

# Recent $CP$ violation results in heavy flavour involving multibody decays

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IGFAE

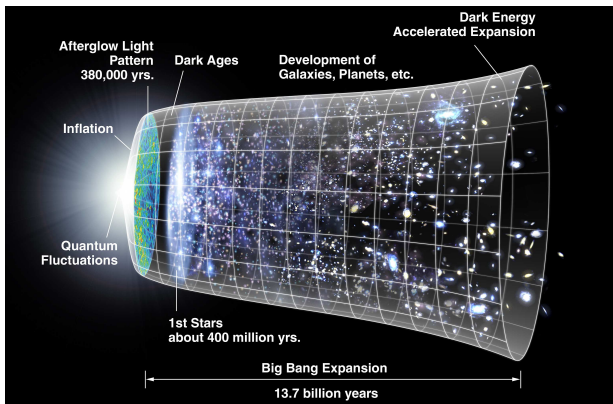
Instituto Galego de Física de Altas Enerxías



XUNTA  
DE GALICIA

The Standard Model (SM) of Particle Physics is incomplete

Predicts almost all visible matter would annihilate right after the Big Bang  
Cosmological observations show this is incorrect by  $\mathcal{O}(10^9)$

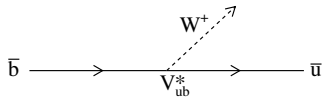


There must be new sources of matter-antimatter asymmetry

Matter-antimatter asymmetry manifests as violation of charge-parity ( $CP$ ) symmetry

$CP$  broken in the charged-current Lagrangian term of the weak interaction,  $\mathcal{L}_{EW}^+$

Up-type quark can transform to down-type quark mediated by  $W$  boson



Strength of transition described by the CKM matrix,  $V_{CKM}$

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

For 3 quark generations, unitarity constraints leave  $V_{CKM}$  with a **single complex phase**

$$\widehat{CP} \mathcal{L}_{EW}^+ \neq \mathcal{L}_{EW}^+ \text{ if } V_{CKM} \text{ complex}$$

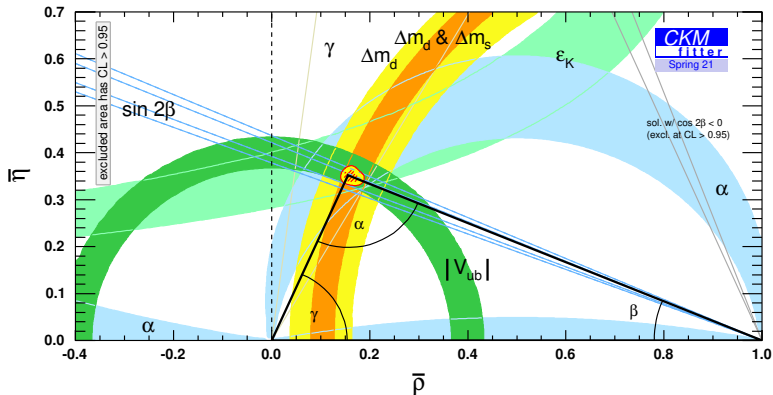
Single complex phase in  $V_{CKM}$  the source of all  $CP$  violation in the SM

# Unitarity Triangle

Unitarity constraint:  $V_{CKM}^\dagger V_{CKM} = \mathbf{1}$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \quad - \text{relevant for } B \text{ decays}$$

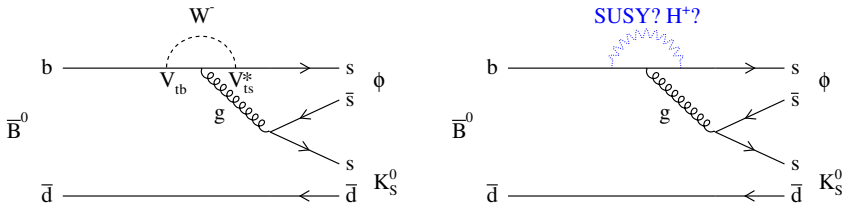
Convenient to represent as the Unitarity Triangle



Angles and sides can be measured through various  $B$  decay processes

Experiment supports CKM mechanism, but room for New Physics at  $\sim 20\%$  level

2nd-order loop diagrams potentially sensitive to New Physics



Unknown heavy particle could be present in the loop

May carry a new  $CP$  violating phase

Short time-scale in loop the key to accessing arbitrarily high energies

Heisenberg Uncertainty Principle:  $\Delta E \Delta t \geq \hbar/2$

Can reach higher mass scales than possible with direct searches at LHC

Mass scale of New Physics through loop processes a matter of statistics rather than CMS energy

Deviation of measured  $CP$  violating phase and Standard Model expectation a clear signature of New Physics

# Conditions for $CP$ violation in decay

Several other types of  $CP$  violation: in mixing, mixing-induced

In flavour-specific  $B$  decays, presence of multiple amplitudes may lead to (direct)  $CP$  violation in decay

$$A(B \rightarrow f) = \sum_i |A_i| e^{i(\delta_i + \phi_i)}$$

$$\bar{A}(\bar{B} \rightarrow \bar{f}) = \sum_i |A_i| e^{i(\delta_i - \phi_i)}$$

Strong phase ( $\delta$ ) invariant under  $CP$

Weak phase ( $\phi$ ) changes sign under  $CP$

$$\mathcal{A}_{CP}(B \rightarrow f) \equiv \frac{|\bar{A}|^2 - |A|^2}{|\bar{A}|^2 + |A|^2} \propto \sum_{i,j} |A_i| |A_j| \sin(\delta_i - \delta_j) \sin(\phi_i - \phi_j)$$

3 conditions required for  $CP$  violation in decay

At least 2 competitive amplitudes

Non-zero strong phase difference,  $\delta_i - \delta_j \neq 0$

Non-zero weak phase difference,  $\phi_i - \phi_j \neq 0$

Weak phase comes from different CKM phases in each amplitude

Strong phase structure from decay amplitude in multibody phase space

## 1. Measurement of the $CP$ -violating phase $\gamma$

- ADS method

- $B^\pm \rightarrow D[K^-\pi^+\pi^+\pi^-]K^\pm$

## 2. Charmless baryonic $B$ decays

- Triple-product asymmetries

- $B^0 \rightarrow p\bar{p}K^+\pi^-$

## 3. Charmless 3-body $B$ decays

- Impact of strong phase motion on  $CP$  violation structure

- Binned analysis of  $B^+ \rightarrow h^+h'^+h'^-$

- Amplitude analysis of  $B^+ \rightarrow \pi^+h'^+h'^-$

# $\gamma$ from $B$ decays

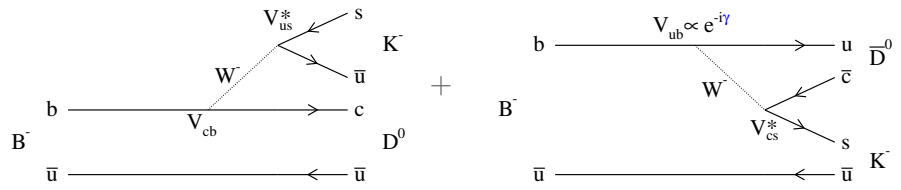
Theoretically cleanest Standard Model measurement from  $B^\pm \rightarrow DK^\pm$   
 $|\delta\gamma|/\gamma \lesssim \mathcal{O}(10^{-7})$  from electroweak corrections

J. Brod and J. Zupan, JHEP **01** (2014) 51

$D^0$  and  $\bar{D}^0$  decay to the same final state

Interference between  $b \rightarrow c\bar{u}s$  and  $b \rightarrow u\bar{c}s$  transitions

$$A_{B^-} \propto A_{D^0} + r_B e^{i\delta_B} e^{-i\gamma} A_{\bar{D}^0}$$



$r_B$ : Ratio of Cabibbo-suppressed to Cabibbo-favoured diagrams

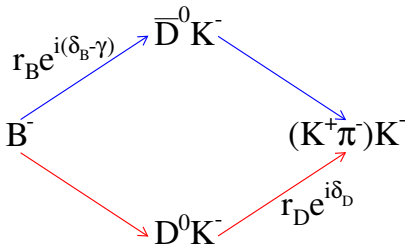
$\delta_B$ : Relative strong phase difference

Phase difference between  $A_{B^+}$  and  $A_{B^-}$  gives  $\gamma$



Match suppressed  $B$  decay with favoured  $D$  decay and *vice versa*

D. Atwood, I. Dunietz and A. Soni, PRL **78** (1997) 3257



Enhances observed  $CP$  asymmetries over other  $\gamma$  methods

$$\Gamma_{B^\pm} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D \pm \gamma)$$

Cost is additional hadronic parameters from  $D$  decays,  $r_D e^{i\delta_D}$

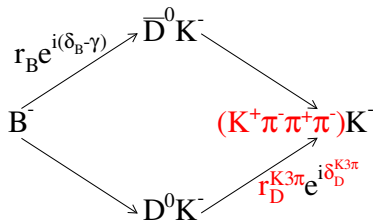
Inputs typically taken from external measurements

Quantum-correlated  $D\bar{D}$  production experiments: BESIII, CLEO-c

$r_D$  from  $D\bar{D}$  mixing measurements: LHCb

Significant source of systematic uncertainty

Approach can be adapted to multibody  $D$  decays



Hadronic  $D$  decay parameters  $r_D^{K3\pi} e^{i\delta_D^{K3\pi}}$ , vary across phase space

External measurements provide averages over phase space

Dilution of decay rate asymmetry,  $R_D^{K3\pi}$

$$R_D^{K3\pi} e^{i\delta_D^{K3\pi}} \propto \int A_{\bar{D}}(\Phi_4) A_D^*(\Phi_4) d\Phi_4$$

$\Phi_4$ : Position in 4-body phase space

$$\Gamma_{B^\pm} = (r_B)^2 + (r_D^{K3\pi})^2 + 2r_B r_D^{K3\pi} R_D^{K3\pi} \cos(\delta_B + \delta_D^{K3\pi} \pm \gamma)$$

Rate further corrected to account for neutral  $D^0$ - $\bar{D}^0$  oscillations

# $B^\pm \rightarrow D[K^-\pi^+\pi^+\pi^-]K^\pm$ at LHCb

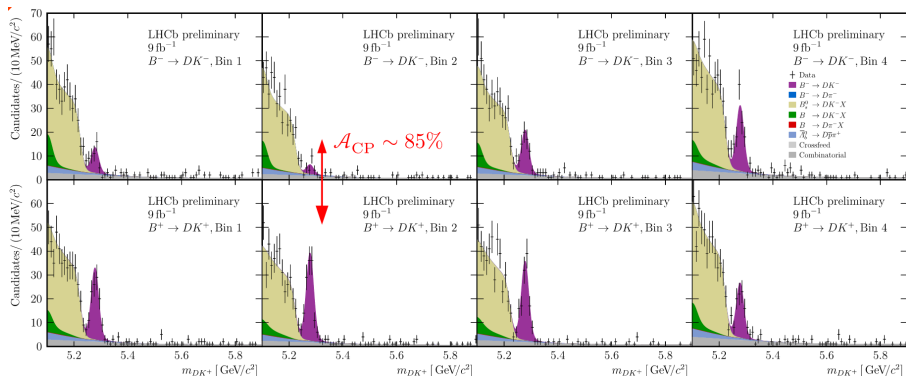
Multibody ADS-like approach further refined to recover sensitivity to  $\gamma$   
 Determine hadronic  $D$  decay parameter averages in bins of phase space

Driven by  $D^0 \rightarrow K^\mp\pi^\pm\pi^\pm\pi^\mp$  amplitude analysis

LHCb collaboration, EPJC **78** (2018) 443

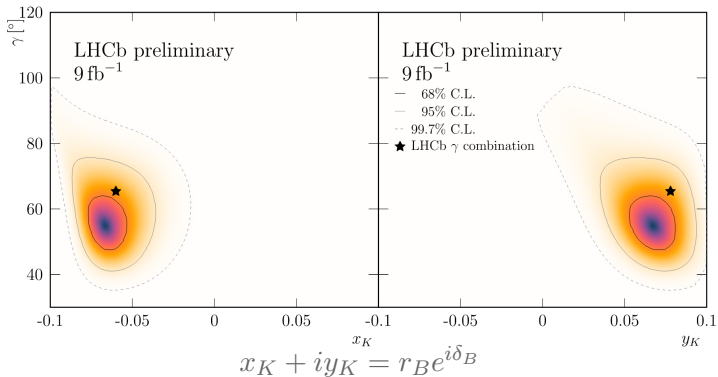
$r_D^{K3\pi}$ ,  $\delta_D^K 3\pi$  and  $R_D^{K3\pi}$  averages from BESIII, CLEO-c and LHCb input

LHCb-PAPER-2022-017 in preparation



# $B^\pm \rightarrow D[K^-\pi^+\pi^+\pi^-]K^\pm$ at LHCb

Combine  $B^\pm$  decay rates and  $D$  decay parameters to measure  $\gamma$



$$r_B = [94.6_{-3.1}^{+3.1} \text{ (stat)} \quad +0.5_{-0.5} \text{ (syst)} \quad +3.0_{-2.3} \text{ (ext)}] \times 10^{-3}$$

$$\delta_B = [134.6_{-6.0}^{+6.0} \text{ (stat)} \quad +0.7_{-0.7} \text{ (syst)} \quad +8.6_{-8.7} \text{ (ext)}]^\circ$$

$$\gamma = [54.8_{-5.8}^{+6.0} \text{ (stat)} \quad +0.6_{-0.6} \text{ (syst)} \quad +6.7_{-4.3} \text{ (ext)}]^\circ$$

Limited by external measurements of hadronic  $D$  decay parameters

Expected to be improved by BESIII in near future

## 1. Measurement of the $CP$ -violating phase $\gamma$

-ADS method

$$-B^\pm \rightarrow D[K^-\pi^+\pi^+\pi^-]K^\pm$$

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-Triple-product asymmetries

$$-B^0 \rightarrow p\bar{p}K^+\pi^-$$

## 3. Charmless 3-body $B$ decays

-Impact of strong phase motion on  $CP$  violation structure

-Binned analysis of  $B^+ \rightarrow h^+h'^+h'^-$

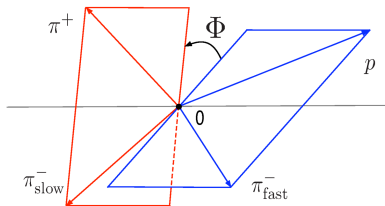
-Amplitude analysis of  $B^+ \rightarrow \pi^+h'^+h'^-$

Rich resonant structure in 4-body decays conducive to  $CP$  violation  
 Amplitude analysis ambitious, begin with model-independent approach  
 Probe  $CP$  violation with triple-product asymmetry measurements

$P$ -odd triple products

$$B: C_{\hat{T}} = \vec{p}_p \cdot (\vec{p}_{\pi_{\text{fast}}^-} \times \vec{p}_{\pi^+}) \propto \sin \Phi$$

$$\bar{B}: \bar{C}_{\hat{T}} = \vec{p}_{\bar{p}} \cdot (\vec{p}_{\pi_{\text{fast}}^+} \times \vec{p}_{\pi^-}) \propto \sin \bar{\Phi}$$



$P$ -odd asymmetries of  $\hat{T}$  operator

$$B: A_{\hat{T}} = \frac{N(C_{\hat{T}} > 0) - N(C_{\hat{T}} < 0)}{N(C_{\hat{T}} > 0) + N(C_{\hat{T}} < 0)}$$

$$\bar{B}: \bar{A}_{\hat{T}} = \frac{\bar{N}(-\bar{C}_{\hat{T}} > 0) - \bar{N}(-\bar{C}_{\hat{T}} < 0)}{\bar{N}(-\bar{C}_{\hat{T}} > 0) + \bar{N}(-\bar{C}_{\hat{T}} < 0)}$$

$P$ -odd observable

$$a_P^{\hat{T}\text{-odd}} = \frac{1}{2}(A_{\hat{T}} + \bar{A}_{\hat{T}})$$

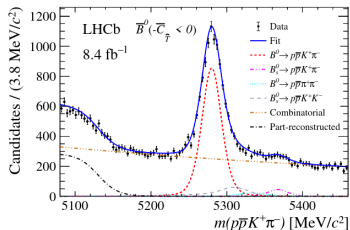
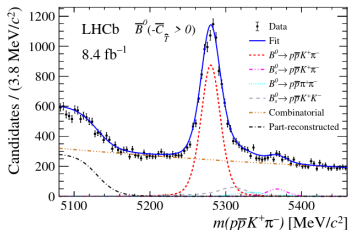
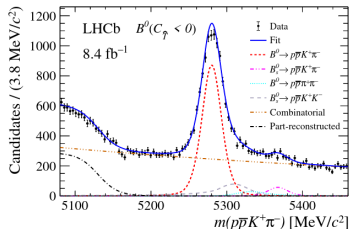
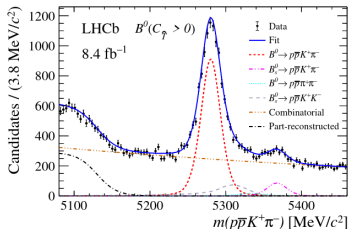
$CP$ -odd observable

$$a_{CP}^{\hat{T}\text{-odd}} = \frac{1}{2}(A_{\hat{T}} - \bar{A}_{\hat{T}})$$

Sensitive to interference between  $P$ -even and  $P$ -odd amplitudes

# $B^0 \rightarrow p\bar{p}K^+\pi^-$ at LHCb

LHCb-PAPER-2022-003

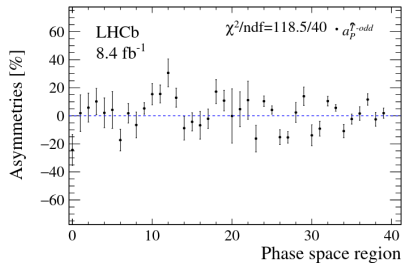
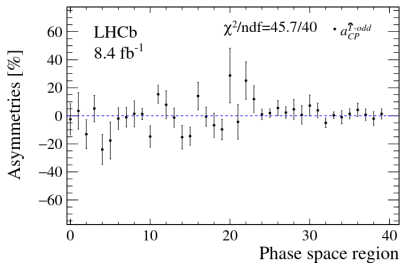


$$a_P^{\hat{T}^{\text{odd}}} = [1.49 \pm 0.85 \text{ (stat)} \pm 0.08 \text{ (syst)}]\%$$

$$a_{CP}^{\hat{T}^{\text{odd}}} = [0.51 \pm 0.85 \text{ (stat)} \pm 0.08 \text{ (syst)}]\%$$

Can enhance sensitivity by dividing phase space into bins

LHCb-PAPER-2022-003



Significant  $P$  violation in low  $p\bar{p}$  and  $K^*(892)^0$  mass regions

$P$  conservation rejected at  $\sim 6\sigma$

$CP$  conserved within  $\sim 1\sigma$

Theoretical prediction up to 20% level not excluded



## 1. Measurement of the $CP$ -violating phase $\gamma$

-ADS method

$$-B^{\pm} \rightarrow D[K^{-}\pi^{+}\pi^{+}\pi^{-}]K^{\pm}$$

## 2. Charmless baryonic $B$ decays

-Triple-product asymmetries

$$-B^0 \rightarrow p\bar{p}K^{+}\pi^{-}$$

## 3. Charmless 3-body $B$ decays

-Impact of strong phase motion on  $CP$  violation structure

-Binned analysis of  $B^{+} \rightarrow h^{+}h'^{+}h'^{-}$

-Amplitude analysis of  $B^{+} \rightarrow \pi^{+}h'^{+}h'^{-}$

Direct  $CP$  violation more complicated in  $B \rightarrow 3h$  decay channels compared to 2-body decays

There are at least 4 possible sources of strong phase

## 1. Short-distance contributions (quark level)

BSS mechanism, PRL **43** 242 (1979)

Tree contribution (a)

Penguin diagram (b) contains 3 quark generations in loop

$S$ -matrix unitarity,  $CPT$  require absorptive amplitude

If gluon in penguin is timelike (on-shell)

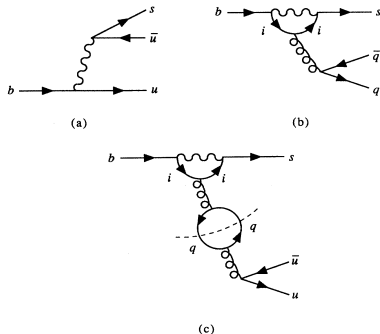
Momentum transfer  $q^2 > 4m_i^2$   
where  $i = u, c$

Imaginary part depends on quark masses

Particle rescattering (c) generates a phase difference

$CP$  violation in 2-body processes caused by this effect

eg.  $B^0 \rightarrow K^+\pi^-$



Remaining sources more associated with multibody decays

Long-distance contributions (hadronic level)

## 2. Breit-Wigner phase

Propagator represents intermediate resonance states

$$T_R^{\text{BW}}(s) = \frac{1}{m_R^2 - s - im_R\Gamma_R(s)}$$

Phase varies across mass-squared,  $s$

## 3. Relative $CP$ -even phase in the isobar model

$$A(B \rightarrow f) = \sum_i |A_i| e^{i(\delta_i + \phi_i)}$$

$$\bar{A}(\bar{B} \rightarrow \bar{f}) = \sum_i |\bar{A}_i| e^{i(\delta_i - \phi_i)}$$

Related to final state interactions between different resonances

## Manifestation of $CP$ violation

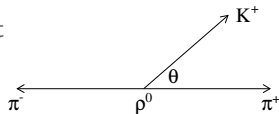
Each source of strong phase leaves a unique signature in phase space  
 Illustrate with series of examples

Consider  $B^\pm \rightarrow K^\pm \pi^+ \pi^-$  with only 2 isobars

$B^\pm \rightarrow \rho^0 K^\pm$  and flat non-resonant (NR) component

$\rho^0$  lineshape a Breit-Wigner,  $T_\rho^{\text{BW}}$

$\rho^0$  is a vector resonance, so angular distribution follows  $\cos \theta$



$$B^+ : A_+ = |a_+^\rho| e^{i\delta_+^\rho} T_\rho^{\text{BW}} \cos \theta + |a_+^{\text{NR}}| e^{i\delta_+^{\text{NR}}}$$

$$B^- : A_- = |a_-^\rho| e^{i\delta_-^\rho} T_\rho^{\text{BW}} \cos \theta + |a_-^{\text{NR}}| e^{i\delta_-^{\text{NR}}}$$

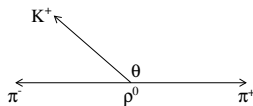
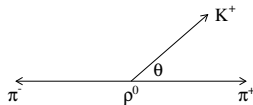
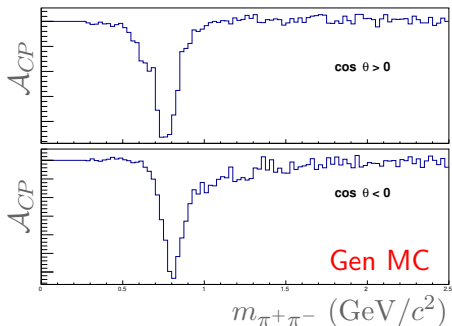
$$\begin{aligned} \mathcal{A}_{CP} &\propto |A_-|^2 - |A_+|^2 \\ &\propto (|a_-^\rho|^2 - |a_+^\rho|^2) |T_\rho^{\text{BW}}|^2 \cos^2 \theta \dots \\ &\quad - 2(m_\rho^2 - s) |T_\rho^{\text{BW}}|^2 \cos \theta \dots \\ &\quad + 2m_\rho \Gamma_\rho |T_\rho^{\text{BW}}|^2 \cos \theta \dots \end{aligned}$$

# Short-distance effects

$$\begin{aligned}
 \mathcal{A}_{CP} \propto & (|a_-^\rho|^2 - |a_+^\rho|^2) |T_\rho^{\text{BW}}|^2 \cos^2 \theta \dots \\
 & -2(m_\rho^2 - s) |T_\rho^{\text{BW}}|^2 \cos \theta \dots \\
 & +2m_\rho \Gamma_\rho |T_\rho^{\text{BW}}|^2 \cos \theta \dots
 \end{aligned}$$

Only depends on  $\rho$  resonance

Maximum difference at  $\rho$  pole, quadratic in helicity



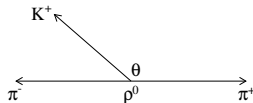
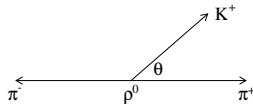
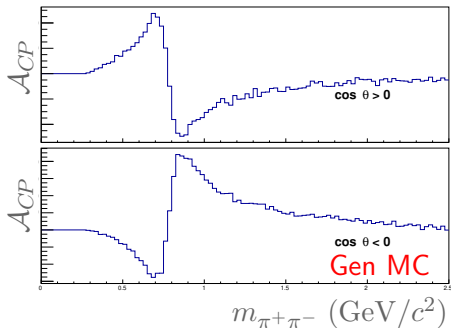
Only short-distance effects can create  $|a_+^\rho| \neq |a_-^\rho|$

# Long-distance effects

$$\begin{aligned}
 \mathcal{A}_{CP} &\propto (|a_-^\rho|^2 - |a_+^\rho|^2) |T_\rho^{BW}|^2 \cos^2 \theta \dots \\
 &\quad - 2(m_\rho^2 - s) |T_\rho^{BW}|^2 \cos \theta \dots \\
 &\quad + 2m_\rho \Gamma_\rho |T_\rho^{BW}|^2 \cos \theta \dots
 \end{aligned}$$

Interference term from real part of Breit-Wigner

Zero at  $\rho$  pole, linear in helicity



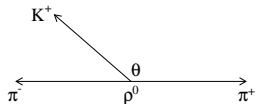
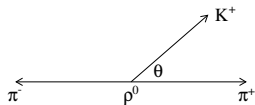
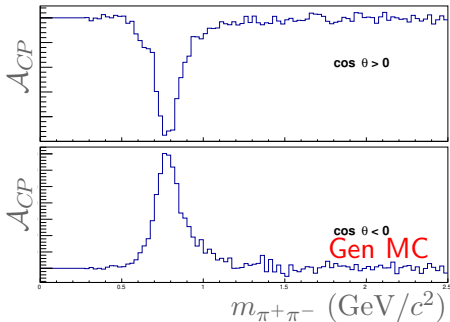
Caused by long-distance effects from final state interactions

# Long-distance effects

$$\begin{aligned}
 \mathcal{A}_{CP} &\propto (|a_-^\rho|^2 - |a_+^\rho|^2) |T_\rho^{\text{BW}}|^2 \cos^2 \theta \dots \\
 &\quad - 2(m_\rho^2 - s) |T_\rho^{\text{BW}}|^2 \cos \theta \dots \\
 &\quad + 2m_\rho \Gamma_\rho |T_\rho^{\text{BW}}|^2 \cos \theta \dots
 \end{aligned}$$

Interference term from imaginary part of Breit-Wigner

Maximum at  $\rho$  pole, linear in helicity



Caused by long distance effects from Breit-Wigner phase and final state interactions

Last source of strong phase

## 4. Final state $KK \leftrightarrow \pi\pi$ rescattering

Can occur between decay channels with the same flavour quantum numbers

eg.  $B^\pm \rightarrow K^\pm K^+ K^-$  and  $B^\pm \rightarrow K^\pm \pi^+ \pi^-$

$CPT$  conservation constrains hadron rescattering

For given quantum numbers, sum of partial widths equal for charge-conjugate decays

$KK \leftrightarrow \pi\pi$  rescattering generates a strong phase

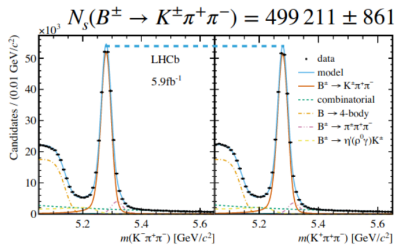
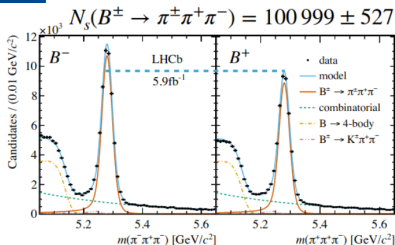
Look into rescattering region

If rescattering phase in one decay channel generates direct  $CP$  violation in this region

Rescattering phase should generate opposite sign direct  $CP$  violation in partner decay channel

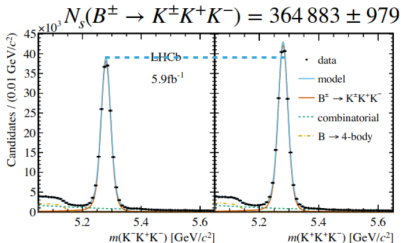
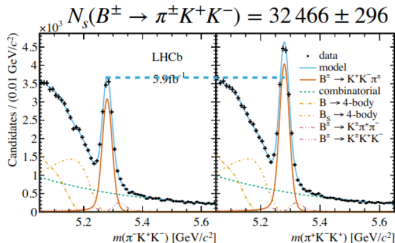


# $B^+ \rightarrow h^+ h'^+ h'^-$ at LHCb



$$A_{CP} = +0.080 \pm 0.004 \pm 0.003 \pm 0.003 \quad (14.1\sigma)$$

$$A_{CP} = +0.011 \pm 0.002 \pm 0.003 \pm 0.003 \quad (2.4\sigma)$$

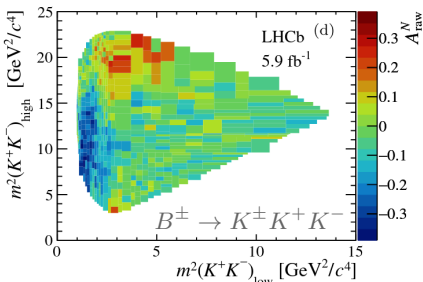
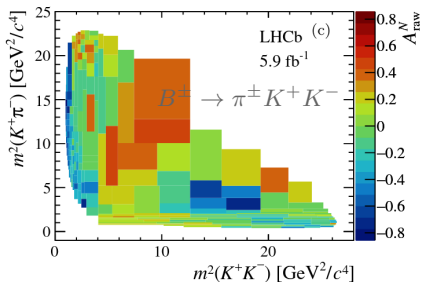
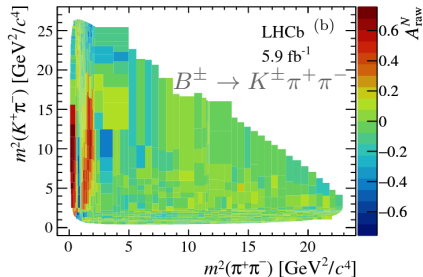
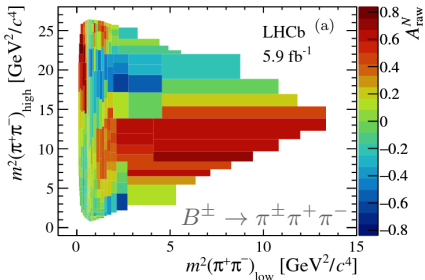


$$A_{CP} = -0.114 \pm 0.007 \pm 0.003 \pm 0.003 \quad (13.6\sigma)$$

$$A_{CP} = -0.037 \pm 0.002 \pm 0.002 \pm 0.003 \quad (8.5\sigma)$$

LHCb-PAPER-2021-049

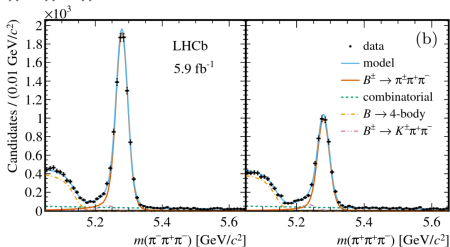
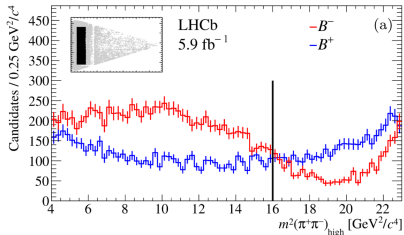
# $B^+ \rightarrow h^+ h'^+ h'^-$ at LHCb



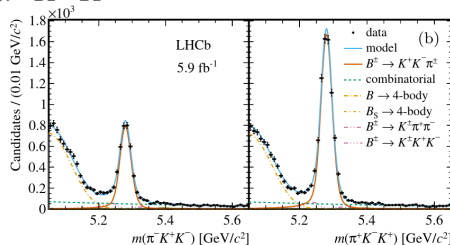
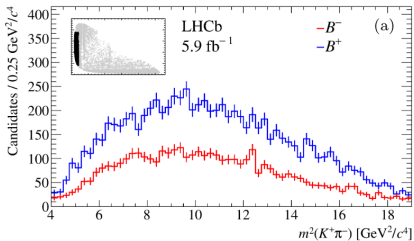
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# $B^+ \rightarrow \pi^+ h'^+ h'^-$ rescattering region

$$B^+ \rightarrow \pi^+ \pi^+ \pi^-$$

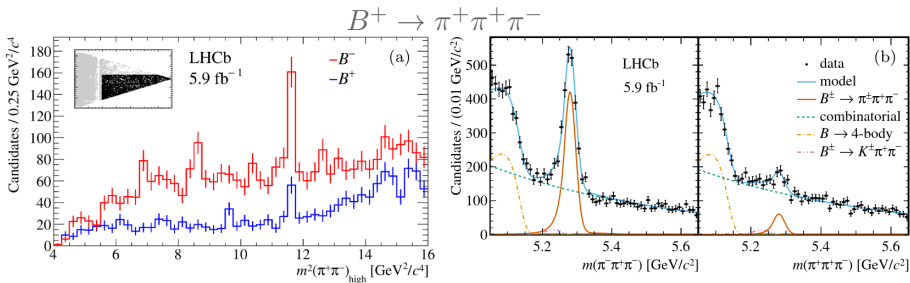


$$B^+ \rightarrow \pi^+ K^+ K^-$$



Clear opposite sign  $CP$  asymmetry in  $CPT$ -coupled  $KK \leftrightarrow \pi\pi$  channels

# $B^+ \rightarrow \pi^+ h'^+ h'^-$ charmonium region



Large amount of  $CP$  violation observed

Double-charm rescattering mechanism proposed

I. Bediaga, T. Frederico and P.C. Magalhães, PLB **806** (2020) 135490

Clear  $CP$  violation involving  $\chi_{c0}(1P)$

Short-distance  $CP$  violation not expected

Large long-distance  $CP$  violation through interference predicted long ago

G. Eilam, M. Gronau and R.R. Mendel, PRL **74** (1995) 4984

Amplitude model sum of contributions to the phase space

$$A^\pm(\Phi_3) = \sum_i A_i^\pm(\Phi_3) = \sum_i c_i^\pm F_i(\Phi_3)$$

$\Phi_3$ : position in phase space

$c_i^\pm$ : complex free parameters of the model

$F_i$ : Decay form factor comprised of several components

Dynamic lineshape, eg. Breit-Wigner

Spin amplitude

Production and decay barrier factors

S-wave description difficult, increasingly turning to multiple approaches

Isobar

Each contribution has clear physical meaning

K-matrix

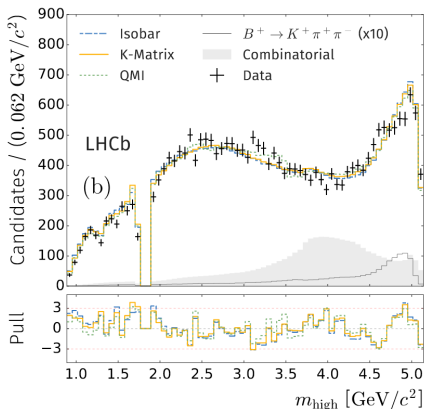
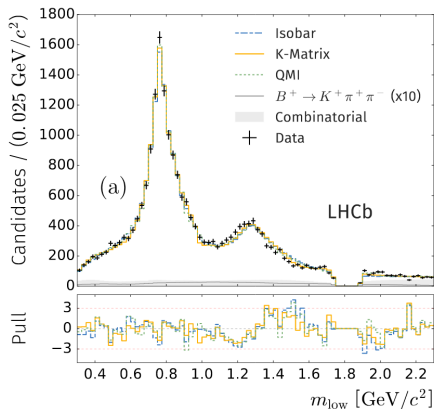
Experimental interface scattering results that enforce 2-body unitarity

Quasi-model-independent

Binned amplitude determined directly from data

# $B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ at LHCb

LHCb Collaboration, PRD **101** (2020) 012006



$B^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  has two identical pions

$m_{\text{low}}$  is the lower  $\pi^+ \pi^-$  invariant mass combination

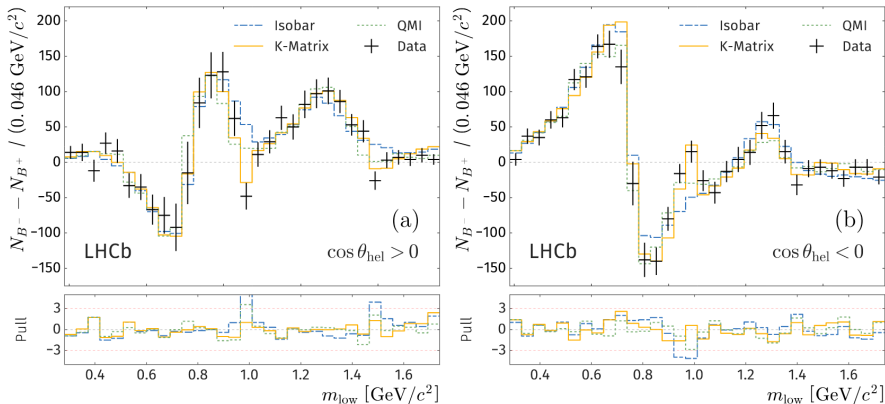
Enhances resonance visibility

$m_{\text{high}}$  is the higher  $\pi^+ \pi^-$  invariant mass combination

Shows spin structure

# Long-distance $CP$ violation by interference

LHCb Collaboration, PRD **101** (2020) 012006



Asymmetry sign-flip across  $\rho(770)^0$  pole in opposing helicity halves

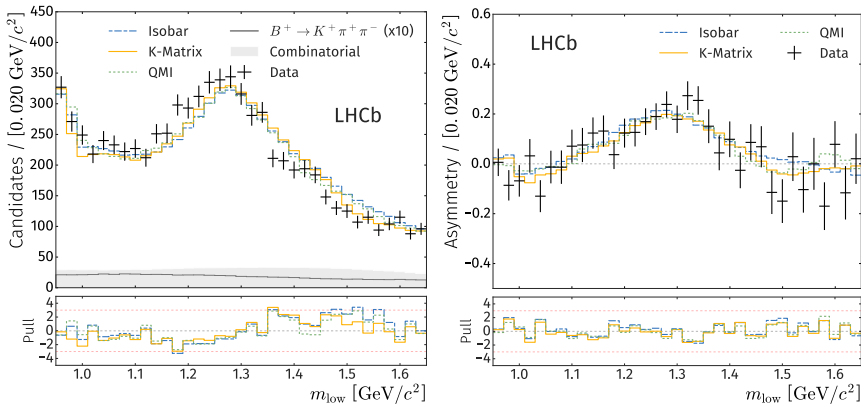
$CP$  violation generated by interference between overlapping S- and P-waves

Over  $25\sigma$  statistical significance

First observation of  $CP$  violation in S-P interference

# Short-distance $CP$ violation in $f_2(1270)$ region

LHCb Collaboration, PRD **101** (2020) 012006



Mass poorly described by all 3 S-wave approaches

Can be resolved, but requires more statistics to confirm

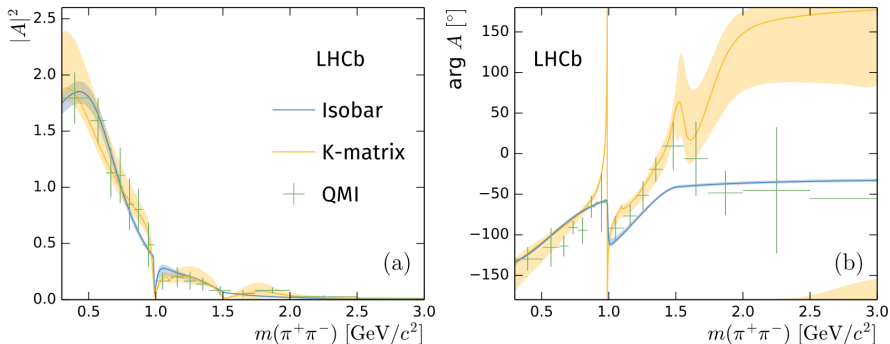
Very large  $CP$  asymmetry well-described by all 3 S-wave approaches

Observation of  $CP$  violation ranges from exceeds  $14\sigma$  (statistical)

First observation of  $CP$  violation in any process involving a tensor



LHCb Collaboration, PRD **101** (2020) 012006



Good agreement on structures in  $|A|^2$

Structure in phase motion qualitatively agreed on

Potential to drive further theoretical work

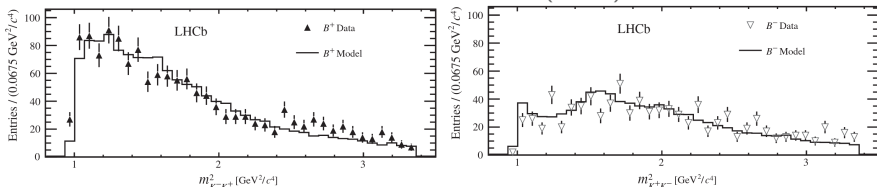
Need Isobar form factors to improve as these have physical meaning

# $B^\pm \rightarrow \pi^\pm K^+ K^-$ at LHCb

$\pi\pi \leftrightarrow KK$  rescattering model for the low  $K^+K^-$  mass

J. R. Peláez and F. J. Ynduráin, PRD **71** (2005) 074016

LHCb Collaboration, PRL **123** (2019) 231802



Largest  $CP$  violation in a single amplitude ever observed

$$\mathcal{A}_{CP} = (-66.4 \pm 3.8 \text{ (stat)} \pm 1.9 \text{ (syst)})\%$$

Multibody decays provide excellent environment for  $CP$  violation studies

- Large measurements more accessible

- Diverse structures provide another view to strong phase motion

Recent results from LHCb

Model-independent measurement of  $\gamma$  in  $B^\pm \rightarrow D[K^-\pi^+\pi^+\pi^-]K^\pm$

- Significant contributor to the  $\gamma$  average

- Cooperation with BESIII required to reduce dominant systematic

Triple-product asymmetries in  $B^0 \rightarrow p\bar{p}K^+\pi^-$  decays

- Still no observation of  $CP$  violation in baryonic  $B$  decays at this time

- Predicted up to the 20% level

Model-independent study of 3-body charmless hadronic  $B^\pm$  decays

- Attention should turn to modelling rescattering regions

- $CP$  violation driven by  $\chi_{c0}(1P)$  foreseen

Amplitude analysis of 3-body charmless hadronic  $B^\pm$  decays

- First observation of  $CP$  violation involving S-, D-waves and S-P interference

- Quasi-model-independent results feed back into the theoretical community