



Experimental hadron spectroscopy

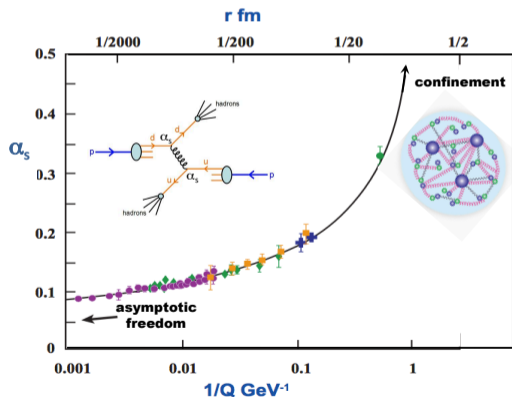
Wolfgang Gradl

International Symposium on Multiparticle Dynamics
1st August 2022

Goal: better understanding of QCD

Quantum Chromodynamics (QCD): strong force, describes interaction of quarks

Study QCD in the regime where non-perturbative effects are important or dominant



Confinement:
observable objects are $SU(3)_C$ singlets,
i.e. colour-neutral bound states

Analogy: atomic spectroscopy

Information on bound systems by observing

- Energy levels
- Transitions between levels

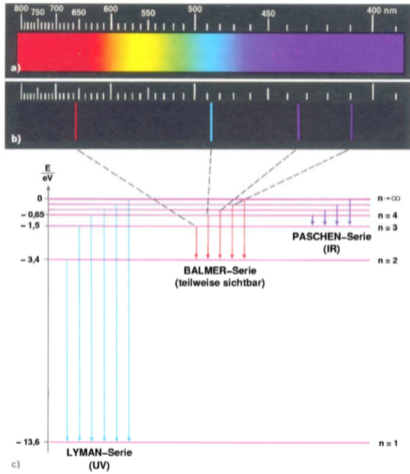
Discovery of discrete spectral lines

➔ Discrete energy levels in atoms

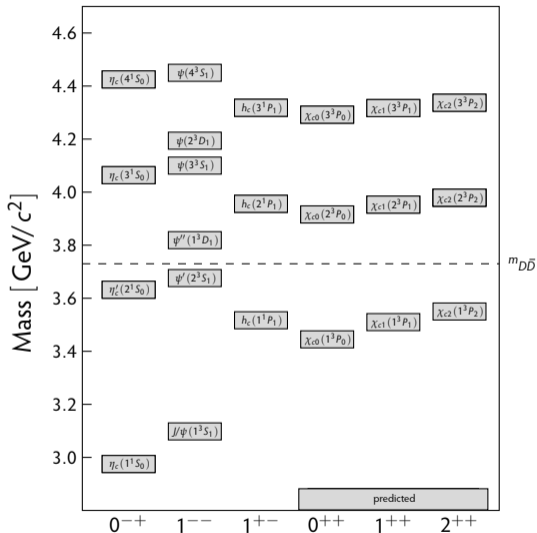
$$E_{nm} = R \left(\frac{1}{n^2} - \frac{1}{m^2} \right)$$

➔ Precision measurements lead to discovery of fine structure, Lamb shift ...

predictions made using QED potential



Example: charmonium spectrum [🍷🍷]



Potential:

$$V_0^{c\bar{c}} = -\frac{4}{3} \frac{\alpha_s}{r} + br + \frac{32\pi\alpha_s}{9m_c^2} \delta(r) \vec{S}_c \vec{S}_{\bar{c}}$$

$$V_{\text{spin-dep.}} = \frac{1}{m_c^2} \left[\left(\frac{2\alpha_s}{r^3} - \frac{b}{2r} \right) \vec{L} \cdot \vec{S} + \frac{4\alpha_s}{r^3} T \right]$$

+ relativistic corrections

Godfrey & Isgur, PRD 32, 189 (1985);

Barnes, Godfrey & Swanson, PRD 72, 054026 (2005)

Use a few well-established states to fix parameters,
then predict remainder of spectrum, and transitions

➔ refine model

The naming of states

spectroscopic notation:

$$n^{2S+1}L_J$$

n radial quantum number

S total spin of quarks

L orbital angular momentum (S, P, D, \dots)

J total angular momentum: $J = |L - S|, \dots, L + S$

Low-lying states historically carry their own names (e.g. J/ψ (1^3S_1), η_c (1^1S_0), ...), indicating quantum numbers and flavour contents

States with the same quantum numbers (and net flavour) can mix

Mixing more pronounced for broad, overlapping states
 \Rightarrow light hadron spectroscopy much more complicated

Properties to determine experimentally

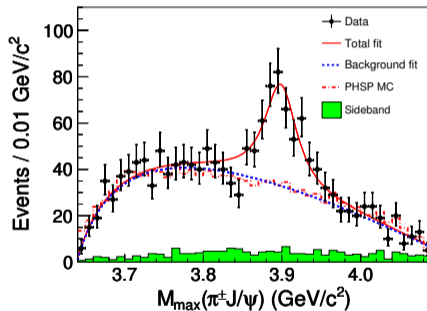
Mass and width (or, more advanced: pole position $M + \frac{i}{2}\Gamma$)

Quantum numbers: spin J , P , C

Quark / flavour composition

Production channels

Decay modes

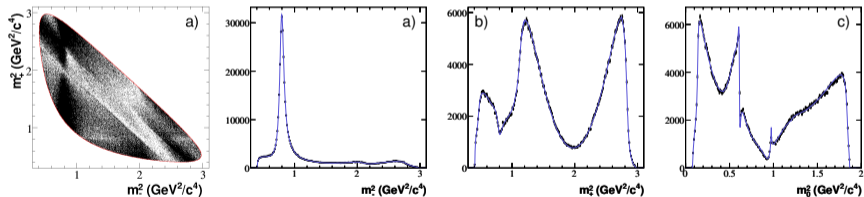


Determine J, P, C

Easy: if state is directly and copiously produced in e^+e^- : $J^{PC} = 1^{--}$

Sometimes, decay modes can provide clues (e.g., $\pi^0\pi^0$ is only possible for $J = \text{even}$)

Multi-body decays: interference with cross-channels provides access to J and P
requires **Dalitz plot**, **partial wave**, **amplitude** analysis



Coherent sum of 10 resonant amplitudes to describe data

BABAR, PRD78 (2008) 034023

Kinematic reflections

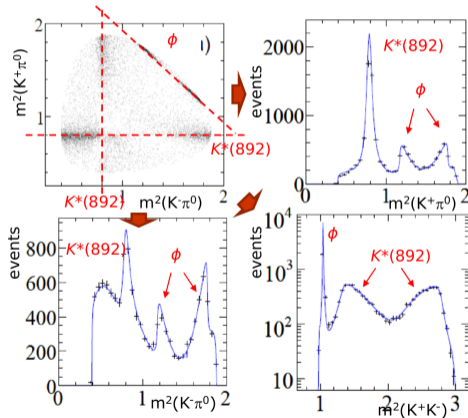
In multi-body decays, resonance in one subchannel can produce peaks in other mass projections (**reflections**)

Not every peak in a mass distribution is a new state!

For example $D^0 \rightarrow K^+ K^- \pi^0$:

relatively easy to understand

decay dominated by $\phi\pi^0$ and $K^{*\pm}K^\mp$



'Exotic' hadrons

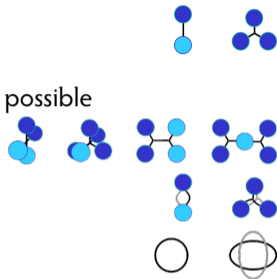
Well-known classes of hadrons: mesons ($q\bar{q}$) and baryons (qqq)

Already on page 1 of the quark model: other colour-neutral combinations possible

multi-quark states (tetraquark, pentaquark, ...)

hybrids (excitation in gluonic degrees of freedom)

glueballs



Manifestly exotic

- Quark contents requires more than $q\bar{q}$ or qqq
- Quantum numbers J^{PC} not reachable for ordinary mesons or baryons

'Cryptoexotic'

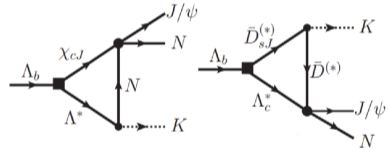
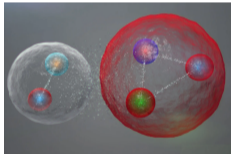
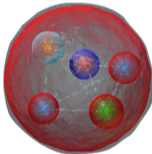
- mass / width not fitting in spectra
- overpopulation of states
- production and/or decay patterns incompatible with standard mesons/baryons

Multiquark states

Search for 'exotics' long-standing motivation for hadron spectroscopy

Now: compelling evidence for multiquark states found in data

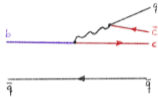
What are they? compact objects, (meson) molecules, triangular singularities?



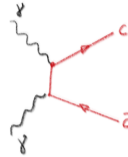
More experimental information needed — other states, line shapes, transitions ...

Exotic hadrons ...and where to find them

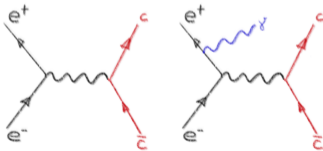
- Decays of hadrons with heavy quarks



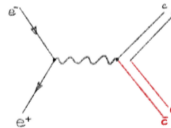
- photon-photon fusion



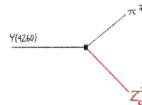
- e^+e^- direct, or via ISR



- double charmonium production



- decays of higher charmonia



- $pp, p\bar{p}$ inclusive
- photo- / electroproduction

Exotic hadrons ...and where to find them

e^+e^-

B factories (*BABAR*, *Belle*, Belle II)

τ -charm factory (BESIII)

Direct production of 1^{--} states (or via ISR)

$\gamma\gamma$ interactions: $C = +1, L$ even states

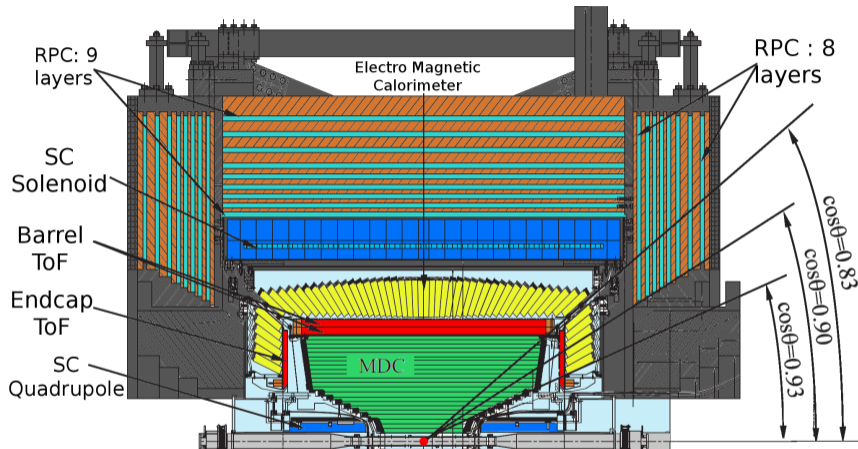
Clean environment, but low cross sections

pp

Production of heavy quarks in initial hard scattering

subsequent hadronisation can produce all sorts of hadrons

At LHC energies: huge production cross sections

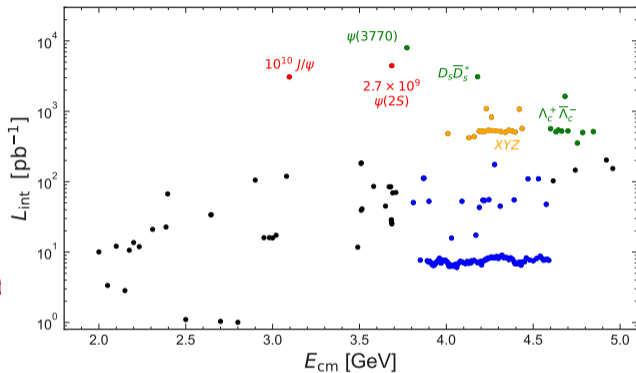


At BEPCII in Beijing: e^+e^- collisions at \sqrt{s} between 2 and 5 GeV

12 years data taking at BESIII

Data sets collected so far include

- 10×10^9 J/ψ events
- 2.7×10^9 ψ' events
- 8 fb^{-1} on $\psi(3770)$
- scan data between 2.0 and 3.08 GeV, and above 3.735 GeV
- large datasets for XYZ studies: scan with $> 500 \text{ pb}^{-1}$ per energy point spaced 10 – 20 MeV apart



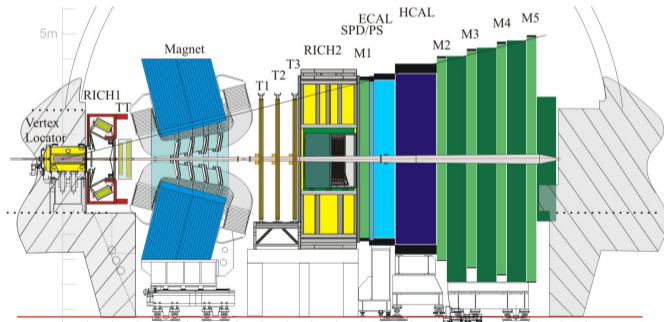
Recent results from BESIII at ISMD2022:

- + **Hadron spectroscopy:** Song Weimin, later this session
- + **R-value measurement:** Christoph Redmer, Tuesday
- + **Light-flavour vector mesons:** Zhang Hao (poster)
- + **Hyperon physics:** Viktor Thorén, Friday

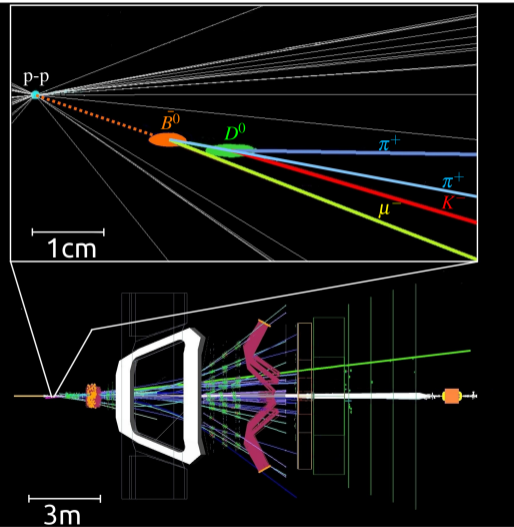
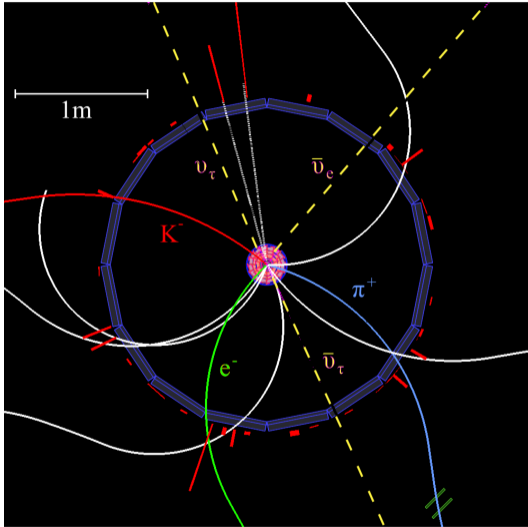
Forward, single-arm spectrometer, pp collisions

Huge production cross sections in fiducial volume: ~ 2.4 mb for $c\bar{c}$, ~ 0.14 mb for $b\bar{b}$ at 13 TeV

Fantastic vertex resolution + large Lorentz boost: decay time resolution 45 fs



e^+e^- vs. pp at LHC energies



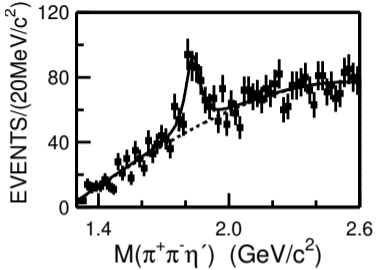
from Ciezarek et al., Nature 546, 227 (2017)

Significant experimental progress in the past several years

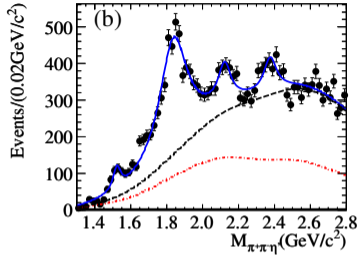
For this talk:

- Light hadron spectroscopy: $X(1835), X(2600) \rightarrow \eta' \pi^+ \pi^-$
and why taking $10^{10} J/\psi$ events was not a bad idea
- Charmonium-like states in e^+e^- collisions:
the story of $Y(4260)$
- exotic states at LHCb:
the power of ultra-high statistics

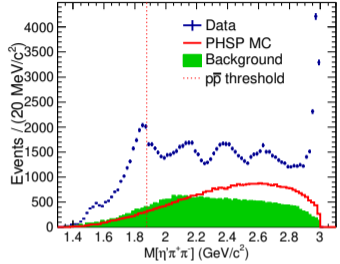
$$J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$$



$58 \times 10^6 J/\psi$ events
 BES, PRL 95 (2005) 262001



$225.2 \times 10^6 J/\psi$ events
 BESIII, PRL 106 (2011) 072002



$1090 \times 10^6 J/\psi$ events
 BESIII, PRL 117 (2016) 042002

Structure just at or below $p\bar{p}$ threshold: $X(1835)$

Non-trivial lineshape: try to fit with Flatté or sum of interfering Breit-Wigners

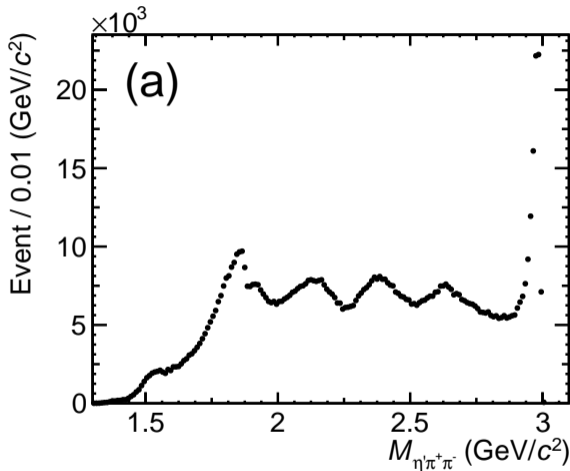
Additional structures: $X(2120)$, $X(2370)$, ??

$$J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$$

$10\,087 \times 10^6 J/\psi$ events

Confirmation of $X(1835)$, $X(2120)$, and $X(2370)$

New structure $X(2600)$
 J^{PC} to be determined



$$J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$$

$10\,087 \times 10^6 J/\psi$ events

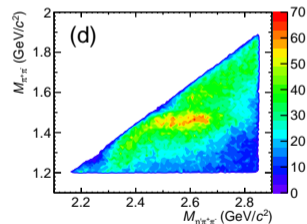
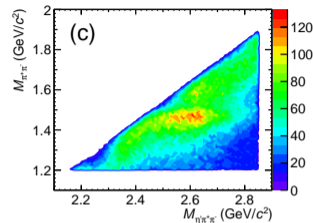
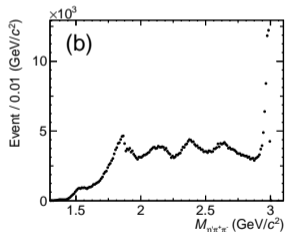
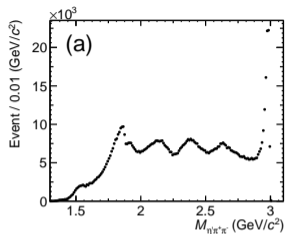
Confirmation of $X(1835)$, $X(2120)$, and $X(2370)$

New structure $X(2600)$

J^{PC} to be determined

connected to complicated structure in $m_{\pi^+ \pi^-}$ around 1.5 GeV

more studies needed!



$X(1835)$

Seen in radiative J/ψ decays to $\eta' \pi^+ \pi^-$
and in Dalitz decays $J/\psi \rightarrow e^+ e^- \eta' \pi^+ \pi^-$

Threshold enhancement in $J/\psi \rightarrow \gamma p \bar{p}$

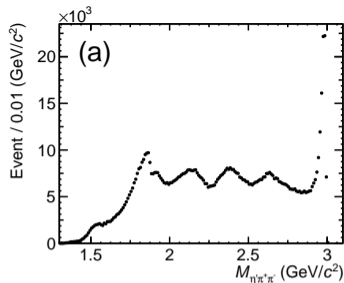
$X(1835)$ seen in other decay modes:

- $J/\psi \rightarrow \gamma 3(\pi^+ \pi^-)$ [225M J/ψ , BESIII, PRD 88 (2013) 091502(R)]
- $J/\psi \rightarrow \eta K_S^0 K_S^0$ [1.3B J/ψ , BESIII, PRL 115 (2015) 091803]
- $J/\psi \rightarrow \gamma \gamma \phi$ [1.3B J/ψ , BESIII, PRD 97 (2018) 051101(R)]

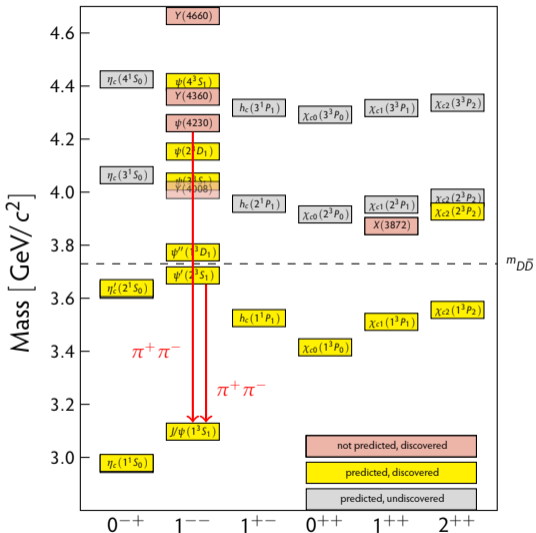
$K_S^0 K_S^0$ and $\gamma \phi$ decays seem to indicate non-negligible $s\bar{s}$ component

➔ second radial excitation of η' ?

Connection to threshold enhancement seen in $J/\psi \rightarrow \gamma p \bar{p}$? Two close-by states?



$$\psi(4230) \rightarrow J/\psi \pi^+ \pi^-$$



e^+e^- collisions near $\Upsilon(4S)$

in ISR production, $e^+e^- \rightarrow \gamma_{\text{ISR}} J/\psi \pi^+ \pi^-$

$$\Rightarrow J^{PC} = 1^{--}$$

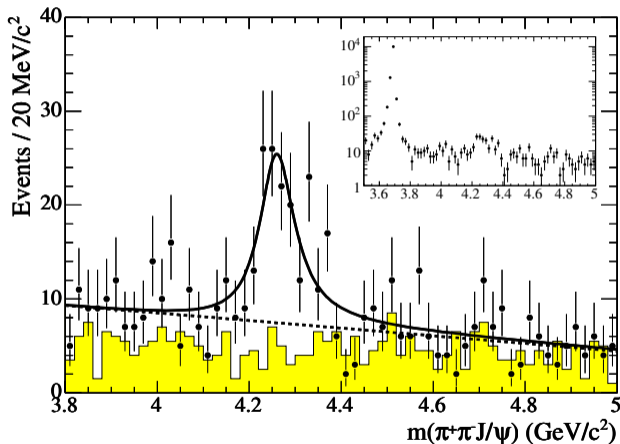
Supernumerary vector state:

all 'ordinary' $c\bar{c}$ vector states already seen

$\psi(4230) \rightarrow J/\psi \pi^+ \pi^-$

BABAR, 211 fb⁻¹, PRL 95 (2005) 142001

Discovered by BABAR in $e^+e^- \rightarrow \gamma_{\text{ISR}} J/\psi \pi^+ \pi^-$



Fit with single Breit-Wigner

$$M = 4259 \pm 8_{-6}^{+2} \text{ MeV}$$

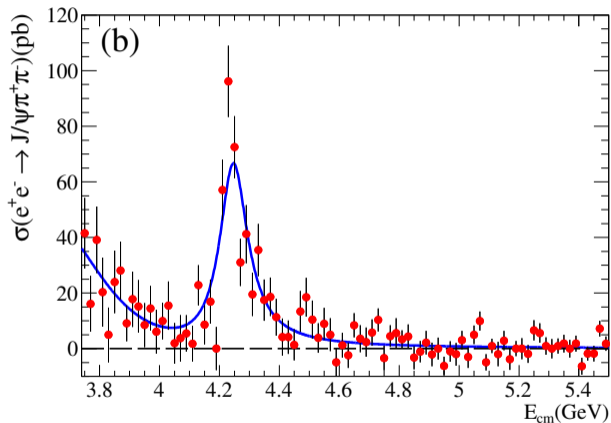
$$\Gamma = 88 \pm 23_{-4}^{+6} \text{ MeV}$$

Call this structure $\Upsilon(4260)$

$\psi(4230) \rightarrow J/\psi \pi^+ \pi^-$

BABAR, 454 fb^{-1} , PRD 86 (2012) 051102

BABAR update with double the data set



Fit with single Breit-Wigner

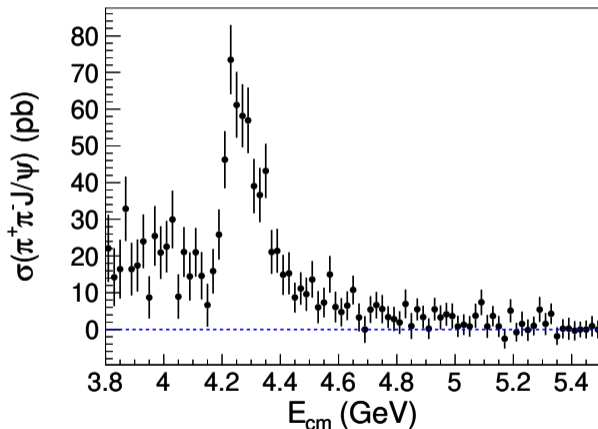
$$M = 4244 \pm 5 \pm 4 \text{ MeV}$$

$$\Gamma = 114_{-15}^{+16} \pm 7 \text{ MeV}$$

$\psi(4230) \rightarrow J/\psi \pi^+ \pi^-$

Belle, 967 fb^{-1} , PRL 110 (2013) 252002

Belle measurement, using ISR, $2 \times$



Single Breit-Wigner fit to line shape
still satisfactory

$$M = 4248.6 \pm 8.3 \pm 12.1 \text{ MeV}$$

$$\Gamma = 134.1 \pm 16.4 \pm 5.5 \text{ MeV}$$

$\psi(4230) \rightarrow J/\psi \pi^+ \pi^-$

BESIII, PRL 118, 092001 (2017)

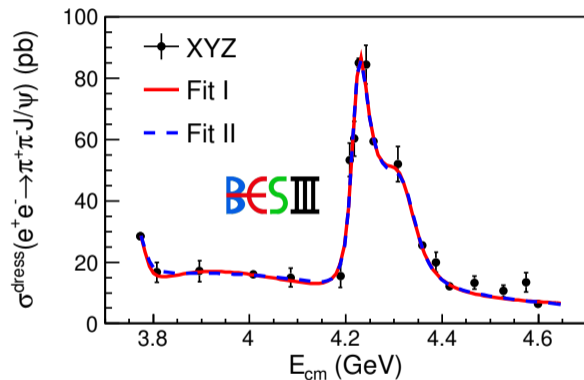
BESIII: make use of first batch of XYZ scan data set

Single Breit-Wigner not appropriate to fit line shape

Two-resonance fit:

Parameter	Fit 1 / MeV	Fit 2 / MeV
$M(R_1)$	$3812.6^{+61.9}_{-96.6}$...
$\Gamma_{\text{tot}}(R_1)$	$476.9^{+78.4}_{-64.8}$...
$M(R_2)$	4222.0 ± 3.1	4220.9 ± 2.9
$\Gamma_{\text{tot}}(R_2)$	44.1 ± 4.3	44.1 ± 3.8
$M(R_3)$	4320.0 ± 10.4	4326.8 ± 10.0
$\Gamma_{\text{tot}}(R_3)$	$101.4^{+25.3}_{-19.7}$	$98.2^{+25.4}_{-19.6}$

Fit 1, Fit 2: different treatment of non-resonant contribution



→ high-statistics datasets essential to resolve finer structure of line shape

$\psi(4230)$ in different decay channels

pdgLive Home > $c\bar{c}$ MESONS > $\psi(4230)$ > $\psi(4230)$ MASS

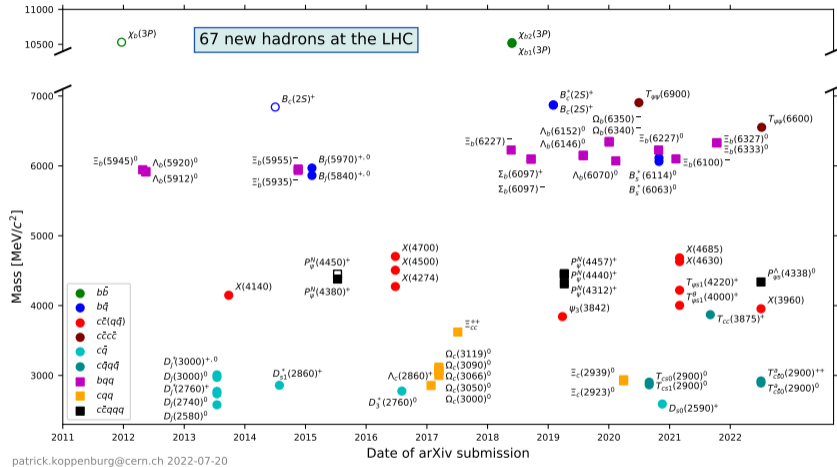
$\psi(4230)$ MASS

INSPIRE search

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
4222.7 ± 2.6	OUR AVERAGE	Error includes scale factor of 1.7. See the ideogram below.		
4234.4 ± 3.2 ± 0.2		¹ ABLIKIM	2021AJ BES3	$e^+ e^- \rightarrow \pi^+ \pi^- \psi(2S)$
4216.7 ± 8.9 ± 4.1		² ABLIKIM	2020AG BES3	$e^+ e^- \rightarrow \mu^+ \mu^-$
4220.4 ± 2.4 ± 2.3		³ ABLIKIM	2020N BES3	$e^+ e^- \rightarrow \pi^0 \pi^0 J/\psi$
4218.6 ± 3.8 ± 2.5		³ ABLIKIM	2020O BES3	$e^+ e^- \rightarrow \eta J/\psi$
4218.5 ± 1.6 ± 4.0		⁴ ABLIKIM	2019AI BES3	$e^+ e^- \rightarrow \omega \chi_{c0}$
4228.6 ± 4.1 ± 6.3		ABLIKIM	2019R BES3	$e^+ e^- \rightarrow \pi^+ D^0 D^{*-} + \text{c.c.}$
4200.6 $^{+7.9}_{-13.3}$ ± 3.0		⁵ ABLIKIM	2019V BES3	$e^+ e^- \rightarrow \gamma \chi_{c1}(3872)$
4222.0 ± 3.1 ± 1.4		⁶ ABLIKIM	2017B BES3	$e^+ e^- \rightarrow \pi^+ \pi^- J/\psi$
4218 $^{+5.5}_{-4.5}$ ± 0.9		ABLIKIM	2017G BES3	$e^+ e^- \rightarrow \pi^+ \pi^- h_c$

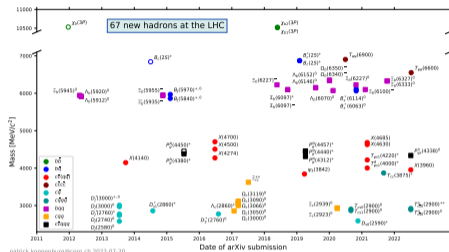
PDG now calls the narrow structure $\psi(4230)$ — seen in many different decay modes, mainly charmonium + light meson(s)

New hadrons discovered at the LHC



<https://www.nikhef.nl/~pkoppenb/particles.html>

New hadrons discovered at the LHC



59 of these seen at LHCb

- Conventional hadrons with heavy flavour (c , b) excited open-charm mesons, doubly-charmed baryons Ξ_{cc} , ...
- Hidden-charm pentaquarks P_{ψ}^N
- Hidden-charm tetraquark candidates
- Tetraquarks with double-charm contents

Far too many to cover in one talk ...

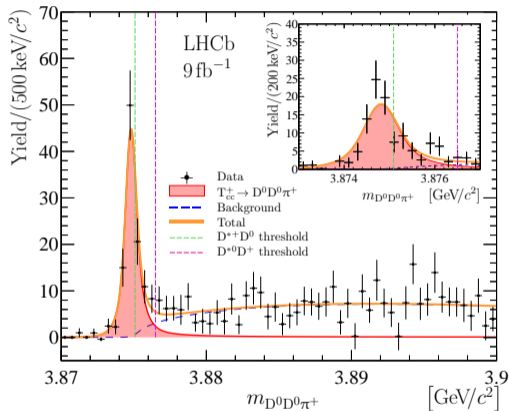
pick out two striking, recent examples:

$$\rightarrow T_{cc}(3875)^+$$

$$\rightarrow T_{c\bar{s}0}^a(2900)^{++} \text{ and } T_{c\bar{s}0}^a(2900)^0$$

Doubly-charmed tetraquark $T_{cc}(3875)^+$

LHCb, Nat. Phys. 18, 751 (2022)



Background-subtracted $D^0 D^0 \pi^+$ mass spectrum

Select two D^0 candidates from same primary vertex, combine with π^+

Clear peak just below $D^* D$ thresholds; decay proceeds likely via off-shell D^{*+}

LHCb, Nat Commun 13, 3351 (2022)

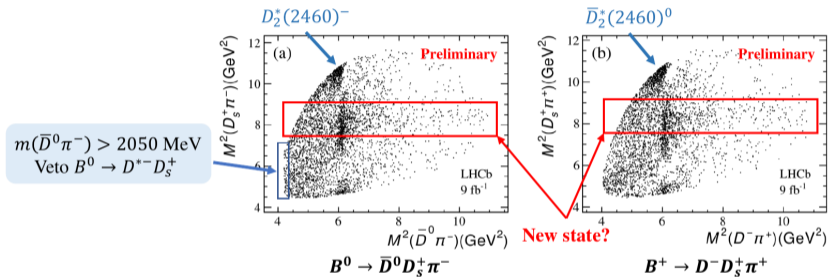
Extremely narrow!

Minimal quark contents: $cc\bar{u}\bar{d}$

- + manifestly exotic
- + prompt production in pp collisions strongly suggests that this is a bound state

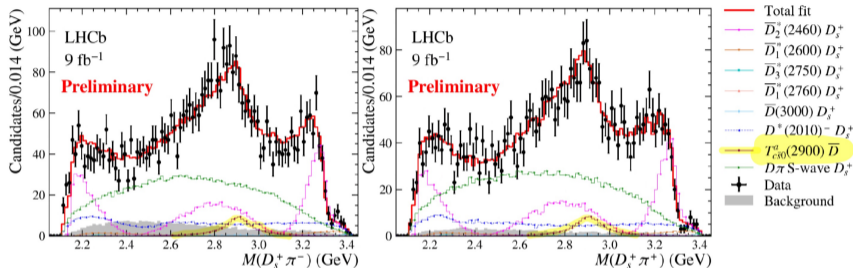
$$T_{c\bar{s}0}^a(2900) \rightarrow D_s^+ \pi$$

Study $B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$ and $B^+ \rightarrow D^- D_s^+ \pi^+$; perform simultaneous amplitude analysis



$$T_{c\bar{s}0}^a(2900) \rightarrow D_s^+ \pi^-$$

Study $B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$ and $B^+ \rightarrow D^- D_s^+ \pi^+$; perform simultaneous amplitude analysis



Doubly-charged tetraquark $T_{c\bar{s}0}^a(2900)^{++} \rightarrow D_s^+ \pi^+$ and neutral partner $T_{c\bar{s}0}^a(2900)^0 \rightarrow D_s^+ \pi^-$
 $J^P = 0^+$ favoured

Four quark flavours: $c\bar{s}u\bar{d}$ and $c\bar{s}d\bar{u}$

Summary

- Compelling evidence for multi-quark states seen by various experiments
not only 'charged charmonium-like states' such as $Z_c(3900)^+$ a.k.a. $T_\psi^b(3900)^+ \rightarrow J/\psi \pi^+$, but
doubly-charmed $T_{cc}(3875)^+$
doubly-charged $T_{c\bar{s}0}^a(2900)^{++}$ + spin-exotic candidates
- Begin to see whole families of such states in data
Large, clean datasets required
Sophisticated amplitude analyses needed to measure quantum numbers
- Connection between these states?
Can we identify the same state in different datasets, with different production mechanisms?
- So, question shifts from "where are they?" to "what are they?"
Experimental input essential