

Thoughts About The Interface

(By theorists, with Natalie Klco and Alessandro Roggero)

Martin J Savage

Qubit Technology Interface control fields

with qubit system

InQubator for Quantum Simulation (IQuS)

UNIVERSITY of WASHINGTON

What does my Title mean?

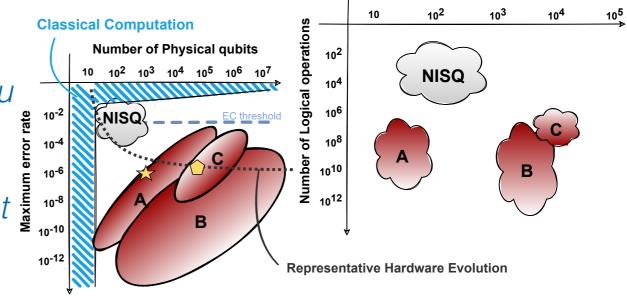
I was asked to give a broader discussion

- We have heard so many interesting talks and great progress!
- Thoughts about going forward in simulations of the Standard Model ...
 with Alessandro Roggero and Natalie Klco arXiv:2107.04769v1 [quant-ph] 10 Jul 2021

Thinking about questions such as (analogous to HPC):

If someone gives you access to a quantum device with 1000 physical qubits with a given connectivity, fixed quantum volume, and a maximum of one million "shots" and asks you to compute a SM quantity of impact - what would you do?

- a) 1 or 2 really good logical qubit probably not
- b) 1000 really poor qubits probably not
- c) Compute using a different Hamiltonian maybe



Number of Logical qubits

Elements in Talk

Entanglement

Collaboration

Complexity

Advancing QIS



Simulating Field Theory

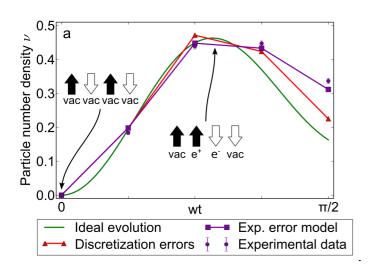
Co-design Co-development

~ 2016 - The Awakening (in the US)



An Office of Science review sponsored jointly by

Identified beyond exascale problems in HEP and NP Real-time, finite density, many-body



Innsbruck demonstration of real-time dynamics in QFT ORNL calculations of deuteron binding energy

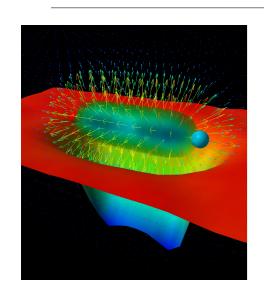


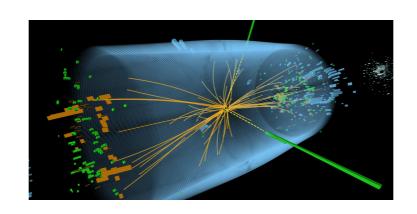
Cloud-accessible quantum devices become available [Available devices have improved dramatically since]

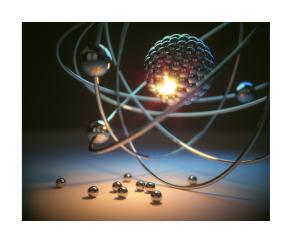
There had been many pioneering theoretical and algorithm developments related to quantum simulations of QFTs and QMBs for scientific applications (on top of QI advances): Banuls, Bermudez, Cirac, Jansen, Jordan, Lee, Lewenstein, Muller, Muschik, Preskill, Weise, Zohar, Zoller, many others

Looking for a quantum advantage

Do not scale well using classical computers

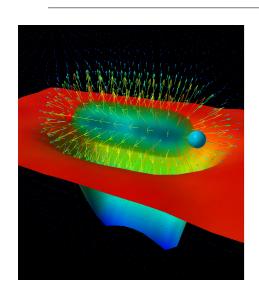


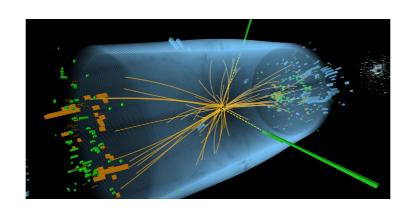


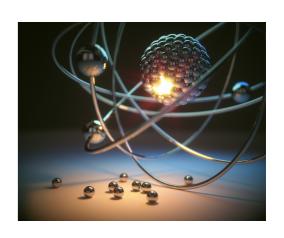


- Real-time Minkowski space evolution
 - highly-inelastic processes, fragmentation, S-matrices
 - non-equilibrium systems
- Large Hilbert spaces quantum field theories, large nuclei
- High-density potentially mitigate classical sign problem(s)

Targets for Quantum Simulation







Quantum Field Theories and Symmetries

- indefinite particle number
- gauge symmetries (constraints)
- entangled states

Real-Time Dynamics

- parton showers and fragmentation
- neutrinos in matter
- early universe
- phase transitions matter?
- non-equilibrium heavy-ions
- nuclear reactions
- neutrino-nucleus interactions

Matter

- neutron stars
- gravity waves ?
- Heavy nuclei
- chemical potentials
- entanglement

I just have to say ...





QCQC: NASA International Conference on Quantum Computing and Quantum Communications

© 1999

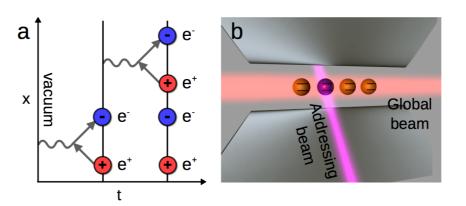
Quantum Computing and Quantum Communications

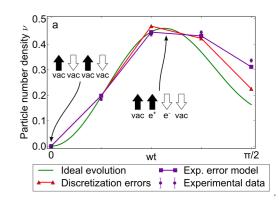
First NASA International Conference, QCQC'98 Palm Springs, California, USA February 17–20, 1998 Selected Papers

Editors (view affiliations)
Colin P. Williams

Real-time dynamics of lattice gauge theories with a few-qubit quantum computer

Esteban A. Martinez,^{1,*} Christine Muschik,^{2,3,*} Philipp Schindler,¹ Daniel Nigg,¹ Alexander Erhard,¹ Markus Heyl,^{2,4} Philipp Hauke,^{2,3} Marcello Dalmonte,^{2,3} Thomas Monz,¹ Peter Zoller,^{2,3} and Rainer Blatt^{1,2}



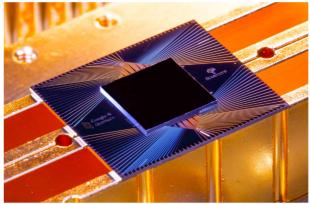


rticle Nature **574**, pages 505–510 (2019), 23 October 2019

Quantum supremacy using a programmable superconducting processor

https://doi.org/10.1038/s41586-019-1666-5 Received: 22 July 2019 Accepted: 20 September 2019 Published online: 23 October 2019

Frank Arute¹, Kunal Arya¹, Ryan Babbush¹, Dave Bacon¹, Joseph C. Bardin¹², Rami Barends¹, Rupak Biswas³, Sergio Boixo¹, Fernando G. S. L. Brandao¹⁴, David A. Buell¹, Brian Burkett¹, Yu Chen¹, Zijun Chen¹, Ben Chiaro³, Roberto Collins³, William Courtney¹, Andrew Dunsworth Edward Farhi¹, Brooks Foxen¹⁵, Austin Fowler¹, Craig Gidney¹, Marissa Giustina¹, Rob Graff¹, Keith Guerin¹, Steve Habegger¹, Matthew P. Harrigan¹, Michael J. Hartmann¹⁶, Alan Ho³, Markus Hofffmann¹, Trent Huang¹, Travis S. Humble², Sergei V. Isakov¹, Evan Jeffrey¹.



Credit: Erik Lucero/Google

Amazed by what has been collectively accomplished! Excellent published works and reviews - I will not be reviewing

Quantum Systems

Quantum mechanics "works the same" at all scales we have probed

- The promise to simulate systems at one scale with systems at another with fidelity (Feynman, Benioff, Manin and others)



First digital devices became cloud accessible ~ 5 years ago - increasing selections of qudits+fabrics

How to map systems we want to simulate to the systems we control? How do we connect the constituents to perform operations? What do we measure (and want to)?

[most answers are correct at present]

What are the "New" Features Beyond HPC?

Quantum-2 provides access to controllable entanglement and coherence in devices for computation

- Hilbert spaces scaling similar to many-body configuration space
- Real-time evolution is in **BQP** (bounded-error requiring polynomial scaling quantum resources)
- ``Bounded Errors theorists and designers can trade-off uncertainties
 - more axes for creativity

Requires us to think ``coherently"

Theory to Simulation

Domain Scientists

Algorithms Identify problem Map to qubits and gates

Quantum Software

Express in native gates/connectivity
Compile & compress circuits
Deploy error correction strategy



Control Engineering

Implement Hamiltonian control with E/M fields

$$i\hbar \frac{\partial |\Psi\rangle}{\partial t} = H(t)|\Psi\rangle$$

Qubit Technology

Interface control fields with qubit system



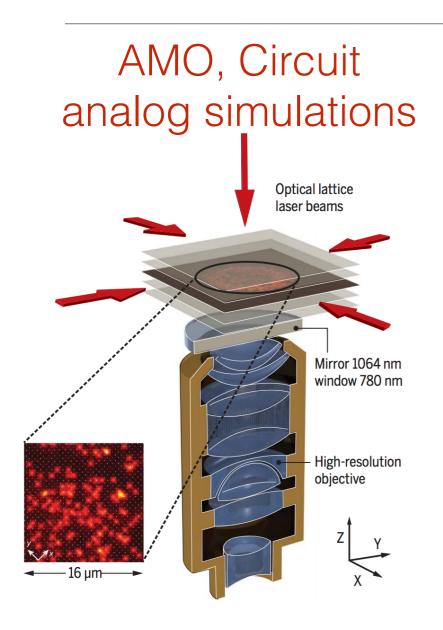
Where many of us in this meeting "sit" How, what?

Depends on available hardware Relies heavily on QC community Benefits from our HPC developments

How we (mostly) engage with devices APIs

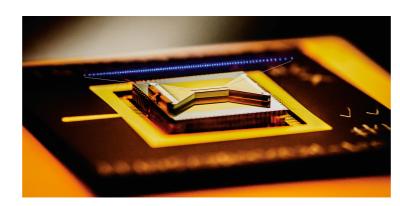
Tech companies and in-house Benefit from our HPC developments

Hardware Development — examples



H: native to system e.g. atoms in optical lattices SRF cavities BECs

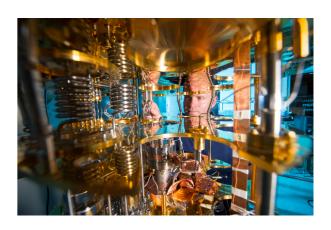
Digital computations

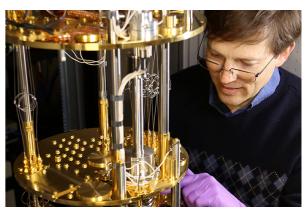




e.g. trapped-ions,superconducting qubitsH: universal gate sets

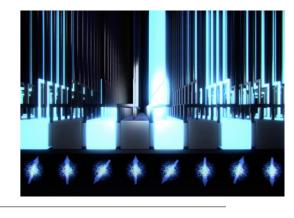
High-Q Cavities





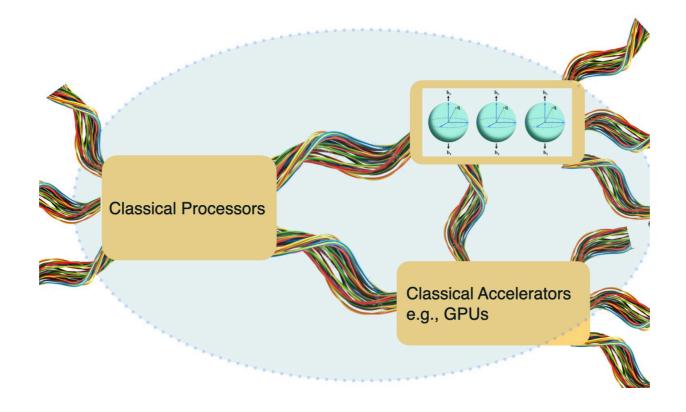
e.g. High-Q RF cavities, classically prepare controls to perform quantum operations

Environments



Quantum devices embedded in HPC environment - Hybrid

- If the system to simulate is (essentially) classical then use HPC
- basis dependent entanglement choose efficient basis
 - identify quantum "parts" of algorithm, e.g., VQE



Entanglement - Perspective

In part:

20th Century HEP - QFT

- —"chasing" short-distance fundamental interactions
- nonperturbative lattice QCD using HPC
- modeling gave way to EFTs leading order separable

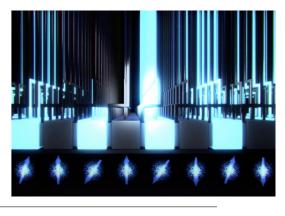
20th Century NP - QMB systems

- "handling" short-distance (phenomenological) repulsion
 - ended NT for a few years! Re-invigorated by RG and EFT from HEP
- quantum many-body computations using HPC
- modeling gave way to EFTs

21st Century HEP+NP - QFT+QMB systems

quantum correlations and non-locality using/for quantum simulation and quantum computing

Entanglement

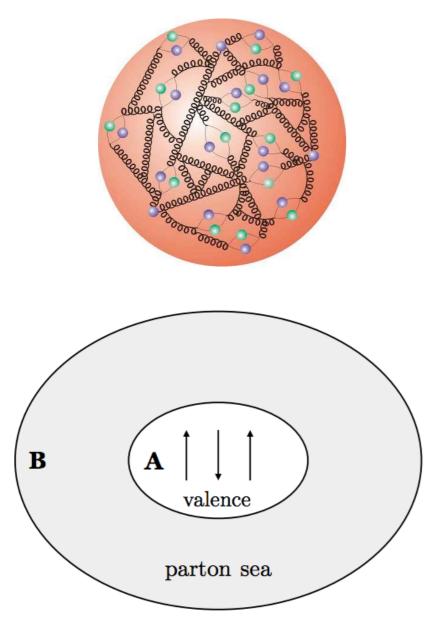


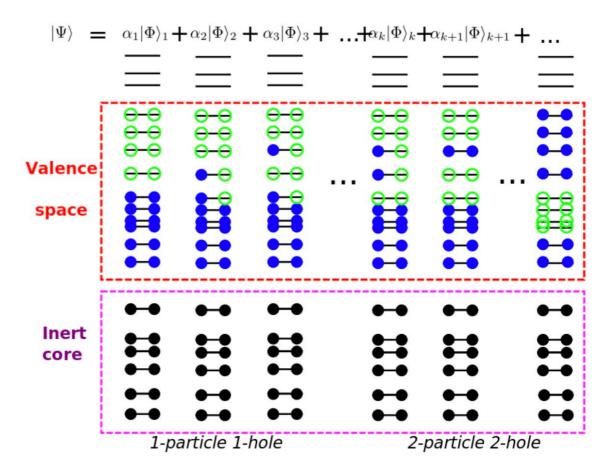
What are the potential roles of entanglement?

- -organzational principle
- -order parameter
- -insight into structure
- -thermalization
- -geometry
- -simulation design
- -computational complexity

Entanglement - Order Parameters, Structures

Beane, Ehlers



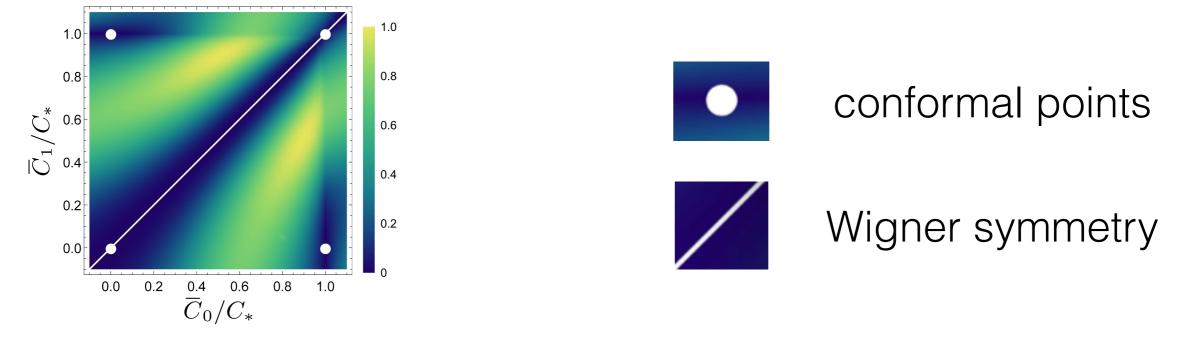


 $| shell model (LO) > = | core > \otimes | valence >$

Entanglement - Emergent Symmetries

$$\hat{\mathbf{S}}_{\sigma} = \frac{1}{4} \left(3e^{i2\delta_3} + e^{i2\delta_1} \right) \hat{\mathbf{1}} + \frac{1}{4} \left(e^{i2\delta_3} - e^{i2\delta_1} \right) \hat{\boldsymbol{\sigma}} \cdot \hat{\boldsymbol{\sigma}} \qquad \qquad \mathcal{E}(\hat{\mathbf{S}}_{\sigma}) = \frac{1}{6} \sin^2 \left(2(\delta_3 - \delta_1) \right)$$

Finding GS of n-body system is in **QMA**-complete - generally beyond QC



SU(4) for 2 flavors and **SU(16)** for 3 flavors (seen in LQCD calculations) - more symmetry than large-Nc, [SU(4) and SU(6)]

Emergent approximate symmetries in nuclear systems

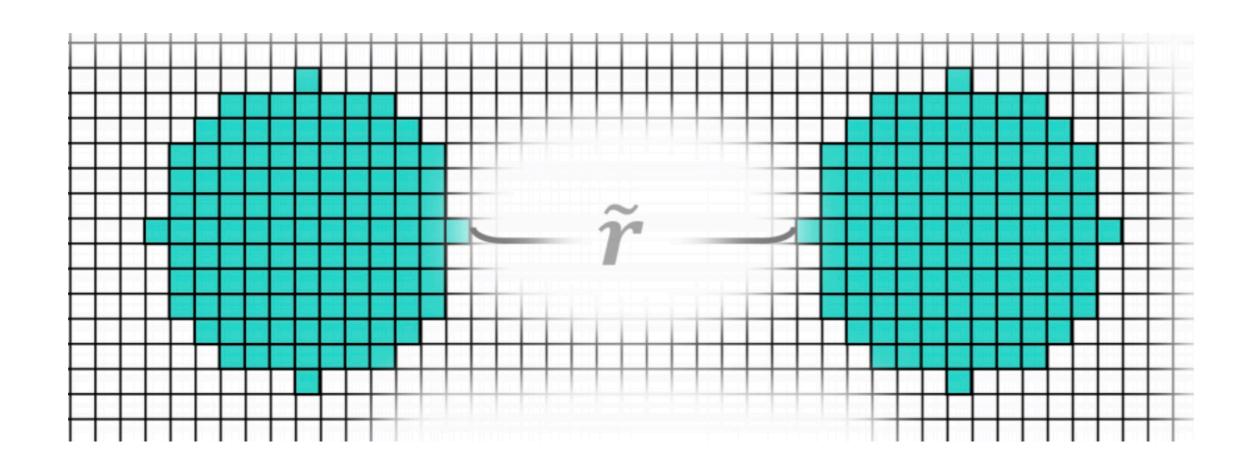


Suppressed fluctuations in entanglement

Suppressed sign problems in classical simulations

Entanglement in Simulation - Subtle

Harmonic chains - many really interesting QI works during the last 20 years Relevant to finite-resource computations



Entanglement - Not Always Beyond Classical

Stabilizer states can be entangled and classically evolved efficiently for certain quantum circuits (Gottesman)

e.g., 3-qubit GHZ states circuits with Paulis, H,S and CNOT.

T-gate required for Universal QC, requires beyond classical. (e.g., single qubit rotations)

.... entanglement alone is insufficient to require a quantum device

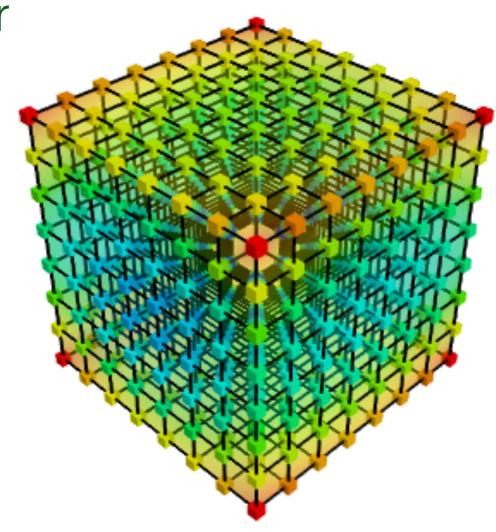
Mapping and Scaling

Expect that n-dof locally interacting for time T requires

n-dof evolved through ~T time steps for a total of

~ nT operations. (fermions : ~ poly(n) T)

D-dim systems optimally simulated with D-dim systems.



e.g., a 2-dim systems of spins will not optimally simulate a 3-dim system of locally interacting dof.

Implications for 3-d QFT and QMBs co-design i.e., understand how to "simply" scale between system and device

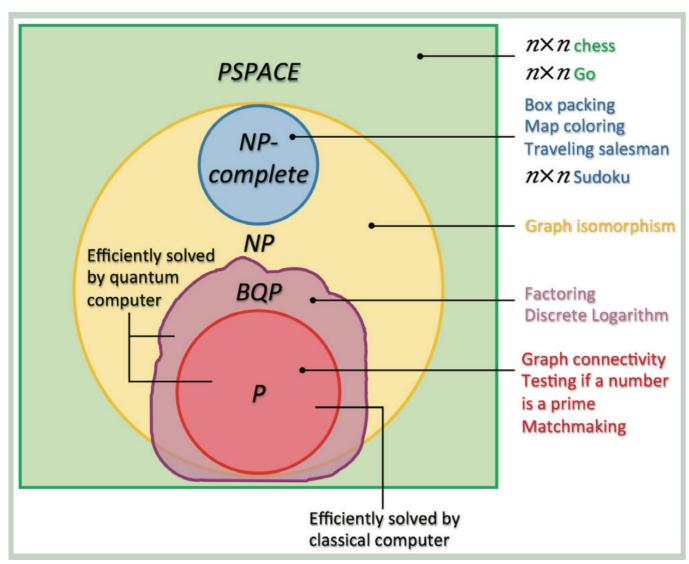
e.g., Exploring Trotterization for Real Time Evolution

Lloyd, Childs, others LCU, .. e.g., H= Ha + Hbe-iHb δ t e-iHa δ t e-iHb δ t e-iHa δ t e-iHa δ t $|\Psi\rangle$ - e - i Η t |Ψ> 2t/nTime 0.25ht 20

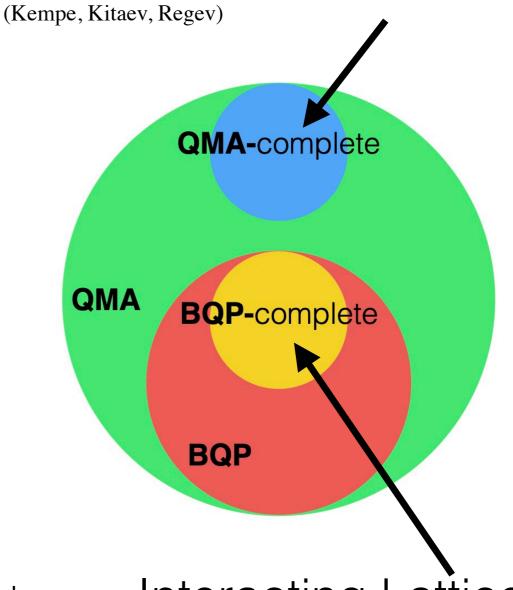
Heyl, Hauke, Zoller, Science 2019

Complexity The scaling of resources required to solve a problem

Scott Aaronson, Sci. Am.



g.s. of k-local Hamiltonian

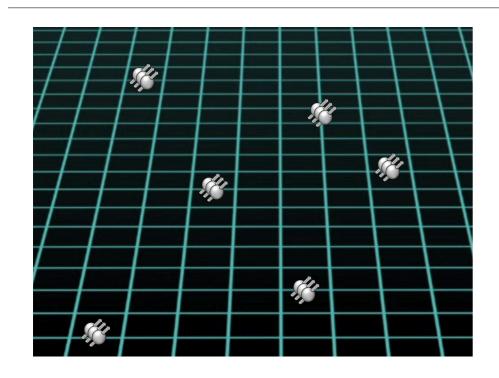


BQP = Polynomial scaling quantum resources to achieve a given precision (Bounded Error) **BPP** (Bounded Probabilistic Polynomial) in BQP

Interacting Lattice Scalar Field Theory

(Jordan, Krovi, Lee, Preskill)

Quantum Field Theories



- Finite lattice to support the fields
- •3-dim
- Real-time Hamiltonian evolution
- Fields mapped to qubits/qudits
- BCs
- Hybrid tasks for QPU?
- Different mappings (most "efficient" path to continuum physics?)
 - "qubits arranged" with fermions on sites and gauge fields on links (KS)
 - or continuum fields de-localized. (e.g. quantum link models)
 - truncations/samplings in gauge rotations or irreps
 - and/or Integrate out gauge freedoms
 - and/or Gauss's law explicit/implicit, error correction to enforce

Truncations, convergence and errors (gauge field, spacetime)
Ultimately, we will need to establish a complete quantification of uncertainties.

Scattering in Scalar Field Theory -Gold Standard for Algorithmic Design for SM

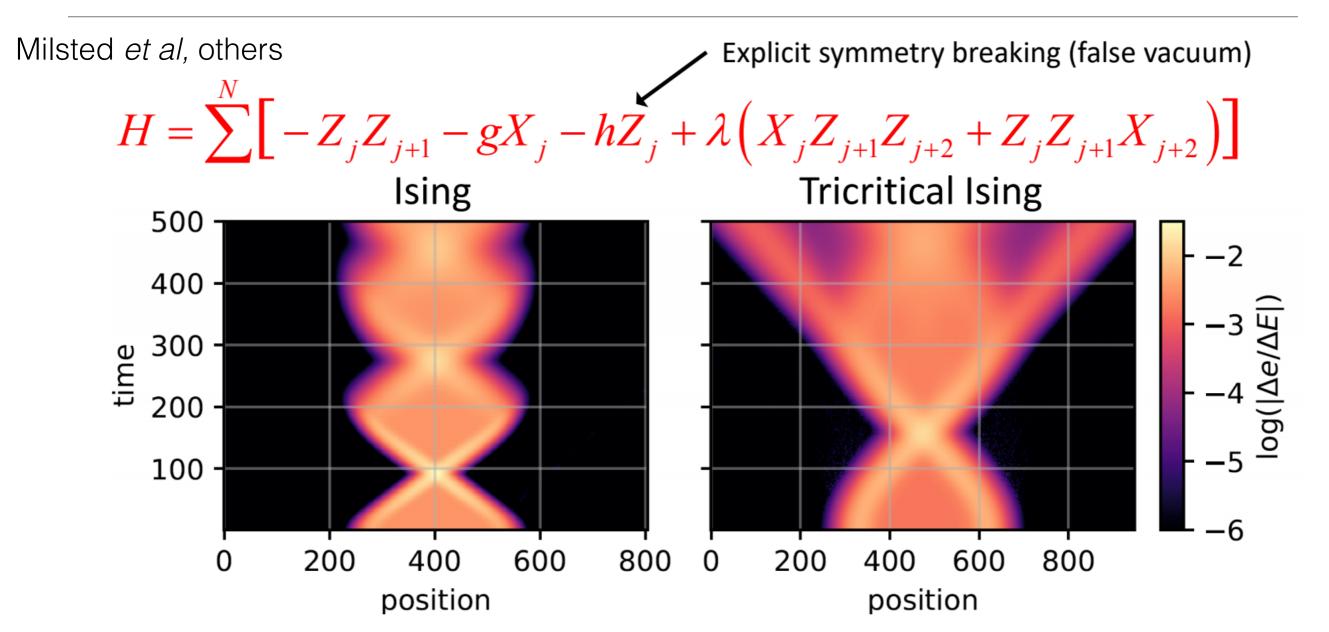
Quantum Computation of Scattering in Scalar Quantum Field Theories

Stephen P. Jordan, * Keith S. M. Lee, * and John Preskill * *



- 1. nQ qubits per spatial site, H(3) lattice, digitized field-operator basis
- 2. Create wavepackets of free theory
- 3. Adiabatically evolve the system to interacting system
- 4. Evolve the prepared state forward
- 5. Adiabatically evolve systems to free theory/introduce localized detectors into the simulation

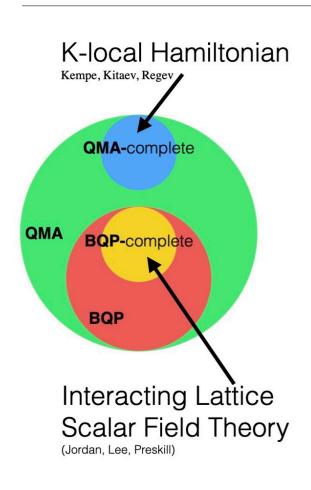
Powerful Classical Demonstrations Simulations of Spin Systems



Remarkable developments in general classical techniques for many-body systems and field theories. Tensor methods.

The audience has made important contributions

But should Complexity be a limitation? Not until it is...



Finite resources are not asymptotic.

 X^{10} is worse than $e^{+0.01} \times until x \sim 9000$ $10^6 \times until x \sim 2000$ (Highlighted by quantum chemists - what are the coefficients?)

Complexity class indicates worst case - can be much easier

The "B" in BQP gives latitude to change theories "a little"

Analogous to BPP and lattice QCD, and MC in general

With a target precision, can use pertubative expansions to potentially change problem difficulty at (tractible) LO. [e.g. includes field truncations]

Examples

1) HQET

$$|Q\bar{l}\rangle \sim |Q\rangle \otimes |\bar{l}\rangle$$

1) 1/M expansion of Hamiltonian about classical trajectories

2) Lattice QCD

- Finite volume and lattice spacing effects mitigated by EFT expansions -Symanzik action, ChiPT
- 2) pQCD matching at lattice scale —- untangled at LO

3) Wigner Symmetry

- 1) SU(4) limit emerges in large-N limit
 - 1) S-matrix has vanishing entanglement power
 - 1) classical or highly entangled
 - 2) no sign problem for MC
- 2) Numerically evolve with SU(4) symmetry, then turn on SU(4) breaking

A Path

A coordinated combination of theory, computation (and experiment) is required

Develop perturbative expansions

- LO should lie within **BQP** or be "simple configuration" within **QMA**
- ullet perturbation theory should converge result to below laket

Solve a LO Hamiltonian (typically with enhanced symmetry) using a quantum device that gets close, then use a "special-purpose" perturbation theory to reduce systematics. Typically pushes numerical errors to be of NLO, and not LO size.

Quantum Fields for EC

Stabilization of information against errors — the discovery of EC in

1995 (Shor, Knill+Laflamme+Zurek,Aharonv+Ben-Or)

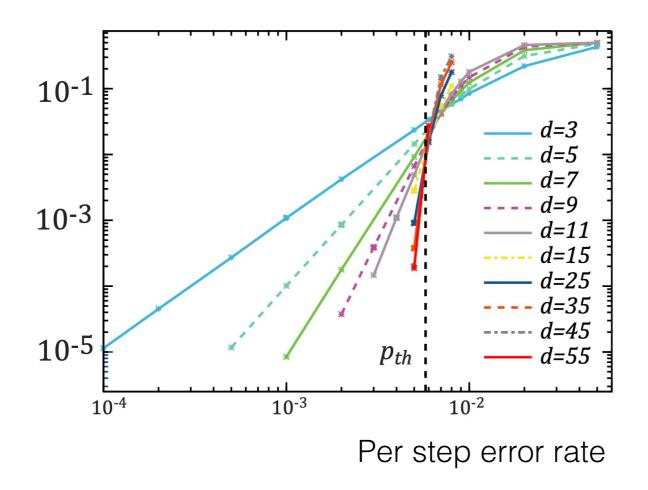
Toric Code (Kitaev)

- both hardware and algorithmic advances
- entangled, topologically ordered ground states of spin systems, with ancillars and (repeated...) application of stabilizers.

— e.g. toric, surface codes, color codes,....

Logical Qubits

— threshold error rate, below which exponential reduction in logical qubit error rate from increasing number of physical qubits.



Surface codes: Towards practical large-scale quantum computation

Austin G. Fowler

Centre for Quantum Computation and Communication Technology,

School of Physics, The University of Melbourne, Victoria 3010, Australia

Matteo Mariantoni

Department of Physics, University of California, Santa Barbara, CA 93106-9530, USA and California Nanosystems Institute, University of California, Santa Barbara, CA 93106-9530, USA

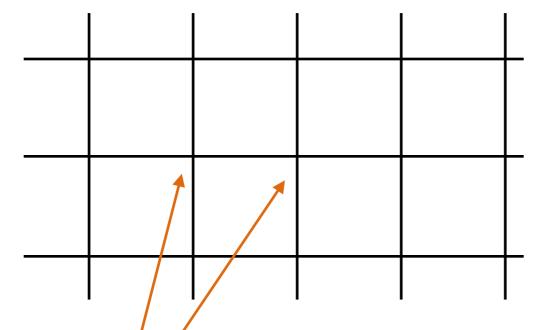
John M. Martinis and Andrew N. Cleland California Nanosystems Institute, University of California, Santa Barbara, CA 93106-9530, USA (Dated: October 26, 2012)

- For our purposes, we are looking to minimize error in simulations of observables of interest.
- Aligns well with LQ design, but might also lead to different configurations

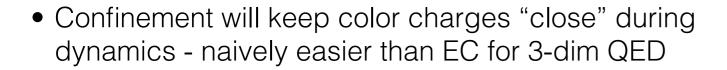
SM Quantum Fields - Errors in QFT

e.g., Yang-Mills, Kogut-Susskind formulation

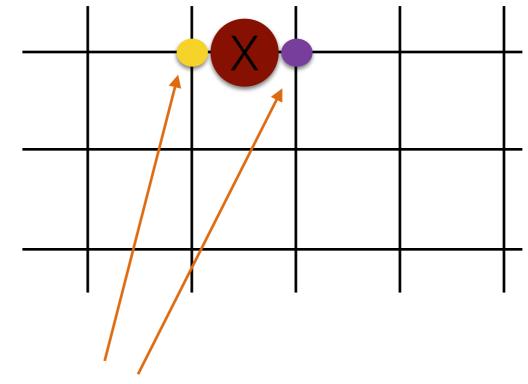
Color =
$$1, 3, \overline{3}, 8, 6, \overline{6}, \dots$$



Gauss's Law satisfied at each vertex, Color = 1



- Single shot EC in color codes
- Related to self-correcting topologically-ordered GS at finite-T.



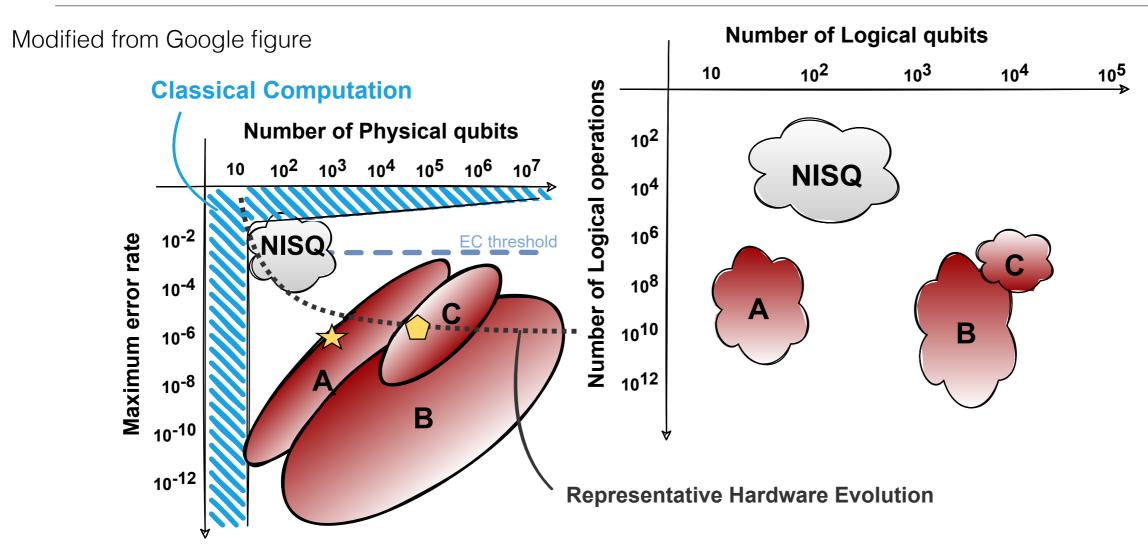
Gauss's Law violated

PHYSICAL REVIEW X 5, 031043 (2015)

Single-Shot Fault-Tolerant Quantum Error Correction

Héctor Bombín

Considerations for Simulations



- EC thresholds for surface code around 0.5%
- \bullet Different problems have different " ϵ ", and different circuits depths
- Can be mapped differently onto hardware
 - A given hardware configuration (device) of physical qubits may be able to address multiple problems
- Co-developed hardware may be required for given problems

Algorithms, Software Interfacing

Classical Simulation

- Simulations of field theories and strongly-coupled QMB
- Codes developed within community for early special purpose LQCD hardware
- SciDAC (US) brought together domain scientists and AM, CS to optimally develop techniques and software
- Hardware co-developed between Technology Companies, Labs and Universities.
- Effectively advanced our field(s) over many decades



Quantum Simulation

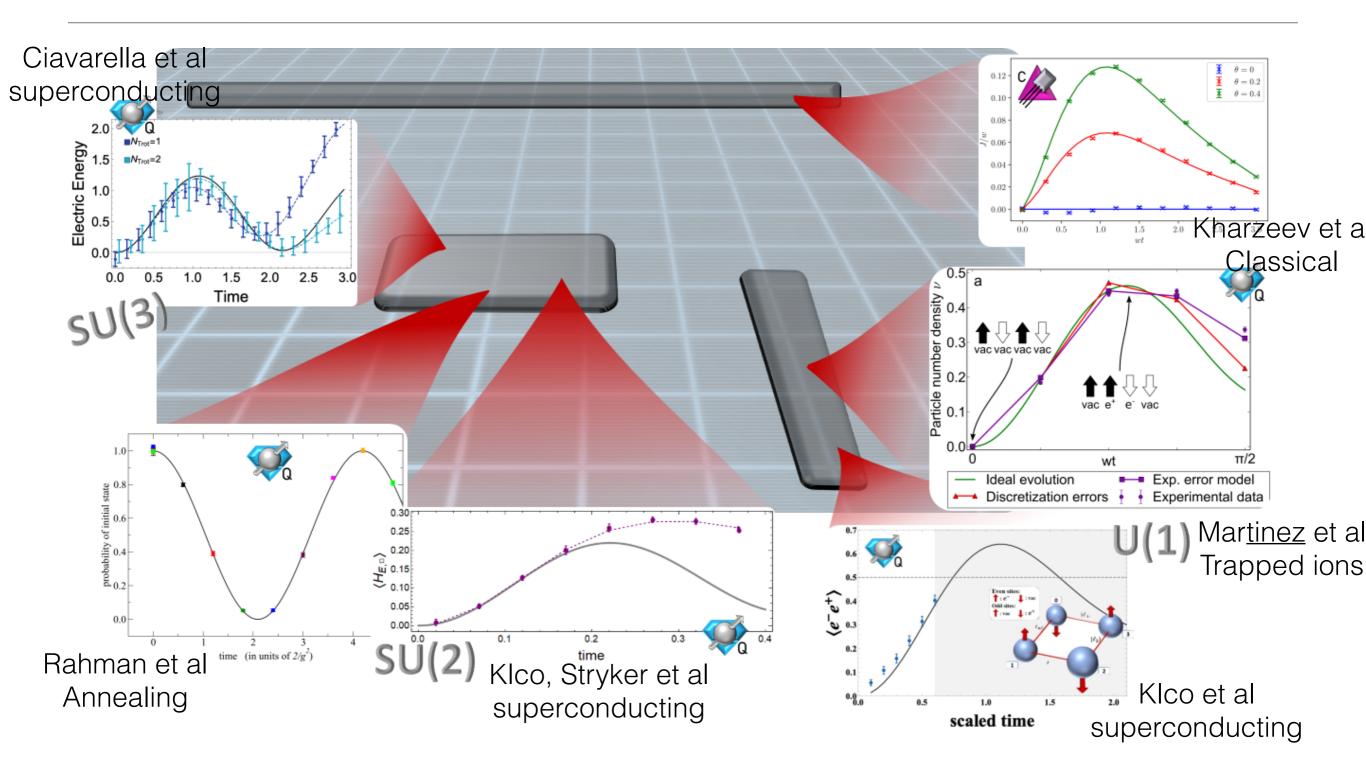
- Technology companies providing "easy" access to devices and light-weight programming languages (with ability to control closer to device)
- Enabled some of the early simulations and "recruited" scientists
- Anticipate coherence in community deep development, parallel and independent efforts for verification purposes.
- Anticipate multiple independent distinct co-design and development (hardware+) activities to address specific scientific requirements.
- IP.... robust and stable science pipeline within labs and universities
- (Many) domain scientists would like API that is architecture-insensitive
 - robustly compiles onto the hardware target without user changes



Google.cirq version = 0.11.0

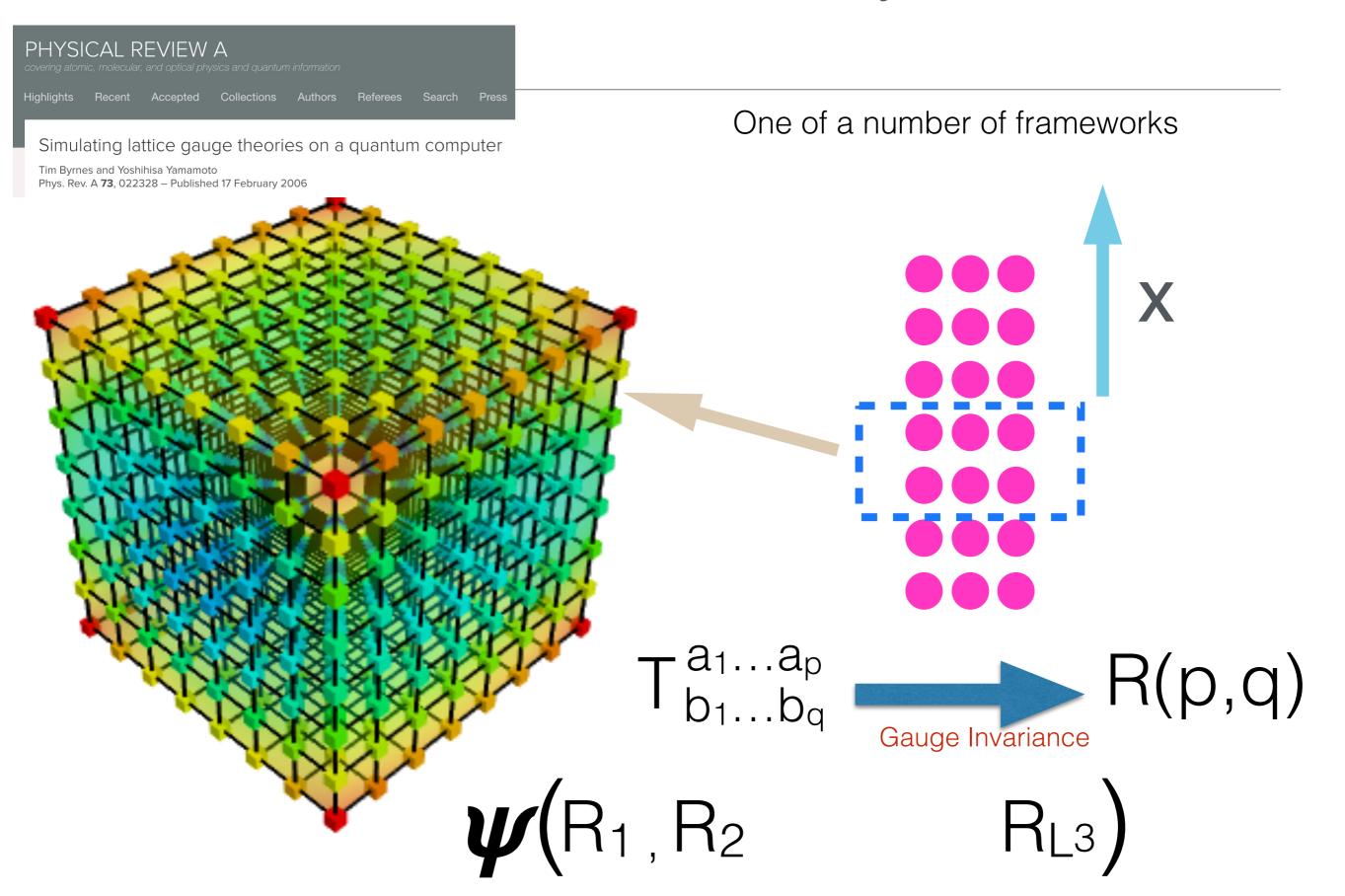
Ion Device:
0-1-2-3-4-5-6-7-

Gauge Theory Simulations on Digital Devices



Trapped-ions, Superconducting, Annealing

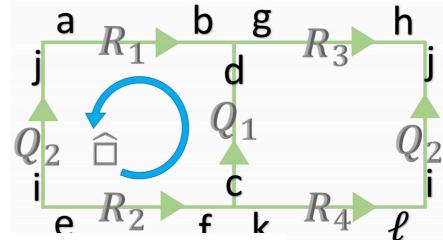
Toward Quantum Chromodynamics



2021 Anthony Ciavarella, 1,* Natalie Klco, 2,† and Martin J. Savage 1,‡

Ciavarella, Klco, MJS

Including $\underline{\mathbf{1}}$, $\underline{\mathbf{3}}$, $\underline{\mathbf{3}}$, $\underline{\mathbf{8}}$ on each link only



 $\{\mathbf{l_3}, \mathbf{Q_2}, \mathbf{R_4}) \rangle$

$$\begin{split} |\psi_{1}^{(\mathbf{1}\mathbf{3}\mathbf{\overline{3}8};+++)}\rangle &= |\chi(\mathbf{1},\mathbf{1},\mathbf{1},\mathbf{1},\mathbf{1},\mathbf{1})\rangle \quad, \\ |\psi_{2a}^{(\mathbf{1}\mathbf{3}\mathbf{\overline{3}8};+++)}\rangle &= \frac{1}{2}\left[\ |\chi(\mathbf{3},\mathbf{\overline{3}},\mathbf{\overline{3}},\mathbf{1},\mathbf{3},\mathbf{1})\rangle + |\chi(\mathbf{\overline{3}},\mathbf{3},\mathbf{3},\mathbf{1},\mathbf{\overline{3}},\mathbf{1})\rangle + |\chi(\mathbf{1},\mathbf{3},\mathbf{1},\mathbf{3},\mathbf{\overline{3}},\mathbf{\overline{3}})\rangle + |\chi(\mathbf{1},\mathbf{\overline{3}},\mathbf{1},\mathbf{\overline{3}},\mathbf{3},\mathbf{3})\rangle \ \right] \\ |\psi_{2b}^{(\mathbf{1}\mathbf{3}\mathbf{\overline{3}8};+++)}\rangle &= \frac{1}{\sqrt{2}}\left[\ |\chi(\mathbf{3},\mathbf{1},\mathbf{\overline{3}},\mathbf{3},\mathbf{1},\mathbf{\overline{3}})\rangle + |\chi(\mathbf{\overline{3}},\mathbf{1},\mathbf{3},\mathbf{\overline{3}},\mathbf{1},\mathbf{3})\rangle \ \right] \\ |\psi_{3}^{(\mathbf{1}\mathbf{3}\mathbf{\overline{3}8};+++)}\rangle &= \frac{1}{\sqrt{2}}\left[\ |\chi(\mathbf{8},\mathbf{1},\mathbf{1},\mathbf{8},\mathbf{1},\mathbf{1})\rangle + |\chi(\mathbf{1},\mathbf{1},\mathbf{8},\mathbf{1},\mathbf{1},\mathbf{8})\rangle \ \right] \\ &\vdots \end{split}$$

$$|\psi_9^{({f 13f 38};+++)}\rangle = |\chi({f 8,8,8,8,8,8})\rangle$$

- 15 basis states (4 qubits)
- Max electric energy ~ 6*3
- •8 ⊗ 8 ⊗ 8

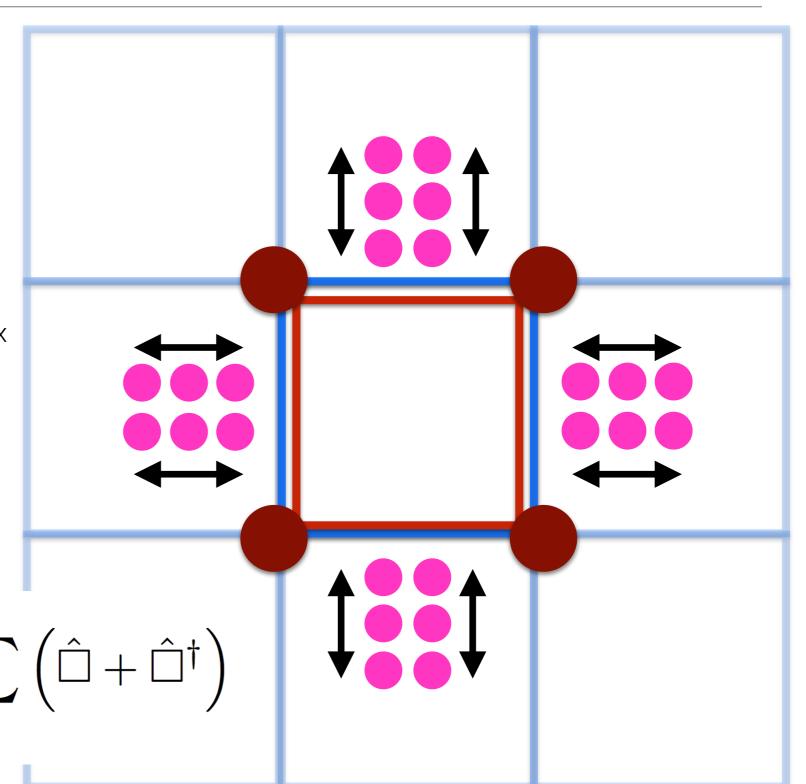
Keeping states with Casimir above 6-threshold includes only part of that higher-energy space

Toward QCD

Local Basis Scales

Building on Byrnes+Yamamoto

- Integrate over gauge space at each vertex (classical Banuls *et al*, Klco, Stryer *et al*)
- Controlled plaquette operators
- Qudits seem natural for link registers

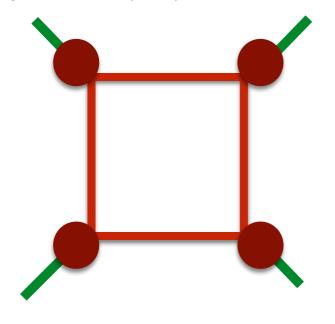


$$\hat{H} = \frac{g^2}{2} \sum_{\text{links}} \hat{E}^2 - \frac{1}{2g^2} \sum_{\square} \left(\hat{\square} + \hat{\square}^{\dagger} \right)$$

To (partially) address Dorota's question: SU(3) KS - Classical/Quantum Resources

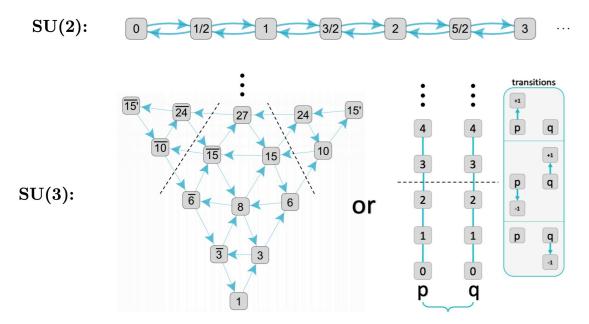
Trailhead for quantum simulation of SU(3) Yang-Mills lattice gauge theory in the local multiplet basis Anthony Ciavarella, Natalie Klco, Martin J. Savage

Phys.Rev.D 103 (2021) 9, 094501 • e-Print: 2101.10227 [quant-ph]



$\Lambda_p = \Lambda_q$	dimensions	physical states	matrix elements	elements/states
1	(1 , 3)	81	81	1
1	(1, 3, 8)	529	1,018	1.92
2	(1, 3, 8, 6)	5,937	$19,\!594$	3.30
2	(1, 3, 8, 6, 15)	59,737	419,316	7.02
2	(1, 3, 8, 6, 15, 27)	139,317	1,049,931	7.54
3	(1, 3, 8, 6, 15, 27, 10)	509,271	4,001,111	7.86
3	(1 , 3 , 8 , 6 , 15 , 27 , 10 , 24)	2,008,297	24,648,819	12.27

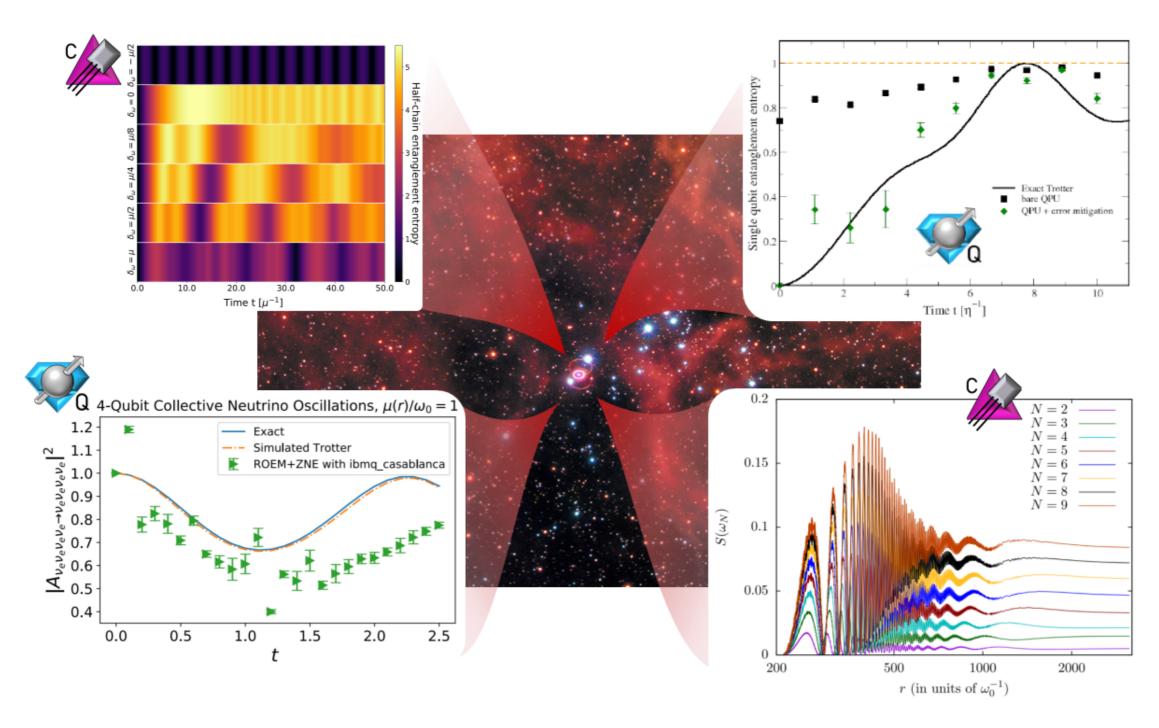
TABLE III. Properties of the plaquette operator truncated in the local index (p,q) basis and at intermediate truncate organized by dimension. The number of physical states constituting the gauge-invariant basis of the plaquette operator, as as the number of non-zero matrix elements within the physical subspace are presented. The ratio of these two quantities shown in the right column.



Require a 3-dim resource costing Exponential convergence in field space

Number of singlets ~ Cut-off ^(2 nR)

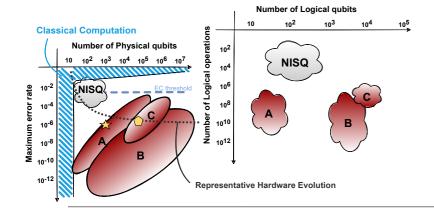
e.g., Neutrinos



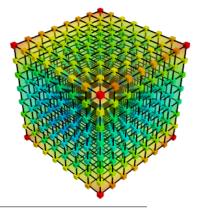
K. Yeter-Aydeniz, S. Bangar, G. Siopsis, and R. C. Pooser, "Collective neutrino oscillations on a quantum computer," (2021), arXiv:2104.03273 [quant-ph].
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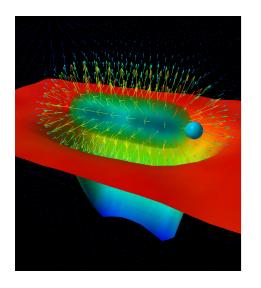
on a quantum computer," (2021), arXiv:2102.12556 [quant-ph].

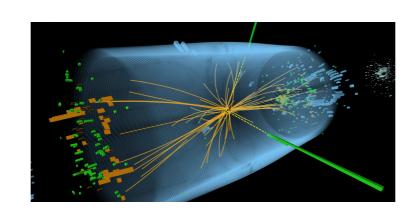
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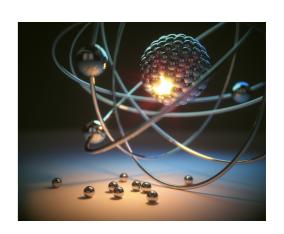


Summary









- Unique time in (scientific) computing device capabilities are rapidly increasing
- HEP and NP need quantum simulation capabilities
- Exciting and encouraging early results
- Embrace entanglement build it in where practical
- Consider techniques/develop EFTs to mitigate complexity
- Collaborate on hardware, theory, algorithms and software
- Explore multiple potential paths forward quantify/benchmark

Thank you to the Organizers!!!

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