

Quenching effects in the jet spectrum at various cone sizes

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and others Joao Barata, Yacine Mehtar-Tani,
Alba Soto-Ontoso, Daniel Pablos, Konrad Tywoniuk

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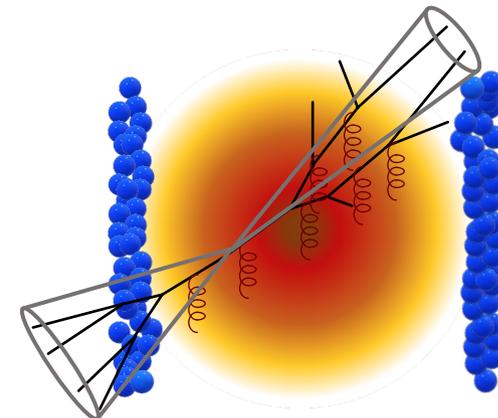
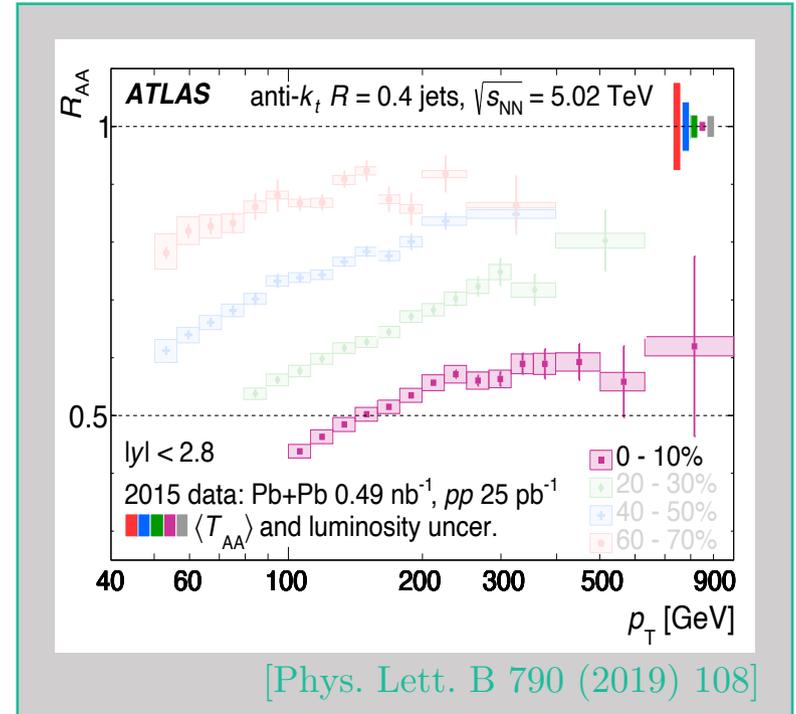
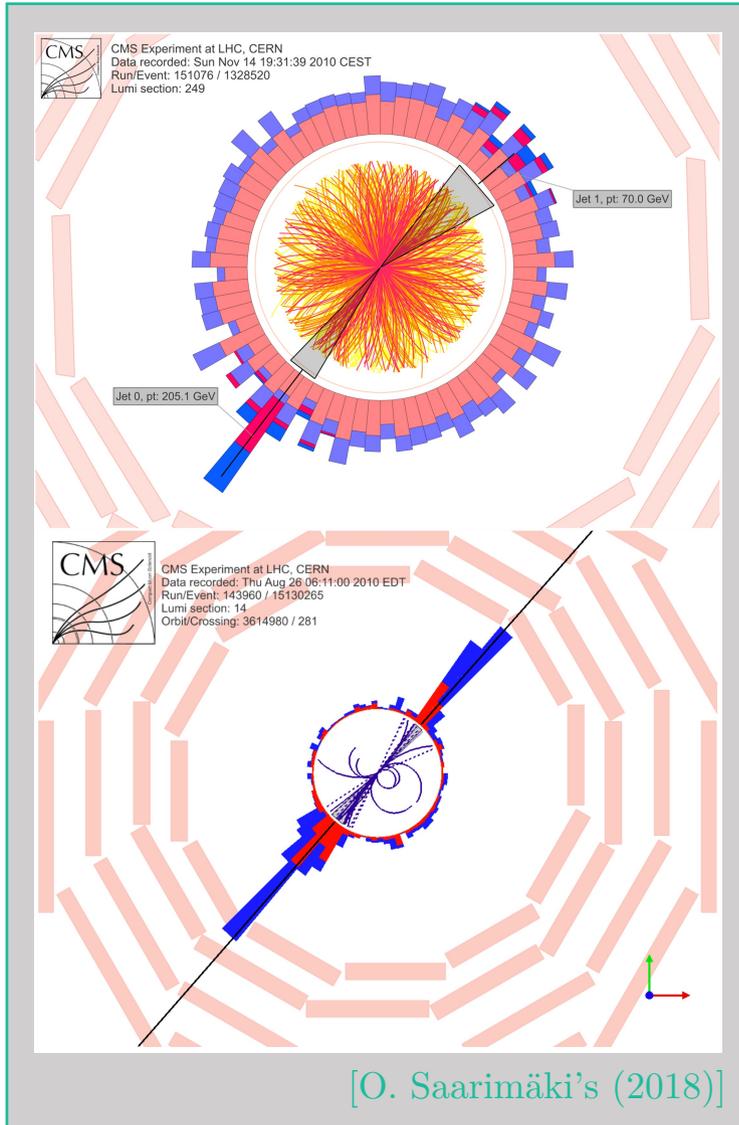
Supported by the Trond Mohn Foundation BFS2018REK01
and MCnetITN3 H2020 Marie Curie Initial Training Network 722104



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Introduction to jet quenching - Phenomenology



Introduction to jet quenching - Framework

[Zakharov, BDMPS, GLV, Wiedemann (1996-2000)
Blaizot, Iancu, Salgado, CGC formalism (2012-)]

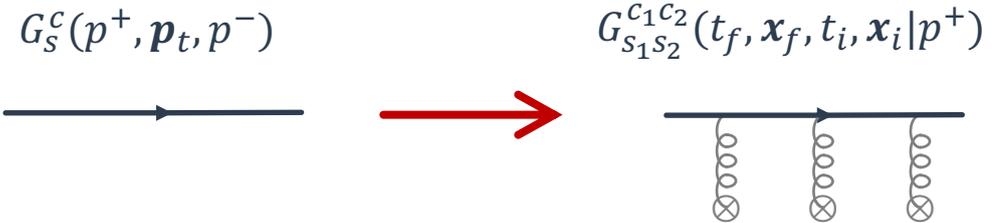
QCD with medium bkg:

- Colored background $\mathcal{A}_0(t, \mathbf{x})$
- Energy is conserved (p^+), transverse kick (\mathbf{p})
- Multiple scatterings

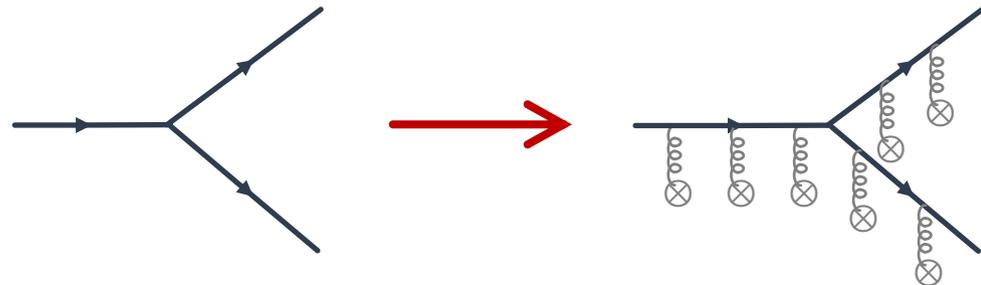


Keeping space-time: partial Fourier space $(p^+, \mathbf{p}, p^-) \rightarrow (p^+, \mathbf{x}, t)$

- Effective propagator:



- Effective vertices:



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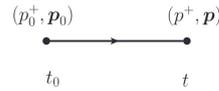
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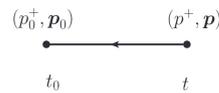
Keeping space-time: parti

- Effective prop
- Effective verti

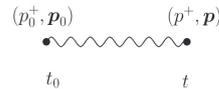
1. Internal lines: which correspond to propagators between time t_0 and t read:



$$\frac{i\gamma^-}{4p^+} (\mathbf{p} | \mathcal{G}_{\text{scal}}(t, t_0) | \mathbf{p}_0) (2\pi) \delta(p^+ - p_0^+) \quad \text{for quarks} \quad (161)$$

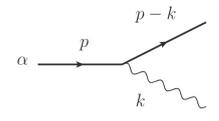


$$\frac{i\gamma^+}{4p^+} (\mathbf{p} | \mathcal{G}_{\text{scal}}^\dagger(t, t_0) | \mathbf{p}_0) (2\pi) \delta(p^+ - p_0^+) \quad \text{for anti-quarks} \quad (162)$$

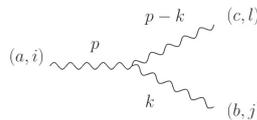


$$\frac{i}{2p^+} \delta^{ij} (\mathbf{p} | \mathcal{G}_{\text{scal}}^{\text{adj}}(t, t_0) | \mathbf{p}_0) (2\pi) \delta(p^+ - p_0^+) \quad \text{for gluons} \quad ; t) \quad (163)$$

2. Vertices:

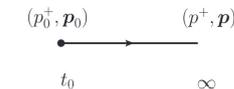


$$\gamma^+ \frac{2igt^a}{z\sqrt{1-z}} \left[\left(1 - \frac{z}{2}\right) (\mathbf{k} - z\mathbf{p})^i + i\frac{z}{2} S^3 e^{ij} (\mathbf{k} - z\mathbf{p})^j \right] \quad (164)$$

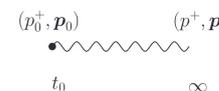


$$-2gf_{abc} \left[-\frac{1}{1-z} (\mathbf{k} - z\mathbf{p})^i \delta^{ij} + (\mathbf{k} - z\mathbf{p})^i \delta^{jl} - \frac{1}{z} (\mathbf{k} - z\mathbf{p})^j \delta^{il} \right] \quad (165)$$

3. Outgoing external lines:



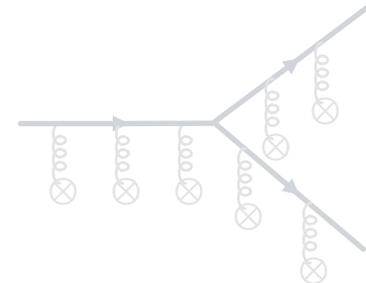
$$\bar{\xi}(s) e^{i\frac{p^2}{2p^+} t_\infty} (\mathbf{p} | \mathcal{G}_{\text{scal}}(\infty, t_0) | \mathbf{p}_0) \quad \text{for quarks} \quad (166)$$



$$\epsilon_\lambda^{*,i}(p) e^{i\frac{p^2}{2p^+} t_\infty} (\mathbf{p} | \mathcal{G}_{\text{scal}}^{\text{adj}}(\infty, t_0) | \mathbf{p}_0) \quad \text{for gluons} \quad (167)$$



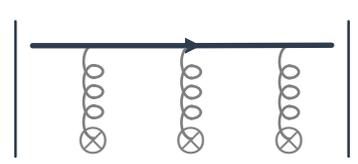
$$G_{S_1 S_2}^{C_1 C_2}(t_f, \mathbf{x}_f, t_i, \mathbf{x}_i | p^+)$$



Introduction to jet quenching - Framework

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Transverse broadening:

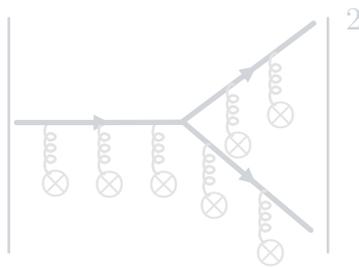


$$\left| \begin{array}{c} \text{---} \rightarrow \\ | \\ \text{---} \circ \text{---} \\ | \\ \text{---} \circ \text{---} \\ | \\ \text{---} \circ \text{---} \end{array} \right|^2 \sim \int \mathcal{D}\mathbf{r} \mathcal{D}\bar{\mathbf{r}} e^{i\frac{p^+}{2} \int_{t_i}^{t_f} ds (\dot{\mathbf{r}}^2 - \dot{\bar{\mathbf{r}}}^2)} \underbrace{\frac{1}{d_R} \left\langle \text{Tr} e^{-ig \int_{t_i}^{t_f} ds [\mathcal{A}_0(\mathbf{r}) - \mathcal{A}_0^+(\bar{\mathbf{r}})]} \right\rangle}_{\approx \exp \left[-N_c \int_{t_0}^t ds n(s) \sigma(\mathbf{r} - \bar{\mathbf{r}}) \right]}$$

Gaussian broadening: $N_c n \sigma(\mathbf{r}) \approx \hat{q} r^2 / 2$

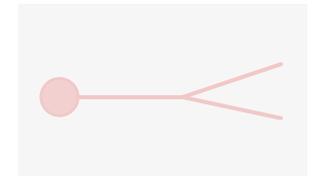
$$\mathcal{P}(\mathbf{p}, t) = \frac{4\pi}{\hat{q}t} e^{-\frac{\mathbf{p}^2}{\hat{q}t}} \quad \langle \mathbf{p}^2 \rangle = \hat{q}t$$

Medium induced emission (in addition to vacuum):



$$\sim \frac{dP}{dzdk} \sim \frac{\alpha_s}{z^{3/2}} f(\mathbf{k})$$

+ color decoherence: $\vartheta_{q\bar{q}} \ll \vartheta_c$



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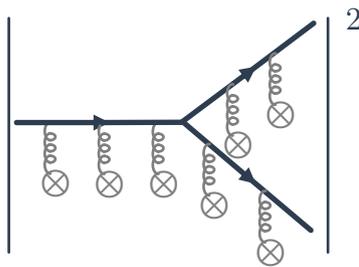
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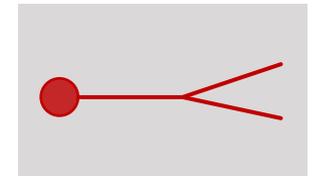
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Medium induced emission (in addition to vacuum): [Implementation: Caucal, Soyez, Iancu & Kutak, Placzek, Rohrmoser, Tywoniuk]



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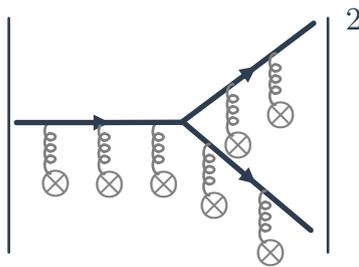
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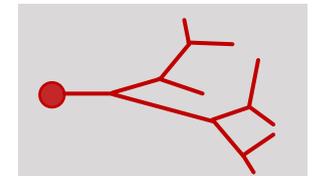
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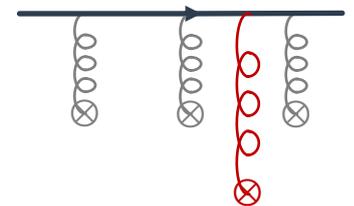
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Improved opacity expansion: [Barata, Mehtar-Tani, Soto-Ontoso, Tywoniuk]

$$\sigma(\mathbf{r}) = \sigma_{HO} + \delta\sigma$$

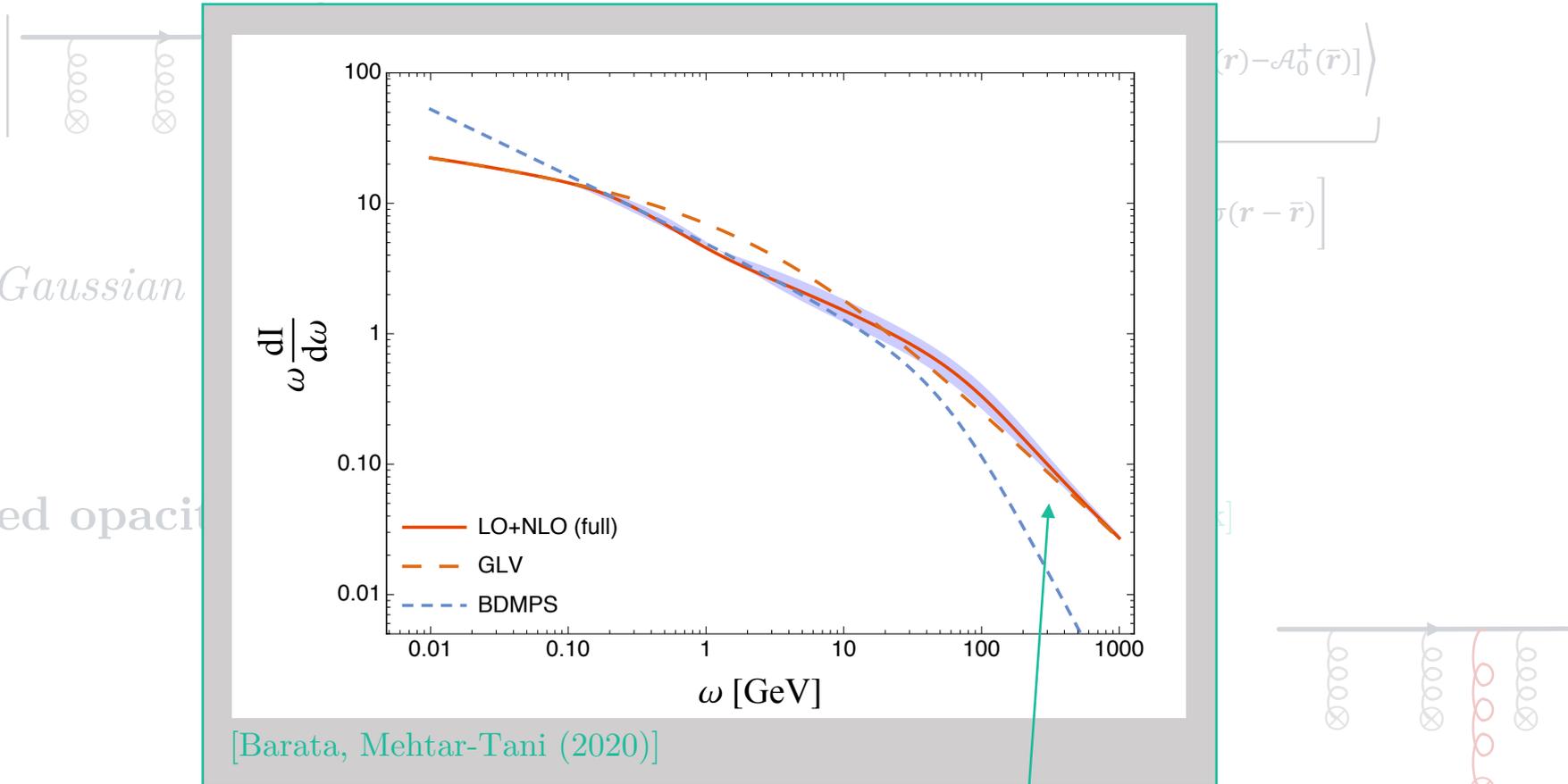
hard scattering



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Transverse broadening:



[Barata, Mehtar-Tani (2020)]

[To identify hard emissions, see Alba's talk about dynamical grooming]



Application: Quenched jet spectrum

[arXiv:2101.01742, 2103.14676]



The quenched spectrum: the quenching weight

[Baier, Dokshitzer, Mueller, Schiff (1998), Salgado, Wiedemann (2001)]

The quenched spectrum (probability \mathcal{P} of losing ε energy)

$$\frac{d\sigma^{med}}{dp_T}(p_T) \equiv \int_0^\infty d\varepsilon \mathcal{P}(\varepsilon) \frac{d\sigma^{vac}}{dp_T}(p_T + \varepsilon) \approx \frac{d\sigma^{vac}}{dp_T}(p_T) \int_0^\infty d\varepsilon \mathcal{P}(\varepsilon) e^{-\frac{n\varepsilon}{p_T}}$$

$\frac{d\sigma^{vac}}{dp_T}(p_T) \sim p_T^{-n}$ [Dasgupta, Dreyer, Salam, Soyez]

The R_{AA} is the quenching weight

$$R_{med}(p_T) \equiv \frac{\frac{d\sigma^{med}}{dp_T}(p_T)}{\frac{d\sigma^{vac}}{dp_T}(p_T)} \approx \int_0^\infty d\varepsilon \mathcal{P}(\varepsilon) e^{-\frac{n\varepsilon}{p_T}} \equiv \mathcal{Q}_{med}(p_T)$$

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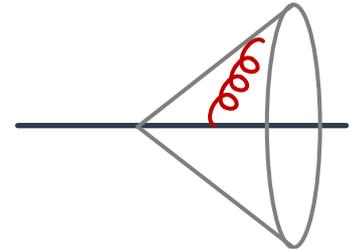
What is $\mathcal{P}(\varepsilon)$?

[Bayesian: Phys. Rev. Lett. 122 (2019)
ML: J. High Energ. Phys. 2021, 206 (2021)]

The quenched spectrum: energy loss probability

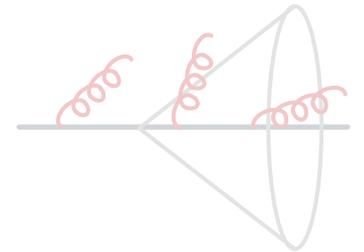
Single parton, single medium induced emission

$$\mathcal{P}_>^{(0)}(\varepsilon) \approx \frac{dI_>}{d\varepsilon}$$



Single parton, multiple induced emission [JHEP09 (2001) 033]

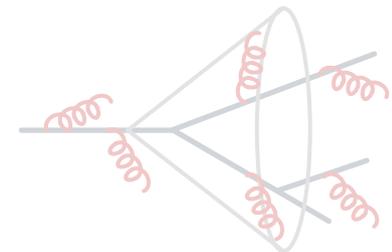
$$\mathcal{P}_>^{(0)}(\varepsilon) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[\prod_j^n \int d\omega_j \frac{dI_>}{d\omega_j} \right] \delta \left(\varepsilon - \sum_{j=1}^n \omega_j \right) e^{-\int d\omega_j \frac{dI_>}{d\omega_j}}$$



$$Q_>^{(0)}(p_T) = \exp \left[- \int_0^{\infty} d\omega \left(1 - e^{-\frac{n\omega}{p_T}} \right) \frac{dI_>}{d\omega} \right]$$

Multi parton (jet), multiple induced emission [Phys.Rev.D98 (2018) 051501]

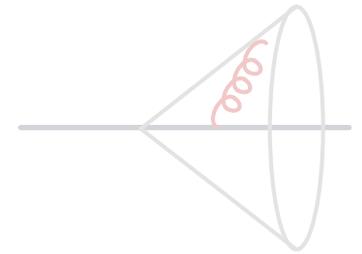
$$Q_>^{jet}(p_T) \approx Q_>^{(0)}(p_T) \mathcal{C}(p_T, R)$$



The quenched spectrum: energy loss probability

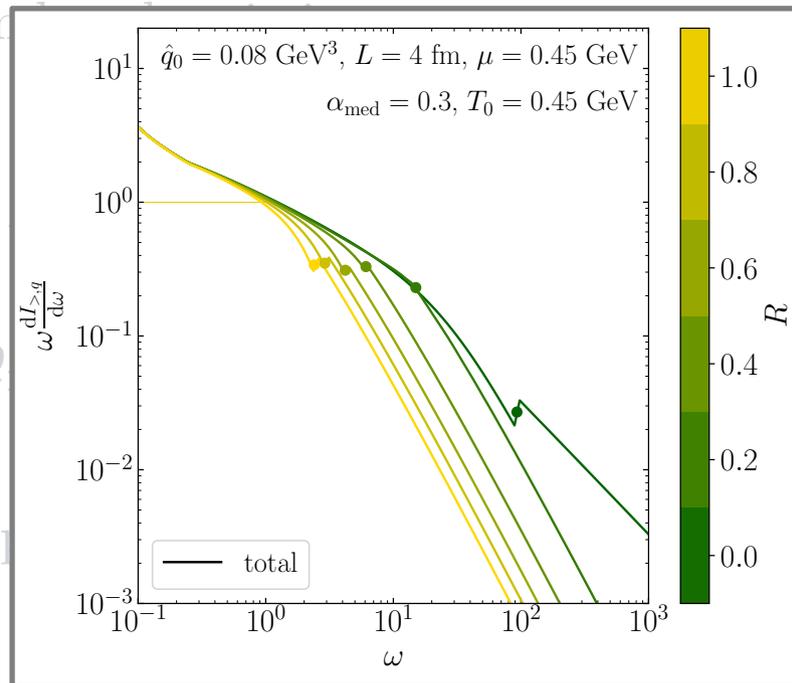
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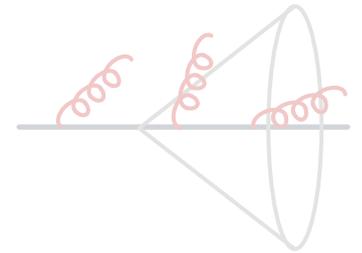


Single parton, multiple induced emissions

$$\mathcal{P}_>^{(0)}(\varepsilon) =$$



$$- \int d\omega_j \frac{dI_{>}}{d\omega_j}$$



Multi parton (jet), multiple induced emissions

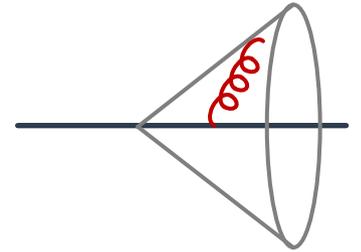
BDMPS-Z + GLV + Matching
 [Nucl.Phys.B484 (1997) 265]
 [JETP Lett.63 (1996) 952]
 [Nucl.Phys.B594 (2001) 371]
 [JHEP10 (2020) 176]



The quenched spectrum: energy loss probability

Single parton, single medium induced emission

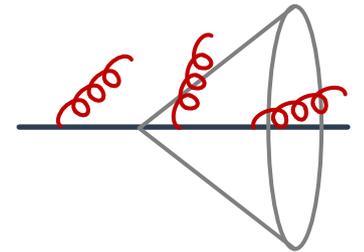
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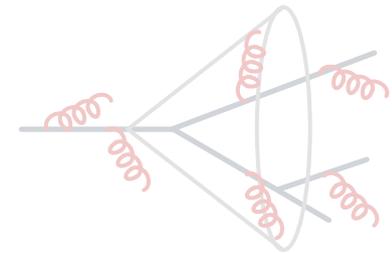
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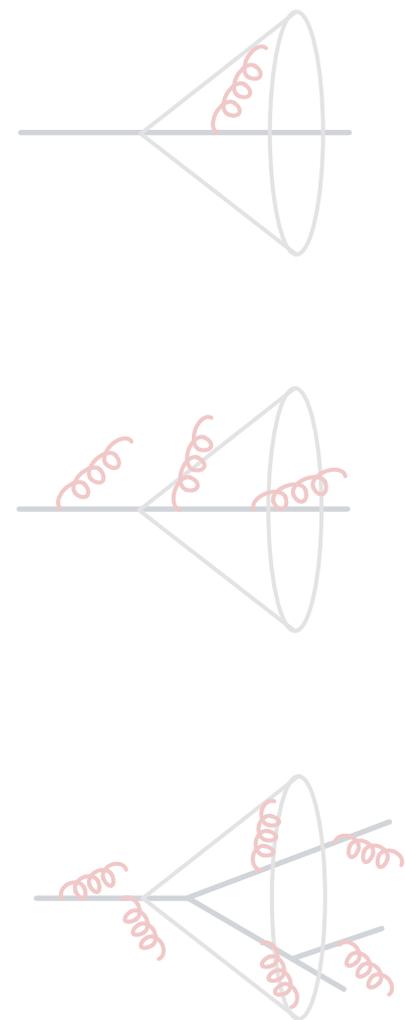
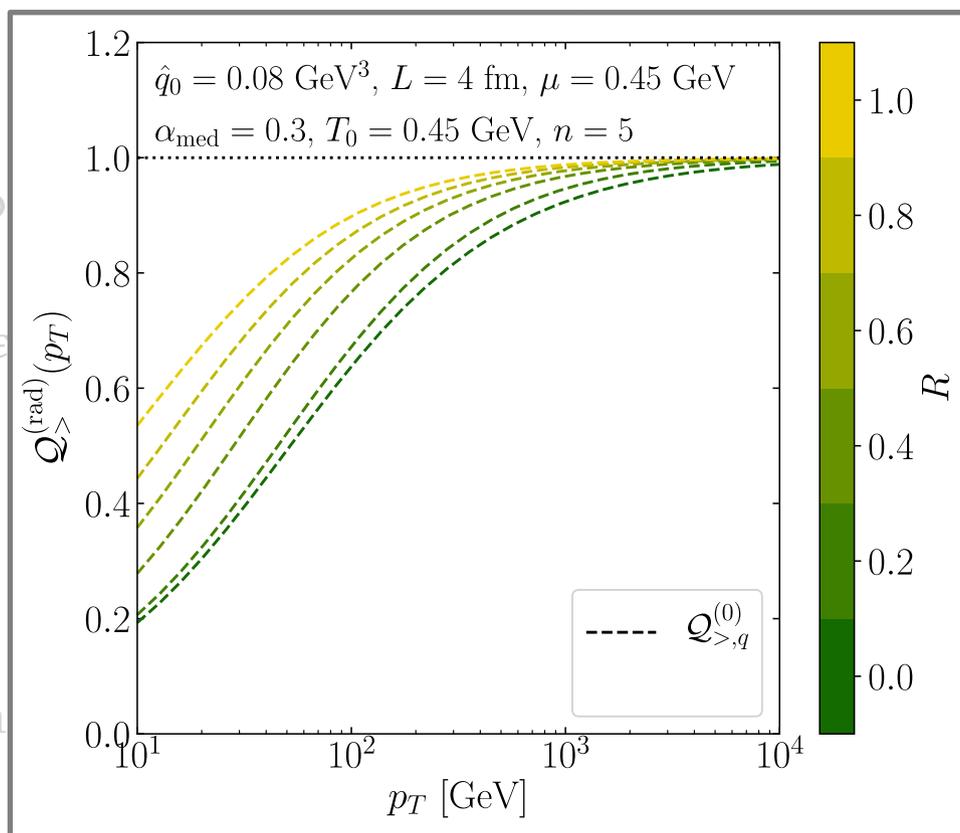
Multi parton (jet), multiple induced emission [Phys.Rev.D98 (2018) 051501]

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The quenched spectrum: energy loss probability

Single parton, single medium induced emission



Single parton, multiple

$$\mathcal{P}_{>}^{(0)}(\epsilon)$$

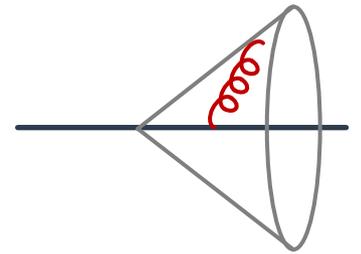
Multi parton (jet), m

$$Q_{>}^{(\text{rad})}(p_T) \approx Q_{>,q}^{(0)}(p_T) \mathcal{C}(p_T, R)$$

The quenched spectrum: energy loss probability

Single parton, single medium induced emission

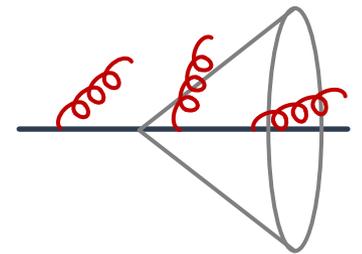
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Single parton, multiple induced emission [JHEP09 (2001) 033]

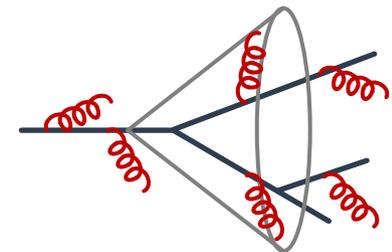
$$\mathcal{P}_{>}^{(0)}(\varepsilon) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[\prod_j^n \int d\omega_j \frac{dI_{>}}{d\omega_j} \right] \delta \left(\varepsilon - \sum_{j=1}^n \omega_j \right) e^{-\int d\omega_j \frac{dI_{>}}{d\omega_j}}$$

$$Q_{>}^{(0)}(p_T) = \exp \left[- \int_0^{\infty} d\omega \left(1 - e^{-\frac{n\omega}{p_T}} \right) \frac{dI_{>}}{d\omega} \right]$$



Multi parton (jet), multiple induced emission [Phys.Rev.D98 (2018) 051501]

$$Q_{>}^{jet}(p_T) \approx Q_{>}^{(0)}(p_T) \mathcal{C}(p_T, R)$$

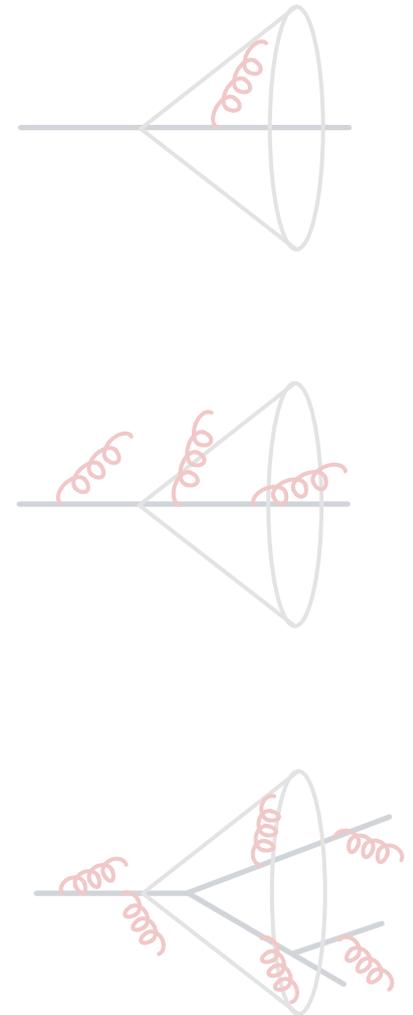
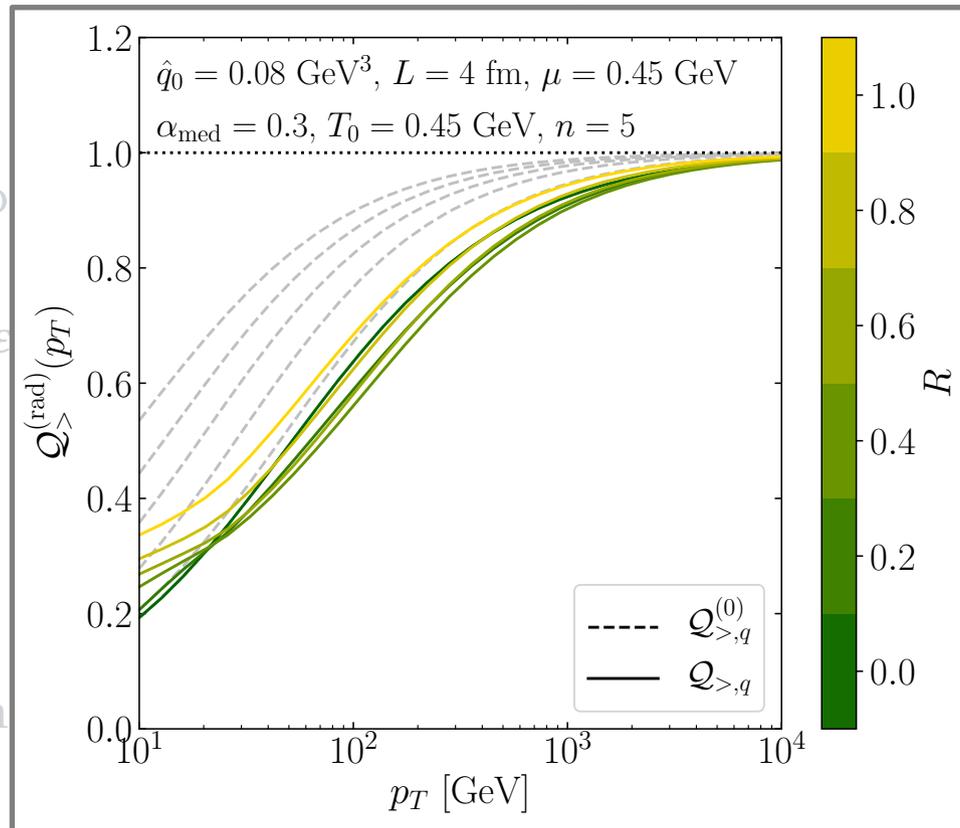


The quenched spectrum: energy loss probability

Single parton, single medium induced emission

Single parton, multiple medium induced emission

Multiple parton (jet), multiple medium induced emission



$$Q_{>}^{(rad)}(p_T) \approx Q_{>,q}^{(0)}(p_T) \mathcal{C}(p_T, R)$$

$$dI_j \frac{dI_{>}}{d\omega_j}$$

51501]

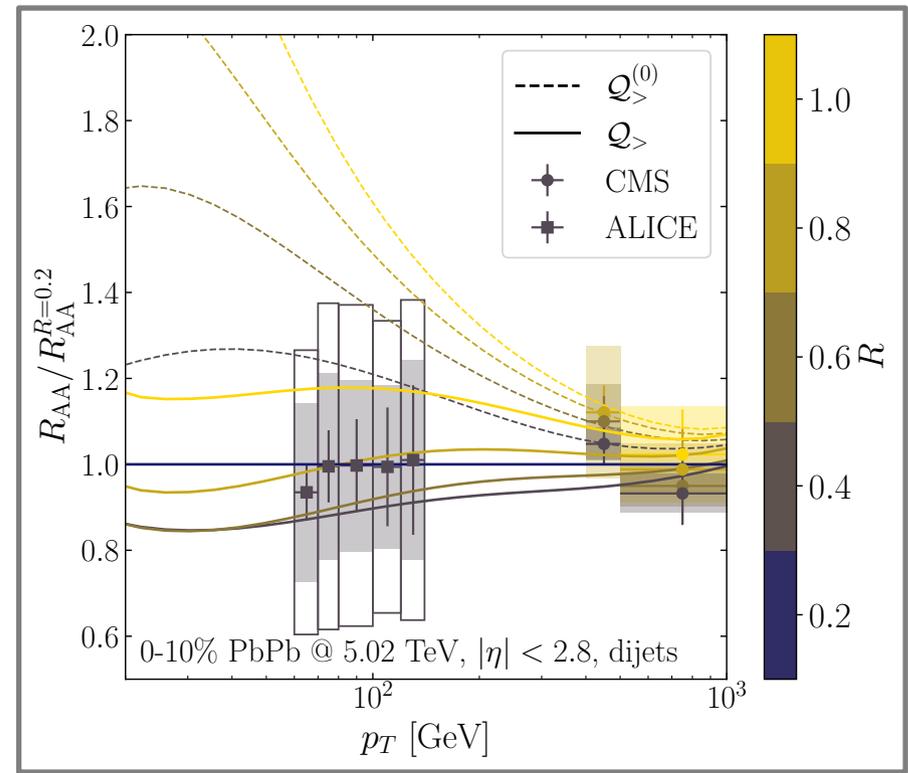
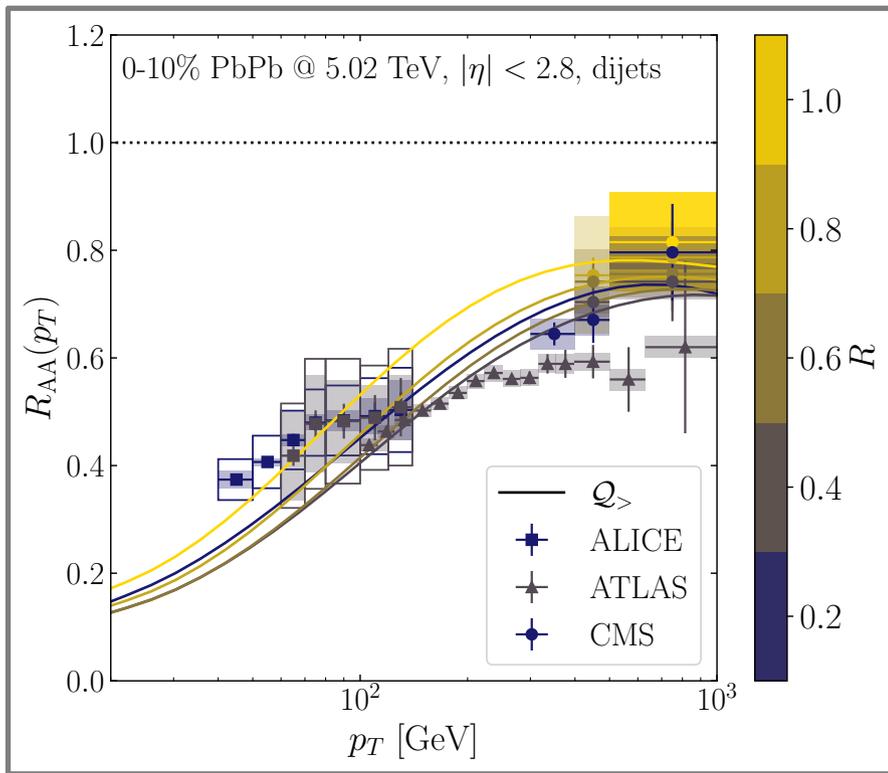
Comparison to data

To include more effects:

- Assuming factorization: PDF and nPDF effects, quark/gluon ratio
- Medium resolution and color coherence effects
- Broadening of the induced gluons in/out of the cone
- Thermalizing soft gluons
- Energy loss from elastic scattering
- Geometry and time dependence
- Fluctuations

0-10% PbPb @ 5.02 TeV, $|\eta| < 2.8$

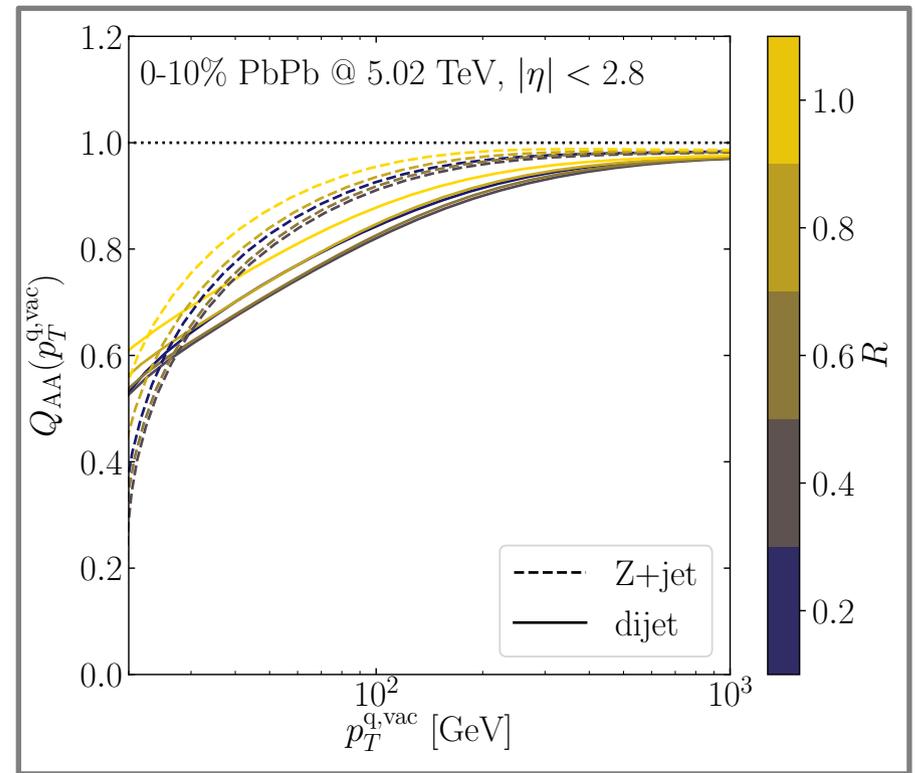
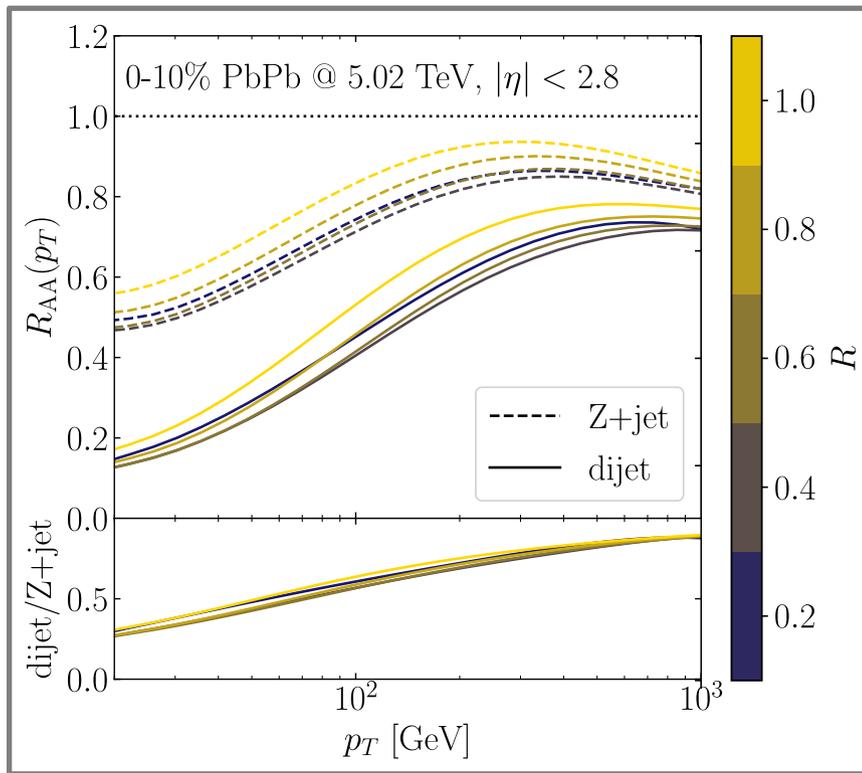
[see RAA also in arXiv:2101.01742, 2103.14676]



Thank you for your attention!



Quenching weight



Introduction: What is the jet R_{AA} ?

- Definition:

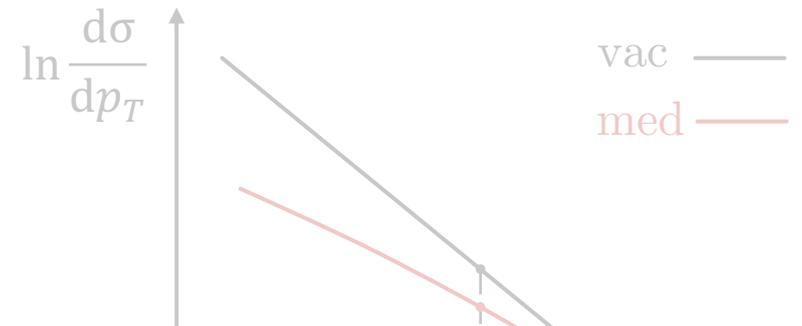
$$R_{AA}(p_T) = \frac{\frac{d\sigma^{\text{med}}}{dp_T}(p_T)}{\frac{d\sigma^{\text{vac}}}{dp_T}(p_T)}$$

- R_{AA} : Compares jets in vacuum to jets in medium at the **same** p_T .
- Jet with p_T in medium loose energy and ends up with $p_T - \varepsilon$.
- **Complication 1:**
 R_{AA} doesn't compare the "same" jets!

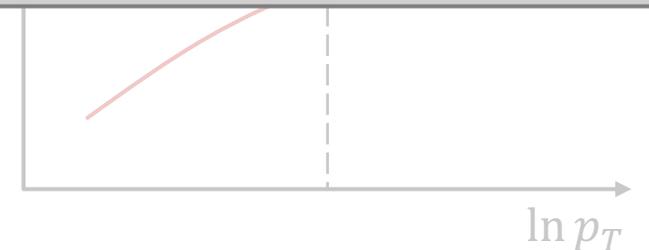
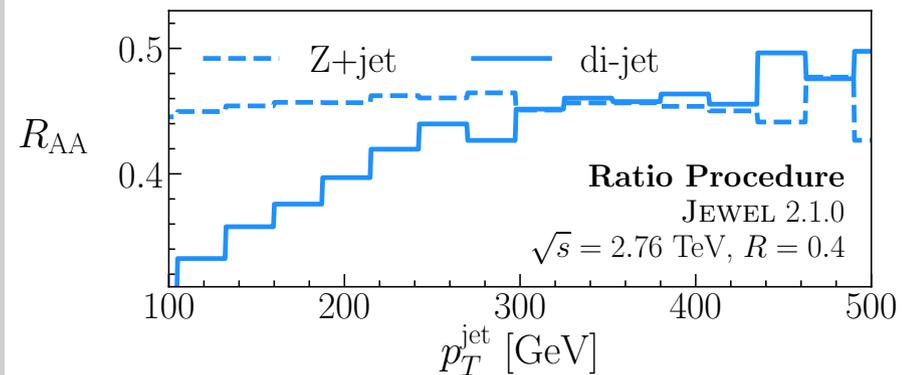
- The spectrum is steeply falling $n \gg 1$.

$$\frac{d\sigma}{dp_T} \sim p_T^{-n}$$

- **Complication 2:**
 R_{AA} is sensitive to n (bias on energy loss)!



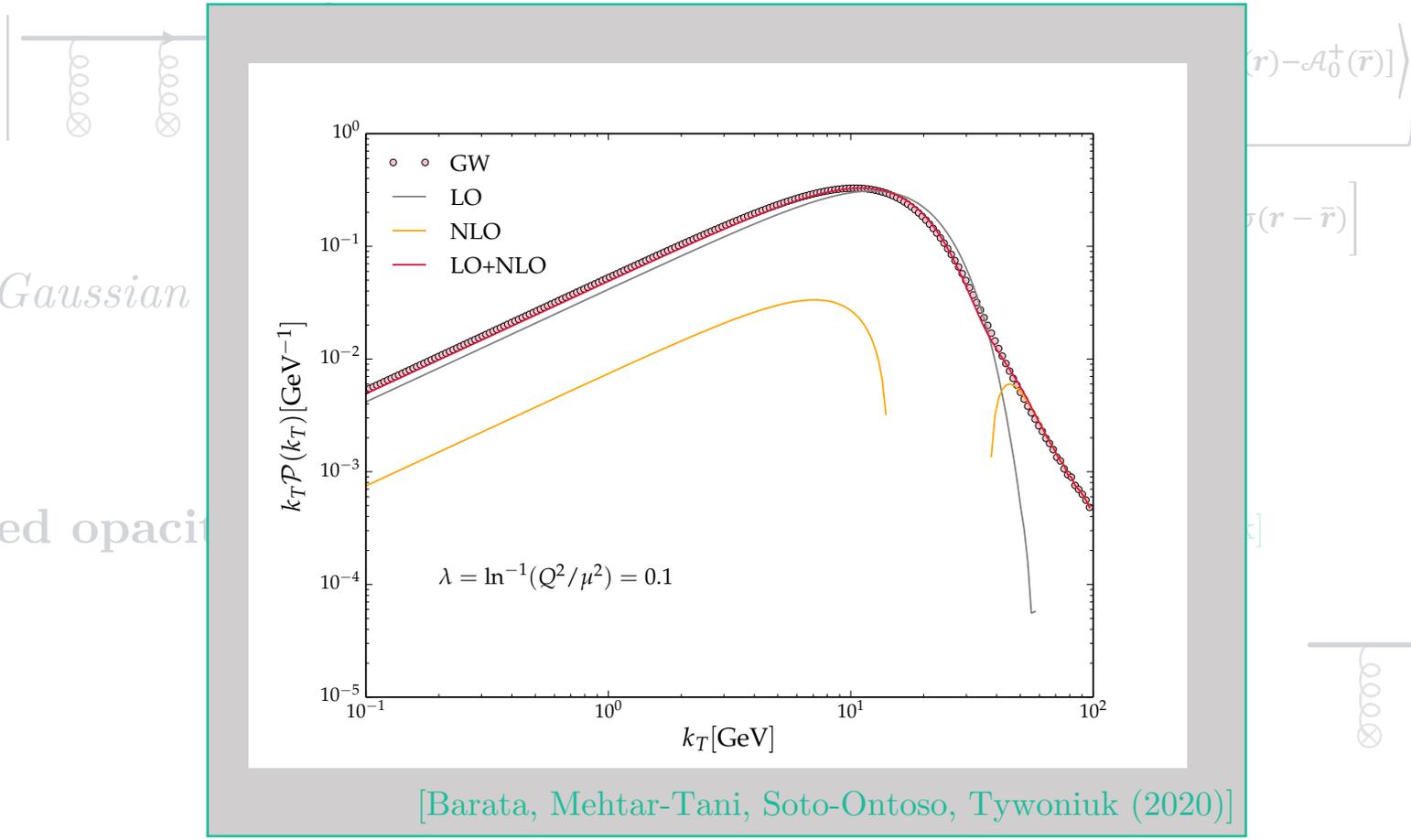
[J.Brewer et. al. Phys.Rev.Lett. 122, 222301 (2019)]



Introduction to jet quenching - Framework

[Zakharov, BDMPS, GLV, Wiedemann (1996-2000)
Blaizot, Iancu, Salgado, CGC formalism (2012-)]

Transverse broadening:



Comparison to data

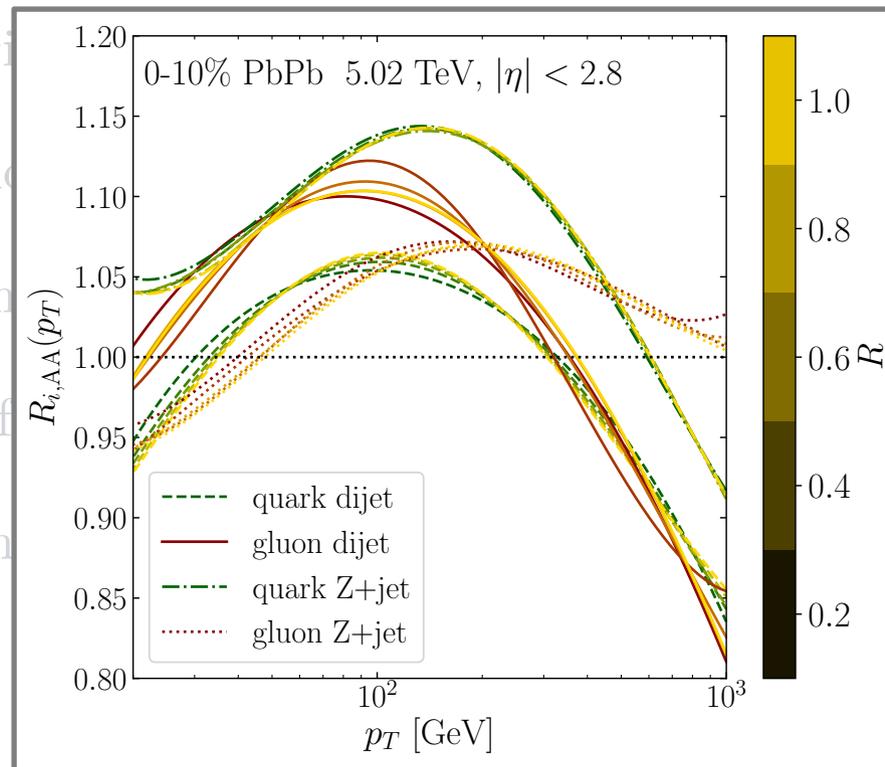
To include more effects:

- Assuming factorization
- Medium resolution
- Broadening of the
- Thermalizing soft
- Energy loss from

Missing:

- Geometry and time dependence
- Fluctuations

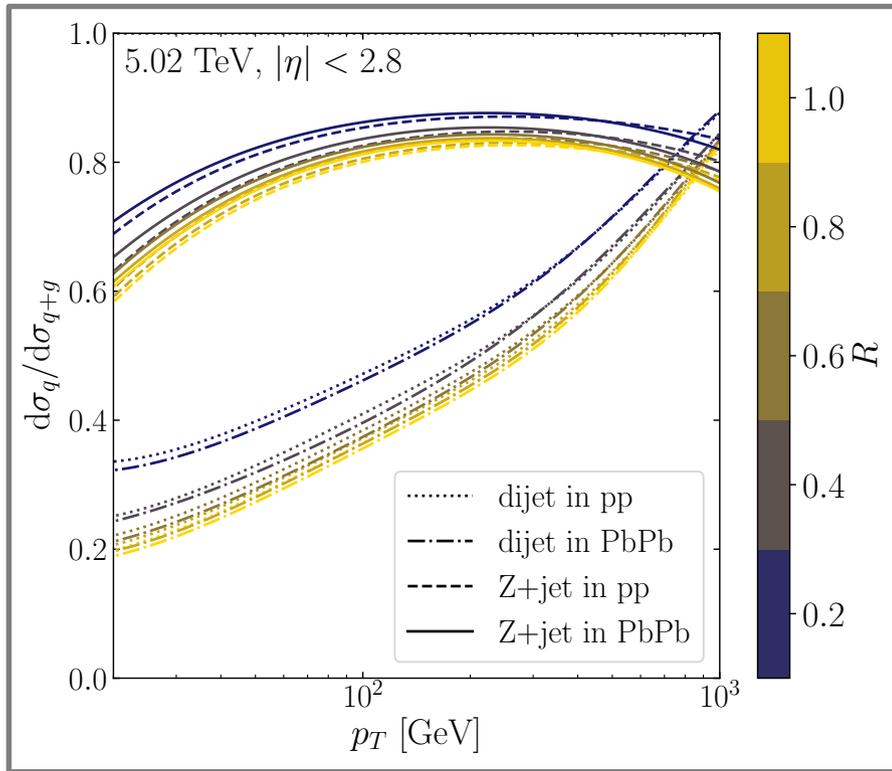
nPDF effects



gluon ratio

Quenching weight

Before quenching



After quenching

