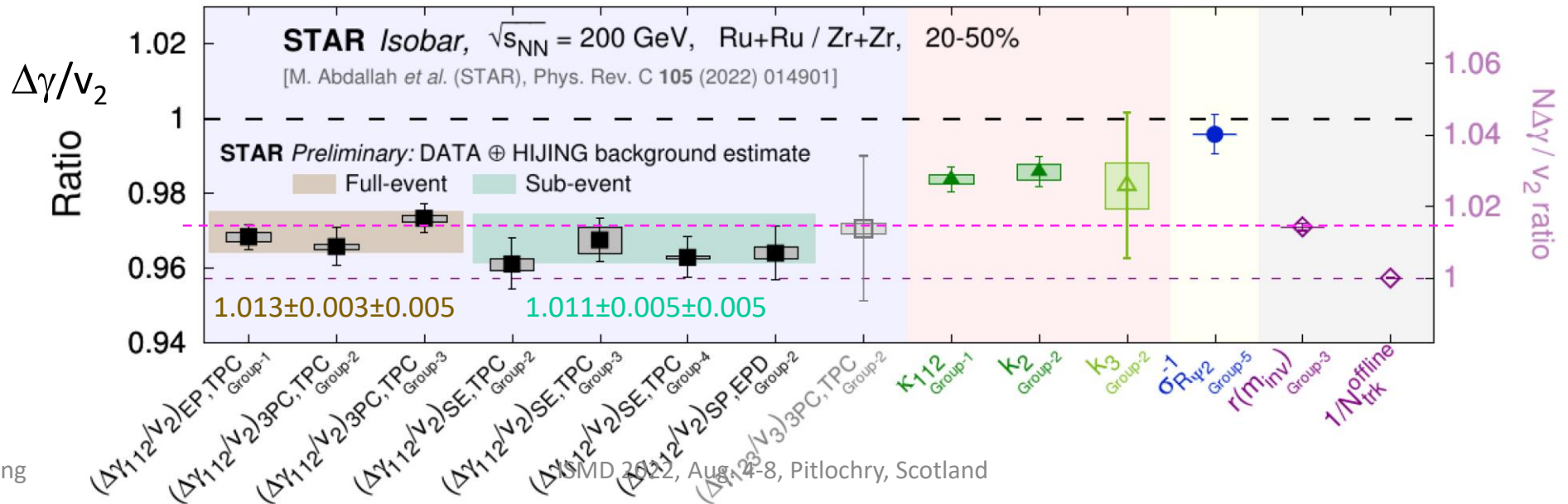
$$v_2^{*2} = v_2^2 + v_{2,nf}^2$$

$$\varepsilon_{nf} \equiv v_{2,nf}^2 / v_2^2$$

$$N \approx N_+ \approx N_-$$

$$\Delta X \equiv X^{Ru} - X^{Zr}$$

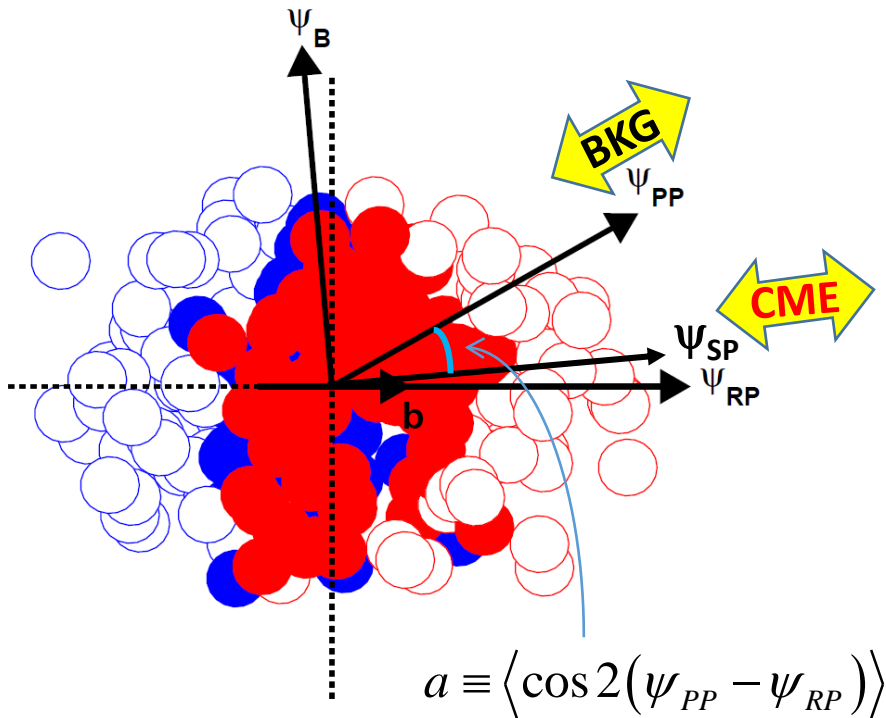
$$\frac{(N\Delta\gamma/v_2^*)^{Ru}}{(N\Delta\gamma/v_2^*)^{Zr}} \equiv \frac{(NC_3/v_2^{*2})^{Ru}}{(NC_3/v_2^{*2})^{Zr}} \approx \frac{\varepsilon_2^{Ru}}{\varepsilon_2^{Zr}} \cdot \frac{(1+\varepsilon_{nf})^{Zr}}{(1+\varepsilon_{nf})^{Ru}} \cdot \frac{\left(1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2}\right)^{Ru}}{\left(1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2}\right)^{Zr}} \approx \frac{\varepsilon_2^{Ru}}{\varepsilon_2^{Zr}} - \frac{\Delta\varepsilon_{nf}}{1+\varepsilon_{nf}} + \frac{\frac{\varepsilon_3/\varepsilon_2}{Nv_2^2}}{1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2}} \left( \frac{\Delta\varepsilon_3}{\varepsilon_3} - \frac{\Delta\varepsilon_2}{\varepsilon_2} - \frac{\Delta N}{N} - \frac{\Delta v_2^2}{v_2^2} \right)$$



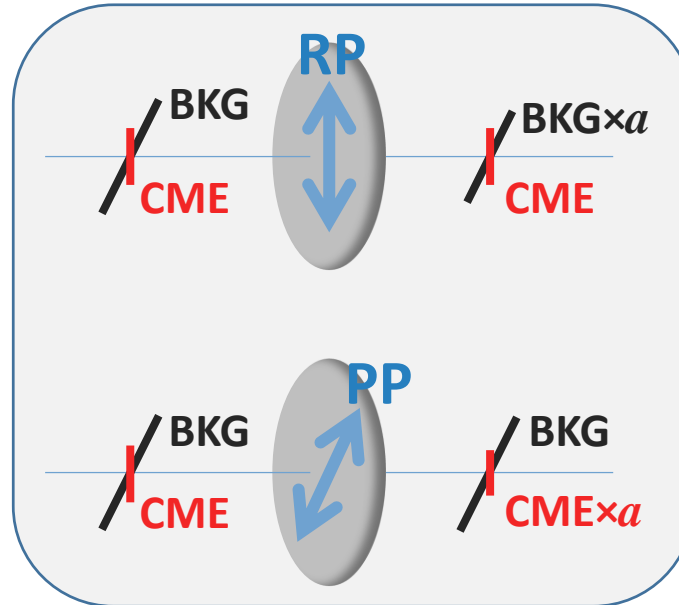
# SPECTATOR & PARTICIPANT PLANES

H.-j. Xu, FW, et al., CPC 42 (2018) 084103, arXiv:1710.07265

S.A. Voloshin, PRC 98 (2018) 054911, arXiv:1805.05300



## INTRA-EVENT "CME- $v_2$ FILTER"



IN THE SAME EVENT

$$\Delta\gamma_{\{SP\}} = a\Delta\gamma_{Bkg\{PP\}} + \Delta\gamma_{CME\{PP\}} / a$$

$$\Delta\gamma_{\{PP\}} = \Delta\gamma_{Bkg\{PP\}} + \Delta\gamma_{CME\{PP\}}$$

$$A = \Delta\gamma_{\{SP\}} / \Delta\gamma_{\{PP\}}$$

$$a = v_2\{SP\} / v_2\{PP\}$$

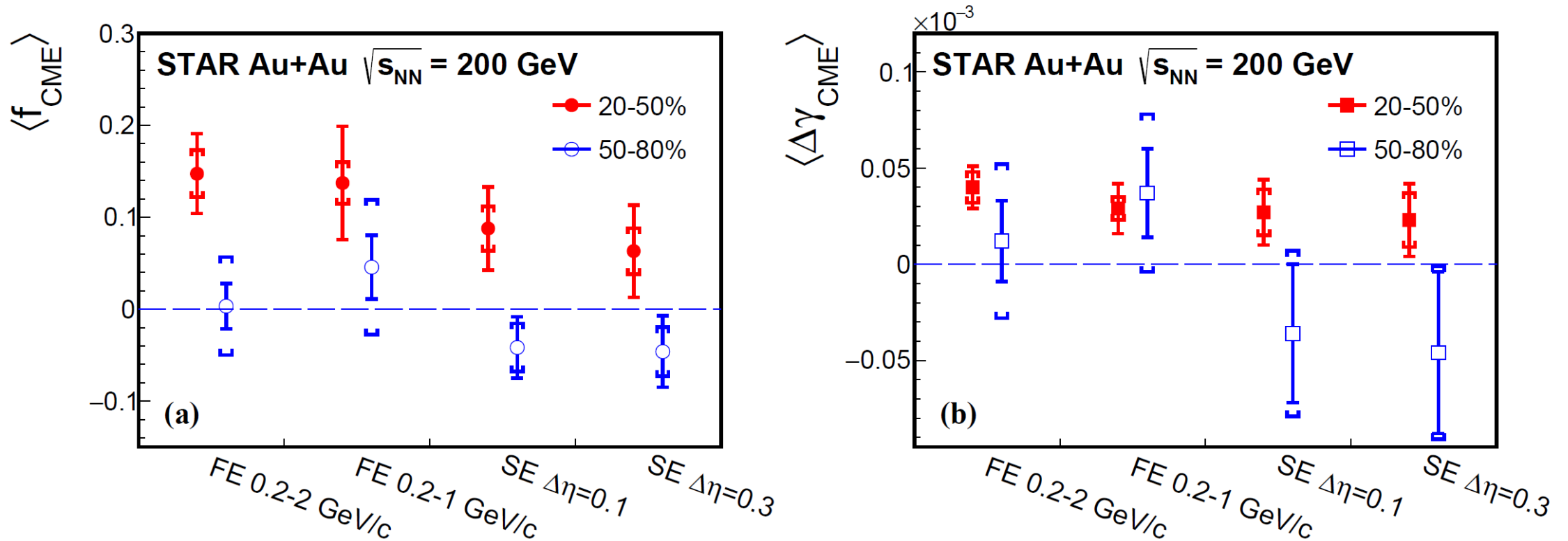
$$\Delta\gamma_{\{SP\}} / a - \Delta\gamma_{\{PP\}} = (1/a^2 - 1)\Delta\gamma_{CME\{PP\}}$$

$$f_{CME} = \frac{\Delta\gamma_{CME\{PP\}}}{\Delta\gamma_{\{PP\}}} = \frac{A/a - 1}{1/a^2 - 1}$$



# Au+Au Collisions at 200 GeV (2.4B MB)

STAR, PRL 128 (2022) 092301, arXiv:2106.09243



- Consistent-with-zero signal in peripheral 50-80% collisions with relatively large errors
- Indications of finite signal in mid-central 20-50% collisions, with 1-3 $\sigma$  significance
- Possible remaining nonflow effects

# REMAINING NONFLOW EFFECTS

STAR, PRL 128 (2022) 092301, arXiv:2106.09243

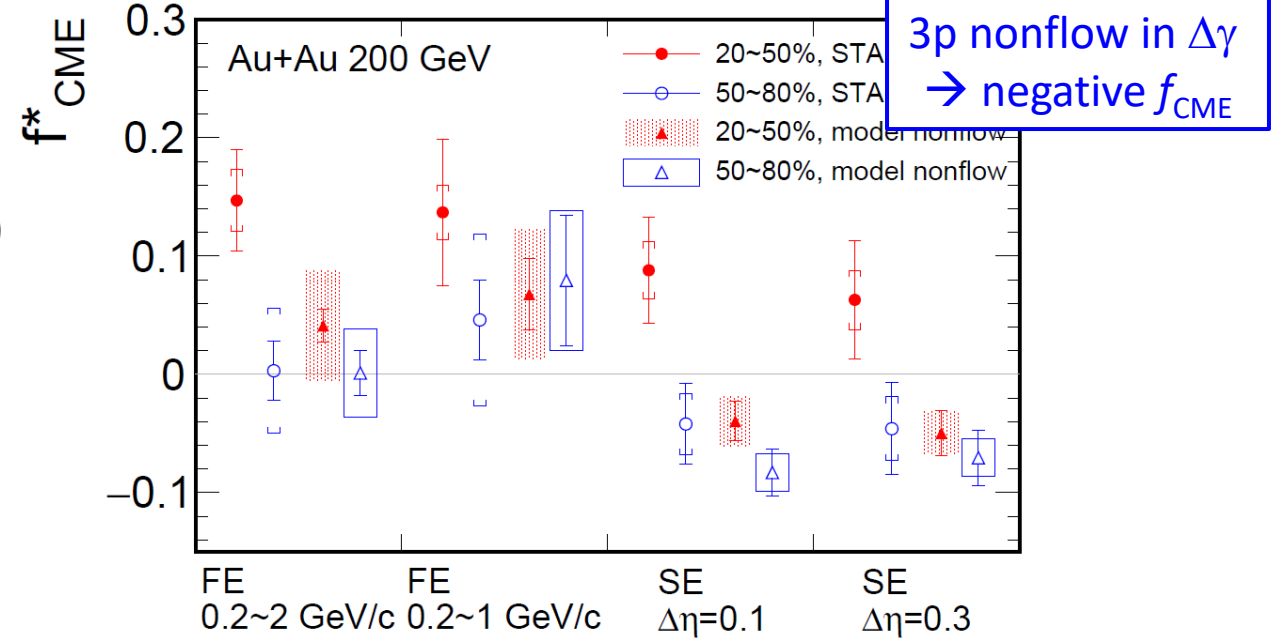
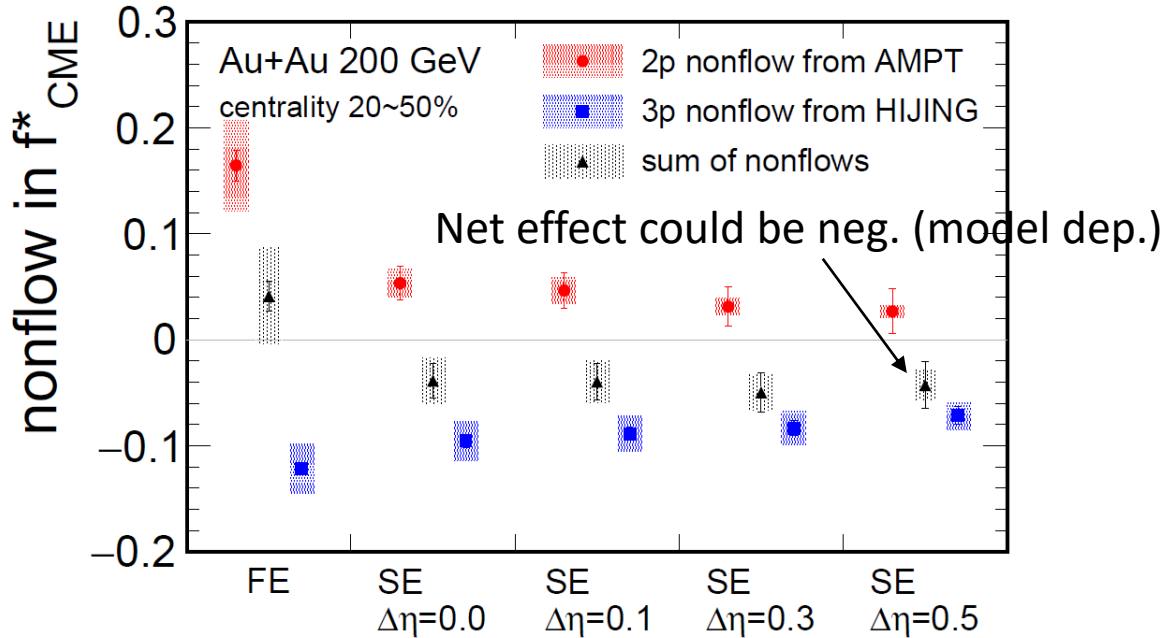
Feng, FW, et al., PRC 105 (2022) 024913, arXiv:2106.15595

$$f_{\text{CME}} = \frac{\Delta\gamma_{\text{CME}}\{\text{PP}\}}{\Delta\gamma\{\text{PP}\}} = \frac{A/a - 1}{1/a^2 - 1}$$

Nonflow in  $v_2$   
→ positive  $f_{\text{CME}}$

$$\frac{(N\Delta\gamma/v_2^*)^{\text{Ru}}}{(N\Delta\gamma/v_2^*)^{\text{Zr}}} \approx \frac{\varepsilon_2^{\text{Ru}}}{\varepsilon_2^{\text{Zr}}} \cdot \frac{(1 + \varepsilon_{\text{nf}})^{\text{Zr}}}{(1 + \varepsilon_{\text{nf}})^{\text{Ru}}} \cdot \frac{\left(1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2}\right)^{\text{Ru}}}{\left(1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2}\right)^{\text{Zr}}}$$

$$\frac{A}{a} = \frac{\Delta\gamma\{\text{SP}\}/v_2\{\text{SP}\}}{\Delta\gamma\{\text{PP}\}^*/v_2\{\text{PP}\}^*} = \frac{C_3\{\text{SP}\}/v_2^2\{\text{SP}\}}{C_3\{\text{PP}\}^*/v_2^2\{\text{PP}\}^*} = \frac{1 + \varepsilon_{\text{nf}}}{1 + \frac{\varepsilon_3/\varepsilon_2}{Nv_2^2\{\text{PP}\}}}$$

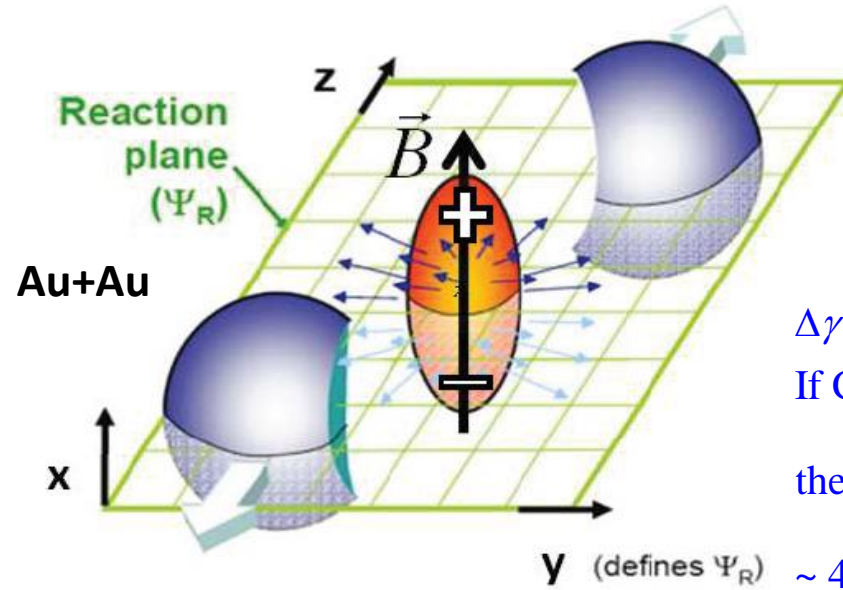


There may indeed be hint of CME in the data

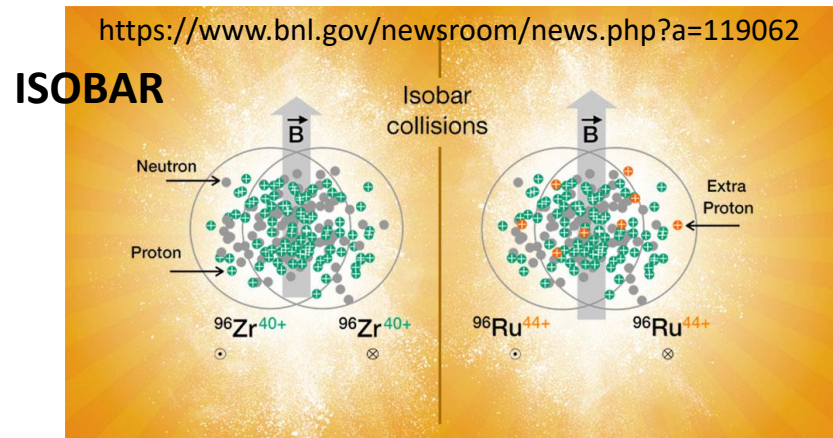
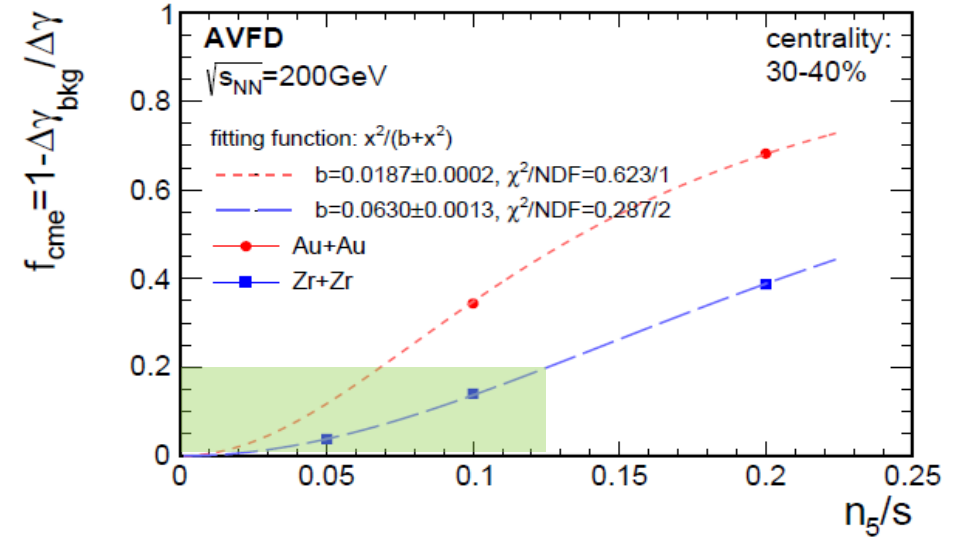


# Au+Au vs. ISOBAR

Feng, FW, et al., PLB 820 (2021) 136549, arXiv:2103.10378



$\Delta\gamma \propto B^2$   
 If CME signal is 10%,  
 then  $\frac{\Delta\gamma^{\text{Ru}}}{\Delta\gamma^{\text{Zr}}} - 1 \approx 1.5\%$   
 $\sim 4\sigma$  effect



$B_{\text{kg}} \propto 1/N \rightarrow \text{isobar/AuAu} \sim 2$

$B \sim A^{1/3} \rightarrow \text{CME: AuAu/isobar} \sim 1.5$

Can be x3 smaller  $f_{\text{CME}}$  @same  $n_5/s$

# SUMMARY & OUTLOOK

- CME is a very important physics. We have to quantify it.
- Background being of the order of 90% is a game changer.
- Isobar collisions: anticipated **precision down to 0.4%**.  
New background estimate, signal consistent with zero, not contradictory to Au+Au.  
**Refine nonflow and extract upper limit.**
- STAR Au+Au data (2.4 B MB events) **hint a finite CME signal** with small significance;  
Need more rigorous nonflow studies.  
**Expect 20B Au+Au from 2023+25 runs.**