

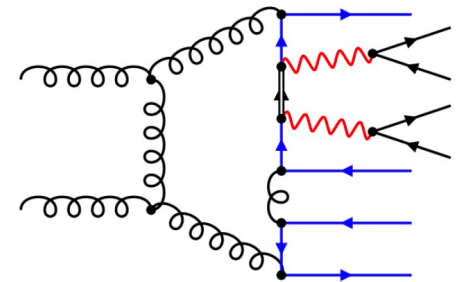
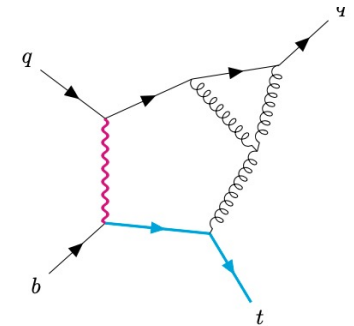
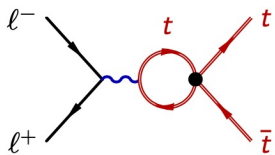
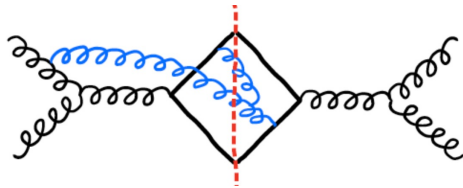
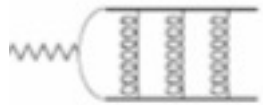
# 14<sup>th</sup> International Workshop on Top Quark Physics TOP2021

## Theory Summary

Doreen Wackerroth



University at Buffalo

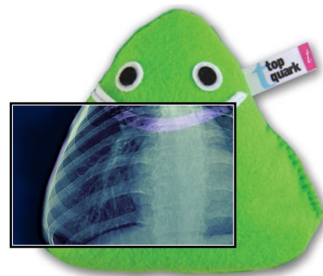
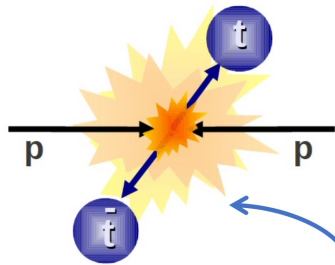


Zoom meeting, 13-17 September 2021

# The Many Facets of Top Quark Physics

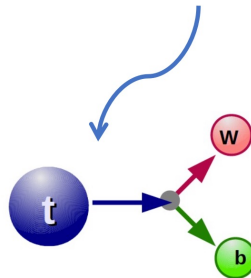
0) It is there!  
and we have the opportunity to study its properties

Andrea Wulzer



## Production:

- Production rate
- Differential distributions
- New production mechanisms
- Single top-quark production
- Top-quark pair production
- Associated production of top quarks with  $W, Z, \gamma, H, j, bb, tt, jj, \gamma\gamma \dots$
- ...



- Top properties are essential ingredients for SM predictions  
we must know them precisely
- The Top is a portal to EWSB  
Composite Higgs  $\Rightarrow$  Composite Top  
The 4-tR vertex opportunity
- The (Top) EFT  
A **clear** path towards top couplings characterisation  
A full-fledged BSM search strategy, with discovery potential  
**Clear  $\neq$  Easy!** Needs EXP/QCD/PDF/BSM work



## Intrinsic properties:

- Mass
- Charge
- Lifetime
- Width
- ...

Malgorzata Worek

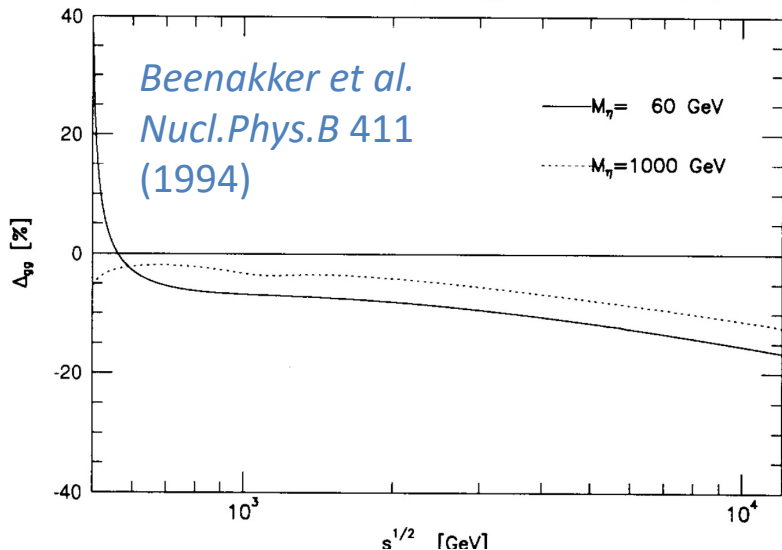
## Decays:

- Various decay channels
- SM & BSM
- Couplings  $W, Z, \gamma$  &  $H$
- Spin correlations
- ...

# Exploration of Top-pair production in 1994 and 27 years later ...

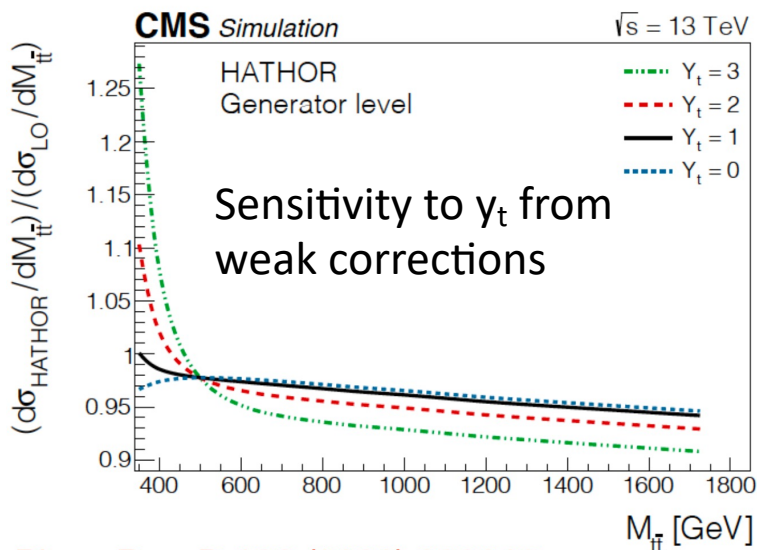
## Weak 1-loop corrections to top-pair production

Fig. 12: Relative correction to the parton  $gg \rightarrow tt$  cross section,  $m_t = 250$  GeV

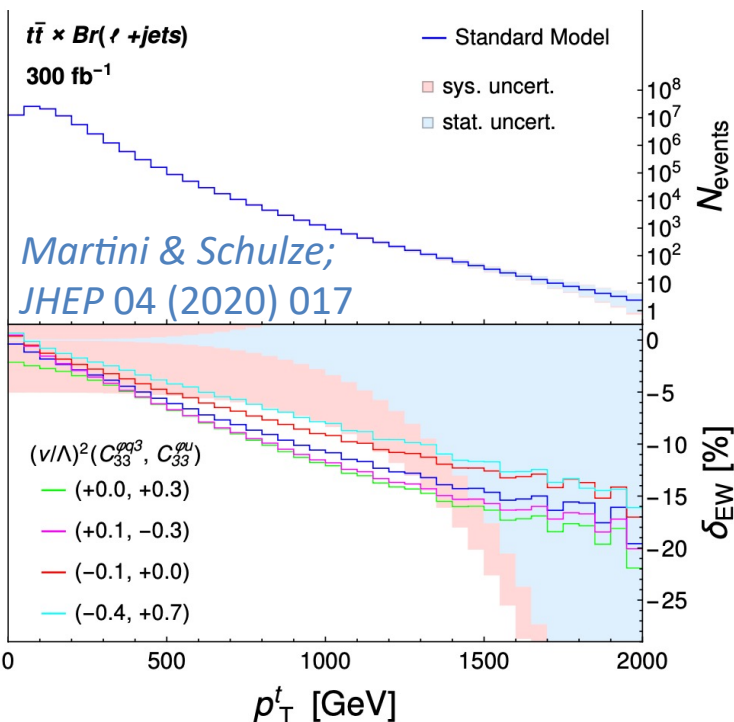
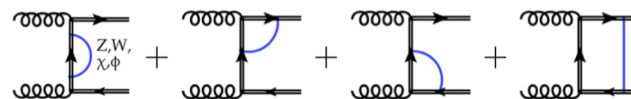


Beenakker et al.  
Nucl.Phys.B 411  
(1994)

Update:  
Kühn, Scharf  
& Uwer; PRD  
91 (2015)  
1,014020  
[PRD 100,  
072007  
(2019)]



## Weak corrections in SMEFT



Martini & Schulze;  
JHEP 04 (2020) 017

Now in:  
Hathor  
MCFM

See Ken Mimasu's talk

See Sebastian Wuchter's talk

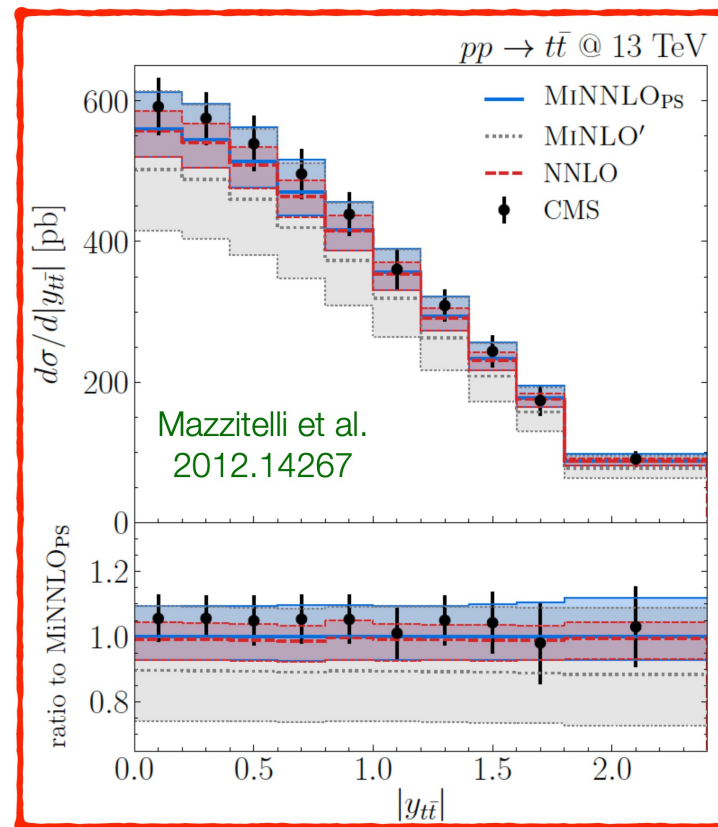
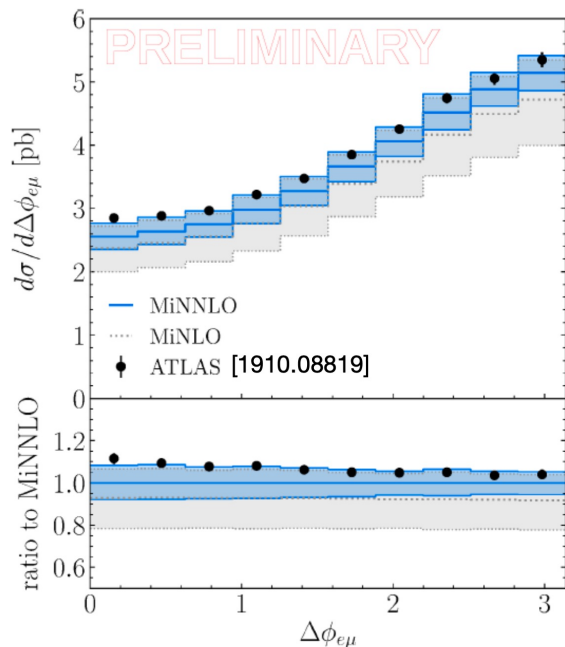
$$Y_t = 1.16_{-0.08}^{+0.07} (\text{stat})_{-0.34}^{+0.23} (\text{syst})$$

# Top-pair production: NNLO+PS

Giulia Zanderighi

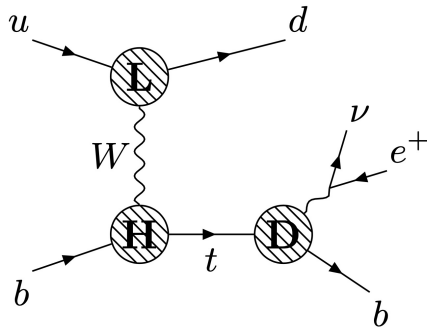
- Presented results for  $t\bar{t}$  matched to parton shower preserving NNLO accuracy using MiNNLO<sub>PS</sub> procedure
- Code implemented in POWHEG BOX V2 and publicly available upon request
- First NNLO+PS generator for a coloured process
- Validation with NNLO results
- Good agreement with ATLAS/CMS data
- Preliminary results including top-decays with spin correlations
- Further phenomenological studies (e.g. scale settings) and further validation to come

$$\frac{d\sigma}{dp_T d\Phi_{t\bar{t}}} = \frac{d}{dp_T} \left\{ \sum_c \frac{e^{-\tilde{S}_c(p_T)}}{2m_{t\bar{t}}^2} \langle M_{c\bar{c}}^{(0)} | (\mathbf{V}_{\text{NLL}})^\dagger \mathbf{V}_{\text{NLL}} | M_{c\bar{c}}^{(0)} \rangle \sum_{i,j} \left[ \text{Tr}(\tilde{\mathbf{H}}_c \mathbf{D}) (\tilde{C}_{ci} \otimes f_i) (\tilde{C}_{\bar{c}j} \otimes f_j) \right]_\phi \right\} + R_f + \mathcal{O}(\alpha_s^2)$$



# Single top production: t-channel@NNLO

John Campbell



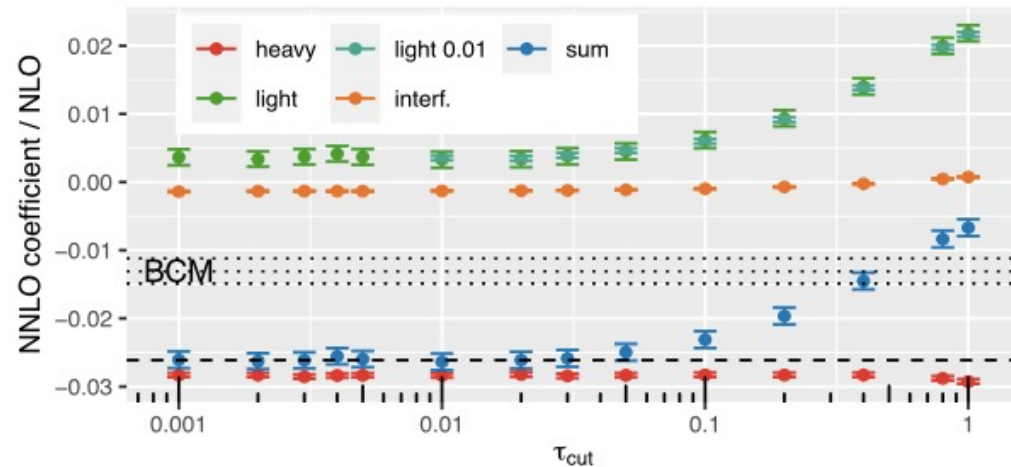
Berger, Gao, Yuan, Zhu, <https://arxiv.org/abs/1606.08463>;  
<https://arxiv.org/abs/1708.09405>

Brucherseifer, Caola, Melnikov, <https://arxiv.org/abs/1404.7116>

- New calculation based on SCET approach, all ingredients re-computed from scratch and independently verified where possible.

JC, Neumann, Sullivan, <https://arxiv.org/abs/2012.01574>)

		$\sigma_{\text{NNLO}}^{\text{BGZ}}$	$\sigma_{\text{NNLO}}$
7 TeV	top	$42.05^{+1.2\%}_{-0.6\%}$	$41.99(4)^{+1.4\%}_{-0.7\%}$
	anti-top	$21.95^{+1.2\%}_{-0.7\%}$	$21.90(3)^{+1.4\%}_{-0.8\%}$
14 TeV	top	$153.3^{+1.1\%}_{-0.5\%}$	$153.2(2)^{+1.2\%}_{-0.6\%}$
	anti-top	$91.81^{+1.0\%}_{-0.5\%}$	$91.5(1)^{+1.2\%}_{-0.7\%}$

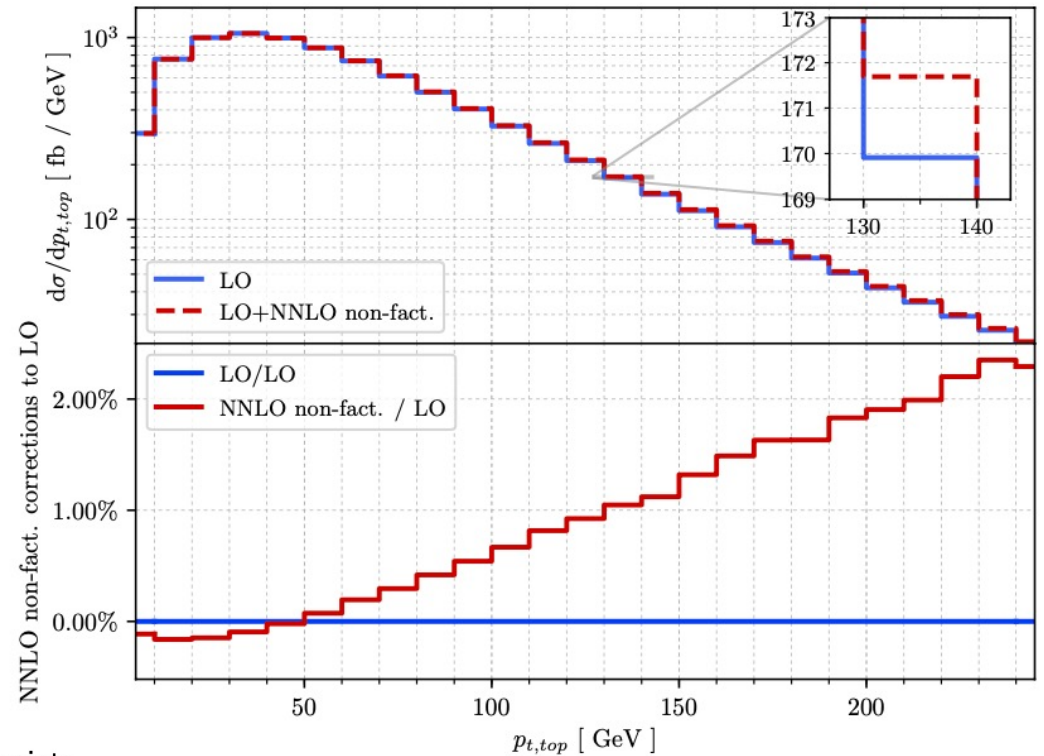
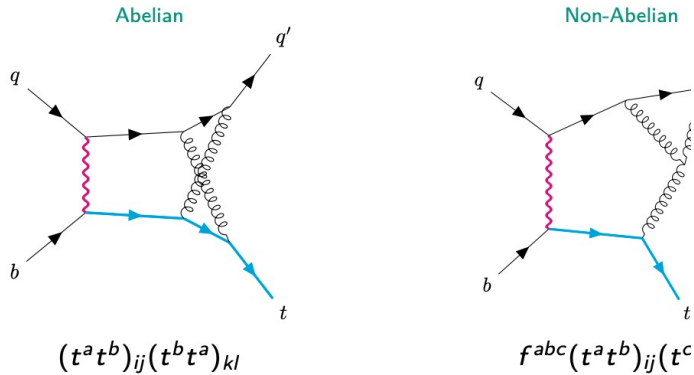


same O(1%) difference with BCM

# Single top production: t-channel@NNLO

## Non-factorizable corrections

Christian Bronnum-Hansen



- Double-virtual cross-section calculation from fixed grid of 100k points

$$\sigma_{pp \rightarrow dt}^{ub} = \left( 90.3 + 0.3 \left( \frac{\alpha_s(\mu_{\text{nf}})}{0.108} \right)^2 \right) \text{pb}$$

arXiv:2108.09222

- Correction of about 0.3% for  $\mu_{\text{nf}} = 173 \text{ GeV}$

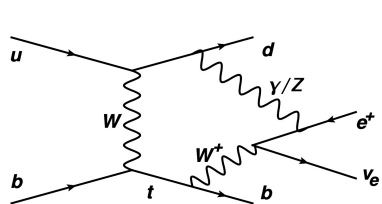
# Single top production: all contributions at NLOPS+EW

- Study including all NLO QCD and EW effects + QCD shower in MG5\_aMC@NLO

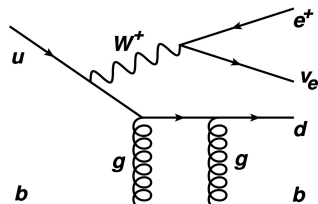
John Campbell

- t-channel signature: lepton, light jet, b-jet, missing  $E_T$

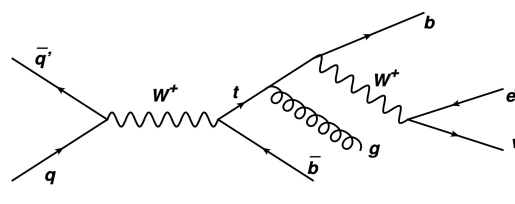
Frederix, Pagani and Tsinikos,  
<https://arxiv.org/abs/1907.12586>



“NLO EW t-channel”

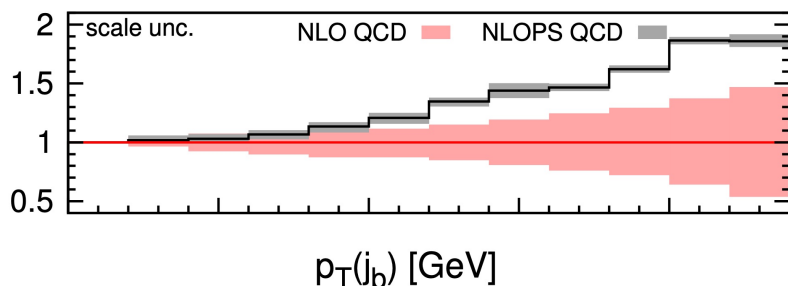
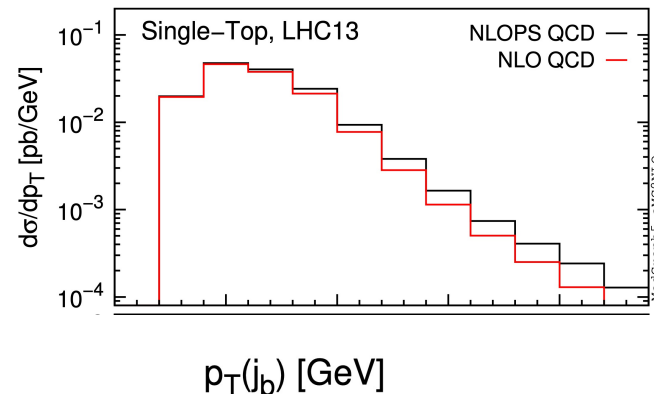


“NLO QCD W+2 jets”

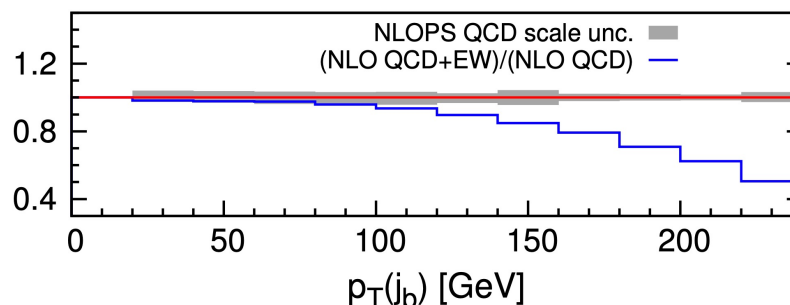


“NLO QCD s-channel”

- Complementary approach: include all contributions to a given final-state signature (at some order), traditional channels emerge by applying cuts
  - less assumptions, e.g. reliance on narrow-width approximation ✓
  - much more complicated, not highest formal accuracy (no NNLO) ✗



Large uncertainty at fixed order due to jet veto remedied in NLOPS.



EW effects substantial in distributions.

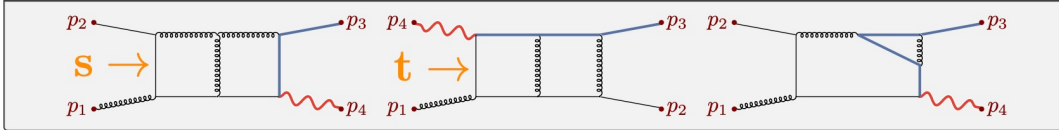
# Single top production: Towards tW-channel@NNLO

Ming-Ming Long

Consider the partonic process below at NNLO QCD,

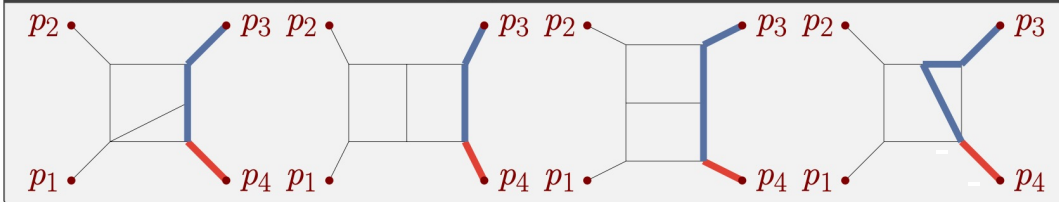
$$g(p_1) + b(p_2) \rightarrow t(p_3) + W(p_4), \text{ with } p_{1,2}^2 = 0, p_3^2 = m_t^2 \text{ and } p_4^2 = m_W^2.$$

Sample Feynman diagrams with up to 3 massive internal lines



We can identify two integral families. Family 1 (**60 MIs**) includes first two diagrams. Second family (**36 MIs**) contains the last diagram.

Sample MIs (most complicate examples)

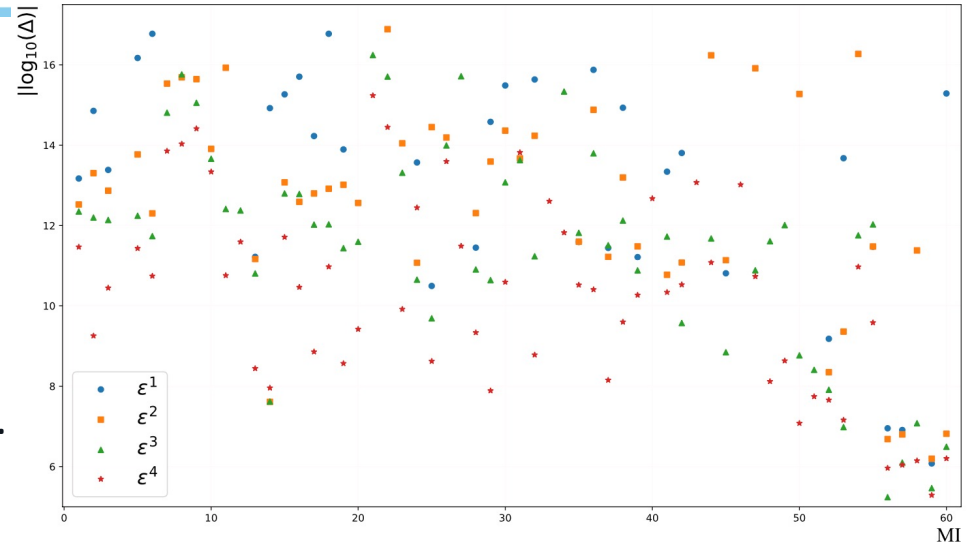


See also Long-Bing Cheng, Jian Wang, arXiv:2106.12093 (integral family with one massive propagator)

Analytic results for MIs in terms of Goncharov polylogarithms.

- Comparison with pySecDec [3] at  $r = (-6, -13, 5, 12)$  for MIs of family 1.

$\Delta = |1 - \text{Numerical integration}/\text{Analytical evaluation}|$ .  
Locating at higher means better agreement.

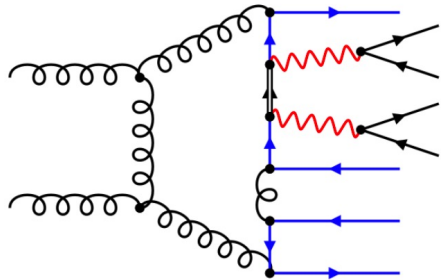




# Full Off-shell $t\bar{t}b\bar{b}$ @NLO QCD

Manfred Kraus

A quick glimpse at the **complexity** of  $pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}b\bar{b}$



271528 loop diagrams,  
up to 90 CS Dipoles;  
Calculation based on  
HELAC-NLO

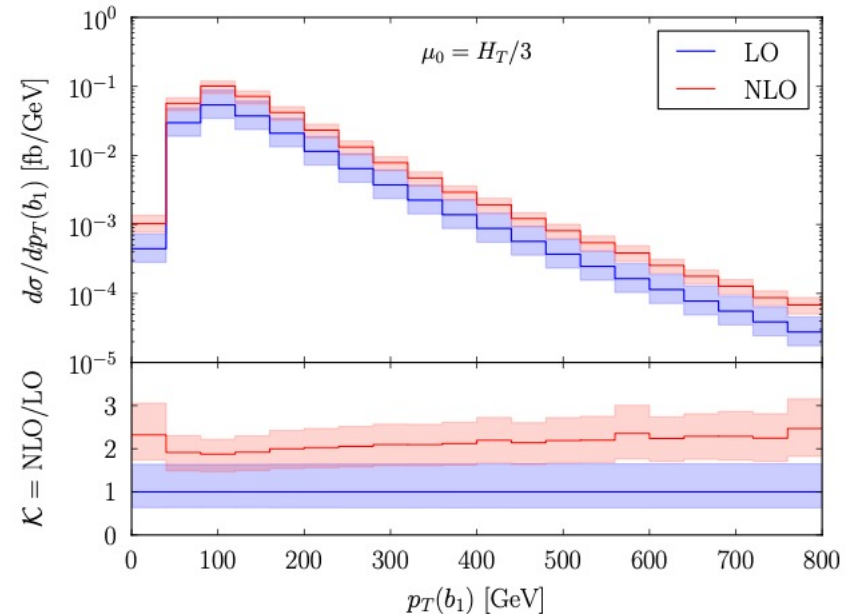
Comparison with results from **Denner, Lang, Pellen '20**

## Integrated cross section

$$\sigma_{\text{HELAC}}^{\text{NLO}} = 10.28(1)_{-21\%}^{+18\%} \text{ fb}$$

$$\sigma_{\text{DLP}}^{\text{NLO}} = 10.28(8)_{-21\%}^{+18\%} \text{ fb}$$

$p_T(b)$	$\sigma^{\text{LO}}$ [fb]	$\delta_{\text{scale}}$	$\sigma^{\text{NLO}}$ [fb]	$\delta_{\text{scale}}$	$\delta_{\text{PDF}}$	$K = \sigma^{\text{NLO}}/\sigma^{\text{LO}}$
$\mu_R = \mu_F = \mu_0 = m_t$						
25	6.998	+4.525 (65%) -2.569 (37%)	13.24	+2.33 (18%) -2.89 (22%)	+0.19 (1%) -0.19 (1%)	1.89
30	5.113	+3.343 (65%) -1.889 (37%)	9.25	+1.32 (14%) -1.93 (21%)	+0.14 (2%) -0.14 (2%)	1.81
35	3.775	+2.498 (66%) -1.401 (37%)	6.57	+0.79 (12%) -1.32 (20%)	+0.10 (2%) -0.10 (2%)	1.74
40	2.805	+1.867 (67%) -1.051 (37%)	4.70	+0.46 (10%) -0.91 (19%)	+0.08 (2%) -0.08 (2%)	1.68
$\mu_R = \mu_F = \mu_0 = H_T/3$						
25	6.813	+4.338 (64%) -2.481 (36%)	13.22	+2.66 (20%) -2.95 (22%)	+0.19 (1%) -0.19 (1%)	1.94
30	4.809	+3.062 (64%) -1.756 (37%)	9.09	+1.66 (18%) -1.98 (22%)	+0.16 (2%) -0.16 (2%)	1.89
35	3.431	+2.191 (64%) -1.256 (37%)	6.37	+1.07 (17%) -1.36 (21%)	+0.11 (2%) -0.11 (2%)	1.86
40	2.464	+1.582 (64%) -0.901 (37%)	4.51	+0.72 (16%) -0.95 (21%)	+0.09 (2%) -0.09 (2%)	1.83



- Large shape distortions (+90% – 135%)
- Scale dependence: ±20 – 30%
- PDF uncertainties small-ish ( $\leq 10\%$ )

$$p_T^{\text{veto}}(j) = 50 \text{ GeV}$$

$$K = 1.11 \text{ \& } K = 1.23$$

# Full Off-shell $t\bar{t}b\bar{b}$ @NLO QCD

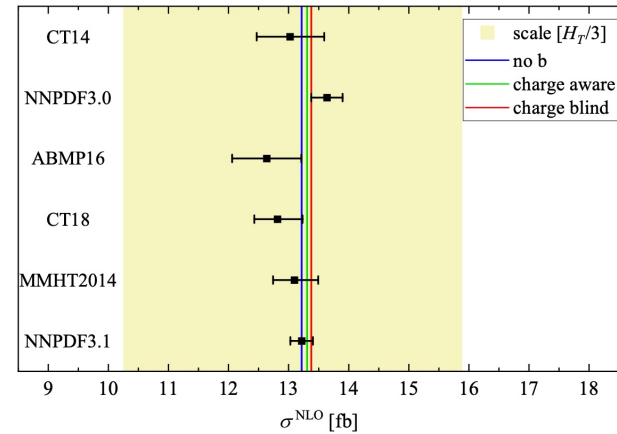
Michele Lupattelli

$pp \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b \bar{b} b \bar{b}$  @ LHC<sub>13TeV</sub>

Theoretical predictions	$\sigma_{e\mu+4b}$ [fb]
SHERPA+OPENLOOPS (4FS)	$17.2 \pm 4.2$
POWHEG-BOX+PYTHIA 8 (4FS)	16.5
POWHEL+PYTHIA 8 (5FS)	18.7
POWHEL+PYTHIA 8 (4FS)	18.2
HELAC-NLO (5FS)	$20.0 \pm 4.3$
Experimental result (ATLAS)	$25 \pm 6.5$

[ATLAS collaboration '18, Bevilacqua et al. '21]

Is there sensitivity to b-initiated processes?



We investigated the contribution of the  $b$ -quark initial states. We defined two  $b$ -jet tagging schemes:

- **Charge aware tagging scheme** ( $b\bar{b} \rightarrow g, bb \rightarrow b, \bar{b}\bar{b} \rightarrow \bar{b}, bg \rightarrow b \bar{b}g \rightarrow \bar{b}$ )  $N_b \geq 2 \ \& \ N_{\bar{b}} \geq 2$
- **Charge blind tagging scheme** ( $b\bar{b} \rightarrow g, bb \rightarrow g, \bar{b}\bar{b} \rightarrow g, bg \rightarrow b \bar{b}g \rightarrow \bar{b}$ )  $N_{b/\bar{b}} \geq 4$

$b$ -jet tagging	$\sigma^{\text{LO}}$ [fb]	$\frac{\sigma_i}{\sigma_{\text{no } b}} - 1$ [%]	$\sigma^{\text{NLO}}$ [fb]	$\frac{\sigma_i}{\sigma_{\text{no } b}} - 1$ [%]
no $b$	6.813(3)	-	13.22(3)	-
aware	6.822(3)	0.1	13.31(3)	0.7
blind	6.828(3)	0.2	13.38(3)	1.2

# A New Flavor-sensitive IRC-safe jet algorithm

Michal Czakon

The argument for introduction of the flavor  $k_T$  algorithm:  
**Starting from NNLO a wide angle soft quark-anti-quark pair leads to incorrect flavor assignment**

Banfi, Salam, Zanderighi, '06

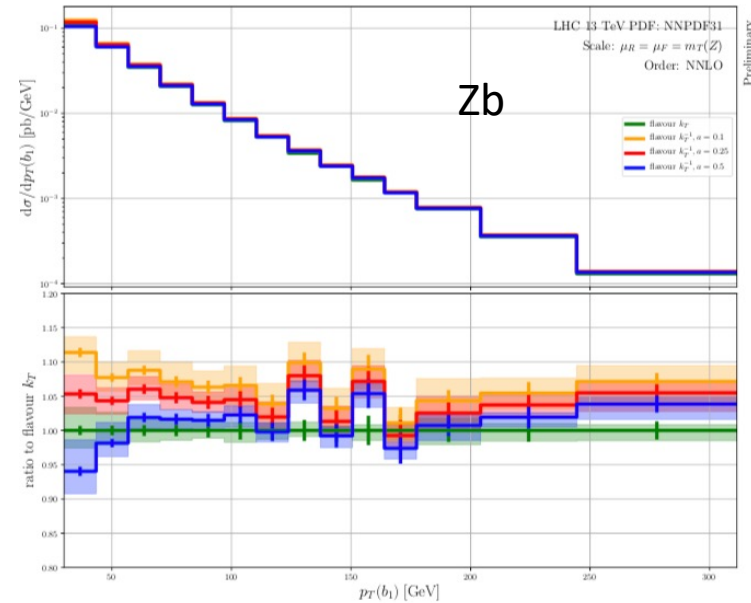
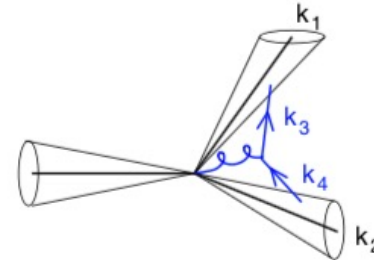
Distance measure depends on flavor:

$$d_{ij} = \frac{\Delta y_{ij}^2 + \Delta \phi_{ij}^2}{R^2} \begin{cases} \max(k_{ti}, k_{tj})^\alpha \min(k_{ti}, k_{tj})^{2-\alpha} & \text{softer of } i, j \text{ is flavoured,} \\ \min(k_{ti}, k_{tj})^\alpha & \text{softer of } i, j \text{ is unflavoured} \end{cases} \quad \begin{matrix} 0 < \alpha \leq 2 \\ \text{typically} \\ \alpha = 2 \end{matrix}$$

$$d_{i\bar{B}} = \begin{cases} \max(k_{ti}, k_{t\bar{B}}(y_i))^\alpha \min(k_{ti}, k_{t\bar{B}}(y_i))^{2-\alpha} & \text{softer of } i, j \text{ is flavoured,} \\ \min(k_{ti}, k_{t\bar{B}}(y_i))^\alpha & \text{softer of } i, j \text{ is unflavoured} \end{cases}$$

$$k_{tB}(y) = \sum_i k_{ti} (\Theta(y_i - y) + \Theta(y - y_i) e^{y_i - y})$$

$$k_{t\bar{B}}(y) = \sum_i k_{ti} (\Theta(y - y_i) + \Theta(y_i - y) e^{y_i - y})$$



Process defined with the **flavor  $k_T$  algorithm** in  
Gauld, Gehrmann-De Ridder, Glover, Huss, Majer '20

Studies also for top-pair production.  
 New flavor anti- $k_T$  is close to classic anti- $k_T$ .

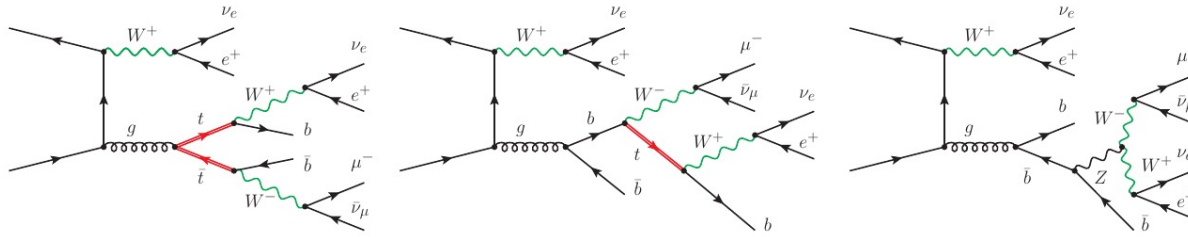
- Flavor anti- $k_T$  algorithm proposal MC, A. Mitov, R. Poncelet

$$d_{ij}^{(F)} = d_{ij} \begin{cases} \mathcal{S}_{ij} & \text{if } i, j \text{ is a flavoured pair} \\ 1 & \text{else} \end{cases}$$

$$\mathcal{S}_{q\bar{q}}^a = 1 - \theta(1-x) \cos\left(\frac{\pi}{2}x\right) \quad \text{with} \quad x = \frac{k_T(q)^2 + k_T(\bar{q})^2}{a2k_{T,\max}^2}$$

# Full Off-shell $t\bar{t}W^\pm$ @ NLO QCD

Jasmina Jasufi



- First NLO QCD calculation with full off-shell effects in this channel completed in 2020

G. Bevilacqua, H.-Y. Bi, H. B. Hartanto, M. Kraus, and M. Worek, JHEP 08, 043 (2020)

- Independent computation NLO QCD with full off-shell A. Denner, G. Pelliccioli (2020), 2007.12089
- Results for combined NLO QCD+EW with full off-shell effects A. Denner and G. Pelliccioli (2021), 2102.03246

	$\sigma_{\text{NLO}}^{t\bar{t}W^+}$ [ab]	$\sigma_{\text{NLO}}^{t\bar{t}W^-}$ [ab]
<b>Full off-shell</b>	$124.4^{+3\%}_{-6\%}$	$68.6^{+5\%}_{-7\%}$
<b>NWA</b>	$124.2^{+3\%}_{-6\%}$	$68.7^{+5\%}_{-7\%}$
<b>NWA<sub>LOdecay</sub></b>	$130.7^{+10\%}_{-10\%}$	$72.0^{+11\%}_{-11\%}$

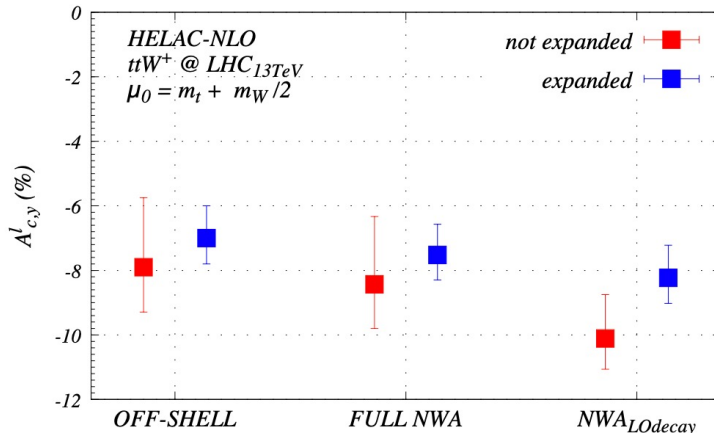
Bevilacqua et al., Eur. Phys. J. C 81, 675 (2021)

$$\mathcal{R} \equiv \sigma_{t\bar{t}W^+}^{\text{NLO}} / \sigma_{t\bar{t}W^-}^{\text{NLO}} = 1.81 \pm 0.03(\text{scale}) \pm 0.03(\text{PDF})$$

NNLO (2% – 3%) precision independent of modelling!

$$A_{c,y} = \frac{\sigma(\Delta|y| > 0) - \sigma(\Delta|y| < 0)}{\sigma(\Delta|y| > 0) + \sigma(\Delta|y| < 0)} \quad \Delta|y| \equiv |y_{\ell_t}| - |y_{\ell_{\bar{t}}}|$$

Modelling impacts central value and theoretical uncertainties.



# Impact of Off-shell Effects in DM Searches

➔ Calculate signal strength exclusion limits to quantify the relevance of these effects

Jonathan Herman

**Signal:**  $pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu\chi\bar{\chi}$  (tt+DM)

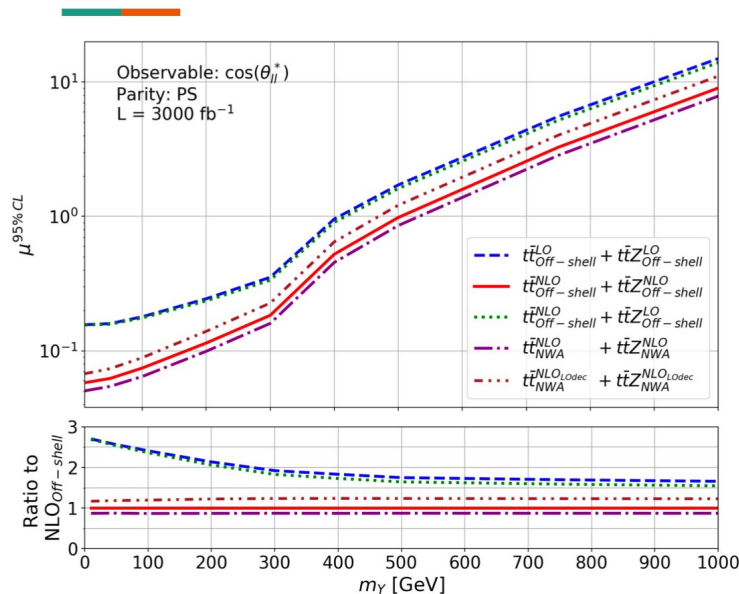
- > Spin-0 s-channel mediator model, DMSimp implementation [Backović, Krämer, Maltoni, Martini, Mawatari, Pellen '15](#)
- > generated with MadGraph [Alwall, Frederix, Frixione, Hirschi, Maltoni, Mattelaer, Shao, Stelzer, Torrielli, Zaro '14](#)
- > always kept at NLO with LO decays

**Background:**  $pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu$  (tt) [Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek '11](#)

$pp \rightarrow b\bar{b}e^+\mu^-\nu_e\bar{\nu}_\mu\nu_\tau\bar{\nu}_\tau$  (ttZ) [Bevilacqua, Hartanto, Kraus, Weber, Worek '19](#)

- > generated with HELAC-NLO [Bevilacqua, Czakon, Garzelli, van Hameren, Kardos, Papadopoulos, Pittau, Worek '11](#)
- > Compare LO & NLO as well as NWA & full off-shell

## Exclusion limits - Modelling



- LO inadequate due to large uncertainties, even if only using it for ttZ
- NLO with LO decays still too large due to large uncertainties and overestimated normalization
- In NWA, tt contribution is zero
- Full NWA results are too good due to missing off-shell tt contribution

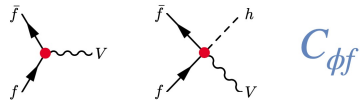
[J.H. Worek, arXiv:2108.01089](#)

# Interpretation of Precision Top Measurements: SMEFT

Ken Mimasu

## Top operator glossary

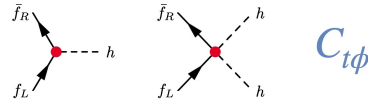
**currents**  $i(\bar{\varphi}^\dagger \overleftrightarrow{D}^\mu \varphi)(\bar{Q}\gamma^\mu Q)$



$C_{\phi f}$

- Shift SM  $f\bar{f}V$  couplings
- $f\bar{f}Vh$  contact interactions

**Yukawa**  $(\bar{q} t \tilde{\varphi})(\varphi^\dagger \varphi)$



$C_{t\phi}$

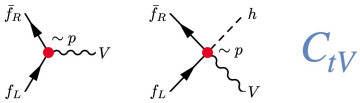
- Decouple  $m_t$  &  $y_t$
- $t\bar{t}hh(h)$  contact interactions

**Indirect:** new physics is heavy  $\Rightarrow$  modifies top “properties”

- Precision measurements seeking new physics via new interactions
- Complementary to direct searches

Established framework: **SMEFT**  $\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{c_i}{\Lambda^{D-4}} \mathcal{O}_i^D$

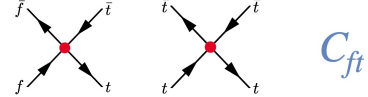
**dipole**  $(\bar{q} \sigma_{\mu\nu} t \tilde{\varphi})V^{\mu\nu}$



$C_{tV}$

- Chirality flipping  $f\bar{f}V$  couplings
- $f\bar{f}V(V)h$  contact interactions
- $W, B$  &  $G$  fields

**4 fermion**  $(\bar{q}\gamma_\mu q)(\bar{Q}\gamma^\mu Q)$



$C_{ft}$

- Contact interactions
- 2-heavy-2-light or 4-heavy
- Numerous ( $\sim O(20)$  w/ top)

The future is bright for top physics in SMEFT

- Global SMEFT analyses are **rapidly expanding** & probing model space
- New precision tools available (**SMEFTatNLO**): **NLO** & **loop-induced** effects
- Being incorporated into experimental interpretations
- Rare EW top production: **high energy** & **high multiplicity**
- Towards **global measurements** for global fits

# Interpretation in SMEFT: Theory Challenges

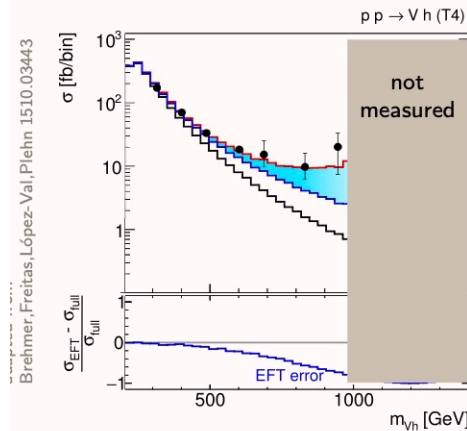
Ilaria Brivio

## Good news:

- ✓ ~common conventions for bases, tools for translation
- ✓ consistent formulation with/without flavor symmetries
- ✓ correct treatment of input parameters
- ✓ LO predictions fully automated (any operator in any process), NLO QCD to a good extent
- ✓ understanding of NLO EW improved substantially
- ✓ 1-loop RGE running well understood and automated
- ✓ 1-loop matching to BSM models automated
- ✓ 1-loop matching to LEFT/WET
- ✓ good understanding of measurements' constraining power
- ✓ global analyses with up to ~ 30 free parameters
- ✓ strategies to handle unconstrained directions (PCA) and understand fit structure (Fisher info)

How about theoretical uncertainties due to missing higher EFT orders?

EFT obtained from matching to full model



**top-down:**  $C_i$  fixed by matching  
→ EFT not valid in high-E region

**bottom-up:** fit  $C_i$  to data  
tends to make EFT match full result  
→ find wrong values of  $C_i$

how to keep this into account?

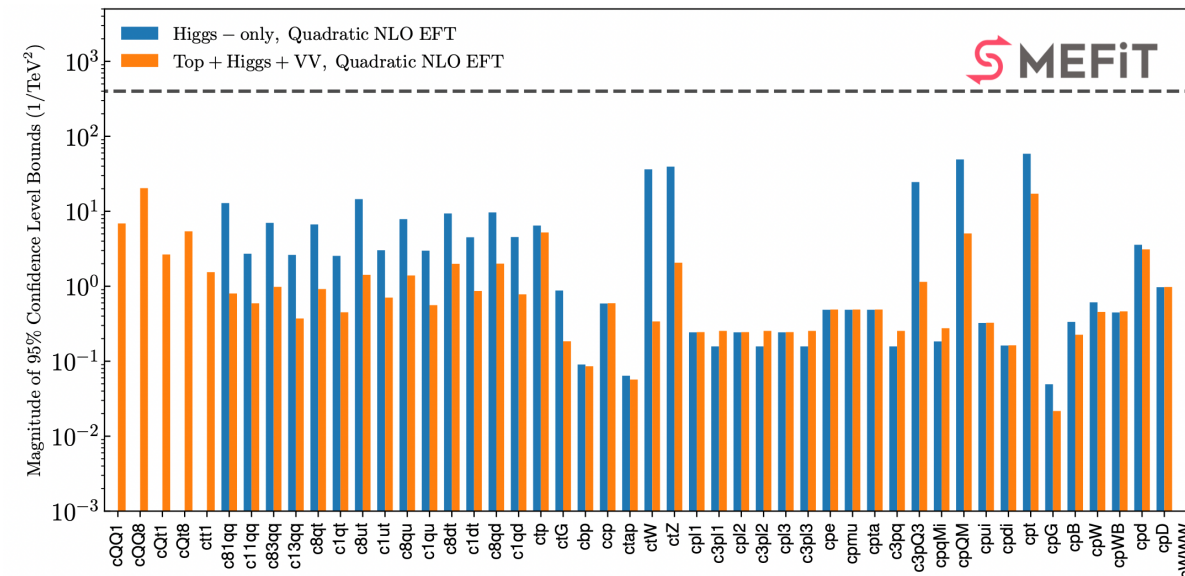
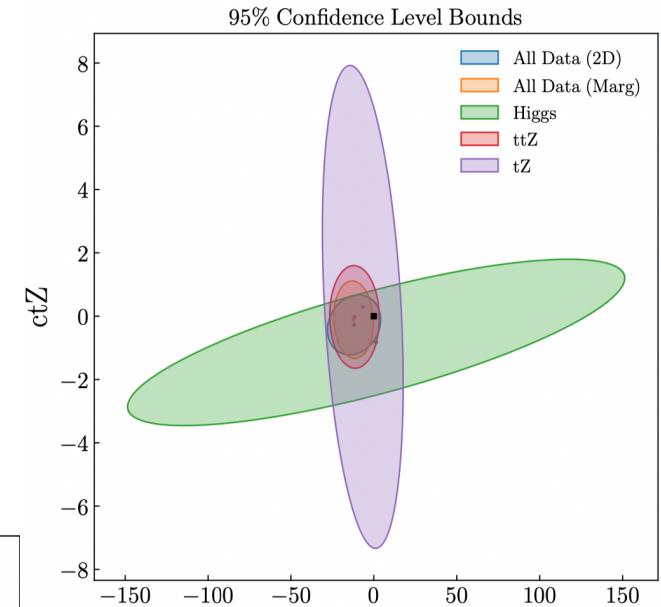
## More challenges:

- ▶ Inclusion of CP violating terms
- ▶ Unified flavor treatment → combination with low-E
- ▶ Streamlining/automating NLO EW calculations in SMEFT
- ▶ 2-loop RGE running (consistency with 1-loop matching)
- ▶ Treatment of scale uncertainties in NLO SMEFT calculations
- ▶ Implementation of unitarity constraints & positivity bounds
- ▶ Handling fits with 50+ parameters → bayesian?
- ▶ Interplay with direct searches
- ▶ SMEFT in non-perturbative effects? PDF, hadronization...

# Interpretation in SMEFT: Top-Higgs interplay

Luca Mantani

Category	Processes	$n_{\text{dat}}$
Top quark production	$t\bar{t}$ (inclusive)	94
	$t\bar{t}Z, t\bar{t}W$	14
	single top (inclusive)	27
	$tZ, tW$	9
	$t\bar{t}t, t\bar{t}b\bar{b}$	6
	<b>Total</b>	<b>150</b>
Higgs production and decay	Run I signal strengths	22
	Run II signal strengths	40
	Run II, differential distributions & STXS	35
	<b>Total</b>	<b>97</b>
Diboson production	LEP-2	40
	LHC	30
	<b>Total</b>	<b>70</b>
Baseline dataset	<b>Total</b>	<b>317</b>



Plans: Add new data (e.g. VBS); improve theory (e.g. more systematic in including NLO QCD,EW; improve fit methodology)

J. Ethier, F. Maltoni, E. Nocera, J. Rojo, E. Slade, E. Vryonidou and C. Zhang, arXiv:2105.00006



# Interpretation in SMEFT: Towards a Global Fit

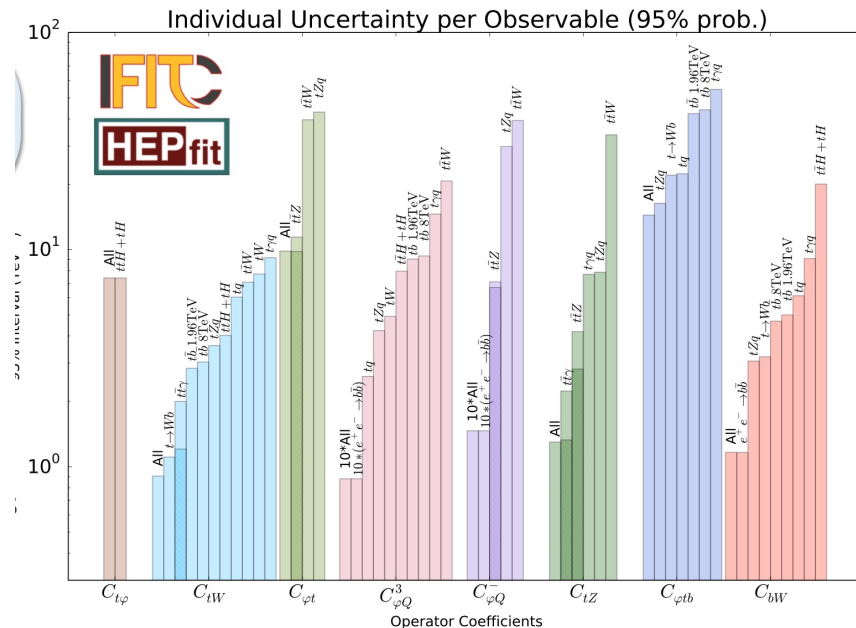
Maria Moreno Llacer

Process	Observable	$\sqrt{s}$	$\int \mathcal{L}$	Experiment
$pp \rightarrow t\bar{t}H$ NLO	cross section	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow t\bar{t}W$ NLO	cross section	13 TeV	36 fb <sup>-1</sup>	CMS
$pp \rightarrow t\bar{t}Z$ NLO	(differential) x-sec.	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow t\bar{t}\gamma$ NLO	(differential) x-sec.	13 TeV	140 fb <sup>-1</sup>	ATLAS
$pp \rightarrow tZq$ NLO	cross section	13 TeV	140 fb <sup>-1</sup>	CMS
$pp \rightarrow t\gamma q$ NLO	cross section	13 TeV	36 fb <sup>-1</sup>	CMS
$pp \rightarrow tb$ (s-ch) NLO	cross section	8 TeV	20 fb <sup>-1</sup>	ATLAS+CMS
$pp \rightarrow tW$ NLO	cross section	8 TeV	20 fb <sup>-1</sup>	ATLAS+CMS
$pp \rightarrow tq$ (t-ch) NLO	cross section	8 TeV	20 fb <sup>-1</sup>	ATLAS+CMS
$t \rightarrow W^+b$ NLO	$F_0, F_L$	8 TeV	20 fb <sup>-1</sup>	ATLAS+CMS
$p\bar{p} \rightarrow t\bar{t}$ (s-ch) LO	cross section	1.96 TeV	9.7 fb <sup>-1</sup>	Tevatron
$e^-e^+ \rightarrow b\bar{b}$ LO	$R_b, A_{FBLR}^{bb}$	$\sim 91$ GeV	202.1 pb <sup>-1</sup>	LEP

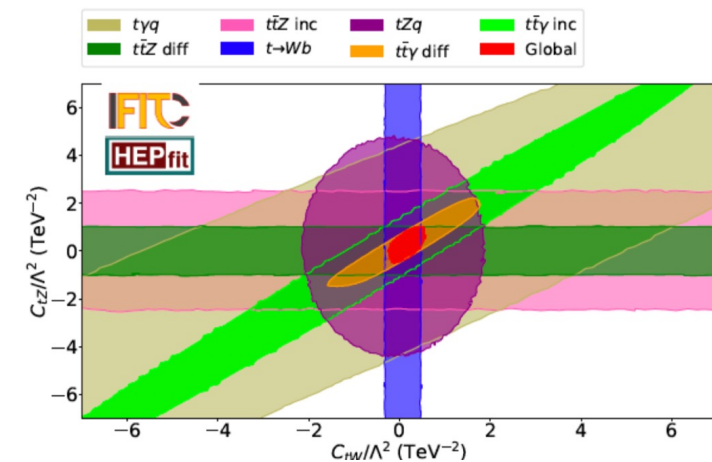
Here, we consider 8 dim-six operators in the Warsaw basis:

- ☆ Left/Right-handed couplings of top/bottom to Z:  $O_{\varphi t}, O_{\varphi Q}, O_{\varphi Q}^{(3)}$
- ☆ EW dipole operators:  $O_{tZ}, O_{tW}, O_{bW}$
- ☆ Top Yukawa:  $O_{t\varphi}$
- ☆ Charged current interaction:  $O_{\varphi tb}$

arXiv: 2107.13917



2D 95% probability contours showing complementarity between measurements



## Implications for top physics - top decays

### CC top decays

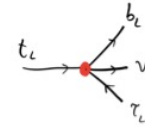
Solutions addressing  $R(D^{(*)})$  only via LH couplings contribute to

$$[O_{lq}^{(S)}]^{333} = (\bar{l}_l^3 \gamma_\mu l_l^3) (\bar{q}_l^3 \gamma^\mu q_l^3) \supset V_{tb}^* (\bar{\nu}_\tau \gamma_\mu \tau_l) (\bar{b}_l \gamma^\mu t_l)$$

Buttazzo, Greife, Isidori, DM 1706.07808

with a typical size of O(few %) of the SM amplitude:  $C_{lq} \sim (2\text{TeV})^{-2}$

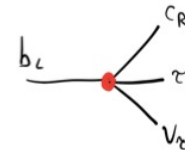
$\longrightarrow$   $Br_{\text{BSM}} \sim 10^{-7}$



### FCNC top decays

Solutions addressing  $R(D^{(*)})$  via **mixed LH and RH interactions**, such as via **S<sub>1</sub>** and **R<sub>2</sub>** leptoquarks, also require a **sizeable coupling to C<sub>R</sub>**.

$$\mathcal{L}_{\text{eff}} = \frac{\lambda_{C\tau}^R \lambda_{b\tau}^{L+}}{2 M_1^2} \left[ (\bar{l}_l^3 \tau_R) \varepsilon (\bar{q}_l^3 C_R) - \frac{1}{4} (\bar{l}_l^3 \gamma_\mu \tau_R) \varepsilon (\bar{q}_l^3 \gamma^\mu C_R) \right] \longrightarrow$$



Directly correlated with  $R(D^{(*)})$

$$t_L \longrightarrow C_R, \tau_R, \tau_L \sim \frac{\lambda_{C\tau}^R \lambda_{b\tau}^L}{M_1^2} \sim (2\text{TeV})^{-2}$$

$Br_{\text{FCNC}} \sim 10^{-7}$

- While in most models NP has **sizeable couplings to top quark**, **effects in top decays** are expected to be **very small**, due to the large scale of NP.
- Top quarks play instead a **major role as final states of leptoquark searches**, crucial to discovery or putting limits.

# Interpretation in SMEFT: $tWZ$ production at NLO QCD

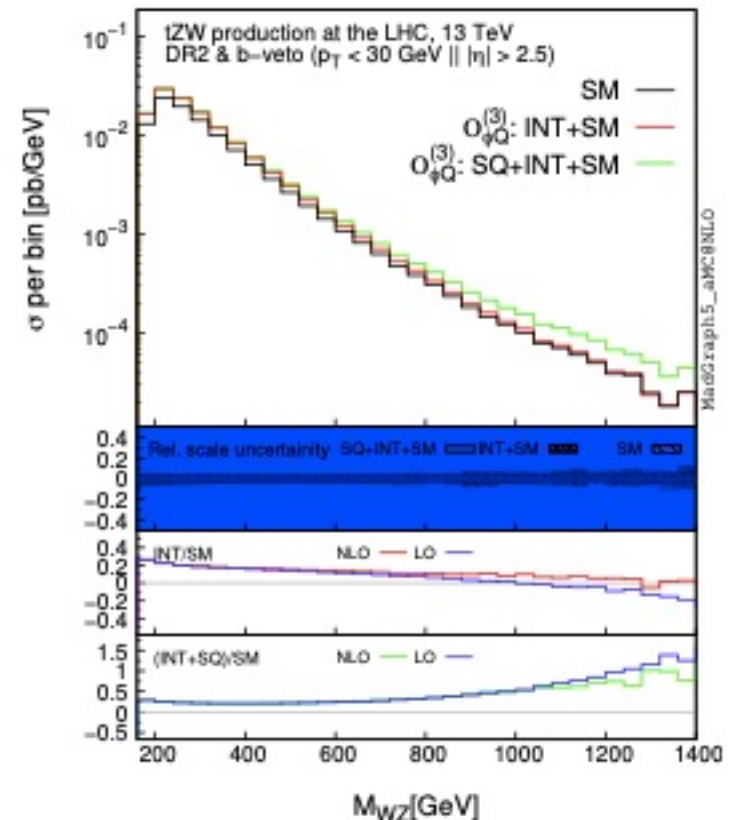
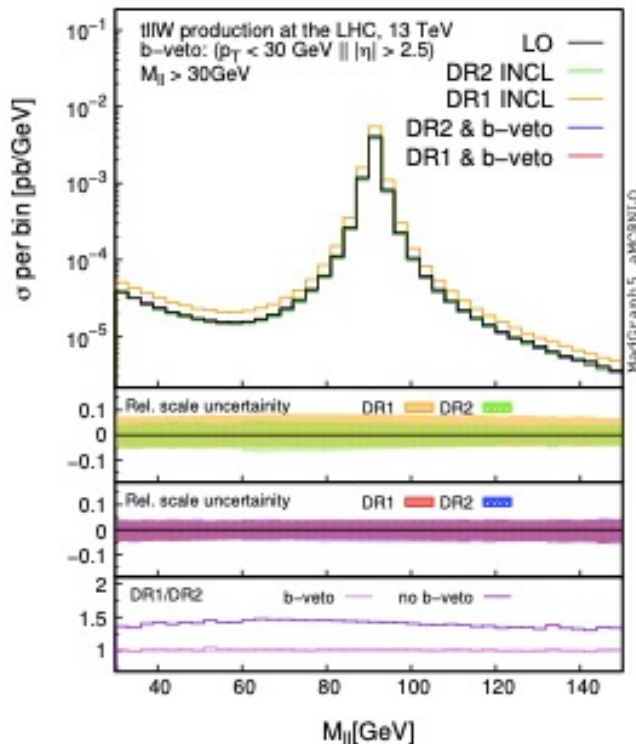
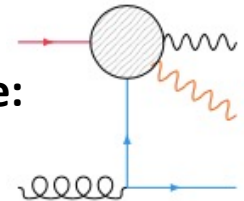
Hesham El Faham

$tWZ$  at NLO is non-trivial due to its overlap with other processes:

The  $tWZb$  final state can also have resonant contributions, from  $ttZ, t \rightarrow Wb$ , or  $tt, t \rightarrow WZb$  and not necessarily the non-resonant  $tWZb$

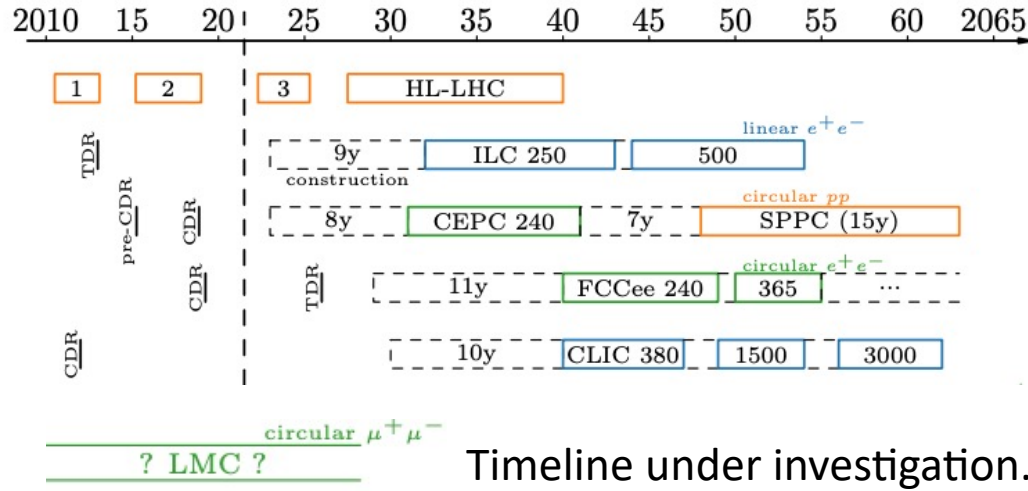
$tWZ$  in the SMEFT

The  $bW \rightarrow tZ$  sub-amplitude:



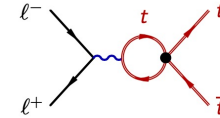
# Many Possible Paths to an Exciting Future!

Gauthier Durieux



## Leptons for tops

ideal for electroweak couplings ... as clean as a dream

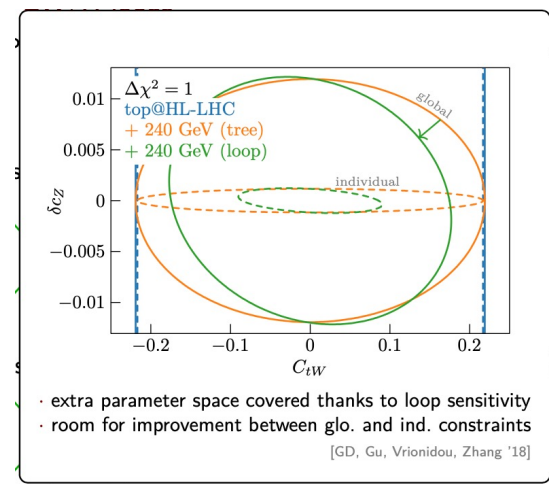
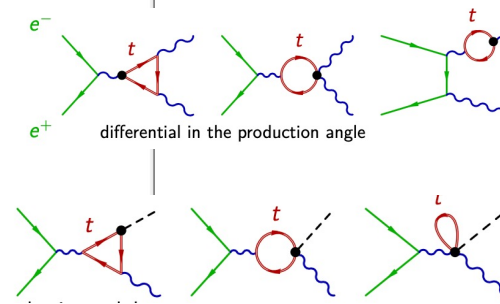
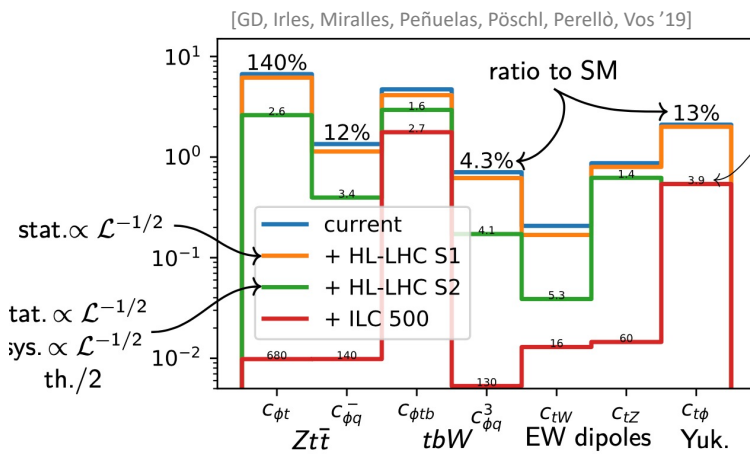


beating LHC on four-fermions

... with great potential for heavy BSM

reaching quantum/loop sensitivities

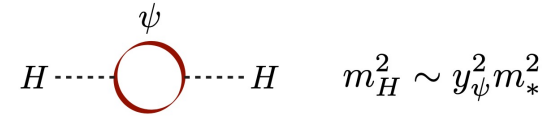
... Higgs processes become also top processes



# Top Compositeness @ Future Colliders

Javier Serra-Mari

- Top (effective) compositeness is a very motivated target for high-energy colliders.  
In particular because of its connection to the origin of the electroweak scale.



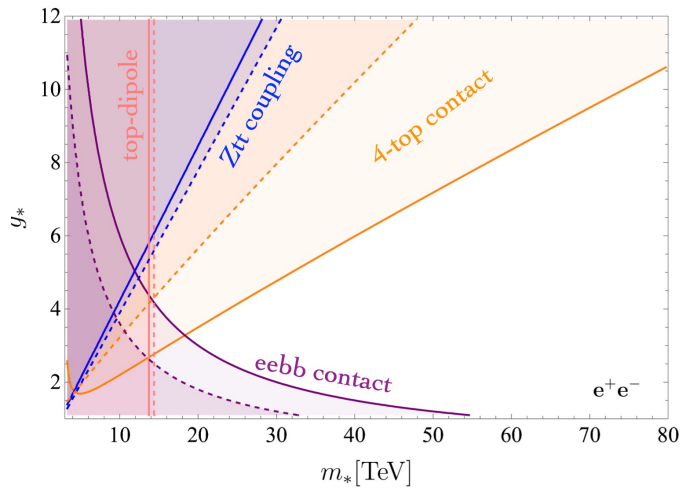
- Current LHC measurements are becoming very interesting.  
Probes of genuine strong 4-top production competitive with Higgs precision.

- Future colliders would provide very powerful tests of a strongly-interacting top.  
Hadron colliders, directly via strong  $tt$ -scattering in 4-top production.  
Lepton colliders, indirectly via RGE effects in top-pair production.

$$\frac{m_*}{g_*} \Big|_{\text{LHC, 36/fb}}^{4t} \gtrsim 0.73 \text{ TeV} \quad \frac{m_*}{g_*} \Big|_{\text{FCC-hh}}^{4t} \gtrsim 6.5 \text{ TeV} \quad \frac{m_*}{g_*} \Big|_{\text{CLIC 3}}^{t\bar{t}} \gtrsim 7.7 \text{ TeV} \quad \frac{m_*}{g_*} \Big|_{\text{muon 10}}^{t\bar{t}} \gtrsim 18 \text{ TeV}$$

$$\frac{c_{\psi\psi}}{m_*^2} (\bar{\psi}\gamma_\mu\psi)^2$$

$c_{\psi\psi} \sim g_*^2$



— CLIC  
 $\sqrt{s} = 0.38, 1.4, 3 \text{ TeV}$   
 $L = 0.5, 1.5, 3 \text{ /ab}$

- - - ILC  
 $\sqrt{s} = 0.5, 1 \text{ TeV}$   
 $L = 0.5, 1 \text{ /ab}$

Based on reinterpretation of results for sensitivity to the individual operators: Durieux, Perelló, Vos, Zhang '18. See also Durieux, Matsedonskyi '18.

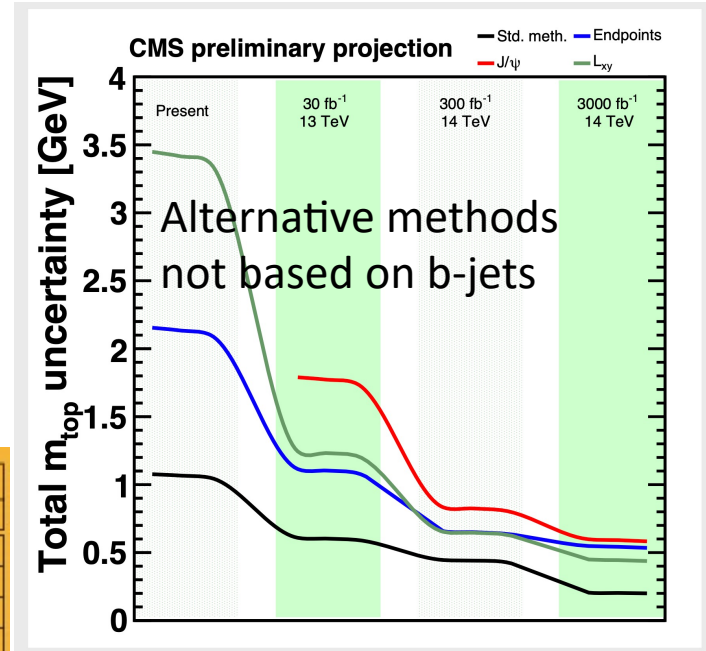
# Top Physics Opportunities @ HL-LHC

Roberto Franceschini

For each observable used in top quark mass measurement with b-jets a derived observable can be defined using the B-hadron instead of the b-jet (and JES  $\leftrightarrow$  Hadronization)

$$m(\text{b-jet, lepton}) \Rightarrow m(\text{B-hadron, lepton})$$

What are the hadronization uncertainties ?



1712.05801 Corcella, RF, Kim

- Top quark mass
- Yukawa coupling
- CP tth, th+X, tt+mET

$$\mathcal{L}_{ht} = -\frac{y_t}{\sqrt{2}} \bar{t}(\kappa + i\tilde{\kappa}\gamma_5)th$$

Sensitivity to shower and hadronization PYTHIA parameters of the top quark mass extracted from the first Mellin moment of mass-sensitive observables:

Mellin-1	$\Delta_{m_t}^{(O)}$	$\frac{dm_t}{d\mathcal{M}_1}$	$\Delta_{\theta}^{(m_t)}$					
			$\alpha_s, FSR$	$p_{T, \min}$	recoil	$r_B$	$a$	$b$
$E_B$	1.1	2.4	0.43	0.019	0.028	0.039	0.020	0.039
$E_B + E_B$	1.2	0.99	0.42	0.019	0.032	0.046	0.023	0.034
$p_{T, B}$	1.2	3.3	0.43	0.021	0.027	0.043	0.022	0.042
$p_{T, B} + p_{T, B}$	1.2	1.47	0.36	0.017	0.024	0.042	0.016	0.044
$m_{B\ell, \min}$	1.0	2.6	0.26	0.011	0.016	0.041	0.011	0.031
$m_{B\ell, \text{true}}$	1.2	1.63	0.24	0.008	0.013	0.031	0.009	0.022

$\alpha_s$  needed at 1%

$a, b, r_B, \text{recoil}$ , and  $p_{T, \min}$ : determining them to a 10% accuracy

should be enough to warrant a 0.5% precision on  $m_t$ . *Agashe, Airen, RF, Kim, Sathyan – B decay length*

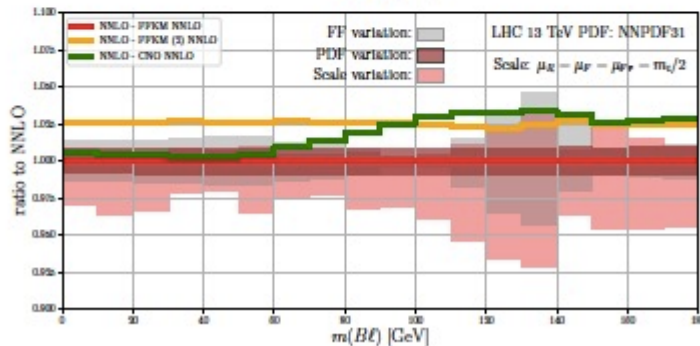
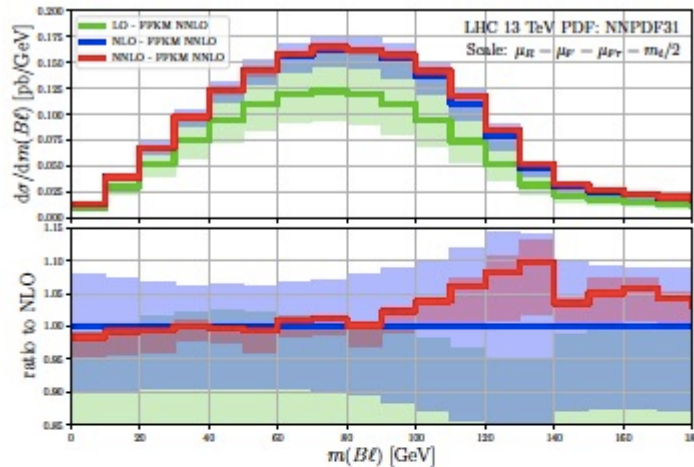
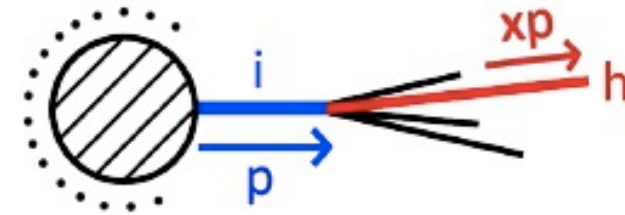
# Top-pair production with B hadrons @ NNLO QCD

- Process considered:

$$p p \rightarrow t(\rightarrow B W^+ + X) \bar{t}(\rightarrow \bar{b} W^-)$$

$\hookrightarrow \ell^+ \nu_\ell$                        $\hookrightarrow \ell^- \bar{\nu}_\ell$

Terry Generet



- Implementation of fragmentation in a numerical code for NNLO cross sections

- "Standard" recipe for theory errors:

$$\sigma_{tot} = \sigma_{scale} \oplus \sigma_{PDF} \oplus \sigma_{FF}$$

Michał Czakon, Terry Generet, Alexander Mitov, René Poncelet  
arXiv:2102.08267

# $M_{\text{top}}$ from $t\bar{t}j$ @ LHC: scale uncertainty

$$\mathcal{R}(m_t, \rho) = \frac{1}{\sigma_{t\bar{t}+1 \text{ jet}}} \frac{d\sigma_{t\bar{t}+1 \text{ jet}}}{d\rho}(m_t, \rho)$$

$$\rho = \frac{2m_0}{m_{t\bar{t}j}}, \quad m_0 = 170 \text{ GeV}$$

arXiv:1303.6415

ATLAS measurement ( $\sqrt{s} = 8 \text{ TeV}$ , 2019)[2]

$$m_t^{\text{pole}} = 171.1 \pm 0.4(\text{stat}) \pm 0.9(\text{sys}) {}^{+0.7}_{-0.3}(\text{th}) \text{ GeV}$$

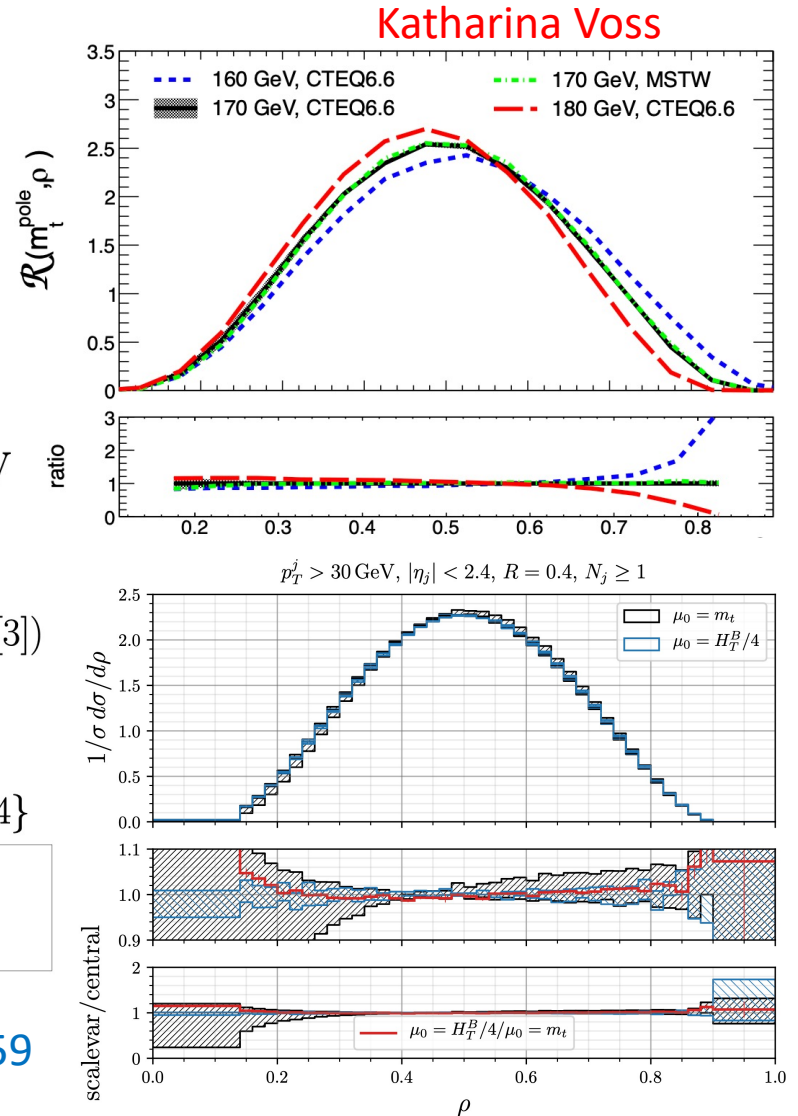
arXiv:1905.02302

- POWHEG-BOX  $t\bar{t}j$  reimplementation V2 (previous version V1[3])
- $N_j \geq 1$ ,  $p_T^j > 30 \text{ GeV}$ ,  $|\eta_j| < 2.4$ , anti- $k_T$  with  $R = 0.4$
- PDF set: CT18NLO

Study of fixed ( $\mu_0 = m_t$ ) and dynamical scale ( $\mu_0 \in \{H_T^B/2, H_T^B/4\}$ )

$$H_T^B = \left( \sqrt{p_{T,t}^B{}^2 + m_t^2} + \sqrt{p_{T,\bar{t}}^B{}^2 + m_t^2} + p_{T,j}^B \right)$$

arXiv:1609.01659





# $t\bar{t}H(M_{\text{top}}(\overline{\text{MS}})) @ \text{LHC}$

Andrej Saibel

- First study of  $t\bar{t}H$  production with top quark running mass!

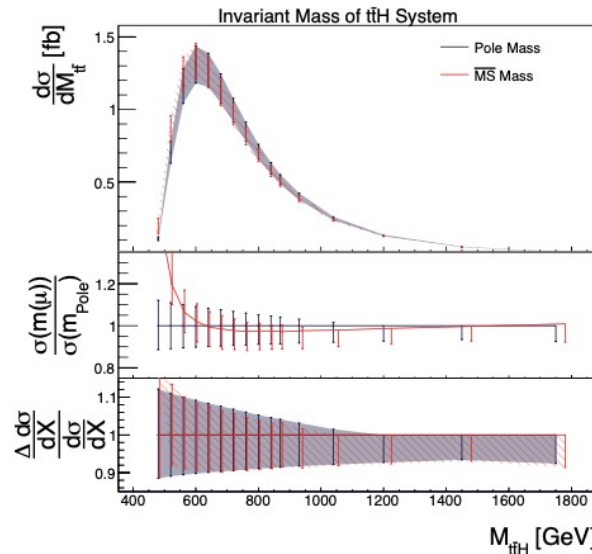
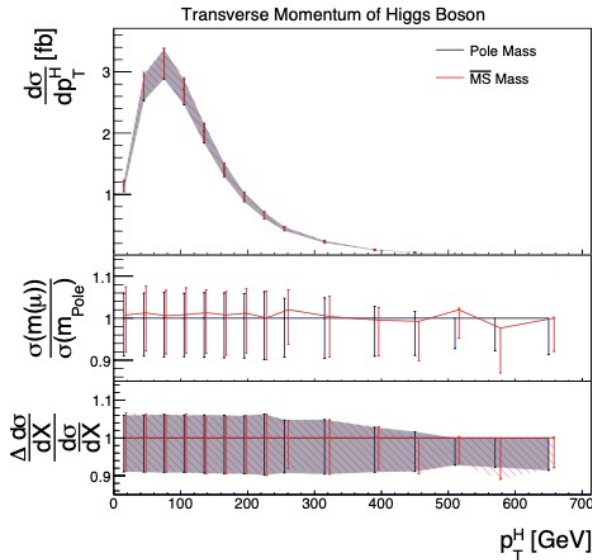
With MARIA ALDAYA MARTIN, SVEN-OLAF MOCH

Using the relationship

$$m_t^{\text{pole}} = m(\mu_R) \left( 1 + \frac{\alpha_s}{\pi} d_1 + \dots \right)$$

$\sigma(m_t^{\text{pole}})$  is used to calculate  $\sigma(m(\mu_R))$

- Energy dependence of mass ( $m(\mu_R)$ )
- **Improved convergence** and **smaller scale dependences** compared to pole mass shown for  $t\bar{t}$  production



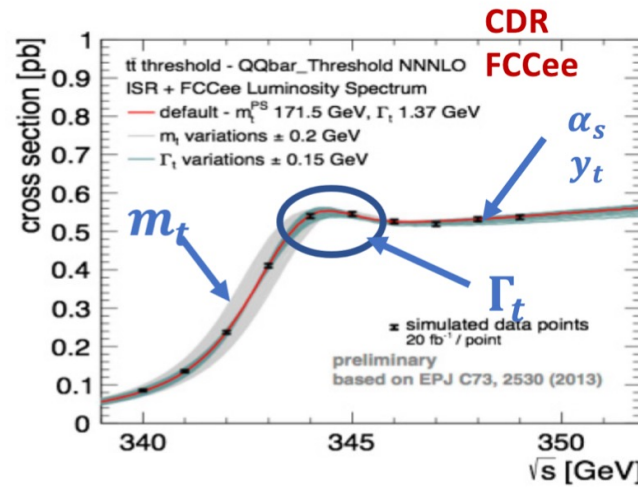
Impact on reduction of scale uncertainties small  
– Largest impact on  $M_{t\bar{t}H}$

# Top Threshold Physics @ $e^+e^-$ Colliders

Andre Hoang

$$v \sim \alpha_s \sim 0.1$$

Requires resummation of singular velocity terms done within nonrelativistic QCD (NRQCD) by solving a Schroedinger-type eq. for propagation of the top-anti-top system.



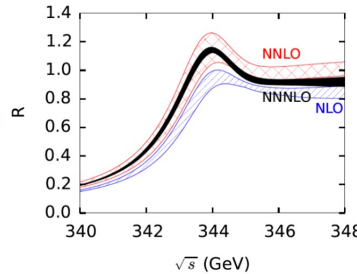
- Threshold runs: ILC, CLIC, FCC-ee
- Typical:  $100 \text{ fb}^{-1}$  integrated luminosity
- Typical:  $\sigma_{\text{tot}} \sim 1 \text{ pb} \rightarrow 10^5 \text{ ttbar pairs}$
- Threshold scan: high precision method for top quark mass measurement in a well-defined scheme:  $(\Delta m_t^{\text{PS,1S,MSR}} \sim 50 \text{ MeV})$
- Sensitivity to  $\Gamma_t, \alpha_s, y_t$
- Need: precise knowledge of beam effects

• Simple factorization formula up to NNLO/NNLL<sub>QCD</sub> + LO<sub>EW</sub> :

$$\sigma_{t\bar{t}} \propto c(v)^2 \text{Im} G(0,0,\sqrt{s}) + \dots$$

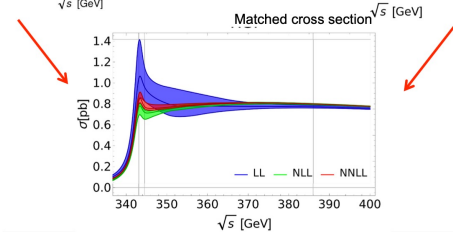
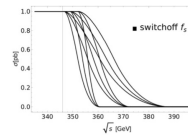
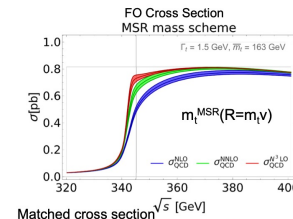
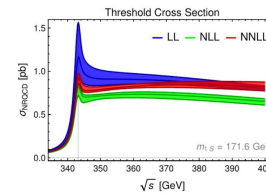
→ More complicated beyond

$$\left( -\frac{\nabla^2}{m} - \frac{\nabla^4}{4m^3} + V(\mathbf{r}) - (\sqrt{s} - 2m - 2\delta m) - i\Gamma_t \right) G(\mathbf{r}, \mathbf{r}') = \delta^{(3)}(\mathbf{r} - \mathbf{r}')$$



• Total cross section in good shape:  $d\sigma_{\text{tot}}/\sigma_{\text{tot}} \sim 2\text{-}3\%$  (for NNLL<sub>QCD</sub> / NNNLO<sub>QCD</sub>)

• Combination of NNLL<sub>QCD</sub> and NNNLO<sub>QCD</sub> to be done.



Scale-setting subtle!  
Dependence on matching function smaller than scale-dependence.  
Uncertainties much larger in the pole mass scheme.

Combination of the of NNNLO FO and NNLO+NNLL threshold cross section

$$\sigma_{\text{matched}} = \sigma_{\text{QCD}} + (\sigma_{\text{vNRQCD}} - \sigma_{\text{double-counted}}) \cdot f_s$$

← Switchoff- function

Fully differential treatment + MC simulations still in infancy.

Differential cross sections in Whizard (NLOFO + LLthreshold) **Bach, Neja, AHH, Kilian, Reuter '17**

# Heavy flavor and top quark physics @ Snowmass 2021

EF03 Topical Group Conveners:

Reinhard Schwienhorst ([schwier@msu.edu](mailto:schwier@msu.edu)), DW ([dw24@buffalo.edu](mailto:dw24@buffalo.edu) )

- We invite you to contribute to Top/Heavy Flavor production studies
  - EF03 wiki page at [https://snowmass21.org/energy/heavy\\_flavour](https://snowmass21.org/energy/heavy_flavour)
  - Email the conveners: [schwier@msu.edu](mailto:schwier@msu.edu), [dw24@buffalo.edu](mailto:dw24@buffalo.edu)
  - Mailing list [SNOWMASS-EF-03-TOP\\_HEAVY-FLAVOR@FNAL.GOV](mailto:SNOWMASS-EF-03-TOP_HEAVY-FLAVOR@FNAL.GOV)
  - Please contact conveners to schedule a presentation at our biweekly meetings
- Many opportunities to contribute to Top/Heavy Flavor production physics
  - So far most input from ILC and HL-LHC,
  - Top physics potential talks from FCC-ee, LHeC and FCC-eh
  - Study top at other colliders (new: muon collider)
  - Need many more HL-LHC studies to explore full program
- Informal (incomplete) list of projects, possible collaborations, open questions, etc.:

<https://docs.google.com/document/d/17aPp9XpJAImmPInPNtgV21rG2zEiFS2IHkO-ooC4rcQ>

# Thank you!

## **International Advisory Committee:**

Jorgen D'Hondt, VUB Brussels  
Andreas Jung, Purdue University  
Seung J. Lee, Korea University  
Hongbo Liao, IHEP CAS  
Fabio Maltoni, UC Louvain  
Michelangelo Mangano, CERN  
Alexander Mitov, Cambridge University  
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Ben Pecjak, Durham University  
Francesco Spanò, Royal Holloway College  
Roberto Tenchini, INFN Pisa  
Malgorzata Worek, RWTH Aachen  
University (Chair)

## **Local Organizing Committee:**

Huey-Wen Lin, Michigan State University  
Christopher Neu, University of Virginia  
Reinhard Schwienhorst, Michigan State  
University (Chair)  
Pekka Sinervo, University of Toronto

Special thanks to the speakers and poster presenters for making this such an exciting workshop!