

# Searching for Heavy Neutrino at Future Hadron Collider

**Chang-Yuan Yao**

(Nankai University, Tianjin, China)

Based on arXiv:2103.03548

In collaboration with Chengcheng Han and Tong Li

# Outline

- **Type I Seesaw in  $U(1)_{B-L}$  extension model**
- **Heavy neutrino decay patterns**
- **LNV signature with tau lepton at the LHC upgrade**
- **Summary**

# Seesaw model

Weinberg operator:

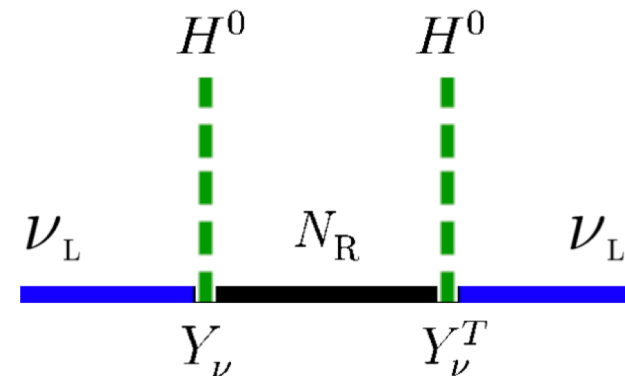
$$\mathcal{L} = -\frac{1}{2} \frac{g_{\alpha\beta}}{\Lambda} \left( \overline{\ell_{L\alpha}^C} \tilde{H}^* \right) \left( \tilde{H}^\dagger \ell_{L\beta} \right) + \text{H.c.}$$

**Type-I seesaw:** SM + right-handed neutrinos + **L** violation  
(Minkowski **1977**; Yanagida **1979**; Glashow **1979**; Gell-Mann, Ramond, Slansky **1979**; Mohapatra, Senjanovic **1980**)

$$\begin{aligned} -\mathcal{L} &= \overline{\nu_L} M_D N_R + \frac{1}{2} \overline{(N_R)^c} M_R N_R + \text{h.c.} \\ &= \frac{1}{2} \begin{bmatrix} \overline{\nu_L} & \overline{(N_R)^c} \end{bmatrix} \begin{pmatrix} 0 & M_D \\ M_D^T & M_R \end{pmatrix} \begin{bmatrix} (\nu_L)^c \\ N_R \end{bmatrix} + \text{h.c.} \end{aligned}$$

Seesaw formula:

$$M_\nu \approx -M_D M_R^{-1} M_D^T$$



# $U(1)_{B-L}$ extension

4

$U'(1)$  is a linear combination of  $U(1)_Y$  and  $U(1)_{B-L}$  after the spontaneous breaking of **electroweak** and **B-L** symmetry

$$D_\mu \ni ig_1 Y B_\mu + i(g'_1 Y + g' Y_{BL}) B'_\mu = ig_1 Y B_\mu + ig_X (x'_1 Y + x' Y_{BL}) B'_\mu$$

Most economical extension:  $x' = 1, x'_1 = 0$   $U(1)' = U(1)_{B-L}$  and  $g_X = g'$

A new scalar  $S \sim (1, 1, 0, 2)$  is introduced to break the  $U(1)_{B-L}$  symmetry and generate the masses of right-handed neutrinos  $N_R \sim (1, 1, 0, -1)$

A new gauge boson  $Z'$  can get mass  $M_{Z'} = 2g'v_S$  from the kinetic term

$$\mathcal{L}_k = (D_\mu S)^\dagger (D^\mu S) \quad \text{with} \quad D_\mu S = \partial_\mu S + i2g' B'_\mu S$$

The interaction for  $Z'$  and fermions  $\psi$  is obtained from the kinetic term

$$\mathcal{L}_k = i\bar{\psi}\gamma^\mu D_\mu\psi \quad \text{with} \quad D_\mu\psi = \partial_\mu\psi + ig'Y'_\psi B'_\mu\psi$$

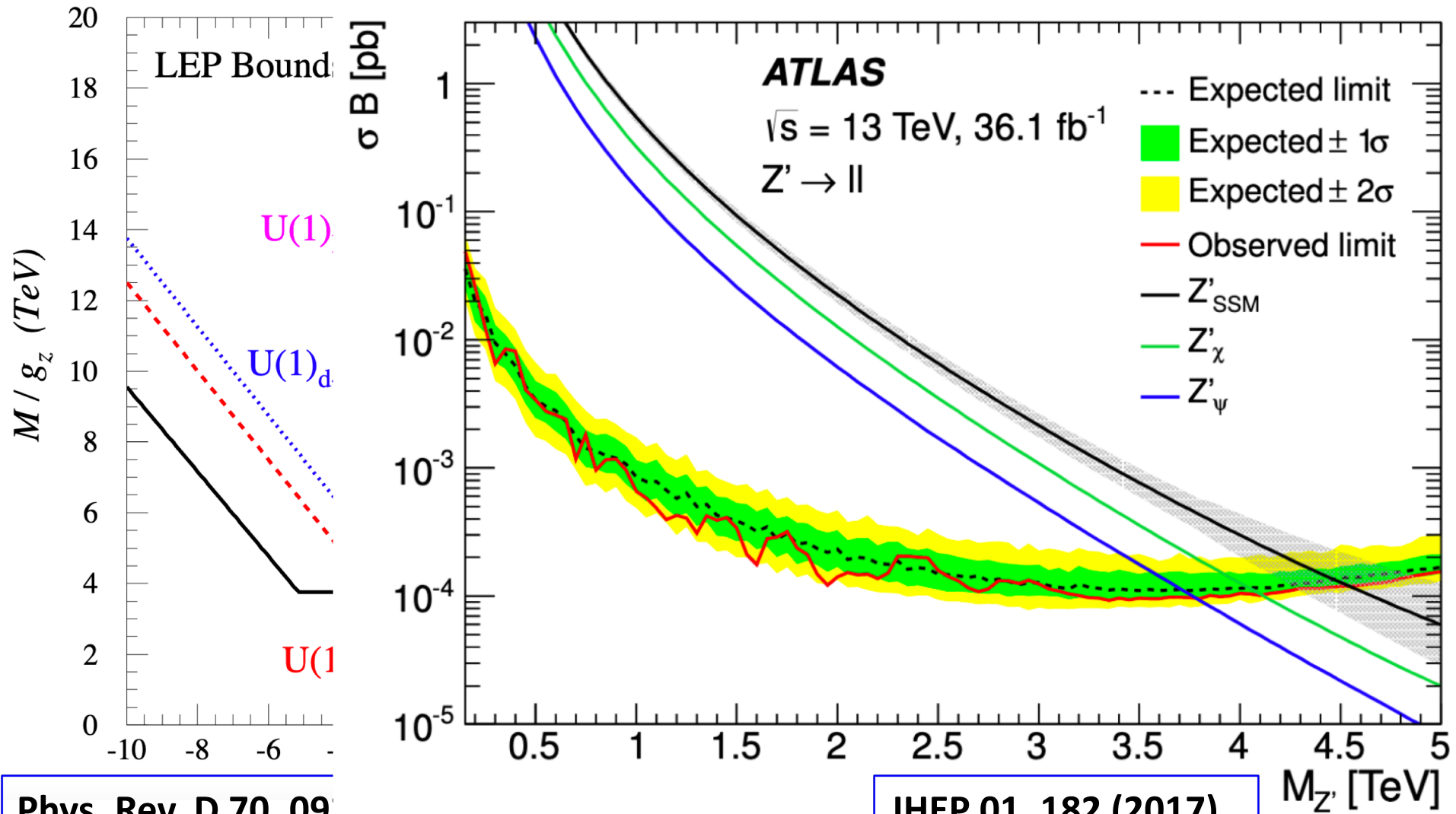
Production and decay of  $Z'$

$$pp \rightarrow Z' \rightarrow NN, \ell^+\ell^-, \tau^+\tau^-$$

# Exp. constraints

LEP-II lower bounds  $M_{Z'}/g' \gtrsim 6\text{TeV}$

LHC 13TeV 36 fb<sup>-1</sup> lower limit  $M_{Z'} \gtrsim 4.1\text{TeV}$



# Exp. constraints

Requirement of the  $U'(1)$  charge:

$$3(Q'_1 + Q'_2 + Q'_3) + Q'_e + Q'_\mu + Q'_\tau = 0$$

Quark charges

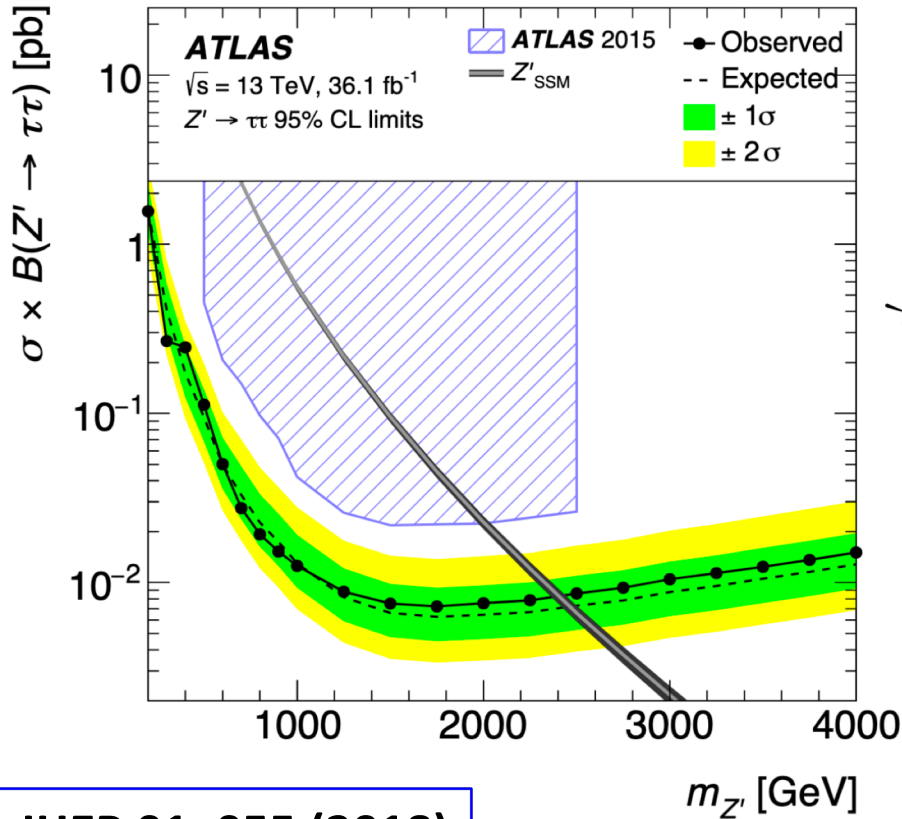
Lepton charges

Flavored  $U(1)_{(B-L)_3}$

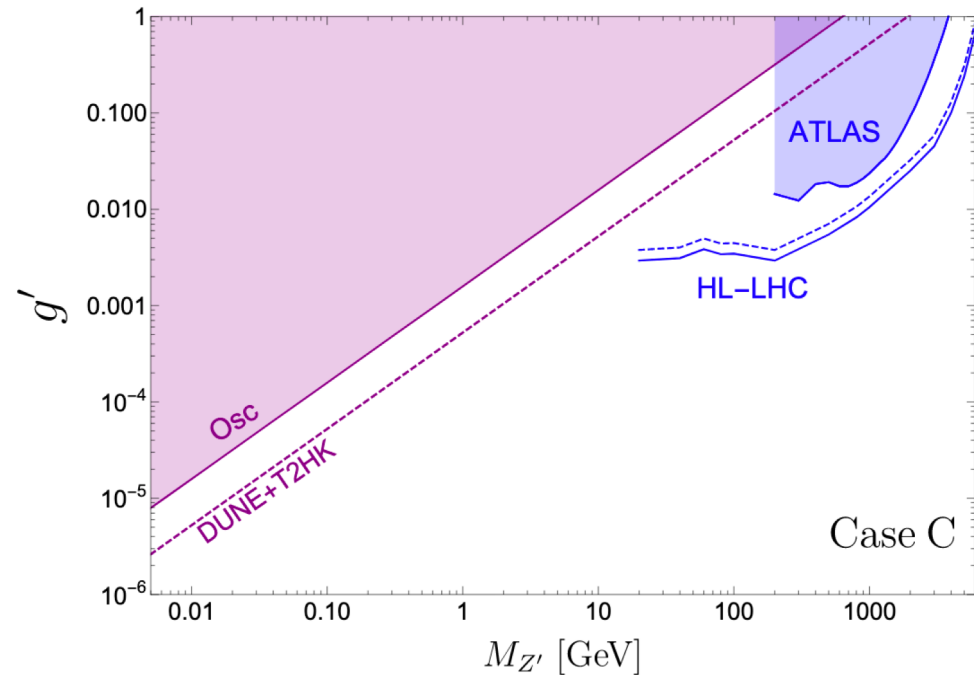
$$3Q'_3 = -Q'_\tau = 1$$

$$Q'_1 = Q'_2 = Q'_e = Q'_\mu = 0$$

The  $Z'$  can only be produced through  $b\bar{b} \rightarrow Z'$  and decay into  $\tau^+\tau^-$  and a pair of one single heavy neutrino



JHEP 01, 055 (2018)



JHEP 11, 028 (2019)

# $U(1)_{B-L}$ extension

**B-L accidental symmetry** + **Majorana neutrino masses**

$U'(1)$  is a linear combination of  $U(1)_Y$  and  $U(1)_{B-L}$  after the spontaneous breaking of **electroweak** and **B-L** symmetry

$$U(1)_Y, U(1)_{B-L} \rightarrow U'(1)$$

**anomaly cancellation**



**neutrino masses**

**Yukawa interaction:**

$$-\mathcal{L}_Y^I = Y_\nu^D \bar{l}_L \tilde{H} N_R + \frac{1}{2} Y_\nu^M \overline{(N^c)_L} N_R S + h.c.$$

$$N_R \sim (1, 1, 0, -1)$$

$$S \sim (1, 1, 0, 2)$$

After  $H, S$  receives the **vev**  $\langle H \rangle = v/\sqrt{2}$  and  $\langle S \rangle = v_S/\sqrt{2}$ , one has the diagonalization of the mass matrix

$$N^\dagger \begin{pmatrix} 0 & m_D \\ m_D^T & M \end{pmatrix} N^* = \begin{pmatrix} m_\nu & 0 \\ 0 & M_N \end{pmatrix}$$

**with**

$$M_R = Y_\nu^M v_S / \sqrt{2}$$

$$m_D = Y_\nu^D v / \sqrt{2}$$

# U(1)<sub>B-L</sub> extension

**Eigenstate transformation:**

$$\begin{pmatrix} \nu_L \\ (N^c)_L \end{pmatrix} = \mathbb{N} \begin{pmatrix} \nu_L \\ (N^c)_L \end{pmatrix}_{mass}, \quad \mathbb{N} = \begin{pmatrix} U & V \\ X & Y \end{pmatrix}$$

The **PMNS** matrix and **light-heavy** mixing matrix:

$$E^\dagger U \equiv U_{PMNS}, \quad E^\dagger V \equiv V_{\ell N}$$

**E** diagonalize the charged lepton mass matrix

**Relation between mixing matrices and mass eigenvalues:**

$$U_{PMNS}^* m_\nu^{diag} U_{PMNS}^\dagger + V_{\ell N}^* M_N^{diag} V_{\ell N}^\dagger = 0$$

$$m_\nu^{diag} = (m_1, m_2, m_3)$$

$$M_N^{diag} = (M_{N_1}, M_{N_2}, M_{N_3})$$

**Casas-Ibarra parametrization:**

$$V_{\ell N} = U_{PMNS} (m_\nu^{diag})^{1/2} \Omega (M_N^{diag})^{-1/2}$$

For simplicity, we take the arbitrary orthogonal complex matrix as  $\Omega = I$

$$U_{PMNS} = \begin{pmatrix} c_{12}c_{13} & c_{13}s_{12} & e^{-i\delta}s_{13} \\ -c_{12}s_{13}s_{23}e^{i\delta} - c_{23}s_{12} & c_{12}c_{23} - e^{i\delta}s_{12}s_{13}s_{23} & c_{13}s_{23} \\ s_{12}s_{23} - e^{i\delta}c_{12}c_{23}s_{13} & -c_{23}s_{12}s_{13}e^{i\delta} - c_{12}s_{23} & c_{13}c_{23} \end{pmatrix} \times \text{diag}(e^{i\Phi_1/2}, 1, e^{i\Phi_2/2})$$



# Mixing parameters

## Tree-flavor oscillation parameters [NuFIT 5.0 (2020)]

	Normal Ordering (best fit)		Inverted Ordering ( $\Delta\chi^2 = 7.1$ )		
	bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range	
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.44^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.86$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.573^{+0.016}_{-0.020}$	$0.415 \rightarrow 0.616$	$0.575^{+0.016}_{-0.019}$	$0.419 \rightarrow 0.617$
	$\theta_{23}/^\circ$	$49.2^{+0.9}_{-1.2}$	$40.1 \rightarrow 51.7$	$49.3^{+0.9}_{-1.1}$	$40.3 \rightarrow 51.8$
	$\sin^2 \theta_{13}$	$0.02219^{+0.00062}_{-0.00063}$	$0.02032 \rightarrow 0.02410$	$0.02238^{+0.00063}_{-0.00062}$	$0.02052 \rightarrow 0.02428$
	$\theta_{13}/^\circ$	$8.57^{+0.12}_{-0.12}$	$8.20 \rightarrow 8.93$	$8.60^{+0.12}_{-0.12}$	$8.24 \rightarrow 8.96$
	$\delta_{\text{CP}}/^\circ$	$197^{+27}_{-24}$	$120 \rightarrow 369$	$282^{+26}_{-30}$	$193 \rightarrow 352$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3l}^2}{10^{-3} \text{ eV}^2}$	$+2.517^{+0.026}_{-0.028}$	$+2.435 \rightarrow +2.598$	$-2.498^{+0.028}_{-0.028}$	$-2.581 \rightarrow -2.414$

# Decay patterns of $N$

Asymptotic behavior holds when  $M_{N_i} \gg M_W, M_Z, M_h$

$$\Gamma(N_i \rightarrow \sum_{\ell} \ell^{\pm} W^{\mp}) \approx \Gamma(N_i \rightarrow \sum_{\nu} \nu Z + \bar{\nu} Z) \approx \Gamma(N_i \rightarrow \sum_{\nu} \nu h + \bar{\nu} h)$$

Partial decay width

$$\Gamma(N_i \rightarrow \ell^{\pm} W^{\mp}) = \frac{G_F}{8\sqrt{2}\pi} |V_{\ell N_i}|^2 M_{N_i} (M_{N_i}^2 + 2M_W^2) \left(1 - \frac{M_W^2}{M_{N_i}^2}\right)^2$$

Benchmark decay branching ratios of  $N_i$  for NH(IH) case

BR( $N_i$ )	$e^{\pm} W^{\mp}$	$\mu^{\pm} W^{\mp}$	$\tau^{\pm} W^{\mp}$
$N_1$	17% (17%)	1.85% (3.8%)	6.15% (4.2%)
$N_2$	7.43% (7.43%)	9.15% (7.14%)	8.42% (10.43%)
$N_3$	0.55% (0.56%)	14% (14.04%)	10.45% (10.4%)

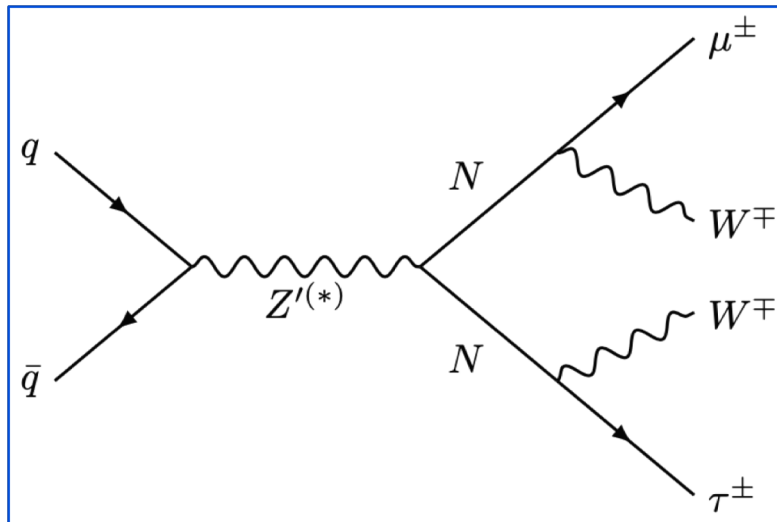
# LNV signature

## Signal

In the  $U(1)_{(B-L)_3}$  model, the most appealing **signal** channel is

$$b\bar{b} \rightarrow Z' \rightarrow NN \rightarrow \ell^\pm \tau^\pm W^\mp W^\mp$$

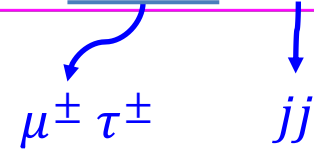
with **hadronically** decaying W boson



## Background

The major irreducible SM **backgrounds** include

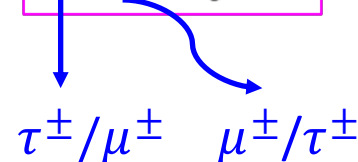
$$t\bar{t}W^\pm \rightarrow b\bar{b}W^\pm W^\pm W^\mp$$



$$t\bar{t}Z \rightarrow b\bar{b}W^+W^-Z$$



$$WZ + \text{jets}$$



# Reconstruction & Cuts

## Charged leptons

- select events with exactly one **muon** and one **tau** with **same sign**
- Muon with  $|\eta(\mu)| < 2.4$ ,  $p_T > 25\text{GeV}$  and tau with  $|\eta(\tau)| < 2.5$ ,  $p_T > 25\text{GeV}$

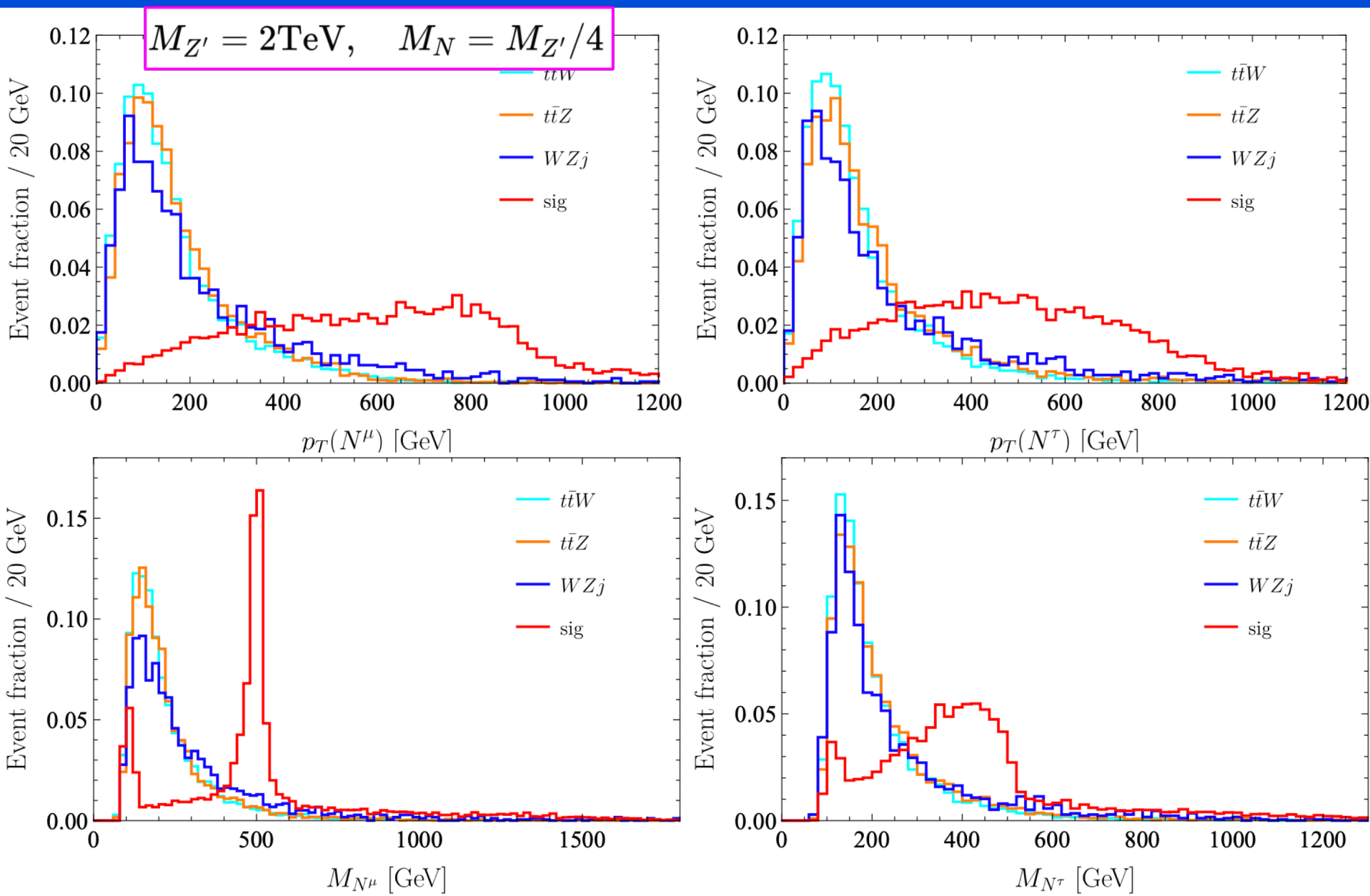
## W boson

- Resolved W
  - reconstruct each W boson from two resolved jets with  $|\eta| < 2.4$ ,  $p_T > 25\text{GeV}$
- Boosted W
  - The fat jet is reconstructed via the anti-kT algorithm with  $R=0.8$ . The fat jet with  $65 < M_J < 95\text{GeV}$ ,  $p_T(J) > 250\text{GeV}$  and  $|\eta(J)| < 2.5$  is identified as boosted W candidate

## Reconstruct $N_R$

- Given the same-sign  $\mu$  and  $\tau$  and the two reconstructed W bosons, we find the combination that minimizes  $\Delta R(\mu, W_1) + \Delta R(\tau, W_2)$  and then construct  $N^\mu$  and  $N^\tau$  respectively denoting the heavy neutrino decay into  $\mu$  and  $\tau$
- Apply  $p_T$  and mass window cut:  $p_T(N^\mu) > 250\text{GeV}$ ,  $p_T(N^\tau) > 200\text{GeV}$ ,  $|M_{N^\mu} - M_N| < 0.1M_N$ ;

# Distributions

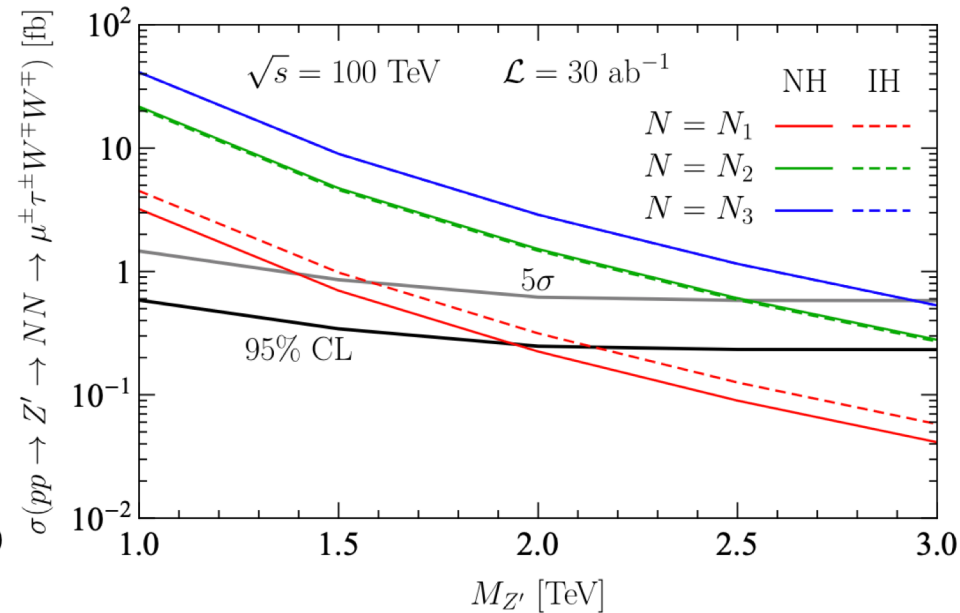
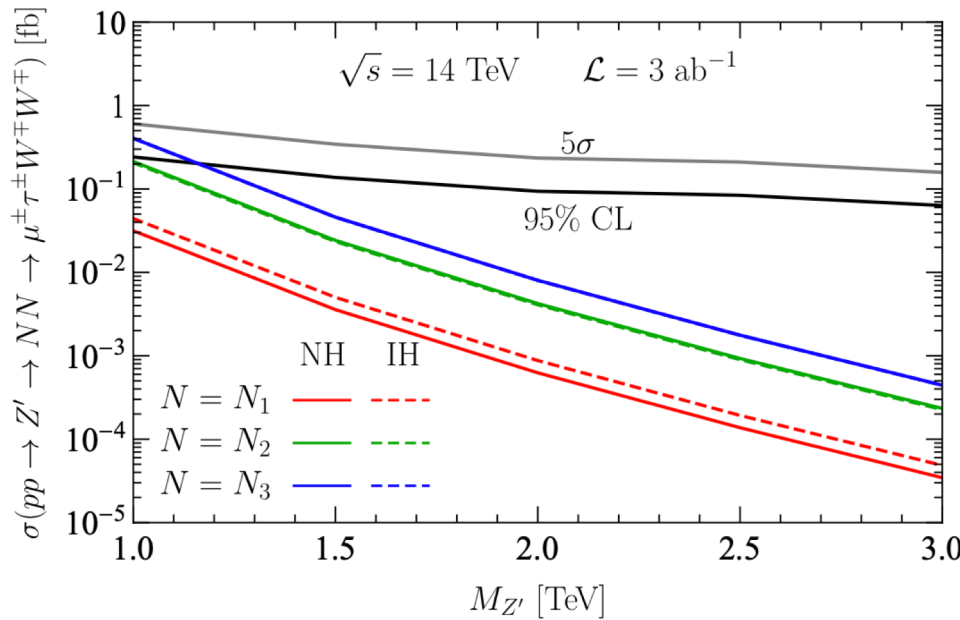


# Projected sensitivity

The **significance** is calculated by the Gaussian method  $S/\sqrt{B}$

$$S = L \times \sigma_0 \times 2 \times \text{BR}^2(W^\pm \rightarrow q\bar{q}') \times \epsilon_{NN}^\tau$$

$$\sigma_0 \equiv \sigma(pp \rightarrow Z' \rightarrow NN) \times \text{BR}(N \rightarrow \tau^\pm W^\mp) \times \text{BR}(N \rightarrow \ell^\pm W^\mp)$$

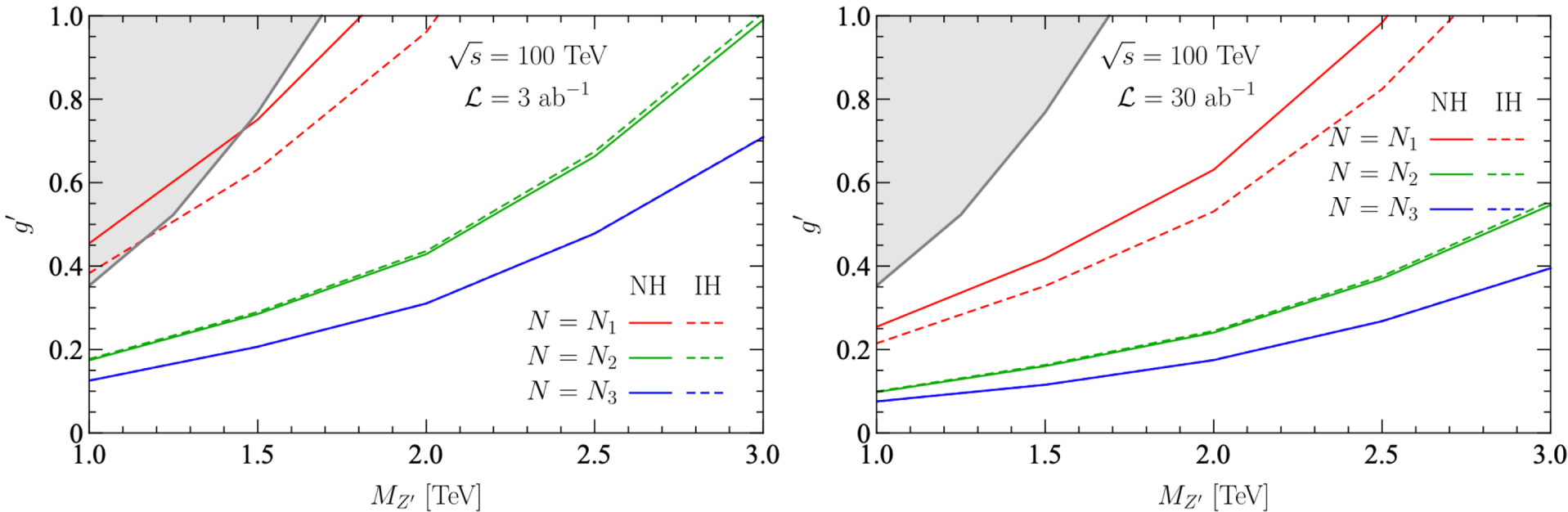


- The **HL-LHC** can produce at most 20 LNV events for  $M_{Z'} = 1$  TeV and **cannot** reach  $5\sigma$  discovery
- The **FCC-hh** can discover the LNV signal with tau lepton for  $M_{Z'}$  up to 3 TeV and  $N = N_3$  with the fixed  $g' = 0.6$  and the integrated luminosity of  $30 \text{ ab}^{-1}$

# Projected sensitivity

15

Projected sensitivity of the gauge coupling  $g'$  versus  $M_{Z'}$ ,



- The gray curve shows the 95% C.L. limit from the search for  $Z' \rightarrow \tau\tau$  at LHC
- The searches for  $Z' \rightarrow b\bar{b}$  or  $Z' \rightarrow t\bar{t}$  do not place severe constraint
- The gauge coupling  $g'$  down to 0.12 (0.07) can be probed through the LNV signature with tau lepton by the FCC-hh with the integrated luminosity of 3 (30)  $\text{ab}^{-1}$  and  $M_{Z'} = 1$  TeV.

# Summary

- The lepton number violation at colliders can be probed by the  $U(1)_{B-L}$  extension of the canonical Type I Seesaw
- Flavored  $U(1)_{(B-L)_3}$  model has weaker constraints from experiments
- The **HL-LHC** cannot reach  $5\sigma$  discovery for heavy neutrinos
- The **FCC-hh** can discover the LNV signal with tau lepton for  $M_{Z'}$  up to 2.2 (3) TeV with  $g' = 0.6$  and the integrated luminosity of 3 (30)  $\text{ab}^{-1}$
- The gauge coupling  $g'$  down to 0.12 (0.07) can be probed through the LNV signature with tau lepton by the **FCC-hh** with the integrated luminosity of 3 (30)  $\text{ab}^{-1}$  and  $M_{Z'} = 1$  TeV.



# Backup

**Lesson 1:** two necessary conditions to test a seesaw model with heavy right-handed Majorana neutrinos at the **LHC**:

- Masses of heavy Majorana neutrinos must be of O (1) **TeV** or below
- Light-heavy neutrino mixing (i.e.  $M_D/M_R$ ) must be large enough

**Lesson 2:** **non-unitarity** of the light  $\nu$  flavor mixing matrix might lead to observable effects in  $\nu$  oscillations and rare processes.

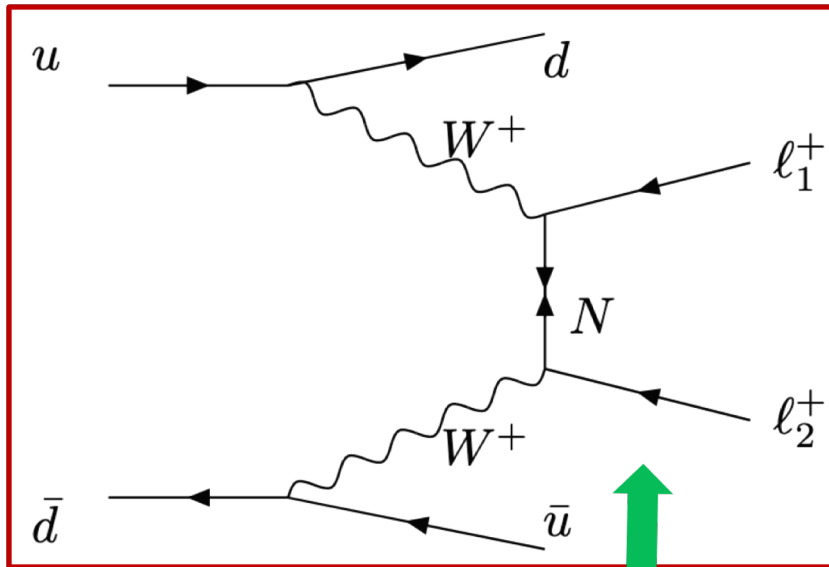
**Lesson 3:** nontrivial limits on heavy Majorana  $\nu$ 's could be derived at the **LHC**, if the SM backgrounds are small for a specific final state.

$\Delta L=2$  like-sign dilepton events

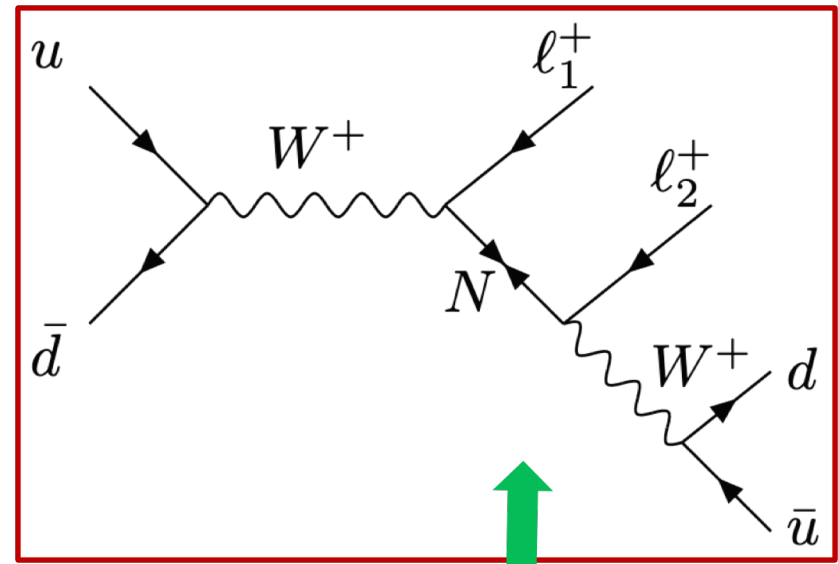
$$pp \rightarrow W^\pm W^\pm \rightarrow \mu^\pm \mu^\pm jj \quad \text{and} \quad pp \rightarrow W^\pm \rightarrow \mu^\pm N \rightarrow \mu^\pm \mu^\pm jj$$

# Backup

**Lepton number violation:** like-sign dilepton events at hadron colliders, such as Tevatron ( $\sim 2$  TeV) and LHC ( $\sim 14$  TeV).



collider analogue to  $0\nu\beta\beta$  decay



dominant channel

$N$  can be produced on resonance