

# off-shell $t\bar{t}b\bar{b}$ in the di-lepton channel

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Based on: [JHEP 08 \(2021\) 008](#)



## Motivations for $t\bar{t}b\bar{b}$ at the LHC

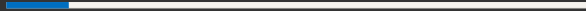
- the need for more precision
- state of the art

## off-shell $t\bar{t}b\bar{b}$ @ NLO QCD

- Size of corrections
- Differential distributions
- Impact of  $b$  jet definitions

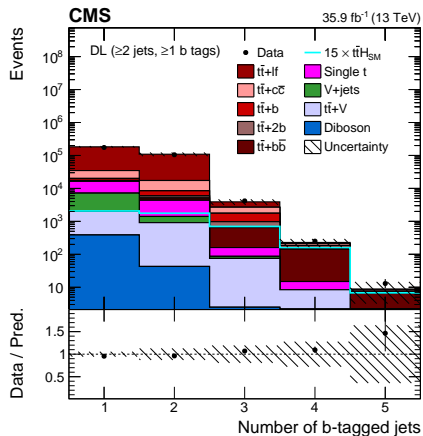
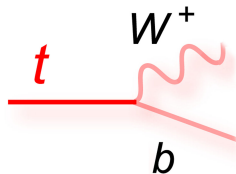
## Summary & Outlook

# Motivation

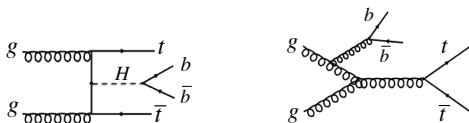


# Motivation - Background

- Measurements of  $pp \rightarrow t\bar{t}H$  with  $H \rightarrow b\bar{b}$  are challenging!
- Large **irreducible** background due to  $pp \rightarrow t\bar{t}b\bar{b}$
- **Reducible** background:  $pp \rightarrow t\bar{t}jj$
- extra  $b$  jets from top decay:  $t \rightarrow Wb$



$\Rightarrow t\bar{t}b\bar{b}$  main background for  $N_{b \text{ jets}} \geq 4$

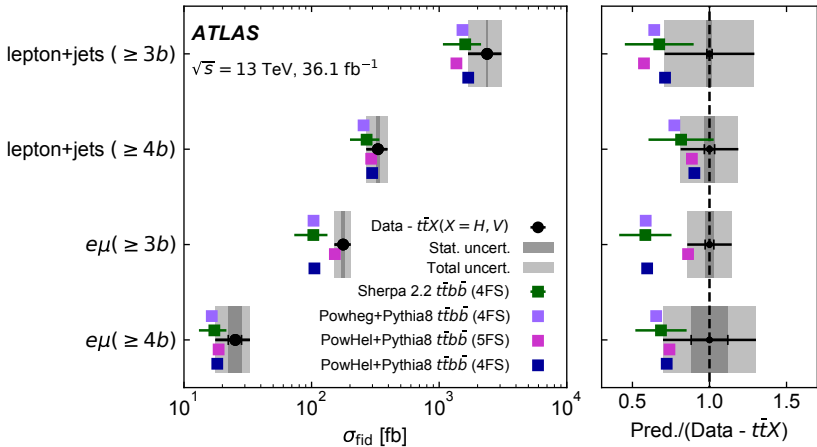


[CMS arXiv:1804.03682]

# Motivation - Signal

$pp \rightarrow t\bar{t}b\bar{b}$  measurement

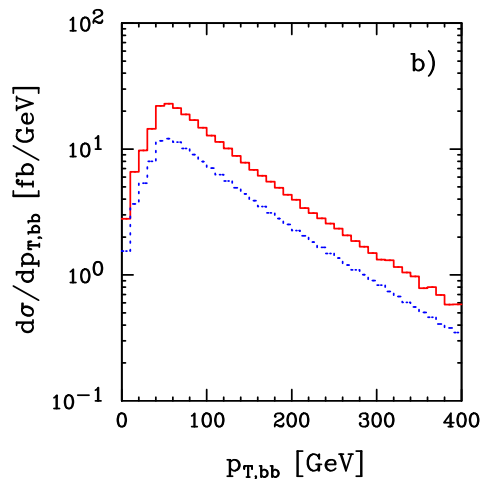
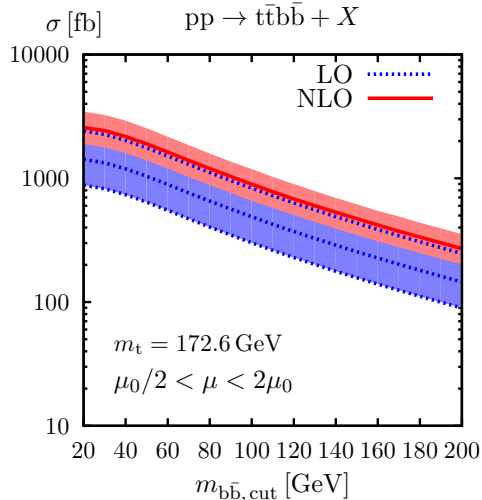
[ATLAS arXiv:1811.12113]



- Current predictions are systematically below data
- Can off-shell  $t\bar{t}b\bar{b}$  model fiducial volumes better?

# Motivation - Theory

[Bredenstein, Denner, Dittmaier, Pozzorini '09]



[Bevilacqua, Czakon, Papadopoulos, Pittau, Worek '09]

- $t\bar{t}b\bar{b}$  is a true **multi-scale** process
- theoretically very challenging!

## NLO QCD fixed order

$$pp \rightarrow t\bar{t}b\bar{b}$$

[Bredenstein, Denner, Dittmaier, Pozzorini '08,'09'10]

[Bevilacqua, Czakon, Papadopoulos, Pittau, Worek '09]

[Worek '12] [Bevilacqua, Worek '14]

$$pp \rightarrow t\bar{t}b\bar{b}j$$

[Buccioni, Kallweit, Pozzorini, Zoller '19]

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}b\bar{b}$$

[Denner, Lang, Pellen '20]

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

## NLO + PS

- POWHEG matching

[Kardos, Trócsányi '14]

[Garzelli, Kardos, Trócsányi '15]

[Bevilacqua, Garzelli, Kardos '17]

[Ježo, Lindert, Moretti, Pozzorini '18]

- MC@NLO matching

[Cascioli, Maierhöfer, Moretti, Pozzorini, Siebert '14]

off-shell  $t\bar{t}b\bar{b}$

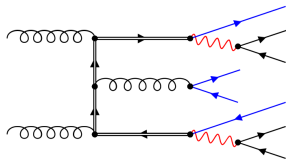
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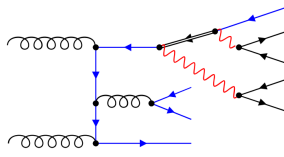
NLO QCD corrections to  $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b}$  for LHC at  $\sqrt{s} = 13$  TeV

- Full off-shell effects

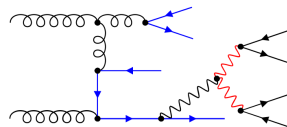
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Double resonant



Single resonant



Non resonant

- off-shell tops described by Breit-Wigner propagators
- All interferences at the matrix element level

- Event selection:

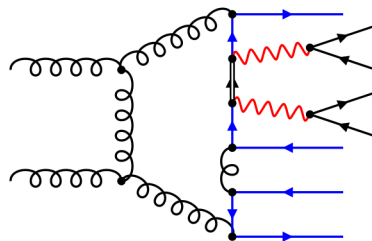
$$p_T(\ell) > 20 \text{ GeV}, \quad p_T(b) > 25 \text{ GeV}, \quad |y(\ell)| < 2.5, \quad |y(b)| < 2.5$$

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

# A very complicated computation

A quick glimpse at the **complexity** of  $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b}$

One-loop correction type	Number of Feynman diagrams
Self-energy	93452
Vertex	88164
Box-type	49000
Pentagon-type	25876
Hexagon-type	11372
Heptagon-type	3328
Octagon-type	336
Total number	271528



Partonic Subprocess	Number of Feynman diagrams	Number of CS Dipoles	Number of NS Subtractions
$gg \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b} g$	41364	90	18
$q\bar{q} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b} g$	9576	50	10
$gq \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b} q$	9576	50	10
$g\bar{q} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b} \bar{q}$	9576	50	10

⇒ Computation performed with **HELAC-NLO**

# Comparison with literature

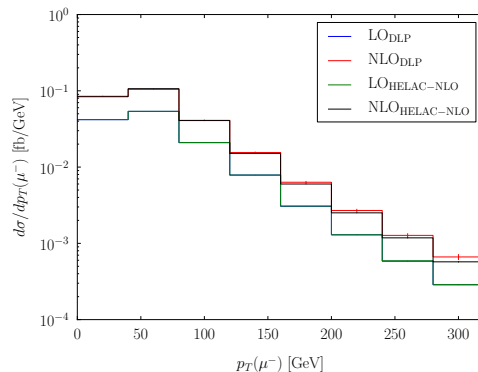
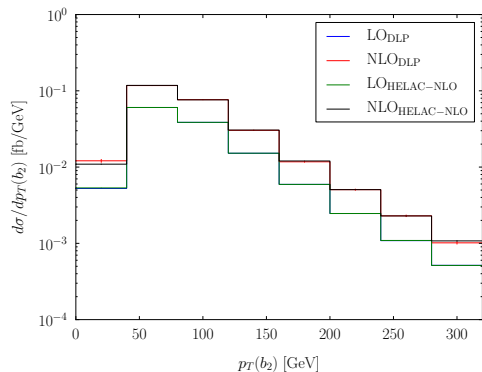
Comparison with results from **Denner, Lang, Pellen '20**

## Integrated cross section

$$\sigma_{\text{HELAC}}^{\text{NLO}} = 10.28(1)^{+18\%}_{-21\%} \text{ fb}$$

$$\sigma_{\text{DLP}}^{\text{NLO}} = 10.28(8)^{+18\%}_{-21\%} \text{ fb}$$

## Differential distributions



**Excellent agreement!**

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

# Integrated fiducial cross sections

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b} \bar{b} @ LHC_{13T eV}$$

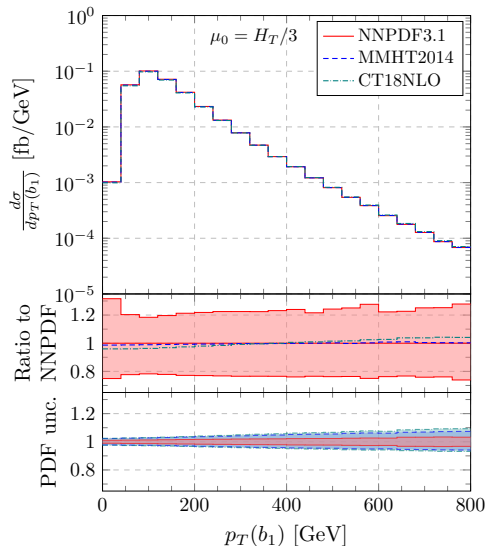
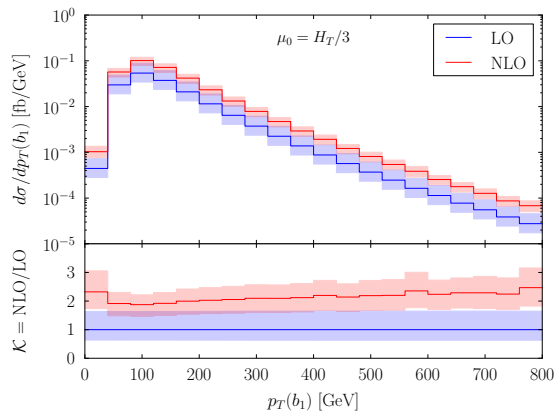
$p_T(b)$	$\sigma^{\text{LO}}$ [fb]	$\delta_{\text{scale}}$	$\sigma^{\text{NLO}}$ [fb]	$\delta_{\text{scale}}$	$\delta_{\text{PDF}}$	$\mathcal{K} = \sigma^{\text{NLO}}/\sigma^{\text{LO}}$
$\mu_R = \mu_F = \mu_0 = m_t$						
25	6.998	+4.525 (65%) -2.569 (37%)	13.24	+2.33 (18%) -2.89 (22%)	+0.19 (1%) -0.19 (1%)	1.89
30	5.113	+3.343 (65%) -1.889 (37%)	9.25	+1.32 (14%) -1.93 (21%)	+0.14 (2%) -0.14 (2%)	1.81
35	3.775	+2.498 (66%) -1.401 (37%)	6.57	+0.79 (12%) -1.32 (20%)	+0.10 (2%) -0.10 (2%)	1.74
40	2.805	+1.867 (67%) -1.051 (37%)	4.70	+0.46 (10%) -0.91 (19%)	+0.08 (2%) -0.08 (2%)	1.68
$\mu_R = \mu_F = \mu_0 = H_T/3$						
25	6.813	+4.338 (64%) -2.481 (36%)	13.22	+2.66 (20%) -2.95 (22%)	+0.19 (1%) -0.19 (1%)	1.94
30	4.809	+3.062 (64%) -1.756 (37%)	9.09	+1.66 (18%) -1.98 (22%)	+0.16 (2%) -0.16 (2%)	1.89
35	3.431	+2.191 (64%) -1.256 (37%)	6.37	+1.07 (17%) -1.36 (21%)	+0.11 (2%) -0.11 (2%)	1.86
40	2.464	+1.582 (64%) -0.901 (37%)	4.51	+0.72 (16%) -0.95 (21%)	+0.09 (2%) -0.09 (2%)	1.83

- Large NLO corrections
- 20% scale uncertainty
- mild  $p_T(b)$  dependence for  $\mu_0 = H_T/3$
- dominated by real radiation
- $p_T^{\text{veto}}(j) = 50 \text{ GeV}$   
 $K = 1.11$  &  $K = 1.23$

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

# Differential distributions - Uncertainties

$$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b} @ LHC_{13TeV}$$

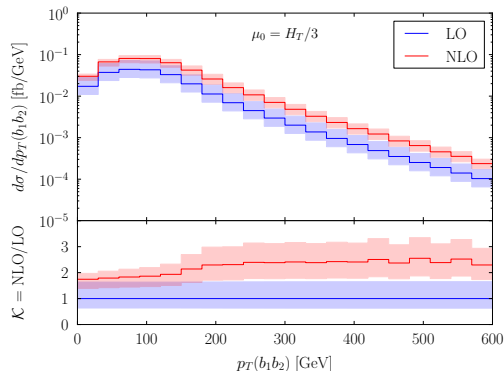
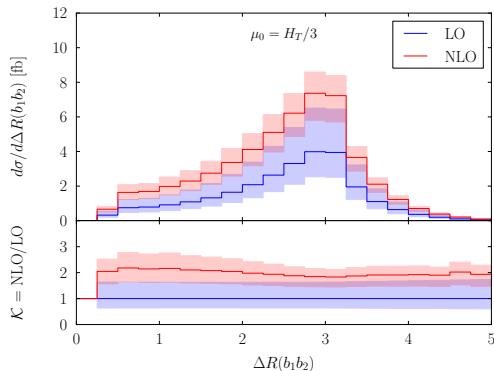


- Large shape distortions (+90% – 135%)
- Scale dependence:  $\pm 20 - 30\%$

- PDF uncertainties small-ish ( $\leq 10\%$ )

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

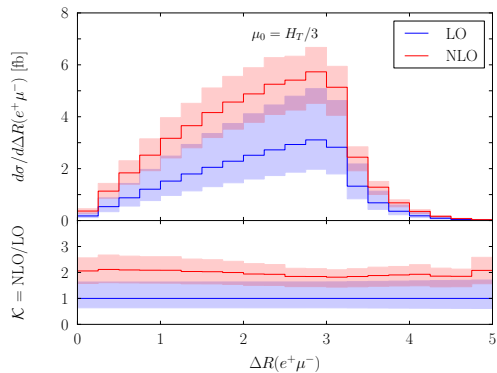
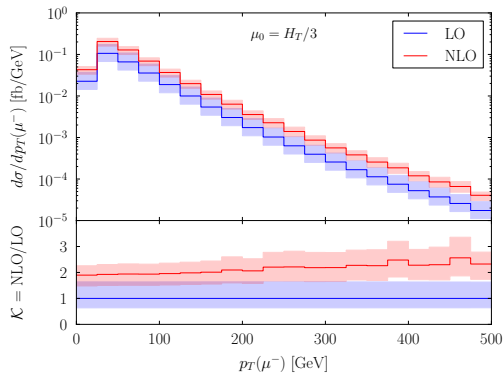
# Differential distributions – $b$ jets



- Hardest  $b$  jets produced back-to-back  $\rightarrow$  mainly from tops
- Large corrections  $\sim 150\%$  for  $p_T(b_1 b_2)$  due to real radiation
- Scale uncertainties: 25 – 30%

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

# Differential distributions – leptons



- NLO QCD corrections: 80 – 150%
- Scale uncertainties: 20 – 25%

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

# Impact of $b$ jet definitions

Can we ignore initial state  $b$  quarks in off-shell  $t\bar{t}b\bar{b}$ ?

$$b\bar{b}/\bar{b}b \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b}$$

$$bb \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} bb$$

$$\bar{b}\bar{b} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} \bar{b}\bar{b}$$

$$b\bar{b}/\bar{b}b \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} g$$

$$bb \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} bb g$$

$$\bar{b}\bar{b} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} \bar{b}\bar{b} g$$

$$bg/gb \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} b$$

$$\bar{b}g/g\bar{b} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b} b\bar{b} \bar{b}$$

Assess differences in  $b$  jet def. in two schemes

charge blind

$$N_{b/\bar{b}} \geq 4$$

$$b\bar{b} \rightarrow g, \quad bg \rightarrow b, \quad \bar{b}g \rightarrow \bar{b},$$

$$bb \rightarrow g, \quad \bar{b}\bar{b} \rightarrow g$$

charge aware

$$N_b \geq 2 \ \& \ N_{\bar{b}} \geq 2$$

$$b\bar{b} \rightarrow g, \quad bg \rightarrow b, \quad \bar{b}g \rightarrow \bar{b},$$

$$bb \rightarrow b, \quad \bar{b}\bar{b} \rightarrow \bar{b}$$

Jets clustered with anti  $k_T$  jet algorithm with  $R = 0.4$

Beyond NLO fixed-order  $\rightarrow$  flavor  $k_T$  [Banfi, Salam, Zanderighi '06]

$\rightarrow$  flavor anti- $k_T$  [Czakon yesterday]



LO

$$\begin{aligned}\sigma_{\text{no b}}^{\text{LO}} &= 6.813(3) \text{ fb} \\ \sigma_{\text{aware}}^{\text{LO}} &= 6.822(3) \text{ fb} \\ \sigma_{\text{blind}}^{\text{LO}} &= 6.828(3) \text{ fb}\end{aligned}$$

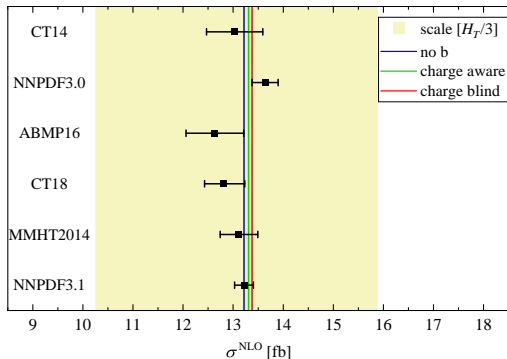
NLO

$$\begin{aligned}\sigma_{\text{no b}}^{\text{NLO}} &= 13.22(3) \text{ fb} \\ \sigma_{\text{aware}}^{\text{NLO}} &= 13.31(3) \text{ fb} \\ \sigma_{\text{blind}}^{\text{NLO}} &= 13.38(3) \text{ fb}\end{aligned}$$

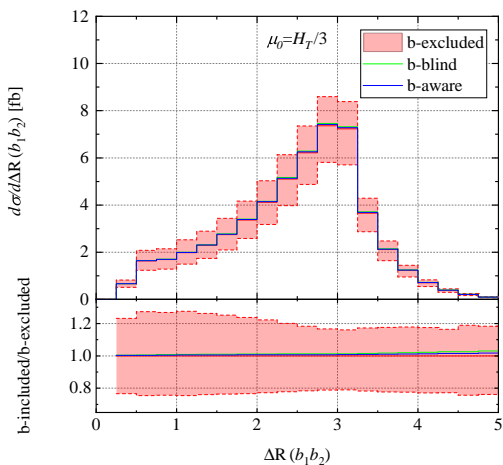
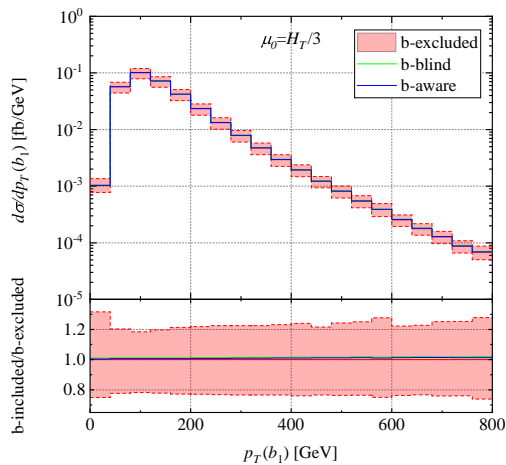
Differences are of the order of **0.2%**

Differences are of the order of **1%**

How important are these effects?



# Differential distributions



- initial-state  $b$  contribution negligible
- even in extreme phase space regions  $\Delta R \gtrsim 4$

[Bevilacqua, Bi, Hartanto, MK, Lupattelli, Worek '21]

## Summary & Outlook

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## Summary:

- NLO QCD corrections for off-shell  $pp \rightarrow t\bar{t}b\bar{b}$ 
  - full off-shell effects
  - Large NLO corrections  $\sim 89\%$
  - Scale uncertainties  $\sim 20 - 30\%$
- Full agreement with previous calculation: [Denner, Lang, Pellen '20]
- Impact of initial state  $b$  quarks:
  - charge blind vs. charge aware tagging schemes
  - differences:  $0.2\%$  @ LO and  $1\%$  @ NLO
- More details: Poster session  $\rightarrow$  Michele Lupattelli

## Outlook:

- Comparison with Narrow Width Approximation
- Can we distinguish  $b$  jets from tops vs. prompt  $b$  jets?